Letters of Euler on different subjects in physics and philosophy.

Addressed to a German princess / Translated from the French by Henry
Hunter, with original notes and a glossary. Of foreign and scientific terms.

#### **Contributors**

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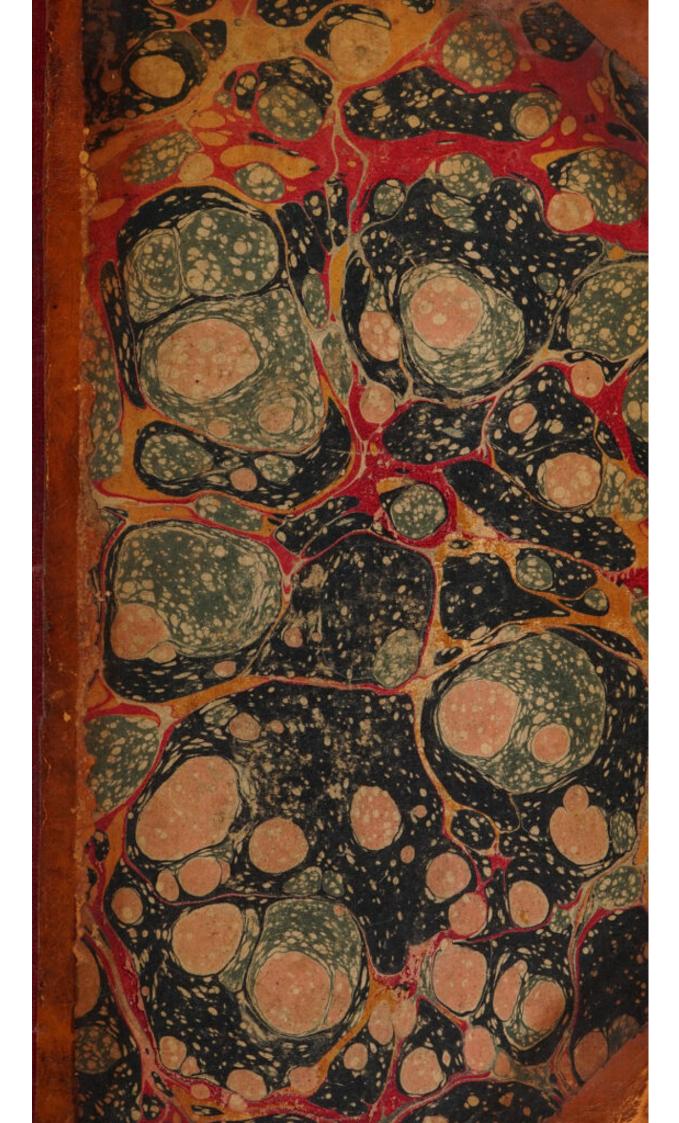
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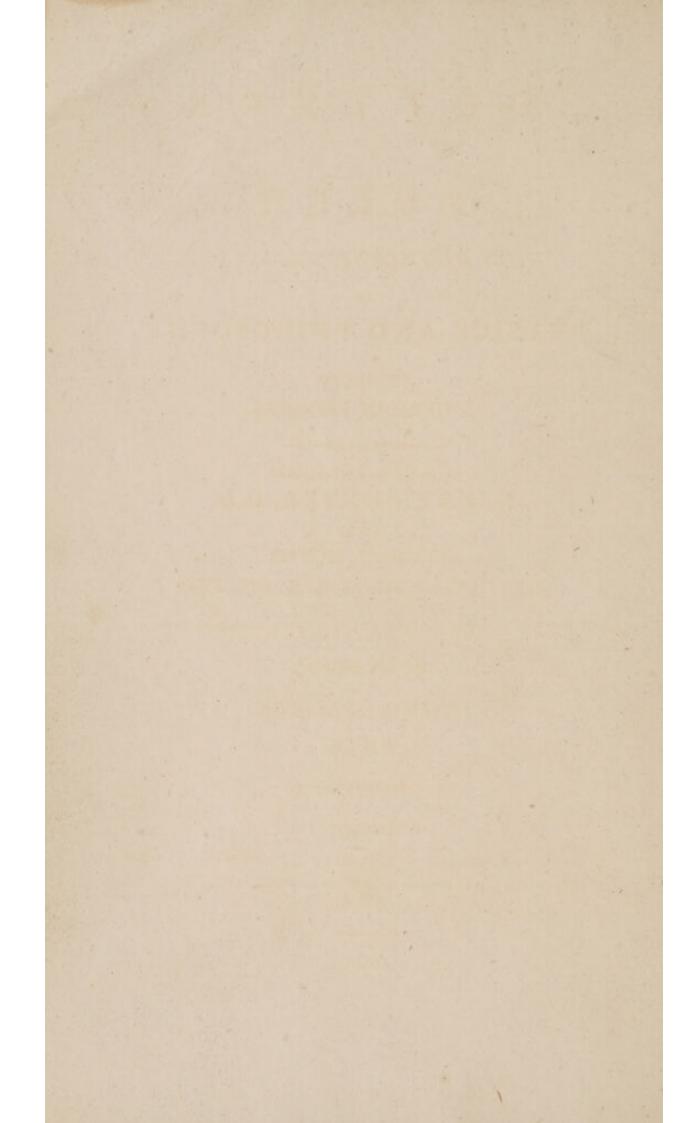


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# LETTERS

OF

# EULER

ON DIFFERENT SUBJECTS

IN

## PHYSICS AND PHILOSOPHY.

ADDRESSED TO

A GERMAN PRINCESS.

TRANSLATED FROM THE FRENCH BY

## HENRY HUNTER, D.D.

WITH

## ORIGINAL NOTES,

And a Gloffary of Foreign and Scientific Terms.

Second Edition.

IN TWO VOLUMES.

VOL. I.

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In confequence of the three Volumes of EULER in French being comprized in two, in the Translation, a few inaccuracies have occurred in the numbering of the Plates, which however will be remedied by the Plates being placed opposite the Pages, as above.

# PREFACE.

T was long a matter of furprize to me, that a Work fo well known, and fo justly esteemed, over the whole European Continent, as Euler's Letters to a German Princess, should never have made it's way into our Island, in the language of the Country. While Petersburg, Berlin, Paris, nay the capital of every petty German principality, was profiting by the ingenious labours of this amiable man, and acute philosopher, the name of Euler was a found unknown to the ear of youth in the British metropolis. I was mortified to reflect that the specious and seductive productions of a Rouffeau, and the poisonous effufions of a Voltaire, should be in the hands of fo many young men, not to fay

fay young women, to the perversion of the understanding, and the corruption of the moral principle, while the simple and useful instructions of the virtuous Euler were hardly mentioned.

I frequently suggested the idea of a translation to more than one literary friend, in whose ability for the task I could place greater considence than in my own: but not finding it undertaken, I determined, at length, to attempt it myself, with the ability which I had; and, in doing this, I considered myself as rendering a meritorious service to my country.

As foon as Providence had beflowed on me the bleffing of children, I felt it to be my duty to charge myfelf with their inftruction. How I have fucceeded it becomes not me to fay: but every day I live, the importance of early and proper



A confiderable part of our common fehool education, it is well known, confifts of the fludy of the elegant and amufing poetical fictions of Antiquity. Without meaning to decry this, may I not be permitted to hint, that it might be of importance frequently to recall young minds from an ideal world, and it's ideal inhabitants, to the real world, of which they are a part, and of which it is a shame to be ignorant. Let your pupil, by all means, read the poets; let him read Ovid, and, after he has amused himself with the golden age of old Saturn, lead him out into the open firmament of heaven, and shew him the venerable planet of that name, coeval with time, yet shining with unimpaired lustre, after fo many revolutions of ages. Having administered the antidote that may repel the poison, which a display of the lewd intrigues of a fabulous Jupiter or Venus naturally instill; let him view, through the

the telescope, the two beautiful stars so called, emitting their chafte and modest light to the unpolluted eye of fober reason. When he has diverted himself with the transformation of a lady into a bear, and that bear into a conftellation, point out to him the heavenly northern light, which never changes it's place, and, with undeviating fidelity, conducts the mariner through the feas of a hemisphere. Let him accompany Phaeton to the palace of the fun, and fmile at beholding the adventurous boy mount the flaming chariot; and then check his mirth by pointing to the glorious orb of day, travelling in the greatness of his strength; not dragged round the earth by fiery-footed steeds, but wheeling worlds on worlds, each in his feveral orbit, around him, with irrefiftible force.

Why should not the boy be taught the principle on which his kite flies?

Vol. I. b What

What more pleafant amusement can he have than to communicate to the needle the magnetic virtue, and to steer his course through the hazel grove, by a compass of his own constructing? Why not teach him to elicit the electric spark; and to assonish and delight his sisters with the wonders of the magic lantern?

EULER wrote these Letters for the infiruction of a young and sensible semale, and in the same view that they were written, they are translated, namely, the improvement of the semale mind; an object of what importance to the world! I rejoice to think I have lived to see female education conducted on a more liberal and enlarged plan. I am old enough to remember the time when well-born young women, even of the north, could spell their own language but very indifferently, and some hardly

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What

read it with common decency; when the young lady's hand-writing prefented a medley of outlandish characters; and when a column of pounds, shillings and pence presented a labyrinth as inextricable as the extraction of the cube root. While the boys of the family were conversing with Virgil, perhaps with old Homer himself, the poor girls were condemned to cross-stitch, on a piece of gauze-canvass, and to record their own age at the bottom of a sampler.

They are now treated as rational beings, and fociety is already the better for it. And wherefore should the terms female and philosophy seem a ridiculous combination? Wherefore preclude to a woman any source of knowledge to which her capacity, and condition in life, entitle her to apply? It is cruel and ungenerous to expose the frivolity of the sex, after reducing it to the necessity of being filly and frivolous. Cul-

tivate a young woman's understanding, and her person will become, even to herself, only a secondary concern; let her time be silled up in the acquisition of attainable and useful knowledge, and then she will cease to be a burden to herself and to every body about her; make her acquainted with the world of nature, and the world of art will delude her no longer.

The time, I trust, is at hand, when the Letters of Euler, or some such book, will be daily on the breakfasting table, in the parlour of every semale academy in the kingdom; and when a young woman, while learning the useful arts of pastry and plain-work, may likewise be acquainting herself with the phases of the moon, and the slux and resux of the tides. And I am persuaded she may thrum on the guitar, or touch the keys of the harpsichord, much more agreeably both to herself and others, by studying

fludying a little the theory of found. I have put the means of this in her power; it will be at once her fault and her folly if she neglect it.

In translating the Work, I have followed the last Paris Edition, given by Messirs. de Condorcet & de la Croix, in 1787, for the purpose of introducing the ufeful notes of these gentlemen; but I have taken the liberty to reftore, from the original edition, that of Mietau and Leipfic, in 1770, feveral paffages which the French Editor had thought proper to suppress. To some notes of my own I have added feveral others, furnished by two ingenious friends, whose names I am not at liberty to publish. The course of thirty-four years of a scientific age, must have supplied abundance of new facts and experiments, by which the philosophy of even a Euler may be corrected and improved. The translated notes of the Paris Edition, I have, for the fake of diffinction, marked with the characters F. E. and the original notes of this Edition, with the initials E. E. And I think it my duty, in this place, to vindicate to our ingenious countryman, Mr. Dollond, the optician, the difcovery of achromatic glaffes for telefcopes, mentioned in the letters on dioptrics; for that gentleman is, in truth, the Author of this valuable improvement.

I have had the illustrative plates engraved in a better style and manner than French artists generally employ on mathematical sigures: and to do credit to myself, not to say Euler, he appears in his English dress with every advantage which the stationer and printer could bestow. At the same time, in order to keep down the price as much as possible, instead of dividing the Work into Three

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Three Volumes, as in all the foreign editions, I have reduced mine to Two; as the division is altogether indifferent to the subjects.

It being generally acceptable to the Reader to know fomething about the man with whom he is converfing as an author; to gratify this curiofity, I have likewife given a translation of the Elogium of EULER, read before the Academy of Sciences, and prefixed to M. de Condorcet's edition, because it contains fome interesting traits of the character and events of the life of this diftinguished personage. But what is the life of a literary or fcientific man, and where are we to find the history of it? In his works. NEWTON and EULER are their own best biographers; and the library of every scholar in Europe exhibits a never-dying representation of what they were, and what they atchieved. We

b 4

have hardly a trace of Wren's personal and domestic habits; but every stone of St. Stephen's Walbrook, and of St. Paul's, is inscribed with his name, and transmits a memoir of the Architect.

It being generally acceptable to the

The frequent, tirefome, courtly address of Your Highness, except at the first setting out, I have entirely omitted; out of no disrespect to Princes, but because it seemed to me a mere unnecessary waste of words, which only encumber and disfigure a work of science. The Princess and her instructor are both gone to that awful world, in which the distinctions of the present, those of virtue excepted, are for ever obliterated.

As every book should be as complete in itself as possible, and this being deftined to the use of the unlearned, I have subjoined a glossary of the foreign and scientific words which occur in the course of these Letters. Some will, perhaps, think I may have fwelled this beyond the necessary fize, and given an explanation of many terms already fufficiently understood. If this be an error, it is on the fafe fide. I would rather infert twenty words of this description, than omit one with which an ordinary reader might be unacquainted, and his progrefs thereby retarded. And I well know, that there is often a vague and obscure idea of words floating in the brain, which a fhort description or an example would inftantly render precise and diftinet: and many young perfons would, without hefitation, confult a gloffary, who might be afraid, or ashamed, or, perhaps, too proud, to ask a question.

H. H.

Hoxton, 1802.



# ADVERTISEMENT.

BY THE FRENCH EDITOR.

THE Letters of EULER to a German Princess have acquired, over all Europe, a celebrity, to which the reputation of the Author, the choice and importance of the feveral fuljects, and the clearness of elucidation, justly entitle them. They have defervedly been confidered as a treasury of fcience, adapted to the purposes of every common feminary of learning. They may be studied to advantage without much previous elementary knowledge; they convey accurate ideas respecting a variety of objects, highly interesting in themselves, or calculated to excite a laudable curiofity; they inspire a proper taste for the sciences, and for that found philosophy which, supported by science, and never losing fight of her cautious, fleady, methodical advances, runs no risk of perplexing, or misleading the attentive fludent.

The only censure that can be passed on these Letters is, now and then, a digressive detail, somewhat

fomewhat too tedious, on questions rather foreign to the fciences, and confiderable inaccuracy in point of style. Without failing in the respect due to EULER, I thought myself at liberty to omit fome paffages altogether, and to correct the style of others. Few Readers, furely, will be fo fastidious as to refuse the admiration attached to the name of this illustrious man, for the fake of fome flight blemishes, in a work of such confiderable length. A genius, like his, which has fignalized itself by so many important discoveries, can fuffer no diminution of greatness, from his not having written a foreign language with claffical purity. A man whose transcendant powers have aftonished and confounded even those whom habits of profound reflection must have rendered hard to please, respecting prodigies of this fort, is not less worthy of veneration, that he did not apply the whole force of his mind to every object which presented itself. It is of the last indifference to his glory, whether these small specks are effaced, or fuffered to remain.

But the case is widely different as to the perfons for whose use the perusal of this work is particularly designed. It is of importance for young people, whether of France, or of any other country, to deser reading till they thoroughly understand the language of books, in which the rules of that language may be frequently violated. And the youth of the French nation must be cautioned against turning into ridicule a few uncouth expressions which, in the hurry of composition, may have dropped from the pen of a man of genius. Respect for every thing which merits this appellation is one of the sentiments which education ought most powerfully to inculcate, as it is one of the most infallible preservatives against prejudice of every kind, against the illusions of vanity and self-love, nay, against the passions which deprive us of the force necessary to our approximation toward these objects of universal admiration.

As to other retrenchments, they affect, almost all of them, reflections which relate less to the sciences and philosophy, than to theology, and frequently even to the peculiar doctrines of that ecclesiastical communion in which EULER lived. It is unnecessary to assign a reason for omissions of this description.

I have prefixed to this edition the Elogium of EULER, read before the Academy of Sciences, omitting only fome scientific details, which might have appeared tedious to certain Readers.

As the Letters of EULER contain nothing, on feveral questions, capable of interesting the generality of mankind, I have made some additions,

but without throwing them into the form of letters. Those published at the same time with this edition, have for their only object the calculation of probabilities. I took for granted that persons disposed to give them a perusal, must have already made a confiderable progress in mathematical knowledge. This branch of knowledge occupies at present, and ever must, a diftinguished place in a course of liberal education. If it is not absolutely impossible to do without it, in order to the attainment of accurate ideas in physics, and respecting the laws of the universe, and the calculations of probability, we shall, at least, by the study of mathematics, fave much time and trouble, and acquire a habit of thinking and reasoning on other subjects with greater exactness.

The idea which some have formed of the difficulty of this science, obstructs the progress of knowledge, and is not sounded in truth. There are sew minds, unless a previous education has already impressed false ideas, and a factitious delicacy, but what are capable of receiving the ideas necessary to mathematical combination, of acquiring the habit of pursuing them, and a relish for the simple truths which they present. As to the extraordinary powers which are deemed requisite, I venture to affirm, that there are sew persons.

perfons, even of moderate capacity, who may not, by employing a little more time, and purfuing a course somewhat more deliberate, by entering more attentively into detail, and from frequently repeated applications, attain a degree of mathematical knowledge, far beyond what is really useful, nay, I add, necessary, to all men of liberal education. perfors, even of moderate capacity, who may not, by employing a little more time, and purfuing a courie formewhat more deliberate, by entering more attentively into detail, and from fixquently repeated applications, attain a degree of mathematical knowledge, far beyond what is really ufeful, may, I add, necessary, to all men of liberal education.

## ELOGIUM OF EULER.

EONARD EULER, President of the Mathematical School, in the Academy of Petersburg, and previously in that of Berlin; Fellow of the Royal Society in London; and of the Academies of Turin, Lisbon and Bâle; Foreign Associate of that of the Sciences, was born at Bâle, April the 15th, 1707, being the son of Paul Euler and Margaret Brucker.

His father who, in 1708, undertook the pastoral charge of the village of Riechen, in the vicinity of Bâle, was his first instructor; and he enjoyed betimes the pleasure of contemplating the progress of his son's expanding faculties, and dawning glory, a cordial so reviving to the heart of a parent, advance under his own eye, and gather strength from his own assiduities.

He had studied mathematics under James Bernouilli. It is well known, that this celebrated scholar united to a great genius for the sciences, a profound philosophy, which is not always the companion of this genius, but which serves to give it a wider range, and to render it's exertions more useful. In teaching, he endeavoured to impress on his pupils, that geometry is not a detached science, but exhibited it to them as, at once, the basis and the key-stone of Vol. I.

all human knowledge; as the science in which the progress of the mind may be the most distinctly observed; the science, the cultivation of which exercises our faculties to the greatest advantage, as giving to the understanding, at one and the same time, strength and accuracy; sinally, as a study equally valuable, from the number and the variety of it's applications, and from it's tendency to inure the student to a method of reasoning, which may, afterwards, be successfully employed, in the investigation of every species of truth, and as a guide in the conduct of life.

Paul Euler, who had fully imbibed the principles of his mafter, inftructed his fon in the elements of mathematics, though he had deftined him, ultimately, to the fludy of theology; and fuch was young Eu-LER's early proficiency, that on being fent to the university of Bâle, he was deemed not unworthy of the attention and particular inftructions of John Bernouilli. Such was his application, and fuch his happy dispositions, as quickly to secure to him the friendship of Daniel and Nicolas Bernouilli, the pupils, and, by this time, the rivals of their father. Nay, he had the felicity of getting into the good graces of the fevere John Bernouilli himfelf, who carried his condefcension so far as to give him a private lesson, once a week, in the view of removing any difficulties which might occur in the course of reading and study. EULER employed the other days of the week in fuch a manner as would enable him to make the most of this diftinguished mark of favour.

This excellent method of profecuting his ftudies, preferved opening genius from exhaufting it's ftrength, in combating infuperable difficulties, and from wandering in unknown mazes, which it might attempt to unravel: it directed and feconded his own exertions; but, at the fame time, laid him under the heceffity of calling forth all his powers, which, accordingly, received conftant increase from an exercise proportioned to his age, and to the progress in knowledge which he had already made.

But of this fingular advantage he was foon deprived; for fearcely had he attained the degree of Master of Arts, when his father, who intended him for his own successor, enjoined him to exchange the study of mathematics for that of theology. Happily, the effect of this act of authority was of short duration. It proved no difficult matter to persuade the father, that his son was destined to supply, to the learned world, the place of John Bernouilli, and not to sink into the obscure, parson of Riechen.

An effay, composed by EULER in his nineteenth year, on the masting of ships, a subject proposed by the Academy of Sciences, procured him, in 1727, an addition to his academical honours, so much the more respectable, that the youthful native of the Alps could have derived no affistance from practical knowledge, and that he yielded the palm to Mr. Bouguer alone, an able geometrician, then at the zenith of his reputation, and, for ten years before, professor of hydrography in a maritime city.

About the fame period, EULER stood candidate

for a vacant chair in the university of Bale: but it is fate, or chance, that settles the dispute between competitors for offices of this fort, and, on this occasion, it was unfavourable, I do not say to EULER, but to his country, which, a few days afterward, lost him for ever.

Two years before this, Daniel and Nicolas Bernouilli had been invited to Russia. Euler felt the sincerest regret at parting with the friends of his youth, and engaged them to promise their utmost exertions to procure him a similar invitation, which he was eager to participate. This needs to excite no surprize. The splendor of the capital of a vast empire, the glare dissusing itself over the pursuits of which it is the theatre, and over the very persons of it's inhabitants, scems to confer a glory on them, capable of easily seducing a youthful imagination, and of dazzling the free, but poor and obscure, citizen of a petty republic.

The brothers, Bernouilli, were conscientiously faithful to their promise, and exerted themselves as strenuously, to bring forward a competitor so formidable, as ordinary men would have done to keep a rival out of sight.

EULER's journey to Russia commenced under auspices the most melancholy and discouraging. It was not long before he received intelligence, that Nicolas Bernouilli had fallen a victim to the severity of the climate; and the very day he set foot on Russian ground, Catharine I. paid the debt of nature. This event, at first, seemed to threaten the approach-

ing diffolution of the Academy, whose establishment that Princess had just completed, in compliance with the will of the deceased Czar, her husband.

EULER, at a prodigious distance from his native country, destitute of the advantage which Daniel Bernouilli possessed, that of an illustrious and respected name, to prepare his way, formed the resolution of entering into the Russian marine service. One of the admirals of Peter I. had already promised to procure him a situation; when, happily for geometry, the storm, which lowered over the sciences, spent itself. Daniel Bernouilli retired to his own country: EULER was declared Professor of Geometry, and successor to his illustrious friend, in 1733. The same year he married a young lady of the name of Gsell, a compatriot of his own, the daughter of a painter, whom Peter I. had brought with him to Russia, on returning from his sirst voyage.

From this time forward, to use Bacon's expression, Euler selt that he had given hostages to fortune: and that the country, in which he could hope to form an establishment for his family, was necessarily transformed into his native country. Born and educated in the bosom of a nation, all whose governments preserve, at least, the appearance and the language of a republican constitution; in which, notwithstanding distinctions more real, than those which separate between the highest slave of a despot and the lowest of his subjects, the forms of equality have always been scrupulously observed; in which the respect due to the laws extends to usages the most indifferent, pro-

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vided they have the fanction of antiquity, and of vulgar opinion: EULER found himself in a country, where the Prince exercises unlimited authority; where the most facred law of absolute governments, that which regulates the fuccession to the throne, was at that time uncertain, or treated with contempt; where grandees, enflaved to the fovereign, rule with a defpotic fway over an enflaved people; where, at the very moment, a vast empire, under the government of an ambitious, jealous and cruel foreign despot, was enduring all the tyranny of the unrelenting Biren, and prefenting a spectacle as terrifying as instructive to men of letters, who had been enticed to feek in it's bosom, glory, fortune, and the power of enjoying, in perfect fecurity, the calm delights of literary refearch.

It is easier to conceive, than to describe, what must have been the seelings of Euler, bound to remain in such a situation, by chains which it was impossible for him to burst asunder. To this circumstance, however, we are, perhaps, indebted for that unremitted application to literary pursuits, of which he then acquired the habit, and which became his only resource, in a capital, silled with the parasites, or the enemies, of a violent Minister; the former intent on feeding and slattering his suspicious temper; the latter employed in securing themselves from it's sanguinary effects. This had made so deep an impression on the mind of Euler, that we find the traces of it so late as 1741, the year after Biren's fall, when tyranny had given place to a government more mild

and humane. At that period he went from Petersburg to Berlin, on the earnest solicitation of the King of Prussia. He was presented to the Queenmother. This Princess took great pleasure in the conversation of enlightened men: she received them with that noble familiarity which announces, in Princes, the fentiment of a perfonal greatness, independent of rank and title, and which has become one of the characteristic marks of that august family. The Queen of Prussia, however, could extract from EULER monofyllables only: fhe taxed him with a timidity and referve, which the cordiality of his reception could not possibly have inspired: Why, then, will you not talk to me, faid the Queen? Because Madam, replied he, I have just come from a country, where people are banged, if they talk.

Feeling myself now called upon to give some account of EULER's immense scientific labours, I shrink from the impossibility of following him in detail, of conveying any thing like an accurate idea of that multiplicity of discoveries, of new methods of investigation, of ingenious views, dissused over more than thirty separate publications, and over near seven hundred memoirs, of which about two hundred, deposited in the Academy of Petersburg previous to his death, are destined to enrich, in their order, the future collections published by that learned body.

But a particular character feems, to me, to distinguish Euler from the other illustrious men who, in pursuing the same career, have attained a glory which his has not eclipsed; that character is, his having embraced the mathematical fciences in their univerfality; his having brought to perfection, one after another, the different parts; and, enriching the whole by important discoveries, his having produced a very beneficial revolution in the manner of treating them. I imagined, therefore, that in sketching a methodical representation of the different branches of these sciences, in pointing out the progress of each, and the happy improvements to be ascribed to the genius of Euler, I should give, at least as far as my ability permits, a juster idea of this wonderful man, who, by uniting so many extraordinary talents, has presented a phenomenon, if the expression may be allowed, of which the history of science has hitherto furnished no example.

Algebra had long been a science of very limited use and application. The mode of considering the idea of magnitude, only in the highest degree of abstraction of which the human mind is susceptible; it's rigoroufly feparating from that idea every thing which, by employing imagination, might give fupport, or repose, to the understanding; finally, the extreme generality of the figns which this fcience makes use of, render it in some measure too foreign to our nature, too remote from ordinary conception, to admit of the mind's taking extraordinary pleafure in it, and of eafily acquiring a habit of tracing it's operations. The algebraic method is apt to discourage even perfons the most disposed to abstract speculation. If the object of pursuit be ever so little complicated, we are forced to lose fight of it entirely,

and to confine our whole attention to dry algebraic characters; the road is fafe and fure, but the point which is aimed at, and that from whence we took our departure, equally vanish from the eye of the geometrician; and it required no flight degree of courage, to venture out of fight of land, without any other pilot than a recently discovered science. Accordingly, on examining the works of the great geometricians of the last age, even of those to whom algebra is indebted for the most important discoveries, we shall see how little they were accustomed to handle this very weapon, which has been brought to fuch a state of perfection; and it is impossible to refuse to EULER the praise of having effected a revolution, which renders algebraic analysis a mode of calculation luminous, univerfal, of general application and of eafy acquisition.

Thus, at certain epochs, when after strenuous exertions the mathematical sciences seemed to have exhausted all the resources of genius, and to have reached the ne plus ultra of their career; all at once a new method of calculation is introduced, and the face of the science is totally changed. We find it immediately, and with inconceivable rapidity, enriching the sphere of knowledge, by a solution of an incredible number of important problems, which geometricians had not dared to attempt, intimidated by the difficulty, not to say the physical impossibility, of pursuing calculation to a real issue. Justice would, perhaps, demand, in favour of the man who invented

and introduced these methods, and who first taught their use and application, a share in the glory of all those who have practised them with success; he has, at least, claims upon their gratitude, which cannot be contested without a crime.

EULER had neglected no part of analysis: he has demonstrated some of the theorems of Fermat, on indeterminate analysis, and has discovered many others, no less curious, and of no less difficult investigation. The knight's movement, in the game of chefs, and different other problems of fituation, have likewife excited his curiofity, and exercifed his genius. He blended with refearches the most important, amusements of this fort, frequently more difficult, but of little use either to the progress of the science itself, or to the applications hitherto attempted. EULER was too discreet, not to be sensible of the impropriety of devoting much of his attention to refearches of mere curiofity; but at the fame time of a mind too enlarged not to difcern, that their inutility could only be momentaneous, and that the only means of exposing their inutility, was to attempt to unfold and generalize them.

The particular questions which do not strictly belong to the regular body of mathematical science, which do not enter into the applications of which it is susceptible, ought not to be considered merely as the means of exercising the powers, and displaying the genius of the geometrician: in cultivating the sciences, we almost always set out with attaching ourselves to some detached parts, in preference; in proportion as successive discoveries multiply, the relations which unite the parts gradually appear; and to the illumination resulting from this union, we are most frequently indebted for the great discoveries, which form an era in the history of the human mind.

I shall conclude this brief representation of EULER's labours, on pure analysis, with observing, that it would be injust to limit it's influence on the progress of mathematics, to the innumerable discoveries with which his works abound. The communications which he has opened between all the parts of a science so extensive; those general views which sometimes he does not so much as indicate, but which cannot escape an attentive observer; the paths, whose entrance he has satisfied himself with clearing by removing the first obstacles which opposed; these are so many more benefits conferred on the sphere of science, and of which posterity will undoubtedly avail itself, while perhaps the hand which bestowed them may be forgotten.

The treatife on mechanics, which EULER gave to the world in 1736, is the first great work in which analysis has been applied to the science of motion. The number of things, entirely new, or exhibited in a new light, which this book contains, would have astonished geometricians, had not EULER already published, separately, the greatest part of it.

In his endless labours on the same science, he was ever faithful to analysis, and the happy use he made of it, has at last procured for the analytical method a preference to every other.

The problem of vibrating chords, and all those which belong to the theory of sound, or the laws of the oscillation of the air, have been subjected to analysis, by the new methods with which he enriched the calculation of partial differences. A theory of the motions of sluids, sounded on the same calculation, astonished every one by the clearness which he has diffused over questions so intricate, and the facility which he has communicated to modes of operation, sounded on an analysis so profound.

All the problems of physical-astronomy, treated in the present age, have been resolved, by the analytical method peculiar to Euler. His calculation of the perturbations of the earth's orbit, and especially his theory of the moon, may be held up as models of the simplicity, of the precision, to which this method may be carried; and in reading this last work, we see, with no less astonishment, how far a man of great genius, animated with a desire of omitting nothing essential on an important question, has been able to carry the patience and perseverance of application.

Astronomy employed only the geometric method: EULER was sensible of every thing which that science had to expect from the aid of analysis, and he demonstrated it by examples which, imitated since by men of ability and reputation, may in time bestow a new form on astronomy.

He treated, in all it's extent, the naval science; in an elaborate work, to which an intelligent analysis ferves as basis, and in which questions of the greatest difficulty are fubjected to this general and fertile method, which he understood so well to create and to employ. He published, many years afterward, on the fame fubject, an elementary abridgment of this treatife, containing, under the fimplest form, every thing useful in practice, and necessary to be known by perfons who devote themselves to the marine fervice. This work, though defigned by the Author merely for the schools of the Russian empire, procured for him a liberal gratification from the King of France, who judged, that labours beneficial to mankind demanded the grateful acknowledgments of all Sovereigns, and who wished to demonstrate to Europe, from one extremity to another, that talents fo rare could neither be overlooked, nor remain unrewarded. EULER was abundantly fenfible of the value of this mark of respect from a great Prince; and it derived an additional charm, in his eyes, from the hand through which it was transmitted, that of Mr. Turgot, a minister universally respected for his talents and for his virtues; a man formed for commanding opinion, rather than following it, and whose fuffrage, ever dictated by truth, and never by the defire of attracting to himfelf the applause of the public, might be an acceptable piece of flattery, even to a wife man, too much accustomed to glory to be still awake to the voice of fame.

In men of a superior genius, extreme simplicity of character may easily consist with those qualities of mind, which most forcibly announce ability and delicacy of feeling. Euler, accordingly, notwithstanding that simplicity which never forsook him, knew; however, to distinguish with a sagacity, always indulgent it is true, the homage of enlightened admiration from that which vanity lavishes on great men; to secure to itself at least the merit of enthusiasm.

His dioptrical refearches are founded on an analysis less profound, and we are tempted to give him credit for it, as being a kind of facrifice. The different rays of which a folar ray is formed, fubfift in the same medium of different refractions; separated thus from adjacent rays, they appear fingle, or less blended, and give the fenfation of the colour proper to them. This refrangibility varies in different mediums for every ray, and in conformity to a law which is not the same with that of the mean refraction in these mediums. This observation suggested a belief, that two unequal prisms, and of different fubstances, combined, might divert a ray from it's direction, without decompounding it, or rather by replacing the elementary rays, by refraction, in a parallel direction. On the truth of this conjecture might depend, in telescopes, the destruction of the iris, which colours objects viewed through lenticular glasses. Euler was convinced of the possibility of fuccefs, conformably to this metaphyfical idea, that, if the eye is composed of different humours, it is only in the

the view of destroying the effect of the aberration of refrangibility. The only thing requisite, therefore, was an attempt to imitate the operation of nature, and he proposed the means of execution according to a theory which he had formed. His first essays induced naturalists to attend to an object which they feemed to have neglected. Their experiments did not correspond to Euler's theory, but they confirmed the views he entertained respecting the perfection of telescopes. And, instructed by these, in the laws of dispersion, in different mediums, he abandoned his first ideas, subjected to calculation the refult of their experiments, and enriched dioptrics with analytical formules, fimple, commodious, general, and applicable to inftruments of every poffible construction.

We have, befides, fome effays of EULER, on the general theory of light, the phenomena of which he endeavoured to reconcile with the laws of the ofcillations of a fluid; because the hypothesis of the emission of rays in a straight line, appeared to him to present insurmountable difficulties. The theory of the loadstone, that of the propagation of sire, the laws of the cohesion of bodies, and those of friction, surnished him, likewise, with subjects of ingenious calculations, but, unfortunately, supported by hypothesis, rather than by experiment.

The calculation of probabilities and political arithmetic were farther objects of his indefatigable application. I shall here only mention his researches

on bills of mortality, and the means of deducing them from phenomena with greater exactness; his method of striking a medium from the observations made; his calculations respecting the establishment of a reversionary fund, in the view of securing to widows, or orphans, either a fixed sum, or an annual revenue, payable after the death of a husband or father; an ingenious and humane method, devised by philosophic geometricians to counterbalance the moral evil resulting from the settlement of life-annuities, and to convert, to the relief of families, the smallest savings from the principal's daily earnings, or from the revenue of a commission, a place or a pension.

We have feen in the elogium of Daniel Bernouilli, that he had divided with EULER alone the glory of having carried off thirteen prizes, proposed by the Academy of Sciences: They often contended for the fame object, and occupied the fame ground: and the honour of triumph over a competitor was likewife divided between them; but this rivalfhip never encroached on the expressions of reciprocal esteem, nor cooled the ardor of mutual friendship. On examining the fubjects for which the one or the other obtained the victory, we find that fuccess depended principally on the character of talent peculiar to each. When the question required address in the manner of taking it up, a dexterous application of experiment, or new and ingenious physical views, Daniel Bernouilli had the advantage: but did it prefent

fent difficulties, which profound and accurate calculation could refolve; was it necessary to create a new method of analysis, victory declared for EULER. Were any one so prefumptuous as pretend to judge between them, he would find that he had to pronounce, not between two men, but between minds of a different genius, between two methods of employing genius.

I should have conveyed but a very imperfect idea of EULER's fertility of invention, unless I added to this faint sketch of his labours, that there are very few subjects of importance, once treated by him, that he did not retrace; nay, so far as to recompose his first work several times over. Sometimes he substituted a direct and analytical method, in place of one more indirect: sometimes he extended his first solution to cases which had at first escaped him; adding almost always new examples, which he knew how to select with singular skill among those which presented, or some useful observation, or curious remark.

The intention merely of giving to one of his productions a form more methodical, of rendering it fomewhat more luminous, of bestowing on it a higher degree of simplicity was to him motive sufficient for engaging in labours incredible. Never did geometrician write so much, and no one ever carried his works to such a height of perfection. When he published a memoir on a new subject, he simply explained the track which he pursued; he pointed out

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ing, with ferupulous exactness, made them accompany the progress of his own mind, in his first essays, he shewed them afterwards how he had been enabled to trace a simpler path. It is evident, that he preferred the instruction of his disciples to the silly satisfaction of dazzling them by his own superiority; and that he did not believe he had done enough for science, unless he added, to the new truths with which he was enriching it, a candid exposition of the ideas which led to discovery.

On reading the life of a great man, whether it be a conviction of the imperfection attached to frail humanity; whether it be, that the justice of which we are capable, does not rife so high as to induce us to acknowledge a superiority for which nothing can be an adequate compensation; or, sinally, whether it be, that the idea of perfection in another mortises or humbles us still more than that of his greatness, but some how or another it seems necessary for us to sind out some weak part; we hunt after the discovery of a defect in him, which may reconcile us to ourselves; and we are involuntarily disposed to call in question the impartiality of the Biographer, unless he points out the weak part, unless he withdraws the impertinent veil which conceals the defect.

EULER fometimes appeared to be taken up with the mere pleasure of calculation, and to consider the point of mechanics, or physics, which he was examining, only as an occasion of exercising his genius, and of the learned have accordingly accused him of lavishing his talent for calculation on physical hypotheses, or even on metaphysical principles, of which he had not sufficiently examined either the probability or the solidity. He has likewise been accused of depending too much on the resources of calculation, and of having neglected those with which he might have been supplied, by the examination of the very questions which he proposed to resolve.

We must admit, that the sirst of these charges is not altogether destitute of foundation. In EULER, undoubtedly, the metaphysician, or even the naturalist was not so great as the geometrician; and we are constrained to regret, that in many parts of his works, those, for instance, which he composed on the naval science, on artillery, have been of little use, except to the progress of the science of calculation.

But the fecond charge appears by no means fo well founded. We observe uniformly, through all the works of Euler, an unremitting effort to add to the riches of analysis, to extend, and to multiply the applications of it: at the same time that it appears to be his only instrument, we see clearly that it is his wish to make it universally so. The natural progress of the mathematical sciences must have, in time, brought about this revolution; but he saw it, if I may say so, completed under his own eye: to his genius we are indebted for it; and it has been the

reward of all his exertions and discoveries. Accordingly, even when he appears to be misapplying analysis, and exhausting all it's secret stores in resolving a question, of which a few reslections, foreign to calculation, would have given him an easy and simple solution, he was frequently only aiming at a demonstration of the power and resources of his art; and he merits forgiveness at least, if sometimes, while he seemed taken up with another science, it was still to the progress and propagation of analysis that his attention was devoted; and the revolution which this has effected in the world of science, is one of his first claims on the gratitude of mankind, and the fairest title to glory.

I thought myself obliged not to interrupt the detail of *Euler*'s scientific pursuits, by a recital of the few and simple events of his life.

He fettled at Berlin in 1741, and remained there till 1766.

The Princess d'Anhalt Dessau, niece to Frederick II. King of Prussia, was desirous of receiving from him some lessons in natural philosophy. These lessons have been published, under the title of Letters to a german princess, a work inestimable for the singularly clear light in which he has displayed the most important truths of mechanics, of physical-astronomy, of optics, and of the theory of sound; and for the ingenious views, less philosophical but more sage, than those which have made Fontenelle's Plurality of Worlds outlive the System of Vortices.

The name of EULER, so great in the sphere of science; the respectful idea attached to his works, employed in unfolding all that is intricate and abstract in analysis, disfuse a singular charm over these letters, so simple, and so easy. Those who have not studied mathematics, astonished, perhaps slattered, at being able to understand a work of EULER, will feel grateful to him for having descended to their level; and these elementary details of the sciences acquire a species of greatness, from their approximation to the glory, and the genius, of the illustrious man who traced them.

The King of Prussia employed EULER in calculations respecting the coinage; on constructing the aqueduct of Sans-Soucis; on the formation of several navigable canals. That great Prince had a mind too enlarged to believe that extraordinary talents, and profound knowledge, ever could be useless or dangerous qualities; and the felicity of being able to do good, an advantage reserved by nature for ignorance and mediocrity.

In 1750, EULER made a journey to Frankfort, to receive his mother, then a widow, and to conduct her to Berlin. He had the happiness to preserve her till 1761. For eleven years, then, she enjoyed the glory of her highly distinguished son, in the way that the maternal heart knows how to enjoy, and was still more happy, perhaps, in the tender and assiduous expressions of silial affection, the value of which that glory greatly enhanced.

During his refidence at Berlin, EULER, united to Mr. de Maupertuis by the ties of gratitude, thought himself obliged to defend the principle of the least action, on which the President of the academy of Prussia had founded the hope of a reputation fo exalted. The means which EULER thought proper to use could hardly have been employed by any other perfon but himfelf; it was to refolve, on this principle, feveral of the principal and most difficult problems of mechanics. Thus, in the age of fable, the Gods vouchfafed to forge, for their favourite warriors, armour impenetrable by all the blows of their enemies. It were to have been wished, that Euler's gratitude had confined itself to a protection so noble, and so worthy of himself; but it cannot be denied, that there is an infusion of asperity, rather too strong, in his replies to Kænig; and with forrow we are conftrained to recognize a great man, among the enemies of an unfortunate and perfecuted scholar. Happily for EULER, the whole tenor of his life shelters him from a more ferious fuspicion. But for that fimplicity, that indifference to the voice of fame, which he uniformly manifested, it might have been sufpected, that the pleafantries of an illustrious partifan of Kanig (pleafantries which Voltaire himfelf has justly configned to oblivion) had formewhat foured the temper of the gentle and fage geometrician; but if on this occasion he is chargeable with a fault, it must be imputed folely to an excess of gratitude; and if once in his life he acted wrong, the motive at least is respectable.

The Ruffian forces having, in 1760, penetrated into the marches of Brandeburg, plundered a farm of EULER's, near Charlottenburg: but General Tottleben had not come to make war on the sciences. Being informed of the lofs which EULER had fuftained, he haftened to repair it, by ordering payment far beyond the real value of the property, and having communicated to the Empress Elizabeth, an account of this involuntary difrespect, she was pleased to add a gratuity of four thousand florins to an indemnification already more than fufficient. anecdote is not fo generally known as it deferves to be, while we quote, with enthusiastic admiration, fimilar actions transmitted to us from antiquity. Is not this difference in the judgments we form, a proof of the happy progress of the human species, which certain authors still obstinately persevere in denying, apparently to shun the imputation of having contributed to it?

The government of Russia had never treated Eu-LER as a stranger. Notwithstanding his absence, part of his falary was always regularly paid; and in 1766, the Empress having given him an invitation to return to Petersburg, he complied.

In 1735, the exertion occasioned by an astronomical calculation, for which other academicians demanded several months, but completed by him in a few days, brought on an indisposition, which issued in the loss of one of his eyes. He had reason to apprehend a total loss of sight, if he continued to ex-

pose himself in a climate, the influence of which was unfavourable to his constitution. The interest of his family got the better of this apprehension; and if we reflect that, to EULER, study was an exclusive passion, we shall readily conclude, that few examples of paternal tenderness have more completely demonstrated, that it is the most powerful, and the sweetest of all our affections.

A few years after, he was overtaken by the calamity which he forefaw and dreaded: but happily for himfelf, and for the sciences, he preserved still the faculty of distinguishing large characters traced on a slate with chalk. His sons, his pupils, copied his calculations; wrote, as he dictated, the rest of his memoirs; and if we may form a judgment of these from their number, and frequently from the genius transfused through them, it will appear abundantly credible, that from the absence still more absolute of all distraction, and from the new energy which this constrained recollection gave to all his faculties, he gained more, both as to facility and means of labour, than he lost by a diminution of sight.

Besides, Euler, by the nature of his genius and his habits of life, had even involuntarily laid up for himself extraordinary supplies. On examining those great analytical formules, so rare before his time, but so frequent in his works, the combination and display of which unite so much simplicity and elegance, whose very form pleases the eye as well as the mind, it will be evident, that they are not the re-

fult of a calcalation traced on paper, but that, produced entirely in the head, they are the creation of an imagination equally vigorous and active.

There exift in analysis, and Euler greatly multiplied their number, formules of a common and almost daily application; he had them always present to his mind, knew them by heart, repeated them in conversation; and Mr. d'Alembert, when he saw him at Berlin, was aftonished at an effort of memory, which demonstrated, that EULER possessed at once a strength and a clearness of recollection almost incredible. At length his facility of calculation by the head was carried to fuch a degree as would exceed all belief, had not the hiftory of his labours accuftomed us to prodigies. He has been known, in the view of exercifing his little grandfon in the extraction of the fquare and cube roots, to have formed to himself the table of the fix first powers of all numbers from 1 to 100, and to have preserved it exactly in his memory. Two of his pupils had calculated as far as to the seventeenth term of a convergent feries, abundantly complicated; their refults, though formed after a written calculation, differed one unit at the fiftieth figure: they communicated this difference to their mafter: EULER went over the whole calculation in his head, and his decision was found to be the true one.

From the time he loft his fight, his chief amusement was to make artificial magnets, and to give lessons in the mathematics to one of his grand-chil-

dren,

dren, who feemed to have a promising disposition to that science.

He made a point of still going occasionally to the Academy, especially if delicate circumstances demanded his attendance, or when he deemed his prefence necessary to the maintenance of liberty. It is eafy to conceive how much it is in the power of a perpetual prefident, appointed by the court, to difturb the peace of an Academy, and how much fuch a feminary has to apprehend from one who, not being elected from their own number, does not feel himfelf restrained even by a sense of that support which his reputation needs from the fuffrages of his colleagues. How is it possible for men, employed folely in calm literary pursuits, and understanding no language but that of the sciences, to defend themselves in fuch a case; especially if strangers, unconnected, far from their country, they derive their whole fupport from that government, to which they would appeal for justice against an imperious president, whom that very government had placed over them.

But there is a degree of glory, which places a man beyond the reach of fear: it is, when all Europe would rouse itself to resent a personal injury offered to a great man, that he can without risk oppose to injustice the authority of his reputation, and elevate, in support of the sciences, a voice which will make itself heard. Euler, gentle, modest as he was, was sensible of his power, and oftener than once made a very happy use of it.

In

In 1771, the city of Petersburg suffered severely from a terrible conflagration: the flames had caught the house of EULER. One Peter Grimm, a native of Bâle, whose name well deserves to be transmitted to posterity, apprized of the danger of his illustrious compatriot, now blind and enfeebled, burst through the midst of the fire, reaches his apartment, places him on his shoulders, and faves EULER's life, at the hazard of his own. His library, his furniture was destroyed, but the zeal and exertions of Count Orloff preferved his manufcripts. The attention paid to this, at the height of a calamity fo dreadful, is the most honourable and flattering homage which public authority could have offered to science. The house of Euler was one of the Empress's gifts to him; a fimilar act of munificence speedily repaired the lofs.

He had by his first wife thirteen children, eight of whom died young. His three sons survived him, but he had the misfortune to lose both his daughters, the last year of his own life. Of thirty-eight grand-children, twenty-six were living at the time of his death. In 1776 he entered a second time into the married state, by espousing a Miss Gsell, sister to his sirst wife's father. He had always retained all that simplicity of manners, of which his father's house had set the example. As long as his sight remained, he every evening collected, to domestic devotion, his grand-children, his domestics, and such of his pupils as lodged in the house; he read to them a portion

of Scripture, and fometimes accompanied it with an exposition.

He was of a very religious turn of mind. He published a new demonstration of the existence of God, and of the spirituality of the soul: this last treatise has been admitted as a standard book into several colleges of divinity. With scrupulous exactness he adhered to the religion of his country, which is rigid Calvinism: and it does not appear that, after the example of most scholars of the protestant persuasion, he ever took the liberty of adopting peculiar ideas, or of forming a system of religion for himself.

His erudition was very extensive, especially in the history of mathematics. It is alleged that he had carried his curiofity fo far as to acquire the knowledge of the processes and rules of astrology; and that he had even made fome applications of them. However, when in 1740 he was commanded to calculate the nativity of Prince Ivan, he excused himfelf, by reprefenting that this was the proper business of Mr. Kraaff, in quality of royal astronomer. Credulity of this fort, which we are aftonished to find at so recent a period in the Court of Ruffia, prevailed, the age before, in all the Courts of Europe: those of Asia have not yet shaken off this abfurd yoke, and it must be acknowledged, that if we except the common maxims of morality, there is no one truth which can boaft of having been fo generally adopted, and through fuch a fuccession

fuecession of ages, as certain ridiculous or pernicious errors.

EULER had studied almost every branch of physics, anatomy, chemistry, botany; but his superiority in mathematics did not permit him to attach the slightest importance to his proficiency in any other branch of science, though it was such as might have induced a person more susceptible of the slattery of self-love to aspire to the title of an universal scholar.

The fludy of ancient literature, and of the learned languages, had formed part of his education: he retained a tafte for these to the end of life, and never forgot any thing he had once acquired; but he had neither time nor inclination to prosecute farther his attainments in classic literature. He had not so much as read the modern poets, but knew the Eneid by heart. Euler, however, did not lose sight of the mathematics, even in reciting the verses of Virgil. Every thing concurred to present him with this darling object of his thoughts, and we find among his works, an ingenious memoir on a question in mechanics, the first idea of which, he tells us, was suggested by a line of Virgil.

It has been faid that, to men of great talents, the pleafure of exertion is a reward still more gratifying than glory itself: were it necessary to prove this truth by examples, that of EULER would put it beyond a doubt.

In his most profound discussions with celebrated geometricians, he never betrayed the slightest symptom

tom which could excite a suspicion of his being actuated by motives of felf-love. He discovered no eagerness to affert his title to the merit of his discoveries; and if any thing in his works was claimed as the discovery of another, he was at pains to repair the involuntary offence, even without enquiring too fcrupuloufly, whether rigid juffice demanded an abfolute renunciation. Did any one pretend to have detected him in error, if the charge was unfounded, he forgot it; if just, he corrected it, without stopping to observe that, in many cases, the merit of those who boasted of having made the detection, confifted wholly in an eafy application of the methods which he himself had taught them, to theories, the greatest difficulties of which he had before-hand removed.

Men of middling ability almost always endeavour to make themselves of consequence, by an affected severity, proportional to the losty idea which they wish to convey of their understanding, or of their genius. Inexorable to all that rises above them, they give no quarter even to inseriority; so that we are tempted to say, a secret consciousness shews them the necessity which they are under of lowering others. An instinctive emotion engaged Euler, on the contrary, to celebrate genius the moment that it's first exertions had challenged his attention, and without waiting till public opinion courted the sanction of his suffrage.

He has been known to employ his time in refolving problems

problems already folved, which was to procure for him, at most, the inferior praise of greater elegance, or exactness of method; and this with the same ardor and perseverance that he could have exerted in the prosecution of a new truth, the discovery of which might have brought him an increase of reputation. Besides, had an ardent desire of glory actually existed in his breast, it would have been impossible for him, such was the frankness of his character, to conceal it's emotions. But the glory which he was so little solicitous to pursue, sought and sound him out. The singular fertility of his genius was a striking phenomenon, even to persons who were not in a condition to understand his works.

Though wholly devoted to geometry, his reputation challenged the attention of men little versed in that science; and he appeared in the eyes of all Europe not only the first of geometricians, but a great man. It is the custom of Russia to bestow military titles on men wholly unconnected with the fervice. This is paying homage to a prejudice which would reprefent the profession of a soldier as the only title to nobility, but the practice is at the fame time a direct acknowledgment of it's complete falfity. Some of the Literati have even arrived at the rank of Major-General: EULER never had, and indeed never would have, any distinction of this fort; but what title in the power of Princes to bestow. could do honour to the name EULER? And then, regard for the prefervation of the natural rights of humanity,

humanity, imposes, in some measure, the duty of setting the example of a sage indifference to these baubles of human vanity, so childish and yet so dangerous.

Most of the Princes of the North, to whom he was personally known, gave him marks of their esteem, or rather of a veneration which they could not with-hold from the union of a virtue so simple with a genius so vast and elevated. When the Prince Royal of Prussia travelled to Petersburg, he did not wait for a visit from Euler, but went first to his house, and passed some hours by the bed-side of the venerable old man, holding his hands in his own, with one of Euler's grand-children in his lap, whom early symptoms of a genius for geometry had rendered the particular object of paternal affection.

All the noted mathematicians of the present day are his pupils: there is no one of them who has not formed himself by the study of his works, who has not received from him the formules, the method which he employs; who is not directed and supported by the genius of Euler in his discoveries. This honour he owes to the revolution effected in the mathematical sciences, by subjecting all to analysis; to his indefatigable application, which has enabled him to embrace the whole extent of these sciences; to the order in which he has arranged his great works; to the simplicity, to the elegance, of his formules; to the clearness of his methods and demonstrations;

demonstrations; and all this greatly enhanced, by the multiplicity and the choice of his examples. Neither *Newton*, nor *Descartes*, whose influence was once so powerful, has arrived at this pitch of glory; and hitherto, Euler alone, of geometricians, has possessed it entirely, and without a rival.

But, as Professor, he has formed pupils in a peculiar fense his own. Among these, we mention his eldest fon, whom the Academy of Sciences elected to fupply his place, without any apprehension that this honourable fuccession granted to the name of EULER, as to that of Bernouilli, could ever become a dangerous precedent: a fecond fon, now engaged in the study of medicine, but who, in his youth, obtained from that Academy the prize propofed for determining the alterations of the mean motion of the planets; Mr. Lexell, whose premature death has just left a blank in the world of science; and, to mention no more, Mr. Fufs, the youngest of his scholars, and the companion of his last labours; who, fent from Bale to EULER by Daniel Bernouilli, has, by his works, done credit to Bernouilli's recommendation, and EULER's inftructions, and who, after having paid public homage in the Academy of Peterfburg, to his illustrious master, married his granddaughter.

Of fixteen professors belonging to the Academy of Petersburg, eight had been formed by him; and all of them, well known from their productions, and decorated with academic honours, value themselves

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on being able to add, to all the reft, that of disciple to EULER.

He had retained all his facility of thought, and, apparently, all his mental vigour: no decay feemed to threaten the sciences with the sudden loss of their great ornament. On the 7th of September, 1783, after amufing himfelf with calculating on a flate the laws of the afcending motion of air-balloons, the recent discovery of which was then making a noise all over Europe, he dined with Mr. Lexell and his family, talked of Herschell's planet, and of the calculations which determine it's orbit. A little after he called his grand-child, and fell a playing with him as he drank tea, when fuddenly, the pipe, which he held in his hand, dropped from it, and he ceafed to calculate and to breathe.

Such was the end of one of the greatest and most extraordinary men ever produced by the hand of nature: a man whose genius was equally capable of the greatest efforts, and of the most unwearied application; who multiplied his productions far beyond what could have been expected from powers merely human, and was, nevertheless, original in every one; whose head was incessantly employed, and his spirit always tranquil; who, finally, by a deftiny unfortunately too rare, united, and that defervedly, a felicity hardly ever interrupted, to a glory which no one ever disputed with him.

His death was confidered as a public lofs, even in the country which he inhabited. The Academy of Petersburg went into deep mourning for him, and voted a marble buft of him, at their own expence, to be placed in their Affembly-Hall. An honour still more distinguished had already been conferred on him, by that learned body, in his life-time. In an allegorical painting, a figure of Geometry is reprefented leaning on a tablet, exhibiting mathematical calculations, and the characters inscribed, by order of the Academy, are the formules of his new theory of the moon. Thus, a country which, at the beginning of the prefent century, we confidered as fcarcely emerged out of barbarism, is become the instructor of the most enlightened nations of Europe, in doing honour to the life of great men, and in embalming their memory: it is fetting these nations an example, which fome of them may blush to reflect, that they have had the virtue neither to propose, nor to imitate.

Peterform when the desp moneing for him, and their own expenses to the places in their allegate that the bonour to the places in their allegate that the bonour still more distributed had already them conferred on things of the places of the lifetime. The an elegand painting a figure of Commenty is the an elegand of the himself of the himself of the manifest of the conferred the moon. They are continued of his new them, are the transfers manifest of his new them, and the moon of the prefer of the transfers of the moon of the prefer of the continue of the prefer of the first of the continue of the prefer of the transfer of the transfer of the himself of the moon of the prefer of the transfer of the continue of the prefer of the transfer to th

# LETTERS

ON

### DIFFERENT SUBJECTS

IN

### PHYSICS AND PHILOSOPHY.

#### LETTER I.

Of Magnitude, or Extension.

MADAM,

THE hope of having the honour to communicate, in person, to your Highness, my lessons in Geometry, becoming more and more distant, which is a very sensible mortification to me, I feel myself impelled to supply personal instruction by writing, as far as the nature of the objects can permit.

I begin my attempt, by affifting you to form a just idea of magnitude; producing, as examples, the smallest as well as the greatest extensions of matter actually discoverable in the system of the Universe. And first, it is necessary to six on some one determinate division of measure, obvious to the senses, and of which we have an exact idea, that of a foot, for instance. The quantity of this, once established, and rendered familiar to the eye, will enable us to form the idea of every other quantity, as to length, great

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or fmall; the former, by afcertaining how many feet it contains; and the latter, by afcertaining what part of a foot measures it. For, having the idea of a foot, we have that also of it's half, of it's quarter, of it's twelfth part, denominated an inch, of it's hundredth, and of it's thousandth part; which is so small as almost to escape the fight. But it is to be remarked, that there are animals, not of greater extension than this last subdivision of a foot, which, however, are composed of members through which the blood circulates, and which again contain other animals, as diminutive compared to them, as they are compared to us. Hence it may be concluded that animals exist, whose smallness eludes the imagination; and that these again are divisible into parts inconceivably fmaller. Thus, for example, though the ten thoufandth part of a foot be too small for fight, and, compared to us, ceases to be an object of sense, it nevertheless furpasses in magnitude certain complete animals; and must, to one of those animals, were it endowed with the power of perception, appear extremely great.

Let us now make the transition from these minute quantities, in pursuing which the mind is lost, to those of the greatest magnitude. You have the idea of a mile;\* the distance from hence to Magdeburg is computed to be 18 miles;† a mile contains 24,000 feet, and we employ it in measuring the distance of the different regions of the globe, in order to avoid

numbers

<sup>\*</sup> The German mile is equal to 4 3-5ths miles English, nearly.
† About 83 English miles.

numbers inconceivably great, in our calculations, which must be the case if we used foot instead of mile. A mile then, containg 24,000 feet, when it is faid that Magdeburg is 18 miles from Berlin, the idea is much clearer, than if the distance of these two cities were faid to be 432,000 feet: A number fo great almost overwhelms the understanding. Again, we shall have a tolerably just idea of the magnitude of the earth, when we are told that it's circumference is about 5,400 miles. And the diameter being a ftraight line paffing through the centre, and terminating, in opposite directions, in the surface of the fphere, which is the acknowledged figure of the earth, for which reason also we give it the name of globe, the diameter of this globe is calculated to be 1720 miles;\* and this is the measurement which we employ for determining the greatest distances discoverable in the heavens. Of all the heavenly bodies the moon is nearest to us, being distant only about 30 diameters of the earth, which amount to 51,600 miles, t or 1,238,400,000 feet; but the first computation of 30 diameters of the earth, is the clearest idea. The fun is about 300 times farther from us than the moon; and when we fay his distance is 9,000 diameters of the earth, we have a much clearer idea, than if it were expressed in miles, or in feet.

<sup>\*</sup> About 7,920 English miles. The diameter of our earth is really 7,964 English miles, it's circumference 25,020. The mean distance of the moon is 240,000 miles, which scarcely exceeds the 400th part of the sun's mean distance, or 93,720,000 miles.

<sup>†</sup> About 237,360 miles English.

You know that the earth performs a revolution round the fun in the space of a year, but that the fun remains fixed. Befide the earth, there are five other fimilar bodies, named planets, which revolve round the fun; two of them at finaller diftances, Mercury and Venus; and three at greater, namely Mars, Jupiter and Saturn. All the other stars which we fee, comets excepted, are called fixed; and their diftance from us is incomparably greater than that of the fun. The diffances are undoubtedly very unequal, which is the reason that some of these bodies appear greater than others. But the nearest of them is, unquestionably, above 5,000 times more distant than the Sun: it's diftance from us, accordingly, exceeds 45,000,000 of times the earth's diameter, that is 77,400,000,000 of miles;\* and this again multiplied by 24,000 will give that prodigious diftance expressed in feet. And this, after all, is the distance only of those fixed stars which are the nearest to us; the most remote which we see, are perhaps a hundred times farther off. It is probable, at the fame time, that all thefe ftars taken together, constitute only a very fmall part of the whole universe, relatively to which these prodigious distances are not greater than a grain of fand compared to the earth. This immenfity is the work of the Almighty, who governs the greatest bodies and the smallest.†

Berlin, 19th April, 1760.

<sup>\* 356,050,000,000</sup> miles English.

<sup>†</sup> This letter, in the original edition, that of Leipfig, 1770, is dated, Berlin 19th April, 1760, and concludes with these words, (which

### LETTER II.

## Of Velocity.

be pleased to accept the continuation of my infiructions, a specimen of which I took the liberty of presenting to you in a former letter, I proceed to unfold the idea of velocity, which is a particular species of extension, and susceptible of increase and of diminution. When any substance is transported, that is, when it passes from one place to another, we ascribe to it a velocity. Let two persons, the one on horseback, the other on foot, proceed from Berlin to Magdeburg, we have, in both cases, the idea of a certain velocity; but it will be immediately assimmed, that the velocity of the former exceeds that of the latter. The question then is, Wherein consists the

(which are with great propriety omitted by the philosophic French editor of the work, twenty-seven years afterwards) and who is now crowning with fuccess the arms in which we are so deeply interested. This is, no doubt, a dreadful "falling off" from the majesty of the subject. Who cares now about the success of the Prussian arms in 1760? But philosophers, as well as other men, are under the dominion of local and temporary circumstances. Frederick II. was then in the zenith of his glory; Euler was living at Berlin, and giving lessons in philosophy to the niece of that illustrious prince. Is it to be wondered, then, that he should sink for a moment into the courtier, and offer a drachm of incense to a great lady; or, that a soul so uniformly devout, should acknowledge the providence of the Almighty in a particular instance?

difference which we observe between these several degrees of velocity? The road is the same to him who rides and to him who walks: but the difference evidently lies in the time which each employs in performing the same course. The velocity of the horseman is the greater of the two, as he employs less time on the road from Berlin to Magdeburg; and the velocity of the other is lefs, because he employs more time in travelling the fame distance. Hence it is clear, that in order to form an accurate idea of velocity, we must attend at once to two kinds of quantity, namely, to the length of the road, and to the time employed. A body, therefore, which in the fame time paffes through double the space which another body does, has double its velocity; if, in the fame time, it passes through thrice the distance, it is faid to have thrice the velocity, and fo on. We shall comprehend, then, the velocity of a body, when we are informed of the space through which it passes in a certain quantity of time. In order to know the velocity of my pace, when I walk to Lytzow,\* I have observed that I make 120 steps in a minute, and one of my steps is equal to two feet and a half. My velocity, then, is fuch, as to carry me 300 feet in a minute, and a space fixty times greater, or 18,000 feet in an hour, which however does not amount to a mile, for this, being 24,000 feet, would require an hour and 20 minutes. Were I, therefore, to walk from hence to Magdeburg, it would take exactly 24 hours. This conveys an accurate idea of the velo-

<sup>\*</sup> A village about a league from Berlin.

city with which I am able to walk. Now it is eafy to comprehend what is meant by a greater or less velocity. For if a courier were to go from hence to Magdeburg in 12 hours, his velocity would be the double of mine: if he went in eight hours, his velocity would be triple. We remark a very great difference in the degrees of velocity. The tortoife furnishes an example of a velocity extremely small. If the advances only one foot in a minute, her velocity is 300 times less than mine, for I advance 300 feet in the fame time. We are likewife acquainted with velocities much greater. That of the wind admits of great variation. A moderate wind goes at the rate of 10 feet in a fecond, or 600 feet in a minute; its velocity therefore is the double of mine. A wind that runs 20 feet in a fecond, or 1200 in a minute, is rather ftrong; and a wind which flies at the rate of 50 feet in a fecond is extremely violent, though its velocity is only 10 times greater than mine, and would take two hours and twenty-four minutes to blow from hence to Magdeburg.

The velocity of found comes next, which moves 1000 feet\* in a fecond, and 60,000 in a minute. This velocity, therefore, is 200 times greater than that of my pace; and were a cannon to be fired at Magdeburg, if the report could be heard at Berlin, it

<sup>\*</sup> The velocity of found is generally computed at 1,142 feet each fecond, but varies with the elafticity and density of the air. The earth travels in her orbit 1,612,000 miles in the space of 24 hours, and therefore with a velocity more than 50 times greater than that of a cannon ball. Light moves about 13 millions of miles every minute.

would arrive there in feven minutes. A cannon ball moves with nearly the fame velocity; but when the piece is loaded to the utmost, the ball is supposed capable of flying 2,000 feet in a fecond, or 120,000 in a minute. This velocity appears prodigious, though it is only 400 times greater than that of my pace in walking to Lytzow; it is at the fame time the greatest velocity known upon earth. But there are in the heavens velocities far greater, though their motion appears to be extremely deliberate. You know that the earth turns round on it's axis in 24 hours: every point of it's furface, then, under the equator, moves 5,400 miles\* in 24 hours, while I am able to get through only 18 miles.† It's velocity is accordingly 300 times greater than mine, and lefs notwithstanding than the greatest possible velocity of a cannon ball. The earth performs it's revolution round the fun in the space of a year, proceeding at the rate of 128,250 milest in 24 hours. It's velocity, therefore, is 18 times more rapid than that of a cannon ball. The greatest velocity of which we have any knowledge is, undoubtedly, that of light, which moves 2,000,000 of miles § every minute, and exceeds the velocity of a cannon ball 400,000 times.

22d April, 1760.

<sup>\* 24,840</sup> English miles ‡ 589,950 English.

<sup>†</sup> About 83 English. § 9,200,000 miles English.

#### LETTER III.

### Of Sound, and it's Velocity.

THE elucidations of the different degrees of velocity, which I have had the honour to lay before your Highness, carry me forward to the examination of found, or noise in general. It must be remarked, that a certain portion of time always intervenes before found can reach our ears, and that this time is longer in proportion to our distance from the place where the found is produced; a second of time being requisite to convey found 1000 feet.

When a cannon is fired, those who are at a diftance do not hear the report for some time after they have feen the flash. Those who are a mile, or 24,000 feet diftant, hear not the report till 24 feconds after they faw the flame. You must no doubt have frequently remarked, that the noise of thunder reaches not the ear for some time after the lightning: and it is by this we are enabled to calculate our diftance from the place where the thunder is generated. If, for example, we observe that 20 seconds intervene between the flash and the thunder-clap, we may conclude that the feat of the thunder is 20,000 feet diftant, allowing 1000 feet of diftance for every fecond of time. This primary property leads us to inquire, In what found confifts? Whether it's nature is fimilar to that of finell, that is, whether found issues from the body which produces it, as fmell is emitted

emitted from the flower, by filling the air with fubtile exhalations, proper to affect our fense of fmelling. This opinion was formerly entertained, but it is now demonstrated, that from a bell struck nothing proceeds that is conveyed to our ear, and that the body which produces found loses no part of it's fubstance. When we look upon a bell that is struck, or the string of an instrument when touched, we perceive that these bodies are then in a state of trembling, or agitation, by which all their parts are affected; and that all bodies, susceptible of such an agitation of their parts, likewife produce found. These shakings or vibrations are visible in the string of an inftrument when it is not too fmall; the tenfe string A C B passes alternately into the situation AMB and ANB. (See plate I. fig. 1. in which I bave represented these vibrations much more obvious to sense than they are in fact.) It must be further obferved, that these vibrations put the adjacent air into a fimilar vibration, which is fuccessively communicated to the more remote parts of the air, till it come at length to strike our organ of hearing. It is the air, then, which receives these vibrations, and which transmits the found to our ear. Hence it is evident, that the perception of found is nothing else but the impression made on our ear by the concussion of the air, communicated to us through the organ of hearing; and when we hear the found of a string touched, our ear receives from the air as many strokes as the firing performs vibrations in the fame time. Thus, if the string performs 100 vibrations in a fecond,

cond, the ear likewise receives 100 strokes in the fame time; and the perception of these strokes is what we call found. When these strokes succeed each other uniformly, or when their intervals are all equal, the found is regular, and fuch as is requifite to music. But when the strokes succeed unequally, or when their intervals are unequal among themselves, an irregular noise, incompatible with music, is the refult. On confidering fomewhat more attentively the mufical founds, whose vibrations take place equally, I remark first, that when the vibrations, as well as the ftrokes impreffed on the ear, are more or less strong, no other difference of found results from it, but that of stronger or weaker, which produces the distinction, termed by musicians, forte & piano. But there is a difference much more effential, when the vibrations are more or lefs rapid, that is, when more or fewer of them are performed in a fecond. When one string makes 100 vibrations in a fecond, and another ftring makes 200 vibrations in the fame time, their founds are effentially different; the former is lower or more flat, and the other higher or more fharp. Such is the real difference between the flat and fharp founds, on which all music hinges, and which teaches how to combine founds different in respect of flatness and sharpness, but in such a manner as to produce an agreeable harmony. In the flat founds there are fewer vibrations in the fame time than in the fharp founds; and every key of the harpsichord contains a certain and determinate number of vibrations, which are completed in a fecond.

Thus the note marked by the letter C,\* makes nearly 100 vibrations in a fecond; and the note marked makes 1600 vibrations in the fame space of time. A string which vibrates 100 times in a second, will give precisely the note C; and if it vibrated only 50 times, the note would be lower or more flat. But with regard to our ear, there are certain limits beyond which sound is no longer perceptible. It would appear that we are incapable of determining either the sound of a string which makes less than 30 vibrations in a second, because it is too low; or that of a string which would make more than 7552 in a second, because such a note would be too high.

26th April, 1760.

\* The note C is that which is produced by touching the thickeft firing of a violoncello; the note c is the fourth octave of the first; accordingly, these two notes, represented by the usual method of pricking music, are



Mr. Euler marks the progression of octaves thus:

1st octave, 2d octave, 3d octave, 4th octave.

C, or ut. c. c c c c

and in like manner for the other notes of the gamut; D. E. F. G. A. B. or re, mi, fa, fol, la, fi.

In writing the chromatic scale, he employs the following signs: C. Cs, D, Ds, E, F, Fs, G, Gs, A, B, H, c ut, ut x, re, re x, mi, fa, fa x, fol, fol x, la, fi b, fi x, ut.

#### LETTER IV.

### Of Consonance and Dissonance.

T RESUME my remark, that on hearing a fimple mufical found, our ear is ftruck with a feries of strokes equally distant from each other, the frequency and number of which, in a given space of time, conflitute the difference which fublifts between low notes and high: fo that, the finaller the number of vibrations or strokes produced in a given time, fay a fecond, the lower we estimate that note; and the greater the number of fuch vibrations, the higher is the note. The perception of a fimple mufical found may, therefore, be compared to a feries of dots equidiftant from each other, as ...... If the intervals between these dots be greater or smaller, the found produced will be lower or higher. It cannot be doubted, that the perception of a fimple found is fomewhat fimilar or analogous to the fight of fuch a feries of dots equidiffant from each other: we are enabled thus to reprefent to the eye what the ear perceives on hearing found. If the distances between the dots were not equal, or were these dots scattered about confufedly, they would be a reprefentation of a confused noise, inconsistent with harmony. This being laid down, let us confider what effect two founds emitted at once must produce on the ear. First, it is evident, that if two founds are equal, or if each performs the fame number of vibrations in the fame time, the ear will be affected in the very fame manner as by a fingle note; and, in music, these two notes are said to be in unison, which is the simplest accord: we mean by the term accord the blending of two or more sounds heard at once. But if two sounds differ in respect of low and high, we shall perceive a mixture of two series of strokes, in each of which the intervals are equal among themselves, but greater in the one than in the other; the greater intervals corresponding to the lower note, and the smaller to the higher. This mixture, or this accord of two notes, may be represented to the eyes by two series of dots arranged on two lines A B and C D;

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1000													-
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and in order to form a just idea of these two series, we must have a clear perception of the order which subsists among them, or, in other words, of the relation between the intervals of the one line and of the other. Having numbered and marked the dots of each line, and placed No. 1. under No. 1; those marked with the sigure 2, will not exactly correspond, and still less those marked 3: but we find No. 11 exactly over No 12: from which we discover that the higher note makes 12 vibrations, and the other only 11. If we had not affixed the sigures, the eye would hardly have perceived this order; it is the same with the ear, which would with much difficulty

difficulty have traced it in the two notes which I have reprefented by two rows of dots. But in the following figure,

you discover at the first glance that the upper line contains twice as many dots as the under, or that the intervals in the under line are twice as great as those of the upper. This is undoubtedly, next to unifon, the simplest of all cases, in which you can at once discover the order which sublists between these two series of dots; and the same thing holds with respect to the two notes represented by these two lines of dots: the number of vibrations contained in the one will be precifely the double of the vibrations contained in the other, and the ear will eafily perceive the pleafing relation of these two founds; whereas, in the preceding cafe, it was extremely difficult, if not impossible, to discriminate. When the ear readily discovers the relation sublisting between two notes, their accord is denominated confonance: and if it be very difficult, or even impossible to catch this relation, the accord is termed dissonance. The fimplest confonance, then, is that in which the high note produces precifely twice as many vibrations as the low note. This confonance, in the language of music, is called octave: every one knows what it means; and two notes which differ precifely an octave, harmonize fo perfectly, and possess fuch a complete refemblance, that musicians mark them by the fame letters. Hence it is that in church-music the women fing an octave higher than the men, and yet imagine they are uttering the fame founds. You may eafily afcertain the truth of this by touching the keys of a harpfichord, when you will perceive with pleasure the delightful accord of all the notes which are just an octave distant, whereas any other two notes whatever will strike the ear less agreeably.

29th April, 1760.

#### LETTER V.

### Of Unison and Octaves.

TOUR Highness has by this time remarked, that the accord which musicians call an octave, firikes the ear in a manner fo decided, that the flightest deviation is easily perceptible. Thus, having touched the Key marked F, that marked f, which is an octave higher, is eafily attuned to it, by the judgment of the ear only. If the string which is to produce this note be ever fo little too high or too low, the ear is inftantly offended, and nothing is eafier than to put the two keys perfectly in tune. Thus we observe, that in singing the voice slides easily from one note to another, which is just an octave higher or lower. But were it required to pass immediately from the note F to the note d, for example, an ordinary finger might eafily fall into a miftake, unless affifted by an instrument. Having fixed the note F, it is almost impossible all at once to make the tranfition to the note d. What then is the reason of this

this difference, that it is fo eafy to make note f harmonize with note F, and fo difficult to make note d accord with it? The reason is evident from the remarks already made: it is this, that note F and note f make an octave, and that the number of vibrations of note f is precifely double that of note F. In order to have the perception of this accord, you have only to confider the proportion of one to two, which, as it inftantly ftrikes the eye by the reprefentation of the dots I formerly employed, affects the ear in a fimilar manner. You will eafily comprehend, then, that the more fimple any proportion is, or expressed by finall numbers, the more diffinctly it prefents itfelf to the understanding, and conveys to it a sentiment of fatisfaction.\* Architects likewife carefully attend to this maxim, as they uniformly employ in their works proportions as fimple as circumstances permit. They usually make the height of doors and windows double the breadth, and endeavour to employ throughout proportions capable of being expressed by small numbers, because this is obvious and grateful to the understanding. The same thing holds good in music: accords are pleasing only in so far as the mind perceives the relation fubfifting between the founds, and this relation is fo much more

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<sup>\*</sup> In order to have a clear conception of what follows, it must be recollected, that the terms relation and ratio are synonimous, and that the author is here confidering geometrical proportion, which confists in the number of times that the first term is contained in the second.—F. E.

eafily perceptible, as it is expressed by finall numbers. Now, next to the relation of equality, which denotes two founds in unifon, the ratio of two to one is undoubtedly the most simple, and it is this which furnishes the accord of an octave: hence it is evident, that this accord possesses many advantages above every other confonance. Having thus explained the accord, or interval of two notes denominated by muficians an octave, let us confider feveral notes, as F, f, f, f, each of which is an octave higher than the one immediately preceding: fince then the interval of F from f, of f from 7, of 7 from 7, of 7 from 7 is an octave, the interval of F to 7 will be a double octave, that of F to 7, a triple octave, and that of F to 7. a quadruple octave. Now, while note F makes one vibration, note f makes two, note 7 makes four, note # makes eight, and note # makes fixteen: hence we fee, that as an octave corresponds in the relation of 1 to 2, a double octave must be in the ratio of 1 to 4, a triple in that of 1 to 8, and a quadruple in that of 1 to 16. And the ratio of 1 to 4, not being fo fimple as that of 1 to 2, for it does not fo readily strike the eye, a double octave is not so easily perceptible to the ear as a fingle; a triple is still less perceptible, and a quadruple still much less fo. When, therefore, in tuning a harpfichord, you have fixed the note F, it is not fo eafy to attune the double octave 7 as the fingle f; it is still more difficult to attune the triple octave and the quadruple without rifing through the intermediate octaves. Thefe

These accords are likewise comprehended in the term consonance; and as that of unison is most simple, they may be arranged according to the following gradations:

I. Degree, unifon, indicated by the relation of I to I.

II. Degree, the immediate octave, in the ratio of 1 to 2.

III. Degree, the double octave, in that of 1 to 4.

IV. Degree, the triple octave, in that of 1 to 8.

V. Degree, the quadruple octave, in that of 1 to 16.

VI. Degree, the quintuple octave, in that of 1 to 32.

And fo on, as long as found is perceptible. Such are the accords denominated confonances, to the knowledge of which we have been thus far conducted; but hitherto we know nothing of the other species of consonance, and still less of the dissonances employed in music. Before I proceed to the explication of these, I must add one remark respecting the name octave, given to the interval of two notes, the one of which contains twice the vibrations contained in the other. You fee the reason of it in the principal ftops of the harpfichord, which rife by feven degrees before you arrive at the octave C, D, E, F, G, A, B, c, fo that ftop c is the eighth, reckoning C the first. And this division depends on a certain feries of mufical intervals, the nature of which shall be unfolded in the following letters.

3d May, 1760.

#### LETTER VI.

### Of other Consonances.

TT may be affirmed, that the relations of one to 2, of 1 to 4, of 1 to 8, of 1 to 16, which we have hitherto confidered, and which contain the progreffion of octaves, are all formed by the number 2 only; fince 4 is 2 times 2; 8, 2 times four; 16, two times 8. Were we to admit, therefore, the number 2 alone into mufic, we fhould arrive at the knowledge of only the accords or confonances which muficians call the fingle, double, or triple octave; and as the number 2, by its reduplication, furnishes only the numbers 4, 8, 16, 32, 64, the one being always double the preceding, all other numbers would remain unknown. Now, did an instrument contain octaves only, as the notes marked C, c, c, c, and were all others excluded, it could not produce an agreeable music, on account of its too great simplicity. Let us introduce, then, together with number 2, the number 3 likewife, and observe what accords or confonances would be the refult. The ratio of 1 to 3 prefents at once two founds, the one of which makes 3 times more vibrations than the other in the fame time. This ratio is undoubtedly the most easily to be comprehended, next to that of I to 2; it will, accordingly, furnish very pleasing consonances, but of a nature totally different from that of octaves. Let us suppose, then, that in the proportion of 1

to 3, number 1 corresponds to note C; since note c is expressed by number 2, number 3 gives a found higher than c, but at the same time lower than note , which corresponds to number 4. Now, the note expressed by 3 is that to which musicians affix the letter g, and they denominate the interval from c to g, a fifth, because in the keys of a harpsichord that of g is the fifth from c, as c, d, e, f, g. If then number 1 produces the found C, number 2 will give c; number 3 gives g, number 4 the note ; and note ; being the octave of g, the number corresponding to it will be 2 times 3, or 6. Rifing still an octave, the found = will correspond to a number twice greater, that is 12. All the notes with which the two numbers 2 and 3 furnish us, indicating note C by 1, therefore are,

C, c, g,  $\bar{c}$ ,  $\bar{g}$ ,  $\bar{c}$ ,  $\bar{g}$ ,  $\bar{c}$ ,  $\bar{g}$ ,  $\bar{c}$ .

1, 2. 3. 4. 6. 8. 12. 16.

Hence it is clear, that the ratio of 1 to 3 expresses an interval, compounded of an octave and a fifth, and that this interval, on account of the simplicity of the numbers which represent it, must be, next to the octave, the most grateful to the ear. Musicians accordingly assign the second rank among consonances to the fifth; and the ear catches it so easily, that there is no difficulty in tuning a fifth. For this reason, in violins, the four strings rise by sifths, the lowest being g, the second ā, the third ā, and the fourth ē; \* and every musician puts them in tune

<sup>.</sup> That is, in the language of fol-faing, fol, re, la, mi.

by the ear only. A fifth, however, is not so easily tuned as an octave; but the fifth above the octave, as from C to g, being expressed by the proportion of 1 to 3, is more perceptible than a simple sifth, as from C to G, or from c to g, which is expressed by the proportion of 2 to 3: and it is likewise known by experience, that having sixed the note C, it is easier to attune to it the higher sifth g, than the simple G. If unity had marked the note F, number 3 would mark the note; so that,

F, f, c, f, c, f, e, would be marked by

1. 2. 3. 4. 6. 8. 12. where, from f to c the interval is a fifth in the relation of 2 to 3; from 7 to 2, from 7 to 2 are also fifths, as the ratio of 4 to 6, and of 8 to 12, is the fame as that of 2 to 3. For if two strings perform, in the same time, the one 4 vibrations, the other 6, the former string will make, in a time equal to half the first space of time, two vibrations, and the fecond, in the fame time, will make three. Now the founds emitted from these strings are the fame in both cases; of consequence the relation of 4 to 6 expresses the same interval as that of 2 to 3, that is, a fifth. Hence we have arrived at the knowledge of another interval contained in the ratio of 3 to 4, which is that of 7 to 7, and confequently also of c to f, or of C to F. Musicians call it a fourth; and being expressed by greater numbers, it is not fo agreeable, by a great deal, as the fifth, and still less fo than the octave. Number 3 having furnished us new accords or confonances, namely the fifth and the fourth,

fourth, before we call in any others, let us take it again three times, in order to have the number 9, which will give a higher note than note  $3^*$ , or  $\overline{z}$  one octave and one fifth. Now,  $\overline{z}$  is the octave of  $\overline{z}$ , and  $\overline{z}$  the fifth of  $\overline{z}$ ; number 9 then gives the note  $\overline{z}$ , fo that  $\overline{z}$ ,  $\overline{z}$ ,  $\overline{z}$ ,  $\overline{z}$ , will be marked by

6. 8. 9. 12; and if these notes be taken in the lower octaves, the relations remaining the same, we shall have:

C, F, G; c, f, g; c, f, g; c, f, g; e.

6. 8. 9; 12. 16. 18; 24. 32. 36; 48. 64. 72. 96.

which leads us to the knowledge of new intervals.

The first is that of F to G, contained in the ratio of 8 to 9, which musicians call a second or tone. The second is that of G to f, contained in the ratio of 9 to 16; called a seventh, and which is one second, or one tone less than an octave. These proportions, being already expressed by very great numbers, are not reckoned among the consonances, and musicians call them dissonances or discords.

Again, if we take three times the number 9, or 27, it will mark a tone higher than 5, and precisely a fifth higher than g; it will be accordingly the tone 5, and it's octave 5 will correspond to twice the number 27, or 54, and it's double octave 5 to twice the

<sup>\*</sup> Great care must be taken to guard ourselves from affixing to numbers the idea of a perfect identity with the sounds which they represent. The first express only the relation of the number of vibrations performed in the same time, by the bodies which emit the sounds in question. There is no real analogy between number and sound.—F. E.

number, 54, or 108. Let us represent these tones some octaves lower, in the manner following:

C, D, F, G; c, d, f, g, c, d, f, 24, 27, 32, 36; 48, 54, 64, 72; 96, 108, 128,  $\bar{g}$ ;  $\bar{c}$ ,  $\bar{d}$ ,  $\bar{f}$ ,  $\bar{g}$ ;  $\bar{c}$ .

144; 192, 216, 256, 288; 384.

Hence we see, that the interval from D to F is contained in the ratio of 27 to 32, and that of F to d in the ratio of 32 to 54, the two terms of which are divisible by 2; and then in place of this relation we have that of 16, to 27. The first interval is called a tierce minor, or lesser third, and the other a greater sixth. The number 27 might be still farther multiplied by 3, but music extends not so far, and we limit ourselves to number 27, resulting from 3, multiplied three times by itself: other musical tones still wanting are introduced by means of number 5, and shall be unfolded in my next Letter.

3d May, 1760.

#### LETTER VII.

Of the twelve Tones of the Harpsichord.

THE present subject of my correspondence with your Highness is so dry, that I begin to apprehend it may be growing tiresome. That I may not waste too much time on it, and be relieved from the necessity of recurring frequently to a topic so difgusting,

gufting, I fend you by this conveyance three letters at once. My intention, in undertaking it, was to render visible the real origin of musical notes, with which muficians themselves are almost totally unacquainted. It is not to theory they are indebted for the knowledge of all these founds; but rather to the fecret power of genuine harmony, operating fo efficaciously on their ears, that they have been constrained, if I may be allowed to fay it, to receive tones actually in use, though they are not hitherto perfectly agreed respecting their just determination. The principles of harmony are ultimately reducible to numbers,\* as I have demonstrated; and it has been remarked, that the number 2 furnishes octaves only, fo that having fixed, for example, the note F, we are conducted to the notes f, 7, 7, 7, The number 3 afterwards furnishes C, c, c, c, c, which differ one fifth from the preceding feries; and the repetition of this fame number 3, furnishes again the sifths of the sirst, namely G, g, g, g, g and finally, the third repetition of this number 3 adds farther the notes D, d, d, d, d, d, d, The principles of harmony then being attached to fimplicity, feem to forbid our pushing farther the

<sup>\*</sup> This is true only to a certain degree; for, if we except the knowledge of the relation of notes, or the numerical expression of intervals, numbers cannot be introduced into music, as Mr. d'Alembert has justily remarked, but as a piece of useless parade; and the scanty knowledge they surnish is far short of the theory of composition, which is founded on the pleasure of the ear, and hitherto no one has attempted to make this a subject of calculation.

—F. E.

repetition of number 3; hitherto, accordingly, we have only the following notes for each octave:

F. G. c. d. f.

16. 18. 24. 27. 32. which certainly would not furnish a very copious music. But let us introduce, in addition to these, number 5, and observe the tone which shall emit five vibrations while F emits only one. Now, f makes two vibrations in the fame time; 7 makes four; and 5 fix. The note in question then, is between 7 and 2. It is that which muficians indicate by letter a, the accord of which, with note 7, is denominated a greater third, and is found to produce a very agreeable concord, being expressed by the very fimple ratio of 4 to 5. Farther, note a with note 5 produces an accord contained in the ratio of 5 to 6, which is almost as agreeable as the former, and which is denominated a leffer third, represented by the ratio of 27 to 32, and it's difference from the first is almost imperceptible to the ear. This fame number 5 being applied to the other notes G, c, d, will give us, in like manner, their greater thirds, taken in the fecond octave below, that is to fay, the notes 5, 6, and f, which, being transposed, will give the following notes, with their corresponding numbers.

F. Fs. G. A. B. c. d, e, f, 128. 135. 144. 160. 180. 192. 216. 240. 256,

Take away the notes Fs, and you will have the principal touches of the harpfichord, which, according to the ancients, conflitute the genus denominated diatonic, refulting from number 2, from number 3, thrice repeated, and from number 5. Admitting these

thefe founds only, we are in a condition to compose harmonies very agreeable and various, the beauty of which is founded on the fimplicity alone of the numbers corresponding to the notes. Finally, upon applying, a fecond time, the number 5, we shall be furnished with the thirds of the four new tones, A, E, B, Fs, which we have just found, we shall have the notes Cs Gs Ds and B, fo that now the octave is completed of the 12 tones received in music. All these tones derive their origin from the three numbers 2, 3, and 5, multiplying 2 by itself, as often as the octaves require; but we carry the multiplication of 3 only to the third stage, and of five to the fecond. All the tones of the first octave are contained in the following table, in which you will fee how the fundamental numbers 2, 3, and 5, enter into the composition of those which express the relation of these notes.

ut or C	2, 2,	2, 2,	2, 2	2, 2,	3 .	 384	Difference.
ut 🗷 Cs	2, 2,	2, 2,	5, 5	5		 400	16
re D	2, 2,	2, 2,	3, 3	3, 3.		 432	32
re 🗷 Ds	2, 3,	3, 5,	5.			 450	18
mi E	2, 2,	2, 2,	2, 3	3, 5.		 480	30
fa F	2, 2,	2, 2,	2, 2	2, 2,	2, 2	 512	32
fa × Fs	2, 2,	3, 3,	3, 5			 540	28
fol G	2, 2,	2, 2,	2, 2	2, 3,	3 .	 576	36
fol   Gs	2, 2,	2, 3,	5, 5	5		 600	24
la A	2, 2,	2, 2,	2, 2	2, 2,	5 .	 640	40
fi b. Bb	3, 3,	3, 5,	5.			 675	35
fin B <sup>3</sup>	2, 2,	2, 2,	3, 3	3, 5.		 720	45
ut c	2, 2,	2, 2,	2, 2	2, 2,	3, 3	 768	48

While note C makes 384 vibrations, the tone Cs gives 400, and the others as many as are marked by their corresponding numbers: note c will give then, in the same time, double the number of vibrations marked by 384, that is 768. And for the following octaves, you have only to multiply these numbers by 2, by 4, or by 8. Accordingly note 7 will give twice 768, or 1536 vibrations, note = twice 1536, or 3072 vibrations, and note = twice 3072, or 6144 vibrations. In order to comprehend the formation of founds, by means of thefe numbers 2, 3, and 5, it must be remarked, that the points placed between the numbers in the preceding table fignify that they are multiplied into each other; thus, taking the tone Fs, for example, the expression 2, 2, 3, 3, 3, 5, signifies 2 multiplied by 2, that product by 3, that again by 3, that again by 3, and that by 5. Now 2 by 2 make 4, that by 3 make 12, that by 3 make 36, that by 3 make 108, and that by 5 make 540. Hence it is feen that the differences between these tones are not equal among themselves; but that some are greater, and others lefs. This is what real harmony requires. The inequality, however, not being confiderable, we commonly look on all these differences as equal, denominating the interval from one note to another, femitone; and thus the octave is divided into 12 semitones. Many modern musicians make them equal, though this be contrary to the principles of harmony, because no one fifth or third is perfectly exact, and the effect is the fame as if thefe tones were

not perfectly in tune.\* They likewife admit, that we must give up exactness of accord in order to obtain the advantage of equality of femitones, fo that the transposition from any one tone whatever to another may in no respect injure the melody. They acknowledge, however, that the fame piece played in the tone C, or a half tone higher, that is Cs, must confiderably affect it's nature. It is evident, therefore, that in fact all femitones are not equal, whatever efforts may be made by musicians to render them fuch; because true harmony resists the execution of a defign contradictory to it's nature. Such, then, is the real origin of the mufical notes already in use; they are derived from the numbers 2, 3, and 5. Were we farther to introduce number 7, that of the tones of an octave would be increased, and the art of music carried to a higher degree of perfection. But here the mathematician gives up the mufician to the direction of his ear.

3d May, 1760.

\* The alteration thus forced upon the fifths, in order that every key of the harpfichord may ferve equally for the higher note flattened, and for the lower sharpened, and that, at the end of the subdivision, the octaves may be exact, is called temperament. It has been remarked that fifths may be a little weakened without hurting the ear very much; whereas greater thirds become harsh and disagreeable when they are strengthened.—F. E.

#### LETTER VIII.

# Of the Pleasure derived from fine Music.

IT is a question as important as curious, Whence is it that a fine piece of music excites a sentiment of pleafure? The learned differ on this fubject. Some pretend that it is mere caprice, and that the pleafure produced by music is not founded on reason, because what is grateful to one is difgusting to another. This, far from deciding the question, renders it only more complicated. The very point to be determined is, How comes it, that the same piece of music produces effects fo different, feeing all admit that nothing happens without reason? Others maintain that the pleasure derived from fine music consists in the perception of the order which pervades it. This opinion appears at first fight fusficiently well founded, and merits a more attentive examination. Music presents objects of two kinds, in which order is effential. The one relates to the difference of the sharp or flat tones; and you will recollect, that it confifts in the number of vibrations performed by each note in the fame time. This difference, which is perceptible between the quickness of the vibrations of all founds, is what is properly called harmony. The effect of a piece of music, of which we feel the relations of the vibrations of all the notes that compose it, is the production of harmony. Thus two notes which differ an octave, excite a perception of the relation

lation of 1 to 2; a fifth, of that of 2 to 3; and a greater third, of that of 4 to 5. We comprehend then the order which is found in harmony, when we know all the relations which pervade the notes of which it is composed, and it is the perception of the ear which leads to this knowledge. This perception more or lefs delicate, determines why the fame harmony is felt by one, and not at all by another, especially when the relations of the notes are expressed by fomewhat greater numbers. Music contains, befide harmony, another object equally fusceptible of order, namely the measure, by which we assign to every note a certain duration: and the perception of the measure consists in the knowledge of this duration, and of the relations which refult from it. The drum and tymbal furnish the example of a mufic in which meafure alone takes place, as all the notes are equal among themselves, and then there is no harmony. There is likewife a mufic confifting wholly in harmony, to the exclusion of measure. This mufic is the choral, in which all the notes are of the fame duration; but perfect music unites harmony and meafure. Thus the connoisseur who hears a piece of music, and who comprehends, by the acute perception of his ear, all the proportions on which both the harmony and the measure are founded, has certainly the most perfect knowledge poslible of that music; while another, who perceives these proportions only in part, or not at all, understands nothing of the matter, or possesses at most a very slender knowledge of it. But the fentiment of pleafure excited

cited by fine music must not be confounded with the knowledge of which I have been speaking, though it may be confidently affirmed, that a piece of music cannot produce any, unless the relations of it are perceived. For this knowledge alone is not fufficient to excite the fentiment of pleafure; fomething more is wanting, which no one hitherto has unfolded. In order to be convinced that the perception alone of all the proportions of a piece of music is insufficient to produce pleasure, you have only to consider music of a very simple construction, such as goes in octaves alone, in which the perception of proportions is undoubtedly the easiest. Such music would be far from conveying pleafure, though you might have the most perfect knowledge of it. It will be faid then that pleafure requires a knowledge not quite fo eafily attained, a knowledge that occasions some trouble; which must, if I may use the expression, cost us something. But, in my opinion, neither is this a fatisfactory folution. A diffonance, the relations of which are expressed by the highest numbers, is caught with more difficulty; a feries of diffonances, however, following without choice, and without defign, cannot pleafe. The composer must therefore have purfued in his work, a certain plan, executed in real and perceptible proportions. Then a connoiffeur on hearing fuch a piece, and comprehending, beside the proportions, the very plan and defign which the compofer had in view, will feel that fatisfaction which constitutes the pleasure procured by exquisite music to an ear accustomed to relish the beauties and delicacies



fuch as that by which mufical ftrings, bells, and other fonorous bodies are agitated, transmits the concussion to our ears. It will be immediately asked, What is air? For it does not appear, at first fight, to be a material fubstance. As we perceive no fensible body in it, furrounding fpace feems to contain no matter whatever. We feel nothing; we can walk, and move every limb in it, without meeting the flightest obstacle. But you have only to move your hand brifkly, to be fenfible of fome refistance, and even to perceive a stream of wind excited by that rapid movement. Now the wind is nothing elfe but air put in motion; and feeing it is capable of producing effects fo furprifing, how is it possible to doubt that air is a material fubstance, and consequently a body?\* For the terms body and matter are fynonymous.

Body is divided into two great classes, folid and fluid. The air, it is evident, must be referred to the class of fluids. It has several properties in common with water; but it is much more subtile and fine. Experiments have ascertained that air is about 800 times more subtile and more rarefied than water;

<sup>\*</sup> It is an erroneous principle that the air is diftinguished from other fluids by it's susceptibility of compression. All fluids are perfectly elastic, only the force required to produce a certain degree of compression differs very widely in each. Thus the same force which causes water to suffer a contraction of only the thirty thousandth part of it's bulk, condenses air into one half. The real distinction between the aerisorm and liquid fluids seems to be, that the reaction of the sormer is proportional to their density, while that of the latter is proportional to the quantity of compression.—E, E.

and that if air were to be rendered 800 times denfer than it is, it would have the fame confiftency as the other fluid. A principal property of air, by which it is diftinguished from other fluids, is it's quality of being compressed, or reduced into a smaller space. This is demonstrated by the following experiment. Take a tube of metal or glass A B C D (plate I. fig. 2.) close shut at the end A B, and open at the other, into which is introduced a pifton, filling exactly the cavity of the tube. On pushing the piston inwards, when it has arrived at the middle E, the air which occupied at first the cavity A B C D will be reduced one half, and confequently will have become twice as dense. If the piston is pushed still farther in, as far as F, half way between B and E, the air will be reduced to a space four times smaller than at first; and if you continue to drive forward the pifton to G, fo that B G shall be the half of B F, or the eighth part of the whole length B D, the same air which in the beginning was expanded over the whole cavity of the tube, will be contracted to a space eight times fmaller. Going on in the fame manner to contract it into a space 800 times smaller, you will obtain an air 800 times denfer than ordinary air. It would then be as denfe as water, which it would be eafy to prove by other experiments. Hence it appears, that air is a fluid fubstance, capable of compression, or, in other words, of being reduced to a smaller space, and in this respect it differs entirely from water. For, let the tube A B C D be filled with this last fluid, and attempt to introduce the piston, you will find it impossible to drive it forward. Employ what force you may, you will gain nothing; the tube will burft fooner than you can reduce the water to a space senfibly fmaller. This then is the effential difference between air and water: the latter is fusceptible of no compression, but air may be compressed to any degree you pleafe. The more the air is compressed, the denfer it becomes; thus the air which occupied a certain space, when compressed or reduced to half that space, becomes twice as dense; if reduced to a space 10 times smaller, it is rendered 10 times more denfe; and fo on. I have already remarked, that could it be rendered 800 times more denfe, it would then be as dense as water, and consequently as heavy, for weight increases in the same proportion as denfity. Gold, the heaviest substance with which we are acquainted, is likewise the most dense. It is found by experiment to be 19 times heavier than water; and that a mass of gold, in form of a cube of one foot, would weigh 19 times a mass of water of the fame dimensions. Now fuch a mass of water weighs 70 pounds; the mass of gold therefore would weigh 19 times 70, that is 1330 pounds. It follows that were it possible to compress air till it were reduced to a space 19 times 800, that is, 15,200 times fmaller, it would become as denfe and as weighty as gold.

But it is very far from being possible to carry the compression of air to that degree. You may at first without disticulty drive forward the piston, but the farther you advance, the resistance becomes more powerful;

powerful; and, before you are able to reduce the air to a space 10 times smaller, such a force must be employed as would burst the tube, unless it were of uncommon strength. And not only would such a force be necessary to drive the piston farther, but an equal force would be requisite to keep it in that state, for on the slightest relaxation of the power, the compressed air would drive it backward. The more compressed the air is, the more violent are it's efforts to expand, and to recover it's natural state. This is what we call the spring or elasticity of the air, of which I propose to treat in my next letter.

10th May, 1760.

## LETTER X.

# Rarefaction and Elasticity of the Air.

HAVE remarked, that air is a fluid, about 800 times more fubtile than water; fo that could water, without being reduced to vapour, be expanded over a fpace fo many times greater, and could become of confequence fo many times more fubtile, it would be of a fimilar confiftence with the air which we breathe. But air has a property which water has not, that of fuffering compression into a smaller space, and of being proportionably condensed, as I demonstrated in the preceding letter. And we discover in air another property no less remarkable: it is capable of being expanded over a greater space, and thus

rendered still more subtile. This operation is called the rarefaction of air.

You have only to take, as before, a tube A B C D, (plate I. fig. 3.) at the bottom of which A C, let there be a fmall aperture O, fo that, on introducing the piston as far as to F, the air may escape by that aperture without being condenfed. The air which now occupies the cavity A CEF, will then be in it's natural state; let the aperture O be closely stopped. On drawing back the pifton, the air will gradually expand through the greater space, so that when the pifton is brought back to the point G, the space C G being double the space C F, the same air which was contained in the space A C E F, will fill a space twice as great; it will be of course only half as dense, or, which is the same thing, twice as rare. If you draw back the pifton to the point H, the space C H being four times as great as the space CF, the air will become four times as rare as it was at first, as it is then expanded over a space four times as great. And could the pifton be drawn back till the space became 1000 times as great, the air would ftill equally expand through that fpace, and confequently become 1000 times as rare. Here then, likewife, air differs effentially from water: for if the cavity A C E F were filled with water, to no purpose would you draw back the pifton; the water would continue to occupy the fame space as at first, and the rest would remain empty. Hence we fee that the air possesses an intrinsic power of expanding itself more and more, which it exerts not only when it is condenfed,

but also when rarefied. In whatever state of condenfation or rarefaction the air may be, it makes unremitting efforts to extend itself over a larger fpace, and is continually expanding fo long as it meets no obstacle. This property is called the elafticity of air; and it has been demonstrated by experiments which I shall prefently describe, that this elastic power is in proportion to the density; in other words, the more the air is condenfed the greater are it's efforts to expand itself; and the more rarefied it is, the feebler are those efforts. It will be demanded, perhaps, why the air now in my chamber does not make it's escape by the door, being endowed with an expansibility continually impelling it to occupy a greater space? The answer is obvious. This would infallibly happen, did not the external air make equal efforts to extend itself; but the efforts of the air of the chamber to get out, and that of the external air to press in, being equal, they balance each other, and remain in a state of rest. Had the external air accidentally acquired a greater degree of denfity, that is, more elafticity, it would in part force it's way into the chamber, where the air being compressed, would likewife acquire a greater degree of elafticity; this current would accordingly last till the elasticity of the internal became equal to that of the external air. And should the air of the chamber suddenly become more denfe, and it's elafticity greater than that of the external air, it would force it's way out, and it's denfity gradually diminishing, it's elasticity too would diminish, till it became equal to the external air; the D 4

the current would then ceafe, and the air in the chamber would be in equilibrium with the external. Free air, then, is in a ftate of rest only when it has the fame degree of elafticity with that which furrounds it; and as foon as that of the one tract becomes more or less elastic than the adjoining, the equilibrium can no longer fubfift; but if the elafticity is greater, the air will expand itself and slide into spaces where it is smaller: and from this motion of the air refults the wind.\* Hence it comes to pass that the elasticity of the air is sometimes greater, fometimes less in the same place; and this variation is indicated by the barometer, the description of which merits a particular confideration. I confine myfelf, at present, to these qualities of air, it's condenfation and rarefaction, intreating you to recollect, that the more condenfed it is, the greater power of expansion or elasticity it acquires; and that on the contrary, the more it is rarefied, the more this quality is diminished. Experimental philosophers have invented one machine for rarefying of air, and another for condenfing it: the former is called the air-pump, the latter the condenser. These machines ferve to perform many curious experiments, with which you are already well acquainted. I referve to myfelf, however, the liberty of recapitu-

<sup>\*</sup> The action of the moon upon the atmosphere, and the motion of the earth's rotation likewise produce regular winds. Chains of mountains sometimes change the direction of winds. Hence we see that the known cause of currents of air are of three kinds, regular, accidental, and local.—F. E.

lating fome of them, because they are necessary to elucidate and explain the nature and properties of air, which, as they powerfully contribute to the preservation of animals, and the production of plants, press upon us the importance of forming a just idea of them.

14th May, 1760.

# LETTER XI.

# Gravity of the Air.

THAVE endeavoured to demonstrate, that the air is a fluid, endowed with the particular property of fuffering compression into a smaller space, and of expanding into a greater, when no obstacle interposes. This property of air, known by the name of fpring, or elafticity, from it's refemblance to a fpring, which it requires an effort to unbend, and which refumes it's form as foon as the effort ceases, is accompanied by another, in common to it with all bodies in general, namely, gravity or weight, in virtue of which all bodies tend toward the centre of the earth, and by which they are under the necessity of falling down, unless supported. The learned are very much divided, and very uncertain, respecting the primary and mechanical cause of this power, but it's existence is indubitable.\* Daily experience evinces

<sup>\*</sup> The properties of matter must ultimately be referred to the arbitrary appointment of the Author of Nature. There are certain

it. We know even the quantity of it, and can meafure it exactly. For the weight of a body is nothing elfe but the power which constrains it to descend; and as the weight of every body may be exactly meafured, we know perfectly well the effect of gravity, though the cause, or that invisible power which acts upon all bodies, forcing them to descend, may be absolutely unknown to us. It follows, that the more matter any body contains, the heavier it is. Gold and lead are heavier than wood or a feather, as they contain more matter in the fame bulk, or in the fame extent. But as air is a very fubtile and thin fubstance, and it's gravity of consequence very little, this property usually escapes our senses. Experiments, however, may be made, capable of producing full conviction that it possesses gravity. You have feen how the air may be rarefied in a veffel or a tube; and by means of the air-pump, this rarefaction may be carried fo far, as almost entirely to exhaust the air, and to leave the receiver fenfibly a vacuum. Or you may take a tube A B C D, (plate I. fig. 4.) into which you introduce the pifton, fo as perfectly to touch the bottom, and to leave no air between the two furfaces. To perform the experiment with more advantage, let there be at the bottom of the

tain principles at which the prudent philosopher will choose to stop, lest, by pushing his researches too far, he involve himself in greater obseurity. Those who attempted to account for gravity by mechanical impulse, committed an egregious oversight; for the question still recurs, What produces this impulse? No metaphysical work has ever done so much service to philosophy as Mr. Hume's admirable essay on "Necessay Connexion."—F. E.

tube a little aperture G, through which the air may escape, as the piston is pushed forward. Let the aperture then be closely stopped, that not a particle of air may be included between the pifton and the bottom of the tube. Having made this arrangement, draw back the pifton, and the external air not being able to force it's way into the tube, there will remain between the bottom of the tube and the pifton, a perfect vacuum, which may be increased at pleasure, by continuing to draw back the pifton. You may thus exclude the air contained in a veffel; and fuch veffel, reduced to a vacuum, being tried in accurate scales, will be found to weigh less than when filled with air. Hence we deduce this very important conclusion, That the air contained in an empty vessel increases it's weight, and that the air itself possesses gravity. Were the veffel large enough to contain 800 pounds weight of water, we might discover by this experiment, that the body of air which fills it would weigh nearly one pound. Hence we conclude, that air is 800 times lighter than water. I must be understood as speaking of the common air which furrounds us, and which we breathe; for you know that with the affistance of art, air may be compressed by forcing it into a smaller space, and it's gravity thereby increased. Were the vessel which I have mentioned, to be filled with air compressed to twice the confistency of common air, it would weigh two pounds more than when empty. Were it filled with air 800 times more compressed than common air, it would weigh 800 pounds more than when empty, that

that is, as much as if it were filled with water. The air, then, possessing a certain degree of gravity, though in the natural state of this sluid it's gravity is extremely fmall, it must, however, as well as all other bodies, tend toward the centre of the earth, and confequently preffes on every thing which oppofes this tendency. For this reason the superior air presses downward on the inferior, and this last undergoes a compression from the weight of the whole mass of air which is above it. Hence it comes to pass, that in these regions, the air has a certain degree of compression or density, which is the effect of the gravity of the fuperior air; and that if the fuperior air had more or less gravity, the air which furrounds us would likewise become more or less dense. It is thus that the air below supports the weight of the fuperior air, and that the more we afcend, the more it loses it's denfity and rarefies; so that were it posfible to continue to afcend, the air would at length be totally loft, or would become fo fubtile and fo rarefied, as to be no longer perceptible. Were you to descend, on the contrary, into a very deep pit, you would find the denfity of the air continually increafing, from the increase of the mass of air pressing downward upon it.

would weigh 800 bounds more class when empty,

17th May, 1760.

# mos really and he are a LETTER XII.

Of the Atmosphere, and the Barometer.

HAVING demonstrated that air is a fluid, elastic, and possessed of gravity, I proceed to remark, that the earth is furrounded on all fides by this fluid, and that the space which it fills is called the atmofphere. It would be absolutely impossible for a perfect vacuum to exist on any part of the earth's furface; for the air of the adjoining regions, compressed by the weight of the superior air, and making incessant efforts to dilate, would force itself into the empty space and fill it. The atmosphere, therefore, occupies the whole region which furrounds the earth; the inferior air is continually compressed by the weight of the fuperior air, and that until the degree of elafticity which refults from this compression, is able to form an equilibrium to the compressing power. Then, although this air is compressed only in a downward direction, it produces, in virtue of it's elafticity, efforts to expand itself not only downwards, but fideways also. For this reason, the air in a chamber is as much compressed as the external, which appeared a paradox to certain philosophers. For they reasoned thus: In a chamber, the inferior air is compressed only by the small quantity of superior air included in that chamber, whereas the external air is compressed by the weight of the whole atmosphere, the height of which is immense.

which air possesses, of expanding itself when compressed in all directions. Now the air in the chamber is at first reduced, by the external air, to the same degree of compression and elasticity with itself; hence, whether I am in my chamber, or in the open air, I feel the same compression; being always understood, that I mean at the same height, or at the same distance from the centre of the earth. For I have already remarked, that on getting to the summit of a high tower, or of a lofty mountain, the compression of the air is less, because the weight of the superior air is then diminished. Various phenomena constirm this state of the compression of the air.

Take, for instance, (plate I. fig. 5.) a tube A B, close at the end A, and having filled it with water, or any other fluid, invert it, fo that the open end B may be undermost, and you will find that the fluid does not run out. The elasticity of the air acting at B, in opposition to the fluid, supports it in the tube. But if you make an aperture into the tube at A, the fluid immediately descends: the air which is admitted by the aperture acts then from above, by it's preffure upon the water, and forces it downward; which demonstrates, that while the tube was close at top, it was the external air which supported the water in it. And were fuch a tube to be placed in a receiver, from which the air was extracted by the air-pump, the fluid would inftantly defcend. The ancients, to whom this property of air was unknown, alleged, that nature supported the water in the tube, from the

the horror which it has of a vacuum. For, faid they, were the fluid to defcend, there must be a vacuum at the upper end of the tube, as the air could find no admission into it. According to them, therefore, it was the horror of a vacuum which kept the fluid suspended in the tube. It is now demonstrated, that it is the force of the air which supports the weight of the sluid in the tube; and as this force has a determinate quantity, the effect cannot exceed a certain limit.

It is found by experiment, that if the tube A B is more than 33 feet in length, water will no longer remain fuspended in it, but will run out till it comes to the height of 33 feet; the space left a-top will, of course, be a real vacuum. The force of the air then cannot support water in the tube at more than the height of 33 feet; and as the fame force supports the whole atmosphere, it is concluded, that a column of the atmosphere is of equal weight, the basis being equal with a column of water 33 feet high. If, inflead of water, you were to use mercury, which is 14 times heavier, the force of the air could support it in the tube at the height of only 28 inches; and if you go beyond that, the mercury descends, till it's height corresponds to the pressure of the atmosphere, leaving the space a-top in the tube a vacuum. Such a tube close above, and open below, being filled with mercury, forms the instrument called the Barometer, by means of which it has been discovered, that the atmosphere is not always of equal gravity. For it's real gravity is afcertained by the barometer, from the height

height of the mercury, which, as it rifes or falls, indicates that the density of the air, or the pressure of the atmosphere, is increasing or diminishing.

zoth May, 1760.

## LETTER XIII.

Of Wind-Guns, and the Compression of Air in Gun-

Having explained that remarkable property of air which is denominated compressibility, by means of which it is reducible into a smaller space, we are enabled to give an account of several productions of both nature and art. I shall begin with an explanation of the wind-gun, though I have no doubt but you are well acquainted with that instrument. It's construction is similar to that of the common fusil; but instead of powder, we employ condensed air to discharge the bullet.

In order to comprehend the process of this operation, it must be observed, that air can be compressed only by a force proportional to the degree of condensation which you wish to obtain; in this state, it strives to extend itself, and the efforts which it makes are precisely equal to the force necessary to reduce it to the size which it actually occupies. The more, then, that the air is condensed, the more violent are it's efforts to dilate; and if the air is raised to a density twice as great as when it is free, which is the

case when we reduce it to half the space which it occupies in it's natural flate, the force with which it endeavours to expand is equal to the pressure of a column of water 33 feet high. Figure to yourfelf a great cask of this height, filled with water; this fluid will, undoubtedly, make a strong pressure on the bottom of the veffel. If you make a hole in it near the bottom, the water will force itself out with confiderable violence: and on ftopping the aperture with your finger, you will be abundantly fenfible of this pressure of the water. The bottom of the cask fustains throughout a fimilar preffure. Now a veffel containing air twice as dense as that of the atmofphere, must undergo precisely such a pressure, and if it were not fufficiently ftrong to fuftain it, would burft. The fides, then, of this veffel must be as strong as the bottom of the cask I have mentioned. If in the fame veffel the air were three times as denfe as common air, the force with which it would act upon the fides must be increased in the proportion of one more, and would be the fame which is fuftained by the bottom of a cask full of water, of 66 feet in height. You will eafily conceive that this force must be very great, and that it must go on increasing in the same ratio, according to the different degrees of condenfation of the air. This being laid down, there is, at the bottom of the air-gun, a cavity strongly fortified on all fides, into which the air is more and more compressed, in order to reduce it to as high a degree of density as the force employed for VOL. I. that

that purpose can admit. The air confined in this cavity will thereby acquire a prodigious power to force itself out: and if an aperture is made, it will fly off with a velocity proportional to that power. Now there is fuch an aperture which terminates in the cavity of the tube into which the ball is put. It is closely stopped; but when you wish to discharge the piece, you open, for an inftant, the valve which shuts it; and the air rushing forth, forces out the ball with all the velocity which we remark in shooting. Every time you discharge, the valve is kept open only a fingle moment; a certain quantity of air, therefore, and no more, can escape, and enough ftill will remain for feveral shot. But on discharge, it's denfity and corresponding elasticity diminish; and for this reason, the latter discharges are less forcible than the former, till the force is at length entirely exhausted. Were the valve to remain open any confiderable time, more air would make it's escape, which would all go to waste; for this force acts upon the ball only while it is in the barrel of the gun; as foon as it is shot off, it is useless to leave a paffage for the air. Hence it appears, that were it possible to carry the condensation of this fluid a great deal farther, you will produce from the wind-gun the fame effects as from the guns and cannons in common use.

The effect of artillery is accordingly founded on the fame principle. Gunpowder is only a fubftance, which contains in it's pores an air extremely condenfed. densed.\* Nature produces here the same operations which we employ for compressing the air, but carries the condensation to a much higher degree. All that is necessary is to open the little cavities in which this dense air is confined, that it may have liberty to escape. This is performed by means of sire, which

- · Recent experiments have fomewhat corrected this explanation. Gunpowder, it is well known, is a composition of fulphur, nitre and charcoal. In the detonation of this substance, the heat puts the fulphur and charcoal in a condition to diffolve the acid of the nitre, and to take from it the dephlogistic air which enters into it's composition. The atmospheric mephites, which is another principle of this acid, finding itself thereby difengaged, begins to expand, and forms a first elastic permanent fluid. The firing of the charcoal produces fixed air, which is a fecond elaftic permanent fluid. That of the fulphur produces the vitriolic acid, which is reduced to vapour by the heat of the inflammation (a). Finally, the water which enters into the composition of the powder, is likewise converted into vapour. Here, then, are four elastic fluids produced in the progress of this operation. To their expansion the phenomenon of the explosion is to be ascribed. The two last, brought back to a liquid flate by being cooled, form the fmoke we perceive after the discharge .- F. E.
- (a) This account of the aeriform fluids, extricated by the inflammation of gun-powder, feems very embarraffed. Sulphur is not an effential ingredient in gun-powder; but as it burns at a low heat, it renders the mass more susceptible of catching fire. The inflammation of gunpowder is precisely the same phenomenon with the detonation of charcoal and nitre. That salt is composed of vegetable alkali and nitrous acid, which confists of pure and mephitic airs united in a certain proportion. By means of the heat at first applied, and then rapidly evolved during the process of inflammation, the nitrous acid is decomposed; it's mephitic air is expelled, while it's pure air, combining with the charcoal, forms fixed air, which is also discharged. It appears from experiment, that this aerial compound, at the inflant of it's extrication, has upwards of five hundred times the elasticity of common air.—E. E.

bursts open these little envelopes: the air then suddenly slies off, with incredible velocity, and forces before it bullets and balls in a manner entirely similar to that which we have remarked in the case of the wind-gun, but with much greater impetuosity. Here, then, are two very surprising effects produced from the condensation of air, with this single difference, that in the one, it is the work of art; and in the other, that of nature. We see therefore in this, as in every thing else, how infinitely the operations of human skill are surpassed by those of nature.

- 24th May, 1760.

#### LETTER XIV.

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The Effect produced by the Heat and Cold on all Bodies, and of the Pyrometer and Thermometer.

BESIDE the properties already mentioned, air has another very remarkable quality, in common to it with all bodies, not excepting fuch as are folid; I mean the change produced on it by heat and cold. It is observable, in general, that all bodies, being heated, dilate or increase in size. A bar of iron made very hot, is somewhat longer and thicker than when it is cold. There is an instrument called the *Pyrometer*, which accurately indicates the slightest differences of length or shortness, that a bar of iron undergoes, to which it is applied. You know that

in a watch, some of the wheels move very flowly, though they communicate motion to others which revolve with confiderable rapidity. By a fimilar mechanism it is possible, from a change almost imperceptible, to produce one very confiderable, as is the case of the pyrometer, which I have just mentioned. It has an index, which runs over a very confiderable fpace, on the flightest change produced in the length of the body on which the experiment is made. On applying this instrument to a bar of iron, or any other metal, placed over a burning lamp, the index is immediately put in motion, and flews that the bar is becoming longer; and, as the heat increases, the bar likewife increases in length. But on extinguishing the lamp, and the bar growing cold again, the index moves in a contrary direction, and thereby fhews that the bar is growing shorter. The difference, however, is fo flight, that, without the help of this instrument, it would be difficult to perceive it. Yet this variation is abundantly perceptible in the motion of pendulum time-pieces. The use of the pendulum is to regulate the motion. If you lengthen it, the clock goes flower, and if you fhorten it, the clock goes faster. Now it is remarked, that in very hot weather all clocks lofe time, and proportionably gain it in very cold weather; which clearly demonstrates, that the pendulum is lengthened or fhortened, according to the temperature of the air.

All bodies undergo this alteration, but the quantity differs greatly, according to the nature of the

fubstance of which they are composed. In fluids, especially, this variability is very perceptible. To ascertain it, take a glass tube, B C, (plate I. fig. 6) joined at the end B to a hollow ball A, and let it be filled with any liquor you pleafe up to M. On heating the ball A, the liquor will rife from M toward C: when it becomes cold again, the liquor will fall toward B. This clearly proves that the fame liquid occupies a greater space when it is heated, and a fmaller when cold. It is likewise clear, that this variation must be more perceptible, when the ball is large, and the tube narrow. For, if the whole mass of liquor increases or diminishes by a thousandth part, that thousandth part will occupy, in the tube, a space great in proportion to it's narrowness. Such an inftrument then is exceedingly proper to indicate to us the different degrees of heat and cold; for if the liquor rifes or falls, it is a certain indication that the heat is increasing or diminishing. This instrument is called the Thermometer, which points out the changes that take place in the temperature of the air, and of the bodies which furround us. It must not be confounded with the barometer, whose use is to indicate the gravity of the air, or rather the force with which it is compressed. This caution is the more necessary, that the barometer and thermometer have a confiderable refemblance: being both glass tubes filled with mercury; but their conftruction, and the principles on which they are founded are entirely different. This quality of body, extension by heat,

heat, and contraction by cold, belongs likewise, in a very superior degree, to air. I shall explain it at greater length in my next letter.\*

27th May, 1760.

#### LETTER XV.

Changes produced in the Atmosphere by Heat and Cold.

HEAT and cold produce the same effect on air, as on every other body. Air is rarefied by heat, and condensed by cold. From what I have said of the elasticity of air, you easily perceive, that a certain quantity of this sluid is not determined to occupy only a certain space, as all other bodies are; but by

\* There are three kinds of thermometers in use at present, that of Reaumur is adopted in France, Switzerland, and Italy; that of Celfius in Sweden and Denmark. In both of thefe, the scale commences at the freezing point; but the interval, between that and the boiling point, is divided, in the former, into 80 parts, and the latter, into 100. Farenheit's thermometer is used in Britain and Holland; the freezing point is marked on it 32, and the boiling 212, the interval containing 180 degrees. The freezing point is very nearly permanent, but the boiling point depends on the preffure of the atmosphere, and near the surface of the earth it varies one degree and fix-tenths for every inch of variation in the height of the barometer. Water has been heated in a close veffel to such a degree, as to melt lead and tin; and in the receiver of an airpump, it may be converted into vapour, at the ordinary temperature of the air. Hence the reason why water boils so quickly on the fummit of lofty mountains. The boiling point would be at 172° on the heights of the Andes .- E. E.

it's nature, it has a perpetual tendency to dilate, and actually does expand itself, as long as it meets no ob-fracle.

This property of air is denominated elafticity. When this fluid is confined in a veffel, it makes efforts in every direction to burst it; and these efforts are greater or less in proportion to it's condensation. Hence we come to this conclusion, that the elasticity of air is in exact proportion to it's denfity; fo that when it's denfity is doubled, it's elafticity is likewife doubled; and that, in general, a certain degree of elafticity corresponds to a proportional degree of denfity. It must be remarked, however, that this takes place no longer than while the air preferves the fame degree of heat. Whenever it becomes hotter, it acquires greater power of expansion than what correfponded to it's denfity; and cold produces the oppofite effect, by diminishing it's expansive power. In order then to determine the elafticity of a mass of air, it is not fufficient to know it's denfity; you must likewise know it's degree of heat. In order to set this in a clear light. Let us suppose two chambers closely shut on all sides, but united by a door of communication; and that the heat in both is equal. In order to this the air in both chambers must have the fame degree of denfity. For were the air more denfe, and confequently more elaftic, in the one than in the other, part of it would escape from the one, and force it's way into the other, till the denfity in both were the fame. But let us suppose that one of the chambers has become hotter than the other, the air thereby acquiring

acquiring a greater elasticity, would of course force itself into the other, and reduce that which it found there into a fmaller space, till the elasticity in both chambers was brought to the fame degree. During this change there will be a current of air, through the door, from the chamber which is more, into that which is less heated; and when the equilibrium is restored, the air will be more rarefied in the warm apartment, and more condenfed in the cold; and yet the elasticity of both will be the same. From this it clearly follows, that two maffes of air of different denfity, may have the fame elafticity, when the one is hotter than the other; and this circumstance taken into confideration, it may happen, that with the fame degree of denfity, they may be endowed with different degrees of elafticity.

What I have faid of two chambers may be applied to two countries; and hence it may be concluded, that when one country becomes warmer than the other, there must of necessity be a current of air from the one to the other: and from this results the wind.

Here, then, is one fruitful fource of winds, though there are perhaps others, which confift in the different degrees of heat, which prevail in different regions of the earth; and it is demonstrable, that the whole air which furrounds the earth could not be in a state of rest, unless that, universally, at equal heights, there were found the same degree, not only of density, but likewise of heat. And should it happen that there were no wind over the whole surface of the earth, it might with certainty be concluded, that the air would likewife be every where equally denfe and warm at equal heights. Now as this never happens, there must of necessity always be winds, at least in fome regions. But these winds are, for the most part, to be met with only on the furface of the earth; and the higher you rife, the lefs violent winds are. Winds are hardly perceptible at the fummit of very high mountains; \* there perpetual tranquillity reigns; from which it is impossible to doubt, that at confiderable elevations, the air is always in a ftate of reft. Hence it follows, that in regions remarkably elevated, there univerfally prevails all over the earth, the fame degree of denfity and heat; for were it hotter in one place than in another, the air could not be in a state of rest. And, as there is no wind in these elevated regions, it must necessarily follow, that the degree of heat there must be universally and always the fame; which is a very furprizing paradox, confidering the great variations of heat and cold which we feel on the furface of the earth, during the course of a year, and even of one day; without taking into the account the difference of climate, that is, the intolerable heats felt under the equator, and the

\* This does not appear perfectly exact. A perpetual current of wind, from east to west, must be produced by the motion of the earth's rotation. It results, likewise, from M. d'Alembert's theory of winds. Besides, the attraction of the moon, which is capable of raising the waters of the globe, undoubtedly communicates some motion to the atmosphere. Here, then, we have superior currents.

When aërostation is carried to perfection, it will, perhaps, procure us satisfying information respecting this article of meteorology.—F. E.

dreadful

dreadful cold which ever prevails toward the poles of the earth. Experience itself, however, confirms the truth of this aftonishing fact. The snow and ice remain equally, fummer and winter, on the mountains of Switzerland, and are equally unchangeable on the Cordeliers, lofty mountains of Peru, fituated under the very equator, and where there perpetually reigns, nevertheless, a cold as excessive as that of the polar regions. The height of these mountains is not a German mile,\* or 24,000 feet. From this it may be, with confidence, concluded, that were it possible for us to afcend to the height of 24,000 feet, above the earth, we fhould always and univerfally meet with the fame degree of cold, and that cold exceffively fevere. † We should remark there no sensible difference during either fummer or winter, under the equator, or near the poles. At this height, and ftill higher, the ftate of the atmosphere is univerfally, and at all feafons, the fame; and the variations of heat and cold take place near the furface of the earth alone. It is only in these inferior regions, that the effect of the rays of the fun becomes perceptible. You have, undoubtedly, fome curiofity to know the reason of this. It shall be the subject of the following letter.

31st May, 1760.

LETTER

<sup>\*</sup> About 4 3-5ths miles, English.

<sup>†</sup> M. Charles, in his aërial voyage of the 1st Dec. 1783, felt this change of temperature in a very sensible manner; for then, on the surface of the earth, the sluid in the thermometer stood at 7° above the freezing point, and after about 10 minutes of ascension, it had sallen to 5° below it.—F. E.

## LETTER XVI.

The Cold, felt on high Mountains and at great Depths, accounted for.

TT appears very furprifing, that we should feel the I same degree of cold in all regions, after we have risen to a certain height, fay 24,000 feet; considering that the variations with respect to heat, on the earth, not only in different climates, but in the fame country, at different feafons of the year, are fo perceptible. This variety, which takes place at the furface of the globe, is undoubtedly occasioned by the fun. It appears, at first fight, that his influence must be the fame above and below, especially when we reflect, that a height of 24,000 feet, or a mile, though very great with respect to us, and even far beyond the height of the loftiest mountains, is a mere nothing, compared to the distance of the sun, which is about thirty millions of miles.\* This is, therefore, a very important difficulty, which we must endeavour to folve. For this purpose I begin with remarking, that the rays of the fun do not communicate heat to any bodies, but fuch as do not grant them a free paffage. You know that bodies, through which we can discern objects, are denominated transparent, pellucid, and diaphonous. These bodies are glass, crystal,

diamond,

<sup>\*</sup> Mr. Euler always means German miles, of 4000 fathoms each, or fomewhat under 4 3-5ths miles English.—E. E.

diamond, water, and feveral other liquids, though fome are more or less transparent than others. One of these transparent bodies being exposed to the fun, is not heated to fuch a degree as a body not transparent, as wood, iron, &c. Bodies not transparent are denominated opaque. A burning-glass, for example, by transmitting the rays of the fun, sets on fire opaque bodies, while the glass itself is not fensibly heated. Water exposed to the fun becomes fomewhat warm, only because it is not perfectly transparent; when we fee it confiderably heated by the fun at the brink of rivers, it is because the bottom, being an opaque body, is heated by the rays which the water transmits. Now, every heated body communicates that heat to all adjoining bodies; the water accordingly derives heat from the bottom. If the water be very deep, fo that the rays cannot penetrate to the bottom, it has no perceptible heat, though the fun bears upon it.

As air is a very transparent body to a much higher degree than glass or water, it follows that it cannot be heated by the sun, because the rays are freely transmitted through it. The heat which we frequently feel in the air is communicated to it by opaque bodies, which the rays of the sun have heated; and were it possible to annihilate all these bodies, the air would scarcely undergo any change in it's temperature by the rays of the sun: exposed to it or not it would be equally cold. But the atmosphere is not perfectly transparent: it is even sometimes so loaded with vapours, that it loses almost entirely it's transparency,

transparency, and presents only a thick fog. When the air is in this state, the rays of the sun have a more powerful influence upon it, and heat it immediately.

But these vapours rise to no great height; at the height of 24,000 feet, and beyond, the air is fo fubtile and fo pure, that it is perfectly transparent; and for this reason the rays of the sun cannot immediately produce any effect upon it. This air is likewife too remote from terrestrial bodies to receive a communication of heat from them; they act only upon fuch as are adjacent. Hence you will eafily perceive that the rays of the fun cannot produce any effect in regions of the air very much elevated above the furface of the earth; and that the fame degree of cold must always and universally prevail in such regions, as the fun has no influence there, and as the heat of terrestrial bodies cannot be communicated fo far. This is nearly the case on the summit of very high mountains, where it is always much colder than on plains and in vallies.\*

<sup>\*</sup> There are clouds, however, above these mountains, and in almost as great a quantity as above the plains, which is demonstrated by the snows which cover the highest summits. There are sew naturalists who have not been surprised by clouds in their excursions upon the mountains. The heat that is selt when such clouds are formed must be attributed almost entirely to the transmission of the water which sound itself dissolved in the air, under the form of elastic sluid, to a liquid state. The heat of the solar rays, intercepted by the cloud, can produce no change in the inferior temperature, as it would have been transmitted from the ground.—F. E.

The city of Quito, in Peru, is almost under the equator, and were we to form our judgment from it's fituation on the globe, we would suppose it oppressed with intolerable heat; the air, however, is abundantly temperate, and differs very little from that of Paris. Quito is fituated at a great height above the real furface of the earth. In going to it from the fea fhore you have to afcend for feveral days; it is accordingly built in an elevation equal to that of our highest mountains, though surrounded by others ftill much higher, called the Cordeliers. This last circumstance would afford a reason for thinking that the air there must be as hot as at the furface of the earth, as it is contiguous on all fides to opaque bodies, on which the rays of the fun fall. The objection is folid; and no folution can be given but this. That the air at Quito, being very elevated, must be much more subtile, and of less gravity than with us; and the barometer, which always stands confiderably lower, incontestably proves it.

Air of fuch a quality is not fo fufceptible of heat as common air, as it must contain less vapour and other particles which usually float in the atmosphere; and we know by experience that air very much loaded is proportionably susceptible of heat. I must here subjoin another phenomenon no less surprising: In very deep pits, and lower still, if it were still possible to descend, the same degree of heat always and universally prevails, and nearly for the same reason. As the rays of the sun exert their influence only on the surface of the earth, and as the heat which they

there

there excite communicates itself up and down, this effect at very great depths is almost imperceptible. The same thing holds respecting considerable heights. This elucidation will, I flatter myself, prove satisfactory.\*

3d June, 1760.

#### LETTER

\* The reason which Professor Euler assigns for the cold that prevails in the higher regions of the atmosphere feems plausible, but will not fland an accurate examination. Light is much impaired in it's paffage through the atmosphere, and the heat communicated is in every case proportional to the quantity of absorption. It appears, from fome ingenious experiments of M. Bouguer, that we receive only four-fifths of the rays of a vertical fun; and when that luminary approaches the horizon, the portion of his light which reaches the furface of the earth, is much smaller. Thus at an elevation of 20 degrees it is one half; at that of 10 degrees one third; and at that of five degrees one-eighth. Hence the fun-beams are most powerful on the fummits of losty mountains, for they fuffer the greatest diminution in passing through the dense air of the lower regions. If the air derived it's heat from the furface of the earth, those countries would be warmest which enjoyed the greatest quantity of fun-shine. The British islands are shrouded in clouds nine months of the year; yet our climate is milder than that of the same parallel on the Continent, where the fky is generally ferene. The elevated town of Quito, exposed to a brilliant fun, enjoys a temperate air; while the Peruvian plains, shaded with fleecy clouds, are parched with heat. Were the reasoning in the text to be admitted, we should conclude that the tops of mountains are warmer than their bases. To say that air, much rarefied, is not susceptible of heat, is a very extraordinary affertion, fince we are acquainted with no fubstance whatever that may not be heated. Besides, a more intense cold may be artificially produced than what prevails in the lofty regions of the atmosphere. We must recur to other principles for the true folution

#### LETTER XVII.

Of Light, and the Systems of Descartes and Newton.

HAVING spoken of the rays of the sun, which are the socus of all the heat and light that we enjoy, you will undoubtedly ask, What are these rays? This is beyond question one of the most important inquiries in physics, as from it an infinite number

folution of the fact. It is indifferent what portion of the air first receives the heat; the effect depends entirely on the nature of it's distribution. If the atmosphere were of an uniform density throughout, the heat would at all heights be likewise the same. But as the density varies according to the altitude, the distribution of heat is affected by that circumstance, and follows a certain corresponding law. I would gladly develope the principles from which this theory is deduced, but the popular nature of the present treatise forbids all abstract discussion. I shall therefore content myself with giving a table of the diminution of heat at different altitudes.

Altitude in	to the	Diminution of heat, in degrees, of Farenheit,					
3,000	_	2	_		120		
6,000	-	_		_	241		
9,000	-		-		38		
, 12,000	-		-	-	53		
15,000	_	-	-	_	681		
18,000	-		-	-	861		
21,000	-	1000	-	-	041		

The diminution of heat, on the afcent, is not quite fo great in extensive continents; for the intercourse between the rare and the dense portions of the atmosphere is, in this case, necessarily slow, and the heat, which is principally formed at the surface, will only be partially dispersed.

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number of phenomena is derived. Every thing that respects light, and that renders objects visible, is closely connected with this inquiry. The ancient philosophers seem to have taken little interest in the solution of it. They contented themselves with saying that the sun is endowed with the quality of shining, of giving heat and light. But is it not worth while to inquire, Wherein does this quality consist? Do certain portions, inconceivably small, of the sun himself, or of his substance, come down to

It is a common mistake to suppose, that the same heat obtains, at a certain depth, in every part of the globe. The fact is, that heat, originally derived from the sun, is communicated very slowly to the matter below the surface, which, therefore, does not feel the vicissitude of seasons, but retains the average temperature of the climate for many ages. Hence the utility of examining the heat of springs, which is the same with that of the substances through which they flow. The following table exhibits the average heat of places on the level of the sea, computed by the celebrated astronomer, Professor Meyer, for every five degrees of latitude.

Latitude. Averag		Temperature	Latitude	. Average Tempera			rature.		
	0	-	2001270	840	50	-	-	5320	
	5	-	07	831	55	-		49	
	10	-	-	821	60	-	-	45	
	15	-	-	801	- 65	-	-	412	
	20	-	-	78	70	-	-	38	and the
	25	-	-	745	75	-		351	
	30	-	-	71	80	-	-	335	
	35	-	-	67	85	-	-	321	
	40	-	-	$62\frac{1}{2}$	190	-	-	32	
	45	-	of house house	58	and no a				ME

By comparing this table with the preceding, it is easy to difeover, for any latitude, the altitude of the curve of congelation, or where the average temperature is 32°.—E. E. us? Or is the transmission similar to the sound of a bell, which the ear receives? though no part of the substance of the bell be separated from it, as I observed in explaining the propagation and perception of sound.

Defcartes, the first of modern philosophers, maintained this last opinion, and having filled the whole universe with a subtile matter composed of small globules, which he calls the second element, he supposes that the sun is in a state of continual agitation, which he transmits to these globules, and pretends that they again communicate their motion in an instant to every part of the universe. But since it has been discovered that the rays of the sun do not reach us instantaneously, and that they take eight minutes to fly through that immense distance,\* the opinion of Descartes, which laboured beside under other dissipations, has been given up.

The great Newton afterwards embraced the former fystem, and maintained that the luminous rays are really separated from the body of the sun, and the particles of light thence emitted with that inconceivable velocity which brings them down to us in about eight minutes. This opinion, which is that of most modern philosophers, particularly the English, is

<sup>\*</sup> This important fact was discovered toward the end of the last century by Roemer, a learned Dane, of the ancient Academy of Sciences. It was an inequality of the satellites of Jupiter which led him to it. The cause of this aberration, discovered by Bradley in 1728, incontestably demonstrates the same phenomenon.— F. E.

called the fystem of emanation; it being imagined that rays emanate from the sun and other luminous bodies, as water emanates or springs from a fountain.

This opinion appears at first fight very bold, and irreconcileable to reafon. For were the fun emitting continually, and in all directions, fuch floods of luminous matter, with a velocity fo prodigious, he must speedily be exhausted, or at least some alteration must, after the lapse of so many ages, be perceptible. This, however, is contradicted by observation. It cannot be a matter of doubt, that a fountain which should emit streams of water in all directions, would be exhaufted in proportion to the velocity of the emission; much more the fun, whose rays are emitted with a velocity fo inconceivable. Let the particles of which rays of light are formed be supposed as subtile as you pleafe, nothing will be gained: the fyftem will ever remain equally untenable. It cannot be affirmed that this emanation is not made in all directions: for, wherever you are placed, the whole fun is visible, which proves incontestably, that rays from every point of the fun are emitted toward the fpot which you occupy. The cafe is very different from that of a fountain, which should emit streams of water in all directions. For one point in the fountain could furnish only one stream directed to a particular fpot, but every point of the fun's furface must emit an infinite number, diffufing themfelves in all directions. This circumstance alone infinitely increases the expenditure of luminous matter, which the fun would have to make.

Another

Another difficulty, and which appears equally infuperable, is, that the fun is not the only body which emits rays, but that all the flars have the fame quality: and as every where the rays of the fun must be crofling the rays of the ftars, their collision must be violent in the extreme. How must their direction be changed by fuch collision! This collision must take place with respect to all luminous bodies, visible at the same time. Each, however, appears distinctly, without fuffering the flightest derangement from any other: a certain proof that many rays may pass through the fame point, without diffurbing each other, which feems irreconcileable to the fystem of emanation. Let two fountains be fet a playing upon each other, and you will immediately perceive their different streams disturbed and confounded: it must of confequence be concluded, that the motion of the rays of light is very effentially different from that of a jet d'eau, and in general from all fubstances forcibly emitted.

Considering afterwards transparent bodies through which rays are freely transmitted in all directions, the supporters of this system are under the necessity of affirming that these bodies contain pores, disposed in straight lines, which issue from every point of the surface, and proceed in all directions; it being inconceivable how there could be any line through which a ray of the sun might be transmitted with such amazing velocity, and even without the slightest collision. Here then are bodies wonderfully po-

rous, which have the appearance, nevertheless, of being extremely folid.

Finally, in order to enjoy vision, the rays must enter into the eye, and penetrate it's substance with the same velocity. All these difficulties, taken together, will, I doubt not, sufficiently convince you, that the system of emanation has in no respect a soundation in nature; and you will certainly be astonished that it could have been conceived by so great a man, and embraced by so many enlightened philosophers. But it is long since Cicero remarked, that nothing so absurd can be imagined as to find no supporter among philosophers. For my part, I am too little a philosopher to adopt the opinion in question.

7th June, 1760.

## LETTER XVIII.

Difficulties attending the System of Emanation.

Newton may appear, that rays proceed from the fun by a continual emanation, it has, however, been so generally received, that it requires an effort of courage to call it in question. What has chiefly contributed to this is, no doubt, the high reputation of the great English philosopher, who first discovered the true laws of the motions of the heavenly bodies:

and

and it is this very discovery which led him to the fystem of emanation.

Descartes, in order to support his theory, was under the necessity of filling the whole space of the heavens with a fubtile matter, through which all the celestial bodies move at perfect liberty. But it is well known that if a body moves in air, it must meet with a certain degree of reliftance; from which Newton concluded, that however fubtile the matter of the heavens may be supposed, the planets must encounter fome reliftance in their motions. But, faid he, this motion is not subject to any resistance: the immense space of the heavens, therefore, contains no matter. A perfect vacuum, then, univerfally prevails. This is one of the leading doctrines of the Newtonian philosophy, that the immensity of the universe contains no matter in the spaces not occupied by the heavenly bodies. This being laid down, there is between the fun and us, or at least from the fun down to the atmosphere of the earth, an absolute vacuum. In truth, the farther we ascend, the more fubtile we find the air to be; from whence it would apparently follow, that at length the air would be entirely loft. If the space between the fun and the earth be an absolute vacuum, it is impossible that the rays should reach us in the way of communication, as the found of a bell is transmitted by means of the air. For if the air, intervening between the bell and our ear, were to be annihilated, we should absolutely hear nothing, let the bell be ftruck ever fo violently.

Having established, then, a perfect vacuum between the heavenly bodies, there remains no other opinion to be adopted but that of emanation; which obliged Newton to maintain, that the fun and all other luminous bodies emit rays which are always particles, infinitely fmall, of their mass, darted from them with incredible force. It must be such to a very high degree, in order to impress on rays of light that inconceivable velocity with which they come from the fun to us in the space of eight minutes. But let us fee whether this theory be confiftent with Newton's leading doctrine, which requires an abfolute vacuum in the heavens, that the planets may encounter no manner of reliftance to their motions. You must conclude, on a moment's reflection, that the space in which the heavenly bodies revolve, inftead of remaining a vacuum, must be filled with the rays, not only of the fun, but likewise of all the other ftars which are continually paffing through it from every quarter, and in all directions, with incredible rapidity. The heavenly bodies which traverse these spaces, instead of encountering a vacuum, will meet with the matter of luminous rays in a terrible agitation, which must disturb these bodies in their motions much more than if it were in a ftate of rest.

Thus Newton, apprehensive lest a subtile matter, such as Descartes imagined, should disturb the motions of the planets, had recourse to a very strange expedient, and quite contradictory to his own intention, as, on his hypothesis, the planets must be expedied to a derangement infinitely more considerable.

I have already submitted to you several other insuperable objections to the system of emanation; and we have now seen that the principal and indeed the only reason which could induce Newton to adopt it, is so self-contradictory as wholly to overturn it. All these considerations united, leave us no room to hesitate about the rejection of this strange system of the emanation of light, however respectable the authority of the philospher who invented it.

Newton was, without doubt, one of the greatest geniuses that ever existed. His prosound knowledge, and his acute penetration into the most hidden mysteries of nature, will be a just object of admiration to the present, and to every future age. But the errors of this great man should serve to admonish us of the weakness of the human understanding, which, after having soared to the greatest possible heights, is in danger of plunging into manifest contradiction.\*

10th June, 1760.

LETTER

\* The pious as well as learned and ingenious Author, in the first edition of these Letters, subjoined to this reflection on Newton's doctrine of emanation a series of reflections which do equal honour to his understanding and his heart. The French Editor, for what reason it does not appear, has thought proper to suppress them. Could he imagine a philosophical work disgraced by a modest and not unseasonable insusion of religious sentiment? Be how it will, the English Editor selt himself obliged to restore the passage, in presenting the too long neglected Euler to the British nation.—

It follows:

<sup>&</sup>quot; If we are liable to weaknesses and inconsistencies so humiliat-

#### LETTER XIX.

A different System respecting the Nature of Rays and of Light, proposed.

YOU have feen that the fystem of the emanation of the rays of light labours under insuperable disticulties, and that the doctrine of a vacuum for the heavenly bodies to range in, is equally untenable; as the rays of light would completely fill it. Two things, then, must be admitted: first, the space through which the heavenly bodies move is filled with a subtile matter; secondly, rays are not an actual emanation from the sun and other luminous bodies, in virtue of which part of their substance is

" ing, in our refearches into the phenomena of this vifible world, " which lies open to the examination of our fenses, how wretched " must we have been had God left us to ourselves with respect to " things invifible, and which concern our eternal falvation? On " this important article a Revelation was absolutely necessary to " us; and we ought to avail ourselves of it with the most pro-66 found veneration. When it presents to us things which may " appear inconceivable, we have but to reflect on the imperfection. " of human understanding, which is so apt to be misled, even as " to fensible objects. Whenever I hear a pretended Freethinker " inveighing against the truths of religion, and even sneering at " it with the most arrogant self-sufficiency, I say to myself: poor " weak mortal, how inexpressibly more noble and sublime are the " fubjects which you treat fo lightly, than those respecting which " the great Newton was fo grofsly mistaken! I could wish your " Highness to keep this reflection ever in remembrance: occasions " for making it occur but too frequently."-E. E.

violently

violently emitted from them, according to the doctrine of Newton.\*

That fubtile matter which fills the whole space in which the heavenly bodies revolve, is called *Ether*. Of it's extreme subtilty no doubt can be entertained. In order to form an idea of it, we have only to attend to the nature of air, which, though extremely subtile, even on the surface of the earth, becomes more and more so as we ascend; and entirely ceases, if I may use the expression, when it comes to be lost in the ether. The ether, then, is likewise a fluid as the air is, but incomparably siner and more subtile, as we are assured that the heavenly bodies revolve

. The materiality of light is supported by the most convincing proofs that physics can afford. The inflection, refraction, and reflection of it's rays, thew manifestly that, like other bodies, it is fubject to attraction and repulsion; and the simple application of the doctrine of forces not only explains fatisfactorily the phenomena, but affigns the precise effects with the most periect accuracy. The difficulties which feem to attend the theory of emanation vanish on a close investigation. So vast is the tenuity of light, that it utterly exceeds the powers of conception. The most delicate instrument has never been certainly put in motion by the impulse of the accumulated fun-beams. Even on the most unfavourable fupposition it appears from calculation that, in the space of 385,130,000 Egyptian years (of 360 days) the fun would lofe only the 1,217,420th of his bulk, from the continual efflux of light. On the same hypothesis the force impressed upon the earth by each emission is such as would make it recede only the two billionth part of an inch in an hundred feconds, and it's effect, during a feries of ages, would therefore be altogether infenfible. After flating numbers of a magnitude fo enormous, it would be fuperfluous to confider the quantity of stroke which the eye receives.

freely through it, without meeting any perceptible refistance. It is also without doubt possessed of elasticity, by means of which it has a tendency to expand itself in all directions, and to penetrate into spaces where there would otherwise be a vacuum; so that if by some accident the ether were forced out of any space, the surrounding sluid would instantly rush in and fill it again.

In virtue of this elafticity, the ether is to be found not only in the regions which are above our atmofphere, but it penetrates the atmosphere univerfally, infinuates itself by the pores of all bodies, and passes irrefiftibly through them. Were you, by the help of the air-pump, to exhauft the air from a receiver, you must not imagine that you have produced an absolute vacuum; for the ether, forcing itself through the pores of the receiver, completely fills it in an instant. Having filled a glass tube of the proper length with mercury, and immerged it, when inverted, in the ciftern, in order to make a barometer, it might be supposed that the part of the tube which is higher than the mercury is a vacuum, because the air is completely excluded, as it cannot penetrate the pores of glass: but this vacuum which is apparent only, is undoubtedly fupplied by the ether, infinuating itfelf without the fmallest difficulty.

It is by this fubtilty and elafticity of ether that I shall by and by explain to you the remarkable phenomena of electricity. It is even highly probable that ether has an elasticity much superior to that of air, and that many of the phenomena of nature are produced

produced by means of it. For my own part I have no doubt that the compression of the air in gunpowder is the effect of the elastic power of ether. And as we know by experiment that the air in it is condensed almost 1000 times more than common air, and that in this state it's elasticity is likewise 1000 times greater, the elasticity of the ether must in this case be so too, and consequently 1000 times greater than that of common air. We shall then have a just idea of ether, in considering it as a sluid in many respects similar to air, with this difference, that ether is incomparably more subtile and more classic.\*

Having seen then that the air, by these very qualities, is in a proper state for receiving the agitations or shakings of sonorous bodies, and to disfuse them in all directions, as we find in the propagation of sound, it is very natural to suppose that ether may in the same circumstances likewise receive agitations in the same manner, and transmit them to the greatest distances.† As the vibrations of the air produce

<sup>\*</sup> This, perhaps, is what in modern times they denominate the matter of heat.—F. E.

<sup>†</sup> The hypothesis of an ether is a clumfy attempt to preclude the necessity of admitting action at a distance. It has been a received maxim, that cause and effect must exist in the same place; but the least resection will convince us that, were this principle true, there could never be any communication of motion. The dissiculty is really the same, to conceive action exerted at the distance of the thousandth part of an inch, as at that of a thousand miles. The particles of matter are far from being in mutual contact, other-



to the rays of light; for were it possible to separate them from the fmoke and other exhalations, the luminous quality alone would occasion no expenditure. Mercury may, by means of art, be rendered luminous, as you have probably feen, and that without any diminution of it's fubstance, which proves that light alone produces no wafte of luminous bodies. Thus though the fun illuminates the whole world by his rays, he lofes nothing of his own fubstance, his light being only the effect of a certain agitation, or violent concussion of his minute particles, communicated to the adjoining ether, and thence transmitted in all directions by means of this fluid to the remotest distances, as a bell when struck communicates it's own agitation to the circumambient air. The more we confider this parallel between fonorous and luminous bodies, the more we shall find it conformable to nature, and justifiable by experience; whereas the more we attempt to reconcile the phenomena of nature to the fystem of emanation, the more difficulties we encounter.

14th June, 1760.

## LETTER XX.

# Of the Propagation of Light.

THE propagation of light in the ether is produced in a manner fimilar to that of found in the air; and just as the vibrations occasioned in the particles of air constitutes found, in like manner the vibration

of the particles of ether conftitutes light or luminous rays; fo that light is nothing else but an agitation or concussion of the particles of ether, which is every where to be found on account of it's extreme subtilty, in virtue of which it penetrates all bodies.

These bodies, however, modify the rays of light in many different ways, by transmitting or stopping the propagation of the concussions. Of this I shall treat at large in the sequel. I confine myself at present to the propagation of rays in the ether itself, which fills the immense space in which the heavenly bodies revolve. There the propagation takes place in perfect liberty. The first thing which here presents itself to the mind is the prodigious velocity of the rays of light, which is about 900,000 times more rapid than that of sound, though this last travels no less than 1000 feet in a second.

This amazing velocity would be fufficient of itself to overturn the system of emanation; but in that which I am attempting to establish, it is a natural consequence, from the principles laid down, as I hope to demonstrate. They are the same with those on which is founded the propagation of sound in the air, and this depends at once on it's density and elasticity. It is evident that if the density of air were diminished, sound would be accelerated, and if the elasticity of the air were increased, the same thing would happen. If the density of the air diminished, and it's elasticity increased at once, we should have a two-fold reason for the increase of the velocity of sound. Let us conceive, then, the density of the air diminished,

diminished, and it's elasticity increased, till it's denfity and elafticity became equal to those of ether, and we should then no longer be surprised that the velocity of found had become many thousands of times greater than it actually is. For you will be pleafed to remember, that, according to the first ideas we formed of ether, this fluid must be inconceivably rarer, and more elastic than air. Now both of these qualities equally contribute to accelerate the velocity of vibrations. From this explanation, the prodigious velocity of light is fo far from prefenting any thing irreconcileable to reason, that it rather perfectly harmonizes with the principles laid down; and the parallel between light and found is in this respect so firmly established, that we may confidently maintain, That if air should become as subtile and as elastic as ether, the velocity of found would become as rapid as that of light.

The fubtlity of ether, then, and it's great elafticity, are the reason which we assign for the prodigious velocity of the motion of light; and so long as the ether preserves this same degree of subtlity and elasticity, this velocity must continue the same. Now it cannot be doubted that the ether has, through the whole universe, the same subtlity and the same elasticity. For were the ether less elastic in one place than in another, it would force itself into it till the equilibrium was perfectly restored. The light of the stars, therefore, moves with as great velocity as that of the sun; and as the stars are at a much greater distance from us than the sun, a much greater quan-

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However great the distance of the sun may appear, whose rays, nevertheless, reach the surface of our globe in eight minutes, the fixed star nearest to us is at least 400,000 times more distant than the sun: a ray of light issuing from that star will employ then 400,000 times eight minutes in travelling to us, that is 53,333 hours, or 2,222 days, or six years nearly.

It is then upwards of fix years fince the rays of light iffued from that fixed ftar, the leaft remote and probably the most brilliant, in order to render it vifible to us, and these rays have employed a period so confiderable to fly through the space which separates us from that star. Were God just now to create a new fixed ftar, at the fame diftance, it could not become visible to us till more than fix years had elapsed, as it's rays require that length of time to travel this distance. Had one been created at the beginning of the world a thousand times more distant than that which I have mentioned, it could not yet be visible to us, however brilliant, as 6000 years are not yet elapfed fince the Creation. The first preacher of the court of Brunfwick, Mr. Jerufalem, has happily introduced this thought in one of his fermons; the paffage runs thus:

"Raise your thoughts from the earth which you inhabit to all the bodies of the vast universe, which are so far above you: launch into the immensity of space which intervenes between the most remote which your eyes are able to discover, and those whose light, from the moment of creation till

"till now, has not as yet, perhaps, come down to us.
"The immensity of the kingdom of God justifies
"this representation." (Sermon on the Heavens, and
Eternal Beatitude.)

I flatter myfelf that these reslections will excite a desire of further instruction respecting the system of light, from which is derived the theory of colours, and of vision.

17th June, 1760.

#### LETTER XXI.

Digression, on the Distances of the Heavenly Bodies, and on the Nature of the Sun, and his Rays.

THE observations which I have been making refrecting the time which the light of the stars employs in making it's progress down to us, convey a striking idea of the extent and greatness of the universe. The velocity of sound, which slies through the space of 1000 feet in a second, surnishes us with nearly the first standard of measurement. It is about 200 times more rapid than the pace of a man who is a good walker. Now the velocity of the rays of light is 900,000 times still more rapid than that of sound: these rays accordingly perform, every second, a course of 900 millions of feet, or 37,500 German miles.\*

What aftonishing velocity! Yet the nearest fixed

<sup>\*</sup> More than 170,000 miles English .- E. E.

ftar is fo remote, that it's rays, notwithstanding this prodigious velocity, would take more than six years in descending to us. And were it possible for a great noise, such as that of the siring of a cannon, issuing from that star, to be conveyed to our ears, it would require a period of 5,400,000 years to reach us. And this is applicable only to those stars which are the most brilliant, and are probably nearest to us. Those which appear the smallest are, very probably, ten times still farther remote, and more. A whole century then, at least, must elapse, before the rays of these stars could possibly reach us. How prodigious must that distance be, which cannot be passed through in less than 100 years, by a velocity which slies at the rate of 37,500 German miles every second!

Were, then, one of these stars to be just now annihilated, or eclipsed only, we should still continue to see it for 100 years to come, as the last rays which it emitted could not reach us in less time.

The generality of mankind is very far from having any thing like just ideas respecting the vast extent of the universe. Many consider it as a work of little importance, which chance alone might have produced. But what must be the astonishment of one who reslects, on observing, that all these immense bodies are arranged with the most consummate wisdom, and that the more knowledge we acquire on the subject, though it must ever be very impersect, the more we must be disposed to admire their order and magniscence?

I return to the great luminous bodies, and particularly

cularly the fun, which is the principal fource of the light and heat which we enjoy on the earth. It will be asked, in the first place, Wherein consists the light which the fun is inceffantly diffusing through the whole universe, without ever fuffering the smallest diminution? The answer is obvious, according to the fyftem which I have been endeavouring to eftablish. But that of emanation furnishes no satisfactory folution. The whole universe being filled with that extremely fubtile and elastic fluid, which is called ether, we must suppose, in all the parts of the fun, an inceffant agitation, by which every particle is in a constant motion of vibration, and this, by communicating itself to the circumambient ether, excites in that fluid a fimilar agitation, and is thence transmitted to regions the most remote, with the rapidity which I have been describing.

And, to keep up the parallel between found and light, the fun would be in a ftate fimilar to that of a bell which should be ringing continually. The particles of the fun must, consequently, be kept in this incessant agitation, to produce in the ether the undulations which we call rays of light. But it is still no easy matter to explain, by what power this agitation in the particles of the fun is constantly kept up, as we observe, that a match does not long continue burning, but presently goes out, unless it be supplied with combustible matter. But it must be remarked, that as the fun is a mass many thousand times greater than our whole globe, if it is once thoroughly inflamed, it may continue in that state

for feveral ages, without fuffering any fensible diminution. Besides, the case is not the same with the sun and our fires and candles, a considerable part of whose substance is dissipated in smoke and exhalations, from which a real waste results. Whereas, though perhaps some particles may be forced from the sun in form of smoke, they cannot remove to a great distance, but speedily fall back into it's mass, so that there cannot be any real expenditure, to occasion a diminution of his substance.\*

The only thing of which we are still ignorant refpecting this subject, is, the power which incessantly maintains all the particles of the sun in this agitation. But as it contains nothing inconsistent with good sense, and as we are under the necessity of acknowledging our ignorance of many other things much less remote than the sun, we ought to be satissied, if our ideas are not involved in contradiction.

21/t June, 1760.

\* The Author is evidently embarraffed in his explanation of the continual inflammation of the fun. And though he has faid above, that the fystem of emanation was untenable, on account of the frequent and unavoidable collision of rays proceeding from different luminous bodies, which must disturb, and even obstruct the vision of several of these bodies at once, as he has not explained how two sounds may be heard at the same time, a similar objection might be made to his system, which is analogous to the phenomena of sound.—F. E.

thoroughly indemed it may continue in that



fubtilty. It requires vibrations much more frequent. An agitation fo rapid could not take place but in the minutest particles of bodies which elude our senses. The light of the sun, then, is produced by a very violent agitation, which affects all his infinitely minute particles, each of which must shake many thousands of times every second.

It is a fimilar agitation which likewife produces the light of the fixed stars, and of all sires, such as candles, tapers, torches, &c. which give us light, and supply the place of the sun during the night. On attentively observing the slame of a wax-light, you will easily perceive that, in the minutest particles, there is a constant and surprizing agitation; and I do not apprehend that my system is liable on this side to any contradiction, while that of Newton requires a most enormous agitation, capable of launching the minutest particles with the velocity of 37,500\* German miles in a second.

This, then, is the explanation of the nature of bodies luminous of themselves: for there are luminous bodies which are not so immediately, such as the moon and the planets, which are similar to our globe. We see the moon only when, and in as far as, she is illuminated by the sun; and this is the case of all terrestrial bodies, sires excepted, which have a light of their own. But other bodies, which are denominated opaque, become visible to us only when they are illuminated by some luminous body.

In a very dark night, or in an apartment, fo closely

<sup>\*</sup> Upwards of 170,000 English miles.

thut on every fide, that no light can find admission, to no purpose will you turn your eyes toward the objects which furround you in the dark: you perceive nothing. But the moment a taper is introduced, you immediately fee, not the taper only, but the other bodies which were before invisible. We have here, then, a very essential difference between luminous and opaque bodies. I have already employed the term opaque to denote bodies which are not transparent; but it comes to almost the same thing, and we must accommodate ourselves to the common modes of expression, though they are not perfectly accurate. Luminous bodies are visible by their own light, and never affect our organs of fight more than when the darkness is otherwise most profound. Those which I here denominate opaque, are rendered visible to us only by means of a light that is foreign to them. We perceive them not while they remain in darkness; but as soon as they are exposed to a luminous body, whose rays strike upon them, they become visible; and they disappear the moment that foreign light is withdrawn. It is not even necessary, that the rays of a luminous body fhould fall upon them immediately; another opaque body, when well illuminated, produces nearly the fame effect, but in a feebler manner.

The moon is an excellent inftance. We know that the moon is an opaque body; but when she is illuminated by the sun, and we see her during the night, she diffuses a feeble light over all opaque bodies, and renders visible to us those which we could not have perceived

perceived without her affiftance. Placed in the day time in an apartment, whose aspect is toward the north, and into which, of course, the rays of the fun cannot enter, it is, however, perfectly clear, and I am able to diftinguish every object. What can be the cause of this clearness, but that the whole heaven is illuminated by the fun? What we call the azure fky, and befides, the walls opposite to my apartment, and the other furrounding objects, are likewife illuminated, either immediately by the fun, or mediately by other opaque bodies, exposed to the action of that focus of light; and the light of all these opaque, but illuminated, bodies, as far as it has admission into my apartment, renders it luminous, and that in proportion as the windows are high, wide, and well placed. The glass is little or no interruption, being, as I have already remarked, a transparent body, which freely transmits the rays of light.

When I completely exclude the light from the apartment, by closing the window-shutters, I am reduced to a state of darkness, and discern no object, unless I call for a candle. Here, then, is an essential difference between luminous and opaque bodies; and likewise a very striking resemblance, namely, that opaque bodies, when illuminated, illuminate other opaque bodies, and produce, in this respect, nearly the same essential as bodies luminous of themselves. The explanation of this phenomenon has, hitherto, greatly perplexed philosophers, but, I slatter myself, that my solution of it has been clear and satisfactory.

24th June, 1760. Walling clott au of chilly ambare





fide, with the ledge B C, an angle B C F, exactly equal to the angle of incidence A C E. This angle, B C F, formed by the line in which the ball recoils, is called the angle of reflection. And this law always takes place when a body in motion meets with an obstacle.

A cannon ball, fhot against a wall sufficiently strong to refift it, is reflected conformably to this law. It extends, in like manner, to founds, which are frequently reflected from certain bodies; and you know that this reflection of found is called echo. It cannot be doubted, that the fame thing frequently takes place with respect to the rays of light. The objects which we fee in mirrors, are represented to us by the reflection of rays, and every well polished furface reflects the rays of light which fall upon it. It is undoubtedly certain, therefore, that there are cases without number in which the rays that fall on certain bodies are reflected; and philosophers have thence taken occasion to maintain, that opaque bodies are rendered visible by means of reflected rays.

I fee just now houses, opposite to my windows, which are illuminated by the sun. According, then, to the opinion of those philosophers, the rays of the sun falling on the surface of these houses, are reslected from them; they enter into my apartment, and render these houses visible to me. In the same manner, if we believe those philosophers, the moon and the planets become visible, and these are, unquestionably, opaque bodies. The rays of the sun which

fall on these bodies, and illuminate the parts which are exposed to them, are reflected, and are thence transmitted to us, just as if the bodies were luminous of themselves. According to this opinion, we see the moon and the planets only by the rays of the sun which they reflect; and you must frequently have heard it assimmed, that the light of the moon is a reflection of the light of the sun. In the same manner, say they, the rays of the sun are reflected by the sirst opaque bodies which are exposed to them, on other bodies of the same nature, and undergo a series of similar reflections, till they are entirely weakened.

But, however plaufible this opinion may at first fight appear, it involves so many absurdities, when closely examined, that it is absolutely untenable, which I hope to demonstrate, as a preparation for the true solution of this phenomenon.

28th June, 1760.

## LETTER XXIV.

Examination and Refutation of Newton's System.

AFFIRM, then, that when we see an opaque body illuminated by the sun, it is impossible to maintain that it reslects luminous rays, and that, by means of such rays, it is rendered visible to us. The example of a mirror, which, undoubtedly, reslects the rays, and is employed to support this opinion, rather

rather confutes it. The mirror, beyond contradiction, fends back the rays which fall upon it; but when these resected rays enter into our eyes, What do they represent? You will readily answer, that it is not the mirror, but the objects from which they originally proceeded; and the reslection does nothing else, but enable us to see these objects in another place. Besides, we see those objects, not on the surface of the mirror, but rather within it, and it may be said with truth, that the mirror itself remains invisible to us.

But, on looking at an opaque body illuminated by the fun, we do not fee in it the image of that glorious orb; we fee only the furface of the bodies, with all the variations to be found on them. We perceive, then, a very effential difference between the rays which are reflected from a mirror, and those by means of which opaque bodies are rendered visible. But there is, befides, another difference equally palpable in the mirror; for on changing the place of the objects, or our own fituation, the appearance will always change, and the rays, reflected from the mirror, will continually reprefent to our eyes other images, corresponding to the nature and position of the objects, and to the place where we are stationed: but, as I have already faid, thefe reflected rays never represent to us the mirror itself.

Now, let a body be illuminated by the fun, or other bodies, whether luminous or opaque, already illuminated; in whatever manner this body may change it's place, or we change our's relatively to it, it's appearance is always the fame; we fee always the fame object, and remark in it no change relative to the different circumstances above mentioned. This furnishes a new proof, that we do not fee opaque bodies by means of the rays reflected from their furface.\*

\*This can hardly be deemed a fair statement. It is true, that opaque bodies are seen only by reflected light, but it by no means follows, that all the incident light is again reflected. Some bodies are, by their constitution, disposed to reflect certain kinds of rays the most freely, and as the rest are absorbed, the peculiar colour predominates. This colour will, therefore, not be the same, whatever be the quality of the incident light, but will receive an analogous shade. For the same reason, no substance restects only one species of rays. The elective attractions and repulsions, between the particles of light and a body, are most remarkable at very minute distances; and hence the colour is prominent when the surface is rough, for the light, suffering then a partial repulsion only, gains a nearer approach. I cannot imagine how Mreuler would explain these facts on his own principles.

It is in a polished furface only, that the furrounding bodies can be feen by reflection, for diffinct vision requires the rays, proceeding from different points, to be transmitted with regularity. No fubstance is, indeed, perfectly smooth, but the different repulfions, exerted by the fuperficial particles, may balance each other, and produce an uniform effect, at the diffance where the reflection takes place. Mr. Euler's principles would lead to the conclusion, that polish is not at all necessary to a mirror. Echo is formed from furfaces which are very uneven, fince the air is heaped on the obstacle, and the principal reflux of the undulation commences at a fensible diffance from it. The same obtains in water, though in a less degree; and is, in general, more remarkable, in proportion to the rarefaction of the fluid. How wonderful, then, in that respect, must ether be, which is supposed to be the most subtle of all fluids? We might expect the walls of a house to reflect the most enchanting picture of the landscape in front .- E. E.

An objection will, perhaps, be started, drawn from the dove's neck, and certain kinds of stuff, which present different objects, according as our point of view changes. But this in no respect weakens my conclusion with regard to ordinary opaque bodies, which are not subject to this change. The objection only proves, that these singular objects are endowed with certain qualities: as, for example, that their minuter particles are sinely polished, and that a real reslection takes place, beside the usual and ordinary manner in which bodies are rendered visible to us.

Now, it is easy to comprehend, that this reflection must be clearly distinguished from the manner in which ordinary opaque bodies are illuminated.

Finally, the rays reflected from a mirror always represent to us, likewise, the colours of the bodies from which they originally proceed, and the mirror, which reflects, makes no change in this respect. One opaque body illuminated by any other body, in whatever manner, always presents the same colours; and every body may be said to have it's proper colour. This circumstance absolutely overturns the opinion of all those who maintain, that we see opaque bodies by means of the rays which their surface reflects.

Putting together all the reasons which I have now submitted to your consideration, there can be no hessitation in pronouncing, that this opinion is totally untenable in philosophy, or rather, in physics. I cannot, however, flatter myself with the hope, that philosophers, wedded to opinions once adopted,

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should yield to these reasons. But the naturalist, who is more nearly related to the mathematician, will have less difficulty in resigning an opinion, overthrown by reasons so convincing. You will again recollect what Cicero has said on this subject: That nothing so absurd can be conceived, as not to be supported by some philosopher. In sact, however strange the system which I have been resuting may appear to you, it has, hitherto, been propagated and defended with much warmth.

It is impossible to fay, to what a degree the difficulties and contradictions which I have been endeavouring to expose, were unknown to, or overlooked by, the partisans of this system. The great Newton himself strongly selt their force: but as he rested in a very untenable idea respecting the propagation of light, it is not to be wondered at, that he should overlook these great difficulties; and, in general, depth of understanding does not always prevent a man from falling into absurdity, in supporting an opinion once embraced.

But if this fystem, that opaque bodies are rendered visible by reflected rays, be false, say it's partisans, What then is the true one? They even think it impossible to imagine another explanation of this phenomenon. It is, besides, rather hard and humiliating for a philosopher to acknowledge ignorance of any subject whatever. He would rather maintain the grossest absurdities; especially if he possesses the secret of involving them in mysterious terms, which no one is capable of comprehending. For in this

case, the vulgar are the more disposed to admire the learned; taking it for granted, that what is obscurity to others, is perfectly clear to them. We ought always to exercise a little mistrust, when very sublime knowledge is pretended to, knowledge too sublime to be rendered intelligible. I hope I shall be able to explain the phenomenon in question, in such a way as to remove every difficulty.

1/t July, 1760.

#### LETTER XXV.

A different Explanation of the Manner in which opaque Bodies illuminated become visible.

A LL the phenomena of opaque bodies, which I have unfolded in the preceding letter, incontestably demonstrate, that, when we see an opaque body illuminated, it is not by rays reslected from it's surface, that it becomes visible, but because it's minuter particles are in an agitation similar to that of the minuter particles of luminous bodies; with this difference, however, that the agitation in opaque bodies is far from being so strong as in bodies luminous of themselves; for an opaque body, however much illuminated, never makes on the eye an impression so lively as luminous bodies do.

As we see the opaque bodies themselves, but by no means the images of the luminous bodies which H 2 enlighten

enlighten them, as must be the case, if we saw them by the reflection of their furface; it must follow, that the rays emitted by opaque bodies are proper to them, just as the rays of a luminous body are peculiar to itself. As long as an opaque body is illuminated, the minuter particles of it's furface are in a state of agitation proper to produce, in the ether, a motion of vibration, fuch as is necessary for forming rays, and for painting in our eyes the image of the body from which they proceed. For this effect, rays must be diffused, from every point of the surface, in all directions; as experience evidently confirms. For, from whatever fide we look at an opaque body, we fee it equally in all it's points; from which it follows, that every point emits rays in all direc-This circumftance effentially diftinguishes these rays from such as are reflected, whose direction is always determined by that of the rays of incidence; fo that if the incident rays proceed from one fingle quarter, fay the fun, the reflected rays can follow only one fingle direction.

It must be admitted, then, that when an opaque body is illuminated, all the particles on it's surface are put in a certain agitation, which produces rays, as is the case with bodies luminous of themselves. This agitation, likewise, is stronger, in proportion as the light of the illuminating body is more intense. Thus the same body, exposed to the sun, is agitated much more violently, than if, in a room, it were illuminated only by day-light, or in the night-time, by a taper, or by the moon. In the first case, it's image

image is painted with much greater vivacity on the bottom of the eye, than in the others, especially the last; the light of the moon being scarcely sufficient to enable us to distinguish, or to read, writing of a large size. And when the opaque body is conveyed into a close room, or into the dark, nothing is then to be seen; a certain proof, that the agitation in it's parts has entirely ceased, and that they are now in a state of rest.

In this, therefore, confifts the nature of opaque bodies; their particles are, of themselves, at rest, or, at least, destitute of the agitation necessary to produce light. But these same particles are so disposed, that when illuminated, or struck with rays of light, they are immediately put into a certain agitation, or motion of vibration, proper to produce rays; and the more intense the light is, which illuminates these bodies, the more violent also is this agitation. As long as an opaque body is illuminated, it is in the fame state as luminous bodies; it's particles are agitated in the fame manner, and are capable of exciting, of themselves, rays in the ether; with this difference, that the agitation kept up in luminous bodies by an intrinsic force, subsists always of itself; whereas, in opaque bodies, this agitation is only momentaneous, and produced by the motion of the light which illuminates them.

This explanation is confiftent with every phenomenon, and labours under none of the difficulties which determined us to abandon the other, namely, that founded on reflection. Whoever will take the

trouble condidly to weigh all these reasons, must admit their force. But a very great difficulty still remains to be solved: How comes it that illumination, simply, can put the particles of an opaque body into an agitation capable of producing rays; and that this agitation should always continue nearly the same, whatever difference there may be in the illumination?

I acknowledge, that were it impossible to answer this question, it would be a great defect in my theory, though it would not amount to a complete resutation, for it contains nothing contradictory. Supposing I were ignorant, how illumination produces an agitation in the particles of opaque bodies, this would only prove that the theory is incomplete: and till it is demonstrated to be absolutely impossible that illumination should produce this effect, my system must subsist. But I shall endeavour to supply this defect, by shewing you, how illumination agitates the minutest particles of bodies.

5th July, 1760.

#### LETTER XXVI.

Continuation of the Same Subject.

I HAVE undertaken to shew how the illumination of an opaque body must produce in it's minutest particles, an agitation proper to excite the rays of light, which render that same opaque body visible.

The parallel between found and light, which differ only in respect of less and more, light being the same thing relatively to ether that found is relatively to air, this parallel, I fay, will enable me to fulfil my engagement. Luminous bodies must be compared to mufical inftruments actually in a ftate of vibration. It is a matter of indifference whether this be the effect of an intrinsic or of a foreign power: it is fufficient for my purpose that found is emitted. Opaque bodies, as long as they are not illuminated, must be compared to mufical inftruments not in use, or, if you will, to ftrings which emit no found till they are touched.

The question, then, being transferred from light to found, is refolved into this, Whether it be possible for the ftring of an inftrument, in a ftate of rest, when brought within the sphere of activity of the found of instruments in a state of vibration, to receive, in certain circumstances, some agitation, and emit found, without being touched? Now this is confirmed by daily experience. If you take the trouble, during a concert, to attend to a particular string in proper tune, you will observe that string fometimes to tremble without having been touched, and it will emit the fame found as if it had been immediately put into vibration. This experiment will fucceed still better, if the instruments strike the same note with the ftring. Confider attentively the ftrings of a harpfichord not played upon, while a violin strikes the note a, for example, and you will observe on the harpfichord the string of the same note begin fenfibly

H 4

fensibly to tremble, and even to emit sound, without having been touched; some other chords will likewise be agitated, particularly those which are distant an octave, a fifth, and even a third, provided the instrument be perfectly in tune.

This phenomenon is well known to musicians, and Mr. Rameau, one of the most celebrated French composers, established his principles of harmony upon it. He maintains, That octaves, sisths, and thirds, must be considered as consonances, because one chord is agitated by the found only of another chord, which is in unison, or an octave, a sisth, or a third, from the sirst. But it must be admitted that the principles of harmony are so well established by the simplicity of the relations which sounds have to each other, that they have no need of a new consirmation. In truth the phenomenon observed by Mr. Rameau is a very natural consequence from the principles of harmony.

To render this more fensible, let us attend to two chords wound up to unison; on striking the one, the other will begin of itself to tremble, and will emit it's found. The reason is abundantly clear; for as a chord communicates to the air by it's trembling a motion of vibration similar to it's own, the air, agitated by this motion of vibration, must reciprocally make the chord tremble, provided that by it's degree of tension, it be susceptible of this motion. The air being put into vibration, strikes the chord ever so little at every reverberation, and the repetition of strokes soon impresses on the chord a sensible mo-

tion; because the vibrations to which it is disposed by it's tension accord with those of the air. If the number of vibrations in the air is the half, or the third, or any other whose relation is sufficiently simple, the chord does not receive a new impulse at every vibration, as in the preceding case, but only at the second, or the third, or the fourth, which will continue to increase it's tremulous motion, but less than in the first case.

But if the vibrations of the air have not any fimple relation with that which corresponds to the chord, the agitation of that fluid will produce no effect whatever upon it; the vibrations of the chord, if there be any, not corresponding to those of the fluid, the following impulsions of the air destroy for the most part the effect which the first might have produced; and this is completely confirmed by experience. Thus when a chord is shaken by a found, that found must, in order to it's being perceptible, be precifely the fame with that of the chord. Other founds which have a confonance with that of the chord, will produce, it is true, a fimilar but less fenfible effect, and dissonances will produce none at all. This phenomenon takes place not only in mufical ftrings, but in all fonorous bodies whatever. One bell will refound by the noise only of another bell which is in unifon with it, or at the distance of an octave, a fifth, or a third.

The instance of a person who could break glasses by his voice farther confirms what I have advanced. When a glass was presented to him, by striking it he found found out the note; he then began to fquall in unifon, and the glass immediately caught the vibration; proceeding to give to his voice all the force he was able, always preserving the unison, the vibration of the glass became at length so violent, that it broke. It is consirmed, then, by experience that a chord and every other sonorous body is put into vibration by it's kindred sound. The same phenomenon must take place with regard to opaque bodies, of which the minuter particles may be put into a state of agitation by illumination only: which is the question I proposed to solve. The following letter will contain a more ample discussion of it.

8th July, 1760.

### LETTER XXVII.

Conclusion: Clearness and Colour of opaque Bodies illumined.

A FTER what has just been submitted to your consideration, you will no longer be surprised that an opaque body is capable of receiving, from illumination alone, an agitation in it's particles similar to that of the particles of luminous bodies, and which gives them the property of producing rays that render them visible. Thus the great objection to my explanation of the visibility of opaque bodies is happily removed; while the other theory, founded on the reslection of rays, has to encounter difficulties

culties which grow in proportion as you attempt to make a more direct application of them to known phenomena.

It is then an established truth, that the particles of the furfaces of all bodies which we fee, undergo an agitation fimilar to that of a chord in vibration, but their vibrations are much more rapid; whether it be that this agitation is the effect of an intrinsic force, as in bodies luminous of themselves, or whether it be produced by the rays of light which fall upon the bodies, that is to fay by illumination, as is the cafe in opaque bodies. It is false, then, that the moon being an opaque body, reflects the rays of the fun, and that, by means of this reflected light, she is rendered visible to us, as is commonly understood. But the rays of the fun, falling on the furface of the moon, excite in it's particles a concussion, from which refult the rays of the moon; and thefe, entering into our eyes, paint it's image there; it is the fame with the other planets, and with all opaque bodies. This agitation of opaque bodies, when illumined, lasts only during the illumination which is the cause of it: and as soon as an opaque body ceases to be illumined, it ceases to be visible.

But is it not possible that this agitation, once impressed on the particles of an opaque body, may be for some time kept up, as we see that a string once ftruck, frequently continues to vibrate, though no new impression be made upon it? I do not pretend to deny the fact: I even believe that we have examples of it in those substances which Mr. Margraff

prefented

presented to you, and which, once illumined, preferve their light for some time, though conveyed into a dark room. This, however, is an extraordinary case; the vibration of the minuter particles disappearing in all other bodies, with the illumination which occasioned it. But this explanation, which thus far is perfectly self-consistent, leads me forward to researches of still greater importance.

It is undoubtedly certain, that we find an infinite difference between the particles of opaque bodies, according to the variety of the bodies themselves. Some will be more fusceptible of vibrations, and others lefs, and others finally not at all fo. This difference in bodies occurs but too evidently. One, whose particles easily receive the impression of the rays which strike it, appears to us brilliant; another, on the contrary, in which the rays fcarcely produce any agitation, cannot appear luminous. Among feveral bodies, equally illumined, you will always remark a great difference, fome being more brilliant than others. But there is besides another and a very remarkable difference between the particles of opaque bodies, respecting the number of vibrations which each of them, being agitated, will make in a certain time.

I have already observed, that this number must always be very great, and that the subtilty of ether is such as to require many thousands in a second. But the difference here may be endless; if some particles, for example, should make 10,000 vibrations in a second, and others 11,000, 12,000, 13,000, according

to the smallness, the tension, and the elasticity of each, as in the case of musical chords, in which the number of vibrations given in a fecond may be varied without end; and thence it is I have deduced the difference of high and low notes. As this difference is effential in founds, and as the ear is affected by it in a manner fo particular as to render it the foundation of the whole theory of mufic, it cannot be called in question that a similar difference in the frequency of the vibrations of rays of light must produce a variation as particular in vision. If, for example, a particle makes 10,000 vibrations in a fecond, and produces rays of the fame species, the rays which enter into the eye will strike the nerves of that organ 10,000 times in a fecond; and this effect, as well as the fenfation, must be totally different from those produced by a different particle which should make more or less vibrations in a second. There will be in vision a difference similar to that which the ear perceives on hearing fliarp or flat notes.

You will no doubt be defirous to know into what this difference in vision is to be refolved; and what different fensations correspond to the number, greater or less, of the vibrations produced in every body during a second? I have the honour of informing you, That diversity of colours is occasioned by this difference; and that difference of colour is to the organ of vision what sharp or slat sounds are to the ear. We have resolved, therefore, without going after it, the important enquiry respecting the nature of colours, which has long employed the attention of the greatest

greatest philosophers. Some of them have called it a modification of light absolutely unknown to us. Descartes maintains, that colours are only a certain mixture of light and shade. Newton accounts for difference of colour by tracing it up to the rays of the sun; which, according to him, are a real emanation, whose matter may be more or less subtile; and thence settles the rays of all the colours, as red, yellow, green, blue, violet, &c.

But as this fystem falls to pieces of itself, all that has been said respecting colours conveys no information; and you are now clearly sensible, that the nature of each colour consists in the number of vibrations produced in a certain time by the particles which present them to the eye.

12th July, 1760.

## LETTER XXXVIII.

# Nature of Colours in particular.

THE ignorance which prevailed respecting the true nature of colours, has occasioned frequent and violent disputes among philosophers; each of whom made an attempt to shine, by maintaining a peculiar opinion on the subject. The system which made colours to reside in the bodies themselves, appeared to them too vulgar and too little worthy of a philosopher, who ought always to soar above the multitude. Because the clown imagines that one body

body is red, another blue, and another green, the philosopher could not distinguish himself better than by maintaining the contrary; and he accordingly affirms that there is nothing real in colours, and that there is nothing in bodies relative to them.

The Newtonians make colours to confift in rays only; which they diftinguish into red, yellow, green, blue, and violet; and they tell us that a body appears of fuch and fuch a colour when it reflects rays of that species. Others, to whom this opinion seemed abfurd, pretend that colours exist only in ourselves. This is an admirable way to conceal ignorance; the vulgar might otherwife believe that the fcholar was not better acquainted with the nature of colours than themselves. But you will readily perceive that these affected refinements are mere cavil. Every fimple colour (in order to diffinguish from compound colours) depends on a certain number of vibrations, which are performed in a certain time; fo that this number of vibrations, made in a fecond, determines the red colour, another the yellow, another the green, another the blue, and another the violet, which are the fimple colours reprefented to us in the rainbow.

If, then, the particles of the furface of certain bodies are disposed in such a manner, that being agitated, they make in a second as many vibrations as are necessary to produce, for example, the red colour, I call such a body red, just as the clown does; and I see nothing like a reason for deviating from the common mode of expression. And rays which make make fuch a number of vibrations in a fecond, may, with equal propriety be denominated red rays; and finally, when the optic nerve is affected by these same rays, and receives from them a number of impulsions, sensibly equal, in a second, we receive the sensation of the red colour. Here every thing is clear; and I see no necessity for introducing dark and mysterious phrases, which really mean nothing.

The parallel between found and light is so perfect, that it hits even in the minutest circumstances. When I produced the phenomenon of a musical chord, which may be excited into vibration by the resonance only of certain sounds, you will please to recollect, that the one which gives the unison of the chord in question is the most proper to shake it, and that other sounds affect it only in proportion as they are in consonance with it. It is exactly the same as to light and colours; for the different colours correspond to the different musical sounds.

In order to display this phenomenon, which completely confirms my affertion, let a dark room be provided; make a small aperture in one of the shutters; before which, at some distance, place a body of a certain colour, say a piece of red cloth, so that, when it is illumined, it's rays may enter by the aperture into the darkened room. The rays thus transmitted into the room will be red, all other light being excluded: and if you hold on the inside of the room, opposite to the aperture, a piece of cloth of the same colour, it will be perfectly illumined, and its red colour appear very brilliant; but if you sub-

ftitute in it's place a piece of green cloth, it will remain obscure, and you will hardly see any thing of it's colour. If you place on the outside, before the aperture, a piece of green cloth, that within the chamber will be perfectly illumined by the rays of the first, and it's green colour appear very lively. The same holds good as to all other colours; and I do not imagine that a more convincing demonstration of the truth of my system can be demanded.

We learn from it, that, in order to illuminate a body of a certain colour, it is necessary that the rays which fall upon it should have the same colour; those of a different colour not being capable of agitating the particles of that body. This is farther confirmed by a well known experiment. When the spirit of wine is fet on fire in a room, you know that the flame of fpirit of wine is blue, that it produces only blue rays, and that every perfon in the room appears very pale, their faces, though painted ever fo deep, have the afpect of death. The reason is evident; the blue rays, not being capable of exciting, or putting in motion the red colour of the face, you fee on it only a feeble and bluish colour: but if one of the company is dreffed in blue, fuch drefs will appear uncommonly brilliant. Now the rays of the fun, those of a wax taper, or of a common candle, illuminate all bodies almost equally; from whence it is concluded, that the rays of the fun contain all colours at once, though he himfelf appears yellowish.

In truth, when you admit into a dark room the rays of all the fimple colours, red, yellow, green, Vol. I. blue,

blue, and violet, in nearly equal quantities, and blend them, they reprefent a whitish colour. The same experiment is made with various powders, coloured in like manner; on being mixed together, a whitish colour is the refult. Hence it is concluded that white is nothing lefs than a fimple colour; but that it is rather a compound of all the fimple colours; accordingly we fee that white is adapted to the reception of all colours. As to black, it is not properly a colour. Every body is black when it's particles are fuch that they can receive no motion of vibration, or when it cannot produce rays. The want of rays, therefore, produces the fensation of that colour; and the more particles there are found in any body not fusceptible of any motion of vibration on it's furface, the more blackish and obscure it appears.

15th July, 1760.

## LETTER XXXIX.

Transparency of Bodies relative to the Transmission of Rays.

I HAVE already remarked, that there are bodies, fuch as glass, water, and especially air, which transmit the rays of light, and, on account of this property, are denominated pellucid or diaphonous. The ether, however, is the medium in which the rays of light are formed, to which this property most intimately appertains; and other transparent bodies

are endowed with it only by means of the ether which they contain, and with which they are fo blended, that the agitations excited by the light may be communicated farther without being interrupted in their progrefs. But this transmission is never performed to freely as in the pure ether, though it always lofes fomething; and this in proportion as the transparent body is more or less gross. The groffness may even become so considerable, that the light fhall be wholly loft in it; and then the body is no longer transparent. Thus, though glass be a transparent body, a great lump of glass several feet thick is not fo. In like manner, however pure the water of a river may be, you cannot fee the bottom where it is very deep, though you can very eafily where it is fhallow.\*

Transparency, then, is a property of bodies rela-

\* The common diffinction of bodies into opaque and transparent is inaccurate, for every body has a certain degree of transparency. All fubstances absorb light in it's passage, but in some this absorption is prodigious, and the quantity of light which penetrates through a certain thickness is so exceedingly minute as to clude our powers of perception. When the thickness is much diminished, the light becomes fensible, even in the case of bodies that are usually termed opaque; thus we can see through a plate of ivory and a leaf of gold. The different properties of substances with respect to the transmission of light, seems to depend on the greater or less regularity of the disposition of their elementary particles, and on their proximity or distance from each other; as these circumstances augment or diminish the chance of a ray's passing within the limit of absorption. Whatever be the intensity of the incident light, the same proportion of it is, in a given body, transmitted through the same thickness .- E. E.

tive only to their thickness; and when this property is ascribed to glass, to water, &c. it must always be understood with this restriction, that these bodies are not too gross; and that to every species there is a certain measure of thickness beyond which the body ceases to be transparent. There is not one opaque body, on the contrary, which may not itself become transparent, if reduced to a plate extremely sine. Thus, though gold is not transparent, gold leaf is so; and on examining the minuter particles of all bodies with a microscrope, they are found to be transparent. It may then be with truth assimmed, that all bodies are transparent when reduced to a certain degree of sineness; and that no one is so when too gross.

In common language we denominate transparent the bodies which preserve this quality to a certain degree of thickness, though they lose it when they go beyond that bound. But with respect to ether, it is of it's own nature perfectly transparent, and it's extent diminishes not this quality in the smallest degree. The prodigious distance of the fixed stars prevents not their rays from being transmitted to us. But though our air appears to be of a perfect transparency, if it extended as far as the moon, that transparency would be entirely lost, and would prevent every ray of the sun, and of the other heavenly bodies, from penetrating to us. We should then be involved in Egyptian darkness.

The reason of it is evident, and we remark the same thing in sound, whose resemblance to light is confirmed

confirmed in every respect. Air is the most proper medium for the propagation of found; but the agitations excited in the air are capable of shaking also the particles of all bodies; and thefe again putting in motion the interior particles, finally transmit the vibration through the fubftance of all bodies, unless they be too thick. There are bodies, then, which, relatively to found, are the fame thing which transparent bodies are relatively to light; and all bodies have this property with relation to found, provided they are not too thick. When you are in your apartment, you can hear almost every thing that paffes in the ante-chamber, though the doors are closely shut, because the agitation of the air in the ante-chamber communicates itself to the partitions, and penetrates through them into the inner apartment with fome lofs, however. Were the partition removed, you would undoubtedly hear more diftinctly. Now the thicker the walls are, the more of it's force does the found lofe in piercing through them: and the walls may be made fo thick that nothing could be heard from without, unless it were fome terrible noise, such as a discharge of cannon.

This leads me forward to a new remark; that very powerful founds may be heard through walls which are impenetrable to founds more feeble; and, confequently, in order to form a judgment whether a wall is capable of transmitting founds, it is necessary to take into the account not only the thickness of the wall, but likewise the strength of the found. If the found is very feeble, a very thin wall is suffi-

cient to ftop it, though a louder could find an eafy transmission. The same thing holds as to bodies which are permeable only to a very strong light. Objects not very brilliant are invisible through a glass blackened with smoke, but the rays of the sun force themselves through it, and it transmits perfectly well the image of that luminary. Astronomers employ this method to observe him; for without such precaution he would dazzle the eye. And when you happen to be in a dark room, with an aperture in the shutter exposed to the sun, in vain will you attempt to exclude the light by opposing your hand to the aperture; the rays of the sun will force themselves through.

It is perceivable at the same time that the light of the sun loses much of it's lustre in passing through a body which, relatively to other objects, is not itself transparent. But a very strong light may lose much of it's lustre, before it is entirely extinguished, while a feebler light is lost at once. A piece of very thick glass, then, will not be transparent, with respect to objects less brilliant, though the sun may be visible through it.

These remarks on transparent bodies lead me to the theory of refraction, of which you have frequently heard, and which I shall endeavour to place in it's proper light.

18th July, 1760.

#### LETTER XXX.

Of the Transmission of Rays of Light, though transparent Mediums, and their Refraction.

A S long as light moves in the fame medium, whether it be ether, air, or any other transparent body, the propagation proceeds in ftraight lines, denominated rays, as they proceed from the luminous point, in all directions, as the radii of a circle, or a globe, iffue from the centre. In the fystem of emanation, the particles darted from luminous bodies move in ftraight lines; the fame thing holds, in that which I have had the honour of proposing, in which the agitations are communicated in straight lines, as the found of a bell is transmitted in a straight line, by which also we judge from what quarter the found comes; the rays in both fystems, then, are represented by ftraight lines, as long as they pass through the fame transparent medium; but they may undergo fome inflection, in passing from one to another; and this inflection is called the refraction of the rays of light, the knowledge of which is necessary to account for many phenomena. I proceed, therefore, to lay down the principles, in conformity to which, refraction takes place.\*

\* The quantity of refraction is not proportional to the denfity of the medium. Sir Isaac Newton remarks, that inflammable sub-stances, though specifically lighter than water, produce a much greater refraction: and it was this analogy which suggested to him, that diamonds belong to the same class; a conjecture which has been verified within these sew years.—E. E.

It is an invariable law, that, when a ray, fuch as E C (plate I. fig 8.) falls perpendicularly on the furface A B of another medium, it continues it's progress in the same straight line extended, as CF; it will, in this case, undergo no inflection or refraction. If, then, E C is a ray of the fun, falling perpendicularly on the furface A B of water, or of glass, it will enter it in the fame direction, and continues it's progress in the line C F, which is, likewise, perpendicular to the furface A B, fo that E F shall be in one and the fame straight line. This is the only case in which there is no refraction. But as often as the ray falls not perpendicularly on the furface of another tranfparent body, it does not purfue it's progress in the fame straight line; it recedes less or more from it, and undergoes a refraction.

Let P C (plate I. fig. 9.) be a ray, falling obliquely on the furface A B, of another transparent medium. On entering into this medium, it will not continue it's progress in the direction of the straight line C Q, which is the line P C produced; but will recede from it, in the direction of the line C R, or C S. It will undergo, then, at the point C, an inflection, which we call refraction, which depends partly on the difference of the two mediums, and partly on the obliquity of the direction of the ray P C.

In order to comprehend the laws of this inflection, it is necessary to explain certain terms employed in treating this subject.

Ift. The furface A B, which separates the two mediums, that from which the ray comes, and that into

which it enters, is called the refringent furface. 2dly. The ray P C, which falls upon it, is called the incident ray; and, 3dly, the ray C R, or C S, which purfues, in the other medium, a course different from C Q, is called, the broken, or refracted ray. And, having drawn through the surface A B, the perpendicular line E C F, we call, 4thly, the angle P C E, formed by the incident ray P C, with the perpendicular E C, the angle of incidence; and, 5thly, the angle R C F, or S C F, formed by the refracted ray C R or C S, with the perpendicular C F, is called the angle of refraction.

Therefore, because of the inflection, which the ray of light undergoes, the angle of refraction is not equal to the angle of incidence P C E; for producing the line P C to Q, the angles P C E and F C Q being vertical, are equal to each other;\* as you will eafily recollect. The angle Q C F, then, is equal to the angle of incidence P C E; therefore, the angle of refraction R C F or S C F, is greater or lefs. There are, then, only two cases which can exist; the one, in which the refracted ray being C R, the angle of refraction R C F, is less than the angle of incidence PCE; and the other, in which the refracted ray being C S, the angle of refraction is greater than the angle of incidence P C E. In the former case, we fay, that the ray C R approaches the perpendicular CF; and in the other, that the refracted ray CS, recedes or deviates from the perpendicular.

It is necessary, then, to enquire, In what cases the

<sup>\*</sup> Euclid's Elements, Book I. Prop. 15.



Finally, it must likewise be remarked, that the disference between the angle of incidence and the angle of refraction is so much greater, as the angle of incidence is greater, or, as the incident ray recedes farther from the perpendicular, the greater will be the inflection or refraction of the ray. A relation of all these angles exists, and is determinable by geometry; but it is not now necessary to enter into the detail. What has been already said, is sufficient for understanding what I have farther to propose on the subject.

22d July, 1760.

## LETTER XXXI.

# Refraction of Rays of different Colours.

YOU have feen, that when a ray of light paffes obliquely from one transparent medium to another, it undergoes an inflection, which is called refraction, and that the refraction depends on the obliquity of the incidence, and the density of the mediums. I must now call upon you to remark, That diversity of colours occasions, likewise, a small variety in the refraction. This arises, undoubtedly, from hence, that the rays which excite in us the fensations of different colours, perform unequal numbers of vibrations in the same times, and that they differ among themselves, in the same manner as sharper or flatter sounds do. Thus, it is observable,

that rays of red undergo the least inflection or refraction; after them come the orange; the yellow, the green, the blue and the violet, follow in order; so that violet-coloured rays undergo the greatest refraction; it being always understood, that the obliquity of the incidence, and the density of the mediums are the same. Hence, it is concluded, that rays of different colours have not the same refrangibility; that the red are the least refrangible, and the violet-coloured the most so.

If then, P C (plate I. fig. 10.) is a ray passing, for example, from air into glass; the angle of incidence being P C E, the refracted ray will approach the perpendicular C F; and if the ray be red, the refracted ray will be in the direction C—red; if it be orange, the refracted ray will be C—orange, and so of the rest, as may be seen in the sigure. All these rays deviate from the line C Q, which is P C produced, toward the perpendicular C F; but the red ray deviates the least from C Q, or undergoes the least in-slection, and the violet recedes the farthest from C Q, and undergoes the greatest inslection.

Now, if PC is a ray of the fun, it produces, at once, all the coloured rays indicated in the figure; and if a piece of white paper is placed to receive them, you will, in effect, fee all these colours; hence, it is affirmed, that every ray of the fun contains, at once, all the simple colours. The same thing happens, if PC is a ray of white, or if it proceeds from a white body. We see all the colours produced from it by refraction, whence it is concluded,

that white is an affemblage of all the simple colours, as we shewed formerly. In truth, we have only to collect all these coloured rays into a single point, and the colour of white will be the result.

It is thus we discover what are the simple colours. Refraction determines them incontestibly. In following the order which it presents, they are these:

1. red, 2. orange, 3. yellow, 4. green, 5. blue, 6. violet. But it must not be imagined, that there are but six: for as difference of colours arises from the number of vibrations which rays perform in one and the same time, or rather the undulations which produce them: it is clear, that the intermediate numbers equally give simple colours.\* But we want names, by which to design these colours; for be-

\* This remark, that the number of primitive colours much exceeds fix, is very just. The colours of the rainbow, or of the spectrum, formed by a prism, pass into each other by insensible shades, so that it is impossible to define their boundaries. There is reason to suspect, that, even the great Newton was, in this instance, misled, by a predilection for the number seven, which during many ages, has been regarded with a fort of mystical veneration. The correspondence, which he observed, between the divisions of the spectrum, and those of the monochord, and which fo many authors have fince repeated, is wholly ideal; for the proportions, between the extent of the different colours are, in a great measure, determined by the peculiar quality of the refracting mediums. Thus a prism of glass, in which alkali predominates, forms a spectrum, extremely unlike that formed by one of glass, composed principally of lead. Were a person to reckon only the most conspicuous of the primitive colours, he would, most probably, felect the number fix, for the indigo can hardly be diftinguished .- E. E.

tween yellow and green, we evidently perceive intermediate colours, for which we have no feparate names.

In conformity to the fame laws, are produced the colours visible in the rainbow. The rays of the fun, in passing through the drops of water which float through the air, are, by them, reflected and refracted, and the refraction decompounds them into the simple colours. You must, undoubtedly, have remarked, that these colours follow each other, in the same order, in the rainbow, the red, orange, yellow, green, blue, and violet; but we discover in it, also, all the intermediate colours, as fhades of one colour to another, and had we more names to diftinguish these degrees, we might find more of them from the one extremity to the other. A more copious language may, perhaps, enable another nation actually to reckon up a greater number of different colours; and another, it may be, cannot reckon up fo many; if, for example, it wants a term to express what we call orange. Some to these add purple, which we perceive at the extremity of the red, but which others comprehend under the fame name with red.

C.	D.	E.	F.	G.	A.,	В.
Purple.	Red.	Orange	Yellow	Green.	Blue.	Violet.

These colours may be compared to the notes of an octave, as I have done here, because the relations

of colours, as well as those of sounds, may be expressed by numbers. There is even an appearance, that by straining the violet a little more, you may come round to a new purple, just as in rising from sound to sound, on going beyond B, you come round to so, which is the octave above C. And, as in music, we give to these two notes the same name, because of their resemblance, the same thing takes place in colours, which, after having risen through the intervals of an octave, resume the same names: or, if you will, two colours, like two sounds, in which the number of vibrations in the one, is precisely the double of the other, pass for the same, and bear the same name.

On this principle it was, that father Caftel, in France, contrived a species of music of colours. He constructed a harpsichord, of which every key displayed a substance of a certain colour, and he pretended, that this harpsichord, if skilfully touched, would present a most agreeable spectacle to the eye. He gave it the name of the ocular harpsichord, and you must, undoubtedly, have heard it talked of. For my part, painting rather seems to be that to the eye, which music is to the ear; and I greatly doubt, whether the representation of several shreds of cloth; of different colours, could be very agreeable.

27th July, 1760.

### LETTER XXXII.

Of the Azure-colour of the Heavens.

YOU have just seen, that the cause of the visibility of objects, is a motion of vibration extremely rapid, by which the minuter particles of their surfaces are agitated, and that the frequency of these vibrations determines the colour.

It is the fame thing, whether these particles be agitated by an intrinsic force, as in luminous bodies. or whether they receive their agitation from illumination, or from foreign rays, by which they are illumined, as in opaque bodies. The frequency or rapidity of the vibrations depends on the groffness of these particles, and on their elasticity, as that of the vibrations of a mufical ftring depends on it's thicknefs, and degree of tenfion; thus, as long as the particles of a body preserve the same elasticity, they reprefent the fame colour; as the leaves of a plant preferve a green colour, as long as they are fresh; but when they begin to dry, the difference of elafticity, which then takes place, produces, likewife, a different colour. This fubject I have already difcuffed. I now proceed to explain, Why the heavens appear to us of a blue colour in the day-time.

On observing this phenomenon with a vulgar eye, it would appear, that we are surrounded by a prodigious vault of azure, as painters represent the sky on a ceiling. I have no occasion to undeceive you respecting

respecting this prejudice: a small degree of reflection is sufficient to make you comprehend, that the heavens are not an azure vault to which the stars are assixed, like so many luminous studs. You are perfectly convinced, that the stars are immense bodies, at inconceiveable distances from us, and which move freely through a space almost void, or which is silled only by that subtile matter called ether. And I will shew you, that this phenomenon is to be ascribed to our atmosphere, which is not perfectly transparent.

Were it possible to rise higher and higher above the surface of the earth, the air would become gradually more and more rare, till it ceased to assist respiration; and would, at length, entirely cease; we should then have reached the region of pure ether. Accordingly, in proportion as we ascend on mountains, the mercury in the barometer continues to fall, because the atmosphere becomes lighter and lighter: and then, likewise, it is remarked, that the azure colour of the heavens becomes fainter; and were it possible to mount into pure ether, it would entirely disappear; on looking upward, we should see nothing at all, and the heavens would appear black as night; for where no ray of light can reach us, every thing wears the appearance of black.

There is good reason, then, for asking, Why the heavens appear to be blue? This phenomenon could not exist, were air a perfectly transparent medium, as ether is: in that case, we should receive from above no other rays but those of the stars: but the lustre of day-light is so great, that the feeble light

of the stars is absorbed by it. You could not perceive the slame of a taper in the day-time, at any considerable distance; but that same slame, in the night, would appear very brilliant at much greater distances. This clearly proves, that we must look for the cause of the azure-colour of the heavens, in the want of transparency in the air. The air is loaded with a great quantity of small particles, which are not perfectly transparent, but which, being illuminated by the rays of the sun, receive from them a motion of vibration, which produces new rays proper to these particles; or else they are opaque, and become visible to us from being illumined.

Now, the colour of these particles is blue; and this explains the phenomenon: the air contains a great quantity of small blue particles: or it may be said, that it's minuter particles are bluish, but of a colour extremely delicate, and which becomes sensible to us only in an enormous mass of air. Thus, in a room, we perceive nothing of this blue; but when the bluish rays of the whole atmosphere penetrate our eyes at once, however delicate the colour of each singly, their totality may produce a very deep colour.

This is confirmed by another phenomenon, with which you must be well acquainted. If you look at a forest, from a moderate distance, it appears quite green; but in proportion as your distance increases, it acquires a bluish cast, and this gradually becomes deeper and deeper. The forests on the mountains of Hartz, which may be seen from Magdeburg, appear thence

thence to be blue, but viewed from Halberstadt, they are green. The great extent of air between Magdeburg and these mountains, is the reason of it. However delicate or rare the bluish particles of the air may be, there is such a prodigious quantity of them in that interval, the rays of which enter into the eye at once, that they represent a tolerable deep blue.\*

\* This explanation of the blueness of the sky is strained and unfatisfactory. The air is, like water, perfectly colourless, otherwife any portion of it might be diftinguished by the fight. Befides, the blueness of the sky, even in clear weather, is not uniformly the fame, but acquires different degrees of intenfity, and different shades, from a variety of circumstances, the climate, the feafon, and the elevation of the place. The true explanation of the phenomenon must be fought from other principles. The most refrangible rays are, at minute distances, attracted or repelled, by colourless substances, with the greatest force. A funbeam, therefore, in it's paffage through the atmosphere, will first lofe it's violet rays most profusely, next the indigo, then the blue, and if the track be of fufficient length, perhaps a few of the green. The rays, thus separated, are either absorbed by the air, or they are reflected, and cause the blue appearance. Hence, on the summits of lofty mountains, the colour of the heavens feems faint and dark, and inclined fomewhat to violet. On the contrary, in dense humid air, the colour is a light milky blue. Hence, also, the bright azure which paints the fky of the fouthern regions, owing to the dryneis of the air, and the shortness of the light's tract. For the same reason, not only the quantity, but even the quality, of the light which we receive from the fun, depends on his altitude. At rifing, and fetting, those rays which reach the furface, and even the lower range of clouds, are chiefly the reddish; at a greater elevation of the fun, the prevailing colour of his beams is fomewhat orange; and when still higher, it is a dilute yellow.

The same principles will account for the colour of the ocean,

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We remark a fimilar phenomenon in a fog, when the air is loaded with a great quantity of opaque particles of a whitish colour. On looking to only a finall distance, you scarcely perceive the fog; but when the distance is considerable, the whitish colour becomes very perceptible; to such a degree, that it is impossible to see through it. The water of the sea appears green at a certain depth; but when you take up a small quantity, as much, for instance, as a glass will contain, it is sufficiently diaphonous, and has no sensible colour: but in a great extent, when you look toward the bottom, so many greenish rays collected produce a deep colour.

27th July, 1760.

which is dark blue. It is only in feas, not exceeding one hundred fathoms in depth, that the reflection from the white bottom dilutes the proper colour, and forms a glaucous hue. This appearance is an invariable fign of the shallowness of the water, which is often a token of the proximity of the land. Dr. Hally relates an observation that he made in a diving-bell, which confirms these reasonings; after descending to a great depth in the sea, he ftretched out his hand, on which the fun shone through the water, and painted a beautiful crimfon. The fame observation may be extended, even to fubitances that are reckoned opaque. Hold an ivory knife in the focus of a burning glafs, perpendicular to the pencil of light, and a bright yellowish spot will be perceived on the back. Incline the knife gradually, and the colour of the fpot will pass through all the intermediate shades, and terminate in a fine red. It is scarce necessary to remark, that this experiment must be performed expeditiously, lest the ivory be scorched.—E.E.

### LETTER XXXIII.

Of Rays issuing from a distant luminous Point, and of the visual Angle.

A S long as the rays produced by the rapid vibration of the minuter particles of a body, move in the fame transparent medium, they preserve the fame direction, or diffuse themselves in all directions, in straight lines. These rays may be represented by the radii of a circle, or rather of a sphere, which, issuing from a centre, proceed in straight lines to the circumference; and it is on account of this resemblance, that we employ the same term radius, or ray, to express them, though, properly speaking, the light does not consist of lines, but of very rapid vibrations, going continually forward, in the direction of straight lines; and, for this reason, light may be considered as straight lines, issuing from a luminous point, in all directions.

Let C (plate I. fig. 11.) be a luminous point, from which rays iffue in all directions. Let two spheres be described round C, as a centre, of the one of which, let the great circle be a b de, and of the other ABDE. The light diffused over the surface of the smaller sphere a b de, will likewise occupy that of the greater sphere ABDE. The light, then, must be more faint and weak at the surface of this last, than on that of the smaller sphere a b de. Hence it may be concluded, that the effect of light must be smaller,

K 3.

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in proportion to the distance from the luminous point. If we suppose, that the radius of the greater sphere is double that of the smaller, the surface of the greater sphere will be four times as great. Since, therefore, the same quantity of light is disfused over the surface of the greater sphere, and over that of the smaller, it must follow, that light, at double the distance, is four times more faint; at thrice the distance, nine times; at a quadruple distance, sixteen times; and so on.\*

On applying this rule to the light of the fun, it will appear, that if the earth were removed to double the distance from the fun, the light derived from him would be rendered four times more faint; and if the fun were a hundred times farther from us, his brightness would be a hundred times a hundred, that is, ten thousand times less. Supposing, then, a fixed star to be as great, and as luminous as the fun, but that it was 400,000 times farther from us, it's light will be 400,000 times 400,000, that is, 160,000,000,000 times more faint than that of the fun. Hence we see, that the light of a fixed star is nothing, compared to that of the sun; and this is the reason that we do not see the stars in the day time; a feebler light

<sup>\*</sup> As the furfaces of spheres are to one another as the squares of their radii, it must be concluded, from what the Author has just now said, that the intensity of light, at different distances from the point which produces it, is in the inverse ratio of the square of these distances. It must be recollected, that the square of a number is the product which results from the multiplication of that number by itself.— $F_{\bullet}$   $E_{\bullet}$ 

always disappears in presence of one much more bright. The same thing holds good with respect to candles, and all other luminous bodies, which administer less light, in proportion to their distance from us; and you must have frequently remarked, that however strong a light may be, it is insufficient to affist us in reading a printed book, if you remove from it to any considerable distance.

There is still another circumstance, closely connected with what I have just observed; namely, that the same object appears smaller to us, in proportion to it's distance. A giant, at a great distance, does not appear taller than a dwarf near us. To form a clearer judgment of this, it is necessary to attend to the angles at which these objects are seen by us.

Let us suppose, then, (plate I. fig. 12,) A B to be an object, say a man, and that the eye looks at it from the point C. Draw from that point the straight lines, A C and B C, which represent the extreme rays proceeding from the object to the eye; we call the angle formed at C, the visual angle of that object for the point C. If we look at the same object from a smaller distance, at D, the visual angle D will be, undoubtedly, greater: hence it is clear, that the more distant the same object is, the smaller is it's visual angle; and the nearer it approaches, it's visual angle becomes greater.

Aftronomers measure very accurately the angles under which we see the heavenly bodies, and they have found, that the visual angle of the sun is somewhat more than half a degree. If the sun were

twice farther from us, this angle would be reduced to the half; and then it will not feem furprizing that it should furnish us four times less light. And if the fun were 400 times farther off, his vifual angle would become fo many times lefs, and then that luminary would appear no greater than a ftar. We must, therefore, carefully distinguish the apparent greatness of any object from it's real greatness. The first is always an angle greater or less, according as the object is nearer or more diffant. Thus the apparent greatness of the fun, is an angle of about half a degree, whereas his real magnitude far furpasses that of the earth; for the fun being a globe, his diameter is estimated to be 172,000 German miles,\* while the diameter of the earth is only 1720† miles. t

29th July, 1760.

<sup>\* 790,000</sup> miles English. † 7,920 miles English.

<sup>‡</sup> Astronomers likewise call the apparent diameter of a star the angle under which it is seen. Thus, they say, that the mean diameter of the sun is 31'58"; that of the earth, viewed from the sun, would be 17". Hence it follows, that the diameter of the earth being 2865 leagues, that of the sun is 323,000 leagues. The German mile contains 4000 sathoms, or 24,000 feet. The league of France contains 2282 sathoms. Hence it is easy to reduce the one measurement into the other.—F. E.

### LETTER XXXIV.

Of the Supplement which Judgment lends to Vision.

WHAT I have now fubmitted to you on the phenomenon of vision, belongs to optics, which is a branch of mixed mathematics, and which, likewise, holds a considerable rank in physics. Beside colours, the nature of which I have endeavoured to explain, it is the business of optics to treat of the manner in which vision acts, and of the different angles under which objects are seen.

You must have already remarked, that the same object may be viewed, fometimes under a greater vifual angle, fometimes under a fmaller, as it is lefs or more diftant from us. I fay farther, That a fmall object may be viewed under the same angle as a great one, when the former is very near, and the latter very diftant. A finall dish may be placed before the eye in fuch a manner, as to cover the whole body of the fun; and, in effect, a plate of half a foot diameter, at the diffance of 54 feet, exactly covers the fun, and is feen under the fame angle: and yet what a prodigious difference between the fize of a plate and that of the fun: The full moon appears to us under nearly the fame vifual angle as the fun, and, of confequence, nearly as great, though in reality much fmaller; but it is to be confidered, that the fun is almost 400 times more remote from us than the moon,

The vifual angle is a point of fo much the more importance in optics, that the images of the objects, which paint themselves on the bottom of the eye, depend upon it. The greater or less the vifual angle is, the greater or less they (the objects) are great or little. And as we see objects out of ourselves, only fo far as their images are painted on the bottom of the eye, they constitute the immediate object of vision or sensation. One of these images, therefore, leads us to the knowledge only of three things. First, it's figure and it's colours conduct to the conclusion, That there is, out of us, a similar object, of fuch a figure, and fuch a colour. Secondly, it's magnitude discovers the visual angle under which the object appears to us: and, finally, it's place on the bottom of the eye makes us fensible of the direction of the external object, relatively to us, or that in which the rays emitted from it reach our eyes.

In these three particulars consists the phenomenon of vision; and we only perceive, 1st, the sigure and colours; 2dly, the visual angle, or the apparent magnitude; and, 3dly, the direction, or the place in which we conclude that the object exists. Vision, then, discovers to us nothing respecting either the real magnitude of objects, or their distances. Though we frequently imagine, that we can determine by the eye the magnitude and distance of an object, this is not an act of vision, but of the understanding. The other senses, and habits of long standing, enable us to calculate at what distance an object is from us. But this faculty extends only to objects at no great distance.

distance. Whenever their distance becomes considerable, our judgment cannot exercise itself with certainty; and if sometimes we venture to hazard a decision, it is generally very remote from the truth.

Thus, no one can pretend to fay that he fees the magnitude or the distance of the moon; and when the vulgar imagine they can judge of the first, by considering it as equal to that of the terrestrial bodies which are seen under the same angle, it is not by vision they are deceived, but by their judgment, which they want to apply to an object far beyond their reach. It is certain, therefore, that the eyes alone can determine nothing respecting the distance and magnitude of objects.

To this fubject may be referred the very remarkable case of a man born blind, who obtained sight, by means of an operation, at an advanced period of life:\* This person was at first dazzled: he could distinguish nothing as to the magnitude and distance of objects. Every thing appeared so near, that he wanted to handle them. A considerable time, and long practice, were requisite to bring him to the real use of sight. He was under the necessity of serving a long apprenticeship, such as we person during the term of childhood, and of which we afterwards preserve no recollection.

This it is which inftructed us, that an object appears to us fo much the more clear and distinct as it

<sup>\*</sup> This was the blind man, on whom the famous Cheffelden performed the operation of the couching cataract, -F. E.

is nearer; and reciprocally, that an object which appears clear and distinct is near; and when it appears obscure and indistinct, that it is at a distance. It is thus that painters, by weakening the tints of the objects which they wish to appear remote, and strengthening those which they would represent as nearer, are enabled to determine our judgment, conformably to the effect which they mean to produce. And they succeed so perfectly, that we consider some of the objects represented in painting as more distant than others: an illusion which could not take place, if vision discovered to us the real distance and magnitude of objects.

ist August, 1760.

### LETTER XXXV.

Explanation of certain Phenomena relative to Opties.

YOU have just feen, that vision alone discovers to us nothing, respecting either the real magnitude or the distance of objects; and that all we imagine we see, whether as to the distance or magnitude of any object, is the effect of judgment. We must carefully distinguish that which the senses represent to us, from what judgment adds, in which we frequently deceive ourselves. Many philosophers, who have declaimed against the accuracy of the senses, and who meant thence to infer the uncertainty

Hence

tainty of all human knowledge,\* have confounded the proper representations of our senses with judgment.

This is their mode of reasoning: We see the sun no bigger than a trencher, though it be infinitely greater; therefore the fense of seeing deceives us; therefore all our fenses deceive us; at least, we cannot depend on them: therefore, all the knowledge we acquire by means of the fenses, is uncertain, and probably false: We, therefore, know nothing. Such is the reasoning of these sceptics, who boast, so vain gloriously, of their ingenuity; though there be nothing fo eafy as to fay, that every thing is uncertain; and the greatest dunce may make a shining figure in this fublime philosophy. But it is absolutely false, that the fight reprefents to us the fun no bigger than a pewter plate; it determines nothing whatever respecting his magnitude; it is our judgment alone that deceives us. When the objects, however, are not very diftant we can pronounce with tolerable exactness on their dimensions and distances; and the other fenses, joined to the degree of clearness with which we see these same objects, render our judgments fufficiently certain. Now, as foon as we have the idea of the distance of an object, we form to ourselves, likewise, that of it's real magnitude, knowing that it depends on that distance.

<sup>\*</sup> Such were the Pyrrhonists. We still give the name of fcepticism, or Pyrrhonism, to this state of universal doubt or uncertainty.—F. E.

Hence, the more distant we reckon an object to be, the greater we conclude is it's magnitude; and reciprocally, the nearer we conclude it is, the smaller we suppose it. We, of course, frequently take one body for another of much greater magnitude, when a suspension of judgment prevents our taking distance into the account. The reason is that a very large body may be seen at a great distance, under the same angle as a small object placed near us.

There is another phenomenon, well known to every one, and which has given occasion to many disputes among the learned, and which it is now perfectly easy to explain. The full moon appears to every eye at the time of her rising to be much greater than when she has got to a considerable height above the horizon, though the visual angle of the apparent magnitude be the same. The sun, too, at the time of rising and setting, appears to every one greater than at noon. What then is the soundation of this judgment, so universal, and so false? It is undoubtedly because we judge the sun and the moon in the horizon to be at a greater distance from us than when they have got to a considerable height.

But how come we to form fuch a judgment? The common answer is, that when the sun and the moon are in the horizon, we perceive a great many objects between them and us which seem to increase their distance; whereas when the sun and moon have risen to a great height, we perceive nothing between them and us, and therefore conclude that they are

nearer. I know not whether this explanation will be fatisfactory. It may be objected that an empty apartment appears greater than one completely furnished, though the fize be exactly the fame; feveral intervening objects, therefore, do not always lead us to imagine that one more remote is at a greater diftance than is really the case. I flatter myself that the following solution will be deemed more natural, and better founded.

Let the circle A (plate I. fig. 13.) represent the earth, and the dotted circle the atmosphere, or air with which the earth is furrounded; fuppose yourfelf stationed at the point A, if the moon is in the horizon, the rays will reach you in the direction of the line B A; but in her extreme height, the rays will defcend in the line C A. In the first case the rays pass through the greater space B A; and in the fecond cafe through the finaller space C A. Now, you will please to recollect, that the rays of light which pass through a transparent medium have their force diminished in proportion to the length of the paffage. The atmosphere or air, then, being a transparent medium, the ray B A must in it's passage lose much more of it's force than the ray CA. Hence it follows, in general, that all the celeftial bodies appear much less brilliant in the horizon than when fully rifen and elevated. We are able to look directly even at the fun, when he is in the horizon; but when once he has gained a certain height, the eye is conftrained to fhrink from his luftre.

I conclude from this that the moon, too, appears lefs

less brilliant in the horizon than when elevated.\*

Now, you will recollect what I said a little above, in speaking of essect in painting, that the same object appears

\* This explanation of the appearance of the horizontal moon was offered, in the beginning of the present century, by the acute Dr. Berkeley, Bishop of Cloyne. It has since been resuted by that excellent optician, Dr. Smith, who was the first that completely investigated this curious subject. The following is an abtract of the theory, from Dr. Priestley's "History of Vision, Light, and Colours."

"If the furface of the earth were perfectly plane," fays Dr. Smith, "the diffance of the visible horizon would scarce exceed 5000 times the height of the eye above the ground, or the distance of miles (supposing the height of the eye to be between five and fix feet) and all objects placed beyond that diffance would appear in the vifible horizon. All objects and clouds, likewife, placed at any diffance beyond this, must consequently, if they be visible at all, appear to be in the horizon. "Hence," he fays, "if we suppose a vast wall to be built at the extremity of the plane, beyoud the point of vifible diffance, it will not appear ftraight, but circular, as if built upon the circumference of the horizon; and, if continued infinitely, would make a perfect femi-circle. If now this round plane, with the wall upon it, be imagined to be raifed, till it come perpendicular to the rest of the plane, on which a perfon frands, the wall will appear like the concave figure of the clouds over his head. But though the wall in the horizon appear in the shape of a semi-circle, yet the cieling will not, but much flatter; because the horizontal plane was a visible surface, which fuggefted the idea of the fame diftances quite round the eye; but in the vertical plane, extended between the eye and the cieling, there is nothing that affects the fense with an idea of it's parts. Confequently the apparent distances of the higher parts of the cieling will be gradually diminished. Now, when the sky is quite overcast with clouds of equal gravities, they will all float in the air at equal heights above the earth, and confequently will comappears to us more distant when it's light is weakened: the moon, then, being in the horizon, must appear more distant than at any point of elevation.

pose a surface resembling a large cieling, as flat as the visible surface of the earth. It's concavity, therefore, is not real, but apparent; and when the heights of the clouds are unequal, since their real shapes and magnitudes are all unknown, the eye can seldom distinguish the unequal distances of those clouds which appear in the same directions, unless when they are very near us, or are driven by contrary currents of the air. So that the visible shape of the whole surface remains alike in both cases. And when the sky is either partly overcast, or perfectly free from clouds, it is a fact that we still retain much the same idea of it's concavity, as when it was quite overcast. But if any one thinks that the reflexion of light from the air is alone sufficient to suggest that idea, he would not dispute it."

"The concavity of the heavens appears to the eye, which is the only judge of an apparent figure, to be a less portion of a spherical surface than an hemisphere. In other words," he says, "the center of the concavity is much below the eye; and, by taking a medium among several observations, he found the apparent distance of it's parts, at the horizon, was generally between three and four times greater than the apparent distance of it's parts over head."

"This he determined by measuring the actual height of some of the heavenly bodies, when, to his eye, they seemed to be half way between the horizon and the zenith. In this case their real altitude was only 23 degrees."

Upon these principles Dr. Smith constructed the following table:

Sun or Moon's altitude,	Apparent Diameters,
in degrees.	or diffances.
00	100
15	68
30	50
45	40
60	34
75	31
90	30 E.E.
Vol. I.	L The

The consequence is obvious; as we judge the distance of the moon greater in the horizon, we must likewise judge her magnitude greater. And in general all the stars, when near the horizon, appear to us greater, because their apparent distance is greater.

3d August, 1760.

## LETTER XXXVI.

Of Shade.

HAVE endeavoured to explain almost all that is usually treated of in optics. All that remains is to speak of shade. You already know too well what is meant by shade to render it necessary for me to dwell long on the subject. Shade always supposes two things: a luminous body, and an opaque body, which does not transmit the rays of light. The opaque body, then, prevents the rays of a luminous body from getting behind it, and the space which the rays cannot reach, from this interception, is called the shade of the opaque body, or, what comes to the same thing, shade includes all that space in which the luminous body is not to be seen, because the opaque body obstructs it's rays.

Let A (plate I. fig. 14.) be a luminous point, and B C D E an opaque body. Draw the extreme rays A B M, A D N, touching the opaque body. It is evident that no ray of light proceeding from A, can penetrate into the space M B E D N; and in what-

ever point within that space the eye may be placed, at O for example, it will not see the luminous body. This space is the shade of the opaque body, and we see that it is continually increasing, and may extend to infinity. But if the body from which the rays proceed be itself of great magnitude, the determination of the shade is somewhat different. There are three cases which demand consideration; the first is, when the luminous body is less than the opaque; the second, when they are equal; and the third, when the luminous body is the greater. The first case is that which we have now been considering, in which the light is smaller than the opaque body.

The fecond is represented, (plate I. fig. 15.) in which the luminous body A is of the same magnitude with the opaque body B C E D. If you draw the extreme rays A B M, A E N, the space M B E N will be shaded, and through the whole of that space it will be impossible to see the luminous body. You see, likewise, that the lines B M and E N are parallel, and that the shade extends to infinity, always preserving the same breadth.

The third case is exhibited, (plate I. fig. 16.) in which the luminous body A A is greater than the opaque body B C E D. The extreme rays, touching the opaque body in B and E, if produced, will meet in the point O, and the space of the shade B O E becomes finite, and terminates in O. The shade, in this case, is termed conical. It is only into this space that the light has no admission, and in which it is

impossible to see the luminous body. To this third case belong the shades of the celestial bodies, which are much smaller than the luminous body which enlightens them, namely the sun.

We have here, then, another display of the Creator's wisdom. For if the sun were smaller than the planets, their shades would not be terminated, but extend to infinity, which would deprive immense spaces of the benefit of the sun's light. But the magnitude of that luminary surpassing by so many times that of the planets, their shades are contracted to very narrow bounds, from which alone the light of the sun is excluded.

It is thus that the earth and the moon project their conical shades; and the moon may occasionally plunge into the fhade of the earth either partially or totally. When this takes place, we fay the moon is eclipfed, either wholly or in part. In the former case we call it a total eclipse of the moon; in the other, a partial eclipfe. The moon, likewife, projects her shade, but it is smaller than that of the earth. It may happen, however, that the shade of the moon should extend as far as to the earth; and then those who are involved in that shade, undergo an eclipse of the sun. An eclipse of the sun, then, takes place when the moon, interpoling, prevents our feeing the fun wholly, or in part. We fee not the fun by night, though there be no eclipfe; but we are then in the fhade of the earth, which causes our greatest obscurity.

Hitherto

Hitherto we have confidered only the cases in which the rays of light are transmitted in straight lines, which is the professed object of optics. But it has been already remarked, that the rays of light are fometimes reflected, and fometimes broken, or refracted. You will recollect, that when the rays fall on a well-polished furface, fuch as a mirror, they are reflected from that furface; and when they pass from one transparent medium to another, they undergo refraction, and are in some sense broken. Hence arife two other sciences. That which considers vifion in reference to reflected rays is called catoptrics; and that which has for it's object vision, in reference to broken or refracted rays, is termed dioptrics. Optics treat of vision relatively to direct rays of light. I shall present you with a summary of these two sciences, catoptrics and dioptrics, as they disclose phenomena which are every day prefenting themfelves, and of which it is of importance to investigate the causes and the properties. Every thing relating to the fubject of vision is, beyond contradiction, an object highly worthy of exciting curiofity; and of engaging attention.

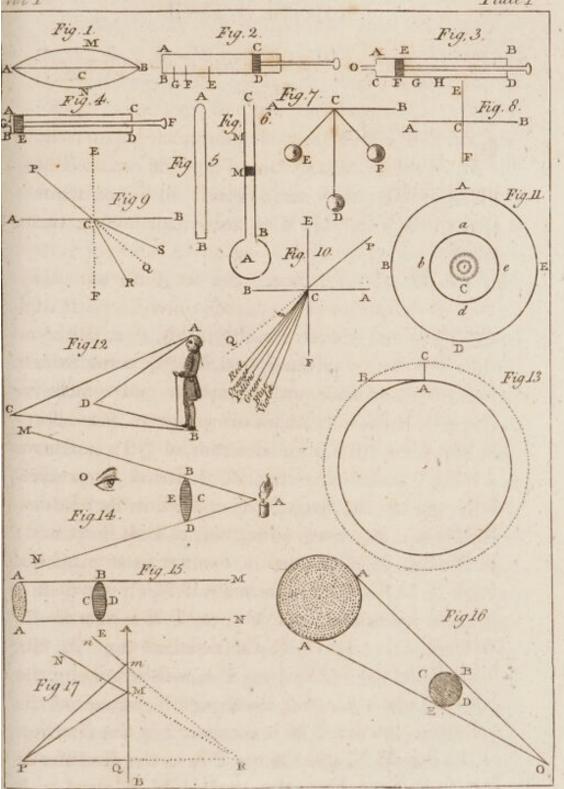
<sup>\* 51</sup>b August, 1760.

#### LETTER XXXVII.

Of Catoptrics, and the Reflection of Rays from plain Mirrors.

CATOPTRICS treat of vision relatively to reflected rays. When rays of light fall on a well polished surface, they are reslected in such a manner that the angles on all sides are equal among themselves.

To fet this in a clear light, let A B (plate I. fig. 17.) be the furface of a common mirror, and Paluminous point, whose rays P Q, P M, P m, fall upon the mirror. Of all these rays, let PQ be that which falls perpendicularly on the mirror, and which has this particular and remarkable property, that it is reflected upon itself in the direction of Q P; just as on a billiard table, when the ball is ftruck perpendicularly against the ledge, it is repelled in the felf-same direction. But every other ray, as P M, is reflected in the line M N, in fuch a manner as to make the angle A M N equal to the angle B M P; in which it is to be remarked, that the ray P M is named the incident ray, and M N the reflected ray. In like manner, to the incident ray P m, will correspond the reflected ray m n; and, confequently, because of the reflection, the ray P M is continued in the direction of the line M N, and the ray P m in the direction of m n, fo that we have the angle A M N, equal to B M P, and the angle A m n, equal to the angle B m P.





This property is thus enounced: The angle of reflection is always equal to the angle of incidence.

I have already taken notice of this striking property; but my design, at present, is to shew what the phenomema in vision are which result from it. First, it is evident, that an eye, placed at N, will receive from the luminous point P, the resected ray M N; thus the ray which excites in that eye the sensation of the body from whence it proceeded, comes in the direction M N, just as if the object P were in some point of that line; hence it follows that the eye must see the object P in the direction N M.

In order the more clearly to elucidate this fact, we must have recourse to geometry; and you will recollect with pleafure the propositions on which the following reasoning is founded. Let the perpendicular ray P Q be produced on the other fide the mirror to R, fo that Q R shall be equal to P Q; I will flew you that all the reflected rays, M N, and m n being produced behind the mirror, must meet in that point. For, taking the two triangles P Q M and R O M, they have first the fide M O common to both; then the fide Q R was made equal to the fide PQ; and, finally, the angle PQM being a right angle, it's adjacent angle R Q M must likewise be a right angle.\* Therefore thefe two triangles, having each an equal angle contained by two equal fides, shall be every way equal, † and consequently the angle

<sup>\*</sup> Euclid's Elements, book I. Prop. 13.

<sup>+</sup> Euclid, book I. Prop. 4.

P M Q equal to the angle R M Q. But the angle A M N, and the angle R M Q, being vertical, are equal to each other,\* therefore also the angle A M N shall be equal to the angle P M Q; that is, the angle of reflection shall be equal to the angle of incidence.

In the fame manner it is demonstrated that the reflected ray m n being produced, would likewife pass through the point R, and confequently produce in the eye the same effect as if the object P were actually placed behind the mirror at R, this point being in the perpendicular P Q R, at the same distance as P from the furface of the mirror, but on different fides. This will enable you to comprehend clearly why mirrors represent objects as if they were behind them; and why we judge that these objects are placed as far behind the furface of the mirror as they really are before it. It is thus the mirror transports objects into another place, without changing their appearance. To diffinguish in the mirror that apparent object from the real, we name the apparent object the image, and we fay that the images represented by reflected rays are behind the mirror. This denomination ferves to diftinguish real objects from the images of them represented in mirrors; and the images which we fee in mirrors are perfectly equal and fimilar to the objects, with this exception, that what in the object is on the left appears in the image on the right, and reciprocally. Thus a person wearing his fword on the left fide, appears with it in the mirror on his right.

<sup>\*</sup> Euclid, book I. Prop. 15.

From what has been faid, it is always eafy to fettle the image of any object whatever behind the mirror.

For AB (plate II. fig. 1.) being a mirror, and EF an object, fay an arrow: draw from the points E and F the perpendiculars E G and F H, to the furface of the mirror, and produce these to e and f, so that E G shall be equal to e G, and F H to f H, e f will be the image fought, which will be equal to the object E F, because the quadrilateral figure G e f H is in all respects equal to the quadrilateral figure G E FH. It must be still farther remarked, that were you even to cut off from the mirror a part, as C B, and A C was the mirror, the image e f would not be changed. And confequently when the mirror is not fufficiently large to admit the falling of the perpendiculars E G and F H upon it, we must suppose the plane of the mirror to be extended, as we produce lines in geometry when we want to let fall perpendiculars upon them. What I have faid respects only common mirrors, whose furface is perfectly plain. Convex and concave mirrors produce different effects. 7th August, 1760.

# LETTER XXXVIII.

Reflection of Rays from convex and concave Mirrors.

Burning Mirrors.

VERY thing relating to the reflection of rays is reduced, as you have feen, to two things; the one of which is the place of the image which the reflected rays represent; and the other the relation of

the image to the object. In ordinary or plain mirrors, the image of the object is behind the mirror, at a distance equal to that of the object before the mirror, and it is equal and similar to the object. To both of these circumstances we must attend when the mirror is not plain; but when it's surface is convex or concave; for in either case the image is, for the most part, strangely dissigured. You must frequently have remarked that on presenting any object before a spoon very highly polished, you see it's image greatly dissigured, whether reslected from it's interior surface, which is concave, or from it's exterior, which is convex.

A globe of filver, finely polifhed, reprefents objects with fufficient accuracy, but in miniature. If the interior furface of the globe is well polished, objects appear upon it magnified; provided always that they are not too distant. For the same objects may likewife appear fmaller and inverted, if they are removed far from the mirror. There is no occasion to take a whole globe; any part of it's furface whatever produces the same effect. These mirrors are denominated spherical; and there are two forts of them. The one is convex and the other concave, according as they are taken on the exterior or interior furface of the fphere. They are compounded of various metals, fusceptible of a fine polish; whereas plain mirrors are made of a plate of glass, and covered on one fide with a preparation of mercury, defigned to stop the passage of the rays, and to reslect them. I begin with convex mirrors.

Let A C B (plate II. fig. 2.) be a mirror, the fegment of a fphere, whose centre is G. If you place before this mirror an object E, at a great distance, it's image will appear behind the mirror, at the point D, the middle point of the radius of the sphere CG; and the magnitude of this image will be to that of the object, in the relation of the lines C D and CE: it will, therefore, be in this case much smaller than the object, as the line CD is, in effect, much fmaller than the line CE. If the object E approaches to the mirror, fo likewife will it's image. This is all demonstrable on geometrical principles, by supposing that any incident ray whatever, fay E M, is reflected in the direction of M N, fo that the angle B M N may be equal to the angle C M E. Thus, when the eye is at N, receiving the reflected ray M N, it will fee the object E, according to that direction, and will observe it in the mirror, at the point D: or, in other words, D will be the image of the object placed at E, but finaller. It is likewife eafy to fee, that the fmaller the fphere is, of which the mirror is a fegment, the more, likewife, is the image diminished.

I proceed to concave mirrors, the use of which is very common on many occasions. Let A C B (plate II. fig. 3.) be a mirror, forming part of a sphere, whose centre is G, and G C a radius. Let us suppose an object E, very distant from the mirror, it's image will appear before the mirror at D, the middle point of the radius C G: for any ray of light whatever, E M, from the object E, falling on the surface of the mirror, at the point M, will be reslected thence,

thence, in such a manner, as to pass through the point D; and when the eye is placed at N, it will see the object at D; but this image will be to the object in the ratio of CD to CE, and consequently in this case smaller than it. And when you bring the object nearer to the mirror, the image retires; the object being placed even at the centre G, the image is there likewise. If you bring the object still forward to D, the image will retire infinitely beyond E. But if the object be placed still farther forward, between C and D, the image will fall behind the mirror, and appear greater than the object.

When you look at yourfelf in fuch a mirror, at fome point between D and C, your face will appear frightfully large. This is explained by the nature of reflection, in virtue of which the angle of incidence, E M A, is always equal to the angle of reflection, C M N. To this species must be referred burning mirrors, and every concave mirror may be employed to burn. This remarkable property merits a more particular explanation.

Let A B C (plate II. fig. 4.) be a concave mirror, whose centre is G, and instead of the object, let the sun be at E; his reslected rays will represent the image of the sun at D, the middle point between C and G. Now, the magnitude of this image will be determined by the extreme rays S C, S C. This image of the sun will be, accordingly, very small, and as all the rays of the sun which fall on the mirror A C B are reslected in this image, they will be collected there, and will have so much more force, as

the image D is smaller than the surface of the mirror. But the rays of the sun are endowed with the property of heating the bodies on which they fall, as well as that of illuminating them; hence it follows, that there must be at D a great degree of heat; and when the mirror is sufficiently large, this heat may become stronger than the most ardent sire. In fact, by means of such a mirror, you may burn in an instant any combustible body, and even melt metals of every kind. It is the image of the sun alone which produces these surprising effects. This image is usually denominated the focus of the mirror; it falls always in the middle point of the radius C G; between the mirror and it's centre G.

You must carefully distinguish burning mirrors from burning glasses, of which I shall give some account in my next letter.

9th August, 1760.

# LETTER XXXIX.

# Of Dioptrics.

AVING explained the principal phenomena of catoptrics, which refult from the reflection of the rays of light; I proceed to treat of dioptrics, whose object is to unfold the phenomena of the refraction of rays, which takes place when they pass through different transparent mediums. A ray of light does not pursue the same straight line unless it continues

continues it's progress through the same medium. As soon as it enters another transparent medium, it changes it's direction more or less, according as it salls upon it more or less obliquely. There is only one case in which it pursues a rectilinear course, namely, when it enters the other medium perpendicularly.

The inftruments principally to be confidered in dioptrics are the glaffes employed in the conftruction
of telescopes and microscopes. These glaffes are of a
circular form, but with two faces. Every thing relating to them is reducible to the figure of these two
faces, which may be plain, or convex, or concave.
Their convexity, or concavity, is always equal to
that of a sphere, of which the radius must be known,
it being considered as the measure of the curve of
those surfaces. This being laid down, we shall have
several kinds of dioptric glasses.

The first species, No. I. (plate II. fig. 5.) is that whose two faces are plain. By cutting a circular piece out of a plate of glass, of equal thickness, we shall have one of this species, which makes no change on objects either as to magnitude or distance. Glass No. II. has one of its surfaces plain, and the other convex; and such are termed plano-convex. The third species, No. III. has one face plain, and the other concave, and these are called plano-concave. The fourth, No. IV. has two convex surfaces, and is called double-convex. No. V. has two concave surfaces, and is called double-concave. The species Nos. VI. and VII. have one surface convex and the other concave; and

we give them the name of menifeus. All these lenses are reducible to two classes; the one containing those in which convexity prevails, as Nos. II. IV. VI.; in the other, concavity is predominant, namely, Nos. III. V. VII. The former class is simply denominated convex, and the latter concave. These two classes are distinguished by the following property.

Let A B (plate II. fig. 6.) be a convex glass, exposed to a very distant object, E F, whose rays G A, G C, G B, fall on the glafs, and, paffing through it, undergo a refraction, which will take place in fuch a manner, that the rays proceeding from the point G shall meet on the other side of the glass in the point g. The fame thing will happen to the rays which proceed from every point of the object. By this alteration all the refracted rays A I, B m, C n, will purfue the fame direction as if the object were at e, g, f, and inverted; and it will appear as many times fmaller as the diftance C g shall be contained in the diftance C G. We fay, then, that fuch a glafs represents the object E F behind it at e f, and this representation is called the image, which is confequently inverted, and is, with the object itself, in the ratio of the distances of the glass from the image, and of the glass from the object.

It is clear, then, that if the fun were the object, the image represented at e f would be that of the fun; though very small, it will be so brilliant, as to dazzle the eye, for all the rays which pass through the glass meet in this image, and there exercise their double power of giving light and heat. The heat

there is nearly as many times greater, as the furface of the glass exceeds in magnitude the image of the sun, named it's focus, from which, if the glass be very great, you may produce the greatest effects of heat. Combustible substances, placed in the focus of such a glass, are instantly consumed. Metals are melted, and even vitrissed by it; and other effects are produced far beyond the reach of the most active and intense sire.

The reason is the same as in the case of burning mirrors. In both the rays of the sun, dissured over the whole surface of the mirror, or glass, are collected in the small space of the sun's image. The only difference is, that in mirrors the rays are collected by reflection, and in glasses by refraction. Such is the effect of convex glasses, which are thicker in the middle than at the extremities, and which I have represented in Nos. II. IV. and VI. Those represented in Nos. III. V. and VII. are thicker at the extremities than at the middle, and being all comprehended under the term concave, produce a contrary effect.

Let A C B (plate II. fig. 7.) be a glass of this form. If you expose to it, at a great distance, the object E G F, the rays G A, G C, G B, proceeding from the point G, will undergo a refraction, on leaving the glass, in the direction of A I, C m, and B n, as if they had issued from the point g; and an eye placed behind the glass, at m, for example, will see the object just as if it were placed at e g f, and in a situation similar to that in which it is at the point G, but as many times smaller as the distance C G exceeds the

distance G g. Convex glasses, then, represent the image of a very distant object behind them; concave glasses represent it before them; the former represent it inverted, and the latter in it's real situation. In both, the image is as many times smaller as the distance of the object from the glass exceeds that of the glass from the image. On this property of glasses is founded the construction of telescopes, spectacles, and microscopes.

11th August, 1760.

### LETTER XL.

Continuation. Of burning Glasses and their Focus.

CONVEX glasses furnish some farther remarks, which I beg leave to lay before you. I speak here of those glasses in general which are thicker in the middle than at the extremities; whether both surfaces be convex, or one plane and the other convex; or, finally, one concave and the other convex, provided, however, that the convexity exceed the concavity, or that the thickness be greater at the middle than at the extremities. It is farther supposed that the glasses have a spherical sigure.

They have first this property, that being exposed to the sun, they present behind them a focus, which is the image of that luminary, and which is endowed, like it, with the property of illuminating and burning. The reason is that all the rays issuing from

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the fun, and falling on this furface, are collected by the refraction of the glass into a single point. The fame thing happens whatever be the object exposed to such a glass; it always presents the image of it, which you see instead of the object itself. The following sigure will render what I have said more intelligible.

Let A B C D (plate II. fig. 8.) be a convex glass, before which is placed an object E G F, of which it will be fufficient to confider the three points E, G, F. The rays which, from the point E, fall upon the glass, are contained in the space A E B; and are all collected in the space A e B by refraction, so as to meet in the point e. In the fame manner the rays from the point G, which fall on the glafs, and which fill the fpace A G B, are comprehended, by means of refraction, in the space A g B, and meet in the point g. Finally, the rays from the point F, which fall on the glass in the angle A F B, are refracted so as to meet in the point f. Thus we shall have the image egf in an inverted position behind the glass; and an eye placed at O, behind the image, will be affected in the same manner as if the object were at egf, inverted, and as many times finaller as the diffance Dg is fmaller than the distance C G.

In order to determine the place of the image e g f, we must attend as well to the form of the glass as to the distance of the object. As to the first, it may be remarked, that the more convex the glass is, in other words, the more that the thickness of the middle C D exceeds that of the extremities, the nearer the

image will be to it's furface. With regard to the distance, if you bring the object E F nearer to the glafs, it's image ef retires from it, and reciprocally. The image cannot be nearer to the glass than when the object is at a very great distance from it; it is then at the fame diftance as that of the fun would be, which is denominated the focus of the lens. When the object, then, is very distant, the image falls in the very focus, and the nearer you bring the object to the glass the farther the image retires from it, and that in conformity to a law in dioptrics, by means of which you can always determine the place of the image, for every distance of the object, provided you know the focus of the glass, that is, the distance at which it collects the rays of the sun, in a fpace fufficiently fmall to fet on fire a body exposed to it.

The point where the rays meet is, as has been faid, the place of the image. Now, this point is eafly found by experience. The different denominations of glasses are derived from it, as when we say, such a glass has it's focus at the distance of an inch, another at the distance of a foot, another at the distance of ten feet, and so on; or, more concisely, a glass of an inch, a foot, or ten feet focus. Long telescopes require glasses of a very distant focus, and it is extremely dissicult to make them exact. I once paid 150 crowns for one lens, which I fent to the academy of Petersburg; it has it's focus at the distance of 600 feet: I am convinced it was of no great value; but they would have it on account of it's rarity.

To be fatisfied that the reprefentation of the image egf, in the preceding figure, is real, you have only to hold at that place a piece of white paper, the particles of which are fusceptible of the different kinds of vibrations on which colours depend. Then all the rays from the point E of the object, on meeting at the point e, will put the particles of the paper into a movement of vibration fimilar to that which the point E has, and confequently you will fee the point e of the fame colour as the point E. In like manner the points g and f will have the fame colours as the points G and F of the object; and you will likewife fee on the paper all the points of the object expressed in their natural colours; which will reprefent the most exact and the most beautiful picture of the object. This will fucceed perfectly well in a dark room by applying a convex lens to a hole made in the flutter. You will then see on a sheet of white paper, placed opposite to the aperture in the shutter, all the external objects fo exactly painted, that you may trace them with a pencil. Painters make use of fuch a machine for defigning landscapes and other views.\*

13th August, 1760.

<sup>\*</sup> The hypothesis of light, contained in the preceding letters, was first proposed in the middle of last century by the ingenious Mr. Huggens; but after the brilliant discoveries of Sir Isaac Newton, it fell into oblivion, where it ought ever to have remained. What induced Mr. Euler to revive it, it is difficult to conceive. This hypothesis is not likely to have many abettors in the present age. As it appeals wholly to the imagination, it requires not any formal resultation. I shall mention a single objection, which seems to be conclusive: If ether were the vehicle of light, as air and water are of found, the ear would likewise be, in some degree, an organ of vision.

#### LETTER XLL

# Of Vision, and the Structure of the Eye.

T AM now enabled to explain the phenomena of vivision, which is undoubtedly one of the greatest operations of nature that the human mind can contemplate. Though we are very far short of a perfect knowledge of the fubject, the little we do know of it is more than fufficient to convince us of the power and wifdom of the Creator. We difcover in the structure of the eye perfections which the most exalted genius could never have imagined.

I shall not detain you at present with an anatomical description of the eye. It is sufficient to remark, that the exterior membrane a A b (plate II. fig. 9.) is transparent, and is called the cornea of the eye; behind this, on the infide, is another membrane a m, b m, circular and coloured, which we call the iris, in the middle of which is an aperture m m, called the pupil, which appears to us to be black. We find behind this aperture, the crystalline humour b B C a, which is a body fomewhat like in form to a fmall burning glass; it it perfectly transparent, and of a membranous fubftance. Behind the crystalline humour the cavity of the eye is filled with a transparent jelly, called the vitreous humour. The anterior space between the horny tunicle a A b, and the crystalline talline a b contains a liquor fluid as water, which, for that reason, is called the aqueous bumour.

Here, then, are four transparent substances, through which the rays of light, that enter into the eye, must pass: 1. the horny tunicle, or cornea; 2. the aqueous humour, between A and B; 3. the crystalline b B C a; 4. the vitreous humour. These four substances differ as to density; and the rays passing from one to another, undergo a particular refraction; and they are so arranged, that the rays coming from a point of any object, are still collected within the eye in a point, and there present an image.

The bottom of the eye at E G F, or the retina, is furnished with a whitish tissue, adapted to the reception of images; and it is thus, you will please to recollect, that the images of objects may be represented on a white ground. Conformably to the same principle, all the objects, whose rays enter into the eye, are found painted on the retina. Take the eye of an ox, and having removed the exterior parts which cover the retina, you will see all the objects painted there so exactly, that no artist could exceed it, or even arrive at such a degree of perfection. And in order to see any object whatever, the object must almays be painted on the retina; and when, unfortunately, any of the parts of the eye are injured, or lose their transparency, the person becomes blind.

But it is not fufficient, in order to our feeing objects, that their images should be painted on the retina; some are blind, though this takes place. Hence

we see that images painted on the retina are not, after all, the immediate object of vision, and that the perception of the soul is communicated some other way. The retina is a reticulated contexture of nerves the most subtile, communicating with a great nerve, which, coming from the brain, enters the eye at O, and is denominated the optic nerve. These small nerves of the retina are agitated by the rays of light which form the image at the bottom of the eye; and this agitation is transmitted by the optic nerve to the brain. It is there, undoubtedly, that mental perception is formed: but the most dextrous anatomist is unable to pursue these nerves to their source: the union of the soul with the body must for ever remain, a mystery.

15th August, 1760.

# LETTER XLII.

00-16-00

Continuation. Wonders discoverable in the Structure of the Eye.

IT will not be difagreeable to you, I hope, to contemplate with me, fomewhat more attentively, the wonders difcoverable in the structure of the eye.

And first the pupil presents an object highly worthy of admiration. It is that aperture which we find in the middle of the iris or star, by which the rays pass into the inside of the eye, and which appears black. The larger it is, the greater quantity of rays can enter into the eye, to form on the retina the image which appears painted there; thus, the more the pupil is opened, the more brilliant this image will be.

On carefully examining the human eye, we obferve, that the aperture of the pupil is fometimes greater and fometimes finaller. It is generally remarked, that the pupil is contracted when exposed to a very strong light; and, on the contrary, very much dilated where the light is faint. This variation is absolutely necessary to the perfection of vision. When we are in a very ftrong light, the rays being more powerful, fewer of them are wanted to agitate the nerves of the retina; the pupil, accordingly, is then more contracted. Were it more dilated, and confequently admitted more rays, their force would agitate the nerves too violently, and occasion pain. It is for this reason we are unable to look upon the fun without being dazzled, and without fenfible pain in the bottom of the eye.

Were it possible for us to contract the pupil still more, so as to admit only a very small quantity of rays, we should not be very greatly incommoded by it; but the contraction of the pupil is not in our own power. Eagles posses this advantage, and are able to look directly at the fun; it is accordingly remarked, that their pupil is then so much contracted, as to appear reduced to a point. A clear light, requiring a very small dilatation of the pupil, in proportion as the light decreases, the pupil dilates, and in the dark is so enlarged, as almost to occupy the whole

whole of the iris. If it remained in the same state of contraction as in the light, the rays which enter into it would be too weak to agitate the nerves as much as is necessary to perception; the rays must, therefore, be then admitted in greater abundance, in order to produce a sensible effect.

Were it in our power to open the pupil still more, we should be able to see in a greater degree of darkness. To this purpose we are told of a person, who, having received a blow on his eye, the pupil was so dilated by it, that he could read, and distinguish the minutest objects in the dark. Cats and several other animals which roam in the dark, have the faculty of enlarging the pupil much more than the human species; and owls have theirs at all times too much dilated to bear even a moderate degree of light.

Now, when the pupil of the human eye dilates or contracts, it is not by an act of the will; man not having the power of dilating or contracting the pupil at pleafure. As foon as he enters into a luminous fituation, it fpontaneously contracts and dilates on his return to darkness. But this change is not produced in an instant; it requires a little time for this organ to accommodate itself to circumstances.

You must, no doubt, have remarked, that as often as you make a very sudden transition from a clear light to a dark place, as in the theatre of Schuck, you could not at first distinguish the company. The pupil was still too narrow to permit the sew feeble rays which it admitted to make a fensible impression; but it gradually dilated to receive a sufficiency of rays.

The contrary happens, when you pass suddenly from darkness to a clear light. The pupil being then very much expanded, the retina is struck in a lively manner, you are quite dazzled, and under the necessity of shutting your eyes.

It is then a very remarkable circumstance that the pupil should dilate and contract according as vision requires, and that this change should take place almost spontaneously and independently of any act of the will. Philosophers who examine the structure and the functions of the human body, are greatly divided in opinion as to this subject, and there is little appearance that we shall ever have a satisfying solution of this wonderful phenomenon. The variability of the pupil is, however, an object essentially necessary to vision; and without which it would be very imperfect. But various other particulars are discoverable, equally entitled to admiration.

171b August, 1760.

## LETTER XLIII.

Farther Continuation. Astonishing Difference between the Eye of an Animal, and the artifical Eye, or camera obscura.

THE principle on which the structure of the eye is founded, is, in general, the same as that according to which I explained the representation of objects on white paper by means of a convex lens.

Both

Both of them must be resolved into this, that all the rays, proceeding from one point of the object, are again collected in a single point by refraction; and it seems of little importance whether this refraction is performed by a single lens, or by the several transparent substances of which the eye is composed. It might even be inferred from thence, that a structure more simple than that of the eye, by employing one single transparent substance, would have been productive of the same advantages; which would amount to a very powerful objection against the wisdom of the Creator, who has assuredly pursued the simplest road in the formation of all his works.

Perfons have not been wanting who, from not having attentively examined the advantages refulting from the apparent complication, prefumed to cenfure this beautiful production of the Supreme Being with a levity worthy of cenfure. They have pretended it was in their power to produce a plan more fimple for the structure of the eye, because they were ignorant of all the functions which that organ had to discharge. I shall examine this plan of theirs; and I hope to convince you, that it would be highly defective, and altogether unworthy of being put in competition with that which actually exists.

Such an eye, therefore, would be reduced to a fimple convex lens, A B C D, (plate II. fig. 10.) which collects, in a point, all the rays coming from one and the fame corresponding point in the object. But this is only near to the truth. The spherical form, given to the surfaces of a lens, is liable to this inconvenience,

inconvenience, that it does not completely collect in one and the fame point the rays which pass through it's centre, and those which pass through the extremities. There is always a small difference, though almost imperceptible, in the experiments, by means of which we receive the image on a piece of white paper; but if this happened in the eye itself, it would render vision very confused.

The perfons to whom I have been alluding, allege, that it may be possible to find another figure for the furfaces of the lens, which shall have the property of collecting anew all the rays iffuing from the point O, in a point R, whether they pass through the centre, or through the extremities. I admit that this may be possible; but supposing the lens to possess this property, with respect to the point O, at the fixed distance C O, it would not possess it at points at a greater or less distance from the lens; or, even admitting this to be possible, which it is not, the lens would most certainly lose that property with regard to objects placed on one fide, at T, for instance. Accordingly we fee that when objects are represented on white paper, though fuch as are directly before the lens, fay at O, may be fufficiently well expressed, those which are obliquely situated, as at T, are al, ways much disfigured, and very confufedly expressed: and this is a defect which the most ingenious artist is incapable of rectifying.

But there is another and one not less considerable. In speaking of rays of different colours, I remarked, that in passing from one transparent medium to anot

ther,

ther, they undergo a different refraction; that rays of a red colour undergo the least refraction, and vior let-coloured rays the greatest. Hence, if the point O were red, and if it's rays, in passing through the lens A B, were collected at the point R, this would be the place of the red image. But if the point O were violet, the rays would be collected nearer to the lens, at V. Again, as white is an assemblage of all the simple colours, a white object, placed at O, would form several images at once, situated at different distances from the point O; the result of which would be, on the retina, a coloured spot that would greatly disturb the representation.

It is accordingly observable, that when in a dark room the external objects are represented on white paper, they appear bordered with the colours of the rainbow, and it is impossible to remedy this defect by employing only one transparent body. But it has been remarked, that this may be done by means of different transparent substances; but neither theory nor practice have hitherto been carried to the degree of perfection necessary to the execution of a structure which should remedy all these defects.\* The human

<sup>\*</sup> A similar defect has been remarked in the common telescope, Objects do not appear in it very clearly. You see, besides, at the circumference of the field which it encompasses, a mixture of colours, which is called iris. To remedy this inconveniency, achromatic telescopes have been constructed, whose object-glass, being composed of more than one lens of different densities, and which of consequence refract the rays differently, produce an effect analogous to that of the transparent substances of the eye, of which our Author has been treating.—F. E.

eye, however, labours under none of the imperfections which I have mentioned, nor many others to which the hypothetical eye we have been analyzing would be liable. What a fublime idea must we form of Him who has furnished not only the whole human species, but every animal, nay even the vilest insects, with an organ of such curious construction!\*

\* The object of the Translator being not only to display Euler's philosophy, but likewise to exhibit the man as designed by his own pencil, he takes the liberty of presenting the English Reader with the conclusion of this letter, in the Author's own manner and words, transcribed from the original edition of this work. Though a French philosopher and statesman may feel ashamed of the alliance of science to religion, and endeavour to keep it out of sight, it would surely ill become us to follow the example. Let the Author express his own sentiments in his own way.

"But the eye which the Creator has formed is subject to no one of all the impersections under which the imaginary confiruction of the freethinker labours. In this we discover the true reason why infinite wisdom has employed several transparent fubstances in the formation of the eye: it is thereby served against all the defects which characterise every work of man. What a noble subject of contemplation! How pertinent that question of the Psalmist! He who formed the eye, shall he not see? and He who planted the ear, shall He not hear? The eye alone being a master-piece that far transcends the human understanding, what an exalted idea must we form of Him, who has bestowed this wonderful gift, and that in the highest persection, not on man only, but on the brute creation, nay, on the vilest of insects!"—E. E.

of confequence refruct the rough differently, produce an effect and

19th August, 1760.

### LETTER XLIV.

Perfections discoverable in the Structure of the Eye.

THE eye, then, infinitely furpaffes every piece of mechanism which human skill is capable of producing. The different transparent substances of which it is composed, have not only a degree of density capable of causing different refractions, but their sigure is likewise determined in such a manner that all the rays proceeding from one point of the object are exactly collected in one and the same point, whether that object be more or less distant, whether it be situated directly or obliquely with respect to the eye, and though it's rays undergo different refractions.

Were the least change to be made in the nature and figure of these substances, the eye would lose all the advantages which we have been admiring. The strength of our sight is exactly proportioned to the extent of our necessities; and far from complaining that objects too remote escape this organ, we ought, on the contrary, to consider it as one of the most precious gifts of the Supreme Being.\*

It

<sup>\*</sup> Mr. Euler's idea is ingenious, that the three pellucid fubstances of which the eye is composed serve to correct the unequal refrangibility of the rays of light, and produce a perfect picture on the retina. Unfortunately this perfection is merely ideal, nor is the eye an achromatic intrument. A very simple experiment will evince the truth of this remark. Make two parallel black strokes adjacent to each other, on a bit of paper; thut the one eye, and

It must be farther remarked, that in order to see objects distinctly, it is not fusicient that the rays which come from one point should be collected in another. It is likewise necessary, that the point of re-union should fall precisely on the retina; if it fell either fhort of, or beyond it, vision would become confused. Now, if for a certain distance of objects, this point of union fall upon the retina, those of more distant objects would fall in the eye short of the retina; and those of nearer objects would fall beyond the eye. In either case there would be a confusion in the image painted on the retina-

The eyes of every man, therefore, are constructed for a certain distance. Some persons see distinctly only fuch objects as are very near to their eyes; we call them Myops, that is, short-fighted. Others, on the contrary, named Prefbytes, fee distinctly objects only which are very distant. And those who see distinctly objects at a moderate distance, are said to have good eyes. Both the other two, however, have the power of contracting or dilating the globe of the eye to a certain degree, and thereby of bringing

hold the paper about half a foot from the other, in a firong light, and bring it gradually nearer; at a certain diftance the strokes will appear fringed with rainbow-colours. The Roman characters III or IIII, on the dial-plate of a watch, will, answer still better. But though the eye is not constructed with mathematical accuracy, that organ is adapted, with fufficient nicety, for all the ordinary purposes of life. They mistake extremely the views of nature, who look for perfection in her works: she is, in general, sparing in her favours, and referves exquisite skill for extraordinary occafions. - E. E. nes and a regard to tid a no realto fions of the nearest

nearer, or of removing, the retina, which enables them, likewife, to fee clearly, objects a little more or less distant; this, undoubtedly, greatly contributes to render the eye more perfect, and it cannot surely be ascribed to chance merely.

Those who have good eyes, derive most advantage from their structure, as they are thus in a condition to see distinctly, objects very distant, and very near; but this never exceeds a certain bound. There is, perhaps, no one who can see at the distance of an inch, and, consequently, still less at a smaller distance. If you hold a writing close to your eyes, you will see the characters but very confusedly. This is all I presume to offer, on a subject of such high importance.

21st Aug. 1760.

# LETTER XLV.

Of Gravity, considered as a general Property of Body.

AVING now treated of light, I proceed to the confideration of a property common to all bodies, that of gravity. We find that all bodies, folid and fluid, fall downward, when they are not fupported. I hold a ftone in my hand; if I let it go, it falls to the ground, and would fall ftill farther, were there an aperture in the earth. While I write, my paper would fall to the ground, were it not fupported by the table. The fame law applies to every Vol. I.

body with which we are acquainted. There is not one that would not fall to the ground, if it were not fupported, or stopped by the way.

The cause of this phenomenon, or of this propensity of all bodies, is denominated gravity. When it is said, that bodies are heavy, or possess gravity, we mean, that they have a propensity to fall downward, and actually would fall, if we remove what before supported them.

The ancients were little acquainted with this property. They believed that there were bodies which had, naturally, a tendency to rife, fuch as fmoke and vapours; and fuch bodies they termed light, to diftinguish them from those which have a tendency to fall. But it has been discovered, by experiment, that it is the air which raises these substances aloft; for in a space void of air, it is well known, by means of the air-pump, that fmoke and vapours defcend as well as stone, and that these substances are, of their own nature, heavy, like others. When, therefore, they rife into the air, the fame law acts upon them which acts upon a log of wood plunged into the water. Notwithstanding it's gravity, it springs up, as foon as you leave it to itself, and fwims, because it is not fo heavy as water; and, in virtue of a general rule, all bodies rife in a fluid of more gravity than themselves.

If you throw a piece of iron, of copper, of filver, and even of lead, into a vessel full of quicksilver, they swim on the surface, and if you force them down, they re-ascend when left to themselves. Gold

alone

alone finks, because it is heavier than quicksilver. And, fince there are bodies which rise in water, and in other sluids, notwithstanding their gravity, for this reason merely, that they are not so heavy as water, or those other sluids; it is not at all surprizing, that certain bodies, less weighty than air, such as smoke and vapours, should rise in it.

I have already remarked, that air itself possesses gravity, and that by means of this gravity, it supports the mercury in the barometer. When, therefore, it is affirmed, that all bodies are heavy, it is to be understood, that all bodies, without a single exception, would fall downward in a vacuum. I might venture to add, that they would fall with an equal degree of rapidity; for a feather and a piece of gold descend with equal velocity in an exhausted receiver.

It might be objected to this general property of body, that a shell, discharged from a mortar, does not at once fall to the ground, like a stone, which I let drop from my hand, but mounts into the air. It cannot, however, be inferred, that the shell has no gravity; for it is evident, that the strength of the powder hurls the bomb aloft, and but for this, it would, without doubt, immediately fall to the ground. And we see, in fact, that it does not continue always to ascend, but as soon as the force, which carries it upward, is exhausted, down it comes with a rapidity, that crushes every thing it meets, a sufficient proof of it's gravity.

When, therefore, it is affirmed, that all bodies are heavy, no one means to deny that they may be N 2 ftopped,

ftopped, or that they may be thrown aloft; but this is effected by an external power, and it remains indubitably certain, that all bodies whatever, as foon as left to themselves, at rest, or without motion, will assuredly fall when no longer supported. There is a cellar under my apartment, but the stoor supports me, and preserves me from falling into it. Were the sloor suddenly to crumble away, and the arch of the cellar to tumble in at the same time, I must infallibly be precipitated into it, because my body is heavy, like all other bodies with which we are acquainted. I say, with which we are acquainted, for there may, perhaps, be bodies destitute of weight; such as, possibly, light itself, the elementary sire, the electric shuid, or that of the magnet.\*

Except these bodies, the gravity of which is not

\* I must once more take the pious Euler out of the hands of the quondam Marquis, and let him speak for himself. The instance which the Author adduces, of bodies that, possibly, are desistute of gravity, is one taken from divine Revelation, that of the angels. "Such," says he, "as the bodies of angels, which have formerly appeared to men. A body, like this, would not fall downward, though the floor were suddenly to be removed from under it, but would move as firmly through the air, as on the earth." It is amusing to observe, with what solicitude the Parisian Annotator keeps clear of every thing that savours of religion. He seems apprehensive, that a single drop of water from Scripture, would contaminate the whole mass of philosophy. His terror is, with a little variation, that of Macbeth.

Will all great Neptune's ocean wash this blood
Clean from my hand? No; this my hand will rather
The multitudinous seas incarnadine,
Making the green one red.

Shakespear.

yet confirmed by experiment, gravity may be confidered as a general property of all the bodies which we know, in virtue of which, they all have a tendency to fall downward, and actually do fo, when nothing opposes their descent.

23d Aug. 1760,

## LETTER XLVI.

# Continuation. Of Specific Gravity.

YOU have just seen, that gravity is a general property of all the bodies with which we are acquainted, and that it consists in the effect of an invincible force, which presses them downward.

Philosophers have warmly disputed, whether there actually exists a power, which acts in an invisible manner upon bodies; or whether it be an internal quality, inherent in the very nature of the bodies, and, like a natural instinct, constraining them to descend. The question amounts to this: If the cause of gravity is to be found in the very nature of every body; or if it exists without it, so that were this extrinsic power to fail in it's operation, the body would cease to be heavy? Before we attempt a solution of this, it will be necessary to examine, more carefully, all the circumstances connected with gravity.

I remark, first, that when you support a body to prevent it's falling, if it rests on a table, it's pressure is equal to the force with which it would tend to fall; and if a thread is affixed to it, by which it may be fuspended, the thread is stretched by that force; in other words, by the gravity of that body; fo that if the thread were not of a certain strength, it would break. We fee, then, that all bodies exercife a degree of force on the obstacles which support them, and prevent their falling, and that this action is precifely the fame as that which would make the body descend, if it were at liberty. When a stone is laid upon a table, the table is pressed by it. You have but to put your hand between the stone and the table, to be fenfible of this force, which may be increased to such a degree as even to crush the hand. This force is called the gravity of the body; and it is clear, that the weight, or the gravity, of every body, fignifies the fame thing, both denoting the force with which that body is preffed downward, whether this force exists in the body itself, or out of it.

We have an idea too clear of the weight of bodies, to make it necessary to dwell longer on the subject. I only remark, that when two bodies are joined together, their weight too is added, so that the weight of the compound is equal to the sum of the weight of the parts. From this we see, that the weight of bodies may be very different. We have also the certain means of exactly measuring and comparing them, by the help of a balance, which has the property of resting in equilibrium, when the bodies, put in it's two scales, are of equal gravity. In order

to make this comparison, we agree on some sixed measurement, of a certain determinate weight, such as a pound, and, by means of a good balance, all bodies may be weighed, and their gravity ascertained, according to the number of pounds which they contain. A body too great to be put into the scale of a balance may be divided, and the parts being weighed separately, you have only to add the particulars. The weight of a whole house, however large, may be thus ascertained.

You must, no doubt, have frequently remarked, that a finall piece of gold weighs as much as a piece of wood greatly fuperior in fize; a proof that the gravity of bodies is not always regulated by their magnitude; a very fmall body may be of great weight, while a very large one may be light. Every body, then, is fusceptible of two measurements, entirely different from each other. The one determines it's magnitude or extent, called likewife it's fize; this measurement belongs to the province of geometry, which teaches the method of meafuring the magnitude or extent of bodies. The other mode of meafurement, by which their weight is determined, is totally different, and ferves to diffinguish the nature of the different fubstances of which bodies are formed.

You can eafily conceive feveral maffes of different fubstances, all of the same magnitude, or extent; each, for example, of a cubic sigure, whose length, breadth, and height, shall be a foot. Such a mass, if it be of gold, would weigh 1330 pounds; if of N4 silver,

filver, 770 pounds; if of iron, 500 pounds; and if of water, only 70 pounds; were it of air, it would weigh no more than the twelfth part of a pound. From this you fee, that the different fubstances of which bodies are composed, vary considerably in respect of gravity.

To express this difference, we employ certain terms, which might appear equivocal, if they were not perfectly understood. Thus, when it is faid, that gold is heavier than filver, it is not to be underftood, that a pound of gold is heavier than a pound of filver; for a pound, of whatever fubftance, is always a pound, and has always precifely the fame weight; but the meaning is, that having two maffes of the fame fize, the one gold and the other filver, the weight of the mass of gold will exceed that of the filver. And when it is faid, that gold is 19 times heavier than water, we mean, that having two equal masses, the one of gold, the other of water, that which is of gold will have 19 times the weight of that which is of water. When we thus express ourfelves, we fay nothing of the absolute weight of bodies, we only fpeak by way of comparison, and with a reference always to maffes of an equal fize. Neither is it of importance, whether the fize be great or fmall, provided they be equal.

25th Aug. 1760.

#### LETTER XLVII.

Terms relative to Gravity, and their true Import.

GRAVITY, or weight, feems fo effential to the nature of bodies, that it is almost impossible to form the idea of a body divested of this quality. And it's influence is so universal, in all our operations upon body, that we must, in every instance, pay attention to it's gravity, or weight. As to our own persons, whether we stand, sit, or lie, we continually feel the effect of the gravity of our own body: we could never fall, if the body were not, as well as all it's parts, endowed with this force. Language itself is regulated according to this property of bodies. The place toward which a body tends in it's descent, we term low; and the opposite direction from the body, we term bigh.

It must be remarked, that when a body, in falling, is at perfect liberty, it always descends in a straight line, pursuing which, it's direction is said to be downward. This line is likewise called vertical, by which term we always mean a straight line, drawn from high to low; and if we conceive this line produced upward, till it reaches heaven, we call that point in the heavens our zenith, an Arabian word, denoting that point in the heavens which is directly over our head. You comprehend, then, that a vertical line, is that straight line in which a body falls, when no longer supported. When you assix a thread

to any body, holding it fast at the other end, that thread will be stretched out into a straight line, and that line will be vertical. Masons employ a small cord, with a leaden ball at one end, which they call a plummet, to direct the perpendicularity of the walls which they raise; for these, to be solid, must be vertical.

All the floors of a house ought to be so level, that the vertical line shall be perpendicular to them; the floor, in that case, is said to be horizontal; and you will please to remember, that a horizontal plane is always that to which the vertical line is perpendicular. When you are in a perfect plane, bounded by no mountain, it's extremities are termed the horizon, a Greek word, which signifies the boundary of sight; and this plane then represents a horizontal plane, just as the surface of a lake.

We make use of still another term to express what is horizontal. We say that such a surface or line is level. We likewise say, that two points are on the level, when a straight line, passing through these two points, is horizontal, so that the vertical, or plumb line, shall be perpendicular to it. But two points are not on the level, when the straight line, drawn through these points, is not horizontal; for then one of them is more elevated than the other.

This is the case with rivers; their surface has a declivity; for were it horizontal, the river would be stagnant, and run down no longer, whereas all rivers are continually slowing toward places less elevated. There are instruments, by means of which we can ascertain,

afcertain, whether two points are on the fame level, or which is the higher, and by how much. This instrument is called a *level*, and the application of it is called the art of levelling.

Were you to draw a straight line from any point, in your apartment at Berlin, to a given point in your apartment at Magdeburg, you might, by means of fuch an instrument, ascertain, whether this line were horizontal, or whether one of these points were more or less elevated than the other. I believe the point at Berlin would be more elevated than that at Magdeburg: and I found this opinion on the course of the rivers Sprée, Havel, and Elbe. As the Sprée runs into the Havel, it must, of course, be higher; and, for the fame reason, the Elbe must be lower than the Havel: Berlin, therefore, stands higher than Magdeburg, provided you compare two points at an equal degree of elevation from the ground; for were a straight line to be drawn from the street pavement at Berlin to the pinnacle over the dome at Magdeburg, that line would perhaps be horizontal.

Hence you see how useful the art of taking levels is, when the conducting of water is concerned. For as water can run only from a more to a less elevated situation, before digging a canal, you must be well assured, that one of the extremities is more elevated than the other, and this is discovered by taking the level.

In building a city, the streets should be so disposed, as that, by means of a declivity on one side, the water may run off. It is otherwise in the construc-

tion of houses, the floors of which should be perfectly horizontal, and without the smallest declivity, because there is no water to be discharged, except in
the floors of stables, which are constructed with a
gentle declivity. Astronomers take great pains to
have the floors of their observatories perfectly level,
to correspond with the real horizon in the heavens.
The vertical line, produced upward, marks the zenith.

27th August, 1760.

#### LETTER XLVIII.

Reply to certain Objections to the Earth's Spherical Figure, derived from Gravity.

YOU know well that the figure of the earth is nearly that of a globe. It has, indeed, been demonstrated, that it's form is not perfectly spherical, but somewhat flattened toward the poles. The difference, however, is so trifling, that it does not at all affect the object I have in view. Neither does the difference of mountain and valley excite any solid objection to it's globular figure; for it's diameter being 1720 German miles,\* whereas the highest mountains being scarcely half a mile† in height, sink into nothing, compared to this prodigious mass.

The ancients had a very imperfect notion of the

<sup>\* 7900</sup> miles English.

<sup>†</sup> About 12,000 feet, or 2 3 miles English.

real figure of the earth. It was in general confidered as a huge maffy fubstance A B C D (plate II. fig. 11.) flattened above as A B, and covered partly with earth, partly with water. According to their idea, the furface A B alone was habitable; and it was impossible to go beyond the points A and B, which they confidered as the extremities of the world. When, in the progress of discovery, it was found that the earth was nearly fpherical, and univerfally habitable, fo that there were upon the globe fpots diametrically opposite to us, the inhabitants of which are therefore called our antipodes, because their feet are turned directly toward ours; this opinion met with fuch violent contradiction, that certain fathers of the church represented it as a dreadful herefy, and thundered out anathemas against all who believed in the existence of the antipodes. A man, however, would now pass for an idiot, who would call it in question; especially since the opinion has been confirmed by the experience of navigators, who have actually more than once failed round the globe. But another difficulty here prefents itself, the folution of which must affist us in discovering the real direction of gravity.

If the circle A B (plate II. fig. 12.) fay they, represents the earth, and we are at A, our antipodes will be diametrically opposite, at B. As we, then, have the head upward, and the feet downward, our antipodes must have the feet upward and the head downward, supposing these words to indicate the same direction as when we pronounce the same words

words at the place where we are. For navigators who have made the circuit of the globe, observe, that their head and feet had throughout maintained the same position relatively to the surface of the terrestrial globe.

Some perfons whom this phenomenon embarraffed, formerly thought of explaining it, by the comparison of a globe, over the furface of which you
fee slies and other infects crawl on the under as well
as the upper part. But they did not consider that
the infects on the dependent surface adhere to it by
their claws, and, without this assistance, would prefently fall off. The antipode, then, must have his
shoes furnished with hooks to hold him fast to the
furface of the earth: but though he has none, he
falls not any more than we do. Besides, as we imagine ourselves to be on the uppermost surface of the
earth, the antipode has the same idea of his situation,
and considers us as undermost.

But the whole phenomena are eafily accounted for, on the hypothesis which experience has demonstrated, that the direction of gravity is sensibly perpendicular to the surface of the earth, at every point of that surface; that it varies at these different points; and that at those which are antipodes to each other, it must be exactly opposite. The terms upward and downward, therefore, do not express an invariable direction, but the direction of gravity, wherever it is. Our antipodes have their heads downward only with relation to us, but not with relation to themselves; they, as well as we, are in the position which



the power of gravity constrains them to preserve; and that position is similar relatively to the surface of the earth. You had, undoubtedly, no need of this explanation; but there was a time, and it is not long elapfed, when it would have been necessary even to perfons who were then honoured with the appellation of the learned.

28th August, 1760.

## LETTER XLIX.

True Direction and Action of Gravity relatively to the Earth.

HOUGH the furface of the earth is unequal, because of the mountains and valleys which overspread it, it is, however, perfectly level wherever there is fea; the furface of water being always horizontal, and the vertical line, in the direction of which bodies fall, being perpendicular to it. If, then, the whole globe were covered with water, at whatever fpot of the furface a person was, the vertical line would be perpendicular to the furface of the water.

Thus, the figure ABCDEFGHI (plate III. fig. 1.) reprefenting the earth, it's furface being every where horizontal; at A the line a A will be vertical; at B the line b B; at C the line c C; at D the line d D; at F the line f F; and fo of the rest. Now, at every place the vertical line determines what is to be denominated upward or downward; to persons at A,

then,

then, the point A is downward, and the point a upward: and to perfons at F, the point F will be downward, and the point f upward, and fo for every other spot on the surface of the earth. All these vertical lines a A, b B, c C, d D, &c. are likewise named the directions of gravity, or weight, because bodies universally descend in the direction of these lines; thus a body left to itself at g, would fall in the direction of the line g G. Hence it is evident, that bodies, universally, must fall toward the earth, and that perpendicularly to the surface of the earth, or rather of the water, if it were water.

At whatever place of the earth, therefore, you may happen to be, as bodies fall there toward it's furface, we call downward that which is directed toward the earth, or is nearest to it; and upward what is placed in the opposite direction, or is farthest from the earth: and, univerfally, men having their feet pressed to the earth, their feet will be downward, and their heads upward. If the earth were a perfect globe, all the vertical lines a A, b B, c C, being produced inwardly, would meet at the centre of the globe, which is likewife that of the earth; and for this reason we say that bodies universally tend toward the centre of the earth. Thus, wherever you are placed, when asked, what is downward? the anfwer must be, what approaches nearest to the centre of the earth. In fact, were you to dig a hole in the earth at whatever place, and to continue your labour inceffantly, digging always downward and downward perpendicularly, you would at length

reach the centre of the earth. You will remember how Voltaire used to laugh at the idea of a hole reaching to the centre of the earth, mentioned by Maupertuis. It is true such a project could never be executed, as it would be necessary to dig to the depth of 860 German miles;\* but there is no harm in supposing it, in order to discover what would be the result.

Let us suppose, then, such a hole (plate III. fig. 2.) to be dug at A, and continued beyond the centre of the earth O, the whole length of the diameter, as far as to our antipodes B, and that we were to descend along this aperture. Before arriving at the centre O, and having reached, for example, to point E, the centre of the earth O will there appear downward, and the point A upward; and, unless something fupported us, we fhould fall toward O. But having passed beyond the centre to F, for example, our gravity would then have a tendency toward O; this point, and much more the point A, would appear downward, and the point B upward. Thus the terms upward and downward would fuddenly change their fignification, though we should have passed from A to B, in the direction of a straight line.

As long as we are on the passage from A to O, we are descending; but in going from O to B, we are actually rising, for we are removing from the centre of the earth; our own gravity being always directed toward that point; so that, if we were to fall, whether from E or from F, we should always fall toward

· 3950 miles English.

the centre of the earth. Our antipode at B, if he wanted to pass from B to A, would be in precisely the fame fituation. From B to the centre O he would have to descend; but from O to A it would be all an afcent. These considerations lead us thus to define gravity or weight. It is a power by which all bodies are forced toward the centre of the earth. The fame body which, being at A, is forced in the direction A O, if transported to B, will be forced, by the power of gravity, in the direction BO, which is directly opposite to the other. By the direction of gravity, then, we every where regulate the fignification of the terms upward and downward, rife and defcend, as gravity or weight has a very effential influence on all our operations and enterprifes, and as even our own bodies are animated by it to fuch a degree, as univerfally to feel it's effects.

29th August, 1760.

## LETTER L.

Different Action of Gravity with respect to certain Countries and Distances from the Centre of the Earth.

OU are now fensible that all bodies are forced directly towards the centre of the earth, and perpendicularly to it's furface by their gravity: the perpendicular lines at the furface of our globe are accordingly considered as the directions of the power of gravity.

With

With strict propriety is the term power applied to gravity, as every thing capable of putting a body in motion is expressed by that name. Thus we ascribe power to horses, because they are able to draw along a chariot; or to the current of a river, or to the wind, because by their means mills may be put in motion. There can be no doubt, therefore, that gravity is a power, as it forces bodies downward: and we are abundantly sensible of the effect of this power, by the pressure which we feel when we carry a load.

Now, in every power two things are to be confidered: first, the direction in which it acts, or forces along bodies; and, secondly, it's quantity, which is estimated by the effect it produces. As to the direction of gravity, it is sufficiently known, for we are fure that it forces all bodies toward the centre of the earth, or, which amounts to the same thing, that it acts perpendicularly to the surface of our globe.

It remains, therefore, that we examine it's quantity. This power is always determined by the weight of every body,\* and as bodies differ greatly with refpect

\* In order to form an exact idea of the weight of a body, it must be recollected, that gravity impresses, or has a tendency to impress, on every particle of bodies, in an instant, a certain velocity, with which they would fall, if they were not supported; and that, abstracting the influence of the air, this velocity would be the same for each of the particles of bodies, whatever be their substance. This being laid down, we must understand by the weight of a body the effort necessary to prevent it from falling; and it is evident that, in order to this, it is necessary to destroy the velocity

fpect to weight, those which are heaviest are likewise forced downward with the greatest violence. It has been asked, Whether the same body, transported to a different place of the globe, preserves always the same weight? I speak of bodies which lose nothing by evaporation. It has been demonstrated, by undoubted experiments, that the same body weighs somewhat less toward the equator, than toward the poles of the earth.

It will readily occur to you, that it is impossible to ascertain this difference by the exactest balance, because the standard weights employed for determining the weight of matter in bodies, undergo the

which gravity has impressed on every particle. This effort must, therefore, be equal to the sum of the velocities of all these particles. Hence it may be easily concluded, that bodies the most compact, that is, those whose particles are the closest, and which, consequently, contain a greater number of them in the same bulk, will weigh more than others, because the weight being the sum of the velocities impressed on each particle, that sum must be so much greater, as there are more material particles contained in the mass of the body.

From what I have just said, "we see the necessity of carefully distinguishing between the effect of gravity and that of weight: "the former is the power of transmitting, or a tendency to transmit into every particle of matter a certain velocity, which is ab"folutely independent on the number of material particles; and the second is the effort which must be exercised to prevent a given mass from obeying the law of gravity. Weight, accordingly, depends on the mass, but gravity has no dependance at all upon it."

I thought myfelf obliged to enter thus minutely into the subject, as the notions commonly entertained of it are not very exact.

-F. E.

fame variation. Thus a mass, which with us might weigh 100 pounds, being transported to the equator, would still nominally be 100 pounds weight, but the effort will be somewhat less than here. This variation has been discovered by the effect itself of the power of gravity, which is the velocity of the descent, for it is found that the same body, under the equator, does not descend with so great velocity as in high latitudes. It is certain, therefore, that the same body, being transported to different places of the earth, undergoes a little change as to weight.

Let us now return to the aperture made in the earth through it's centre; it is clear, that a body at the very centre must entirely lose it's gravity, as it could no longer move in any direction whatever, all those of gravity tending continually toward the centre of the earth. Since, then, a body has no longer gravity at the centre of the earth, it will follow that, in descending to this centre, it's gravity will be gradually diminished; and we accordingly conclude, that a body, penetrating into the bowels of the earth, lofes it's gravity, in proportion as it approaches the centre. You must be sensible, then, that neither the intensity nor the direction of gravity is a confequence from the nature of every body, as not only it's intenfity is variable, but likewife it's direction, which, on passing to the antipodes, becomes quite contrary.

Having travelled, in idea, to the centre of the earth, let us return to it's furface, and afcend to the fummit of the loftiest mountains. We shall observe

there no fensible change in the gravity of bodies, though there is very good reason to believe that the weight of a body diminishes in proportion as it removes from the earth. You have but to imagine a body gradually removing from our globe, till it reached the fun, or one of the fixed stars, it would be ridiculous to think that such a body must fall back to the earth, as it is almost a nothing compared to these stars. Hence, then, it may be concluded, that a body in removing from the earth must undergo a diminution of gravity, which will become smaller and smaller, till at last it wholly disappear.

There are reasons, however, which demonstrate, that a body removed to the distance of the moon, will ftill have fome weight, though 3600 times lefs' than it had on the earth. Let us conceive fuch a body to weigh 3600 pounds on the earth, no one, furely, is capable of fupporting it here; but convey it to the distance of the moon, and I shall engage to fupport it with one of my fingers, for then it will weigh only one pound; and farther removed, would weigh still less. We are certain, therefore, that gravity is a power which forces all bodies toward the centre of the earth, that this power acts with the greatest force at the furface of the earth, and is diminished in proportion as it removes from thence, whether by penetrating toward the centre, or rifing above the furface of the globe. I have ftill much to fay on this fubject.

30th August, 1760.

#### LETTER LI.

# Gravity of the Moon.

I HAVE faid that a terrestrial body, placed at the distance of the moon, would be reduced to the 3600th part of it's weight, or, in other words, would be forced toward the centre of the earth with a power 3600 times less than it has at the furface of the globe. This power, however, would be sufficient to make it descend to the earth, if it were no longer supported. It is true we are incapable of proving this by any experiment, as no means exist of raising ourselves to such a height. There is, however, a body at that height, the moon: she must, therefore, be subject to this effect of gravity, and yet we see she does not fall to the earth.

To this I answer, that if the moon were at rest, she would certainly fall, but the rapid motion which carries her along prevents her falling. There are experiments which prove the solidity of this answer. A stone dropped from the hand, without having any motion impressed upon it, falls immediately, in the direction of a straight vertical line; but if you throw this stone, impressing on it a motion which forces it out of that direction, it does not fall immediately downward, but moves in a curve line before it reaches the earth, and this will appear more sensibly in proportion to the velocity impressed upon it.

A cannon ball, discharged in a horizontal direc-O 4 tion, tion, does not come to the earth till it has got to a confiderable distance; and were it fired from the top of a high mountain, it might, perhaps, sly several miles before it reached the ground. If the direction of the cannon is farther elevated, and the quantity and strength of the powder increased, the ball will be carried much farther. This might be carried so far, that the ball should not light till it had reached the antipodes: nay, farther still, till it should not fall at all, but return to the place where it was shot off, and thus perform a new tour round the globe. It would thus be a little moon, making it's revolutions round the earth like the real moon.

You will now please to reflect on the height of the moon, and the prodigious velocity with which she moves, and you will no longer be surprised that she should not fall to the earth, though forced by gravity toward it's centre. There is another reflection which will place this in a clearer light. We have only to consider the path described by a stone thrown, or a cannon ball shot off, in an oblique direction. It is always a curve, such as represented in the annexed figure (plate III. fig. 3).

Let A be the fummit of a mountain from which the cannon ball is fired off, which, after having moved in the direction A E F B, falls to the ground at B; and the path which it describes is a curve line. I remark, then, that if the ball were not heavy, that is, if it were not forced toward the earth by the power of gravity, it would not fall, though left to itself, as gravity is the only cause of it's descent; much

much less, being fired off at A, as represented in the figure, would it ever fall to the ground. Hence we see, it is gravity that brings it down to the ground, after having described the curve A E F B; gravity, therefore, directs it's path in the curve A E F B; and if it were destitute of gravity, the ball would not describe a curve, but proceed forward in the direction of the straight line A C, the direction in which it was fired off.

This being laid down, let us attend to the moon, which affuredly does not move in a ftraight line; her path must of necessity be a curve, as she always preserves nearly the same distance from us, and that curve almost a circle, such as you would describe round the earth, with a radius equal to the moon's distance.

It is very reasonable to demand, Why the moon does not move in a straight line? But the answer is obvious; for as gravity occasions the curve direction of the path pursued by a stone thrown, or a cannon ball fired off, there is good ground for maintaining, that gravity acts likewise upon the moon, forcing her toward the earth; and that this gravity occasions also the curve direction of her orbit. The moon, then, has a certain weight, she is, of consequence, forced toward the earth; but this weight is 3600 times less than it would be at the surface of the earth. This is not merely a probable conjecture, but a truth demonstrated. For this gravity being supposed, we are enable to determine, on the most established ma-

thematical

thematical principles, the path which the moon must pursue; and this is found persectly to agree with that in which she actually does move; and this is a complete demonstration of the truth of the affertion.

1st September, 1760.

## LETTER LII.

Discovery of universal Gravitation by Newton.

GRAVITY, then, or weight, is a property of all terrestrial bodies, and it extends, likewise, to the moon. It is in virtue of gravity that the moon presses toward the earth; and gravity regulates her motion just as it directs that of a stone thrown, or of a cannon ball fired off.

To Newton we are indebted for this important difcovery. This great English philosopher and geometrician, happening one day to be lying under an apple-tree, an apple fell upon his head, and suggested to him a multitude of reslections. He readily conceived that gravity was the cause of the apple's falling, by overcoming the force which attached it to the branch. Any person whatever might have made the same reslection; but the English philosopher pursued it much farther. Would this force have always acted upon the apple, had the tree been a great deal higher? He could entertain no doubt of it.

But had the height been equal to that of the moon?

Here

Here he found himself at a loss to determine whether the apple would fall or not. In case it should fall, which appeared to him, however, highly probable, since it is impossible to conceive a bound to the height of the tree, at which it would cease to fall, it must still have a certain degree of gravity forcing it toward the earth; therefore, if the moon were at the same place, she must be pressed toward the earth by a power similar to that which would act upon the apple. Nevertheless as the moon did not fall on his head, he conjectured that motion might be the cause of this, just as a bomb frequently slies over us, without falling vertically.

This comparison of the motion of the moon to that of a bomb, determined him attentively to examine this question; and, aided by the most sublime geometry, he discovered, that the moon in her motion was subject to the same laws which regulate that of a bomb, and that if it were possible to hurl a bomb to the height of the moon, and with the same velocity, the bomb would have the same motion as the moon, with this difference only, that the gravity of the bomb at such a distance from the earth, would be much less than at it's surface.

You will fee, from this detail, that the first reafonings of the philosopher on this subject were very simple, and scarcely differed from those of the clown; but he soon pushed them far beyond the level of the clown. It is, then, a very remarkable property of the earth, that not only all bodies near it, but those also which are remote, even as far as to the distance of the moon, have a tendency toward the centre of the earth, in virtue of a power which is called gravity, and which diminishes in proportion as bodies remove from the earth.

The English philosopher did not stop here. As he knew that the other planets are perfectly similar to the earth, he concluded, that bodies adjacent to each planet possess gravity, and that the direction of this gravity is toward the centre of such planet. This gravity might be greater or less there than on the earth; in other words, that a body of a certain weight with us, transported to the surface of any planet, might there weigh more or less.

Finally, this power of gravity of each planet extends, likewife, to great distances around them; and as we fee that Jupiter has four fatellites, and Saturn five, which move round them just as the moon does round the earth, it could not be doubted, that the motion of the fatellites of Jupiter was regulated by their gravity toward the centre of that planet; and that of the fatellites of Saturn by their gravitation toward the centre of Saturn. Thus, in the fame manner as the moon moves round the earth, and their respective satellites move round Jupiter and Saturn, all the planets themselves move round the fun. Hence Newton drew this illustrious and important, conclusion: That the fun is endowed with a fimilar property of attracting all bodies toward it's centre, by a power which may be called folar gravity.

This power extends to a prodigious distance around him, and far beyond all the planets, for it is this power which modifies all their motions. The fame great philosopher discovered the means of determining the motion of bodies from the knowledge of the power by which they are attracted to a centre; and as he had discovered the powers which act upon the planets, he was enabled to give an accurate description of their motion. In truth, before he arose, the world was in a state of profound ignorance respecting the motion of the heavenly bodies; and to him alone we are indebted for all the light which we now enjoy in the science of astronomy.

It is aftonishing to think how much of their progress all the sciences owe to an original idea so very simple. Had not Newton accidentally been lying in an orchard, and had not that apple by chance fallen on his head, we might, perhaps, still have been in the same state of ignorance respecting the motions of the heavenly bodies, and a multitude of other phenomena depending upon them.\* This subject, undoubtedly, is altogether worthy of your attention, and shall therefore be resumed in a future letter.

3d September, 1760.

<sup>\*</sup> Newton was asked one day, How he had discovered the system of the universe? By continually thinking upon it, replied he. This anecdote has a greater air of probability than the story of the apple.—F. E.

### LETTER LIII.

Continuation. Of the mutual Attraction of the heavenly Bodies:

THE Newtonian fystem, you will easily believe, made at first a great noise, and with good reason, as no one had hitherto hit upon a discovery so very fortunate, and which disfused, at once, such clear light over every branch of science. It has been expressed by several names, of which it is proper you should be informed, because it is frequently the subject of conversation.

It has been denominated, the fystem of universal gravitation; for Newton maintained, that not only the earth, but all the heavenly bodies, in general, are endowed with this property, of attracting those which surround them, with a power similar to that of weight, or gravity: hence is derived the term Gravitation. This power is, however, totally invisible; for we see nothing acting upon bodies, and pressing them toward the earth, and still less toward the heavenly bodies.

The loadstone, by which iron and steel are attracted, without our being able to discern the cause, presents a phenomenon somewhat similar. Though it be now certain, that this is produced by a substance extremely subtile, which penetrates through the pores of the loadstone and of the iron, it may, however, be affirmed, that the loadstone attracts iron, and that iron

iron is attracted by it, provided this manner of speaking does not exclude the true cause. It may likewise be affirmed, then, that the earth attracts all bodies that are near it, nay those which are at very great distances; and we may consider the weight, or gravity, of bodies, as the effect of the attraction of the earth, which acts even upon the moon.\*

Again, the fun, and all the planets, are endowed with a fimilar power of attraction, which extends to all bodies. In conformity to this manner of fpeaking, we fay, that the fun attracts the planets, and that Jupiter and Saturn attract their respective fatellites; hence Newton's system has likewise been denominated, the system of Attraction. As there can be no doubt that bodies very near the moon must likewise be pressed to it by a power similar to gravity, it may likewise be affirmed, that the moon, too, attracts adjoining bodies.

It was natural to suppose, that this attraction of the moon should extend as far as the earth, though it must be, undoubtedly, very feeble, as we have seen

<sup>\*</sup> So far is the existence of a magnetic fluid from being undeniable, that it is highly improbable, if not absurd. The various phenomena of magnetism may clearly be derived from two laws, or general facts; than which a greater simplicity can hardly be expected. If we recur to the agency of a fluid, we must gratuitously bestow on it a number of properties; and, after all, we shall find it extremely difficult, I might say, impossible, to preserve consistency in our complicated hypothesis; nor shall we ever be able, from our assumptive principles, to account for the facts observed. Such, at least, has been the sate of the speculations hitherto offered on the subject of magnetism.—E, E.

that of the earth upon the moon to be; now, the fame philosopher has placed this, also, beyond the reach of doubt, by demonstrating that the flux and reflux of the waters of the sea, of which I shall take occasion to speak afterwards, are caused by the attraction of the moon. It can no longer be doubted, therefore, that Jupiter and Saturn are reciprocally attracted by their respective satellites; and that the fun itself is subject to the attraction of the planets, though this attractive power be exceedingly small.

This is the origin of the fystem of universal attraction, in which it is maintained, and with good reason, that not only does the sun attract the planets, but is reciprocally attracted by each of them; nay, that all the planets exert their attractive power upon each other. The earth, then, is attracted, not only by the sun, but also by all the other planets, though their power be almost imperceptible, compared to that of the sun.

You will easily comprehend, that the motion of a planet, which is attracted not only by the fun, but by the other planets, in however small a degree, must be somewhat different from what it would have been, were it attracted by the sun only; and that, consequently, the attractions of the other planets must cause some small derangement of that motion. Now these derangements are, likewise, consirmed by experience; and this has carried the system of universal attraction to the highest possible degree of certainty, so that no one now presumes to dispute it's truth.

I must likewise remark, that comets, too, are subject to this law; that they are principally attracted by the fun, whose action regulates their motion; but that they, likewise, feel the attractive power of all the planets, especially when they are not very diftant from them. It is a general rule, as we shall fee afterwards, that the attraction of all the heavenly bodies diminishes in proportion to the distance, and increases in proportion to the nearness. Now, comets, likewife, are endowed with a power, by which other bodies are attracted toward them, and fo much the more fenfibly, as they approach nearer. When, therefore, a comet passes somewhat more closely to a planet, it may derange the motion of that planet by it's attractive power; and it's own will likewise be diffurbed by that of the planet. These consequences are verified by real observation.

Examples might be adduced to prove, that the motion of a comet has been deranged by the attraction of the planets, near which it happened to pass,\*

\*The comet of 1682, which should have re-appeared in 1757, underwent, from the attractive powers of Jupiter and Saturn, near which it passed, a considerable derangement, which retarded it's appearance nearly two years. Mr. Clairant calculated, theoretically, the perturbations which it's motion must have suffered, and predicted the return of that comet, with a degree of exactness, which constitutes a convincing proof in favour of the system of gravitation. There was, however, an error of two months. But Mr. de la Place has since demonstrated, that it would have been much less, had we then been able to calculate the perturbations of Jupiter and Saturn, with as much exactness as it now can be done.—F. E.

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and that the motion of the earth, and of the other planets, has already undergone fome derangement, from the attraction of comets.

The fixed ftars being bodies fimilar to the fun, are likewise endowed, no doubt, with an attractive power, but their enormous distance prevents our feeling any sensible effect from it.

5th Sept. 1760.

#### LETTER LIV.

Different Sentiments of Philosophers, respecting universal Gravitation. The Attractionists.

T is established, then, by reasons which cannot be controverted, that an universal gravitation pervades all the heavenly bodies, by which they are attracted toward each other; and that this power is greater in proportion to their proximity.

This fact is incontestable, but it has been made a question, Whether we ought to give it the name of impulsion, or attraction? The name, undoubtedly, is a matter of indifference, as the effect is the same. The astronomer, accordingly, attentive only to the effect of this power, gives himself little trouble to determine, whether the heavenly bodies are impelled toward each other, or whether they mutually attract one another: and the person, who examines the phenomena only, is unconcerned, whether the earth at-

tracts

tracts bodies, or whether they are impelled toward it, by fome invisible cause.

But, in attempting to dive into the mysteries of nature, it is of importance to know, if the heavenly bodies act upon each other by impulsion, or by attraction; if a certain subtile invisible matter impels them toward each other, or if they are endowed with a secret, or occult, quality, by which they are mutually attracted? On this question philosophers are divided. Some are of opinion, that this phenomenon is analogous to an impulsion; others maintain, with Newton, and the English in general, that it consists in attraction.

It must be observed, that the terms attract, and draw, are not perfectly synonymous; that, accordingly, it is not to be supposed, there is an intermediate body between the sun and the earth.

The English, and those who have adopted the same opinion, explain it in this manner. They maintain, that the quality of mutual attraction is proper to all bodies; that it is as natural to them as magnitude, and that it is a satisfying solution of the question, That the Creator willed this mutual attraction of bodies. Had there been but two bodies in the universe, however remote from each other, they would have had, from the sirst, a tendency toward each other, by means of which they would have, in time, approached and united. Hence it sollows, that the greater a body is, the more considerable is the attraction which it exerts upon others; for, as this

quality is effential to matter, the more of it any body contains, the greater is it's attractive force.

As the fun, therefore, confiderably furpaffes all the planets in magnitude, it's attractive force must be much greater than theirs. They likewise remark, that the mass of Jupiter, being much greater than that of the earth, the attractive force which he exercises over his fatellites, is much more powerful than that with which the earth acts upon the moon.

According to this fystem, the gravity of bodies on the earth, is the result of all the attractions exercised upon them by the particles of our globe; and if it contained more matter than it actually does, it's attraction would become more powerful, and the gravity of bodies would be increased. But if, on the contrary, the mass of the earth should happen, by some accident, to be diminished, it's attractive force, too, would be diminished, as well as the gravity of bodies, at it's surface.

It has been objected to these philosophers, that, on their hypothesis, any two bodies, whatever, at rest, for instance, on a table, must attract each other, and, consequently, approach. They admit the consequence, but they insist, that, in this case, the attraction would be too small to produce any sensible esfect; for, if the whole mass of the earth, by it's attractive force, produces in every body, only that esfect which we perceive in the weight of a body, a mass many millions of times smaller than the earth, will produce an essect as many times smaller. It must readily be admitted, that if the weight of a body became many millions of times less, the effect of gravity upon it must be reduced to almost nothing: attraction, therefore, cannot be perceptible, except in bodies of very great magnitude. The partizans of the system of gravitation, therefore, are not vulnerable on this side, and they produce, in support of their opinion, an experiment made in Peru, by the French academicians,\* in which they perceived the effect of a slight attraction of a prodigious mountain on adjacent bodies. In adopting, therefore, the system of attraction, we need to be under no apprehension of it's leading us to salse consequences; and it has hitherto been always consirmed by the new facts which have been discovered.

7th September, 1760.

### LETTER LV.

Power by which the Heavenly Bodies are mutually at-

YOU are well acquainted with the property of the loadstone, that of attracting iron. You have seen small bits of iron and steel, such as needles, when

\* The academicians fent to Peru, in 1735, to measure a degree of the meridian, observed a deviation of 8" in the plumb-line of their quadrant, occasioned by the attraction of Pichencha, a mountain near the place where they were making their observations. Dr. Maskelyne has more recently made observations for ascertaining the effect of the attraction of the mountains of Scotland.—F. E.

P 3

placed

placed near the loadstone, move to it with a force proportioned to their proximity. As you see nothing that impels them toward the loadstone, we say that the loadstone attracts them, and this phenomenon we call attraction. It cannot be doubted, however, that there is a very subtile, though invisible, matter, which produces this effect, by actually impelling the iron toward the loadstone; but as modes of expression are regulated by appearances, it has become customary to say, that the loadstone attracts iron.

Though this phenomenon be peculiar to the loadftone and iron, it is perfectly adapted to convey an
idea of the fignification of the word attraction, which
philosophers so frequently employ. They allege,
then, that all bodies, in general, are endowed with a
property similar to that of the loadstone, and that
they all mutually attract; but that this effect becomes
not perceptible, unless they are very great, and cannot be perceived when they are small.

However great, for example, a stone may be, it exercises no sensible attraction on other bodies adjacent to it, because it's power is too small. But if it's mass were to increase, and to become many thousands of times greater, it's essect would, at length, become perceptible. It has already been remarked, that, from actual observation, it was found, that a losty mountain in Peru had produced attraction, though, indeed, in a very small degree. A mountain still greater, would produce, therefore, a more sensible attraction; and a body much greater, such

as the whole globe, would attract others with a force proportionably greater; and this force would be precifely, the gravity with which we see that they are actually impelled toward the earth.

According to this fystem, then, the gravity which obliges all bodies to descend, is nothing else but the result of the attraction of the whole mass of the earth. If this mass were greater, or less, the gravity, or weight, of bodies would be proportionably greater or less. Hence it follows, that all the other great bodies in the universe, as the sun, the planets, and the moon, are endowed with a similar attractive power, but greater or less, in proportion as they themselves are so.

As the fun is many thousands of times greater than the earth, his attractive power exceeds that of the earth, so many thousand times. The mass of the moon is calculated to be forty times less than that of the earth: it will follow, that her attractive force is so many times less; and the same rule applies to all the heavenly bodies.

9th September, 1760.

### LETTER LVI.

The same Subject continued.

IN virtue of the fystem of attraction, or universal gravitation, each of the heavenly bodies attracts all the rest, and is reciprocally attracted by them.

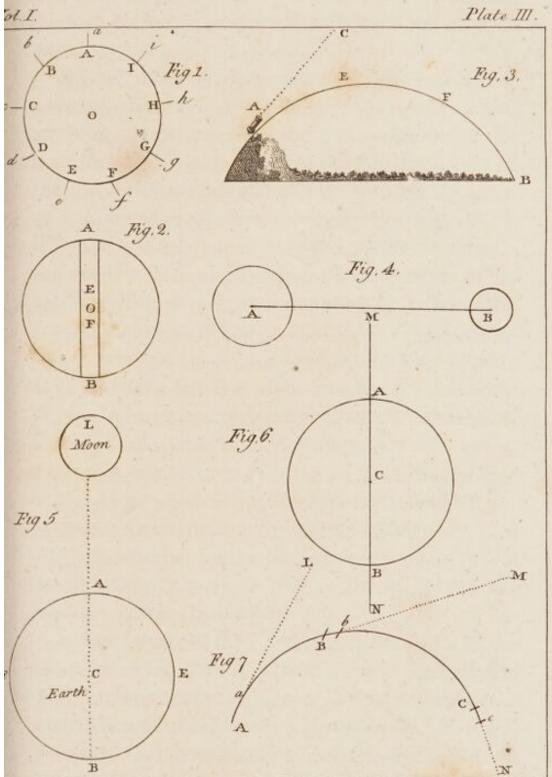
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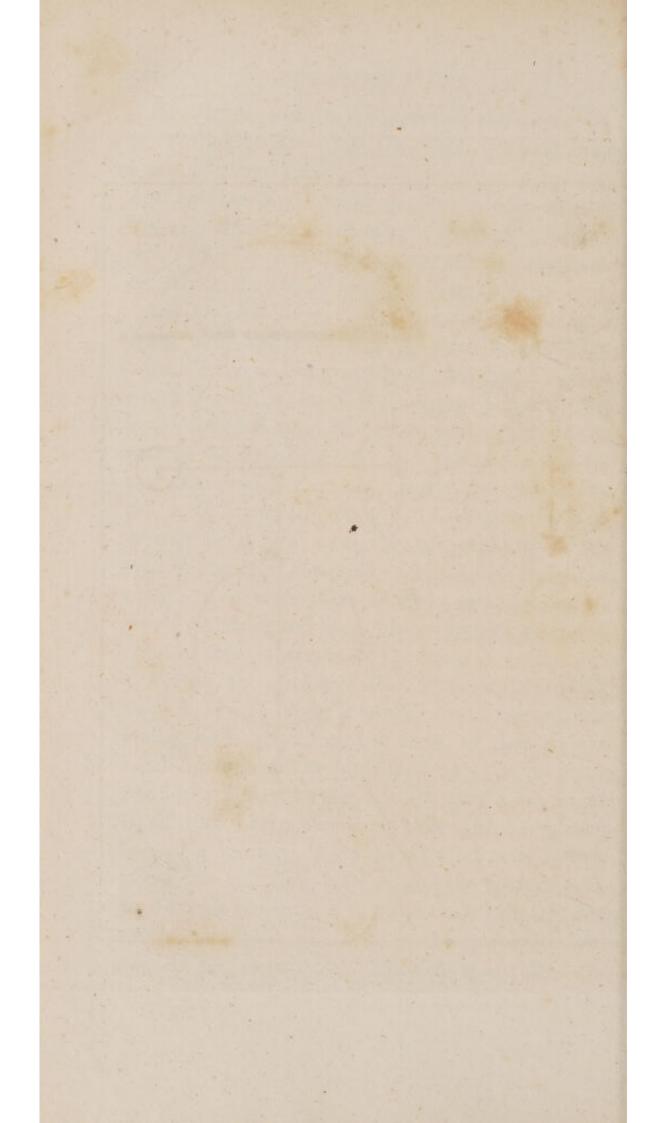
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In order to form a judgment of the force with which these bodies attract the others, we have only to consider two bodies, whose attraction is mutual. And here we must attend to three things; first, to the body attracting; secondly, to the body attracted; and, sinally, to their distance; for on these three circumstances the attractive power depends.

Let A (plate III. fig. 4,) be the attracting body, and B the body attracted; both of them spherical, the heavenly bodies being nearly of this sigure. Take for their distance that of their centres A and B, that is, the straight line A B. Now, with respect to the mass of the attracting body A, it must be remarked, that the greater it is, the greater also will be it's power to attract the body B. Consequently, if A were twice as great as B, this last would feel an attraction, twice as powerful, exercised over it, by the other; if it were three times as great, the effect would be triple, and so on, always supposing the distance of their centres to be the same.

If, then, the earth contained more or less matter than it actually does, it would attract all adjacent bodies, with greater or less force, or their weight would be increased or diminished. And, as the earth itself is attracted by the sun, the same thing might be affirmed as to it, should the mass of that luminary happen to change. As to the attracted body B, supposing the attracting body A, and the distance A B, to continue the same, it is to be remarked, that the greater or smaller it's mass is, the greater or less, also, is the power with which it is attracted toward





ward A. Thus, if the body B were twice as great, it would be attracted toward A, with double the force; if three times greater, with triple the force, and fo on.

In order more clearly to elucidate this remark, we have only to substitute the earth in the place of the attracting body A; then the force with which the body B is attracted, is nothing elfe but the weight of that body. Now, it is demonstrated, that the greater or finaller the body B is, the greater or lefs, alfo, is it's gravity; hence it follows, that while the attracting body A, and the distance, A B continue the same, the attraction which B feels, precifely follows the magnitude of that body. To express this circumstance, mathematicians employ the term proportional; thus they fay, The body B is attracted by the body A, with a force proportional to it's mass; the meaning of which is, that if the mass of body B were twice, thrice, or four times greater, the attractive power would be precifely fo many times increased. Thus, with respect to the attracting body A, they say, that the power which it exercises over the body B, is proportional to it's mass, so long as that of B, and the distance A B continue the same.

I must farther observe, that when we speak of the quantity of the attracting body A, or of the attracted body B, we mean the quantity of matter which each contains, and not their magnitude merely. You will recollect, that bodies differ considerably, in this respect, and that there are some, which, in a very small compass, contain a great deal of matter, gold, for example,

example, while others, fuch as air, contain very little in a great space. When, therefore, we here speak of bodies, we are always to be understood as referring to the quantity of matter which they contain: this is what we mean by their mass.

All that now remains is, to examine the third circumstance, namely, the distance A B of the two bodies, supposing them to continue always the same. It must be observed, that as the distance A B increases, the attraction diminishes: and that as they approach nearer, it increases: but in conformity to a law, which it is not fo eafy to express. When the distance becomes twice as great, the force with which the body B is attracted toward the body A, will be twice two, or four times less; and for triple the diftance, the attraction becomes three times three, that is nine times lefs. If the diffance becomes four times greater, the power of attraction becomes four times four, that is fixteen times lefs, and fo on. Finally, for a distance a hundred times greater, the power of attraction will be a hundred times a hundred, or ten thousand times less. From this it follows, that at very great distances, it must become altogether imperceptible. And reciprocally, when the distance A B is very small, the attraction may be very confiderable, though the bodies may be of no great magnitude.

11th September, 1760.

#### LETTER LVII.

## The same Subject continued.

I HAVE now demonstrated, that when a body B is attracted by a body A, the power of attraction is proportional to the mass of the attracting body A, and to that of the attracted body B; but it depends, to such a degree, on the distance of these bodies, that if it should become twice, thrice, sour or sive times greater, the power of attraction would become four, nine, sixteen, or twenty-sive times less.

In order to ascertain the rule of these quantities, we must multiply, into itself, the number which marks how many times the distance is increased, and the product will shew how many times less the power of attraction has become. To put this rule in it's clearest light, it must be observed, that when we multiply a number into itself, the product, resulting from it, is called it's square. Thus, to find these squares, we must multiply the numbers by themselves, as below.

It is clear, from this last example, that the square of number 12 is 144; and if you wish to know the square of any number whatever, say 258, you must multiply that number by itself, as in the following separation:

From which we fee, that the fquare of 258 is 66564; and the fquares, of all numbers whatever, may be calculated in like manner.

As the distance of bodies, then, must be multiplied by itself, it is evident, that the power of attraction diminishes, as much as the square of the distance increases: or, that the square of the distance becomes as many times greater, as the power of attraction is diminished.

In treating subjects of this nature, mathematicians employ expressions, whose signification it is proper you should know, because they sometimes occur in the course of conversation. If the attractive power increased in proportion to the square of the distance, we would call it proportionally to the square of the distance; but as the direct contrary takes place, and as the attractive power diminishes as the square of the distance increases, we employ the term recipro-

rally, to express this contrariety, saying, that the power is reciprocally proportional to the square of the distance.\* It is a geometrical mode of expression, the meaning of which you perfectly comprehend, and it refers to what I have just been attempting to explain.

In order to judge aright of the power which one body exercises over another, you have only to remark, that this power is, first of all, proportional to the mass of the attracting body: then, to that of the body attracted; and finally, reciprocally to the square of their distance. Hence, it is evident, that though the earth, and the other planets, are likewise attracted toward the fixed stars, this power must be imperceptible, on account of their prodigious distance.

Supposing, therefore, the mass of a fixed star to be equal to that of the sun, at equal distances, the earth would be attracted toward it, with a force as great as toward the sun; but as the distance of the fixed star is 400,000 times greater than that of the sun, the square of this number being 160,000,000,000, that is, a hundred and sixty thousand millions, the power with which it acts upon our globe, is a hundred and sixty thousand millions of times less than that of the sun; and, consequently, too seeble to produce any perceptible effect. For this reason, the attractive power of the sixed stars does not at all affect the earth's motion, nor that of the planets and the

<sup>\*</sup> It is more customary to say, that attraction is in the direct ratio of the masses of the attracting and attracted bodies; and in the inverse ratio of the square of their distance.—F. E.

moon; but it is that of the fun which chiefly regulates their motions, because his mass exceeds many thousands of times the mass of each planet.

When, however, two planets approach, fo that their distance becomes less than that of the sun, their attractive power increases, and may become sufficiently perceptible to derange their motion. Such derangement has, in fact, been observed; and constitutes an irresistible proof of the system of universal gravitation. Accordingly, when a comet approaches very near to a planet, the motion of this last may be considerably affected by it.

x3th September, 1760.

### LETTER LVIII.

Motion of the heavenly Bodies. Method of determining it by the Laws of universal Gravitation.

FROM what has been faid, respecting the power by which all the heavenly bodies mutually attract each other, proportionally to their mass and distance, you are enabled to comprehend, how their motions may be determined, and the real place of each body, at any given time, accurately assigned.

In this aftronomy confifts; the object of which is an exact knowledge of the motions of the heavenly bodies, in order to be able to determine, for every instant of time, whether past or to come, the place in which each of them must be, and in what place of



Mars, Venus, and Mercury, if they were attracted only by the fun. But the earth being attracted, not only by him, but by all the other heavenly bodies, the question becomes infinitely more complex and disticult, from the great diversity of powers to which we must pay attention.\* You may neglect, however, the powers with which it is attracted toward the fixed stars, because, however enormous their masses may be, they are so prodigiously distant, that the power which they exercise upon the earth, may be considered as just nothing.

The motion of the earth, therefore, and of the other planets, will always be as perfectly the fame, as if the fixed stars did not exist. Excepting, then, the power of the sun, we have only to consider the power with which the planets mutually attract each other. Now, these powers are extremely small, compared to those by which each planet is attracted toward the sun, because the mass of the sun is much greater than that of each planet.

As, however, these powers increase according as the distances diminish, so that a power four times greater corresponds to a distance twice less; and a

<sup>\*</sup>They are usually combined by three and three; that is, the effect resulting from the attraction of two bodies upon a third is fought. This celebrated problem, known by the name of the problem of three bodies, has been an object of the researches of all the great geometricians of our age; and though it has hitherto been resolved only by an approximation to the truth, the most fortunate applications have, however, been made, such as the theory of the moon, that of Jupiter, of Saturn, &c.—F. E.

power nine times less corresponds to a distance three times greater, and fo on, according to the squares of the numbers, as I explained the fubject in the preceding letter, it might be possible for two planets to approach fo near, that their attractive power should become equal to that of the fun, nay, greatly exceed it.

Fortunately, this never takes place in our fystem, and the planets always remain at fuch a diftance from each other, that their attractive power is ever incomparably fmaller than that of the fun. For this reason, without extending our views beyond what is thus certainly known, we may confider every planet as attracted only by the power of the fun, and by that it is easy to determine it's motion. This, however, can take place, only when we are disposed to rest satisfied with a result near the truth; for if we wish to have more exact information, we must attend to those feebler powers with which the planets act upon each other; powers which really produce the little irregularities clearly observed by astronomers; and to the attainment of the perfect knowledge of these, is directed all the fagacity of both aftronomers and geometricians. 15th September, 1760.

meduch, in at their bedies; they are not in a

### LETTER LIX.

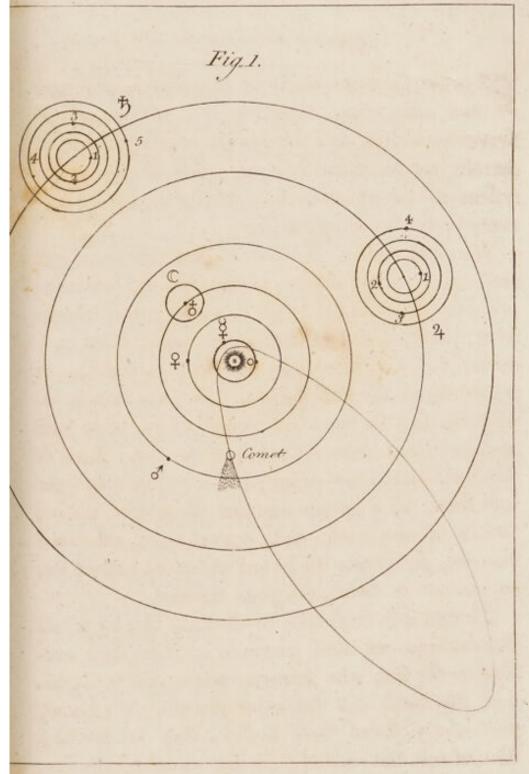
# System of the Universe.

IN order the more clearly to elucidate what I have been advancing, respecting the motion of the heavenly bodies, and the powers which produce it, permit me to present to you, (plate IV. fig. 1.) the system of the universe, or a description of the heavenly bodies which compose it.

We must, first of all, observe, that the fixed stars are bodies entirely similar to the sun, and luminous of themselves; that they are at a very great distance from that luminary; and also very distant from each other, and that every one of them is, perhaps, of equal magnitude with the sun. You are already informed, that the fixed star nearest to us, is at least 400,000 times more distant than the sun. Each of the fixed stars seems designed to communicate light and heat, to a certain number of opaque bodies, similar to our earth, and, undoubtedly, inhabited likewise, placed near them, but which we cannot see, on account of their prodigious distance.

Though it is impossible to ascertain this by actual observations, we must conclude it, from their analogy to the sun, who serves to warm and to illuminate the earth and the other planets. We know, particularly, six of these bodies; they are not in a state of rest, but each of them moves round the sun, in the direction of a curve line, somewhat different

from





from a circle, and which is called the planet's orbit. The fun himself is, nearly, in a state of rest, as well as all the fixed stars; the motion which they appear to have, being entirely owing to that of the earth.

I have, accordingly, represented on the annexed sheet, what is called the solar system, which contains all the opaque bodies that move round the sun, and derive from him all the benefits which he imparts to us. This sign (plate IV. fig. 1.) represents the sun at rest. You see, besides, six concentric circles, representing the orbits described by the planets in their motion round him.

That nearest to the sun is Mercury, marked by the sign &, and the black dot you see in the orbit represents the body of Mercury, who performs his revolution round the sun in about 88 days.

Next comes Venus, marked by 2, who completes a revolution round the fun in feven months nearly.

The third circle is the orbit of the earth, marked by the fign 5, and which completes a revolution round the fun in a year. We have no other meaning, in truth, to the word year, but the time employed by the earth in performing a revolution round the fun; and the duration of the common year nearly approaches to this folar year.

But while the earth is moving round the fun, there is another body moving round the earth, and keeping the direction of it's orbit; this is the moon, whose own circle, or orbit, is marked by D.

The two first planets, Mercury and Venus, have

no visible bodies which attend them; neither has Mars &, which is the fourth, and performs his revolution in about two years.

The fifth circle is the orbit of Jupiter, marked by 24, who performs his revolution in twelve years nearly. Round him move four fatellites, represented in the plate, with their orbits, and marked by the figures 1, 2, 3, 4.

Finally, the fixth and last circle is the orbit of Saturn, marked thus, h, who employs almost thirty years in performing one revolution round the sun. This planet is attended, in his course, by five satellites, marked by the sigures 1, 2, 3, 4, 5. Thus, then, the solar system consists of six primary planets, Mercury &, Venus &, the Earth &, Mars &, Jupiter 4, Saturn h, and ten secondary planets or satellites, namely, the moon, the sour attendants of Jupiter, and the sive of Saturn.\*

\* To this enumeration must now be added, the planet discovered at Bath the 17th of March, 1781, by Mr. Herschel, and taken at first for a comet. It is more distant from the sun than Saturn, and it's orbit must be represented by a seventh circle, circumscribing all the others. The period of it's revolution is about 83 years. Tables of it's motion have been constructed, which represent already the observations with an exactness, that announces the perfection both of the instruments, and of the method of calculation.

It is admitted, that this star was seen in 1756, in the month of September, by Mr. Mayer, of Gottingen; but that astronomer took it for a fixed star, and having observed it only once, he could not ascertain it's motion: his determination agrees in other respects with the place which the tables assign to the planet of Mr.

Herschel,

This fyftem contains, befides, feveral comets, the number of which is unknown. The figure on the plate reprefents one of them, whose orbit differs from that of the planets, because it is drawn out into extreme length, fo that a comet fometimes approaches very near to the fun, and fometimes removes to fuch an immense distance, as entirely to disappear. Of comets it has been remarked, that one finishes his revolutions in his orbit, in about fixty years; this is the one that was visible last year: As to the other comets, it is certain, that they employ feveral centuries in performing one revolution in their orbits; and as, in past ages, no exact observations were made of them, we are totally in the dark with respect to their return. Of these, then, consists the solar system; and, most probably, every fixed star has one fimilar to it.\*

17th September, 1760.

Herschiel, for that epoch. It bears the name of the person who discovered it.

The mean distances of the planets from the sun, may be thus respectively expressed: that of Mercury by 4, that of Venus by 3, that of the earth by 10, that of Mars by 15, that of Jupiter by 52, that of Saturn by 95, and, finally, that of the planet Herschel (a) by 191—F. E.

- \* Aftronomers expect about 1790 the comet observed in 1531, and in 1661, which they believe to be the same star, and the period of which appears to be about 130 years.—F. E.
- (a) In compliment to his patron, King George III. Mr. Herfchel named his recently discovered planet Georgium Sidus. The republican Condorcet, in contempt of Kings, gives it the name of the Discoverer.—E. E.

### LETTER LX.

# The Same Subject continued.

IN addition to what I have faid respecting the solar system, I must communicate some observations for the explanation of the sigures. And, sirst, it must be remarked, that the lines which mark the paths in which the planets move, have no real existence in the heavens, as the whole immensity of space in which they move is a vacuum, or rather silled with that subtile matter which we call the ether, and which I have already so often mentioned.

Again, the orbits of the planets are not all in the fame plane, as the figure prefents them: but if the orbit which the earth describes round the sun, is properly represented on the paper, we must imagine the orbits of the sive other planets to be partly elevated, and partly depressed, with reference to it; or, that the orbit of each planet bears upon it an oblique direction, making an intersection with the paper, under a certain angle, which it is impossible to represent in a figure drawn upon a plane.

Farther, the orbits of the planets are not circles, as the figure appears to indicate, but rather somewhat oval, one more, another less so; no one, however, recedes very considerably from the circular form. The orbit of Venus is almost a perfect circle; but those of the other planets are more or less extended

tended lengthwise, so that these planets are sometimes nearer to the sun, sometimes farther off.

The orbits of comets are particularly diftinguishable, being greatly extended in length, as I have represented it in the figure. As to the moon, and the fatellites of Jupiter and Saturn, their orbits, too, are nearly circular.

Neither must we conceive them as moving in one and the same direction, as they appear on the plane of the paper; for they do not remain in the same place, but are themselves carried round the sun along with the primary planet to which they belong. It is thus we must understand the lines represented in the sigure. Imagination must supply what it is impossible, on a plane surface, accurately to exhibit.

You are now enabled to comprehend, with ease, what the late Mr. de Fontenelle meant to display, in his book on the plurality of worlds. The earth, with it's inhabitants, is sometimes denominated a world; and every planet, nay, every one of the satellites, has an equal right to the same appellation, it being highly probable, that each of these bodies is inhabited as well as the earth.

There are fixteen worlds, then, in the folar fystem alone. And every fixed star being a sun, round which a certain number of planets perform their revolutions, and of which some have, undoubtedly, their satellites, we have an almost infinite number of worlds, similar to our earth, considering, that the number of stars, perceptible to the unaffisted eye,

Q 4 exceeds

exceeds some thousands, and that the telescope discovers to us an incomparably greater number.

If it is meant to comprehend under the name of world the fun, with the planets and their fatellites, and which derive heat and light from him, we shall have as many worlds as there are fixed stars. But if by the term world, we understand the earth, with all the heavenly bodies, or all the beings which were created at once, it is clear that there can be but one world, to which we refer every thing that exists. It is in this sense the term world is employed in philosophy, particularly in metaphysics; it is in this sense we say, that there is but one world, the assemblage of all created beings, past, as well as present, and future, whose existence is subject to general laws.

When, therefore, philosophers dispute, whether our world is the best or not, they proceed on the supposition of a plurality of worlds; and some maintain, that the one which exists, is the best of all those which could have existed. They consider the Deity as an architect, who, intending to create this world, traced several different plans, of which he selected the best, or that in which the greatest perfections were all combined, in the highest degree, and executed it in preference to all the others.

But the great quantity of evil that prevails, and is diffused over the surface of our globe, and which flows from the wickedness of man, suggests an important enquiry, namely, Whether it would have been possible to create a world, wholly exempted from these evils? In my opinion, a distinction must be carefully made, between the plans of a world, which should contain corporeal substances only, and those of another world, which should contain beings intelligent and free. In the former case, the choice of the best, would be involved in very little difficulty; but in the other, where beings intelligent and free constitute the principal part of the world, the determination of what is best is infinitely beyond our capacity; and even the wickedness of free agents may contribute to the perfection of the world in a manner which we are unable to comprehend.

It would appear, that philosophers have not been fufficiently attentive to this distinction, however effential it may be. But I am too fensible of my own incapacity, to enter any deeper into this disticult question.

19th September, 1760.

### LETTER LXI.

Small Irregularities in the Motions of the Planets, caused by their mutual Attraction.

IN order to determine the motion of the bodies which compose the solar system, it is necessary to distinguish the primary planets, which are Mercury, Venus, the Earth, Mars, Jupiter, and Saturn, from their satellites, namely, the moon, the sour satellites of Jupiter, and the five of Saturn.

It has been explained to you, that these six planets are principally attracted toward the sun, or, that the force with which they are impelled toward him, is incomparably greater, than the powers which they exert one upon another, because his mass is incomparably greater than that of the planets, and because they never sufficiently approach to each other to render their reciprocal attraction very considerable. Were they attracted only toward the sun, their motion would be sufficiently regular, and easily determined. But the feebler powers of which I have been speaking, occasion some slight irregularities in their motion, which astronomers are easer to discover, and which geometricians endeavour to determine, on the principles of motion.

An important question is here agitated, namely, The powers which act upon a body being known, how to find the motion of that body? Now, upon the principles above laid down, we are acquainted with the powers, to the influence of which every planet is subjected. Thus the motion of the earth is somewhat affected; sirst, by the attraction of Venus, which sometimes passes very near it; and, secondly, by that of Jupiter, which, on account of the prodigious mass of this planet, becomes considerable, though he be always at a great distance. The mass of Mars is too small to produce any perceptible effect, though he is sometimes very near us; and Saturn, though his mass be the greatest, next to that of Jupiter, is too distant.

The moon, though her mass be very small, pro-

duces, however, fome derangement, from her being very near the earth. The comet, which appeared last year, was seven times nearer to us than the fun, when his diftance was fmallest; there is a great degree of probability, therefore, that it may have deranged the earth's motion, especially if his mass was confiderable, a circumstance with which we are not acquainted. If this comet were as great as the earth, the effect must have been very considerable; but it's apparent smallness induces me to believe, that it's mass is much less than that of the earth, and, confequently, it's effect must have been proportionally less. When we faw this comet, however, it had got to a great distance; at the time when it was nearest, it was invisible to us, but it must have appeared very brilliant to our antipodes.

What has been faid, respecting the derangements occasioned in the earth's motion, takes place likewise in the other planets, regard being had to their mass, and to their proximity. As to the moon, and the other secondary planets, the principle of their motion is somewhat different. The moon is so near the earth, that the attraction she feels from hence greatly exceeds that of the sun, though the mass of this luminary be many thousands of times greater than that of the earth. Hence it is, that the motion of the moon follows that of the earth, and that she remains, as it were, attached to it, which makes the moon to be considered as a satellite to our planet.

Had the moon been placed much farther from us, and had she been attracted less toward the earth than toward the fun, she would have become a primary planet, and performed her own revolutions round the fun; but she is 300 times nearer to us than she is to the fun; hence it is evident, that he must exercife a much feebler influence upon her than the earth does. The moon being principally attracted by two bodies, the fun and the earth, it is evident that the determination of her motion, must be much more difficult than that of the primary planets, which are fubject to the attraction of the fun only, excepting the flight derangements which have been mentioned. The motion of the moon has, accordingly, in all ages, greatly embarraffed philosophers; and never have they been able to afcertain, for any future given time, the exact place of the moon in the heavens.

You perfectly comprehend, that in order to predict an eclipfe, whether of the moon or of the fun, we must be able accurately to ascertain the moon's place. Now, in calculating eclipses, formerly, there was frequently a mistake of an hour or more: the eclipse actually taking place an hour earlier or later than the calculation. Whatever pains the ancient astronomers took to determine the moon's motion, they were always very wide of the truth. It was not till the great Newton discovered the real powers which act upon the moon, that we began to approach nearer and nearer to truth, after having surmounted many obstacles which retarded our progress.

I too have employed much time and attention on the fubject; and Mr. Meyer, of Gottingen, pursuing the track which I had opened, has arrived at a degree of precision, beyond which it is perhaps impossible to go. Not much more, then, than ten years have elapsed since we could boast of any thing like accurate knowledge of the moon's motion. Since that time we are able to calculate eclipses so exactly, as not to make the mistake of a single minute, whereas, before, there was frequently the difference of eight minutes, and more. To analysis, then, we are indebted for this important discovery, the source of unspeakable advantages, not to the astronomer only, but likewise to the geographer, and the navigator.

23d September, 1760.

## LETTER LXII.

Description of the Flux and Reflux of the Sea.

THE attractive power of the heavenly bodies extends, not only to the mass of the earth, but to all the parts of which it is composed. Thus all the bodies, which we see on the surface of the earth, are attracted, not only toward the earth itself, from which results their gravity, and the weight of every one in particular, but, likewise, toward the sun, and toward all the other heavenly bodies, and that more or less, according to the mass of these bodies and their distance.

Now, it is evident, that the force with which a body,

body, fay a stone, is attracted toward the earth, must be incomparably greater than that with which the same body is attracted toward the sun, the other planets, and the moon, because of their great distance. Such a body, being at a distance from the centre of the earth, equal to a radius of this globe, is 60 times farther from the moon. Though, then, the mass of the moon were equal to that of the earth, the attraction toward the moon would be 60 times 60, that is 3600 times less than the attraction toward the earth, or, the gravity of the body. But, the mass of the moon is about 70 times less than that of the earth; hence the attractive power of the moon becomes still 70 times 3600, that is, 252,000 times less than the gravity of the body.

Again, though the sun be many thousands of times greater than the earth, he is about 24,000 times more distant from us, than the centre of the earth; and for this reason, the attraction of the sun upon a stone is extremely small, compared to it's gravity. Hence you see, that the gravity of terrestrial bodies, which is nothing else but the force with which they are attracted toward the earth, cannot be perceptibly affected by the attraction of the heavenly bodies.

Though this attraction, however, be very inconfiderable, there refults from it a remarkable phenomenon, which long puzzled philosophers; I mean the flux and the reflux of the sea. It occurs so frequently, even in common conversation, that it is almost a matter of necessity to understand it. For this reason, I propose to explain more minutely, this singular phenomenon, and to unfold the causes which produce it.

I begin, then, with the description of the well-known phenomenon, of the flux and reflux of the sea. Hardly any one is ignorant, that by far the greatest part of the surface of our globle is covered with a mass of water, called the Sea, or the Ocean. This immense sluid mass is very different from rivers and lakes, which, according to the different seasons of the year, contain sometimes less water, sometimes more, whereas, in the sea, the quantity of water, at all times, continues nearly the same. It is, however, observed, that the water of the sea rises and falls alternately, with wonderful regularity, twice every twenty-four hours.

If, for inftance, in a harbour, the water is now at it's greatest height, it will presently begin to subside, and this decrease continues for six hours, at the end of which, it's depth will be at the lowest. It then begins again to rise, and the increase, likewise, lasts six hours, when it is again at it's greatest depth. It immediately begins again to fall for six hours, and then rises as many, so that in the space of about 24 hours, the water rises and falls twice; and arrives, alternately, at it's greatest and least depth.

It is this alternate increase, and diminution of the water of the sea, which we call it's flux and reflux, or it's flowing and ebbing: and more particularly, the flux denotes the time, during which it encreases or rises, and the reflux, the time of it's decrease or falling. The flux and reflux together, likewise, go by

the name of tide. This alternation, then, is to be the subject of our present disquisition.

It is, first of all, to be remarked, that the difference between rising and falling, keeps pace with the variations of the moon. At full, and new moon, the water rises higher than at the quarters: and about the time of the vernal, and autumnal equinoxes, in the months of March and September, this alternate motion of the sea is most considerable. A great difference is, likewise, observed, according to the situation of the coasts. The flux, in some places, is never more than a few feet, while, in others, the rise is 40 feet and upwards. Such are the tides in the ports of St. Malo, in France, and of Bristal, in England.

It is farther to be remarked, that this phenomenon is perceptible, chiefly, in the ocean, where there is a vast extent of water, and that in seas bounded and confined, such as the Baltic, and the Mediterranean, it is much less considerable. The interval, from the slux to the succeeding reslux, is not exactly six hours, but about 11 minutes more; so that the same changes do not take place, the day after, at the same hour, but fall out about three quarters of an hour later: so that a revolution of 30 days is requisite, to bring them round to the same hour; now, this is precisely the period of one revolution of the moon, or the interval, between one new moon, and that which immediately follows.

lux and rellux together; libewil

2616 September, 1760. 10

#### LETTER LXIII.

Different Opinions of Philosophers respecting the Flux and Reflux of the Sea.

WHEN the water of the sea rises at any place, we are not to imagine that it swells from any internal cause, as milk does when put in a vessel upon the sire. The elevation of the sea is produced by a real increase of water slowing hither from some other place. It is a real current which is very perceptible at sea, conveying the waters toward the place where the slux is.

In order to have a clearer comprehension of this, you must consider that in the vast extent of the ocean there are always places where the water is low, while it is high at others; and that it is conveyed from the former to the latter. When the water rifes at any place, there is always a current, conveying it from other places, where it is of course at that time low. It is an error, therefore, to imagine, with fome authors, that during the flux of the fea the total mass of water becomes greater, and that it diminishes during the reflux. The entire mass or bulk of water remains ever the fame; but it is fubject to a perpetual ofcillation, by which the water is alternately tranfported from certain regions to others; and when the water is high at any place, it is of course low somewhere elfe, fo that the increase at places where it is VOL. I. high

high is precifely equal to the decrease at those where it is low.

Such are the phenomena of the flux and reflux of the fea, the caufe of which ancient philosophers endeavoured to discover, but in vain. Kepler, in other respects a great astronomer, and the ornament of Germany, believed that the earth, as well as all the heavenly bodies, was a real living animal, and confidered the flux and reflux of the sea as the effect of it's respiration. According to this philosopher, men and beasts were just like insects feeding on the back of the huge animal. You will hardly expect I should go into the resutation of an opinion so ridiculous.

Descartes, that great French philosopher, endeavoured to introduce a more rational philosophy; and remarked, that the flux and reflux of the sea was principally regulated by the moon's motion; which was indeed a very important discovery, though the ancients had already suspected a connection between these two phenomena. For if high water or the top of the flux happen to-day at noon, it will be low water at 11 minutes after six in the evening: it will rise till 22 minutes after midnight; and the next low water will be 33 minutes after six in the morning of the day after; and the ensuing high water, or flux, will be three quarters of an hour after noon: so that from one day to another the same tides are later by three quarters of an hour.

And as the fame thing precifely takes place in the moon's motion, which rifes always three quarters of

an hour later than the preceding day, it was prefumable that the tides followed the course of the moon. If at any given place, for example, on the day of new moon, high water happen to be at three of the clock, afternoon, you could rest assured, that ever after, on the sirst day of the moon, the slux would invariably be at the height at three o'clock asternoon, and that every following day it would fall later by three quarters of an hour.

Again, not only the time when every flux and reflux happen exactly follows the moon, but the flrength of the tides, which is variable, appears still to depend on the position of the moon. They are every where stronger after the new and full moon, that is, at these periods the elevation of the water is greater than at other times; and after the first and last quarters, the elevation of the water, during the flux, is smaller. This wonderful harmony between the tides, and the motion of the moon, was, undoubtedly, sufficient ground to conclude, that the chief cause of the flux and reflux of the sea was to be fought for in the action of the moon.

Defcartes accordingly believed, that the moon, in passing over us, pressed the atmosphere, or the air which surrounds the earth, and that the air pressing on the water, in it's turn, forced it to subside. Had this been the case, the water must have been depressed at the places over which the moon was, and that the same effect should be produced 12 hours after, in the ensuing tide; which, however, does not happen. Besides the moon is too distant from the earth,

and the atmosphere too low to be impressed by the moon; and admitting that the moon, or any other great body, were to pass along the atmosphere, it would be very far from undergoing any pressure from it, and still less would the sea feel this pretended pressure.

This attempt of *Descartes* to explain the flux and reflux of the sea, has therefore failed; but the connection of this phenomenon with the moon's motion, which this philosopher has so clearly unfolded, enabled his successors to employ the application of their researches with more success. This shall be the subject of some following letters.

30th September, 1760.

## LETTER LXIV.

Explanation of the Flux and Reflux, from the attractive Power of the Moon.

DESCARTES's method of explaining the flux and reflux of the fea, by the prefiure of the moon upon our atmosphere, not having succeeded, it was reasonable to look for the cause of it in the attraction which the moon exercises upon the earth, and consequently also upon the sea.

The attractive power of the heavenly bodies having been already fufficiently established, by so many other phenomena, as I have shewn, it could not be doubted that the flux and reflux of the sea must be an effect of it. As foon as it is demonstrated that the moon, as well as the other heavenly bodies, is endowed with the property of attracting all bodies, in the direct ratio of their mass, and in the inverse ratio of the square of their distance, it is easily comprehended that it's action must extend to the sea; and the more so, as you must frequently have observed, that the smallest force is capable of agitating a fluid. All that remains, therefore, is to enquire, whether the attractive power of the moon, such as we suppose it, is capable of producing in the sea the agitation known to us by the name of slux and reflux.

Let the annexed figure (plate III. fig. 5.) represent the earth and the moon. A is the place where we fee the moon over the earth; B that which is directly opposite, or the antipodes of A; and C is the centre of the earth. As the point A is nearer the moon than the point B, a body at A is more powerfully attracted toward the moon than a fimilar body at B. And if we suppose a third similar body to be placed at the centre of the earth C, it is evident that the body A will be more powerfully attracted toward the moon than the body C, and this last than the body B, because the body A is nearer to the moon, and the body B more remote than the body C. But fimilar bodies placed at E and F, are almost as much attracted by the moon as that which is at the centre of the earth C, as they are all three nearly equi-diftant from the moon.

Hence we fee that bodies placed on the furface of R 3 the

the earth are not all equally attracted toward the moon. This inequality of attraction depends on the inequality of their distance from the centre of the moon L, so that a body is so much the more powerfully attracted by the moon, as it's distance is less; and the contrary takes place according as the distance is greater.

To these differences in the action of the moon on bodies differently situated, we must here chiefly pay attention; for if all bodies were equally attracted toward the moon, they would equally obey this power, and no derangement could take place in their mutual situation.

You can eafily form the idea of feveral carriages drawn along by powers perfectly equal; they will proceed on the road, always preferving the fame order, and the fame diffances; but as foon as fome of them advance more brifkly, and others more flowly, the order will be deranged. The fame thing takes place in the case of the different bodies which are attracted by the moon; if they all felt, in the fame degree, the action of that luminary, they would preferve the fame relative fituation, and we should perceive no change in them: but as foon as the force with which they are attracted toward the moon varies as to each of them, their order and their relative fituation necessarily change, unless they are attached to each other by bands which that power is unable to burft afunder.

But this is not the case with the sea, as all the particles of a sluid are easily separated from each other, and every one may obey the impressions which it receives. It is evident, then, that when the powers which act on the different parts of the sea are not equal to one another, an agitation, or derangement, must be the consequence.

We have just seen that the different parts of the sea are attracted unequally by the moon, according as they are unequally distant from her centre; the sea must, therefore, be agitated by the force of the moon, which, continually changing her situation, with respect to the earth, and performing a revolution round it in about twenty-four hours and three quarters, makes the sea undergo the same changes, and presents the same phenomena in the same period of twenty-four hours and three quarters; the slux and reslux must, therefore, be retarded from one day to another three quarters of an hour, which is confirmed by constant experience.

It now remains that we shew, How the alternate elevation and depression of the sea, which succeed each other after an interval of six hours and eleven minutes, result from the inequality of the powers of the moon. This I propose to examine in my next letter.

4th October, 1760.

child while our

#### LETTER LXV.

## The same Subject continued.

OU have feen that the moon causes no alteration in the state of the earth, but in so far as she acts unequally on it's different parts. The reason of it is, that if all it's parts equally felt the same action, they would be equally attracted, and no change in their relative situation would result from it.

But a body being at A (plate III. fig. 5.) nearer the moon than the centre of the earth C, is more powerfully attracted to it than a body at C would be: it will approach it, then, with greater velocity than this last: from hence it necessarily follows, that the body A retires from the centre C, and approaches the moon: as if there were two chariots, the one at A, the other at C, and if the chariot A were drawn toward L with greater force than the chariot C, it would remove from C. It is thus that the power of the moon has a tendency to withdraw the point A from the centre C.

Now to remove a body from the centre of the earth is to raise it: and the water at A being now the thing in question, it is certain that the force of the moon tends to raise the water which is at A, by a power equal to the excess of the attraction toward the moon felt at A, above that felt at C. By this power, then, the moon raises the waters of the earth which are immediately under her.

Let us now, likewise, attend to a body at B, directly opposite to the point A; the centre of the earth C, more powerfully attracted by the moon than the point B, will approach nearer to it, and this last, so to speak, will remain behind, just as a chariot, which was drawn more slowly than that which precedes it. The point B will consequently remove from the centre C, and rise; for to remove from the centre of the earth, and to rise, is one and the same thing.

It is evident, therefore, that the power of the moon tends to raise the waters, not only at A, but likewise at B, the point diametrically opposite, and that by a force equal to the difference of the attraction of the moon at B and at C, which is less at B than at C. Now, those who are at A, have the moon directly above them, or in their zenith; and those who are at B see nothing of the moon, because she is then in a point of the heavens diametrically opposite to their zenith, called Nadir.

Hence it appears, that at whatever part of the fea it may be, the water must rise equally when the moon is in the zenith of that place, and in it's nadir, or, when the moon is at it's greatest elevation above the horizon, or at it's greatest depression under it. At the intermediate periods, when the moon is in the horizon, either rising or setting, she exercises no power capable of raising the sea; a small contrary power tends even to make it fall.

According to this fyftem, at the place of the fea, where the moon is in the zenith, it's power has a tendency

tendency to raife the waters; about fix hours after, when she has reached the horizon, her power has a tendency to make them fall. Twelve hours and twenty-two minutes after, the moon being then at the point most distant, under the horizon, she exercises the same power to raise the water; and at the end of eighteen hours, thirty-three minutes, when she has got to the opposite horizon, the waters are fallen: till at length, twenty-four hours and forty-five minutes from the first period, she returns to the zenith, raising the water as on the preceding day; and this is consirmed by uniform experience.

This alternate elevation and depression of the sea, at intervals of six hours and eleven minutes, having such a persect conformity with the moon, leaves us no room to doubt that the slux and ressux of the sea are caused by the attractive power of the moon.

It is a remarkable circumstance that she acts equally on the sea, in raising it, whether she is at her greatest height above the horizon, or at the most distant point under it. This appeared at sirst very strange to philosophers, who imagined that the moon must produce, under the horizon, an effect contrary to that which she produces when in the zenith. But you see clearly that the moon produces the same effect in these two diametrically opposite positions, as I have demonstrated in the sigure above referred to, that the effect of the moon is the same at A and at B.

7th Odober, 1760.

#### LETTER LXVI.

# The same Subject continued.

ROM what has been faid respecting the flux and restlux of the sea, you must be sensible that the system of Newton, which I have adopted, is directly contrary to that of Descartes. According to this last, the moon exercises a pressure, and the sea must subside at places situated directly under her; but, according to Newton, she acts by attraction, and forces the water to rise at these very places.

Experience, then, must determine which of these two systems is to be received. No more is necessary than to consult the observations made with respect to the ocean, in order to see whether the water rises or falls when the moon is in the zenith. Recourse has actually been had to this; but it is found that when the moon is at either the zenith, or nadir, of a given place, the water there is neither high nor low; and that high water does not take place till some hours after the moon has passed the zenith.

From this circumstance, persons who examine things superficially, concluded at once, that neither of the systems was admissible; and the Cartesians have taken advantage from it, presuming, that if Newton's was rejected, that of Descartes must necessarily be adopted, though the observations referred to are as contrary to the system of Descartes as they appear to be to that of Newton.

But the fystem of *Descartes* is overturned by this single phenomenon, that the sea is always in the same state after a period of twelve hours and twenty-two minutes, or that it's state is always the same, whether the moon be above or below the horizon; and it is impossible for it's supporters to shew how the moon, being over the heads of our antipodes, can produce the same effect as when she is over ours. To this purpose, see plate III. sig. 6.

Experience proves that the state of the water at A is the same, whether the moon be at M, the zenith of the point A, or at N, it's nadir, which is consequently the zenith of the antipodes at B. The essect, of the moon, then, on the water at A, is the same in both cases. But if the moon acted by pressure, according to Descartes, it would follow, that when the moon is at M, the water at A must fall; and if she were at N, it is impossible that the water at A should undergo the same pressure.

In the fystem of attraction, on the contrary, it is incontestably certain, that the action of the moon must be nearly the same, whether that luminary be at M or at N; and this is demonstrated by actual obfervation.

I must here repeat a preceding explanation, because it is a matter of the utmost importance. When the moon is at M, the point A is nearer it than the centre C; it is, therefore, more powerfully attracted than the centre; the point A will remove from the centre, consequently it will then rise: the moon being at M, has a tendency to raise the water at A.

Let us now fee what effect the moon, being at N, will produce, where she arrives in twelve hours and twenty-two minutes after she was at M. As the point A is more distant from the moon at N than the centre C, it will be more feebly attracted; the centre C will advance with greater velocity toward N, than the point A; the distance A C will accordingly become greater; the point A will, therefore, be more distant from the centre C. But to be more distant from the centre of the earth is to rise, consequently the moon being at N, makes the point A to ascend, that is, she has a tendency to raise the water at A, as if the moon were at M.

But here experience prefents a very formidable objection; for it is observed, that the moon being at M, or at N, the water is not then at it's greatest elevation at A. This does not take place till a considerable time after, and thence some have been induced to reject this explanation altogether. But you will easily see that their decision is extremely precipitate.

I have not faid, that when the moon is at M or N, the water at A is at it's greatest height; I have only faid, that the power of the moon has then a tendency to make the water rise. But the water at A could not rise, unless it's quantity were increased; and that increase can be produced only by the slowing of the water from other parts, some of them very distant. A considerable time, therefore, is requisite to the accumulation of a sufficient quantity of water; it is, then, very natural to suppose, that high water at A should not take place for some time after the moon

has passed M or N. This observation, therefore, is so far from overturning our system, that it tends strongly to confirm it.

There is no room to doubt that the power which has a tendency to raise the sea, must precede it's greatest elevation, nay, that a considerable time must intervene, as the water must flow thither from places very remote, that is, from places where the water must be low, while it is high at A. If the water has to pass through straights, or has it's current otherwise obstructed, high water will be still more retarded; and if, in the ocean, it is high water at A, two hours after the moon has passed M or N, it will not be at the height, in narrow and bounded seas, for three hours or more: and this perfectly agrees with daily observation.

11th October, 1760.

\* It may be proper, in this place, to give a popular view of so interesting a subject as that of tides. Suppose, therefore a cistern of water communicates with another, also of water, and in the fame flate; the furface of both will conflantly preferve, or endeavour to preserve, the same level. But if one of the cisterns were filled with oil, or any fuch light fluid, the furface would evidently rife above the level of the other; and the more fo, the greater was the depth of the oil. The same consequence would follow, if, by any cause, the specific gravity of the water in one of the cisterns was diminished. And this is actually the effect which the moon and fun produce on the waters of the ocean; those particles nearest these luminaries are more attracted by them than the particles at the centre, or at the extremities of the transverse diameter, which are more attracted than the particles on the farthest fide; and therefore, in both cases, the tendency to the centre is diminished. Hence a protuberance will be formed on the nearer and farther

#### LETTER LXVII.

# The same Subject continued.

It is no longer, then, a matter of doubt, that the flux and reflux of the fea is caufed by the attractive power of the moon. But there remains one difficulty more to be removed: Why is the motion of the fea much more confiderable at the time of new and full moon than at the other quarters? If the moon were nearer the earth when fhe is new, or full, than when fhe is in her quarters, there would be no difficulty in the question, as her proximity would increase her power. But though the moon approaches the earth sometimes more, sometimes less,

fides of the globe, proportional to the depth of the ocean. But this general fwell is never fuffered to attain it's just elevation; for the necessary motions are not supported a sufficient length of time, and the impressions soon give a contrary tendency. The slow of the waters is most obstructed in narrow seas, which are remote from the great ocean. Hence the lateness and irregularity of the tides in such seas. When a large river, or an arm of a sea, frequently contracts and widens, it often happens that the tide, in pushing up, occasions a great swell in the narrows, which produces a strong current, that continuing, after it's cause has ceased to operate, reduces the water below it's proper level, till a quantity is again accumulated, and repeats the same effects; and thus an ebb and slow may happen several times in the course of a day. This is particularly remarked in the river St. Lawrence, in North America.

A large lake cannot have any fentible tides, for every portion of it's waters is almost equally attracted by the sun or moon. the difference is always too fmall to occasion a change fo considerable in the flux and reflux of the sea.

Besides, this difference is not regulated by the new and full moon; and it may happen, that the moon, in the intermediate quarters, should be nearer to us than when she is new or full. We must have recourse, therefore, to another cause capable of increasing the slux and reslux of the sea at the new and full moon, and of diminishing it at the intermediate quarters.

The fystem of attraction shews us, at sirst, that it is the action of the sun which, joined to that of the moon, furnishes a complete solution of all the phenomena presented to us by the slux and reslux of the sea. Indeed, all that I have said respecting the power which the moon exercises on the sea, is equally applicable to the sun, whose attractive power acts likewise unequally on all the parts of the earth, according as they are more or less remote from him. The attraction of the sun is even much more intense than that of the moon, as it chiefly regulates the motion of the earth, and carries it round it's orbit.

As to the motion which he communicates to the fea, it depends on the inequality of that action, with relation to the different points of the furface of the earth, which are more or lefs attracted toward the fun than it's centre, as I have already shewed you, in explaining the effect of the moon. If all the parts of the earth were attracted equally, no change in their mutual situation would take place. But though the power of the sun be much greater than that of

the moon, the inequality, with relation to different parts of the earth is, nevertheless, smaller, on account of the great distance of the fun, which is 300 times farther from us than the moon. The difference of the power with which the centre of the earth, and the points of it's surface, are attracted toward the fun, is, therefore, very small; and from calculations actually made, it is found to be three times less, nearly, than that of the moon upon these points. The attractive power of the sun alone, then, would likewise be capable of causing the slux and resux of the sea; but it would be about three times less than that which is the effect of the combined influence of these two luminaries.

It is evident, then, that the flux and reflux of the fea are produced by the power of both the fun and the moon, or that there are really two tides, occafioned, the one by the moon, the other by the fun, and called the lunar tide and the folar tide. That of the moon, nearly three times greater, follows it's motion, and from one day to another is retarded three quarters of an hour: that which follows the action of the fun, would constantly correspond to the fame hours of the day, if it existed alone, or if there were no moon. These two tides, the lunar and the folar together, produce the flux and reflux of the fea; but as the one and the other, feparately, make the waters of the fea alternately to rife and fall, when it happens that these two causes, conjointly, make the fea rife and fall, it's flux and reflux become much more confiderable; but when the one tends to raife the III VOL. I.

the fea, and the other to lower it, at the fame place, when they act in contrary directions, the one will then be diminished by the other, and the lunar tide will be weakened by the folar. According as these two tides assist, or check, each other, the flux and results will, then, be more or less considerable.

Now, as at the time of new moon, the fun and moon are in the fame parts of the heavens, their effects being perfectly in unifon, the flux and reflux must then be greatest, being equal to the sum of the two tides. This will equally take place at the time of full moon, when the moon is opposite to the sun, as we know that she produces the same effect, though she be in a point of the heavens diametrically opposite to the first. The slux and ressum must, therefore, be greater at new and full moon, than at the first and last quarters. For then the power of the sun is exerted to lower the waters, and that of the moon to raise them. It is evident, therefore, that, at these seasons, the slux and ressum must be less considerable, and actual observation confirms it.

It might be still farther demonstrated, by calculation, that the effect of the moon, or of the sun, is somewhat greater, when these bodies are at the equator, or equally distant from the two poles of the globe: which happens at the time of the equinoxes, toward the end of the months of March and September. It is found, too, that then the tides are strongest. It follows beyond all doubt, then, that the tides, or the slux and reslux of the sea, are caused by the attractive power of the moon and of the sun,

in as much as these powers act unequally on the different parts of the sea. The happy explanation of this phenomenon, which had so dreadfully perplexed the ancients, is a complete confirmation of the system of attraction, or of universal gravitation, on which is founded the motion of all the heavenly bodies.

14th October, 1760.

#### LETTER LXVIII.

More particular Account of the Dispute respecting uni. versal Gravitation.

HAVING given you a general, but exact, idea of the powers which produce the principal phenomena of the universe, and on which are founded the motions of all the heavenly bodies, it is of importance to consider, with more attention, those powers which are the principal points of the system of attraction.

It is supposed, in this system, that all bodies mutually attract each other, in the ratio of their mass, and relatively to their distance, in conformity to a law already explained. The satisfying manner in which most of the phenomena in nature are accounted for, proves that this supposition is sounded in truth; and that the attraction which different bodies exercise upon each other, may be considered as a most undoubted sact. It now remains, that we enquire into the cause of these attractive powers; but this

refearch belongs rather to the province of metaphyfics than of mathematics. I dare not, therefore, flatter myfelf with the profpect of affured fuccess in the profecution of it.

It being certain, that any two bodies whatever are attracted to each other, the question is, What is the cause of this attraction? On this point philosophers are divided. The English maintain, that attraction is a property essential to all the bodies in nature, and that these bodies, hurried along by an irresistible propensity, tend mutually to approach, as if they were impelled by feeling.

Other philosophers confider this opinion as abfurd, and contrary to the principles of a rational philofophy. They do not deny the fact; they even admit, that powers exift, which are the causes of the reciprocal tendency of bodies toward each other; but they maintain, that they are foreign to the bodies; that they belong to the ether, or the fubtile matter which furrounds them, and that bodies may be put in motion by the ether, just as we see that a body, plunged into a fluid, receives feveral impreffions from it. Thus, according to the first, the cause of the attraction refides in the bodies themselves, and is effential to their nature; and, according to the last, that it is out of the bodies, and in the fluid which furrounds them. In this case, the term attraction would be improper; and we must rather fay, that bodies are impelled toward each other. But as the effect is the same, whether two bodies are reciprocally impelled, or attracted, the word attrac-

tion

tion need not give offence, provided it is not pretended, by that term, to determine the nature itself of the cause.

To avoid all confusion which might result from this mode of expression, it ought rather to be said, that bodies move, as if they mutually attracted each other. This would not decide, whether the powers which act on bodies reside in the bodies themselves, or out of them; and this manner of speaking might thus suit both parties. Let us confine ourselves to the bodies which we meet with on the surface of the earth.

Every one readily admits, that all these would fall downward, unless they were supported. Now, the question turns on the real cause of this fall. Some say, that it is the earth which attracts these bodies, by an inherent power natural to it; others, that it is the ether, or some other subtile or invisible matter, which impels the body downward: so that the effect is, nevertheless, the same in both cases. This last opinion is most satisfactory to those who are fond of clear principles in philosophy, as they do not see, how two bodies at a distance can act upon each other, if there be nothing between them. The others have recourse to the divine Omnipotence, and maintain, that God has endowed all bodies with a power of mutual attraction.

Though it be dangerous to venture on disputing concerning the limits of divine power, it is, nevertheless, certain, that if attraction were an immediate work of that power, without being founded in the

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nature of bodies, this would be the fame thing as faying, that God immediately impels bodies toward each other, and this would amount to a perpetual miracle.

Let us suppose, that before the creation of the world, God had created only two bodies, at a distance from each other; that nothing absolutely existed out of them, and that they were in a state of rest; would it be possible for the one to approach the other, or that they should have a propensity to approach? How could the one feel the other at a distance? Whence could arise the desire of approaching? These are perplexing questions. But if you suppose that the intermediate space is silled with a subtile matter, we can comprehend, at once, that this matter may act upon the bodies, by impelling them; the effect would be the same as if they possessed a power of mutual attraction.

Now, as we know, that the whole space which separates the heavenly bodies, is silled with a subtile matter, called ether, it seems more reasonable to ascribe the mutual attraction of bodies to an action which the ether exercises upon them, though it's manner of acting may be unknown to us, rather than to have recourse to an unintelligible property.

Ancient philosophers satisfied themselves with explaining the phenomena of nature, from qualities which they called occult, saying, for example, that opium causes sleep, from an occult quality, which disposes it to procure sleep. This was saying just nothing, or rather was an attempt to conceal igno-

rance.

rance. We ought, therefore, likewise to consider attraction as an occult quality, in as far as it is given for a property essential to bodies. But, as the idea of all occult qualities is now banished from philosophy, attraction ought not to be considered in this sense.

18th October, 1760.

#### LETTER LXIX.

Nature and Essence of Bodies: or Extension, Mobility, and Impenetrability of Body.

THE metaphysical disquisition, Whether bodies may be endowed with an internal power of attracting each other, without being impelled by an external force, cannot be terminated, till we have examined more particularly the nature of body in general. As this subject is of the last importance, not only in mathematics and physics, but in every branch of philosophy, you must permit me to go into a more particular detail of it.

First, it is asked, What is body? However absurd this question may appear, as no one is ignorant of the difference between what is body and what is not, it is, however, difficult to ascertain the real characters which constitute the nature of bodies. The Cartesians say, it consists in extension, and that whatever is extended is a body. They clearly understand, that extension has, in this case, three dimensions.

fions; and that a fingle dimension, or extension in length only, gives only a line; and that two dimensions, length and breadth, form only a surface, which still is not a body. To constitute a body, therefore, we must have three dimensions, and every body must have length, breadth, and depth, or thickness; in other words, an extension in three dimensions.

But, it is asked, at the same time, if every thing which has extension is a body? This must be the case, if the definition of *Descartes* be just. The idea which the vulgar form of spectres contains extension; it is, however, denied that they are bodies. Though this idea be purely imaginary, it serves to prove, however, that something may have extension without being a body. Besides, the idea which we have of space, contains, undoubtedly, an extension with three dimensions. It is admitted, nevertheless, that space alone is not a body; it only furnishes the place which bodies occupy and fill.

Let us suppose, that all those which are at present in my apartment, air and every thing, were annihilated by the divine Omnipotence, there would remain still in the apartment the same length, breadth and height, but without a body in it. Here, then, is the possibility of an extension that shall not be a body. Such a space, without body in it, is called a vacuum; a vacuum then is extension without body.

It may likewise be said, according to the vulgar superstition, that a spectre has extension, but that body, or corporality, is wanting to it. It is clear, then, that extension is not sufficient to constitute a

body,

body, that fomething more is necessary; hence it follows, that the definition of the Cartesians is not exact. But what more is necessary, beside extension, to constitute a body? The answer is, mobility, or the possibility of being put in motion; for, though a body be at rest, whatever may be the causes which preserve it in that state, it would, however, be possible to move it, provided the powers applied to it were sufficient. By this, space is excluded from the class of bodies, as we see that space, which only serves to receive bodies, remains immoveable, whatever motion the bodies that it contains may have.

It is likewife faid, that, by the help of motion, bodies are transported from one place to another; by which we are given to understand, that the places and space remain unchangeable. My apartment, however, with the vacuum which I have above fupposed, might undoubtedly be moved, and actually is fo, as it follows the motion which carries round the earth itself; here, then, is a vacuum in motion, without being a body. The vulgar fuperfition, too, bestows motion on spectres; and this is sufficient to prove, that the power of being moved, and extenfion, alone, do not constitute the nature of bodies. Something more is wanting; there must be matter to conflitute a body, or rather, it is this which diftinguishes a real body from simple extension, or from a spectre.

Here, then, we are reduced to explain what is to be underflood by the term *matter*, without which extension cannot be body. Now, the fignification of these two terms is so much the same, that all body is matter, and all matter is body; so that even now we have made no great progress. We easily discover, however, a general character, inseparable from all matter, and, consequently, pertaining to all bodies; it is impenetrability, the impossibility of being penetrated by other bodies, or the impossibility that two bodies should occupy the same place at once. In truth, impenetrability is what a vacuum wants in order to be a body.

It will, perhaps, be objected, that the hand may be eafily moved through air and through water, which are, nevertheless, acknowledged bodies; these, then, must be penetrable bodies, and, consequently, impenetrability is not an inherent character of all bodies. But it is worthy of remark, that when you plunge your hand into water, the particles of the water make way for your hand, and that there is no water in the fpace which your hand occupies. If the hand could move through the water, while that fluid did not make room for it, but remained in the place which the hand occupied, then it would be penetrable; but it is evident this is not the case. Bodies, then, are impenetrable: a body, therefore, always excludes, from the place which it occupies, every other body; and as foon as a body enters into any place, it is abfolutely necessary that the body which occupied it. before should leave it. This is the fense which we must affix to the term impenetrability.

21/1 October, 1760.

#### LETTER LXX.

## Impenetrability of Bodies.

THE instance of a spunge will, perhaps, be produced as an objection to the impenetrability of bodies; which, plunged into water, appears completely penetrated by it. But the particles of the fpunge are very far from being fo, in fuch manner as that one particle of the water should occupy the fame place with one particle of the fpunge. We know that fpunge is a very porous body; and that before it is put into the water, it's pores are filled with air; as foon as the water enters into the pores of the spunge, the air is expelled, and disengages itfelf under the form of little bubbles; fo that, in this case, no penetration takes place, neither of the air by the water, nor of the water by the air, as this last always makes it's escape from the places into which the water enters.

It is, then, a general, and effential property of all bodies, to be impenetrable; and, confequently, the justness of this definition must be admitted: that a body is an impenetrable extension; as not only all bodies are extended and impenetrable, but likewise, reciprocally, as that which is, at the same time, extended and impenetrable, is, beyond contradiction, a body. Vacuum is, accordingly, excluded from the class of bodies; for, though it has extension, it wants impenetrability; and wherever we meet with a vacuum, there

there bodies may be introduced, without thrusting any thing out of it's place.

We must attempt to remove another difficulty, raised against the impenetrability of bodies. There are, say the objectors, bodies, which admit of compression into a smaller space, as, for example, wool, and especially air, which it is possible to reduce into a space a thousand times smaller than what it occupies. It appears, then, that the different particles of air are reduced in the same place, and that, consequently, they mutually penetrate.

There is, however, nothing in this; for the air, too, is a body, or a fubstance full of empty pores, or filled with that fluid, incomparably more fubtile, which we call ether. In the first case, no penetration will enfue, as the particles of air only approach nearer to each other, according as the vacuum is diminished; and, in the other case, the ether finds a sufficiency of small passages by which to escape, as the particles of the air approach each other, but all the while without any mutual penetration. For this reason, it is necessary to employ a greater force, when we want to compress the air more: and if the air were compressed to such a degree, that it's minute particles touched each other, we could not carry the compression farther, because, were it possible, the minute particles of the air must mutually penetrate.

It is, then, a necessary and fundamental law in nature, that no two bodies can penetrate each other, or occupy the same place at once: and it is in a conformity to this principle, that we must look for the real source

fource of all the motions which we observe in all bodies, and of the changes which befal them. As two bodies cannot continue their motion without penetrating each other, it is absolutely necessary that the one should give place to the other. If, then, two bodies are moving in the fame line, the one to the left, the other to the right, as it frequently happens at billiards, if each were to continue it's motion, they must mutually penetrate, but this being imposfible, as foon as they come to touch, a flock takes place, by which the motion of each body is almost inftantly changed; and this shock is produced, in nature, only to prevent penetration. The motion of each body is precifely changed no further than is necessary to prevent all penetration; and in this confifts the real cause of all the changes which happen in the world. I want and add not to ont at the

When all these changes are attentively considered, they are found always to take place, in order to prevent some penetration, which, without these changes, must have ensued. At the moment I am writing, I observe, that if the paper were penetrable, the pen would pass freely into it, without writing: but as the paper sustains the pressure of my pen, moistened with ink, it receives from it some particles which form these letters; which could not happen if bodies penetrated each other.

This property of all bodies, known by the term impenetrability, is, then, not only of the last importance, relatively to every branch of human knowledge, but we may consider it as the master-spring which

which nature fets a-going, in order to produce all her wonders. It merits, then, an attentive examination, in order that we may be enabled to explain more clearly the nature of bodies, and the principles of every species of movement, commonly called law of motion.

25th October, 1760.

#### LETTER LXXI.

Of the Motion of the Bodies, real and apparent.

A LL bodies are at rest, or in motion. However evident this distinction may be, it is almost impossible to judge whether a body is in the one state, or in the other. The paper which I see on my table seems to me really at rest; but when I reslect that the whole earth is moving with that astonishing velocity which I explained in a former letter,\* my house, my table, and the paper, must absolutely be carried along with the same rapidity. Thus every thing that seems to be at rest, has, in reality, the same motion as the earth.

We must therefore distinguish between two kinds of rest, the one absolute, the other apparent. Absolute rest takes place when a body remains constantly in the same place, not with relation to the earth, but with relation to the universe. If the fixed stars remained always in the same place of the universe,

they would be at rest, though they seem to move very rapidly; but as we are not certain of it, we must not pretend to assirm, that the sixed stars are in a state of absolute rest.

A body is faid to be in a flate of apparent rest, when it preserves the same situation on the earth. It is likewise to be presumed, that these terms, rest and motion, have been introduced into language to mark rather appearances than truth; and in this sense, I assimply as the whole earth; and that the sun and the fixed stars are in motion, and that a very rapid motion, although they are really at rest. We should, therefore, be ascribing strange and purely metaphysical ideas to these expressions, if we understood by them absolute rest, or motion; and it is absurd to employ, as some persons do, passages of the Holy Scriptures to prove that the earth is at rest, and the sun in motion.

Language is formed for general use; and philosophers are under the necessity of forming a particular language for themselves. As we are incapable to judge of absolute rest, it is very natural for us to consider those bodies as at rest which preserve the same situation relatively to the earth; as it is very probable the inhabitants of other planets, likewise, form their judgment of rest from the same situation relatively to their respective planet.

We observe, that navigators consider as at rest the objects which preserve the same situation relatively to their vessel, and that the coasts which they dis-

cover appear to them to be in motion; and no one thinks of finding fault with their using the common modes of expression. There is, therefore, a great difference between rest and motion, real or absolute, and between rest and motion apparent, or relative to a body, considered at the time as in a state of rest, though perhaps it may be in motion. The principles or laws of motion refer chiefly to the absolute state of bodies, that is, to their rest or motion, real or absolute. In order to discover these laws, we begin with considering a body singly and abstractedly from all others.

This hypothesis, though it never can take place, is, in reality, very proper to affift us in distinguishing what is operated by the nature of body itself, from that which other bodies are capable of operating upon it.

Let a body, then, be alone, and at rest; it may be asked, Will it continue at rest, or will it begin to move? As there is no reason which should incline it to move to one fide rather than to another, it is concluded that it would remain always at reft. The fame thing must happen, on the supposition of the existence of other bodies, provided they do not act on the body in question; hence results this fundamental law: When a body is once in a state of rest, and nothing external acts upon it, it will remain always in that state: and if it begin to move, the cause of motion would be out of it, so that there is nothing in the body itself which is capable of putting it in motion. When, therefore, we see a body which has been at rest begin to TOVED move,

move, we may rest assured that this motion has been occasioned by an exterior power, as there is nothing in the body itself capable of putting it in motion; and if it were alone, and cut off from all communication with other bodies, it would remain always at rest.

However well founded this law may be, and however entitled to rank with geometrical truths, there are perfons little accustomed to profound investigation, who pretend that it is contradicted by experience. They allege the example of a thread, to which a stone is appended; the stone is at rest, but falls the moment that the thread is cut. It is certain, say they, that the action by which the thread is cut is not capable of making the stone move; the stone, therefore, must fall by a power which is proper to itself, and internal.

The fact is certain; but it is evident, at the fame time, that gravity is the cause of the descent, and not an internal power in the stone.

They fay farther, that gravity may be an intrinsic power, attached to the nature of the stone; on which it must be remarked, that gravity is produced either by a subtile matter, or by the attraction of the earth. In the sirst case it certainly is that subtile matter which causes the descent of the stone; in the second, which appears savourable to our opponents, it can with no propriety be affirmed, that the stone descends by an intrinsic power; it is rather the earth which contains the cause of it, and which produces the descent of the stone, by it's attractive power:

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for if the earth did not exist, or were deprived of it's attractive power, they admit that the stone would not descend.

It is certain, therefore, that the cause of the defcent does not refide in the stone itself: the cause, then, is always extrinsic, whether it be in the fubtile matter or in the earth, fuppoling it to be endowed with an attractive power, as the partifans of attraction pretend. This difficulty being removed, the law, which I have laid down, fubfifts in full force; namely, That a body, once at reft, will always remain fo, unless it be put in motion by some foreign cause. This law must take place, provided the body has been at rest but a fingle instant, though it was in motion immediately before; and, when once reduced to a ftate of rest, it will always preserve that state, unless some foreign cause intervene to put it again in motion. This principle being the foundation of all mechanics, it was necessary for me to establish it with all possible precision.

28th October, 1760.

### LETTER LXXII.

Of uniform, accelerated, and retarded Motion-

I RETURN to the case of a body placed in such a manner as to have no connection with any other. Let us suppose it to have received some motion from whatever cause; it remains that we enquire, What

will afterwards happen to it? Will it continue to move? Or will it fuddenly return to a state of rest; or after some time? You must be sensible, that this is an enquiry of some importance, and that all our researches respecting the motion of bodies depend upon it. Let us examine if, by means of reasoning, we are able to resolve it.

A body is at rest, as long as it, and all it's parts, remain in the same place; and it is in motion when that body, or some of it's parts only, pass from one place to another. Now, there are two things to be considered in motion, the direction and the velocity. The direction is the place toward which the body is carried, and the velocity is the space, greater or less, through which it moves in a certain time. I am persuaded you have already juster ideas of this than I could communicate by the most ample explanation. I remark only, that as long as a body preserves the same direction, it moves in a straight line; and reciprocally, as long as a body moves in a straight line, it preserves the same direction; but when it moves in a curve, it is continually changing it's position.

If a body, then, (plate III. fig. 7.) moves in the curve A B C; when it is at A, it's direction is the small line A a; when it is at B, it's direction is the small line B b; and at C, the small line C c. Let these small lines be produced; the continuations of which are marked by the straight dotted lines A L, B M, C N; and it will be affirmed, that when the body passes through A, it's direction is the straight line A L, because, if the body preserved the same di-

rection which it had at A, it would move in the straight line A L. It is evident, then, that it moves in the curve only in so far as it is continually changing it's direction. And when it arrives at B and at C, the direction from which it deviates is expressed by the straight lines B M and C N.\*

A body preferves the same velocity in it's motion as long at it moves through equal spaces in equal times. This motion is called *uniform*. Thus, for example, if a body moves in such a manner as always to proceed ten feet during every second, we call this motion uniform. If another body proceeds twenty feet in a second, it's motion too would be uniform, but it's velocity would be twice as great as that of the preceding.

\* The argument, causa sufficiens, or sufficient reason, is a fort of jargon introduced by fome metaphyficians in the beginning of the present century, which has still it's advocates on the continent. To conclude that a thing is fuch because we see no sufficient reafon to the contrary, is, indeed, a strange method of reasoning. What can be more prepofterous than to employ our ignorance as the instrument of discovering truth? And yet this is the plain flatement of the argument. The instance mentioned in the text, is a noted one, though the ingenious Father Boscovich remarks, that any inference whatever may with equal justice be drawn from the fame premises. Thus, we may say, that no sufficient reason can be given that a moving body A should approach a point B, rather than recede from it; it will, therefore, keep conftantly at the fame diffance, and, confequently, describe a circle about that point. Hence bodies move not in firaight lines, but in circles. In the same manner we might say that motion is not uniform, and indeed prove any thing we pleafe. The fact is, that we derive no part of our knowledge from any abstract reasoning on the nature of things. From

From what I have just said of the uniformity of motion, it is easy to comprehend what is not uniform motion; for when the velocity of a body is not equal, it's motion is not uniform. When the velocity of a body goes on increasing, it's motion is said to be accelerated, and when it is continually diminishing, we say it is retarded. In this last case, the velocity may come to be retarded to such a degree, that the body shall at length come to a state of rest.

Having made these remarks on the velocity and direction of moving bodies, I return to the case of a solitary body, which I suppose to be put in motion by any cause whatever. As soon as it has begun to move, it must have acquired a certain direction, and a certain velocity: and the question is, Will it afterwards preserve the same direction and the same velocity; or, Will it undergo some alteration? We cannot affirm that it will be reduced to a state of rest in an instant, for, in this case, it could not have had any motion, all motion supposing duration, however short. Now, as long as the motion lasts, it is certain that the direction will remain the same.

In truth, it is impossible to conceive why the body should go out of it's road, to one side rather than to another; and, as nothing comes to pass without reason, it follows, that the body in question will always persevere in the same direction, or, that it's motion will proceed in a straight line, which is a great step made toward the decision of the question.

It is likewise maintained, that the velocity of the T 3 body,

body, of which I speak, cannot change: for in that case it must either increase or diminish, and no reason can be assigned capable of producing this change. Hence it is concluded, that this body will always continue to move with the same velocity, and in the same direction, or that it will proceed continually in the direction of a straight line, without ever deviating from it, and always with equal speed. This motion will be performed, then, always in a straight line, and with an equal velocity, without ever being slackened or retarded; the body, therefore, will never be reduced to a state of rest.

What has been faid of a body, which I have fupposed solitary, would happen in like manner to our
globe, if no other bodies had any influence upon it,
for then it would be the same thing as if they did
not exist. The question, then, is resolved. A body
in motion will always preserve it in the same direction, and with the same velocity, unless some external cause interpose, capable of altering it's motion.
So long, therefore, as a body is not subject to the action of some external cause, it will remain at rest, if
it has once been in a state of rest; or will be moved
in the direction of a straight line, and always with
the same velocity, if it has once been put in motion;
and this is the first and principal law of nature on
which the whole science of motion must be founded.

From it we deduce at once this conclusion, that as often as we see a body which was at rest put in motion, or a body moving in a curve line, or whose ve-

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locity changes, it is certain, that an external cause acts upon it. No change can possibly take place either as to direction or velocity, but what is the operation of a foreign cause.

1st November, 1760.

#### LETTER LXXIII.

Principal Law of Motion and Rest. Disputes of Philo-Sophers on the Subject.

WITH whatever folidity this principle is established, that every body put in motion continues to move in the same direction, and with the same velocity, unless some exterior cause interpose to derange this motion; it has, nevertheless, been combated by certain philosophers, who have never made any great progress in the science of motion; while those to whom we are indebted for all the great discoveries which have been made in this science, unanimously agree, that all their researches have proceeded entirely on this principle. It is attacked by two sects of philosophers, whose objections I proceed to propose, and shall endeavour to refute.

It is alleged by the one, That all bodies have a propenfity to rest, which is their natural state, and that motion is to them a state of violence; so that when a body is put in motion, it has a tendency, from it's very nature, to return to the state of rest; and that it makes every effort to destroy it's motion,

independently of every external or foreign cause. They allege, in proof, experience, fo convincing, according to them, that we know of no motion in nature that does not very fenfibly betray this reluctance. Do we not fee, fay they, on the billiard table, that with whatever force we strike a ball, it's motion is quickly flackened, and it foon returns to a flate of rest. As soon as the motion of a clock ceases to be kept up by the external force which fet it a going, it stops. It is remarked of all machines in general, that their motion lasts no longer than the external powers by which they are agitated. Hence they conclude, that a body put in motion is fo far from preserving it from any thing in it's own nature, that, on the contrary, an external force must be employed to keep it up.

You must be sensible that, if this conclusion is just, our principle is completely subverted; as, in virtue of this principle, the ball and the machines in question, once put in motion, must always preserve the same, unless external causes have occasioned some change in it. Thus, in the experiments referred to, had there been no external cause which tended to destroy the motion, we should have been under the necessity of abandoning our principle.

But, if we attend to every thing, we shall find so many obstacles opposed to the motion, that we need no longer wonder it should be so speedily extinguished. In fact, it is first the friction on the billiard table which diminishes the motion of the ball, for it cannot advance without rubbing against the cloth.

Again.

Again, the air being a fubstance, causes likewise a refistance capable of diminishing the motion of bodies. To be convinced of this, you have only to move your hand rapidly through the air. It is evident, then, that in the case of the billiard table, it is the friction and the resistance of the air which counteract the motion of the ball, and soon reduce it to a state of rest.

Now, these causes are external, and it is easily comprehensible that, but for these obstacles, the motion of the ball must have always continued. The same reasoning is applicable to machines of all kinds, in which the friction which acts on the different parts is so considerable, that it is visibly a very sufficient cause of soon reducing the machine to rest.

Having, then, discovered the real causes which produce, in the cases alleged, the extinction of motion, and that these causes are external, and not resident in the moving body, it is evidently false, that bodies have in their nature a propensity to rest. Our principle, therefore, subsists in full force, and even acquires additional strength from the preceding objections. Every body, then, always preserves the motion which it has once received, unless foreign causes interpose to change the direction or the velocity, or both at once. And thus we have got rid of one phalanx of the adversaries who combat our principle.

The other is more formidable, for they are no less than the celebrated Wolfian philosophers. They do not, indeed, openly declare against our principle, nay they even express much respect for it; but they advance others which directly oppose it.

They maintain, That all bodies, in virtue of their nature, are making continual efforts to change their state; that is, when they are at rest, they make an effort to move; and, if they are in motion, make continual efforts to change their velocity and direction. They allege nothing in proof of this affertion, except certain crude reasonings, drawn from their system of metaphysics, which I shall hereafter take occasion to lay before you. I only remark, at prefent, that this opinion is contradicted by the principle which we have so simply established; and by experience, which is in perfect conformity with it.

In fact, if it be true that a body at rest remains, in virtue of it's nature, in that state, it must be undoubtedly false that it should make, in virtue of it's nature, continual efforts to change it's state. And if it be true that a body in motion preserves, in virtue of it's nature, this motion, in the same direction, and with the same velocity, it is impossible that the same body should, in virtue of it's nature, be making continual efforts to change it's motion.

These philosophers, in attempting to maintain, at the same time, the true principle of motion, and their own absurd opinion, have fallen into self-contradiction, and thereby subverted their own system. It is, therefore, placed beyond the reach of dispute, that our principle is sounded in the very nature of body, and that whatever is contrary to it ought to be banished from sound philosophy: and this same principle ciple enables us to clear it of certain fubtilties in which it has been involved.

This principle is commonly expressed in the two following propositions: First; A body once at rest will remain eternally at rest, unless it be put in motion by some external or foreign cause: Secondly; A body once in motion will preserve it eternally, in the same direction, and with the same velocity; or will proceed with an uniform motion, in a straight line, unless it is disturbed by some external, or foreign cause. In these two propositions consists the foundation of the whole science of motion, called mechanics.

4th November, 1760.

#### LETTER LXXIV.

Of the Inertia of Bodies : Of Powers.

As we fay, that a body, so long as it is at rest, remains in the same state, so we likewise say of a body in motion, that as long as it moves in the same direction, and with the same velocity, it remains in the same state. To continue in the same state, then, signifies nothing more than to remain at rest, or to preserve the same motion.

This manner of speaking has been introduced for the purpose of expressing more succinctly our grand principle, that every body, in virtue of it's nature, preserves itself in the same state, till an extraneous cause come to disturb it, that is, to put the body in motion when at rest, or to derange it's motion. It must not be imagined that a body, in order to preserve the same state, must remain in the same place; this, indeed, is the case when the body is at rest; but when it moves with the same velocity, and in the same direction, we say, equally, that it continues in the same state, though it is every instant changing it's place. It was necessary to make this remark, to prevent the possibility of consounding change of place with that of state. If it be now asked, Why bodies continue in the same state? The answer must be, that this is in virtue of their peculiar nature.

All bodies, in as far as they are composed of matter, have the property of remaining in the same state, if they are not drawn out of it by some external cause. This, then, is a property sounded on the nature of bodies, by which they endeavour to preserve themselves in the same state, whether of rest or motion. This quality with which all bodies are endowed, and which is essential to them, is called inertia,\* and it enters as necessarily into their constitution as extension and impenetrability; to such a de-

\* We have already in common use, in our own language, the adjective inert, and the adverb inertly, and their meaning is generally understood. But hitherto no author of name, except in works of philosophy, has ventured to introduce the correspondent substantive noun into general composition, much less to clothe it with an English form. The Latin term inertia is, therefore, retained in this translation. The linguist and the philosopher need no interpretation. The unlearned reader is referred to what Mr. Euler says in the context, or to the explanation of foreign and scientific terms affixed to this work.—E. E.

gree, that it would be impossible for a body to exist, divested of this inertia.

This term was first introduced into philosophy by those who maintained that all bodies have a propensity to rest. They considered bodies as somewhat resembling indolent persons, who prefer rest to exertion, and ascribed to bodies an aversion to motion, similar to that which sluggards have for labour; the term inertia signifying nearly the same thing as sluggishness. But though the salfeness of this opinion has been since detected, and though it is certain that bodies remain equally in their state of motion, as in that of rest, yet the term inertia has been still retained to denote in general the property of all bodies to continue in the same state, whether of rest or of motion.\*

The exact idea of inertia, therefore, is a repugnance to every thing that has a tendency to change the state of bodies; for as a body, in virtue of it's nature, preserves the same state of motion, or of rest, and cannot be drawn out of it but by external causes, it follows that, in order to a body's changing it's

\* The diftinguishing property of inanimate matter is it's absolute passiveness or want of disposition to change it's state, whether that of rest, or of motion. The term inertia is improper, since it conveys an idea of sluggishness, or a reluctance to be put in motion; whereas bodies are obedient to the smallest impulse, and the action generated is ever proportioned to the force. The expression vis inertiæ, commonly used, is really a contradiction of terms. Indeed, it would be no differvice to natural philosophy, if the law that "action and re-action are equal and opposite," were entirely omitted.—E. E.

ftate, it must be forced out of it by some external cause: without which it would always continue in the same state. Hence it is, that we give to this external cause the name of power or force. It is a term in common use, though many by whom it is employed have but a very imperfect idea of it.

From what I have just said you will see that the word force signifies every thing that is capable of changing the state of bodies. Thus, when a body which has been at rest is put in motion, it is a force which produces this effect; and when a body in motion changes it's direction, or velocity, it is likewise a force which produces this change. Every change of direction, or of velocity, in the motion of a body, requires either an increase or a diminution of force. Such force, therefore, is always out of the body whose state is changed; for we have seen that a body left to itself, preserves always the same state, unless a force from without acts upon it.

Now, the *inertia* by which a body tends to preferve itself in the same state, exists in the body itself, and is an essential property of it: when, therefore, an external force changes the state of any body, the *inertia* which would maintain it in the same state, opposes itself to the action of that force; and hence we comprehend, that the *inertia* is a quality susceptible of measurement, or that the *inertia* of one body may be greater or less than that of another body.

But bodies are endowed with this inertia in as far as they contain matter. It is even by the inertia, or the relistance which they oppose to every change of

state, that we judge of the quantity of a body; the inertia of a body, accordingly, is greater in proportion to the quantity of matter which it contains. Hence we conclude, that it requires a greater force to change the state of a great body, than that of a small one; and we go on to conclude, that the great body contains more matter than the small one. It may even be affirmed that this single circumstance, the inertia, renders matter sensible to us.

It is evident, then, that the *inertia* is fusceptible of measurement, and that it is the same with the quantity of matter which a body contains: as we denominate, likewise, the quantity of matter in a body, it's mass, the measure of the *inertia* is the same as that of the mass.

To this, then, is reduced our knowledge of bodies in general. First, we know, that all bodies have an extension of three dimensions; fecondly, that they are impenetrable; and hence refults their general property, known by the name of inertia, by which they preferve themselves in their state; that is, when a body is at rest, by it's inertia it remains so; and when it is in motion, it is likewife by it's inertia that it continues to move with the fame velocity, and in the fame direction; and this prefervation of the fame state lasts till some external cause interpose to produce a change in it. As often as the ftate of a body changes, we must never look for the cause of fuch change in the body itself; it exists always out of the body, and this is the just idea which we must form of a power or force.

8th November, 1760.

## LETTER LXXV.

Changes which may take place in the State of Bodies.

THE fundamental principle of mechanics, with the idea of inertia, which I have endeavoured to explain, enables us to reason on solid ground respecting various phenomena presented to us in nature. On seeing a body in motion, which should proceed uniformly in a straight line, that is, which should preserve the same direction, and the same velocity, we would say, that the cause of this continuation of motion is not to be found out of the body, but that it is founded in it's very nature, and that, in virtue of it's inertia, it remains always in the same state; as we would say, were the body at rest, that this took place in virtue of it's inertia.

We would likewise be right in saying that this body undergoes no action from any external cause; or, if any such existed, that these powers reciprocally destroyed each other in such a manner that the body is in the state in which it would be if no force acted upon it.

If it is asked, then, Why the body continues to move in this manner? The answer is obvious. But if it is asked, Why this body has begun thus to move? The question is totally different. It must be said, that this motion has been impressed upon it by some external force, if it was before at rest; but it would be impossible to assirm any thing with cer-

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tainty respecting the quantity of that sorce, because, perhaps, no traces of it remain. It is, therefore, abundantly ridiculous to ask, Who impressed motion on every body at the beginning of the world? Or, Who was the prime mover? Those who put the question admit, then, a beginning, and, consequently, a creation; but they imagine that God created all bodies at rest. Now, it may be answered, That he who could create bodies could impress motion upon them. I ask them, in my turn, If they believe it to be more easy to create a body at rest than in motion? They both equally require the omnipotence of God, and this question belongs not to the province of philosophy.

But when a body has once received motion, it preserves that motion by it's own nature, or by it's inertia, in the same state in which it must constantly remain, until a force, or some foreign cause, oppose an obstacle to it. As often, then, as we observe that a body does not remain in the same state, that a body at rest begins to move, or that a body in motion changes it's direction, or velocity, we must admit that this change has it's cause out of the body, and that it is occasioned by a foreign force. Thus, as a stone, left to itself, descends, the cause of that descent is foreign to the body, and it is not from it's own nature that the body descends, but from the effect of a foreign cause, to which we give the name of gravity.

Gravity, then, is not an intrinsic property of body; Vol. I. U it

it is rather the effect of a foreign force, the fource of which must be sought for out of the body. This is geometrically true, though we know not the foreign forces which occasion gravity. It is the same when we throw a ftone. We fee clearly, that it does not follow, in it's motion, the direction of a straight line, and that it's velocity does not always continue the fame. It is gravity, likewife, which changes the direction or the velocity of the body; but for it, the stone would describe a straight line in the air, and proceed forward with the fame velocity; and were gravity to be fuddenly annihilated, during the motion of the stone, it would continue to move in a ftraight line, and would preferve the fame direction, and the fame velocity, which it had at the instant when gravity ceafed to act upon it.

But as gravity acts continually, and upon all bodies, we need not be furprized, that we meet with no motion in which the direction and the velocity continue the fame. The case of rest may very well take place; it is when something invincibly opposes the fall of a body; thus the sloor of my apartment prevents my falling into that below it. But the bodies which appear to us at rest, are carried along by the motion of the earth, which is neither rectilinear nor uniform: it cannot be affirmed, therefore, that these bodies remain in the same state. Neither is there one of the heavenly bodies which moves in a straight line, and always with the same velocity: they are continually changing their state; and even the forces which produce

duce this continual change are not unknown to us; they are the attractive powers which the heavenly bodies exercise over one another.

I have already remarked, that these forces may, very probably, be caused by the subtile matter which surrounds all the heavenly bodies, and fills the whole space of the heavens; but, according to the opinion of those who consider attraction as a power inherent in matter, this force is always foreign to the body on which it acts. Thus, when we say the earth is attracted toward the sun, it is acknowledged, that the force which acts upon the earth is not resident in the earth itself, but in the sun; as in fact, if the sun did not exist, there would be no such force.

This opinion, however, that attraction is effential to all matter, is fubject to fo many other inconveniences, that it is hardly possible to allow it a place in a rational philosophy. It is certainly much fafer to proceed on the idea, that what is called attraction, is a power contained in the subtile matter which fills the whole space of the heavens; though we cannot tell how. We must accustom ourselves to acknowledge our ignorance on a variety of other important subjects.

11th November, 1760.

#### LETTER LXXVI.

# System of the Monads of Wolff.

BEFORE I attempt to make you fensible of the truth of the principle, that all bodies, of them-felves, always preserve the same state of rest, or motion, I must remark, that if we consult experience only on the subject, without thoroughly investigating it by the powers of reasoning, we would be disposed to draw the directly opposite conclusion, and to maintain, That bodies always have a propensity to be continually changing their state; as we see nothing in the whole universe, but a perpetual change in the state of bodies. But we have just shewn what are the causes which produce these changes, and we are assured, that they are not to be found in the bodies whose state is changed, but out of them.

The principle, then, which we have established, is so far from being contradicted by experience, that it is, on the contrary, confirmed by it. You will easily judge from this, how several great philosophers, misled by an experience not accurately understood, have fallen into the error of maintaining, That all bodies are endowed with powers, disposing them continually to change their state.

It is thus that Wolff has reasoned. He says: 1. Experience shews us all bodies perpetually changing their state; 2. Whatever is capable of changing the state of bodies, is called force; 3. All bodies, there-

fore,

fore, are endowed with a force capable of changing their state; 4. Every body, therefore, is making a continual effort to change; 5. Now, this force belongs to body, only so far as it contains matter; 6. It is, therefore, a property of matter to be continually changing it's own state; 7. Matter is a compound of a multitude of parts, denominated the elements of matter; therefore, 8. As the compound can have nothing but what is founded in the nature of it's elements, every elementary part must be endowed with the power of changing it's own state.

These elements are simple beings; for if they were composed of parts, they would be no longer elements, but their parts would be so. Now, a simple being is likewise denominated monad; every monad, therefore, has the power of continually changing it's state. Such is the foundation of the system of monads, which you may have heard mentioned, though it does not now make such a noise as it formerly did. I have marked by sigures the several propositions on which it is established, for the purpose of making a more distinct reference, in the reslections I mean to make upon them.

I have nothing to fay respecting the sirst and second; but the third is very equivocal, and altogether salse, in the sense in which it is taken. Without meaning to say, that the forces which change the state of bodies, proceed from some spirit, I readily agree, that the sorce, by which the state of every body is changed, subsists in body, but, it being always understood, that it subsists in another body, and never

in that which undergoes the change of state; which has rather the contrary quality, that of persevering in the same state. In so far, then, as these forces subsist in bodies, it ought to be said, that these bodies, as long as they have certain connections with each other, may be capable of supplying forces by which the state of another body is changed. It follows, that the sourch proposition must be absolutely salse; and the result, from all that went before, rather is, that every body is endowed with the power of remaining in the same state, which is directly the opposite of the conclusion which these philosophers have drawn.

And I must here remark, that it is rather absurd to give the name of force to that quality of bodies by which they remain in their state; for if we are to understand by the term force every thing that is capable of changing the state of bodies, the quality by which they persevere in their state, is rather the opposite of a force. It is, therefore, by an abuse of language, that certain authors give the name of force to the inertia, which is that quality, and which they denominate the inert force.

But, not to wrangle about terms, though this abuse may lead to very gross errors, I return to the system of monads: and as proposition 4, is false, those that follow, which are successively founded upon it, must, of necessity, be so too. It is false, then, likewise, that the elements of matter, or monads, if such there be, are possessed of the power of changing their state. The truth is rather to be founded in the opposite quality,

quality, that of perfevering in the same state; and thereby the whole system of monads is completely subverted.

These philosophers attempted to reduce the elements of matter to the class of beings, which comprehends spirits and souls, endowed, beyond the power of contradiction, with the faculty of changing their state; for, while I am writing, my soul continually represents other objects to itself, and these changes depend entirely on my will: I am thoroughly convinced of it, and not the less so, that I am mastter of my own thoughts; whereas the changes which take place in bodies, are the effect of an extraneous force.

Add to this, the infinite difference between the state of body, capable only of one velocity and of one direction, and the thoughts of spirit, and you will be entirely convinced of the falsehood of the sentiments of the materialists, who pretend that spirit is only a modification of matter. These gentlemen have no knowledge of the real nature of bodies.

15th November, 1760.

### LETTER LXXVII.

Origin and Nature of Powers.

T is, undoubtedly, very furprizing, that, if every body has a natural disposition to preserve itself in the same state, and even to oppose all change, all the bodies in the universe should, nevertheless, be U 4 continually

continually changing their state. We are well assured, that this change can be produced only by a force not resident in the body whose state is changed. Where, then, must we look for those powers, which produce the incessant changes that take place in all the bodies of the universe; and which are, nevertheless, foreign to body?

Must we then suppose, besides these existing bodies, particular beings which contain those powers? Or, are the powers themselves particular substances existing in the world? We know but of two kinds of beings in it, the one which comprehends all bodies, and the other all intellectual beings, namely, the spirits and souls of men, and those of animals. Must we establish, then, in the world, besides body and spirits, a third species of beings, under the name of power, or force? Or, are they spirits which incessantly change the state of bodies?

Both of these labour under too many disticulties to be hastily adopted. Though it cannot be denied, that the souls of men, and of beasts, have the power of producing changes in their bodies, it were, however, absurd to maintain, that the motion of a ball, on the billiard table, was retarded and destroyed by some spirit; or that gravity was produced by a spirit continually pressing bodies downward; and that the heavenly bodies, which, in their motion, change both direction and velocity, were subjected to the action of spirits, according to the system of certain ancient philosophers, who assigned to each of the heavenly bodies, a spirit, or angel, who directed it's course.

Now, on reasoning with solidity, respecting the phenomena of the universe, it must be admitted, that, if we except animated bodies, that is, those of men and beasts, every change of state which befalls other bodies, is produced by merely corporeal causes, in which spirits have no share. The whole question, then, is reduced to this, Whether the forces which change the state of bodies, exist separately, and constitute a particular species of beings, or whether they exist in the bodies?

This last opinion appears, at first fight, very unaccountable; for if all bodies have the power of preferving themselves in the same state, how can it be possible they should contain powers that have a tendency to change it? You will not be surprized to hear, that the origin of sorce has, in all ages, been a stumbling-block to philosophers. They have all considered it as the greatest mystery in nature, and as likely to remain for ever impenetrable. I hope, however, I shall be able to present you with a solution, so clear of this pretended mystery, that all the difficulties which have hitherto appeared insurmountable, shall wholly vanish.

I fay, then, that however strange it may appear, this faculty of bodies, by which they are disposed to preserve themselves in the same state, is capable of supplying powers which may change that of others. I do not say, that a body ever changes it's own state, but that it may become capable of changing that of another. In order to enable you to get to the bottom of this mystery, respecting the origin of sorce,

it will be fufficient to confider two bodies, as if no others existed.

Let the body A (plate III. fig. 4.) be at rest, and let the body B have received a motion in the direction B A, with a certain velocity. This being laid down, the body A is disposed to continue always at rest; and the body B to continue it's motion along the straight line B A, always with the same velocity, and both the one and the other in virtue of it's inertia. The body B will, at length, then come to touch the body A. What will be the confequence? As long as the body A remains at rest, the body B could not continue it's motion, without paffing through the body A, that is, without penetrating it; it is impossible, then, that each body should preserve itself in it's state, without the one's penetrating the other. But this penetration is impossible; impenetrability being a property common to all bodies.

It being impossible, then, that both the one and the other should preserve it's state, the body A must absolutely begin to move, to make way for the body B, that it may continue it's motion; or, that the body B, having come close to the body A, must have it's motion destroyed; or, the state of both must be changed, as much as is necessary, to put them in a condition to continue, afterward, each in his proper state, without mutual penetration.

Either the one body, therefore, or the other, or both, must absolutely undergo a change of their state, and the cause of this change, infallibly exists in the impenetrability of the bodies themselves; since every cause, capable of changing the state of bodies, is demonstrated force, it is then, of necessity, the impenetrability of the bodies themselves, which produces the force, by which this change is effected.

In fact, as impenetrability implies the impossibility, that bodies should mutually penetrate, each of them opposes itself to all penetration, even in the minutest parts; and to oppose itself to penetration, is nothing else, but to exert the force necessary to prevent it. As often, then, as two or more bodies cannot preserve themselves in their state, without mutual penetration, their impenetrability always exerts the force necessary to change it, as far as is requisite, to prevent the slightest degree of penetration.

The impenetrability of bodies, therefore, contains the real origin of the forces, which are continually changing their state in this world: and this is the true solution of the great mystery, which has perplexed philosophers so grievously.

18th November, 1760.

# LETTER LXXVIII.

The same Subject. Principle of the least possible Action.

OU have now made very confiderable progrefs in the knowledge of nature, from the explanation of the real origin of the powers capable of changing the state of bodies; and you are, at prefent, in a condition easily to comprehend, why all those

those of this world are subject to an incessant change of state, from rest to motion, or from motion to rest.

First, we are certain, that the world is filled with matter. Here below, it is evident, that the space which feparates the grofs bodies fenfible to feeling, is occupied by the air, and that, when we make a vacuum in any fpace, the ether inftantly fucceeds, and it, likewife, fills the space in which the heavenly bodies move. All space being thus full, it is imposfible that a body in motion should continue it a single instant, without meeting others, through which it must pass, if they were not impenetrable. And, as this impenetrability of bodies exerts always, and univerfally, a force which prevents all penetration, it must be continually changing the state of bodies; it is not at all furprizing, then, that we should observe perpetual changes in the state of bodies, though every one has a tendency to preferve itself in the fame state.

If they could penetrate each other freely, nothing would prevent any one from remaining perfeveringly in it's state; but being impenetrable, there must thence, necessarily, result force sufficient to prevent all penetration; and no more results than what is precisely needful.

While they can continue in the fame state, without any injury to impenetrability, they then exert no force, and bodies remain in their state; it is only to prevent penetration, that impenetrability becomes active, and supplies a force sufficient to oppose it.

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When, therefore, a small force suffices to prevent penetration, impenetrability exerts that, and no more; but when a great force is necessary for this purpose, impenetrability is ever in a condition to supply it.

Thus, though impenetrability fupplies these powers, it is impossible to say, that it is endowed with a determinate force; it is rather in a condition to supply all kinds of sorce, great or small, according to circumstances; it is even an inexhaustible source of them. As long as bodies are endowed with impenetrability, this is a source which cannot be dried up; this force absolutely must be exerted, or bodies must mutually penetrate, which is contrary to nature.

It ought, likewife, to be remarked, that this force is never the effect of the impenetrability of a fingle body; it refults always from that of all bodies at once, for if one of the bodies was penetrable, the penetration would take place, without any need of a power to effect a change in their state. When, therefore, two bodies come into contact, and when they cannot continue in their state without penetrating each other, the impenetrability of both acts equally; and it is by their joint operation, that the force neceffary to prevent the penetration is fupplied: we then fay, that they act upon each other, and that the force, refulting from their impenetrability, produces this effect. This force acts upon both of them; for as they have a tendency toward mutual penetration, it repels both the one and the other, and thus prevents their penetration.

It is certain, then, that bodies may act upon each other; and we fpeak fo frequently of this action, as when two billiard balls clash, it is said, the one acts upon the other, that you must be well acquainted with this mode of expression. But it must be carefully remarked, that, in general, bodies do not act upon each other, but in so far as their state becomes contrary to impenetrability; from whence results a force capable of changing it, precisely so much as is necessary to prevent any penetration; so that a small force would not have been sufficient to produce this effect.

It is very true, that a greater force would, like-wife, prevent the penetration; but when the change produced in the state of bodies is sufficient to prevent mutual penetration, the impenetrability acts no farther, and there results from it the least force that is capable of preventing the penetration. Since, then, the force is the smallest, the effect which it produces, that is, the change of state which it operates, in order to prevent penetration, will be proportional; and, consequently, when two or more bodies come into contact, so that no one could continue in it's state without penetrating the others, a mutual action must take place, which is always the smallest that was capable of preventing penetration.

You will find here, therefore, beyond all expectation, the foundation of the fystem of the late Mr. de Maupertuis, so much cried up by some, and so violently attacked by others. His principle is, that of

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the least possible action; by which he means, that, in all the changes which happen in nature, the cause which produces them, is the least that can be.

From the manner in which I have endeavoured to unfold this principle to you, it is evident, that it is perfectly founded in the very nature of body, and that those who deny it, are much in the wrong, though still less than those who would turn it into ridicule. You will already, perhaps, have remarked, that certain persons, no great friends to Mr. de Maupertuis, take every opportunity of laughing at the principle of the least possible action, as well as at the hole continued down to the centre of the earth; but, fortunately, truth suffers nothing by their pleafantry.

22d Nov. 1,60.

### LETTER LXXIX.

30-360 m

On the Question, Are there any other Species of Powers?

THE origin of powers, founded on the impenetrability of bodies, which I have been endeavouring to explain, is by no means inconfistent with the opinion of those who maintain, that the fouls of men, and those of beasts, have the power of acting on their bodies. There is nothing to hinder the existence of two kinds of power, which produce all the changes that take place in the world; the one corporeal, which derives it's origin from the impenetrability netrability of bodies: and the other spiritual, which the souls of animals exercise over their bodies: but this last power operates only upon animated bodies; and the Creator has so clearly distinguished it from the other, that it is not permitted, in philosophy, to consound them.

But this distinction greatly embarrasses those, who consider attraction as an inherent quality of bodies; for, if they act upon each other, only to maintain their impenetrability, attraction cannot be referred to this case. Two distant bodies may preserve each it's state, without at all interesting their impenetrability, and without there being any reason, of consequence, why the one should act upon the other, even by attracting it.

Attraction, therefore, ought to be referred to a third fpecies of power, which should be neither corporeal nor fpiritual. But it is always contrary to the rules of a rational philosophy to introduce a new fpecies of powers, before their existence is incontestably demonstrated. It would have been necessary, therefore, for this effect, to have proved, beyond contradiction, that the powers by which bodies mutually attract, could not derive their origin from the fubtile matter which furrounds them; but this imposlibility is not yet demonstrated. It would appear, on the contrary, that the Creator has expressly filled the whole space of the heavens with a subtile matter, to give birth to these powers, which impel bodies toward each other, conformably to the law, before established, respecting their impenetrability.

In fact, the fubtile matter might very well have a motion fuch as that a body in it should not be able to preserve it's state, without being penetrated by it; and then this force must be derived, as well from the impenetrability of the subtile matter, as from that of the body itself.

Were there a fingle case in the world, in which two bodies attracted each other, while the intermediate space was not filled with a subtile matter, the reality of attraction might very well be admitted; but as no such case exists, we have, consequently, reason to doubt, nay, even to reject it. We know, then, but two sources of all the powers which produce these changes, the impenetrability of body, and the action of spirit.

The disciples of Wolff reject, likewise, this law, and maintain, That no spirit, or immaterial substance, can act upon a body; and they are very much embarraffed, when it is alleged, that, according to them, God himself, who is a spirit, could not have the power of acting upon bodies, which favours ftrongly of atheism. They are, accordingly, reduced to this feeble reply, that it is by infinity God is able to act upon body; but if it be impossible for a spirit, as a fpirit, to act upon a body, this impotence necessarily recoils on God himfelf. And who can deny, that our foul acts upon our body? I am to fuch a degree mafter of my members, that I can put them in action as I pleafe. The fame thing may be affirmed, likewife, of the brute creation; and as, according to the fystem of Descartes, at which we have good VOL. I. reafon reason to smile, beasts are mere machines, without any feeling, like a watch, as the Wolsians would have it, men too are merely machines.

These same philosophers, in their speculations, go, likewise, so far as to deny the first species of powers, of which they know nothing. For, not being able to comprehend how one body acts upon another, they boldly deny it's action, and maintain, that all the changes which befall a body, are produced by it's own powers.

They are the philosophers whom I formerly mentioned, as denying the first principle of mechanics, respecting the preservation of the same state, which is sufficient to subvert their whole system. The error into which they have fallen, as I have already remarked, arises from their reasoning inconclusively respecting the phenomena which bodies present to us. They concluded precipitately, from observing almost all bodies continually changing their state, that they contained in themselves the powers, by which they incessantly exert themselves to change it, whereas they ought to have drawn the directly opposite conclusion.

It is thus, that, by confidering objects in a fuperficial manner, we hurry into the groffest errors. I have already pointed out the defects of this reasoning; but, once fallen into error, they have abandoned themselves to the most absurd ideas. They, first, ascribed these internal powers to the primary elements of matter, which, according to them, are continual efforts to change their state, and concluded from from it, that all the changes to which every element is subjected, are produced by it's own power, and that two elements, or simple beings, cannot act upon each other. This being laid down, it was necessary to divest spirits, as simple beings, of all power of acting upon body, excepting, however, the Supreme Being; and then, as bodies are composed of simple beings, they were under the necessity of denying, also, that bodies could act upon each other.

It was in vain to object to them, the case of bodies which clash, and the change of their state, which results from it. Obstinately prepossessed in favour of the solidity of their reasoning, they scorned to abandon it: they chose rather to assirm, that every body, from it's own nature, produces the change which besalls it, and that the collison has nothing to do with it; that it is a mere illusion which makes us believe the collison to be the cause of it; and they go off in triumph at the sublimity of a philosophy, so far beyond the comprehension of the vulgar. You are now in a condition to estimate it, according to it's real importance.

25th November, 1760.

### LETTER LXXX.

Of the Nature of Spirits.

I FLATTER myfelf, that you are now convinced of the folidity of the reasonings, on which I have established the knowledge of bodies, and that of the X 2 powers

powers which change the state of them. The whole is founded on experiments the most decisive, and on principles dictated by reason. They involve no absurdity, nor are they contradicted by other principles, equally certain. It is not long since any successful progress was made in researches of this kind. Such strange ideas were, formerly, entertained respecting the nature of bodies, that all kinds of powers were ascribed to them, of which some must necessarily design the others.

Certain philosophers have even gone so far, as to imagine, that matter itself might be endowed with the faculty of thought. These gentlemen, known by the name of materialists, maintain, that our fouls, and all spirits, in general, are material; or rather, they deny the existence of fouls and spirits. But when once we have got into the right road to the knowledge of bodies; the inertia, by virtue of which they continue in their state; and impenetrability, that quality by which they are fubjected to powers capable of changing it; all those phantoms of powers, to which I alluded, vanish away, and nothing appears a more glaring abfurdity than to affirm, that matter is capable of thought. To think, to judge, to reafon, to possess mental feeling, to reflect and will, are qualities incompatible with the nature of bodies; and beings invefted with them, must be of a different nature. Such are fouls and fpirits; and He who poffesses those qualities in the highest degree, is Goo.

There is, then, an infinite difference between body and fpirit. Extension, inertia, and impenetrability, qualities qualities which exclude all thought, are the properties of body: but spirit is endowed with the faculty of thinking, of judging, of reasoning, of feeling, of reflecting, of willing, or of determining, in favour of one object preferably to another. There is here neither extension, nor inertia, nor impenetrability; these material qualities are infinitely remote from spirit.

It is asked, What is a spirit? I acknowledge my ignorance in respect of this, and I reply, That we cannot tell what it is, as we know nothing of the nature of spirit.

But it is not the lefs certain, that this world contains two kinds of beings; beings corporeal or material, and beings immaterial or spiritual, which are of a nature entirely different, as they manifest themselves to us by properties which have no relation to each other. These two species of beings are, nevertheless, most intimately united, and upon their union, principally, depend all the wonders of the world, which are the delight of intelligent beings, and lead them to glorify their CREATOR.

It is certain, that spirits constitute the principal part of the world, and that bodies are introduced into it merely to serve them. For this reason it is, that the souls of animals are in an union so intimate with their bodies. Not only do the souls perceive all the impressions made upon their bodies; but they have the power of acting upon these bodies, and of producing in them corresponding changes: and thus

they exercise an active influence over the rest of the world.

This union of the foul with the body, undoubtedly, is, and ever will be, the greatest mystery of the divine Omnipotence, a mystery which we shall never be able to unfold. We are perfectly sensible, that the human foul cannot act immediately on all the parts of the body; as soon as a certain nerve is cut, I can no longer fold my hand: from which it may be concluded, that the soul has power only over the extremities of the nerves, which all terminate and unite in a portion of the brain, the place of which the most skilful anatomist is unable exactly to assign. To this, then, the power of the soul is restricted. But that of God, being unlimited, extends to the whole universe, and exerts itself by means which far exceed our comprehension.

19th November, 1760.

### LETTER LXXXI.

Of the Union between the Soul and the Body.

A S spirits and bodies are beings, or substances, of a nature totally different, the world contains, then, two kinds of substances, the one spiritual, and the other corporeal, or material. The strict union which subsists between them merits a very particular attention.

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This union of foul and body, in every animal, is a most wonderful phenomenon. It is reduced to two things, the one, that the foul feels, or perceives, all the changes which befall it's body, by means of the fenses, which, as you know perfectly well, are five in number, namely, seeing, hearing, smelling, tasting, and touching. By these, then, the soul takes cognizance of every thing that passes, not only in it's own body, but out of it. Touching and tasting represent to it those objects only which are in immediate contact with the body; smelling, objects at a small distance; hearing extends to distances much more remote; and sight procures for us the knowledge of the most distant objects.

All this knowledge is acquired, only in fo far as the objects make an impression on some one of our senses, but still, this is not sufficient, it is necessary, that the organ of such sense should be perfectly sound, and the nerves belonging to it must not be deranged. You will recollect, that, in order to see, the objects must be painted distinctly in the bottom of the eye, on the retina; but still, this representation is not the object of the soul; one may be blind, though it is perfectly well expressed. The retina is a contexture of nerves, the continuation of which extends to the brain; and if this continuation is interrupted by any injury done to this nerve, called the optic nerve, there will be no sight, however perfect the representation on the retina may be.

It is the fame with respect to the other senses, all of which operate by means of nerves destined to con-

vey the impression made on the organ, employed in the sensation, up to it's first origin in the brain. There is, then, in the brain, a certain place where all the nerves terminate; there the soul resides, and there perceives the impressions made upon it by means of the senses.

From these impressions, the soul derives all the knowledge it has of things out of itself; thence it derives it's first ideas, and by their combination forms judgments, reslections, reasonings, and every thing necessary to perfect it's knowledge; such is the work of the soul, in which the body has no share. But the first impression comes to it from the senses, through the bodily organs: and the first faculty of the soul is to perceive, or to feel, what passes in that part of the brain, in which all the sensitive nerves terminate. This faculty is denominated seeling, or sensation, and the soul, nearly passive, does nothing, in the first instance, but receive the impressions which the body presents to it.

But it possesses, in it's turn, an active faculty, by means of which it has the power of influencing it's body, and of producing motions in it, at pleasure: in this consists it's power over the body. Thus I am able to move my hands and my feet by an act of my will; and, What motions are my fingers making, as I write this letter? My foul, however, cannot act immediately on any one of my fingers; in order to put a fingle one in motion, it is necessary that several muscles should be put in action, and this action, again, exerts itself by means of nerves terminating

in the brain: if fuch a nerve be injured, to no purpose will I wish my singer to move; it will no longer obey the orders of my soul: thus the power of my soul extends only to a small portion of the brain, where all the nerves unite; sensation is likewise restricted to this place of the brain.

The foul, then, is united only with these extremities of the nerves, on which it has not only the power of acting, but by means of which it can view, as in a mirror, every thing that makes an impression on the organs of it's body. What wonderful address, to be able to conclude, from the slight changes which take place in the extremity of the nerves, that which occasioned them out of the body!

A tree, for example, produces on the retina, by it's rays, an image which is perfectly fimilar to it: but how feeble must the impression be which the nerves receive from it! It is this impression, however, continued along the nerves up to their origin, which excites in the soul the idea of that tree. Asterwards, the slightest impressions which the soul makes on the extremities of the nerves, are instantly communicated to the muscles, which, put in action, oblige the member which it wills to move, exactly to obey it's orders.

Machines, which receive certain motions by the drawing of a string, present but a coarse mechanism, compared to our bodies and the bodies of animals. The works of the Creator infinitely surpass the productions of human skill,

### LETTER LXXXII.

Different Systems, relative to this Subject.

IN order to elucidate the twofold union of foul and body, we may compare the foul to a man, who contemplates, in a dark room, the external objects, and from their images derives the knowledge of what is paffing out of the room. The foul viewing, in like manner, if I may fo express myself, the extremities of the nerves, which unite in a certain part of the brain, perceives all the impressions made upon the nerves, and arrives at the knowledge of the external objects, which have made these impressions on the organs of fense. Though we do not know wherein confists the refemblance of the impressions made on the extremities of the nerves, with the objects themselves which occasioned them, they are, however, very proper to fupply the foul with a very just idea of them.

The action by which the foul, operating on the extremities of the nerves, can put in motion, at pleafure, the members of the body, may be compared to that of a player on puppets, who, by pulling a ftring, makes them ftrut about, and move their limbs as he pleafes. This comparison is, however, very imperfect, for the union of the foul and body is infinitely more intimate.

The foul is not fo indifferent, in refpect of feeling, as the man placed in the dark room; it is much more deeply

deeply interested in what is going on. There are sensations highly agreeable to it, and others very disagreeable, and even painful. What more disagreeable than acute pain, though it proceed but from a bad tooth? This, however, is no more than a nerve irritated in a certain manner, and yet it excites, in the soul, pain intolerable.

In whatever light we confider the strict union of foul and body, which constitutes the essence of a living man, it must ever remain an inexplicable mystery; and, in all ages, philosophers have taken fruit-less pains, in the hope of arriving at a satisfactory solution. Various systems have been devised in this view.

The first is, that by which a real influence is eftablished of body on foul, and of foul on body; fo that the body, by means of the fenses, supplies the foul with it's first perceptions of external things; and that the foul, by acting immediately on the nerves, in their origin, excites in the body the motion of it's members; though it is, at the fame time, acknowledged, that the manner of this mutual influence is abfolutely unknown to us. We must, undoubtedly, have recourse to the omnipotence of God, who has given to every foul, a power over the portion of matter containing the extremities of the nerves of the body, fo that the power of every foul is restricted to a small part of the body, whereas the power of God extends to all the bodies of the universe. This fystem seems the most conformable to truth, though we are very far from pretending to have a particular knowledge of it.

The other two fystems are the invention of philofophers, who boldly deny the possibility of a real influence of spirit upon bodies; though they are under the necessity of allowing it to the Supreme Being. According to them, the body cannot supply the soul with the first ideas of external things, nor the soul produce any motion in the body.

One of these two systems was the invention of Descartes; it goes by the name of the system of occassional causes. According to this philosopher, when the organs of sense are excited by exterior bodies, God immediately impresses on the soul, at the same instant, the ideas of these bodies; and when the soul wills, that any member of this body should move, still it is God, who immediately impresses, on that member, the motion desired, but all the while, the soul is in no manner of connection with it's body. It was, therefore, altogether unnecessary, that the body should be a machine of such admirable construction, as the dullest mass would have answered the purpose equally well.

This fystem, accordingly, soon lost much of it's credit, when the celebrated Leibnitz substituted, in it's place, that of the pre-established harmony, which you have, no doubt, frequently heard mentioned in conversation.

According to this fystem of pre-established barmony, the soul and the body are two substances out of all connection, and exercising no manner of influence on each other. The soul is a spiritual substance, which, from it's own nature, receives, or assumes, all it's

ideas,

ideas, it's thoughts, it's perceptions, without the body's having the least share in the matter; and the body is a machine most ingeniously constructed, like a clock, which produces all it's motions, in fuccession, without any manner of influence on the part of the foul. But God, having forefeen, from the beginning, all the refolutions, which every foul would at every inftant form, arranged the machine of the body, fo as that it's motions should, at every inflant, harmonize with the refolutions of the foul. Thus, when I at this moment raise my hand, Leibnitz fays, that God having forefeen my foul would will, at this moment, my hand to be raifed, disposed the machine of my body in fuch a manner, that, in virtue of it's proper organization, my hand should necessarily rife at the same instant; and, in like manner, that all the motions of the members of the body are performed in virtue of their proper organization, which has been, from the beginning, fo disposed, as to be at all times in harmony with the determinations of the foul.

6th December, 1760.

#### LETTER LXXXIII.

Examination of the System of pre-established Harmony.

An Objection to it.

THERE was a time, when the fystem of pre-established harmony had acquired such a high reputation over all Germany, that to dare to call it

in question was to incur the imputation of ignorance, or bigotry. The supporters of this system boasted, that, by means of it, the omnipotence and omniscience of the Supreme Being were set in their clearest light, and that it was impossible for any one, who believed in these exalted perfections of God, to entertain a doubt of the truth of this sublime system.

In fact, fay they, we fee, that poor, pitiful mortals, are capable of conftructing machines fo ingeniously, as to fill the vulgar spectator with aftonishment: how much ftronger reason, then, have we to admit, that God having known, from all eternity, all that my foul would wish and defire, at every instant, should have been able to construct such a machine, which, at every inftant, should produce motions conformable to the determinations of my foul? Now, this machine is precifely my body, which is united to my foul, only by this harmony; fo that if the organization of my body were deranged to fuch a degree, as to be no longer in harmony with my foul, this body would no more belong to me, than the body of a rhinoceros in the heart of Africa: and if, in the case of a derangement of my body, God should adjust that of a rhinoceros, so that it's motions were in fuch harmony with the determinations of my foul, as to raife it's paw at the moment I willed it; this body would then be mine, and would belong to my foul, as my prefent body now belongs to it, without having undergone itself, on that account, any change whatever.

Mr. Leibnitz himfelf has compared the foul and the body

body to two clocks, which continually indicate the fame hour. A clown who should see this beautiful harmony of these two clocks, would undoubtedly conclude, that they acted upon each other, but he would be under a mistake, for the one performs it's motions independently of the other. The soul and the body are likewise two machines totally independent, the one being spiritual, the other material; but their operations are always in a harmony so complete, that we are induced to believe them to belong to each other, and that the one has a real influence upon the other, which is, however, a mere illusion.

In order to form a judgment of this fystem, I remark, first, That it cannot be denied to be possible for God to create a machine which should be always in harmony with the operations of my foul; but it appears to me that my body belongs to me by other rights than fuch a harmony, however beautiful it may be: and, I believe, you will not be disposed haftily to adopt a fystem which is founded on this principle alone, that no spirit can act upon a body; and that, reciprocally, a body cannot act upon, or fupply ideas to, a fpirit. This principle is, befides, destitute of all proof, the chimeras of it's partisans, respecting simple beings, having been completely refuted. And if God, who is a spirit, has the power of acting upon bodies, it is not abfolutely impossible that a spirit, such as the human foul, should be able likewise to act upon a body. Accordingly, we do not pretend to fay, that our foul acts upon all bodies, but only upon a fmall particle of matter, with respect respect to which it has received the power of God himself, though to exercise it in a manner which we are utterly unable to comprehend.

Farther, the fystem of pre-established harmony labours under other great difficulties. According to it the foul derives all it's knowledge from it's own proper fund, without any contribution on the part of the body and the fenfes. Thus, when I read in the Gazette that the Pope is dead, and I come to the knowledge of the Pope's death, the Gazette and my reading have nothing to do with the communication of this knowledge, as these circumstances respect only my body and my fenses, which have no manner of connection with my foul. But, conformably to this fystem, my foul derives, at the same time, from it's own proper fund, the ideas which it has of this fame Pope. It concludes, he must absolutely be dead, and this knowledge comes to it with the reading of the Gazette, fo that I imagine the reading of the Gazette furnished me with this knowledge, though I really derived it from the proper fund of my foul.

But this idea is perfectly abfurd. How was it posfible for me so boldly to affert, that the Pope must necessarily have died at the moment mentioned in the Gazette, and that, only from the idea which I had of the Pope's condition and health, though, perhaps, I knew nothing about him, while I am infinitely better acquainted with my own situation, without knowing, however, what shall befall me tomorrow.

In like manner when you do me the honour to

read these letters, and derive the knowledge of some truth from them, it is your soul which extracts that truth from it's own proper fund, without my contributing at all to it by my letters. The reading of them serves only to maintain the harmony which the Creator meant to establish between the soul and the body. It is only a formality, altogether superfluous, with respect to the knowledge itself. I shall, nevertheless, continue to tender you my instructions:

9th December, 1760.

## LETTER LXXXIV.

## Another Objection.

THERE is another objection to be made to the fystem of pre-established harmony; namely, that it is utterly destructive of human liberty. In fact, if the bodies of men are machines, similar to a watch, all their actions are a necessary consequence of their construction. Thus, when a thief steals my purse, the motion made by his hands is an effect as necessary of the machine of his body, as the motion of the hand of my clock, now pointing to nine. You will readily comprehend what must be the conclusion. As it would be unjust, nay, ridiculous, to think of being angry at the clock, and of chastising it, because it pointed to nine, it would be equally so, with respect to the thief, whom it would be absurd to punish for having stolen my purse.

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Of this we had a well-known example in the reign of his late Majesty, when Mr. Wolff taught at Halle the fystem of the pre-established harmony. The King informed himself of this doctrine, which was then making a prodigious noise; and one of his Court having fuggested to him that, according to Mr. Wolff's doctrines, foldiers were mere machines, and that when one deferted, it was a necessary confequence of his particular structure, and therefore ought not to fubject him to punishment, as would be the case, were a machine an object of punishment, for having performed fuch and fuch a motion; the King was fo provoked at this reprefentation, that he gave orders to banish Wolff from Halle, with certification, that if he was found there at the end of twenty-four hours, he should be hanged up. The philosopher upon this took refuge at Marburg, where I converfed with him foon after.

But the partifans of this fystem have always maintained that the pre-established harmony by no means encroached on human liberty. They admit that the exterior actions of men are necessary essects of the organization of the body, and that, in this respect, they take place as necessarily as the motions of a watch: but that the mental determination enjoyed perfect liberty: that these may be deserving of punishment, though the corporeal action was necessary: that the criminality of an action consists less in the act, or motions of the body, than in the resolution or intention of the soul, which remains entirely free. Let us conceive, say they, the soul of a thief, determining

mining, at a certain time, to commit a robbery: God having foreseen this intention, has provided it with a body, organized in such a manner as to produce, precisely at the same time, the motions requisite for the commission of this robbery: the action, say they, is itself the necessary effect of the organization of the body, but that the intention of the thief is a free act of his soul, which is not, on that account, less culpable and less punishable.

Notwithstanding this reasoning, the supporters of the system of pre-established harmony will always find themselves very much embarrassed to maintain the liberty of the determinations of the soul. For, according to them, the soul is itself similar to a machine, though of a nature totally different from that of the body; the representations produced in it are occasioned by those which precede, and these again by others anterior to them, and so on, so that they sollow each other as necessarily as the motions of a machine. In fact, say they, men act always from certain motives, sounded on the representations of the soul, which succeed each other, conformably to it's state.

You will recollect that, according to this fystem, the soul derives no one idea from the body, not being in any real connection with it; but all from it's own proper fund. Present ideas slow from those which preceded, and are a necessary consequence of them; so that the soul is nothing less than master of it's own ideas, which generate it's resolutions, and which are therefore as little under it's power: and,

confequently, all it's actions are founded on it's prefent flate, that on the immediately preceding, and fo on, are a necessary effect of the first state in which it was created, over which it certainly could have no power, and, of confequence, could not be free. In depriving men of their liberty, all their actions become necessary, and can no longer be considered as either right or criminal.

No one of those philosophers has hitherto been able to remove these difficulties; and their adversaries have a right to object to them, that this opinion is subversive of all morality, and makes every crime which men commit to recoil on God himself, which is, undoubtedly, the grossest impiety. We must not, however, load them with the imputation of such consequences, though they slow very naturally from their principles. The article of liberty is a stumbling block in philosophy; and it is extremely difficult to steer clear of the dangers which press on all sides.\*

13th December, 1760.

The King of Pruffia (Frederick II.) though no believer in the pre-eftablished harmony, hastened to do justice to Wolff, the moment he mounted the throne. The original cause of his perfecution was the resentment of an ecclesiastic, jealous of Wolff, as Voctius was of Descartes. The pride of men of this description has long endeavoured to subject thought itself to their opinions or to their interest; but the world begins to entertain for them the horror and the contempt which they deserve.\*

Besides, these objections respecting liberty are not peculiar to

<sup>\*</sup> So, because one Prussan theologian was jealous, and a bigot, according to Mr. Condorcet, he perm to himself to brand the whole order with the imputation of these odious qualities. The impartial Reader will judge whether it is not as possible for a philosopher and a free-thinker to be uncandid and illiberal, as for an ecclesiastic.—E. E.

#### LETTER LXXXV.

Of the Liberty of Spirits; and a Reply to Objections against Liberty.

THE greatest dissiculties on the subject of liberty, even those which appear insurmountable, arise from want of distinguishing, with sufficient attention, between the nature of spirit and that of body. The Wolsian philosophers even go so far as to put spirits, and the elements of body, on the same footing, and give to both the one and the other the name of monads, the nature of which, according to them, consists in the power of changing their state; from whence result all the changes in bodies, and all the representations and actions of spirits.

Since, then, in this fystem, the actual state of bodies and of spirits derives it's determination from that which immediately preceded; and as the actions of spirits are derived, like those of bodies, from their preceding state, it is evident, that liberty is no more an attribute of spirit than it is of body. As to body, it is impossible to conceive the least shadow of liberty in it; for liberty always supposes the power of committing, of admitting, or of suspending an action,

the fystem of pre-established harmony, but common to all. It is certain that in such and such circumstances I will perform such an action, and yet I shall have the power of acting otherwise. This action will infallibly take place but not necessarily. This is the real difficulty.—F. E.

and this is directly opposite to all that passes in body. Would it not, then, be ridiculous to expect that a watch should point to any other hour than what it actually does, and to think of punishing it on that account? Would it not be absurd to sly into a passion at a puppet, because, after several other gestures, it had turned it's back to us?

All the changes which take place in bodies, and which are all reducible to their state of rest, or of motion, are the necessary consequence of the powers which act upon them; and their action once admitted, no changes in bodies can take place, but precifely fuch as do take place: what refpects body, therefore, is an object of neither praise nor blame. However ingeniously a piece of mechanism may be constructed, the commendation which we bestow upon it reverts to the artist; the machine itself has no interest in what passes; the artist, too, is alone responsible for the defects of a clumfy and aukward machine; the machine itself is perfectly innocent. While, therefore, the enquiry is restricted to bodies, they are clearly in no respect responsible; no reward, no punishment can possibly attach to them; all the changes and motions produced in them, are the necessary consequences of their structure.

But spirits are of a very different nature, and their actions depend on principles directly opposite. Liberty, entirely excluded from the nature of body, is the effential portion of spirit, to such a degree, that without liberty, a spirit could not exist; and this it is which renders it responsible for it's actions. This

property

property is as effential to fpirit as extension or impenetrability is to body; and as it would be impossible for the divine Omnipotence itself to divest body of these qualities, it would be equally impossible for it to divest spirits of liberty. A spirit without liberty, would no longer be a spirit, as a body without extension would no longer be a body.

It has in all ages been a subject of eager enquiry among philosophers, How God could have permitted fin to enter into the world? Had they reslected that the souls of men are beings necessarily free, from their very nature, the controversy would have been easily settled.

The objections commonly made to human liberty are these: A spirit, it is said, or a man, is never determined to an action, but from motives; and after having carefully weighed the reasons on both sides, he finally decides in favour of that which he deems the preferable. Hence they conclude that motives determine the actions of men, just as the motion of a ball on the billiard table is determined by the stroke impressed upon it, and that the actions of men are no more free than the motion of the ball. But it must be considered that the motives which engage a man to undertake any enterprize, refer very differently to the foul, from what the stroke does to the ball. The stroke produces it's effect necessarily; but a motive, however powerful, prevents not the action from being voluntary. I had very powerful motives to undertake a journey to Magdeburg: a regard to my promise; the prospect of enjoying the felicity of Y 4 paying

paying my respects to your Highness; but I am perfectly sensible, at the same time, that I was not forced to it: and that it was entirely in my own power to take that journey, or to have remained at Berlin. But a body, impelled by any power, necessarily obeys, and it cannot be affirmed that it was at liberty to obey, or not, as it pleased.

The motive which determines a spirit to regulate it's resolves, is of a nature wholly different from a cause or sorce acting upon body. Here, the effect is produced necessarily; and there, the effect remains always voluntary, and the soul has power over it. On this is founded the imputability of the actions of a spirit, which makes it responsible for them, and which is the true soundation of right and wrong. As soon as we have settled this infinite difference between spirit and body, the question respecting liberty presents very little difficulty.

16th December, 1760.

## LETTER LXXXVI.

The same Subject continued.

THE difference which I have just established between the motives, conformably to which spirits act, and the causes or powers which act on bodies, discovers to us the true foundation of liberty.

· Imagine a puppet fo artfully conftructed with wheels and fprings, as to be able to approach my pocket, pocket, and to pick out my watch, without my perceiving it. This action being a necessary confequence of the organization of the machine, could not be confidered as a robbery; and I should render myfelf ridiculous if I got into a passion at it, and insisted on having the machine hanged. Every one would fay that the puppet was innocent, and incapable of committing a blameable action; it would be, befides, equally indifferent to the puppet to be hanged, or placed on a throne. But if the artist had contrived this machine on purpose to steal, and to enrich himfelf by fuch means, however much I might admire the ingenuity difplayed on the mechanism, I should reckon myfelf obliged to bring him to juftice as a thief. It follows, then, that even in this cafe the criminality reverts upon an intelligent being, or a fpirit, and that fpirits alone are responsible for their actions.

Let every man examine his own actions, and he will always find that he was not forced into them, though he might be induced by motives. If his actions are commendable, he is perfectly conscious of meriting the praises bestowed upon him. However he might be deceived in his other judgments, he cannot in this case; the sentiment of his liberty is so intimately connected with that liberty itself, that they are inseparable. It is possible to entertain a doubt where the liberty of another is concerned, but it is impossible ever to be deceived respecting one's own. A clown, for example, on seeing the puppet above described, might easily imagine it to be a real thief.

thief, and that it likewise was a free agent: in this he would be mistaken; but with respect to his own liberty, it is impossible for him to mistake; as he deems himself free, he is so in fact. It might likewise happen, that the clown in question, undeceived as to the puppet, should afterwards consider a dexterous thief as a machine, destitute of all sentiment, and of liberty: here he would fall into the opposite error, but as to his own actions, he will never be mistaken.

It would, therefore, be ridiculous to affirm, that it might be possible for a watch to imagine that it's hand turned freely, and to believe that it now points to nine, because it pleases to do so, but could point to any other hour, if it thought proper: the watch would undoubtedly deceive itself. But the whole supposition is manifestly absurd. You must first ascribe to the watch fentiment and imagination, and accordingly suppose it a spirit or soul, which necessarily implies liberty; and afterwards consider it as a mere machine, divested of liberty, which is a manifest contradiction.

Another objection, however, is started against liberty, founded on the divine prescience. God, it is said, foresaw, from all eternity, every resolution which I should form, and every action which I should do, during every instant of my life. If God foresaw I should just now continue to write, that I should, by and by, lay down my pen, and rife to take a walk, my action would be no longer free, for I am under the necessity of writing, of laying down the

pen, and of rifing to walk; and it would be impossible for me to act otherwise, as it was impossible God should be deceived in what he foresees?

The reply is obvious. Because God foresaw, from all eternity, that I should perform, on such a day, such an action, it does not follow that I shall perform it, because God foresaw it. For it is evident that it ought not to be alleged, in the cause supposed, That I go on to write, because God foresaw I should go on to write; but, on the contrary, as I judge it proper to go on to write, God foresaw that I would do so. Thus the prescience of God by no means encroaches on my liberty; and all my actions remain equally at liberty, whether God foresaw them or not.

Some, however, in the view of supporting liberty, have gone fo far as to deny the divine prescience; but you will have little difficulty in detecting the falsehood of this opinion. Is it so surprising that the Supreme Being, who is acquainted with all my propenfities, should be able to foresee the effect which every motive will produce on my foul, and, confequently, all the refolutions which I shall form, in conformity to these effects, when simple mortals, such as we are, frequently exercise a similar prescience? You can eafily imagine to yourfelf a man extremely covetous, who has a fair opportunity of making a confiderable advantage. You know, for certain, he will not fail to avail himfelf of it. Your knowledge of this, however, has no influence upon the man; he goes into it with the full determination of his own mind, as if you had never spent a thought upon him.

him. Now, as God is infinitely better acquainted with men, and all their dispositions, it is not to be doubted that he could have foreseen their actions, in all situations. The prescience of God, with respect to the free actions of spirits, is, nevertheless, sounded on another principle than that of the changes which must take place in the corporeal world, where all is under the power of necessity. This distinction shall be the subject of my next letter.

201b December, 1760.

#### LETTER LXXXVII.

Influence of the Liberty of Spirits upon Events.

If the world contained bodies only, and if the changes which take place in it, were necessary confequences of the laws of motion, conformably to the powers with which they act upon each other, all events would be necessary, and would depend on the first arrangement which the Creator had established of the bodies of the universe; so that this arrangement, once established, it should be impossible for other events afterwards to take place, than those which happen in the actual order of things. The world would, undoubtedly, be in this case, a mere machine, similar to a watch, which, once wound up, afterwards produces all the motions by which we measure time.

Imagine to yourfelf a mufical clock; fuch a clock, once regulated, all the motions which it performs, and

and the airs which it plays, are produced in virtue of it's conftruction, without any fresh application of the hand of the master, and, in that case, we say it is done mechanically. If the artist touches it, by changing the notch, or the cylinder, which regulates the airs, or by winding it up, it is an external action, which, not being founded on the organization of the machine, no longer appertains to it. And if God, as Lord of the universe, should change immediately any thing in the course of successive events, this change would no longer appertain to the machine: it would then be a miracle.

A miracle, confequently, is an immediate effect of the divine Omnipotence, which could not have taken place, had God left the machine of the universe freely to take it's course. Such would be the state of the universe, if it contained bodies only; in that case it might be said, that all events take place in it from an absolute necessity, each of them being a necessary effect of the structure of the universe; unless it pleased God to work miracles.

The fame thing would happen, on admitting the fystem of pre-established harmony, though it allows the existence of spirits; for, according to this system, spirits do not act upon bodies, but these perform all their motions and actions only in virtue of their structure, once established; so that when I raise my arm, this motion is an effect as necessary of the organization of my body, as that of the wheels in a watch. My soul, in no respect, contributes to it; it

is God who, from the beginning, arranged the matter, so that the action of my body must necessarily result from it, at a certain time, and raise the arm at the instant that my soul willed it. Thus, my soul has no influence upon my body, any more than upon those of other men and of animals: and, consequently, according to this system, the universe is merely corporeal, and events are a necessary effect of the primitive organization which God has established in the universe.

But, if we allow to the fouls of men and of animals the power of producing motion in their bodies, which their organization alone would not have produced, the fystem of the universe is not a mere machine, and events do not necessarily take place as in the preceding case.

The universe will present events of two kinds; the one, those over which spirits have no manner of influence, which are corporeal, or dependant on the machine, as the motion and phenomena of the heavenly bodies; these take place as necessarily as those of a watch, and depend entirely on the primitive establishment of the universe. The others depend on the soul, united to the body of men and animals, and are no longer necessary, as the preceding, but result from the liberty, as from the will, of these spiritual beings.

These two kinds of events distinguish the universe from a mere machine, and raise it to a rank infinitely more worthy of the almighty Creator, who formed it. The government of this universe will likewise ever inspire us with the most sublime idea of the sovereign wisdom and goodness of God.

It is certain, therefore, that liberty, which is abfolutely effential to fpirits, has a very great influence on the events of the world. You have only to confider the fatal confequences of these wars, which all result from human actions, determined by their will, or their caprice.

It is likewise certain, at the same time, that the events which take place do not depend only on the will of men and animals. Their power is very limited, being restricted to a small portion of the brain, in which all the nerves terminate: and this action is confined to the communication of an impression of a certain motion on the members, which may afterwards operate on other bodies, and these again on others, so that the slightest motion of my body may have a very great influence on a multitude of events.

Man, however, though mafter of the first motion of his body, which occasions these events, is not so of the consequences of his action. These depend on so many circumstances, that the most fagacious mind is incapable of foreseeing them: accordingly, we every day see the best concerted projects failing. But it is here that we must acknowledge the government and providence of God, who, having from all eternity foreseen all the counsels, the projects, and the voluntary actions of men, arranged the corporeal world in such a manner, that it brings about, at all times, circumstances which cause these enterprizes to

fail or to fucceed, according as his infinite wisdom judges to be most fit. God thus remains absolute sovereign of all events, notwithstanding the liberty of men, all whose actions, though free, are, from the beginning, part of the plan which God intended to execute, when he created this universe.

This reflection plunges us into an abyss of wonder and adoration at the infinite perfections of the Creator; while we consider that there is nothing so mean in itself as not to be, from the beginning of the world, an object worthy of entering into the original plan which God proposed to himself.

23d December, 1760.

#### LETTER LXXXVIII.

Of Events, natural, supernatural, and moral.

IN common life, we carefully diftinguish events produced by corporeal causes from those in which men and animals co-operate. Those of the former description are denominated natural events, or produced by natural causes; such are the phenomena of the heavenly bodies, eclipses, tempests, whirlwinds, earthquakes, &c. These are called natural phenomena, because it is understood that neither men nor animals are active in the production of them.

If we fee a tree torn up by the roots, through the violence of the wind, we call it a natural effect: but if it were done by the strength of man, or the proboscis

boscis of an elephant, no one would call this a natural effect. When our plains are deluged by an inundation, or destroyed by the hail, we say the cause of this calamity was natural; but if the mischief were done by the invasion of an enemy, we would no longer deem the cause of it to be natural.

If fuch an evil were to be produced by a miracle, or by the immediate power of God, we would fay the cause of it was *supernatural*; but if the event were occasioned by men or animals, we would not, in that case, give it the name of either natural or supernatural. We would characterize such an event simply by the name of action, which denotes an effect that is neither natural nor supernatural. It might with greater propriety be denominated moral, as it depends on the liberty of an intelligent agent.

Thus, when Quintus Curtius gives us a detail of the actions of Alexander the Great, he communicates to us the knowledge of the events brought about by the voluntary determinations of that hero. Such an action always supposes freedom of resolution in a spiritual being; a power of determination which depends upon his will, and of which he is master. I say, of which he is master; for there is a great variety of motions, the production of which, were we to determine to will them ever so much, we should not, however, be obeyed, because over such movements we have no power.

I am not mafter even of all the motions performed in my own body; that of my heart and of my blood Vol. I. Z is

is not fubject to my power, or to the empire of my foul, as the action which I perform when I write this letter. There are other motions which partake of the nature of both these, such as respiration, which it is in my power to accelerate, or to retard to a certain degree, but of which I am by no means the absolute master.

Language is not fufficiently rich to express, by one appropriate term, all these different kinds of events. There are fome produced by natural causes merely, and which are necessary consequences of the arrangement of bodies in the universe; and as these necesfarily come to pass, the knowledge of this arrangement enables us to foretel a great number of them, fuch as the fituation of the heavenly bodies, eclipfes, and other phenomena depending on them, for any given time whatever. There are other events which depend only on the will of free and spiritual beings, as the actions of every man and of every animal. It is impossible for us to foresee any thing of these, in particular, unless by conjecture merely; and in this we are frequently very grossly mistaken. God alone possesses this knowledge in a supreme degree.

From these two kinds of events there arises a third, in which natural causes concur with such as are voluntary, and dependant on a being exercising it's liberty. Of this the billiard table furnishes an example. The strokes impressed on the balls depend on the will of the players; but as soon as motion is communicated to them, the continuation of that motion,

motion, and their collision with each other, or with the cushion, are necessary consequences of the laws of motion.

In general, most of the events which take place on the earth, must be referred to this species, as there are scarcely any over which men and animals have not fome influence. The cultivation and produce of our fields require, in the first instance, the voluntary exertions of men or beafts, but the fequel is an effect of causes purely natural. It is accordingly of importance to remark, that God acts in a manner totally different toward bodies and spirits. God has establifhed, for bodies, laws of rest and motion, conformably to which all changes necessarily take place; as bodies are merely paffive beings which preferve themfelves in their state, or necessarily obey impressions made upon them by others, as I formerly explained; whereas spirits are susceptible of no force or constraint, but are governed of God by precepts and prohibitions.

With respect to bodies, the will of God is always perfectly accomplished; but with respect to spiritual beings, such as men, the contrary very often happens. When it is said to be the will of God that men should love one another, we mean by that expression a commandment which men ought to obey; but this is very far from being the case. God does not force men to it, for this would be contrary to the liberty which is essential to them; but He endeavours to engage men to the observance of this

commandment, by proposing to them motives the most powerful; but it always depends on the will of man, whether he is to obey or not. In this sense we are to understand the will of God, when it refers to the free actions of spiritual beings.

27th December, 1760.

## LETTER LXXXIX.

Of the Question respecting the best World possible; and of the Origin of Evil.

YOU know well, that it has been made a queftion, Whether this world be the best possible? It cannot be doubted, that the world perfectly corresponds to the plan which God proposed to himfelf, when he created it.

As to bodies, and material productions, their arrangement and structure are such, that certainly they could not have been better. Please to recollect the wonderful structure of the eye, and you will see the necessity of admitting, that the conformation of all it's parts is perfectly adapted to suffil the end in view, that of representing distinctly exterior objects. How much address is necessary to keep up the eye in that state, during the course of a whole life? The juices which compose it must be preserved from corruption; it was necessary to make provision, that they should be constantly renewed, and maintained in a fuitable state.

A structure

A structure equally marvellous is observable in all the other parts of our bodies, in those of all animals, and even of the vilest infects. And the structure of these last, is so much the more admirable, on account of their smallness, that it should perfectly satisfy all the wants which are peculiar to each species. Let us examine only the sense of seeing in these infects, by which they distinguish objects so minute, and so near, as to escape our eyes, and this examination alone will fill us with associations.

We discover the same perfection in plants: every thing in them concurs to their formation, to their growth, and to the production of their flowers, of their fruits, or of their feeds. What a prodigy to behold a plant, a tree, fpring from a finall grain, cast into the earth, by the help of the nutritious juices with which the foil supplies it? The productions found in the bowels of the earth are no less wonderful: every part of nature is capable of exhausting our utmost powers of research, without permitting us to penetrate all the wonders of it's construction. Nay, we are utterly loft, while we reflect, how every fubstance, earth, water, air, and fire, concur in the production of all organized bodies; and, finally, how the arragement of all the heavenly bodies is fo admirably contrived, as perfectly to fulfil all these particular deftinations.

After having reflected in this manner, it will be difficult for you to believe, that there should have been men who maintained, that the universe was the effect of mere chance, without any defign. But there always have been, and there still are, persons of this description; those, however, who have a solid knowledge of nature, and whom sear of the justice of God does not prevent from acknowledging Him, are convinced, with us, that there is a Supreme Being, who created the whole universe, and, from the remarks which I have just been suggesting to you, respecting bodies, every thing has been created in the highest persection.

As to spirits, the wickedness of man seems to be an infringement of this perfection, as it is but too capable of introducing the greatest evils into the world, and these evils have, at all times, appeared incompatible with the sovereign goodness of God. This is the weapon usually employed by insidels against religion, and the existence of God. If God, say they, was the author of the world, He must also be the author of the evil which it contains, and of the crimes committed in it.

This question, respecting the origin of evil; the dissiculty of explaining, How it can consist with the sovereign goodness of God, has always greatly perplexed philosophers and divines. Some have endeavoured to give a solution, but it has satisfied only themselves. Others have gone so far as to maintain, that God was, in fact, the author of moral evil, and of crimes; always protesting, at the same time, that this opinion ought to bring no imputation on the goodness and holiness of God. Others, finally, confider

fider this question as a mystery which we cannot comprehend; and these last, undoubtedly, have embraced the preserable sentiment.

God is supremely good and holy; He is the author of the world, and that world swarms with crimes and calamities. These are three truths which it is, apparently, difficult to reconcile: but, in my opinion, a great part of the difficulty vanishes, as soon as we have formed a just idea of spirit, and of the liberty so essential to it, that God himself cannot divest it of this quality.

God having created spirits, and the souls of men, I remark, first, that spirits are beings infinitely more excellent than bodies; and, secondly, that, at the moment of creation, spirits were all good: for time is requisite to the formation of evil inclinations: there is, therefore, no difficulty in affirming, that God created spirits. But it being the essence of spirits to be free, and liberty not being capable of subsisting without a power to sin, to create a spirit possessed of the power of sinning, has nothing inconsistent with divine perfection, because a spirit could not be created destitute of that power.

God has, befides, done every thing to prevent crimes, by prefcribing to fpirits, precepts, the obfervance of which must always render them good and happy. There is no other method of treating spirits, which cannot be subject to any constraint; and if some of them have abused their liberty, and transgressed these commandments, they are responfible for it, and worthy of punishment, without any impeachment of the Deity.

There remains only one objection more to be confidered: namely, that it would have been better not to create fuch spirits, as God foresaw they must fink into criminality. But this far furpaffes human understanding; for we know not, whether the plan of the world could fubfift without them. We know, on the contrary, by experience, that the wickedness of fome men frequently contributes to the correction and amendment of others, and thereby conducts them to happiness. This consideration, alone, is sufficient to justify the existence of evil spirits. And, as God has all power over the consequences of human wickedness, every one may rest assured, that in conforming to the commandments of God, all events which come to pass, however calamitous they may appear to him, are always under the direction of Providence, and, finally, terminate in his true happiness.

This providence of God, which extends to every individual, in particular, thus furnishes the most fatisfactory solution of the question respecting the permission, and the origin, of evil.\*

30th December, 1760.

\* Mr. Euler concludes this letter, with the following fhort fentence: "This likewise is the foundation of all religion, the alone object of which is to promote the falvation of mankind." What reason could there be for suppressing a sentiment so natural, so much in place, and so inostensive?—E. E.

# LETTER XC.

Connection of the preceding Considerations with Religion.
Reply to the Objections of the philosophic Systems against
Prayer.

BEFORE I proceed farther in my leffons on philosophy and physics, I think it my duty to point out to you their connection with religion.\*

I begin with confidering an objection, which almost all the philosophic systems have started, against prayer. Religion prescribes this as our duty, with an assurance, that God will hear and answer our vows and prayers, provided they are conformable to the precepts which he has given us. Philosophy, on the other hand, instructs us, that all events take place in strict conformity to the course of nature, estab-

\* I take the liberty, likewise, to restore the following passage, which M. de Condorcet, in his philosophic squeamishness, has thought unworthy of a place in his edition of the work.

"However extravagant and abfurd the fentiments of certain "philosophers may be, they are so obstinately prepossessed in fa-

" vour of them, that they reject every religious opinion and doc-

" trine, which is not conformable to their fystem of philosophy.

" From this fource are derived most of the fects and herefies in re-

" ligion. Several philosophic fystems are really contradictory to

" religion; but in that case, divine truth ought, furely to be pre-

" ferred to the reveries of men, if the pride of philosophers knew

" what it was to yield. Should found philosophy sometimes seem

" in opposition to religion, that opposition is more apparent than

" real; and we must not suffer ourselves to be dazzled with the

" speciousness of objection."-E. E.

lished from the beginning, and that our prayers can effect no change whatever; unless we pretend to expect, that God should be continually working miracles, in compliance with our prayers. This objection has the greater weight, that religion itself teaches the doctrine of God's having established the course of all events, and that nothing can come to pass, but what God foresaw from all eternity. Is it credible, say the objectors, that God should think of altering this settled course, in compliance with any prayers which men might address to him?

But I remark, first, that when God established the course of the universe, and arranged all the events which must come to pass in it, he paid attention to all the circumftances which should accompany each event; and particularly to the dispositions, to the defires, and prayers, of every intelligent being; and that the arrangement of all events was disposed, in perfect harmony, with all these circumstances. When, therefore, a man addresses to God a prayer worthy of being heard, it must not be imagined, that such a prayer came not to the knowledge of God till the moment it was formed. That prayer was already heard from all eternity; and if the Father of mercies deemed it worthy of being answered, He arranged the world expressly in favour of that prayer, fo that the accomplishment should be a consequence of the natural course of events. It is thus that God answers the prayers of men, without working a miracle.

The establishment of the course of the universe, fixed

fixed once for all, far from rendering prayer unneceffary, rather increases our confidence, by conveying to us this consolatory truth, That all our prayers have been already, from the beginning, presented at the feet of the throne of the Almighty, and that they have been admitted into the plan of the universe, as motives conformably to which events were to be regulated, in subserviency to the infinite wisdom of the Creator.

Can any one believe, that our condition would be better, if God had no knowledge of our prayers before we prefented them, and that He should then be disposed to change, in our favour, the order of the course of nature? This might well be irreconcileable to his wifdom, and inconfiftent with his adorable perfections. Would there not, then, be reason to say, that the world was a very imperfect work? that God was entirely disposed to be favourable to the wishes of men; but, not having forefeen them, was reduced to the necessity of, every instant, interrupting the course of nature, unless he were determined totally to difregard the wants of intelligent beings, which, nevertheless, constitute the principal part of the universe? For to what purpose create this material world, replenished with fo many great wonders, if there were no intelligent beings, capable of admiring it, and of being elevated by it, to the adoration of God, and to the most intimate union with their Creator, in which, undoubtedly, their highest felicity confifts?

Hence, it must, absolutely, be concluded, that intelligent the principal object, in fubordination to which, God regulated the arrangement of this world; and we have every reason to rest assured, that all the events which take place in it, are in the most delightful harmony with the wants of all intelligent beings, to conduct them to their true happiness; but without constraint, because of their liberty, which is as essential to spirits, as extension is to body. There is, therefore, no ground for surprize, that there should be intelligent beings, which shall never reach felicity.

In this connection, of spirits with events, consists the divine Providence, of which every individual has the consolation of being a partaker; so that every man may rest assured, that, from all eternity, he entered into the plan of the universe. How ought this consideration to increase our considence, and our joy in the providence of God, on which all religion is founded! You see then, that on this side religion and philosophy are by no means at variance.

3d January, 1761.

### LETTER XCI.

The Liberty of intelligent Beings in Harmony with the Doctrines of the Christian Religion.

IBERTY is a quality fo effential to every spiritual being, that God himself cannot divest them of it, just as He cannot divest a body of it's extension,

tension, or of it's inertia, without entirely destroying, or annihilating it: to diveft a fpirit of liberty, therefore, would be the same thing as to annihilate it. This must be understood of the spirit, or soul itself, and not of the actions of the body, which the foul directs, in conformity to it's will. If you would prevent me from writing, you have but to bind my hands; to write is, undoubtedly, an exercise of liberty; but then, though you may fay, that you have deprived me of the liberty of writing, you have only deprived my body of the faculty of obeying the dictates of my foul. Bind me ever fo hard, you cannot: extinguish in my spirit an inclination to write; al'1 you can do is to prevent the execution of it.

We must always carefully distinguish between in clination, or the act of willing, and execution, whic h is performed by the ministration of the body. The act of willing cannot be reftrained by any exteri or power, not even by that of God, for liberty is in fependent of all exterior force. But there are me ans of acting on spirits, by motives which have a tendency, not to constrain, but to perfuade. Let a 1 man be firmly determined to engage in any enterp fize, and let us suppose the execution of it preven ted; without making any change in his intention a, or will, it might be possible to suggest motives, which should engage him to abandon his purpose, w' sthout employing any manner of constraint: he wever powerful these motives may be, he is always master of his own will; it never can be faid, that lae was forced, or conftrained, to it, at least the ex pression would

would be improper; for the proper term is perfuade, which is fo fuitable to the nature, and the liberty, of intelligent beings, that it cannot be applied to any other. It would be very ridiculous, for example, in playing at billiards, to fay, that I perfuaded the ball to run into the hazard.

This fentiment, respecting the liberty of spirits, appears, however, to fome perfons, contrary to the goodness, or the power, of the Supreme Being. Liberty, from it's very nature, can submit to no degree of constraint, even on the part of God. But without exercifing any conftraint over spirits, God has an infinite variety of means of prefenting them with perfualive motives; and, I believe, that all poffible cases are adapted by Providence to our condition, in fuch a manner, that the most abandoned wretches might derive from them the most powerful I notives to conversion, if they would but listen to t! 1em: and that a miracle would not produce a better el lect on these vicious spirits; they might be affected by it, for a feafon, but would not become better. It is thus that God co-operates in our conversion, by fur mishing us with motives the most efficacious, and by the circumstances and opportunities which his pro vidence fupplies.

It; for example, a man, who hears an awakening fern on, is affected by it, repents, and is converted; the act of his foul is evidently his own work; but the occasion of the fermon, which he was so happy as to hear, precisely at the time, when he was disposed to profit by it, was nothing less than his work; the divine

divine Providence over-ruled that circumstance, so falutary to him. In fact, without the opportunity, over which the man had no power, he would have persisted in a sinful course.

Hence, you will eafily comprehend the meaning of fuch expressions as these: "Man can do nothing of "himself; all depends on divine grace; it is God "that worketh to will and to do." The favourable circumstances which Providence supplies to men, are sufficient to elucidate these expressions, without having recourse to a secret force, which acts by constraint on human liberty; as these circumstances are directed of God, in conformity to the most consummate wisdom, in the view of conducting every intelligent being to happiness and salvation, unless he wilfully rejects the means by which he might have attained true felicity.

6th January, 1761.

### LETTER XCII.

Elucidation respecting the Nature of Spirits.

In order more clearly to elucidate what I have just faid respecting the difference between body and spirit; for it is impossible to be too attentive to what constitutes that difference, as it extends so far, that spirit has nothing in common with body, nor body with spirit, I think it necessary to subjoin the following reslections.

Extension,

Extension, inertia and impenetrability, are the properties of body; Spirit is without extension, without inertia, without impenetrability. All philosophers are agreed, that extension cannot have place in respect of spirit. It is a self-evident truth, for every thing extended is divisible, and you can form the idea of it's parts; but a spirit is susceptible of no division; you can have no conception of it's half, or of it's third part. Every spirit is a complete being, to the exclusion of all parts; it cannot, then, be affirmed, that a spirit has length, breadth, or thickness. In a word, all that we conceive of extension, must be excluded from the idea of a spirit.

It would appear, therefore, that as spirits have no magnitude, they must resemble geometrical points, the definition of which is, that they have neither length, breadth, nor depth. Would it be a very accurate idea to represent to ourselves a spirit by a mathematical point? The scholastic philosophers have professed this opinion, and considered spirits as beings infinitely small, similar to the most subtile particles of dust, but endowed with an inconceivable activity and agility, by which they are enabled to transport themselves, in an instant, to the greatest distances. They maintained, that in virtue of this extreme minuteness, millions of spirits might be inclosed in the smallest space; they even made it a question, How many spirits could dance on the point of a needle?

The disciples of Wolff are nearly of the same opinion. According to them, all bodies are composed of particles extremely minute, divested of all magnitude,

tude, and they give them the name of monads. A monad, then, is a substance destitute of all extension, and on dividing a body, till you come to particles so minute, as to be susceptible of no farther division, you have got to the Wolsian monad, which differs, therefore, from the most substille particle of dust, only in this, that the minutest particles of dust are not, perhaps, sufficiently small, and that a farther division is still necessary to obtain real monads.

Now, according to Mr. Wolff, not only all bodies are composed of monads, but every spirit is merely a monad; and the Supreme Being, I tremble as I write it, is, likewise, a monad. This does not convey a very magnificent idea of God, of spirits, and of the souls of men. I cannot conceive, that my soul is nothing more than a being, similar to the last particles of a body, or that it is reduced almost to a point. It appears to me still less capable of being maintained, that several souls joined together, might form a body, a slip of paper, for example, to light a pipe of tobacco. But the supporters of this opinion, go upon this ground, that as a spirit has no magnitude, it must, of necessity, resemble a geometrical point. Let us examine the solidity of their reasoning.

I remark, first, that as a spirit is a being of a nature totally different from that of body, it is absurd to apply to it standards, which suppose magnitude, and that, consequently, it would be folly to ask, how many feet, or inches, long, a spirit is, or how many pounds, or ounces, it weighs? These questions are applicable only to things which have length, or Vol. I.

A a weight:

weight: and are as abfurd as if, speaking of time, it were to be asked, how many feet long an hour was, or how many pounds it weighed? I can always, confidently, affirm, that an hour is not equal to a line of 100 feet, or of ten feet, or of one foot, or any other standard of measure; but it by no means follows, that an hour must be a geometrical point. An hour is of a nature entirely different, and it is impossible to apply to it any standard, which supposes a length, which may be expressed by feet, or inches.

The fame thing holds good as to spirit. I can always boldly affirm, that a spirit is not ten feet, nor 100 feet, nor any other number of feet; but it does not hence follow, that a spirit is a point, any more than that an hour must be one, because it cannot be measured by feet or inches. A spirit, then, is not a monad, or in any respect similar to the ultimate particles into which bodies may be divided; and you are perfectly able to comprehend, that a spirit may have no extension, without being, on that account, a point, or a monad. We must, therefore, separate every idea of extension from that of spirit.

To ask, In what place does a spirit reside? would be, for the same reason, likewise, an absurd question; for to connect spirit with place, is to ascribe extension to it. No more can I say, in what place an hour is; though assuredly an hour is something; something, therefore, may exist, without being attached to a certain place. I can, in like manner, assimple that my soul does not reside in my head, nor out of my head, nor in any particular place; without it's being

being deduced, as a confequence, that my foul has, therefore, no existence; just as it may be with truth affirmed of the hour now paffing, that it exists neiin my head, nor out of my head. A fpirit exists, then, though not in a certain place; but if our reflection turns on the power which a spirit has, of acting upon a body, the action is, most undoubtedly, performed in a certain place.

My foul, then, does not exist in a particular place, but it acts there, and as God possesses the power of acting upon all bodies, it is, in this respect, we fay, He is every where, though his existence is attached to no place.

10th Fanuary, 1761.

# LETTER XCIII.

20-X-00

The Subject continued. Reflections on the State of Souls after Death.

YOU will, probably, be furprized at the fentiment which I have just now ventured to advance, that fpirits, in virtue of their nature, are in no place. In thus affirming, I shall, perhaps, be in danger of paffing for a man who denies the existence of spirits, and, consequently, that of God. But I have already demonstrated, that fomething may exist, and have a reality, without being attached to any one place. The example drawn from an hour, though feeble, removes the greatest difficulties, though there is an infinite difference between an hour and a spirit.

The idea which I form of spirits, appears to me incomparably more noble than that of those who consider them as geometrical points, and who reduce God himself to this class. What can be more shocking than to consound all spirits, and the Supreme Being among the rest, with the minutest particles into which a body is divisible, and to rank them in the same class with these particles, which it is not in the power of the learned term monad to ennoble?

To be in a certain place, is an attribute belonging only to corporeal things, and, as spirits are of a totally different nature, it is not a matter of surprize to say, that they are not to be found in any place, and I am under no apprehension of reproach, for the elucidations which I have submitted to you on this subject. It is thus I exalt the nature of spirits insinitely above that of bodies.

Every spirit is a being that thinks, reslects, reafons, deliberates, acts freely, and, in one word, that lives: whereas body has no other qualities but that of being extended, susceptible of motion, and impenetrable; from whence results this universal quality, that every body remains in the same state, as long as there is no necessity of mutual penetration, or of their undergoing some change; and in case of the necessity of their penetrating each other, if they continued to remain in their state, their impenetrability itself supplies the powers requisite to change their state, state, as far as it is necessary to prevent all penetra-

In this confift all the changes which take place in bodies: all is passive, and necessarily befalls them in conformity to the laws of motion. There is, in body, neither intelligence, nor will, nor liberty: these are the supereminent qualities of spirits, while bodies are not even susceptible of them.

It is fpirit, likewife, which produces, in the corporeal world, the principal events, the illustrious actions, of intelligent beings, which are all the effect of the influence which the fouls of men exercise upon their bodies. This power, which every foul has over it's body, cannot but be considered as a gift of God, who has established this wonderful union between foul and body. And as I find my foul in such an union with a certain particle of my body, concealed in the brain, it may be said, that the seat of my foul is in that spot, though, properly speaking, my soul resides no where, and is referable to that place of my body, only in virtue of it's action, and of it's power.

It is also the influence of the soul upon the body which constitutes it's life, which continues as long as this unison subsists, or as the organization of the body remains entire. Death, then, is nothing else but the dissolution of this union, and the soul has no need to be transported elsewhere; for, as it resides in no place, all places must be indisserent to it; and, consequently, if it should please God, after my death, to establish a new union between my soul, and

an organized body in the moon, I should instantly be in the moon, without the trouble of a long journey. And if, even now, God were to grant to my soul, a power over an organized body in the moon, I should be equally here, and in the moon; and this involves no manner of contradiction. It is body only which cannot be in two places at once; but there is nothing to prevent spirit, which has no relation to place, in virtue of it's nature, to act at the same time, on several bodies, situated in places very remote from each other; and, in this respect, it might be said, with truth, that it was in all these places at once.

This supplies us with a clear elucidation of the omnipresence of God: it is, that his power extends to the whole universe, and to all the bodies which it contains. It appears to me, of consequence, an improper expression, to say, that God exists everywhere, as the existence of a spirit has no relation to place. It is more consonant with propriety to say, God is every where present.

Let us now compare this idea with that of the Wolfians, who, reprefenting Deity under the idea of a point, attach him to one fixed place, as, in fact, a point cannot be in feveral places at once; and how is it possible to reconcile the divine omnipotence, with the idea of a point?

Death being a dissolution of the union subsisting between the soul and body during life, we are enabled to form some idea of the state of the soul after death. As the soul, during life, derives all it's knowledge through the medium of the fenses, being deprived, by death, of the information communicated through the senses, it no longer knows what is passing in the material world; this state might, in some respects, be compared to that of a man who should, all at once, become blind, deaf, dumb, and deprived of the use of all the other senses. Such a man would retain the knowledge which he had acquired, through the medium of sense, and might continue to reslect on ideas previously formed; his own actions, especially, might supply an ample store, and, finally, the faculty of reasoning might remain entire, as the body, in no respect whatever contributes to it's exercise.

Sleep, likewife, furnishes us with fomething like an example of this ftate, as the union between foul and body is then, in a great measure, interrupted; though the foul, even in fleep, ceases not from exerting it's activity, being employed in the production of what we call dreams. These dreams are usually very much disturbed, by the remains of the influence which the fenfes still exercise over the foul; and we know, by experience, that the more this influence is fuspended, which is the case in very profound fleep, the more regular and connected, likewife, our dreams are. Thus, after death, we shall find ourselves in a more perfect state of dreaming, which nothing shall be able to discompose: it shall confift of representations, and reasonings, perfectly well kept up. And this, in my opinion, is nearly all we can fay of it, at leaft, with any appearance of reason.

<sup>13</sup>th Jan. 1761.

#### LETTER XCIV.

Considerations on the Action of the Soul upon the Body, and of the Body upon the Soul.

As the foul is the principal part of our being, it is of high importance, thoroughly to inveftigate it's operations. You will please to recollect, that the union between the foul and the body, contains a two-fold influence: by the one, the foul perceives and feels all that passes in a certain part of the brain; and by the other, it has the power of acting on that same portion of the brain, and of producing certain motions in it.

Anatomists have taken infinite pains to discover this part of the brain, which is justly called the seat of the soul; not that the soul actually resides there, for it is not confined to any place, but because the power of acting is attached to that spot. It may be said, that the soul is present there, but not that it exists there, or that it's existence is limited to it. This part of the brain is, undoubtedly, that in which all the nerves terminate; now, anatomists tell us, that this termination is in a certain portion of the brain, which they term the callous body. This, therefore, we may consider as the seat of the soul, and the Creator has bestowed, upon every soul, such a power over this callous membrane \* of his body, that it not

<sup>\*</sup> Since anatomists have given us a more exact and particular defeription of the brain, we have been obliged to relinquish this opinion:

only perceives all that paffes there, but is, likewife, able to produce a reciprocal impression. Here, then, we observe a two-fold action: the one, by which the body acts upon the foul, and the other, by which the foul acts upon the body, but these actions are insinitely different from those which bodies exercise upon other bodies.

The foul, from it's union with the corpus callofum, finds itfelf intimately connected with the whole body, by means of the nerves, which are thence univerfally diffused. Now, the nerves are fibres so wonderfully constructed, and, to all appearance, filled with a sluid so subtile, that the slightest change which they undergo, at one extremity, is instantly communicated to the other extremity in the brain, where the seat of the soul is. And, reciprocally, the slightest impression made by the soul, on the extremities of the nerves, in the corpus callosum, is immediately transmitted through the whole extent of every nerve; and it is thus, that the muscles and members of our bodies are put in motion, and obey the commands of the soul.

This wonderful structure of the body, places it in a very close connection with all exterior objects, whether near or remote, which may act upon it, either by immediate contact, as in feeling and tasting; or by their exhalations, as in smelling. Bodies, at a

opinion: but their labours may, perhaps, one day inform us, what we are to understand by the origin of the nerves, and even, to a certain point, in what manner they transmit to the brain the impressions which they receive.—F. E.

great distance, act on the sense of hearing, when they make a noise, and exert in the air vibrations which strike our ears; they act, likewise, upon the sight, when they are illumined, and transmit into our eyes the rays of light, which consist, in like manner, in a certain vibration, caused in that medium, much more subtile than the air, which we call Ether. It is thus that bodies, both near and remote, may act upon the nerves of our body, and produce certain impressions in the corpus callosum, from which the soul derives it's perceptions.

From every thing, therefore, which makes an impression on our nerves, there results a certain change in the brain, of which the soul has a perception, and, thereby, acquires the idea of the object which caused it. We have here, then, two things to be examined: the one is corporeal, or material, which is the impression, or the change produced in the corpus callosum of the brain; the other spiritual, namely, the perception, or the information, which the soul derives from it. It is, if I may so express myself, from the contemplation of what passes in the corpus callosum, that all our knowledge is derived.

You must permit me to enter into a more particular detail, on this important article. Let us, first, consider one single sense, say, that of smelling, which being the least complicated, seems the most proper to affist us in our researches. Suppose all the other fenses annihilated, and that a rose was applied to the nose; it's exhalations would, at once, excite a certain agitation in the nerves of the nose, which, thence thence transmitted to the corpus callosum, will occafion there, likewise, some change, and in this consists
the material circumstance, which is the subject of our
investigation. This slight change, produced in the
corpus callosum, is then perceived by the soul, and it
thence acquires the idea of the smell of a rose: and
this is the spiritual operation which takes place; but
we cannot explain in what manner this is done, as it
depends on the incomprehensible union which the
Creator has established between the body and the
foul.

It is certain, however, that upon this change, in the corpus callofum, there is excited in the foul the idea of the fmell of a rose, or the contemplation of this change furnishes to the foul a certain idea, that of the fmell of a rose, but nothing more: for, as the other fenfes are fufpended, the foul can form no judgment of the nature of the object itself, which fuggested this idea; the idea of the smell of a rose alone, was excited in the foul. Hence, we comprehend, that the foul does not form this idea of itself, for it would have remained unknown, but for the presence of a rose. But farther, the foul is not indifferent with respect to it; the perception of this idea is agreeable; the foul itself is, some how, interested in it. Accordingly, we fay, that the foul feels the odour of the rose, and this perception we call sensation.

It is the fame with all the other fenses; every object, by which they are struck, excites in the corpus callosum a certain change, which the soul observes with a sensation, agreeable or disagreeable, and from which

which it derives the idea of the object which caused it. This idea is accompanied with a sensation, so much the stronger, and more intense, as the impression made on the corpus callosum is more lively. It is thus, that the soul, by contemplating the changes produced in the corpus callosum of the brain, acquires ideas, and is affected by them; and this is what we understand by the term sensation.

- 17th Jan. 1761. Sold Read Sugmont

# LETTER XCV.

Of the Faculties of the Soul, and of Judgment.

AD we no other fense but that of smelling, our knowledge would be very limited; we should, then, have no other sensation than that of odours, the diversity of which, were it ever so great, could not very much interest our soul; being restricted to this, that agreeable smells would procure some degree of pleasure, and such as are disagreeable, would excite some disgust.

But this very circumstance carries us forward to a most important inquiry: Whence is it, that one smell is agreeable, and another disgusting? It cannot be a matter of doubt, that agreeable smells excite, in the corpus callosum, a different agitation from that which is produced by the disagreeable; but how comes it, that one agitation, in the corpus callosum, can give pleasure to the foul, while another is offensive, and

even, frequently, becomes insupportable? The cause of this difference resides no longer in body, and matter; we must look for it, in the nature of the soul itself, which enjoys a certain pleasure in feeling certain agitations, while others excite uneasiness: and the real cause of this effect we do not know.

Hence we comprehend, that the foul does more than fimply perceive what passes in the brain, or corpus callosum; it subjoins to sensation, a judgment respecting what it finds agreeable, or disgusting, and, consequently, exercises, beside the faculty of perceiving, another, and a different faculty, that of judging: and this judgment is wholly different from the simple idea of a smell.

The fame confideration, of the fense of finelling only, discovers to us still other acts of the soul. When the fmells are changed, when you apply to the nofe a carnation after a rofe, the foul has not only a perception of both finells, but, likewife, remarks a difference between them. Hence we conclude, that the foul still retains the preceding idea, to compare it with that which follows; in this confifts reminifcence, or memory, by which we have the power of recalling ideas, antecedent and past. Now, the real source of memory is entirely concealed from us. We know well, that the body has much to do in it; for experience affures us, that difeafe, and various accidents, which befall the body, weaken, and frequently destroy, the memory: it is equally certain, at the same time, that the recollection of ideas is the proper work of the foul. A recollected idea is effentially

different from an idea excited by an object. I have a perfect recollection of the fun, which I faw to day, but this idea greatly differs from that which I had while I was looking at the fun.

Some authors pretend, that when we recall an idea, there happens in the brain an agitation fimilar to that which first produced it; but if this were the case, I should actually see the sun; it would no longer be a recollected idea. They admit, indeed, that the agitation which accompanies the recalled idea, is much weaker than that from which the original idea proceeded; but still I am not satisfied with this, for it would thence follow, that when I recal the idea of the sun, it would be much the same as when I see the moon, the light of which, you will please to remember, is about 200,000 times weaker than that of the sun. But actually to look at the moon, and simply to recollect the sun, are two things absolutely different.

We may fay with truth, that the recollected ideas are the fame with the actual ideas; but this identity respects only the soul; with regard to the body, the actual idea is accompanied with a certain agitation in the brain, whereas the recollected one is destitute of it. Accordingly, we say, that the idea which I feel, or which an object acting on my senses excites in my soul, is a sensation; but it can with no propriety be said, that a recollected idea is a sensation. To recollect, and to feel, always remain two things, absolutely different.

When, therefore, the foul compares two different fmells,

finells, when it has the idea of the one from the prefence of an object acting on the fense of smelling, and that of the other from recollection, it has, in fact, two ideas at once, the actual idea, and the recollected idea: and in pronouncing, whether of the two is more or less agreeable, or disagreeable, it exerts a particular faculty, distinct from that by which it only contemplates what is presented to it.

But the foul performs still other operations; when a fuccession of several different smells is presented to it; for while it is struck with each of these, in it's turn, the preceding are recollected, and a notion is thereby acquired of past and present, and even of future, when new fenfations are propofed, fimilar to those of which it has already had experience. It thence, likewife, derives the idea of fuccession, in as much as it undergoes feveral impressions successively, and hence refults the idea of duration, and of time. Finally, on remarking the diversity of fensations, which fucceed each other; it begins to reckon one, two, three, &c. though this should not go farther, from want of figns, or names, wherewith to mark numbers. For, fuppofing a man has just begun to exift, and who has hitherto experienced no fenfations, but those of which I have been speaking; far from having created a language for himfelf, he only knows how to exert his first faculties, on the simple ideas which the fenfe of fmelling prefents to him.

You see, then, that the man in question, has already acquired the capacity of forming to himself ideas of diversity, of the present, of the past, and

even of the future; afterwards, of fuccession, of the duration of time, and of number, or at least of the elements of these ideas. Some authors pretend, that fuch a man could not acquire the idea of the duration of time, without a fuccession of different sensations; but it appears to me, that the fame fenfation, the finell of the rose, for example, being continued for a confiderable time together, he would be differently affected by it, than he would, if it were prefently withdrawn. A very long duration, of the fame fenfation, would, at length, become tirefome, which would, necessarily, excite in him the idea of duration. It must certainly be allowed, that his foul would be fenfible of a very different effect, if the fenfation were continued long, than if it lasted only for a moment: and the foul will clearly perceive this difference; it will, accordingly, have fome idea of duration, and of time, without any variation of the fenfations.

These reflections which the soul makes, occasioned by it's sensations, are what properly belong to it's spirituality, the body surnishing only simple sensations. The perception of these sensations is, already, an act of the soul's spirituality; for a body can never acquire ideas.

20th January, 1761.

# LETTER XCVI.

Conviction of the Existence of what we perceive by the Senses. Of the Idealists, Egotists, and Materialists.

In all the fenfations which we experience, when one of our fenfes is struck by any object, it is a matter of high importance to remark, that the soul not only acquires an idea, conformed to the impression made on the nerves, but that it judges, at the same time, there must exist an exterior object, which furnished this idea. Though habit makes us consider this judgment as extremely natural, yet we have reason to be assonished at it, when we examine, more attentively, what then passes in our brain.

An example will place this in a clear light. I shall suppose you looking at the full moon, by night; the rays which enter into your eyes will, at once, paint on the retina, an image similar to the moon, for the minute particles of the retina are, by the rays, put into a vibration similar to that which agitates those of the moon. Now, the retina, being only a contexture of nerves, extremely subtile, you easily comprehend, that these nerves must hence undergo a certain agitation, which will be transmitted to the origin of the nerves in the brain. There will be excited, therefore, likewise, in that portion of the brain, a certain agitation, which is the real object that the soul contemplates, and from which it derives an article of knowledge, which is the idea of the moon.

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Consequently, the idea of the moon is nothing else, but the contemplation of this slight agitation, affecting the origin of the nerves.

The activity of the foul is fo much attached to the fpot in which the nerves terminate, that it abfolutely knows nothing of the images painted on the bottom of the eye, and still less of the moon, whose rays have formed these images. The foul, however, does not satisfy itself with the mere speculation of the agitation in the brain, which supplies it immediately with the idea of the moon, it subjoins to this, the judgment, that there really exists, out of us, an object, which we call the moon. This judgment is reduced to the following reasoning.

There has taken place in my brain a certain agitation, a certain impression; I do not absolutely know by what cause it has been produced, as I know nothing even of the images, which are the immediate cause of it upon the retina; nevertheless, I boldly pronounce, that there is a body out of me, the moon, which supplied me with this sensation.

What a consequence? May it not be more probable, that this agitation, or this impression, is produced, in my brain, by some internal cause, such as the motion of the blood, or, perhaps, merely by chance? What right have I, then, to conclude, that the moon actually exists? If I conclude from it, that there is, at the bottom of my eye, a certain image, this might pass; as, in fact, this image is the immediate cause of the impression made on my brain; though it was sufficiently bold to hazard even this conclusion.

conclusion. But I go much farther, and, because there is a certain agitation in my brain, I proceed to conclude, that there exists, out of my body, nay, in the heavens, a body which is the first cause of such impression, and that this body is the moon.

In fleep, when we imagine we fee the moon, the foul acquires the fame idea: and, perhaps, a fimilar agitation is then produced in the brain, as the foul imagines that it then really fees the moon. It is, undoubtedly, certain, that, in this, we deceive ourfelves: but what affurance have we, that our judgment is better founded when we are awake? Philofophers have loft their way, more than once, in endeavouring to folve this difficulty.

What I have just faid, respecting the moon, takes place with regard to all the bodies which we see. The consequence is not apparent, that there must exist bodies out of us, because our brain undergoes certain agitations, or impressions. This applies even to our own limbs, and to our whole body, of which we know nothing but by means of the senses, and of the impressions which they make in the brain: if, then, these impressions, and the ideas which the soul derives from them, prove nothing as to the existence of body, that of our own body becomes equally doubtful.

You will not, therefore, be furprized, that there should be philosophers, who have openly denied the existence of bodies; and, in truth, it is not easy to refute them. They derive a very strong argument from dreams, in which we imagine, that we see so

many bodies, which have no existence. It is said, with truth, that then it is pure illusion; but what assurance have we, that we are not under the power of a similar illusion when awake? According to these philosophers, it is not an illusion: the soul, they admit, perceives a certain impression, an idea, but they boldly deny it to be a consequence, that bodies really exist, which correspond to those ideas. The supporters of this system are called *Idealists*, because they admit the *ideas* only of material things, and absolutely deny their existence. They may, likewise, be denominated *Spiritualists*, as they maintain, that no beings exist, except spirits.

And as we do not know other spirits, but by means of the senses, or of ideas, there are philosophers who go so far as to deny the existence of all spirits, their own soul excepted, of the existence of which every one is completely convinced. These are called *Egotists*, because they pretend that nothing exists but their own soul.

To them are opposed the philosophers, whom we denominate *Materialists*, who deny the existence of spirits, and maintain, that every thing which exists is matter, and that what we call our soul is only matter, extremely subtile, and thereby rendered capable of thought.

: 24th January, 1761.

### LETTER XCVII.

# Refutation of the Idealists.

I WISH it were in my power to furnish you with the arms necessary to combat the Idealists and the Egotists, by demonstrating, that there is a real connection between our sensations and the objects themselves, which they represent; but the more I think of it, the more I feel my own incapacity.

It would be ridiculous to think of engaging with the Egotists: for a man who imagines he alone exists, and who does not believe in my existence, would act in contradiction to his own fystem, if he paid any attention to my reasoning, which, according to him, would be that of an imaginary being. It is, likewife, a hard talk to confute the Idealists, nay, it is impossible to convince, of the existence of bodies, a man obstinately determined to deny it. Though no fuch philosophers existed, it would be highly interefting to be able to convince ourselves, that as often as our foul experiences fenfations, it may be with certainty concluded, that bodies likewife exift; and that, when my foul is affected by the fenfation of the moon, I may thence boldly infer the existence of the moon.

But the union which the Creator has established between the foul and the brain, is a mystery so unfathomable, that all our knowledge of it amounts only to this: Certain impressions made in the brain, where the seat of the soul is, excite in it certain ideas, or sensations; but the bow, of this influence, is absolutely unknown to us. We ought to satisfy ourselves with knowing, that this influence subsists, which experience sufficiently confirms; and it is in vain to investigate bow this is produced. Now, the same experience which proves it, informs us, likewise, that every sensation always disposes the soul to believe that there exists, out of it, some object which excited such sensation; and that sensation discovers to us several properties of the object.

It is, then, a most undoubted fact, that the soul always concludes, from any sensation whatever, the existence of a real object, out of us. This is so natural to us, from our earliest infancy, and so universally the case with all men, and even with animals, that it cannot, with any propriety, be called a prejudice. The dog that barks when he sees me, is certainly convinced that I exist; for my presence excites in him the idea of my person. The dog, then, is not an idealist. Even the meanest infects are assured that bodies exist, out of them, and they could not have this conviction, but by the sensations excited in their souls.

I believe, therefore, that fenfations include much more than those philosophers are disposed to admit. They are not only simple perceptions of certain impressions made in the brain; they supply the soul not with ideas only, but they effectively represent to it objects externally existing, though we cannot comprehend how this is done.

In fact, what refemblance can there be between the luminous idea of the moon, and the flight impression which it's rays may produce in the brain, by means of nerves?

The idea, even in as far as the foul perceives it, has nothing material; it is an act of the foul, which is a fpirit: it is not necessary, therefore, to look for a real relation between the impressions of the brain, and the ideas of the foul; it is enough for us know, that certain impressions made in the brain, excite certain ideas in the foul, and that these ideas are representations of objects externally existing, of whose existence they give us the assurance.

Thus, when my brain excites in my foul the fenfation of a tree, or of a house, I pronounce, without hesitation, that a tree, or a house, really exists, out of me, of which I know the place, the size, and other properties. Accordingly, we find neither man nor beast, who calls this truth in question. If a clown should take it into his head to conceive such a doubt; and should say, for example, he does not believe that his bailiss exists, though he stands in his presence, he would be taken for a madman, and with good reason; but when a philosopher advances such sentiments, he expects we should admire his knowledge and sagacity, which infinitely surpass the apprehensions of the vulgar.

It appears to me, accordingly, abundantly certain,
B b 4 that

that fuch extravagant fentiments would never have been maintained, but from pride, and an affectation of fingularity: and you will readily agree, that the common people have, in this respect, much more good sense than those learned gentlemen, who derive no other advantage from their researches, but that of bewildering themselves in a labyrinth of chimeras, unintelligible to the rest of mankind.\*

Let it be established, then, as a certain rule, that every fenfation not only excites in the foul an idea, but shews it, if I may so express myself, an external object, of whose existence it gives full assurance, without practifing a deception. A very formidable objection, however, is started against this, arising from dreams, and the reveries of fick persons, in which the foul experiences a great variety of fenfations of objects which no where exist. The only reflection I shall suggest on this subject is, that it must be very natural for us to judge that the objects, the fenfations of which the foul experiences, really exist, as we judge after this manner even in fleep, though then we deceive ourselves; but it does not thence follow, that we likewife deceive ourfelves when we are awake. In order to folve this objection, it is

necessary

<sup>\*</sup> Mr. Euler feems here to be confounding two different questions, that of the existence of exterior objects, and that of a kind of real resemblance between these objects and the idea which we have of them. Barclay has, however, carefully distinguished them, and has clearly pointed out the difference. All we can at present do, is to refer the reader to the article Existence, in the Encyclopedia, the only work in which these questions have been treated with an exact analysis.—F. E.

necessary to know better the difference of the state of the man who is asleep, and of him who wakes; and none, perhaps, know this less than the learned, which must surely be a matter of some surprize to you.

27th January, 1761.

# LETTER XCVIII.

The Faculty of Perceiving. Reminiscence, Memory, and Attention. Simple and compound Ideas.

You are by this time fensible, that objects, by acting upon our fenses, excite in the soul sensations, from which we judge that they really exist, out of us. Though the impressions which occasion these sensations are made in the brain, they present, then, to the soul, a species of image similar to the object which the soul perceives, and which is called the sensible idea, because it is excited by the senses. Thus, on seeing a dog, the soul acquires the idea of it, and it is by means of the senses that the soul comes to the knowledge of external objects, and acquires sensible ideas of them, which are the soundation of all our attainments in knowledge.

This faculty of the foul, by which it acquires the knowledge of external things, is denominated the faculty of perception, and depends, no doubt, on the wonderful union which the Creator has established between the foul and the brain. Now, the foul has

still another faculty, that of recalling ideas already communicated by the senses; and this faculty is named reminiscence, or imagination. Thus, having once seen an elephant, you will be able to recollect the idea of that animal, though it is no longer before you. There is, however, a mighty difference between actual and recollected ideas: the former make an impression much more lively and interesting than the latter, but the faculty of recalling ideas is the principal source of all our knowledge.

Did we lofe the ideas of objects as foon as they ceafe to act upon our fenfes, we should never be able to make any reflection, any comparison; and our knowledge would be entirely confined to the things which we should feel at the moment, all preceding ideas being extinguished, as if we had never possessed them.

It is, therefore, a faculty effential to reasonable beings, and with which animals too are endowed, that of being able to recollect past ideas. You know the faculty of which I speak is memory. It by no means follows, however, that we have it always in our power to recall all our past ideas. How frequently do we exert ourselves in vain to recollect certain ideas which we formerly had? Sometimes we forget them entirely; but for the most part only partially.

If you should happen, for example, to forget the demonstration of the Pythagorean theorem; with all your efforts, perhaps, you should not be able to recollect it, but this would be only a partial forget-fulness;

fulness; for as soon as I had again drawn the figure, and put you into the train of the demonstration, you will presently recollect it, and this second demonstration will make on your mind quite a different impression from the first. We see, then, that the reminiscence of ideas is not always in our power, though they may not be wholly extinguished; and a slight circumstance is frequently capable of reproducing them.

We must, therefore, carefully distinguish between sensible and recollected ideas. Sensible ideas are represented to us by the senses; but we ourselves form recollected ideas, on the model of the sensible, as far as we remember them.

The doctrine of ideas is of the last importance for the purpose of a thorough disquisition of the real fources of human knowledge. And first, ideas are diftinguished into fimple and complex. A simple idea is that in which the foul finds nothing to distinguish, and remarks no parts different from each other. Such is, for example, the idea of a fmell, or of a fpot on a fubstance of one colour; such is, likewise, that of a star, in which we perceive only one luminous point. A complex idea is a reprefentation in which the foul is able to diffinguish feveral different things. When, for inftance, we look attentively at the moon, we discover several dark spots, surrounded by contours more luminous; we remark, also, her round figure, when she is full, and her horned figure, when waxing or waning. On viewing her through the telescope, telescope, there are many other particulars distinguishable.

How many different things do we not perceive in beholding a noble palace, or a fine garden? When you do me the honour to read this letter, you will discover in it the different traits of the characters, which you can with eafe diffinguish from each other. This, then, is a complex idea, as it contains a variety of fimple ideas. Not only this letter, taken in whole, prefents a complex idea, from it's confifting of a plurality of words; but every word, too, is a complex idea, being composed of feveral characters; nay, every character is one, from the fingularity of the form which diffinguishes it from others: but the elements or points which constitute every character, may be confidered as fimple ideas, in as much as you no longer perceive in them any diversity. A greater degree of attention will likewise discover some variety in thefe elements, on viewing them through a microscope.

There is a great difference, therefore, even in the manner of contemplating objects. When we observe them only slightly and transiently, we perceive very little variety; but, to an attentive consideration, every particular detail stands disclosed. A favage, on throwing his eyes over this letter, will take it for a piece of paper scribbled all over, and will distinguish only the black from the white, whereas an attentive reader observes in it the peculiar form of every character. Here, then, we have a new faculty of the foul,

foul, denominated attention, by which it acquires the fimple ideas of the different things that meet in one object.

Attention requires address, the result of long and frequent exercise, to render it capable of distinguishing the different parts of an object. A clown and an architect, paffing by a palace, will both receive the impression of the rays which enter into their eyes; but the architect will discover a thousand minute particulars, of which the clown has no perception. Attention alone produces this difference.

31/t January, 1761.

#### LETTER XCIX.

Division of Ideas into clear and obscure, distinct and confused. Of Distraction.

TF we confider, in a flight manner only, a reprefentation made to us by the fenfes, the idea which we acquire from it is very imperfect, and we fay it is obscure: but the more attention that we employ to diftinguish all it's parts, the more perfect or distinct our idea will become. In order to acquire a perfect or distinct idea of an object, it is not then fusicient that it should be represented in the brain, by impresfions made upon the fenfes, the foul, too, must apply it's attention, which is properly an act of the foul, independent upon the body.

It is farther necessary that the representation in the

the brain should be well expressed, and contain the different parts and qualities which characterize the object. This takes place when the object is presented to the senses in a suitable manner. When, for example, I see a piece of writing, at the distance of ten seet, I am unable to read it, let me employ whatever degree of attention I may; the distance of the characters prevents their being accurately expressed on the bottom of the eye, and consequently also in the brain: but if the same writing is brought to a proper distance, I can read it, because then all the characters are distinctly represented on the bottom of the eye.

You know that we employ certain instruments in order to procure a more perfect representation in the organs of sense; such as microscopes and telescopes; which are intended as supplements to the imperfection of vision. But, in employing their assistance, we are incapable of attaining a distinct idea, without attention; otherwise we acquire but an obscure idea, nearly such as we should have had by taking a glimpse of the object only.

I have already remarked, that sensations are by no means indifferent to the soul, but agreeable or disagreeable: and this agreeableness, or it's opposite, excites our attention, unless the soul is pre-occupied by several other sensations which entirely engross it: this last state of the soul is termed distraction.

Exercise, likewise, greatly contributes to strengthen attention: and there cannot be a mode of exercise more suitable to children than teaching them to read; for they are thereby laid under the necessity

of fixing their attention fuccessively on every character, and of impressing on their minds a clear idea of the figure of each. It is easy to see that this exercise must be at first extremely painful; but such a habit is speedily acquired, that even a child, after a little application, can read with astonishing quickness. In reading a piece of writing, we must have a very distinct idea of every character; thus attention is susceptible of a very high degree of perfection from exercise.

With what amazing rapidity will a proficient in music execute the most difficult piece, though he never faw it before. It is certain that his attention must have run over all the notes, one after another, and that he remarked the fignification of each. His attention, however, is not confined only to thefe notes; it prefides, likewife, over the motion of the fingers, not one of which moves but by an express order of the foul; he remarks, likewife, at the fame time, how the other performers execute their parts. It is, upon the whole, altogether furprifing to what a height the address of the human mind may be carried by application and exercife. Shew the fame piece of music to a beginner; how much time does it require to impress on his mind the fignification of every note, and to give him a complete idea of it: while the mafter acquires it by almost a fingle glance.

This ability extends equally to all other kinds of objects, in which one man may infinitely furpass another. There are persons who, with one glance fixed on a person passing before them, acquire a distinct idea, not only of all the features of the face,

but the particulars of his whole drefs, down to the minutest trisles, while others are incapable of remarking the most striking circumstances.

We observe, in this respect, an infinite difference among men. Some promptly catch all the different marks of an object, and form to themselves a distinct idea of it, while that formed by others is extremely obscure: This difference depends, not only on mental penetration, but likewife on the nature of the objects. A musician catches at once the whole piece of music, and acquires a distinct idea of it: but prefent him with a piece of writing in Chinese characters, and he will have only very obfcure ideas indeed of fuch writing: the Chinese, on the contrary, will know, at first fight, the real import of each character, but will, in his turn, understand nothing of mufical notes. The botanist observes in a plant which he never faw before, a thousand particulars which escape the attention of another; and the architect difcerns, by a fingle glance, in a building, many things which another, with a much greater degree of attention, could not have discovered.

It is always useful to form distinct ideas of the objects presented to our senses; in other words to remark all the parts of which they are composed, and the marks which distinguish and characterize them. From these observations you will easily comprehend the division of ideas into obscure and clear, into confused and distinct. The more distinct they are, the more they contribute to the advancement of knowledge.

3d February, 1761.

#### LETTER C.

Of the Abstraction of Notions. Notions general and individual. Of Genus and Species.

THE fenses represent objects only which exist externally; and sensible ideas all refer to them; but of these sensible ideas the soul forms to itself a variety of other ideas, which are indeed derived from these, but which no longer represent objects really existing.

When, for example, I look at the full moon, I defix my attention only on it's contour, I form the idea of roundness; but I cannot affirm, that roundness exists of itself. The moon is round, but the round figure does not exist separately out of the moon. It is the same with respect to all other figures; and when I see a triangular, or square table, I may have the idea of a triangle, or of a square, though such a sigure exists no where of itself, or separately from an object possessing that sigure.

The ideas of numbers have the fame origin. Having feen two or three perfons, the foul forms the idea of two or three, without attaching it any longer to the perfons. Having already acquired the idea of three, the foul is able to proceed, and to form the ideas of greater numbers, of four, five, ten, a hundred, a thousand, and so on, without ever having precisely seen so many things together. A single instance, therefore, in which we have seen two or three

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objects, may carry the foul forward to the formation of the ideas of other numbers, be they ever fo great.

The fame thing holds as to figures; and you have the power of forming to yourfelf the idea of a polygon, with 1761 fides, for example, though you never have feen an object of that form, and though no one fuch, perhaps, ever existed.

Here the foul exerts a new faculty, which is called the power of abstraction; this takes place when the foul fixes it's attention on only one quantity or quality of the object, and considers it separately, as if it were no longer attached to the object. When, for instance, I put my hand on a heated stone, and confine my attention to the heat only, I form from it the idea of heat, which is no longer attached to the stone. This idea of heat is formed by abstraction, as it is separated from the stone, and the soul might have derived the same idea from touching a piece of wood heated, or by plunging the hand into hot water.

Thus, by means of abstraction, the soul forms a thousand other ideas of the quantities and properties of objects, by separating them afterwards from the objects themselves: as, when I see a red coat, and six my attention only on the colour, I form the idea of red, separate from the coat, and it is obvious that a red slower, or any other substance of that colour, would have enabled me to form the same idea.

These ideas, acquired by abstraction, are denominated notions, to distinguish them from sensible ideas, which represent to us objects really existing.

It is alleged that the power of abstraction is a prerogative of men, and of other rational beings, and that the beafts are entirely deftitute of it. A beaft may experience the fame fenfation of hot water that we do, but is unable to feparate the idea of heat and that of the water itself: it knows heat only in so far as it is connected with the water, but has not the abstract idea of heat which we have. It is faid, that these notions are general ideas, which extend to several things at once, as we may find heat in ftone, wood, water, or any other body; but our idea of heat is not attached to any one body; for if my idea of heat were attached to a certain stone, which first fupplied me with that idea, I could not affirm that wood or other bodies were hot. Hence it is evident, that these notions, or general ideas, are not attached to certain objects, as fensible ideas are; and as they diftinguish man from the brute creation, they properly exalt him to a degree of rationality wholly unattainable by the beafts.

There is still farther a species of notions, likewise, formed by abstraction, which supply the soul with the most important subjects on which to employ it's powers: these are the ideas of genus and species. When I see a pear-tree, a cherry-tree, an apple-tree, an oak, a sir, &c. all these ideas are different; I, nevertheless, remark in them several things which they have in common; as the trunk, the branches, and the roots; I stop short only at those things which the different ideas have in common, and the object,

in which all fuch qualities meet, I call a tree. Thus the idea of tree, which I have formed in this manner, is a general notion, and comprehends the fenfible ideas of the pear-tree, the apple-tree, and, in general, of every tree that exists.

Now, the tree which corresponds to my idea of tree, no where exists; it is not the pear-tree, for then the apple would not be comprehended under it; for the same reason, it is not the cherry-tree, nor the plumb, nor the oak, &c.; in a word, it exists only in my soul; it is only an idea, but which is realized in an infinite number of objects. In like manner, when I speak of a cherry-tree, it too is a general notion, which comprehends all the cherry-trees that exist: this notion is not restricted to a particular cherry-tree in my garden: for then every other cherry-tree would be excluded.

With respect to general notions, every existing object, comprehended under one, is denominated an individual, and the general idea, say that of the cherry-tree, is denominated species or genus. These two words signify nearly the same thing, but genus is the more comprehensive, including in it a variety of species. Thus the notion of a tree may be considered as a genus, as it includes the notions of peartrees, apple-trees, oaks, firs, and so on, which are species; and of so many others, each of which contains a great number of existing individuals.

This manner of forming general ideas is, therefore, likewife, performed by abstraction, and it is here, chiefly,

chiefly, that the foul exerts the activity and performs the operations from which all our knowledge is derived. Without these general notions, we should differ nothing from the brutes.

7th February, 1761.

### LETTER CI.

Of Language; it's Nature, Advantages, and Necessity, in order to the Communication of Thought, and the Cultivation of Knowledge.

WHATEVER aptitude a man may have to exercife the power of abstraction, and to furnish himself with general ideas, he can make no considerable progress without the aid of language, spoken or written. Both the one and the other contains a variety of words, which are only certain signs, corresponding to our ideas, and whose signification is settled by custom, or the tacit consent of several men who live together.

It would appear, from this, that the only purpose of language to mankind is mutually to communicate their sentiments, and that a solitary man might do very well without it; but a little reslection only is necessary to be convinced, that men stand in need of language, as much to pursue and cultivate their own thoughts, as to keep up a communication with others.

To prove this, I remark, first, that we have scarcely

C c 3 a word

a word in any language whose signification is attached to one individual object. If each cherry-tree in a whole country had it's proper name, as well as every pear-tree, and, in general, every individual tree; what an enormous complication, in language, would result from it? Were I under the necessity of employing a particular term to denote every sheet of paper in my bureau, or if I should, from caprice, think sit to give each a particular name, this would be as useles to myself as to others.

It is, then, a very imperfect description of language to say, that men have, from the first, imposed on all individual objects, certain names to serve them for signs. The words of a language express general notions, and you will rarely find one which marks only a single individual. The name, Alexander the Great, is applicable to one particular person; but then it is a compound name. There may have been many thousands of Alexanders, and the epithet great, extends to an infinite number of things. It is thus, that all men bear names, to distinguish them from others, though these names may be frequently common to many.

The effence of a language confifts, rather, in it's containing words to denote general notions; as that of tree corresponds to a prodigious number of individual beings. These words serve not only to convey to others, who understand the same language, the same idea which I affix to the words; but they are, likewise, a great affistance to me, in representing this idea to myself. Without the word tree, which represents

reprefents to me the general notion of a tree, I must imagine to myself at once a cherry-tree, a pear-tree, an apple-tree, a fir, &c. and thence extract what they have in common. This would necessarily oppress the mind, and speedily involve it in the greatest perplexity. But having, once for all, determined to express, by the term tree, the general notion formed by abstraction, this term always excites in my foul the fame notion, without my having occasion to recollect it's origin; and, accordingly, the word tree alone, for the most part, constitutes the object of the foul, without the representation of any real tree,

The word man is, in like manner, a fign to denote the general notion of what all men have in common, and it would be very difficult to tell or to make the enumeration of all that this notion contains. Would you fay that he is a living two-legged being? A cock would likewife be included in this description. Would you fay, in the words of Plato's definition, that he is a two-legged animal without feathers? You have only to strip the cock of his feathers, in order to obtain the Platonic man.

I do not know whether those who say that man is an animal endowed with reason, express themselves more accurately: for how often do we take for men certain beings of whose rationality we have no affurance. On viewing an army, I have not the leaft doubt that every foldier is a man, though I have not the finallest proof that they are all endowed with reason. If I were to make an enumeration of all the members necessary to constitute a man, some men

would

would always be found defective in one, perhaps in feveral of these, or we might find some beast who had them all. On investigating, therefore, the origin of the general notion of man, it is almost impossible to say wherein it consists.

No one, however, has any doubt refpecting the fignification of the word; because every one, wishing to excite this notion in his soul, has only to think on the word man, as if he saw it written on paper, or heard it pronounced, according as the respective language of any one may be.

Hence we see that, for the most part, the objects of our thoughts are not so much the things them-selves, as the words by which these things are denoted in language; which greatly facilitates the exercise of thought. What idea, in fact, do we associate with the terms virtue, liberty, goodness, &c.? Not surely a sensible image; but the soul having once formed the abstract notions which correspond to these terms, afterwards substitutes them, in it's thoughts, in place of the things which they denote.

You may eafily conceive how many abstractions it was necessary to make, in order to arrive at the notion of virtue. The actions of men were sirst to be considered; they were, then, to be compared with the duties imposed on them; in consequence of this, we give the name of virtue to the disposition which a man has to regulate his actions conformably to his duties. But, on hearing the word virtue rapidly pronounced in conversation, do we always connect with it this complex notion? And what idea is ex-

cited in the mind, on hearing the particle and or also pronounced? It is readily seen, that these words import a species of connection, but take what pains you please to describe this connection, you will find yourself under the necessity of employing other words, whose signification it would be equally difficult to explain; and if I were to attempt an explanation of the import of the particle and, I must make frequent use of that very particle.

You are now enabled to judge of what advantage language is to direct our thoughts; and that, without language, we should hardly be in a condition to think at all.

10th February, 1760.

### LETTER CII.

Of the Perfections of a Language. Judgments and Nature of Propositions, affirmative and negative; universal, or particular.

I HAVE been endeavouring to fhew you, how neceffary language is to man, not only for the mutual communication of fentiment and thought, but, likewife, for the improvement of the mind, and the extension of knowledge.

These signs, or words, represent, then, general notions, each of which is applicable to an infinite number of objects: as, for instance, the idea of hot, and of heat, to every individual object which is hot; and

the idea, or general notion of tree, is applicable to every individual tree in a garden, or a forest, whether cherries, pears, oaks, or firs, &c.

Hence you must be sensible how one language may be more perfect than another. A language always is so, in proportion as it is in a condition to express a greater number of general notions, formed by abstraction. It is with respect to these notions that we must estimate the perfection of a language.

Formerly there was no word in the Russian language to express what we call justice. This was certainly a very great defect; as the idea of justice is of very great importance in a great number of our judgments and reasonings, and as it is scarcely possible to think of the thing itself without a term expressive of it. They have, accordingly, supplied this defect, by introducing into that language a word which conveys the notion of justice.

These general notions, formed by abstraction, are the source of all our judgments and of all our reasonings. A judgment is nothing else but the affirmation, or negation, that a notion is applicable, or inapplicable; and when such judgment is expressed in words, we call it a proposition. To give an example: All men are mortal, is a proposition which contains two notions; the first, that of men in general; and the second, that of mortality, which comprehends whatever is mortal. The judgment consists in pronouncing and affirming, that the notion of mortality is applicable to all men. This is a judgment, and, being expressed in words, it is a proposition; and, because

it affirms, we call it an an affirmative proposition. If it denied, we would call it negative, such as this, no man is righteous. These two propositions, which I have introduced as examples, are universal, because the one affirms of all men, that they are mortal, and the other denies that they are righteous.

There are likewise particular propositions, both negative and affirmative; as, some men are learned, and some men are not wise. What is here affirmed, and denied, is not applicable to all men, but to some of them.

Hence we derive four species of propositions. The first is that of affirmative and universal propositions, the form of which in general is:

## Every A is B.

The fecond species contains negative and univerfal propositions, the form of which in general is:

### No A is B.

The third is, that of affirmative propositions, but particular, contained in this form:

### Some A is B.

And, finally, the fourth is that of negative and particular propositions, of which the form is:

### Some A is not B.

All these propositions contain, essentially, two notions, A and B, which are called the terms of the proposition: the first of which affirms or denies some thing; and this we call the subject; and the second, which we say is applicable, or inapplicable, to the first, is the attribute. Thus, in the proposition, All men are mortal, the word man, or men, is the subject, and the word mortal the attribute: these words are much

much used in logic, which teaches the rules of just reasoning.

These four species of propositions may likewise be represented by sigures, so as to exhibit their nature to the eye. This must be a great affistance toward comprehending more distinctly wherein the accuracy of a chain of reasoning consists.

As a general notion contains an infinite number of individual objects, we may consider it as a space in which they are all contained. Thus for the notion of man we form a space (plate I. fig. 1.) in which we conceive all men to be comprehended. For the notion of mortal, we form another, (fig. 2.) in which we conceive every thing mortal to be comprehended. And when I affirm, all men are mortal, it is the same thing with affirming, that the first figure is contained in the second.

I. Hence it follows, that the representation of an affirmative universal proposition is that in which the space A, (fig. 3.) which represents the fubject of the proposition, is wholly contained in the space B, which is the attribute.

II. As to negative universal propositions, the two spaces A and B, of which A always denotes the fubject, and B the attribute, will be represented thus,
(fig. 4.) the one separated from the other; because
we say, no A is B, or that nothing comprehended in
the notion A, is in the notion B.

III. In affirmative particular propositions, as, fome A is B, a part of the space A will be comprehended in the space B: (fig. 5.) as we see here, that something

thing comprehended in the notion A, is likewise in B.

IV. For negative particular propositions, as, fome A is not B; a part of the space A must be out of the space B, (fig. 6.) This sigure resembles the preceding; but we here remark, principally, that there is something in the notion A, which is not comprehended in the notion B, or which is out of it.

14th February, 1761.

#### LETTER CIII.

Of Syllogifms, and their different Forms, when the first Proposition is universal.

THESE circles, or rather these spaces, for it is of no importance of what sigure they are of, are extremely commodious for facilitating our reslections on this subject, and for unfolding all the boasted mysteries of logic, which that art finds it so dissicult to explain; whereas, by means of these signs, the whole is rendered sensible to the eye. We may employ, then, spaces formed at pleasure to represent every general notion, and mark the subject of a proposition, by a space containing A, and the attribute, by another which contains B. The nature of the proposition itself always imports either that the space of A is wholly contained in the space B, or that it is partly contained in that space; or that a part, at least,

least, is out of the space B; or, finally, that the space A is wholly out of B.\*

The two last cases, which represent particular propositions, seem to contain a doubt, as it is not decided, whether it be a great part of A which is contained, or not contained, in B. It is even possible,

\* Mr. Euler, who is ever minutely exact in all his details, subjoins here the following diagram, with this short introduction: "I shall once more give you a visible representation of these figures or emblems of the four species of propositions."

Emblems of the four Species of Propositions.

Affirmative univerfal.  B  Affirmative univerfal.	Negative univerfal.  A  B  No A is B.
Affirmative particular.  (A) B  Some A is B.	Negative particular.  A B Some A is not B.

The omission of this scheme, in the Paris edition, is the more unaccountable, that the very next paragraph immediately refers to it, and is lame and inconclusive without it.—E. E.

in the case of a particular proposition, that the notion A may contain the notion B entirely, as in plate I. fig. 7; and that, at the same time, as is clear from the sigure, a part of the space A may be in the space B, and that a part of A may no the in B. Now, if A were, for example, the idea of tree in general, and B that of oak, which is contained wholly in the sirst, the following propositions might be formed:

I. All oaks are trees.

II. Some trees are oaks.

III. Some trees are not oaks.

In like manner, if of two spaces one is entirely out of the other, as in plate I. fig. 4. I can as well fay, no A is B, as no B is A; as if I were to say: no man is a tree, and no tree is a man.

In the third case, where the two notions have a part in common, as in plate I. fig. 5. it may be said:

I. Some A is B.

II. Some B is A.

III. Some A is not B.

IV. Some B is not A.

This may fuffice to flew you how all propositions may be represented by figures: but their greatest utility is manifest in reasonings which, when expressed in words, are called syllogisms, and of which the object is to draw a just conclusion from certain given propositions. This method will discover to us the true forms of all syllogisms.

Let us begin by an affirmative universal proposition: Every A is B, (plate I. fig. 3.) where the space A is wholly in the space B, and let us see how a third notion notion C, must be referred to each of the other two notions A and B, in order to draw a fair conclusion. It is evident in the following cases.

I. If the notion C is entirely contained in the notion A, it will be fo, likewise, in the notion B: (plate I. fig. 8.) hence results this form of fyllogism:

Every A is B:

But Every C is A:

Therefore Every C is B.

Which is the conclusion.

Let the notion A, for example, comprehend all trees; the notion B every thing that has roots, and the notion C all oaks, and then our fyllogism will run thus:

Every tree has roots:

But Every oak is a tree:

Therefore Every oak has roots.

II. If the notion C has a part contained in A, that part will likewise be so in B, because the notion A is wholly included in the notion B, (plate I. fig. 9 and 10.)

Hence refults the fecond form of fyllogism:

Every A is B:

But Some C is A:

Therefore Some C is B.

If the notion C were entirely out of the notion A, nothing would follow with respect to the notion B: it might happen that notion C should be entirely out of B, (fig. 11.) or wholly in B, (fig. 12.) or partly only in B, (fig. 13.) fo that no conclusion could be drawn.

III. But if notion C were wholly out of notion B, it would likewise be wholly out of notion A, as we see in fig. 11. Hence results this form of syllogism:

Every A is B:

But No C is B, or no B is C:

Therefore No C is A.

IV. If the notion C has a part out of the uotion B, that same part will certainly likewise be out of the notion A, because this last is wholly in the notion B, (fig. 14.) Hence this form of fyllogism:

Every A is B:

But Some C is not B:

Therefore Some C is not A.

V. If the notion C contains the whole of notion B, part of notion C will certainly fall into notion A: (fig. 15.) Hence this form of fyllogism.

Every A is B:

But Every B is C:

Therefore Some C is A.

No other form is possible, while the first proposition is affirmative and universal.

Let us now suppose the first proposition to be negative and universal; namely,

### No A is B.

It is represented in fig. 4. where the notion A is entirely out of notion B; and the following cases will furnish conclusions.

I. If notion C is entirely in notion B, it must likewise be entirely out of notion A, (fig. 16.) Hence this form of fyllogism:

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### No A is B:

But Every C is B:

Therefore No C is A.

II. If notion C is entirely comprehended in notion A, it must also be entirely excluded from notion B, (fig. 17.) Hence a syllogism of this form:

No A is B:

But Every C is A:

Therefore No C is B.

III. If notion C has a part contained in notion A, that part must certainly be out of notion B; as in fig. 18. or in fig. 19. and 20. Hence a syllogism of this form:

No A is B:

But Some C is A, or fome A is C:

Therefore Some C is not B.

IV. In like manner, if notion C has a part contained in B, that part will certainly be out of A: as in fig. 21. as also fig. 22. and 23. Hence the following fyllogism:

No A is B:

But Some C is B, or some B is C:

Therefore Some C is not A.

As to the other forms, in which the first proposition is particular, affirmative, or negative; I shall shew, in another letter, how they may be represented by figures.

17th February, 1761.

#### LETTER CIV.

Different Forms of Syllogisms, whose first Proposition is particular.

In the preceding letter I have prefented you with the different forms of fyllogisms, or simple reasonings, which derive their origin from the first proposition, when it is universal, affirmative, or negative. It still remains that I lay before you those fyllogisms, whose first proposition is particular, affirmative, or negative, in order to have all possible forms of syllogism that lead to a fair conclusion.

Let, then, the first proposition, affirmative, and particular, be expressed in this general form.

Some A is B. (Plate I. fig. 5.)

in which a part of the notion A is contained in the notion B.

Let us introduce a third notion C, which, being referred to notion A, will either be contained in notion A, as in fig. 24, 25, and 26; or will have a part in the notion A, as in fig. 27, 28, and 29; or will be entirely out of notion A, as in fig. 1, 2, and 3, of plate II. No conclusion can be drawn in any of these cases; as it might be possible for notion C to be entirely within notion B, or in part, or not at all.

But if notion C contains, in itself, notion A, it is certain, that it will likewise contain a part of notion B: as in fig. 4 and 5, of plate II. Hence results this form of syllogism:

Some A is B: But Every A is C: Therefore Some C is B.

It is the fame when we compare notion C with notion B: we can draw no conclusion unless notion C contains notion B entirely; (see fig. 6 and 7.) for in that case, as notion A has a part contained in notion B, the same part will then certainly be contained likewise, in C: hence we obtain this form of syllogism:

Some A is B:

But Every B is C:

Therefore Some C is A.

Let us finally suppose, that the first proposition is negative and particular, namely,

Some A is not B.

It is represented in plate II. fig. 8. in which part of notion A is out of notion B.

In this case, if the third notion C contains notion A entirely, it will certainly also have a part out of notion B, as in fig. 9 and 10: which gives this syllogism:

Some A is not B:

But Every A is C:

Therefore Some C is not B.

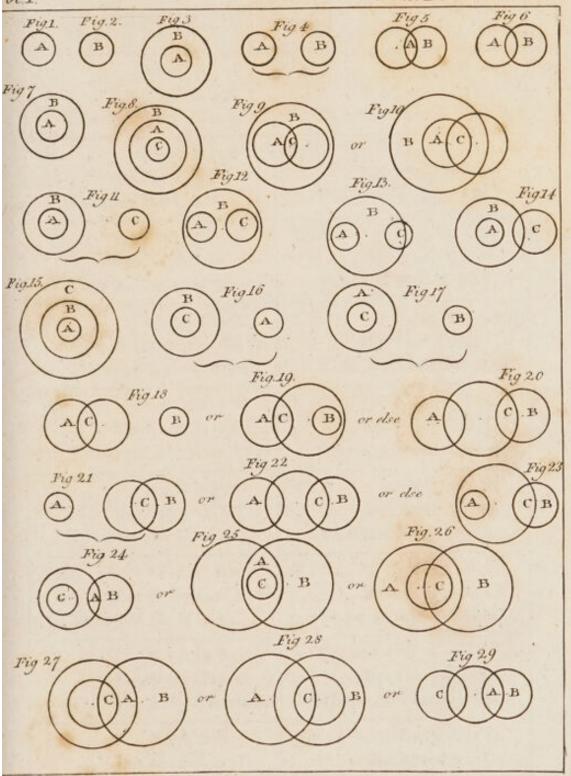
Again, if notion C is wholly included in notion B, as A has a part out of B, that same part will like wise certainly be out of C, (see fig. 11 and 12.) Hence this form of syllogism:

Some A is not B:

But Every C is B:

Therefore Some A is not C.

It may be of use to collect all these forms of syllogism into one table, in order to consider them at a single glance.





NEW REAL OF SHIPS TON TON THE	BOTTON CONTRACTOR
I. Every A is B:	XI. No A is B:
But Every C is A:	But Some C is B: Therefore Some C is not A.
Therefore Every C is B.	**************************************
II. Every A is B:	XII. No A is B:
But Some C is A: Therefore Some C is B.	But Some B is C: Therefore Some C is not A.
III. Every A is B: But No C is B:	XIII. Some A is B:
Therefore No C is A.	But Every A is C: Therefore Some C is B.
IV. Every A is B: But No B is C:	XIV. Some A is B: But Every B is C:
Therefore No C is A.	Therefore Some C is A.
V. Every A is B:	XV. Some A is not B:
But Some C is not B:	But Every A is C:
Therefore Some C is not A.	Therefore Some C is not B.
VI. Every A is B:	XVI. Some A is not B:
But Every B is C:	But Every C is B:
Therefore Some C is A.	Therefore Some A is not C.
VII. No A is B:	XVII. Every A is B:
But Every C is A:	But Some A is C:
Therefore No C is B.	Therefore Some C is B.
VIII. No A is B:	XVIII. No A is B:
But Every C is B:	But Every A is C:
Therefore No C is A.	Therefore Some C is not B.
IX. No A is B:	XIX. No A is B:
But Some C is A:	But Every B is C:
Therefore Some C is not B.	Therefore Some C is not A.
X. No A is B:	XX. Every A is B:
But Some A is C: Therefore Some C is not B.	But Every A is C: Therefore Some C is B.
Therefore Some Cisnot B.	Therefore Boule O Is D.

Of these twenty forms, I remark, that XVI. is the same with V. the latter changing into the former, it you write C for A, and A for C, and begin with the second proposition: there are, accordingly, but nine teen different forms.

The foundation of all these forms is reduced to two principles, respecting the nature of containing and contained.

1. Whatever is in the thing contained, must likewise be in the thing containing.

II. Whatever is out of the containing, must likewise be out of the contained.

Thus, in the last form, where the notion A is contained entirely in notion B, it is evident, that if A is contained in the notion C, or makes a part of it, that same part of notion C will certainly be contained in notion B, so that some C is B.

Every fyllogism, then, consists of three propositions, the two sirst of which are called the *premises*, and the third the *conclusion*. Now, the advantage of all these forms, to direct our reasonings, is this, that if the premises are both true, the conclusion, infallibly, is so.

This is, likewise, the only method of discovering unknown truths. Every truth must always be the conclusion of a syllogism, whose premises are indubitably true. Permit me only to add, that the former of the premises is called the major proposition, and the other the minor.

21st February, 1761.

### LETTER CV.

# Analysis of some Syllogisms.

If you have paid attention to all the forms of fyllogism, which I have proposed, you must see, that every syllogism necessarily consists of three propositions: the two sirst are called premises, and the third, the conclusion. Now the force of the nineteen forms, laid down, consists in this property common to them all, that if the two sirst propositions, or the premises, are true, you may rest, considently assured of the truth of the conclusion.

Let us confider, for example, the following fyllogifm.

But some slanderers are learned men:

Therefore some LEARNED MEN ARE NOT VIR-

Whenever you allow me the two first propositions, you are obliged to allow the third, which necessarily follows from it.

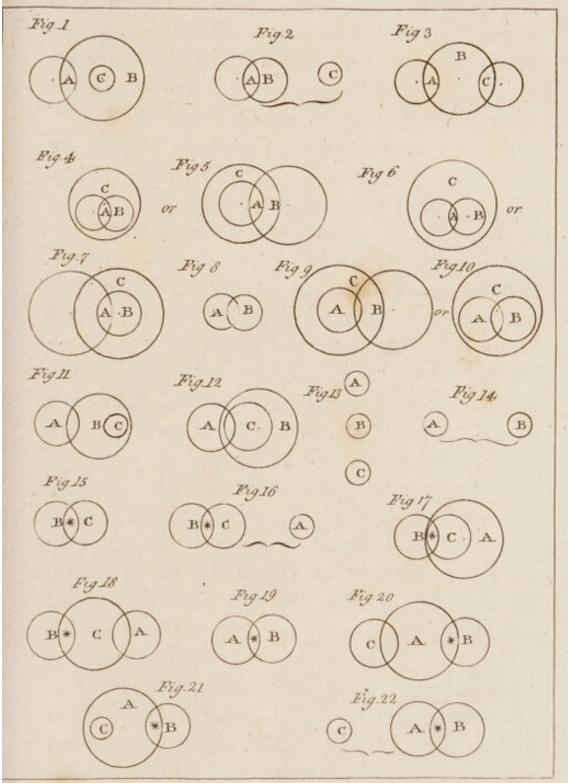
This fyllogism belongs to form XII. The same thing holds with regard to all the others, which I have laid down, and which the sigures, whereby I have represented them, render sensible. Here we are presented with three notions: (plate II. fig. 13.) that of virtuous men, that of slanderers, and that of learned men.

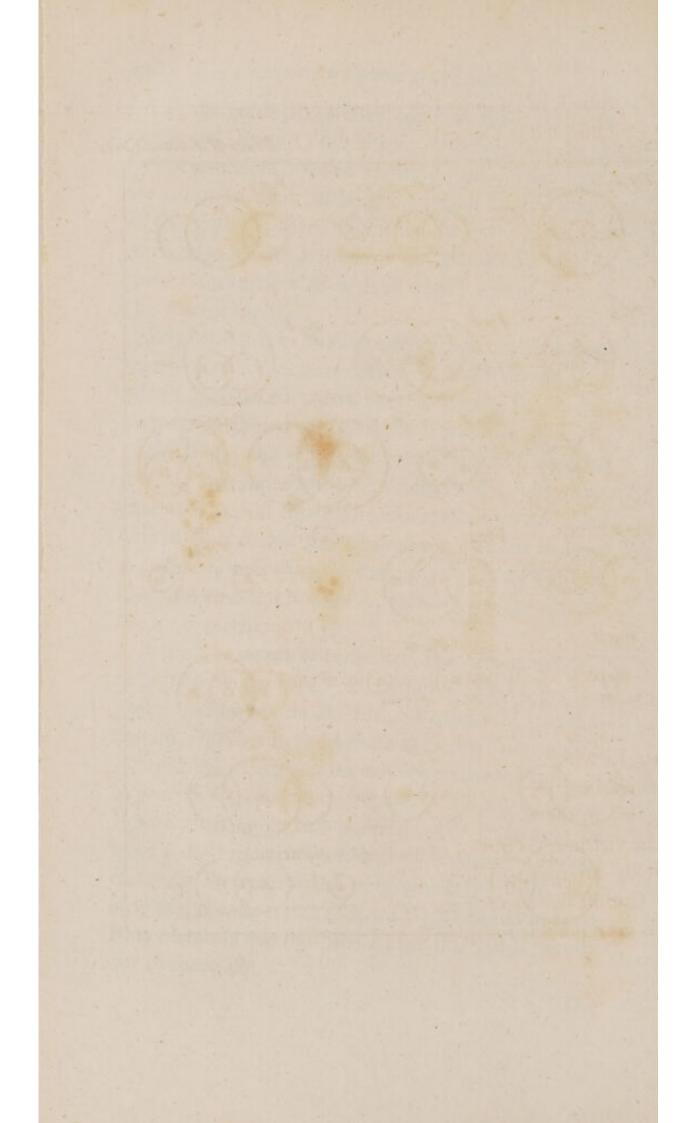
Let the space A represent the sirst, space B the second, and space C the third. It being said, in the sirst proposition, That no virtuous man is a slanderer; we maintain, that nothing contained in the notion of the virtuous man, that is, in the space A, is comprehended in the notion of the slanderer: that is, space B: therefore space A is wholly out of space B, (see plate II. fig. 14.)

But it is faid, in the fecond proposition, that some men comprehended in notion B, are, likewise, contained in that of learned, that is, in space C: or else, you may say, that part of space B is within space C; (plate II. sig. 15.) where the part of space B, included in C, is marked with a \*; which will be, likewise, part of space C. Since, therefore, some part of space C is in B, and that the whole space B is out of space A, it is evident, that the same part of space C must, likewise, be out of space A, that is, some learned men are not virtuous.

It must be carefully remarked, that this conclusion respects only the part \* of notion C, which is comprehended in notion B: for as to the rest, it is uncertain, whether it be likewise excluded from notion A, as in plate II. sig. 16, or wholly contained in it, as in plate II. sig. 17, or only in part, as in plate II. sig. 18.

Now, this being left uncertain, the remainder of space C falls not at all under consideration; the conclusion is limited to that only which is certain, that is to say, the same part of space C, contained in space B, is certainly out of space A, for this last is wholly out of space B,





The justness of all the other forms of fyllogism may be demonstrated in like manner; but all those which deviate from the nineteen forms laid down, or which are not comprehended under them, are destitute of foundation, and lead to error and falshood.

You will clearly difcern the fault of fuch a fyllogifm, by an example, not reducible to any of the nineteen forms:

SOME LEARNED MEN ARE MISERS:

But NO MISER IS VIRTUOUS:

Therefore SOME VIRTUOUS MEN ARE NOT LEARNED.

This third proposition, may, perhaps, be true; but it does not follow from the premises. They too (the premises) may very well be true, and, in the present instance, they actually are so, but the third is not, for that, a fair conclusion: because it is contrary to the nature of just syllogism, in which the conclusion always must be true, when the premises are so. Accordingly, the fault of the form, above proposed, is immediately discovered, by casting your eyes on fig. 13. of plate II. Let space A contain all the learned; space B all the avaricious; and space C all the virtuous. Now, the sirst proposition is represented by fig. 19. in which part \* of space A, (the learned) is contained in space B, (the avaricious).

Again, in the fecond proposition, the whole space C, (the virtuous) is out of space B, (the avaricious): but it by no means follows, (fig. 20.) that part of space C must be out of space A.

It is even possible for space C, to be entirely within space

space A, as in fig. 21, or entirely out of it, as in fig. 22. and, at the same time, entirely out of space B.

A fyllogism of this form, accordingly, is totally false and absurd.

Another example will put the matter beyond a doubt:

#### SOME TREES ARE OAKS:

But NO OAK IS A FIR:

Therefore some firs are not trees.

This form is, precifely, the fame with the preceding, and the falshood of the conclusion is manifest, though the premises are undoubtedly true.

But whenever a fyllogism is reducible to one of the above nineteen forms, you may be affured, that if the two premises are true, the conclusion unquestionably always is so too. Hence you perceive, how, from certain known truths, you attain others before unknown; and that all the reasonings, by which we demonstrate so many truths in geometry, may be reduced to formal syllogisms. It is not necessary, however, that our reasonings should always be proposed in the syllogistic form, provided the fundamental principles be the same. In conversation, in discourse, and in writing, we rather make a point of avoiding syllogism.

I must farther remark, that, as the truth of the premises brings forward that of the conclusion, it does not thence necessarily follow, that when one or both of the premises are false, the conclusion must be so likewise: but it is certain, that when the conclusion

fion is false, one of the premises, or both, absolutely must be false; for if they were true, it would be impossible that the conclusion should be false, I have still some farther reslections to submit to you, on this subject, which is the foundation of the certainty of all the knowledge we acquire.

24th February, 1761.

### LETTER CVI.

Different Figures and Modes of Syllogisms.

THE reflections which I have still to make on the subject of syllogism, may be reduced to the following articles:

I. A fyllogism contains only three notions, named terms, in as far as they are represented by words. For though a fyllogism contains three propositions, and each proposition two notions, or terms; it must be considered, that each term is twice employed in it, as in the following example:

EVERY A is B:

But EVERY A is C:

Therefore SOME C is B.

The three notions are marked by the letters A. B. C. which are the three terms of this fyllogism: of which, the term A enters into the first and second proposition; the term B into the first and third proposition; and the term C into the second and third proposition.

II. You must carefully distinguish these three terms of every syllogism. Two of them, namely, B and C, enter into the conclusion, the one of which, C, is the subject, and the other, B, the attribute, or predicate. In logick, the subject of the conclusion, C, is called the minor term, and the predicate of the conclusion, B, the major term. But the third notion, or the term A, is found in both premises, and it is combined with both the other terms, in the conclusion. This term, A, is called the mean or medium term. Thus, in the following example.

NO MISER IS VIRTUOUS:

But some learned men are misers:

Therefore some Learned Men are not virtuous.

The notion learned is the minor term, that of virtuous is the major, and the notion of mifer, is the mean term.

III. As to the order of the propositions, it is a matter of indifference, whether of the premises is in the first or second place, provided the conclusion holds the last, it being the consequence from the premises. Logicians have, however, thought proper to lay down this rule:

The first proposition is always that which contains the predicate of the conclusion, or the major term; for this is the reason that we give to this proposition the name of the major proposition.

The second proposition contains the minor term, or the subject of the conclusion, and hence it has the name of the minor proposition.

Thus, the major proposition of a fyllogism contains the

the mean term, with the major term, or predicate of the conclusion; and the minor proposition contains the mean term, with the minor term, or subject, of the conclusion.

IV. Syllogisms are distinguished under different figures, according as the mean term occupies the place of subject, or attribute, in the premises.

Logicians have established four figures of fyllogisms, which are thus defined:

The first figure is that in which the mean term is the subject, in the major proposition, and the predicate, in the minor.

The fecond figure, that in which the mean term is the predicate, in both the major proposition, and the minor.

The third figure, that in which the mean term is the fubject, in both the major and minor propofitions. Finally,

The fourth figure, is that in which the mean term is the predicate, in the major proposition, and the subject, in the minor.

Let P be the minor term, or subject of the conclusion: Q the major term, or predicate, of the conclusion, and M the mean term; the four sigures of syllogism will be represented in the manner following:

# Figure First.

Major Proposition	M		-	Q
Minor Proposition	P	-	-	M
Conclusion	P	1912	91 27	Q

Major Proposition   Q - M Minor Proposition   P - M Conclusion   P - Q
Minor Proposition P - M
Conclusion   P Q
and the same of the same
Figure Third.
Major Proposition   M Q
Minor Proposition   M - P
Conclusion   P Q
re clares bands and man dalla
Figure Fourth.
Major Proposition   Q — M
Minor Proposition   M - P
Conclusion P — Q

V. Again, according as the propositions themselves are universal, or particular, affirmative, or negative, each figure contains several forms, called *Modes*. In order, the more clearly, to represent these modes of each figure, we mark by the letter A, universal affirmative propositions; by the letter E, universal negative propositions; by the letter I, particular affirmative propositions: and, finally, by the letter O, particular negative propositions: or else,

A represents an universal affirmative proposition. E represents an universal negative proposition. I represents a particular affirmative proposition. O represents a particular negative proposition.

VI. Hence, our nineteen forms of fyllogism, above described, are reducible to the four sigures, which I have just laid down, as in the following tables;

I. Modes

## I. Modes of the First Figure.

ift Mode.

A. A. A.

Every M is Q;

But Every P is M:

Therefore Every P is Q.

2d Mode.

A. I. I.

Every M is Q;

But Some P is M:

Therefore Some P is Q.

3d Mode.

E. A. E.

No M is Q;

But Every P is M: Therefore no P is Q. 4th Mode.

E. I. O.

No M is Q;

But Some P is M:

Therefore Some P is not Q.

## II. Modes of the Second Figure.

ist Mode.

A. E. E.

Every Q is M;

But No P is M:

Therefore No P is Q.

2d Mode.

A. O. O.

A. U. U.

Every Q is M; But Some P is not M:

Therefore Some P is not Q.

3 Mode.

E. A. E.

No Q is M;

But Every P is M:

Therefore No P is Q.

4th Mode.

E. I. O.

No Q is M;

But Some P is M:

Therefore Some P is not Q.

# III. Modes of the Third Figure.

A. A. I.  Every M is Q;  But Every M is P:  Therefore Some P is Q.	I. A. I. Some M is Q; But Every M is P: Therefore Some P is Q.
3d Mode.  A. I. I.  Every M is Q;  But Some M is P:  Therefore Some P is Q.	4th Mode. E. A. O. No M is Q; But Every M is P: Therefore Some P is not Q.
5th Mode. E. I. O. No M is Q; But Some M is P: Therefore Some P is not Q.	6th Mode. O. A. O. Some M is not Q; But Every M is P: Therefore Some P is not Q.

## IV. Modes of the Fourth Figure.

ıft Mode.	2d Mode.
A. A. I.	I. A. I.
Every Q is M;	Some Q is M;
But Every M is P:	But every M is P:
Therefore Some P is Q.	Therefore Some P is Q.
3d Mode.	4th Mode.
A. E. E.	E. A. O.
Every Q is M;	No Q is M;
But No M is P:	But Every M is P:
Therefore No P is Q.	Therefore Some P is not Q.

5th Mode.
E. I. O.
No Q is M:
But Some M is P:
Therefore Some P is not Q.

You see, then, that the first sigure has four modes; the second four; the third six; the fourth sive; so that the whole of these modes, together, is nineteen, being precisely the same forms which I have above explained, and have just now disposed in the four sigures. In other respects, the justness of each of these modes has been already demonstrated, by the spaces which I employed, to mark the notions. The only difference consists in this, that here I make use of the letters, P, Q, M, instead of A, B, C.

28th February, 1761.

### LETTER CVII.

Observations and Reflections, on the different Modes of Syllogism.

FLATTER myfelf, that the following reflections will contribute, not a little, to place the nature of fyllogisms in a clearer light. You must pay particular attention to the species of the propositions which compose the fyllogisms, of each of our four sigures, that is to say, whether they are,

- 1. Univerfal affirmative, the fign of which is A; or
- 2. Universal negative, the fign of which is E; or
- 3. Particular affirmative, the fign of which is I; or, finally,
- 4. Particular negative, the fign of which is O; and you will readily admit the justness of the following reflections:

Vol. I. Ee I. In

I. In no one inflance are both premifes negative propositions. Logicians have hence formed this rule:

From two negative propositions, no conclusion can be drawn.

The reason is evident, for laying down P and Q, as the terms of the conclusion, and M as the mean term, if both premises are negative, the affirmation is, that the notions P and Q, are either wholly, or in part, out of M: it is, accordingly, impossible to conclude any thing, respecting the conformity, or disconformity, of the notions P and Q. Though I knew from history, that the Gauls were not Romans, and that neither were the Celtæ Romans, this would not contribute in the least to inform me whether the Celtæ were Gauls or not. Two negative premises, therefore, lead to no conclusion.

II. Both premises are, in no one instance, particular propositions; hence this rule is logic:

From two particular propositions, no conclusion can be drawn.

Thus, for example, because some learned men are poor, and some others malevolent, it is impossible to conclude, that those who are poor are malevolent, or that they are not so. If you reflect ever so little on the nature of a consequence, you must immediately perceive, that two particular premises lead to no conclusion whatever.

III. If either of the premises is negative, the conclusion too must be negative.

This is the third rule which logic prefcribes. When fomething

fomething is denied in the premifes, it is impossible to affirm any thing in the conclusion; we must absolutely deny there likewise. This rule is perfectly confirmed by all the laws of fyllogism, whose justice has been above demonstrated.

IV. If one of the premises is particular, the conclusion too must be particular.

This is the fourth rule prescribed in logic. The character of particular propositions being the word fome, if we speak only of some in one of the premises, it is impossible to speak generally, in the conclusion; it must be restricted to some. This rule, likewise, is consirmed by all the laws of syllogism, whose justness is indubitable.

V. When both premises are affirmative, the conclusion is so likewise. But though both premises may be universal, the conclusion is not always universal, sometimes it is particular only, as in the first mode of figures third and fourth.

VI. Beside universal and particular propositions, we, sometimes, make use of singular propositions, the subject of which is an individual; as when I say:

## Virgil was a great Poet.

The name of *Virgil* is not a general notion, containing feveral beings in itself: it is the proper name of a real individual, who lived a great many years ago. This proposition is called *fingular*; and when it is introduced into a fyllogism, it is of importance to determine, whether we are to consider it as holding the rank of an universal, or particular, proposition.

E e 2 VII. Certain

VII. Certain authors infift, that a fingular propofition must be ranked in the class of particulars; it being considered, that a particular proposition speaks only of some beings comprehended in the notion, whereas an universal proposition speaks of all. Now, say these authors, when we speak of only a singular being, this is still less than when we speak of some: and, consequently, a singular proposition must be considered as very particular.

VIII. However well founded this reasoning may appear, it cannot be admitted. The essence of a particular proposition consists in this, that it does not speak of all the beings, comprehended in the notion of the subject, whereas an universal proposition speaks of all, without exception. Thus, when it is faid:

# Some citizens of Berlin are rich,

the fubject of this proposition is the notion of all the citizens of Berlin; but this subject is not taken in all it's extent, it's signification is expressly restricted to some: and, by this, particular propositions are essentially distinguished from universal, as they turn only on a part of the beings comprehended in their subject.

IX. It is clearly evident, from this remark, that a fingular proposition must be considered as universal; as, in speaking of an individual, say Virgil, it, in no respect, restricts the notion of the subject, which is Virgil himself, but rather admits it in all it's extent: and, for this reason, the same rules which take place in universal propositions apply, likewise, to singular propositions.

fitions. The following is, accordingly, a very good fyllogifm:

> VOLTAIRE IS A PHILOSOPHER; But VOLTAIRE IS A POET :

Therefore SOME POETS ARE PHILOSOPHERS. And it would be faulty, if the two premifes were particular propositions, but being considered as univerfal, this fyllogism belongs to figure third, and the first mode of the form A. A. I. The individual idea of Voltaire is the mean term, which is the fubject of both major and minor; and this is the character

of figure third.

X. Finally, I must remark, that hitherto I have fpoken only of fimple propositions, which contain only two notions, the one of which is affirmed or denied, univerfally, or particularly. With respect to compound propositions, logic prescribes peculiar rules.

3d March, 1761.

### LETTER CVIII.

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Hypothetical Propositions, and Syllogisms constructed of them.

TATE have, hitherto, confidered fimple propofitions only, or fuch as contain but two notions, the one of which is the fubject, the other the predicate. These propositions can form no other fyllogifms, except those which I have laid before you, and which are contained in the four figures above explained. But we, likewife, frequently employ Ee 3

compound

compound propositions, which contain more than two notions, and respecting which other rules are to be observed, in order to deduce fair conclusions from them.

Of these compound propositions, the most common are those which are called *bypothetical*, or *conditional*, which contain two complete propositions, with an affirmation, that, if the one is true, the other is so likewise: the following is an example of a conditional proposition:

If the Gazette fpeaks truth, peace is not very diffant.

Here are two propositions, the first, the Gazette speaks truth, or, the Gazette is true: and the other, peace is not very distant, or peace is approaching.

Now, these two propositions must be connected together in such a manner, that if the sirst is true, the second is so likewise; or, it is maintained, that the second proposition is a necessary consequence of the sirst, so that the former cannot be true, without establishing the truth of the other also. Supposing, then, that the Gazettes announce the approach of peace, we are warranted in saying, that, if the Gazettes are true, peace must be at hand.

Without this condition, fuch a proposition leads to nothing: but if this condition is complied with, then with the addition of some other proposition, there are two ways of drawing a conclusion from it:

1st, When some person assures us, that the Gazette speaks truth; for, hence we conclude, that peace is near: 2d, When we are told, that peace is still very distant;

distant; then we make no hesitation in thence concluding, that the Gazette does not speak truth.

You see that these two conclusions are general, and give two forms of hypothetical, or conditional, syllogisms, which may be thus represented:

First Form.

If A is B, C will be D;

But A is B:

Therefore C is D.

Second Form.

If A is B, C will be D;

But C IS NOT D:

Therefore A IS NOT B.

These two are the only just conclusions; and you must be carefully on your guard against the fallacy of the two following forms:

First erroneous Form.

If A is B, C will be D;

But A IS NOT B:

Therefore C IS NOT D.

Second erroneous Form.

If A is B, C will be D;

But C is D:

Therefore A is B.

These are both fallacious. In the example adduced, I should reason inconclusively, if I argued in this manner:

If THE GAZETTE SPEAKS TRUTH, PEACE IS APPROACHING;

But the GAZETTE DOES NOT SPEAK TRUTH: Therefore PEACE IS NOT APPROACHING.

It is, undoubtedly, true, that the Gazette may not fpeak truth; nevertheless, it is very possible that peace may be approaching.

The other form is equally erroneous;

If THE GAZETTE IS TRUE, PEACE AP-

But PEACE APPROACHES:

Therefore THE GAZETTE IS TRUE.

Let us suppose, that this consolatory truth, peace approaches, were revealed to us, so as to be put beyond the possibility of doubt, it would by no means sollow that Gazettes are true, or that they never contain untruths. I hope, at least, that peace is at hand, though I am very far from putting considence in the truth of Gazettes.

These two last forms of syllogisms, therefore, are fallacious; but the two preceding are certainly good, and never lead into error, provided that the first conditional proposition is true, or that the last part be a necessary consequence of the first.

Of this conditional proposition:

If A is B, C will be D.

The first part, A is B, is called the antecedent, and the other, C will be D, the consequent. Logic prescribes the two following rules to direct us in this style of reasoning:

I. Whoever admits the antecedent, must likewise admit the consequent.

II. Whoever denies, or rejects, the confequent, must likewise deny, or reject, the antecedent.

But you may very well deny the antecedent with-

out denying the confequent, and likewife admit the confequent without admitting the antecedent.

There are still other compound propositions, of which also fyllogisms may be formed. It will, perhaps, be fufficient to produce a fingle example. Having this proposition:

Every fubstance is body or spirit: the conclusion will run in the following manner:

I. But Such a fubstance is not body; Therefore It is spirit.

II. But Such a fubftance is body; Therefore It is not spirit.

But it is entirely unnecessary to detain you longer on this fubject.

7th March, 1761.

#### LETTER CIX.

Of the Impression of Sensations on the Soul.

JAVING endeavoured to unfold the principles of logic, whose object it is to lay down infallible rules for right reasoning, I must still detain you a little longer on the subject of ideas.

We, undoubtedly, derive them, in the first instance, from real objects, which strike our fenses; and as far as they are struck with any object, a sensation corresponding is thereby excited in the foul. Not only do the fenses represent to the soul the idea of that object, but they give it full affurance of it's

existence-

existence, out of us; and it is of importance to remark, that the fensation is not indifferent to the soul, but always accompanied with some pleasure, or disgust, to a greater or less degree.

Now, having once acquired, through this medium, the idea of any object, the foul loses it not when the object ceases to act on our senses; it is only the sensation, by which the soul is agreeably, or disagreeably affected, that is lost; but it still preserves the idea of the object itself. Not that the idea is ever present to it, or that it continually cherishes such idea in thought; but it possesses the power of awakening, or recalling, the idea, at pleasure.

This faculty of the foul, by which it is enabled to recollect ideas once perceived, is called reminiscence, which contains the source of memory. Deprived of the power of recalling past ideas, that of perceiving would answer little or no purpose; if we lost, every moment, the recollection of ideas once perceived, we should always be in the state of new-born infants, that is, in a state of the most profound ignorance. Reminiscence, then, is the most precious gift which the Creator has bestowed on the soul of man, and here it's spirituality shines in the brightest lustre; for, by means of this faculty, the soul gradually rises to the attainment of knowledge the most sublime.

But though recollected ideas represent to us the same objects which perceived ideas do, they differ from them, however, in this, that they are not accompanied with the sensation, nor with the conviction, that the objects really exist. If you have once

been spectator of a conflagration, you can recall the idea of it whenever you will, without imagining, however, that there really is one. It is even possible, that for a very long time, you may not have thought of such a conflagration, but without having lost the power of recalling the idea of it.

It is the fame with respect to all the ideas which we have once perceived; but it frequently happens, that we lose, almost entirely, the recollection, or, in other words, forget them. We remark, nevertheless, a very great difference between ideas forgotten, and ideas wholly unknown, or such as we never had. With respect to the first, as soon as the same object presents itself afresh to our senses, we much more easily catch the idea of it, and we recollect perfectly, that it is the same which we had forgotten: this would not be the case had we never possessed it.

It is here the materialists boast of having found a demonstration of their opinions. They conclude from it, that it is extremely clear, the soul is nothing else but a subtile matter, on which external objects are capable of making some slight impression, by means of the senses: that this impression is nothing else but the idea of the objects; and that as long as it remains, the recollection is preserved; but that we forget it, when the impression is totally essaced.

If this reasoning were solid, ideas must necessarily remain always present with us, till we forgot them; this, however, is not the case; for we recall them when we please; and if the impression were estaced, how could matter recollect, that it formerly had that impression,

impression, or receiving it asresh? And, though it be very certain, that the action of objects, on the senses, produces some change in the brain; this change is very different from the idea which is occasioned by it; and the sentiment of pleasure, or disgust, as well as the judgment respecting the object itself, which caused this impression, equally require a being wholly different from matter, and endowed with qualities of quite a different nature.

Our advances in knowledge are not limited to ideas perceived: the fame ideas, recollected in the memory, form for us, by abstraction, general ideas of them, which contain, at once, a great number of individual ideas; and how many abstract ideas do we form, respecting the qualities and accidents of objects, which have no relation to any thing corporeal, such as the notions of virtue, of wisdom, &c.?

This, after all, refers only to the understanding, which comprehends but a part of the faculties of the foul; the other part is not less extensive, namely, the will and liberty, on which depend all our resolutions and actions. There is nothing in the body relative to this quality, by which the soul freely determines itself to certain actions, even after mature deliberation. It pays regard to motives, without being forced to submit to their influence; and liberty is so essential to it, as well as to all spirits, that it would be as impossible to imagine a spirit without liberty, as a body without extension. God himself could not divest a spirit of this essential property.

It is by this, accordingly, that we are enabled to

folve all the perplexing questions respecting the origin of evil, the permission of sin, and the existence of all the calamities by which the world is oppressed; their great and only source is human liberty.

10th March, 1761.

# LETTER CX.

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Of the Origin and Permission of Evil; and of Sin.

THE origin and permission of evil in the world, is an article which has, in all ages, greatly perplexed theologians and philosophers. To believe that God, a Being fupremely good, fhould have created this world, and to fee it overwhelmed with fuch variety of evil, appears fo contradictory, that fome found themselves reduced to the necessity of admitting two principles, the one fupremely good, the other fupremely evil. This was the opinion entertaided by the ancient heretics, known in history by the name of Manicheans; who, feeing no other way of accounting for the origin of evil, were reduced to this extremity. Though the question be extremely complicated, this fingle remark, that liberty is a quality effential to fpirits, difpels, at once, a great part of the difficulties, which would otherwife be infurmountable.

In truth, when God had created man, it was too late to prevent fin, his liberty being susceptible of no constraint. But, I shall be told, it would have been

been better not to create fuch and fuch men, or fpirits, who, as God must have foreseen, would abuse their liberty, and plunge into fin. I should deem it rather rash to enter upon this discussion, and to pretend to judge of the choice which God might have been able to make, in creating spirits; and, perhaps, the plan of the universe required the existence of spirits of every possible description. And, in fact, when we reflect, that not only our earth, but all the planets, are the habitations of rational beings; and that even all the fixed stars are funs, each of which may have around it a fystem of planets, likewise habitable, it is clear, that the number of all the beings endowed with reason, which have existed, which do exist, and which shall exist, in the whole universe, must be infinite.

It is, therefore, unpardonable prefumption to infinuate, that God ought not to have granted existence to a great number of spirits; and the very perfons, who thus reproach their Maker, would certainly not wish to be of the number of those to whom existence was denied. This sirst objection, then, is sufficiently done away; and it is no way inconsistent with the Divine perfections, that existence has been bestowed on all spirits, good and bad.

It is next alleged, that the mischievousness of spirits, or reasonable beings, ought to have been repressed by the divine Omnipotence. On this I remark, that liberty is so essential to all spirits, as to be beyond all power of constraint; the only method of governing spirits consists in the use of motives, to dispose

them

them to what is good, and to diffuade them from evil; but, in this respect, we find not the slightest ground of complaint. The most powerful motives have, undoubtedly, been proposed to all spirits, to incline them to good, these motives being sounded on their own salvation; but they by no means employ constraint, for this would be contrary to their nature, and in all respects impossible.

However wicked men may be, it never can be in their power to excuse themselves, from ignorance of the motives which would have prompted them to good: the divine law, which constantly aims at their everlasting happiness, is engraven on their heart, and it must always be their own fault if they plunge into evil. Religion discovers to us, likewise, so many other means which God employs to reclaim us from our wanderings, that, on this side, we may rest considently assured, that God has omitted nothing which could have prevented the malignant explosions of men, and of other reasonable beings.

But those who bewilder themselves in such doubts respecting the origin and the permission of evil in the world, perpetually confound the corporeal with the spiritual world; they imagine that spirits are, as bodies, susceptible of constraint. Severe discipline is, frequently, capable of preventing, among the children of a family, the soldiers of an army, or the inhabitants of a city, the open eruption of perverse dispositions; but it must be carefully remarked, that this constraint extends only to what is corporeal; it, in no respect, restrains the spirit from being as vicious,

vicious, and as malignant, as if it enjoyed the most unbounded licence.

Human governments must rest contented with this exterior, or apparent tranquillity, and give themfelves little trouble about the real dispositions of men's minds; but, before God, the thoughts all lie open, and perverse inclinations, however concealed from men, are as abominable in his sight, as if they had broke out into the most atrocious actions. Men suffer themselves to be dazzled by salse appearances; but God has respect to the real dispositions of every spirit, according as they are virtuous, or vicious, independently of the actions which slow from them.

The Holy Scriptures contain, to this purpose, the most pointed declarations, and inform us, that he who meditates only the destruction of his neighbour, suffering himself to be hurried away by a spirit of hatred, is as criminal in the sight of God, as the actual murderer; and that he who indulges a covetous desire of another's property is, in his estimation, as much a thief as he who really steals.

In this respect, therefore, the government of God over spirits, or rational beings, is infinitely different from that which men exercise over men like themselves; and we greatly err, if we imagine that a government, which appears the best in the eyes of men, is really so in the judgment of God. This is a respection of which we ought never to lose sight.

14th March, 1761.

### LETTER CXI.

# Of moral and physical Evil.

WHEN complaint is made of the evil which prevails in the world, a distribution of them into two classes takes place: moral evils and physical evils. The class of moral evils contains the perverse or vicious inclinations, the dispositions of spirits to what is evil or criminal, which is undoubtedly the most grievous calamity and the greatest impersection which can exist.

In truth, with regard to spirits, it is impossible to conceive a more deplorable irregularity, than when they deviate from the eternal laws of virtue, and abandon themselves to the commission of vice. Virtue is the only means of rendering a spirit happy; to bestow felicity on a vicious spirit is beyond the power of God himself. Every spirit addicted to vice is necessarily miserable, and, unless it return to virtue, it's misery cannot come to an end: such is the idea I form of demons, of wicked and infernal spirits; an idea which, to me, appears consonant to what Scripture suggests on the subject.

Infidels make a jest of this; but as men cannot pretend to be the best of all rational beings, neither can they boast of being the most wicked; there are, undoubtedly, beings much more deprayed than the most malignant of mankind, such as devils. But I have already made it appear, that the existence of so Vol. I.

many corrupted men and spirits, ought not to form any objection against the perfection of this world, much less be considered as an imputation of the Supreme Being.

A spirit, the devil not excepted, is always a being, excellent, and infinitely fuperior to every thing that can be conceived in the corporeal world; and this world, as far as it contains an infinite number of fpirits, of all orders, is always a work of the highest perfection. Now, all fpirits being effentially free, criminality was possible from the commencement of their existence, and could not be prevented even by the divine Omnipotence. Besides, spirits are the authors of the evils which necessarily result from sin, every free agent being always the only author of the evil which he commits; and, confequently, thefe evils cannot be imputed to the Creator; as among men, the workman who makes the fword is not refponsible for the mischief that is done with it. Thus, with respect to the moral evils which prevail in the world, the fovereign goodness of God is sufficiently justified.

The other class, that of physical evils, contains all the calamities and miseries to which men are exposed in this world. It is admitted, that most of these are a necessary consequence of the malice, and other vicious propensities with which men, as well as other spirits, are infected; but as these consequences are communicated by means of bodies, it is asked, Why God should permit to wicked spirits, the power of acting so efficaciously on bodies, and of employing them

them as inftruments to execute their pernicious purposes? A father, who saw his son on the point of
committing a murder, would fnatch the sword out
of his hand, and prevent the perpetration of a crime
so heinous. I have already observed, that this abandoned son is equally guilty before God, whether he
has actually accomplished his design, or only made
inessectual efforts to execute it, and the father, who
prevented him, does not thereby render him better.

We may, nevertheless, confidently maintain, that God does not permit a free course to the wickedness of man. Did nothing refift the execution of all the pernicious purpofes of the human heart, how miferable should we be! We frequently see, that the wicked have great difficulties to encounter, and though they fhould fucceed, they have no power over the confequences of their actions, which always depend on fo many other circumstances, that, in the issue, they produce the directly opposite effect from what was intended. It cannot be denied, at the fame time, that there may refult from these, calami. ties and miferies to torment mankind; and it is imagined, that the world would be infinitely better governed, were God to interpose an effectual restraint to the wickedness and audacity of men.

It would, undoubtedly, be very easy for God to crush to death a tyrant, before he could realize his cruel and oppressive designs, or to strike dumb an unjust judge, who was going to pronounce an iniquitous sentence. We might then live quietly, and enjoy all the comforts of life, supposing God were

M.L.L.

to grant us the bleffings of health, and all the good things we could wish for: our happiness would thus be perfect. On this plan they would have the world governed, in order to render us all happy: the wicked disabled to perpetrate their criminal purposes, and the good in possession of the peaceful enjoyment of all the bleffings which they can defire.

It is believed, and with good reason, that God wishes the happiness of men, and it is matter of surprize, that this world should be so different from the plan which is imagined the most proper for the attainment of this end. We rather see the wicked frequently enjoying, not only all the advantages of this life, but put in a condition to execute their machinations, to the confusion and distress of persons of worth, while the good are oppressed and overwhelmed by the most sensible evils, pains, diseases, mortifications, loss of goods, and, in general, by every species of calamity; and that, at last, the good as well as the bad, must infallibly die, which appears to be the greatest of all evils.

Looking on the world in this point of view, one is tempted to call in question the supreme wisdom and goodness of the Creator; but it is a hazard which we must take great care to shun.

17th March, 1761.

### LETTER CXII.

Reply to Complaints of the Existence of physical Evil.

SUPPOSING our existence limited to the present life, the possession of the good things of this world, and the enjoyment of every delight, would be very far from filling up the measure of our happiness. All are agreed, that true felicity consists in mental tranquillity and satisfaction, which are feldom, if ever, accompanied with that brilliancy of condition, which is considered as such an inestimable blessing, by those who judge only from appearances.

The infufficiency of temporal good things to render us happy, becomes still more manifest, when we come to reslect on our real destination. Death does not put a period to our existence, it rather transmits us into another life, which is to endure for ever. The faculties of our soul, and our attainments in knowledge, will then, no doubt, be carried to the highest perfection; and it is on this new state that our real happiness depends, and this state cannot be happy without virtue.

The infinite perfections of the Supreme Being, which we now perceive only as through a thick cloud, shall then shine in the brightest lustre, and shall become the principal object of our contemplation, admiration, adoration. There, not only shall our understanding find the most inexhaustible stores of pure and perfect knowledge, but we shall be perfect when the perfect was a supreme being.

mitted to hope for admission into favour with the Supreme Being, and to aspire after the most endearing expressions of his love. How happy do we reckon the peculiar favourites of a great prince, especially if he is really great, though the favours which he bestows are marred by many infusions of bitterness? What will it then be, in the life to come, when God himself shall shed abroad his love in our hearts, a love the essects of which shall never be interrupted nor destroyed! This shall, thenceforward, constitute a felicity infinitely surpassing all that we can conceive.

In order to a participation of these inexpressible favours, slowing from the love of the Supreme Being, it is natural that, on our part, we should be penetrated with sentiments of the most lively affection to him. This blessed union absolutely requires, in us, a certain disposition, without which we should be incapable of participating in it; and this disposition consists in virtue, the basis of which is the love of God, and that of our neighbour. The attainment of virtue, then, should be our chief, our only object in this life, where we exist but for this end, to prepare for, and to render ourselves worthy of partaking in supreme and eternal felicity.

In this point of view, we must form a judgment of the events which befall us in this life. It is not the possession of the good things of this world that renders us happy; it is rather, a situation which most effectually conducts to virtue. If prosperity were the certain means of rendering us happy, we might be suffered to complain of adversity; but ad-

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versity may rather have the effect of confirming our virtue, and, in this view, all the complaints of men, respecting the physical evils of life, are, likewise, completely done away.

You have no difficulty, then, in comprehending, that God had the most solid reasons for admitting into the world so many calamities and miseries, as the whole obviously contributes to our salvation. It is unquestionably true, that these calamities are, for the most part, natural consequences of human corruption; but it is in this very thing, that we must principally admire the wisdom of the Supreme Being, who knows how to over-rule the most vicious actions, for our final happiness.

Many good people would not have reached fuch a fublimity of virtue, had they not been oppressed, and tormented, by cruelty and injustice.

I have already remarked, that bad actions are fuch, only with regard to those who commit them: the determination of their soul alone is criminal, the action itself being a thing purely corporeal, in as much as, considered independently of the person who commits it, there is nothing, either good or evil, in the case. A mason falling from the roof of a house upon a man, as certainly kills him as the most determined assassin. The action is absolutely the same; but the mason is not guilty in the slightest degree; whereas the assassing deserves the severest punishment. Thus, however criminal actions may be, with regard to those who commit them, we must consider them in quite a different light as they

affect ourselves, or produce an influence on our situa-

We ought, therefore, to reflect, that nothing can befall us, but what is perfectly confonant to the fovereign wisdom of God. The wicked may be guilty of injustice towards us, but we cannot upon the whole suffer from it; no one can ever injure us, though he may greatly hurt himself; and in every thing that comes to pass, we ought always to acknowledge God, as if it befell us immediately by his express appointment. We may, moreover, rest assured, that it is not from caprice, or merely to vex us, that God disposes the events in which we are concerned, but that they must infallibly terminate in our true happiness. Those who consider all events in this light, will soon have the satisfaction of being convinced, that God exercises a peculiar care over them.

21/t March, 1761.

# LETTER CXIII.

The real Destination of Man; Usefulness and Necessity of Adversity.

I HOPE you have no doubts remaining, with refpect to this great question: How the evils of this world can be reconciled to the supreme wisdom and goodness of the Creator? The solution of it is incontestably founded on the real destination of man,

and of other intelligent beings, whose existence is not limited to this life. The moment that we lose fight of this important truth, we find ourselves involved in the greatest perplexity, and if man were created only for this life, it would affuredly be impossible to establish a consistency between the perfections of God and the distresses and miseries with which this world is oppressed. Those miseries would be but too real; and it were absolutely impossible to explain, How the prosperity of the wicked, and the misery of so many good people, could consist with the divine justice.

But no fooner do we reflect that this life is but the commencement of our existence, and that it is ferving as a preparation for one that shall endure eternally, the face of things is entirely changed, and we are obliged to form a very different judgment of the evils with which this life appears to be overfpread. I have already remarked, that the profperity which we enjoy in this world is the reverse of a fuitable preparation for a future life, and for rendering us worthy of the felicity which there awaits us. However important to our happiness the possession of the good things of this world may appear, this quality pertains to them only in fo far as they are impressed with the signatures of divine goodness, independent of which no earthly possessions could constitute our felicity.

Real happiness is to be found only in God himfelf; all other delights are but an empty shade, and are capable of yielding only a momentary satisfaction. tion. Accordingly we fee that those who enjoy them in the greatest abundance, are quickly satisfied; and this apparent selicity serves only to inslame their desires, and to disorder their passions, by estranging them from the Supreme Good, instead of bringing them nearer to Him. But true selicity consists in a perfect union with God, which cannot subsist without a love and a considence in his goodness, transcending all things: and this love requires a certain disposition of soul, for which we must be making preparation in this life.

This disposition is virtue, the foundation of which is contained in these two great precepts:

Thou shalt love the Lord thy God with all thy heart; with all thy soul, with all thy strength, and with all thy mind;

and the other, which is like unto it:

Thou shalt love thy neighbour as thyself.

Every other disposition of soul which deviates from these two precepts, is vicious, and absolutely unworthy to partake of true happiness. It is as impossible for a vicious man to enjoy happiness in the life to come, as for a deaf man to relish the pleasure of an exquisite piece of music. He must be for ever excluded from it, not by an arbitrary decree of God, but by the very nature of the thing; a vicious man not being, from his own nature, susceptible of supreme felicity.

If we consider the order and economy of the world, in this point of view, nothing can be more perfectly disposed for the attainment, of this great

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end. All events, the calamities themselves which we undergo, are the most suitable means for conducting us to true happiness: and in this respect, it may be with truth affirmed, that this is, indeed, the best world possible, as every thing in it concurs to promote our eternal salvation. When I reslect, that nothing befalls me by chance; but that every event is directed by Providence, in the view of rendering me truly and everlastingly happy, how ought this consideration to raise my thoughts to God, and to replenish my soul with the purest affection!

But, however efficacious these means may be in themselves, they exercise no force upon our minds, to which liberty is so essential, that no degree of constraint can possibly take place. Experience, accordingly, frequently demonstrates that our attachment to the objects of sense renders us too vicious to listen to these salutary admonitions. Abuse of the means which would have improved our virtue, plunges us deeper and deeper into vice, and hurries us aside from the only path that leads to happiness.

24th March, 1761.

### LETTER CXIV.

Of true Happiness. Conversion of Sinners. Reply to Objections on the Subject.

HE holy life of the apostles, and of the other primitive Christians, appears to me an irresistible proof of the truth of the Christian Religion. If true happiness consists in union with the Supreme Being, which it is impossible for a moment to doubt, the enjoyment of this happiness necessarily requires, on our part, a certain disposition, founded on fupreme love to God, and the most perfect charity toward our neighbour, fo that all those who are deftitute of this disposition, destroy their own pretenfions to celeftial felicity; and wicked men are, from their very nature, necessarily excluded from it, it being impossible for God himself to render them happy. For the Divine Omnipotence extends only to things which are in their nature possible, and liberty is fo effential to spirits, that no degree of constraint can take place with respect to them.

It is only by motives, therefore, that spirits can be determined to that which is good: now what motives could be proposed to the apostles and other disciples of Jesus Christ, to embrace a virtuous life, more powerful than the inftructions of their divine Mafter, his miracles, his fufferings, his death and refurrection, of which they were witnesses. All these striking events, united to a doctrine the most fublime, must have excited, in their hearts, the most fervent love and the most profound veneration for God, whom they could not but consider and adore as at once their heavenly Father, and the absolute Lord of the whole universe. These lively impressions must necessarily have stifled in their breasts every vicious propensity, and have consistent them, more and more, in the practice of virtue.

This falutary effect on the minds of the apostles, has nothing in it, of itself, miraculous, or which encroaches, in the smallest degree, on their liberty, though the events be supernatural. The great requisite was, simply, a heart docide and uncorrupted by vice and passion. The mission, then, of Jesus Christ into the world, produced, in the minds of the apostles, this disposition, so necessary to the attainment and the enjoyment of supreme happiness; and that mission still supplies the same motives to pursue the same end. We have only to read attentively, and without prejudice, the history of it, and seriously to meditate on all the events.

I confine myself to the salutary effects of our Saviour's mission, without presuming to dive into the mysteries of the work of our redemption, which infinitely transcend the powers of human understanding. I only remark, that these effects, of the truth of which we are convinced by experience, could not be produced by illusion, or human imposture; they are too salutary not to be divine. They are likewise perfectly in harmony with the incontestable principles which

which we have laid down, that spirits can be governed only by motives.

Theologians have maintained, and fome still maintain, that conversion is the immediate operation of God, without any co-operation on the part of man. They imagine that an act of the Divine will is fufficient to transform, in an inftant, the greatest miscreant into a virtuous man. These good gentlemen may mean extremely well, and confider themselves as thus exalting the divine Omnipotence; but this fentiment feems to me inconfiftent with the justice and goodness of God, even though it were not subversive of human liberty. How, it will with reason be faid, if a fimple exertion of the divine Omnipotence is fufficient for the inflantaneous conversion of every finner, can it be possible that the decree should not actually pass, rather than leave so many thoufands to perish, or employ the work of redemption, by which a part only of mankind is faved? I acknowledge that this objection appears to me much more formidable than all those which infidelity raises against our holy religion, and which are founded entirely in ignorance of the true destination of man; but, bleffed be God, it can have no place in the fyftem which I have taken the liberty to propofe.

Some divines will perhaps accuse me of herefy, as if I were maintaining that the power of man is sufficient for his conversion; but this reproach affects me not, as I am conscious of intending to place the goodness of God in it's clearest light. In the work

of conversion, man makes perfect use of his liberty, which is unsusceptible of constraint, but man is always determined by motives. Now, these motives are suggested by the circumstances and conjunctures of his condition. They depend entirely on divine Providence, which regulates all events, conformably to the laws of sovereign wisdom. It is God, therefore, who places men every instant in circumstances the most favourable, and from which they may derive motives the most powerful, to produce their conversion; so that men are always indebted to God for the means which promote their salvation.

I have already remarked, that however wicked the actions of men may be, they have no power over their confequences, and that God, when he created the world, arranged the course of all events, so that every man should be every instant placed in circumstances to him the most salutary. Happy the man who has wisdom to turn them to good account!

This conviction must operate in us the happiest effects: unbounded love to God, with a firm reliance on his providence, and the purest charity toward our neighbour. This idea of the Supreme Being, as exalted as it is consolatory, ought to replenish our hearts with virtue the most sublime, and effectually prepare us for the enjoyment of life eternal.

28th March, 1761.

### LETTER CXV.

The true Foundation of human Knowledge. Sources of Truth, and Classes of Information derived from it.

AVING taken the liberty to lay before you my opinion respecting the most important article of human knowledge, I flatter myself it will be sufficient to dislipate the doubts which naturally arise out of the subject, from want of exact ideas of the liberty of spirits.

I shall now have the honour of submitting to your consideration the true foundation of all our knowledge, and the means we have of being assured of the truth and certainty of what we know. We are very far from being always certain of the truth of all our sentiments; for we are but too frequently dazzled by appearances, sometimes exceedingly slight, and whose salfehood we afterwards discover. As we are, therefore, continually in danger of deceiving ourselves, a reasonable man is bound to use every effort to avoid error, though he may not always be so happy as to succeed.

The thing to be here chiefly confidered is the folidity of the proofs on which we found our perfuafion of any truth whatever, and it is abfolutely neceffary that we should be in a condition to judge if they are sufficient to convince us or not. For this effect I remark, first, that all truths within our reach are referable to three classes, essentially distinguished from each other.

The first contains the truths of the senses; the second, those of the understanding; and the third, those of belief. Each of these classes requires peculiar proofs of the truths included in it, and in these three classes all human knowledge is comprehended.

Proofs of the first class are reducible to the senses, and are thus expressed:

This is true, for I faw it, or am convinced of it by the evidence of my senses.

It is thus I know that the magnet attracts iron, because I see it, and experience furnishes me with incontestable proofs of the fact. Truths of this class are called *sensible*, because they are founded on the senses, or on experience.

Proofs of the fecond class are founded in ratiocination; thus:

This is true, for I am able to demonstrate it on principles of just reasoning, or by fair syllogisms.

To this class, principally, logic is to be referred, which prescribes rules for reasoning consequentially. It is thus, we know, that the three angles of a rectilineal triangle are together equal to two right angles. In this case I do not say I see it, or that my senses convince me of it; but I am assured of it's truth by a process of reasoning. Truths of this class are called intellectual, and here we must rank all the truths of geometry, and of the other sciences, in as much as they are supported by demonstration. You must be sensible, that such truths are wholly different from Vol. I.

those of the first class, in support of which we adduce no other proofs but the senses, or experience, which assure us that the fact is so, though we may not know the cause of it. In the example of the magnet, we do not know how the attraction of iron is a nececessary effect of the nature of the magnet, and of iron; but we are not the less convinced of the truth of the fact. Truths of the first class are as certain as those of the second, though the proofs which we have of them are entirely different.

I proceed to the third class of truths, that of faith, which we believe, because persons worthy of credit relate them; or when we say:

This is true, for several creditable persons have assured us of it.

This class, accordingly, includes all bistorical truths. You believe, no doubt, that there was formerly a king of Macedon, called Alexander the Great, who made himself master of the kingdom of Persia, though you never saw him, and are unable to demonstrate, geometrically, that such a person ever existed. But we believe it on the authority of the authors, who have written his history, and we entertain no doubt of their sidelity. But may it not be possible that these authors have concerted to deceive us? We have every reason to reject such an infinuation, and we are as much convinced of the truth of these facts, at least of a great part of them, as of truths of the sirst and second classes.

The proofs of these three classes of truths are extremely different; but if they are folid, each in it's kind,

kind, they must equally produce conviction. You cannot possibly doubt that Russians and Austrians have been at Berlin, though you did not see them: this, then, is to you a truth of the third class, as you believe it on the report of others; but to me it is one of the first class, because I saw them, and conversed with them, and as many others were assured of their presence by means of other senses. You have, nevertheless, as complete conviction of the fact as we have.

31 A March, 1761.

END OF THE FIRST VOLUME.

T. Gillet, Printer, Salifbury-square.

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