

**The elements of clock and watch-work, adapted to practice. In two essays
/ By Alexander Cumming.**

Contributors

Cumming, Alexander, 1733-1814.

Publication/Creation

London : printed for the author, 1766.

Persistent URL

<https://wellcomecollection.org/works/xequs2xu>

License and attribution

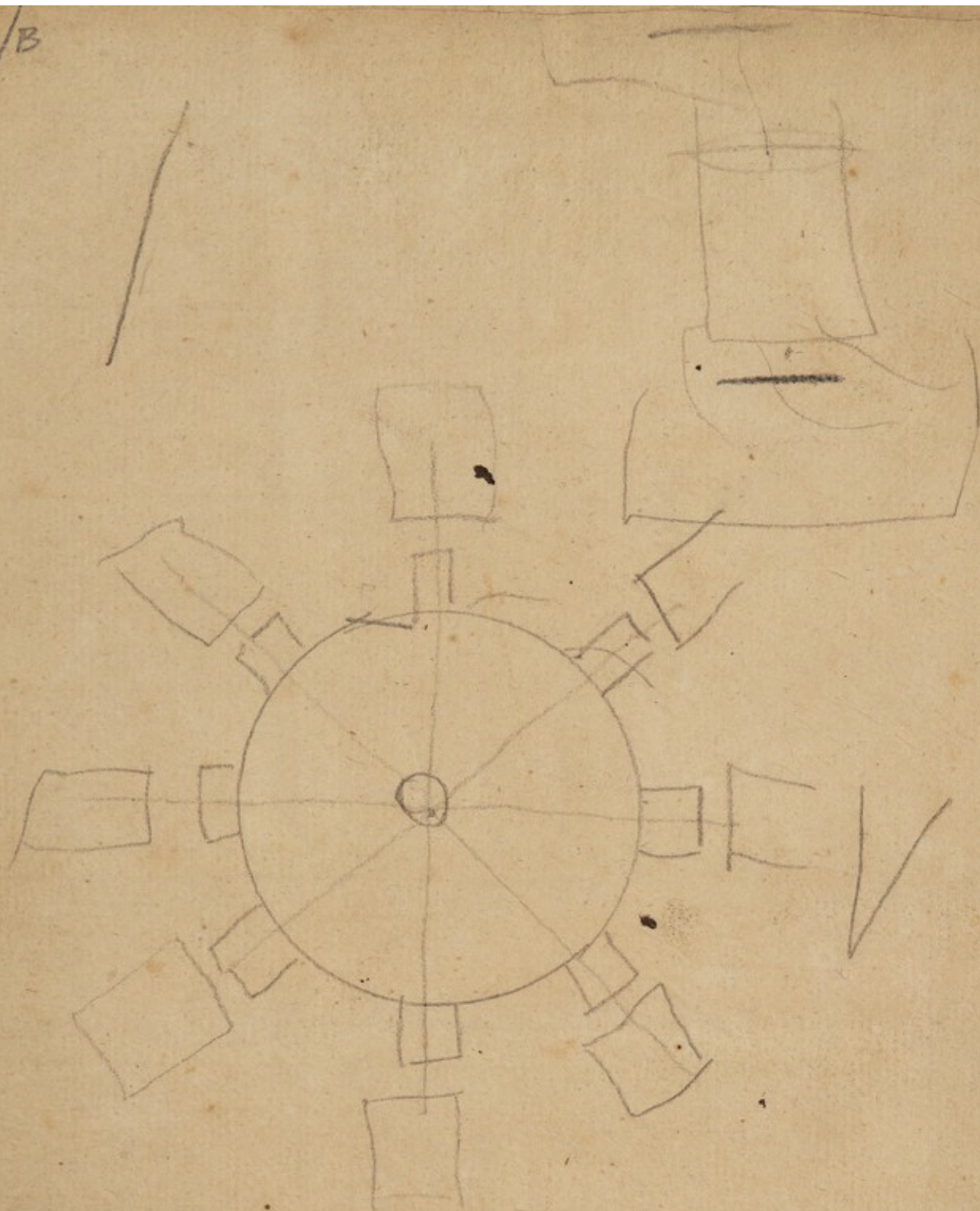
This work has been identified as being free of known restrictions under copyright law, including all related and neighbouring rights and is being made available under the Creative Commons, Public Domain Mark.

You can copy, modify, distribute and perform the work, even for commercial purposes, without asking permission.



Wellcome Collection
183 Euston Road
London NW1 2BE UK
T +44 (0)20 7611 8722
E library@wellcomecollection.org
<https://wellcomecollection.org>

410/B



8378

THE *Robt Joyce*
ELEMENTS
OF
CLOCK and WATCH-WORK,

Adapted to PRACTICE.

IN TWO ESSAYS.

By ALEXANDER CUMMING,
Member of the Phil. Soc. Edinb.

LONDON: Printed for the AUTHOR;

And sold by him, and the following Booksellers;

A. MILLAR, and D. WILSON, in the Strand; J. DODSLEY, Pall-mall;
S. BAKER, York-street, Covent-garden; Messrs. RICHARDSON and
URQUHART, at the Royal Exchange; Messrs. FLETCHER and
ANDERSON, St. Paul's Church-yard; T. PAYNE, at the Meuse
Gate; J. ROBSON, New Bond-street: And by A. KINCAID,
G. HAMILTON, and J. BALFOUR, in Edinburgh.

MDCCCLXVI.



T O T H E
K I N G.

S I R,

YOUR MAJESTY's approbation of my former endeavours for improvement in the art which I profess, induced me to compose these Essays ; and as Your bounty has afforded me the leisure to pursue my researches, nothing could give me greater happiness, than the permission of thus laying them at Your MAJESTY's feet.

IT is almost the peculiar glory of Your MAJESTY's reign, that the peace which

A 2 the

DEDICATION.

the success of Your MAJESTY's arms prescribed to Europe, and the wisdom of Your councils planned for Your people, is adorned by Your MAJESTY's MUNIFICENT PATRONAGE of all the Arts, useful as well as ornamental. The subject of the following pages partakes of both : and their author humbly hopes that they tend to public utility ; the only return which Your MAJESTY requires, and the only retribution he can make for Your Royal bounty.

HE begs leave to assure Your MAJESTY, that he shall ever be impressed with the deepest sense of Your MAJESTY's exalted virtues, as well as with the deepest gratitude for the favours Your MAJESTY has been most graciously pleased to extend to him, and that they shall be employed in his hourly endeavours to deserve them.

WITH

D E D I C A T I O N.

WITH the most profound veneration,
he presumes to subscribe himself,

May it please Your MAJESTY,

Your MAJESTY's Most Faithful,

Dutiful, and Devoted

Subject and Servant,

LONDON,
Feb. 26th, 1766.

ALEXANDER CUMMING.

DECEMBER

With the most profound veneration

to the memory of the late

James A. Smith

Your Most Obedient Servant

Samuel H. Smith

Subject and Return

AMERICAN GLEANINGS

T O T H E
R E A D E R.

TH E very favourable opinion which the Author of the following Essays entertains, and (notwithstanding all malicious reports to the contrary) always has entertained, of the great natural abilities of Mr. JOHN HARRISON, induced him to delay this publication, till Mr. HARRISON had received the reward of his long and unwearied application, by discovering the result of his labours. That discovery being now made, the public from thence will judge of the merits of his improvements; and possibly from a comparison between them and the following Theory, the Reader may be enabled to decide, how far the calumny, so groundlessly conceived, and so artfully propagated against me, was well founded. Should any further vindication be necessary, I am ready, if called on by my accusers, publicly to declare the reasons for such part of my former conduct, as has so much displeased them, and obviate any objections to the following performance, if fairly and candidly urged: but no regard will be paid to any anonymous opponent, in a controversy that has truth alone for its object.

TO THE

R E A D E R.

THE very favourable opinion which the Author of the following Essays entertains, and (notwithstanding all malicious reports to the contrary) always has entertained, of the great natural abilities of Mr. John Harrison, induced him to draw out this Dissertation, till Mr. Harrison had received the result of his long and unwearied application, by discovering the result of his labour. That discovery being now made, the public from hence will judge of the merit of his improvements; and possibly form a comparison between them and the following Theory, the Reader may be enabled to decide. How far the former is groundlessly conceived, and so artfully propagated against me, was well founded. Should any further vindication be necessary, I am ready, if called on by my accusers, publicly to declare the reasons for every part of my former conduct, as has been already intimated; and to waive any objections to the following performance, if fairly and candidly urged; but no regard will be paid to any anonymous objections, or a contro-
versy that has nothing to do with the subject.

E R R A T A.

Parag.	Line.	
1.	4.	<i>for construed, read constructed</i>
47.	2.	<i>after are, insert in theory</i>
68.	2.	<i>for only is the motive force, read alone is the moving power</i>
70.	4.	<i>for motive force, read moving power</i>
98.	2.	<i>after fixed point, insert within the ball</i>
152.	6.	<i>for that will corroborate, read to corroborate</i>
203.	1.	<i>for planes, read plane</i>
226.	—	<i>The last part of the first note of this paragraph is wrong expressed; but as the first part comprehends the whole meaning, the Reader may draw his pen through that part which follows, i. e.</i>
271.	8.	<i>for being, read been</i>
296.	2.	<i>for Pl. 7. read Pl. 5.</i>
311.	13.	<i>for pivots, read points</i>
334.	11.	<i>for upwards, read downward</i>
	12.	<i>for downward, read upwards</i>
343.	9.	<i>for rod, read rods</i>
		<i>Page 98. line 5. from the bottom; for dilation, read dilatation</i>
365.	11.	<i>for easily, read easie</i>
380.	5.	<i>for therefore, read but</i>
399.	13.	<i>for vibration, read vibrations</i>
424.	1. & 2.	<i>for is as its thickness, read increases with its thickness</i>
440.	5.	<i>for in the proportion, read in proportion</i>
479.	10.	<i>after the word expect, insert that</i>
526.	—	<i>In the first line of the note, for pl. 16. read pl. 15.</i>
532.	—	<i>From the beginning; read If the train be continued the same, the number of leaves in the third-wheel pinion may be increased, in the same proportion as the number of teeth in the horizontal wheel, &c.</i>
546.	4.	<i>for any how lessened, read sensibly lessened</i>
		<i>In the conclusion, page 192. line 5. for practical theory, read a practical theory.</i>

Whereas some persons seem either to misunderstand the author's meaning, or are disposed to dispute about words; it is proper here to mention, that

By MOMENTUM, is meant, *the effective power*, or force which a body exerts before its whole motion is destroyed;

By MOVING POWER, that force which causes motion, whether it takes effect in whole or in part;

And by the FORCE IMPRESSED is meant, such part of the *moving power* as really takes effect.

Thus if a wheel be moved by a stream of water, the whole stream is the *moving power*: but the force which it *impresses* depends as much on the velocity of the wheel, as on the velocity or force of the stream; for if the wheel moves with a velocity equal to that of the stream, the latter can *impress no force* on the former, nor add to its velocity.

By MOTIVE FORCE, is meant, the quantity of motion generated by the *impressed force*.

And in this sense the author apprehends these words have always been understood.

AN
ESSAY

TOWARDS THE
Improvement of CLOCK-WORK.

GENERAL PLAN.

1. *I* *T*is universally allowed, that the most ordinary Clock with a royal Pendulum, measures Time better than any Watch, construed in the manner hitherto practised. And,

2. *T*hat Watches are, in general, as well executed as Clocks. From which it is evident,

3. *T*hat Clocks derive their superiority from principle: and that a due attention to their natural properties, may at least, be the means of improving Watch-work.

Clocks go better than Watches.

Watches as well executed as Clocks.

Clocks derive their superiority from principle.

B

4. The

Clock-work into
two general Heads.

4. The Theory of Clock-work naturally divides itself into the two following general Heads, viz.

First.

5. *What pendulous Vibrations have their Isochronism least influenced by equal causes?* And,

Second.

6. *What construction of a Clock will least alter the Isochronism of the same Pendulum?*

CLASSES.

7. All Clocks may be reduced to two Classes; namely, ORDINARY and ACCURATE.

In ordinary Clocks
particular regard
to expence and
simplicity.

8. In ORDINARY Clocks, such as are generally used for domestic purposes, particular regard should be had to their simplicity and expence.

In the more accu-
rate, no expence
should be spared.

9. In Clocks that are intended for astronomical and other *very accurate* Observations, no expences should be spared, while the performance can be further improved. *I shall therefore enquire,*

First enquiry.

10. In the first place, *How far the performance of Clocks may be improved, without much increasing their expence.*

Second.

11. And in the second, *What is the utmost degree of perfection, of which they seem susceptible.*

Pendulum only
has a natural ten-
dency to measure
the Time.

12. Since a Pendulum is the only part of a Clock that has a natural tendency to measure Time, I shall here mention its known properties in its *simple state*, detached from Clocks, and describing circular Arc's.

Its natural Proper-
ties in a detached
state.

13. First, *A Pendulum once put in motion, would ever continue to vibrate equal Arc's, if no external cause did tend to destroy its motion.* And,

14. Second, *All those equal Vibrations would be performed in equal times.* OF PENDULOUS
VIBRATIONS.

15. Third, *The momentum of Pendulums is as the versed sine of their angle of Vibration into their quantity of matter.*

16. Fourth, *Pendulums of equal length, though unequal weight, will (cæteris paribus) perform their Vibrations in equal times.*

17. Fifth, *All Pendulums alter their time of Vibration in different latitudes. And their times of ascent and descent are equally influenced.*

18. Sixth, *A Pendulum cannot rest but when its centre of gravity is directly below its point of suspension.*

19. Seventh, *The shorter Vibrations in circular Arc's are performed in less time than the longer*.*

20. The foregoing properties are chiefly demonstrated by Mr. HUGENS in his HOROLOGIIUM OSCILLATORIUM, and translated into English in KEIL's Introduction to Natural Philosophy, and a strict attention to them seems absolutely necessary to the improvement of Clock-work. Demonstrated
chiefly by Mr.
Hugens.

21. If a pendulous body be made to vibrate in a resisting medium, (as air,) each Vibration Motion lost.

* Mr. HUGENS has demonstrated, that 29 semicircular Vibrations take as much time as 34 of the shortest Vibrations of the same Pendulum, independent of the influence of the Air.

Of PENDULOUS
VIBRATIONS.

How they may be
rendered isochro-
nal.

Enquiry.

Whether long or
short ones are most
influenced.

Princ. Math. Prop.
28. Coroll. 2.

will, by means of such resistance, become shorter than the preceding one, till at last the Pendulum comes to rest; hence (19) those Vibrations *will not* be performed in equal times.

22. But if the resistances of the medium, &c. were *uniformly the same*, and a power could be applied that would communicate to the Pendulum at each Vibration as much motion as those resistances destroy; then would all the Vibrations be *of equal length*, and performed in *equal times*.

23. But as neither the resistances that tend to destroy the motion, or the power that maintains the Vibrations of Clock-Pendulums, are perfectly uniform; I proceed to enquire

24. *Whether long or short Vibrations have their Isochronism least influenced by those irregularities.*

25. Sir ISAAC NEWTON has demonstrated;
“ That a *Funipendulous Body* “ vibrating in a
“ resisting medium, would have its short Vi-
“ brations more isochronal than its longer;”
That is, *in other words*; that the longer Vibrations being more resisted than the shorter ones, do sooner alter their lengths, and consequently (19) their times of Vibrations. But

26. Let a power be any how applied that will communicate as much motion to the Pendulum as the resistances of the medium, &c.
do

do destroy; then will the Vibrations continue equal and isochronal.

Of PENDULOUS
VIBRATIONS.

27. Thus, we are not to consider *the total resistances of the air, friction, &c.* since a power can be easily applied that will ballance them, so long as they continue uniform. *And this power, from whatever cause; I call the MAINTAINING POWER.*

Total resistance
of the Air not to be
regarded.

28. But we are to enquire, what influence *any Change*, in the resistance, or in the maintaining power, would have on Pendulums of equal weight, but describing unequal Arc's.

29. Let any power be applied to the pendulous body B, capable of moving it from its place of rest, to M or G; join M G, and draw O N parallel to the line M G, and let M O, the *perpendicular height* to which it is raised, be divided into any number of equal parts, suppose five; through the extremity of each part, draw a straight line parallel to M G, till they meet the Arc in the points L, K, I, H, and if the power that raises the body B to M, be also divided into five equal parts, one of those parts will raise B to H; two parts will raise it to I; three parts will move it to K; four parts to L, &c.

PLATE I.
FIG. I.

Comparative advantage of long
and short Arc's.

30. Here it is to be observed, that though the power be applied by equal portions, the spaces described are unequal; but agree in *perpendicular height* with the power applied.

Equal powers give
unequal spaces,
but agree in
height.

31. Let

OF PENDULOUS
VIBRATIONS.

PLATE I.
FIG. I.

Construction of
the Figure.

Increase in height
as the power, and
decrease as the re-
sistance.

Illustration.

Experiment.

31. Let the Arc BG, be divided into five equal parts by the points C, D, E and F, through which points draw straight lines parallel to MG, till they meet AB and GN; then will the line GN represent the power necessary to raise the body B, to the point G; *and its parts*; the powers necessary to raise it, to *their* corresponding points in the Arc*.

32. Now since the increase of perpendicular height is as the increase of power applied (30), it follows that the decrease in perpendicular height, will be as the increase of resistance; or as the diminution of power: *Therefore,*

33. Let there be any number of Clocks, *suppose five*, whose Pendulums are *exactly equal*, but whose angles of Vibration are to each other, as 1, 2, 3, 4 and 5; or let the bodies C, D, E, F and G, represent their relative Pendulums at the extremity of their Vibrations.

34. If those five Clocks be exposed to the same degree of cold, their oil will be equally influenced, and by that means, *their maintaining powers equally diminished*: And consequently, there will happen an equal diminution in the

* It is evident, GN is divided into a scale of versed sines; therefore if gravity alone opposed the ascent of the Pendulum, the powers necessary to raise it to any of the positions, C, D, E, F, G, would be as the relative versed Sine of those Arc's; as would also the momentum of the Pendulum in descending from any of those points.

perpen-

perpendicular height of the Vibrations of each Pendulum (32). Of PENDULOUS
VIBRATIONS.

35. Let those Clocks continue exposed to the cold, till some one of them is deprived of all its motion; it is required, Which Pendulum will first come to rest? *and in what degree the others are influenced?*

36. Since all the Pendulums are equal (33), it is obvious that the one which described the shortest Arc, will soonest come to rest (15). Shortest Vibration
soonest comes to
rest.

37. But the Pendulum C has (36) lost all its motion, and consequently its perpendicular ascent: *Therefore, (32, 34,) deduce from the height of the other Pendulums D, E, F and G, each, a space equal to the greatest height of C; as represented on the scale G N; through those points, draw lines parallel to G M till they meet the Arc B G, on which, they will show the diminution in the length of Vibration in each Pendulum; as represented in the figure, by dotted lines. Or*

38. Deduce the versed sine of the angle described by the Pendulum C, from each of the versed sines of the angles described by the Pendulums D, E, F, and G, at beginning of all their Vibrations; and the remainders will be the versed Sines of each respective Vibration, when the Pendulum C has lost all its motion.

39. From which it plainly appears, *That in Clock Pendulums, equal causes do most alter the lengths of the shortest Vibrations.* 40. It

OF PENDULOUS
VIBRATIONS.

PLATE I.
FIG. I.

Comparative ad-
vantages in dupli-
cate proportion of
the Arc's.

PLATE I.
FIG. 2.

Another illustra-
tion.

Construction of
the Fig.

Demonstration.

40. It is further to be observed, that although the same causes did shorten the Arcs of Vibration of *all* those Pendulums *equally*, the effect it would have on their times, would be, as the change produced in each Vibration, to *the whole length of Vibration* (14).

41. But equal causes produce less alteration in the length of long Vibrations, than it does in short ones (39). Therefore (40), *the comparative advantages of different Vibrations in Clock Pendulums are* (cæt. par.) *in the duplicate proportion of their relative length.* Which may otherwise be illustrated; thus,

42. Let any body E, vibrate in the circular Arc A C E, I say that the advantages of its longer Vibrations are to that of its shorter ones, in the *duplicate proportion* of the length of those Arc's.

43. For, join A E, and from C, the lowest point of the Arc, draw a line perpendicular to A E; which perpendicular divide into four equal parts, and through their extremities draw straight lines parallel to A E, till they are terminated by the Arc; join E C, and parallel to it, draw a line touching the Arc in D; then E D will be equal to D C, and consequently E C will be double of D C. *Now*

44. Let two equal bodies E and D describe the Arc's E C, and D C; it is evident (32), that four times as much resistance will be required

quired to bring E to rest, as will destroy the motion of D; in the same manner is proved, that four times as much resistance is necessary to destroy the motion from D to C, as from h to C.

OF PENDULOUS
VIBRATIONS.

45. What is above said of whole Arc's, is equally true of their proportional parts; for, if the whole resistance, necessary to destroy the motion of any body, describing a circular Arc, be divided into sixteen equal parts, it will require twelve of those parts to reduce the Vibration to half the length; three more parts will reduce it to a fourth of the whole length; and if the remaining Sixteenth of the momentum be again divided as above, the same proportion will hold, till the Arc entirely vanishes.

Equally true of
the proportional
parts as the whole.

46. Therefore (by the 12th Prop. Book Fifth Euc.) the resistance necessary to produce proportional effects in the Isochronism of Vibrations of different lengths (41), will be to each other *c p*, as the resistance that destroys their whole motion, i. e. (32) as their relative versed sines:

The resistances
that produce pro-
portional altera-
tions, are as those
that destroy the
whole motion.

And therefore,

47. In Clocks, *the advantages of long Vibrations, are universally in the duplicate ratio of the Arc's described.*

Conclusion in fa-
vour of long Vi-
brations.

48. But lest it should be objected, that the power necessary to maintain Vibrations of different lengths, will be in the duplicate ratio of their respective Arc's; and that the friction on
C the

OF PENDULOUS
VIBRATIONS.

the movement will increase as the power; and consequently, that the power necessary to maintain the motion in Clocks, will bear a greater proportion to the momentum of the Pendulum, in long Vibrations than in short ones; *it is necessary to observe; that,*

49. Though the whole friction increases as the weight, or power applied to a Clock, it does not follow, that the changes, or accidental variations in it observe the same law (27).

Further considera-
tion.

50. The *natural* friction* continues uniformly the same while the pressure on the rubbing surfaces is uniform; and if any certain quantity of the maintaining power be constantly destroyed by friction, it can no way affect the Isochronism of the Pendulum; for what could be more absurd than allowing for the influence of any power, *where it never reaches.*

51. Since any increase in the maintaining power, will have the same effect on the Pendulum as a diminution in the resistance of the Air; and *vice versa* (32); It follows that,

What has been
said of resistance
is applicable to
the maintaining
power.

52. What has been said concerning the resistance of the medium, &c. is equally applicable to the changes of the maintaining power (32, 41, 47).

* I do not here mean to assert, that there are not exceptions to what is said of the uniformity of natural friction; but as such exceptions do not invalidate what is here said, they are reserved for another place.

53. I formerly observed, (27, 28,) that the *changes only* that happen in the resistance of the medium, &c. to Clock Pendulums, are to be regarded; the same is true concerning the action of the Wheels on the Pendulum (50).

OF PENDULOUS
VIBRATIONS.

Changes only in the maintaining power to be regarded.

54. As to the irregularity of action in Wheel-work; their fluctuations are constant and *periodical*, and in the action of each Tooth, correct themselves; so that, if the effect does not become perceptible during the action of any one Tooth of a Wheel, it will not, in any number of revolutions; for the error does not accumulate.

Action of the
Wheels.

55. The changes that happen in the maintaining power from the different states of fluidity in the oil, are of a contrary nature; for the times of their duration, and returns, and consequently the errors arising therefrom, are *uncertain*, as depending upon external causes; and they accumulate, as shall be shewn hereafter.

Fluidity of the oil,
&c.

As to the Time of going without winding.

56. It is only to be regarded so far as it tends to render the machine more or less complicated; for, *in Clocks*, we have power at command, and may have any degree of influence at pleasure on

Does not matter
so much in Clocks
as in Watches.

TIME OF GOING.

Theory.

the pallets, without regard to the continuation of the Clock's going : *Thus,*

57. *In theory*, if a weight of two pounds be necessary to maintain a Vibration of any given length, *suppose one degree*, for eight days ; a weight of eight pounds will maintain the same for thirty-two days (one month) ; and a weight of one hundred and four pounds will maintain it for a year ; supposing the perpendicular descent of the weight the same in each case.

58. Now let us enquire which of those three cases is most advantageous for practice.

Friction greatest
in those Clocks
that go longest.

59. By supposition (57) the influence, or action of the Wheels on the pallets, is equal in each case ; the Vibrations are equal (57) also ; therefore the friction on the pallets, as also on all the correspondent parts of each Clock, will be equal ; but the month Clock has one Wheel, and the year Clock two Wheels, more than the week Clock ; and each Wheel has its friction ; consequently the friction is greater in the month Clock than in the weekly one, and still greater in the annual Clock than either : *But*

Not hurtful to the
performance if it
remains uniform.

60. If the friction remains uniform, an additional power may be applied that will render the action on the pallets equal in each Clock ; in which case, the Pendulums (*cæteris paribus*) would vibrate in equal times ; nor would their Isochronism be any how influenced by the above *uniform* difference in friction (50).

61. But

61. But the influences of heat and cold on the oil applied, will tend to vary the action of the Wheels on the pallets, and consequently the length of Vibration (52) and Isochronism of the Pendulum (19).

TIME OF GOING.

Influences of the Oil.

62. And, as this influence may reasonably be supposed equal, on the corresponding parts of those Clocks ; the additional Wheels must have their additional influence ; and the Isochronism of the Pendulum is more disturbed in an annual, than a monthly Clock ; and in it, than a weekly one (55).

Most hurtful in those Clocks that go longest.

63. It may possibly be said, that for the same reason, a 24 hour Clock should go better than an eight-day one ; but the inconveniences attending the use of the former might more than ballance its advantages.

Why 24 hour Clocks are not used.

64. If any should say, that Clocks in general either stand, or have a retrograde motion in time of winding, and that this error is least in Clocks of long continuation ; I answer, that every good mechanic knows how to remedy this imperfection : But this I pass, as foreign to my purpose.

Clocks stand in time of winding up.

65. *From the above considerations it appears, that for an accurate measure of time, eight-day Clocks are preferable to those of a longer continuation.*

Eight-day Clocks best.

Weight

Weight of the Pendulum.

Velocity as the
motive force.

66. Since the velocity generated is $c p$ as the motive force impressed: *it follows*,

Times inversely.

67. That the times of Vibration of a Pendulum will always be inversely as the motive force *.

In detached Pendulums, gravity only the motive force.

68. In Pendulums *detached from Clocks*, the action of gravity *only*, is the motive force: *Hence*,

All Pendulums of equal length, isochronal, &c.

69. The Vibrations of all Pendulums of *equal length*, and describing *equal Arc's*, are isochronal in the same latitude †.

Not so in Clocks.

70. But when a Pendulum is applied to a Clock, the *Impetus of the Wheels*, together with *the action of gravity*, constitute the motive force.

Alteration in the action of the Wheels, destroys the Isochronism.

71. *Hence*, any alteration in the action of the Wheels on the Pendulum, will alter the time of Vibration (67).

Proportion of such alteration in time.

72. And the alteration that will happen in the times of Vibration of a Clock, will always be to the whole time of its Vibrations, nearly as the

* The Vibrations are here supposed of the same length; or that all the parts that constitute the motive force, do act during the whole time thereof.

† For the action of gravity, and the *Vis Inertiae* will bear the same proportion to each other, whatever be the quantity of matter.

alteration

alteration in the motive force, to the whole motive force (66, 70).

WEIGHT OF THE
PENDULUM.

73. Thus, it is obvious, that (*cæt. par.*) the heavier the Pendulum, the less proportion will any alteration that may happen in the action of the wheels bear to its whole motive force (70), and consequently, the smaller the alteration in the times of its Vibration (72) *.

Heavy Pendulums
least influenced.

74. To illustrate this farther, let us suppose the action of the Wheels equal to the action of gravity on the Pendulum, and let this action of the Wheels be so applied, that it oppose the ascent and promote the descent in the very same manner that gravity does: then, will the times of Vibration be only half as long as they would, if gravity alone acted; for the velocity will be doubled (66), and the length of Vibration remain the same.

Illustration.

75. And if by any means the action of the Wheels on the Pendulum be diminished, suppose $\frac{1}{30}$ the motive force of the Pendulum will (70, 74,) be diminished $\frac{1}{60}$, which will also diminish the velocity in the same proportion.

Ditto.

76. But if the weight of the Pendulum be double the action of the Wheels, and their action as formerly, be diminished $\frac{1}{30}$, it will only

Ditto.

* Because the action of gravity on the Pendulum is unalterably the same, in the same place.

WEIGHT OF THE
PENDULUM.

make a difference of $\frac{1}{90}$ in the velocity; and consequently in the time (67).

Ditto.

77. Let the weight of the Pendulum be quadruple the action of the Wheels, then will an alteration of $\frac{1}{30}$ of the action of the Wheels make only an alteration of $\frac{1}{120}$ of the motive force (70); and consequently in the velocity and times.

Ditto.

78. Let the action of gravity be to the impetus of the Wheels on the Pendulum, as 100 to 1; then if the action of the Wheels as formerly be represented by 30, the *whole motive force* of the Pendulum will be 3030, and a diminution of $\frac{1}{30}$ in the action of the Wheels, will make an alteration of $\frac{1}{3030}$, in the motive force and velocity of the Pendulum: Hence a Clock would lose, one minute in 3030.

Application.

79. Thus it appears, that *the same cause* that produces an alteration of *one minute per hour*, with a Pendulum whose weight is equal to the action of the Wheels (74), * will only cause an alteration of a minute in an *hour and half*, when the weight of the Pendulum is double the action of the Wheels (76); *a minute in two hours and a half*, when the weight of the Pendulum is quadruple the action of the Wheels (77); and an alteration of one minute in 3030, (*two days*,

* That is, a Pendulum, on which the influences of the maintaining power and gravity, are equal: or in which each of them contribute equally to its motive force.

two hours, and 30 minutes), when the weight of the Pendulum is to the action of the Wheels, as 100 to 1 (78).

WEIGHT OF THE
PENDULUM.

80. Hence it is evident, that *the alteration in the measure of time*, is (cæt. par.) *to the whole time*, as *the alteration of the motive force of the Pendulum* (70) *to its whole motive force*.

Alteration in the
whole time: as, &c.

81. And therefore, the advantages of Pendulums, are (cæt. par.) as their weight *.

Advantage of Pen-
dulums, &c.

82. I have here considered the action of the Wheels, as opposing the whole ascent, as well as accelerating the descent: in which case, any alteration in it, (commencing at the extremity of Vibration) would have the same effect with an alteration in the power of gravity; that is, it would alter the velocity and times, without altering the Arc of Vibration.

83. But *in all Clocks*; the action of the Wheels, must promote the descent, more than it opposes the ascent of the Pendulums (or the contrary,) and consequently, the Arc of Vibration will be increased or diminished with the action of the Wheels: and the times of Vibration rendered more isochronal than above stated (79); but the relative proportions of the changes that will happen in the times, will nearly remain the

Why the Arc's
are increased and
diminished.

* Though I have here stated the advantage of heavy Pendulums as unlimited, I shall hereafter endeavour to shew, why the practice may not, beyond certain limits, agree with the theory.

same *. *I now proceed to compare, the MOMENTA OF PENDULUMS, differently acquired.*

84. I have in a former part of this Essay shewn, *that the advantages of long Vibrations, bear a duplicate proportion to their Arc's* (41, 47).

85. Therefore, if there be two Pendulums, of equal weight and describing equal Arc's, and it be required to increase the momentum in each equally; but in the one by weight, and in the other by increasing the Vibration, it may be done as follows:

Table of the momenta described.

86. Suppose each Pendulum six pound weight, and to vibrate one degree from its point of rest, then will their momentum and advantages be equal; but if their momenta be equally increased (85), as above, the weight of the one, and the angle of Vibration of the other, must be, *as in the following table*; where you have in the first column, the increase of momentum, and directly opposite to it, the weight of *the one Pendulum* in pounds, and the angle of Vibration of *the other*, in degrees and minutes.

* The height to which a Pendulum will rise, depends on its velocity at its lowest point; without any regard to the means by which such velocity was acquired: Hence, though the action of the Wheels on the pallets, accelerates the descent, it in some measure corrects such acceleration in circular Arc's, by enlarging the following Vibration (19). But this does not happen in cycloidal Arc's.

87. This

87. This table also gives the momentum of the same, or equal Pendulums, vibrating different angles. *Thus :*

88. Find the angles of Vibration in the last column, and opposite to them in the first, you have the momen-

Momen- tum.	Weight in lbs.	Angle of Vibration in deg. and min.
1	6	1
2	12	1 25
3	18	1 44
4	24	2
5	30	2 15
6	36	2 27
7	42	2 39
8	48	2 50
9	54	3
10	60	3 10
20	120	4 28
40	240	6 19
80	480	8 57
100	600	10 1

MOMENTUM OF
THE PENDULUM.

Further uses,

ta. *Ex.* If the one vibrates *one degree*, and the other *ten degrees*, their momenta will nearly be, as *one hundred to one* : If the one vibrates two degrees fifteen minutes, and the other eight degrees fifty-seven minutes, their relative momenta will be, as *five to eighty* ; and their advantages in correcting the irregularities of the movement, are as the relative momenta (47, and 81,) that is, directly as the weight, and in the duplicate ratio of the Arc.

Ditto.

89. *But to come closer to the purpose* ; let us suppose that there be given a Pendulum of eight pound weight, describing an Arc of *ten degrees from the lowest point* ; if it be required to make a Pendulum that shall have equal momentum with the former, and only vibrate *thirty minutes from its lowest point*, its weight in round numbers must be 3000 pounds ; a weight, that I am apt to think, the greatest admirer of short Vibrations would not, without apprehensions,

Example.

D 2 apply

SHORT
VIBRATIONS
EXAMINED.

Objection to long
Vibrations, and its
answer.

apply to a House-clock : but *there appears not the least risque or inconveniency in acquiring the same momentum, by enlarging the Vibration as above.*

90. It may be further urged in favour of short Vibrations, that the influence of the oil on the pivots of the verge, is diminished as the angle of Vibration. But is it possible to imagine ! that any person should think of this, without having first attempted to diminish the influence of the oil *on the pallets* ; where the effect is at least two hundred times as great ?

Further illustration
in the following
parts, &c.

91. Those who are not yet satisfied of the advantages of long Vibrations, may have further satisfaction, when the influences of the oil on the pallets and the resistance of the air are considered. *And*

Query.

92. As some may enquire, what could have induced so many learned, and ingenious men, *to prefer short Vibrations to long ?* I shall endeavour to point out such arguments, as appear of greatest weight in support of short Vibrations.

Argument first, in
favour of short
Vibrations.

93. *First*, Because short Arc's of a circle, deviate little from the cycloidal curve : *They are supposed to partake of the same properties.*

Argument second.

94. *Secondly*, Because short Vibrations are less liable to communicate motion to the point of suspension. *And*

Argument third.

95. *Thirdly*, Because they meet with less resistance from the air, *and consequently* are maintained by a smaller power ; they are thought preferable to long ones. *But*

But let us now enquire, whether these are real or imaginary advantages.

SHORT
VIBRATIONS
EXAMINED.

96. And first, of the *cycloidal properties*, they seemingly having introduced short Vibrations; I here confine my remarks to the established theory only, and pass all the imperfections of materials or execution.

Cycloidal properties.

97. Mr. HUGENS demonstrated, that a Pendulum, vibrating in the cycloidal curve, would perform all its Vibrations, whether long or short, in equal times*; and directly thought of applying this to Clock-pendulums, and pointed out a method, by which the center of oscillation of a Pendulum might be made to describe a cycloid.

By whom applied to Clocks.

98. *But here*, the center of oscillation was considered as *a fixed point*; which cannot be in a Pendulum vibrating between cycloidal cheeks; for the Pendulum alters its length in every part of the Vibration, and consequently the center of oscillation must be continually changing its place, and so describe a curve different from the cycloid; nor has any method been yet proposed for obviating this difficulty.

Center of oscillation, not a fixed point in cycloidal Vibrations.

99. But, *supposing this objection removed*, what is demonstrated of Pendulums describing a cycloid, is by no means true, after such Pendulum is applied to a Clock.

Other objections to cycloidal cheeks &c.

* But this demonstration does not include the influences of the medium.

OF SHORT VI-
BRATIONS.

Sir ISAAC NEW-
TON aware of this.

Argument in fa-
vour of cycloidal
Vibrations.

Supposition not
true.

Action of the
Wheels can never
coincide in every
respect with gra-
vity on the Pendu-
lum.

Reason.

100. Sir ISAAC NEWTON was well aware of Mr. HUGENS's oversight in both these articles; for, when HE shews how to make a Pendulum describe a cycloid, he supposes it a *point*. See his Prin. Math. Prop. 50.

101. And when HE demonstrates the cycloidal properties of a Pendulum, (Prop. 51.) he expressly says, "THAT GRAVITY ALONE, shall act on the Pendulum;" which tacitly suggests, that when the Wheels of a Clock act on the Pendulum, the cycloidal properties are destroyed.

102. But it may be said, that if the Wheels of a Clock are made to act on the Pendulum, *in the very same manner that gravity does*, the cycloidal properties may be preserved: but this supposes the action of the Wheels, as invariable as the action of gravity, which I imagine is not the case in any Clock, *that has yet been made*; and if any alteration happen in the action of the Wheels, thus applied; it will have *the same effect* on the measure of time, as *an alteration in the power of gravity*.

103. Nor is it possible to make the action of the Wheels, *in every respect*, to coincide and cooperate, with gravity; *for* gravity promotes the descent in every point, and in the same manner opposes the ascent; which can never happen in the action of the Wheels on the Pendulum; *for*,

104. Though *it* may promote the descent, in the very same manner that gravity does, it can never

never oppose the ascent, *as much*, and *in the same manner*; for in that case, it would counter-act itself, and *cease to maintain the Vibrations*: but of this more hereafter.

Of SHORT VI-
BRATIONS.

105. Let us for a few minutes divest ourselves of cycloidal prejudices, and found our enquiries on common sense, and the following considerations will naturally present themselves.

Enquiry.

106. Whenever cycloidal cheeks are applied, it is supposed that the longer Vibrations are slower than the shorter ones; but though this is the case in detached Pendulums, it is quite otherwise in those applied to Clocks with recoiling pallets. For,

Cycloidal Vibrations hurt the performance with recoiling pallets.

107. If we add, to the moving power of a Clock on the recoiling principle, its Vibrations will become longer, and at the same time quicker: this is a truth of which few, if any Clock-makers, are ignorant, and of which any person in possession of a Clock of the recoiling principle, may soon be convinced*.

An easy experiment on recoiling clocks.

108. How

* It may possibly be here said, that though this has been generally if not universally the case, yet a certain mode and quantity of recoil, may be established, that will give in practice, all the properties that the cycloid does in theory: but I am apt to think that such investigation, is much more difficult than that of the cycloid; and that the application of such theory to practice, must be more critical than even that of the cycloid. For, admitting that the mode and quantity of recoil is investigated, the application to practice, will be more difficult than the cycloidal cheeks, in proportion, as the face of the pallets is shorter

Further arguments
against cycloidal
Vibrations and a
recoil.

Effect with a dead-
beat postponed, &c.

IMPROVEMENT OF

108. How absurd then would it be, to render *those quickest Vibrations, yet quicker*, by the application of cycloidal cheeks?

109. *If thus, it appears*, that the application of the cycloid to Clocks, does even in *theory* increase the evil: What must they do? when we add, the *imperfections of execution*, the *elasticity of cycloidal cheeks*, together with *the many changes that happen therein* by heat and cold, and *the bad effects that may arise from the corrosion of the metals, &c. &c.* *

110. I cannot here investigate the effect of cycloidal cheeks with the dead-beat, without anticipating the theory of pallets, but shall hereafter endeavour to shew the impropriety of any application of them, since the effect of the density of the air, on the *motive force* of the Pendulum, does exactly balance the effects of its resistance in circular Arc's: so far as they influence the measure of time, as shall be shewn in its proper place. *But here*

shorter than such cheeks: and I shall shew hereafter, that in Clocks where the maintaining power is uniform, circular Vibrations are preferable to cycloidal ones; and the same objections stand in the way of any recoil of whatever kind.

* This chiefly alludes to such Clocks as have a recoil, which has been the case with most, to which cycloidal cheeks have been applied; and in all Mr. HUGENS's Clocks: but I shall shew in its proper place, that the cycloidal Vibrations are inferior to the circular, in a resisting medium whose density is changeable, whatever be the construction of pallets.

III. It

III. It seems no more than reasonable to conclude; *that short Vibrations derive no greater advantages from any affinity they may be supposed to have to the cycloid; than the cycloid possesses.*

Of SHORT VI-
BRATIONS.

III2. And though all that hath been demonstrated of the cycloid, had been as unexceptionable in *Clock-pendulums* as in *imaginary* ones; it would not follow; that short Arcs would have any more of the cycloidal properties, than straight lines have of the properties of short Arcs; and if such inaccuracies are admitted as mathematical reasoning, we need not be surprised to hear it asserted, that there is no difference between a cycloid and a semicircle; *we may deceive ourselves by such reasoning*, but cannot impose on nature; the smallest part of the *one*, for part of the *other*.

Impropriety of
supposing that
short Arcs, &c.

III3. As to the motion that may be communicated to the point of suspension (94), I have only here to observe, that it may be more advantageously prevented by rendering the point of suspension more immoveable, than by rendering the Vibration shorter; since by this means, we may preserve the one advantage; without losing the other. *Of this more hereafter.*

Suspension.

*As to the resistance * of the Air.*

Its changes only
to be considered.

114. I formerly have observed (27, 28), that we are only to consider the alterations that happen therein; and if in this respect short and long Vibrations are found on a level, *the latter* is to be preferred, for reasons already given (89, 47).

Shortens the time
of ascent, as
much, &c.

115. Since the *resistance of the air* shortens *the time of ascent* (17), as much as it prolongs *the time of descent* (17); let an ascent, and descent, be taken together; and any change in the resistance, can only affect their times, by rendering the Vibrations longer or shorter (19). *And therefore †,*

* By the resistance of the air, we are only to understand the effects of its *Vis inertiae*, by which the motion of bodies passing through it is destroyed: *such effects as arise from its different specific gravities, independent of its Vis inertiae*, shall be considered towards the end of this Essay.

† Sir ISAAC NEWTON takes notice in the 2d Corol. to Prop. 27. Prin. Math. V. 2. "That the time of descent of a funipendulous body, is somewhat more prolonged (by the resistance of the air) than the time of its ascent is contracted, *in proportion as the descent is longer than the subsequent ascent*;" which is not the case in Clock-pendulums, where the time of descent is contracted by the action on the pallets: and if the resistance arising from the *Vis inertiae* of the air, tends to render the Vibrations shorter, and quicker in circular Arcs (19) in proportion to its density; the specific gravity of the air independent of the *Vis inertiae*, tends to render them slower, in the same proportion. See 6 Corol. to Prop. 24. of his Principles; where he says: "That the comparative weight is the motive force of a body in any heavy medium: and therefore does the same thing in such a *non-resisting* medium, as the absolute weight does in a vacuum." But of this hereafter.

116. The

116. The isochronism will be least altered in those Vibrations, that undergo the least *proportional alteration* in their length (14), *from any change*, in the resistance of the air; or in the maintaining power.

RESISTANCE
OF THE AIR.

Its effects least in
those Vibrations,
&c.

117. The resistance that a Pendulum meets with from the air, bears a duplicate proportion to the length of the Vibration: and the resistance that gravity makes to the ascent of the Pendulum, is also in the same proportion. *Therefore,*

118. All that has been said *concerning the comparative advantages of long and short Vibrations* (from 29 to 48), is equally applicable to the uniform resistance of the air *.

Reference, &c.

119. And, though the *whole resistance* is much greater in long, than in short Vibrations; the *change* that any *alteration in the density of the air*, will make in the resistance; will bear *no less proportion to the whole resistance* in short Vibrations than in long: *And therefore*, (116, 118).

120. *If no other consideration than the uniform resistance of the air, did take place; THE*

Long Vibrations
preferable, &c.

* Here it is to be observed, that the uniform resistance of the air, tends to diminish the effect of any change in the maintaining power, in the duplicate proportion of the Arc of Vibration. See Plate 1. Fig. 1 and 2. where the resistance of the air as well as that of gravity may be represented by the perpendicular heights (117), (i. e. the versed sines,) so that the former must have a similar effect with the latter in preserving the Vibration of a more equal length, (41, 46, 47) and more isochronal (14).

RESISTANCE
OF THE AIR.

LONGER VIBRATIONS IN CLOCK-PENDULUMS *are much preferable to the shorter*; nor do the *alterations that happen in such resistance* render them inferior (119) *.

Sir ISAAC NEWTON's demonstration not applicable to Clock-pendulums.

121. Some admirers of short Vibrations, may urge what Sir ISAAC NEWTON has wrote in the 2d Cor. to the 27th Prop. V. 2. of his Principia; but I may venture to assert, that if their attention in reading, is equal to his judgment in writing, they will not apply any part of what he there says, to Clock-pendulums:

His words, &c.

122. His words are, " That the shorter oscillations are more isochronal, and very short ones are performed nearly in the same times, as in a *non-resisting medium* †."

Funipendulous bodies.

123. But let it be observed; that what HE has demonstrated, is expressly of *funipendulous bodies* ‡, to distinguish them, from such bodies as have a maintaining power, and are kept in *constant motion*.

* If a pendulum approaches near to a solid body, at the extremities of its Vibration, the repercussion of the air from such body may tend to accelerate the descent; and so contract both, the times of ascent and descent; on which account, Clock-pendulums should have so much room as never to approach very near to the case.

† By a non-resisting medium is here meant, a medium deprived of its *Vis inertiae*; and it is also implied that its density remains the same: otherwise the times of Vibration might be altered, even in a non-resisting medium.

‡ Bodies suspended by threads.

124. His

124. His *meaning therefore, may be expressed thus*; since the resistance of the air is in the duplicate proportion of the velocity, the longer Vibrations (where there is no maintaining power) must lose more motion than the shorter ones do: and when the Vibrations become very short, the resistance is so small, as to produce no sensible effect in the *length, or time, of many Vibrations.*

RESISTANCE
OF THE AIR.

His meaning
otherwise expressed.

125. *Any one who reads with due attention, his demonstrations concerning Pendulums, will clearly see that he did not intend they should be understood of such as were applied to Clocks; For,*

Did not intend
them to be applied
to Clocks.

126. When he gives the method of causing a Pendulum to oscillate in a cycloid (Prop. 50.) he supposes it, *a point*; and this supposition removes in his demonstrations, any inaccuracies that may be found in Mr. HUGENS's; who expressly says *Clock-pendulums are meant*; and that the center of oscillation is *a fixed point* within them. But of this more hereafter.

Reasons.

127. Moreover, when Sir ISAAC demonstrates the properties of Pendulums oscillating in a cycloid (Prop. 51.) he says, "*That gravity alone, acts on it*;" does not this even suggest, that the addition of any other power would destroy these properties?

128. If any further proof seemed necessary; that OUR INCOMPARABLE PHILOSOPHER did not mean, any of the demonstrations of *funipendulous bodies*, to be understood of *Clock-pendulums*; and

He was well
aware of, &c.

RESISTANCE
OF THE AIR.

and that he was well aware of the changes that the application of a Clock would cause in the motion of a Pendulum.

Prop. 27. Corol. 2.
Vol. 2.

Reasons.

129. *I might further observe* ; that in the above cited corollary (121) he says, " But the
" times of those (Vibrations) which are performed
" in *greater Arcs* are a little greater, because
" the resistance in the descent of the body, *by*
" *which the time is prolonged*, is greater, in *pro-*
" *portion to the length described in the descent*,
" *than the resistance in the subsequent ascent*, by
" *which the time is contracted.*"* This cannot
be understood of Clock-pendulums, for it sup-
poses *each subsequent ascent* shorter than the pre-
ceding descent, which must terminate in rest.

Descent quickest
in Clock-pendu-
lums, &c.

Further reasons,
&c.

130. But as soon as a Clock-movement is ap-
plied to a Pendulum, the descent is performed in
less time than the ascent, because the action of
the Wheels promotes the descent, and renders *each*
subsequent ascent, as long as the *preceding* ;
MOREOVER ; what HE means to be understood of
Clock-pendulums, he expressly mentions ; See
Cor. 2. Prop. 53. Pr. Math.

* Because the resistance, is in each, as the squares of their velocities : i. e. as the squares of the spaces described : if the spaces described remained the same, so would the resistances : but this, not being the case ; it is evident that what Sir ISAAC here says ; is by no means to be understood of pendulums having a maintaining power.

131. *It does not therefore appear, that short Vibrations derive any advantages from their supposed affinity to the cycloid; nor that Sir ISAAC NEWTON any where meant, to recommend them in Clocks; if the improvement of Clock-work, had been his motive for writing, it cannot be doubted, that he would have shewn as much Mathematical skill and accuracy in this, as in other subjects; but his views were more exalted.*

RESISTANCE
OF THE AIR.

Conclusion relative to short Vibrations.

132. We must then judge of short Vibrations, *solely, by the known properties of the circle; and when we have compleated a probable theory, experiment will best determine its merits.*

Practice the criterion of all theory.

133. One reason more, against short Vibrations and heavy Pendulums; is, that the spring that suspends the Pendulum, must increase in strength, as the Pendulum does in weight; and since all springs alter their dimensions, and consequently their elastic force, by heat and cold; it follows, *That*

Another reason, &c.

134. Such changes, must in every spring bear a certain proportion to the whole elastic force; therefore, the changes that will arise in the forces of different springs by equal changes in their degree of heat and cold, will be to each other, *as the relative forces of such springs; And*

Changes in Pendulum springs.

135. Though I have hitherto considered the motive force of the Pendulum, as composed wholly of gravity and the action of the Wheels; (70), it would be absurd, *not to add to them the elastic*

Whole motive force of the Pendulum, &c.

elastic force of the above spring, since it opposes the ascent as much, and in the same manner, as it promotes the descent, and therefore has a constant tendency to shorten the times of Vibration *.

Effect of changes
in the Pendulum
springs.

136. And the effect that this elastic force will have on the times of Vibration, will be (80) *as the elastic force, to the motive force of the Pendulum*; And,

As the whole force
of such springs.

137. Since the alterations in this force, are, in different springs, *nearly as their whole force*, (134), it follows, that the relative effect that such changes in the force of the springs would have on the times of Vibration, would be directly as the whole force of such springs.

As the weight of
the Pendulum.

138. But as the force of those springs must increase as the weight of the Pendulum, the alterations that will happen in the times, will be (137) as the weight of the Pendulum; and consequently when the momenta are equal, it will be much greater in short, than in long Vibrations (89) †.

* Some chuse stiff springs, as they resist most towards the extremities of the Vibrations, from which they acquire in some degree the properties of the cycloid: But any alteration in the action of this spring, has the same effect as an alteration, in power of gravity: which alters the times of Vibration, in cycloidal, as well as in circular Arcs.

† Nor will the centrifugal force of the longer Vibrations, at its lowest points, nearly ballance this inconveniency in the heavier Pendulums.

139. Some

139. Some may possibly expect that I should here mention the exact limits for the length of Vibrations and weight of Pendulums, but though I have endeavoured to run a parallel betwixt the advantages of each, I do not pretend to prescribe for the practice of others ; and though *in common* I use Pendulums from 6 to 16 pounds vibrating from *three to six degrees, from the point of rest** ; I do not assert that those limits are best ; on the contrary, I imagine that Vibrations may advantageously be enlarged to ten degrees *on each side* the point of rest ; but this requires further improvement in Clock-work : of which more hereafter.

140. In this enquiry into the nature of Vibrations, I have endeavoured to use such reasoning as may be understood by every man of sound sense, though not possessed of the advantages of a Mathematical education ; and I expect that by having thus, as much as in me lies, increased the number of my judges ; impartiality will believe, that I wish no oversight of mine to mislead or pass unobserved.

Address to the reader.

141. Some further objections to cycloidal Vibrations are reserved for an after part of this essay, when the different effects of such alterations as happen in the density of the air are considered.

* That is, Arcs from 6 to 12 degrees.

IMPROVEMENT OF

142. HAVING SHEWN, *That* the advantages of different Vibrations, in correcting the influence of any changes that may happen in the maintaining power are (*cæt. par.*) in the duplicate proportion of their respective lengths (41, 47).

243. *That* the constant resistance of the air, has the same tendency to correct any irregularity in the maintaining power, and to limit the length of the Vibration; *that* the action of gravity has (118).

144. And *that* such uniform increase of friction as takes place by increasing the maintaining power, cannot influence the performance of the Clock (50, 60).

145. *That* the resistance of the medium has the same effect in altering the length of Vibration, as diminishing the maintaining power would have (51, 52). And consequently *what* is said of the former, (41, 47), is equally applicable to the latter.

146. *That* short Vibrations derive no advantage by being maintained by a smaller power in proportion to their momentum, than long Vibrations are (48 to 51).

147. *That* no method is yet investigated for giving the true cycloidal properties to Pendulums, (98, 99); and that any remaining error is diminished by enlarging the Vibration (41, 47).

148. *That* admitting all that Mr. HUGENS has demonstrated of the cycloid; short Vibra-
tions

tions in a circle, *derive no advantage from their supposed affinity thereto* (112). RECAPITULATION.

149. *That the resistance of the air can only alter the times of circular Vibration, by altering their lengths* (115).

150. *That Sir ISAAC NEWTON has no where recommended short Vibrations for Clocks ; nor did he intend that his demonstrations of funipendulous bodies should be any how applied to Clock-work* (121 to 133).

151. *That momentum may be acquired to a greater degree and more advantage, in long than in short Vibrations* (133 to 138), and, that on the whole, long Vibrations are inferior to short ones in one article only ; which takes its rise from the imperfections of execution ; and may therefore be remedied by proper care in the mechanic (113), as I shew hereafter.

152. FROM ALL WHICH, *it may be concluded, that long Vibrations are less influenced by equal causes, than short ones : which concludes the first part of the theory of Clock-work* (5). I now proceed to the SECOND: in which many articles will occur, that will corroborate what has been already said. Long Vibrations less influenced in every respect, than short ones, &c.

153. *The subject of enquiry in the second part of this Essay is, WHAT CONSTRUCTION OF A CLOCK, tends least to alter the isochronism of the same Pendulum.* Second part of the theory, &c.

INFLUENCES OF
THE OIL ON THE
PIVOTS.

Considerations re-
ferred, &c.

Influences on the
oil irregular, &c.

154. As the influence of heat and cold on the Pendulum, and the irregularities of action, with wheels and pinions, take place in almost all Clocks; I refer the consideration of them to a subsequent place; and only observe here, *that in each of them, equal causes always produce equal effects.*

155. The influences of heat and cold on the oil applied in Clocks, *is of a more irregular nature*; for the qualities of the oil, are through time changed by the motion of the Clock, in so much that *equal degrees of heat and cold will have different effects at different times*; which makes it impossible to apply a remedy by means of, the expansion of metals; and it would even seem that a perfect remedy had been despaired of unless by discontinuing the use of oil: this is also big with difficulties, and at the end we will find, that we have (at a considerable expence) *only* substituted a smaller imperfection for a greater.

Proposal.

156. I shall *here* endeavour to shew; *how this imperfection may be much reduced, and what construction of a Clock will be least influenced by it, when thus reduced.*

Smaller quantity
of oil sooner de-
stroyed by motion,
&c.

157. Since a smaller quantity of oil, is sooner destroyed by motion, than a greater; the effect will be rendered less, and always more proportionable to the cause, by supplying the pivots with a greater quantity of oil, which should be contained

contained in a metal not so liable to corrode as brass*; for most oils unless concentrated by cold, contain more or less of saline, acid or aqueous parts, sometimes all the three; which corrode the brass; and the parts thus corroded, mix with and destroy the oil: care must also be taken not to use a soft malleable metal however fine, for dust, &c. will stick to it, and tear the pivots: I have used hardened steel for this purpose, *in preference to any other metal.*

INFLUENCES OF
THE OIL.

Contains saline, &c.
parts.

Steel bushes.

158. If the same oil be applied to any number of Clocks, equal degrees of heat and cold will have equal effect on the fluidity thereof in each Clock, without regard to their moving powers: *Therefore,*

Foundation of the
theory.

159. If there be any number of Clocks whose moving powers are as 5, 10, 20, 40, &c. *having the same oil applied, and equally exposed;* any change of heat or cold will equally add to, or subtract from, their moving powers (158); suppose one degree of diminution in each, then will the moving powers acting on the pallets, be as 4, 9, 19, 39; so that *the alteration, is to the whole moving power in each, inversely as the moving powers to each other.*

Illustration by
Clocks equally ex-
posed to cold.

* The expence of diamonds or rubies, is the only reason of my not recommending the use of them. But I here treat of the improvement of Clocks, for domestic uses, wherein expence must as much as possible be avoided.

INFLUENCES OF
THE OIL.

Immediate effect
of any change, &c.

Momentum accu-
mulates with the
increase of power.

Its effect in the
inverse duplicate
proportion of the
motive force.

Clocks should
move freely, &c.

The variation in
time is greater
with small, than
great weights.

160. But the *immediate* alteration that any change in the moving power will cause in the measure of time, will be to the whole time, as the alteration in the moving power to the whole motive force of the Pendulum (80).

161. Every Clock continues to increase its Vibration *till the resistance of the air, &c. becomes equal to the maintaining power*; and therefore, the momentum accumulated in the Pendulum increases with the maintaining power; and since the momentum is increased *nearly as the motive force of the Wheels*; and the *comparative influences of the oil* diminish in the same proportion (159); *It follows that,*

162. The influences of the oil, will affect the going of a Clock, (*cæt. par.*) *nearly in the inverse duplicate proportion* of the motive force of the Wheels (161). And *therefore,*

163. Though the execution of all Clocks should be such as render their motion as free and easy as possible, no advantage is gained by using the smallest weights that will maintain the motion of the Pendulum; *but the contrary*: this answers well for proving the care and judgment of the workman, but so soon as that end is obtained, *the moving power should be increased* in order to improve the performance (162).

164. Example: A Clock that will go for eight days with two pounds, will measure time much better, *if a weight of twelve pounds be applied*;

applied ; for the momentum of the Pendulum will by this means be increased, nearly as twelve to two (161), and the influences of the oil, will be diminished in the same proportion (160), therefore the alterations occasioned in the measure of time, *by equal changes in the oil*, would be in *the former case*, to the alteration in *the latter* as thirty-six to one *.

INFLUENCES OF
OF THE OIL.

165. Thus it appears *how much those are mistaken, who use very small weights to Clocks* : for though an increase of weight is attended with an increase of friction, it only argues that the longer Vibrations require more maintaining power in practice than in abstract theory (50) †.

Mistake of using
small weights.

166. What has been hitherto said of the influence of the oil, *is more particularly to be understood of that applied to the pivots* : for, though

Greater on the
pallets than pivots.

* I have admitted, that the momentum is increased exactly as the maintaining power, for the sake of a simple illustration ; not with any view of deceiving : and if it appears that the advantages increase with the maintaining power, though not in the exact proportion here stated, my end is obtained.

† It also appears, that an increase of maintaining power is advantageous, even without regard to the increase of momentum acquired by it. Hence it is not so great an advantage in short Vibrations, that they are maintained with smaller weight ; for if the maintaining power was as uniformly the same, as the exertion of gravity, it would constitute as advantageous a motive force : Hence it is not the *quantity*, but *the irregularities* of the maintaining power, that hurts the performance of Clocks : and therefore the most regular is to be preferred, without regard to the proportion it bears to the momentum of the Pendulum.

it

INFLUENCES OF
THE OIL.

it also applies to the oil used on the pallets, the effect of any change in it, is much greater than has been hitherto mentioned ; for any diminution in its fluidity tends *to destroy* the momentum which the Pendulum had already acquired, as well as to *diminish the maintaining power* ; here, action and re-action conspire to alter the isochronism of the Pendulum.

As the revolutions,
&c.

167. If the influence of the oil on any pivot during one revolution, be expressed by one, the influence of two revolutions, will be two ; on three revolutions, three ; &c. *Therefore the influence of the oil, on any pivot in any given time, will be as the number of its revolutions.*

As the space, &c.

168. The space described is also as the revolutions ; therefore *the influence of the oil will be (cæt. par.) as the space described.*

Comparative on
each pivot, &c.

169. Thus, may the *comparative influence of the oil* on each pivot in a Clock be found, if allowances be made for their different diameters. Example : Since the swing wheel makes sixty revolutions for one of the minute wheel ; if their pivots were of equal size, the influence of the oil on the former, would be to its influence on the latter as 60 to 1 ; but allowing the pivots of the minute wheel to be thrice as thick as those of the swing wheel, the relative influences on them, will be as twenty to one.

170. If

170. If it be desired to represent the influence of the oil on each pivot in an eight-day Clock, it may be done as in the margin.

ON THE PAL-
LETS.

171. In the first column you have the Wheel; in the second, its number of revolutions; in the third, the mean size of both pivots; and in the fourth, the influences of the oil:

Wheels.	Revolutions.	Mean size of the pivots.	Influence of the oil.
First,	1	7	7
Minute,	12	3	36
Third,	96	$1\frac{1}{2}$	144
Seconds,	720	1	720

Use of the table.

by which it appears; that *the influence on the pivots of the swing wheel is nearly four times as great as on all the other pivots in the Clock.*

The influences of the oil ON THE PALLETS are next to be considered.—

On the pallets.

172. Let A B C, Plate 2d, represent the swing wheel of a Clock, and H K D the pallets; if the Pendulum be made to vibrate, the least angle that will possibly allow the Wheel, to escape; the influence of the oil on the pallets during one Vibration, will be as the length of the plane F A or C D on which the Wheel acts (168), and the influence during two Vibrations, will be as both these planes; therefore, if A O, is made equal to F A and C D, together, it will represent the influence during two Vibrations; but A O, is greater than the Arc A L M, and therefore, will bear a greater proportion to any third quantity, and the influences are as the spaces (168); therefore the influence on O A, will bear a greater

Demonstration, of the least possible.

G

proportion

INFLUENCES OF
THE OIL

proportion to the influence on the swing wheel pivots; than the influence on the Arc A L M, would bear to it: but let us here suppose the influence, *only as the Arc A L M*, then will the influence on the pallets, during one revolution of the swing wheel, be to the influence on its pivots, *as the diameter of the wheel, to the mean diameter of both pivots*.

Action, and re-
action have effect.

173. It may here possibly be said, that though this influence takes place at the same time on both the pivots, it does not so on the pallets; but let it be remembered, that on them, action and re-action have *each an effect* (166), but in no other part of the movement; therefore the least influence *that can possibly take place on the pallets* (172), will be to the influence of both pivots of the swing wheel; *as the circumference of the wheel to the mean circumference of both its pivots*.

Wheel to its pi-
vots, as 50 to 1.

174. We may reasonably suppose, that the circumference of the swing wheel is to that of its pivots, as 50 to 1; in which case, the influence of the oil on the pallets, *with the least possible vibration*, will be to the influence on the swing wheel pivots as 50 to 1 (173): but the influence of the oil on the swing wheel pivots, has already been proved equal to four times the influence on all the other pivots (171); therefore, *the least possible influence, that the oil will have on the pallets, is two hundred times as great as the influence*

influence on all those other pivots : or forty times as great as the influence on all the pivots, those of the swing wheel included.

ON THE PAL-
LETS.

On the pallets to
that on the pivots
as 40 to 1.

175. I have hitherto *supposed the Vibration as short as could possibly allow the Wheel to escape*, in which case, the influence would be the same; *whether the pallets were constructed on the RECOIL-ING principle, or that of the DEAD-BEAT*; but,

176. Let us now *suppose*, the pallets constructed on the principle of the DEAD-BEAT, and that *the Vibration is doubled*, then will the Wheel embrace the circular part of the pallet, and each tooth will move from F to P, and from P to F again; before it begins to act on the plane F A; therefore (168), *the influence of the oil will now be, to what it formerly was, as twice F P together with F A, to F A*; and if F P be to F A, as two to three, twice F P will be to F A, as four to three; and therefore (168), *the influence on the pallets will now be, to what it formerly was (174), as seven to three*; and *to the influence on all the pivots, nearly as ninety-two to one**; and this I take to be the general proportion of influence on the pallets in Mr. GRAHAM'S Clocks, and in the generality of others that go with small weights,

With the dead-
beat.

PLATE III.

In Mr. GRAHAM'S
Clocks, &c.

* Or to the influence on all the pivots, those of the swing wheel excepted, nearly as 466 to 1.

IMPROVEMENT OF

and where the pallets take in twelve teeth of the swing wheel *.

177. *Let us now suppose the above pallets, constructed on the RECOILING PRINCIPLE; and enquire what will be the influence on them; all other circumstances as formerly.*

PLATE II.

With a recoil.

178. Let AF be produced to H , and it will represent the plane on which the Wheel acts; by the construction of the figure, FO , will be greater than FA , for they subtend equal angles at the center; but we shall here *suppose them equal*. Now, let the tooth C , escape the pallet CD , and the tooth M , will drop in the point F ; when the whole Vibration is performed; that is, when the Pendulum is at the extremity of its Arc, the tooth M , will be at O , from whence it must return to A , before it can escape the pallet. *Thus it appears, that in each Vibration the tooth describes on the pallet, a space equal to thrice AF ; therefore, the influence of the oil on the*

* Plate 3. Fig. 3. exhibits at one view the length of the pallet, and the distances of the center of the verge from that of the swing wheel, according to the number of teeth of the Wheel which the pallets take in, from 2 to 12: By which it appears, that the distance of those centers, is the secant; and the length of the pallets the tangent, of half the angle subtended at the center of the swing wheel, by such number of teeth.

pallets,

pallets, during each Vibration, will in this case be to the influence on F A, as three to one.

ON THE PAL-
LETS.

179. And (174), *the whole influence on the pallets* will here be, to the influence on all the pivots, as one hundred and twenty to one; but the influence with the DEAT-BEAT has been proved, to be to that on all the pivots, as ninety-two to one (176); consequently, *the influence of the oil on the pallets*, with the RECOIL, is to the influence with the DEAD-BEAT, (in this case) as one hundred and twenty to ninety-two.

To that on the pivots.

180. I have in the above calculations considered the influence *on the pallets only*, but if we allow for *the additional influence on the pivots with the recoil*, the whole will be greater than above stated; for the whole influence on the pivots, will be as the space described by the point of any tooth in the wheel during sixty Vibrations; to the circumference of the Wheel.

Additional on the pivots, its proportion.

181. In the above comparative view, the face of the pallet has been considered as a plain; but the demonstrations will apply, supposing them curves; only observing that in such case, the influence will be increased in the proportion that the length of such curve bears to a straight line joining its extremities; and the relative influences on all the parts of *those two Clocks* may be represented as follows.

On curve pallets.

On all the pivots	{	With the dead beat	—	—	1
		With recoiling pallets	—	—	3
					The

INFLUENCES OF
THE OIL

On the pallets	{	The least possible	40
		Dead-beat and double Vibration —	92
		Recoiling pallets and double Vibrat.	120*

182. Having thus considered the influences of the oil on the pallets, and shown that it will *always be greater (cæt. par.) with a recoil than dead-beat*: I now proceed to enquire; *how this influence may be diminished by the construction of ordinary pallets.*

Dead-beat to prevent a recoil, &c.

183. An attentive view of Plate 2d may satisfy us, that the *dead-beat* is chiefly intended *to remove the recoil and its bad effects*; and that in pallets, where friction and the influences of oil take place, *no advantage, is acquired by increasing the time of rest.* Example:

Illustration.

PLATE II.

Time of rest considered.

184. If the Pendulum vibrate any angle O, K M, the slope of the pallet should subtend the whole of that angle or nearly so, as P A: for if the slope only subtends one half of the angle as F A, the influences of the oil will be increased in the proportion that twice F P together with F A bear to P A; but P F and F A together, are greater than P A; therefore twice P F and F A, will be much greater than P A; and consequently (168), *the friction and influence of the*

* It is not meant here to assert, that this proportion will universally hold; for it will vary in proportion to the quantity of the recoil; but will ever be greater with it than the dead-beat.

oil, will be increased in the same proportion, *by thus increasing the time of rest.*

ON THE PAL-
LETS.

185. As all Clocks vibrate further when the oil is clean and fluid, than when it becomes dirty and glutinous, we must always allow the Arc of rest as P F, to subtend an angle equal to the greatest change that can happen from the different states of the oil; nor should any great latitude be taken here, since Clocks should always be cleaned, when their Vibration is sensibly diminished.

How long it should
be.—

186. Thus it were well that in constructing pallets, on the principle of the dead-beat, more regard was paid to this consideration; and, that the time of rest, was made no longer than is *absolutely necessary.*

187. But we daily see, that *some increase the time of rest*, while others *increase the recoil*, each with intent to improve the performance: but on the whole, increasing the time of rest, where the influence of oil takes place, increases the evil, though not so much as an equal increase of recoil does (182).

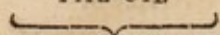
Increase of recoil,
or rest: increase it.

188. It may here probably be urged that the influences of the oil on the pallets, must always be greater with long Vibrations than with short; for P A, is longer than F A; *but if this be generally the case, it does not follow*, that it must remain so; For,

P L A T E II.

189. In equal Vibrations, *those influences are as the length of the pallets.* See Plate 3. Fig. 1. which

As the length of
the pallets.

INFLUENCES OF
THE OILPLATE III.
FIG. I.

which represents the place of action of four pair of pallets, whose lengths are as 1, 2, 3 and 4; if the Arc of rest, and slope, subtend the same angle in each; as represented by the dotted lines, it is obvious that the influences of the oil and friction, are in each, as the length of the pallets from the center of motion to the point of action.*

Pallets shortened.

190. Therefore when the Vibration is enlarged, the *pallets should be shortened*, and care should be taken *never to have them longer* than what is *absolutely necessary*; for no advantage can be thus gained, and the disadvantages are obvious (189).

Long pallets no
advantage.

191. *As some are of opinion*, that a longer pallet will maintain the motion of a Pendulum, with less power than a shorter; I must once more refer to Plate 3. Fig. 1. where it will appear; that what is gained in power *by the length of the pallet*, is lost *by the inclination of the plane on which this Wheel acts*; if it be proposed to make the inclination equal in all the pallets, and thereby to acquire an advantage in proportion to their length, let it be remembered that if the power is made to act *four times as strong*, it will only continue to act *one fourth of the time*, so that what is gained in power, is lost in time. *On the whole,*

* And the length of the pallets, *c. p.* depends on the number of teeth which they take in. See Plate 3. Fig. 3. (176).

192. Since

192. Since the power of the *swing wheel* is limited, any attempt to increase its effect, by lengthening the pallets, will be fruitless; for it cannot escape the pallets, however short; before it has exerted all its force thereon. Example: Every mechanic knows that the exertion of gravity, on bodies descending by inclined planes, is always as the *perpendicular height*, and therefore, never attempt to gain power by *lengthening* the plane; the case is exactly similar with regard to long and short pallets: for if the Wheel be capable of exerting a certain force, in a whole revolution, it can exert no more than one sixtieth of that force in a sixtieth of its revolution; that is, during one Vibration.*

ON THE PAL-
LETS.

No power can be gained by lengthening the pallets.

193. It may possibly be said, that if the influence of the oil was so great *as above stated*, its effects on the performance of Clocks would be more sensible than they are: To this it is answered; that if *no other* imperfection took place, this effect would become considerable; but since the friction on the pallets, *as well as the influence of the oil* increases as the space which the teeth of the Wheel describe on the pallets; while the oil is attenuated by heat, the increase of friction on the pallets, arising from the increase

Why its effects not more sensible on the performance.

* And the progressive motion of the Wheel, in the one case, may properly be compared to the perpendicular descent, in the other; each, being the line of direction of the power, by which, its exertion must always be estimated.

INFLUENCES OF
THE OILFriction on them,
cannot ballance it.Different effects
counteract each
other, &c.The whole Varia-
tions bear less pro-
portion to the
causes, &c.

of Vibration *partly* compensates the increase of power, and preserves the length of Vibration more equal *c. p.* than if no friction took place, and *vice versa*.*

194. But the effects of friction on the pallets can never remedy the influences of the oil, for the former is of *a more uniform nature*, and the latter *very changeable*.

195. Heat lengthens the Pendulum rod of *a Clock*, and so tends to make it go slow; the same heat makes the oil more fluid; and by thus increasing the action of the swing wheel, on the pallets, tends to make it go faster †.

196. Thus, *do the effects of heat and cold on the Pendulum, together with the friction on the pallets* (193), always counteract, and in many cases overcome, *the influence of the oil on the pallets, &c.* (193, 195); and by this means, *the whole variation in the performance of Clocks*, bears a less proportion to the whole causes, than would happen if they did not counteract each

* It is not here meant, to recommend the friction on the pallets, as a desirable remedy against any imperfection in the performance: for if it be diminished to such a degree, as to render the application of oil unnecessary, the Vibration will by that means, be increased so as to be less influenced by any alteration in the tenacity of the oil on the pivots (41, 173, 174). It is therefore instrumental only, in diminishing an evil of which it is the cause, and which it never can ballance; nor can its advantage in any respect equal its hurt: as I shall shew hereafter.

† Particularly with recoiling pallets.

other ;

other ; or if each was taken separately. ON THE
WHOLE IT APPEARS,

ON THE PAL-
LETS.

RECAPITULA-
TION.

197. *That* oil is of a changeable nature, and that no perfect remedy can be applied for its effects by opposition (155 194).

198. *That* increasing the moving power in Clocks, will diminish the relative effect of such influence on every part of the movement and pallets (162).

199. *That* increasing the quantity of oil will render its influence less, and more uniform (157).

200. *That* the *recoiling pallets* increase the influence of the oil and friction *on all the pivots*, as well as on the pallets : but the *dead-beat* does not (180).

201. *That* the influence and the friction on *recoiling pallets*, (cæt. par.) are greater than on those constructed on the principle of the *dead-beat* (181).

202. *That* the influence of the oil and friction, is least on those pallets, where the *recoil*, or *time of rest*, is least (187) : Therefore,

203. *That* the slope (or planes of action) of the pallet should nearly subtend the whole angle of Vibration (184), where friction takes place.

204. *That* the influence of the oil is greater in pallets whose place of action is a curve, than those that are straight (181).

INFLUENCES OF
THE OIL

205. *That* the influence increases (*cæt. par.*) as the diameter of the swing wheel (172) *.

206. *That* the influence of the oil, and friction increases as the length of the pallets (189).

207. *That* no advantage is acquired by long pallets, *but the contrary*; and therefore they should be made as short as circumstances will allow (191) †.

RECAPITULA-
TION.

208. *That* the influences of the oil and friction may be as much diminished in long as short Vibrations (190, 172).

209. *And, that* the friction on the pallets counteracts the influences of the oil, *but never can ballance it* (193, 194).

210. Thus have I endeavoured to shew, *how the changes that happen in the fluidity, &c. of the oil, do influence the performance of Clocks; and how far the effect may be diminished* WITHOUT MUCH EXPENCE: and if what I have here advanced proves any how instructive to those who know less; or procures a better investigation, from those who know more of this matter; my end is answered.

* Here the friction does not increase as the influence of the oil; as will appear, when we consider the nature of the horizontal wheel and cylinder.

† This rule only applies in pallets, where friction takes place; but I shall shew hereafter, how a considerable advantage may be gained by lengthening such pallets, as have neither friction nor recoil.

211. *I now proceed to enquire into the different methods that have been heretofore used, for removing the influences of the oil.—*

ON THE PIVOTS
DIMINISHED.

212. When two hard bodies rub against each other, there arises a resistance which we commonly call *friction*; and though by experiments of short duration, repeated at different times, we find no sensible difference in this resistance; it increases by continuation; so as in some cases to equal the moving power.—

Friction accumulates.

213. If a common Clock be set a going without any oil, it moves pretty freely at beginning: in time, loses its Vibration; and in the end, comes to rest; and if the rubbing be constant, the times in which this will happen, will be shortened by increasing the pressure, or relative velocities of the rubbing surfaces*.

Example.

24. All solid bodies are heated by friction, or attrition of any kind; and *the heat* thus generated is at least in some degree, proportioned to the force and velocity with which the bodies act on each other; nor is it improbable, that *it* opens the pores of metals or produces such other changes in their textures, as to occasion *this increase of friction*; to prevent the pernicious effects of which, OIL has been applied to Clocks; there-

A probable reason, why.

* The application of oil will immediately recover the motion; which tends to prove, that such decrease was not solely owing to such roughness of the surfaces, as commonly takes place.

fore

INFLUENCES OF
THE OIL

Friction pullies.

fore, if friction be removed, by any mechanical means, the application of IT will become unnecessary, and its influences no longer take place.

215. *Thus* have friction pullies been introduced, and if materials and execution could be supposed perfect, and no regard paid to expence, *the friction of the pivots* might by their means be sufficiently reduced for common purposes; nor would I disapprove the use of them, unless a more simple and effectual remedy could be offered; of which more in its place.

Winding up every
half minute.

216. The next attempt of removing the influences of oil *from the pivots*, we owe Mr. HUGENS, which contrivance he describes thus in his *Horologium Oscillatorium, published in the year 1673*; “To that Wheel which is next the
“Pendulum, and has its teeth cut like a saw, we
“hung a *small weight* by a slender chain, by means
“of *which*, that Wheel alone was moved, all the
“rest of the machine answering no other pur-
“pose than the winding up that small weight
“every half minute.”

When first applied.

217. Mr. HUGENS informs us that he applied the above contrivance, to two *spring-clocks* that were sent to sea in the year 1664, in order to discover the Longitude; and that their motion was by *the above means* rendered more uniform (at land) than in any of his former Clocks: he gives a full description of them, with an account

of their success, in the above cited book, from page 16, to 21, to which I refer the curious.

ON THE PIVOTS
DIMINISHED.

218. The advantage of this ingenious contrivance is manifest *in spring-clocks that are fixed at land*: for we may *thus*, have the convenience of the spring (as the first mover); and the more uniform action of gravity *for maintaining the Vibrations*; but we are not to conclude, that by this means Clock-work is perfected.

Advantages of this
contrivance.

219. *I have already shewn* (174) that the least possible proportion that the influence of the oil *on the pallets*, bears to the influence on *all the pivots*, in an eight-day Clock, (those of swing wheels excepted) is as 200 to 1. *Therefore*, this contrivance, can only remove a 200th part of the whole influence of the oil in an eight-day Clock *.

Its utmost effect.

220. Some may possibly think, that great advantage is acquired by removing the irregularities of action in the Wheels; without considering that this little weight must be wound up every half minute; and that the swing wheel must *as oft* unlock the part which winds it: *thus*, there arises a periodical inequality in the action of the swing wheel on the pallets, which is no more innocent than the periodical fluctuations in the action of Wheels and pinions, as shall

Comparative ad-
vantage considered.

* See the note to par. (176): by which it appears, that the influence of the oil on the pallets, and the pivots of the swing wheel together; is 466 times as great as on all the other pivots in an eight-day Clock, though here, stated only at 200.

INFLUENCES OF
THE OIL.

Conclusion rela-
tive to its uses in
standing Clocks.

The contrivance
ingenious.

Not so advanta-
geous in portable
machines as above
stated.

be further shewn hereafter. ON THE WHOLE IT
APPEARS,

221. *That even in fixed Clocks, this contrivance serves only to take off the imperfections of the main spring so as to render the action on the pallets as uniform as in Clocks wherein gravity is the first mover; and to remove a 200th part of the influence of the oil on the whole movement (174).*

222. I would not be understood by this inquiry, to depreciate an invention that indicates as much genius as some others of more utility; nor wantonly to detract from the merits of a person to whom Clocks owe their greatest improvement; *I have ever preferred demonstration, to opinion, nor is the least disrespect meant, wherever the former is opposed to the latter.*

223. When I treat of Watches, it will appear *that the advantages of the above contrivance cannot be so great in any PORTABLE MACHINE as above stated*; and that it is more than probable, it hurts the performance; but let us now *suppose*, that it has all the desired effect, and that the influences of the oil on *all the pivots* be totally remedied; the influence on the pallets still remains; and consequently $\frac{1}{40}$ only of the whole influence on the Clock is removed (181)*.

* What is admitted at the close of this paragraph, is intirely for the sake of illustration; for this contrivance has no tendency to remove or diminish the influence of the oil on the swing wheel pivots, therefore its utmost advantage is stated (221).

224. If

224. If any attempts have been made by the mechanics of the last age, towards removing the influence of the oil from the pallets, I am unacquainted with them ; and though many have been made by those of the present, it does not appear that they have been attended with all the wished for effect ; *for it is necessary, not only to remove the influences of the oil ; but that no other cause be introduced that can be productive of similar effects.*

225. I have seen pallets of a very ingenious construction, with Mr. *John Harrison* of *Red-Lion-Square*, and with Mr. *Hindley* of *York* ; in each of which, the friction and influences of the oil were *almost annihilated* ; but if I mistake not, in removing these, *other imperfections have been introduced* ; which, however short of the former, merit serious attention.

226. The contrivances used by each of those gentlemen, *so well known for their mechanical abilities*, were much of the same nature ; nor did they differ materially in principle in any article that I could see ; but Mr. *Harrison* informed me ; “ that in his regulator, the action of the Wheel “ on the Pendulum was the same with the action “ of gravity thereon* : nor do I in the least

ON THE PAL-
LETS, DIMI-
NISHED.

Introduction.

Pallets by Messrs.
HARRISON and
HINDLEY.

Much of the same
principle.

* By which I understood, that the action of the swing wheel on the pallets, increased and diminished in every part of the Vibration, in the very same manner that the action of gravity did on the Pendulum-ball ; i. e. that the action was in every part, as the versed sine of the angle contained between the center of oscillation of the Pendulum, and its point of rest.

IMPROVEMENT OF

doubt the assertion, though I have never seen those pallets ; but cannot conceive what real improvement can follow ; however, to the best of my remembrance, no such attempt was made in Mr. *Hindley's*, but *the following articles were common to both their pallets, that I did see* *.

Articles that are
common to both.

227. First, *That* the teeth of the Wheel, *do not* rub on the *pallets*, but continue to act (or press) *on them* alternately during their respective Vibrations.

* We are informed in the Phil. Trans. Vol. XLVII. pag. 517. and in the Supplement to Mr. HINTON'S Dict. of Arts, &c. (See PENDULUM), "that this manner of applying the action of the "Wheels to the Pendulum, prevents its being affected by the "different resistance of the air : " BUT I cannot imagine, that so ill-grounded an assertion, was thus publicly made with Mr. HARRISON'S consent : when it requires but a few minutes reasoning, to prove, that such an application of the maintaining power, must be hurtful to the performance of the Clock, by increasing the effects, which, *any alteration* in the density of the air, would otherwise have on the measure of time.

Does not any *increase* of density (or resistance) in the air diminish the angle of Vibration ? and consequently ; this accelerating effect on the pallets (note 226) ; how then can the *latter* ballance the *former*, when the one increases as the other diminishes ? And, admitting that this accelerating effect, did increase and diminish with, the density of the air, its effect on the measure of time, would be no better than above stated : unless we suppose, that the time of ascent of a Pendulum, as well as the time of its descent, is increased by the resistance of the air : But Sir ISAAC NEWTON informs us, That the time of ascent is shortened, and the time of descent, lengthened by such resistance : nor is it difficult, (if it was necessary) to confirm his assertion by experiment : but of these matters more in their proper place.

228. Se-

228. Secondly, *That* the *one pallet* cannot disengage itself from the Wheel, till the *other* begins to act, so as to cause a *recoil*, or retrograde motion of the Wheel ; *which* was much more considerable in those scapements, than in common ones.

229. *Thirdly, That* during the progressive motion of the Wheel, a *slender spring* is bent, that disengages the pallet from the Wheel, *so soon as the recoil begins.*

230. Fourthly, *That* when the pallet is thus thrown from the Wheel, it is received by *another spring*, the office of which, is to keep it in a certain position, in which the teeth of the Wheel may always find it.

231. Fifthly, *That* during the retrograde motion of the Wheel, those *last mentioned springs* are bent, by which means they oppose the ascent of the Pendulum, and by their unbending, promote its descent.

232. *The conclusion concerning those pallets must be deferred, till the effect of a RECOIL in general is explained ; to which I now proceed.*

Conclusion deferred.

233. I have formerly observed ; that the DEAD-BEAT was invented to remove the bad effects of a *recoil* (183) ; and *shewn* ; that the influences of the oil and friction, is greater on pallets that have a recoil, than on those that have none (182) : *I now enquire into the comparative*

OF A RECOIL IN
GENERAL.All pallets reducible
to two CLASSES.General uses of
the maintaining
power.Used by some to
render the Vibra-
tions more isochro-
nal.

PLATE II.

advantages of the DEAD-BEAT and RECOIL, when neither friction, nor influence of the oil take place.

234. All pallets whatever, must have *some recoil, or no recoil*: if *the former*; they take their name from thence: if *the latter*; they belong to the DEAD-BEAT: and thus may all pallets be reduced to TWO CLASSES: *and what I am now to observe of those two kinds of pallets, will apply WITHOUT EXCEPTION, in all the variety of constructions that can possibly be invented*; since it wholly depends on the quantity of recoil, independent of all other circumstances.

235. The action of the Wheels, in all Clocks, serves to maintain the Vibrations; and their revolutions, give the number of Vibrations; these are ends, which the maintaining power must answer in all Clocks; but some have attempted to render the Vibrations more isochronal, by giving a recoil; and thus making the action of the Wheels oppose the ascent of the Pendulum at the extremity of its Vibration; and they seem to prefer this opposition of the Wheels, to the more *unalterable* opposition of gravity; because the former increases and diminishes as the maintaining power; and consequently, opposes the ascent most, when it has the greatest tendency to enlarge its limits: but *this imaginary advantage vanishes*, when we consider, That;

236. When the tooth C, Plate 2. is disengaged from the pallet C D, the tooth M, will drop

drop on the pallet H A at F, and as the Pendulum continues its progress, the Wheel will have a retrograde motion on the pallet; suppose, from F to O; it is obvious that the Wheel *will promote the descent and lengthen the next ascent* by its motion from O to F; *as much as it opposed and contracted the ascent* by its motion from F to O; and thus, *the action* from O to F, and *the resistance* from F to O, do exactly ballance each other, so far as relates to the length of Vibration; And therefore,

OF A RECOIL IN
GENERAL.

Can have no tendency to limit the Vibration.

237. A RECOIL *can have no tendency whatever, to render the length of the Vibrations, more or less equal; nor to maintain the motion* *.

Nor to maintain the motion.

238. It is well known that any increase in the power of gravity, accelerates the motion of a Pendulum, *and shortens its time of Vibration*; and that *the times of ascent and descent, are equally contracted by this increase of gravity* (17). Hence we may with truth infer, *THAT whatever opposes the ascent of a Pendulum, shortens its time of Vibration as much as if it had promoted the descent. Therefore, any power that both opposes the ascent, and promotes the descent*

Effect of gravity considered.

* The effect of friction on the pallets will be considered fully hereafter, and shewn to be very hurtful to the performance, even though it has a tendency to preserve the Vibrations more nearly of an equal length.

OF A RECOIL IN
GENERAL.

Recoil has a two-fold effect on the times.

Space described as the impressed force.

Impropriety of too much limiting the Vibration.

of a Pendulum ; must produce a double effect on its times of Vibration *.

239. And *thus it appears* that any change, in the action of the Wheels, *during the time of recoil*, will have a double effect in altering the natural times of Vibration (238), *without the least tendency to render the length thereof more equal* (237)†.

240. If a certain impressed force, give a certain velocity, a double force, will give a double velocity ; a triple force, a triple velocity, &c. and the spaces described in equal times, will be as the respective velocities : *that is*, as the respective forces impressed.

241. Thus *if the impressed force and velocity of a Pendulum be doubled*, and the length of Vi-

* Here it is to be observed ; that any power co-operating with gravity, contracts ; and the same power opposed to it, prolongs, the times of Vibration. Hence whatever power, acts during the time of ascent, and promotes it ; or opposes the descent, will prolong the times ; and this should be carefully attended to : for on this principle, the maintaining power may be applied, in such manner as either to prolong or contract the natural times of Vibration.

† If it should be urged that the recoil may render the times of Vibrations of different lengths more isochronal, without having any tendency to limit their lengths ; the mode and quantity of recoil should be investigated with as great accuracy as the cycloidal properties ; in which case it will altogether be unnecessary and improper to apply the cycloidal cheeks ; nor can such an investigation as above mentioned, be made, before each separate effect that the application of a Clock has on the Pendulum, are accurately ascertained ; and even then, it is liable to all the same objections with the cycloidal Vibrations ; of which in their place.

bration remains the same, *the number of Vibrations will be doubled*; but if the length of Vibrations be *also doubled*, they will be performed in the same times, as those of half their length with half the velocity; *and universally*; if the length of Vibration increases, as the impressed force, the times will be equal; and on this account *it would be very improper to give a recoil*, on the supposition that it did render all the Vibrations more nearly of an equal length *.

OF A RECOIL IN
GENERAL.

242. It may possibly be urged by some, that the resistance is greater at the extremities of cycloidal, than circular Arcs; and therefore, that no error can arise by thus increasing the resistance at the extremities of Vibrations in circular Arcs: but let me beg of those to recollect; that *all the demonstrations concerning cycloidal Vibrations*; suppose, that the action on the Pendulum in its descent, is exactly equal to the opposition with which it meets in its ascent; which is not the case in Clock-pendulums; for the velocity in their descent, is greater than in their ascent: and that more, or less, in proportion to the length of Vibration; even beyond what happens in detached Pendulums.

Difference in the
theory of detached,
and Clock-pendu-
lums.

* The same objection, with many others, stand in the way of correcting the length of Vibration, by an increase of friction. See (259, 260).

243. And

OF A RECOIL IN
GENERAL.

Properties of the
cycloid cannot
with any propriety
recommend a re-
coil.

When too great
in circular Vibra-
tions.

Never to be ad-
mitted in cycloidal
Vibrations.

243. And though certain properties have been demonstrated of the cycloid ; it does not follow, that every curve that deviates from a circle possesses those properties, even when gravity alone acts : and much less, when any foreign power is applied ; *therefore*, the cycloidal properties in detached Pendulums vibrating in a non-resisting medium ; can by no means recommend a recoil, with those applied to Clocks.

244. *On the whole, we may be well assured, that in all cases where an increase of weight or maintaining power, makes a Clock go faster ; the recoil is too great : nor can it be supposed, that any, who have art enough to make the center of oscillation of a Pendulum describe the true CYCLOIDAL curve, and faith enough in ITS properties ; would think of giving a recoil, to correct those Vibrations that are (by their theory) already perfect ** ; from which appears the absurdity of applying cycloidal cheeks with a recoil : but of this more hereafter.

* As the recoil is intended to co-operate with the action of gravity on the Pendulum, in such manner as to render its motive force in every part of the Vibration, as the distance from the lowest point ; the mode and quantity of such recoil must be demonstrated with the same certainty, at least, as that of the cycloid : and I imagine that *this* will be much more difficult than *that* ; not to mention the much greater difficulties of execution in the latter, and the uncertainty, relative to the theory of the former when applied to Clocks.

245. *I now resume the consideration of those*
 PALLETS *wherein the friction and influences of the*
oil have been removed; the reader will please here
to peruse from Par. (227 to 232).

OF A RECOIL IN
 GENERAL.

Messrs. HARRI-
 SON and HIND-
 LEY's pallets re-
 sumed.

246. Let us here admit, *that the action of the*
swing wheel is as uniform as gravity; it has at
each Vibration not only to maintain the motion of
the Pendulum, but also to bend a small spring
 (229); therefore, whatever power is necessary
 to bend this spring, must be deducted from the
 maintaining power: and as all springs alter their
 stiffness by heat and cold; *that part of the ac-*
tion of the swing wheel, that maintains the Vi-
bration, can no longer be uniform, than the
air is of the same temperature: and thus, will the
length of Vibration be altered, and the accelera-
ting effects of the recoil take place (239), and alter
the times of Vibration: even supposing the cy-
cloidal properties perfect, and the density of the
air invariable.

Supposition.

Render the most
 perfect maintaing
 power unequal.

247. Again; *because those springs that are bent*
during the recoil (231), are liable to the same
changes; they will produce the same effect, with
an equal change in the maintaining power during
the recoil (239). And,

Another defect.

248. However trifling those articles may at
 first appear, they become of more weight, when
 we consider; *that they operate in that very part*
of the Clock where they produce the greatest pos-
sible effect, on the measure of time; and that

Further considera-
 tions.

K

those

PALLETS WITH-
OUT FRICTION.

Manner of apply-
ing the maintaining
power.

those springs are so small, as to be affected by the least changes in the temperature of the air ; nor can those effects be thoroughly remedied by a gridiron, or any other Pendulum, since they feel such small changes, as cannot sensibly affect such thicker pieces of metal ; add to this, that an alteration of one 86,400 part of the time of each Vibration, will amount to an error of one second per day ; a 604,800 part, in the time of Vibration, to a second per week ; and a 2,592,000 part, to an error of one second per month.

249. As to the property mentioned in Par. (226), it does not appear to me that any advantage is gained by it in maintaining the motion of a Pendulum : See Sir ISAAC NEWTON's II^d law of motion, where he says, " If any force generates a motion, a double force, will generate double the motion ; a triple force, triple the motion ; whether that force be impressed altogether and at once, or gradually and successively" (237). And so far as regards the measure of time, *it is hurtful* ; as will appear hereafter.*

250. And as to the isochronism of the Vibration, when the *dead-beat* is applied ; I shall hereafter shew in *what cases*, it is best to apply the

* It may be proper however, here to observe, that this method is preferable to others, wherein the recoil (being undetermined) may bear a greater proportion to the angle of Vibration.

maintaining power, gradually and successively ; and in which, it may more advantageously be applied nearly at once ; leaving those who better conceive the advantages of a recoil to give a like investigation when it is used.

PALLETS WITH-
OUT FRICTION.

251. I would not be understood to depreciate, or *totally disapprove* this ingenious invention : or to assert, that no good performance can be obtained when these pallets are applied ; on the contrary, I think them preferable to any that I have yet seen *wherein the influence of the oil takes place* ; but a proper regard must here be paid to *what has been said concerning the diminution of the influence of the oil (164)* ; for whatever be the cause of any change in the maintaining power, *the effect on the measure of time, will be (cæt. par.) as such change, to the whole power ; this argues for great maintaining power and long Vibrations.*

General remarks
on their advantages,
&c.

252. *If it is proved ; that the use of springs in pallets, renders the effect of the most perfect maintaining power unequal (246, 247) ; that a recoil, increases the effect of any such change (239) ; and that any alteration in the stiffness of those springs that act during the recoil, co-operates with the action of the wheels during such recoil, in altering the times of Vibration (247) :*

Inconveniences
brought into one
point of view.

253. *It naturally follows ; that however small the effect of those IMPERFECTIONS, the performance*

Conclusion.

PALLETS WITH-
OUT FRICTION.

Motive for this ex-
amination.

*mance of Clocks will be improved, by totally re-
moving them (248).*

254. If I have here pointed the way, to further improvement, my end is obtained; and when it is considered, that I propose hereafter to remove every imperfection so far as the nature of things will permit; and consequently, that every difficulty and imperfection that I now mention, do in that case, become so many weapons against me; candour will allow, that no other motive, than a real desire of improvement could have induced me to this examination.

Introduction.

255. Having pointed out the disadvantages of a recoil, and observed that the *dead-beat* was invented to remove them, it may be thought superfluous to say any thing more on that head; But,

256. *As the imperfections and properties of all objects, become the more obvious of being viewed in different lights; I shall now endeavour to shew the advantages of the DEAD-BEAT, in a manner different from what I have hitherto done; by which it will appear, that its comparative advantages, to the RECOILING principle, are greater than I have hitherto stated them.*

General remarks.

257. When a Pendulum is actuated by *the power of gravity only*, it rises to the same height from whence it fell; *allowing for the resistances of the air, &c.* Therefore, if the action of the *Wheels in the descent of a Pendulum* be equal to the

the resistances *in the descent and ascent together* : the *former* will at each Vibration, communicate as much motion as the *latter* destroys.

DEAD BEAT
FURTHER CONSIDERED.

258. And the velocity and length of Vibration, will continue uniformly the same while *this equilibrium* is preserved. But,

Vibrations continue equal, &c.

259. If the maintaining power be any how *increased* or *diminished*, so will *the Vibration* ; till the resistances of the air, &c. equal the maintaining power ; and *the velocity of the descent*, will increase with the power (257)*. Therefore,

Increase, &c. as the maintaining power.

As does the velocity of descent.—

260. The descents in the longer Vibrations, will be comparatively quicker than those of the shorter (240), in this case, than in detached Pendulums †.

Descents quicker than the ascents in Clock-pendulums.

261. And since the Pendulum in its ascent is not any how connected with the action of the Wheels (*as with a recoil*) it will *ascend agreeable to the laws of detached Pendulums* ; in which case, Mr. HUGENS has demonstrated that 29 of the longest Vibrations, are equal in time, to 34

Time of ascent in them, the same as in detached ones, cæt. par;

* But if we suppose the maintaining power applied in the time of ascent of the Pendulum ; it leaves room for some exceptions. But as those matters are fully explained where I treat of watch pallets, I leave the application here as no improper exercise for the reader's genius and attention ; as sufficient data are already furnished for the investigation.

† This, among many other circumstances, is entirely overlooked when cycloidal cheeks are applied.

DEAD-BEAT.

of the shortest, of the same Pendulum, *independent of the resistance of the air**.

The alteration in the time of a whole Vibration less, than in detached pendulums.

262. Now since in Clocks with a DEAD-BEAT, *the descent is quicker* (260), and *the ascent is slower* (19) in the longer than on the shorter Vibrations; the alterations in the time of an ascent and descent taken together, will bear a less proportion to the change in the *length* of Vibration, than in detached Pendulums; where the times of *ascent* and *descent* increase or diminish *together*†.

Dead-beat diminishes the effect of any change, &c.

263. And *thus*, does the *dead-beat* diminish *the natural effect* of any change that may happen in the length of circular Vibrations; whether occasioned by an alteration in the moving power, or in the density of the air:

264. In all that has been said (from Par. 233) *neither friction, nor the influences of the oil*, are supposed in the least degree to take place; and therefore, the less they do, the better will the theory and practice agree; *I have already shewn* (184), that in pallets where the influence of the oil takes place, such influence is increased by increasing the time of rest.

* It may here probably be said, that in pallets where *friction* takes place; the natural times of Vibration, (during the rest of the wheel) will be influenced *thereby*: but we must not forget, that such friction, opposes both ascent and descent equally and thence corrects itself (238); so far as uniform friction only, is considered.

† On this account, the cycloidal curve as hitherto investigated cannot have the desired effect on Clock-pendulums: with, or without, a recoil.

265. *And also (185) that the slope, or place of action in such pallets, should, as nearly as can be, subtend the whole angle of Vibration ; which implies, that the maintaining power should be applied gradually and successively, and this may serve as a general rule, in all pallets where oil is used **.

DEAD-BEAT.

Maintaining power gradually applied.

266. But the contrary should be observed, of *such pallets as have neither friction nor influence of the oil, during the time of rest ; for by this means, the influences of the oil, during the time of action, will be diminished †.*

Applied at once.

267. Where *the maintaining power is perfectly invariable, and where the isochronism of the*

May be applied in either way.

* I shall shew hereafter, that when the influence of the oil on the pallets is removed ; the effect of any alteration in the maintaining power, on the measure of time, will be (*c. p.*) as the time of action on the pallets to the whole time of Vibration ; but this will not apply where oil is used to the pallets.

† In all pallets where the action of the Wheel is suspended during part of the time of Vibration ; and where the maintaining power is not perfectly invariable ; the performance will be improved by applying the action of the Wheel, in such manner that one half its exertion take place in the descent, and the other in the ascent of the Pendulum ; for without particular regard to this, the Vibrations of Clock-pendulums, whether circular or cycloidal, can never have their natural properties (238). This matter will be fully explained and exemplified, when I treat of Watch pallets, (where a strict attention to it, becomes more necessary) ; only observing, that what is there said of the action of the ballance-spring, is here to be applied to the action of gravity on the Pendulum. It will also appear why it is more advantageous to apply the action of the Wheels to the Pendulum in its ascent than descent.

Pendu-

DEAD-BEAT.

Pendulum is neither influenced by friction nor the changes in the oil ; *it matters not, whether it be applied all at once, or gradually* ; I do not here mean, that in such case, the manner of applying the maintaining power will not alter the whole time of each Vibration ; nor do I pay any regard to such effect, provided it be uniformly the same in each succeeding one : *for such uniform effect*, is corrected by the length of the Pendulum.

268. It may probably be alledged, that more is here advanced in favour of the DEAD-BEAT, than agrees with the general comparative observations on the performance of Clocks constructed on the principles of the *dead-beat* and *recoil* : but WHOEVER *recollects* what has been said, *concerning the maintaining power* (164), *length of Vibration* (41), and *length of pallets* (189) ; will probably agree with me, *that no fair comparative trial has yet been made of the principles of the recoil and dead-beat.*

No fair comparative trial yet made of the dead-beat and recoil.

Maintaining power greater with the recoil than the dead-beat.

269. Is not the maintaining power always much greater *in common Clocks with recoiling pallets*, than in *the finest regulators with a DEAD-BEAT* ? frequently as 3, 4, or 5 to 1 ?

Vibration longer with the recoil.

270. Is not the Vibration always much longer in those common Clocks ; than in *these* constructed with the *dead-beat* ? And

Recoiling pallets shorter, &c.

271. *Are not the pallets always much longer with the dead-beat than the recoil* ? all which, ARTICLES OF THE GREATEST IMPORTANCE, have hitherto

hitherto (it would appear) been *accidental concomitants* of the recoiling pallets ; and every advantage arising from THEM, been imputed to the recoil? whereas, all the imperfections arising from a *contrary practice* have as erroneously being imputed to the *dead-beat*. Thus it appears ; *that*,

272. No comparative trial can be decisive, *unless where the maintaining power, length of Vibration and pallets*, are equal in each Clock *: in which case, the superiority of the *dead-beat*, will become evident : *And*

In what cases the advantages of the dead-beat will become evident.

273. If the greater number, and most eminent of the profession, have used longer pallets with the DEAD-BEAT, than the RECOIL, they can best assign reasons for so doing ; for none occur to me : nor does, the propriety of imitating precedents, in which neither theory nor practice seem to promise any real improvement.

274. FROM ALL THAT HAS BEEN SAID relative to PALLETS, the following general rules may be collected.

That *the recoil in pallets, increases the effect of any change that may happen in the maintaining power ; whether friction and the influence of the oil, DO ; or DO NOT ; take place* (238). RECAPITULATION.

That *this effect, always increases as twice the recoil* (238).

* As represented in Plate 3. Fig 2.

IMPROVEMENT OF

That *the friction and influences of the oil, do also increase (cæt. par.) as twice the recoil (178); and consequently,*

Compared with
the recoil.

That *it is advantageous in all cases to diminish the recoil as much as possible.*

That *the dead-beat diminishes the alteration that would naturally happen in the time of Vibration of a detached Pendulum, from any change in the length of such Vibration (262).*

That *the influence of the oil and friction, is always less on the dead-beat, than on the recoil; all other circumstances being alike (181).*

That *the recoil can have no tendency to keep the Vibrations of more equal length (237). Therefore,*

That *in all cases whatsoever, the DEAD-BEAT is preferable to the RECOIL; And that*

The use of springs in pallets, tend to vary the maintaining power (246); and also, have the effect of a RECOIL (247); and therefore, never to be admitted.

275. Having thus shewn; that *the dead-beat diminishes the natural effect of any change in the length of Vibration; when neither friction, nor the influence of oil take place during the time of rest: I now come to shew the manner of constructing pallets, wherein the PRACTICE will agree with the THEORY: and as a superficial view of those matters, may leave some doubt, whether a diminution of friction on the pallets, may not be*
hurtful

hurtful to the performance: that matter shall be considered in the notes*.

PALLETS IMPROVED.

276. Plate 4. represents the construction of such pallets; Fig. 1. is a front view of the pallets and the *swing wheel*: the pallets A, B, C, have their planes of action, constructed as in common pallets: (See Plates 2d and 3d); they are screwed to a hollow brass cylinder O P, which serves as a *verge* or axis, and moves on two small pivots as common verges do: to one end of the cylinder, is screwed, the crutch F, Fig. 2. by means of which, the pallets A and C, communicate motion to the Pendulum.

New Pallets.

PLATE IV.
FIG. 2.

277. d d

* There are two means, by which the length of Vibration in Clocks may be altered, independent of the density of the air: and the effect which the friction on the pallets will have on the performance, will in some measure depend, on which cause, affects.

First, The length of Vibration may be altered in Clocks, by altering the weight that maintains the motion; and in this case, the friction (or total resistance) on the pallets, *c. p.* increases, as the angle of Vibration: on which account the length of Vibration, will not bear so great a proportion to the weight applied, as if no such friction took place. But admitting, that the friction, in such case, does diminish the effect of any alteration in the maintaining power: as an alteration of the above kind, can never happen by accident: and as every such increase of the maintaining power, must be made with intent to enlarge the Vibration, it follows: that the friction on the pallets must, in such case, be hurtful, as tending to diminish the *desired effect*.

Secondly, admitting the weight that is applied to a Clock, to remain invariably the same, its effect in lengthening the Vibration, will be increased or diminished according to the fluidity, &c. of the oil; which is constantly fluctuating, according to the de-

IMPROVEMENT OF

277. *dd* and *ee*, are detents, that move concentric to the brass cylinder, on small axles within the cavity thereof, (See Fig. 2.) and suspend the Wheel so as to allow the Pendulum to move without friction, or influence of the oil, on either pallets or pivots during the whole time of rest.

Their operation.

278. *Thus*; when the tooth *i*, escapes the pallet *A*, the tooth *k*, drops on the detent *e*, and is suspended,

gree of heat and cold to which it is exposed. And the effect of the oil applied to the pallets, in lengthening and shortening the Vibrations, has already been shewn to bear, to that, on all the pivots, at a mean; the proportion of 80, to 1, (176). Therefore it appears; that in this case, by removing the friction, and the influences of the oil on the pallets, we diminish the alterations that are so frequently occasioned in the length of Vibration, by the influences of heat and cold on the oil, to one eightieth of what they are, where friction takes place: and this becomes the more deserving of attention, that there seems no other means of removing this evil.

It is also to be remembered: that as this friction on the pallets diminishes the effect of the maintaining power, in enlarging the Vibration (whether long or short) it must, on that account also, be hurtful to the performance (41, 46, 47). Add to this; that it tends to correct such alterations, as happen in the length of Vibration, owing to the different densities of the air, more than it does those arising from any other cause whatever; and this is hurtful to the measure of time, as shall be shewn hereafter; when the different means, by which any alteration in the density of the air do affect the times of Vibration, are considered. From each, and all, of the above considerations it appears; That the friction on Clock-pallets can in no respect mend the performance of Clocks; but on the contrary, does by its unavoidable consequences, give rise to some of the greatest causes of error, that take place in Clocks; and those, incurable by any other means than the removal of such friction on the pallets (155).

suspended, while the pallet C, proceeds towards (n) the bottom of the tooth, and returns, (in the direction of the dotted Arc) ; joins itself to the *detent* ; displaces it ; *and thus* receives the tooth k on the plane of action ; and so, maintains the motion of the Pendulum ; and when the tooth k has escaped the pallet, C, the tooth m, will drop on the detent d, &c.

PALLETS IMPROVED.

279. Fig. 2. is a section of the hollow cylinder ; (along the line g h) and represents the pallets, crutch, and axles of the detents.

Sections, &c.

280. Fig. 3. a view of part of the cylinder, pallets, and detents (*in the direction of the line g h*, Fig. 1 and 2.) and shows how the detents are brought into the same plane of action with the pallets.

PLATE IV.

281. Fig. 4. shows how the planes of action A and C, are screwed to the pallets : the small hole in the stalk, serves to screw and unscrew them.

282. Fig. 5. represents part of a Wheel that will admit of Vibrations of any length.

283. Fig. 6. Section of ditto at the line, a b : N. B. *In all those figures, the same letters refer to the same pieces.*

284. The detents should be fitted very closely to the pallets, but *the contact should not be very extensive*, lest the effects of *cohesive attraction* become sensible ; And,

Attraction to be guarded against, &c.

285. The

IMPROVEMENT OF

285. The greatest care is to be taken, that neither detents nor pallets have any degree of *magnitism*. And

286. Thus may the friction and influences of the oil, during the time of rest of the swing wheel, be removed; *without any of the disadvantages that attend the application of springs**.

287. But though *this construction of pallets*, does *much enlarge the Vibration*, and diminish, the natural effect, which any alteration in the length of Vibration would have on the measure of time in a detached Pendulum (263); as well as remove $\frac{3}{4}$ of the influence of the oil on the Clock (174); *it cannot be said totally* to remove, the effect of every imperfection of the movement. Therefore,

288. I shall next describe *a construction of pallets*, that not only removes the friction and influences of the oil, during the time of rest; but also during the motion, of the swing wheel; *so far as they can any how influence the Vibrations*

More perfect pallets proposed.

* Such pallets I finished in the year 1763, for a Clock which I had the honour of making for the KING; for journalizing all the changes that happen in the height of the Mercury in the Barometer. Which it does in such manner, that a person who has not seen a Barometer for the whole year, may by inspecting its Dial, know with the greatest ease and certainty, not only what changes have happened in any particular day of that year; but also, every one change that exceeds the 100 of an inch, which happens in the whole year; with the day and hour, as well as, the particular manner in which each, did happen.

of the Pendulum : these pallets, do also correct all the irregularities of action in *the main spring*, wheels and pinions ; or any other irregularity that can possibly happen in the movement, from any cause whatever : though the causes of such irregularities should altogether escape the attention of the artificer.

PALLETS IM-
PROVED.

289. Plate 5. represents such a pair of pallets, and the swing wheel ; where,

A, B, C, is the wheel,

D E, the pallets,

H I, two small weights that are fixed on the same axles with the pallets, one to each ;

F G, the detents, which are firmly attached to each other, as well as to the crutch ; by means of,

P P, a hollow cylinder of brass, which serves as an axis to the detents ; and to which they are screwed : as well as ; L, the crutch, which only serves to unlock the detents.

M, a weight that exactly ballances the detents, and crutch, by means of which, they retain any position that is given them ; n, o, are pins attached to the *Pendulum*, (See Plate 7.) and by means of which, the balls I and H, do by their gravity, maintain *its* motion.

290. Plate 6. Fig. 1. represents these pallets &c. in the direction of M L : and also answers to the above description.

Fig. 2.

Fig. 2. a section of the hollow cylinder P P, at right angles to its axis ; representing the front of the collar to which the detents, or crutch, are screwed.

291. All the other figures of this Plate, represent separately, the pieces belonging to those pallets ; and are lettered the same, as in the foregoing description ; except W W the axles of the pallets ; And

292. Z, a section of those pieces that are fitted into the ends of the brass cylinder, and in which the pivots of the axles W W move ; the small hole that is next the pivot serves occasionally to take this piece, out of the cylinder (into which it must be very truly fitted ;) the other two holes are for pinning it, in its place ; the small pieces D, F, G, E, (under Fig. 2. Plate 6.) are side views of the lower ends of the pallets and detents that are marked with the same letters.

293. Plate 7. Fig. 1. is a front view, of the wheel, pallets, detents, and upper parts of the Pendulum ; the parts of which that have been described in the former Plates, are here marked with the same letters, nor do the pallets represented in this Plate, differ from those in Plates 5 and 6. in any other respect, than that in those, the pallets are placed over the wheel ; and in these under it.

294. Fig. 2. Plate 7. is a side view of Fig. 1. where, V's, represent part of the Clock-frame, S's

upper part of the Pendulum ; to the lower end of which, the other part is attached by means of a screw, in such manner that each of the springs T T, shall bear half its weight.—Q, R, are two screws that move with the Pendulum, and by means of which, the detents F and G are alternately unlocked when the Pendulum comes to the extremity of its Vibration.

PALLETS IMPROVED.

The Operation of those Pallets.

295. Let us first conceive the Pendulum at rest ; and that the pallets, detents, crutch, and pins n, o, remain in the positions in which they are represented in Plates 5. and 7.

296. If the Pendulum be moved towards the detent F, Plate 7. the pin, n, will rise towards the arm that supports the little weight H ; and the screw R, must be so adjusted, that it will unlock the detent F ; and allow the Wheel to advance at the same instant that the pin, n, feels the weight H : in which case, the pallet D, will be disengaged from the tooth A, and the weight H allowed to descend with, and press upon the pin, n ; and by this means, maintain the motion of the Pendulum.

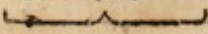
Their operation.

297. No sooner does the Pendulum begin its motion toward F, than the pin, o, is relieved from the weight I ; for the pallet E, rests against the tooth, C, and prevents the further descent of I ;

M

and

PALLETS IM-
PROVED.



and thus, the action of the pallet E on the *wheel*, diminishes *its* pressure on the detent F, so as to allow it *unlock with the greater ease*, which done; the *wheel* advances, and by *its* action on the pallet E, continues to raise the weight I till the detent G stops *its* motion.

PLATE VII.

298. And, when the tooth C, comes to rest on the detent G, the weight I, will remain *at rest* till the Pendulum comes to the extremity of its Vibration towards G; when the pin o, will feel the weight I, and the screw Q unlock the detent G, and allow the small weight I, to descend with, and press upon the pin o, and by that means, promote the descent of the Pendulum; mean time that the wheel raises the weight H, for promoting the following descent.

Motion maintain'd
by the natural ac-
tion of gravity.

299. Thus are the Vibrations of the Pendulum constantly maintained, by the alternate descent of the little weights H and I; and *since those weights, begin each descent from absolute rest* (298); it follows; that the power, or velocity with which they are raised, *can by no means influence the effect of their descent*; And therefore,

No irregularity of
action in the
movement can
influence the
Pendulum.

300. However great the irregularities of action, *in the main spring, wheels and pinions, &c. whether arising from the influences of heat and cold on the metals, oil, or friction, &c.* if there remain power, sufficient to raise the weights H and I; *the maintaining power of the Pendulum, will be as invariable as the natural action of gravity:*

vity : and by that means, all the effects of any imperfection in the movement, of whatever kind, are totally avoided *.

PALLETS IMPROVED.

301. Nor does any part of the construction of those pallets tend to diminish the advantages thus acquired ; *which must be the case wherever springs are used* (274).

The practice equals the theory.

302. Though I have hitherto represented the weights H and I, as small balls supported by slender arms ; I here take notice, that they should be made of bars of steel, of the same shape and dimensions with the Pendulum rod ; that heat, and cold, may equally affect them, and that the same provision may remove their influence in both.

Observation relative to the small weights.

303. The only article that seems wanting of *Mathematical accuracy* in those pallets, is, that any change in the action of the wheels may tend to alter the friction on the detents ; but if the same precautions are here used, as in common Clocks, having pinions of eight ; and the face of the detents be made of hardened steel or dia-

The only imperfection, in those pallets, can have no sensible effect on the measure of time.

* Since the Arc of Vibration increases, till the resistance of the medium is in each Vibration equal to the maintaining power (259) : it follows ; that *with an uniform maintaining power*, Vibrations performed in a medium of uniform density, would be invariably of the same length ; in a medium of fluctuating density, the lengths of the Vibration bear an inverse proportion to such density : and that, *in either case* ; the *total resistance* of the medium to the Pendulum will remain uniformly the same.

mond, and the teeth of the wheel of tempered steel ; any effect that can arise from this cause, can by no means become perceptible either in the length of Vibration, or measure of time (297). But,

304. I avoid saying too much in defence of an article that *candour will scarce call in question* ; and despise the attacks of prejudice, where I have it in my power to give experimental proof of my assertions * : but he who produces a more perfect construction of pallets, is fully intitled to find fault with this ; nor shall I be backward in making my publick acknowledgments to him who at once points out *the disease and its cure*, in any part of this theory.

Farther use of this
construction.

305. It is further to be observed, that by means of the screws Q and R, the alterations that any change in the density of the air will

* It is extremely easy to know the effect that any accidental alteration in the action of the wheels, could have on the measure of time ; with such pallets : for if the maintaining power be designedly altered $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{6}$, or $\frac{1}{10}$, such *alteration* will produce the same effect, as if it had been accidental ; and as it may be continued for any given time, and its whole effect be accurately observed, we may with great certainty from such effect (if it becomes sensible) estimate the effects of such smaller changes as may probably happen in the pressure of the wheel on the detents, by the influences of the oil on the pivots.—The resistance which such friction makes to the Pendulum, in unlocking the detents, may be reduced to any degree at pleasure, by rendering the ball M so much lighter than the crutch and detents, that their excess of weight may be made to co-operate, in any degree with the Pendulum, in unlocking the Wheel.

produce in the length of Vibration may be accurately ascertained.

PALLETS IMPROVED.

306. I make no farther attempt to improve the theory of CLOCK-MOVEMENTS; but now proceed to enquire *how far the advantages already acquired may yet be lost*; and *what are the most effectual means of preserving them*.

307. THE THREE FOLLOWING causes may yet tend to alter the true times of Vibration in Clock-pendulums.

First, *Any change in the elasticity, or weight of the body to which the Pendulum is suspended*.

Secondly, *The influences of heat and cold on the Pendulum-rod*. And,

Thirdly, *Any alteration in the action of gravity*.

308. As those causes tend to alter the times of Vibration, independent of any imperfection in the movement; they shall be considered separately, *and in the above order*.

309. When the CENTER OF MOTION, OR POINT of SUSPENSION of a Pendulum, is considered as a fixed point; *its center of gravity will describe a true Arc of a circle, whose radius is, the distance of the center of gravity from the point of suspension*.

310. But if the point of suspension be any how at liberty to change its place, the times of Vibration will thereby be altered.

311. Example.

OF THE SUS-
PENSION, &c.

PLATE VIII.

311. Example. PLATE VIII. If a pendulous body B, vibrate round an *immoveable point* A, its center of gravity will describe a *perfect Arc of a circle* as B B B, whose radius is A B; but if the point of suspension moves at each Vibration, suppose from A, to a, on either side; the center of gravity will describe a different curve, as C B C, which may here, for the sake of illustration, be considered as a true circular Arc: let the center of this Arc be found *thus*; round the point B describe any circle, and also round the points C, C, describe Arcs cutting the said circle any where, as at the pivots e, e, e, e, and, through those points of intersection, draw lines towards A, and they will pass through the points a, a, and meet in D, which will be the center of the Arc C B C; and consequently the times of Vibration in the Arc C B C, will be the same, as if D B, was the length of the Pendulum, and the point of suspension immoveable.

Motion of it,
worse than a
change of length
of the Pendulum.

312. And *thus it appears*, that any motion of the point of suspension, will alter the times of Vibration, *more than* an equal change in the length of the Pendulum would do; *in the proportion of* A D, to a a.

Wood; why im-
proper for it.

313. All sorts of wood attract and imbibe moisture, and by this means alter their degree of elasticity; and consequently, if a Pendulum be

be suspended thereto, the motion of its point of suspension, will vary with the elasticity of the wood; and the times of Vibration will also be altered (312); and this effect, will always be considerable in the measure of time, wherever the Pendulum is suspended in the common manner, or is any how dependent on the *case*; for *its* elasticity is liable to change by every change in the moisture, &c. of the air. OF THE SUSPENSION, &c.

314. The changes that happen in the weight of the case, will also concur with the former, in altering the times of Vibration: for it is certain, that in most Clocks, the case, &c. are moved by the Pendulum at each Vibration; and it is no less certain, that the same power will move a lighter body (*cæt. par.*) further than a heavier; therefore, the heavier the *Clock-case*, the shorter space will the Pendulum move it; and thus, will any change in the weight, as well as elasticity of the case, alter the motion of the point of suspension, and consequently the times of Vibration (312)*. Further reasons.

* Were it necessary to satisfy the reader, that the case and Clock are generally moved by the Vibrations of the Pendulum, I would recommend to him the use of a small pamphlet, by Mr. John Ellicott, intituled; An account of the influence, which two Pendulum Clocks were observed to have upon each other, &c. And of Hugen's Horologium Osc. pages 18 & 19. in each of which he will meet with incontestible proofs, that the point of suspension is not fixed, but moves with the Pendulum.

OF THE SUS-
PENSION, &c.

Brick and free-
stone, liable to
some objections.

Lead, or marble
best.

PENDULUM
RODS.

Wooden Pendu-
lum rods.

315. What is above said of wood, is applicable in a less degree to brick, freestone, or any substance that imbibes moisture: and for this reason; LEAD, and MARBLE *seem the fittest substances for suspending Clock-pendulums to*: and to render such suspension perfect; a block of either, of at least 4 or 500 weight, should be built as compactly as possible in a wall, and the Pendulum suspended near its middle; for by this means, the point of suspension would be rendered much more immoveable, and the times of Vibration *more isochronal* (312).

The influences of HEAT and COLD on the PENDULUM ROD comes next in course (308).

319. In all that has been hitherto said, the length of the Pendulum has been considered as invariably the same, *but the contrary happens in practice*: for *heat dilates, and cold contracts* all metals; by which means, *the same Pendulum is longer in summer than in winter*.

317. Various expedients have been thought of for correcting this imperfection; all of which that occur to me, *except one*, depend on the opposition of expansion, to expansion; in such manner, that the one should shorten the Pendulum as much as the other lengthened it: and the contrary.

318. The *only method* that does not depend upon the above principle, is by making the Pendulum rod of the straightest grained wood; *the longitudinal*

*longitudinal expansion of which is so very small, that it answers sufficiently for ordinary purposes, and is equal to any other, in Clocks wherein the influences of the oil take place on the pallets (193, 195) *.*

INFLUENCE OF
HEAT AND COLD
ON THE PENDU-
LUM ROD.

319. All the ways that have been, or can be used, *for applying the expansion of metals*, may be reduced to two general CLASSES; namely,

Thermometers all
reducible to two
CLASSES.

320. Such as DO; OR DO NOT; *move with the Pendulum.* Namely,

321. Those that *do not* move with the Pendulum, are either attached to the frame, or case of the Clock; and so construed as to raise the Pendulum-spring betwixt two cheeks just as much as the whole rod is lengthened; and the contrary; by which means, the distance of those

Of those that do
not move, &c.

* If I was to adopt any principle or contrivance, on the reputation of its inventor, it would be this; it being invented, and often applied with good success, by my late Noble Patron ARCHIBALD DUKE OF ARGYLL, whose superior abilities and penetration, might with many, justify a conduct in direct opposition to those rules which HE constantly observed in philosophical enquiries: and if the fullest conviction of His abilities; joined to the most grateful sense of that goodness, to which, (under Providence) I may justly be said, in the first place, to owe every blessing which I do, or can enjoy; are not arguments sufficient, for adopting without further inquiry or experiment, a contrivance worthy of the greatest philosopher of his age: surely none other have reason to imagine that any indignity is meant, when the merits of their inventions are minutely examined.

INFLUENCE OF
HEAT AND COLD

Inconvenience.

cheeks from the center of oscillation, is always preserved the same.

322. Here it is to be observed, that as the spring is to move freely up and down, between those cheeks, it is apt to have some shake in its Vibration, which is no desirable circumstance where great accuracy is required.

Ditto.

323. Secondly, That every change in the temperature of the air, that influences this Thermometer; also alters the length of that part of the Pendulum-spring that acts in the Vibration: consequently its stiffness will be altered, which will vary the time of Vibration (137).

Ditto.

324. Thirdly, Since this Thermometer remains in its place *without motion*, any change that happens in the temperature of the air, will not affect it, *so soon* as the Pendulum rod; which is in constant motion, and by that means, making continual approaches to particles of air, whose temperature have undergone no change from their former propinquity to it; or if they have, again recover the same temperature, before the return of the Pendulum rod: *and thus it appears,*

Immoveable thermometers too slow in their effect.

325. That *any Thermometer that is immoveable, can never be so soon influenced by the changes of heat and cold, as the Pendulum rod*: and therefore the evil must take place for some time, before the remedy is applied; this is universally true of all the Thermometers *of this class* (321).

326. *How*

326. *How different is the case in the MERCURIAL PENDULUM?* for as the *cylinder of Mercury* moves quicker through the air, than the *mean motion* of the Pendulum rod, *IT will be sooner heated and cooled* by the air, *than the Pendulum rod*; and if we add to this, that no body in nature of the same density is sooner heated and cooled than Mercury; it will appear that this Mercurial Thermometer, is as much too quick, as the other is too slow: and consequently,

ON THE PENDULUM ROD.

Mercurial Pendulums too quick, &c.

327. That *neither the Mercurial Pendulum, (326) nor any Thermometer that does not move with the Pendulum (325),* can have a perfect effect.

And neither, can ever be rendered perfect.

328. *From what has been said* it appears, that in order to make a Thermometer perform properly, it should be made of the same metal with the Pendulum rod (326).

Properties necessary to all thermometers.

329. *Secondly,* It should consist of bars of the same exact dimensions with the Pendulum rod; and each of its parts, should in every respect have the same exposure to the air with the corresponding part of the Pendulum rod.

Ditto.

330. *And lastly,* Each part of the Thermometer should be extended, or compressed, with the very same degree of power with which the corresponding part of the Pendulum rod is extended or compressed: *nor can any Thermometer ever perform to the utmost exactness of which their nature admits,* without very particular re-

Ditto.

INFLUENCE OF
HEAT AND COLD

The gridiron and
Mr. Ellicott's best,
on those accounts.

gard is paid to each of the above articles, (328 to 331).

331. *The GRIDIRON Pendulum*, and Mr. EL-
LICOTT's, correspond with those particulars more
fully, than any other construction with which I
have met; *on which account*, I shall attempt a
more particular examination of them; and to
the best of my judgment, point out the advan-
tages and imperfections of each: so far as it can
tend to improvement.

Of the Gridiron Pendulum *.

Its general prin-
ciples.

332. The expansion of brass, is always al-
lowed to exceed that of steel, generally in the
proportion of 5 to 3; on which supposition, if
any piece of steel by the application of a certain
degree of heat, expands $\frac{3}{10}$ of an inch: a piece of
brass of the same length will, with the same heat,
expand $\frac{5}{10}$ of an inch; and, since the whole
length of brass expands $\frac{5}{10}$ and the expansion
through the whole is supposed uniform; if it be
divided into five equal parts, each part, will have

* It may seem unnecessary here to say, that Mr. John
Harrison is generally reputed the inventor of this ingenious con-
trivance; and that, if Mr. Ellicott's name is oftener mentioned,
in describing the following invention, than Mr. Harrison's, in
this; it proceeds from no partiality: but because Mr. Elli-
cott's invention is known only by his name.

expanded

expanded $\frac{1}{10}$ of an inch; therefore if we take away $\frac{2}{5}$ of its whole length, the expansion of the remaining $\frac{3}{5}$ will be $\frac{3}{10}$ of an inch: but the expansion of the whole bar of steel, is also $\frac{3}{10}$ of an inch (by the hypothesis), *therefore*, the expansion of a bar of steel, is equal to the expansion of a bar of brass of $\frac{3}{5}$ its length. *And universally,*

ON THE PENDULUM ROD.

— V —

Proportion of the brass and steel wires.

333. When the length of the bars, is *inversely* as the expansion of the relative metals; the whole expansion in each bar, will be equal: and consequently may be applied to ballance each other; this being the foundation of the *gridiron*. I now come to *the application*

334. Let A B Fig. 1. Plate 9. represent the length of any given Pendulum to which a *gridiron* is to be applied; bisect A B, in C, and make B D, D E and E F, each equal to A C or C B, then, A F, will be to B F, (that is, H G,) as 5 to 3; therefore (332) if A F be steel, and H G, brass, their expansions and contractions with any degree of heat and cold will be equal: and if G H, be firmly attached to A F at their extremity F G; and A F be suspended by the point A; A F, will expand upwards, as much as G H, does downwards; and the points A and H will always keep the same distance from each other; *consequently*;

PLATE IX.
FIG. 1.

335. *If*

IMPROVEMENT OF

335. *If a Pendulum be constructed whose point of suspension is A, and its center of oscillation H, it can neither be lengthened nor shortened, by any change of heat and cold; And, thus*

The bars may be cut into any convenient lengths.

336. It appears (334), that whatever be the length of a Pendulum; three half lengths of steel, and as much of brass, must be added, in order to have as much expansion upwards as downwards: *and when the whole length of bars is thus ascertained, they may be cut into such several lengths as may best suit the purpose, and evade the inconveniencies of having any part of them below the ball of the Pendulum* *:

The brass to expand upwards, &c.

337. Always observing, *that the expansion of the steel tend downwards, and that of the brass upwards; in which case, they will ballance each other, without regard to the number of pieces into which they are cut; for the effect of the whole, consists of the effects of all its parts: Therefore,*

PLATE IX.
Illustration,

338. If the steel bar A F, Plate IX. Fig. 1. be cut into three unequal lengths, and the brass

* Here it is to be observed, that the screw by which the length of the Pendulum is adjusted; should act as near as possible to the center of *gravity* of the ball: by which means any expansion of the ball can no ways alter the distance of the center of oscillation from the point of suspension: and this may be effected by means of a long socket attached to the nut at the bottom of the Pendulum, and passing up through the ball, to its center of gravity; WHERE, it must act on the screw, and support the ball.

bar

bar H G into two; and those five pieces be applied and connected with each other, as in Fig. 2. *the brads will expand upwards* as much as *the steel does downwards*, and the center of oscillation B, always keep the same distance from A, the point of suspension; nor will the expansion of the little cross pieces that connect the bars, be of any effect, it acting laterally only.

ON THE PENDU-
LUM ROD.

339. *Though in theory five bars only*, are necessary for constructing a gridiron (338); *nine are requisite in practice*; in order that the bar to which the Pendulum is immediately suspended, be equally supported on each side: to prevent such tremulous motion or bending of the bars, as might otherwise take place; See Fig. 3. where it appears by inspection that the corresponding bars on either sides the center, co-operate in such manner, as to move both ends of the cross bars equally, and by that means, prevent such bending of the upright ones, as must otherwise happen by the weight of the ball B; nor do those additional bars, *thus applied*, any how increase the expansion.

Why more wires
necessary in prac-
tice than in theory.

PLATE IX.

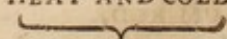
340. Fig. 4. represents the manner of connecting the bars in a *gridiron*; and is drawn of the size commonly used for royal Pendulums; the bars could not be represented here at full length, and are therefore broke in the middle; the letters with which the round bars are marked serve to denote the metal of which each is made;

Drawing at full
size.

I

and

INFLUENCE OF
HEAT AND COLD



and that part of the middle rod which is above the piece E, serves only for keeping the three bars on each side thereof, in the same plane with the two outside ones ; it also answers a like purpose at the lower end of the gridiron, *and is pin'd in the cross piece E, only ; and moves freely, but without shake, in the pieces C, D, F and G.*

Two springs best.

341. I have always preferred the suspension by two springs, to that with one ; and have here represented, *the piece to which the springs are attached, together with the piece C, to which it is screwed, in several different views ; all the other cross pieces, are also represented separately, and marked with the same letters as in the Pendulum.*

Cross bars.

342. The upright bars, or wires, are generally connected towards the middle by one or more cross pieces, that serve still further to prevent any tremulation that might arise from their elastic flexibility ; those pieces are pin'd to the two extreme bars, and allow the other seven to move freely, yet without shake, in their holes.

How the gridiron
is adjusted.

343. In all that has been hitherto said, *the expansion of brass has been supposed to bear to that of steel, the exact proportion of five to three ; and that all dimensions have been accurately laid down agreeable thereto ; but, left on trial, the contrary should appear, the gridiron may be adjusted, by shifting the cross piece F, upwards or downwards, for which purpose, several holes*
are

are made in the upright rod, that correspond exactly with those in the piece F. See Fig. 4.

344. It is further to be observed in constructing gridirons; *that round wires* are much preferable to square bars, *even in theory*, and independent of all practical advantages; as there is a more *equal* and *free* admission of air to each wire; in order to promote which, *the wires should never stand close to each other*; and thus it appears:

345. THAT gridirons composed of square bars, closely fitted to each other, do in some degree partake of the inconvenience of immoveable Thermometers (325); though not to such a degree, as where hollow cylinders are used.

I NOW COME to the theory of Mr. ELLICOTT'S PENDULUM, *the description, &c. of which are here given in his own words.*

346. "Plate 10. Fig. 1. represents the Pendulum: in which a b, is a bar of brass made quite fast at the upper end by pins, and held contiguous at several equal distances, by the screws 1, 2, &c. to the rod of the Pendulum, which is a bar of iron; and so far as the brass bar reaches, is filed of the same size and shape, and consequently does not appear in the figure; but a little below the end of the brass bar, the iron is left broader, as at d d, for the convenience of fixing the work to it, and is made of a sufficient length

ON THE PENDULUM ROD.

Round wires better than square, even in theory.

And hollow cylinders, worse than square bars.

Mr. Ellicott's Pendulum described.

PLATE X.
FIG. 1.

INFLUENCE OF
HEAT AND COLDMr. Ellicott's Pen-
dulum described.

length to pass quite through the ball of the Pendulum to c. The holes 1, 2, &c. in the brass, through which the shanks of the screws pass into the iron rod of the Pendulum, are filed as in the drawing, of a sufficient length to suffer the brass to contract and dilate freely by heat and cold, under the heads of the screws; e e e e, represent the ball of the Pendulum; f f, two strong pieces of steel, or levers, whose inner centers, or pivots, turn in two holes drilled in the broad part of the Pendulum rod, and their outer ones in a strong bridge, or cock, screwed upon the same part of the rod, but omitted in the draught, because when put on, it covers this mechanism; g g are two screws entering at the edge, and reaching into the cavity near the center of the ball. The ends of the screws next the center, are turned into the form represented in the drawing, which, pressing with the weight of the ball against the longer arms of the levers, cause the short ends to press against the brass bar at b. Things being in this situation, let us suppose, that the rod of the Pendulum, and the brass annexed to it, grow longer by heat, and that the brass lengthens more than the iron of the same length; then the brass by its excess of dilation, will press the short ends of the levers downwards at b, and at the same time necessarily lift up the ball, which rests on the long ends of the same levers at f f, to any proportion necessary: and provided

provided the ends of the screws do press upon the levers at a proper distance from the centers, the said ball will be always kept at the same distance from the point of suspension, notwithstanding any alteration the rod of the Pendulum may be liable to from heat or cold. What this distance ought to be, may very nearly be determined, if the difference of expansion between the iron and brass bars is known; for the proportion the shorter arms of the levers ought to bear to the longer ones, will always be as the excess of expansion of the brass is to the whole expansion of the iron, as may be thus easily demonstrated."

Plate 10. Fig. 2. "Let the line a b, drawn perpendicular to the line e f, represent a bar of iron; the line e d, a bar of brass; the pricked line b g, the expansion of the iron bar by any particular degree of heat; the pricked line d h, the expansion of the brass bar by the same degree of heat; let the line g i, be drawn parallel to the line e f; then will i h, represent the difference of the expansion of the two metals: through the points h, g, draw a right line cutting the line e f, as in k; this line may be supposed to represent one of the levers turning upon its center at g; h the point where the brass bar acts on the shorter end of the lever, and k, the point where the screw acts upon the longer end of the lever, which being the place where it intersects the line e f, it is evident the ball of the

ON THE PENDU-
LUM ROD.

Mr. Ellicott's Pen-
dulum described.

PLATE X.
FIG. 2.

INFLUENCE OF
HEAT AND COLD

Mr. Ellicott's Pen-
dulum described.

Pendulum will be as much raised by the lever, as it would have been depressed by the expansion of the iron; but the triangle $i h g$, is similar to the triangle $b g k$; and therefore, as $i h$, the excess of the expansion of the brass, is to $b g$, the whole expansion of the iron, so will $h g$, the shorter arm of the lever, be to $g k$, the longer arm of the lever, Q. e. d."

PLATE X.

"At c , Fig. 1. is placed a strong double spring, whose ends pressing against the under edge of the ball, hinder it from bending the brass bar by its forcible motion thereon, at the point b , which, when the ball is of a considerable weight it might otherwise be very liable to do. The description here given is exactly agreeable to the original contrivance: and the only alteration I have since made in it, consists in placing the screws $g g$, within the ball of the Pendulum."

Characteristick of
true demonstra-
tions.

347. *I shall not attempt any further explanation of the above contrivance, which its author has described in a very clear and distinct manner; nor does any error appear to me in his demonstration, if the suppositions on which it is partly founded are allowed; but it is necessary, not only, that all mathematical demonstrations, be founded on data that are strictly true; but also, that they comprehend every circumstance that can any how affect the result; in which case only, the theory and practice can agree.*

348. It

348. It is obvious, that the above demonstration *supposes the Pendulum rod perfectly inflexible, and that all the parts move without friction*; in which case, the operation must be perfectly smooth and uniform: *But*

ON THE PENDU-
LUM ROD.

Mr. Ellicott's Pen-
dulum examined.

349. If the Pendulum rod be in any degree flexible, and friction take place in any part of the contrivance, the operation cannot be perfectly smooth, and the irregularity of the motion, will increase with the friction and flexibility of the rod. Example,

Objection.

350. If two rods of different metals be firmly attached to each other at one end, but at liberty to move freely and without resistance on each other, *towards the other end*, they will expand and contract uniformly and without the least tendency to bend: as in Plate II. Fig. 1.

Illustration.

351. But if those rods be connected with each other, *not only at their extremities*, but also *at several intermediate spaces*; and have different expansions, they will form themselves into a circular Arc, as in Fig. 2. Plate II: and the resistance which those elastic rods make to the bending, *increases as the spaces to which they are bent*. Therefore,

PLATE XI.
FIG. 1.

352. If such rods be firmly attached to each other, *at one end only*; and *by a limited power at the other*; they will, on any change of heat or cold, continue to bend, till the stiffness of the rods (351) does somewhat exceed the uniform limited power

INFLUENCE OF
HEAT AND COLD

Mr. Ellicott's Pen-
dulum examined.

power with which they are connected; at which period, the rods will suddenly slip on each other and become straight; this limited power being no longer able to ballance the resistance of the rods: and *thus will they bend*, and *move* alternately, by means of the changes of heat or cold; and the spaces to which they bend, will always depend on the proportion which the limited power that connects the *rods*, bears to *their* stiffness.

PLATE XI.

Jerks rendered
more minute and
frequent.

353. Let two such rods be suspended, at one end, and a weight applied to the other, as in Fig. 3. Plate II. And *this weight, as well as the stiffness of the rods*, will tend to oppose *their* bending, and the opposition which it makes, *increases as the versed sine of the Arc into which the rods or bars are bent* (See the dotted lines in the Fig.) and the application of this weight will render the bendings *less*, and *more frequent*; so as more nearly to approach an uniform motion.

Application of the
preceding theory.

354. Now if we consider *the friction on all the parts* of such a Pendulum as represented in Plate 10. as a limited power, that connects the lower ends of the brass and steel bars; (for they can have no relative motion till this friction is overcome) the bending of the rods will (*cæt. par.*) be proportioned to it (352, 353); so *that by diminishing the friction, the motion is rendered more uniform*; of which, the ingenious inventor, was

Double spring
applied,

so well aware, that he judiciously applied the double spring below the ball.

ON THE PENDU-
LUM ROD.

355. But this spring *must not sustain the whole weight of the ball*; and therefore, though the friction may be very much diminished, it can never be totally removed by the application of a spring; nor can we be absolutely certain that the screws g g, Plate 10. Fig. 1. bear equally on the levers; if they do not, it must incline the ball to one side, so as to rub at the upper *part*, against the bars; which will generate a friction of such a nature as must ever be attended with jerks*.

Mr. Ellicott's Pendulum examined.

Friction cannot be wholly removed by the application of a spring.

356. Since the friction on the levers is at least *nearly uniform*, and the resistance, which the weight, and stiffness of the rods make to the bending, is of an *accumulating nature* (352, 353); it follows, that when the rods are straight,

* In some cases, friction generates friction; as when a wetted finger is moved forward along a smooth table, as represented in PLATE X. Fig. 3. it will always move by jerks; but if moved backwards, it slips smoothly: the case will be somewhat similar here, if the levers should not bear an equal pressure from the screws that support the ball.—In a Pendulum which I have now making, with the improvements here proposed; the spring which sustains the ball, is made of a helical form (like these in small portable still-yards,) so that it moves with the greatest freedom, and by means of a screw at the bottom of the ball, (within which, is the spring): its action may be increased or diminished at pleasure, so that the levers shall sustain any assigned part of the weight. In it, I have also somewhat altered the manner of adjusting the levers from that in Mr. Ellicott's; by which means, the length of the Pendulum is less liable to be altered, by such adjustment.

the

INFLUENCE OF
HEAT AND COLD

Mr. Ellicott's Pen-
dulum examined.

Jerks must take
place while fric-
tion remains.

Proposal for reme-
dying the fore-
going inconve-
niences, &c.

the resistance to the bending totally ceases; nor can it be supposed to take place, before the rods are somewhat bent; *nor will the bending cease, till this resistance is so much increased, as to exceed the friction* (354); consequently while there is a friction, there must be a bending, and this bending must produce an irregularity in the motion; which, however small, or imperceptible, it may be to our sight, in any experiment, must still render the effect less perfect, than if the motion was more uniform; *and therefore*, such a construction as does not admit of a probability of such irregularity of motion is certainly to be preferred*.

357. Having endeavoured to point out the chief inconveniences, that *I imagine* Mr. ELLICOTT's *Pendulum* in its present state liable to; I shall next endeavour to obviate *them*, or any others that occur to me, so as to give it all those advantages of which the construction seems *peculiarly susceptible*: nor have I the least doubt of meeting with His approbation, if I

* It is probable that any improvement of Mr. Ellicott's Pendulum beyond its present state, might answer no great end in improving the performance, while the influences of the oil, or any other imperfections of the movement, can tend to disturb the natural tendency of the Vibration: but when all those evils are removed, these merit attention; and the effect of removing them will, I doubt not, then become sensible in the performance of the Clock.

succeed

succeed in the improvement of a contrivance which HE so candidly laid before the public; nor do I imagine *that malice itself, can construe this examination into a breach of friendship*, when it is declared that my approbation of the contrivance induced me to it: and if I spare not the inventions of those whom the public esteem; and I always wish to reckon among the number of my friends; *it proves, that I adhere to my resolution* of preferring demonstration to opinion; and that no disrespect is meant wherever the one is opposed to the other.

358. If three bars of metal (one of brass and two of steel) be firmly connected at one end, and held together by any determined power towards the other end; any increase of heat will expand the brass bar more than the steel ones; and if it were connected with one of the steel bars only, they would be bent, as in Fig. 2. Plate 11. but here, it being connected with a steel bar *on each side*, they endeavour, by means of the limited power which connects them, to bend it; *each operating its own way*, by which means they counteract and destroy each other's effect, so that no bending can *in this case* take place: but the least change in their expansions, will alter the relative positions at their extremities, and the motion will be uniform and regular, unless the resistance be so very great, as actually to compress or stretch the bars, which I am apt to believe,

ON THE PENDU-
LUM ROD.

Mr. Ellicott's Pendulum examined.

Three bars of metal applied, &c.

No bending.

INFLUENCE OF
HEAT AND COLD

Mr. Ellicott's Pendulum examined.

How the three bars are to be applied, &c.

lieve, can never be the case in a Pendulum that is executed with discretion. *Therefore,*

359. In *Pendulums with levers*, two bars of steel and one of brass should be used, as represented by Fig. 7. Plate 11. the screws that connect the *bars*, are made to allow the *one of brass*, to move freely between those of steel; and the rods are kept at a small distance from each other, so as to give *a free admission of the air to the brass bar*, that it may be heated and cooled *at the same instant* with the steel ones; which must have a more perfect effect, than where the brass is affected by its communication with the steel: nor is even this trifling circumstance unworthy of notice, when we recollect what is said in paragraph (248).

Further cautions.

360. From what is above said (358), it might at first sight be thought, that, with this addition, little or no regard needs be paid to the quantity of friction: or whether the levers bear an equal weight; but let it be observed, that though the bending of the bars, is by this means prevented in the direction wherein it naturally takes place in the highest degree, an unequal bearing on the levers would tend to bend the bars edgewise; and though such bending must be very trifling, even when compared with what has been heretofore considered, the effect cannot be hurt, and may be rendered more perfect, by removing as much as in our power, *even the probability* of any jerk or bending, however small.

361. Plate 11. Fig. 5. represents one of the steel bars with the *brass bar* and levers; on which *it* is made to act, (by means of the piece b,) *in such manner, that each shall have equal pressure*, notwithstanding any inaccuracies of execution, &c.

ON THE PENDU-
LUM ROD.

Mr. Ellicott's Pendulum improved.

362. N° 1. (under Fig 5. Plate 11.) represents the lower end of the brass bar, together with the cylinder c, and piece b, each separately; and N° 2, and 3. are different views of the levers.

Improvements.

363. Fig. 6. Plate 11. part of one of the steel bars, to be screwed to the bars Fig. 5. as represented by Fig. 7. the large opening in it, serves to shew, the ends of the levers with the piece b, &c. From what has been said, it appears, that Mr. ELLICOTT'S *Pendulum*, can no more be rendered perfect, *with two bars*, than *the gridiron can with five* (339); nor can the effect be perfect in any *Pendulum with levers*, where *each* does not bear an equal weight (360); and consequently, *any Pendulum constructed with one lever*, can never have a perfect effect.

Remark.

364. From what is above said it is not to be understood, that this *Pendulum* in its present state, is as imperfect as a gridiron of five bars (339), *though it does in a less degree, partake of the same inconveniency*: but when three bars are used, and the bearing on each lever, rendered equal;

In favour of Mr. Ellicott's Pendulum.

INFLUENCE OF
HEAT AND COLDOf Mr. Ellicott's
Pendulum.

the effect of Mr. *Ellicott's*, will in every respect equal that of the gridiron Pendulum; *with the superior advantage of being much more easily, and accurately adjusted*, than any gridiron Pendulum that I have seen; not to mention some smaller advantages (329).

Objection to it.

365. The objection that will most probably be yet made to Mr. *Ellicott's Pendulum*, is, that it is *regulated* by raising the Pendulum spring through a slit, &c. by which means the length of the spring is altered, in regulating the length of the Pendulum: but, though this is allowed to be an imperfection in the construction of *Clock-thermometers* (323), it is not of equal moment in this case; for when the Pendulum is once got to vibrate true time, *the length of its spring is no more altered*: besides it is easily to substitute other methods of regulating, that shall in no degree be liable to this objection.

Answered.

Further remarks.

366. As to the increase of resistance that may take place owing to the cavity in the ball; I shall endeavour to shew hereafter, how the resistance of the air may be diminished with this, and all other Pendulums, by altering the shape of their balls.

Objection to the
gridiron.

367. If in the gridiron Pendulum, the *ball* be supported by the lower edge, the whole expansion *thereof* will tend upwards; and its contraction, downwards; nor can the effects of heat or cold, on so thick a body, keep pace with those

those of the Pendulum rod ; therefore in this case the effect of a gridiron is less perfect than Mr. *Ellicott's* ; but this may be corrected by supporting the ball, by its center of gravity. ON THE WHOLE,

ON THE PENDU-
LUM ROD.

Of Mr. Ellicott's
Pendulum.

368. The only material difference that I can discover in the advantages of those ingenious contrivances, in their most improved state, is: *That Mr. ELLICOTT'S is by much the easiest adjusted ** ; and *that, when the air has free admission between its bars, they are more equally heated and cooled, than even those of the GRIDIRON ; in which, the bars at the extremities, are sooner affected by any changes in the temperature of the air, than those towards the middle : so that the effect must be most perfect where all the bars are most equally heated and cooled (329).*

Mr. Ellicott's easiest adjusted, and more perfect, in effect.

369. I shall now endeavour to bring into one point of view, the substance of what has been said relative to the influence of heat and cold on Pendulums.

That *wooden Pendulum rods may answer for Clocks wherein the influences of the oil take place on the pallets (318).*

RECAPITULATION.

* Mr. Ellicott's Pendulum may be adjusted to the greatest nicety, without stopping the Clock many seconds, or running so great a risque of altering the former length of the Pendulum, as in all the gridiron Pendulums I ever saw.

That,

That, before the influence of the oil is removed in Clocks, their performance may be hurt, by totally remedying the influences of heat and cold on the Pendulum, particularly with recoiling pallets (195, 196).

That, no Thermometer that remains immovable in its place, can perfectly remove the influence of heat and cold on the Pendulum rod (325).

That, the Mercurial Pendulum is too soon affected by the changes of heat and cold; and therefore can never have a perfect effect, in remedying their influences (326).

That, the GRIDIRON, and MR. ELLICOTT'S methods for removing the influences of heat and cold, are the best that have yet appeared (331).

That, no Pendulum can be constructed with one lever, so as to have a perfect effect (363).

That, the bars are more equally heated and cooled in MR. ELLICOTT'S than the GRIDIRON Pendulum (368).

And that, the former is much more easily adjusted than the LATTER (368).

Pendulum with
levers, preferable.

370. Which two last properties, do for general use give the preference to the construction with levers. If I have in this examination committed any oversight or error; the manner which has been observed through the whole, lays them open to the detection of those who reason with more propriety.

371. Some

371. Some may expect, that the method of determining when such Pendulums are accurately adjusted, should be here given; but where time admits, a due attention to the performance of the clock, is the best means, as it includes every circumstance that can affect.

ON THE PENDU-
LUM, &c.

372. As to the changes that may happen in the ACTION of GRAVITY (307); they only take place from a change of latitude, and must be corrected in the length of the Pendulum.

CHANGES IN
THE ACTION
OF GRAVITY.

373. Having shewn above, how to render the maintaining power *perfectly uniform* (300), the point of suspension *immoveable* (315), and the length of the Pendulum *invariable* (316 to 373); such changes as happen in the DENSITY of the air, seem now, the *only remaining cause*, that can alter the *length, or time* of Vibration.

Introduction to the
changes of density
in the air.

374. I therefore proceed to enquire into, the comparative effects that such changes may have on the times of Vibration performed in *cycloidal* and *circular* Arcs, when no other cause tends to alter their times.

Enquiry.

375. If a Pendulum was made to oscillate in an exhausted receiver, free from resistance of any kind, its Vibrations would continue *equal*, and *isochronal* (14), whether performed in the *cycloidal* or *circular* curve: And,

376. And if the action of gravity, on *such* Pendulum, was altered, so would its times of Vibration

Absolute gravity,
in what case the
motive force,

DENSITY OF
THE AIR.

Alteration in the action of gravity will not alter the length of Vibration.

Times inverſely as the motive force.

Comparative weight, the motive force.

In a non-reſiſting medium, cycloidal and circular Vibrations are on a level.

Not ſo in air.

bration (17); for in this caſe, the *absolute gravity of the Pendulum*, is its motive force.

377. Nor would any alteration in the action of gravity, alter the length of the Vibrations; for, *the oppoſition to its aſcent*, increaſes and diminifhes *as its power of deſcent*.

And, the velocity of ſuch Pendulum will be as its motive force; and *its times*, inverſely as the velocity; i. e. *inverſely as its motive force*.

378. But when a Pendulum vibrates in any heavy medium; its *comparative weight*, is the motive force; i. e. the weight of its bulk of the medium, being deducted from its *absolute weight*, *the remainder only*, is its motive force*. *Therefore*,

379. Any alteration in the density of the medium, will alter the *motive force* (378); and if ſuch *medium* be conſidered as *non-reſiſting*, it will not alter the *length of Vibration* (377); conſequently every alteration in its density, would by altering the motive force, cauſe equal alteration in the velocities and times, of ſuch Vibrations as were performed, in cycloidal or circular Arcs. *But*,

380. *Air*, being a reſiſting medium; *its reſiſtance* will increaſe. &c. *as its density*, as will the effect of ſuch reſiſtance, in deſtroying the

* See 6th Corol. Prop. 24. of Sir ISAAC NEWTON'S Princip. Math. Vol. 2.

*motion of the Pendulum ; and contracting its Arcs of Vibration : therefore, those alterations that happen in the resistance of the air (considered separately) do not affect the times **.

CYCLOIDAL AND
CIRCULAR VI-
BRATIONS COM-
PARED.

381. But, *the shorter Vibrations in circular Arcs are performed in less time than the longer (19) : therefore, any increase of resistance of the air, will, by contracting such Arcs, also shorten the times of Vibration : and this effect will always be, as such density of the air (300) †.*

The alteration in the length of Vibration, as that in the density of the air.

382. Now, since any increase of density in the air, will, *independent of its resistance, prolong the times of cycloidal, as well as circular Vibrations, in proportion to such increase of density (378) ; and as the resistance of the air is always as its density, and contracts the Arcs of Vibration in the same proportion ; it follows, that in circular Arcs the resistance of the air, contracts the times of Vibration (19), as much, as the diminution in the motive force of the Pendulum, from such change of density, prolongs them (378) : And the contrary.*

Circular Arcs correct the effects of such changes as happen in the density of the air.

* See notes (238, 19).

† The resistance of the air does somewhat more prolong the time of descent, than it contracts the time of ascent of a Pendulum ; and this difference will increase, or diminish, with the total resistance of the air in each Vibration : but the total resistance to Clock Pendulums, is as the maintaining power (300) ; therefore, the *former* will be uniform, when the *latter* is so ; and will in such case, *equally* affect the time of each Vibration ; which *uniform effect* is corrected in the length of the Pendulum.

All the times of
Vibration in
Clocks rendered
isochronal.

Circular Vibration
better than cy-
cloidal.

IMPROVEMENT OF

383. Hence, a Clock-pendulum, having its motion continued by a maintaining power *perfectly uniform* (300), and at *liberty to enlarge its Arc of Vibration*, in proportion to the *diminution of density* in the air; and the contrary; will have all its Vibrations in *circular Arcs*, isochronal (382); which *would not* happen in the cycloidal curve; in which, all the Vibrations of *whatever length*, are *isochronal in a medium of uniform density only*, (379, 380). And thus it appears, that in CLOCK-PENDULUMS, *Vibrations performed in the Arc of a circle are much superior*, to those performed *in the cycloid*, when the maintaining power is uniform, and the density of the medium fluctuating*.

CONCLUSION.

Having thus endeavoured to investigate separately, the effect of each cause, that I imagine can influence the performance of a Clock; and compared such effects, with their causes, in the present state of Clock-work: I am therefrom induced to expect so much amendment in the per-

* What is here objected to the cycloidal curve, is equally applicable to the friction on the pallets; the most perfect mode of a recoil, or any cause whatever, that has a tendency either to render the Vibrations of more equal length than is here proposed; or to accelerate the Vibrations more, in proportion to their length. And if the nature of pallets is not so fully considered in this Essay as the reader could wish, it will be further explained in the next.

formance, from the improvements already proposed, as will render any further enquiry into the nature of pendulous Vibrations, of no material service to *the immediate improvement* of Clock-work ; but if my leisure, was equal to my inclination of establishing a practical theory of Clock and Watch-work, and rendering it of general utility, I would not desist, before I had made such number of experiments, as would not only illustrate, but confirm, the truth of every improvement proposed in this Essay : but prudence forbids an attempt, that requires so much time, expence, and application.

End of the First Essay.

formance, from the improvements already proposed, as will render any further enquiry into the nature of pendulous Vibrations, of no material service to the immediate improvement of Clock-work; but if my leisure, was equal to my inclination of establishing a practical theory of Clock and Watch-work, and rendering it of general utility, I would not doubt, before I had made such number of experiments, as would not only illustrate, but confirm the truth of every improvement proposed in this Essay: but this design forbids an attempt, that requires so much time, expense, and application.

End of the First Essay.

A N

E S S A Y

TOWARDS THE

Improvement of WATCH-WORK.

A N

E S S A Y

TOWARDS THE

IMPROVEMENT OF WATCH-WORK

IMPROVEMENT OF WATCH-WORK.

THE PLAN.

384. **I**T BEING UNIVERSALLY ALLOWED, *that* WATCH-WORK.
Watches are as well executed as Clocks,
but measure time worse ; it naturally follows,
that the defect arises, more from the imperfec-
tions of principle, than execution. Errors arise from
principle, more
than execution.

385. I SHALL THEREFORE ENQUIRE,
Wherein do Watches differ from Clocks ? Enquiries.
What defect will arise from each difference ?
How ? and in what degree ? may those defects
be remedied ?

386. The articles wherein Watches differ from Watches differ
from Clocks.
Clocks are,

FIRST, That in Clocks ; the motion is ge-
nerally maintained by weight ; *but in Watches*
by springs.—

SECONDLY,

CLOCKS GO BY
WEIGHT,

SECONDLY, That in Clocks, the motion is regulated by a Pendulum; *but in Watches, by a Balance and spiral Spring.*—

THIRDLY, Clocks are not capable of beginning their own Vibrations; *but Watches are.*

FOURTHLY, Clocks are larger *than Watches.* And,

FIFTHLY, Clocks are fixed in their place; *but Watches are portable.*

387. The above five articles, being all that occur to me, wherein Watches differ from Clocks; I shall enquire into the effect of each article separately, and how it may be most effectually removed.

Clocks go by weight, &c.

First inconveniency of Springs,

388. The first inconveniency of Springs, is that their action is not uniform, but diminishes as they unbend: but this is totally remedied by the application of a well adjusted FUSEE.

Second Ditto.

389. Heat and cold, contract and dilate all metals; *and consequently* alter the elastic force of Springs in such manner, that their exertion is not the same at all times; but in a state of fluctuation, depending on the temperature of the air, or the degree of heat or cold to which they may occasionally be exposed.

How remedied.

390. But this *evil*, however bad, is not incurable; for the same cause always producing the same

same effect, *it* may with certainty be remedied by *an opposition of expansion*; of which more when I treat of Thermometers.

WATCHES BY
SPRINGS.

391. I have shewn (155), that the influence of heat and cold on the oil applied to the pallets, was of the most pernicious nature, as no remedy could be applied by opposition; the same is applicable to the oil applied to the main Spring; for the coils of the spring lying in many places in contact with each other, any change in the tenacity of the oil, may considerably alter the exertion of the Spring on the Fusée; and consequently the action of the wheels on the pallets.

Application of oil
to the main Springs
hurtful.

392. But the use of oil on *main Springs* may be discontinued, by tapering *them* more towards the inner end; by which means the exterior coils being thickest, will soonest unbend; and the exertion of the Spring will become progressive from its outer, to inner end, and one coil only act at a time; which will prevent all rubbing, and render the application of oil entirely unnecessary: hence *its* action may (390) be rendered so uniform, that the greatest effect of any remaining irregularities, cannot be perceived in the performance of a Watch.

Rendered unnecessary.

393. It may possibly be objected, that the thickness of such Springs may render their temper less perfect at the external, than the internal end; but it should also be remembered, that the exterior parts of all Springs are bent round

Objection to tapering Springs.

Answered.

R

larger

CLOCKS GO BY
WEIGHT,

larger cylinders, than the interior, and therefore, require less perfect elasticity ; and if due care be taken that Springs be made as broad as the space admits, and no part of their power misapplied ; I am apt to think that no sensible inconveniency or disadvantage will attend the necessary thickness : but even admitting, that thicker Springs are more liable to break, than thinner ones ; that which gives the most perfect performance while it lasts, is in *many cases* to be preferred.

Consideration of
the method of dis-
engaging the
wheels, resumed.

394. When I examined the properties of Mr. HUGENS's method of removing the effects of any irregularities of action in the main Spring (216, to 223), I proposed resuming that subject, in order to enquire, whether that ingenious contrivance would have *an equal effect* in PORTABLE MACHINES, as it was there allowed to have *in Spring Clocks that remain in their place* (221). The reader will please to remember, THAT

395. The chief advantage acquired in *the former case*, was owing to the swing wheel being moved by a small *weight* (216) ; *which would have a direct contrary effect in a portable machine*, of whatever construction : for the action of the weight on the swing wheel, would no longer remain uniform, but depend in a great measure on the direction and velocity, with which the machine was moved.

Illustration.

396. Example. If a heavy body falls freely, it will descend nearly sixteen feet in a second of time :

time: but if two bodies fall together, and with equal velocities, they will be relatively at rest; nor can the one, have the least tendency to draw or propel the other: *and thus*, is the action of the small weight on the swing wheel diminished, in proportion to the velocity with which the whole machine descends; *and the contrary*; by which means, Mr. HUGENS's method of winding up his Marine-clocks every half minute, introduced greater irregularities in their maintaining power (while at sea), than could arise from all the other imperfections of Spring Clocks taken together.

WATCHES BY
SPRINGS.

397. Let us then suppose, a Spring or Springs, substituted for the weight; *it is obvious*, that every inconveniency arising from the motion of the *whole machine*, will be removed; but those Springs, being as subject to the influences of heat and cold, as the main Spring, will be no improvement in this respect; for if any degree of heat or cold should alter the exertion of those small Springs on the Ballance wheel, suppose $\frac{1}{1000}$ part of their whole force, it will affect the times of Vibration, *as much*, as if the main Spring had acted on the Ballance wheel, (without the interposition of such smaller springs) and undergone an alteration of a $\frac{1}{1000}$ part of its *whole force*: for *in either case*, there is an alteration of $\frac{1}{1000}$ part of the *whole maintaining power*; and it was shewn formerly (80), that the altera-

Springs substituted
for weights.

No advantage:

These small
Springs more in-
fluenced than the
main Spring.

No more than a
200th of the in-
fluence of the oil
can be thus re-
moved.

IMPROVEMENT OF

tion in the measure of time depends, (c. p.) on the *alteration in the maintaining power*: therefore the performance of the Watch, will be no ways improved by the above means. *And,*

398. If this method of frequent winding up, does in portable machines, remove the influence of heat and cold on the main Spring: it introduces another effect, that is, *in every case* equal to it (397), and *superior in many*; for, those Springs that propel the Ballance wheel, being so much more slender and exposed than the main Spring, are influenced by many such changes of heat and cold, as have not sufficient duration to affect the main Spring; and therefore, if we only regard the influence of heat and cold on the Springs, this method is hurtful.

399. I have already shewn (392), how to evade the use of oil on the main Spring; and if the influence on all the pivots, those of the Ballance and its wheel excepted, be removed by the disengaging all the wheels but one; it has been already shewn, that *such part of the influence* of the oil, is to its whole influence, *even in Clocks*; only as one to 199, (221): but it will still bear a much less proportion to the whole, in Watches, where the influence on the Ballance pivots, and pallets, become much more considerable on account of the greater angles and number of Vibration, as well as the greater number of wheels.

400. But

400. But admitting, that a 200th part of the influence of the oil, should be removed by this means, a much greater advantage might be gained, by applying *such part* of the action of the main Spring *as is in the above case lost*; for by such means, the influence of the oil would be diminished in the inverse duplicate proportion of the maintaining power (162): for, if a fifth part of the action of the Spring be thus lost, the effect of the influence of the oil (on the measure of time), with the remaining four fifths, will be to its effect, with the whole action of the Spring, as 25 to 16 *; from which it evidently appears, that so far as relates to the influence of the oil, the advantage gained, by applying *the whole exertion* of the main Spring *to the pallets*, is, to the advantage gained, by disengaging the wheels, nearly as 200 to 3.

WATCHES BY
SPRINGS.

Much more advantage gained by increasing the maintaining power.

401. It has been already shewn (398), that, so far as it regards the influence of heat and cold on Springs, this contrivance is hurtful; that, so far as relates to the influence of the oil, it has no better effect (400); and that, unless the periodical fluctuations, in the action of the wheels, have a sensible effect on the measure of time du-

RECAPITULATION.

* For it appears that by increasing the motive force of the wheels, as 5 to 4, the influence of the oil is diminished as 16 to 25, that is, somewhat more than a third: but by disengaging the wheels (however frequent) only a 200th part of the influence can be removed.

CLOCKS GO BY
WEIGHT,

The disengaging
the wheels, &c.
can never be an
advantage in any
portable machine.

Maintaining pow-
er in Watches
can never be ren-
dered as uniform
as in Clocks.

ring the action of one tooth, it never increases (54): and even admitting, that such periodical fluctuations in the maintaining power, were hurtful; those that happen, by unlocking the winding up part, in the above case, are not less so, than those of the wheels and pinions.

402. There does not then appear, the smallest shadow of improvement, *by thus disengaging any number of the wheels, in portable machines of any kind*: on the contrary; by rendering those periods of winding, more frequent, than will require the Springs that propel the Ballance wheel, *each as thick as the Ballance Spring*, the performance must be hurt*; and in 30 hour Watches whose Ballance Springs are of a proper strength, the above rule, will not even admit of detaching one single wheel, much less, of winding up every half minute; *therefore*, we may to good purpose *in all portable machines* save that labour, which this method of disengaging the wheels would occasion.

403. The method which I have given (300) for rendering the maintaining power in Clocks perfectly uniform; would *in portable machines* be liable to the same inconveniencies: *hence it would appear*, that in this respect, Watch-work must ever be inferior to Clocks: though, by a

* This article will be explained, when Thermometers are treated of.

due attention to what has been said in the former Essay relative to the maintaining power, and a *judicious* application of a Thermometer, the action on the pallets, in Watch-work, may be made to disturb the times of Vibration, as little as it generally does in Clocks. *But,*

WATCHES BY
SPRINGS.

404. He who prefers experiment to demonstration may receive no small satisfaction, relative to the errors that arise from all the imperfections of MAIN SPRINGS, even in their present state, by comparing together the performance of two Clocks ; *the one* with a weight, *the other*, with a Spring : and I will venture to assert from trials I have made ; *that*, if the maintaining power, angle of Vibration, and weight of the Pendulum &c. be made equal in two such Clocks ; their performance will prove ; *that a very small part only, of the errors of Watch-work, is owing to the imperfections of the main Spring ; even where no Thermometer is used to counteract it**.

Experiment, and
Conclusion.

* Does not the same heat that lengthens the main Spring and chain, render the oil on the pivots more fluid, and increase the diameter of the Fusee ? by which means, it seems to me more than probable, that the exertion on the pallets is rendered more uniform, than if the action of the main Spring was subject to no alteration from heat or cold : for those contrary effects tend to correct each other.

CLOCKS are regulated by a Pendulum;
 WATCHES *by a Ballance and Spring.*

Plan of enquiry.

405. In order to investigate this matter properly, it is necessary carefully to compare the Ballance and its Spring, with a Pendulum; and enquire, how far they share the same properties: in order to which, I shall here recapitulate *the general properties of the detached Pendulum*, as stated in the foregoing Essay; that it may the more clearly appear, in what respects *those of the Ballance*, do either agree with, or differ from *them*.

First property of
the Pendulum.

FIRST *Property of a Pendulum.*—

406. That, if once put in motion, it would ever continue to vibrate, if no external cause tended to destroy its motion.

*Equalled in the
Ballance.*

The case is similar in the Ballance; for the Spring in unbending, would communicate as much motion to the Ballance, as would enable it, (by means of its vis viva) to bend the Spring as much in a contrary direction. Hence, it would vibrate without diminution, &c.

Second Property
of the Pendu-
lum.

SECOND *Property of the Pendulum.*—

407. All its *equal* Vibrations would be performed in equal times.

The

The same would happen with the Ballance and Spring: because the motive force and space described, remained unalterably the same (406).

CLOCKS REGU-
LATED BY A
PENDULUM, &c.

THIRD Property of the Pendulum.—

408. Its momentum (in circular Vibrations) is as the versed sine of its angle of Vibration, into its quantity of matter: but it increases somewhat quicker, towards the extremities of cycloidal Vibrations; in which, the exertion of gravity on the Pendulum, is constantly as its distance from the point of rest*.

Third property of
the Pendulum.

In the Vibrations of the Ballance, the exertion of the Spring, is also constantly, as the distance of the Ballance from its point of rest†; and therefore its Vibrations, naturally have the properties of the cycloidal Pendulum, oscillating in a medium of unalterable density‡; and their momenta and velocities, at different distances from the point of rest, &c. are to be estimated in the same manner.

More perfect in the
Ballance.

FOURTH property of the Pendulum.—

409. Those of equal length, though unequal weight, will (c. p.) perform their Vibrations in equal times.

Fourth property of
the Pendulum.

Likewise all Ballances wherein the vis insita and strength of the Spring have the same proportion;

Equalled in the Bal-
lance.

* See Sir ISAAC NEWTON's Prin. Prop. 53.

† See Dr. HOOK's Theory of Springs.

‡ For such changes as happen in the density of the air, do not alter the motive force of the Ballance, as they do that of the Pendulum (379).

CLOCKS REGULATED BY A PENDULUM;

Fifth property of the Pendulum.

Equalled in the Ballance and Spring.

A perfect equiliber of action and re-action.

will (c. p.) perform their Vibrations in equal times.

FIFTH property of the Pendulum. —

410. They alter their times of Vibration in different latitudes : (because gravity is altered without the *vis insita*)†.

A Ballance will also alter its times of Vibration, if the strength of its Spring be altered ; without altering its weight or size*.

411. In the vibrating Pendulum ; gravity is made by means of the *vis insita*, to counteract itself : the Ballance Spring is also made to counteract itself in each Vibration, by means of the *vis insita* of the Ballance ; and thus, by having the effect changed into the cause, in each Vibration ; we have, in the vibrating Pendulum, and in the Ballance and Spring, the most perfect equilibrium of action and re-action, that nature can produce ‡ : what can be more equal than any power to itself ?

412. Thus

† In the Pendulum, gravity is the motive force ; and in Ballance, the Spring : the *vis insita* is the resistance in each : and the contrary : therefore, when the motive force is in each, as the resistance, the velocities and times must be equal. Hence it also happens that (c. p.) the Ballance measures the same time in all latitudes.

* Here, by altering the weight, is strictly meant, altering the *vis inertiae* ; for the Vibrations of a Ballance, whose center of gravity coincides with its center of motion, have not the least dependence on gravitation, otherwise it would alter its times in different latitudes, as well as the Pendulum.

‡ For this reason the vibrating Pendulum and the Ballance and Spring will always measure time better than such as perform

412. Thus we find; *that the Ballance and Spring*, are in full possession of all those properties of the Pendulum, on which the isochronism of the Vibrations depend: the *vis insita*, having the same effect *in each*; and *the Spring* producing that effect in the *Ballance*, that *gravity* does in the *Pendulum*. Therefore,

413. All that has been said in the former Essay, relative to, *the length of Vibrations* (41, 47); *weight of the Pendulum* (79, 80); *quantity of maintaining power* (161, 162); *influences of the oil* (163, 164); *and construction of pallets*, (189, 239, 263); is as applicable to *Watches*, as *Clocks**, and need not here be repeated: but as the several articles wherein *Watches* differ from *Clocks* (386) require some considerations in the improvement of the *former*,

WATCHES BY A
BALLANCE AND
SPRING.

The Ballance has
all the properties
of the Pendulum.

All that has been
said relative to the
Pendulum, is
equally applicable
to the Ballance.

whole revolutions: and where the centrifugal force is made to correct the velocity: for in this case, any alteration in the motive force will require a new adjustment of these two powers, which cannot take place till the change of velocity make such an alteration in the centrifugal force as can overcome some small degree of friction: therefore the motive force may remain for a considerable time, either too great or small, for the resistance, to render the revolutions isochronal; and here the most trifling error may, by constant accumulation, become great (248): whereas in the common Pendulum, there is a new adjustment of the motive force and resistance, at the point of rest of each Vibration; where the effect is always changed into the cause.

* Observing always, that what is said in the *One* of the mode or quantity of the exertion of gravity on the Pendulum, is to be understood in the *Other*, of the exertion of the Ballance Spring.

CLOCKS REGULATED BY A PENDULUM;

Maintaining power cannot be rendered so perfect in Watches as in Clocks.

But the same effect may be otherwise produced.

Enquiry concerning the Ballance.

Exertion of its Spring considered as an innate force, &c.

The effect of its *vis insita*.

that were totally unnecessary to the latter; I shall endeavour to point out, in what cases, those *additional improvements* co-operate with, or counteract, those already proposed.

414. It has been already observed (403), that the maintaining power can never be rendered so uniform in Watches as it may in Clocks: but admitting the natural isochronism of the Ballance (408), pallets may be so constructed, as to correct the *effect* of any changes of the maintaining power; by prolonging one half of the *time of Vibration*, as much as the *other* is contracted: which will have the same effect on the measure of time; *as rendering the maintaining power perfectly uniform.*

415. But let us now enquire, whether there are any probable reasons, why the Ballance may not have the same advantages, in practice as in theory.

416. *In the theory* of the Ballance (408), the action of the Spring was considered, as an innate property of the Ballance; whose exertion was in every part of the Vibration, as the distance of the Ballance from its natural point of rest: but no regard was paid to the effects that might arise from the *vis insita*, or *shape* of a Spring, acting in a spiral direction.

417. If all the matter of the Ballance Spring was collected into a circle, *concentric with the Ballance*, its *vis insita* would have a similar effect

fect to *that* of the Ballance; and would tend to promote the action, in the one half of the Vibration, as much as it opposed it, in the other; *and consequently*, no part of the exertion of the Spring would be lost, or destroyed by *its* means. But from the spiral form of the Ballance Spring, the *vis insita* of all its parts, have contrary tendencies, and so destroy each other's effects; so that it cannot promote the bending as much, as it retards the unbending: and thus is a part of the exertion of the Spring lost in each Vibration, which must prolong the times. *But*

WATCHES BY A
BALLANCE AND
SPRING.

418. The part lost of the exertion of the Spring is, (*c. p.*) as the mean motion of all the particles of the Spring taken together: hence it must increase with the angle of Vibration; and such prolongation of times as it occasions, must be greater, in the longer Vibrations than the shorter; and this I imagine is the case, in detached Ballances *with Springs of equal thickness*. *But*

The exertion lost
as the length of
Vibration. Hence
the longer ones
slowest.

419. If the Spring be rendered thinner towards its inner end, the mean motion of its parts, will bear a less proportion to the angle of Vibration; and consequently, the longer and shorter Vibrations will thereby be rendered more isochronal; *and the same is true of all the other means*, by which, the mean motion of the Ballance Spring may be diminished (418). *But*

The Vibrations
rendered more
isochronal.

420. As

CLOCKS REGU-
LATED BY A
PENDULUM.

Mode of action
considered.

The exertion of
tapering spiral
Springs progres-
sive, &c.

Different from
straight tapering
Springs, &c.

420. As the Spring must have some degree of motion in any Vibration whatever the above consideration *alone*, can never render the Vibrations truly isochronal (418).

421. But the longer Vibrations are rendered quicker in proportion to the shorter, with tapering Springs, on account of their mode of action, as well as the diminution of the *vis inertiae*.
Thus

422. If any power be applied to a Ballance, which tends to bend its Spring, the thinnest part thereof will be soonest bent; therefore a tapering Spring will begin to bend at its inner end, and as the resistance of its thinner parts increase (408), the thicker parts are bent: by which means, the exertion of a spiral tapering Spring in bending, is at least in some degree, *progressive from its thinnest to its thickest end*; and in unbending, *the contrary*.

423. It is evident, *that the mode of exertion of a tapering spiral Spring*, is different from *that of a straight Spring of equal length, and taper*, where the power is applied at right angles to the Spring *.

424. But

* The exertion of any power applied at the inner end of a tapering Spring, on any part of such Spring, may be represented by two lines meeting at such part of the Spring; the one at right angles, the other attangent to it: from which it is evident, that such part as is represented by the line attangent, can have
no

424. But the exertion of a Spring is, (*c. p.*) as its thickness; therefore (422), the exertion of a spiral tapering Spring, will increase more in proportion to the spaces to which it is bent, than that of a Spring of equal thickness.

425. Hence, the longer Vibrations of a Ballance will be *quicker in proportion to the shorter ones*, with tapering Springs, than those of equal thickness: *Therefore*,

426. There must be a certain degree of tapering of the Ballance Spring, that will *render* the Vibrations as isochronal, as if the Spring was of *equal thickness*, and *deprived of its vis inertiae* (417). And this I am also induced to believe by observation, as well as theory: *and moreover*, that, by tapering the Ballance Spring beyond the due pitch, the longer Vibrations of the detached Ballance, may be rendered quicker than shorter ones.

427. And though it may be impossible to determine by calculation, the exact shape that will give the above property; it may not be so difficult, to manufacture many, that will have the same

WATCHES BY A
BALLANCE AND
SPRING.

Increases most
towards the extre-
mities in spiral
Springs.

The longer Vibra-
tions quicker,
with tapering
Springs, &c.

A certain degree
of tapering will
give the cycloidal
properties, &c.

Or even render
the longer ones
quickest.

Many such Springs
may be manufac-
tured, &c.

no effect on the bending that part of the Spring, but acts like a cord in bending some other part of it, at the distance of a quarter of a turn from that point: and thus may a weaker part of a spiral Spring be made to bend a thicker, without being so much bent itself as if the Spring was straight: and this accelerating effect of a tapering Spring will increase with the size of the collet to which it is attached.

property,

CLOCKS REGULATED BY A PENDULUM;

All the properties of cycloidal Vibrations may be given the Ballance, even in practice.

Conclusion.

property, when such shape has been once found: and it may be ascertained by trial, whether such property is sufficiently perfect before they be applied to a Watch.

428. And thus it would appear, that even in practice, all the properties of the cycloidal Vibrations of the Pendulum in a medium of *uniform density* may be given the Ballance and spiral Spring. *Therefore,*

429. The great disparity in the performance of CLOCKS and WATCHES, cannot be owing to the *former* being regulated by a Pendulum, and the *latter*, by a Ballance and spiral Spring: *we therefore come to consider, the third article wherein Watches differ from Clocks.*

CLOCKS are not capable of beginning their own Vibration: but WATCHES are.

In all Clocks the action of gravity has more influence on the Pendulum.

430. If the action of the swing wheel was greater than that of gravity on a Clock Pendulum; such Clock would begin its own Vibrations: but as no Clocks do, we may justly infer, that in all of them, the action of gravity has more influence on the Pendulum, than the action of the wheels has.

The contrary in Watches, &c.

431. *All Watches* begin their own Vibrations, because the action of the wheels is equal to that of

of the spiral Spring on the Ballance when the wheel escapes the pallets (486). And therefore Watches are, in this respect, *only on a par* with Clocks having such light Pendulums that they would begin their own Vibrations (413).

WATCHES BY A
BALLANCE AND
SPRING.

432. *Let such a Clock be made* with an equal maintaining power as in Watches, and *its* performance will prove, that no small part of the imperfections of Watch-work, is owing to *too small maintaining powers* (164); and the still smaller proportion, that the momentum of the Ballance bears to *them* (80, 81, 413, 487).

Experiment proposed, &c.

433. It is universally allowed that the lightest Pendulum has all the natural properties of the heaviest: but will any assert, that one of an ounce weight, will (*c. p.*) have the same effect in correcting any irregularities of the maintaining power, as one of many pounds: *and is not the case exactly similar with a Ballance and Spring?* (413)*.

Illustration.

434. I shall hereafter have occasion to enquire into the several ways of augmenting the momentum of the Ballance, when it will appear, that in every case, the advantage increases with

The advantage increases with the strength of the Ballance Spring, &c.

* I shall, in an after part, consider the improvements that must yet be made, before the momentum of the Ballance can be much augmented in Pocket-watches, with one Ballance, further than by augmenting the maintaining power and angle of Vibration, and diminishing the angle of scapement.

CLOCKS CANNOT
BEGIN THEIR
VIBRATIONS,
&c.

the strength of the Ballance Spring: *though not equally in all cases* *.

435. Having here pointed out, *one of the greatest causes of error in the performance of Watches*, I now come to the fourth article; wherein *they* differ from Clocks.

CLOCKS are larger than WATCHES.

Wherein Clocks
have the advantage,
&c.

436. Here also, Clocks have the advantage of portable machines, wherein the size is limited: as they admit of *stronger maintaining powers, and greater momentum in the Pendulum*.

Larger Watches
have a like advantage,
&c.

437. For the same reason; a LARGER WATCH will perform better than a smaller: for, though the maintaining power may bear the same proportion to the *weight* of the Ballance in each; *the influences of the oil* will always bear the greatest proportion to the least maintaining power (161 to 164): therefore, the greatest care is to be taken, to acquire in all Watches as great a maintaining power as circumstances can admit: which of course increases the momentum of the Ballance, by which means a double advantage is gained (162, 490).

The Wheels
should be made
light, &c.

438. As to the wheels; *they, only serving to transmit the action of the main Spring to the Bal-*

* Since all that has been said relative to the exertion of the Ballance Spring is equally applicable to the exertion of gravity on the Pendulum (413); it follows, that the more the Arc of Vibration of a Pendulum approaches a straight line, i. e. the shorter the Arc (See Plate 12. Fig. 2.) the worse the performance of the Clock.

lance,

lance, and to number its *Vibrations*; should be made no larger or heavier, than is absolutely necessary, to perform their respective offices with safety; and the judicious mechanic may display his skill, by duly proportioning the strength of each wheel, and the several parts thereof, to the pressure it has to sustain.

CLOCKS ARE
LARGER THAN
WATCHES.

439. Some are inclinable to think, that great advantage is gained by having large wheels, as they may be executed with greater accuracy: but when the theory of wheel-work, and the proper methods of execution, are thoroughly understood, this imaginary advantage will vanish.

The advantage of
large Wheels ima-
ginary.

440. But, the disadvantages of *large heavy wheels*, are of more weight, for heavier wheels require thicker pivots, which increases the influence of the oil in proportion to the size of the pivots; and the friction, in the proportion to the size of the pivots, and weight of the wheel, jointly; which diminishes the maintaining power: as does also, the *vis inertiae* of the wheels; which increases as their weight, and is to be overcome at each Vibration of the Ballance.

Disadvantages of
heavy Wheels,
&c.

441. On the whole it appears; that, the more Watches approximate Clocks in point of maintaining power, and momentum of the Ballance, the more is their performance improved (413): and that, though an increase of external size is necessary to acquire those advantages; it is not always a certain proof of their being acquired.—

Conclusion, &c.

I now come to the fifth article, wherein Watches differ from Clocks.—

CLOCKS are fixed in their place, but
WATCHES are portable.

Plan.

442. As the above difference gives rise to an error in Watches, to which Clocks are only in a very small degree liable; *I shall endeavour to shew*, by what means any EXTERNAL MOTION of a Watch does influence its times of Vibration: what kind of motion has the greatest influence: and by what means those influences may be evaded or corrected.

Machine described.

443. Plate 12. Fig. 1. represents a machine intended to illustrate this theory experimentally.

A B C D, is a square board, or frame, on which moves round a hollow socket, (through which the verge or axis of the Ballance passes).

E F G, a round board, or plate of metal, to which is attached the one end of a spiral Spring: the other end of which is fixed to a small collet near the center of the Ballance N O, in every respect in the same manner as the Ballance Spring is applied in Watches.

L M, a scale fixed to the board E F G, and serves to shew the relative motion of the Ballance therewith; by means of a mark made on the Ballance (when at rest) opposite the middle of the scale: hence, as this mark recedes from, or
I approaches

approaches the middle of the scale; the Ballance is said to recede from, or approach, its POINT OF REST.

INFLUENCE OF
EXTERNAL MO-
TION.

I K, is a scale on the board A B C D, having holes in it corresponding with the divisions of L M; by means of a small pin occasionally put in either of these holes, the board E F G, (when disengaged from the catch H), may be made to move any number of spaces, and with different velocities, by the action of a weight or weights, suspended to the end of a small pliable cord, which is applied round the circumference of the board E F G, and passes over a pulley at B.

444. Now if the board E F G, represent the frame of a Watch, and N O, the Ballance: and the former be made to move any number of spaces on the scale I K; the influences of such motion on the Ballance, with Springs of different strength, Ballances of different weight, and motions of different angles and velocities, will be given on the scale L M; for it matters not, whether the ballance of a Watch describes a certain number of degrees on the frame; or the frame moves the same, and the Ballance remain at rest; for in either case, *their relative motion is the same*, and will allow one tooth of the wheel which acts on the Ballance, to pass at *each relative Vibration*; and the time shewn by a Watch depends on the number of such teeth, that escape the pallets, whether owing to the *absolute*, or *relative* motion of the Ballance.

Use of the ma-
chine.

One tooth passes
each relative Vi-
bration.

Introduction to the
experiments.

IMPROVEMENT OF

445. I shall therefore here suggest, a few of the many experiments, that may be made with this machine, to illustrate the influences of external motion.

Experiment.

446. Let the spiral Spring be taken from the Ballance, and the Index F, be made to move any number of divisions on the scale I K; the Ballance will retain its position by means of its *vis inertiae*; and so be made to describe as many spaces on the scale L M, as the Index F, does on the scale I K *.

Application.

Influence of external motion greatest, when no Spring is applied to the Ballance.

447. This experiment shews, that any external motion of a Watch, will (*c. p.*) have the greatest influence possible on its performance, when no Spring is applied to its Ballance (444); for in this experiment, the influence of external motion (shewn on the scale L M), is equal to the external motion, on the scale I K.

Experiment.

448. Let the point N, of the Ballance, be brought to the middle of the scale, and the whole

* It is here to be understood, that the motion be not very slow; for in that case, the friction on the pivots might occasion the Ballance to move with the scale, and preserve its relative position.

machine be moved in a straight line, with any velocity, or in any direction, the relative position of the Ballance and frame, will be no wise altered by such motion.

INFLUENCE OF
EXTERNAL MO-
TION.

Application.

449. This experiment shews, that rectilineal motions do not influence the times of Vibration (442): but it is here understood, that *every point* of the machine, as well as its center of gravity, describes a straight line; for in such case only, will the machine keep parallel to its first position, on which alone the property depends*.

Rectilineation
does not influence
the times, &c.

Experiment.

450. Let a long beam of wood be fixed at right angles to an axis, round which let it move on pivots: if the above machine be attached to the beam, at any distance from the axis, in such manner, that the plane of the Ballance be parallel to the axis of the beam, the relative position of the Ballance with its frame, will not be altered by any motion of the beam round its axis, what-

PLATE XII.
FIG. 3.

* Though rectilineal motion does not of itself any how influence the times of Vibration: it may, by increasing the friction on the Ballance pivots, alter the length of Vibration, and by that means introduce the effect of any imperfection of the Ballance Spring and pallets: but in Watches where these are perfect, such friction will not alter the times.

ever

ever be the angle or velocity of such motion, or the distance of the machine from the axis.

Application.

What curvilinear motions do influence the times, &c.

451. This experiment shews, that no curvilinear motions, that do not in some degree, incline to the direction of the Vibrations of the Ballance, can influence its times of Vibration*.

Experiment.

452. Let the foregoing experiment be repeated, with the axis of the Ballance parallel to that of the beam; and the relative motion of the Ballance on its scale, will always be as the angle described by the beam, without regard to

* Therefore a Watch carried on shipboard cannot have its times of Vibrations influenced by any motion, or motions, whose axils are parallel to the plane of the Ballance. Hence the best position for a Watch that is carried on shipboard, is to have the plane of its Ballance nearly parallel to the decks: (unless some internal defect, arising from the execution, should render the performance more imperfect in this than in its other positions.) It is also to be observed, that the best place in a ship for laying a Watch in, is near its center of gravity; for here the agitation is the least. It may possibly here be enquired, From what internal defects a Watch does measure time differently, in its different positions? But such enquiry being entirely foreign to the general theory of Watch-work, (the defect arising solely from imperfections of execution) I shall only here observe, that if a Watch is adjusted in six positions, at right angles to each other, it will measure equal time, in all the other positions into which it can possibly be put; they being all compounded of the former.

the

the place of the machine, whether at the center, extremity, or any intermediate part of the beam.

INFLUENCE OF
EXTERNAL MO-
TION.

Application.

453. This experiment shews, that the influence of any curvilinear motion, even in the direction of the Vibrations of a Ballance, does only take place (*c. p.*) in proportion to the angle, which it would make the Ballance describe round its own axis (446); which is always equal to the angle moved by the beam *), without regard to the distance of the machine from the axis, or center of motion: and thus we see, why the Vibrations of a Ballance are much more disturbed in the pocket, or in a carriage, than on ship-board.

Effects of curvilinear motion.

Watches more influenced in the pocket than on shipboard.

454. *The result of the fourth experiment may also be expressed thus:* The influence of any external motion, on the times of Vibration of a Ballance, is, (*c. p.*) as the deviation which such motion occasions in the parallelism of the machine from its former position; which also (by 29 of 1st of Euclid), is always equal to the angle described by the beam. See Plate 12. Fig. 3.

Curvilinear motion otherwise considered.

455. The following experiments all tend to prove, that the influence of external motion, is, in all cases, diminished, by the application of a

Elastic force of the Spring diminishes the influence of external motion.

* See Plate 12. Fig. 3.

INFLUENCE OF
EXTERNAL MO-
TION.

Spring to the Ballance; and that, in proportion to the strength of the Spring; *the Ballance remaining the same.*

Experiment.

PLATE XII.
FIG. 1.

456. Let a Spring be applied to the Ballance, as represented in the Fig. and the index F, be made to move any number of divisions on its scale (as in former experiments); the motion of the point N, on the scale L M, will be diminished by the exertion of the Spring; and with Springs of *double* and *triple*, &c. strength, it will yet be diminished (*c. p.*) to a *half* and a *third*, &c.

457. But a Spring of double or triple, &c. strength, would make the same Ballance vibrate, double, triple, &c. the number of Vibrations in the same time; therefore, (456) the influences of external motion *on a single Vibration of a Ballance*, will be diminished with the time of its Vibration. *Hence, also*

Influence of external motion equal in all Watches having equal trains, &c.

458. In all Watches having *equal trains*, the influence of external motion is, *c. p.* the same, *without regard to the strength of their relative Ballance Springs*: for in each, the weight of the Ballance, must have the same proportion to the strength of the Spring (409), and an increase of the former *augments* the influence of external motion, in the same proportion, that an increase of

of the latter *diminishes it*: as may be proved experimentally, by applying rings of different weights to the Ballance, (by means of the small holes at N and O,) so as to double or triple its weight with the same Spring.

459. And though some of the foregoing experiments are made on Ballances that have neither the action of a Spring or wheels, to give them motion (446, 448, 450, 452), and all the others on Ballances at rest (456, 458,) where the external influence *always generates motion* in the Ballance, which is not the case with a Ballance that performs its Vibrations during the experiment; for its motion will be *increased* or *diminished*, as it happens in the *same*, or a *contrary* direction with the external motion. *But,*

460. The relative influence on a single Vibration, would be the same as above stated, whether the Ballance was at rest, or vibrating, at the beginning of each experiment: or whether the external motion happens to oppose, or conspire with, that of the Ballance: See Sir ISAAC NEWTON'S II. law of motion*.

461. Having thus laid a foundation, for diminishing (443, 449, 454), as well as estimating, *the influence of external motion, on a single Vi-*

INFLUENCE OF
EXTERNAL MO-
TION.

PLATE XII.
FIG. I.

Foregoing experi-
ments made with
Ballances at rest,
&c.

Influences the
same, whether the
Ballance be in mo-
tion or at rest,
&c.

Introduction to the
influences on
many Vibrations.

* Hence those Watches whose Ballances, when at rest, are least liable to be disturbed, or begin their Vibrations by the influence of external motion, have their Vibrations also least influenced.

INFLUENCE OF
EXTERNAL MO-
TION.Illustration, by a
Watch on ship-
board.In a double angle
of Vibration, the
influence only
half.And diminished by
increasing the
maintaining
power.If two Vibrations
be performed, the
one corrects the
other.

bration : I now come to consider *its* effect on many.

462. If a Watch be so placed in a ship, that the axis of the Ballance lies parallel to the axis of the ship's greatest motion ; and *the angular motion of the ship* be equal, to *the angle of Vibration of the Ballance*, and performed in the same time : if those two equal angular motions happen to *oppose* each other, the former will destroy the latter (452, 453), and the Watch come to rest. *But,*

463. If the angular motion of the Ballance had been *double* that of the ship ; the latter could only have destroyed one half of the former (453). *And therefore,*

464. The influence of external motion will be (*cæt. par.*) in the inverse proportion of the angle of Vibration of the Ballance to the angular motion of the ship (462). *But the angle of Vibration increases, with the maintaining power ; therefore, the influence of external motion is diminished by increasing the maintaining power* (463).

465. If *one Vibration only*, be performed during one motion of the ship ; it will be accelerated or retarded (460) in the above mentioned proportion (464) : but if *two Vibrations* be performed, each will receive half the influence, that is, the *one will be accelerated* as much as *the other is retarded* (460) ; and consequently, *both* be performed

formed in the same time, as if no external cause had influenced them : *Thus*,

466. Vibrations of half the duration have a *duplicate* advantage ; for the same cause, will only produce half the effect (452), and they also have a double chance of correcting each other (465) : add to this, that if the whole cause did take place, its effect would be diminished by the superior strength of the Spring (456). Hence,

467. *The influence of external motion, on the performance of a Watch is diminished, at least in the inverse duplicate proportion of its train :* (or number of beats in a given time). And therefore,

468. If two Watches be made in every respect alike ; *only* that the one shall vibrate *five*, the other *six times* in a second, the relative influences of external motion on those Watches will be, inversely as the squares of their number of Vibrations : *that is*, on the former, to the latter, as 36 to 25 : Hence *,

469. We may reasonably entertain hope of diminishing the influence of external motion by such means, (and without any additional parts) to such a degree, as will scarce leave a chance of a Watch with one Ballance, stopping in the pocket.

INFLUENCE OF
EXTERNAL MO-
TION.

Those of half du-
ration have dupli-
cate advantage.

The total influ-
ence of external
motion in the in-
verse duplicate
proportion of the
train.

Application.

Inference.

* It is here supposed that the angles of Vibration are equal in such Watches.

470. And

INFLUENCE OF
EXTERNAL MO-
TION.

The only means
of introducing
strong Ballance
Springs, &c.

Half timing,
what.

Objection.

To be answered
hereafter.

470. And this merits the more serious attention, that it seems the *only means of introducing strong Ballance Springs and heavy Ballances*, into *Pocket-watches*; for until the chances of stopping (or setting) in the pocket, are much more diminished than at present *; we must continue the practice of HALF-TIMING; that is, rendering the exertion of the wheels equal or nearly so to that of the spiral Spring, on the Ballance, *at beginning of its Vibrations*: the disadvantages of which, and the advantages that may be gained by a contrary practice (468, 469), will appear more evident, by perusing what is said in the former Essay from (70 to 79); which is equally applicable here (413).

471. I doubt not, that some will here remark, that every Vibration has its friction, &c. *and consequently*, that by increasing the number of Vibrations in a given time, the friction and influences of the oil are also increased, and the performance thereby much hurt, and the parts sooner impaired. *But,*

472. Thus mentioning *the dreaded evil*, may here convince, that it has not escaped no-

* Thus it appears, why the Ballance Spring, in all Pocket-watches, is made nearly of the same strength with the action of the wheels: for if a Watch having a strong Spring, and heavy Ballance, happens to set in the pocket, by means of any sudden jolt, it must continue at rest, till again put in motion by its wearer, or some other motion equally violent.

tice :

tice: and before this Essay is concluded, I shall endeavour to shew, not only, that the train may be increased to the degree already proposed (468), *but even doubled*, without increasing the *total influence of the oil*, or friction, beyond what now takes place in the best horizontal Watches with common trains: not to mention the diminution that a due increase of maintaining power may occasion in the effect of such influence of the oil. (413. 161 to 164.)

INFLUENCE OF
EXTERNAL MO-
TION.

473. Having now pointed out the means that appear to me, the most simple and advantageous, for diminishing the influence of external motion in ALL PORTABLE MACHINES; and the *only means* by which it can be diminished in Pocket Watches, *with one Ballance*; to such a degree as to admit of a general reformation of principle (470), I now mention the means that have been heretofore used for this purpose; lest I should be accused of having here invidiously passed them in silence.

Introduction to the
means that have
already been used.

474. Dr. Hook about the year 1658 applied to Watches, *two equal Ballances*, so connected that they should vibrate equal angles, *but in contrary directions*; by which means the *one* must always be accelerated as much as the *other* is retarded, by the influence of any external motion; and thus, their *mean motion* could never be altered by any external influence.

Dr. Hook's method.

475. If

INFLUENCE OF
EXTERNAL MO-
TION.

Illustrated.

PLATE XIII.
FIG. 1.

Its inconveni-
encies, &c.

475. If the experiment (446) be made with the machine represented in Plate 13. Fig. 1. each Ballance will have the same relative motion with the frame; and those parts of their circumference that are nearest each other will have equal relative velocities *in contrary directions* (as represented by the darts) and the Ballances are supposed equal also: therefore, if their circumferences be any how connected, those equal and contrary motions of the Ballances will correct each other *.

476. The above very ingenious contrivance, proves its author to be intimately acquainted with the laws of motion, and quick in their application: but here the practice falls short of the theory; for when the Ballances are connected by means of teeth, there arises a resistance, which, however small, when applied in this *most delicate part*, will tend to diminish the momentum of the Ballances; and if the least *irregularity of action*

* I have seen a Watch, made in the year 1715, with intention to discover the longitude, (as appears by an inscription on it) in which, amongst several laborious contrivances applied, were two Ballances; each of which had on its axis a pinion, and both of them were moved by the same wheel, on whose axis were the pallets (see Plate 13. Fig. 3.): by which means both Ballances were made to move in the *same direction*, and consequently (475) rendered as liable to the influences of external motion, as one Ballance. This shews, how general rules, or even the best principles, may be misapplied, when their elements are not properly understood.

should

should take place near the extremity, or *vertex* of the Vibration, it must be attended with the most pernicious effect. *But,*

INFLUENCE OF
EXTERNAL MO-
TION.

477. In order to diminish the above inconveniencies, the Ballances were connected by means of two small wheels, fixed on the arbors of the Ballances, as represented by Fig. 2. Plate 13. * and though some ingenious means have been used, to evade the irregularities of action in such wheels, I pass them here, as also attended with their inconveniencies, and in every respect, *less fit for general use.*

How diminished.

PLATE XIII.
FIG. 2.

478. Mr. HUGENS has, in his *Marine-clocks* already mentioned (216), used a *different* method of removing the influences of external motion ; by preserving the parallelism of position (454) : but though this might, if perfectly attained, have the desired effect on the Vibrations of a Ballance, where the centers of gravity and motion coincide ; it would by no means have the same effect on the Vibrations of a Pendulum (where they do not) ; but the Pendulum can never be ren-

Mr. Hagens's me-
thod.

* It is not improbable that this method and manner may, with some further improvements, be yet applied to good purpose in Pocket-watches ; in which case the weight of the Ballances, and strength of their Spring, (or Springs) may be increased at pleasure. But it seems not clear, that diminishing the size of those wheels that connect the Ballances, to any great degree, is advantageous, since by such means each tooth must subtend the greater angle at the center of the Ballance ; and consequently be the more liable to the inconveniency mentioned in Par. 476.

INFLUENCE OF
EXTERNAL MO-
TION.

Mr. Harrison
united them in the
same machine.

Introduction to
remarks.

Mr. Hugen's
only fit for large
machines.

dered fit for any portable machine, even at sea, for reasons too many to be here mentioned, as no material advantage occurs to me that would follow.

479. Mr. JOHN HARRISON of *Red Lion Square*, has, in each of his three *large machines* for measuring time at sea, united both those methods of diminishing the influences of external motion; and displayed great mechanical abilities, in diminishing the friction, and making the centers of gravity and universal motion of the whole machine, more nearly to coincide than in Mr. HUGEN'S Clocks: but I avoid any remarks on the properties, &c. as there is reason to expect a full account of all his ingenious performances will be soon made public.

480. Having thus mentioned the different methods that may be used, for diminishing the influences of external motion (468, 474, 478): *I shall conclude with a few remarks on their relative advantages.*

481. Mr. HUGEN'S method, from its nature and size, can never be applied to Pocket-watches; and therefore its use is wholly confined to such machines as are carried on ship-board: nor can its effect in those be perfect, unless the center of gravity of the whole machine coincide with its center of universal motion, and the friction of its suspension be totally annihilated: *in which case*, though the *whole machine* would have no ten-
dency

dency to vibrate, *it* would retain any position, which by accident it had got : and thus, a new inconvenience and error in the performance might arise, owing to the machine going in an unusual position ; (probably upside down) ; nor can the friction of suspension ever be removed to such a degree as to prevent this inconvenience : *if it could*, THE LONGITUDE might be ascertained without any measure of time. Let us then consider the effect of rendering the center of gravity so much lower than the universal center of motion, as would regain the former position of the machine, if by any means lost. It is obvious that by such means, the influence of any *motion of the ship*, would be diminished during *its time of continuation* ; but the *effects* of such motion would be continued while the machine retained those Vibrations, of which the ship's motion was the first cause (453)* ; from which it would seem, that a diminution of friction continues the effect for several Vibrations, if it diminishes it in one : hence, it is more calculated to distribute the influence of the ship's motion among many Vibrations, than to destroy it †.

Diminution of friction more calculated to distribute than to destroy the effect, &c.

* And every Vibration of the machine will have the same effect, as if the ship had moved an equal angle (453).

† This method of preserving the parallelism of the machine may in some cases be used, to remove the risque of some parts of the machine being displaced, bent, or broke. But this supposes very great imperfection in the construction.

Dr. Hook's method incomparable in theory.

Increasing the train, preferable to any of the other methods, so far as the nature of materials will admit.

IMPROVEMENT OF

482. Dr. Hook's method, with a double Ballance, would most certainly have all the desired effect ; if the inconveniencies already mentioned could be removed (476) ; in which case, it would in every respect be superior to Mr. HUGENS's : for it would totally remove the influences of any external motion ; by which means *every advantage of a heavy Ballance and strong Spring* might be introduced, even into Pocket-watches.

483. The method proposed for diminishing the influence of external motion by increasing the train (468), is entirely free from the inconveniencies of Dr. Hook's (476) ; and if the influence of the oil, on the Ballance pivots, be increased in the *former*, as the number of Vibrations ; it is doubled in the *latter*, by having twice the number of pivots : and when we consider, that by shortening the time of Vibration, the influences of the external motion is also reduced (466) ; that if the time remained the same, the influences would be diminished, *as the weight of the Ballance to the strength of the Spring* (456) ; that when two Vibrations are performed during one motion of the ship ; *the one corrects the other* (465) : and hence, that it is, *the odd Vibrations only*, that are influenced ; and that, in the inverse duplicate ratio of its time, to that of the external motion (464, 465), that the more frequent (or quick) the Vibrations, *the more commensurable* do the times of two Vibrations become
to

to the time of one motion of the ship ; and if we add to this, that by thus diminishing the influences of external motion, we also diminish the proportion that the maintaining power bears to the whole motive force of the Ballance ; we shall see good reason for preferring this, to any other method, *so far as the nature of materials and oil will admit.*

INFLUENCE OF
EXTERNAL MO-
TION.

484. Having thus endeavoured to shew, how external motions influence the times of all portable machines ; and what are the advantages, &c. of *each method* of diminishing such influence* ; *I next enquire* into the advantages that may be gained by the different ways of increasing the momentum of a Ballance.

Conclusion.

* It has already been observed, that when any external motion *opposes* that of the Ballance, the utmost effect it can have is to stop the Watch. On the other hand, if it increases the motion of the Ballance, its utmost effect will be, to make the Ballance *BANK* ; i. e. to make it strike against the limits of its greatest Vibrations : for by this means several subsequent Vibrations are so much accelerated as to become very sensible to the ear. But this evil may be very much diminished, if not annihilated, by making the Ballance communicate its *excess of motion* to smaller ones, which have no concern with the measure of time, and against which the main Ballance is made to bank, as represented by the 4th Fig. of Plate 13th, where the small spiral Spring serves only to keep those Ballances to a certain position, in which the other may always find them.

Of

Of the Momentum of the Ballance.

Introduction.

485. Since the exertion of a Spring is as the space to which it is bent (408); *it follows*, that if no other force actuate the Ballance, its motive force will be, in all its Vibrations, as the length of the Vibration; and consequently, *the spaces described*, and the *motive force*, will be expressed by the same numbers.

Motive force of the Ballance.

486. And if in *half-timed Watches* the shortest Vibration, *that can allow the wheel to escape the pallets*, be expressed by one: the maintaining power will also be expressed by one (470), and the motive force of the Ballance, be equally composed of the action of the wheels, and Ballance Spring. *But*,

It bears a greater proportion to the action of the Ballance wheel in long than in short Vibrations.

487. If the Vibration be increased by the action of the wheels accumulated in the Ballance, as 2, 3, 4, 5, 6, &c. the exertion of the spiral Spring will increase in the same proportion (485); and the maintaining power (remaining the same) will only constitute $\frac{1}{3}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{1}{6}$, $\frac{1}{7}$; &c. of the motive force of the Ballance *. *Hence*,

* And since the proportion of the whole motive force of the Ballance to the maintaining power, is thus increased as the *length of the Vibration*, it follows, that every endeavour should be used to enlarge it; and that such changes as may happen in the maintaining power, will cause less error with long than short Vibrations (80).

488. Any

488. Any change that happens in the maintaining power, will bear a less proportion to the whole motive force of the Ballance, in its longer Vibrations than its shorter ones, and consequently (80), will less alter the times *.

MOMENTUM OF
THE BALLANCE.

489. The influence of external motion is also diminished, by increasing the *angle of Vibration* (464); therefore (488), every endeavour should be used to enlarge *it*, and to remove every cause that can have any tendency to diminish *it*: as friction, influence of the oil, and the resistance of the air; of which hereafter.

Influence of external motion least, in long Vibrations.

490 And thus it appears (488, 489), how advantageous it is, *to increase the MOMENTUM of the Ballance, by increasing its length of Vibration*; and the length of Vibration increases with the maintaining power: hence, &c.

Conclusion, relative to the advantage of long Vibrations.

491. But the velocity, and consequently the MOMENTUM of a Ballance, may be increased, *by enlarging its diameter*: and though this method *does not diminish the influence of external motion*, it does the risque of breaking or bending the Ballance pivots, by a fall or any other violent motion; but if the friction on the pivots be di-

Increased by augmenting the diameter of the Ballance, &c.

* On this account, when the oil becomes glutinous on the Ballance pivots, the Vibrations become shorter, and sensibly quicker, even though the diminution of recoil has a contrary tendency.

minished

MOMENTUM OF
THE BALLANCE.

Increased by augmenting the weight of the Ballance, &c.

Both ways compared, &c.

Increased by the number of beats, with the advantages therefrom.

minished by this means, *the resistance of the air is augmented* *.

492. Since the MOMENTUM *is as the quantity of matter into the velocity*, it may be augmented by increasing the *former*, as well as the *latter*: hence, a Ballance of twice the weight *will (c. p.) have double* MOMENTUM; and an equal effect in correcting the irregularities of the maintaining power, as one of twice the diameter, and half the weight.

493. And if the friction on the pivots be increased as the weight †, the resistance of the air will be diminished in the *duplicate* proportion of the diameter ‡: hence the only article which renders this method of increasing the momentum inferior to the former (491), is the greater risk of the pivots, by falls, &c.

494. *Lastly*, if the MOMENTUM be augmented by increasing the strength of the Ballance Spring, *and consequently the number of beats*; it

* And unless all the Vibrations of the Ballance and Spring are truly isochronal in their detached state, and the maintaining power be so applied as not to disturb those natural properties, any change that happens in the density of the air, will, by altering the length of the Vibrations, introduce such errors; and that more or less, (*c. p.*) in proportion to the total increase of resistance.

† The friction on the Ballance pivots may be much diminished, by applying two Springs to the Ballance, attached to its collet, diametrically opposite to each other, as in Plate 12. Fig. 4.

‡ See Note 491.

will

will have all the advantages of the former methods in correcting the effects of any irregularities of the maintaining power: and, if it increases the friction on the pivots, and the resistance of the air; it diminishes the influence of external motion (469), to such a degree, as to prevent the danger of a Watch setting in the pocket: and by that means paves the way for such increase of momentum, by either or both the methods last mentioned (491, 492), as may give to the Balance in Watches, the same advantages in regulating the motion of the Wheels, as Pendulums have in Clocks.

495. *And thus*, may the performance of Watches be made, in this respect, to approximate that of Clocks, as much as the nature of things can probably admit: and if due regard be paid to what has been formerly said concerning the influence of external motion (451), any further attempts of diminishing its effect on machines carried on ship-board, will be rendered unnecessary, even for the nicer purposes of navigation.

Conclusion.

Of the THERMOMETER.

496. In order the better to investigate the real effect of each particular cause, *the temperature of the air, has hitherto been considered as invariably the same*; but now, the effect of such

Y

changes

Introduction.

changes as happen therein, together with the most effectual means of removing them, claim our whole attention.

Influence on the
main Spring.

497. Heat dilates, and cold contracts all metals; hence, the main Springs of Watches, &c. act more or less vigorously in proportion to the degree of heat or cold to which they are exposed: and if no other cause of error took place in Watches, *with pallets of the common construction*, they would go *faster in cold* than in warm weather.

On the oil.

498. *Cold* renders oil thick, and *warmth* makes it more fluid: and if this cause alone, took place, it would (by an increase of the maintaining power), make Watches go *faster in warm* weather than in cold. But,

Those two influences oppose each other, &c.

499. *As the immediate influence of heat, on the main Spring*, tends to diminish the maintaining power (497), and its influence on the oil applied to the pivots, to increase it (498), those two errors must, at least in part, correct each other: and the effect that any remainder thereof would have on the measure of time, may be totally annihilated, by constructing the pallets, so that the *maintaining power*, shall prolong the time of one half the Vibration, as much as it contracts the other. *Of which hereafter,*

Influence on the
Ballance and
Spring.

500. *Heat* lengthens the Ballance Spring, and enlarges the diameter of the Ballance, both which effects co-operate in making the Watch go slower;

flower ; and the contrary ; and as those effects are wholly independent of the pallets, they must be corrected by some other means.

OF THE THER-
MOMETER.

501. *The time of Vibration of a Ballance depends* (c. p.) on the length of *such part* of its Spring as acts in the Vibration, without regard to its whole length : and therefore, if the same cause, that enlarges the diameter of the Ballance be made to shorten the acting part of the Spring in a due proportion ; and the contrary ; the times of Vibration will remain the same.

The time of Vibration does not depend on the whole length of the Ballance Spring.

502. I shall therefore here describe one method of adjusting the length of the Spring to the diameter of the Ballance, in such manner, as will render the times of Vibration equal, *without regard to the degree of heat or cold* to which the Watch is exposed : and though the THERMOMETER here to be described, is adapted to an uncommon construction of a Watch, wherein the Spring lies above the Ballance ; when the principle is properly understood, the ingenious mechanic will easily diversify the contrivance, so as to suit his particular purpose.

Introduction to the description of the Thermometer.

503. Fig. 1. Plate 14. is a steel ring with several pins to it ; on which are fitted as many small rollers as represented in Fig. 2 ; to this steel ring is screwed one of brass, cut as represented in the same Figure, and made by its elastic force to press against each of the small rollers, which limit the extent of its circumference.

PLATE XIV.

Description.

Y 2

504. Now

IMPROVEMENT OF

PLATE XIV.
FIG. 2.

504. Now as the expansion of brass exceeds that of steel, it is evident, that any heat applied to this double ring, will bring the ends of the brass ring nearer to each other; and cold will have a contrary effect: and since the one end is screwed to the steel, its excess of expansion or contraction will become very sensible at the other end; and may be ascertained to a nicety, by applying a slender Index, as represented by the dotted lines in Fig. 2. And

FIG. 3.

505. If this brass ring be made to act on the one end of a lever (moving concentric to the Ballance), and to the other end of which, the ballance Spring is attached (as represented in Fig. 3.); the expansions and contractions of the brass ring may be made to move the Ballance Spring between two pins, so as to limit its action in such manner as will render its exertion, in all cases, proportioned to the diameter of the Ballance, and by such means, render the Vibrations (so far as depends on this cause) isochronal: The lever on which the brass ring acts, and to which the Ballance Spring is attached, together with the Ballance Spring, and the pins which limit its action, are represented by Fig. 4. detached from all the other parts; and those pins may be rendered moveable, so as to regulate the Watch, without any how hurting the effect of the Thermometer.

FIG. 4.

506. Fig.

506. Fig. 5. represents a method of increasing or diminishing the influence of the Thermometer (without stopping the Watch), till the performance in different degrees of heat and cold, prove it equal to its intended purpose: here the brass ring (503), acts on the lever to which the Ballance Spring is connected, *by means of another lever*, whose center of motion is moveable by the screw at A, so as to alter the effect, at pleasure.

507. Fig. 6. with its appendages, represent separately, and in different views, the levers, &c. of which Fig. 5. consists (excepting the parts represented by Fig. 2.) — Fig. 7. is a section of Fig. 5. along the line A B.

508. The advantages of this Thermometer are, that as all parts, of the surface of the brass ring are fully exposed to the same air, that influences the Ballance and its Spring; it will be influenced thereby, at the same instant with them: and, if it be made of *a mean thickness between that of the Ballance and its Spring*, with proper allowance for the greater motion of the Ballance*; the influences of heat and cold on it, will *exactly keep pace with*, and *equal* those on the Ballance and its Spring: which can never happen with Thermometers, that only expose

Advantages of this
Thermometer.

* See the properties of Clock Thermometers (328, to 331).

OF THE THER-
MOMETER.

part of their surface to the air, and are so connected with larger masses of metal, that they can only be heated or cooled with them; and consequently, cannot apply the remedy before the evil has had its effect, at least for some short time. And,

Advantages of this
Thermometer.

509. The performance of such Thermometers will also be less liable to decay, through course of time, than in such as have not all the parts of their metal, equally compressed or relaxed by any changes that may happen in the temperature of the air. And,

Influence of the
air on the time of
Vibration.

510. As the different densities of the air, have a tendency to alter the length of Vibration, and by that means introduce such remains of error as may yet take place, from a want of absolute natural isochronism in the Ballance Spring: it is proper here to observe, that as such *density of the air* depends in a great measure, on the degree of heat or cold; its influences on the times of Vibration must have an uniform tendency, either to increase or diminish such errors as arise from the influence of heat and cold on the Ballance and its Spring: and consequently while such error is in any degree sensible, it may be corrected by the Thermometer (506.)

Conclusion.

511. FROM ALL WHICH IT WOULD APPEAR; *that the influences of heat and cold, may be very nearly, if not altogether as much corrected in*
Watches

Watches as in Clocks * ; and the exertion of the Ballance Spring made to preserve the same proportion to the *vis insita* of the Ballance, as much as the exertion of gravity does to the *vis insita* of the Pendulum ; and consequently the Vibrations of the *former* be rendered as isochronal as those of the *latter*.

INFLUENCE OF
THE OIL.

512. I now come to consider, *several articles relative to the nature of pallets*, that may yet tend to influence the times of Vibration ; *and to point out reasons* why Watches constructed on the horizontal principle, must in their *present state*, perform much worse than contrate wheel Watches *if the principle of the former was only equal to that of the latter*.

513. It was formerly observed, that, *the influence of heat and cold on the oil*, was of a most pernicious nature, as no remedy could be applied by an opposition of the expansion of metals (155) ; *I therefore shall enquire* into the comparative degree in which *this influence* takes place in horizontal Watches, and those of the common recoiling principle.

Influence of the
oil, &c.

514. It was shewn in the former Essay (168), that the influence of the oil was always (*c. p.*) as the relative velocity of the parts to which it was applied : *and hence*, how it was to be esti-

How estimated.

* In Clocks, the influence of heat and cold may always be diminished, while they remain in any degree perceptible.

mated

mated on each part of any machine (169); the same method is observed in estimating its influences in the following table, where all the comparative dimensions of the *Pivots*, *Cylinder*, *Horizontal-wheel* and *Ballance*, are taken from an accurate measure of those parts, by the Sector.

515. A TABLE shewing the comparative influence of the oil on the pivots of each wheel in a Watch, with a train of 18,000.

Wheels.	Mean size of both pivots.	Number of Revolutions.	Influence of the oil.
First wheel	12	1	12
Minute wheel	6	4	24
Third wheel	2½	24	56
Fourth wheel	2½	240	600
Horizontal wheel	2	2400	4800

Comparative influence on the horizontal pivots.

416. Thus it appears, that the influence of the oil on the horizontal wheel pivots *alone*, is six times as great as on *all the others taken together*: therefore, if the influence on all the pivots be expressed by 7, that on the horizontal wheel will be 6; and the influence on all the others, *One* (515): And,

Influence of the Ballance pivots.

517. Because the horizontal wheel has 15 teeth, and *every tooth* has its push at *each edge* of the cylinder, it follows, that 30 Vibrations of the Ballance will be performed, for every revolution

volution of the wheel: and if, at a medium, we suppose the Ballance to move one third of a turn at each Vibration, *the motion of its pivots*, in 30 Vibrations (or one turn of the wheel), will be equal to *Ten entire revolutions*. Therefore,

INFLUENCE OF
THE OIL.

518. If the pivots of the Ballance, had been of equal size with those of the horizontal-wheel, *the influence of the oil on the former*, would be to that on the *latter*, as 10 to 1; but the diameter of the Ballance-pivots, are to those of the wheel, only as 3 to 4; and consequently, the influence on the former will only be to that of the latter, (in round numbers), as 7 to 1. And

To that on all the others in a Watch, as 7 to 1.

519. The comparative influence on all the pivots of a Watch, may be expressed as follows.

Comparative, on all the pivots of horizontal Watches.

On the pi-	1, 2, 3 and 4 wheels together	1
vots of the	Horizontal wheel	6
	Ballance	42
		—
On all the pivots together.		49

520. And as the sizes of the pivots, and number of revolutions, are the same in contrate wheel Watches, as in horizontal ones with the same number of beats; the influences of the oil would be equal on the pivots in each, *if no recoil took place*: but let us on account of the recoil (or retrograde motion) suppose the influence on all the pivots of the wheels in the contrate Watch

Influence increased by a recoil.

Z

to

to be doubled ; then will the *total influence* of the oil on such a Watch be expressed as below :
for no oil is applied to its pallets.

On the pivots of	{	The first 4 wheels	2
		The Ballance wheel	12
		The Ballance as formerly	42
			—
		Total	56

On contrate wheel
watches.

521. *And thus it appears*, that the total influence of the oil on all the pivots of a contrate wheel Watch, is greater than in a horizontal Watch : *but in the latter*, oil is applied to the cylinder, the influence of which is yet to be added to that of the pivots.

Influence on the
edges of the cylinder,
&c.

522. The influence of the oil on the *acting part* of the horizontal wheel, (i. e. *on the edges of the cylinder*), will be, to the influence on its pivots, at least as the diameter of the wheel to that of its pivots (172) ; *or nearly as 67 to 1* ; and consequently, if the influence on all the pivots be expressed as formerly by 49 (519), the influence on the edges of the cylinder will be 402. And,

523. If the Ballance be supposed as formerly (517) to vibrate $\frac{1}{3}$ of a turn ; the influence of the oil on the circular part of the cylinder, will at least equal that on its edges ; and consequently may at a mean be expressed also, by 402 : *and the whole*

whole influence of the oil on a horizontal Watch, as now constructed, will be as follows.

INFLUENCE OF
THE OIL.

On all its pivots	—	—	49
On the cylinder	—	—	804
			—
		Total	853

524. The whole influence of the oil in contrate wheel Watches, has already been stated at 56; therefore, the comparative influences on *horizontal* and *contrate wheel* Watches are as 853 to 56, or nearly as 15 to 1. HENCE, if the horizontal principle, was *only equal* to that of contrate wheel Watches with recoiling pallets, in all other respects, the errors in the performance of horizontal Watches, would be to the errors in contrate wheel Watches, as 15 to 1; but *experience proves the contrary*; and therefore, when the influence of the oil is rendered *equal in both*, the performance will clearly prove the superiority of the horizontal principle.

Comparative on
horizontal and
contrate wheel
Watches.

525. It is evident, that the influence of the oil on the cylinder is (*c. p.*) as *its diameter* (168): and as *it* may be diminished, by reducing the size of the horizontal wheel, or by increasing its number of teeth; *let us enquire into the particular advantages of each method.*

How diminished
on the cylinder.

526. FIRST, let the diameter of the wheel be diminished, as represented at E, 4, 2, 1, Plate
Z 2

As the diameter of
the wheel.

PLATE XV.

15.

INFLUENCE OF
THE OIL.

Friction not al-
tered.

Inversely as the
number of teeth.

15. then the cylinder, *and consequently* the influence of the oil on it, will be diminished in the same proportion; for the cylinders bear the same proportion to each other, as the wheel to which they are severally adapted; (as expressed by the numbers annexed) *. But

527. In this case, the friction, and consequently the danger of tearing the cylinder, remains unalterably the same; for the pressure of the tooth on the cylinder is increased, as the length of the tooth diminishes: as may easily be conceived by viewing Plate 15. at E, where the pressure is, (*c. p.*) inversely as the distance of each tooth from the center of motion; i. e. *inversely as the diameter of each Wheel.*

528. Let us then suppose, the number of teeth in the horizontal wheel increased; it is plain, that the length of each must be diminished as their number increases: and the diameter of the cylinder will also be diminished as the length

* The Figure in Plate 16. represents the manner in which the horizontal wheel acts on the cylinder; for when the tooth B has done acting on the edge of the cylinder, the tooth C drops on its outer circumference, on which it rests, till the Vibration is performed, and the other edge of the cylinder comes within its sphere of action; when it will begin to act wedge-like, and continue till the edge of the cylinder gets without the external dotted circle, when the tooth will drop on the inner circumference, as represented by the dotted lines, (and by the cylinder at D); and thus it continues to act on the edges, and rest on the circumference of the cylinder alternately.

of the teeth ; and therefore, (522, 525), the influence of the oil on the cylinder, will be diminished in each Vibration, as the number of teeth increafes. *And*

INFLUENCE OF
THE OIL.

529. The friction in this case, is alfo diminished in each Vibration, in the inverfe proportion of the number of teeth : *for the joint friction of any number of fmall teeth*, rubbing on the edges of the cylinder, (c. p.) will be equal to *the friction on one tooth, that fubtends the fame angle at the center of the wheel* (527) : See Plate 15. E 4 ; and the friction on the circular part of the cylinder, is diminished in the fame proportion as that on its edges (528) ; *therefore*, the total friction, as well as influence of the oil on the cylinder *in each Vibration*, will be inverfely as the number of teeth in the horizontal wheel : *from which it naturally follows, that*

Friction in each
Vibration dimi-
nifhed in the fame
proportion.

530. *The train of a Watch may even be doubled*, without any how increafing friction or influences of the oil on any part of the Watch ; *the Ballance pivots excepted* : and thus may heavy Ballances and ftrong Ballance Springs be introduced, without the risk of fetting, or danger of tearing the cylinder, any more than with a common train (471), &c. Or,

Advantages of this
method.

531. *If the train remain the fame*, the influence of the oil and friction, will be diminished in every part of the Watch (Ballance pivots excepted) as the number of teeth of the horizontal wheel

OF PALLETS, &c.

wheel increafes : thus, if the number of teeth in the horizontal wheel be doubled, and the train remains the fame ; the influence of the oil on the cylinder will be reduced to a half (529) ; and the revolutions of all the wheels, and confequently the friction, and influence of the oil on all the pivots, *will undergo an equal diminution.*
Or,

✓ 532. If the train and number of revolutions of each wheel, be continued the fame ; the leaves of the pinions may be increafed in the fame proportion as the teeth of the *horizontal wheel* ; and this will increafe the action of *that* wheel on the cylinder ; and confequently enlarge the Vibrations, as well as diminifh the influence of the oil on the cylinder (529) *.

Conclufion.

533. *From all which confiderations it appears,* that it is much more advantageous to increafe the number of teeth of the horizontal wheel, than to diminifh its diameter.

Inconveniencies of the horizontal wheel now ufed.

PLATE XV.

534. In the horizontal wheel now univerfally ufed, each tooth is formed into an inclined plane or wedge, as represented in Plate 15. which acts on the edges of the cylinder, and by that means maintains the Vibrations ; and thefe teeth

* The friction, and irregularity of action in pinions, are diminifhed as the verfed fines of the angles fubtended by their leaves : thus, the friction and irregularities of action in a pinion of 6, is to that in a pinion of 9, as 2 to 1 nearly ; and to that in one of 12, nearly as 4 to 1.

after

after performing their office, rest alternately on the *internal* and *external* circumference of the cylinder ; *and therefore*, the friction and influence of the oil on the cylinder, during the time of rest of the wheel, will (*c. p.*) be as the *mean circumference* of the cylinder.

OF PALLETS, &c.

535. But the inside diameter of the cylinder, must be somewhat more than the length of the tooth, and the outside will be yet increased by the necessary thickness of the cylinder ; therefore its mean diameter cannot with this construction of a wheel be reduced to such a degree as will render the application of oil unnecessary. But,

536. If the cylinder be made so thick as to admit of having that inclination formed on its edges, which is now formed on the face of the tooth ; the teeth may then be made straight without any wedge, and of the size of a small needle ; and this will admit of an equal diminution of the inside diameter of the cylinder, which will occasion a proportional decrease of friction, during the rest of the wheel thereon. And,

How remedied.

537. *If the teeth of such wheel*, be formed alternately on *each side thereof*, (as in Fig. 3. Plate 16.) they may always be made to rest on the inside circumference of the cylinder, thus reduced (comparatively to a point) ; and by this means, the friction on the cylinder, during the time of rest, will be so much reduced, as not to require the

Rest performed on the inside of the cylinder.

PLATE XVI.
FIG. 1.

OF PALLETS, &c.

Advantages of
such alteration,
&c.

Conclusion.

PLATE XVI.

FIG. 1.

Any power co-
operating with
the Ballance
Spring, will acce-
lerate the Vibra-
tions.

And the contrary.

the application of oil ; nor will the application of it, during the time of action of the wheel, be more necessary here, than in the common recoiling pallets.

538. And this will improve the performance, not only by removing the influence of the oil from the cylinder, so as to bring horizontal Watches in that respect, on a par with those of the common construction (524) ; but also by diminishing the friction on the cylinder, so as to make the same maintaining power support a much longer Vibration ; *the advantages of which* have already been considered (488), 489).

539. And if such a horizontal wheel, as here described and represented in Plate 16. Fig. 1. be made of well tempered steel, and the parts of action of the cylinder of steel thoroughly hard, or diamond, the performance of such machine, will prove the superiority of the horizontal principle to any other.

540. Since the spiral Spring *promotes the motion of the Ballance towards its point of rest, and opposes its recess therefrom* ; it is plain, that if any other power be made to act on the Ballance *in the same manner*, it will have a similar effect on the times of Vibration, *as an increase of strength in the Spring would have* ; i. e. it will shorten the times. *And*

541. If the same power be applied, *so as to oppose the motion of the Ballance towards its point of*

of rest, and promote the motion therefrom, it will, by such means, *counteract* the exertion of the Spring (411), as much as it assisted in the former case (540); and therefore, will have a contrary effect; i. e. *it will prolong the times of Vibration.* And thus;

542. If the action of the horizontal wheel, be so applied to the edges of the cylinder, *that it shall co-operate with the Ballance Spring in its unbending*, just as much as it *counteracts it in bending* (411), the one half of its action will *contract* the time of Vibration (540), as much as the other *prolongs* it (541); and consequently, those equal and contrary effects will always *balance* each other, and leave the whole time of Vibration the same, as if no such cause took place. Hence, such changes as happen in the action of the wheel on the pallets, cannot alter the times of Vibration.

OF PALLETS, &c.

Those effects
being made equal,
and contrary, will
destroy each other.

543. EXAMPLE. Let there be supposed two concentric circles passing through the extremities of the parts of action of the horizontal wheel, as represented by the dotted lines in Plate 15. it is evident, that the wheel can only act on the edges of the cylinder, while they remain within those circles; and if their distance be divided into two equal parts as at A, and another circle be drawn through that point; the edges of the cylinder when at rest, should terminate in that circle, as represented also at A; in which case, the

Illustrated.

PLATE XV.

A a

maintaining

OF PALLETS, &c.

maintaining power would prolong the time of the one half of the Vibration (542), just as much as it contracted the other. But,

544. If the edges of the cylinder rest within this circle, as at G, the maintaining power will prolong the one half of the Vibration (540), more than it contracts the other (541), in proportion as the edges of the cylinder lie nearer the inner circle, than the outer ; See Plate 15. at G: and consequently, the whole Vibration will take up more time than if performed by the action of the Ballance Spring *only* ; and *this effect* of the maintaining power, will become *greater* as the Vibrations become *shorter* (as shall be shewn hereafter), and produce the same effect on the measure of time, *as if* the shorter Vibrations of the Ballance, when actuated by its Spring alone, were naturally slower than the longer ones *: and this is the case in all horizontal watches ; for if the edges of the cylinder were to rest in the circle, as at A, the points of the teeth would not drop on the circular part of the cylinder, (as at C and D), but on its edge ; which would check the Vibration, and produce the most destructive effect.

Length of Vibration, as the velocity at the lowest point, &c.

545. The length of Vibration in Pendulums, (*c. p.*) depends on their velocity at the point of rest, (i. e. at their lowest point), and the time

* And thus will every change in the action of the wheels, or any other cause that can alter the angle of Vibration, also alter the times.

of the subsequent ascent will be the same, whether such velocity was the *sole effect* of GRAVITY, or the *joint effect* of IT and the *action of the wheels* in the preceding descent *; and the time of the subsequent descent cannot be influenced by the action of the wheels, before such action takes place; it therefore follows †, That,

546. *The influence of the maintaining power on the measure of time*, is, (c. p.) *as the time of its action* (545); nor will its effect in maintaining the Vibrations, be any how lessened by shortening its time of action ‡, and all this, as appli-

OF PALLETS, &c.

Influence of the maintaining power, as its time of action.

Sensibly Lessened

* See Sir ISAAC NEWTON's 4th Definition, where he says, "An impressed force remains no longer in a body, than its action continues; for a body maintains every new state it acquires by its *vis insita* only."

† It also follows, from those considerations, that it is more adviseable, in Clocks, to apply the action of the wheels to the Pendulum, in the time of its ascent than descent; and in Watches, in the time of bending, than the time of unbending the Ballance Spring: for if such action be applied in the time of ascent, its effect on the measure of time ceases with the action; but whatever power adds to the velocity of the Pendulum, &c. in its descent, will influence the time of all the subsequent part of the descent: and for the same reason, it will hurt the performance, to make the maintaining power act more *vigorously* at the beginning than towards the end of descent. (See the Notes to 226.)

‡ See Sir ISAAC NEWTON's Second Law of motion; where he says, "If any force generates a motion, a double force will generate a double motion, a triple force a triple motion, whether that force be impressed altogether and at once, or gradually and successively." I have already (440) endeavoured to shew how the bad effects of the *vis inertiae* of the wheels are to be diminished, and therefore take no notice of it here.

OF PALLETS, &c.

Principle on
which the main-
taining power
cannot alter the
time of Vibration.

Introduction to
further considera-
tions, &c.

cable to the Vibrations of the Ballance, as those of the Pendulum (413).

547. *And thus*, by making a horizontal wheel that will act on the cylinder, *just as much* in the time of *bending the Ballance Spring*, as in the time of *its unbending* * ; the maintaining power may be made to prolong the time of one half the Vibration (541), as much as it contracts the other (540); and *if the least defect yet remains* owing to the execution, &c. *its effect* may be diminished by shortening the time of action of the wheel on the cylinder (546); and by those joint means, the performance may be rendered more compleat IN WATCHES (so far as depends on the maintaining power), *than in Clocks where the influence of the oil takes place* †. But,

548. Having already shewn reason (544), why all horizontal watches hitherto made, or that can be made, with the wheel and cylinder, now in use, must have their Vibrations somewhat slower than if the Ballance was actuated by its Spring alone : and why this effect must become

* That is, that the action of the wheel on the Ballance be equally applied on each side the point of rest; or that the wheel act as much on the *Ballance* in the time of *its* approach to its point of rest, as in the time of its recess therefrom.

† Here it is to be noted, that as the influences of heat and cold on the oil, main Spring, and Fusee, only tend to increase or diminish the *maintaining power*, their effects on the times of Vibration are totally removed by this method of applying *it* to the Ballance.

greater

greater in the shorter Vibrations, than in the longer ones (546) *. I now come to a more particular consideration of a wheel and pallets, that will admit of removing this defect, as well as the influence of the oil; *and by that means leave the Vibrations of the Ballance and Spring in full possession of all their natural properties.*

549. Fig. 1. Plate 16. represents a scapement consisting of one pallet and a detent, by means of which the wheel acts on the Ballance, at *every second Vibration only*; this scapement, if judiciously executed, will have the properties formerly mentioned (547), and admit of very quick Vibrations, as the time of action of the wheel bears so small a proportion to its time of rest; and the inside diameter of the detent and pallet may be made so very small (in proportion to the mean diameter of common cylinders), as almost to annihilate friction, and the influences of the oil during the time of rest (526); by which means, the Vibration will be much increased; *and hence*, a double advantage acquired, even though the use of oil should yet be found necessary †.

Description of a new scapement.

PLATE XVI.

550. This scapement will also serve to prove *experimentally*, what has been said concerning the

Uses of this scapement.

* For which reason every cause that can alter the length of the Vibrations, will also alter their times.

† In this scapement all the teeth of the horizontal wheel stand on one side, as represented by Fig. 2.

OF PALLETS, &c.

nature of scapements (540, 541), and how much the effects of the maintaining power on the times of Vibrations of different lengths, *have hitherto been mistaken for the natural tendency of the Ballance and Spring.*

Experiment.

Longer Vibrations
rendered quickest.

PLATE XVI.

551. If the pallet be in the position represented at A, Fig. 1. when the Ballance is at rest, *the action of the wheel will tend to prolong the time of Vibration* (541); and this effect will be greatest on the shorter Vibrations (546); hence, if the natural tendency of the Vibrations be isochronal, the action of the wheel on the pallets will render *the shorter Vibrations of longer duration than the longer*; and all the Vibrations slower than they would be performed by the sole exertion of the Ballance Spring.

Experiment.

Longer Vibrations
rendered slowest.

PLATE XVI.

552. Let the pallet be in the position represented at C, when the Ballance is at rest; and *the action of the wheel will shorten the time of Vibration* (540), and render them quicker than if performed by the exertion of the Ballance Spring alone; and this accelerating effect also will be greatest in the shorter Vibrations (546); and consequently,

consequently, if all the Vibrations of the Ballance were naturally isochronal, the action of the wheels would, in this case, render the *longer Vibrations slower than the shorter* : how absurd then is it ! to form a conclusion of the *natural tendency* of the longer and shorter Vibrations of the Ballance and Spring, while such foreign and *unobserved* causes influence them.

OF PALLETS, &c.

Experiment.

553. *Lastly*, if when the Ballance is at rest, the pallet be in the position represented at B ; the one half of the action of the wheel on the pallet will be exerted, while the Ballance Spring is *unbending*, and the other half, *while bending* ; and consequently, the former half will contract (540), as much as the latter prolongs (541), the time of Vibration, and the *whole time* will be the same, as if the Ballance was actuated by *its Spring alone*, without any regard to the force, with which the wheel acts on the pallet *.

All the Vibrations have their natural properties, &c.

PLATE XVI.

554. By the above means we may *not only* discover the NATURAL TENDENCIES of the longer

How the defects of the Ballance Spring may be remedied.

* The only inconvenience of this scapement, so far as occurs to me, is, that the interval between the beats will be alternately long and short : but this will in no degree influence the measure of time, or render the Watch less fit for observations of any kind ; for those two beats which come close to each other, may be considered as one.

and

OF PALLETS, &c.

and shorter Vibrations of any Ballance and Spring when no maintaining power is applied (553) ; *but the natural tendency being once known*, if the longer Vibrations be quicker than the shorter, or the shorter quicker than the longer, they may be corrected by altering the position of the pallet as already mentioned (551, 552) †.

Introduction to
another scapement.

555. *Having pointed out the means, by which the natural properties of the Ballance and Spring may be preserved, by a proper attention to the position of the pallet (where one only is used) (553), I now come to consider the means of preserving and recovering them, where two pallets are used, and the wheel acts in every Vibration.*

Description, &c.
of the curve of
action.

PLATE XVI.

556. Fig. 4. Plate 16. shews the nature of the curve, into which the edge of the cylinder is to be formed: from which it appears, that *the wheel has an equal power of moving the Ballance, on whatever part of this curve it acts* ; for if the cylinder be made to move through equal spaces, as marked on the Arc A B, the wheel will advance equal spaces, as marked on the line A D ; and it is to be understood, that the scapement in Fig. 1. as well as the following ones, has this property.

† And what is here said, relative to the position of this *one* pallet, is equally applicable to each pallet, where two are used : and if the relative position of the pallets to each other could be altered, the effect would be as above stated.

557. Fig.

557. Fig. 5. represents the relative position of OF PALLETS, &c. both edges of the cylinder, when the wheel is made to act at each Vibration; and its teeth stand alternately to each side, as in Fig. 3. where it appears, that the same central angle ACB , subtends both the curves on the edges of the cylinder; and that those curves cross each other, exactly at half the thickness of the cylinder; *without which*, the natural tendency of the Vibrations will be disturbed (553).

Relative position of the edges of the cylinder.

558. Here it is to be observed, that as the effect of any imperfection of the maintaining power, is increased or diminished, with the angle which the curve of action on the edge of the cylinder subtends at the center (546); such angle should be diminished, where the *true measure of time* is the chief object of our attention; and *increased*, where we desire by experiments to prove, the theory of pallets and Ballance Springs *.

When the time of action should be rendered long, and when short.

559. It is also to be observed; that when two pallets are used, (*i. e.* when the wheels acts on both edges of the same cylinder) the comparative times of the longer and shorter Vibrations, cannot be altered as with the scapement, Fig. 1. PLATE XVI. (551, 552).

Observation.

* Here it is to be observed, that by increasing or diminishing the angle subtended by the curve of action of the pallet, (*i. e.* the angle of scapement) the time of action of the maintaining power is also increased or diminished.

B b

560. If

OF PALLETS, &c.

Practice cannot, in this respect, equal theory.

560. If execution could be supposed equal to mathematical demonstration, and the teeth of the horizontal wheel as fine as a mathematical line, we might in practice, as well as in theory, preserve the natural properties of the Vibrations, by the means proposed in paragraph (542), and represented by Fig. 5. But as the teeth must have some small thickness, and we must carefully guard against their dropping on the edge (or part of action) of the cylinder, we cannot perfectly preserve the natural properties of the Ballance and Spring, with this construction of pallets; but be in a less degree liable to the retardation, which was said to take place in the common horizontal wheel (544) *.

How those inconveniencies may be avoided.

561. *I therefore come to enquire, by what construction of pallets those inconveniencies may be avoided, and the wheel made to act at each Vibration? i. e. on both edges of the cylinder.*

* Mr. Lepaute, an ingenious French Clockmaker, in his Treatise, published at Paris 1755, describes a construction of pallets of his invention, in which the tooth rests on the inside of the cylinder at each Vibration; by which means, the friction on it, during the time of rest, is very much diminished, and consequently a very considerable advantage gained. But the action of the wheel tends, in his construction, to retard the Vibration, during *its whole time of action*; and this effect will always increase or diminish, in proportion to the length of Vibration, and every cause that can alter the length of Vibration will alter the times; nor has any attempt been ever yet made to obviate this evil, so far as consists with my knowledge.

562. Let

562. Let us then suppose, that the curves on the edges of the cylinder, subtend different angles at the center, as A E B, B E C, Fig. 6. and let the dotted line E B, represent part of the dotted Arc which circumscribes the points of the teeth of the wheel, as at A, Fig. 1. it is evident (551), that the whole action of the wheel on each pallet, will prolong the times of Vibration: but as the angle B K C, subtended by the edge of the cylinder, Fig. 7. may easily be known, we may find another angle E K D *, which the Ballance will be thrice as long in describing: then if L G, be made equal to $\frac{1}{2}$ of F D, and *the* CURVE G F, be formed in the same manner as the curve A D, (or D B, Fig. 4.) *the action of the wheel* on IT will accelerate each Vibration, as much as *it* retards on the curve A D. For

OF PALLETS, &c.

Construction of
the Figure.

PLATE XVI.
FIG. 6.

563. If the power of the wheel in moving the Ballance, was as great on the curve G F, as on A D, (or A B,) the effects on each would be as the relative times of action (446); and each time of action on the curve G F, is (by the hypothesis) thrice as long, as the time of action on the edge of the pallet A D; and the wheel acts on G F, both in the progress of the Ballance towards the extremity of Vibration, and in its return, where-

Demonstration.

* See (408), where the properties of the Vibrations of the Ballance and Spring are shewn to be the same with those of a Pendulum vibrating in the cycloid, &c.

OF PALLETS, &c.

as it acts on A D, *only once in each Vibration*: therefore, the whole time of action on G F, is to the whole time of action on A D, in each Vibration, as 6 to 1. But when a cause is uniformly exerted, the effect will be as the times: hence, if the wheel had the same power of moving the Ballance on the curve G F, that it has on A D, the acceleration on the former, would be six times as great as the retardation on the latter: but the power of the wheel on G F, is to its power on A D, as L G, to F D; *that is, as 1 to 6.* therefore, *the powers being in each inversely as their times of action,* the effects will be equal. *Consequently*

Conclusion:

564. Whatever be the action of the wheels *on pallets of such construction,* it will as much accelerate (*i. e.* contract) the one part of the time of Vibration, as it prolongs the other: and the whole time of any Vibration, of whatever length, will be the same, *as if performed by the sole exertion of the Ballance Spring.*

C O R O L L A R Y.

565. If the curve G F, was continued till it terminated in the center (as represented by the dotted line), the acceleration would constantly increase as the Vibration; but the retardation on A D, is diminished as the Vibration increases

(446); *and therefore*, so soon as the angle of Vibration becomes greater, than twice the angle E K C, the whole time of Vibration would be contracted, and that in proportion to the increase of Vibration: and this shews the necessity of discontinuing the curve F G, at G, and substituting the circular Arc G I M, which should subtend an angle at least equal to the greatest fluctuations of the Vibration.

OF PALLETS, &c.

566. What is above demonstrated of the inside of a cylinder, is equally applicable to the outside, as on the tumbling pallets: but as the wheel has not in them, an equal power of moving the Ballance in every part of its action, the demonstration will not apply: it is also to be observed, that when those pallets are made to have such a proportion to the wheel, that its teech shall act nearly at right angles to the circumference of the cylinder, during the time of rest, *the time of action on the pallets, will bear too great a proportion to the time of rest* (446); by which means, the effect which any external motion or alteration in the action of the wheels, will have on the measure of time, will also be increased, *as well as* the chances of the Watch's stopping by the influence of any external motion: for which reasons I thought it unnecessary here, to give a particular description of them; the necessary remarks on pallets having already far exceeded my intended limits: nor does it appear to me, that any one, who fully understands what

The same demonstration would, c. p. apply to the outside of a cylinder.

But does not in the tumbling pallets.

OF PALLETS, &c.

what has been said in this and preceding essays, can be at any loss, in estimating the merits of any particular construction of pallets, or in constructing new ones, to answer any particular purpose.

Of the Resistance of the Air.

Air, its density does not alter the motive force of the Ballance.

Hence cannot influence the times with perfect pallets, &c.

567. As the times of Vibration of a *Ballance*, have no dependence on gravitation, it follows, that no alteration in the specific gravity of the air, can alter *its motive force*, as it does that of Pendulums (378). *Therefore*,

568. Any alteration of density in the air, can only influence the Vibrations of a Ballance, by shortening the Vibration in proportion to the increase of density: nor can such changes in the length of Vibration, alter its whole time any any other ways, than by introducing any remaining imperfection of the Ballance Spring or pallets; (for it prolongs one half as much as it contracts the other) (238, 129). *Hence*,

569. If the Ballance Spring have the natural tendency to perform all its Vibrations in equal times, and the pallets have the properties described (553, 564); *no alteration of density in the air, can any how alter the times of Vibration.* But,

In what cases it does alter the times.

570. Admitting the natural properties of the Ballance Spring (408), if the maintaining power
has

has any tendency to render the times of the longer Vibrations, either quicker or slower than the times of the shorter (551, 552), and if this effect be corrected, by an unlimited recoil, (or inverted recoil), as represented by the dotted spiral line in Fig. 7. Plate 16. and described (565); I say such being the case, that any change of density of the air will alter *the times*, as well as lengths of the Vibrations; and for this reason, no curve of whatever kind subtending the angle of fluctuations, and having a tendency either to contract or prolong the time, can ever preserve, or recover the natural isochronism of the Vibrations of a Ballance (565).

571. *It also follows*, that where the natural tendency of the Vibration is isochronal, its properties can never be preserved without the dead-beat (565). *But*,

Dead-beat necessary.

572. If the maintaining power and angle of Vibration, be sufficiently increased (487, 488, 489), and the time of action of the wheels on the pallets diminished (546), and some regard paid to what is said (540, 541), a good performance may be procured, *even with pallets of less perfect construction*.

A good performance, with imperfect pallets.

573. But in all cases, where doubt or uncertainty take place, it is safest leaning to the DEAD-BEAT; for IT, *in conjunction with long Vibrations*, will always diminish an error of the maintaining power (263); whereas a recoil, of any

any kind, may have a direct contrary effect; and therefore, like dangerous medicines, are never to be administered, unless where it can be done by weight or measure.

Conclusion.

Having thus endeavoured to settle practical Theory of Clock-work, and to point out the means of acquiring such advantages in PORTABLE MACHINES, as may render their performance nearly equal to that of CLOCKS, even in their improved state; if I have any where misrepresented or omitted any thing material, it was not intentionally: but granting the truth of all that I have advanced, many are the experiments and practical improvements that may yet be made, towards confirming this Theory, and rendering it of general utility. And should this be thought an object worthy of public attention, I shall chearfully contribute my utmost endeavours.

T H E E N D.

I N D E X.

A.

N^o

<p><i>Accelerating effect</i>, of a recoil, increases, as twice the retrograde motion of the swing-wheel</p> <p>— is diminished by any increase of the density of the air : and the contrary</p> <p><i>Action</i>, of the wheels on the pallets, — in what cases it should be applied, regularly and successively</p> <p>— when it should be applied all at once</p> <p>— in either way</p> <p>— its effect, on the measure of time, <i>c. p.</i> as the whole time of action</p> <p>— in what cases its time of action should be rendered long or short in Watches</p> <p>— it may be applied so as to render the times of vibration either longer or shorter at pleasure</p> <p>— it should be applied in time of ascent rather than descent of the Pendulum</p> <p>— may have the same effect on the times of vibration, as if the longer ones were naturally quicker than the shorter : or the contrary</p> <p>— the influence of heat and cold on the main spring and chain, render it more perfect</p>	<p>238, 239</p> <p>226, 300 and Notes</p> <p>265</p> <p>266</p> <p>267</p> <p>546</p> <p>558</p> <p>238, 540, 541</p> <p>Note 545</p> <p>551, 552</p> <p>404</p>
C c	<i>Action,</i>

- Action*, the effect that any irregularity in it would have on the times of vibration : how corrected in the construction of the pallets 542, 547, 553, 560 to 564
- of a spring on the ballance, preferable to that of gravity — 410
- of the ballance spring : — how it may be preserved proportional to the diameter of the ballance. See *Thermometer*.
- Air*, its resistance, *c. p.* as the versed sines of the angle of vibration — 117
- its resistance contracts the times of ascent of the pendulum as much as it prolongs the times of its descent — 129, 238 and *Note*
- its constant uniform resistance does not affect the times of vibration — 27, 28, 115
- but its accidental changes of *density* may introduce other errors — 115, 568
- its uniform resistance renders long vibrations preferable to short ones — 116 to 120
- its total resistance, how rendered constantly uniform *Note* 300
- any alteration in its density has a two-fold effect on the time of pendulous vibrations, performed in the arch of a circle ; and these two effects do exactly ballance each other — 382
- any alteration in its density cannot, of itself, alter the times of vibrations of a Watch ballance 567 to 569
- but it may introduce errors, that are mistaken for its own natural effect — 568
- Angle of scapement*, in what cases it should be enlarged : and the contrary — 558

B.

- Ballance*, its properties compared with those of the pendulum — 405 to 412
- all its vibrations isochronal in theory — 408

- Ballance*, reasons why it will measure time better than any
pendulum that describes entire revolutions 411
 — its natural properties superior to those of the pendulum 108,
410
 — the effect, in it, changed into the cause, in each
vibration — — — 411
 — the advantages of increasing its momentum 485 to 495
 — by lengthening the vibration — — — 490
 — by increasing the train — — — 494
 — by enlarging its diameter — — — 491
 — by augmenting its weight — — — 492
 — all that has been said relative to the length of vibra-
tion of pendulums, &c. equally applicable to it 413
 — any change of latitude does not alter its times of vi-
bration *Note* 410
 — the natural tendency of its longer and shorter vibra-
tions could not hitherto be experimentally known
549 to 553
 — how discovered experimentally — — — 553
 — and preserved — — — 554
Ballance-spring, — its theory — — — 415 to 427
 — its action in the shortest possible vibration of Watches
that begin their own motion, only equal to that of
the ballance wheel on the pallets — — — 431
 — increasing its strength, always advantageous; but not
equally in all cases. See *Momentum*.
 — the means by which they may be rendered stronger
in Pocket-watches — — — 469, 477 *Note*
 — their defects, how discovered and remedied 554
 — its exertion may be constantly preserved, proportional
to the *vis insita* of the ballance. See *Infl. of heat*.
Banking, what, and how its effects remedied *Note* 484

<i>Circular pendulum</i> of Dr. Hook and Mr. Hugen's, can never measure time equal to the vibrating pendulum, or the ballance and spring — — —	411
<i>Circular vibrations</i> , (i. e. vibrations performed in circular arcs) correct those variations which any alterations of density in the air would occasion in the cycloidal curve — — —	382
<i>Clocks</i> , compared to Watches — — —	388
<i>Conclusion</i> — relative to the length of vibration in Clock-pendulums — — —	152
— relative to the method of winding every half minute in fixed spring Clocks — — —	221
— in portable machines — — —	402
— relative to the irregularities of the maintaining power — — —	300
— relative to every imperfection of Clock movements — — —	306
— relative to the influences of the air, on the times of vibration of Clock-pendulums, describing circular arcs — — —	382
— relative to the application of cycloidal cheeks — — —	383
— relative to the comparative properties of the pendulum and ballance — — —	429
— relative to Watches beginning their own vibrations — — —	432
— relative to the size of Watches — — —	441
— relative to the length of vibration in Watches — — —	490, 413
— relative to the influence of external motion — — —	483
— relative to increasing the momentum of the ballance — — —	495
— relative to the influences of heat and cold on Watches — — —	511
— relative to the number of teeth in horizontal wheels — — —	533
— relative to the horizontal principle — — —	539
— relative to the construction of Watch pallets — — —	574
— relative to the action of the wheels on the pallets — — —	564
— relative to the influences of the air on the times of vibration of Watch ballances — — —	569
— relative to the use of springs in pallets — — —	252, 253
	<i>Cycloidal</i>

I N D E X.

N^o

Cycloidal vibrations in Clock-pendulums, are hurtful even in theory ————— 383

D.

Dead-beat, its natural effects ————— 255 to 273
 ——— diminishes the natural error of circular vibrations 263
 ——— errors arising from other causes imputed to it 269, 270, 271
 ——— hitherto loaded with disadvantages 269 to 273, 524
 ——— no fair comparative tryal yet made of the effects of IT and the recoil ————— 268 to 273
 ——— absolutely necessary for preserving the natural properties of the vibrations of the ballance 571
Density of the air—the alterations that happen in it, do in the circular vibrations of Clock-pendulums correct themselves ————— 380 to 383
 ——— cannot alter the times of such vibration of a ballance, as are naturally isochronal, with pallets of a proper construction ————— 567 to 572
Disengaging all the wheels but one 216 to 223, 394 to 402
 ——— not advantageous in portable machines ————— 401

E.

External motion, its theory ————— 442 to 484
 ——— experiments, relative to its effect on Watches, &c. 445 to 457
 ——— curvilinear---only affects ————— 449
 ——— in what cases and proportion it affects 451, 453, 454
 ——— much greater in Pocket-watches, than in those that are carried on ship-board ————— 453
 ——— its effects, how diminished ————— 455, to 458
 ——— equal in all Watches having equal trains 458
 ——— Dr. Hook's method of diminishing its influence 474 to 478
External

I N D E X.

N^o

<i>External motion</i> , Mr. Hugen's method of diminishing its influence	478
— All the methods compared	481 to 484

F.

<i>Friction</i> on the pallets, how diminished	174, 184, 189, 190
— can never ballance the influences of the oil thereon	194
— on the horizontal wheel and cylinder	527 to 540

G.

<i>Gravity</i> , its action on the pendulum, only altered by a change of latitude	372
<i>Gridiron pendulum</i> , described	332 to 346
— how adjusted	343
— compared with Mr. Ellicott's (improved)	363 to 369

H.

<i>Half-timing</i> ,—what	470
<i>Harrison</i> , Mr. John, ingenious pallets invented by him	225 to 232, and from 245 to 253
<i>Heat and cold</i> —the effect of their influence on Watch main springs, chains, fusees, and the oil applied to the main spring, and all the pivots of the wheels, is corrected by a proper construction of pallets	564
— their influence on the pendulum	316 to 372
— on the ballance and its spring	500
— on the main spring	Note 404
— on the fusee, &c.	Note 404
— on the oil	498
— on the air	510
<i>Hindley</i> , Mr. of York, ditto by him	225 to 232, and from 245 to 253
<i>Horizontal wheel</i> —its nature explained, &c.	525 to 548
<i>Hugen</i> , Mr. his method of winding up every half minute	216 to 223, 394 to 403
	<i>Influence</i>

I N D E X.

N^o.

I.

- Influence*—of heat and cold. See *Heat*.
 — of the oil. See *Oil*.
 — of the maintaining power. See *Maintaining power*.
 — of external motion. See *External motion*.

L.

- Long vibrations* have a duplicate advantage in correcting the
 irregularities of the maintaining power 41, 47
Long pallets—hurtful where friction takes place and oil is
 applied ————— 189, 190, 206, 207
 — but are advantageous where no friction takes place
 Note 265, 266, 546

M.

- Magnetic attraction*, its effect hurtful in pallets — 285
Maintaining power, — what ————— 27
 — considerations relative to it in Clocks 163 to 166
 — in what case it should be applied gradually in Clocks 265
 — in Watches ————— 559
 — in what cases it should be applied all at once in Clocks 266
 — in Watches ————— 558
 — in what case it may applied in Clocks in either way 267
 — its effects on the times of vibration of a ballance, mis-
 taken for the natural tendency of such vibrations
 550 to 552
 — its effect on the time, c. p. as the distance at which it
 is applied from the lowest point of vibration Note 546
 — why it should be applied in time of ascent of the pen-
 dulum ————— Note 546
 — on the length of vibration: as its quantity, independent
 of its time or place of action ————— 545
 — how rendered perfectly uniform in Clocks 300
 — how it affects the natural times of vibration 540 to 545
 Maintaining

I N D E X.

	N ^o
<i>Maintaining power</i> , its effect on the times of vibration c. p. as its time of action ————	546
— how it may be applied in Watches, or other portable machines, so as not to alter the natural times of vi- bration ————	543 to 565
— increasing it very advantageous in Clocks ————	158 to 164
— in Watches ————	413, 464, 490
— the most perfect rendered irregular by using springs in the pallets ————	246, 247
— rendered more uniform in Watches, by the influence of heat and cold on the main spring ————	Note 404
— increasing its action towards the extremity of the vibration hurtful ————	Note 545
<i>Main spring</i> , conclusion relative to the effects of its imperfec- tions in Watches, &c. ————	404
<i>Mercurial pendulum</i> , its disadvantages ————	326
<i>Momentum</i> of Clock-pendulums how increased ————	84 to 89
— table of it ————	87
<i>Momentum</i> of the ballance See <i>Ballance</i> .	
<i>Motion</i> , external, its influences on the times of vibration See <i>External motion</i> .	

O.

<i>Oil</i> , — its influences—of a very hurtful nature ————	155
— the foundation of its theory ————	158, 159
— its effects on the measure of time, nearly in the inverse duplicate ratio of the maintaining power ————	162
— on the pallets, c. p. as their length ————	189
— how rendered unnecessary on main springs ————	392
— its influence, how estimated ————	167 to 182
— table of it, on each pivot in a Clock ————	171
— its influence on the pallets, estimated ————	172 to 176
— comparative with the dead-beat and recoil ————	176 to 182
— its influence, — how diminished in common pallets ————	172, 182 to 193
	<i>Oil</i> ,

I N D E X.

N^o

Oil, why its effect is not more sensible	193 to 197
— a recapitulation of what has been said relative to it	197 to 210
— of the methods that have been hitherto used for the diminishing it	212 to 232, and from 245 to 254
— diminished on Watches	394 to 403
— table of its influence on all the pivots of the wheels	513 to 540
— increased by a recoil	515
— its comparative influence on the ballance pivots	520
— total influence on horizontal and contrate wheel	519
— Watches compared	524
— how diminished on the former	525 to 540

P.

Pallets, — long ones, no advantage in maintaining the vi- bration	191, 192
— in what cases they are hurtful	189
— and in which advantageous	265, 266
— all reducible to two classes	234
— that have no friction during the time of rest	275 to 288
— that in Clocks remove every imperfection in the movement, of whatever kind	288 to 306
— further considerations relative to them	534 to 568
— that correct the effect of any irregularities of the maintaining power in Watches	553, 564
— tumbling, some remarks on them	566
— ingenious ones seen with Messrs. Harrison and Hindley	225 to 232, and from 245 to 253
— no springs to be admitted in them	246, 247
Pendulum, — its properties in a detached state	12 to 20
— its motion and isochronism destroyed by the resistance of the air, &c.	21

D d

Pendulum,

I N D E X.

	N ^o
<i>Pendulum</i> , detached gravity, its sole motive force	68
— in those applied to Clocks, the <i>maintaining power</i> must be added thereto	70
— in what proportion <i>it</i> alters the natural times of vibration	72
— its total motive force, of what compounded in Clocks	135
— its vibration most isochronal, when their length increases as the motive force	241
— reason why those that describe entire revolutions can never measure time equal to those that vibrate	411
— its long and short vibrations (when applied to a Clock) compared	24 to 48
— its weight considered	66 to 84
— table of its momentum (by weight, and length of vibration)	87
— the influence of heat and cold on it. See <i>Heat</i> .	
— gridiron, its nature and description	332 to 346
— mercurial	326
— Mr. Ellicott's, his own description of it	346
— improved	347 to 364
— rods of wood, in what cases they may be used	318
— all that has been said of it equally applicable to the ballance and spring	413
<i>Plan</i> of the essays	1 to 12, and 384 to 388

Plates, where described,

Plate	1.	Numb.	29.
—	2.	—	176.
—	3.	—	191.
—	4.	—	276.
—	5.	—	289.
—	6.	—	290.
—	7.	—	293.
—	8.	—	311.
—	9.	—	334.
—	10.	—	346.

Plate

I N D E X.

Plate 11. Numb. 361.

— 12. — 443.

— 13. — 475.

— 14. — 503.

— 15. — 543.

— 16. — 549.

N^o

Pocket-watches, in their present state, are only on a par
with Clocks that are capable of beginning their
own vibrations — — 431

— the influence of external motion on them much
greater than on such as are carried on ship-board 453

Power, maintaining. See *Maintaining power.*

Properties, natural, of the ballance and spring, can not be
preserved, without the dead-beat — 571

R.

Recapitulation—relative to the length of vibration in Clock
pendulums — — — 142 to 152
— relative to the influence of the oil — — 197 to 212
— relative to the method of frequent winding up 401
— relative to pallets — — — 274
— relative to the influence of heat and cold on the pen-
dulum — — — 369
— relative to the influence of external motion 483

Recoil, in general — — — 233 to 245
— increases, the friction — — — 178
— the influences of the oil — — — 178
— accelerating effects of it, twofold — — 238, 239
— none to be admitted with an uniform maintaining
power — — — *Note* 383
— advantages—erroneously attributed to it 269 to 272

Resistance of the air. See *Air.*

- Scapement*, is the means by which the action of the wheels
 is applied to maintain the vibration, and generally
 consists only of a wheel and pallets. See *Pallets*.
 — wherewith the theory and practice of the dead-beat
 agree ————— 275 to 288
Scale for finding the length of pallets, &c. for any number of
 teeth of the wheel, from 2 to 12 Note 2, 176
Springs,—never to be used in pallets ————— 246, 247
Suspension,—remarks, &c. relative to it ————— 309 to 316
Swing-wheel,—the influences of the oil on the pallets increase
 as its diameter ————— 172

T.

- Tables*,—of the influences of the oil ————— 171, 515
 — of the momentum of pendulums ————— 87
Thermometers,—all reduceable to two classes 319, 320
 — immoveable ones—can never have a perfect effect in
 Clocks ————— 321 to 326
 — remarks relative to their construction 329, 330
 — one for a Watch described ————— 496 to 512

V.

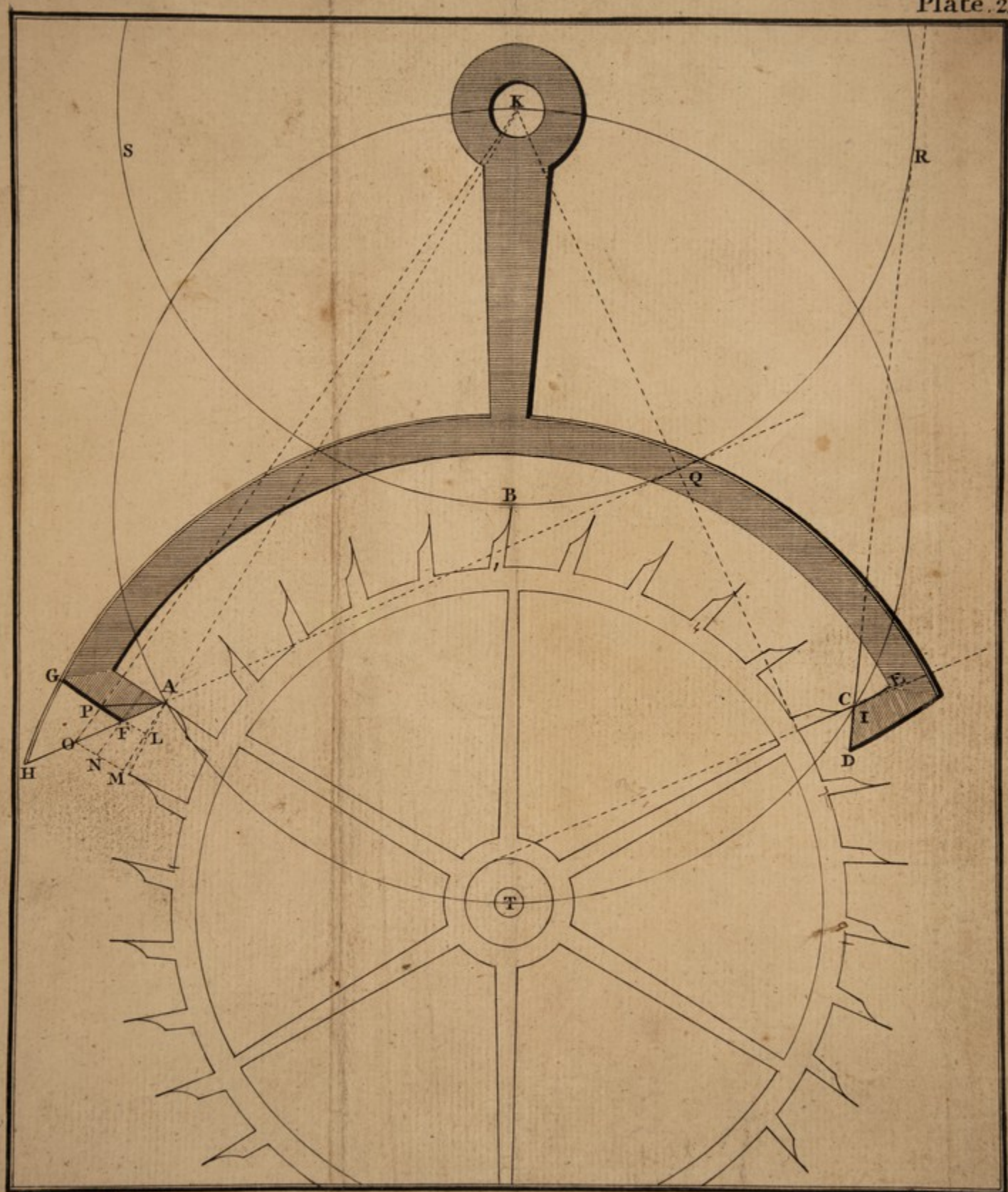
- Vibrations*,—long and short compared ————— 41, 47
 — short ones—arguments commonly used in their favour
 93 to 96
 — nowhere recommended by Sir Isaac Newton for Clocks
 121 to 133
 — arguments in their favour examined ————— 96 to 114
 — cycloidal ————— 96 to 113 and 383
 — conclusions relative to them ————— 111 to 114—152
 — recapitulation relative to them in Clock-pendulums
 142 to 152
Vibrations,

I N D E X.

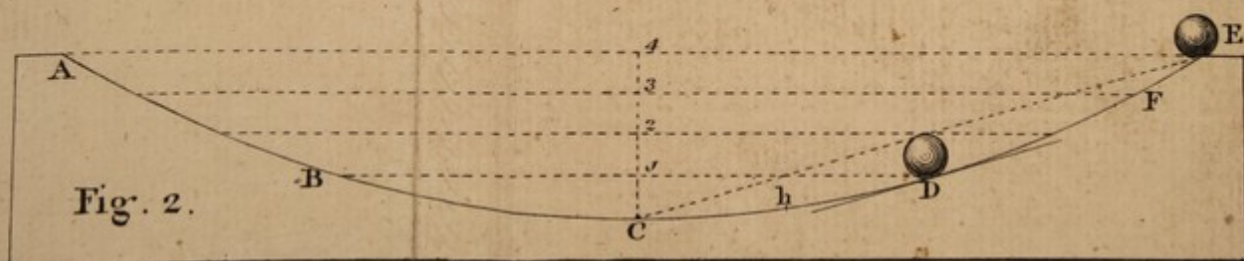
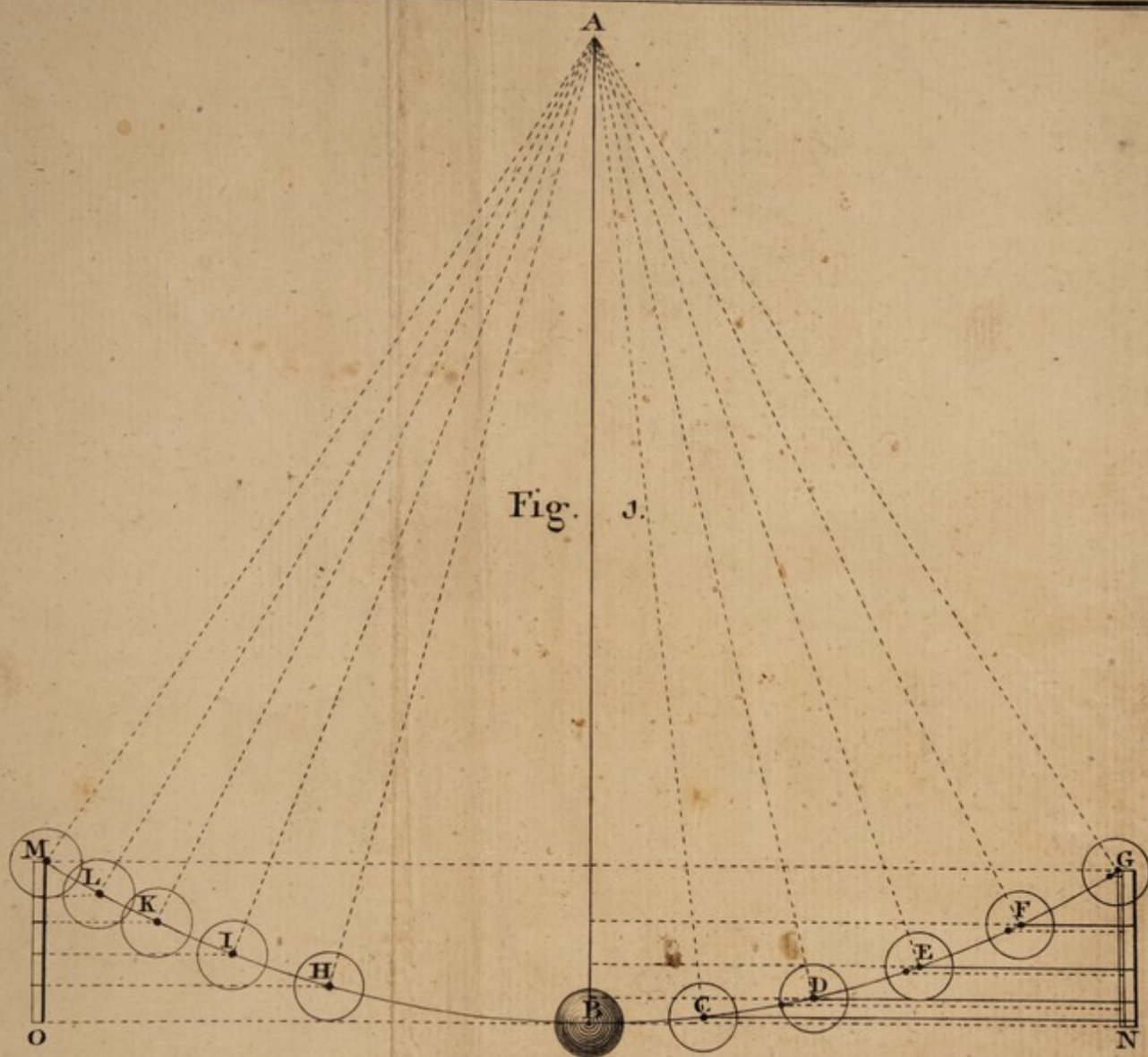
	N ^o
<i>Vibrations</i> , all that has been said in favour of long pendulous ones, is equally true of those of the ballance	413
—— the longer ones of the ballance do best correct the influence of the oil, or any other irregularities of the maintaining power	487
—— do most correct the influences of external motion	489
—— how the longer ones of the ballance may be rendered quicker than the shorter	551
—— how the shorter ones may be rendered quicker than the longer	552
—— how their natural properties may be preserved	553, 564
—— could not heretofore be known experimentally	550, 552
—— have not their times altered by a change of latitude	410
—— nor by any change of density in the air (considered as a non-resisting medium)	568
—— are all naturally isochronous in theory	408
—— the effect of the maintaining power on their times (c. p.) as its times of action	546
—— as twice the recoil	238, 239
—— may vary their length, without altering their times	554, 564
—— those of the pendulum rendered more isochronal by having their length increased as their motive force	241
<i>Vibrating-pendulum</i> ,—reason why it will always measure time better than any that perform entire revolutions	411

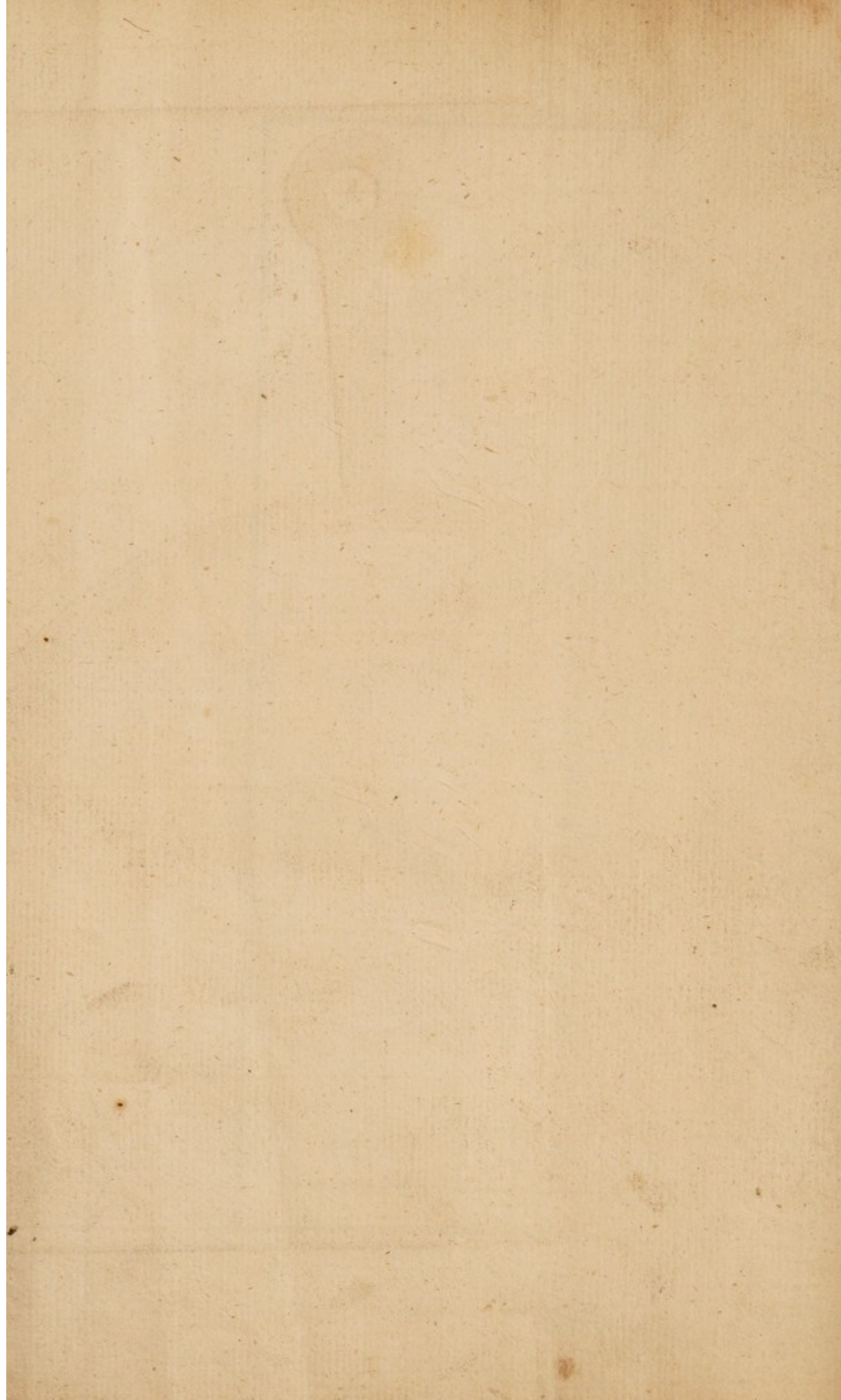
W.

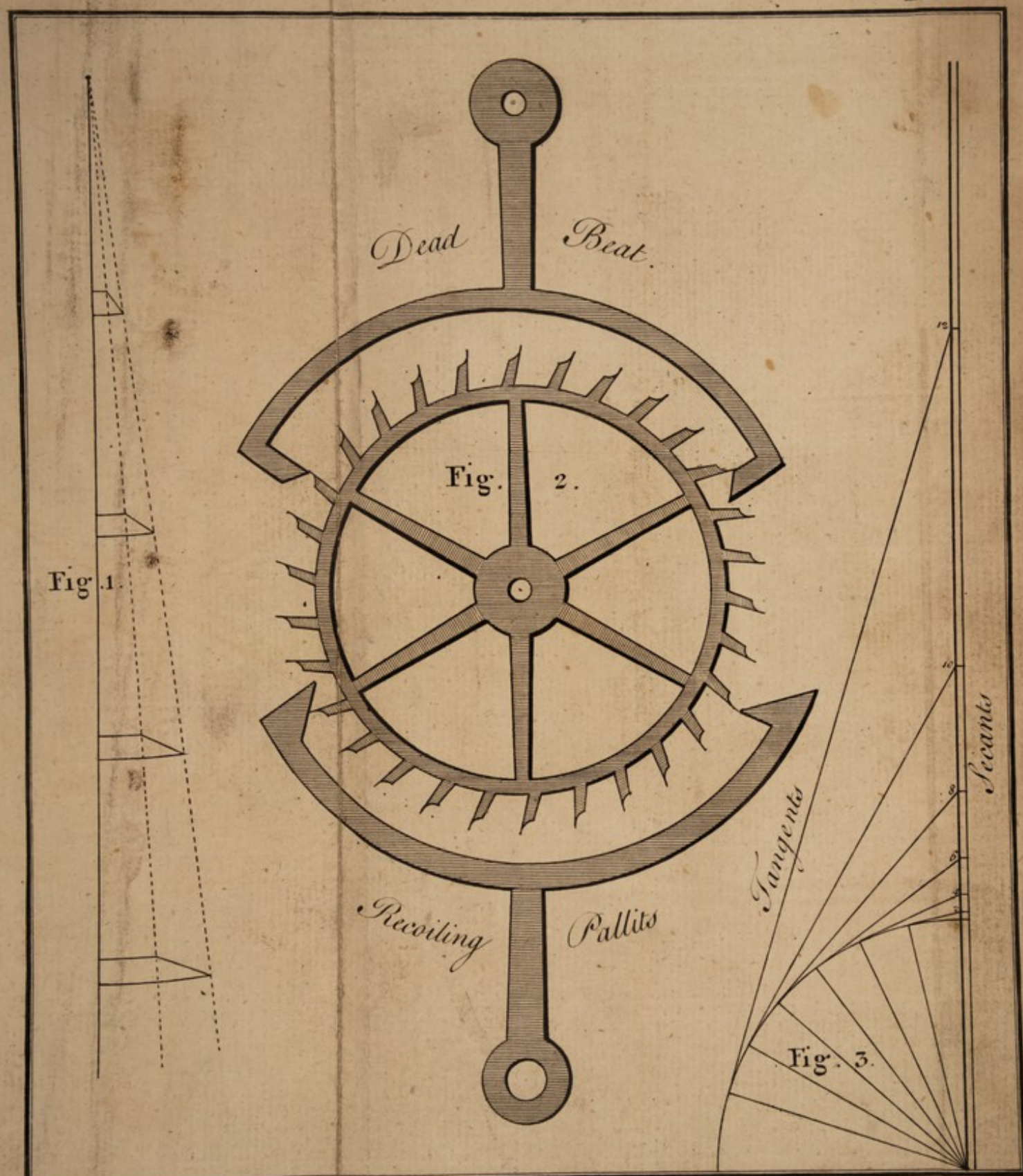
<i>Watches</i> , the larger ones do most approximate the nature and perfection of Clocks	436 to 442
<i>Wheels</i> , the periodical fluctuations in their action, not so hurtful to the performance of Clocks and Watches as generally imagined	54
—— the disadvantages of heavy ones	440
<i>Winding-up</i> , every half minute—its effects	216 to 223, 394 to 403
<i>Wooden pendulum rods</i> , in what cases to be used	318

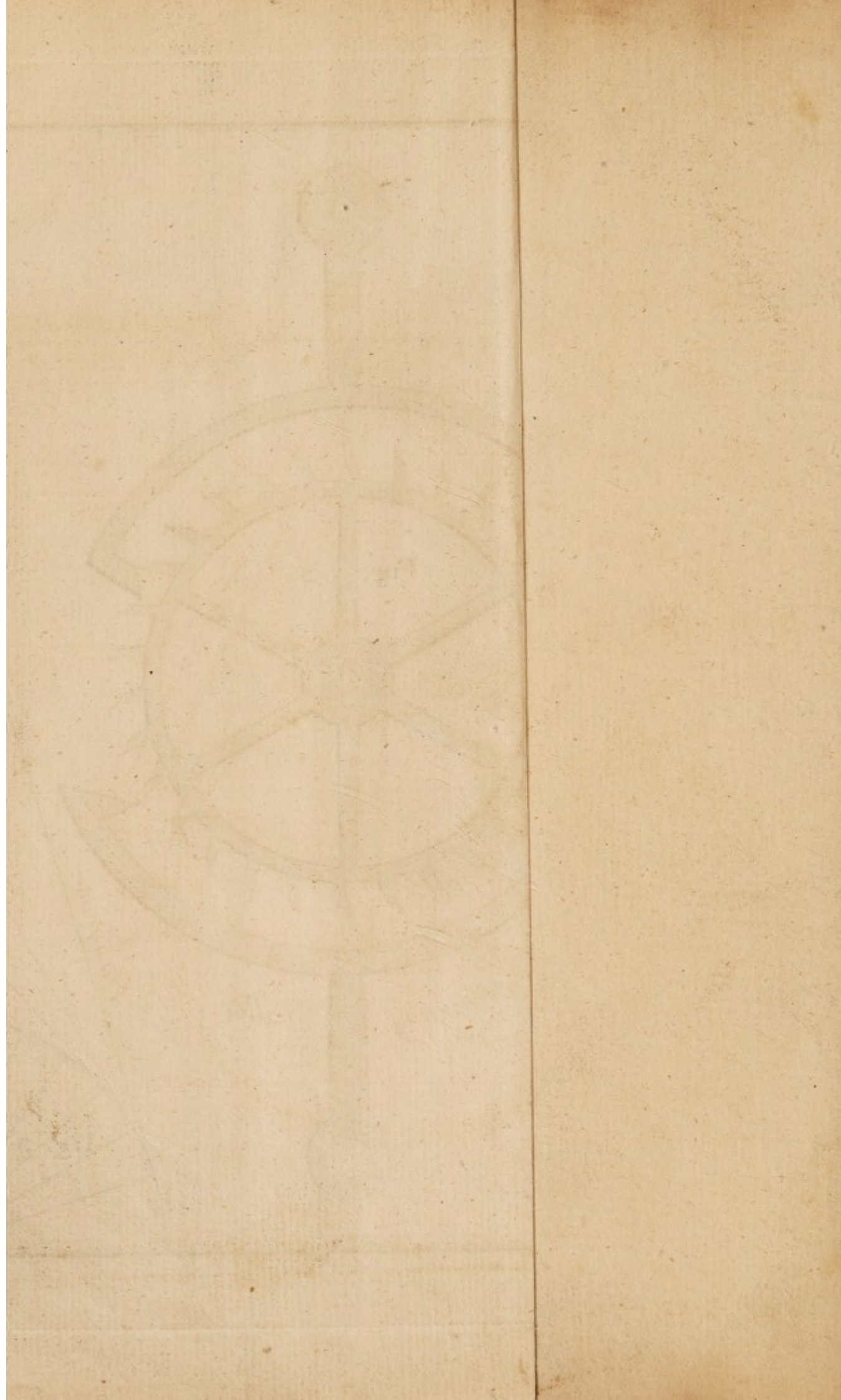


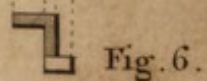
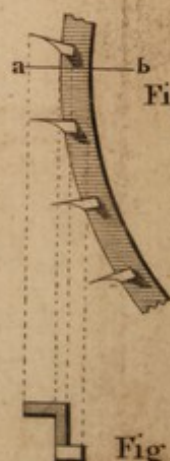
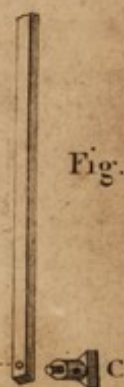
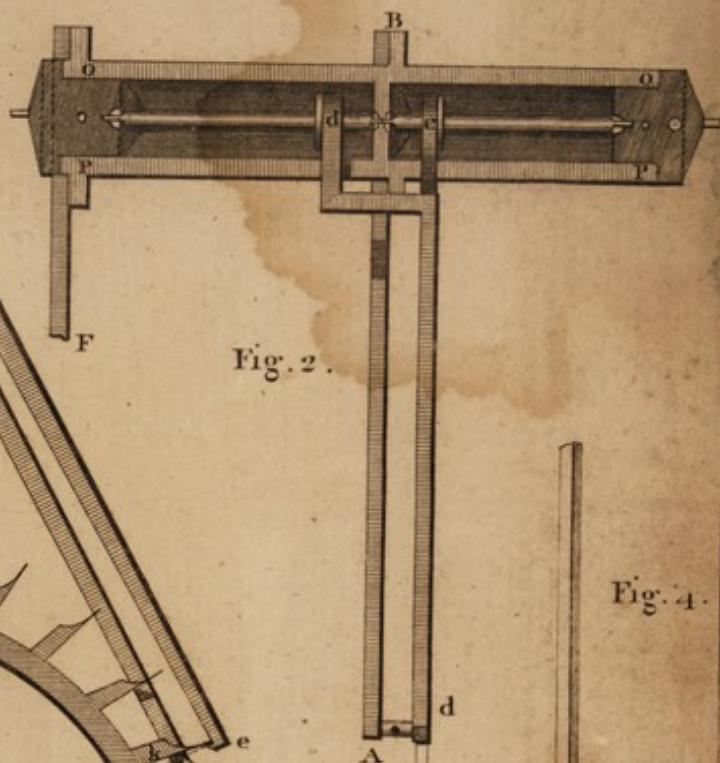
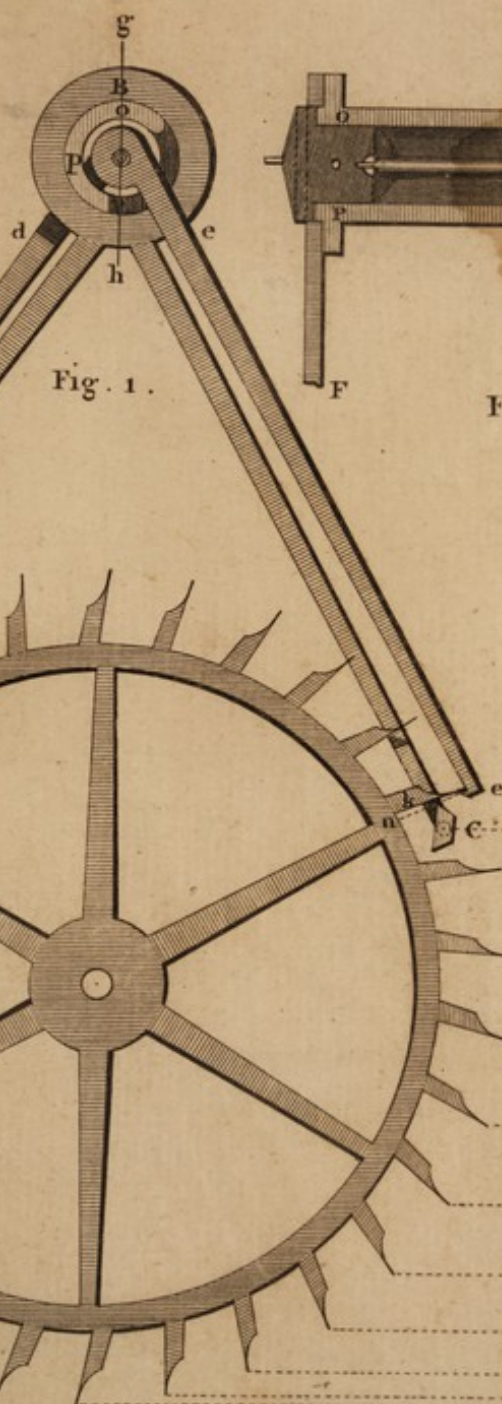
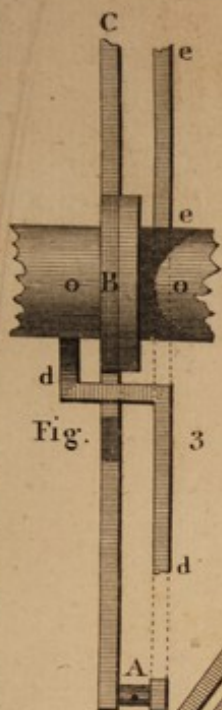




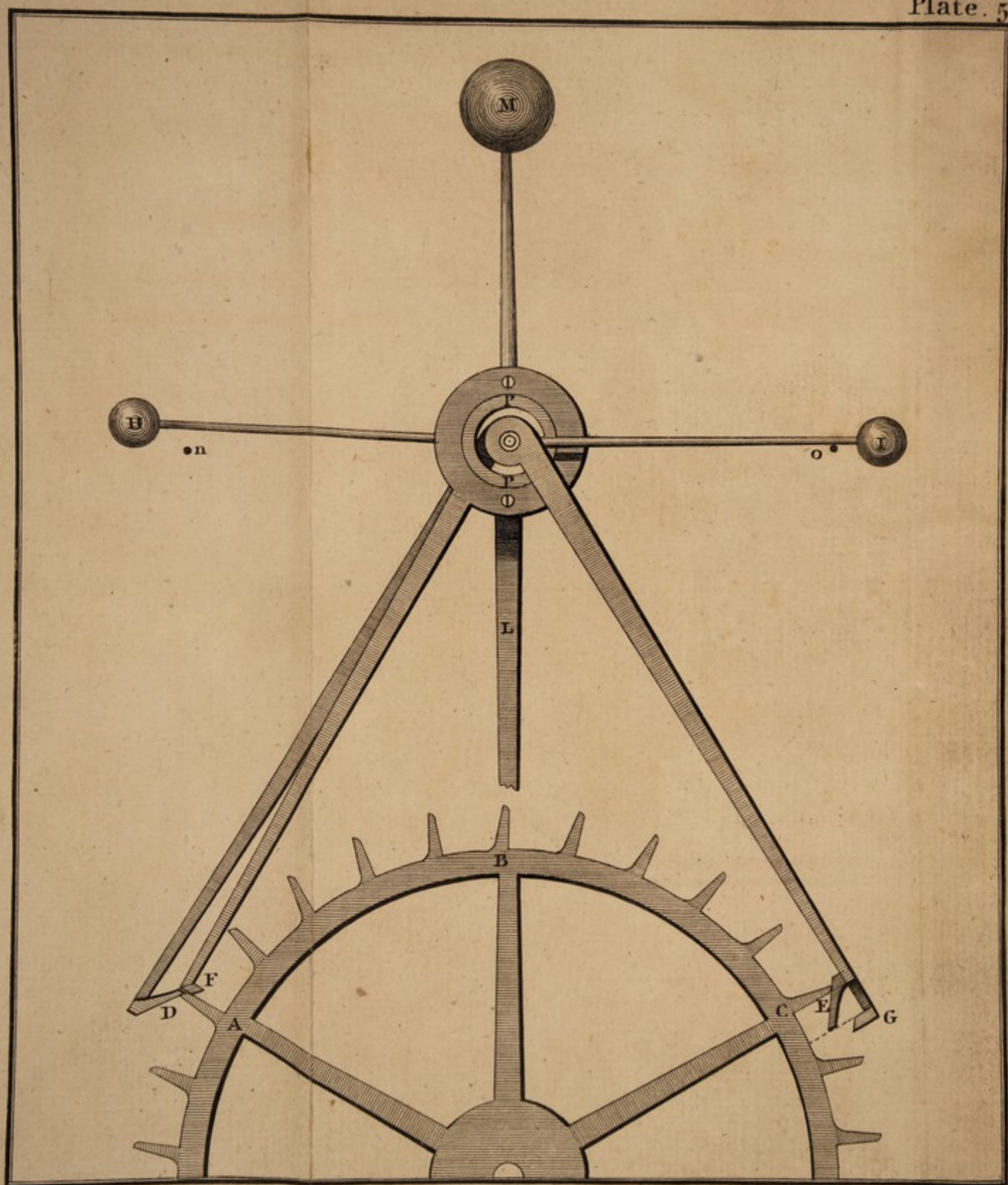


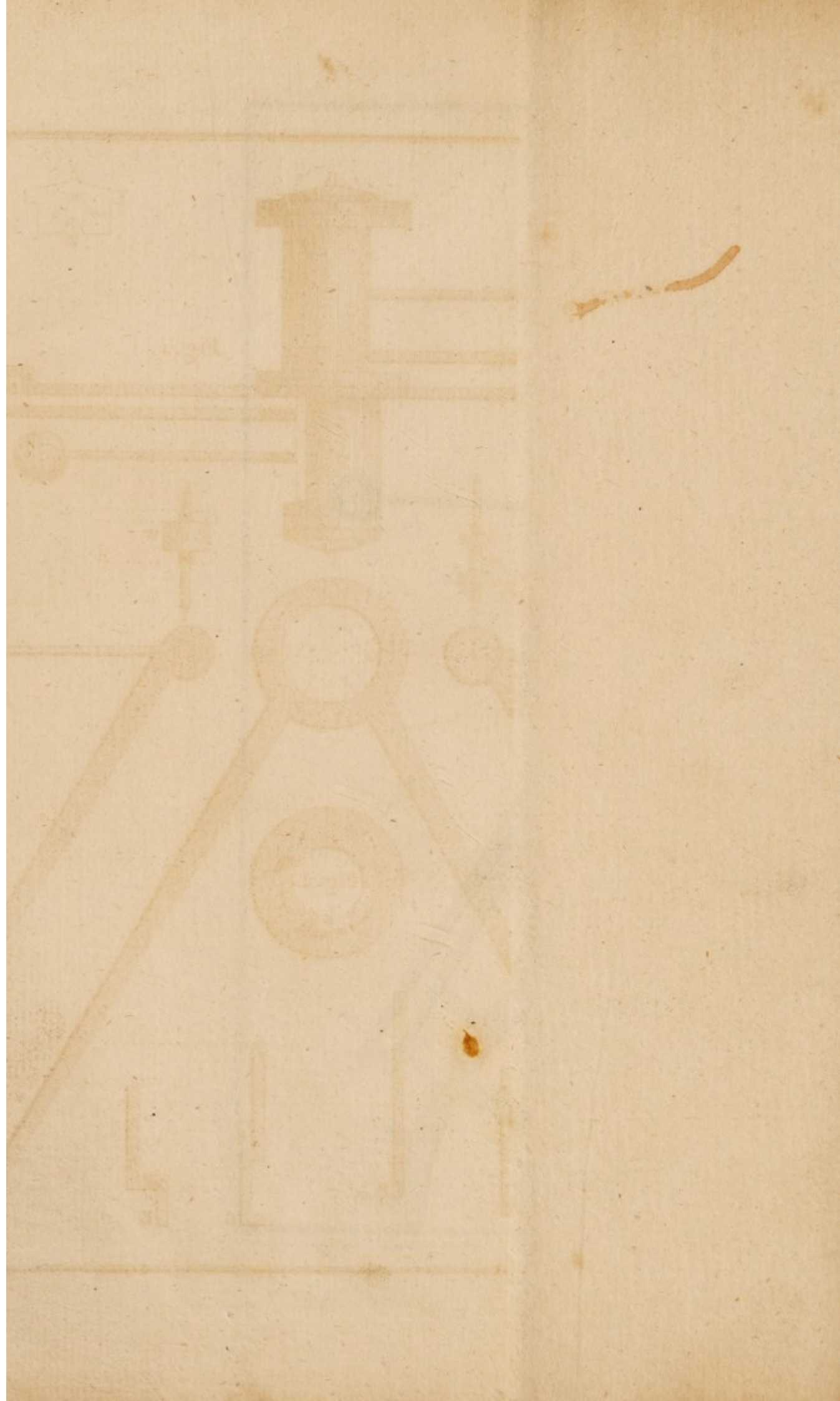


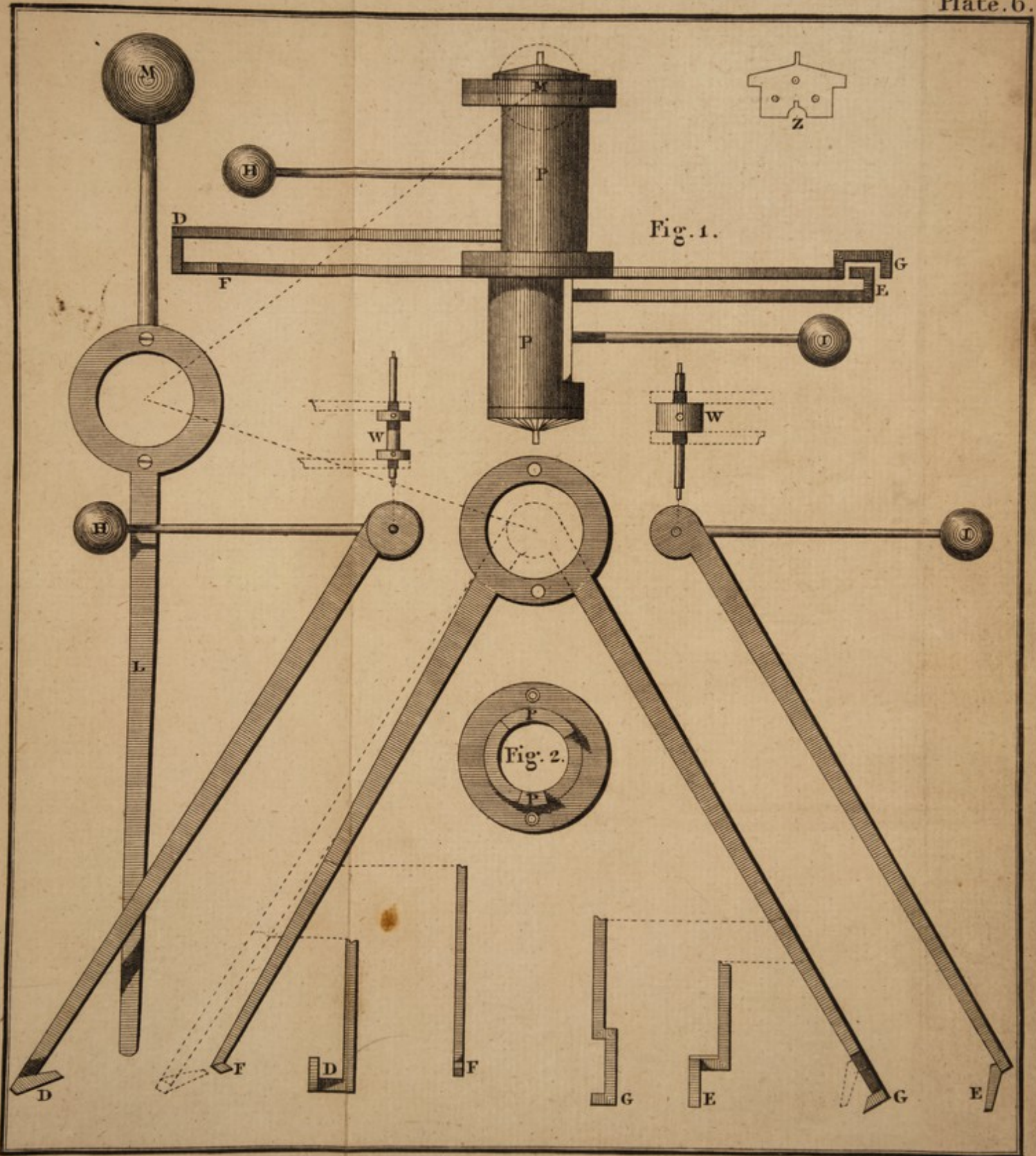


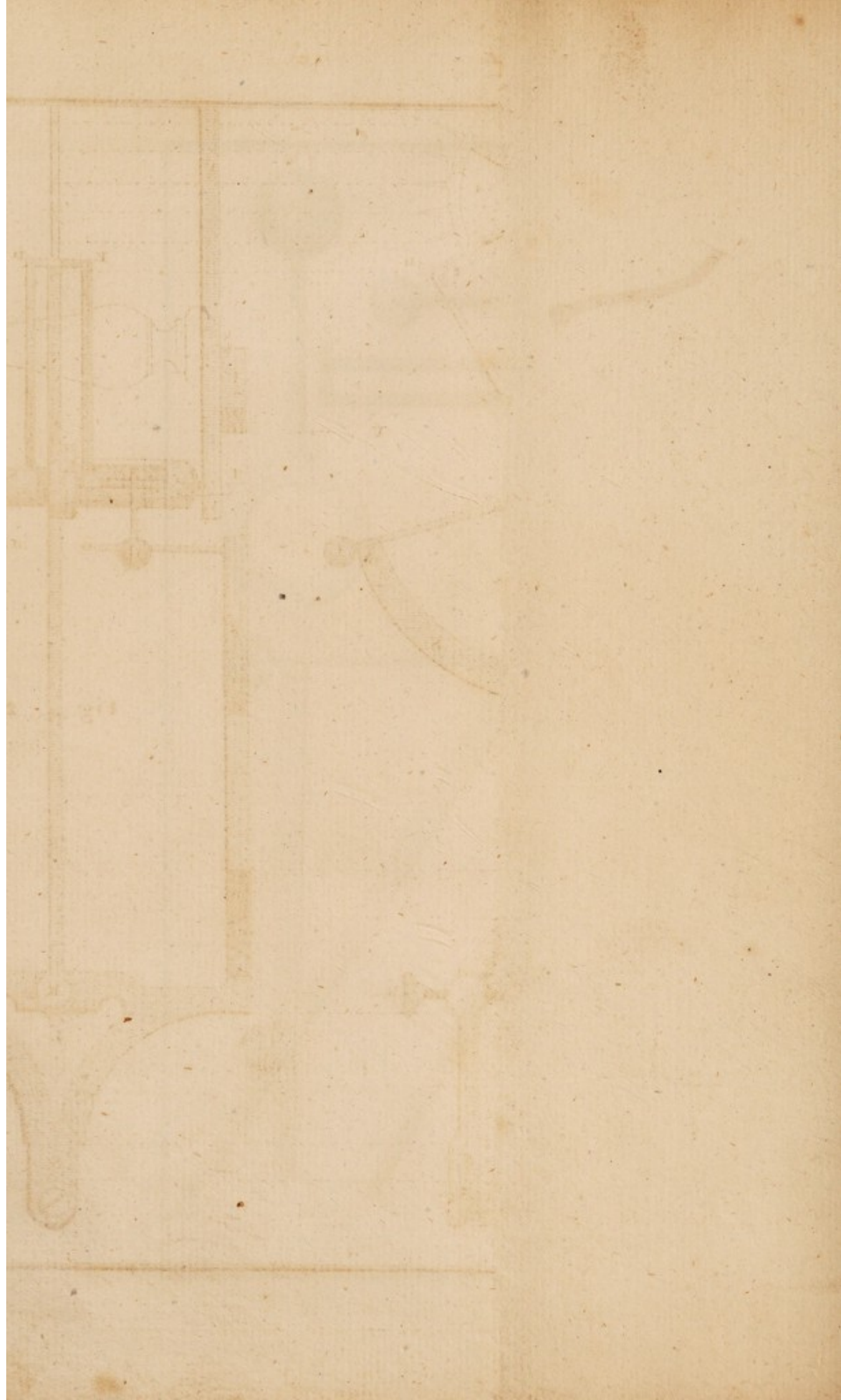


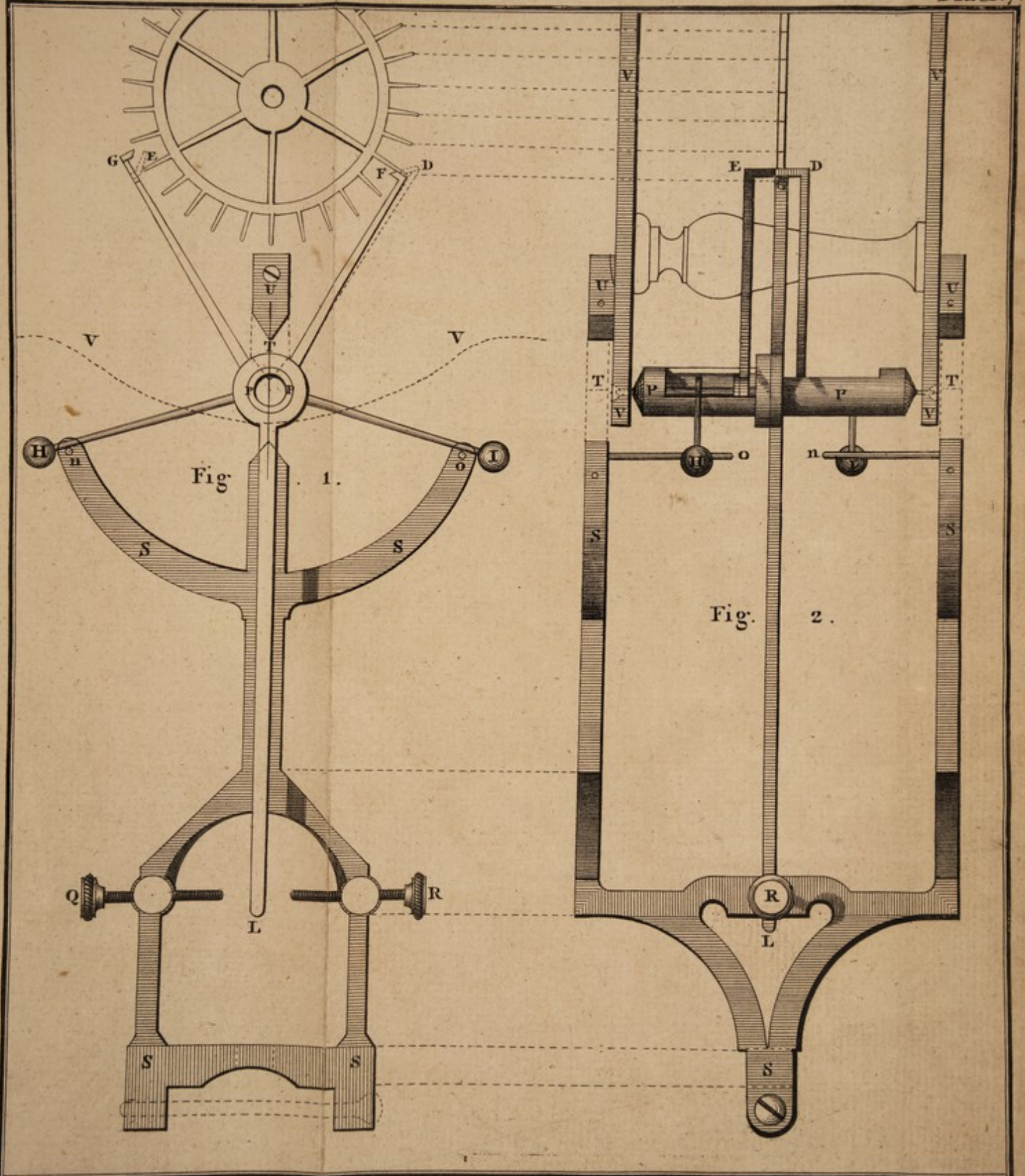






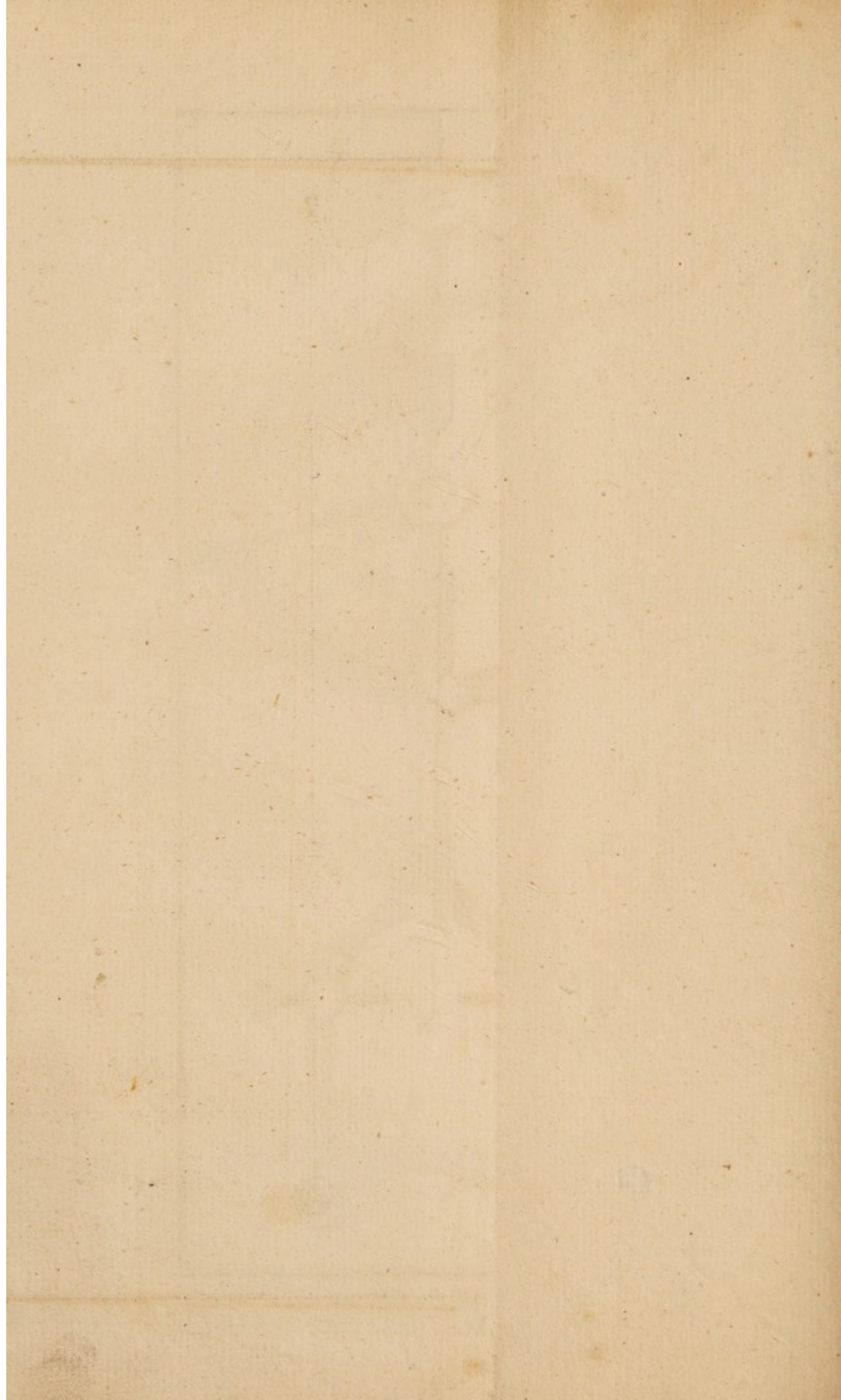


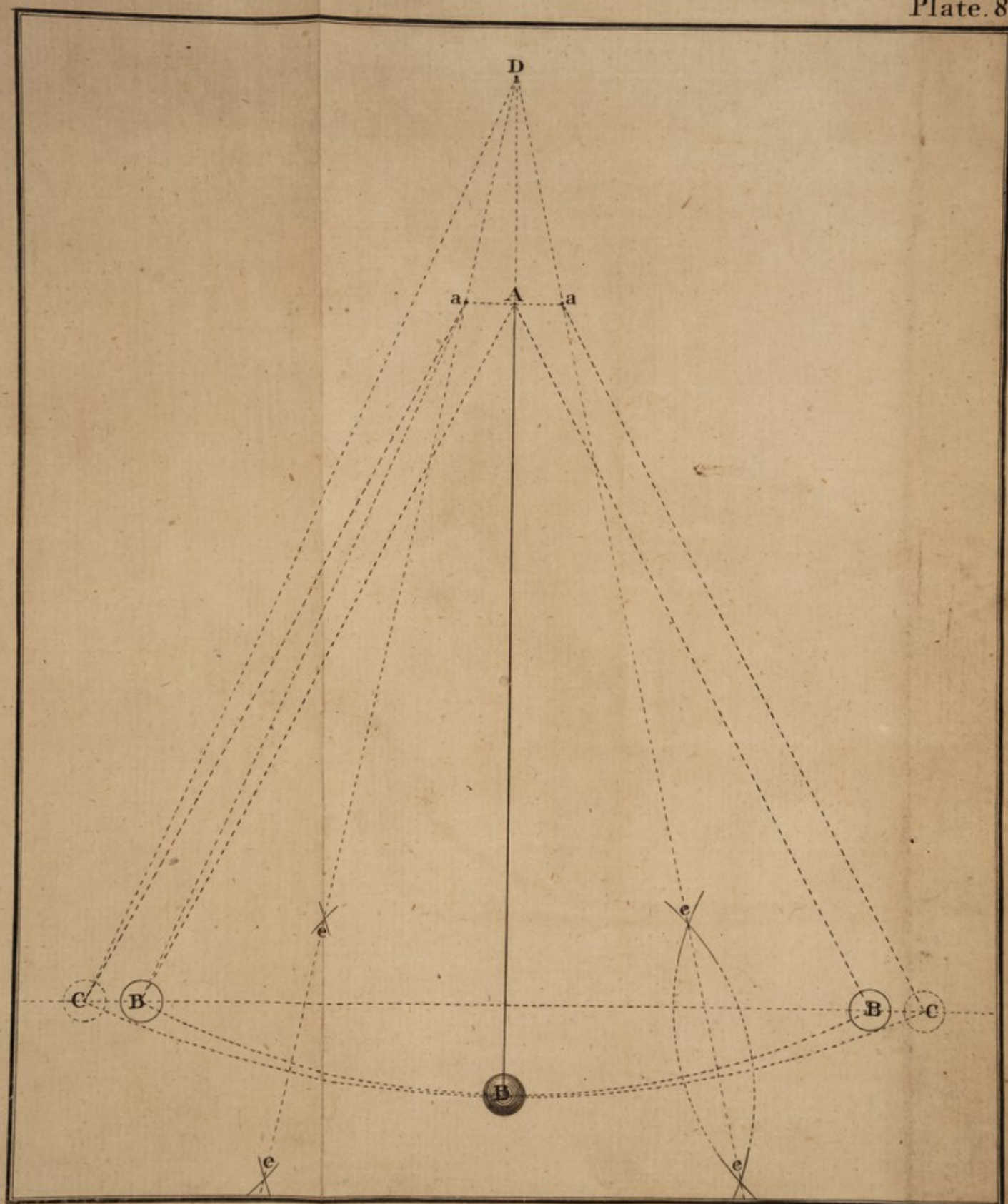




A. Cumming delin.

T. Miller Sculp.





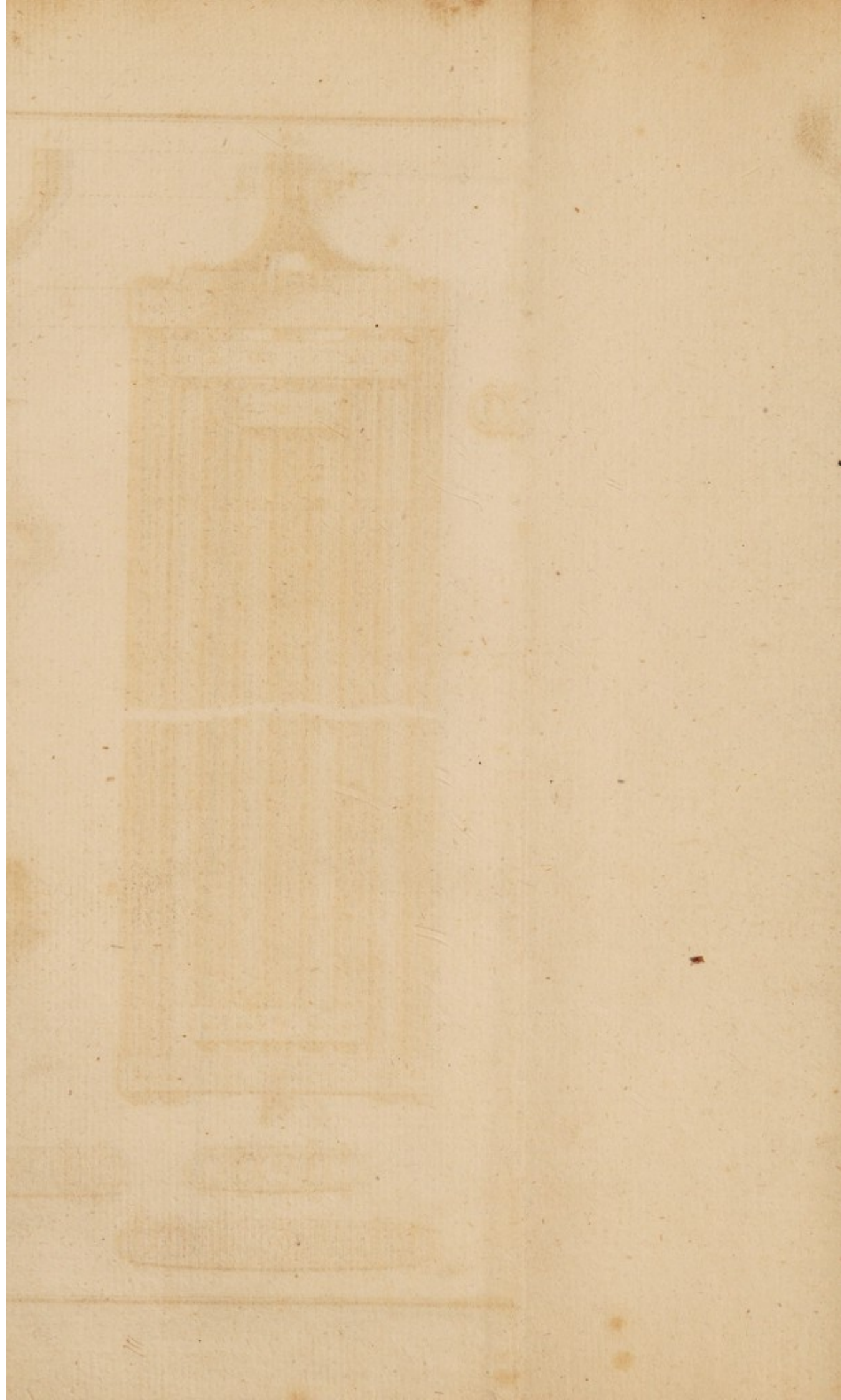


Fig. 1.



Fig. 2.



Fig. 3.

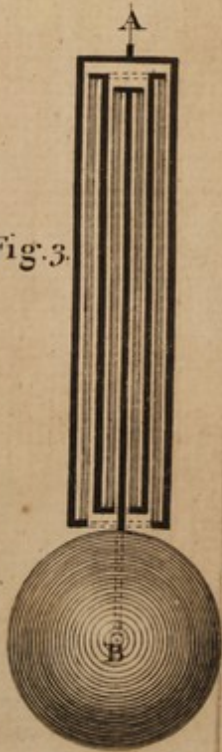
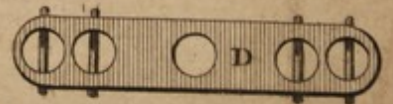
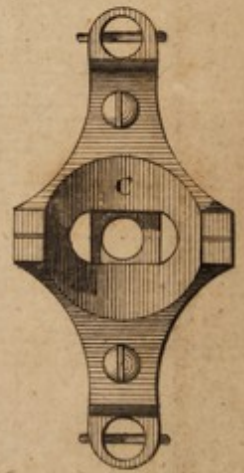
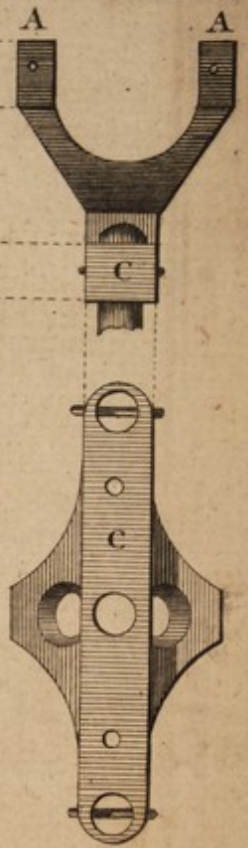
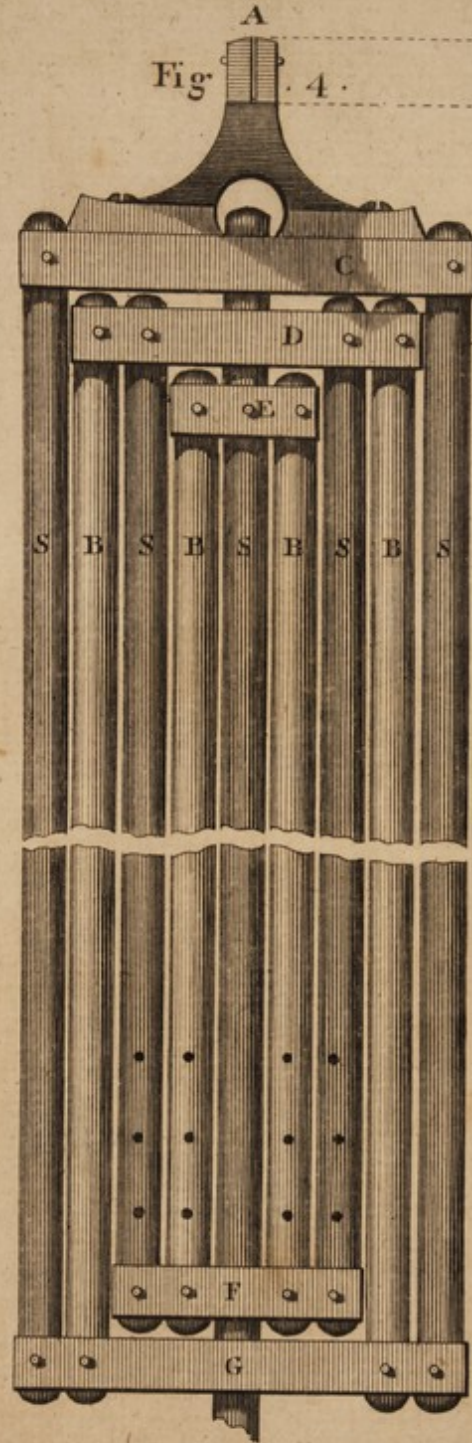
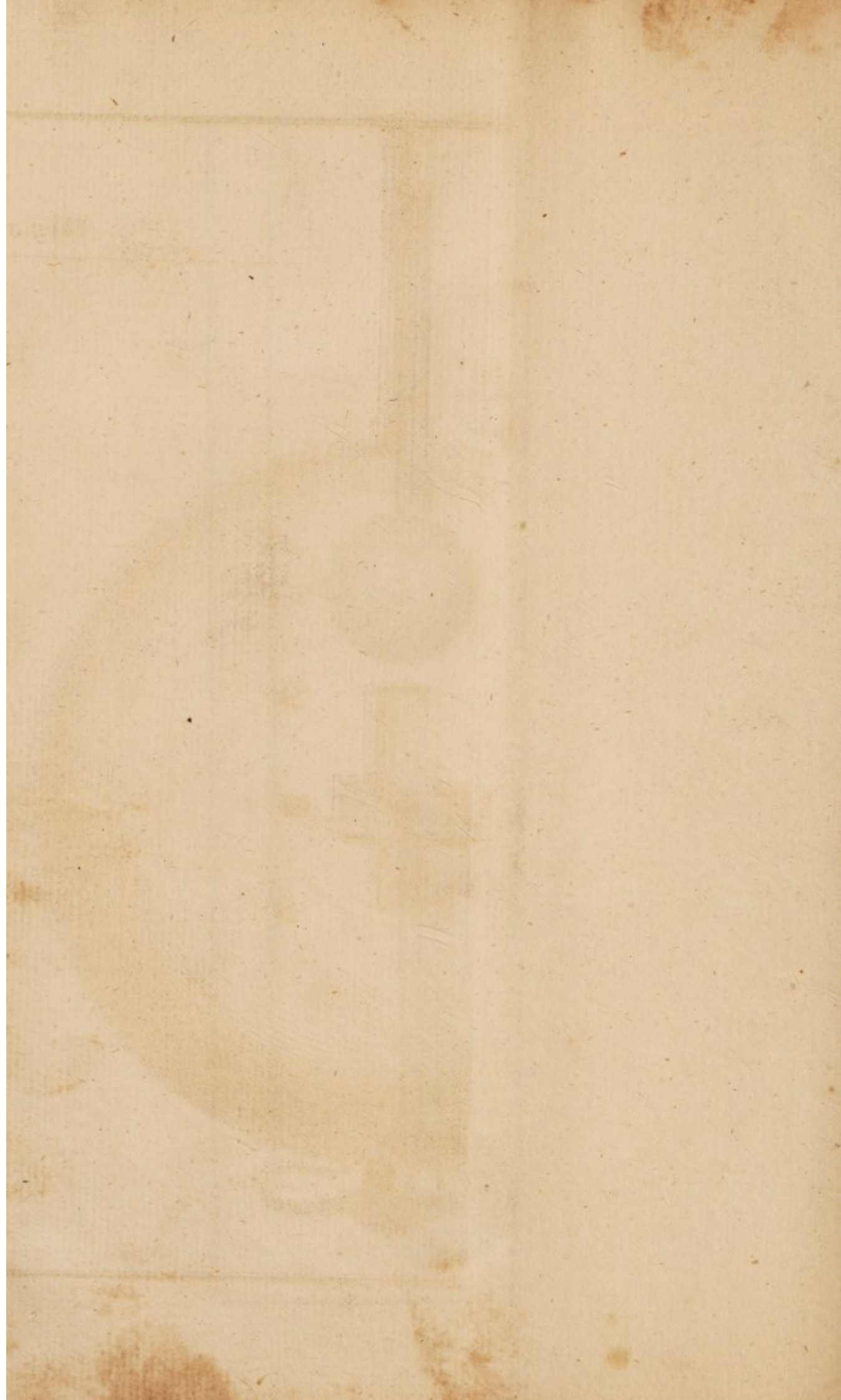
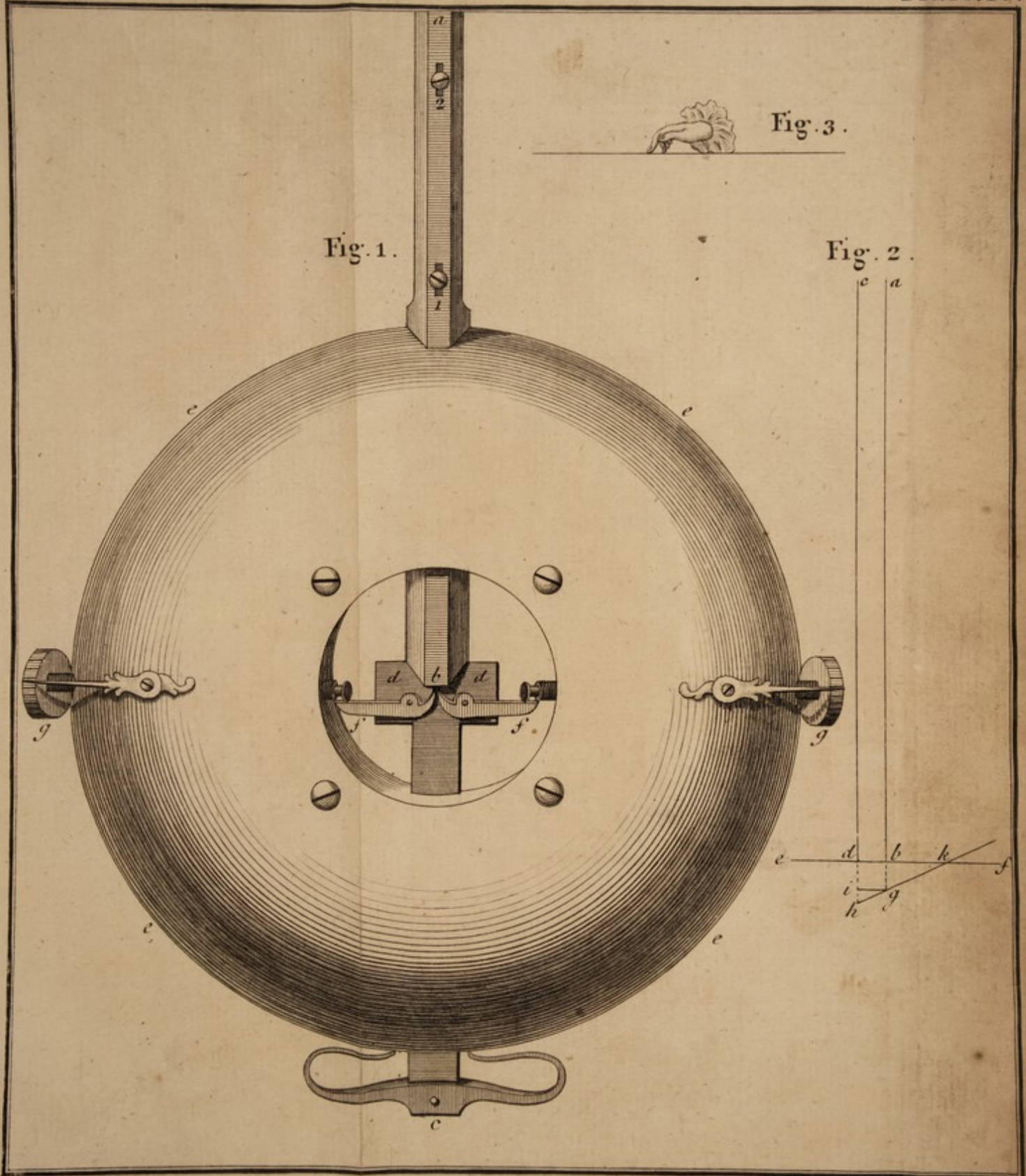


Fig. 4.







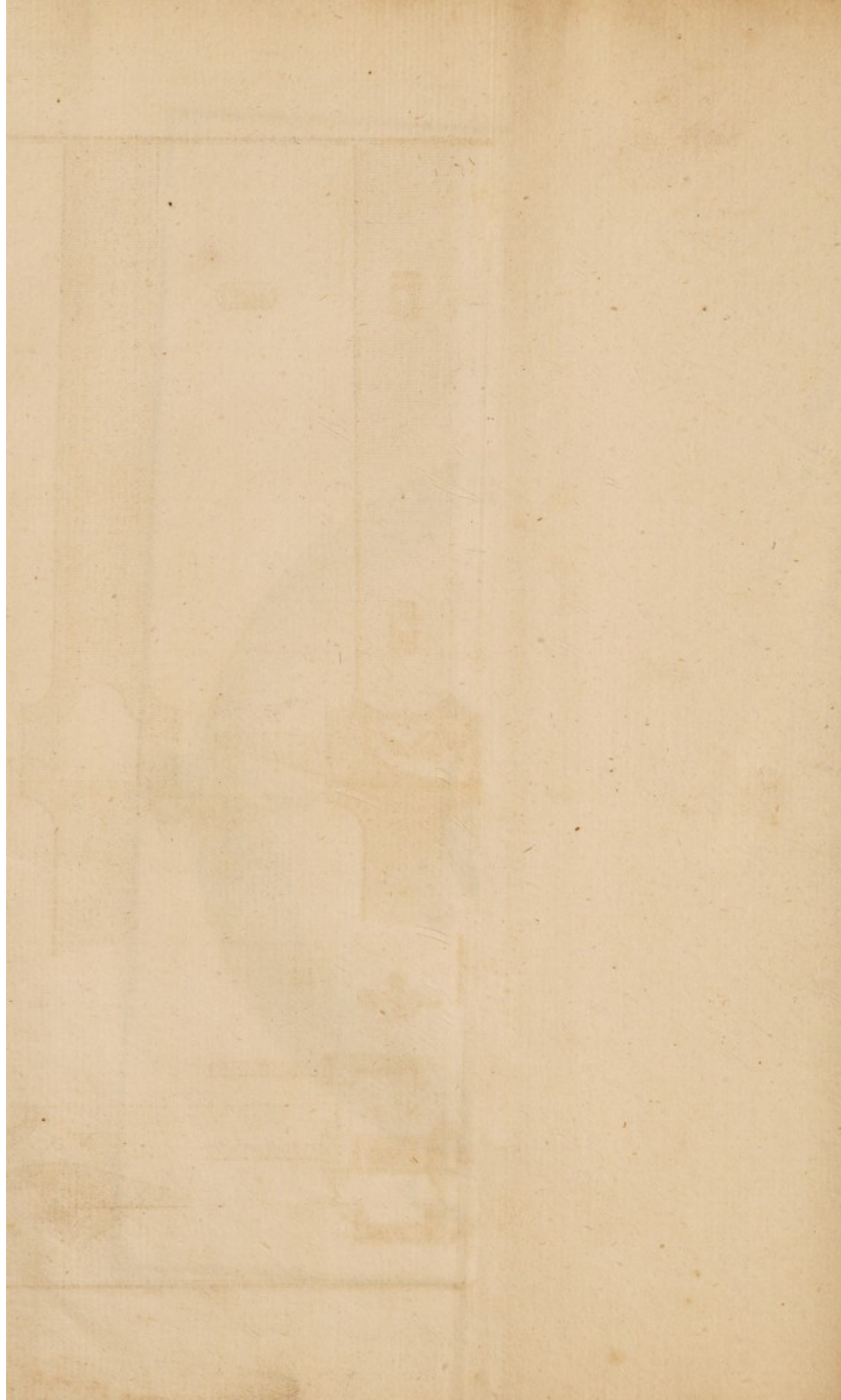


Fig. 1. Fig. 4.

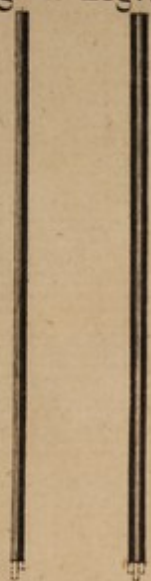


Fig. 2. Fig. 3.

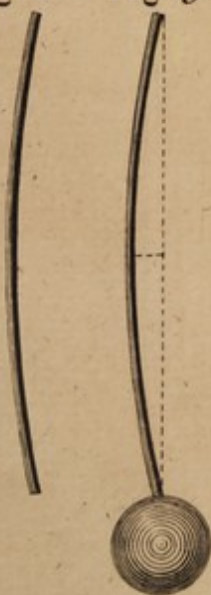
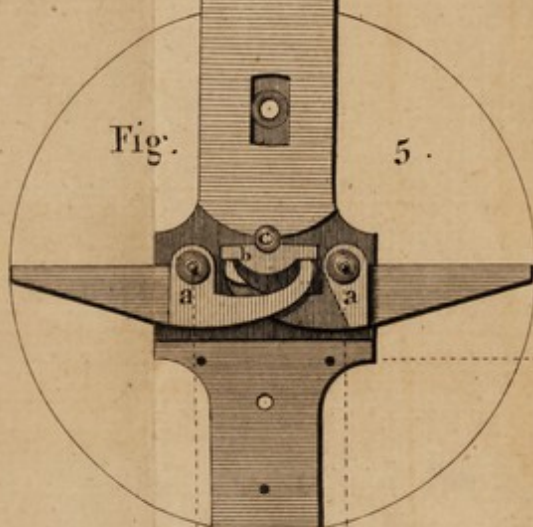
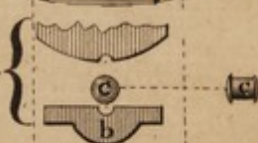


Fig.

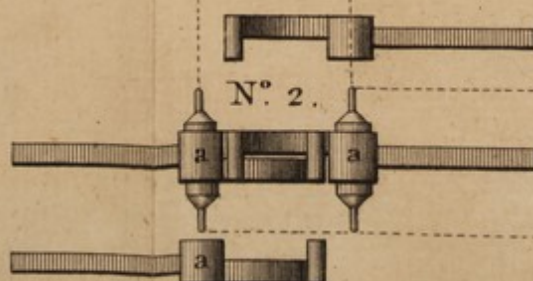
5.



N^o 1.



N^o 2.



N^o 3.



Fig. 6.

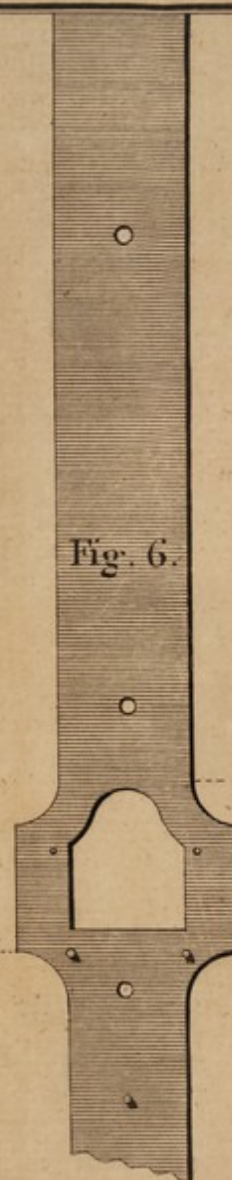
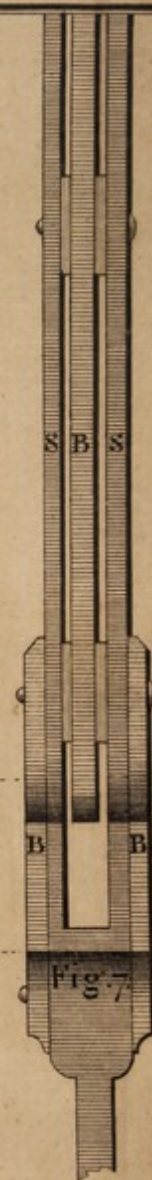


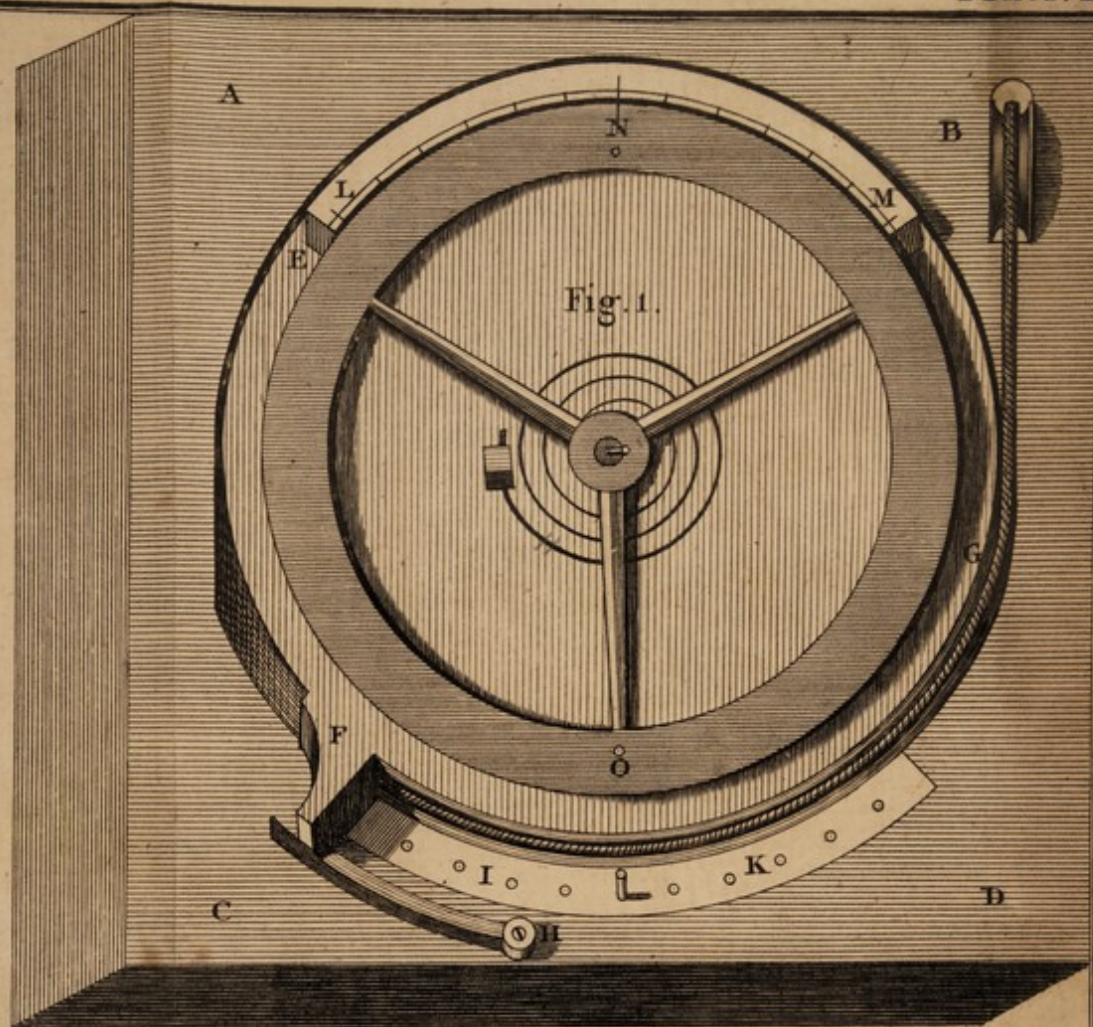
Fig. 7.





G 1 A k H

Fig. 2.



1 2 3

Fig. 3.



Fig 4

C D E F

A. Cumming inv. & delin.

J. Miller Sculp.



