

An account of the discoveries concerning comets, with the way to find their orbits, and some improvements in constructing and calculating their places. For which reason are here added new tables, fitted to those purposes; particularly with regard to that comet which is soon expected to return / [Thomas Barker].

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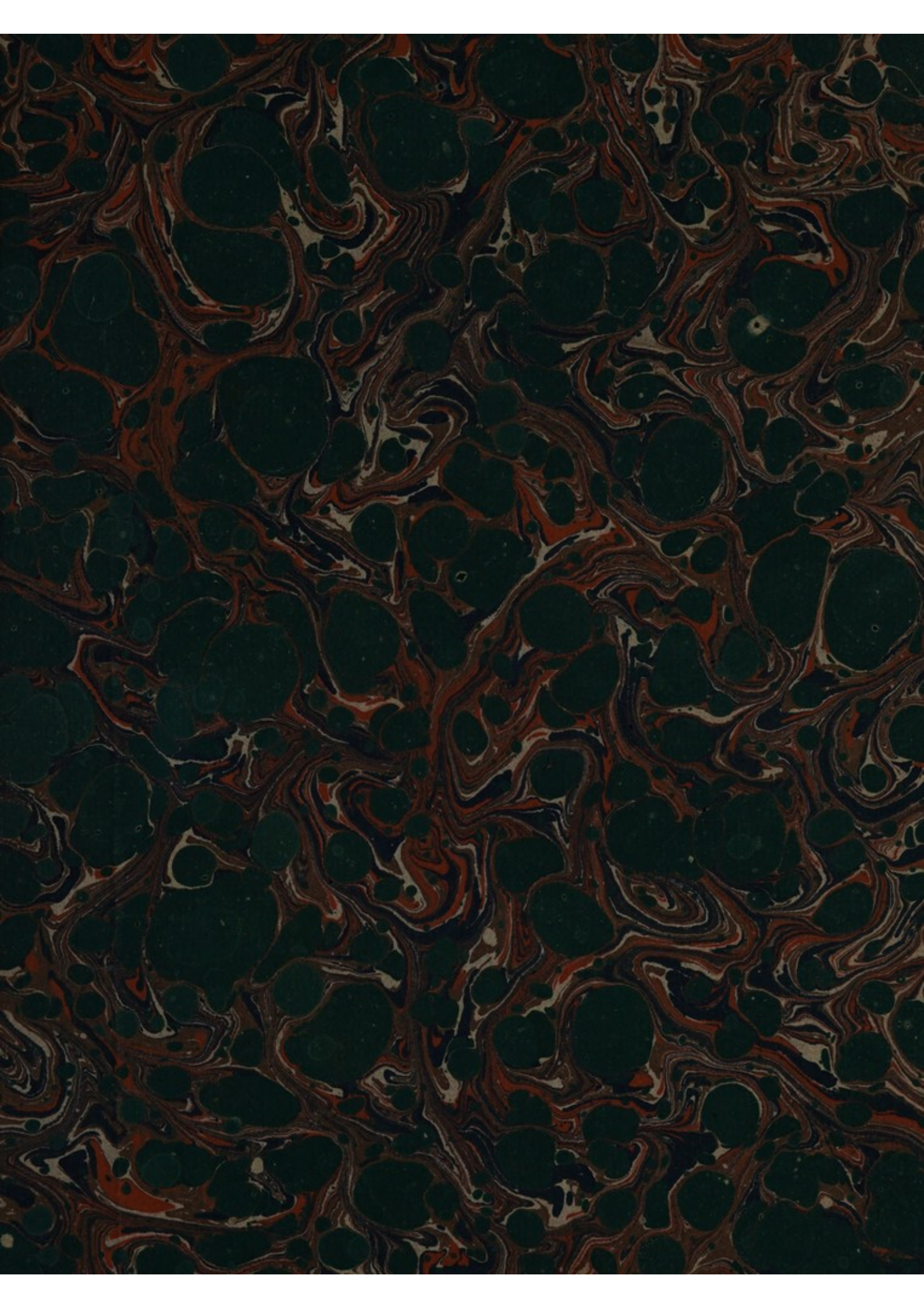
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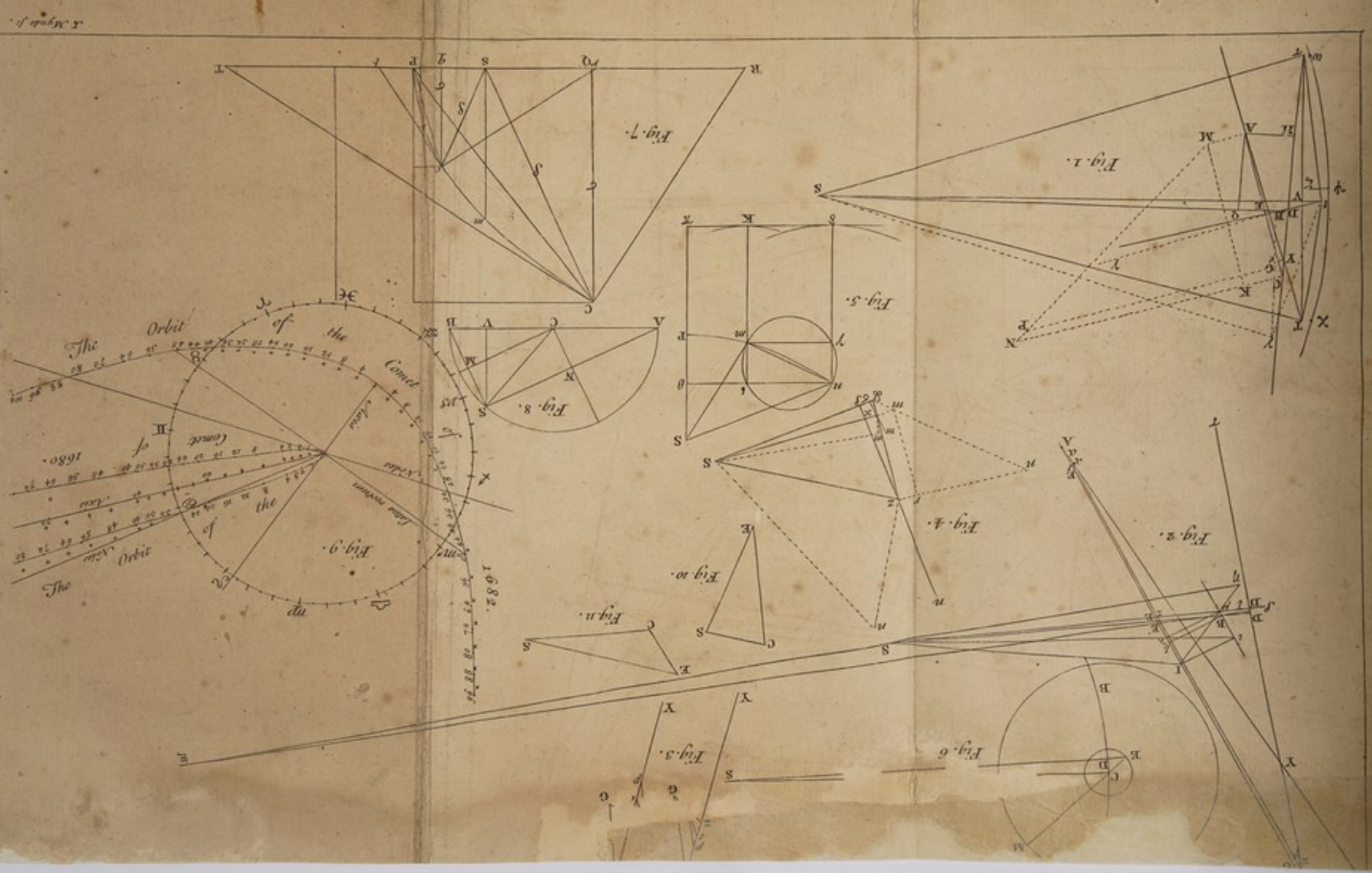
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· A N
A C C O U N T
O F T H E
Discoveries concerning Comets,
W I T H
The Way to find their Orbits,
And some Improvements
In constructing and calculating their Places.

For which Reason are here added

New TABLES, fitted to those Purposes;

Particularly with regard to

That COMET which is soon expected to return.

By THOMAS BARKER, Gent.

JOB XXVI. 14. *Lo, these are a part of his ways: but how little a portion is heard of him!*

SEN. Quæst. Nat. Lib. VII. 31. *Multa seculis tunc futuris, cum memoria nostri exoleverit, reservantur. Pusilla res mundus est, nisi in illo quod querat omnis mundus habeat.*

L O N D O N,

Printed for J. WHISTON and B. WHITE, in Fleet-Street.

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T H E P R E F A C E.

THAT bright comet, which was seen in 1744, having raised in me as well as others a greater curiosity about them; I had once thoughts of undertaking a kind of history of comets, which, beside what is given here, should contain an improvement of Hevelius's and Lubienietz's accounts of the ancient ones, and a continuation of them to the present time. The alterations I designed to make were these: First, To leave out the astrological observations, which the old authors, looking on comets chiefly as prodigies, are full of, and Lubienietz's book is almost all so; to quote nothing but what relates to the comet itself; and in later times, when there are many accounts of the same comet, to insert the principal, and perhaps pass over some of them which contained nothing new. Secondly, Hevelius and Lubienietz take many comets only second hand, from Rockenbach and other modern writers, but I would as much as possible have quoted the original authors. Thirdly, Different persons not using the same chronology, have often made several comets of one. Thus the four Seneca reckons up Nat. Quæst. VII. 17. after the death of Julius Cæsar, under Augustus, Claudius, and Nero, are in Hevelius increased to thirteen; and the two last of them, which he calls the two comets seen in our time VII. 23. Lubienietz has made eight of. Fourthly, Lubienietz swells his history with balls of fire, northern lights, and perhaps other meteors: all these, as also multiplying of real comets, I designed to have avoided where I could. In pursuit of this design, I made a list of the comets which had been seen, with references to the authors who mentioned them, so far as I had then found, leaving room to add more, as I met with them; and began to draw up the account of a few of the first with the authorities, but found so little satisfaction from the very imperfect accounts, that perceiving the benefit would not answer the trouble, I laid the design aside. Yet having now had by me for several years a table of the parabola, which shews the space, and distance from the focus at all angles, and will, I think, by it's length, better answer the end of calculating a comet's place, than Dr. Halley's table can, I chose no longer to conceal it: but that it might not seem too imperfect, by being published alone, I have added a short account of the discoveries about comets, a catalogue of their orbits, the way I calculated the parabolick table,

THE PREFACE.

table, and method of using it, also how to construct a comet's motion speedily. In particular I have given some account of the use of Sir Isaac Newton's famous problem for finding a comet's orbit from three observations, which till lately few persons have study'd; yet seems to me a much better method, than that Caille has given in art. 518—560 of his astronomy, which he shews in art. 520, does not answer in all cases, and requiring so much correction by guess, must I think be very troublesome. In studying this problem of Sir Isaac's I almost got beyond my depth; yet by comparing his explication with Dr. Gregory's, and the assistance at first of Mr. G. Whiston, with a repeated examination since, I hope I have gained a tolerable knowledge of it, and have endeavoured to render the process as exact, easy, and plain as I can. But though mathematicks is a science capable of absolute demonstration, yet in so complex a problem, especially where several parts are only approximations, the mind of man is frail, and may overlook some small circumstance, which may render his reasoning a little defective: such at least I own my understanding to be, and the more as living in a retired place, I am forced to trust to my own strength. If therefore on tryal I be caught tripping, far from taking any friendly admonition amiss, I shall think myself greatly obliged to any one more skilful than myself, who will by letter or otherwise inform me, either where I have mistaken, might have made the method shorter or easier, or have omitted any further use or improvement; I shall not fail on any proper occasion to acknowledge the favour, and, if opportunity offers, to make a due use of it, being desirous to compleat the affair as far as I can.

Lyndon, Rutland.
Sept. 15, 1756.

P. S. Mr. Facio, as Dr. Halley mentions, thought of a use which may now and then be made of comets; by observing the parallax of one when very near the earth, to find the sun's parallax, and consequently it's distance, now known only to a fourth part. The expected comet will not come much nearer the earth than Mars does, if it's perihelion should be in January or July; but would be within 13 000 000 of miles of the earth October 19, with a full minute's parallax, if it's perihelion is November 27; or have $3\frac{1}{2}$ parallax May 4, at 4 000 000 of miles distance, if it's perihelion is March 27.

OF



OF THE
DISCOVERIES
CONCERNING
COMETS.

THOUGH the ancients knew little of the use of conick sections, in comparifon of what has been discovered within these last hundred and fifty years, yet they applied them selves to the study of their properties, and thereby prepared the way for the readier applying them to the uses lately found out. If those who at that time employed themselves in making astronomical observations, had been as careful in attending to the motion of comets, which do not require such depth of thought as abstruse mathematical problems; though they knew too little then of the principles of motion to have found out their real path, yet probably we should not have been so much at a loss, as we still are, as to their periods; but, by comparing their motions in different returns, even though the observations had been but gross, might have arrived to a considerable perfection in the astronomy of comets. But as most of their periods seem to be very long, and it is but a little while that their motions have been carefully watched, it may be some ages yet, before we get any great knowledge about them. Most of the ancients, being of Aristotle's opinion, that comets were only inflamed vapours, raised, continuing, and dispersed in our atmosphere, took little further notice of them than as omens, often mentioning neither the time of year, or place they were seen in; and unless *both* are known, we can neither find their orbit, nor compare them with that of any known comet. Seneca indeed, and some others whom he mentions, believed comets to be *lasting heavenly bodies*, Nat. Quæst. VII. 3 & 22. that *multitudes of them, which could not be seen on account of their position, kept on their stated course, and at certain times, when they got to the*

nearer end of their path, came within sight of men, Chap. 13, 17, 19. and he expected that time and pains would discover what was then unknown, and posterity wonder that they did not know such plain things, Chap. 25. In these several places there is a better guess about comets, than any made for above fifteen hundred years afterward: and further search has since confirmed what he thought, that it is the excentricity of their orbits which occasions their being only now and then seen. In all those dark ages, from the decline of the Roman empire to the Reformation, comets being only considered as ominous meteors, three only have been yet found described enough to determine their orbits, and those but in a gross manner: and I think Appian was the first, who, about 1530, began to observe their motion astronomically; and soon found that, so far from being within our air, they, having no sensible parallax, must needs be much further off than the moon: here then is the first step toward finding out the true nature of comets; and from that time all astronomers have allowed their place to be among the planetary orbits, and many observations were made of their motions by Tycho Brahe and others.

The two comets of 1664 and 65, coming within a few months of one another, made many persons very inquisitive about them; and in Birch's history of the Royal Society, Vol. II. there are two remarkable guesses, both read May 23, 1666. In page 93, are *Mr. Hooke's remarks on Mons. Petit's dissertation on the nature of comets, presented to the society some weeks before.* What that paper contained does not fully appear; but Mr. Hooke said, *the hypotheses were very ingenious, and some of them not improbable, but whether the comets were moved in equal spaces of a curve line in equal spaces of time, which Mons. Petit seemed inclined to believe, deserved to be further examined.* This last clause is remarkable, and that paper, if still preserved, is worth searching, to see how near Mons. Petit was to guessing the truth. The other paper, page 91, is Mr. Hooke's own, endeavouring to account for the planet's motions; where, having proposed the resistance of the æther, he says, *the second cause of inflecting a direct motion into a curve may be from an attractive property of the body placed in the center, whereby it continually endeavours to attract or draw it to itself: for if such a principle be supposed, all the phenomena of the planets seem possible to be explained, by the common principle of mechanick motions; and possibly the prosecuting this speculation may give us a true hypothesis of their motions.*—By this hypothesis the phenomena of the comets as well as of the planets may be solved, and the motion of the secondary as well as of the primary planets: the motion also of the progression of the auge is very evident. This I think was much about the time that Sir Isaac Newton discovered the property of gravity, and seems much like it; only Sir Isaac, being the deeper mathematician, prosecuted the matter further, and cleared it up more fully.

Hevelius was too good an astronomer, not to see that comets were far distant from the earth, and in his *Cometographia*, Book III. p. 149—164, largely

largely shews the absurdity not only of supposing them in our air, but even below the moon, from the vast parallax they would have, and the various places they must needs be seen in at different times of day, as they rise toward the zenith, or descend to the horizon: yet could he not shake off the established opinion that they were meteors; but, to reconcile both, supposes comets to be vapours collected near any of the planets, whirling round about it till thrown out of the atmosphere, and then moving in a straight or curve line till dispersed, Book VII. p. 384; that *comets are not spherical, but round and flat*, p. 338; and, from the time they leave the planet's atmosphere, *always turn one flat side toward the Sun*, p. 666; and though, Book IX. p. 591—632, he calculates the places of several comets, as if moving in a straight line, and generally comes nearer the observed place, than I should expect such an hypothesis to do; yet he thinks that *their course is not really straight*, p. 588; and in more largely treating on the subject, says, *it is a Parabola*, p. 659. It may surprize those who have not read Hevelius, to hear that he first said a comet's orbit is parabolical, a discovery generally attributed to Sir Isaac Newton; and indeed not without reason, for Hevelius did but guess it, and knew not the principle on which its motion depended, but it was Sir Isaac Newton who first proved it, and accounted for its motion in that curve, from that universal principle of Gravity, on which the motion of all the heavenly bodies depend. We may however give Hevelius his due praise as a good astronomer, and by a short extract from his *Cometographia*, Book IX. shew how nearly he guessed at the true motion of comets, without knowing, or even suspecting, the real cause which kept them in such a trajectory. A comet then, he says, "by no means moves in a straight line, but in a curve, always concave toward the sun," p. 658, that is, "*in a Parabola*," p. 659: this he illustrates by "the parabolick motion of projectiles," p. 660. He seems here to be got very near the point, yet shews afterward he did not think of gravity as the cause of a comet's parabola: for "as projectiles move in a parabola, from a compound of their progressive motion and gravity, so comets also have a double motion; one the force given them at leaving the planet's atmosphere, the other not gravity, yet something not unlike it, by which comets turn one of their flat sides toward the sun, as the center of our system, p. 666, as a magnetick needle points toward the North, or toward a loadstone. And as in projectiles gravity, so in comets the inclination of their flat sides, turns them out of their straight course," as a rudder turns about a ship, which he had before largely considered, p. 570—587. "And the farther a comet gets from the sun, the more will its flat side be opposed to its motion, which will not only more and more retard its swiftness, but turn it out of its straight course, p. 667. But a comet differs from a projectile, in that a body thrown up moves slowest at the vertex of its parabola, and swifter both in rising and falling; while a comet moves swiftest at the vertex, where
" a line.

“ a line from the sun is perpendicular to its path, and slower both in
 “ approaching the sun and retiring from it, p. 669. If you ask whether
 “ a comet’s path is not an hyperbola,” he “ will not deny it: it is neither
 “ circle nor ellipsis, but may be any other section of a cone, which is
 “ most bent in the middle, and straighter at each end: yet is satisfied it
 “ is rather a parabola than an hyperbola,” p. 683. Lastly, “ as the
 “ planets regard the sun as their center, so the comets also obey it in their
 “ way,” p. 701. We see here that Hevelius, whether by a mere guess at
 what he thought must needs follow from his notion of comets being flat
 bodies, generally standing oblique to the path they move in, or finding
 such a motion to agree best with his observations, came very near to what
 has since been found to be the truth: that comets move in a parabola,
 concave toward the sun, swiftest at the vertex, that is, when they are
 nearest the sun, and their motion perpendicular to a line from it, and that
 it is an action of the sun on comets which makes them turn out of a
 straight line into a curved trajectory. So far he is right, and seems got
 near the point, but is defective in not suspecting the sun to be the parabola’s
 focus, expressly denying their moving in an ellipsis, and consequently
 returning again; and the doctrine of gravity being a later discovery, he
 is forced to account for their curve another way. We may learn also from
 his book, that studies, of which we do not at first see the benefit, are not
 therefore always useless. Hevelius made many observations and calcu-
 lations of the motion of comets; on which if a person at that time had
 said to him, *cui bono?* why so much time and pains spent on vapours,
 which were collected yesterday, and will be dispersed to-morrow? he, own-
 ing them to be nothing else, could not perhaps have given any sufficient
 reason for it: yet if he and others had not taken that pains, Sir Isaac
 Newton would hardly have found out their real motion; and there is a
 field yet open for further discoveries of future ages about them.

Sir Isaac Newton having discovered that gravity is universal, and that
 a planet whose velocity was in a due proportion to its gravity toward the
 sun, would revolve about it in a perfect circle; but in an ellipsis, of which
 the sun is one focus, if its motion was either faster or slower; on recon-
 sidering the matter, on occasion of that remarkable comet of 1680, he
 found, that, if a body is thrown with a velocity, which is to that necessary
 to keep it in a circle, *as the square root of 2 to 1*; the same universal prin-
 ciple of gravity will make it move in a *parabola*, of which the sun is the
 focus: and this being found agreeable to the observed motion of comets,
 has been since allowed by astronomers to be their real motion. It seems
 however not agreeable to the uniformity of the universe, that after a short
 view of the sun, they should be continually flying farther off, in that wide
 void beyond the planetary bounds, to creep along that dark cold region
 for millions of years; (and in less time than that, they could not reach
 any other system, if the parallax of the fixed stars be two seconds, which

Dr. Bradley has found it cannot exceed;) but that they should rather revolve round the sun, in certain, though long periods: and the likeness of the elements of some of the comets seen in different ages, make it probable they were the same returning again; if so, their trajectories are not *really parabolas*; but they seem a kind of planets, revolving round the sun in *so extremely excentrick ellipses*, that, so far as we can see them, they are not sensibly different from parabolas, which for ease of calculation we always suppose them to be: and that their motion is almost exactly a parabola, I intend to shew particularly as to the comet of 1744, see page 14. The true motion of comets being thus known, Sir Isaac Newton applied himself to find a method, by which a comet's orbit might be determined from a course of observations; and, having attempted many ways in vain, hit at last on one, which he has explained, Boook III. Prop. 41, &c. of his *Principia*, taking for his example the comet of 1680. The same method Dr. Halley used for twenty-three more, some accurately, others grossly, as the observations he met with were; and several more have been done since by others. From the likeness of the elements, some of these are supposed to be different returns of the same comet: first, those of 1531, 1607, and 1682, with a period of 75 or 76 years, may be expected again about 1758: secondly, those of 1532 and 1661, after a period of $128\frac{1}{2}$ years, may probably return about 1789: thirdly, the observations of that in 1556 were very gross, and those in 1264 still more defective, so that neither orbit can be supposed to be at all accurate; yet from their likeness, though not agreeing very well, may not unlikely be the same, and come again, after a period of 292 years, about 1848: lastly, the comet of 1680 was a very remarkable one; and as at equal intervals, *A. C.* 44, *A. D.* 531, and 1106, others were seen in some respects like it, several persons have supposed they might be the same, being 575 years going round the sun; yet, no observations being made at any of the three former times, it was but a guess; and if the comet of 1106 was seen in March in Cancer, as the manuscript Mr. Dunthorne mentions, *Phil. Trans.* XLVII. p. 287, seems to say, it could by no means be the same as that of 1680, which cannot get beyond Taurus in March, nor be seen in Cancer after December; the period therefore of that comet must remain doubtful, till further light appears.

It may be objected, that the two periods of the comet of 1682 being a whole year different one from the other, there is no knowing when to expect it again. The difference indeed is very great, considering how true the planet's motions are found to be; yet I fear we must not expect the same regularity in a comet's orbit as in a planet's, they being subject to many greater errors: first, crossing all or most of the planet's paths, they may come nearer to one or other of them than any of the planets do to each other, and be more affected by their mutual attraction; especially

if near Jupiter or Saturn, the greatness of which bodies, weaker power of the sun, slowness of their motion, and consequent long continuance near one another, and direction of the comet's path nearly toward the sun, all join to make the alteration of its orbit more sensible: 2dly, a small change of angle will make little difference in a planet's orbit, which is always nearly perpendicular to the sun; but when a comet's path makes only five or ten degrees angle with a line from the sun, a little variation will bear a greater proportion to that small angle, than to 90 degrees: 3dly, as a comet's greatest distance is many times its least, if by a planet's attraction the perihelion is altered but a few miles, that may be greatly multiplied in the aphelion; and if the angle at first is changed but one minute, it may make a great alteration of length, in running four times as far as Saturn, and back again: 4thly, there is but little difference in the velocity of a body, going round the sun in one or two hundred years, and of one keeping a perfect parabola; small therefore must be the difference of one revolving in 75 or 76 years, especially if the same power, which increases its velocity, should make its perihelion distance greater. Now the comet of 1682, in its descent toward the sun, may be near Mars, but that being small will hardly affect it much; again, in going from the sun, it may pass near Venus, a little before it gets to the descending node, and near the earth a little after it: if then one or more of these planets should be in that part of their orbit when the comet passes by, they may make some change in its motion. The comet of 1680 is very liable to alteration, as in its descent it may pass not remote from any of the planets, extremely near the earth, and but a little way from Venus; its motion also being all the time almost directly toward the sun, and its perihelion distance so very small, a little change in its motion might make a very great one in its orbit.

The method Sir Isaac Newton gives, in his *Principia*, is from three observations of a comet, at proper intervals, to find its real trajectory; and Book III. Prop. 41, he has explained in order the several processes, designed chiefly for construction, which was the way he used in his example of the comet of 1680. This operose problem Dr. David Gregory has more fully explained and demonstrated, in the fifth book of his astronomy: it may also be reduced to triangles, and calculated by numbers, which is much more accurate than construction by lines; and though consisting of about an hundred triangles, Dr. Halley undertook it for 24 comets, as others have since for 20 more; and some of them, by greater care or nicer observations, to a very great degree of exactness. Yet as a compleat list of the triangles used, and several cautions necessary in practice, are not published, I have chosen to set them down here, not generally repeating the demonstrations, which Sir Isaac Newton and Dr. Gregory have already done, but supposing one of those books at hand, to add some observations for preventing mistakes, and shewing how it may be reduced to triangles: the letters here used are the same as in Sir Isaac Newton, except

except some few which he had not, and are generally those which Dr. Gregory uses.

He then who would calculate a comet's orbit by triangles, should first construct it as true as may be by lines; for as the method is approximation, it is to no purpose to calculate nicely, while the point tried is much wrong, as the first guess will most likely be; and as the accuracy depends on having, in fig. 2. B near μ , (see Greg. V. 18, 19.) he cannot at first chuse such observations as will make it so. First therefore, out of a set of observations on a comet, chuse three so that you guess that interval of time when the comet was nearest the sun is the shortest, but no great nicety is required this first time. On a large sheet of pasteboard, draw a circle ten inches radius for the *magnus orbis*; mark the points the earth was in at the three times of observation, and call them T, t , and τ , (see fig. 1); from these draw the three observed longitudes of the comet, TA, tB , and τC : on tB take any point B, let V be the intersection of St and $T\tau$, and γ the place the comet was in perpendicularly over B; make $S\gamma^3 : SB \times R^2 :: tV : BE$, which set off on the line SB: through E (Newton's *Princip.* III. lemma 7.) draw AC cutting TA and τC , so that AE:EC as the time between the first and second observations, to the time between the second and third. A and C are near enough for the first trial, the curtate places of the comet in its orbit. To try how true they are, let TA be to the perpendicular AM, as radius to the tangent of the comet's apparent latitude the first time, and $\tau C : CN :: R : \text{tang. of apparent latitude the last time}$, and draw MN the chord of the parabolick arc M γ N, along which the comet moved, while the projection of the points on the ecliptick are A, B, C: then say $SB : S\gamma :: SB + \frac{2}{3}BE$ to a fourth number, nearly equal to (SR, see Greg. V. 20.) the distance from the sun at which a comet would move the chord MN, in the same time as it really did go the arc M γ N: let X be the length run by a comet at the earth's mean distance from the sun, in the time between the first and third observations (Newt. *Prin.* III. 40.) then $\sqrt{SR} : \sqrt{\text{radius}} :: X : MP$, being the length a comet would go in the same time at the height SR. If MN be equal to MP, the point B was taken right; but if very different, as may easily be this first time, take a new point b , find $a c$, and try till MN is nearly equal to MP. Being now near the matter, we must be more exact: bisect the truest AC in I, (see fig. 2.) erect a perpendicular $Ii = Bb$, draw Si , and erect $\lambda\mu$: if μ falls on or near B, the observations are rightly chosen; if not, take one or more new observations, to make B as near as possible to μ , and rather between i and μ than otherwise, (Greg. V. 18, 19.)

The circle drawn for the *magnus orbis* will do again, as will T, t and τ , if carefully drawn as to angle and distance, and the same observations are still used; as also the three longitudes TA, tB , and τC . Set off tB as near as now known, draw AC as before, bisect it in I, erect the perpendicular $Ii = Bb$, (see fig. 2.) compleat the rectangle $Ii\lambda\mu$, and μ is nearly the vertex of the parabolick arc ABC; (Greg. V. 19. coroll.) but may be further

further corrected thus. Produce $I\mu$ to n , so that $\mu n = \frac{1}{2}I\mu$; through S draw $n\xi = 3S\eta$, in the line $B\xi$ take a new point E' , and if the former length BE is not true enough, which yet it will generally be for construction, a truer length for BE' may be found, as directed presently for calculation, thus: a sidereal year is to the time between the first and third observations, as the circumference of a circle to the length of the mean arc the earth moves in that time; the square of half that arc divided by twice the radius, is the fall of the earth in half the time: this, if now done accurately, need not be repeated in *N^o. 7* of the calculation: then $SB : S\gamma :: SB + \frac{1}{3}I\mu : SL$ and $SL^3 : R^2 \times SB + \frac{1}{3}I\mu ::$ the fall of the earth : BE the fall of the comet. Through E' draw $A'C'$, and form the rectangle $I'\lambda'\mu'$, μ' is the vertex of the parabolick arc, (*Greg. V. 19. coroll.*) and $B\xi$ divides the chord very nearly in proportion to the times (*V. 18*). It remains then to try whether the point B was guessed right: say then $SB : S\gamma :: S\mu' + \frac{2}{3}I'\mu' : SR$, and as above find MN and MP : if they are not equal, draw GP parallel to $C'N$, then is $C'G$ the error; take a new length tB , and repeat the process to find a new mn and mp , and error $c'g$. The two figures 3, which are the small part YCG of *fig. 1* and 2, shew the two cases of this correction, when C and c are on the same or opposite sides of z ; where a line drawn through G and g the two points of error will cut YC , that is in the point the comet was really over, when, by a wrong guess at the length tB and tb , it came out C and c ; and setting off $A'F$ and $a'f$ equal to $C'G$ and $c'g$, the true point x may be in like manner found. We may now either proceed to calculate the orbit arithmetically, from the length of tB now very nearly known, or find the elements of the orbit by construction thus; (*see fig. 4.*) two points of a parabola m and n , perpendicularly over the curtate places x and z , with the focus the sun, determine the whole curve: draw then xz , and erect two perpendiculars xm and zn , the tangents of the comet's latitude at the first and third observations, Tx and τz being the radii; $S\Omega$ drawn through the sun and the intersection of xz and mn , is the position of the comet's node. $z\varrho$ a perpendicular let fall from z on $S\Omega$, is to zn the tangent of its latitude, as radius, to tangent of the inclination of the orbit. Produce the perpendiculars $x\sigma$ and $z\varrho$ to m and n , as cosine of inclination to radius, which will be in that position to each other, the sun and line of nodes, as the comet was in its orbit at the first and third observations; on m and n (*fig. 5.*) with radius Sm and Sn draw two circles; a tangent to both circles may be drawn by the eye, or thus, bisect mn , draw a circle on that center passing through m and n , and set off $m\iota = n\gamma = Sn - Sm$, which produce to δ and κ ; $\pi\kappa\delta$ being parallel to $m\gamma$, which is perpendicular to both radii $m\kappa$ and $n\delta$, touches both circles, and $S\pi$ a perpendicular on it from S , is double the perihelion distance: (*De la Hire's plain conicks.*) Wherefore P , the bisection of $S\pi$, is the vertex of the parabola or perihelion point, whose position is determined by the angle nSP or mSP ; as is the time the comet was there, because the parabolick space nSm , is to the

the parabolick space mSP , as the time between the observations, to the time between the perihelion and first observation.

Thus are the elements of a comet's orbit found by construction; but if exactness is required, lines will not do it, but the process must be reduced to triangles, and calculated by numbers. And first see that the observations are good, or else be content with construction, for it is to little purpose to calculate nicely by uncertain data. Next try whether the times are rightly chosen, by the directions already given, (see page 7.) and, for further accuracy, be not content with the earth's places as found by the tables of the sun, but correct them by the menstrual parallax. The weight of the earth being to that of the moon as 39.788 to 1, the distance of the moon, is to the distance of the common center of gravity, as 40.788 to 1. (Newt. *Princ.* III. 37. cor. 4 and 6.) In fig. 6. E is the earth, and M the moon, revolving round C their common center of gravity which moves regularly along the *magnus orbis* ACB round the sun S ; then at any time the sine of the moon's horizontal parallax, is to the sine of the sun's parallax divided by 40.788, as SC to CE . In the triangle SCE , given SC , CE and SCE , then CSE is the required correction of the sun's place, and SE the real distance of the earth from the sun. This triangle however need not be solved, the tables IV. and V. giving the required correction in angle, and the length of the line ED , to be added to or subtracted from SC , the distance of the sun as found by the common tables. As the moon has sometimes above five degrees of latitude, and therefore the earth is not absolutely in the plain of the ecliptick, for perfect exactness that should be allowed for; but as the whole menstrual parallax is very small, this, which is but a small part of it, may I suppose be safely neglected. Lastly, before calculating, draw a set of figures suited to the particular case, for no general rule can be given where to add and where subtract; the case I have drawn, and suited the *plus* and *minus* to, is the comet of 1742; and another set of figures will shew, whether to add or subtract in that case. Thus prepared, the following is a list of the triangles required, what is given and what is sought, for fixing the due length of the lines, which determine the comet's trajectory.

N ^o .	Triang.	Given.	Sought.	Remarks.
1	$\triangle T \tau$	ST , $S \tau$, and $TS \tau$	$ST \tau$, $S \tau T$, [and $T \tau$]	$ST \tau - STY = \tau TY$. [$S \tau T - S \tau Y = T \tau Y$]
2	$\triangle TY \tau$	$T \tau$ and τTY (N ^o . 1) and $TY \tau$	TY and τY	See fig. 1.
3	$\triangle SB$	$\angle B$ (a guess) $S \angle$ and $S \angle B$	$\angle SB$ and SB	$S \tau + \angle SB = DS \tau$
4	$\triangle B \gamma$	γ perpendicularly over B	R : tang. ap. [Lat.: $\angle B: B \gamma$]	
5	$\triangle SB \gamma$	SB (N ^o . 3) $B \gamma$ (N ^o . 4) $SB \gamma = (90^\circ)$	$S \gamma$	[Construction]
6		$SB: S \gamma :: SB + \frac{1}{2} I \mu: SL$	$I \mu$ taken from the last	
7		$365.256: U + W :: 2R \times 3.14159: \chi + \omega$	$\frac{\frac{1}{2} \chi + \omega^2}{2R} = \gamma +$	Greg. I. 25. [cor. 1.]

N ^o .	Triang.	Given.	Sought.	Remarks.
8		$SL^3 : R^2 \times SB + \frac{1}{3} I \mu :: \zeta \downarrow$	BE	
9	$DS\tau$	$S\tau, S\tau D$ and $DS\tau$ (N ^o . 3)	SD and τD	$SD + BE - SB = DE$
10		$W : U + W :: DE$	DQ	AH equal and parallel to $[DQ]$
11	AHY	AH (N ^o . 10) AYH and AHY (N ^o . 9)	AY and HY	$\tau D + HY - \tau Y = HD$
12		$U : U + W :: HD$	HC	
13	ACH	AH, HC and AHC	$ACH, CAH,$ [and AC]	$AYC + ACH + YAC$ [$= 180^\circ$]
14		$U + W : U :: AC$	AE	
15	BEb	BE (N ^o . 8) BbE ($= 90^\circ$) BEb ($= SD\tau - ACH$)	$Bb = Ii$	See fig. 2.
16	SEI	SE ($= SB - BE$) IE ($= \frac{1}{2} AC - AE$) SEI (N ^o . 15)	SIE and SI	$SIE + 90^\circ = SIi$
17	SIi	SI, Ii (N ^o . 15) and SIi	SiI	
18	$Ii\lambda$	$Ii, Ii\lambda$ (N ^o . 17) $iI\lambda$ ($= 90^\circ$)	$i\lambda = I\mu$	$I\mu \times 1.5 = In$
19	$SI\mu$	SI (N ^o . 16) $I\mu$ and $SI\mu$ ($= SIE + I\lambda i$)	$S\mu$	
20	$SI\eta$	SI, In (N ^o . 18) and $SI\eta$	ηSI and $S\eta$	$2S\eta = S\zeta, \eta SI - ISE = SE$ [the Suppl. of $BS\zeta$]
21	$SB\zeta$	$SB, S\zeta$ and $BS\zeta$	$SB\zeta$	Greg. V. 18.
22	BDD	BDD (N ^o . 9) DBD' ($= SB\zeta$) BD ($= SD - SB$)	BD' and DD'	
23		$SB : S\gamma :: S\mu + \frac{1}{3} I\mu$	SL	Greg. V. 21.
24		$SL^3 : R^2 \times S\mu + \frac{1}{3} I\mu :: \zeta \downarrow$	BE'	$BD' + BE' = D'E'$
25	$SE'B$	SB, BE' and SBE' (N ^o . 21)	SE' and BSE'	
Repeat 10—19 to find $A'C', SI', I'\mu'$ and $S\mu'$				
(11) 27	$A'HY$	$BD'D$ (N ^o . 22)		$\tau D + H'Y - \tau Y - DD'$ [$= H'D'$]
(15) 31	$BE'b'$	(N ^o . 22 and 29)		
(16) 32	SE'	(N ^o . 25) $SE'I' =$ Suppl. $BE'b'$	$+SB\zeta + BSE'$	
36		$S\mu' : S\mu' + \frac{1}{3} I'\mu'$	$S\rho \div$	
37		$SB : S\gamma :: S\rho$	SR	
38	TAM	$R : \text{tang. Lat.} :: TA'$	$A'M$	
39	$\tau C'N$	$R : \text{tang. Lat.} :: \tau C'$	$C'N$	
40	MKN	MK ($= A'C'$) KN ($= CN - A'M$) MKN (90°)	MN	
41	$\sqrt{SR}$	(N ^o . 37) $\sqrt{R} :: \chi \downarrow \omega$ (N ^o . 7)	MP	Greg. I. 42. and V. 20.
If $MN = MP$, M and N are two true Points in the comet's orbit, proceed therefore to N ^o . 89; and thence find the elements; but if not equal, take a new point b , so that $MN : MP \sqrt{S\gamma'} : \sqrt{S\gamma} :: Ye : Ye'$, and repeat the whole process, except N ^o . 1, 2, and 7.				
80		$MN : NP :: A'C' : C'G = A'F$		
81		$mn : np :: a'c' : c'g = a'f$		See fig. 3.
82	$c'pg$	$c'g, cpg$ ($= A'C'H$ N ^o . 29) $p'c'g$ (N ^o . 67)	$c'p$ and pg	$YC' - Yc' + c'p = C'p$
83		$C'G \pm pg : C'p :: C'g : C'z$		$\tau C' - C'z = \tau z$
84	In like manner find $A'x$			$TA' - A'x = Tx$
85				
86	$I'xm$	$R : \text{tang. Lat.} :: Tx$	xm	
87	τzn	$R : \text{tang. Lat.} :: \tau z$	zn	
88	xyx	Yx ($= Tx - TY$) Yx and xyx	Yzx and xz	
89	STx	ST, Tx and STx	TSx and Sx	
90	$S\tau z$	$S\tau, \tau z$ and $S\tau z$	τzS and Sz	$\tau zS - Yzx = Szx$
91		$(zn - xm) = rn : rm :: zn$	$z\delta$	See fig. 4.
92	$Sz\delta$	Sz (N ^o . 90) $z\delta$ and $Sz\delta$ (N ^o . 90)	$zS\delta$ and $S\delta$	$\tau Sz - zS\delta = \tau S\delta$
93	$Sz\epsilon$	$Sz, zS\epsilon$ and $S\epsilon z$ ($= 90^\circ$)	$z\epsilon$	[Place of the Node.]
94	$nz\epsilon$	$z\epsilon, zn$ and $nz\epsilon$ ($= 90^\circ$) $z\epsilon : zn :: R$	$\text{tang. } z\epsilon n$	Inclination of the Orbit.
95	Sxm	Sx, xm and Sxm ($= 90^\circ$)	Sm	
96	Szn	Sz, zn and Szn ($= 90^\circ$)	Sn	
97	rmn	rm (N ^o . 88) rn (N ^o . 91) rmn ($= 90^\circ$)	mn	
98	Smn	Sm, Sn and mn	Smn and mSn	See fig. 5.
99	$mn\gamma$	$mn, n\gamma$ ($= Sn - Sm$) $m\gamma n$ ($= 90^\circ$)	$mn\gamma$	$180^\circ - Smn - mn\gamma = nSP$

N ^o .	Triang.	Given.	Sought.	Remarks.
100	$S \pi \Omega$	$S \pi, S \Omega$ (N ^o . 92) $S \pi \Omega$	$n S \Omega$	$n SP - n S \Omega = PS \Omega$. Perihelion from [Node.
101	$S \pi \theta$	$S \pi, n S \theta$, and $S \theta \pi (= 90^\circ)$	$S \theta$	$\frac{\theta \pi + S \theta}{2} = SP$. Perihelion Distance.
102		Parabolick space $PS \pi - PS m$, is to $PS m$, as time between the ob- } Time of servations, to time between the Perihelion and first observation } Perihelion.		

N. B. The parabolick space may be either taken out of the table of the parabola, or calculated in the same manner that was done.

N^o. 7. I call the time between the first and second observations U, and that between the second and third W. Then a sidereal year is to the whole time, as the circumference of the circle to the arc moved in that time: and the square of half that arc, divided by twice the radius, is the earth's fall toward the sun in half the time.

N^o. 6, 7, 8. I find BE this way rather than Sir Isaac Newton's, which is only an approximation, and irregularly too great or too small, as the times are more or less unequally divided, and $T \tau$ in the more or less curved parts of the earth's orbit. But this way, if found as in N^o. 23, 24, would be true; and $S \mu$ being not yet known, I use SB for it, which is very nearly the same: nor is $I \mu$ yet found, but as the comet has been already constructed, it is there given near enough for this process.

N^o. 20. Since, by Greg. V. 18, the right line $n S \xi = 3 S \pi$ is the truth, full as easy, and, requiring no taking out natural numbers, is less liable to error, I wonder Sir Isaac chose to approximate it by the point σ , and $\sigma \xi = 3 S \sigma + 3 i \lambda$. (See his fig. Book III. Prop. 41.)

N^o. 23, 24. In Greg. V. 21, the comet's fall at the height SL is $M V = V Z$, (see his fig.) Now B and μ nearly coinciding, by similar triangles $SB : S \gamma$ (N^o. 5) :: $SL (= S \mu + \frac{1}{3} I \mu) : SL$. Again, $SL^2 : R^2 :: \zeta \psi$ (the earth's mean fall) : the fall at the point L. Greg. I. 42. And by similar triangles $SL : S \mu + \frac{1}{3} I \mu ::$ the fall at L : BE; then $SL^3 : R^2 \times S \mu + \frac{1}{3} I \mu :: \zeta \psi : BE$. This is the true length of μZ or BE, and seldom sensibly different from BE' , which yet being more perpendicular to AC, is a little shorter; and if BE is so long and so oblique to AC, that the very small angle EBE' will sensibly alter its length, then the sine of $BE' b$: sine of $BE b :: BE : BE'$ may be something truer.

N^o. 36. The third proportional to $S \mu$ and $S \mu + \frac{1}{3} I \mu$, which is the truth, see Greg. V. 20, is easier found in Logarithms than $S \mu + \frac{2}{3} I \mu$.

N^o. 37. It is here fit to shew cause for this considerable variation from Sir Isaac Newton. Greg. V. 20, shews that a body at the height SR (see his fig.) would move the chord AB, while the comet really moved the arc AVB. Now μ, l and ρ , in fig. 2, are the projection on the plain of the ecliptick of his V, L and R: then SR, the hypotenuse of the right-angled triangle $S \rho R$, is Gregory's line SR, and therefore the length sought. Sir Isaac's $ID = S \mu + \frac{2}{3} i \lambda$ is nearly the same as $S \rho$; but his IO, being the comet's

comet's mean height above the ecliptick, may if the time is unequally divided, and the inclination of the comet great, considerably differ from the height sought at S_e , which is in S_μ produced: therefore, as in N°. 23, $SB : S\gamma :: S_e : SR$, by similar triangles.

N°. 38, 39. M and N being the points the comet was really in, perpendicularly over A' and C', T A', the curtate distance, is to A' M the height, as radius to tang. of the apparent latitude at the first observation. The like of C' N.

N°. 41. The reason of this double proportion is this: MN, and of course A' C' and the perpendicular Y e, is too large in the proportion of MN to MP; but MP will increase or diminish, as $\angle S\gamma'$ is less or greater than $\angle S\gamma$. Greg. I. 27. This however is very hard to find, and only an approximation at last. An easier and as good a way is, to compare the error of the last construction with the error now found by calculation: thus NP — NP the difference of the errors, is to t B — t B the difference of the guesses, as NP the present error, to the required correction of t B.

N°. 80, 81. Sir Isaac Newton takes $CG = NP$; but as the correction is in the plain of AC, not of MN, I make G the projection of P, as C is of N. And if CG is not parallel to cg (fig. 3.) or C c bears not the same proportion to r C, as A a to T A, it may make some difference in the places of x and z, though seldom much.

N°. 80, 81, 82, 84, are not wanted if AC is parallel to ac; for then 83 and 85 will be, $NP \pm np : NP :: Aa : Ax :: Cc : Cz$.

Sir Isaac Newton in his next proposition, and Dr. Gregory V. 31, shew how, by the rule of false, to correct still further the comet's orbit as above found: but that I have here omitted, as hoping and expecting that the directions I have given, being contrived to avoid all error as much as possible, will give the orbit true enough without that laborious correction, which I can hardly think is much less trouble than the calculation of the orbit itself. The changing the comet's *parabolick orbit* into its real *elliptical one*, by this correction, thereby to discover its period, can I doubt be at best but imperfectly done, from the small part of the orbit we can see, especially if so true a parabola as the comet of 1744 had: and unless we see a comet for a very long time, we must be content to wait for that more certain, though tedious discovery, the returning after another period. If any one however, desirous of the utmost exactness, chuses to undertake this last correction, Sir Isaac Newton and Dr. Gregory have both explained and shewn the use of it.

As several persons, especially of late years, have apply'd themselves to finding by Sir Isaac Newton's method, the orbits of several comets, but the result of their labours is no-where that I know of, collected into one view, I have here made a general table of all that I have found. And as since 1700 many are calculated by two persons, I set down both orbits, not always knowing which is best, and thinking it useful to preserve all,

to be at leisure compared, either by observations already made, or by those who shall see their next returns. Some of these different orbits vary little, as that of 1744, others differ widely, as that of 1739; probably sometimes from defectiveness in the observations one or both of the calculators used. I found several difficulties in making this table, from false prints, and authors not being always careful to set down the *ascending node*, having more than once found two persons set down the same comet's node in the opposite signs. By comparing the orbits with the observations, I have aimed to avoid mistakes, but have not met with observations of all of them to compare with, and lesser errors may escape; if therefore the authors, or any one else, shall find any mistake inadvertently slipped in, I shall be obliged to them for an account of it, and not fail to correct it when opportunity offers. See the list in table I.

The first 7 of these comets, and those of 1593 and 1596, being but imperfectly observed, can be but grossly done; as also those of 1678 and 1702, unless the calculators used better observations than I have found: that of 1533 will by no means suit the observations in Hevelius, so that I suspect some mistake or false print: Struijck gives the comet of 1699 from Caille, but makes the perihelion Jan. 2, and the ascending node in ∞ , which is right I do not know, any further than that I have found Caille carelessly setting down the wrong node in other instances: not having met with the observations, I can say nothing of the accuracy of those of 1699, 1706, 7, 29, 43, and 48: Downes's orbit of the comet of 1718 suits best, so far as I have tried it, and Caille's of 1739: none of the orbits of the comet of Jan. 1742 agree well with the set of observations in Phil. Trans. No. 481; mine, which was calculated from the observations there mentioned of Mar. 2 and 16, and Apr. 2, agrees I think as well as any of them, but generally gives the latitude too small, being done a good while ago, from a more imperfect list of triangles than that here given in pages 9, 10, 11: C and Struijck differ 10 degrees in the node of the comet of December 1742, which is probably a false print, but I cannot correct it: the comet of 1747 was seen in August 1746, half a year before its perihelion, being then between two and three times as far from the earth as the sun is, and between three and four times the earth's distance off the sun; and its perihelion being above twice the earth's distance, we must not expect exactness there: Dr. Bradley's two comets of 1723 and 1737 are very accurate; as is also Betts's of 1744, calculated from observations made between Dec. 23, 1743, and Feb. 18, 1743-4; but as it was seen for a little while about two months before, when far distant from the earth, and much more from the sun, I have compared three observations sent me from Mr. Morris with Betts's orbit, and found them to agree perfectly; which proves both the truth of the elements, and that the comet's ellipsis was so far at least insensibly different from a parabola; or else those observations, made four months before the perihelion, and two before the obser-

vations the orbit was found by, would not have agreed so well: the hour of observation not being given, I have in the following table calculated for 8^h 17' each evening.

<i>Comet of 1744, seen in 1743.</i>					
		Observation.		Calculation.	
		Long.	Lat.	Long.	Lat.
Oct. 22	8	26.46	N. 7.35	8 26.41	N. 7.35
27		24.14	8.28	24.15	8.31
Nov. 1		21.25	9.26	21.25	9.28

I collected these orbits from first, Dr. Halley's 24 comets, now printed in his astronomical tables; secondly, Caille's list in his astronomy, art. 560, Robertson's translation, page 236; thirdly, a collection by N. Struick, Phil. Transf. N°. 492; fourthly, several single ones, 1723, 37, 39, 44, and 1264, from Phil. Transf. N°. 382, 446, 461, 474, and Vol. 47, page 283, and Mr. G. Whiston's of 1718, from himself. The reason of my adding and altering some particulars in this table are these: the articles used in calculating a comet's place are, the time of the perihelion, log. of diurnal motion, distance of perihelion from node, cosine and sine of the comet's inclination, place of the node, whether direct or retrograde, and log. of the perihelion distance; these therefore are all inserted: and since, notwithstanding care, false prints will sometimes creep in, and I have met with difficulties from them, I aim to frame this table so as to find them out. The observations will soon shew whether the year of the comet is right; but on the second column I neither have, nor know how to find any check: the log. of the diurnal motion is found from the log. of the perihelion distance, if therefore these articles agree together, both are probably right, if they do not, the natural perihelion distance will shew which is true: the perihelion place is a fictitious thing, for its distance from the node is measured in the plain of the comet's orbit; but that, especially in a very oblique comet, is by no means the same number of degrees on the ecliptick, except at the nodes and their perpendiculars; the only use therefore of inserting it is, by comparing that, the node, and perih. post nod. together, to find out any false print: as to the seventh column, Dr. Halley gave the distance of the perihelion from the node, whether before or after; but I count the number of degrees a comet moves, from passing its ascending node to its perihelion, whether more or less than 180 degrees; this saves a little trouble in computing a comet's place, as I shall shew when I come to explain that, (see page 18). The node, being the connexion of the plain of the ecliptick with the comet's orbit, is the key of the whole work; and whoever calculates or collects orbits, should remember, that it is the *ascend-*

ing node must be inserted, and the article perih. post nod. reckoned from that, or else confusion is caused, and the comet found in false latitude: giving the inclination of the orbit is not strictly necessary, if its sine and cosine are but given, which prove one another: the twelfth column needs no explaining: and in the last I give the calculator's name, where I know it; but as Caille names no author, those taken only from him are marked C, as I can trace them no further.

Dr. Halley made a table of the parabola, for finding a comet's place at any time, printed with his list of orbits, and shewed the way of using it: he goes the direct way, for, dividing the first quadrant of the parabola into 100 equal parts, he gives the angle each is in from the vertex, and its increase of distance from the focus: but the calculation being tedious, and one such part altering the angle but little, at a distance from the vertex, he computed every part only to 100, that is, to the *latus rectum*, and to every second, fourth part, or greater interval afterwards. This table is 240 lines in all, but though very useful has some defects; for, being too short, the differences are often too large, and too unequal, for finding proportional parts truly, especially in the log. of the distance; again, proportional parts can hardly be found at the breaks, where the interval alters from 1 to 2, 4, 10, 20, 50, 100, 200, 500, 1000, and 5000; lastly, it may however serve as far as 1000, that is, $144^{\circ}\frac{1}{2}$ from the perihelion, which is far enough for many comets, but those whose perihelion distance is small, are seen much further; that of 1680 goes near $162^{\circ}\frac{3}{4}$ within four days after its perihelion, and may be seen to about 174° , this table therefore will by no means do for that. Finding these inconveniences, and not caring for so difficult a calculation as Dr. Halley's, I thought of interlining his table by the differences, but found it very troublesome; and being advised to make a new table, on an easier plan, to find the distance and space from the angle, I considered it, and found the demonstration plain, the calculation very easy, the method such as might be carried on regularly, from beginning to end of the table, and having finished it, the differences were more regular than I expected; for proportional parts will determine to about half a second, the angle the comet of 1680 is in from the sun, at the greatest distance we can see it, and the log. of distance almost to perfect exactness, in any part of the table. The principles of this method may be seen in fig. 7. and let R stand for radius, *s* for sine, and *v* for versine.

$$(1) \begin{cases} SC = ST = SR & \text{De la Hire's plain conicks.} \\ Sc = St = Sr & \text{Parabola, Prop. 4, cor.} \end{cases}$$

$$(2) \begin{cases} PQ = PT = SC - SP = s - 1 & \text{Prop. 7.} \\ Pq = Pt = Sc - Sp = s - 1 \end{cases}$$

$$(3) RQ = rq = 2SP \quad \text{Prop. 9.}$$

$$(4) SmnP = \frac{2}{3}Sm \times SP = 1.3 \quad \therefore 1 = \frac{3}{4}SmnP$$

$$(5) \begin{cases} RQ : SC :: v. \text{ of } RSC : R \\ rq : Sc :: v. \text{ of } rSc : R \end{cases} \therefore 2 : s = \frac{2}{v} \quad (\text{See 1. and 3.})$$

$$(6) R : s :: \rho : \sigma = \rho s$$

$$(7) \begin{cases} SC^m P = \frac{1}{2} SP + \frac{1}{8} PQ \times \sigma \\ SC^n P = \frac{1}{2} SP + \frac{1}{8} Pq \times \sigma \end{cases} \text{ Quadrature of parabola.}$$

$$(8) \begin{cases} \frac{3}{4} SC^m P = \frac{3 SP + PQ}{8} \times \sigma = \frac{3 + \rho - 1}{8} \times \sigma = \frac{2 + \rho}{8} \times \sigma \\ \frac{3}{4} SC^n P = \frac{3 SP + Pq}{8} \times \sigma = \frac{3 + \rho - 1}{8} \times \sigma = \frac{2 + \rho}{8} \times \sigma \end{cases}$$

ρ may be found a little easier thus, by fig. 8.

$$(9) SB^2 = AB \times VB = 2 R v \text{ by similar triangles.}$$

$$(10) SM^2 = \frac{R v}{2} = s^2 \text{ of } \frac{1}{2} SCB$$

$$(11) \frac{R}{SM^2} = \frac{2 R}{R v} = \frac{2}{v} = \rho \text{ as before found.}$$

Examples of the first method.

Angle from aphelion $112^\circ.55'$

$65^\circ.50'$

2	0.3010300		0.3010300	
v	0.1428248		9.7712991	
$\sigma \left\{ \begin{array}{l} \rho \\ s \end{array} \right.$	0.1582052	= 1.4394	0.5297309	= 3.3863
	9.9642937	2.	9.9601655	2.
$2 + \rho$	0.5364926	237	0.7312940	55
Ar. Comp. 8.	9.0969100	126	9.0969100	81
ScnP	9.7559015	302	0.3181004	129
		99		34

Examples of the latter method.

Angle r S c $122^\circ.45'$

Angle R S C $61^\circ.10'$

	1.2978		3.8629	
R	0.1132346		0.5869212	
SM ²	9.9248161	268	9.9425171	77
s.	0.5182349	132	0.7681176	74
$2 + \rho$	9.0969100		9.0969100	
Ar. Comp. 8.		334		112
ScnP	9.6531956	106	0.3944659	51

This method of calculation, by which the parabolick table, N^o. II. is made to every fifth minute of angle, supposes, as is the natural and regular way, that the parabolick space at 90 degrees from the vertex is 1, and so I should have entered it in the table, had I been to choose; but Dr. Halley having divided that space into 100 parts, and fitted the log. of diurnal motion and method of reckoning to that, I have, to avoid confusion, suited

my

my table to his, by adding two to the index of the space as above found. The log. of distance proceeds regularly all the way, with increasing differences; but one break was necessary in the mean motion, for the log. of space is extremely unequal near the perihelion, as is the natural space at a great distance from it; the first 45 degrees therefore is the natural space, and the rest of the table its logarithm: yet no difficulty can hence arise, since both are very regular where the table alters. As the differences increase very fast toward the end of the table, No. III. shews how near proportional parts will give a comet's real angle and distance: 45 degrees from the perihelion is tried, because there the differences of the log. of mean motion decrease, while those of the log. of distance increase, yet no sensible error does thence arise: few comets are seen above 155 degrees, nor that of 1680 more than about 174 degrees from the perihelion. The two first columns are the angle, and true log. of mean motion; the third is the angle which proportional parts would give as answering to that logarithm: for instance, 7.522283 is the true log. of mean motion for $178^{\circ}.57'.30''$, but proportional parts would give $178^{\circ}.57'.27''$ for it, that is 3" wrong; and 7.523327, the arithmetical mean between the mean motion at $178^{\circ}.55'$ and 179° , would be called the log. of mean motion for $178^{\circ}.57'.30''$. The fourth column is the true logarithm of distance; and the fifth what logarithm of distance proportional parts would give, as answering to the true log. of mean motion: and though the differences increase so greatly toward the end of the table, yet as both log. of mean motion and log. of distance increase proportionally, no error is thereby caused; and this is the case used in calculating a comet's place: but if on any other occasion, the log. of distance at any certain angle is required, the sixth column gives the log. of distance found by equal divisions, the seventh its error, and the eighth how much that point of the parabola is by this error carried too far from the focus: for instance, 2.115806 is the true log. of distance at $169^{\circ}.57'\frac{1}{2}$, by equal divisions 2.115813 will be found for it, which is 7 too much, and that point is by this means made $\frac{1}{300000}$ th part too far distant from the focus; this is the greatest error between $169^{\circ}.55'$ and 170° , for if tried at $169^{\circ}.56'$, $57'$, $58'$, or $59'$, the error is less. We see then that in the case of computing a comet's place, this table will never err more than half a second in angle, (much nicer than any orbit is known,) and in all places gives the log. of distance true.

Since the velocity of a body moving in a parabola, is to that of one moving in a circle, as $\sqrt{2}$ to 1, (Newton's *Princ.* I. 16, cor. 7.) the periodical time of a planet, is to the time a comet of equal perihelion distance takes to go its first quadrant, as the area of the circle $= 1 \times 3.14159$, to the area of that quadrant divided by the $\sqrt{2}$, that is, $\frac{1 \times \frac{\pi}{4}}{\sqrt{2}} = 1 \times \frac{2}{3} \times \sqrt{2}$; and is therefore thus found, in a comet whose perihelion distance is the radius of the *magnus orbis*:

$$3.14159:\frac{2}{3}\sqrt{2}::365^d.6^h.9'.12'' (365.25639):(109.61543) 109^d.14^h.46'.13''.$$

$$365.25639 = 2.5625978$$

$$\sqrt{2} \quad 0.1505150$$

$$2 \quad 0.3010300$$

$$3 \quad 0.4771212$$

$$3.14159 \quad 0.4971499$$

$$109.61543 = 2.0398717$$

$$100. \quad 2.$$

$$0.9122802 = 9.9601283 \text{ Diurnal motion.}$$

Diurnal motion of comet 1682.

Comet 1664.

$$\text{Log. perih. } 9.765877$$

$$\frac{1}{2} \quad 9.882939$$

$$\text{Perih. fefq. } 9.648816$$

$$9.960128$$

$$\text{Log. d. mot. } 0.311312$$

$$0.011044$$

$$5522$$

$$0.016566$$

$$9.960128$$

$$9.943562$$

Its diurnal motion therefore is 100, the number of parts that quadrant is divided into, divided by $109^h.14^d.46'.13''$, the time it is going it; that is, 0.912280, whose log. is 9.960128. Hence any other comet's diurnal motion is found; for velocity is reciprocally as the square root of the distance from the sun, and the sine of the angle (and therefore in small angles the angle itself) is reciprocally as the distance; the apparent motion therefore of a comet as seen from the sun, is reciprocally as the cube of the square root of its distance: the velocity being the root, the distance is the square, and the apparent motion the cube. The diurnal motion therefore, of which I have just given two examples, is perih. fefq. : 1 :: 0.912280 : diurnal motion.

The log. of diurnal motion thus found, saves the four lines used in finding it every time the comet's place is computed: the log. of the time between the comet's perihelion and time sought (reduced to decimals of a day, by table VII.) added to the log. of diurnal motion, gives the log. of mean motion, and if that is above 1.517428, its natural number is not wanted: find then in the parabolick table, N°. II. the article next below the mean motion sought, and say, difference : remainder :: 300'' : proportional parts :: difference of log. of distance : its proportional parts. Required the angle and log. of distance, answering to 1.519782; this is above $45^\circ.15'$; then $986:378::300:115::263:101$; the angle therefore is $45^\circ.16'.55''$, and the log. of distance 0.069658. The next thing wanted is the comet's

378	2.577	2.577
300	2.477	2.420
986	2.994	2.994
115 = 2.060	101 = 2.003	

angle from the node: here, that we may always find it by addition, and save two lines in doing it by a single process, and not take it first from the perihelion, and thence from the node, I vary from Dr. Halley's method; for the article perih. post nodum is always the angle the comet moves, after passing its ascending node till it comes to the perihelion, be it more or less than 180 degrees; and using always the angle the comet has moved since its

its

its last perihelion, (by taking the supplement to 360° , of the angle found by the parabolick table, if the place computed is before the comet's perihelion,) these two angles must always be added together, whether the comet is direct or retrograde, before or after its perihelion, and in whatever part of the orbit its node is; and rejecting 360° if necessary, if the angle is less than 180° the comet is in *north latitude*, if more, in *south*. The tangent and sine of this angle being used in the two next proportions, we must observe, that an angle, its supplement, and 180° more or less, have the same sine and tangent, and that the angle reduced to the ecliptick, is always nearer 0, 180 , or 360 degrees, than the angle from the node. So then $R : \cos. \text{ of Incl. of the orbit} :: \text{tang. of angle from node} : \text{tang. of the angle on the ecliptick}$, which added to the place of the comet's node if direct, or subtracted if retrograde, gives the *heliocentrick longitude*; as $R : s. \text{ Incl.} :: s. \text{ of angle from node} : s. \text{ of heliocentrick latitude}$.

Again, the log. of the comet's perihelion distance, + log. of its increased distance as above found, + cos. of heliocentrick latitude, gives the projection of the comet's place on the plain of the ecliptick, and the sun's place and distance from the earth being found, in the triangle SCE, fig. 10, are given SC, SE, and CSE, therefore the lesser side is to the greater, as $R : \text{tang. of an angle}$, and $R : \text{tang. of that angle} - 45^\circ :: \text{tangent of half the sum} : \text{tang. of half the difference of the two other angles}$; then $\frac{1}{2}$ the sum + $\frac{1}{2}$ the difference being the greater, and $\frac{1}{2}$ sum - $\frac{1}{2}$ difference the lesser angle, the comet's *geocentrick longitude* is thence known. Lastly, $EC : SC$, that is, sine of angle at the sun : sine of angle at the earth :: tang. of heliocentrick latitude : tang. of *geocentrick*. Taking out natural numbers being troublesome and liable to error, I avoid it as much as may be; for instance, when the sine of the heliocentrick latitude is 9.852389, which is above $45^\circ.23'$, its cosine and tangent are wanted, but not the angle itself; then difference of sine is to difference of tangent, as remainder of sine to remainder of tangent; $21 : 42 :: 18 : 36$ for the tangent, which is therefore 10.005847, as the cosine is 9.846542. In like manner let 10.261606 be the tangent of an angle above $61^\circ.17'.50''$; then the tangent of 45° less, or above $16^\circ.17'.50''$ is thus found, $50 : 78 :: 27 : 42$, the tangent then is 9.465972.

78	1.892
27	1.431
50	1.699
42	1.624

Caille's Comet of 1739.				Barker's Comet of Jan. 1742.			
Log. diurn. mot.	0.217546	May 17 ^d . 8 ^h . 39'		0.130344	Feb. 18 ^d . 8 ^h . 32'		
Time 20.0556	1.302236	Perih. June 6. 9. 59		20.7368	1.316742	Jan. 28. 14. 51	
		20. 1. 20				20. 17. 41	
Log. mean mot.	1.519782	1. 12		1.447086		16. 48	
Natural number		7.12		27.9954		43.12	
Angle	45°. 16'. 55"	378.577	577	39°. 23'. 34"	495.695	695	8 38
Supplement	314. 43. 5	300.477	263.420		300.477	226.354	1 09
Perih. post node	104. 46. 34	986.994	994	328. 30. 10	694.841	841	
		115.060	101.003		214.331	161.208	
Ang. from node	59. 29. 39			7. 53. 44			
Cof. Inclination	9.750778			9.582340			
T. ang. from node	10.229750			9.142021			
		3 ^s . 8 ^s . 17'. 35"	23				
Tangent of angle	9.980528			8.724361			
on ecliptick	43°. 42'. 58"			3°. 2'. 4"			
		3 ^s . 8 ^s . 17'. 35"	0.006154				
Sine of Inclinat.	9.917095			9.965701			
S. ang. from node	9.935294			9.137884			
S. helioc. lat.	9.852389			9.103585			
Helioc. lat.							
Long.	13°. 42'. 16"			2°. 7'. 26"			
Log. of perih.	9.828388			9.886522			
Log. of distance	0.069658			0.052367			
Cof. helioc. lat.	9.846542			9.996473			
Curtate distance	9.744588			9.935362			
Earth from sun	0.006194			9.996530			
Tangent	10.261606	78	8 ^s . 6°. 55'. 50"	10.061168	33 ¹ / ₂	6 ^s . 2°. 7'. 26"	
Angle	61°. 17'. 50"	27	5. 13. 42. 16	49°. 1'. 10"	301	5. 11. 9. 8	
T. of ang. — 45°	9.465972	50	2. 23. 13. 34	8.846994	42 ¹ / ₂	20. 58. 18	
Tang. of $\frac{1}{2}$ sum	10.051465	42	3. 6. 46. 26	10.732633	238	159. 1. 42	
		$\frac{1}{2}$ sum	48. 23. 13			79. 30. 51	
Tang. of $\frac{1}{2}$ diff.	9.517437	$\frac{1}{2}$ diff.	18. 13. 14	9.579627		20. 48. 0	
S. ang. at earth	9.701147		66. 36. 27	9.931756	54	100. 18. 51	
Tang. helioc. lat.	10.005847		30. 9. 59	9.107112	167	58. 42. 51	
S. ang. at sun	9.996958			9.553769	165		
Tang. geoc. lat.	9.710036			9.485099	55		
Geocent. lat.	N. 27°. 9'. 10"	Place observed.	N. 27°. 9'	N. 16°. 59'. 30"	Place observed.	N. 16°. 58'	
Long.	☉ 7. 5. 50		☉ 7. 6	☉ 12. 26. 20		☉ 12. 24	

Besides calculating a comet's place, the parabolick table may be used in drawing any *parabola*. For, first, the natural number of the log. of distance at any angle, is the distance of that point of the parabola from the focus, in parts of the focal length; thus any number of points may be set off, by the angle from the vertex, and distance from the focus. Thus the log.

log. of distance at 42 degrees from the vertex is 0.059697; its natural number 1.14735, that point of the parabola therefore is distant from the focus about $1\frac{1}{7}$ of the focal length.

Secondly, One process reduces this distance from the focus, to any other known measure: as let the focal length of a parabola be 3.6 inches; then a point 42 degrees of angle from the vertex is 4.1305 inches from the focus

Log. dist.	0.059697
3.6	0.556302
	0.615999
Dist. in inches	4.1305

Thirdly, The angle in a parabola, at a great distance from the vertex, alters very little; in that case therefore, the points may perhaps be better set off, by the distances from the focus and from the axis, that is, the ordinate; which is thus found, R:s.

ang. from vertex :: dist. from focus : ordinate. And if it be thought better, it may be done by the ordinate and abscissa, which is always one focal length less than the distance from the focus. Take for instance the ordinate, distance from focus, and abscissa at 170 degrees from the vertex, both in parts of the focal length and inches.

S. 170° —	9.239670	9.239670
Dist. a foc.	2.119408 In.	2.119408
Focal length	3.6 =	0.556302
Ordinate	1.359078	1.915380
	22.8601 Inches	82.2962
Dist. a foc.	131.6461	473.9254
Abcissa	130.6461	470.3254

Fourthly, But the best way to draw a comet's orbit round the sun is, marking the points at some certain interval from each other, as suppose 4, 8, 12, &c. days motion from the perihelion; hereby the point the comet is in at any time may quickly be known. To find these points, multiply the comet's diurnal motion by the number of days; the angle in the table corresponding to that, is the angle it is from the perihelion; as the corresponding log. of distance + log. of perihelion distance, gives the distance from the sun, in parts of the *magnus orbis*. Try the comet of 1682, 40 days from its perihelion.

Fifthly, When a comet whose perihelion distance is very small, is a great way from the sun, its angle from the perihelion alters very slowly; the points therefore, if thought better, may be laid out by the distances from the sun and from the axis, as just now proposed in the third use. Find then the angle distance and ordinate of the comet of 1680, at 120 days from its perihelion. Yet if when a comet is much further from the sun than the earth is, its

Log. diur. mot.	0.311312
40 days	1.602060
	1.913372
Ang. from per.	82° 9'
Log. dist.	0.245413
Log. perih.	9.765877
	0.011290
Comet from sun	1.0263
Log. diur. mot.	3.279469
120 days	2.079181
	5.358650
Angle	174° 30' 35"
Log. dist.	2.639480
Log. perih.	7.787106
	0.426586
2.6705 =	8.908007
S. of angle	
	9.407393
Ordinate	0.2555

angle be not set off in the *magnus orbis*, but on a larger concentrick circle, it will I believe be as well done, by the angle from the perihelion and distance from the sun.

In this manner the angle, distance and ordinate of the comet of 1680, and the angle and distance of that of 1682, are given for every fourth day from the perihelion, as far as they can be seen, in table VIII. Table IX. gives the length of the abscissa and ordinate of a parabola, in parts of the focal length, for every tenth degree, and oftener at last. And table X. gives the hourly motion of a comet, at different distances from the sun, (which is as the square root of its distance,) both in parts of the earth's mean distance, and in miles, supposing the earth 77,000,000 of miles from the sun, that is the sun's parallax $10\frac{1}{2}$ seconds; and the times which comets of different perihelion distances take to go from their perihelion to their *latus rectum*; which are to one another as the square root of the cube of their perihelion distance, as I mentioned above in page 18.

Sixthly, As to the use of the table in the parabolick motion of projectiles, see fig. 7. The abscissa PQ , which is the height they rise, is always equal to $SC - SP$, that is one less than the distance from the focus, which is given by the table: the horizontal distance they fly, is twice the ordinate CQ : and $QT (= 2PQ$, that is twice the abscissa) is to CQ (the ordinate) as radius to cot. of QCT , the angle of elevation.

Calculating a comet's place by a parabola, which is a very regular figure, has no proper difficulty in it; yet, being full 30 lines besides the sun's place, &c. is tedious; therefore an easy way to construct a comet's place may be very useful, where only a general account of a comet's motion is wanted, though by no means sufficient where nicety is required. See then fig. 9. On a sheet of pasteboard draw a circle five or ten inches radius for the *magnus orbis*, the center of which is the sun; and the real distance of the earth may be marked about the eighth degree of each sine, a little without the circle from $\simeq$ to r , and a little within it from r to $\simeq$; and divide the circle into signs and degrees. From the table of elements, N^o. I. mark true, both as to angle and distance, the perihelion of the comet required: through the sun draw the axis of the parabola, and by article 4. of the uses of the parabolick table, (page 21) set off the several points of the orbit, where the comet is at every fourth day's interval, on on each side of its perihelion. But as comets do not move in the plain of the ecliptick, on the proper angle, draw through the sun its line of nodes, and from the several points of the orbit, let fall perpendiculars upon it; on them mark a fresh row of points, whose distance from the line of nodes shall each be to their respective perpendiculars, as the cosine of the inclination of the comet's orbit is to radius. These points, which for distinction I make little crosses, form the curve of the projection of the comet's orbit on the plain of the ecliptick, which is always used in constructing a comet's place, and is, as Caille shews, art. 519 of his astronomy, itself also a parabola,

parabola, yet has by no means the same focus or position of axis, as the orbit itself; as would more plainly appear, by drawing the comet of 1577. For better distinction, the parabola itself is a fine stroke; the figures are written on that side of the orbit which is farthest from the line of nodes, and consequently from the projection of the orbit on the ecliptick; and the titles of the comets, are written the same way as the comet moves. Thus is the orbit of a comet made ready for use at any time, and its apparent place may be thus found:

Count the days from the comet's perihelion to the time required, and mark the point in the projection of the orbit, over which the comet then is; lay one edge of a parallel rule, from that point to the place of the earth at the same time, and the other edge passing through the sun, will cut the *magnus orbis* in the apparent longitude of the comet. Again, draw two right lines, cutting each other in the angle of the comet's inclination; from their intersection set off in one of them the length of the perpendicular from the comet's curtate place to the line of nodes, and a perpendicular erected to the other is the tangent of the comet's apparent latitude, making the curtate distance of the comet from the earth the radius. Thus may first, the course of a known comet quickly be traced, and in what part of the heavens to expect first to see it, when it returns again, be found; for since the period of no comet is yet known exactly, and for the reasons mentioned in page 5, they will not perhaps be always equal, we cannot fix the very month a comet will return in; and should therefore know where to look, if it comes a little sooner or later than is expected. Secondly, when a known comet returns, one observation will, with this scheme, shew its whole future course; for from the earth's place, at the time of observation, draw a line in the observed longitude of the comet, this cuts the projection of the comet's orbit in the place where it then was, whether the latitude agrees may be tried as above directed; and the day's motion marked on that curve, will shew where it will be at any other time. Thirdly, the periods of comets may perhaps be sometimes found by this scheme, when the observations are too defective to calculate the orbit by. For instance, no comet seen in August in $\approx$ can be that of 1682, nor can one seen in June easily be that of 1680, which must be then close to or beyond the sun, but one seen in January between $\approx$ and Π may; it remains then to try, whether the latitude, motion, and other circumstances agree with what might be expected of that comet, and as they agree or not, there is a probability of its being the same, or a proof that it is not.

I have chosen as an example of this method of constructing, the comet of 1682, which is shortly expected to return; and in twelve short tables, N°. XI. supposing its perihelion any month in the year, shew what the apparent course of the comet would be, which are very different one from another; for as appears on view, from April to November it would move direct, be in some of the signs from γ counting forward to $\dagger$, and chiefly in

in north latitude: between November and April it would be retrograde, between Π and ϖ counting backward, and be seen, disappear, and be seen again: that if seen about the beginning of summer, being at or a little after its perihelion, it would make the best shew, and be seen the shortest time; but will make very little figure in winter. The two first articles in each table, are the place about which the comet might be first seen, if its perihelion should prove that day which is set at the head of the table; for instance, if its next perihelion should be Sept. 23, whether 1757 or 1758, then about August 14 it may begin to be seen, being in 24 degrees of Π , with 7 or 8 degrees north latitude. These tables shew in general how the comet would move, but in the middle of its course cannot be depended upon for a nicety; as a small inaccuracy may occasion great error, if the comet should cross the *magnus orbis* in its descent toward the sun about the middle of October, or in its ascent about the beginning of May, when it may move 40° in a day: so also if its perihelion should be a week or fortnight different from what I have supposed, it may make a considerable variation in its track. The two known periods of this comet are indeed more different than one could suspect; for the last was not 75 years, and an equal interval would make its next perihelion July 25, 1757; but if this revolution should be as long as the former was, that is above 76 years, it cannot be till Oct. 25, 1758. Yet as the rest of the elements agree so well all the three times, we cannot but suppose them to be the same; and as I can see no principle in nature to make its period alternately longer and shorter, I can refer the different intervals to nothing but those irregularities to which comet's orbits are liable. Yet on this account I have in another table, N^o. XII. shewn in what part of the heavens the comet may be expected to begin to be seen, in any month of the year; as suppose it first gets near enough to be seen the beginning of July, we find that its apparent motion will be then direct, its place the beginning of Π , the latitude north and increasing, and that it will come to its perihelion about a month afterwards.

Thus I have treated of the motion of comets, the gradual discovery of it, the way to find their real path, and to trace it either with respect to the sun or the earth; by which means we may hope to know the times of their revolutions better hereafter. But of their nature and uses I have not ventured to speak, chusing rather to leave such points as are at present so little, I may almost say not at all known, to those, if any such shall hereafter be, who by greater light afforded them shall be enabled to search deeper into those hidden works of God. The works of an infinite Creator are without number; knowledge, though so greatly increased of late, has by no means compleated the search into the works of nature; fresh subjects of admiration and praise will still appear, as long as God sees fit to continue men upon earth, I nor can suppose that increase of knowledge will then cease. The farther we search into the works of God, the more instances of power, wisdom,

wisdom, and goodness we continually meet with. *There are yet hid greater things than these be, for we have seen but a few of his works,* was a wise remark of the son of Syrach, when contemplating and praising God for his many and wonderful works; and the same acknowledgment we may still make. For to begin near home, multitudes of things, both inanimate, plants, and animals familiar to us, were unknown in former times; and great proofs of wisdom and goodness appear in their several properties, the plentiful provision made for the well-being and support of all, and the fitness of every thing to its proper end, yet new discoveries are continually made. But how greatly does our prospect enlarge, when we look on this world only as one small part of the works of our Creator, and on every other planet and comet as a scene of as many and still various wonders! nor can we regard the most distant bodies otherwise than as multiplied instances of the same power and wisdom: how greatly then, considered in this light, *do the heavens declare the glory of God!*

These are thy glorious works, Parent of good
Almighty; thine this universal frame.

Thus wondrous fair, thyself how wondrous then!

MILTON.

To come then to the present point, *he hath made all things for their uses:* comets, which are much more numerous than the planets, are doubtless designed for as wise ends, yet being so very different from them, both in appearance and motion, serve probably to quite different purposes; and possibly we who inhabit a planet, can have no more idea of the design of a comet, than one who never knew any thing of hearing could have of the use of an ear; he might justly conclude, that so artful a machine was not placed in the head for nothing, and so may we of comets, but the real intention we could in neither case find out. The appearance of a comet's tail is very surprizing, and various have been the guesses at the cause of it; Sir Isaac Newton's I think as plausible as any; yet it is much easier to make objections against any of the opinions, than to give a better.

I mean not hereby to discourage inquiry into the nature and uses of comets; no, there is scarce any employment better becomes a creature, than searching into any of the works of the great Creator. Yet let us not stop at the discovery of the works, but be thereby led to acknowledge the workmaster. *If we are astonished at their power and virtue, let us understand how much mightier he is that made them.* If we observe the uniformity of that universal principle of gravity, let us consider the infiniteness of that one God, who in so wonderful yet hidden a manner, restrains the amazing swiftness of such vast bodies, by a power which yet does not hinder the least creature of its proper motion. When we see that the same power which guides those numberless, vast, and immensely distant bodies, is yet

not unmindful of the most minute, we must remember, that he who regards the good of the merely sensitive beings, will much more observe in every action, how we employ that reason he has entrusted us with: that nothing can be concealed from him who made all things; that one constantly employed in doing good cannot be pleased with trifling, nor the wise with folly; that the holy cannot but hate wickedness, the just abhor injustice, and the merciful detest cruelty; and that the all-powerful maker and ruler of the world, must needs in due time distinguish between *him that serveth God, and him that serveth him not*: and above all, that no swiftness can escape him, who threw the astonishingly swift planets and comets, and guides the still much more impetuous light; no distance avoid him, who is not confined to the entire solar system, nor to those multitudes of others, of which we can but just discover the central bright point; that no craft can deceive him from whom all the wisdom in the world is derived; and no power resist him, at whose rebuke the earth trembles, and the very foundations of the hills shake; nor can any greatness protect from him, who *made the small as well as the great, and careth for all alike*, and by whose stroke the greatest monarch is reduced to the same mouldering dust as the lowest of his subjects.

Again, if we admire the wisdom of God as shewn forth in his works, wonder at those inconceivably vast regions of light, the nebulous stars; the surprizing singularity of saturn's ring; and the entire diversity of the comets from the planets; whose uses are all too far beyond our ken to discover: and to come more within our own view, if we remark that wonderful instinct, by which *the swallow knoweth his appointed time*; the careful sorting of proper fruits and creatures, to all the so various climates on our own earth; and the no less surprizing diversity of inhabitants, allotted to such different mediums as air, water, earth, and still harder substances; and the connecting links as it were in the chain of beings, which are between plants and animals, air and water creatures, beasts and birds, &c. let none then pretend to be wiser than God, or above being taught by him; for as we cannot but know it is our interest to please him in whose power we entirely are, so it is as certain, that none knows his will so well as he does himself: nor can there well be a greater folly, than to prefer the uncertain deductions of frail, created reason, (which 4 or 5000 years experience shewed can never form a uniform system of morality; though it could not refuse its assent, when christianity had explained it;) to the clear discoveries, I do not say of unauthorized human glosses, but of the genuine revelations from perfect, self-existent wisdom. Two extreams are here to be avoided; either despising that noble faculty, and glory of man, *reason*, and refusing to see any thing, because we cannot see every thing; this is slighting the gift of God, hiding our talent in the earth, and tends to *enthusiasm*: or on the other hand so glorying in it, as to forget it is the gift of God, and preferring a candle to the light of the sun when offered;

offered; this is despising God himself, refusing to submit to his governance, and tends to *atheism*. Lastly, if on a review of the whole we may justly say, *the works of the Lord are great, sought out of all them that have pleasure therein*; it will appear from contemplating them, that *there is one wise and greatly to be feared, the Lord sitting on his throne*: and as it is plain, that *the Lord is king, be the people never so impatient*, so it is as true, when we consider his extensive wisdom and goodness, that *the earth may be glad thereof*. When therefore, reflecting on the power, wisdom, and goodness of God, as shining forth in his mighty works, *you glorify the Lord, exalt him as much as you can, for even yet he will far exceed; and when you exalt him put forth all your strength, and be not weary, for you can never go far enough*.



TABLE I. *The Elements of the Orbits of*

	Time of Perihelion.	Perih. Dist.	Log. of it.	L. D. Mo.	Place of Perih.	Per. p. Nod.
1264	July 6 ^a 8 ^b "	44500	9.648360	0.487588	♊ 21° "	122° "
1337	June 2 6 25	40666	9.609236	0.546274	♊ 7 59 0	46 22 0
1472	Feb. 28 22 23	54273	9.734584	0.358252	♊ 15 33 30	236 12 50
1531	Aug. 24 21 18 30	56700	9.753583	0.329754	♊ 1 39 0	107 46 0
1532	Oct. 19 22 12	50910	9.706803	0.399924	♊ 21 7 0	30 40 0
1533	June 16 19 30 0	20280	9.307068	0.999526	♊ 27 16 0	338 28 0
1556	April 21 20 3	46390	9.666424	0.460492	♊ 8 50 0	103 8 0
1577	Oct. 26 18 45	18342	9.263447	1.064958	♊ 9 22 0	256 30 0
1580	Nov. 28 15 0	59628	9.775450	0.296953	♊ 19 5 50	90 8 30
1585	Sept. 27 19 20	1.09358	0.038850	9.901853	♊ 8 51 0	331 8 30
1590	Jan. 29 3 45	57661	9.760882	0.318805	♊ 6 54 30	308 36 10
1593	July 8 13 38	08911	8.949940	1.535218	♊ 26 19 0	12 4 45
1596	July 31 19 55	51293	9.710058	0.395041	♊ 18 16 0	83 56 30
1607	Oct. 16 3 50	58680	9.768490	0.307393	♊ 2 16 0	108 5 0
1618	Oct. 29 12 23	37975	9.579498	0.590881	♊ 2 14 0	286 13 0
1652	Nov. 2 15 40	84750	9.928140	0.067918	♊ 28 18 40	300 8 40
1661	Jan. 16 23 41	44851	9.651772	0.482470	♊ 25 58 40	33 28 10
1664	Nov. 24 11 52	1.02575 $\frac{1}{2}$	0.011044	9.943562	♊ 10 41 25	310 32 35
1665	April 14 5 15 30	10649	9.027309	1.419164	♊ 11 54 30	156 7 30
1672	Feb. 20 8 37	69739	9.843476	0.194914	♊ 16 59 30	109 29 0
1677	April 26 0 37 30	28059	9.448072	0.788020	♊ 17 37 5	99 12 5
1678	Aug. 16 14 3 0	1.23802	0.092727	9.821037	♊ 27 46 0	166 6 0
1680	Dec. 8 0 6	00612 $\frac{1}{2}$	7.787106	3.279469	♊ 22 39 30	350 37 30
1682	Sept. 4 7 39	58328	9.765877	0.311312	♊ 2 52 45	108 23 45
1683	July 3 2 50	56020	9.748343	0.337614	♊ 25 29 30	87 53 30
1684	May 29 10 16	96015	9.982339	9.986620	♊ 28 52 0	330 37 0
1686	Sept. 6 14 33	32500	9.511883	0.692304	♊ 17 0 30	86 25 50
1698	Oct. 8 16 57	69129	9.839660	0.200638	♊ 0 51 15	356 53 0
1699	Jan. 3 8 22	74400	9.871570	0.152773	♊ 2 31 6	289 14 29
1702	Mar. 2 14 12	64590	9.810165	0.244881	♊ 18 41 3	309 15 48
1706	{ Jan. 19 4 22	42581	9.629218	0.516301	♊ 12 29 10	59 17 30
	{ 19 4 56 0	42686 $\frac{1}{2}$	9.630291	0.514692	♊ 12 36 25	59 25 2
1707	{ Nov. 30 23 29	85974	9.934368	0.058576	♊ 19 54 56	27 8 21
	{ 30 23 43 6	85904	9.934013	0.059109	♊ 19 58 9	27 7 40
1718	{ Jan. 4 1 14 55	1.02565	0.010999	9.943629	♊ 1 26 36	6 28 50
	{ 3 23 38	1.02655	0.011380	9.943058	♊ 1 30 0	7 13 0
	{ 4 7 48	1.02743	0.011753	9.942499	♊ 1 3 40	7 17 20
1723	Sept. 16 16 10	99265	9.999414	9.961007	♊ 12 52 20	331 23 40
1729	{ June 14 10 56	4.26140	0.629552	9.015800	♊ 22 40 0	12 7 23
	{ 12 6 35 41	4.06980	0.609573	9.045769	♊ 16 53	11 41 38
1737	Jan. 19 8 20	22282	9.347960	0.938188	♊ 25 55 0	99 33 0
1739	{ June 6 9 59	67358	9.828388	0.217546	♊ 12 38 40	104 46 34
	{ 9 9 14	69614	9.842697	0.196083	♊ 5 11	110 7
1742	{ Jan. 28 4 38	76568	9.884049	0.134055	♊ 7 35 13	328 3 16
	{ 28 4 20 50	76555 $\frac{1}{2}$	9.883693	0.134589	♊ 7 33 44	328 1 1
	{ 28 14 51	77005 $\frac{1}{2}$	9.886523	0.130344	♊ 6 39 20	328 30 10
1742	{ Dec. 30 20 25	83501	9.921690	0.077593	♊ 2 41 45	14 20 30
	{ 30 21 15 16	83811 $\frac{1}{2}$	9.923304	0.075172	♊ 2 58 4	24 47 16
1743	Sept. 9 21 16 18	52157	9.717313	0.384159	♊ 6 33 52	118 42 33
1744	{ Feb. 19 8 12	22206	9.346472	0.940420	♊ 17 12 55	151 27 55
	{ 19 8 3	22250	9.347325	0.939141	♊ 17 10 0	151 23 49
1747	{ Feb. 20 7 10	2.10851	0.342128	9.446936	♊ 7 2 0	230 16 50
	{ 17 11 44 38	2.29388	0.360571	9.419272	♊ 10 5 41	226 52 46
1748	April 17 19 25	84066 $\frac{1}{2}$	9.924624	0.073192	♊ 5 0 50	17 51 25
1748	June 7 1 24 15	65525 $\frac{1}{2}$	9.816410	0.235513	♊ 6 9 24	241 29 41

Ascending Node.	Inclination	Cof. of it.	Sine of it.		Calculator.
♈ 19° 0' 0"	36° 30' 0"	9.905179	9.774388	Direct	Dunthorne.
♈ 24 21 0	32 11 0	9.927549	9.726426	Retrog.	Halley.
♈ 11 46 20	5 20 0	9.998116	8.968249	Retrog.	Halley.
♈ 19 25 0	17 56 0	9.978370	9.488424	Retrog.	Halley.
♈ 20 27 0	32 36 0	9.925545	9.731404	Direct	Halley.
♈ 5 44 0	35 49 0	9.908964	9.767300	Retrog.	Downes. (See p. 13.)
♈ 25 42 0	32 6 30	9.927906	9.725521	Direct	Halley.
♈ 25 52 0	74 32 45	9.425644	9.984007	Retrog.	Halley.
♈ 18 57 20	64 40 0	9.631326	9.956089	Direct	Halley.
♈ 7 42 30	6 4 0	9.997561	9.024016	Direct	Halley.
♈ 15 30 40	29 40 40	9.938932	9.694712	Retrog.	Halley.
♈ 14 14 15	87 58 0	8.549995	9.999726	Direct	C.
♈ 12 12 30	55 12 0	9.756418	9.914422	Retrog.	Halley.
♈ 20 21 0	17 2 0	9.980519	9.466761	Retrog.	Halley.
♈ 16 1 0	37 34 0	9.899078	9.785105	Direct	Halley.
♈ 28 10 0	79 28 0	9.261994	9.992619	Direct	Halley.
♈ 22 30 30	32 35 50	9.925559	9.731371	Direct	Halley.
♈ 21 14 0	21 18 30	9.969247	9.560369	Retrog.	Halley.
♈ 18 2 0	76 5 0	9.381134	9.987061	Retrog.	Halley.
♈ 27 30 30	83 22 10	9.062457	9.997085	Direct	Halley.
♈ 26 49 10	79 3 15	9.278481	9.992026	Retrog.	Halley.
♈ 11 40 0	3 4 20	9.999375	8.729122	Direct	Downes.
♈ 2 2 0	60 56 0	9.686482	9.941539	Direct	Halley.
♈ 21 16 30	17 56 0	9.978370	9.488424	Retrog.	Halley.
♈ 23 23 0	83 11 0	9.074424	9.996919	Retrog.	Halley.
♈ 28 15 0	65 48 40	9.612515	9.960090	Direct	Halley.
♈ 20 34 40	31 21 40	9.931409	9.716363	Direct	Halley.
♈ 27 44 15	11 46 0	9.990777	9.309474	Retrog.	Halley.
♈ 21 45 35	69 20 0	9.547689	9.971113	Retrog.	Caille. (See p. 13.)
♈ 9 25 15	4 30 0	9.998659	8.894643	Direct	Caille.
♈ 13 11 40	55 14 10	9.756024	9.914612	{ Direct	C.
♈ 13 11 23	55 14 5	9.756039	9.914605		Struijck.
♈ 22 46 35	88 36 0	8.387962	9.999870	{ Direct	C.
♈ 22 50 29	88 37 40	8.379260	9.999875		Struijck.
♈ 7 55 20	31 12 53	9.932083	9.714536	{ Retrog.	Downes.
♈ 8 43 0	30 20 0	9.936062	9.703317		C. (See p. 13.)
♈ 8 21 0	30 48 30	9.933940	9.709398		Whiston.
♈ 14 16 0	49 59 0	9.808218	9.884148	Retrog.	Bradley.
♈ 10 32 37	76 58 4	9.353126	9.988667	{ Direct	C.
♈ 10 35 15	77 1 58	9.351010	9.988781		Downes.
♈ 16 22 0	18 20 45	9.977346	9.497968	Direct	Bradley.
♈ 27 25 14	55 42 44	9.750778	9.917095	{ Retrog.	Caille. (See p. 13.)
♈ 25 18	53 25	9.775240	9.904711		Zanotti.
♈ 5 38 29	66 59 14	9.592106	9.963985	{ Retrog.	C.
♈ 5 34 45	67 4 11	9.590631	9.964250		Struijck.
♈ 5 9 30	67 31 40	9.582340	9.965701		Barker. (See p. 13.)
♈ 18 21 15	2 19 33	9.999642	8.608337	{ Direct	C.
♈ 8 10 48	2 15 50	9.999661	8.596619		Struijck.
♈ 5 16 25	45 48 21	9.843290	9.855508	Retrog.	Klinkenberg.
♈ 15 45 20	47 8 36	9.832616	9.865138	{ Direct	Betts.
♈ 15 46 11	47 5 18	9.833064	9.864751		C.
♈ 27 18 50	79 6 20	9.276462	9.992101	{ Retrog.	C.
♈ 26 58 27	77 56 55	9.319707	9.990321		Chezeaux.
♈ 22 52 15	85 27 0	8.899432	9.998629	Retrog.	Maraldi.
♈ 4 39 43	56 59 3	9.736293	9.923513	Direct	Struijck.

TABLE II. *A general Table of the Parabola.*

Angle from Perihelion.	Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.
0 0	0.0545	545	0.000000	0	4 35	3.0030	547	0.000695	25
10	0.1091	546	0.000001	1	40	3.0577	547	0.000720	25
15	0.1636	545	0.000002	1	45	3.1124	547	0.000746	26
20	0.2182	546	0.000004	2	50	3.1672	548	0.000773	27
25	0.2727	545	0.000006	2	55	3.2219	547	0.000800	27
30	0.3272	545	0.000008	2	5 0	3.2766	547	0.000827	27
		546		3			548		28
35	0.3818	545	0.000011	4	5	3.3314	548	0.000855	28
40	0.4363	546	0.000015	4	10	3.3862	547	0.000883	29
45	0.4909	545	0.000019	4	15	3.4409	548	0.000912	29
50	0.5454	546	0.000023	5	20	3.4957	548	0.000941	30
55	0.6000	545	0.000028	5	25	3.5505	548	0.000971	30
1 0	0.6545	546	0.000033	6	30	3.6053	548	0.001001	30
		545		6			548		30
5	0.7091	545	0.000039	6	35	3.6601	548	0.001031	31
10	0.7636	546	0.000045	7	40	3.7149	548	0.001062	31
15	0.8182	545	0.000052	7	45	3.7697	548	0.001094	32
20	0.8727	546	0.000059	7	50	3.8245	548	0.001126	32
25	0.9273	545	0.000066	7	55	3.8793	548	0.001158	32
30	0.9819	546	0.000074	8	6 0	3.9342	549	0.001191	33
		545		9			548		33
35	1.0364	546	0.000083	9	5	3.9890	549	0.001224	34
40	1.0910	545	0.000092	9	10	4.0439	549	0.001258	34
45	1.1456	546	0.000101	10	15	4.0988	549	0.001293	35
50	1.2001	545	0.000111	10	20	4.1536	548	0.001327	34
55	1.2547	546	0.000121	11	25	4.2085	549	0.001362	35
2 0	1.3093	545	0.000132	11	30	4.2634	549	0.001398	36
		546		12			549		36
5	1.3638	546	0.000144	11	35	4.3183	549	0.001434	37
10	1.4184	545	0.000155	12	40	4.3732	549	0.001471	37
15	1.4730	546	0.000167	13	45	4.4281	549	0.001508	37
20	1.5276	545	0.000180	13	50	4.4830	550	0.001545	38
25	1.5822	546	0.000193	14	55	4.5380	549	0.001583	39
30	1.6368	545	0.000207	14	7 0	4.5929	550	0.001622	39
		546		14			550		39
35	1.6914	546	0.000221	14	5	4.6479	549	0.001661	39
40	1.7460	545	0.000235	15	10	4.7028	550	0.001700	40
45	1.8006	546	0.000250	16	15	4.7578	550	0.001740	40
50	1.8552	545	0.000266	15	20	4.8128	550	0.001780	41
55	1.9098	546	0.000281	17	25	4.8678	550	0.001821	41
3 0	1.9644	545	0.000298	16	30	4.9228	550	0.001862	41
		546		18			550		41
5	2.0190	546	0.000314	17	35	4.9778	551	0.001903	42
10	2.0736	547	0.000332	19	40	5.0328	551	0.001945	43
15	2.1283	546	0.000349	18	45	5.0879	551	0.001988	43
20	2.1829	545	0.000368	19	50	5.1429	551	0.002031	43
25	2.2375	546	0.000386	20	55	5.1980	551	0.002074	44
30	2.2922	547	0.000405	20	8 0	5.2531	551	0.002118	44
		546		20			550		45
35	2.3468	547	0.000425	21	5	5.3081	551	0.002163	45
40	2.4015	546	0.000445	21	10	5.3632	551	0.002208	45
45	2.4561	547	0.000465	22	15	5.4183	551	0.002253	46
50	2.5108	546	0.000486	22	20	5.4734	552	0.002299	46
55	2.5654	547	0.000507	23	25	5.5286	551	0.002345	47
4 0	2.6201	547	0.000529	23	30	5.5837	552	0.002392	47
		547		22			551		47
5	2.6748	547	0.000552	24	35	5.6389	552	0.002439	48
10	2.7295	547	0.000574	24	40	5.6940	552	0.002487	48
15	2.7842	547	0.000597	25	45	5.7492	552	0.002535	48
20	2.8389	547	0.000621	25	50	5.8044	552	0.002583	49
25	2.8936	547	0.000645	25	55	5.8596	552	0.002632	50
30	2.9483	547	0.000670	25	9 0	5.9148	552	0.002682	50
		547		25			552		50

A general Table of the Parabola.

31

Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.
0					0				
9	5	5.9700	552	0.002732	50	13	35	8.9744	561
	10	6.0253	553	0.002782	50		40	9.0305	561
	15	6.0805	552	0.002833	51		45	9.0866	561
	20	6.1358	553	0.002884	51		50	9.1428	562
	25	6.1911	553	0.002936	52		55	9.1989	561
	30	6.2464	553	0.002988	52	14	0	9.2551	52
	35	6.3017	553	0.003041	53		5	9.3113	562
	40	6.3570	553	0.003094	53		10	9.3676	563
	45	6.4123	553	0.003148	54		15	9.4238	562
	50	6.4677	554	0.003202	54		20	9.4801	563
	55	6.5230	553	0.003257	55		25	9.5364	563
10	0	6.5784	554	0.003312	55		30	9.5927	563
	5	6.6338	554	0.003367	55		35	9.6490	563
	10	6.6892	554	0.003423	56		40	9.7054	564
	15	6.7446	554	0.003479	56		45	9.7617	563
	20	6.8000	554	0.003536	57		50	9.8181	564
	25	6.8555	555	0.003594	58		55	9.8745	564
	30	6.9109	554	0.003652	58	15	0	9.9310	565
	35	6.9664	555	0.003710	58		5	9.9874	564
	40	7.0219	555	0.003769	59		10	10.0439	565
	45	7.0774	555	0.003828	59		15	10.1004	565
	50	7.1329	555	0.003887	59		20	10.1569	565
	55	7.1885	556	0.003947	60		25	10.2135	566
11	0	7.2440	555	0.004008	61		30	10.2701	566
	5	7.2996	556	0.004069	61		35	10.3267	566
	10	7.3551	555	0.004131	62		40	10.3833	566
	15	7.4107	556	0.004193	62		45	10.4399	566
	20	7.4663	556	0.004255	62		50	10.4966	567
	25	7.5220	557	0.004318	63		55	10.5533	567
	30	7.5776	556	0.004381	63	16	0	10.6100	567
	35	7.6333	557	0.004445	64		5	10.6667	567
	40	7.6890	557	0.004509	64		10	10.7234	567
	45	7.7447	557	0.004574	65		15	10.7802	568
	50	7.8004	557	0.004639	65		20	10.8370	568
	55	7.8561	557	0.004705	66		25	10.8938	568
12	0	7.9118	557	0.004771	66		30	10.9507	569
	5	7.9676	558	0.004838	67		35	11.0076	569
	10	8.0234	558	0.004905	67		40	11.0645	569
	15	8.0792	558	0.004973	68		45	11.1214	569
	20	8.1350	558	0.005041	68		50	11.1783	570
	25	8.1908	558	0.005109	68		55	11.2353	570
	30	8.2467	559	0.005178	69	17	0	11.2923	570
	35	8.3025	558	0.005247	69		5	11.3493	570
	40	8.3584	559	0.005317	70		10	11.4063	570
	45	8.4143	559	0.005388	71		15	11.4634	571
	50	8.4702	559	0.005458	70		20	11.5205	571
	55	8.5262	560	0.005530	72		25	11.5776	571
13	0	8.5822	560	0.005602	72		30	11.6348	572
	5	8.6381	559	0.005674	72		35	11.6919	571
	10	8.6941	560	0.005746	72		40	11.7491	572
	15	8.7501	560	0.005819	73		45	11.8063	572
	20	8.8062	561	0.005893	74		50	11.8636	573
	25	8.8622	560	0.005967	74		55	11.9209	573
	30	8.9183	561	0.006042	75	18	0	11.9782	573
			561		75				573

Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.
18 0	12.0355	573	0.010860	100	22 0	15.1741	589	0.016978	126
5	12.0928	573	0.010961	101	35	15.2331	590	0.017104	126
10	12.1502	574	0.011062	101	40	15.2922	591	0.017231	127
15	12.2076	574	0.011164	102	45	15.3512	590	0.017359	128
20	12.2650	574	0.011266	102	50	15.4103	591	0.017486	127
25	12.3225	575	0.011369	103	55	15.4695	592	0.017615	129
30	12.3800	575	0.011472	103	23 0	15.5286	591	0.017743	128
35	12.4375	575	0.011576	104	5	15.5878	592	0.017873	130
40	12.4951	576	0.011680	104	10	15.6471	593	0.018002	129
45	12.5526	575	0.011784	104	15	15.7063	592	0.018132	130
50	12.6102	576	0.011889	105	20	15.7657	594	0.018263	131
55	12.6679	577	0.011995	106	25	15.8250	593	0.018394	131
19 0	12.7255	576	0.012101	106	30	15.8844	594	0.018526	132
5	12.7832	577	0.012207	106	35	15.9438	594	0.018658	132
10	12.8409	577	0.012314	107	40	16.0032	594	0.018791	133
15	12.8986	577	0.012421	107	45	16.0627	595	0.018924	133
20	12.9564	578	0.012529	108	50	16.1223	596	0.019057	133
25	13.0142	578	0.012637	108	55	16.1818	595	0.019191	134
30	13.0720	578	0.012746	109	24 0	16.2414	596	0.019326	135
35	13.1299	579	0.012855	109	5	16.3011	597	0.019461	135
40	13.1878	579	0.012965	110	10	16.3607	596	0.019596	135
45	13.2457	579	0.013075	110	15	16.4204	597	0.019732	136
50	13.3036	579	0.013186	111	20	16.4802	598	0.019869	137
55	13.3616	580	0.013297	111	25	16.5400	598	0.020005	136
20 0	13.4196	580	0.013409	112	30	16.5998	598	0.020143	138
5	13.4776	580	0.013521	112	35	16.6597	599	0.020281	138
10	13.5357	581	0.013633	112	40	16.7196	599	0.020419	138
15	13.5938	581	0.013746	113	45	16.7795	599	0.020558	139
20	13.6519	581	0.013860	114	50	16.8395	600	0.020697	139
25	13.7100	581	0.013974	114	55	16.8995	600	0.020837	140
30	13.7682	582	0.014088	114	25 0	16.9596	601	0.020977	140
35	13.8264	582	0.014203	115	5	17.0196	600	0.021118	141
40	13.8847	583	0.014319	116	10	17.0798	602	0.021259	141
45	13.9430	583	0.014435	116	15	17.1400	602	0.021401	142
50	14.0013	583	0.014551	116	20	17.2002	602	0.021543	142
55	14.0596	583	0.014668	117	25	17.2604	602	0.021686	143
21 0	14.1180	584	0.014785	117	30	17.3207	603	0.021829	143
5	14.1764	584	0.014903	118	35	17.3810	603	0.021973	144
10	14.2348	584	0.015021	118	40	17.4414	604	0.022117	144
15	14.2933	585	0.015140	119	45	17.5018	604	0.022261	144
20	14.3518	585	0.015259	119	50	17.5623	605	0.022407	146
25	14.4103	585	0.015379	120	55	17.6228	605	0.022552	145
30	14.4688	585	0.015499	120	26 0	17.6833	605	0.022698	146
35	14.5274	586	0.015620	121	5	17.7439	606	0.022845	147
40	14.5861	587	0.015741	121	10	17.8045	606	0.022992	147
45	14.6447	586	0.015862	121	15	17.8651	606	0.023139	147
50	14.7034	587	0.015984	122	20	17.9258	607	0.023287	148
55	14.7621	587	0.016107	123	25	17.9865	607	0.023436	149
22 0	14.8209	588	0.016230	123	30	18.0473	608	0.023585	149
5	14.8797	588	0.016353	123	35	18.1081	608	0.023734	149
10	14.9385	588	0.016477	124	40	18.1690	609	0.023884	150
15	14.9974	589	0.016602	125	45	18.2299	609	0.024035	151
20	15.0563	589	0.016727	125	50	18.2909	610	0.024186	151
25	15.1152	589	0.016852	125	55	18.3519	610	0.024337	151
30		589		126	27 0		610		152

Angle.	Mean Mot.	Diff.	Log. Diff.	Diff.	Angle.	Mean Mot.	Diff.	Log. Diff.	Diff.		
27	5	18.4129	610	0.024489	152	31	35	21.7766	636	0.033417	178
	10	18.4740	611	0.024641	152		40	21.8402	636	0.033596	179
	15	18.5351	611	0.024794	153		45	21.9039	637	0.033776	180
	20	18.5962	611	0.024947	153		50	21.9677	638	0.033955	179
	25	18.6574	612	0.025101	154		55	22.0315	638	0.034136	181
	30	18.7187	613	0.025256	155	32	0	22.0953	638	0.034317	181
	35	18.7800	613	0.025410	154		5	22.1592	639	0.034498	181
	40	18.8413	614	0.025566	156		10	22.2232	640	0.034680	182
	45	18.9027	614	0.025722	156		15	22.2872	640	0.034862	182
	50	18.9641	615	0.025878	156		20	22.3513	641	0.035045	183
	55	19.0256	615	0.026035	157		25	22.4154	641	0.035229	184
28	0	19.0871	615	0.026192	157		30	22.4796	642	0.035412	183
	5	19.1486	616	0.026350	158		35	22.5438	642	0.035597	185
	10	19.2102	616	0.026508	158		40	22.6081	643	0.035782	185
	15	19.2719	617	0.026666	158		45	22.6724	643	0.035967	185
	20	19.3336	617	0.026826	160		50	22.7368	644	0.036153	186
	25	19.3953	617	0.026985	159		55	22.8013	645	0.036339	186
	30	19.4571	618	0.027145	160	33	0	22.8658	645	0.036526	187
	35	19.5189	619	0.027306	161		5	22.9303	645	0.036713	187
	40	19.5808	619	0.027467	161		10	22.9949	646	0.036901	188
	45	19.6427	620	0.027629	162		15	23.0596	647	0.037090	189
	50	19.7047	620	0.027791	162		20	23.1243	647	0.037278	188
	55	19.7667	621	0.027954	163		25	23.1891	648	0.037468	190
29	0	19.8288	621	0.028117	163		30	23.2540	649	0.037658	190
	5	19.8909	621	0.028280	163		35	23.3189	649	0.037848	190
	10	19.9530	622	0.028444	164		40	23.3838	649	0.038039	191
	15	20.0152	622	0.028609	165		45	23.4488	650	0.038230	191
	20	20.0774	623	0.028774	165		50	23.5139	651	0.038422	192
	25	20.1397	624	0.028940	166		55	23.5790	651	0.038615	193
	30	20.2021	624	0.029106	166	34	0	23.6442	652	0.038807	192
	35	20.2645	624	0.029272	166		5	23.7095	653	0.039001	194
	40	20.3269	625	0.029439	167		10	23.7748	653	0.039195	194
	45	20.3894	625	0.029607	168		15	23.8401	653	0.039389	194
	50	20.4519	626	0.029775	168		20	23.9055	654	0.039584	195
	55	20.5145	626	0.029943	168		25	23.9710	655	0.039779	195
30	0	20.5771	627	0.030112	169		30	24.0366	656	0.039975	196
	5	20.6398	627	0.030282	170		35	24.1022	656	0.040172	197
	10	20.7025	628	0.030452	170		40	24.1678	656	0.040368	196
	15	20.7653	628	0.030622	170		45	24.2335	657	0.040566	198
	20	20.8281	629	0.030793	171		50	24.2993	658	0.040764	198
	25	20.8910	629	0.030965	172		55	24.3651	658	0.040962	198
	30	20.9539	630	0.031137	172	35	0	24.4310	659	0.041161	199
	35	21.0169	630	0.031309	172		5	24.4970	660	0.041360	199
	40	21.0799	631	0.031482	173		10	24.5630	660	0.041560	200
	45	21.1430	631	0.031656	174		15	24.6291	661	0.041761	201
	50	21.2061	632	0.031830	174		20	24.6952	661	0.041962	201
	55	21.2693	633	0.032004	174		25	24.7614	662	0.042163	201
31	0	21.3326	633	0.032179	175		30	24.8277	663	0.042365	202
	5	21.3958	634	0.032354	175		35	24.8940	663	0.042567	202
	10	21.4592	634	0.032530	176		40	24.9604	664	0.042770	203
	15	21.5226	634	0.032707	177		45	25.0268	664	0.042974	204
	20	21.5860	635	0.032884	177		50	25.0933	665	0.043178	204
	25	21.6495	635	0.033061	177		55	25.1599	666	0.043382	205
	30	21.7130	636	0.033239	178	36	0	25.2265	666	0.043587	205
					178				667		206

Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Mean Mot.	Diff.	Log. Dist.	Diff.
36	5	25.2932	667	0.043793	40	35	28.9946	0.055650	233
	10	25.3600	668	0.043999		40	29.0652	0.055884	234
	15	25.4268	669	0.044205		45	29.1358	0.056119	235
	20	25.4937	670	0.044412		50	29.2064	0.056353	234
	25	25.5607	670	0.044620		55	29.2772	0.056589	236
	30	25.6277	671	0.044828	41	0	29.3480	0.056825	236
	35	25.6948	671	0.045037		5	29.4189	0.057061	236
	40	25.7619	672	0.045246		10	29.4899	0.057298	237
	45	25.8291	673	0.045455		15	29.5609	0.057536	238
	50	25.8964	673	0.045665		20	29.6320	0.057774	238
	55	25.9637	674	0.045876		25	29.7032	0.058012	238
37	0	26.0311	675	0.046087		30	29.7745	0.058251	239
	5	26.0986	675	0.046298		35	29.8459	0.058491	240
	10	26.1661	676	0.046511		40	29.9173	0.058731	240
	15	26.2337	677	0.046723		45	29.9888	0.058971	240
	20	26.3014	677	0.046936		50	30.0604	0.059213	242
	25	26.3691	678	0.047150		55	30.1321	0.059454	241
	30	26.4369	679	0.047364	42	0	30.2039	0.059697	243
	35	26.5048	679	0.047579		5	30.2757	0.059939	242
	40	26.5727	680	0.047794		10	30.3476	0.060183	244
	45	26.6407	681	0.048010		15	30.4196	0.060426	243
	50	26.7088	682	0.048226		20	30.4917	0.060671	245
	55	26.7770	682	0.048443		25	30.5639	0.060915	244
38	0	26.8452	682	0.048660		30	30.6361	0.061161	246
	5	26.9134	684	0.048878		35	30.7085	0.061407	246
	10	26.9818	684	0.049096		40	30.7809	0.061653	246
	15	27.0502	685	0.049315		45	30.8534	0.061900	247
	20	27.1187	685	0.049534		50	30.9259	0.062148	248
	25	27.1872	687	0.049754		55	30.9986	0.062396	248
	30	27.2559	687	0.049974	43	0	31.0713	0.062644	248
	35	27.3246	687	0.050195		5	31.1441	0.062893	249
	40	27.3933	688	0.050416		10	31.2170	0.063143	250
	45	27.4621	689	0.050638		15	31.2900	0.063393	250
	50	27.5310	690	0.050861		20	31.3631	0.063644	251
	55	27.6000	691	0.051083		25	31.4363	0.063895	251
39	0	27.6691	691	0.051307		30	31.5095	0.064147	252
	5	27.7382	692	0.051531		35	31.5829	0.064399	252
	10	27.8074	692	0.051755		40	31.6563	0.064652	253
	15	27.8766	693	0.051980		45	31.7298	0.064905	253
	20	27.9459	694	0.052206		50	31.8033	0.065159	254
	25	28.0153	695	0.052432		55	31.8770	0.065413	254
	30	28.0848	696	0.052658	44	0	31.9508	0.065668	255
	35	28.1544	696	0.052885		5	32.0246	0.065924	256
	40	28.2240	697	0.053113		10	32.0986	0.066180	256
	45	28.2937	697	0.053341		15	32.1726	0.066436	256
	50	28.3634	699	0.053570		20	32.2467	0.066693	257
	55	28.4333	699	0.053799		25	32.3209	0.066951	258
40	0	28.5032	700	0.054028		30	32.3952	0.067209	258
	5	28.5732	700	0.054259		35	32.4695	0.067468	259
	10	28.6432	702	0.054489		40	32.5440	0.067727	259
	15	28.7134	702	0.054720		45	32.6185	0.067987	260
	20	28.7836	703	0.054952		50	32.6932	0.068247	260
	25	28.8539	703	0.055184		55	32.7679	0.068508	261
	30	28.9242	704	0.055417	45	0	32.8427	0.068769	261
									262

N. B. Here the second column begins to be the Logarithm of the Mean Motion.

Angle.	Log.	Diff.	Log. Diff.	Diff.	Angle.	Log.	Diff.	Log. Diff.	Diff.			
	Mean Mot.					Mean Mot.						
45	5	1.517428	-989	0.069031	-262	49	35	1.569434	-940	0.083983	-292	
	10	1.518417	989	0.069294	263		40	1.570373	939	0.084275	292	
	15	1.519404	987	0.069557	263		45	1.571312	939	0.084567	292	
	20	1.520390	986	0.069820	263		50	1.572250	938	0.084861	294	
	25	1.521376	986	0.070084	264		55	1.573187	937	0.085154	293	
	30	1.522360	984	0.070349	265		50	0	1.574123	936	0.085449	295
	35	1.523343	-983	0.070614	-265		5	1.575059	-936	0.085743	-294	
	40	1.524325	982	0.070880	266		10	1.575994	935	0.086039	296	
	45	1.525306	981	0.071146	266		15	1.576928	934	0.086335	296	
	50	1.526286	980	0.071413	267		20	1.577862	934	0.086631	296	
	55	1.527265	979	0.071680	267		25	1.578794	932	0.086928	297	
46	0	1.528243	978	0.071948	268		30	1.579726	932	0.087226	298	
	5	1.529221	-978	0.072216	-268		35	1.580658	-932	0.087524	-298	
	10	1.530197	976	0.072485	269		40	1.581588	930	0.087823	299	
	15	1.531172	975	0.072755	270		45	1.582518	930	0.088122	299	
	20	1.532146	974	0.073025	270		50	1.583447	929	0.088422	300	
	25	1.533119	973	0.073295	270		55	1.584375	928	0.088723	301	
	30	1.534091	972	0.073566	271		51	0	1.585303	928	0.089024	301
	35	1.535063	-972	0.073838	-272		5	1.586230	-927	0.089325	-301	
	40	1.536033	970	0.074110	272		10	1.587156	926	0.089627	302	
	45	1.537002	969	0.074383	273		15	1.588082	926	0.089930	303	
	50	1.537971	969	0.074656	273		20	1.589007	925	0.090233	303	
	55	1.538938	967	0.074930	274		25	1.589931	924	0.090537	304	
47	0	1.539905	967	0.075204	274		30	1.590855	924	0.090841	304	
	5	1.540870	-965	0.075479	-275		35	1.591778	-923	0.091146	-305	
	10	1.541835	965	0.075755	276		40	1.592700	922	0.091452	306	
	15	1.542799	964	0.076031	276		45	1.593622	922	0.091758	306	
	20	1.543762	963	0.076307	276		50	1.594543	921	0.092065	307	
	25	1.544724	962	0.076585	278		55	1.595463	920	0.092372	307	
	30	1.545685	961	0.076862	277		52	0	1.596383	920	0.092680	308
	35	1.546645	-960	0.077140	-278		5	1.597302	-919	0.092988	-308	
	40	1.547604	959	0.077419	279		10	1.598220	918	0.093297	309	
	45	1.548563	959	0.077698	279		15	1.599138	918	0.093606	309	
	50	1.549520	957	0.077978	280		20	1.600055	917	0.093916	310	
	55	1.550477	957	0.078259	281		25	1.600972	917	0.094227	311	
48	0	1.551433	956	0.078540	281		30	1.601888	916	0.094538	311	
	5	1.552388	-955	0.078821	-281		35	1.602803	-915	0.094850	-312	
	10	1.553342	954	0.079103	282		40	1.603718	915	0.095162	312	
	15	1.554295	953	0.079386	283		45	1.604632	914	0.095475	313	
	20	1.555247	952	0.079669	283		50	1.605545	913	0.095789	314	
	25	1.556199	952	0.079953	284		55	1.606458	913	0.096103	314	
	30	1.557149	950	0.080237	284		53	0	1.607370	912	0.096418	315
	35	1.558099	-950	0.080522	-285		5	1.608282	-912	0.096733	-315	
	40	1.559048	949	0.080807	285		10	1.609193	911	0.097049	316	
	45	1.559996	948	0.081093	286		15	1.610104	911	0.097365	316	
	50	1.560944	948	0.081380	287		20	1.611014	910	0.097682	317	
	55	1.561890	946	0.081667	287		25	1.611923	909	0.098000	318	
49	0	1.562836	946	0.081954	287		30	1.612832	909	0.098318	318	
	5	1.563781	-945	0.082242	-288		35	1.613740	-908	0.098636	-318	
	10	1.564725	944	0.082531	289		40	1.614647	907	0.098955	319	
	15	1.565668	943	0.082820	289		45	1.615554	907	0.099275	320	
	20	1.566611	943	0.083110	290		50	1.616461	907	0.099596	321	
	25	1.567553	942	0.083400	290		55	1.617367	906	0.099917	321	
	30	1.568494	941	0.083691	291		54	0	1.618272	905	0.100238	321
			-940		-292				-905		-322	

Angle.	Log.	Diff.	Log. Diff.	Diff.	Angle.	Log.	Diff.	Log. Diff.	Diff.		
Mean Mot.					Mean Mot.						
0					0						
54	5	1.619177	905	0.100560	322	58	35	1.667334	881	0.118827	354
	10	1.620081	904	0.100883	323		40	1.668214	880	0.119182	355
	15	1.620985	904	0.101206	323		45	1.669095	881	0.119537	355
	20	1.621888	903	0.101530	324		50	1.669975	880	0.119893	356
	25	1.622791	903	0.101855	325		55	1.670854	879	0.120249	356
	30	1.623694	903	0.102180	325	59	0	1.671733	879	0.120606	357
			901	0.102505	325		5	1.672612	879	0.120964	358
	35	1.624595	901	0.102832	327		10	1.673490	878	0.121322	358
	40	1.625496	901	0.103158	326		15	1.674369	879	0.121681	359
	45	1.626397	900	0.103486	328		20	1.675247	878	0.122041	360
	50	1.627297	900	0.103814	328		25	1.676124	877	0.122401	360
	55	1.628197	899	0.104142	328		30	1.677001	877	0.122762	361
55	0	1.629096	899	0.104471	329		35	1.677878	877	0.123123	361
	5	1.629995	898	0.104801	330		40	1.678755	877	0.123485	362
	10	1.630893	897	0.105131	330		45	1.679631	876	0.123847	362
	15	1.631790	898	0.105462	331		50	1.680507	876	0.124211	364
	20	1.632688	896	0.105794	332		55	1.681383	876	0.124574	363
	25	1.633584	896	0.106126	332	60	0	1.682258	875	0.124939	365
	3	1.63448	896	0.106458	332		5	1.683133	875	0.125304	365
	35	1.635376	895	0.106791	333		10	1.684008	875	0.125669	365
	40	1.636271	895	0.107125	334		15	1.684883	875	0.126036	367
	45	1.637166	894	0.107460	335		20	1.685757	874	0.126402	366
	50	1.638060	894	0.107795	335		25	1.686631	874	0.126770	368
	55	1.638954	894	0.108130	335		30	1.687504	873	0.127138	368
56	0	1.639848	892	0.108466	336		35	1.688378	874	0.127507	369
	5	1.640740	893	0.108803	337		40	1.689251	873	0.127876	369
	10	1.641633	892	0.109140	337		45	1.690124	873	0.128246	370
	15	1.642525	892	0.109478	338		50	1.690997	873	0.128616	370
	20	1.643417	891	0.109817	339		55	1.691869	872	0.128987	371
	25	1.644308	891	0.110156	339	61	0	1.692741	872	0.129359	372
	3	1.645199	890	0.110496	340		5	1.693613	872	0.129732	373
	35	1.646089	889	0.110836	340		10	1.694484	871	0.130105	373
	40	1.646978	890	0.111177	341		15	1.695355	871	0.130478	373
	45	1.647868	889	0.111518	341		20	1.696226	871	0.130852	374
	50	1.648757	888	0.111860	342		25	1.697097	871	0.131227	375
	55	1.649645	889	0.112203	343		30	1.697968	871	0.131603	376
57	0	1.650534	887	0.112546	343		35	1.698838	870	0.131979	376
	5	1.651421	888	0.112890	344		40	1.699708	870	0.132356	377
	10	1.652309	887	0.113235	345		45	1.700578	870	0.132733	377
	15	1.653196	886	0.113580	345		50	1.701448	870	0.133111	378
	20	1.654082	886	0.113925	345		55	1.702317	869	0.133490	379
	25	1.654968	886	0.114271	346	62	0	1.703186	869	0.133869	379
	30	1.655854	885	0.114618	347		5	1.704055	869	0.134249	380
	35	1.656739	885	0.114966	348		10	1.704924	869	0.134629	380
	40	1.657624	885	0.115314	348		15	1.705793	868	0.135010	381
	45	1.658509	884	0.115662	348		20	1.706661	868	0.135392	382
	50	1.659393	884	0.116012	350		25	1.707529	868	0.135774	382
	55	1.660277	883	0.116362	350		30	1.708397	868	0.136157	383
58	0	1.661160	883	0.116712	350		35	1.709265	868	0.136541	384
	5	1.662043	883	0.117063	351		40	1.710133	867	0.136925	384
	10	1.662926	882	0.117415	352		45	1.711000	867	0.137310	385
	15	1.663808	882	0.117767	352		50	1.711867	867	0.137696	386
	20	1.664690	882	0.118120	353		55	1.712734	867	0.138082	386
	25	1.665572	881	0.118473	353	63	0	1.713601	866	0.138468	386
	30	1.666453	881		354						388

Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.		
	Mean Mot.					Mean Mot.					
63	5	1.714407	-866	0.138856	-388	67	35	1.761067	-861	0.160730	-423
	10	1.715334	866	0.139244	388		40	1.761928	860	0.161153	423
	15	1.716200	866	0.139633	389		45	1.762788	861	0.161576	423
	20	1.717066	866	0.140022	389		50	1.763649	861	0.162001	425
	25	1.717932	865	0.140412	390		55	1.764510	861	0.162426	425
	30	1.718797	-866	0.140802	390	68	0	1.765371	-860	0.162852	426
	35	1.719663	865	0.141193	-391		5	1.766231	861	0.163278	-426
	40	1.720528	865	0.141585	392		10	1.767092	861	0.163705	427
	45	1.721393	865	0.141978	393		15	1.767953	860	0.164133	428
	50	1.722258	865	0.142371	393		20	1.768813	861	0.164561	428
	55	1.723123	865	0.142765	394		25	1.769674	861	0.164990	429
64	0	1.723988	-865	0.143159	394		30	1.770535	-860	0.165420	430
	5	1.724853	864	0.143554	-395		35	1.771395	861	0.165850	-430
	10	1.725717	864	0.143950	396		40	1.772256	860	0.166281	431
	15	1.726681	865	0.144346	396		45	1.773116	861	0.166713	432
	20	1.727446	864	0.144743	397		50	1.773977	861	0.167146	433
	25	1.728310	863	0.145141	398		55	1.774838	860	0.167579	433
	30	1.729173	-864	0.145539	398	69	0	1.775698	-861	0.168013	434
	35	1.730037	864	0.145938	-399		5	1.776559	861	0.168447	-434
	40	1.730901	863	0.146337	399		10	1.777420	861	0.168882	435
	45	1.731764	864	0.146737	400		15	1.778281	860	0.169318	436
	50	1.732628	863	0.147138	401		20	1.779141	861	0.169754	436
	55	1.733491	863	0.147540	402		25	1.780002	861	0.170192	438
65	0	1.734354	-863	0.147942	402		30	1.780863	-861	0.170630	438
	5	1.735217	863	0.148344	-402		35	1.781724	860	0.171068	-438
	10	1.736080	863	0.148748	404		40	1.782584	861	0.171507	439
	15	1.736943	862	0.149152	404		45	1.783445	861	0.171947	440
	20	1.737805	863	0.149556	404		50	1.784306	861	0.172388	441
	25	1.738668	862	0.149962	406		55	1.785167	861	0.172829	441
	30	1.739530	-863	0.150368	406	70	0	1.786028	-861	0.173271	442
	35	1.740393	862	0.150774	-406		5	1.786889	862	0.173714	-443
	40	1.741255	862	0.151182	408		10	1.787751	861	0.174157	443
	45	1.742117	862	0.151590	408		15	1.788612	861	0.174601	444
	50	1.742979	862	0.151998	408		20	1.789473	861	0.175046	445
	55	1.743841	862	0.152407	409		25	1.790334	861	0.175491	445
66	0	1.744703	-862	0.152817	410		30	1.791195	-862	0.175937	446
	5	1.745565	862	0.153228	-411		35	1.792057	861	0.176384	-447
	10	1.746427	861	0.153639	411		40	1.792918	862	0.176831	447
	15	1.747288	862	0.154051	412		45	1.793780	862	0.177279	448
	20	1.748150	862	0.154463	412		50	1.794642	861	0.177728	449
	25	1.749012	861	0.154876	413		55	1.795503	862	0.178178	450
	30	1.749873	-861	0.155290	414	71	0	1.796365	-862	0.178628	450
	35	1.750734	862	0.155705	-415		5	1.797227	862	0.179079	-451
	40	1.751596	861	0.156120	415		10	1.798089	862	0.179530	451
	45	1.752457	861	0.156536	416		15	1.798951	862	0.179983	453
	50	1.753318	861	0.156952	416		20	1.799813	862	0.180436	453
	55	1.754179	861	0.157369	417		25	1.800675	862	0.180889	453
67	0	1.755040	-862	0.157787	418		30	1.801537	-863	0.181344	455
	5	1.755902	861	0.158205	-418		35	1.802400	862	0.181799	-455
	10	1.756763	860	0.158624	419		40	1.803262	862	0.182255	456
	15	1.757623	861	0.159044	420		45	1.804124	863	0.182711	456
	20	1.758484	861	0.159465	421		50	1.804987	863	0.183168	457
	25	1.759345	861	0.159886	421		55	1.805850	863	0.183626	458
	30	1.760206	-861	0.160307	421	72	0	1.806713	-863	0.184085	459
					423						459

Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.
72° 5'	1.807576	-863	0.184544	-459	76° 35'	1.854410	-873	0.210408	-498
10	1.808439	863	0.185004	460	40	1.855283	873	0.210907	499
15	1.809302	863	0.185465	461	45	1.856156	873	0.211407	500
20	1.810165	863	0.185926	461	50	1.857029	873	0.211908	501
25	1.811029	864	0.186388	462	55	1.857903	874	0.212409	501
30	1.811892	863	0.186851	463	77° 0'	1.858777	874	0.212911	502
		-864		-463			-874		-503
35	1.812756	864	0.187314	465	5	1.859651	875	0.213414	504
40	1.813620	864	0.187779	465	10	1.860526	875	0.213918	504
45	1.814484	864	0.188244	465	15	1.861400	874	0.214422	504
50	1.815348	864	0.188709	465	20	1.862275	875	0.214927	505
55	1.816212	864	0.189176	467	25	1.863151	876	0.215433	506
73° 0'	1.817077	865	0.189643	467	30	1.864026	875	0.215939	506
		-864		-467			-876		-508
5	1.817941	864	0.190110	469	35	1.864902	876	0.216447	508
10	1.818805	865	0.190579	469	40	1.865778	876	0.216955	508
15	1.819670	865	0.191048	469	45	1.866655	877	0.217464	509
20	1.820535	865	0.191518	470	50	1.867532	877	0.217973	509
25	1.821400	865	0.191988	470	55	1.868408	876	0.218484	511
30	1.822266	866	0.192460	472	78° 0'	1.869286	878	0.218995	511
		-865		-472			-877		-512
35	1.823131	866	0.192932	473	5	1.870163	878	0.219507	512
40	1.823997	865	0.193405	473	10	1.871041	878	0.220019	512
45	1.824862	866	0.193878	474	15	1.871919	879	0.220533	514
50	1.825728	866	0.194352	474	20	1.872798	879	0.221047	514
55	1.826594	866	0.194827	475	25	1.873677	879	0.221562	515
74° 0'	1.827460	866	0.195303	476	30	1.874556	879	0.222078	516
		-867		-476			-879		-516
5	1.828327	866	0.195779	477	35	1.875435	880	0.222594	517
10	1.829193	867	0.196256	478	40	1.876315	880	0.223111	518
15	1.830060	867	0.196734	479	45	1.877195	880	0.223629	519
20	1.830927	867	0.197213	479	50	1.878075	881	0.224148	520
25	1.831794	867	0.197692	480	55	1.878956	881	0.224668	520
30	1.832661	867	0.198172	480	79° 0'	1.879837	881	0.225188	521
		-868		-480			-881		-521
35	1.833529	867	0.198652	482	5	1.880718	882	0.225709	522
40	1.834396	868	0.199134	482	10	1.881600	882	0.226231	522
45	1.835264	868	0.199616	483	15	1.882482	882	0.226753	522
50	1.836132	868	0.200099	483	20	1.883364	882	0.227277	524
55	1.837000	868	0.200582	483	25	1.884247	883	0.227801	524
75° 0'	1.837869	869	0.201067	485	30	1.885130	883	0.228326	525
		-868		-485			-883		-526
5	1.838737	869	0.201552	486	35	1.886013	884	0.228852	526
10	1.839606	869	0.202038	486	40	1.886897	884	0.229378	528
15	1.840475	869	0.202524	487	45	1.887781	884	0.229906	528
20	1.841344	870	0.203011	488	50	1.888665	885	0.230434	528
25	1.842214	869	0.203499	489	55	1.889550	885	0.230962	530
30	1.843083	870	0.203988	489	80° 0'	1.890435	885	0.231492	530
		-870		-489			-885		-530
35	1.843953	870	0.204477	491	5	1.891320	886	0.232022	532
40	1.844823	871	0.204968	491	10	1.892206	886	0.232554	532
45	1.845694	870	0.205459	491	15	1.893092	887	0.233086	532
50	1.846564	871	0.205950	493	20	1.893979	887	0.233618	534
55	1.847435	871	0.206443	493	25	1.894866	887	0.234152	534
76° 0'	1.848306	871	0.206936	494	30	1.895753	887	0.234686	535
		-871		-494			-887		-535
5	1.849177	872	0.207430	494	35	1.896640	888	0.235221	536
10	1.850049	871	0.207924	496	40	1.897528	889	0.235757	537
15	1.850920	872	0.208420	496	45	1.898417	888	0.236294	538
20	1.851792	872	0.208916	496	50	1.899305	889	0.236832	538
25	1.852664	873	0.209412	498	55	1.900194	890	0.237370	539
30	1.853537	873	0.209910	498	81° 0'	1.901084	890	0.237909	540
		-873		-498			-890		-540

A general Table of the Parabola.

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Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.		
o	Mean Mot.				o	Mean Mot.					
81	5	1.901974	-890	0.238449	-540	85	35	1.950678	-915	0.268811	-585
	10	1.902864	890	0.238990	541		40	1.951593	915	0.269396	585
	15	1.903755	891	0.239531	541		45	1.952509	916	0.269982	586
	20	1.904646	891	0.240073	542		50	1.953426	917	0.270569	587
	25	1.905537	891	0.240616	543		55	1.954343	917	0.271156	587
	30	1.906429	892	0.241160	544	86	0	1.955260	917	0.271745	589
	35	1.907321	-892	0.241705	-545		5	1.956178	-918	0.272335	-590
	40	1.908214	893	0.242250	545		10	1.957097	919	0.272925	590
	45	1.909107	893	0.242797	547		15	1.958016	919	0.273516	591
	50	1.910001	894	0.243344	547		20	1.958936	920	0.274108	592
	55	1.910895	894	0.243892	548		25	1.959856	920	0.274701	593
82	0	1.911789	894	0.244440	548		30	1.960777	921	0.275295	594
	5	1.912684	-895	0.244990	-550		35	1.961698	-921	0.275889	-594
	10	1.913579	895	0.245540	550		40	1.962620	922	0.276485	596
	15	1.914475	896	0.246091	551		45	1.963543	923	0.277081	596
	20	1.915371	896	0.246643	552		50	1.964466	923	0.277678	597
	25	1.916267	896	0.247196	553		55	1.965390	924	0.278277	599
	30	1.917164	897	0.247749	553	87	0	1.966314	924	0.278876	599
	35	1.918061	-897	0.248304	-555		5	1.967239	-925	0.279475	-599
	40	1.918959	898	0.248859	555		10	1.968164	925	0.280076	601
	45	1.919857	898	0.249415	556		15	1.969090	926	0.280678	602
	50	1.920756	899	0.249972	557		20	1.970017	927	0.281280	602
	55	1.921655	899	0.250529	557		25	1.970944	927	0.281884	604
83	0	1.922555	900	0.251088	559		30	1.971872	928	0.282488	604
	5	1.923455	-900	0.251647	-559		35	1.972801	-929	0.283093	-605
	10	1.924355	900	0.252207	560		40	1.973730	929	0.283699	606
	15	1.925256	901	0.252768	561		45	1.974659	929	0.284306	607
	20	1.926157	901	0.253330	562		50	1.975589	930	0.284914	608
	25	1.927059	902	0.253892	562		55	1.976520	931	0.285522	608
	30	1.927962	903	0.254456	564	88	0	1.977452	932	0.286132	610
	35	1.928865	-903	0.255020	-564		5	1.978384	-932	0.286742	-610
	40	1.929768	903	0.255585	565		10	1.979317	933	0.287354	612
	45	1.930671	903	0.256151	566		15	1.980250	933	0.287966	612
	50	1.931575	904	0.256717	566		20	1.981184	934	0.288579	613
	55	1.932480	905	0.257285	568		25	1.982119	935	0.289193	614
84	0	1.933385	905	0.257853	568		30	1.983054	935	0.289808	615
	5	1.934291	-906	0.258422	-569		35	1.983990	-936	0.290424	-616
	10	1.935197	906	0.258992	570		40	1.984926	936	0.291040	616
	15	1.936104	907	0.259563	571		45	1.985864	938	0.291658	618
	20	1.937011	907	0.260135	572		50	1.986801	937	0.292276	618
	25	1.937918	907	0.260707	572		55	1.987740	939	0.292896	620
	30	1.938826	908	0.261281	574	89	0	1.988679	939	0.293516	620
	35	1.939735	-909	0.261855	-574		5	1.989619	-940	0.294137	-621
	40	1.940644	909	0.262430	575		10	1.990559	940	0.294759	622
	45	1.941554	910	0.263006	576		15	1.991500	941	0.295382	623
	50	1.942464	910	0.263582	576		20	1.992442	942	0.296006	624
	55	1.943374	910	0.264160	578		25	1.993384	942	0.296631	625
85	0	1.944285	911	0.264738	578		30	1.994327	943	0.297257	626
	5	1.945197	-912	0.265317	-579		35	1.995271	-944	0.297883	-626
	10	1.946109	912	0.265897	580		40	1.996216	945	0.298511	628
	15	1.947022	913	0.266478	581		45	1.997161	945	0.299139	628
	20	1.947935	913	0.267060	582		50	1.998107	946	0.299769	630
	25	1.948849	914	0.267643	583		55	1.999053	946	0.300399	630
	30	1.949763	914	0.268226	583	90	0	2.000000	947	0.301030	631
			-915		-585				-948		-632

A general Table of the Parabola.

Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.		
	Mean Mot.					Mean Mot.					
90	5	2.000948	-948	0.301662	-632	94	35	2.053239	-989	0.337199	-684
	10	2.001897	949	0.302295	633		40	2.054230	991	0.337884	685
	15	2.002846	949	0.302929	634		45	2.055221	991	0.338570	686
	20	2.003796	950	0.303564	635		50	2.056213	992	0.339257	687
	25	2.004746	950	0.304200	636		55	2.057206	993	0.339944	687
	30	2.005697	951	0.304837	637	95	0	2.058200	994	0.340633	689
	35	2.006649	-952	0.305474	-637		5	2.059195	-995	0.341323	-690
	40	2.007602	953	0.306113	639		10	2.060191	996	0.342014	691
	45	2.008556	954	0.306752	639		15	2.061188	997	0.342706	692
	50	2.009510	954	0.307393	641		20	2.062185	997	0.343399	693
	55	2.010465	955	0.308034	641		25	2.063184	999	0.344093	694
91	0	2.011420	955	0.308676	642		30	2.064183	999	0.344787	694
	5	2.012377	-957	0.309320	-644		35	2.065183	-1000	0.345483	-696
	10	2.013334	957	0.309964	644		40	2.066184	1001	0.346180	697
	15	2.014292	958	0.310609	645		45	2.067186	1002	0.346878	698
	20	2.015250	958	0.311255	646		50	2.068189	1003	0.347577	699
	25	2.016209	959	0.311902	647		55	2.069193	1004	0.348277	700
	30	2.017169	960	0.312550	648	96	0	2.070198	1005	0.348978	701
	35	2.018130	-961	0.313199	-649		5	2.071204	-1006	0.349680	-702
	40	2.019091	961	0.313849	650		10	2.072211	1007	0.350383	703
	45	2.020054	963	0.314499	650		15	2.073218	1007	0.351087	704
	50	2.021017	963	0.315151	652		20	2.074226	1008	0.351793	706
	55	2.021981	964	0.315804	653		25	2.075236	1010	0.352499	706
92	0	2.022945	964	0.316457	653		30	2.076246	1010	0.353206	707
	5	2.023910	-965	0.317112	-655		35	2.077257	-1011	0.353914	-708
	10	2.024876	966	0.317768	656		40	2.078270	1013	0.354623	709
	15	2.025843	967	0.318424	656		45	2.079283	1013	0.355334	711
	20	2.026811	968	0.319081	657		50	2.080297	1014	0.356045	711
	25	2.027779	968	0.319740	659		55	2.081312	1015	0.356757	712
	30	2.028748	969	0.320399	659	97	0	2.082328	1016	0.357471	714
	35	2.029718	-970	0.321060	-661		5	2.083345	-1017	0.358185	-714
	40	2.030689	971	0.321721	661		10	2.084363	1018	0.358890	716
	45	2.031660	971	0.322383	662		15	2.085382	1019	0.359617	716
	50	2.032633	973	0.323046	663		20	2.086402	1020	0.360335	718
	55	2.033606	973	0.323710	664		25	2.087423	1021	0.361054	719
93	0	2.034580	974	0.324376	666		30	2.088445	1022	0.361773	719
	5	2.035554	-974	0.325042	-666		35	2.089468	-1023	0.362494	-721
	10	2.036530	976	0.325709	667		40	2.090492	1024	0.363216	722
	15	2.037506	976	0.326377	668		45	2.091517	1025	0.363939	723
	20	2.038483	977	0.327046	669		50	2.092542	1025	0.364663	724
	25	2.039461	978	0.327716	670		55	2.093569	1027	0.365388	725
	30	2.040440	979	0.328387	671	98	0	2.094597	1028	0.366114	726
	35	2.041419	-979	0.329059	-672		5	2.095626	-1029	0.366841	-727
	40	2.042400	981	0.329732	673		10	2.096656	1030	0.367570	729
	45	2.043381	981	0.330406	674		15	2.097687	1031	0.368299	729
	50	2.044363	982	0.331081	675		20	2.098719	1032	0.369029	730
	55	2.045346	983	0.331757	676		25	2.099752	1033	0.369761	732
94	0	2.046330	984	0.332433	676		30	2.100785	1033	0.370493	732
	5	2.047314	-984	0.333111	-678		35	2.101820	-1035	0.371227	-734
	10	2.048299	985	0.333790	679		40	2.102856	1036	0.371962	735
	15	2.049286	987	0.334470	680		45	2.103893	1037	0.372697	735
	20	2.050273	987	0.335151	681		50	2.104931	1038	0.373434	737
	25	2.051261	988	0.335833	682		55	2.105971	1040	0.374172	738
	30	2.052250	989	0.336515	682	99	0	2.107011	1040	0.374911	739
			-989		-684				-1041		-740

A general Table of the Parabola.

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Angle.	Log.	Diff.	Log. Dist.	Diff.	Angle.	Log.	Diff.	Log. Dist.	Diff.		
°	Mean Mot.				°	Mean Mot.					
99	5	2.108052	1041	0.375651	740	103	35	2.165946	1104	0.417289	802
	10	2.109094	1042	0.376392	741		40	2.167051	1105	0.418092	803
	15	2.110138	1044	0.377135	743		45	2.168158	1107	0.418896	804
	20	2.111182	1044	0.377878	743		50	2.169265	1107	0.419701	805
	25	2.112227	1045	0.378623	745		55	2.170374	1109	0.420508	807
	30	2.113274	1047	0.379368	745	104	0	2.171484	1110	0.421316	808
			1048		747				1112		809
	35	2.114322	1048	0.380115	748		5	2.172596	1113	0.422125	810
	40	2.115370	1050	0.380863	749		10	2.173709	1114	0.422935	812
	45	2.116420	1051	0.381612	750		15	2.174823	1115	0.423747	813
	50	2.117471	1052	0.382362	751		20	2.175938	1117	0.424560	814
	55	2.118523	1053	0.383113	752		25	2.177055	1118	0.425374	815
100	0	2.119576	1054	0.383865	753		30	2.178173	1119	0.426189	816
	5	2.120630	1055	0.384618	755		35	2.179292	1121	0.427005	818
	10	2.121685	1057	0.385373	755		40	2.180413	1122	0.427823	819
	15	2.122742	1057	0.386128	757		45	2.181535	1123	0.428642	820
	20	2.123799	1058	0.386885	758		50	2.182658	1125	0.429462	821
	25	2.124857	1060	0.387643	759		55	2.183783	1126	0.430283	823
	30	2.125917	1061	0.388402	760	105	0	2.184909	1127	0.431106	824
	35	2.126978	1062	0.389162	761		5	2.186036	1129	0.431930	825
	40	2.128040	1063	0.389923	762		10	2.187165	1130	0.432755	826
	45	2.129103	1064	0.390685	764		15	2.188295	1132	0.433581	827
	50	2.130167	1065	0.391449	764		20	2.189427	1133	0.434408	829
	55	2.131232	1067	0.392213	766		25	2.190560	1134	0.435237	830
101	0	2.132299	1068	0.392979	767		30	2.191694	1136	0.436067	832
	5	2.133367	1068	0.393746	768		35	2.192830	1137	0.436899	832
	10	2.134435	1070	0.394514	769		40	2.193967	1138	0.437731	834
	15	2.135505	1071	0.395283	770		45	2.195105	1140	0.438565	835
	20	2.136576	1072	0.396053	771		50	2.196245	1141	0.439400	836
	25	2.137648	1074	0.396824	773		55	2.197386	1142	0.440236	838
	30	2.138722	1074	0.397597	774	106	0	2.198528	1144	0.441074	839
	35	2.139796	1076	0.398371	775		5	2.199672	1145	0.441913	840
	40	2.140872	1077	0.399146	776		10	2.200817	1147	0.442753	841
	45	2.141949	1078	0.399922	777		15	2.201964	1148	0.443594	843
	50	2.143027	1079	0.400699	778		20	2.203112	1150	0.444437	844
	55	2.144106	1081	0.401477	779		25	2.204262	1151	0.445281	845
102	0	2.145187	1081	0.402256	781		30	2.205413	1152	0.446126	847
	5	2.146268	1083	0.403037	782		35	2.206565	1154	0.446973	848
	10	2.147351	1084	0.403819	783		40	2.207719	1156	0.447821	849
	15	2.148435	1085	0.404602	784		45	2.208875	1156	0.448670	850
	20	2.149520	1087	0.405386	785		50	2.210031	1158	0.449520	852
	25	2.150607	1088	0.406171	786		55	2.211189	1160	0.450372	853
	30	2.151695	1088	0.406957	788	107	0	2.212349	1161	0.451225	854
	35	2.152783	1090	0.407745	789		5	2.213510	1163	0.452079	856
	40	2.153873	1092	0.408534	790		10	2.214673	1164	0.452935	857
	45	2.154965	1092	0.409324	791		15	2.215837	1166	0.453792	858
	50	2.156057	1094	0.410115	792		20	2.217003	1167	0.454650	859
	55	2.157151	1095	0.410907	794		25	2.218170	1168	0.455509	861
103	0	2.158246	1096	0.411701	795		30	2.219338	1170	0.456370	862
	5	2.159342	1098	0.412496	796		35	2.220508	1172	0.457232	864
	10	2.160440	1099	0.413292	797		40	2.221680	1173	0.458096	864
	15	2.161539	1100	0.414089	798		45	2.222853	1174	0.458960	866
	20	2.162639	1101	0.414887	799		50	2.224027	1176	0.459826	868
	25	2.163740	1102	0.415686	801		55	2.225203	1178	0.460694	869
	30	2.164842	1104	0.416487	802	108	0	2.226381	1179	0.461563	870

A general Table of the Parabola.

Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.
	Mean Mot.					Mean Mot.			
108 5	2.227560	1179	0.462433	870	112 35	2.293634	1270	0.511468	946
10 10	2.228740	1180	0.463304	871	40	2.294005	1271	0.512416	948
15 15	2.229922	1182	0.464177	873	45	2.296177	1272	0.513365	949
20 20	2.231106	1184	0.465051	874	50	2.297452	1275	0.514315	950
25 25	2.232291	1185	0.465926	875	55	2.298728	1276	0.515267	952
30 30	2.233478	1187	0.466803	877	113 0	2.300007	1279	0.516221	954
35 35	2.234666	1188	0.467681	878	5	2.301287	1280	0.517176	955
40 40	2.235856	1190	0.468561	880	10	2.302569	1282	0.518133	957
45 45	2.237048	1192	0.469441	880	15	2.303853	1284	0.519091	958
50 50	2.238241	1193	0.470324	883	20	2.305139	1286	0.520050	959
55 55	2.239435	1194	0.471207	883	25	2.306426	1287	0.521012	962
109 0	2.240631	1196	0.472092	885	30	2.307716	1290	0.521974	962
5 5	2.241829	1198	0.472978	886	35	2.309007	1291	0.522938	964
10 10	2.243028	1199	0.473866	888	40	2.310300	1293	0.522938	966
15 15	2.244229	1201	0.474755	889	45	2.311596	1296	0.523904	967
20 20	2.245432	1203	0.475645	890	50	2.312893	1297	0.524871	969
25 25	2.246636	1204	0.476537	892	55	2.314192	1299	0.525840	971
30 30	2.247842	1206	0.477430	893	114 0	2.315493	1301	0.526811	971
35 35	2.249049	1207	0.478324	894	5	2.316796	1303	0.527782	974
40 40	2.250258	1209	0.479220	896	10	2.318101	1305	0.528756	975
45 45	2.251468	1210	0.480117	897	15	2.319407	1306	0.529731	976
50 50	2.252680	1212	0.481016	899	20	2.320716	1309	0.530707	979
55 55	2.253894	1214	0.481916	900	25	2.322027	1311	0.531686	979
110 0	2.255110	1216	0.482817	901	30	2.323339	1312	0.532665	981
5 5	2.256327	1217	0.483720	903	35	2.324654	1315	0.533646	983
10 10	2.257546	1219	0.484624	904	40	2.325970	1316	0.534629	985
15 15	2.258766	1220	0.485530	906	45	2.327289	1319	0.535614	986
20 20	2.259988	1222	0.486437	907	50	2.328609	1320	0.536600	987
25 25	2.261212	1224	0.487345	908	55	2.329932	1323	0.537587	989
30 30	2.262437	1225	0.488255	910	115 0	2.331257	1325	0.538576	991
35 35	2.263664	1227	0.489166	911	5	2.332583	1326	0.539567	992
40 40	2.264893	1229	0.490079	913	10	2.333912	1329	0.540559	994
45 45	2.266124	1231	0.490993	914	15	2.335242	1330	0.541553	996
50 50	2.267356	1232	0.491909	916	20	2.336575	1333	0.542549	997
55 55	2.268590	1234	0.492826	917	25	2.337909	1334	0.543546	999
111 0	2.269826	1236	0.493744	918	30	2.339246	1337	0.544545	1000
5 5	2.271063	1237	0.494664	920	35	2.340585	1339	0.545545	1002
10 10	2.272302	1239	0.495585	921	40	2.341925	1340	0.546547	1003
15 15	2.273543	1241	0.496508	923	45	2.343268	1343	0.547550	1005
20 20	2.274785	1242	0.497432	924	50	2.344613	1345	0.548555	1007
25 25	2.276029	1244	0.497432	925	55	2.345960	1347	0.549562	1009
30 30	2.277275	1246	0.498357	927	116 0	2.347309	1349	0.550571	1010
35 35	2.278523	1248	0.499284	929	5	2.348660	1351	0.551581	1011
40 40	2.279772	1249	0.500213	930	10	2.348660	1354	0.552592	1014
45 45	2.281023	1251	0.501143	931	15	2.350014	1355	0.553606	1015
50 50	2.282276	1253	0.502074	933	20	2.351369	1357	0.554621	1016
55 55	2.283531	1255	0.503007	934	25	2.352726	1360	0.555637	1018
112 0	2.284788	1257	0.503941	936	30	2.354086	1362	0.556655	1020
5 5	2.286046	1258	0.504877	937	35	2.355448	1364	0.557675	1022
10 10	2.287306	1260	0.505814	939	40	2.356812	1365	0.558697	1023
15 15	2.288568	1262	0.506753	940	45	2.358177	1368	0.559720	1025
20 20	2.289832	1264	0.507693	941	50	2.359545	1371	0.560745	1027
25 25	2.291097	1265	0.508634	943	55	2.360916	1372	0.561772	1028
30 30	2.292364	1267	0.509577	945	117 0	2.362288	1375	0.562800	1030
		1270	0.510522	946		2.363663	1377	0.563830	1032

A general Table of the Parabola.

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Angle.	Log.	Diff.	Log. Dist.	Diff.	Angle.	Log.	Diff.	Log. Dist.	Diff.
Mean Mot.					Mean Mot.				
117 5	2.365040	1377	0.564862	1032	121 35	2.442820	1506	0.623184	1125
10	2.366418	1378	0.565895	1033	40	2.444328	1508	0.624315	1131
15	2.367799	1381	0.566930	1035	45	2.445839	1511	0.625448	1133
20	2.369183	1384	0.567966	1036	50	2.447352	1513	0.626582	1134
25	2.370568	1385	0.569005	1039	55	2.448868	1516	0.627719	1137
30	2.371956	1388	0.570045	1040	122 0	2.450387	1519	0.628858	1139
		1390		1042			1521		1140
35	2.373346	1392	0.571087	1043	5	2.451908	1524	0.629998	1143
40	2.374738	1394	0.572130	1045	10	2.453432	1527	0.631141	1143
45	2.376132	1397	0.573175	1047	15	2.454959	1529	0.632285	1144
50	2.377529	1399	0.574222	1047	20	2.456488	1532	0.633431	1146
55	2.378928	1401	0.575271	1049	25	2.458020	1535	0.634580	1149
118 0	2.380329	1403	0.576321	1050	30	2.459555	1537	0.635730	1150
		1406		1052			1540		1152
5	2.381732	1408	0.577373	1054	35	2.461092	1543	0.636882	1155
10	2.383138	1410	0.578427	1056	40	2.462632	1546	0.638037	1156
15	2.384546	1413	0.579483	1057	45	2.464175	1548	0.639193	1158
20	2.385956	1415	0.580540	1059	50	2.465721	1552	0.640351	1161
25	2.387369	1417	0.581599	1061	55	2.467269	1554	0.641512	1162
30	2.388784	1419	0.582660	1063	123 0	2.468821	1556	0.642674	1165
		1422		1064			1560		1166
35	2.390201	1424	0.583723	1066	5	2.470375	1562	0.643839	1168
40	2.391620	1426	0.584787	1068	10	2.471931	1565	0.645005	1171
45	2.393042	1429	0.585853	1070	15	2.473491	1568	0.646173	1172
50	2.394466	1431	0.586921	1071	20	2.475053	1570	0.647344	1175
55	2.395892	1434	0.587991	1074	25	2.476618	1574	0.648516	1176
119 0	2.397321	1436	0.589062	1075	30	2.478186	1577	0.649691	1179
		1438		1076			1579		1181
5	2.398752	1440	0.590136	1079	35	2.479756	1582	0.650867	1183
10	2.400186	1443	0.591211	1080	40	2.481330	1585	0.652046	1184
15	2.401622	1446	0.592287	1083	45	2.482907	1588	0.653227	1187
20	2.403060	1447	0.593366	1084	50	2.484486	1591	0.654410	1189
25	2.404500	1451	0.594446	1085	55	2.486068	1593	0.655594	1192
30	2.405943	1452	0.595529	1088	124 0	2.487653	1597	0.656781	1193
		1455		1090			1599		1195
35	2.407389	1458	0.596613	1091	5	2.489241	1603	0.657970	1197
40	2.408836	1460	0.597698	1093	10	2.490832	1605	0.659162	1200
45	2.410287	1462	0.598786	1095	15	2.492425	1608	0.660355	1202
50	2.411739	1465	0.599876	1097	20	2.494022	1612	0.661550	1203
55	2.413194	1468	0.600967	1098	25	2.495621	1614	0.662747	1206
120 0	2.414652	1470	0.602060	1101	30	2.497224	1617	0.663947	1208
		1472		1102			1621		1211
5	2.416112	1475	0.603155	1105	35	2.498829	1623	0.665149	1212
10	2.417574	1477	0.604252	1106	40	2.500437	1626	0.666352	1214
15	2.419039	1480	0.605350	1108	45	2.502049	1630	0.667558	1217
20	2.420507	1482	0.606451	1110	50	2.503663	1632	0.668766	1219
25	2.421977	1485	0.607553	1111	55	2.505280	1635	0.669977	1221
30	2.423449	1488	0.608658	1114	125 0	2.506901	1639	0.671189	1223
		1490		1115			1641		1225
35	2.424924	1492	0.609764	1118	5	2.508524	1645	0.672403	1228
40	2.426401	1495	0.610872	1119	10	2.510150	1648	0.673620	1229
45	2.427881	1498	0.611982	1121	15	2.511780	1650	0.674839	1232
50	2.429363	1500	0.613093	1123	20	2.513412	1654	0.676060	1235
55	2.430848	1503	0.614207	1125	25	2.515047	1657	0.677283	1236
121 0	2.432336	1506	0.615322	1127	30	2.516686	1660	0.678508	1238
				1129					1241
5	2.433826		0.616440		35	2.518327		0.679736	
10	2.435318		0.617559		40	2.519972		0.680965	
15	2.436813		0.618680		45	2.521620		0.682197	
20	2.438311		0.619803		50	2.523270		0.683432	
25	2.439811		0.620928		55	2.524924		0.684668	
30	2.441314		0.622055		126 0	2.526581		0.685906	

Angle.	Log. Mean Mot.	Diff.	Log. Diff.	Diff.	Angle.	Log. Mean Mot.	Diff.	Log. Diff.	Diff.
126 0	2.528241	1660	0.687147	1241	130 0	2.622869	1847	0.757649	1371
5	2.529905	1664	0.688390	1243	35	2.624720	1851	0.759023	1374
10	2.531571	1666	0.689636	1246	40	2.626575	1855	0.760400	1377
15	2.533241	1670	0.690883	1247	45	2.628434	1859	0.761779	1379
20	2.534914	1673	0.692133	1250	50	2.630296	1862	0.763161	1382
25	2.536590	1676	0.693385	1252	55	2.632162	1866	0.764546	1385
30	2.538269	1679	0.694639	1254	131 0	2.634032	1870	0.765933	1387
35	2.539951	1682	0.695896	1257	5	2.635907	1875	0.767324	1391
40	2.541637	1686	0.697155	1259	10	2.637785	1878	0.768716	1392
45	2.543326	1689	0.698416	1261	15	2.639667	1882	0.770112	1396
50	2.545018	1692	0.699679	1263	20	2.641553	1886	0.771510	1398
55	2.546714	1696	0.700945	1266	25	2.643443	1890	0.772911	1401
127 0	2.548412	1698	0.702213	1268	30	2.645336	1893	0.774314	1403
5	2.550114	1702	0.703484	1271	35	2.647234	1898	0.775721	1407
10	2.551819	1705	0.704756	1272	40	2.649136	1902	0.777130	1409
15	2.553528	1709	0.706031	1275	45	2.651042	1906	0.778541	1411
20	2.555240	1712	0.707309	1278	50	2.652952	1910	0.779956	1415
25	2.556955	1715	0.708588	1279	55	2.654866	1914	0.781373	1417
30	2.558674	1719	0.709870	1282	132 0	2.656784	1918	0.782794	1421
35	2.560395	1721	0.711155	1285	5	2.658706	1922	0.784217	1423
40	2.562121	1726	0.712442	1287	10	2.660632	1926	0.785642	1425
45	2.563849	1728	0.713731	1289	15	2.662562	1930	0.787071	1429
50	2.565581	1732	0.715022	1291	20	2.664497	1935	0.788502	1431
55	2.567316	1735	0.716316	1294	25	2.666435	1938	0.789936	1434
128 0	2.569055	1739	0.717612	1296	30	2.668378	1943	0.791373	1437
5	2.570798	1743	0.718911	1299	35	2.670325	1947	0.792813	1440
10	2.572544	1746	0.720212	1301	40	2.672276	1951	0.794255	1442
15	2.574293	1749	0.721516	1304	45	2.674231	1955	0.795701	1446
20	2.576045	1752	0.722822	1306	50	2.676191	1960	0.797149	1448
25	2.577801	1756	0.724130	1308	55	2.678155	1964	0.798601	1452
30	2.579561	1760	0.725441	1311	133 0	2.680123	1968	0.800055	1454
35	2.581324	1763	0.726754	1313	5	2.682095	1972	0.801512	1457
40	2.583090	1766	0.728070	1316	10	2.684071	1976	0.802972	1460
45	2.584860	1770	0.729388	1318	15	2.686052	1981	0.804435	1463
50	2.586634	1774	0.730708	1320	20	2.688037	1985	0.805900	1465
55	2.588411	1777	0.732031	1323	25	2.690027	1990	0.807369	1469
129 0	2.590192	1781	0.733357	1326	30	2.692021	1994	0.808841	1472
5	2.591976	1784	0.734685	1328	35	2.694019	1998	0.810316	1475
10	2.593764	1788	0.736015	1330	40	2.696022	2003	0.811793	1477
15	2.595556	1792	0.737348	1333	45	2.698029	2007	0.813274	1481
20	2.597351	1795	0.738684	1336	50	2.700040	2011	0.814757	1483
25	2.599150	1799	0.740022	1338	55	2.702056	2016	0.816244	1487
30	2.600952	1802	0.741363	1341	134 0	2.704077	2021	0.817734	1490
35	2.602758	1806	0.742706	1343	5	2.706101	2024	0.819226	1492
40	2.604568	1810	0.744051	1345	10	2.708131	2030	0.820722	1496
45	2.606381	1813	0.745399	1348	15	2.710165	2034	0.822221	1499
50	2.608198	1817	0.746750	1351	20	2.712203	2038	0.823722	1501
55	2.610019	1821	0.748103	1353	25	2.714246	2043	0.825227	1505
130 0	2.611843	1824	0.749459	1356	30	2.716293	2047	0.826735	1508
5	2.613671	1828	0.750818	1359	35	2.718345	2052	0.828246	1511
10	2.615503	1832	0.752179	1361	40	2.720401	2056	0.829760	1514
15	2.617339	1836	0.753543	1364	45	2.722463	2062	0.831277	1517
20	2.619179	1840	0.754909	1366	50	2.724528	2065	0.832797	1520
25	2.621022	1843	0.756278	1369	55	2.726599	2071	0.834321	1524
30		1847		1371	135 0		2075		1526

A general Table of the Parabola.

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Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.
135 5	2.728674	2075	0.835847	1526	139 35	2.848199	2357	0.923268	1714
10	2.730754	2080	0.837377	1530	40	2.850561	2362	0.924986	1718
15	2.732838	2084	0.838910	1533	45	2.852930	2369	0.926708	1722
20	2.734927	2089	0.840446	1536	50	2.855304	2374	0.928434	1726
25	2.737021	2094	0.841985	1539	55	2.857684	2380	0.930163	1729
30	2.739120	2099	0.843527	1542	140 0	2.860070	2386	0.931897	1734
		2104		1546			2392		1737
35	2.741224	2108	0.845073	1549	5	2.862462	2398	0.933634	1741
40	2.743332	2113	0.846622	1552	10	2.864860	2405	0.935375	1746
45	2.745445	2118	0.848174	1555	15	2.867265	2410	0.937121	1749
50	2.747563	2123	0.849729	1558	20	2.869675	2416	0.938870	1753
55	2.749686	2128	0.851287	1562	25	2.872091	2422	0.940623	1758
136 0	2.751814	2132	0.852849	1565	30	2.874513	2428	0.942381	1761
5	2.753946	2138	0.854414	1569	35	2.876941	2435	0.944142	1765
10	2.756084	2142	0.855983	1571	40	2.879376	2440	0.945907	1770
15	2.758226	2147	0.857554	1575	45	2.881816	2447	0.947677	1773
20	2.760373	2153	0.859129	1578	50	2.884263	2453	0.949450	1778
25	2.762526	2157	0.860707	1582	55	2.886716	2459	0.951228	1781
30	2.764683	2162	0.862289	1585	141 0	2.889175	2466	0.953009	1786
35	2.766845	2167	0.863874	1588	5	2.891641	2472	0.954795	1790
40	2.769012	2173	0.865462	1592	10	2.894113	2478	0.956585	1794
45	2.771185	2177	0.867054	1595	15	2.896591	2484	0.958379	1799
50	2.773362	2182	0.868649	1598	20	2.899075	2491	0.960178	1802
55	2.775544	2188	0.870247	1602	25	2.901566	2497	0.961980	1807
137 0	2.777732	2193	0.871849	1605	30	2.904063	2504	0.963787	1811
5	2.779925	2198	0.873454	1609	35	2.906567	2510	0.965598	1815
10	2.782123	2203	0.875063	1612	40	2.909077	2517	0.967413	1819
15	2.784326	2208	0.876675	1616	45	2.911594	2523	0.969232	1824
20	2.786534	2214	0.878291	1619	50	2.914117	2530	0.971056	1828
25	2.788748	2218	0.879910	1623	55	2.916647	2536	0.972884	1832
30	2.790966	2224	0.881533	1626	142 0	2.919183	2543	0.974716	1837
35	2.793190	2229	0.883159	1629	5	2.921726	2550	0.976553	1841
40	2.795419	2235	0.884788	1633	10	2.924276	2556	0.978394	1845
45	2.797654	2240	0.886421	1637	15	2.926832	2562	0.980239	1850
50	2.799894	2245	0.888058	1640	20	2.929394	2570	0.982089	1854
55	2.802139	2250	0.889698	1644	25	2.931964	2576	0.983943	1859
138 0	2.804389	2256	0.891342	1647	30	2.934540	2584	0.985802	1863
5	2.806645	2262	0.892989	1651	35	2.937124	2590	0.987665	1867
10	2.808907	2267	0.894640	1654	40	2.939714	2596	0.989532	1872
15	2.811174	2272	0.896294	1659	45	2.942310	2604	0.991404	1877
20	2.813446	2277	0.897953	1661	50	2.944914	2611	0.993281	1881
25	2.815723	2283	0.899614	1666	55	2.947525	2617	0.995162	1885
30	2.818006	2289	0.901280	1669	143 0	2.950142	2625	0.997047	1890
35	2.820295	2294	0.902949	1672	5	2.952767	2631	0.998937	1895
40	2.822589	2300	0.904621	1677	10	2.955398	2639	1.000832	1899
45	2.824889	2306	0.906298	1680	15	2.958037	2645	1.002731	1904
50	2.827195	2311	0.907978	1684	20	2.960682	2653	1.004635	1909
55	2.829506	2316	0.909662	1687	25	2.963335	2659	1.006544	1913
139 0	2.831822	2323	0.911349	1692	30	2.965994	2667	1.008457	1918
5	2.834145	2328	0.913041	1695	35	2.968661	2675	1.010375	1922
10	2.836473	2333	0.914736	1699	40	2.971336	2681	1.012297	1928
15	2.838806	2340	0.916435	1702	45	2.974017	2689	1.014225	1932
20	2.841146	2345	0.918137	1707	50	2.976706	2696	1.016157	1937
25	2.843491	2351	0.919844	1710	55	2.979402	2703	1.018094	1941
30	2.845842	2357	0.921554	1714	144 0	2.982105	2711	1.020035	1947

Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.
	Mean Mot.					Mean Mot.			
144 5	2.984816	2711	1.021982	1947	148 35	3.143162	3166	1.134894	2243
10	2.987534	2718	1.023933	1951	40	3.146338	3176	1.137143	2249
15	2.990259	2725	1.025889	1956	45	3.149523	3185	1.139398	2255
20	2.992992	2733	1.027850	1961	50	3.152718	3195	1.141660	2262
25	2.995732	2740	1.029816	1966	55	3.155922	3204	1.143928	2268
30	2.998480	2748	1.031787	1971	149 0	3.159137	3215	1.146202	2274
		2756		1976			3224		2281
35	3.001236	2763	1.033763	1980	5	3.162361	3234	1.148483	2288
40	3.003999	2771	1.035743	1986	10	3.165595	3245	1.150771	2293
45	3.006770	2778	1.037729	1991	15	3.168840	3254	1.153064	2301
50	3.009548	2786	1.039720	1996	20	3.172094	3265	1.155365	2307
55	3.012334	2794	1.041716	2000	25	3.175359	3274	1.157672	2313
145 0	3.015128	2802	1.043716	2006	30	3.178633	3285	1.159985	2321
5	3.017930	2809	1.045722	2011	35	3.181918	3296	1.162306	2327
10	3.020739	2818	1.047733	2016	40	3.185214	3305	1.164633	2333
15	3.023557	2825	1.049749	2022	45	3.188519	3316	1.166966	2340
20	3.026382	2833	1.051771	2026	50	3.191835	3327	1.169306	2348
25	3.029215	2841	1.053797	2032	55	3.195162	3337	1.171654	2354
30	3.032056	2850	1.055829	2037	150 0	3.198499	3347	1.174008	2360
35	3.034906	2857	1.057866	2042	5	3.201846	3358	1.176368	2368
40	3.037763	2865	1.059908	2047	10	3.205204	3369	1.178736	2375
45	3.040628	2874	1.061955	2053	15	3.208573	3379	1.181111	2381
50	3.043502	2882	1.064008	2058	20	3.211952	3390	1.183492	2389
55	3.046384	2889	1.066066	2063	25	3.215342	3402	1.185881	2396
146 0	3.049273	2898	1.068129	2069	30	3.218744	3412	1.188277	2402
5	3.052171	2907	1.070198	2074	35	3.222156	3423	1.190679	2410
10	3.055078	2915	1.072272	2080	40	3.225579	3434	1.193080	2417
15	3.057993	2923	1.074352	2085	45	3.229013	3445	1.195506	2424
20	3.060916	2931	1.076437	2090	50	3.232458	3456	1.197930	2432
25	3.063847	2940	1.078527	2096	55	3.235914	3468	1.200362	2439
30	3.066787	2949	1.080623	2102	151 0	3.239382	3479	1.202801	2446
35	3.069736	2957	1.082725	2107	5	3.242861	3490	1.205247	2453
40	3.072693	2965	1.084832	2113	10	3.246351	3502	1.207700	2461
45	3.075658	2974	1.086945	2118	15	3.249853	3513	1.210161	2469
50	3.078632	2983	1.089063	2124	20	3.253366	3524	1.212630	2475
55	3.081615	2992	1.091187	2129	25	3.256890	3537	1.215105	2484
147 0	3.084607	3000	1.093316	2136	30	3.260427	3548	1.217589	2491
5	3.087607	3009	1.095452	2141	35	3.263975	3559	1.220080	2498
10	3.090616	3018	1.097593	2146	40	3.267534	3572	1.222578	2506
15	3.093634	3027	1.099739	2153	45	3.271106	3583	1.225084	2514
20	3.096661	3036	1.101892	2158	50	3.274689	3596	1.227598	2522
25	3.099697	3045	1.104050	2165	55	3.278285	3607	1.230120	2530
30	3.102742	3054	1.106215	2170	152 0	3.281892	3620	1.232650	2537
35	3.105796	3063	1.108385	2176	5	3.285512	3631	1.235187	2545
40	3.108859	3072	1.110561	2181	10	3.289143	3644	1.237732	2553
45	3.111931	3081	1.112742	2188	15	3.292787	3656	1.240285	2562
50	3.115012	3090	1.114930	2194	20	3.296443	3669	1.242847	2569
55	3.118102	3100	1.117124	2200	25	3.300112	3681	1.245416	2577
148 0	3.121202	3109	1.119324	2206	30	3.303793	3693	1.247993	2586
5	3.124311	3118	1.121530	2212	35	3.307486	3706	1.250579	2593
10	3.127429	3128	1.123742	2218	40	3.311192	3719	1.253172	2602
15	3.130557	3137	1.125960	2224	45	3.314911	3732	1.255774	2610
20	3.133694	3146	1.128184	2230	50	3.318643	3744	1.258384	2619
25	3.136840	3156	1.130414	2237	55	3.322387	3758	1.261003	2626
30	3.139996	3166	1.132651	2243	153 0	3.326145	3770	1.263629	2636

Angle.	Log.	Diff.	Log. Diff.	Diff.	Angle.	Log.	Diff.	Log. Diff.	Diff.
°	Mean Mot.				°	Mean Mot.			
153	5	3.329915	3770	2636	157	35	3.555279	4611	3181
	10	3.333698	3783	2644		40	3.559908	4629	3194
	15	3.337495	3797	2652		45	3.564556	4648	3206
	20	3.341305	3810	2661		50	3.569223	4667	3218
	25	3.345128	3823	2669		55	3.573910	4687	3231
	30	3.348964	3836	2678	158	0	3.578615	4705	3243
			3850	2687		5	3.583340	4725	3256
	35	3.352814	3864	2696		10	3.588085	4745	3269
	40	3.356678	3877	2705		15	3.592849	4764	3281
	45	3.360555	3890	2713		20	3.597633	4784	3295
	50	3.364445	3905	2722		25	3.602437	4804	3307
	55	3.368350	3918	2732		30	3.607260	4823	3320
154	0	3.372268	3933	2740		35	3.612105	4845	3334
	5	3.376201	3946	2750		40	3.616969	4864	3347
	10	3.380147	3961	2759		45	3.621855	4886	3360
	15	3.384108	3975	2768		50	3.626760	4905	3374
	20	3.388083	3989	2778		55	3.631687	4927	3388
	25	3.392072	4004	2786	159	0	3.636635	4948	3401
	30	3.396076	4018	2797		5	3.641604	4969	3415
	35	3.400094	4033	2805		10	3.646595	4991	3429
	40	3.404127	4048	2816		15	3.651607	5012	3443
	45	3.408175	4062	2825		20	3.656640	5033	3457
	50	3.412237	4077	2834		25	3.661696	5056	3472
	55	3.416314	4092	2844		30	3.666774	5078	3486
155	0	3.420406	4108	2855		35	3.671873	5099	3500
	5	3.424514	4122	2864		40	3.676995	5122	3515
	10	3.428636	4138	2874		45	3.682140	5145	3530
	15	3.432774	4153	2883		50	3.687308	5168	3544
	20	3.436927	4169	2894		55	3.692499	5191	3560
	25	3.441096	4184	2905	160	0	3.697713	5214	3575
	30	3.445280	4200	2914		5	3.702950	5237	3589
	35	3.449480	4216	2925		10	3.708210	5260	3606
	40	3.453696	4232	2935		15	3.713495	5285	3621
	45	3.457928	4247	2945		20	3.718803	5308	3636
	50	3.462175	4264	2956		25	3.724135	5332	3652
	55	3.466439	4280	2966		30	3.729492	5357	3668
156	0	3.470719	4297	2977		35	3.734873	5381	3684
	5	3.475016	4313	2988		40	3.740279	5406	3700
	10	3.479329	4329	2998		45	3.745710	5431	3717
	15	3.483658	4346	3010		50	3.751166	5456	3733
	20	3.488004	4363	3020		55	3.756647	5481	3749
	25	3.492367	4380	3031	161	0	3.762154	5507	3767
	30	3.496747	4397	3043		5	3.767687	5533	3783
	35	3.501144	4414	3053		10	3.773246	5559	3800
	40	3.505558	4431	3065		15	3.778831	5585	3817
	45	3.509989	4449	3076		20	3.784442	5611	3835
	50	3.514438	4466	3087		25	3.790080	5638	3852
	55	3.518904	4484	3099		30	3.795745	5665	3869
157	0	3.523388	4501	3111		35	3.801437	5692	3888
	5	3.527889	4519	3122		40	3.807157	5720	3905
	10	3.532408	4538	3134		45	3.812904	5747	3923
	15	3.536946	4555	3145		50	3.818679	5775	3942
	20	3.541501	4574	3158		55	3.824483	5804	3960
	25	3.546075	4593	3170	162	0	3.830315	5832	3979
	30	3.550668	4611	3181				5860	3998

Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.	Angle.	Log. Mean Mot.	Diff.	Log. Dist.	Diff.
162 5	3.836175	5860	1.615333	3998	166 35	4.204152	7924	1.865001	5353
10	3.842065	5890	1.619349	4016	40	4.212128	7976	1.870389	5388
15	3.847983	5918	1.623385	4036	45	4.220155	8027	1.875810	5421
20	3.853931	5948	1.627440	4055	50	4.228235	8080	1.881266	5456
25	3.859909	5978	1.631514	4074	55	4.236367	8132	1.886756	5490
30	3.865917	6008	1.635608	4094	167 0	4.244553	8186	1.892282	5526
		6038		4114			8241		5562
35	3.871955	6069	1.639722	4134	5	4.252794	8296	1.897844	5599
40	3.878024	6100	1.643856	4154	10	4.261090	8352	1.903443	5635
45	3.884124	6131	1.648010	4175	15	4.269442	8408	1.909078	5672
50	3.890255	6162	1.652185	4195	20	4.277850	8465	1.914750	5710
55	3.896417	6194	1.656380	4216	25	4.286315	8523	1.920460	5748
163 0	3.902611	6226	1.660596	4237	30	4.294838	8582	1.926208	5788
		6258		4258			8642		5826
5	3.908837	6291	1.664833	4280	35	4.303420	8701	1.931996	5866
10	3.915095	6324	1.669091	4301	40	4.312062	8763	1.937822	5907
15	3.921386	6358	1.673371	4324	45	4.320763	8825	1.943688	5947
20	3.927710	6392	1.677672	4345	50	4.329526	8888	1.949595	5989
25	3.934068	6425	1.681996	4368	55	4.338351	8951	1.955542	6031
30	3.940460	6459	1.686341	4390	168 0	4.347239	9016	1.961531	6073
		6494		4413			9082		6117
35	3.946885	6530	1.690709	4436	5	4.356190	9147	1.967562	6161
40	3.953344	6565	1.695099	4459	10	4.365206	9215	1.973635	6205
45	3.959838	6600	1.699512	4482	15	4.374288	9284	1.979752	6250
50	3.966368	6637	1.703948	4507	20	4.383435	9352	1.985913	6296
55	3.972933	6673	1.708407	4530	25	4.392650	9423	1.992118	6342
164 0	3.979533	6710	1.712889	4555	30	4.401934	9494	1.998368	6390
		6747		4579			9567		6437
5	3.986170	6785	1.717396	4603	35	4.411286	9640	2.004664	6486
10	3.992843	6823	1.721926	4629	40	4.420709	9714	2.011006	6535
15	3.999553	6861	1.726481	4654	45	4.430203	9790	2.017396	6585
20	4.006300	6900	1.731060	4680	50	4.439770	9867	2.023833	6636
25	4.013085	6940	1.735663	4705	55	4.449410	9945	2.030319	6688
3	4.019908	6979	1.740292	4731	169 0	4.459124	10024	2.036854	6740
		7019		4758			10104		6792
35	4.026769	7060	1.744946	4785	5	4.468914	10186	2.043439	6847
40	4.033669	7101	1.749626	4811	10	4.478781	10269	2.050075	6902
45	4.040609	7142	1.754331	4839	15	4.488726	10353	2.056763	6956
50	4.047588	7185	1.759062	4866	20	4.498750	10438	2.063503	7014
55	4.054607	7227	1.763820	4894	25	4.508854	10526	2.070295	7072
165 0	4.061667	7269	1.768605	4923	30	4.519040	10614	2.077142	7130
		7313		4950			10704		7190
5	4.068768	7357	1.773416	4980	5	4.529309	10796	2.084044	7250
10	4.075910	7401	1.778255	5009	10	4.539662	10888	2.091002	7312
15	4.083095	7446	1.783121	5038	15	4.550100	10982	2.098016	7374
20	4.090322	7491	1.788015	5069	20	4.560626	11079	2.105088	7438
25	4.097591	7537	1.792938	5098	25	4.571240	11176	2.112218	7503
30	4.104904	7584	1.797888	5129	30	4.581944	11276	2.119408	7568
		7630		5160			11377		7636
35	4.112261	7678	1.802868	5191	35	4.592740	11480	2.126658	7703
40	4.119662	7727	1.807877	5223	40	4.603628	11585	2.133970	7773
45	4.127108	7775	1.812915	5255	45	4.614610	11691	2.141344	7844
50	4.134599	7824	1.817984	5288	50	4.625689	11799	2.148782	7916
55	4.142136	7874	1.823082	5320	55	4.636865	11910	2.156285	7988
166 0	4.149720	7924	1.828211	5353	30	4.648141	12023	2.163853	8064
5	4.157350		1.833371		35	4.659518		2.171489	
10	4.165028		1.838562		40	4.670998		2.179192	
15	4.172755		1.843785		45	4.682583		2.186965	
20	4.180530		1.849040		50	4.694274		2.194809	
25	4.188354		1.854328		55	4.706073		2.202725	
30	4.196228		1.859648		171 0	4.717983		2.210713	

A general Table of the Parabola.

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Angle.	Log.	Diff.	Log.	Diff.	Angle.	Log.	Diff.	Log.	Diff.
Mean Mot.			Diff.		Mean Mot.			Diff.	
171 0	4.730006	12023	2.218777	-8064	175 35	5.641401	24304	2.828331	16227
10	4.742144	12138	2.226916	8139	40	5.666171	24770	2.844868	16537
15	4.754398	12254	2.235133	8217	45	5.691424	25253	2.861727	16859
20	4.766771	12373	2.243429	8296	50	5.717178	25754	2.878919	17192
25	4.779266	12495	2.251806	8377	55	5.743454	26276	2.896459	17540
30	4.791884	12618	2.260264	8458	176 0	5.770274	26820	2.914362	17903
35	4.804629	12745	2.268806	-8542	5	5.797661	27387	2.932641	18279
40	4.817502	12873	2.277433	8627	10	5.825639	27978	2.951314	18673
45	4.830506	13004	2.286148	8715	15	5.854233	28594	2.970398	19084
50	4.843645	13139	2.294951	8803	20	5.883472	29239	2.989911	19513
55	4.856919	13274	2.303845	8894	25	5.913384	29912	3.009872	19961
172 0	4.870333	13414	2.312831	8986	30	5.944003	30619	3.030304	20432
5	4.883890	13557	2.321912	-9081	35	5.975361	31358	3.051229	20925
10	4.897591	13701	2.331089	9177	40	6.007496	32135	3.072670	21441
15	4.911441	13850	2.340364	9275	45	6.040446	32950	3.094655	21985
20	4.925443	14002	2.349740	9376	50	6.074254	33808	3.117211	22556
25	4.939599	14156	2.359219	9479	55	6.108965	34711	3.140369	23158
30	4.953913	14314	2.368803	9584	177 0	6.144629	35664	3.164162	23793
35	4.968389	14476	2.378494	-9691	5	6.181299	36670	3.188625	24463
40	4.983031	14642	2.388295	9801	10	6.219035	37736	3.213798	25173
45	4.997842	14811	2.398209	9914	15	6.257900	38865	3.239723	25925
50	5.012826	14984	2.408237	10028	20	6.297962	40062	3.266446	26723
55	5.027986	15160	2.418383	10146	25	6.339298	41336	3.294018	27572
173 0	5.043328	15342	2.428649	10266	30	6.381991	42693	3.322494	28476
5	5.058856	15528	2.439039	10390	35	6.426134	44143	3.351936	29442
10	5.074574	15718	2.449555	10516	40	6.471828	45694	3.382412	30476
15	5.090486	15912	2.460200	10645	45	6.519185	47357	3.413996	31584
20	5.106598	16112	2.470978	10778	50	6.568332	49147	3.446773	32777
25	5.122914	16316	2.481891	10913	55	6.619409	51077	3.480836	34063
30	5.139440	16526	2.492944	11053	178 0	6.672573	53164	3.516289	35453
35	5.156181	16741	2.504140	11196	5	6.728001	55428	3.553253	36964
40	5.173143	16962	2.515483	11343	10	6.785896	57895	3.591860	38607
45	5.190331	17188	2.526976	11493	15	6.846486	60590	3.632263	40403
50	5.207752	17421	2.538624	11648	20	6.910035	63549	3.674638	42375
55	5.225412	17660	2.550430	11806	25	6.976847	66812	3.719188	44550
174 0	5.243317	17905	2.562400	11970	30	7.047273	70426	3.766148	46960
5	5.261474	18157	2.574537	12137	35	7.121727	74454	3.815792	49644
10	5.279890	18416	2.586847	12310	40	7.200699	78972	3.868447	52655
15	5.298574	18684	2.599334	12487	45	7.284771	84072	3.924502	56055
20	5.317532	18958	2.612004	12670	50	7.374647	89876	3.984427	59925
25	5.336772	19240	2.624862	12858	55	7.471189	96542	4.048794	64367
30	5.356304	19532	2.637913	13051	179 0	7.575464	104275	4.118316	69522
35	5.376136	19832	2.651165	13252	5	7.688819	113355	4.193892	75576
40	5.396278	20142	2.664621	13456	10	7.812987	124168	4.276675	82783
45	5.416738	20460	2.678290	13669	15	7.950251	137264	4.368189	91514
50	5.437527	20789	2.692179	13889	20	8.103703	153452	4.470494	102305
55	5.458657	21130	2.706293	14114	25	8.277670	173967	4.586475	115981
175 0	5.480137	21480	2.720641	14348	30	8.478504	200834	4.720368	133893
5	5.501980	21843	2.735230	14589	35	8.716043	237539	4.878730	158362
10	5.524199	22219	2.750069	14839	40	9.006769	290726	5.072549	193819
15	5.546806	22607	2.765167	15098	45	9.381582	374813	5.322426	249877
20	5.569815	23009	2.780532	15365	50	9.909853	528271	5.674608	352182
25	5.593240	23425	2.796174	15642	55	10.812942	903089	6.276668	602060
30	5.617097	23857	2.812104	15930	180 0				
		24304		16227					

50

TABLE III. *Errors in taking Proportional Parts of the above Parabolick Table.*

Ang. from Per.	Log.M.M.	Ang.byPro. Par.	Log. of Distance			Error.	Diff.too great.
			True.	FromM.M.	Equal Div.		
45° 2' 30"	1.516934	45° 2' 30"	0.068900	900	900	.000000	
154 57 30	3.418358	154 57 29.9	1.327903	903	904	.000001	
159 57 30	3.695102	159 57 29.8	1.518870	870	872	.000002	
169 57 30	4.576581	169 57 29.7	2.115806	806	813	.000007	1.00002
173 57 30	5.234333	173 57 29.5	2.556394	394	415	.000021	1.00005
174 57 30	5.469352	174 57 29.4	2.713437	437	467	.000030	1.00007
178 57 30	7.522283	178 57 27.0	4.082860	859	3555	.000695	1.00108
179 52 30	10.284669	179 52 4.5	5.924485	486	75638	.051153	1.12500

TABLE IV. *Equation of the Sun's Place, from the Menstrual Parallax.*

Add.		☉'s Per.		☉'s Ap.		Subtract.	
°	'	°	'	°	'	°	'
5	25					5	25
10	20	3	3	2	3	10	20
15	15					15	15
20	10	5	6	5	6	20	10
25	5					25	5
1	0	8	9	7	8	7	0
5	25					5	25
10	20	10	12	10	11	10	20
15	15					15	15
20	10	12	14	11	13	20	10
25	5					25	5
2	0	13	15	13	14	8	0
5	25					5	25
10	20	14	16	14	15	10	20
15	15					15	15
20	10	15	17	14	16	20	10
25	5					25	5
3	0	15	17	15	17	9	0

TABLE V. *Increase or Decrease of the Earth's Dist. from the Sun, from the Menstrual Parallax.*

Add.		☉'s Par.		54	55	56	57	58	59	60	61	Subtract.	
°	'	°	'	°	'	°	'	°	'	°	'	°	'
5	25			0.0000795	780	766	753	740	727	715	703	6	0
10	20			0.0000791	777	763	750	737	724	712	701	5	25
15	15			0.0000783	768	755	741	729	716	704	693	10	20
20	10			0.0000767	753	740	727	714	702	691	679	15	15
25	5			0.0000747	733	720	707	695	683	672	661	20	10
1	0			0.0000720	707	694	682	671	659	648	638	25	5
5	25			0.0000688	675	663	652	641	630	619	609	7	0
10	20			0.0000651	639	628	617	606	596	586	576	5	25
15	15			0.0000609	598	587	577	567	557	548	539	10	20
20	10			0.0000562	552	542	532	523	514	506	497	15	15
25	5			0.0000511	501	492	484	476	467	460	452	20	10
2	0			0.0000456	447	439	432	424	417	410	403	25	5
5	25			0.0000397	390	383	376	370	364	358	352	8	0
10	20			0.0000336	330	324	318	313	307	302	297	5	25
15	15			0.0000272	267	262	257	253	249	245	241	10	20
20	10			0.0000206	202	198	195	191	188	185	182	15	15
25	5			0.0000138	135	133	131	128	126	124	122	20	10
3	0			0.0000069	68	67	66	64	63	62	61	25	5
5	25			0.0000000	000	000	000	000	000	000	000	9	0

Tables IV. and V. are to be thus used: From the moon's place subtract the sun's, and against the remainder in table IV. is the angle CSE (fig. 6.) to be added to, or subtracted from the sun's place as found by the common tables. Against the remainder in table V. is given the length of the line ED in parts of the earth's mean distance, to be added to, or subtracted from the distance of the earth from the sun, which the tables of the sun give.

TAB. VI. *Decimals of a Degree reduced to Minutes and Seconds.*

°	'	°	'	°	'
.001	3.6	.01	0 36	.1	6 0
.002	7.2	.02	1 12	.2	12 0
.003	10.8	.03	1 48	.3	18 0
.004	14.4	.04	2 24	.4	24 0
.005	18.0	.05	3 0	.5	30 0
.006	21.6	.06	3 36	.6	36 0
.007	25.2	.07	4 12	.7	42 0
.008	28.8	.08	4 48	.8	48 0
.009	32.4	.09	5 24	.9	54 0

TABLE VII. *Decimals of a Day reduced to Hours, Minutes, and Seconds.*

h	m	s	h	m	s
.00001	0.864	.0001	0 8.64	.001	1 26.4
.00002	1.728	.0002	0 17.28	.002	2 52.8
.00003	2.592	.0003	0 25.92	.003	4 19.2
.00004	3.456	.0004	0 34.56	.004	5 45.6
.00005	4.320	.0005	0 43.20	.005	7 12.0
.00006	5.184	.0006	0 51.84	.006	8 38.4
.00007	6.048	.0007	1 0.48	.007	10 4.8
.00008	6.912	.0008	1 9.12	.008	11 31.2
.00009	7.776	.0009	1 17.76	.009	12 57.6

TABLE VIII.

Comet 1680.				Comet 1682.			
Days Mot.	Ang. from Per.	Diff. fr. ☉	Ordnate.	Ang. from Per.	Diff. fr. ☉		
$\frac{1}{4}$	132 58 6	0.03847	0.02815				
$\frac{1}{2}$	143 53 13	0.06375	0.03757				
1	151 56 38	0.10425	0.04903				
2	158 1 52	0.16874	0.06312				
3	160 54 58	0.22289	0.07287				
4	162 42 52	0.27124	0.08059	12 26 46	0.59022		
8	166 21 18	0.43402	0.10239	24 16 54	0.61027		
12	168 6 23	0.57059	0.11760	35 10 54	0.64192		
16	169 12 25	0.69249	0.12968	44 54 55	0.68294		
20	59 19	0.80453	0.13986	53 27 18	0.73117		
24	170 35 4	0.90929	0.14875	60 53 1	0.78470		
28	171 3 36	1.00836	0.15670	67 20 5	0.84204		
32	27 7	1.10281	0.16392	72 56 25	0.90196		
36	47 0	1.19339	0.17055	77 50 28	0.96361		
40	172 4 8	1.28067	0.17671	82 8 50	1.02634		
44	19 6	1.36508	0.18247	85 57 18	1.08969		
48	32 21	1.44697	0.18789	89 20 35	1.15334		
52	44 12	1.52661	0.19301	92 22 36	1.21703		
56	55 7	1.60424	0.19777	95 6 32	1.28059		
60	173 4 36	1.68003	0.20251	97 34 58	1.34390		
64	13 28	1.75416	0.20696	99 50 6	1.40686		
68	21 39	1.82676	0.21120	101 53 41	1.46943		
72	29 12	1.89796	0.21529	103 47 13	1.53154		
76	36 13	1.96783	0.21923	105 31 54	1.59316		
80	42 44	2.03651	0.22304	107 8 50	1.65430		
84	48 51	2.10403	0.22672	108 38 53	1.71491		
88	54 35	2.17050	0.23028	110 2 49	1.77501		
92	59 59	2.23597	0.23373	111 21 16	1.83461		
96	174 5 4	2.30049	0.23709	112 34 48	1.89368		
100	9 53	2.36413	0.24036	113 43 54	1.95225		
104	14 27	2.42692	0.24354	114 49 0	2.01032		
108	18 46	2.48892	0.24665	115 50 27	2.06791		
112	22 54	2.55005	0.24965	116 48 35	2.12501		
116	26 50	2.61065	0.25261	117 43 42	2.18163		
120	30 35	2.67046	0.25550	118 36 2	2.23779		

TABLE IX. *Abscissa and Ordinate of a Parabola at different Angles from the Vertex.*

Angle	Abscissa.	Ordinate.	Angle	Abscissa.	Ordinate.
10°	0.00765	0.17498	130°	4.59891	4.28901
20	0.03109	0.35265	140	7.54863	5.49495
30	0.07180	0.53590	150	13.92821	7.46410
40	0.13247	0.72794	160	32.16343	11.34254
50	0.21744	0.93261	170	130.64610	22.86011
60	0.33333	1.15470	175	524.58248	45.80752
70	0.49029	1.40042	176	820.03500	57.27250
80	0.70409	1.67820	177	1458.35842	76.37693
90	1.00000	2.00000	178	3282.13970	114.57992
100	1.42028	2.38351	179	13130.55876	229.17730
110	2.03961	2.85630	179 $\frac{1}{2}$	52524.23496	458.36332
120	3.00000	3.46410	179 $\frac{3}{4}$	210098.93985	916.73103

TABLE X. 51

Hourly Motion of Comets.

Perih. Dist.	Parts of M. O.	Miles.
Comet 1680	.012952	997000
0.1	.003205	247000
0.2	.002267	175000
0.3	.001851	143000
0.4	.001603	123000
0.5	.001434	110000
0.6	.001309	101000
0.7	.001212	93000
0.8	.001133	87000
0.9	.001068	82000
1.0	.001014	78000
1.5	.000828	64000
2.0	.000717	55000
2.5	.000641	49000
3.0	.000585	45000
3.5	.000542	42000
4.0	.000507	39000
Time from Perih. to Lat. rect.		
Comet 1680	Dec. of Days.	d h ' "
0.052545	0	1 15 40
0.1	3.46635	3 11 11 32
0.2	9.80430	9 19 18 12
0.3	18.01165	18 0 16 46
0.4	27.73076	27 17 32 16
0.5	38.75490	38 18 7 4
0.6	50.94464	50 22 40 17
0.7	64.19757	64 4 44 30
0.8	78.43440	78 10 25 33
0.9	93.59129	93 14 11 27
1.0	109.61543	109 14 46 13
1.5	201.3764	201 9 2
2.0	310.0392	310 0 56
2.5	433.2929	433 7 2
3.0	569.5785	569 13 53
3.5	717.7507	717 18 1
4.0	876.9232	876 22 9

TABLE XI.

Apparent Motion of the Comet of 1682, at its next Return, whatever Month of the Year its Perihelion happens in.

Time.	Long.	Lat.	Curt. Diff.	Time.	Long.	Lat.	Curt. Diff.	Time.	Long.	Lat.	Curt. Diff.
Perihelion April 20.				Perihelion October 23.							
Apr. 20	♈ 1.8	N. 8.2	1.18	Sept. 3	♐ 29.2	N. 6.3	1.01	Mar. 1	♈ 9.5	S. 3.4	1.02
30	3.3	9.1	0.80	13	♑ 7.6	13.0	0.62	11	0.2	8.7	0.80
May 10	11.9	9.8	0.41	23	♒ 9.3	31.0	0.28	21	♈ 12.9	16.4	0.62
20	♑ 2.2	1.5	0.17	Oct. 3	♐ 6.0	28.7	0.34	31	♐ 13.3	24.2	0.54
30	♒ 26.5	S. 7.1	0.48	13	♑ 26.8	14.6	0.73	Apr. 10	♐ 13.0	25.6	0.63
June 9	♒ 6.7	8.1	0.85	23	♈ 0.2	8.7	1.12	20	♐ 24.9	22.5	0.85
								30	16.7	19.5	1.13
Perihelion May 21.				Perihelion November 22.				Perihelion February 19.			
May 11	♈ 23.2	N. 8.5	1.29	Sept. 13	♐ 27.7	N. 2.6	1.25	Nov. 1	♐ 15.7	S. 4.1	1.21
21	26.2	10.8	0.90	23	29.8	5.2	0.88	11	4.6	3.1	0.98
31	♈ 12.3	14.4	0.50	Oct. 3	♑ 1.9	12.6	0.50	21	♈ 18.6	1.3	0.83
June 10	♑ 15.1	12.1	0.32	13	12.	51.	0.11	Dec. 1	♈ 26.9	N. 1.0	0.78
20	♒ 28.3	0.4	0.60	15	♒ 7.	74.	0.04	11	8.0	3.2	0.86
30	♒ 10.8	S. 3.5	0.97	16	♐ 16.	78.	0.03	21	♈ 24.8	4.6	1.00
				23	♈ 23.	31.	0.28	Mar. 11	♐ 10.9	3.6	1.10
Perihelion June 21.				Nov. 2	25.6	15.8	0.66	21	4.8	0.4	0.83
June 11	♈ 15.9	N. 10.7	1.01	12	24.5	10.2	1.03	31	♈ 24.0	S. 6.3	0.54
21	♐ 1.2	15.3	0.62	Perihelion December 21.				Apr. 10	♈ 22.2	22.2	0.30
July 1	♑ 20.4	17.0	0.42	Oct. 2	♐ 26.7	N. 0.7	1.12	20	♐ 17.1	29.2	0.33
11	♒ 4.7	6.0	0.65	12	23.0	3.5	0.77	30	♐ 21.3	21.7	0.61
21	19.1	0.2	1.02	22	11.1	10.7	0.42	May 10	12.9	17.8	0.93
				Nov. 1	♈ 16.6	28.3	0.21	Perihelion March 20.			
Perihelion July 23.				11	♐ 12.2	20.2	0.39	Nov. 30	♈ 21.2	S. 3.3	1.13
July 3	♐ 2.6	N. 9.7	1.10	21	♈ 26.5	13.4	0.70	Dec. 10	7.2	2.7	1.09
13	16.0	15.1	0.80	Dec. 1	20.8	10.5	1.01	20	♈ 24.3	1.0	1.14
23	♑ 27.7	20.4	0.45	Feb. 19	♈ 16.4	S. 9.2	1.13	Mar. 30	♈ 6.5	N. 7.0	1.18
Aug. 2	♒ 15.9	11.1	0.56	Mar. 1	3.8	13.8	0.98	Apr. 9	3.9	4.7	0.76
12	♐ 1.5	3.9	1.03	11	♐ 19.0	19.1	0.88	19	♐ 29.0	0.8	0.40
				21	0.2	23.0	0.83	29	♈ 22.	S. 50.	0.05
Perihelion August 22.				31	♐ 12.4	23.8	0.91	30	♈ 11.	62.	0.04
July 23	♐ 12.9	N. 8.8	1.13	Perihelion January 20.				May 9	♐ 10.8	20.1	0.33
Aug. 2	26.3	13.9	0.75	Oct. 12	♐ 24.3	S. 2.3	1.31	19	8.6	14.8	0.70
12	♒ 0.7	22.8	0.45	22	18.7	1.1	0.99	29	9.0	13.8	1.07
22	♒ 26.0	16.5	0.58	Nov. 1	6.8	N. 1.2	0.71				
Sept. 1	♐ 15.1	7.8	0.95	11	♈ 6.4	5.2	0.51				
				21	♈ 4.2	9.2	0.50				
Perihelion September 23.				Dec. 1	♈ 8.8	9.5	0.66				
Aug. 14	♐ 23.9	N. 7.4	1.09	11	♐ 25.0	9.2	0.89				
24	♑ 4.5	13.2	0.71	21	16.9	8.5	1.11				
Sept. 3	♒ 8.3	25.4	0.39								
13	♐ 12.3	22.0	0.47								
23	♐ 4.1	11.4	0.85								

T A B L E XII.

Place where the Comet of 1682 may be first expected to appear any Month.

	Longitude.	Latitude.	Dist. from Perihelion.	Bearing and Time.
January	Scarce to be seen.			
February	End Retrog. between 30° and 15° of ♈	Small increasing S.	7 weeks after its perih.	{ Low S. E. morning.
March	Beginning — 30 and 15 of ♈	Small N. or S.	{ A month after perih.	
	End — 30 and 0 of ♈	Small N. decreasing	{ 2 or 3 weeks after.	{ Low E. morning.
April	Beginning — 15 and 0 of ♈	Small N. decreasing		
	End Stationary 10 ♈ and 20 ♈	Small N.	{ About the perihelion.	
May	Beginning — Middle of ♈	{ N.	{ 1, 2, or 3 weeks before.	{ E. morning. N. E. morning.
June	End Direct — Beginning of ♈			
	Beginning — End of ♈	{ N. increasing	{ 2, 3, 4, or 5 weeks.	{ Low N. E. morning.
July	Beginning — Beginning of ♈			
	End — Middle of ♈	{ Small increasing N.	{ 5, 6, 7, or 8 weeks.	{ Rifles N. E. midnight.
August	Beginning — End of ♈			
September	End of 25 and 30 of ♈	Small S. or N.	{ 2 months before.	{ — N. E. at 11.
October	End of Retrograde — End of ♈	Small S.		
November	Beginning — Beginning of ♈	Small S.	{ 2 or 3 months.	{ — N. E. at 7.
	End — 5 ♈ and 20 ♈	Small S.		
	Beginning — Beginning of ♈	Small S. or N.	{ 3 months before per.	{ Low E. evening.
December	End — Begin. of ♈, End of ♈	Small S. or N.		
	Beginning of ♈	Very faint.	{ 11, 12, 13, or 14 weeks.	{ S. E. evening.

E R R A T A.

Page	Line	for	read	Tab.	Col.	for	read
1	7	—	themselves	1	1718	6° 28' 50"	6° 28' 44"
2	12	—	{ in some measure	2	64° 15'	1.726681	1.726581
		—	{ astronomically	7	Line 7	18h 48'	16h 48'
10	Nº. 22	Col. 2	BDD'	10	0.4	27d 17h 32' 16"	27d 17h 32' 18"
24	Line 43	I nor can	nor can I	11	{ Perih. Mar. 20	0	0
					Line 9	10.8	10.8

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Corrections and Improvements in BARKER's *Discoveries concerning Comets*,
found out since it was published.

- P. 10, N^o 15 BEb=HAC
 31 BE'b'=H'A'C'
 32 SE'I'=suppl.H'A'C'+suppl.SE'B
 41 for $\chi\psi\omega$, read $\chi\psi\omega \times \sqrt{2}$.
 82 HC'—Hc'=cp = Cp.
 83 for C'g read C'G
 51 Tab. VIII. 4. for 12° 26' 46'' read 12° 25' 5''
 for 0.59022 read 0.59018.

If in Page 9 and 10, N^o 5, 6, and 37, are not correct enough, (as in a very oblique Comet perhaps they may not) SL N^o 6, and SR N^o 37, may be found more correctly thus:

Take SB, S μ and B γ as found by a former construction or calculation; and omitting N^o 5 and 6, say,

Former SB : former S μ :: present SB : present S μ

Former B γ : present B γ :: former $\mu\nu$: present $\mu\nu$. ν is the point in the orbit perpendicularly over μ , and found as below.

Then S μ : $\mu\nu$:: R : tang. $\mu S\nu$

cof. $\mu S\nu$: R :: S μ + $\frac{1}{3}$ I μ : SL

To find $\mu\nu$, omit N^o 37, and having by N^o 39 found KM=AC, and KN=CN—AM.

In the triangle SB μ' , from SB, BS μ' (=IS μ' —I'SE'—BSE') and S μ' B (=S μ' I' + I' λ' i') find B μ' .

KM : KN :: B μ' : x $\therefore$ B γ —x = $\mu\nu$.

Then S μ' : $\mu\nu$:: R : tang $\mu S\nu$.

cof. $\mu S\nu$: R :: S μ' : SR.

