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#### Contributors

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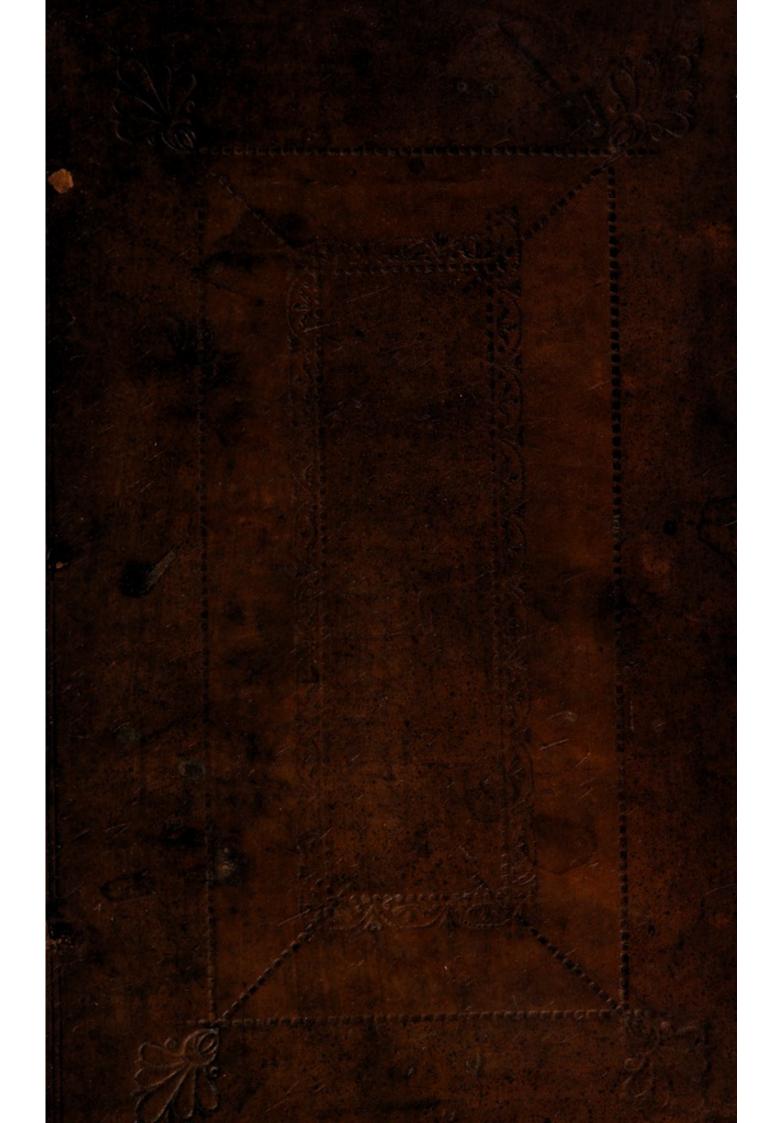
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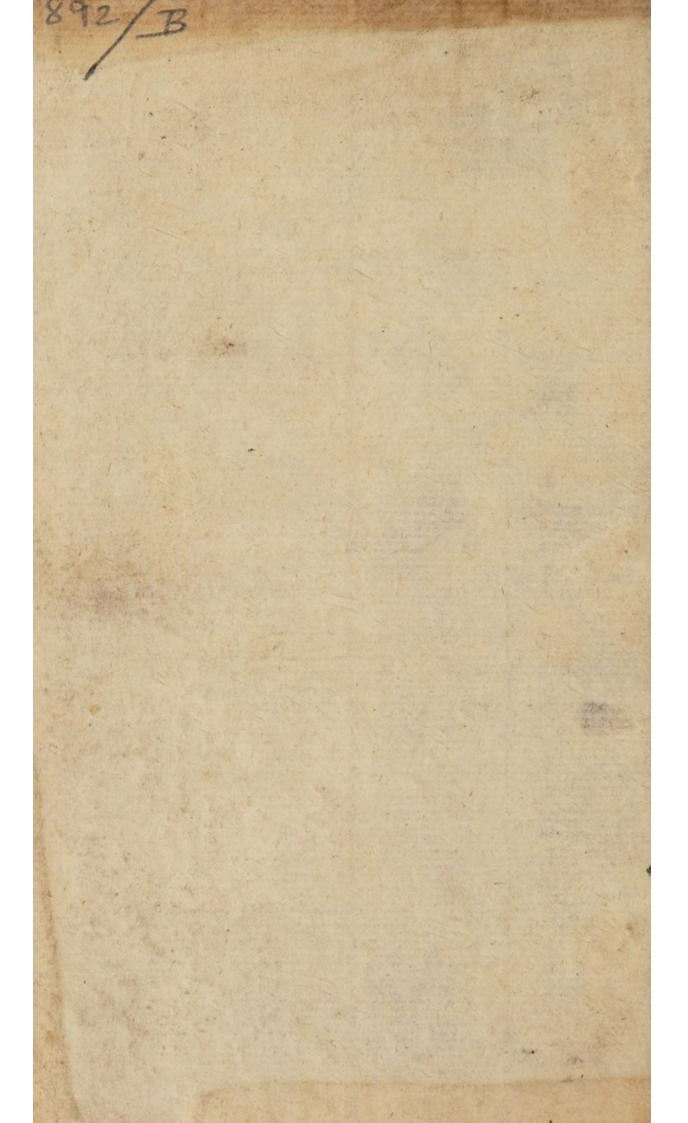
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A MATHEMATICAL

820

## MANUAL:

## OR,

## Delightful Associate.

#### CONTAINING,

- I. A Defcription and Use of the GELESTIAL GLOBE: How to know the Stars in each Constellation, and their Magnitude; also their Latitude, Longitude, Right Ascension, Declination, Semi-diurnal Ark, Rising, Southing, Setting, Altitude, Azimuth, Distances, Ge. The Sun's Place, his Rising and Setting, Length of the Day and Night, Ge. Also Dialling by this Globe.
- II. Twelve Problems relating chiefly to the MOON: And a truer Way than has been given to find EASTER, Grc. The Hour of the Night by the Moon shining on a Sun-Dial, Grc.
- III. A Defcription and Use of the TERRESTRIAL GLOBE, as to Climates, Zones, Shadows, Inhabitants, Latitude and Longitude of Places: And a large TABLE; shewing where all the most remarkable Places in the World may be placed on Dials; and the Bearing and Distance of such Places from London.
- IV. A full Description and Use of all Kinds of MAPS: With a copious TABLE of the Latitude, Longitude, and Situation of the chief Cities on Earth: And many other curious Matters.
- . V. The Original of the Lines in a SECток defcrib'd; with the full Use of that Instrument in Trigonometry, Ge. in an Easy Natural Method.
  - VI. How to make a Line of NUMBERS, or LOGARITHMS, to any Length, and the full Use in all Parts of Arithmetic.
  - VII. MYSTERIOUS CURIOSITIES in Numbers: Or, Numerical NOVELTIES. In Twenty-five PROPOSITIONS, mostly New, and very Eafy and Delightful.

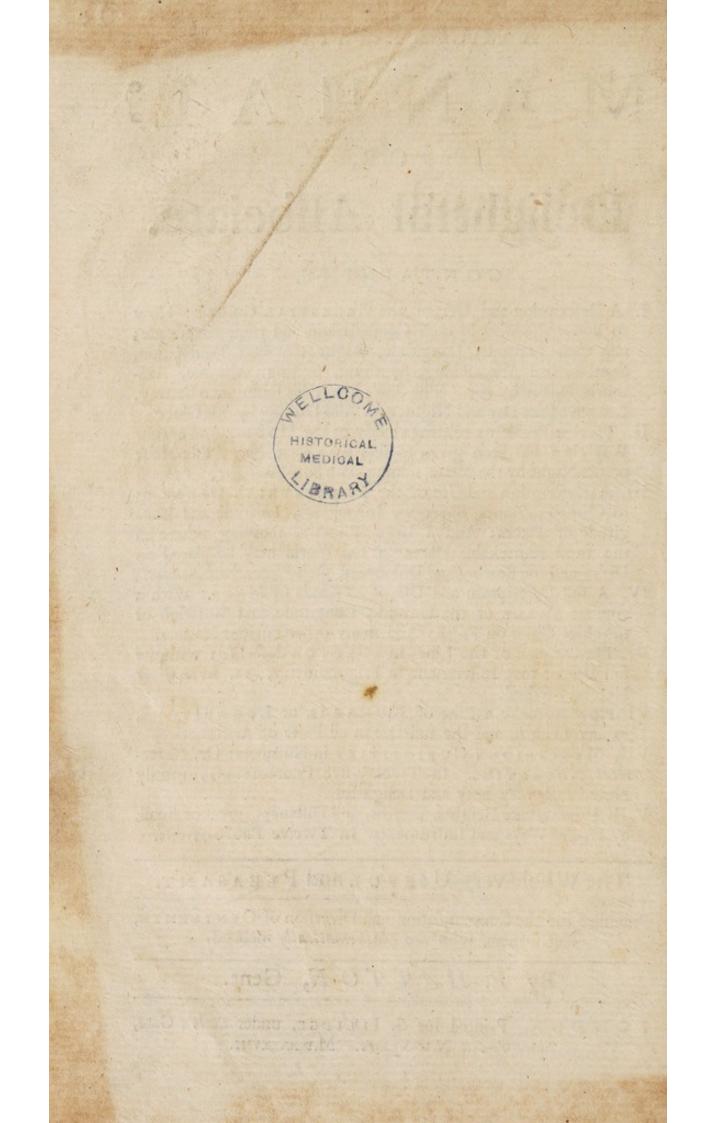
VIII. How to take Heights, Depths, and Diftances, great or finall, by feveral Ways and Inftruments. In Twelve Propositions.

### The Whole very USEFUL and PLEASANT.

Published for the Contemplation and Diversion of GENTLEMEN, and Others, who are Mathematically inclined.

## By E. HATTON, Gent.

LONDON, Printed for S. ILLIDGE, under Serle's Gate, Lincoln's-Inn New-Square. M.DCC.XXVIII.



## TO Thomas Frewen, Efq; Of Brickwall in the County of Sussex; ASA

Judicious Favourer of LEARNING,

#### AND

Encourager of Useful and Commendable SCIENCES;

#### THIS

TREATISE, With Sincere Respect, And Profound Deference, Is DEDICATED;

> By his Moft Obedient Humble Servant,

> > E. HATTON.

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Of Brickwall in the County

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Hample Saram,



# READER.



HIS is now the Twelfth Treatife (mostly on the Subject of Numbers) wherewith I have endeavoured to

be of fome Service, and to oblige Mankind; to whom I must acknowledge my Gratitude justly due for the kind Acceptance I have met with; near Forty-thousand having been fold off, besides some Thousands also of the four Books by me perused and corrected. And as this will be the last that I intend to write, so I am not without Hopes it will meet with the like Reception, so many of the Contents being Copious and New, as well as Pleasant and Delightful, handled in an Easy and vi To the READER. and Familiar Way, Intelligible by a mean Capacity.

But the' the Publick in general bath favoured me, yet I have not had the Good-Fortune to find such Encouragement from those who should (I think, without a fond Partiality to Self) have shewed some Regard to my Labours, which have chiefly been calculated and adapted to the promoting the Science of Trade and Commerce. But, alas ! there are too many who are so indolent and little concern'd about those Matters (which, next to Religion itself, do claim our greatest Respect) Humour and Pleasure having so much the Ascendant, that the Author of a Play or whimfical Novel Shall Sooner meet with the Reward of confiderable Business, or an Employment of Profit, than he who hath spent more than half an Age of Sixty-three Years in Studies which tend very greatly to the Knowledge and Increase of Trade and Merchandizing,

## To the READER.

chandizing, the principal Instruments of the Nation's Grandeur and Riches. However, as it is our Duty, so is it our Wisdom and Interest, to be submissive to the Allotment of Providence, that if we fall short of receiving from Men what we with good Reason presume we deferve; we may be so far resigned, as not impiously to defire more than we have.

But fince I am upon this Topic, I hope to be excused, if I relate one Instance of Service more immediately to the Government; which was this : In the Year 1697, I compos'd Tables for the Use of the Collectors and Receivers of the Capitation Tax; which contained not only all Duties payable by the feveral Classes or Degrees of People, but also the precise Weight, in the old Clipt Money, that would answer those Payments, all in so plain a Method, that the Collectors, both in the City and Country, declared they did not know what to do without them; and mine zvere

## viii To the READER.

were the only Tables for that necessary Use that were made publick.

As to this Book, I have only farther to fay in general, That it contains many Things more than the Title intimateth; and I doubt not but will every Way answer the Expectation of a judicious and impartial Reader: and for the critical Carper Zoilus, 'tis not neceffary to bespeak his Candour.

Our Globes and Maps, and most other Instruments, only having Degrees, we are forced in most Cases to guess at the Minutes : And therefore, as the precise Truth in them is not very necessary; so it cannot be expected that the Minutes should be better exhibited, setting aside Trigonometrical Calculations, which would differ from the Use of Instruments, in the very Subject, and of the Art's Denomination; one being the Use of Globes, Maps, &c. and the other plain or spherical Trigonometry.

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wherein the Poles are fixed, and which dott

## A MATHEMATICAL MANUAL.

## this or the Terrebriel Globe, for both which one Quadrant. If A.T. O HIS Kent, and 'tis

Bitude, which is on Deere

The Description and Use of the CELESTIAL GLOBE.



HE Globe is every way round ; the Ambits, or Circumferences, being equal, which way foever you take them, in the Middle of the Globe.

the Meridian, that the Polo is its

II. The Parts of the Globe are, 1. The Ball or Body of the Globe whereon the Circles of the Sphere are drawn, and the Stars are painted in B feveral

2

feveral Constellations. 2. The Axis, which is fupposed to extend through the Middle of the Globe, the Ends of which are the North and South Poles of the World. 3. The brazen Meridian, which encompasseth the Ball, and wherein the Poles are fixed, and which doth reft on a Pedestal under the Ball ; which Meridian is to be moved fo as to bring the Poles nearer to, or farther from, the Horizon. 4. The Horizon is, as it were, the Frame wherein the Globe is fixed, and which the Meridian croffes at right Angles; of which more below. 5. The Quadrant of Altitude, which is 90 Degrees, marked out upon a thin Piece of Brafs, that will comply fo as to measure any Distance on this or the Terrestrial Globe, for both which one Quadrant of Altitude is fufficient, and 'tis made to fcrew on the Meridian, and upon a Rivet to turn round any way. 6. The Hour-Circle, which is divided into twice twelve Hours, for Morning and Afternoon : It is fixed fo to the Meridian, that the Pole is its Center ; whereon is put, 7. The Index, fo contrived as to turn round with the Ball, and yet is not fo fast but that it may be turned and fet to any Hour. It is put upon the Pole, or End of the Axis of the Globe.

III. The Circles defcribed on the Celestial Globe are these; fix Great, and four Small. A Great Circle

Circle is one that divideth the Globe into two equal Parts : As,

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1. The Equinoffial, which extends round the Globe in the middle Way between the two Poles of the World, and 'tis divided into 360 equal Parts, beginning at the Place where it is interfected by the Ecliptic, and by one of the Colures. From this Circle the Declination of the Sun and Stars is reckoned in the Meridian Northward and Southward; and alfo their right Afcenfion is computed upon this Circle from the first Point of Aries. And when the Sun comes to this Circle (which it does twice in the Year, about the 10th of March, and 12th of September) it makes equal Days and Nights: Whence its Name.

2. The Meridian here most observable, is that of Brass, wherein the Poles are fixed : For there are fuppos'd innumerable Meridians; but the Brazen one is of chief Use, because any Star or Sun's Place can be brought to it, and the Altitudes, Right Afcenfion, Declination, Ec. are thereby difcover'd. It is divided into 4 Nineties, or 4 times 90 Degrees ; and a Degree must therefore be the 360th Part of any Circle. When the Sun comes to the Meridian of any Place, it is there 12 of the Clock at Noon ; and again 12, or Midnight, 12 Hours afterwards. And there are Meridians drawn B 2 through 0113

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through every 30 Degrees of the Equinoctial (or 12 in all;) fo that 15 Degrees being equal to 1 Hour, 30 are 2 Hours; and confequently the 12 Meridians, each 2 Hours of the Equinoctial, make 24 Hours. And in that Proportion of 15 Degrees of Motion being 1 Hour of Time, 1 Degree is 4 Minutes of Time.

3. The Ecliptic Line is the third Great Circle. It is divided into 12 equal Parts, anfwering to the 12 Signs of the Zodiac, and each Sign into 30° (or Degrees) marked thus:

Aries, mark'd	r	Libra, Libra,	1
Taurus,	V	Scorpio,	m
Gemini,	n	Sagittarius,	Z
Cancer,	5	Capricorn,	vs
Leo,	A	Aquarius,	
Virgo,	m	Pisces,	ж

The Circles that divide the Ecliptic into 12 equal Parts at right Angles, are Great Circles, called Circles of Longitude; becaufe from them to the first Point of Aries is reckoned the Longitude of the Stars: as the Latitude is upon those Circles (or others made by the Quadrant of Altitude) from the Ecliptic to the Star and Pole of the Ecliptic, as appears hereafter.

4. The Horizon, which is that Circle which divides the visible from the invisible Parts of the

the Heavens. It is the Frame of the Globe, whereon are fhewn the 12 Signs, painted between the Degrees in each Sign. Secondly, You have the Days in every Month anfwering to those Signs, and the Letters for every Day, by Way of Calendar, according to the Julian (or common) Account; and farther outward are the like, according to the Roman, or New, or Gregorian Account; and farther outward are the 32 Points of the Compass, each Point being  $11\frac{1}{4}$  Degrees. This Circle, or Horizon, is used in finding the Sun's Rifing, Amplitude, Azimuth, &c. as in the following Problems appears.

5. The Equinoctial Colure, which is a great Circle paffing through the Poles of the World, and cutting the Equinoctial at right Angles in the first Point of the two Equinoctial Signs Aries and Libra; whence, and toward each Pole, this Circle is divided into four ninety Degrees.

6. The Solftitial Colure is another great Circle, paffing through the Poles of the World, and croffes both the Equinoctial and Ecliptic at right Angles, in the first Points of Cancer and Capricorn; to which when the Sun comes, begins Summer and Winter; as it does by the other Colure diftinguish Spring and Autumn.

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7. The lesser Circles are, first, The Tropic of Cancer, the Boundary of the Sun's Course, and 23°. 30'. from the Equinoctial Northward. As,

8. The Tropic of Capricorn is the Boundary of the Sun's Courfe, and is 23°. 30'. from the Equinoctial Southward.

## 9. The Artic ; and,

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10. The Antartic Circles. The first 23°. 30'. from the North Pole, and the second as much from the South Pole: Of which more in the Description and Use of the Terrestrial Globe.

finding

IV. The Points to be observed are, 1. The North Pole; 2. The South Pole; each 90° from the Equinoctial. 3. The Poles of the Ecliptic, which are each 90 Degrees from it, and 23°. 30'. from the Poles of the World.
4. The Zenith is the Point directly over your Head wherefoever you be. 5. The Nadir, or Point under your Feet. Thefe are the Poles of the Horizon, being 90 Degrees from it.

The Politions of the Globe are 3, viz.

other Colare diffinguish Spring and Autumn.

tions, or those to near the North Pole as to be

1. Direct, when the Poles are in the Horizon; as it is to those who live under the Equinoctial.

2. Parallel Sphere is when the Poles are in the Zenith and Nadir, and the Equinoctial is coincident with the Horizon; as it is to those that live under the Poles.

3. The Oblique Sphere is when the Poles are elevated or depressed fome Number of Degrees between the Horizon and the Zenith or Nadir, and the Equinoctial and Parallels of Declination do cut the Horizon at Oblique Angles.

The Stars put on the Globe are to be known alfo, by the Eye, in the Heavens, by their Magnitudes and Declination, or Diftance North or South from the Equinoctial, or from the Pole. The Magnitudes are diftinguished on the Globe thus: Stars of

Magn.	. Rays,	Magn.	10 8 5	Rays.
I	have 16	-4	have	6
2	Ior offer.	ns 5 b	e To I	5
3	8	6	S miles	. 3

They are alfo painted in feveral Conftellations (or Figures of Men, Women, Birds, Beafts, Fish, &c.) The Northern Conftella-B 4 tions,

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tions, or those so near the North Pole as to be visible in our Horizon, are,

Urfa Minor, with the Pole Star at the End of his Tail, of the fecond Magnitude.

Ursa Major, having 4 in his Body, and 3 in his Tail, of the fecond Magnitude.

Cor Caroli, under the Tail of the Great Bear, 1 of the fecond Magnitude.

And there are more having Stars of Note, viz.

Cephus (a King of Ethiopia, Father of Andromeda;) 3 of 3d, and 4 of the 6th Magn.

Draco, (the Dragon) next the Little Bear, 7 of the 3d.

Bootes is the next; 6 of 3d, and 1 of the 1st.

Corona Septent. (or North Crown;) 1 of 2d, and 5 of 4th.

Lyra, the Harp; I of Ist, and 2 of 3d.

Hercules; 8 of 3d.

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Coma Berenice, (the Hair of Ptolomy's Daughter;) I of 3d, and 10 leffer.

Cygnus, (the Swan) South from Draco; 1 of 1st, 1 of 2d, and 6 of 3d.

Cassiopea (Cephus's Daughter) and her Chair; 5 of 3d, and 1 of 4th.

Perfeus,

Perseus, (Son of Jupiter, that cut off Medusa's Head;) 1 of 2d, and 6 of 3d.

Andromeda, with her Chain; 3 of 2d, and 3 of 3d.

Auriga, and his Goat, Hircus; 1 of 1st, and 2 of 2d.

Pegasus, (or the Flying-Horse of Perseus;) 3 of 2d, and 4 of 3d.

Aquila, (the Eagle volant) South from Lyra; 1 of 2d, and 5 of the 3d.

The Dolphin, between Pegasus and the Eagle; 3 of 3d.

The Triangle, Southward from Andromeda's Foot; 3 of 4th.

The following are in the twelve Signs.

Right Thumb, and 1 on his Right Ence,

Aries, (the Ram) between his Horns; 1 of 3d.

Taurus, (the Bull) his Eye, or rather his Forehead, Aldebaran; 1 of 1st. Alfo in the Bull are the Pleïades, or 7 Stars; 1 of 4th, and one of 5th.

Gemini, (the Twins) Castor and Pollux; 3 of 2d, and 4 of 3d.

Cancer, (the Crabfish ;) 1 of 3d, and 2 of 4th.

Leo.

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Leo, (the Lion,) his Heart and Tail; 2 of the 1st; also 2 of the 2d.

## Virgo's Spike; 1 of 1st, 3 of 3d.

Libra, (the Ballance,) the South-Westerly I of the 1st; North-Easterly I of the 2d; and the Center of Gravity in the Beam, (Zubeneneschemati;) I of the 2d.

Scorpio's Heart, 1 of 1st. Near his Tail, 1 of the 2d, and 2 of the 3d.

Sagittarius, (the Bowman;) one in his Left-Hand, and 2 in that Arm, of 3d.

Capricornus, (the Sea-Goat;) 2 by his Horns, and 2 in his Tail, of 3d.

Aquarius, I in his Left Shoulder, I on his Right Thumb, and I on his Right Knee, of the 3d.

Pisces, 7 of the 5th Magnitude.

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Fomabant, under Aquarius's Water-pot, and about 8°, when on the Meridian, above the South Horizon; 1 of the 1st.

Cetus, the Whale; I in his Mouth, of the 2d; 4 in his Head, and 5 in his Body, of the 3d; and I near his Belly and Tail, of the 2d.

inito in (the Grainfill ) a of 3d, and a of 4th.

Orion; on his Left Thigh, 1 of the 1st; 1 on his Right, and 1 on his Left Shoulder, and 3 in the Belt, of the 2d; 2 in his Skirt, and 1 on his Left Side, of the 3d.

- Lepus, (the Hare;) 4 on his Left Side, of the 3d; and 5 more of the 4th and 5th.
- Canis Major (the Greater Dog, Syrius;) 1 on his under Jaw, of the 1st; 1 on his Right Foot, of the 2d; and 5 more, of the 3d.
- Canicula (the Little Dog, or Procyon;) I on his Left Thigh, of the 2d; and I in his Neck, of the 3d.
- Hydra's Heart, (Alphard;) 1 of the 1st; and in his Body, 5 of 3d.
- Corvus (the Greedy Cormorant) near Hydra's Tail; 2 of the 3d.
- Antinous (or the Youth of Bithynia in Natolia, or Lesser Afia;) 5 of the 3d, under Aquila.

These make 40 Constellations, having about 850 Stars

11.5 P 100 15 23

And in the Southern Part, or below the Horizon, there are the *Peacock*, the *Centaur*, *Ca*melion, &c. about 18 Conftellations (invifible to us) having about 500 Stars.

So much for the DESCRIPTION.

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The Use of the CELESTIAL GLOBE.

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To Rectify the GLOBE.

thead; and y more of the ath and yels.

and I on his Left Side, of the ad.

FIX the Pole of the World, which is in the Brass Meridian, so many Degrees above the Horizon, as is the Latitude of the Place, and fcrew the Quadrant of Altitude in the Zenith, or the Complement of the Latitude, which for the Lat. of London, 51.32, is 38°. 28'. Neck, of the gd.

## PROBLEM I.

The Day of the Month given to find the Sun's Place in the Ecliptic.

THIS is done by the Table delineated on the Frame of the Globe, or Horizon : Finding there the Day of the Month, you have right against it the Sun's Place. Thus,

January 1. the Sun's Place is :	21 46	rs
April 1.	22 20	A.
May 28 Moitallation 81 100		
hour soo Stars 4. vol		
margaren all de a	1	

PRO-

## the Deprees then cut by the Meridian in the PROB. II.

## The Sun's Place in the Ecliptic given to find the Day of the Month.

LOOK in the Divisions next the Ball, or fecond from it, for the Sun's Place, and in the third divided Circle from the Ball you have the Day of the Month according to our Julian Account: Some Equip in the Equip of a sink.

The Sun being in	The Day of the Month is
° 21 46 V3	Jan. 1.
17 00 II	May 28, &c.

crees, equal to the Antwer

#### PROB. III.

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To find the Sun's Right Ascension by having the Day of the Month given.

THE Right Afcenfion of the Sun is an Arch of the Equinoctial, which comes to the Meridian with the Degree and Minute of the Sun's Place in the Ecliptic, reckon'd from the ist Point of Aries.

So that having rectify'd the Globe as above, find the Sun's Place in the Ecliptic; as by Prob. I. Then

13 I nen bring the Sun's Place to the Meridian, and

14

Then bring the Sun's Place to the Meridian, and the Degrees then cut by the Meridian in the Equinoctial from the first Point of Aries, is the Answer.

## EXAMPLE.

## What is the Right Ascension of the Sun, May 28?

THE Sun's Place found, as before, is 17 Degrees of Gemini, which bring to the Meridian, and there will then be from the first Point of Aries to the Meridian in the Equinoctial 76 Degrees, equal to the Answer. In like manner,

estione sas fo	Sun's	Place.	i til S	Right A	cension.	
•	0	'		0	•	
Jan. I.	21	46 0	f vs	293	10	
Apr. 1.	22	20	r	20	40	
Nov. 4.	22	46	m	230	30	
Dec. 25.	14	50	vs	286	00	

#### PROB. IV.

To find the Sun's Right Scention

To find the Sun's Declination.

THE Day of the Month given, find the Sun's Place for that Day, as before, then bring it to the Meridian, and the Degrees there between the Sun's Place and the Equinoctial is the Declination required. Thus,

the Sun's Place in the Ecliptic; as by Prob. I.

riori T

fan.

is brought t sles.	Sun's	Place.	stic.	Dec	Place moitheni
Jan. I.		46 VS	Sink		36 South.
Apr. 1.0	22	20 Y	0	8	20 N.
Nov. 4.28	22	46 m	22	18	35 S.
Dec. 25.	14	50 VS	22	22	30 S.A.
255 30		46 III	22		Nov.4.

## PROB. V.

SES

## To find the Sun's Amplitude any Day.

THE Amplitude is an Arch of the Horizon, contained between the Sun's Place in the Ecliptic and the East or West Points of the Horizon: So bring the Sun's Place to the Horizon, and you see the Answer. So

Auril Millinale	Sun's	Place.		From t	the East.
	0	1.1	0	0	
Jan 1.	21	46 VS	Ampl.=	37	00 S.
Apr. I.	22	20 Y	22	13	30 N.
Nov. 4.	22	46 页	22	31	00 \$.
Dec. 25.	14	50 VS	41	39	50 S.

#### PROB. VI.

## To find the Oblique Afcension of the Sun;

WHICH is an Arch of the Equinoctial, included between the East Point of the Horizon and the first Point of Aries, after the Sun's Place

Dec. 25.

I

Place in the Ecliptic for that Day is brought to the Horizon : As by these Examples.

i so south	12	Sun's	Place.	21	Oblique Asce	nsion:
Solv.	8	•	N'02	22.	0.T.1	N. S.
Jan. I.	8i	21	46 VS	22	324	00
Apr. I.	22	22	20 Y	14	IO A	10
Nov. 4.		22	46 m		255	30
Dec. 25.		14	50 VS	P 1	318	10

PROB. VII.

To find the Sun's Meridian Altitude any Day.

THIS is an Arch of the Meridian between the Sun's Place and the Horizon. As for Example,

Fruit the East.	Sun':	Sun's Place.		Merid. Altitude.	
and the	0		0	0	1
Jan. 1.	= 21	46 VS	.12	16	30
Apr. 1.	22	20 Y	22	46	30
Nov. 4.	22	46 m		19	30
Dec. 25.	14	50 VS	i.	16	00

### PROB. VIII.

To find the Time of the Sun's Rising or Setting any Day.

PUT the Sun's Place in the Ecliptic to the Meridian, then fet the Index of the Hour-Circle to

to the upper 12; then turn the Sun's Place to the East Part of the Horizon; and then the Index will cut the Time of the Sun's Rising in the faid Hour-Circle.

EXAMPLE.

-21	op-osu	n's Plac	e.	o- Sun	riseth.
-91	007-56			20 h.S	.20.35
Jan. 1	. 21	46	vs	08	00
Apr. 1.	22	20	p	9 o5	21
Nov. 4.	the 22	46	m	50 Time	40
Dec. 25	. 14	, 50	vs	08	02

Note, That having the Time of the Sun's Rifing, you have alfo the Time of the Sun's Setting, by deducting from 12: And the Length of the Day is double the Time at which the Sun fets; and the Length of the Night is double the Time of Sunrifing. Thus,

move the Ball and Quadrant of Altitude on the

Welt Side of the Meridian, till the Degree of

the opposite Sine fall just under 18 Degrees of

the Quadrant of Alcitude; then the Index will

DIFA

out the Time of Day-break in the Hour-Fan. I.

17

lace the	Sun rifes.	Sun fets:	Length of Day.	Length of Night.
DI SUINI	h. *	b. 1	b. •	<i>b.</i> •
Jan. 1.	8-00	4-00	08-00	16-00
Apr. 1.	5-21	6-39	13-18	10-42
Nov. 4.	7-40	4-20	08-40	15-20
Dec.25.	8-02	3-58	07-56	16-04

PROB. IX.

To find the Time of Day-Break, and End of Twy-light. This is when the Sun is eighteen Degrees below the Horizon, before its Rising, and after its Setting.

R ECTIFY the Globe as to Latitude, and the Quadrant of Altitude fcrew'd in the Zenith; then (for Day-Break) first find the Sun's Place in the Ecliptic, and bring that to the Meridian, and the Hour Index to 12; then bring the Degree of the opposite Sine to the Meridian, and move the Ball and Quadrant of Altitude on the West Side of the Meridian, till the Degree of the opposite Sine fall just under 18 Degrees of the Quadrant of Altitude; then the Index will cut the Time of Day-break in the Hour-Circle.

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And for the End of Twylight (or the Light of the Sun after its Setting) deduct the Time of Day-break from 12 Hours. Thus,

Sun's Place.	Day breaks.	Troyl. ends.
i o	Ъ. '	b. •
Jan. 1. 21-46 VS	5-40	6-20
Apr. 1. 22-20 Y	3-09	8-51
Nov. 4. 22-46 m	5-38	6-22
Dec. 25. 14-50 VS	5-48	6-12

63

- 13

Note, The opposite Signs are thus :

Aries,	Libra,
Taurus,	Scorpio,
Gemini,	Sagittarius,
Cancer,	Capricorn,
Leon que po	Aquarius,
Virgo, a compo	Pisces.

10.10 . IO- 80 4. DL

C 2 PROB.

## And for the End B. B. P. R. O. B. X. inte Light of the Sun after X. B. O. S. C. the Time of

To find the Sun's Altitude at any Time of the Day, the Sun's Place and Time of Day given.

HAVING brought the Sun's Place in the Ecliptic to the Meridian, and put the Hour to 12 a-Clock; turn the Globe till the Hour's Index points to the Hour of the Day given; then lay the Quadrant of Altitude on the Sun's Place, and it will cut the Altitude.

## EXAMPLE. SIT

What is the Altitude of the Sun on the Days and Hours following?

Sun's Place.	Time of Day.	Alt. sought.
0 '	<i>b.</i> '	• •
Jan. 1. 21-46 VS	<i>b.</i> 02—30 p.m.	09-30
Apr. 1. 22-20 V	04—30 p. m.	21-00
Nov. 4. 22-46 m	09—30 a.m.	12-30
Dec. 25. 14-50 VS	10—30 a.m.	13-00

PROB

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when the data

## PROB. XI.

Quadrant meet, and full on the Sun's Place;

To find the Sun's Azimuth (or what Point of the Compass it Shines from) at any Altitude.

TURN the Globe to the Weftward if Afternoon, or to the Eaftward if Morning, till the Sun's Place lies just under the Sun's Altitude on the Quadrant of Altitude, which will then cut the Azimuth in the Horizon.

Sun's Place.	Altitude.	Azimuth from South,
0 1	o 1	0 1
21-46 VS	09—30 p.m.	34-30 S.W.byS.near
22-20 r	21—00 p.m.	76-00 W. by S.
22-46页	12—30 a.m.	36-30 S.E. byS near
14-50 VS	13-00a.m.	21-20 S. S. E.

## PROB, XII.

To find the Hour of the Day, having the Sun's Place and Altitude given.

BRING the Sun's Place to the Meridian, and put the Index of the Hour-Circle to 12; then turn the Globe (Eastward if before Noon, or Westward if after) till the Altitude on the C 3 Quadrant

Quadrant meet, and fall on the Sun's Place; when the Index will point to the Hour in the Circle upon the Pole. Thus,

Sun's Place.	Altitude.	Hour of the Day.
• •	0 1	tiendo.
21-46 VS	0930 p. m.	02-30
22-20 Y	21—00 p.m.	04-30
14-50 VS	13—00 a.m.	10-30

#### PROB. XIII.

## To find the Length of the longest Day in any Latitude.

RECTIFY the Globe to the Latitude, fuppofe 51.32; Secondly, Bring the Solftitial Colure to the Meridian; Thirdly, Put the Hour-Index to 12; Fourthly, Bring the Interfection of the Colure, with the Tropic of *Cancer*, to the Horizon; and then the Index will cut 8<sup>h</sup> 15'; which doubled is  $16^{h} 30' =$ the longest Day. And the like by the Tropic of *Capricorn* gives  $3\frac{3}{4}$ <sup>h</sup>; which doubled, gives  $7\frac{1}{2}$ <sup>h</sup>, the shortest Day.

and put the Index of the Hour-Circle to 12;

oz una the Globe ( Bakward if before Noon,

or Weftward if after) all the Alticude on the

BRING the Sails Place to th

So also in the Latitude of 40°, of 30°, or 20°, the longest and shortest Days are as follow:

	The longest Day is	The Shortest Day is
0	b. '	b. •
40	15-00	09-30
30	14-16	10-30
20	13-30	11-00

## PROB. XIV.

XAMPET

To find the Difference in Time contained in the fame Number of Days in different Parts of the Tear.

FIND the Sun's Place, and then the right Afcenfion, and take their first and second Differences; and the last converted into Time, gives the Answer.

Note, 15 Degrees is 1 Hour, and 1 Degree = 4 Min.

Comene chae our suit doch ; that Sun, or

Mark in the Equinodial, will paid found to

laten to that fame Meridian, and confe-

C4 EXAMPLE

so, the longest and sorres Days are as follow :

Sun's Place. Right Afc. Difference. Diff. of Diff.

EXAMPLE II.

Sun's Place. Right Asc. Difference. Diff. of Diff.

 $Mar. I. 21-40 \neq 352-00 \\ 2I. 11-30 \gamma 10-30 \\ 10-30 \\ 10-30 \\ 21-40, or 15 \\ (time prope). \\ 21. 10-50 \\ 21. 10-50 \\ 281-30 \\ 22-10 \\ 22-10 \\ 21. 10-50 \\ 21. 10-50 \\ 281-30 \\ 22-10 \\ 21. 10-50 \\ 21$ 

Now the Reafon of the Difference is this: Suppose another Sun at no Degrees of the Equinoctial to commence its diurnal Rotation from the fame Meridian at the fame Moment that our Sun doth; that Sun, or Mark in the Equinoctial, will pass round to the fame Point again in twenty-four Hours: But the Sun itself will return fometimes later to that fame Meridian, and confequently

quently will make a longer Day than the true Day of twenty-four Hours, made by the Equinoctial, which is called the Civil Day, as that made by the Sun from fome Meridian to that Meridian again, is called the Natural Day.

art. of the Ecliptic which is

dia trip 1

P.ROB.

And this Difference between the Sun's Day and Equinoctial Day is caufed by the Obliquity of the Sun's Orbit ; the Sun's apparent Motion being flower when in his Apogæum, than in his Perigæum.

## PROB. XV.

## To find the Latitude of any Star.

THIS is the Arch of a great Circle which paffeth through the Poles of the Ecliptic and the Body of the Star, contained between the Ecliptic Line and the Center of the Star.

So to find the Latitude of Lyra; bring the Pole of the Ecliptic, which is next the Star, to the Meridian, and fcrew the Quadrant of Altitude just over it; whence laying it over the Star to the Ecliptic, the Distance from the Star to the Ecliptic is  $61^{\circ} 20'$  the Latitude.

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# PROB. XVI.

To find the Longitude of a Star.

THIS is that Part of the Ecliptic which is contained between the first Point of Aries and the Circle of Longitude which passeth from the Pole of the Ecliptic through the Center of the Star, and crosseth the Ecliptic. So to find the Longitude of Lyra (the Harp) the Quadrant of Altitude placed over the Pole of the Ecliptic to extend over the Star, will cut the Ecliptic in  $10^{\circ}$  of Capricorn, which is  $280^{\circ}$  from the first Point of Aries = to the Longitude requir'd.

#### PROB. XVII.

#### To find the Right Ascension of a Star.

BRING the Star to the Meridian, and that Circle will cut the Equinoctial in the right Afcension, or Distance from the first Point of Aries.

unto just over it; whence laving it over the

to the foliptic is fit an' the I suitede.

PROB.

# PROB. XVIII.

To find the Declination of a Star.

THIS is done by bringing the Star to the Meridian, and then the Degrees in that Circle between the Star and the Equinoctial, is the Declination North or South.

EXAMPLES of the four last Problems follow.

STARS.	La	t. 2	Longit.	Right Afc.	Decl. i	Mag.
	0	003	0 1	0 1	01	1. 17.
Lyra,	61	20	280 00	276 40	38 00 N	. I
Arcturus,	31	20	200 00	23 00	20 40	1
North Crown,	43	15	217 40	230 00	27 00	2
Pegafus's Pinion, or Marchab	18	30	349 45	342 00	13 20	2
The Tip of the Wing,	12	20	4 42	357 40	13 12	2
Antinous's Breaft,			296 30	293 45	00 00	3
Capella,	22	15	73 00	74 00	45 30	` <b>I</b>
Cygnus, near the Neck,	353	45	318 00	302 00	36 30	I
Hercules's Left Shoulder,	39	00	234 30	241 45	19 30	3

Note, Sometimes it happeneth that the Stars are opposite to the Pole of the Ecliptic, fo that you cannot take the Latitude or Longitude

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Longitude with the Quadrant of Altitude, as being hinder'd by the Pole of the World. In this Cafe you may measure with a Thread from the Pole of the Ecliptic; and in Cafe of Latitude, measure the Thread on the Quadrant of Altitude.

# PROB. XIX.

# To find the Time when any Star comes to the Meridian (or Culminateth.)

FIR ST, find the Sun's Place for the Day given; Secondly, Bring the Sun's Place in the Ecliptic to the Meridian; Thirdly, Put the Hour-Index to the upper 12; Fourthly, Turn the Globe about till the Star is under the Meridian; and then the Index will point at the Time required.

Thus for the Bull's-Eye will Culminate Jan. 1. 8<sup>h</sup> 50', p. m. So Syrius will be South Nov. 4. at 5'. paft 3 in the Morn. and Virgin's-Spike, April 1. 11<sup>h</sup> 55'.

.**B O A T** metimes it happeneth that the Stars are opposite to the Pole of the Ecliptic, fo that you cannot take the Latitude or Longitude

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# Sant emologia P R O B. XX. EUITIEA XH

To find the Semi-diurnal Arch of any Star ;

WHICH is the Difference in Time between its Rifing or Setting, and its being on the Meridian: For which, bring the Star to the Meridian; Secondly, The Hour-Index to 12; Thirdly, Turn the Globe till the Star come to the Horizon; and then the Hour-Index will shew the Answer: As in the Examples following.

#### PROB. XXI.

00 11 00 8

7 00

0 20 2.377

3 00

-30 A 2 21

#### To find the Time of the Rifing of any Star;

YOU have nothing to do but fubtract the Semi-diurnal Arch from the Time that the Star is South.

#### PROB. XXII.

ine) are not put down, they are the fame

ing the Southing of the Stars, i.e. fabiract

if chere be a Necessity) and the Remainder

converted into Time, frews the Star's

To find the Time that any Star Setteth.

ADD the Semi-diurnal Arch to the Time it is South, and the Sum is the Answer.

EXAMPLES

and Shere :	13.65	Gerenal An	le Semi-u	To had 1
For Dec. 25.	Semi- diurn. Arch.	Rifing.	Southing.	Setting, or under the Pole.
Manal	160	D ONHIN	ho and	Typeen its R
Near and un-	A State of the second	- Ch.	All and a state	6
dertheMouth	- 5 50	7 10p.m.	1 00 m.	6 50 m. 3
of Hydra	)	To allow	States R	B. Same Star
Hydra's Heart	5 30	8 45	2 15	7 45 1
Lion's Heart	7 15	7 35	2 50	10 05 I
Lion's Tail	7 30	9 00	4 30	12 00 I
Charles'sheart		5 35	5 35	5 35p.m. 2
Urla Major,	75 44	an all	· nour	Barry the 1
the End of	>12 00	6 34	6 34	6 34 2
his Tail	(		- 54	lowing.
Arcturns, skirt	5	and the second second	The states	
of Bootes	\$ 8 00	11 00	7 00	300
North. Crown	1 0 .0	VI AT C	8 20	5 08 2
	the state of the s	11 32	A CONTRACTOR OF STREET, ST.	
Bull's-Eye	7 25	Contraction of the second s	9 20 p.m.	
Goat, Capella	12 00	a service de la constante de la	10 00	10 00 I
Harp, Lyra	11 15	12 08	11 23 m.	10 38 p.m. 1
Orion's left Th.	5 15	4 45 p.m.	10 00 p.m.	3 15 m. 1
Pollux Neck	900	3 25	12 25 m.	925 2

# EXAMPLES of these four last Problems take as follow.

Note, Where p. m. (Afternoon,) or m. (Morning) are not put down, they are the fame with the last above.

Semi-diamal Arch from the Time that the Se

Note, 2dly, That there is another Way of finding the Southing of the Stars, i.e. fubtract the Right Afcenfion of the Sun from the Right Afcenfion of the Star (adding 360°. if there be a Neceffity) and the Remainder converted into Time, fhews the Star's Southing.

EXA M-

#### EXAMPLE.

e. as the Equinoctial, from the first Point

When will Arcturus come to the Meridian, or South, the 25th Day of December?

Right Afcenfion 3213, or -14-12To which add 360, or -24-00Sum 38-12The Right Afcenfion of the 319-12Sun deduct = -12

The Remainder is — 19—00

Out of which take 12, and the Remainder is equal to 7 a-Clock; as in the Table last above, which is the Answer. And so of any other Star's Southing.

#### PROB. XXIII.

To find the Distance of two Stars.

TAKE the Quadrant of Altitude, and with that measure the Distance; and if it exceeds 90 Degrees, measure the rest by the Quadrant of Altitude, or the Degrees of any great Circle,

# 32 A Mathematical MANUAL. Circle, as the Equinoctial, from the first Point of Aries.

# EXAMPLE.

THUS between the Harp and Arcturus is  $57^{\circ}$ . 40'. and between the Virgin's Spike and Aldebaran (or Bull's Eye) is = 133 Degrees.

#### PROB. XXIV.

\$ 213, 01 mm 1 4-12

To find what Day of the Year any Star will be upon the South Part of the Meridian at 12 a-Clock at Night.

BRING the Star to the Meridian; then fee what Degree of a Sign is cut by the Meridian in the Ecliptic; Thirdly, Look in the Horizon what Day of the Month stands against that Degree of that Sign: Which is the Anfwer. Thus,

PROB XXIII

ATAX Bothe Ougdrant of Altin

reads no Degrees, moosine the raft by the

The

Place in the South at 12 Mag. Ecliptic. at night. The bright Star un-7 der Ursa Minor's 217 20 m Oct. 30. 2 Neck, Hercules's Head (Nas Algiethi Arace) \$15 30 2 Nov. 25. Draco, near his Eye, 26 40 ? Dec. 7. (Ceginus) \_\_\_\_ } 8 00 m Oct. 20. 3 Lion's Back, -- 13 00 mg Aug. 26. 2 Auriga's Right Shoul- 25 00 II Jun. 5. Perseus's Right Side 317 00 & Apr. 27. 2 Whale's Mouth, 13 30 8 Apr. 23. 2 Andromeda's Head, 28 00 × Mar. 7. 2 Cephus's Right Shoul-30 30 Jan. 25. 3 Andromeda's Chain End, ---Brightest in Coma Be- 3 30 = Sept. 16. 3 D PROB.

Place in the

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#### PROB. XXV.

# To find the Amplitude of any Star;

WHICH is the Number of Degrees in the Horizon that a Star rifeth or fets from the Eaft or West Points towards the North or South : Bring the Star to the Horizon, and it will shew the Answer.

'Thus Fomabant rifes 58°. from the East Southward, and fets 58°. from the West Southward.

#### PROB. XXVI.

To find how long any Star Shines above the Horizon.

BRING the Star to the Eaft Part of the Horizon; Secondly, Put the Index to 12; Thirdly, Turn the Globe Westward, till the Star comes to the Horizon Westward; and, Fourthly, Look at the Index; which will shew the Answer.

EXAMPLES of the two last Propositions.

being given, to find	Time it is a- bove the Horizon.	Ampl. of Rijing.	Mag.
Fomahant, near Pisces (Austrinus'sMouth)	b. ' } 5 20	58 00 S.	I u <b>đ</b> i
Antinous his Right Knee,	310 40	14 30 S.	3
Eagle's Tail, next the End,	<b>}14</b> 30	22 30 N.	3
Middle of Libra (the Ballance)	10 40	14 30 S.	2
Canicula (biggeft in the Little Dog)	13 00	10 00 N.	2
Castor's Forehead,		59 30 N.	
Leo's Neck,	6. 6. 4. 1. 2. 2	34 20 N.	
Andromeda's Hip (Mi- rach)		63 10 N.	

D2 PROB.

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# PROB. XXVII.

# The Altitude of any Star being given, to find its Azimuth.

BRING the Degrees of the Star's Altititude (in the Quadrant of Altitude) to lie juft over the Center of the Star, and then the graduated Edge will cut the Azimuth in the Horizon. So

Altitude.	Azimuth from the Eaft.	Mag.
Aldebaron (or South) or Right Eye of 51 30 the Bull)	66 oo S.	I
Orion's Right Shoul- der (Bed Algense) }33 40	36 45 S.	2
Middle in Ursa Major's }45 00 Tail,	39 30 N.	2
Cassiopea's Right Arm-}48 30 pit (Scheder)	34 20N.	3
Aries his Head, be- tween the Horns, 32 20	06 30 S.	3
Capricorn, (or Sea- Goat) between the 20 20 Horns,	70 40 S. PR	

# PROB. XXVIII.

The Altitude of any Star, and the Sun's Place in the Ecliptic given, to find the Hour of the Night.

BRING the Sun's Place to the Meridian (found as by Prob. I.) Secondly, Put the Hour-Index to 12 at Noon; Thirdly, Turn the Globe and Quadrant till the Altitude of the Star (upon the Quadrant of Altitude) fall just upon the Center of the Star; and then the Hour-Index will shew the Time of the Night.

Examples may be thefe that follow :

Cilla Major ; 1991	Mag.	Stars Alt.	Sun's Place.	Hour of the Night.	Days of Month.
Great Dog's Right Foot, Lepus's Left Side, Canicula's Neck, Virgo's Neck, Aquila's Neck,	3 3 3	15 30 20 00 10 30	2 M 25 M 15 Z	4 45 m. 1 15 m. 11 12 p.m. 1 30 m. 6 30 p.m.	22 Sept. 14 Oct. 6 Nov. 26 Nov. 16 Dec.
Aquarius's Water-pot [or Thumb,] Nova Stella, in the Whale's Neck, Loweft of Orion's Girdle,	3	15 30 12 40	25 VS	6 30 p.m. 9 30 p.m.	4 Jan. 19 Jan,
Loweft in Urfa Ma- jor's Side, next the Middle of his Back,	100	1.	2 X	9 40 p.m. 1 00 m.	10 Feb. 1 Mar

**D** 3

Knee ; Ligecules his Leg.

PRQB.

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#### PROB. XXIX.

To find the Acronical Rifing of any Star.

A STAR rifeth fo, when it doth rife at the Time when the Sun fetteth, and doth confequently fhew when it may be the proper Time of obferving any Star, fo as to know its Altitude, Azimuth, Hour of the Night, thereby, &c. Thus:

STARS Rifing, and a little above the Horizon, at Sun-fet, viz.

lay be thele that follow :

Jan. 10. Orion's Right and Left Shoulder, Belt, and Right Thigh; Caftor and Pollux; and Urfa Major, except its Tail.

Feb. 10. Four in the Hare; the Great and Little Dogs; Hydra's Heart; Lion's Neck, Heart, and Back; Cor Caroli; Coma Berenices; Bootes Head and Left Shoulder.

Mar. 10. Three in the Ship; Lion's Tail; Virgo's Neck; Bootes' Right Shoulder and Knee; Hercules his Leg.

PROB.

Apr.

Apr. 10. Corvus 2; Virgin's Spike; Arcturus; Northern Crown; three in Hercules his Body, and one in each Arm near the Body; Lyra; and four bright ones in the Swan.

- May 10. The bright one in the Middle, and others about Libra's Ballance; three near Scorpio's Tail; Hercules his Head; Swan's Head; and two bright ones in the Eagle's Tail; Andromeda's Chain End.
- June 10. Scorpio's Heart; a bright one in the Eagle's Neck; five in the Dolphin; and four in Andromeda's chained Hand.

three near and under

- July 10. Two in Seorpio's Neck; three in Sagittarius his Left Hand, and three near his Neck; fix bright ones in and near Antinous his Body.
- Aug. 10. Two Horns of Capricorn; Perfeus his Right and Left Shoulder, his Side and Arm; Pegafus his Wing and Scheat, or the bright one near his Tail; Andromeda's Head, Hip, and Foot.

D 4

Sept.

- Sept. 10. 'Two in Capricorn's Tail; Aquarius his Left Shoulder; that near his Right Shoulder, and Right Hand; Ram's Head; Perfeus his Foot; Hircus, the Goat; and Auriga's Right Shoulder.
- Nov. 10. Pisces Austrinus; Aquarius's Knee; two in the Whale's Tail; the bright one near and above his Eye; the Pleiades in the Bull.
- Dec. 10. The bright Star in the Whale's Mouth; three near and under his Eye; Aldebaron; and Auriga's Right Leg.

Note, That the Circumpolar Stars (or those whose Declination is more than the Complement of the Latitude) never rise nor set, but are distinguished by being faid to be under the Pole, and above the Pole.

The foregoing *Table* is made by bringing the Place of the Sun in the Ecliptic to the Horizon in the West, and then the Stars mention'd will be in or a little above the Horizon in the East.

#### PROB.

#### PROB. XXX.

AND becaufe I would endeavour to help the Reader to know the Stars, I will give him the following Table of the circumpolar Stars of moft Note, (with their Declination) the Time when they are Eaftward from the North Part of the Meridian at 45 Degrees of Altitude, and are afcending toward the South Part, or Zenith, at Sun-fet. Degrees 90 lefs, the Latitude 51.32. refts the Compl. Lat. 38°. 28'.

1 66 00 3	Dec	lin.	Mag.	Alt.45°.at Sun-fet.
Swan, near the Neck,	38	30	3	July 14.
Ditto, near the Tail,	43	40	2	Ditto.
Ditto, in the Right Wing,	43	50	3	Ditto.
Hercules's Foot,	46	00	3	May 24.
Bootes's Head,	41	00	3	Apr. 13.
Left Shoulder,	38	40	3	Ditto.
Cor Caroli, a const	40	00	2	Apr. 3.
Auriga's Right Shoulder,	44	50	001 <b>2</b> 21	Jan. 15.
His beloved Hircus,	45	40	I	Jan. 8.
Perseus's Right Knee,	38	30	3	Dec. 30.
Arvenlement of the Al		6.2.	This	Per-

and the second	Declin.	Mag.	Alt. 45°. at Sun-fet.
Perseus's Right Side,	49 00	9 2	Dec. 15.
His Right Arm,	51 00	3	Dec. 8.
His Left Arm,	43 26	3	Dec. 14.
Andromeda's Foot, 3 (Alamac)	40 30	2	Dec. 5.
End of her Chain,	43 20	3	Sept. 18.
Cephus's Right Shoulder,	61 00	3	July 2.
His Belt,	68 4.0	3	June 22.
Two in Draco's Head,	51 00	3	May 18.
Four in his Body, 58 to	66 00	3	Apr. 25.
Three in Urfa Major's } Tail, 51 to	57 30	2	Mar. 28.
Four in his Left Side, 3	63 30	2 2	Feb. 5.
Five in Caffiopea, 54. 30 }	62 00	3	Oct. 15.
Urfa Minor, under his } Neck,	75 00	ead, cif Si	Mar, 25.
One under the last,	73 00	3 .	Apr. 5.
Two in his Body, and t			
76 to 86; Magn. 4,		and the second	A ATA WALL ALL THE ARE TOR
End of his Tail, or H Magn. 2; Sept. 12. a	ole-Star	Dec	1.87 27 ;
-101 -101 - 10 - 10 - 10 - 10 - 10 - 10	. 31.30.	1166.	То

the Azimuth, in

To make the foregoing *Table*; lay 45 Degrees of the Quadrant of Altitude upon the Center of the Star; then fee what Degrees of the Ecliptic are cut by the Horizon Weftward, and find those Degrees in the Scale of the Horizon; and right against that stands the Day of the Month.

Note, That the End of Twylight, or Time of the Stars appearing, is found for the refpective Days in the laft *Table* by the Rules under *Prob.* IX. foregoing: Tho' Stars of the first, second and third Magnitude appear when the Sun is 12, 13, and 14 Degrees below the Horizon; and those of the fourth, fifth, and fixth Magnitude, when the Sun is 15, 16, and 17 Degrees below the Horizon.

#### PROB. XXXI.

which it doth in 40°. 30'. = the Latitude

To find the Latitude of a Place when at Sea, by a Star, having its Altitude, Azimuth, and Declination given.

FIRST, Put the Degrees of the Altitude on the Brafs Meridian to the Horizon; Secondly, Screw the Quadrant of Altitude upon the Complement of the Altitude; Thirdly, Bring the

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the Quadrant of Altitude to the Azimuth in the Horizon from the North Point thereo', and there keep it; Fourthly, Turn the Globe till the Degrees of Declination, reckoned upon the Equinoctial Colure from the Equinoctial, cut the Quadrant of Altitude, which will be in the Latitude required.

#### EXAMPLE.

Andromeda's Head, Altitude =  $55^{\circ}$ ; to which I elevate the Pole above the Horizon; Secondly, I forew the Quadrant of Altitude to the Complement thereof,  $35^{\circ}$ ; Thirdly, I put the Quadrant of Altitude to the Azimuth in the Horizon, *i.e.* to  $100^{\circ}$ . 30'. from the North; Fourthly, I turn the Globe till  $27^{\circ} =$  (the Declination of Andromeda's Head) upon the Equinoctial Colure cut the Quadrant of Altitude, which it doth in  $40^{\circ}$ . 30'. = the Latitude fought.

So likewife the Latitude is found by these Stars:

complement of the Almende; 'I hirdly, Bring

ST. Put the Demress of the Althaderon

Meridian to the Horizon ; Secondly,

Quadrant of Altitude upon the

Procyon

olds I .	Altit.	Azim.	Declin.	Latit.
	0 1	0 1	0 1	0 1
Protyon, or Little }	35 00	98 30	05 45	20 30
Arcturus,	45 30	112 00	20 40	45 30
Bull's Eye, or Forehead, (Al- debaron)	61 00	135 00	15 30	37 30

The Latitude is most eafily found by the Terrestrial Globe for any Place at Land; but the Rule above is for those at Sea.

#### PROB. XXXII.

A most easy and natural Way of finding the Hour Distances on an Horizontal Dial for any Latitude.

HAVING rectify'd the Globe to the Latitude, bring 15°. of the Equinoctial to the Meridian, and then the Equinoctial Colure will cut the Horizon in  $11^{\circ}$ . 51'. = the Diftance of the Hours of 11 and 1 from the Meridian.

In like manner, if you bring 30°, 45°, 60°, and 75°. of the Equinoctial to the Meridian, then the Equinoctial Colure will cut refpectively in the Horizon, the Hour Distances from the Meridian (or 12 a-Clock Hour-Line) of the Dial

# 46 *A Mathematical* MANUAL. Dial 11°. 51'.; 24°. 19'.; 38°. 4'.; 53°. 35'.; and 71°. 6'.; as in the following Table.

Degrees of Equin. at Merid.	Hour Distances cut by the Colure.	For the Hours of
15	11-51	11 & 1
30 21	24-19	10 & 2
found Poy	38-04	9 8 3
at 1661 30	53-35	8 & 4
75	71-06	7 & 5
90 .II	2 90-00 0	6 & 6

the

Sud

And the Hour-Diftances of 5 and 4 in the Morning, and 7 and 8 in the Afternoon are the fame as those before the Hour-Line of and next to that of 6. And the Height of the Stile, or Gnomen, or Cock, is the Latitude of the Place; and fo your Dial is finished.

the Horison in 11º. cr. == the Diffance of

. In like manner, if you bring go', 45°, 60°,

and yr. of the Equipodial to the Meridian.

Meridiad (or 12 a-Clock Mour-Line) of the

A make cals and wateral Way of finding that

B O R Q Coinsolial Colure will cut respectively

# PROB. XXXIII.

before and a after 6 in the Morning,

# To find the Hour-Distances upon the Erect Direct South Dial.

THIS is done as the laft : But only elevate the Globe to 38.28, &c. the Complement of the Latitude, inftead of the Latitude 51.32 : For, bringing 15°. of the Equinoctial to the Meridian, the faid Colure will cut in the Horizon 90°. 27'.; and fo of the reft. And the Angle of the Stile must be 38°. 28'. See the following Table.

Degrees of Equin. at Merid.	Hour-Distances cut by the Colure.	For the Hours of
15	09-27	11 & 1
30	19-45	10 & 2
45	31-53	9 & 3
60	47-09	8 & 4
75	66-42	7 8 5
90	90-90	6 8 6

Note, The crect direct North Dial hath only the 6 a-Clock Hour-Lines, and the 2 before

Ā

48

laft . Rur only elevate

before and 2 after 6 in the Morning, and the fame in the Afternoon, of like Diftance with the laft Dial. And the Stile is the fame, only placed above the Hour-Line of 6, with the Angle downward to the Center of the Dial.

But the best Way of making East, and West, and Decliners, not being by the Globe, I shall fay no farther of them in this Place, but proceed.

son 90. 27, ; and 15 of the reft. And the

Angle of thateile must be 38°. 28'. See the



3.3 00-00

vino dud bill drok North Did bate od I'

that 6 a-Clock Alour-Dines, and the a

belore

SECT.



# SECT. II.

Aftronomical PROBLEMS, relating to the MOON chiefly; containing RULES for Computing Time: Of Use to those who would make Almanacks for any Year to come In a very easy Method, and more Various and New than any one has done before.

#### PROB. I.

To find the Golden Number for any Year (or Cycle of the Moon.



HIS is a Cycle, or Revolution of nineteen Years; in which Time, the Fulls, Changes, and Eclipfes of the

Moon were reckoned to return in the fame Order, or near it.

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#### RULE.

Add 1 to the Year of our Lord, and divide the Sum by 19, and the Remainder is the Golden Number : And if nothing remain, that Year is the last, or 19th of the Cycle.

Note, The Reafon you add 1, is, becaufe 1 Year of the Cycle was gone when the Year of our Lord commenced.

## bas LEAM EXAMPLE.

zoila zoould make Almanacks for any

What is the Golden Number the Year 1726? the Year I wrote this Part.

1726

more 1

any lear (or

RUE E.

19)=1727(90 17 refts. The Anfwer.

#### PROB. II.

To find the Cycle of the Sun.

THIS is a Revolution of 28 Years; in which Time the Leap Years and Dominical Letter come again in the fame Order.

#### RULE.

Add 9 to the Year of our Lord (because 9 Years of this Cycle was gone when the Year, or Æra, of our Saviour's Incarnation did begin) and divide the Sum by 28, and the Remainder is the Answer. Or if o remain, that Year is the last, or 28th, of the Cycle.

EXAMPLE.

found 17 ; as above.

To find the Cycle of the Sun for 1726.

1726 more 9 28)=1735(61 55 27 = the Anfwer.

## PROB. III.

To find the Epast for any Year.

THIS is the 11 Days Difference between the Solar Year of 365 Days, and the Lunar of 354.

#### RULE.

Divide the Golden Number by 3, add 10 times the Remainder to the Golden Number, and the Sum is the Epact.

E 2

EXAMPLE.

#### EXAMPLE.

What is the Epact for the Year of our Lord 1726?

See the Operation following.

The Golden Number for this Year 1726. is found 17; as above.

# 3)17(5

Multiply by 10

BEARPER.

52

20 more 17 is = 37, lefs 30, [refts 7 = the Anfwer.

Or thus: I multiply the Golden Number by 11, and divide the Product by 30, and the Remainder is 7, the Epact, as before.

# PROB. IV.

To find how many Years any Year is from Leap Year.

THE Romans called Leap Year Biffestile, because they put the odd Day, gained by four times fix Hours (the Year being 365 Days and 6 Hours) after the 6th of March, reckoning

# A Mathematical MANUAL. 53 koning that Day twice. But we place the Day after the 28th of February.

#### RULE.

Divide the Year by 4, what's left will be, For Leap Year 0; Years past, 1, 2, or 3.

EXAMPLE.

For,

6

12

refts 2, or the 2d after Leap Year.

PROB. V.

To find the Dominical (or Sunday) Letter.

# RULE.

Divide the Sum of the Year of our Lord; a 4th thereof and 4 by 7; fubtract what remains from 7; and that last Remainder is the Letter required: Reckoning I = A, 2 = B, 3 = C, 4 = D, 5 = E, 6 = F, and 7 = G.

lay, it is alfo. in trag. the Dominical

ANPLE,

54

JAO Y C

But we place the

#### EXAMPLE.

What is the Dominical Letter for the Tear 1726?

> 1726 = the Year. 431 = its 4th. 4 7)2161 = Sum (308 61 5 refts, and 7 lefs 5 = 2, or B.

But Note, That in Leap Year there are two Sunday-Letters ; the one found as above, used all the Year after St. Matthias's Day, February 24. to which Time, from the first of January, the next Letter following is inferted in the Calendar: as in the two laft Leap Years. The Dominical Letter for 1720. is found, by the Rule above, to be B, used from St. Matthias's Day to the End of the Year; and the Letter next in the Alphabet (or C) is used for the Sunday-Letter from the 1st of Fanuary to the 24th of February (or St. Matthias's Day.) So also in 1724. the Dominical Letter, found as above, is D; and from the ift of January to the 24th of February it

55 it is E. The Sunday-Letters being reckon'd backward always in this Cafe.

A Mathematical MANUAL.

Note alfo, That a 4th is added for the Leap Years; and 4, becaufe fo many of this Cycle of the Dominical Letter was gone when the Year of our Lord commenced.

#### PROB. VI.

auf Alignete cohen the Moon

To find the Moon's Age at any Time.

## -or snit shivib RULE.

and Add the Epact, the Day of the Month, and Months from March, together, (including March and the Month you reckon to) and the Sum is the Moon's Age. If that amount to 30 or 60, deduct them.

#### EXAMPLE.

I would know the Moon's Age the Day that I am writing this, which is August 30. 1727.

> 18 =the Epact. 6 = Months from March inclusive. 30 = Day of the Month.

54 Sum, lefs 30 == 24 from 30, the [Day, refts 6, the Age,

SOR OR

But Note, That from January the 1st to March the 1st, you must use the Epact for the Year next preceding.

#### PROB. VII.

To find the Hour and Minute when the Moon comes to the Meridian.

#### RULE.

Multiply the Age by 4, and divide the Product by 5, and the Quotient is the Hour, and the Remainder is fo many times 12 Minutes.

# EXAMPLE.

To know when the Moon comes to the South when it is fix Days old.

6 Multiply by 4 5)24(4 4 refts. 12 mult. 48 Minutes.

So 48 Minutes paft 4 is the Anfwer.

PROB.

57

orle bort

# PROB. VIII.

L'having found the Moon's Age, fup.

To find what Day of the Month Shrove-Sunday is, and consequently the Day of all the Moveable Feasts.

BY Shrovetide is meant Confession-Time. Shrove-Sunday in the Calendar is called Quinquagefima, as being fifty Days before Easter.

#### RULE.

Shrove-Sunday, upon which the reft depend, is always the first Sunday after the second Change of the Moon which happeneth after New-Tear's-Day. And if that Day of the fecond Change be Sunday (as it was Anno 1716, 1717, 1720, 1722, and 1726. then that Sunday is Shrove-Sunday.

#### EXAMPLE.

What Day of the Month was Shrove-Sunday in the Year 1725?

#### RULE.

S-19JTE

In this Cafe you must always use the Epact for the Year before, whereby, &c. as under Prob.

**Prob.** VI. having found the Moon's Age, fuppofe Feb. 15. to be 13 Days old, I run back and find the Day of the fecond Change was February the 2d; and February (as by the Rule in the next Problem) beginning with D, and the Dominical Letter for that Year (as by Prob. V.) being C; therefore D being the first, D is the eighth Day, and of Confequence C is the feventh of February; which being the first Sunday after the fecond Change, is Shrove-Sunday. From which the other Moveable Feasts are found thus:

#### Shrove-Sunday, being found as above, - Feb. 7.

Quadragesima, or first Sunday in Lent, Feb. 14. must be

Easter-Day, being seven Weeks after } Mar.28. Sbrove-Sunday, must be \_\_\_\_\_ } Mar.28.

Easter-Term, beginning a Fortnight } Apr. 14

Rogation-Sunday, being 5 Weeks after 3 May 2. Easter, \_\_\_\_\_

Ascension-Day, being 40 Days after } May 6. Easter, is

Easter-Term ends the Monday after 3 May 10.

unis Cafe you must always use the House,

Preb.

robar as and whereby deraday, Whitfunday,

Whitfunday, feven Weeks after Easter, 3 May 16.

Trinity-Sunday, the next after Whit-} May 23.

Trinity-Term begins Friday after Trinity-Sunday, and ends Wednesday a Fortnight afterward.

tor tor all

Fan.

And the Beginning and End of Hilary and Michaelmas Terms are fixed.

and his very eafy; and which

Note, That Septuagesima is a Fortnight, and Sexagesima a Week before Shrove-Sunday.

Advent-Sunday is always that next the 30th of November, whether before or after it.

Epiphany is reckon'd among the moveable Feafts; but it is always the 6th of January.

Note alfo, I have by me near twenty Years Almanacks, many of different Authors; and I find the Rule given by Mr. Cole in his English Distionary, to be erroneous, particularly for 1709. And the Rule given in the Common-Prayer-Book for finding Easter is wrong, for the following Years;

60

1708,	1709,	1711,
1712,	1715,	1718,
1721,	1722,	1724,
1725,	and	1727.

But my own Rule above, is right for all those Years; and I doubt not but that it will be found genuine for all Years past or to come, and 'tis very easy; and which therefore ought to be inserted in the Room of the false Rule.

# PROB. IX.

To find at any Time what Day of the Week any Day of the Month was, or will be, and the contrary.

# Rule.

To do this, it is neceffary to keep in mind the Letter that every Month (as touching the Days of the Week) begins with, and alfo the Dominical Letter for the Year. It may be of use as to the first, to get these two Lines by Heart.

or Fahrens wrone, for the following Years;

7an.

Jan. Feb. March, April, May, June,
A- Dieu, Dear George, Be Evermore
July, August, Sept. Oct. Novemb. Decemb.
Good Clement's Friend; A Dying Flower !

#### EXAMPLE.

I would know what Day of the Week the 24th of June (or Midsummer-Day) was in the Year 1664.

The Dominical Letter for that Year, found as by Prob. V. above, was B: Now by the faid Verfe, June beginning with E; I fay, E 1, E 8, E 15, E 22, F 23, G 24, A 25, B (which is the Lord's-Day) 26; therefore the 24, or Anfwer, is Friday: For if Sunday be 26, Saturday is 25, and Friday 24.

On the contrary, To find what Day of the Month the laft Friday in June 1664. was; First, B is found to be the Dominical Letter, as above, and E the first of the Month of June; I go forward till I come to Sunday, as  $e_1$ ,  $f_2$ ,  $g_3$ ,  $a_4$ , and  $b_5$ : Now Sunday being the 5th, Friday must be the 3d of June, and Friday 10, Friday 17, and Friday 24; fo the Answer is the 24th of June, and proves the above Example.

E G SI

#### PROB.

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N'IOTTOVE

# PROB. X.

To find by a Sun-dial the true Time of the Nig... by the Shade of the Moon.

# RULE.

By the Prob. above, &c. find when the Moon comes to the South; Secondly, If the Shadow falls in the Forenoon-hours, deduct what the Shadow wants of 12 from the Time that the Moon comes to the Meridian, and the Remainder is the Hour of the Night. Or if the Shade falls in the Afternoon-hours, add what it is paft 12 by the Dial, to the Time the Moon was South.

# EXAMPLE.

Suppose the Moon is South 24 Min. past 10 fome Day; I look at my Dial, and find it 11 a-Clock; therefore I take 1 from 10b. 24'. and the rest is 9b. 24'. the Hour required.

Or the fame Night, fuppofe I find the Hour on my Dial at 1, I may then conclude that the Moon is one Hour paft the Meridian; fo I add 1 to 10 b. 24'. and the Sum is 11 b. 24'. the true Time of the Night.

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## PROB. XI.

To find the Time of the Moon's Rifing and Setting.

I. IT must be observed, That at every New Moon the Sun and Moon are in or near the fame Degree of the fame Sign.

II. That a Sign is 30 Degrees of the Ecliptic, and each Degree 60 Minutes.

III. That the Characters of the 12 Signs, and the Time that the Sun enters into each, are,

T Aries, March 10.
♂ Taurus, April 10.
II Gemini, May 11.
♡ Cancer, June 11.
③ Cancer, June 11.
氧 Leo, July 13.
ℜ Virgo, Aug. 13.
☆ Libra, Sept. 13.
m Scorpio, Octob. 13.
求 Sagittarius, Nov. 12.

Capri-

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64.

VS Capricorn, Dec. 11. ≈ Aquarius, Jan. 10. ¥ Pisces, Feb. 8.

IV. That the Sun's Progrefs through these twelve Signs is once in twelve Months; but the Moon's in lefs than a Month.

V. That the daily Motion of the Moon is about 13 Degrees, 11 Minutes.

### III. That the Characters of the 12 Signs, and E X A M P L E.

## To know when the Moon did set the 14th Day of May, 1625.

By Prob.VI. the Moon changed May the 1ft, when the Sun's Place in the Ecliptic, by the Signs above, and reckoning every Day a Degree, was 21 Degrees of Taurus. From which Place to the 14th of May aforefaid (or when the Moon is thirteen Days old) I find by multiplying 13°. 11'. by the 13 Days,  $5^{fign.}$  21°. 23'.; which added to 21 Degrees of Taurus, gives 6' 12°. 23'. = the Moon's Place the 14th of May aforefaid: Which by the foregoing Account A Mathematical MANUAL. 65 Account of Signs, is 13 Degrees of the Sign Scorpio.

Then by confidering the Time the Sun hath Ingrefs into each Sign, it will appear that the Sun is in that Sign and Degree the 26th of October; and by the Globe, Quadrant, or Tables of the Sun's Rifing and Setting on that 26th of October, the Sun fets 4b. 36'.; which adding to the Moon's Southing the faid 14th of May, viz. to 10 b. 24'. [See Prob. VI, VII, and X.] gives the Sum 3 in the Morning (deducting 12 from the Sum) when the Moon fets the 14th Day of May, 1725. And if we deduct 4b. 36'. (when the Sun fets) from 10 b. 24'. when the Moon is South, there will remain 5b. 48'. when the Moon rifeth the faid 14th of May 1725. As by the following Operation:

Moon South, \_\_\_\_\_\_ b. Moon South, \_\_\_\_\_\_\_ 10-24Sun fets (add) \_\_\_\_\_\_\_ 04-36Sum (Moon fets) = \_\_\_\_\_\_\_ 03-00Or if you deduct the 2d Number from the 1ft, the Rem. gives the Moon's Rifing, \_\_\_\_\_\_ 05-48

F

PROB.

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#### PROB. XII.

## To find the Time of High Water at London-Bridge.

SOME give this RULE, To add three Hours to the Time of the Moon's Southing; but that will only hold exactly true for the Day of the New or Full Moon, when the Moon is always South at 12 a-Clock.

There are two fhort Tables which have been published two or three Years in Mr. Partridge's and Mr. Parker's Almanacks; but fince they have not shewed the making thereof, I shall omit them, and infert a Table of my own Contrivance, as follows; and shew the Calculation both of the Table of the Moon's Southing, and of the High Water at London-Bridge.

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# A TABLE of the MOON's Southing, and High-Water.

	Moon South.	High Water,
A Martin T. U.	h. Min.	h. Min.
A New or Full I	Moon, 0-00	3-00
I Day after,	0-48	3-48
-mail la notion	Aber.	4-21
3 —	- 2-05	4-45
	- 3-12	5-27
5	- 4-00	6-00
	- 4-48	6-33
7	- 5-36	7-06
At the first and feco	and ?	aga mico n
At the first and second quarters =	and { 6-00	07—30
1 Day after,	- 6-48	08-18
2 2	- 7-36	09-21
3	- 8-24	10-24
4	09-12	11-27
.5	10-00	12-30
6	- 10-48	01-33
7	11-36	02-36
1	F 2	CON-

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# CONSTRUCTION of the foregoing TABLE.

THE Moon coming to the Meridian every Day 48 Minutes later for a Week after the New and Full, and after the first and second Quarter, I therefore make the Table of her Southing by the continual Addition of Fortyeight Minutes.

Then for High Water, I add three Hours for one Day after Full or Change, to the Moon's Southing that Day; for two Days after, I add three Hours wanting a Quarter, to the Time the Moon is South that Day; for three Days, I add three Hours wanting two Quarters,  $\mathcal{E}c$ . adding a Quarter of an Hour lefs every Day to the Time the Moon is South that Day.

Secondly, For one Day after the first and fecond Quarters, I add 1 b. 30 min. to 6.48, the Time the Moon is on the Meridian that Day, &c. adding for every Day fifteen Minutes more than the Day before, from the first Day, gives the feveral Times of High Water in the Column next the Right Hand.

USE

## USE of the TABLE.

This is fo plain, that it needs no Example ; for it shews, that three Days after the New or Full Moon, it is South 24 Minutes after two ; and that it is High Water that Day 54 Minutes past 4.

So alfo, That two Days after the First or Second Quarters, the Moon is South 36 Minutes past 7, and that High Water is 21 Minutes past 9.

There is a pretty Mathematical Way contriv'd by Mr. Philips, published in Philosophical Transactions, N° 34 for finding the Tides, thus:

1. He divides the Periphery of a Circle into twelve equal Parts, or Hours, according to the Moon's Motion from New to Full.

2. He divides the Diameter of that Circle into 90 Parts, or Minutes, according to the Time of the Difference of Tides, after the Moon's Southing, between the New and Full Moon, and the First and Second Quarters, F 3 which

which is an Hour and a Half;) fo that 1, 2, 3, &c. are the Hours round the Ambit from the End of the Diameter next the Right Hand, where ftands 12; and at the End, toward the Left Hand, 6; and the Minutes from the Right Hand towards the Left of the Diameter, 1 to 90.

3. He makes Right Lines crofs the Diameter from the Hours above the Diameter to the Hours below; as from 10 to 2, 9 to 3, 11 to 1, &c.

since paft ", and that High Water is 21 Mis-

4. He reckons the Time of the Moon's coming to the South in the Circumference, and where the Perpendicular Lines cut the Diameter, it fhews what Minutes must be abated from the Time of High Water in the New and Full, or added for the Quarters to the Difference between the Moon's Southing and High Water, at the First and Second Quarters.

The Learned and most Celebrated Sir Ifaac Newton fully accounts for the Tides in his Theory thereof; and fays, That the Spring-Tides about the New and Full Moons are caused by the attractive Power of the Sun being added to that of the Moon.

Note;

Note, The Spring-Tides are three Days before, and ftill higher, three after the New and Full Moon; and all the other Tides about the Quadratures, &c. are called Neip-Tides.



F4 SECT,



# SECT. III.

The Description and Use of the TERRESTRIAL GLOBE.



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HIS is a Reprefentation of the Earth and Water on the Convexity of a Sphere or Globe, near unto which Figure the Terraqueous Bo-

dy is found to be.

II. 'The Earth is diftinguish'd by

I. Continents,

- 2. Islands,
- 3. Peninfula's,

4. Ithmus's,

that Mack of Land that m

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and not an Illand, is colled,

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4. Ifthmus's,

5. Promontories, and

6. Capes.

III. A Continent is where many Kingdoms and Territories of Princes are contiguous, without being feparated by an Ocean. According to which, Europe, Afia, and Africa are but one Continent, and America is another. The Ocean and Seas that furround them will be mention'd under the IXth and Xth Heads following.

IV. An Island is a Quantity of Land wholly environ'd by an Ocean, Sea, & c. as Great Britain and Ireland, bounded by the Western and Northern Oceans, the North Sea, the English Chanel, and St. George's Channel; also Cyprus, Candia, Sicily, Sardinia, Minorca, Majorca, and Tvica, all in the Mediterranean Sea. You have also Madagascar, the Ladrone, Philippian, Caribbee, and Hundreds of other Islands.

V. A Peninfula is almost an Island, being only joined to other Land in some small Part; the most confiderable of which is Africa, North and South America, Spain, Italy, &c. And that

## 74 *A Mathematical* MANUAL. that Neck of Land that makes it a *Peninfula*, and not an *Ifland*, is called,

#### VI. An Isthmus.

VII. A Promontory is a mountainous Part of Land which extends a confiderable Way into Sea; the Extremity of which is called

VIII. A Cape; as that of Good-Hope in the South of Africa, Comorin in the South of India, Cape Horn in Terra del Fuego, &c.

be mention'd under the IXth and Xth Heads

Candid, Sicily, Sardinia,

atthesis and milla

bee, and Hundreds of other

#### IX. The Water is diftinguish'd by

I. Oceans,

- 2. Gulphs,
- 3. Streights,
- 4. Lakes,
- 5. Bays, and
  - 6. Rivers.

X. An Ocean is a vaft Quantity of Water, which commonly boundeth fome of the four Quarters of the World; as the Western and Atlantic

I Peninfula is aimoft an 10and

Atlantic Oceans, which bound Europe and Africa towards the Weft; Northern and Southern Ocean, which is their Bounds toward the North and South; Indian Ocean, on the South of India; Eastern Ocean, to the East of China; and the Pacific Ocean, to the South West of America, &c.

XI. A Sea is commonly lefs than an Ocean, and hath Communication therewith; as the Mediterranean, which parts Europe from Africa; the Ethiopian Sea, South-Weft of Africa; the Baltic Sea, which parts Muscowy, Poland, and Germany from Sweden; the Red Sea, between Afia and Africa, &c.

XII. Gulph is Water shooting up into the Land from a Sea; as the Gulphs of Venice, Persia, Bassora, Finland, Ec.

XIII. A Streight is a narrow Paffage of Water between an Ocean and a Sea; as Gibraltar, Sundy, Baffora, and Babelmandel, or those into the Red-Sea, and many others. It makes a Sea differ from a Lake by Water, as an Ifthmus does a Peninfula from an Ifland by Land.

XIV. A Lake is every Way encompassed by Land, having no visible Communication with the

the Ocean, &c. The most confiderable are, the Caspian Sea, the Lake Leman (or of Geneva,) Niger in Africa, the White Lake in Russia, &c.

XV. A Bay is as if the Land received or embraced a confiderable Part of the Sea between its two Arms. The most confiderable Bays are those of Panama in the South-Sea, Biscay (made by the Coasts of France and Spain,) of Bothnia in the Baltic Sea, of Bengal in East India, of Nanking in China, &c.

XVI. A River commonly arifeth in fome mountainous Part of the Earth, and makes its Way (the greateft fome thousands of Miles) into an Ocean or Sea, &c. and in its Courfe many leffer Rivers fall in it. The most confiderable are, La Plata (which I take to be the biggeft in the World) in South America; Euphrates, a large River rifing near Mount Ararat in Armenia, and falls into the Gulph of Baffora, which parts Perfia and Arabia; Danaw, or Danube, which rifes at Furstenburg in the Circle of Suabia, and falls into the Euxine (or Black) Sea; Niger, in Africa, which rifes in the Lake Niger, and falls with the River Gambia into the Atlantic Ocean near Cape Verde; Nyle rifes in the Lake of Tzana in Abyfina in Africa, not far from the Red Sea, and with the great River Nubia (meeting at Tuo) falls into the STIT

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the Mediterranean Sea near Alexandria in Egypt; Wolga rifes near Kafan in Muscowy, and falls into the Caspian Sea near Astracan; Ganges rifes out of the Mount Caucasus near Siba, in the Mogul's Empire, and falls into the Bay of Bengal near Sundiva. I will add the River Thames, which, tho' short, is, like the People, profound, gentle, and filent; it carries perhaps more Ships and more Riches to that incomparable City, London, than can be faid of all these other Rivers put together to all Places.

XVII. The Length of these Rivers I have carefully measured thus :

and

- to a Sirei	English Miles.
La Plata -	
Euphrates .	910
Danube	1400
Niger	- moradi 2450 XID
Nyle	- 1470
Wolga —	- 980
Ganges -	- 940
Thames -	200 near.

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But Note, That the River La Plata is (near the Mouth, where it falls into the Southern Ocean) about 240 Miles broad.

XVIII. And by the foregoing Descriptions, it feems, That

### In Land

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In Water

A Continent may be compared to an Ocean.

A Large Empire — —	to a Sea.
A Peninsula — — —	to a Gulph.
An Isthmus — — —	to a Streight.
An Island —	to a Lake; and
A Promontory	to a Bay.

XIX. But there are many other very confiderable Rivers in the World, befides those mention'd above; as,

In EUROPE.

In FRANCE.

The Save, Morard, Mann, and the Pearl

The Seyne, the Loyre, the Roan, the Garone.

The Nieper or Berifflends, Wefel, and the

In the NETHERLANDS. The Maes, the Rhine, Scheld, and Senne.

In SPAIN. CO MIT

In SWEDEN.

Oskell.

The Duero and Ebro.

In PORTUGAL. The Tajo and Guadiano.

In ITALY.

In ASIA.

The Tyber, the Po, and the Arno.

In GERMANY.

The Weser, Elbe, (besides the Danube and fmall ones.)

3 he Zambre and the Zaire.

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#### In TURKEY in EUROPE.

The Save, Morava, Alauta, and the Pruth.

In, POLAND.

M.F.K.A.K.CE.

The Nieper or Borifthenes, Wesel, and the Bug.

In Muscovy.

The Oby, Tanais, Deesna, Dwina, and Oskoll.

The Duero and Ebro.

The Tajo and Gualiano.

In SWEDEN.

The Dalecarlus, Ellinan, Indais, E3c.

In ASIA.

In CHINA and ARABIA.

The Croceus, Kiang, and Tigris.

In AFRICA.

The Zambre and the Zaire.

In

# In AMERICA.

The River of Amazons, Oroonoko, and Canada.

XX. But I fhall give a more particular Account of the Parts of the Earth, and fhew what Countries are contained in each of the four Quarters of the World, with their chief Cities or Towns, and their Latitude and Longitude, when I come to fhew the Ufe of Maps; no Globes being large enough to have all the Places Situation diftinguistied : Tho' by them we can beft account for the Situation of the Inhabitants in general; which are,

1. Those that live in the same Latitude, and are of the same Side of the Equator, but are 180 Degrees Difference in Longitude, are called *Periesi*: As London being in the Latitude of 51.32. and Longitude 27°. if to 27 I add 180, it makes 207; so that London is in Periesi with that Place (which is Sea) that hath Latitude 51°. 32'. and Longitude 207°. So also

The Havana, in the Island Cuba in America, is Periesi with Bengal in the East Indies.

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Barbados, in the West Indies, is Periesi with Manila, one of the Philippine Islands.

2. Those that have the fame Number of Degrees of Latitude and Longitude, but are the one in North, the other South Latitude, are faid to be fituate in *Antiefi*: As London,  $51^{\circ}$ . 32'. Latitude, and  $27^{\circ}$ . Longitude, is *Antiefi* with a Place at Sea, which is about  $20^{\circ}$ . near S. W. from the Cape of Good-Hope. So also is

The Cape of Good-Hope with (near) Syracufa in Sicily, &c.

The Island Sancta Helena with (near) Godia in Negroland, Africa.

3. Those Inhabitants who have the fame Degrees of Latitude, but are the one South, the other North, and have 180 Degrees Difference of Longitude, are *Antipedes*: As London with a Place which is at Sea, 11°. 30'. from New Zealand Southward, which is about 44 Degrees Eastward from the Middle of New Holland, in the South Part of East India, in the Great Southern Ocean.

#### XXI. The

# XXI. The Circles and Parts of this GLOBE are,

The Meridian, Horizon, Equator, Ecliptic, the two Tropics, and two Polar (or Artic and Antartic) Circles; whose Descriptions and Distances from one another upon the Globe are as the Description of the Celestial Globe: Only it may here be farther added, That the Equinoctial on the Celestial, is called the Equator on the Terrestrial Globe. On which Globe are to be observed five Zones, the Dimensions whereos, with the Distinction of Inhabitants, and their Shadows, are thus:

Nº.	Names of theZones.	Extent	Dimensions.	Shad. caft at Noon.	Inhabitants called
I	Torrid	Betw. Tropics	° , 47 00	3 ways	Amphiscians.
2	Temperate	From the Tro- pics to the Po- lar Circles	43 oo each	1 way	Heteroscians;
2	Frigid	Fr. the Poles to the Polar Circles	23 30 each	all ways	Periscians,

XXII. From what is above, it will follow, That in the Latitude of 51°. 32'. North; for Example,

G 2

83

, thousand I quator,

The Diftance from the Equator to the Tropic Cancer =

From that Tropic 328 02 or 51 32 lefs 23 30 to the Zenith is

From the Zenith to the Artic Cir-1458 43 00 28 02 cle =

From the Artic Circle, to the 23 30 90 00 66 30Pole =

For Proof, the Sum is from the Pole 90 00 to the Equator

And from the Pole 366 30 or 90 00 lefs 23 30 to the Tropic is

 To the Zenith
 38 28 90 00
 51 32

 The Equator to \$51 32
 90 00
 38 28

 the Zenith
 \$51 32
 90 00
 38 28

To the Polar Circle 66 30 90 00 23 30

XXIII. The

XXIII. The Climates fhew the Variation of the Length of Days and Nights, and of the Rifing and Setting of the Stars; as the Zones do the Quality of the Air in refpect to Heat and Cold, and the Diftinction of the Inhabitants, and their Shadows. A Climate is that Space of Earth contained between the Equator (where the Artificial Day is 12 Hours,) and that Place where the longeft Day is increafed half an Hour. So

- The first Climate extends from the Equator Northward or Southward to where the Day is  $12\frac{1}{2}$  Hours.
- The fecond Climate extends from where the longest artificial Day is  $12\frac{1}{2}$  Hours, to where it is 13.
- The third Climate extends from where the longest Day is 13 Hours, to where it is  $13\frac{1}{2}$ , Cc.

So that according to the Increase of Days, there will be twenty-four Climates in each Hemisphere, counting no farther than the Polar Circles.

G 3

XXIV. The

XXIV. The notable Points of the Compass are efteemed by these several Professions thus: The Faces of

Their Right to the Left to the Priefts to the Eaft, —— South —— North. Aftronomers the South, —— Weft —— Eaft. Geographers the North, —— Eaft —— Weft, Poets the Weft, —— North —— South.

XXV. The Parts of this Terrestrial Globe, are as the Celestial, *i.e.* the Ball, Brass Meridian, Hour-Circle, Index, and Quadrant of Altitude; whose Uses follow.

#### PROBLEM I.

#### To find the Latitude of any Place.

THE Latitude is the Diftance reckoned in the Brazen Meridian from the Equator Northward or Southward; fo that if you bring the Place, whose Latitude you would know, to the Meridian, it will shew its Diftance from the Equator.

So

¢

So the Latitude of

2.3

Longitude.

87

Salakende vig		0 1
London is	51—32 North.	27-00
Paris	48-45 N.	27-40
Stockbolm	59—26 N.	43-30
Copenbagen	56—13 N.	41-00
Criaco	49—56 N.	46-47
Vienna .	48—14 N.	47-00
Moscow	55—25 N.	72-00
Rome	41-50 N.	40-30
Madrid	40—25 N.	2340
Amsterdam	52—29 N.	37-00
Dublin	53—20 N.	20-29
Edinburgh	56—07 N.	24-09
Jerusalem	32—00 N.	66-00
Mount Arara	t 39—40 N.	77-30
Eden(Garden	) 32—00 N.	77-00
Store a labora & the state		

Note, The Longitude is here reckoned from St. Michael's, one of the Azora's.

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PROB.

88

PROB.

#### PROB. II.

#### To find the Longitude of any Place on Earth.

'T H E Longitude of the Places above are reckoned in the Equator from the first Meridian, which passeth over the Island of St. Michael, one of the Azora Islands. So to find the Longitude of Jerusfalem, bring it to the Brass Meridian, then look in the Equator, and there, under the faid Meridian, you have 66, the Degrees of Longitude required.

#### PROB. III.

To find what Hour it is any Time in any Part of the World, when it is 12 at London.

SUPPOSE when it is 12 a-Clock at London, I would know what Hour it is at Jerusalem?

Because Jerusalem is Eastward from London, having brought London to the Meridian, and put the Index to 12, turn the Globe toward the East Part of the Horizon, till Jerusalem be under the Meridian, and then the Hour-Index will cut 2 b. 50'. Afternoon.

a Kel

So

So likewife when it is Noon at London,

Party - when it is here	b.		
It will be at Barbados -	8	15	Pekey,
At Jamaica	6	50	Before
At Cape Horn in Terra del Fuego	37	00)	Noon.
At Rome	I	00	After-N.
At Gibraltar	11	45	Morn.
At Constantinople –	2	15	After-N.

# PROB. IV.

To find at any Hour, at London, where it will be Noon, or 12 a-Clock, at any Place in the World.

BRING the Place to the Meridian, and put the Hour-Index to 12; then turn the Globe till London come to the Meridian; and then the Index will shew the Hour, upon a Dial at London, when it will be 12 at the faid Place. And thus may all the following Towns be put upon a Dial at the feveral Times when it 90 A Mathematical MANUAL. it will be 12, or Noon, at the feveral Places put down.

	In the Mor	ning,
	b.	1
Pekin, the Metropolis of China, it when it is here	vill }4	15
Batavia, in the Isle of Java in E India,	aft } 5	00
Middle of the Isle Sumatra	5	30
Middle of the upper End of the E of Bengal	ay } 6	20
Agra, the M. of India	- 6	30
Cape Comorin in East India, betwee Malabar and Cormandel Coasts, -	en }6	45
Bombay, in East India, on the Coast Malabar,	of }7	00
Cape Rasalgate, in Arabia Falix, c tring into the Gulph of Ormus,	en-}8	00
Ispahan, the M. of Persia,	8	22'
Baffora, where the Caravan comes fro Mecca,	<sup>m</sup> 38	35
Babelmandel Streights, entring into t	he}8	52
i the state of the state of the state of the state of the state	dia and	

Middle

.guidenais start.	In the Morr	ning.
	b.	•
Middle of Madagascar it will be i there, when it is here	2 8	53
Moscow, Metropolis of Russia, -	- 9	10
Aleppo and Antioch	- 9	20
Jerusalem — — –	- 9	30
Constantinople —	9	45
Warfaw, M. of Poland,	10	33
Cape of Good-Hope — —	- 10	38
Stockholm, M. of Sweden,	- 10	40
Vienna, M. of Germany,	10	47
Rome, M. of Italy,	IO	53
Copenhagen, M. of Denmark, -	- 11	22
Basil and Turin,	- 11	24
Antwerp,	II	38
Amsterdam,	II	40
Paris, the M. of France,	II	50
Madrid, the M. of Spain	- 12	12
ea a strate from our our st	a and the set	a sample

1.

91

Dublin,

In the My wing.	In the Mo	rning.
	b.	,
Dublin, Metropolis of Ireland, -	- 12	27
Madera	- I	17
St. Mary's, a Western Island, -	- I	48
Cape Trio in South America	- 2	47
Cape Farewel, in North America,	- 3	15
Surinam, in South America,	- 3	45
Barbados	3	50
Antigua — —	4	15
Bermuda, near the Coast of Virginia	, - 4	25
Boston, in New-England,	- ' 4	45
New-York	5	00
Port-Royal, in Jamaica,	- 5	30
Middle of the Streights of Magellan	5	30
Sea-Horse Point	- 6	30
Mexico, in North America,	6	50
Port Nelfon, in Hudson's-Bay,	- 7	20
South End of the Isle California	8	08
ALL	Explanat	
	The second second	1

Explanation of the foregoing TABLEthere needs little more than what is above.

- It shews, for EXAMPLE, That it is 12 a-Clock at Jerusalem, when it is 30' past 9 at London, and the Counties North or Southward of London.
- It shews also the Difference in Time at any Hour: For it being Noon 2b. 30'. at *Jerufalem* before it is at London, it is 3 a-Clock p. m. of confequence at Jerufalem, when half an Hour past 12 here: And so of any other Places and Times that are in the Morning-Hours. But for those in the Afternoon, as Barbados, it is but 12 there, when it is 50' past 3 here; and confequently at 10 in the Morning here, it is but 10' past 6 at Barbados : We being 3 Hours and 50 Minutes before them, as lying so much more Easterly.

you will fee the Paint of Compris the

latter Elece bears from the firft which is brought

PROB.

to the Zenieb.

94

## PROB. V.

# To find the Distance of any two Places on Earth-

LAY the Quadrant of Altitude on the two Places, which gives the Degrees, and multiply them by 70, and the Product is English Miles. It being found, by actual Mensuration, by Mr. Norwood, that there are upwards of 69 Miles in a Degree.

# PROB. VI.

laces and Timer that

## To find the Bearing of any one Place from another.

HAVING rectify'd the Globe as to Latitude, and the Quadrant placed in the Zenith, lay it over the other Place you would know the Bearing of, and then the End will cut the Horizon : Right against which, in the outward Edge, you will fee the Point of Compass the latter Place bears from the first which is brought to the Zenith.

Take

Take the EXAMPLES of the two laft Problems, of the nearest Distance and Bearing of 47 of the most noted Places in the World (as follow) from the opulent and famous City of London.

# In EUROPE.

The second s	Neareft Dift. Eng. Miles.	Bearing, or Point of Compass, from London.
Paris, the Metroplis of France,	3208	near S. by E.
Madrid, the M. of Spain		near S.
Vienna, the M. of Ger- many,	3860	near E. by S.
Stockholm, the M. of Sweden,	3980	near N.E. byN.
Copenhagen, the M. of Denmark,	3700	near E. N. E.
Amsterdam, M. of the United Provinces,	\$210	near E.
Brussels, the M. of the 10 Austr. Provinces,	\$ 190	near E.

Berlin,

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Es of the two laft	Nearest Dist. Eng. Miles.	Bearing, or Point of Compass, from London.
Berlin, Metropolis of Upper Saxony in Ger- many,	5560	E by N.
Hanover, in Lower Saxony in Germany,	3420	E.
Ausburgh, M. of the Circle of Suabia,	\$435	near E. S. E.
Cracow, the M. of Po- land,	3700	near E.
Moscow, the M. of Russia,	\$1530	E. N. E.
Rome, the M. of Italy,	840	S. E.
Constantinople, M. of J Turkey,	1640	E. by S.
Bafil, M. of Switzerland	,400	S. E.
Turin in Savoy,	525	near S. E.
Gibraltar, in the Streights by the Mediterranean,	1250	near S. S. W.
Port Mahon, in the Isle Minorca,	\$710	near S.

Meffina,

Nearest Bearing, or Point Dift. Eng. of Compass, from Bearing, or Point of Campals from Miles. London. London. Messina, Metropolis of 31085 near S.S.E. Venice, the M. of that? Republick, \_\_\_\_\_\_630 near S. E. by E. Belgrade M. of Servia, 3980 E. S. E. in Europe Turkey, 3980 E. S. E. Legborn, a Free-Port in 700 near S. E. by S. Italy, Getman, the Metropolis 7 1330 S. by W. Cape of Good-Hope, the J Aleppo in Syria cons 2350 Incar E. S.E. A1820a. Ifpaban the M. of Perfia 3200 E. by S. Pekin, the M. of China 5180 N. E. Daysh Tartary, about the Middle 4200 near N. E. Agra, the M. of East- 35290 E. by N. IV. AME. H Bombaya

97

Nearest Dist. Eng. Miles. Bearing, or Point of Compass, from London.

Bombay, on the Mala- 35300 ne

near E.

Bengal, on the Corman- 35460 E.

## III. AFRICA.

Alexandria in Egypt, - 2310 S. E. by E.

Tetuan, the Metropolis? 1330 S. by W. of the Empire of Fez, 1330 S. by W.

Cape of Good-Hope, the most South Point of 6160 S. by E. Africa, \_\_\_\_\_

Middle of the Isle Ma-35810 S. E.

Santta Helena, 4830 near S. by W.

, the M. of Mal- 25290 E.

IV. AME-

98

of Compals, from

Bondays

# IV. AMERICA.

20, with N. Wind	Nearest Dist. Eng. Miles.	Bearing, or Point of Compass, from London.
Barbados, one of the Caribbee Islands,	e}4270	near W. by S.
New-England,	- 3360	W. N. W.
Pensilvania,	3710	near W. by N.
Maryland —	- 3780	nearW. N.W.
Virginia,	- 3920	W. N. W.
Carolina,	- 4200	near W.N.W.
Jamaica,	- 4900	near W.
Newfoundland,	- 2100	W. N. W.
North End of Baffin's Bay, the most North Part of America,	\$2730	N. by W.
Cape-Horn, the most Southerly Part, —	38890	S. W. by W.

These are the nearest Distances; but they would be much more, if we compute the Distance a Ship runs upon several Courses to come

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at

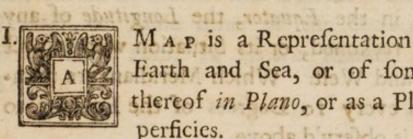
99

A Mathematical MANUAL. 100 at a Port. As for Example, to Bengal in East-India : Miles. VI From London, East about 60, with W. Wind. Thence Southward, 20, with N. Wind. Thence Westward, -750, with E. Wind. Barbydis, one of Thence near South, to make the Cape 6300, with N. Wind. of Good-Hope of Good-Hope, -New-England, ----And thence near } 6930, with S.W.Wind. N.E. to Bengal, } 6930, with S.W.Wind. Sum = 14060 to Bengal in East India 3920 W.N.W. Carolina, 4200 near W.N.W. Famalca. near W. W.W.W. New found North Cape-Horn, the S. W. by W. Southerly Part, hefe, are the nearest Distances; but they be much more, if we compute the Diftance a Ship runs upon feveral Couries to come EI 2 16

A Mathematical MANUAL. 101 Degrees, in the Equator, as appears in the Right-Hand Circle; and from 181 to 360 in-KIPCA TRADE SUPPORT

IWIIn this Map of the World the Circles of the Globe areVielineTeco Bh& Equator is at was quite through the Middle of both the A DESCRIPTION and USE of MAPS.

meet in the Poles of the World. And by thefa



1. MAP is a Representation of the A Earth and Sea, or of fome Part thereof in Plano, or as a Plane Superficies. avoda b'vraido el en sode

II. A Map of the World shews, in two Circles, the Situation or Polition of the four Quarters of the World : That Circle towards the Right Hand containing Europe, Afia, and Africa, with the Isles thereto belonging; and that toward the Left hath in it America, with the Iflands appertaining to it. are number d 10, 20, 80, 62. And the Dou-

III. The outermost (or entire) Circle, is the grand or first Meridian, from which the Longitude is reckoned Eastward, from 1 to 180 Degrees, H 3

Degrees, in the Equator, as appears in the Right-Hand Circle; and from 181 to 360 inclufive, or to the grand Meridian again, which is evident in the Equator, and in the Left Hand Circle.

IV. In this Map of the World the Circles of the Globe are delineated. The Equator is . drawn quite through the Middle of both the faid Circles, divided into Degrees as abovefaid, and through every five of those Degrees there passet here passet in the Poles of the World. And by these Degrees in the Equator, the Longitude of any Place is reckoned, or its Situation with respect to East and West. Which Meridians are number'd in every 10 Degrees of the Equator to 360, as is observ'd above.

But the Latitude of Places is computed by the Degrees in the grand Meridian, reckon'd from the Equator upward or downward, *i.e.* Northward or Southward, and is diffinguished by curved Lines, which run (or are suppos'd) parallel to the Equator through every five Degrees of the grand Meridian; which Parallels are number'd 10, 20, 30, & And the Double Lines 23 ½ Degrees above the Equator, is the Tropic of Cancer, and so much below is the Tropic of Capricorn. And the curved Line, divided into

into Degrees, which paffes through both Circles, and croffeth the Middle of the Equator, touching the Tropics, doth reprefent the Ecliptic.

V. There are also Maps of Part of the World; as the four Quarters, Europe, Afia, Africa, and America. These have the Degrees of Latitude on the East and West Sides, and of Longitude on the North and South, all expressed by curved Lines.

VI. In fome Maps the Longitude is reckon'd from London at the Bottom; and from Teneriff, or fome other of the Canary, Madera, Cape Verd, or Azora Islands, at the Top.

VII. In Maps of Part of the World, there are fo much only of the Meridians and Parallels expressed, as fall within fuch Portion or Part. And in the Maps of Kingdoms only, the faid Meridians and Parallels are expressed by streight Lines.

VIII. In all Maps the upper Part is the North, the lower South, the Right-Hand Degrees East, and the Left West; which are sometimes thus marked :

North

North \_\_\_\_\_ Borealis, or Septentriovalis.

South — Meridionalis, or Auftralis. Eaft 10 orientalis. Eaft 10 Orientalis. Weft 200 Occidentalis. Weft 200 Occidentalis.

Note, As to the Zones, Climates, Denominations of the feveral Parts of Land and of Water, and different Situation of Inhabitants with respect to Shadows, and Antiefi, Periefi, and Antipodes, they are fully accounted for in the Use of the Terrestrial Globe, foregoing.

VIII. In Maps of Part of the World, there

ion or Part.

Dy fireight

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are to much only of the veridians and Parallels

VIII. In all Maps the upper Part is the

Month, the lower South, the Right-Hand Do-

crees Eafle and the Left Weft ; which are

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expredicd, as

Alcridians al

fomotimes thus marked :

And in the

LANCS.

The

The LATITUDE and LONGITUDE of the most noted Places in the World, the Longitude from the Isle Teneriff; and all North Latitude, except what is marked S.

North La.

DI TI

IL I. IN EUROPE.

I. In GREAT BRITAIN, &c.

of that County, 54 47

Darba

Chefter, in Chefhire, ---- 53 17. 15 51

Long. from North La-Teneriff. Country of Cam- 2 50 24 18 40 [ ONDON, the Metro-}51 32 18 36 York, the Chief of that County, 54 00 17 46 Edinburgh, the Chief of {56 07 15 50 Scotland, Lincoln, in that County, 53"-17 Dublin, the Chief of Ire- 353 20 12.00 land; The other Cities in England, i.e. Bath, in Somerfetshire, \_\_\_\_ 51 23 16 14 Brifto! Peterboroughs

Hagrienod han an		th La- inde.	Long. Ter	from
		;	•	î
Bristol, Part in Somersetsbire,	51	30		00
Canterbury, in Kent,	51	20	19	46
Carlisle, in Cumberland,	54	50	15	56
Chester, in Cheshire,	53	17	15	51
Chichester, in Suffex,	50	51	17	51
Coventry, in Warwicksbire, -	52	27	17	14
Durbam, M. of that County,	54	47	17.	16
Ely, in the County of Cam-}	52	24	18	46
Exeter, in Devonsbire, -	50	44	15	02
Gloucester, in that County,	51	56	16	26
Hereford, in that County,	52	08	15	44
Lincoln, in that County,	53	17	18	00
Litchfield, in Staffordshire, -	52	44	17	00
Norwich, M. of Norfolk,	52	43 .	19	46
Oxford, M. of that County,	51	47	17	16

Peterborougk,

50 5 5 10 A 5 3	North La- țiende.	Long. from Teneriff.
Peterborough, in Northamp- tonshire,	\$52 34	• / 18 16
Rochefter, in Kent,	51 24	19 15
Salisbury, in Wiltsbire,	-51 03	16 51
Wells, in Somersetsbire,	-51 13	16 14
Winchester, in Hampshire,	51 03	17 21
Worcester, in that County,	52 17	16 21
Cambridge University,	- 52 13	18 32

The four Welfb Cities are, St. Afapb, in Flintsbire, 53 23 15 21 Bangor, in Caernarvonsbire, 53 21 14 36 St. David's, in Pembrokesbire, 52 02 13 36 Llandaff, in Glamorgansbire, 51 32 15 21

on M. of French Country approp

In

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New Bist-

Long. from

2. In FRANCE; as,

AE SE - North La- Long. from titude. Teneriff. 31 81 Paris, the Metropolis of the 348 45 21 30 Salisbury, in Willbirg ---12 61 51 03 Amiens, M. of Picardy, --- 49 54 21 26 Rheims, M. of Champaigne, -49 13 23 18 Rouen, M. of Normandy, - 49 26 20 02 Rheimes, M. of Bretagne, - 48 03 16 30 Orleans, M. of Orleanois, - 47 44 20 42 Dijon, M. of Burgundy, 43 47 1 24 05 Isons, M. of Lyonoife, 45 24 024 08. Bourdeaux, M. of Guienne, or 44 50 17 50 Gascoigny, Thoulouse, M. of Languedoc, 43 29 19 48 Llandaff, in Glamorganshire, 51 32 15 21 Grenoble, M. of Dauphine, 44 54 25 40 Aix, M. of Provence, ---- 43 04 24 40 Nancy, M. of Loraine, ----- 48 40 25 40 Befanson, M. of French Compte, 47 07. 25 28

3. In

3. In SPAIN; as,

Asren La.

Long. From

Teneriff.

13 55

82 TE Staris to silocortoM Lang. from North La-Long. from titude Madrid, the Metropolis, in 340 25 13 40 Compostella, the M. of Galicia, 43 00 08 16 Oviedo, the M. of Austuria, -43 23 II 05 Bilboa, M. of Biscay, \_\_\_\_ 43 47 14 22 Pampeluna, M. of Navarre, - 42 52 16 06 Saragofa, M. of Aragon, \_\_\_\_\_A1035 17 09 Barcelona, M. of Catalonia, - 40 34 20 23 Lurin, M. of the P. Valentia, M. of the Kingdom 39 25 17 15 of that Name, \_\_\_\_\_ 39 25 17 15 Murcia, M. of that Kingdom, 38 04 16 34 Genan, M. of the State o Burgos, M. of Old Castile, - 42 25 13 30 Leon, M. of that Kingdom, 42 44 MII 48 Placentia, M. of Estramadura, 39 48 II 50 Seville, M. of Andalusia, 1 + 37 30M , II 14 Cadiz, in Ditto, Atomic 1861321 , 19:42 Granada Trieft,

	North La- titude.	Long. from Teneriff.
Granada, Metropolis of that?	• /	• 1
Granada, Metropolis of that Kingdom,	37 28	13 55
Majorca, M. of ditto Isle,	39 04	20 33
Citadella, M. of Minorca, 3	a strategicary	22 30
Manager 43 azis II og	the Af. of	Opinio,
4. ITALY;	as,	Billions
Rome, M. of Italy,	41 50	20 02
Chambery, M. of the Dutchy? of Savoy,	45 04	25 24
Turin, M. of the Principa-}	44 34	27 26
Cafale, M. of Montferrat, - 4	14 40	28 17
Genoa, M. of the State of }	43 53	29 00
Milan, M. of that Dutchy,	44 55	29 13
Parma, M. of that Dutchy,-	14 24	30 40
Modena, M. of that Dutchy, 4	14 14	31 32
Mantua, M. of that Dutchy, 4	14 52	31 10
Granada	2	Trieft,

	North La- titude.	Long. from Teneriff.
	• 1	• 1
Triest, in Istria,	45 44	34 55
Venice, Metropolis of that Commonwealth,	<b>}</b> 45 20	33 04
Florence, M. of the Dutchy of Tuscany,	<b>}</b> 43 20	32 10
Legborn, in Ditto,	43 52	31 00
Naples, M. of the Kingdom of Naples,	\$40 56	36 15
Palermo, M. of Sicily, -	- 37 26	34 50
Cagliari, M. of Sardinia,-	- 38 10	30 24
5. In GERMA		Padila M
Vienna (the Metropolis) in Austria,	\$48 14	37 05
Hanover, in Lower Saxony,	52 35	29 36
Berlin, M. of Brandenburgh	52 33	33 52
Dresden, in Upper Saxony, -	- 51 06	33 50

Magde-

t

North La- Long. from North La. Long Som Teneriff. Teneraff. titude. 52 17 32 00 Fenice, Metropolis of th Munster, M. of Westphalia, - 52 00 27 12 Strasburg, M. of the Circle 3 48 28 27 26 cle of the Upper Rhine, \_\_\_\_\_\_ 48 28 27 26 Gologn, M. of the Circle of \$50 55 26 32 the Lower Rhine, \_\_\_\_\_ \$50 55 26 32 Augsburg, M. of Swabia, -48 14 30 57 Nurenburg, M. of Franconia, 49 24 31 11 34 50 Munich, M. of Bavaria, 47,58 31 36 And GE Prague, M. of Bobemia, --- 49 58 34 33 Basil, M. of Switzerland, - 47 34 27 16 Antwerp, M. of German Ne- 351 16 23 36 Auferias Bruffels, M. of Brabant, - 50 54. 23 36 Berlin, M. of Brandenlungh, 52 33 33 52 Presden, in Upper Saxony, - 51 06 33 50 Magde-

1

# 6. In the UNITED PROVINCES.

.

	North La- titude.	Long. from Teneriff.
Amsterdam M. of the Seven	• • /	• 1
Amsterdam M. of the Seven United Provinces,	1 ods	24 00
Hague, in Holland,	52 . 8	23 22
** * * ****	52 31	23 36
AS 02 TZ 7. IN SWED		Stofwick,
Stockbolm, the Metropolis, -	59 26	39 5
Riga, M. of Livonia, now under the Czar, —	56 54	45 34
Notteburg, M. of Ingria,	59 52	.9 34 00
Abo, M. of Finland	60 23	43 33
Lunden, M of Schonen,		33 22
Revel, in Eastland, now	59 13	
Narva, M. of Eastland, now		
Tornia, M. of Lapland	56 35	34 16
nl or I		8. In

# 8. In DENMARK.

he Seven	North La- titude.	Long. from Teneriff.
Copenhagen, the Metropolis	- 56 13	32 30
Bergen, M. of Norway, -	61 00	24 15
Hamburg, M. of Holftein, -		29 20
Slefwick, M. of South Jut- land,	3 55 57	29 24
Wyburg, M. of North Jut- land,	3 56 47	28 52
9. In RUSSIA or	Musco	V.Y.

Moscow, the Metropolis - 55 25 63 00 Archangel, M. of Dwina - 64 50 65 10 Novogrod, M. of Novogrod 358 10 55 18 Weliki, \_\_\_\_\_ 358 10 55 18 Aftracan, M. of that King- 347 72 30 dom, Petersburg, at the upper End 30 of the Gulf of Finland - 30 50 30 10. In

8. In

#### IO. IN POLAND.

Lour. from

North La. titude. Long. from Temeriff. S,  $Cracow, the Metropolis of {49 56 40 47}$  Warfaw, M. of Mafforia, - 52 7 42 5 Dantzick, M. of Prufia, - 52 7 42 5 Dantzick, M. of Prufia, - 54 13 40 42 Mittau, M. of Courland, - 57 00 44 00 Wilna, M. of Lithuania, - 54 31 47 14 Lemburg, M. of Ruffia Rubra, 49 36 45 00 Kaminieck, M. of Podolia, -48 50 47 46Brefte, M. of Polefia, - 51 55 45 8

II. In TURKEY in Europe; as,

Constantinople, the Metropolis, 43 00 54 20 Buda, the M. of Lower-Hungary, now under the 42 17 41 44 Emperor, 41 44 Belgrade, M. of Servia now under the Emperor, - 345 20 42 34 I 2 Temif-

WIN POLAND.	rth La- Long, from Tenerifi	
•	, , , , , , , , , , , , , , , , , , , ,	
Temiswar, M. of that Go-346 vernment, und. Emp. 346	5 6 43 24	ł
Adrianople, in Romania, - 4	3 18 51 00	5
Zaza, M. of Dalmatia, - 44	4 34 37 20	2
Posega, M. of Sclavonia, - 43		2
Hermanstad, M. of Tran-}44	6 46 45 4	
Salonica, or Theffalonica, M. 34	I to .M . sulvy I 37 47 90 To .M . suldand	2
Misistbra, M. of the Morea, 3.		
Aloph, M. of Crim Tartary, 340 by fome in Alia, - 340		

# II. ASIA.

North La-North Long. from titude. Teneriff. Aleppo, in Syria, \_\_\_\_\_ and 31 25 ort 58 29 Tripoli, in Syria, \_\_\_\_\_ 34 20 als 63 38 Empire, on Ephefus, in Lesser Afia, - 39,00 55 45 Burfa, in Do. near the Pro-341 49 1000 57339 mandel Coaft, India, Babylon, M. of Affyria, - 35,00 79,00 Balfora, in Arabia Deserta, 31 00 66 00 Famagosta, in Cyprus, - 34000 0058000 lippine Iflands, @ Medina, in Arabia Deferta, 26 00 70 10 Manila, M. of another of Mecca, in Arabia Falix, - 23 00 50 61 00 Ispahan, M. of Persia, ---- 32 26 86 49 Teflis, the M. of Georgia, - 43 5 83 00 Selenginskoi, about the Mid- 357 00 107 30

I 3

Pekin,

Long. from Moreb La-North La-Long. from Teneriff titude. Teneritt. 127 00 in Sprig Pekin, the M. of China, - 40 00 Meaco, the M. of Japan - 35 00 Tribeli 149 00 Agra, the M. of the Mogul's 25 30 89 30 Empire, \_\_\_\_\_ Bombay, on the Malabar 19 00 86 00 Coast, East India, --- 319 00 86 00 Goa, on D° Coaft \_\_\_\_\_ IS 00 83 00 Burfa, in Do. near the Pro-Fort St. George, on the Core- 313 20 94 00 mandel Coast, India, - 313 20 94 00 Fort St. David's, on Ditto } 10 M Coast, 0 10 10 93 00 Mindanao, one of the Phi- 37 00 135 30 lippine Islands, Medine, in Arabia Deferta, 26 00 OI OM Manila, M. of another of 314 30 133 00 De, viz. of Luconia, - 314 30 133 00 Bentouli, in the Island Sumatra, 2 30 112 00 Toffic the M. of Congins - 43 5 83.00 INTARA . In about the Mid- 3 57 00 107 30 Pekins, 1 3

# III. AFRICA.

Canta, upon the Survights 35 soil of to

	North La- titude.	Long. from Teneriff.
MERICA.	0.1	• 1
Madagascar Isle, the Middle,	21 00 S.	59 00
Cape of Good Hope,	34 30 S.	30 00
Santa Helena, in the Atlantic Ocean	15 30 S.	07 30
Cape Coast Caffle, the Middle 3 of the English Factories,	5 00	13 00
Tetuan, the M. of the Empire 3	34 20	8 00
Tunis, on the Coaft of Bar-3	32 10	34 53
Grand Cairo (or Memphis) M. 3 of Egypt,	36 <b>4</b>	38 48
Alexandria, by the Nyle, on the Mediterranean	31 25	58 20

I 4

Ceuta,

• •

Cauto,

North La- Long. from titude. Teneriff.
Ceuta, upon the Streights 35 50 08 10 of Gibraltar, 35 50 08 10
IV. AMERICA.
I. In NORTH AMERICA.
Quebec, the Metropolis of 347 12 304 30 Canada or New France, 347 12 304 30
Boston, M. of New En- 344 00 309 00 gland,
Elizabeth Town, M. of }42 00 306 30
New York, M. of New }42 30 306 00 Tork,
Philadelphia, M. of Pensil-}41 00 306 30
Oxford, Metropolis of Mary-338 30 305 30 land,

41

James

North La- titude.	Long. from Teneriff.
James Town, the M. of 36 30	° / 305 30
Charles Town, M. of Ca- 33 00	296 00
St. Auftin's, the M. of Flo-}29 00	294 00
St. Fé, the Metr. of New 36 00 Mexico,36 00	263 00
Mexico, the Metr. of New 3 20 00 Spain, 320 00	271 00
Califurnia, the Middle of it, 33 30	243 00
2. In South America.	Bermaliz
Panama, in the South-Sea, - 08 30	294 30
Darien, or Calidonia, in $\frac{3}{2}$ 09 00 Terra Firma, — $\frac{3}{2}$ 09 00	295 30
Lima, the Metropolis of $3$ 13 30 S. Peru,	298 00

100 9

St.

1

rive Tours for Treasure	North La- titude.	Long. from Teneriff. 0 1
St. Salvador, the M. of }		
Villa Rica, M. of Para- }	22 30 S.	318 00
St. Jago, the M. of Chili, -	· 34 00 S.	300 50
Carthagena, near the Isth-} mus of Darien,	10 00	300 00
Porto Bello, in Terra Firma,-	-10.00	292 00
CO ITA OS 3. ISLAN	1 3.	Maritan
Newfoundland, Port St. } John's,	47 30	323 00
Bermudas, or the Summer } Islands, St. George, }	33 15	311,00
Havana, M. of Cuba,	23 00	292 00
Port Royal, M. of Jamaica,	18 20	298 30
St. Domingo, the M. of Hif-3 paniola,	18 15	303 00

Bar-

Marsh La. Land from	North La- titude.	Long. from Teneritf.
Barbados, the Middle, M. 3 of the Caribbees,	13 45	Ch EIE OF EIE Part
Antigua, also one of the } English Caribbees, - }		
And Note That	Good-Hepe,	Ser.
Baffin's Bay, the N. End, and most Northerly Part of America, is	outherly Pa	noft
Cape Horn, the most Southerly Part of A- merica, is =	58 00 S.	294 00
Cape Caglia, in the Mo- rea, the most Southerly Part of Europe, is	36 40	39 30
North Cape, the most Northerly Part of Eu- rope, is	71 50	42 00
Cape Comorin, in East India, the most Sou- therly Part of Asia's Continent, is	08 00	93 00

Holy

North La-Long. from North La. Long from Teneriff. titude. Trenerist strade. Holy Cape, in Tartary, 7 arbados, the Mide the most Northerly & 73 30 145 00 Part of Afia, is Antigen, alto one of Streight of Gibraltar, 36 10 the most North Part ( II 00 of Africa, is -----And Note, That Cape of Good-Hope, the ? most Southerly Part of 2 34 30 S. 30 30 Africa, is and molt North Part of America, is Cape Horn, the molt 204 00 Southerly Part of Aanter 16 d. 18 === Eaps Caplia, rea, the mo 29 20 Fait of North C Montherity pope, is ape Comercia, in i india floar say ..... 00.80 that Part of Alia's CONCINCINE, 15 The Ttoly

A Mathematical MANUAL. 125 The USE of the last Tables of LATITUDE.

1. IN straight-lin'd Maps, as those of England, the Latitude and Longitude being found, as in the Beginning of the Table for the Cities, the Latitude of Places of lesser Note may be found, if they lie near or under the fame Meridian with those Cities. Thus the Latitude of Chester being 53° 17' the Latitude of Wigan is found by adding its Diftance in Miles from Chefter, = 22. which makes Wigan in the Latitude of 53° 39': And Preston being 12 Miles farther, that being added to 53.39, gives 53.51, its Latitude; for every Mile, adding a Minute: which is near enough the Truth, and will make no fenfible Error in Dialling, Cc. atug both of bohhs of or sinselw faid Meridian'is marked; to give the L

2. In these Kind of Maps (the Latitude and Longitude being given as by the *Table*) the true Situation of any Place may be found. For, lay a Ruler to the Degrees of Latitude on the East and West Side of the Map; and then about the Place of the Longitude draw a Line with a Black-lead Pencil two or three Inches; then lay your Ruler to the Degrees of Longitude

Longitude at the Top and Bottom of your Map; and where it croffeth the aforefaid fhort Line, there is the Place where the Town or City given, is or fhould be placed in the Map.

3. Or to find the Latitude of any Place in these Kind of Maps, set one Foot of a Pair of Compasses in the (o) which is the true Place of the Town, and extend the other to the next Parallel below; then apply that Distance to the East or West Sides of the Map, and you have the Degrees and Minutes to be added to the Number the faid Parallel is marked with, to give the Latitude.

4. And for the Longitude, take the neareft Diftance from the (0) Town or City to the next Meridian Weftward, and apply that to Top or Bottom of the Map, and that will fhew what is to be added to the Figure with which the faid Meridian is marked, to give the Longitude.

5. But where the Longitude is reckoned from two Places (the one marked by Degrees at the Top, the other at the Bottom, as is obferved under the 6th Article, near the Beginning of this Section) you must apply the faid Distance between your Compasses to the Top or Bottom, according to the Place you are minded

minded to know the Longitude from. And for those Maps whose Meridians and Parallels are curved Lines, the Method is the same, making Allowance for the Curvature : But mind to take the Distance of Places, and measure them from the next Meridian Eastward or Westward, according to their Situation at the Bottom of the Map, if the first Meridian is that of London : For there is o for the Meridian of London, and the other Meridians are number'd 1, 2, 3, &c. Eastward and Westward; Lines being drawn through every five Degrees.

Thus, for Example, I would know the Latitude of Cape St. Vincent, and its Longitude from London: I find the Latitude (by a Map of Europe, as Mr. Moll's) to be 36 Degrees, 50 Min. and the Longitude Weft is 10 Degrees from London (as by the Bottom of the Map) or the Longitude is 9 Degrees Eaftward from Ferro, one of the Canary Iflands.

6. Having thus far shewed the Description of the feveral forts of Maps, and also to find the Latitude and Longitude by them, I proceed to shew how

Minutes in a Degr. c, equal to 70 Miles. There

To

I

## To find the Distance between Places by rightlin'd MAPS.

nded to know the Longitude from. And for

Rule. This is very eafily done: For if you take with a Pair of Compaffes the Diftance between the 2 Places, and apply that to one Side of your Map, it will give the Number of Degrees and Minutes; which Degrees, multiplied by 70, exhibit the Number of Miles. And if there be any Minutes, they are fo many  $\frac{7}{6}$ ; there ore they must be multiplied by 7, and divided by 6.

7. Now the Reafon why we multiply the Degrees by 70, to give the Miles in any Number of Degrees, is, becaufe Mr. Norwood, by actual Meafuring, found, that a Degree upon the Surface of the Earth did contain  $69\frac{2}{3}$ English Statute Miles, of 1760 Yards each. So a Degree in round Numbers, without any confiderable Error, may be called 70 Miles.

Note alfo, The Reafon why the Minutes, when there are any, are to be multiplied by 7, and divided by 6, is, becaufe there are 60 Minutes in a Degree, equal to 70 Miles. Therefore,

20

As

2

As 60 Minutes is to 70 Miles; fo is any Minute to its Miles.

As fuppofe I would know the Miles in 30 Minutes, 'tis thus :

60 : 70 :: 30 : 35

Or, omitting the Cyphers in each of the two first,

6 : 7 :: 30 : 35

Which is half of 70, as 30 is of 60.

And here I think it may be proper to give the Proportion of English to other Country Miles and Degrees.

eafy rolfnd. Diffances winit" heriuriteys "Section?

one Foot of a Pair of Combelles in the one

Place, and extending the other Poor to that

other Place, and applying time Diffence to the

Scale, will give the Miles or Lengues relipee-

The when I to ass K I marin and I The

lefs than the Degrees of Letiende, as they are

roward the Poles (efpecially in all Maps where

the Meridians have, any Curvature,) take the

Distance

Miles or Leagues of Se- veral Countries.	Of which are in 1Degree near.	Or English Miles in 1 of theirs near.
The English Statute Mile of 1760 Yards, ——	3-70	I Av fup)
The Italian Mile,	- 60	II
The German Mile,	- 15	4 78
The Spanish League, -	22.00	mo 3 1 1
The Swedish League, -		4 <del>3 9</del> 5 3
The Hungarian League,	1212	5 36
The Scotifs Mile,		

8. But farther, as to the Distance of Places in Maps; there are Scales of English and other Country Miles and Leagues, by which 'tis very eafy to find Distances with Accuracy. Setting one Foot of a Pair of Compassies in the one Place, and extending the other Foot to the other Place, and applying that Distance to the Scale, will give the Miles or Leagues respectively.

9. In Cafe where Degrees of Longitude are lefs than the Degrees of Latitude, as they are toward the Poles (efpecially in all Maps where the Meridians have any Curvature,) take the 2 Diftance

## A Mathematical MANUAL. 131.

Distance of the two Places between your Compasses, and apply it to the Right or Left Sides of your Map, as near against the Middle of the Diftance between the two Places as you can estimate ; which giving the Degrees, multiply them by 70, and you have the Miles.

#### EXAMPLE.

In Mr. Moll's Map of Europe, I find the Distance between Vienna and Madrid to be 13° 15' by the Degrees on the Side of the Map, from 40 upward ; which is, by the Rule under the 6th Head last above, 927 Miles.

#### And farther, as to Circular Lined Maps.

10. If two Places have the fame Longitude, and are of the fame Side of the Equator, the Difference of their Latitudes is their Diftance in Degrees, &c. as by the 6th Head. So from Arles in Provence, to Utrecht in Holland, is 7° 28, or 522 Miles.

11. If two Places lie under the Equator, the Degrees there contained between them, is their Distance, &c. as by the 6th Head. So from the Island St. Thomas in the Ethiopian Sea, Eastward to the Isle Bassa de Ambra in the Indian Ocean, (as may be seen by a Map of Africa) K 2

is

132 A Mathematical MANUAL. is 40° 20' or 2823 Miles; as by the 6th Head.

of your Map, as ne

12. If two Places given have the fame Longitude, but the one is in South, the other in North Latitude; in this Cafe the Sum of the Latitudes is the Diftance in Degrees,  $\mathcal{E}c$ . So the Diftance from *St. Helena* in 15° 30' of South Latitude to the Middle of the Streights of *Gibraltar* in the Latitude of 35.58 North; here the Sum of the Latitudes is = 51.28; which, by the 6th *Rule* laft above, is 3602 Miles for the neareft Diftance.

If Places differ both in Longitude and Latitude, their Diftance may be found near enough the Truth, by *Rule* the 9th laft above. Or by *Prob*.V. of *Sect.* III. 'tis done eafily and accurately.



a by a Map of A



# SECT. V.

# A DESCRIPTION and USE of the SECTOR.



H E Sector is a fmall Inftrument about a Foot in Length, with a Joint in the Middle, which gives

7. The Line of Longitudes

it two Parts, or Legs, each fix Inches in Length; and their Breadth is fix Tenths of an Inch, and Thicknefs about an Eighth of an Inch.

II. Its Use is to folve Questions in Trigonometry, and many others both Arithmetical and Geometrical.

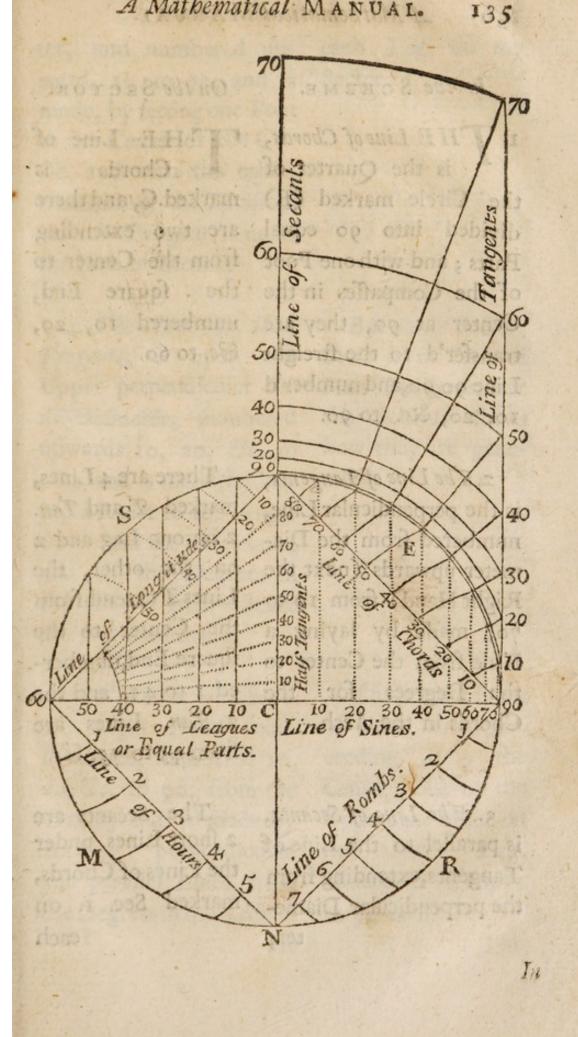
III. The Lines on the Sector are,

K 3

- I. Chords,
- 2. Tangents,
- 3. Secants,
- 4. Half Tangents,
- 5. Sines,
- 6. Leagues, equal Parts, or the Line of Lines.
- 7. The Line of Longitudes,
- 8. The Line of Hours, and
- 9. The Line of Rhombs.

All which proceed, or have their Foundation, from the Circle; as appears by the following *Scheme*.

noncents and shary of the Loth Mithanetical



In the SCHEME.

1. THE Line of Chords, is the Quarter of the Circle marked (E) divided into 90 equal Parts; and with one Foot of the Compassies in the Center at 90, they are transfer'd to the streight Line 90,90, and number'd 10, 20, &c. to 90. On the SECTOR.

THE Line of Chords is marked C, and there are two extending from the Center to the fquare End, numbered 10, 20, Ec. to 60.

2. The Line of Tangents, is the perpendicular Line, numbered from the Diameter upwards (next the Right Hand) from 10 to 70, made by laying a Rule from the Center to the Degrees for the Chords in the Arch.

3. The Line of Secants, is parallel to the Line of Tangents, extending from the perpendicular Diame-

ter,

There are 4 Lines, marked *T* and *Tan*. 2 on one Leg and 2 on the other, the Lines *T* extend from the Center to the fquare End, numbered 1 to 45, and the 2 *Tan*. Lines are from 45 to 75, Ec.

The Secants are 2 fhort Lines under the Lines of Chords, marked Sec. 1. on each

ter, and numbered up- each Leg, on my ward, 10 to 70, and is Sector. made, by fetting one Foot in the Center of the Circle, and with the other, transferring the Divisions on the Tangent Line to dama , buck shi oft C the Center ; and this is

There are on each

4. The Line of Half But on the Sector, Tangents, is upon the there is no Line of Upper perpendicular Se- Half Tangents, but mi-Diameter, numbered the Scheme shews upwards 10, 20, 80. to 90; and is made by laying a Ruler to the Angle 60 toward the Left Hand, and to the Degrees in the Chords from whence the Arch are made.

5. The Line of Sines is the Right Hand Semi-Diameter, numbered 10, 20, 8°c. to 90, from the Center, and is made by drawing perpendicular and parallel Lines, from the Degrees in the Arch of the

next the partner of

Quadrant Diameter (C 90).

how they are generated. of othe bobylb

tudes, is on the n

: bmit

There are 2 Lines of Sines, each proceeding from the Center; one on the Upper, the other on the lower Leg, numbered from 1 to 90 each.

This

Tet:

138 A Mathematical MANUAL. the uppermoft right Hand Quadrant to the Semi-Diameter (C 90).

6. The Line of Leagues, is the Semi-Diameter next the left Hand, numbered 10, 20, &c. to 60, from C the Center; and this is alfo a Line of èqual Parts, made by dividing it, 1ft into 2, and those Parts each into 3; and each of those are supposed to be divided into 10.

7. The Line of Longitudes, is on the upper Chord Line next the Left Hand, and is numbered downward, 10, 20, &c. to 60; and is made by drawing Lines from the equal Parts, parallel to the upperSemi-Diameter, till they cut the Arch (60, 5, 90,) and then fetting one Foot of the Compaffes in 60, you This Line upon the Sector, is commonly called the *Line of Lines*: There are on each Leg one marked L, and is numbered from the Center, 1, 2, &c. to 10; but is really from 1 to 200.

in the Conner of F

This Line is not on the Sector; but you have the two *Lines of Polygons*, next the parting of the two Legs when the Sector is flut, number'd from 4 toward the Left Hand, to 12.

Aleria an inter the local

This

A Mathematical MANUAL. 139 you transfer the Divisions in the Arch to the Chord Line.

8. The Line of Hours, is made by dividing the Arch (60, M N) into 6 equal Parts: and with one Foot of the Compasses in 60, transfer them to the Chord Line (60, 12,)

(Extent of the Cam-

9. The Line of Rhombs, is the Arch (N, R, 90) divided into 8 equal Parts, and with the Compafs's Foot on 90, they are transfer'd to the Chord Line (N 90)

R. o. E. E. M.

the Circle, between your Compaties, and apply

E E the Radins, or Semidiameter, of

This Line of Hours is the uppermoft (on my Sector next the joint End) and is number'd 1 to 6; and under that is a Line of Chords of a fmall Radius.

There are alfo 2 Lines on the S and T Side, at the Bottom next the Joint ; one is of Latitudes, and the other of the Inclination of Meridian, on my Sector.

it on the Lines of Polygons, by a diagonal Better from 6 on one Leg to 6, on the other ! ad T require the Legs at that Difference.

## The USE of the SECTOR.

you transfer the Divilions

THIS Inftrument is commonly used partly opened, according as the Cafe requireth. And whereas the Compasses are fometimes extended on one and the fame Line from the Center End towards the Square End; Secondly, And fometimes athwart, from Divisions on one Leg to those on the other; I shall call

The First, The Lineal (Extent of the Compasses, or) Distance.

The Second, The Diagonal Distance (or Extent) for Shortness. s count

# and with the C. B. O. B. P. R. O. B. I. atitudes,

Side, at the Bot-

Divide a Circle into 4, 5, 6, 8c. to 12 equal Parts; or to make any regular Polygon.

#### RULE.

TAKE the Radius, or Semidiameter, of the Circle between your Compasses, and apply it on the Lines of Polygons, by a diagonal Extent from 6 on one Leg to 6 on the other: Then keeping the Legs at that Diftance,

The Diagonal Extent  $\{s \text{ to } s \}$  will divide  $\{s \text{ equal Parts.} \\ \text{from } -6 \text{ to } 6 \\ \hline 7 \text{ to } 7 \\ \hline 8 \text{ to } 8 \\ \hline 8 \text{ Erc.} \\ \end{bmatrix}$ 

ing Lines, you have the Octagon required

And fo by drawing Lines, you have the Pentagon, Hexagon, Heptagon, Octagon, &c.

#### PROB. II.

#### To make a regular Polygon whose Side shall be any right Line given.

#### RULE.

SUPPOSE you would make an Octagon: Take the Line given between your Compaffes, and opening the Sector, apply that Diftance, on the Line of Polygons, diagonally from 8 on one Leg, to 8 on the other; then, keeping the Legs and that Diftance, take the diagonal Extent from 6 to 6 in the Line of Polygons, and with that Radius defcribing a Circle, the faid diagonal Diftance between 8 and 8 will divide the Circle into 8 equal Parts; fo that drawing

55 the Circle 25 equal Parts.

ing Lines, you have the Octagon required. And the like of any other Polygon.

#### PROB. III.

To set the Sector so, that the two Lines of equal Parts may make a right Angle at the Center.

## RULE.

IN a right-angled Triangle, if the Perpendicular be 3, the Bafe 4, the Hypothenufe will be 5; therefore upon the Line of Lines take from the Center the lineal Diftance to 5; then open the Sector fo, that that Diftance will extend from 3 on one of the Line of Lines, to 4 on the other; and then your two Lines of Lines make a right Angle. But fee after the next *Problem*.

# PROB. IV.

To find a third Proportional to two given Lines; as suppose 40 and 60.

#### 

TAKE the lineal Distance of 60, and set on the diagonal Distance of 40; then the diagonal Distance of 60 will give the lineal Distance of 90.

And

And in like manner,

In 15 and 30, the 3d Proportional is found = 60.

20 and 30, ------= 45.And fo on.

But note as to Prob. III. the fame may be done thus: Take 60 of the Line of Chords, and make that a lineal Diftance of the Line of Lines, it will be 34.5; then take 90 out of the Line of Chords, and fet it a diagonal Diftance on the Line of Lines from 34.5, to 34.5, and the two Lines of Lines will make a right Angle.

# PROB. V.

Two Lines given to find a geometrical mean Proportional between them.

## RULE.

THIS is not done by the Sector, without much Trouble; and therefore the Arithmetical Rule of multiplying the Numbers together, and contracting the Square Root for the Anfwer, is much preferable.

So the Mean between 20 and 80 is = 40; between 15 and 60 is = 30;

And fo on.

PROB,

#### PROB. VI.

## To find a fourth Line in Proportion Geometrical to three given.

#### RULE.

And to on.

THE Lines given being 20:40:30:60: Take the lineal Diftance of 40, and fet it a diagonal Diftance between 20 and 20; then take the diagonal Diftance (upon the laft Angle) from 30 to 30, and it will give you a lineal Diftance of 60, all on the Line of Lines.

Or this may be done, as under the first Rule, by the Sector, in the fifth Cafe of obliqueangled Triangles following.

Too Lines given to find a goometrical mean Fro

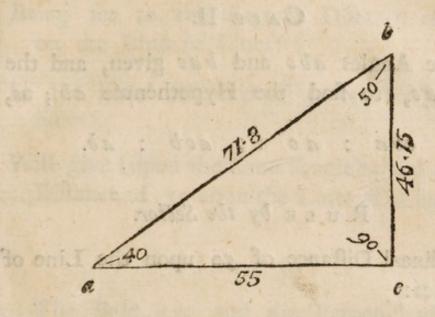
## II. QUESTIONS in Trigonometry, done by the SECTOR.

[Note, That the Angle a cb is the Angle c, a b c the Angle b, and b a c is the Anat a.]

#### contracting the Square Root for the Anfwer, is much preferable.

The Angles abs and bac, and the Base ac given, to find the Perpendicular bc.

As, cba : ac :: bac : bc. Rule



RULE by the SECTOR.

The lineal Diftance of 50 upon the Line of Sines:

Being fet to a diagonal Diftance on the Lines of Lines of 55::

So the Lineal Distance of 40 upon the Line of Sines:

Gives the diagonal Diftance of 46.15 on the Line of Lines (the fame Angle of the Sector continued.)

R o n e by the 1866 or.

iftance of go upon the Line

Being

CASE

#### CASE II.

The Angles *abc* and *bac* given, and the Side *ac*, to find the Hypothenufe *ab*; as,

cba : ac :: acb : ab.

#### RULE by the Sector.

The lineal Diftance of 50 upon the Line of Sines:

Being fet to the diagonal Diftance of 55 on the Line of Lines : :

So the lineal Diftance of 90 on the Line of Sines :

Will (upon the fame Angle) give the diagonal Diftance of 71.8 upon the Lines of Lines.

# So the Lineal Diff. III a s A Dupon the Line of

The Angles *abc* and *bac*; and the Hypothenuse *ab* given: To find the Base *ac*: As,

acb: ab :: abc: ac. mino

#### RULE by the Sector.

ASE

The lineal Distance of 90 upon the Line of Sines:

Being

- Being set to the diagonal Distance of 71.8 on the Lines of Lines : :
- So the lineal Diftance of 50 on the Line of Sines:

Will give (upon the fame Angle) the diagonal Diftance of 55 upon the Lines of Lines.

#### CASE IV.

The Base ac, and the Perpendicular be given, to find the Angle bac: As,

ac: acb :: bc: tang. bac.

RULE by the Sector.

.. The linest Diftance of go on the

The lineal Distance of 55 upon the Line of Lines:

Being set to a diagonal Distance of 90 upon the Line of Sines::

So the lineal Diftance of 46.15 upon the Line of Lines:

Will (upon the fame Angle of the Sector) give the diagonal Diftance of 40 on the Tangents.

L 2

## CASE V.

The Base ac and Perpendicular bc given, to find the Hypothenuse ab;

Ift. as, ac: acb :: bc Tang. bac adly. as, bac : bc :: acb : ab= the Anf.

#### RULE by the Sector.

This is done by two Operations; ift, as in the 4th Cafe to find the Angle b a c: Then, fecondly, lineal Diftance of 40 on the Sines, fet to a diagonal Diftance of 46.15, on the Line of Sines :: The lineal Diftance of 90 on the Lines, will (the Sector continued in the fame Angle) give the diagonal Diftance of 71.8. = the Anfwer.

## CASE VI.

The Hypothenuse ab, and Base as given, to find the Angle abc; as,

ab: acb :: ac: abc.

RULE by the Sector.

As the lineal Diftance of 71.8 upon the Line of Lines: A Mathematical MANUAL. 149 Is to the diagonal Diftance of 90 upon the Line of Sines ::

So is the lineal Diftance of 55 upon the Line of Lines:

To the diagonal Diftance of 50 on the Line of Sines. = the Anfwer.

#### CASE VII.

The Hypothenuse *ab*, and Base *ac* given, to find the Perpendicular *bc*;

Ift. As, ab : acb :: ac: abc;

As Cafe 6, and the Complement of acb, is bac = 40.

2dly. As, abc : ac :: bac : bc.

RULE by the Sector.

Here being two Operations, the first is performed as under Cafe the Sixth: And for the fecond Operation;

As the lineal Distance of 50 upon the Line of Sines:

Is to the diagonal Diftance of 55 upon the Line of Lines :

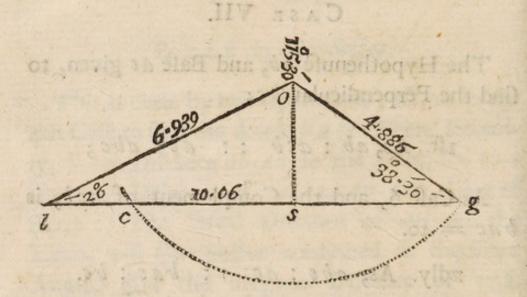
L 3

150 A Mathematical MANUAL. So is the lineal Diftance of 40 on the Line of Sines:

To the diagonal Diftance of 46.15 on the Line of Lines. = the Anfwer.

Here follow five Cases of oblique-angled plain. Triangles.

To the diagonal Difference of to on the Line



## CASE I.

The Angles olg and ogl, and Side ol given; To find the Side og; as,

ogl: ol :: olg: og.

#### RULE by the Sector.

As the lineal Distance 38.30 on the Line of Sines:

24

A Mathematical MANUAL. 151 Is to the diagonal Diftance of 6.9 on the Line of Lines::

So is the lineal Diftance of 26 on the Line of Sines:

To the diagonal Diftance of 4.9 on the Line of Lines.

#### etel glasbie own alle de che vo Sides /g leis CASE II.

The Sides ol and og, and the Angle og l given, to find the Angle olg; as,

ol: ogl.:: og: olg.

RULE by the Sector.

As the lineal Diftance of 6.9 on the Line of Lines:

Is to the diagonal Diftance of 38.30 on the Line of Sines ::

So is the lineal Diftance of 4.9 on the Line of Lines:

To the diagonal Diftance of 26 on the Line of Sines. = the Anfwer.

ASE

an A data Bo contil data and

bba sobia ani L 4

#### CASE III.

- So is the Tangent of half the Sum of the opposite Angles log and lgo:
- To the Tangent of half their Difference log lefs lgo:
- And the half Sum and half Difference added, give the Angle log:
- But the half Sum lefs, the half Difference gives the Angle 1 g o.

#### RULE by the Sector.

I shall leave to the Reader to find out, after fo many Examples of the manner of Operation: And shall only tell the Stranger to Trigonometry, that he may work any of the Cafes above, by the Tables of Sines, Tangents and Logarithms, taking the Sines of the Angles, and the Logarithms of the Sides, adding the fecond

### A Mathematical MANUAL. 153 fecond and third together, and fubtracting the first.

#### CASE IV.

The Sides 1g and go, and the Angle olg given, to find the Angle log; as,

go : olg : : lg : log

Its Complement to 180°.

# RULE by the Sector.

- As the lineal Diftance of 4.886, or 4.9, on the Line of Lines :
- Is to the diagonal Diftance of 26 on the Line of Sines ::
- So is the lineal Diftance of 10.06, or 10, on the Line of Lines :
- To the diagonal Diftance of  $64^{\circ}$  30' on the Line of Sines. = the Anfwer.

But in these Cases, observe, That the Angle now found (log) being very plainly an obtuse Angle, or above 90 Degrees; therefore the 64 30 must be only the Complement to 180 Degrees: So that 180 less 64.30, rests 115° 30' the true Quantity of the Angle log sought. And Note, when

when the obtufe Angle is given, you must work with its Complement.

#### CASE V.

The three Sides of an oblique-angled plain Triangle given, to find an Angle.

- As the Side lg is to the Sum of the Sides oland og = 11.82::
- So is the Difference of those two Sides = 2.053, to the Line lc = 2.413.

This may be done either by natural Numbers, or Logarithms, or by the Sector, thus:

As the lineal Diftance of 10 on the Line of Lines :

Is to the diagonal Distance of 11.8 on that Line of Lines ::

So is the lineal Diftance of the Difference = 2.053 on the Lines :

To the diagonal Diftance of 2.413 on the fame Line of Lines.

Secondly, Then the Side lg = 10.06, lefs 2.413 is = 7.647 = the Line gc; which divided by 2, gives the Side of the right-angled Triangle gs = 3.823.

Thirdly,

a - they a patron A

Thirdly,

As the lineal Diftance of the Side of the Triangle og = 4.886 on the Line of Lines :

- Is to the right Angle osg on the Line of Sines (taken diagonally) ::
- So is the lineal Diftance of s g = 3.823 on the Line of Lines :
- To the Angle (or diagonal Diftance)  $s \circ g = 51^{\circ} 30'$  on the Line of Sines.

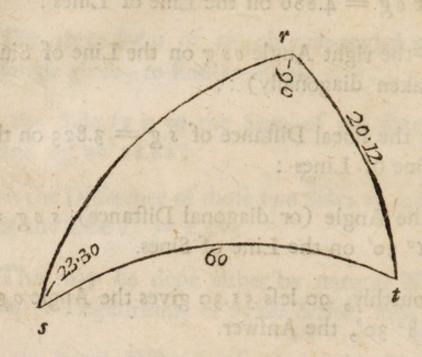
Fourthly, 90 lefs 51.30 gives the Angle og s= 38° 30', the Anfwer.

And thus, though I have not profeffedly treated on Trigonometry; yet the Rules above fhew how to folve any of the Cafes in rightlined plain Triangles, and effectially by the Sector. I fhall fhew next how to folve a Cafe in fpherical Triangles, and conclude the Ufe of this little portable Inftrument.

Note, That in right-lined Triangles the three Angles are equal to two Right, or 180 Degrees; but in fpherical, the three Angles are more than 180 Degrees.

0

The Angles  $srt = 90^{\circ}$  oo', and  $rst = 23^{\circ}$ 30', and Hypothenuse 60°; to find rt.



#### As, srt : st :: rst : rt.

#### RULE by the Sector.

Take the lineal Distance of 90 upon the Line of Sines:

Set that a diagonal Diftance from 60 to 60 on the Lines of Sines :

Then the lineal Diftance of 23.30 on that Line of Sines, will give you the diagonal Diftance 20.12 = rt on the Sines.

2

The

But it is not pretended that all the 28 Cafes of fpheric Triangles can be done the beft way by this Inftrument, of which I have fhewed the Ufe, &c. much more than I have feen done before, and in a more natural Methods

The Making, Defeription, and Ule

of the Line of Numbers, or Log

richms, commonly called Gunter's



SECT.



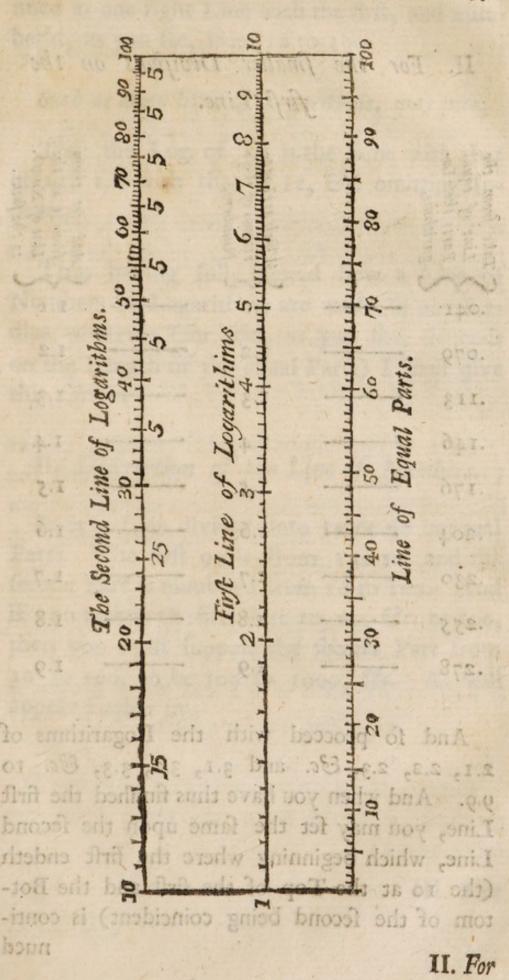
## SECT. VI.

test, much th

The Making, Description, and Use of the Line of Numbers, or Logarithms, commonly called Gunter's-Line.

I. For the great Divisions on the first Line.

in S Take from the D S Line of equal Parts thefe Lo- garithms,	w String are Lo- garithms of the fe Numbers,	8.200	is
.477	 3	-	3
.602	 4	-	4
.698	 5		5
-778	 6		6
.845	 7	A	7
-903	 8	Constitution of the same	8
·954	 9		9 The



159

II.	For	the	<i>Smaller</i>	Divisions	011	the
			firft L	ine.		

is S Take from the Line of equal Parts thefe Lo- garithms,	<ul> <li>Mhich are Loga-</li> <li>Tithms of thefe</li> <li>Numbers,</li> </ul>	I from 1 ou the Line of Numb.
.079	— I.2	I.2
.113	- I.3	I.3
.146	- I.4	1.4
.176	- I.5	1.5
.204 -	- 1.6	1.6
.230	- 1.7	1.7
.255	<u> </u>	1.8
.278	- 1.9	I.9

And fo proceed with the Logarithms of 2.1, 2.2, 2.3, &c. and 3.1, 3.2, 3.3, &c. to 9.9. And when you have thus finished the first Line, you may set the same upon the second Line, which beginning where the first endeth (the 10 at the Top of the first and the Bottom of the second being coincident) is continued A Mathematical MANUAL. 161 nued in one right Line with the first, and number'd, as you see, from 10 to 100.

### Such as know little of Logarithms, may note,

That the Log. of 1.1 is the fame with that of 11, 1.2 with that of 12, &c. omitting Indexes.

Thus having fully shewed how a Line of Numbers or Logarithms are made to any Radius whatever (for that, as you fee, depends on the Length of the equal Parts) I shall give this farther

# II. Description of the Line of Numbers.

It is a Line divided into twice 90 unequal Parts. The first 90 is from 1 to 10, and the fecond Part is number'd from 10 to 100. And if you reckon the first Part 10, 20, &c. to 100, then you must suppose the fecond Part from 10 to 100, to be 100 to 1000, &c. As will appear farther in

Extend the Compasses from t to either Dimension, and the fame will reach from the

QUEST.

other to 27 43.

III. The

## 162 A Mathematical MANUAL - mod bas, find odd ddw odd i digit ono, di bond 111. The Use of the Line in Multiplication, &c. QUESTION I.

What is the Product of 9 times 8?

Extend the Compasses from 1 to 8, and the fame will reach from 9 to 72 in the fecond Part. ebrocci and U.E.S.T. II. what is the Product of 20 by 40.

Here if you suppose the Beginning of the Line 10, then 2 is 20; to which extend the Compasses, and the same Extent will reach from 40 to 800. Or it may be done more plainly on the second Part of the Line.

Extend the Compasses from 1 to either Dimension, and the fame will reach from the other to 7.43.

and an in the second and

QUEST.

## QUEST. IV.

How many square Feet is there in a Table whose Length is 23.5 Foot, and Breadth 2.5 Foot?

Extend the Compasses from 1 to 2.5, and the fame Extent will reach from 23.5 to  $58\frac{3}{4}$ .

## QUEST. V.

## What is the Product of 7 s. 6 d. multiplied by 3 s. 9 d.?

The Pence in both being put in Decimals of a Shilling; then the Queftion will be to multiply 7.5. by 3.75. Therefore extend the Compaffes from 1 to 3.75, and the fame Extent will reach from 7.5 to 28.125, or 28 s.  $1\frac{1}{2}d$ . the true Anfwer: As appears plain; for 3 s. by 7 s. is 21 s. and the Fractions multiplied, make the Product 28.125, or 7 s.  $1\frac{1}{2}d$ . more.

M 2

QUEST,

die fame Estant will reach from 7.33 backward,

IV. The

to 1.75 - the Aufver

## IV. The Use of the Line of Numbers in Division.

## abole Length I. T. 2, Hugand Breadth 2.5

### What is the Quotient of 72 divided by 9?

Extend the Compasses from 1 to 9, and the fame Extent will reach backward from 72 to 8, the Answer. And this is the Rule for all.

## QUEST. II.

## What is the Quotient of 800 divided by 40?

Extend the Compasses from 1 to 4, or 10 to 40, and the fame Extent will reach from 800 backward to 20. = the Anfwer.

# .III .TESTUD the Compaffes

The Content of a long square Plank or Board, is 7.43 Foot, the Length is  $4\frac{1}{4}$ ; What is the Breadth?

Extend the Compasses from 1 to 4.25, and the fame Extent will reach from 7.43 backward, to 1.75. = the Anfwer.

Ma . . . IV. The

#### QUEST.

7.5. by 3.75.

from r to 3.7

#### odradi zanda QUEST. IV. to all sale.V

A Table contains 58.75 Feet, and the Breadth is 2.5 Feet; What must be the Length of fuch a long square Table or Parallelogram?

Extend the Compasses from 1 to 2.5, and the fame will extend backward from 58.75 to 23.5. = the Length, or Answer.

reach from 13 to 30, the Anlwer, in the foond

#### QUEST. Vani. I and to araq

There are two Sums, containing each a certain Number of Shillings and Pence; which being multiplied together, produce 28 s. 1 d.  $\frac{1}{2}$ . One of the Sums is 3 s. 9 d. : What is the other ?

Extend the Compasses from 1 to 3.75, and the fame Extent will reach backward from 28.125 to 7.5, or 7 s. 6 d. The Answer.

from 120 (calling 10, 100; and 2 of the

Note, These five Questions above in Division, prove those five in Multiplication : I shall now proceed to some Questions done by Multiplication and Division; or shew,

at the rate of 5 per Cont.?

Cal

Extend the Compasses Mackward from 100

V. The Use of the Line of Numbers, in the direct Rule of Proportion.

### QUEST. I.

What is the 4th Proportional to 13, when it is as 2 bears proportion to 6?

Extend the Compasses from 2 to 6 in the first part of the Line, and the fame Extent will reach from 13 to 39, the Answer, in the second part of the Line.

## QUEST. II.

Suppose 120 is in proportion to some Number, as 30 is to 80, what is that Number?

Extend the Compasses from 30 to 80 on the first Line (calling 1, 10; 2, 20, &c.) and the fame Extent will reach on the fecond Line from 120 (calling 10, 100; and 2 of the fmaller Divisions 20) to 320 very plainly.

#### QUEST. III.

thole five in Multiplication & thall

What is the Interest of 165 Pounds for a Year, at the rate of 5 per Cent.?

Extend the Compasses backward from 100 (calling 10 at the beginning of the fecond Line fo)

6) to 5 on the first Line, and the fame Extent will reach backward from 165 on the fecond Line, to 8.25 on the first Line, which is 8 and a quarter, or 8l. 5s. = the true and plain Answer:

# Ori; as, ido : 50 :: 165 : 82.5.

But because the Interest is but a 10th Part of 50; 1 therefore take but a 10th of the 4th Proportional 82.5, which is 8.25, or 81. 5 s. as is faid before. I mention this, that you may fee the Lines agree with the Description above.

### QUEST. IV.

#### What is the Interest for Half a Tear, of 3301. 105. at the rate of 6 per Cent.?

Extend the Compasses backward, from the beginning of the fecond Line (calling it 100 as before) to 3 (which is half a Year's Interest) in the first Line, and the same Extent reaches from 3301.55. on the fecond Line, to 9915 on the first Line; for,

As, 100 : 30 : 330.5 : 99.15 A 10th of which laft is 9 l. 18 s.  $3^{\frac{1}{2}}d$ .

Extend the Compafies from " Quarters in the

MA QUEST.

fo) to y on the first Line, and the fame Extent will reach back **y T**, **T B H 9** on the fecond Time, to 8 ay on the first Line, which is 8 and

If 560 lb. of Sugar cost 115 Shillings, what did the 112 lb. cost?

Extend the Compasses from 560 to 115 on the fecond Line (calling 10, 100, &c.) and the fame Extent will reach from 112 on the fecond Line, to 23 on the first Line; fo is 23 s. the Answer.

VI. The Use of the Line, in the single Rule of Proportion Reverse.

hid before. I incution this, th

## QUEST. I.

How much Stuff of 3 Quarters broad, will line 5 Tards of Cloth that is 7 Quarters broad?

Extend the Compasses from 3 to 5, and the fame Extent will reach from 7 (all on the first Line) to  $11\frac{2}{3}$  on the fecond Line.

# QUEST. II. Tribel entrie

How many Tards of Black Cloth of 7 Quarters wide, will bang a Room that is 46 Tards round, and 4 Tards bigh.

Extend the Compasses from 7 Quarters in the first Line to 46 Yards on the fecond Line, and the

the fame Extent will reach from 16 Quarters high, to  $105\frac{1}{7}$  (the first on the first Line, calling 1, 10; and the  $105\frac{1}{7}$  on the second Line, supposing 10 to be 100)

1501. be lent me to retaliate my Favour, suith-

#### QUEST. III. of alol the

fonths on that I

Suppose when the Price of a Bushel of Wheat is 6s. 3d. the Penny Loaf shall weigh 9 Ounces; what must such Loaf weigh, when the Bushel of Wheat is 4s. 2d.?

Extend the Compasses from 4 s. 2d. (or 50d.) to 9; and the fame Extent will reach from 6s. 3d. (or 75d.) to 13.5 Ounces. = the Anfwer.

## Took slode SQUEST. IV. med and it

phesol

If a certain Quantity of Provision will serve 400 Men for 6 Months, how many Men will the fame Quantity serve for 7 Months?

Extend the Compasses from 7 on the first Line to 40 (calling it 400) on the fecond Line; and the fame Extent will reach from 6 on the first Line to 343 (fere) on the fecond Line; which is the Answer.

Fix your Controlled at 40000 (" Hory to.

QUEST.

# bigh, to 105 V. T. S. T. S. On the first Line,

the fame Extent will reach from 16 Quarters

If I lend 2001. for 8 Months; how long must 1501. be lent me to retaliate my Favour, without Loss to either Party?

Extend the Compasses from 150 on the fecond Line (calling 10, 100, &c.) to 8 Months on the first Line, and the fame Extent will reach from 200 on the fecond Line, to  $10\frac{2}{3}$  Months on that Line. = the Answer.

# VII. The Use of the Line of Numbers in extracting the Square Root, &c.

COMDARCE NOM

Stit brisize

If the Sum be 100 or more, whole Root you would know, do it by the upper or fecond Line; but if lefs, do it by the first Line.

And if you point over Unit's Place, and fo over every other, the Points will shew the Places that the Root is to have.

# and the fame Baren of UEST. I.

# What is the Square Root of 40000?

Fix your Compasses at 40000 (calling 10, 10000) and take Half the Distance between that and 10, which will fall at 20; and because by

1

by the Rule above, 40000 would have three Points over; therefore this 20 must be 200, or have three Places, and fo is 200 the Square Root of 40000, found very plainly and accurately.

# Diffance to Io is 20. = the Anfwer, or Perpendienlar. By 47. II FT 2 H UD

#### What is the Square Root of 144?

Take half the Diftance between 144 and 10, which will fall at 12, the Root. And if it were required to fquare any Number, extend the Compasses from 1, or 10, &c. to that Number, and on that Point turn the Compasses, and the other Point will fall on the Square required. Thus,

# QUEST. III He Him Ist

#### What is the Square Root of 200°?

Extend the Compasses from 10, calling it 100, &c. to 20 or 200, and giving the Compasses a Turn on that Foot, the other will extend to 40000.

# QUEST. IV.

Having any two of the three Sides of a rightangled plain Triangle, to find the third? As fuppose the Hypothenuse be 50, the Base 40, and the Perpendicular is required? by the Rule above, acces would have three

172

By the laft Rule, fquare 50, which is 2500, and from that take the Square of 40, which is 1600, and the Remainder is 900; to which fet one Foot of your Compasses, and half the Distance to 10 is 30. = the Answer, or Perpendicular. By 47, 1 Euclid.

# QUEST. V.

I but is the addine Rook of Iga !

Suppose the Area of an Ellips, or other irregular Figure be 552.25; and I would know the Side of a Square, equal to the Ellips?

Set one Foot of the Compasses (as hath been taught) in the second Part of the Line, and take half the Distance thence and 10, which Half will fall at 23.5 the Side of the Square required.

VIII. The Use of the Line of Numbers, in extracting the Cube-Root.

## QUEST. I. .....

paffes a Tara on that Foot, the other will ex-

#### What is the Cube-Root of 1728?

Extend the Compasses on the second Line, calling 10, 1000, to a third of the Distance between 1728 and 10; then turn the Compasses towards 10 from the 1728, is one Third of the Distance; A Mathematical MANUAL. 173Diftance; and again, the fecond Turn, or two Thirds, is the Cube-Root fought = 12.

simmer of the ferend Fare of the This to sol

Note, If the Sum, whole Cube-Root you know, be 1000 or upward, do your Operation by the fecond or upper Line; but if lefs, by the first Line.

And if you point over Unit's Place of the Sum given, to have its Root extracted, and over every Third, the Points will shew the Places that the Root will confiss of.

that 20 is made 400, and 400, 8000, 60.

# QUEST. II.

#### What is the Cube-Root 8000?

By the Rule above of Pointing, it is plain that the Root must have two Places; therefore fetting your Compasses at 8000 (calling that 10 at the beginning of the fecond Part of the Line 1000, &c.) divide the Distance from that to 10, into three equal Parts; the End of the fecond Part next 10 from 8000 is 20, the Cube-Root required.

# Then fet one I at a of the Compasses at 154.8 and two. III .T 2 3 U 9 minutes from

For Proof of the last Question; I say, What is the Cube of 20?

Dir A.

# 174 A Mathematical MANUAL. Diffance: and again, the fecond Turn, or two

If you extend the Compasses from the beginning of the fecond Part of the Line to 20, giving the Compasses two Turns, the first will extend from 20 to 400, = the Square of 20; and the fecond Turn will extend from 400 to 8000, = the Cube of 20, or 20 times 4003and thus may the Cube-Root of any other Number be proved to be true. For, as in the last Example; because the Root confists of two Places, every Turn of the Compasses will increase by 10, and the Figure it extends to: So that 20 is made 400, and 400, 8000, Cc.

# QUEST. IV.

OUEST. II.

If a Sphere be 56 lb. weight, whose Diameter is 6 Inches; what is the Diameter on another Sphere of the same Matter, whose weight is 40lb.?

Extend the Compasses from 56 to the Cube of 6 (which is 216) and the same Extent will reach from 40 to 154.3 fere.

Then fet one Foot of the Compasses at 154.3 and two Thirds of the Distance from that to one backward, will fall at 5.36. The Answer.

And fo much for the Ufe of the Line, its Defcription and Making; which is more full and ample than has been done, I believe.

And it may be noted, That as the Weight, fo the Solidity of Spheres are in a triplicate Ratio of their Diameters.

Mysterious CURIOSITIES. in Mum-

bers; or, Numerical Novelties.



X A M

SECT.

A Mathematical MANUAL. 176 And to much for the Ufe of the Line, its STORE THE THE STORES And it may be noted, 'I hat as the Weight, fo the Solidity of Spheres are in a triplicate

# S E C T. VIII.

# Mysterious CURIOSITIES in Numbers; or, Numerical Novelties.

### PROPOSITION I.



HERE is a Number confifting of nine Digits; which being multiplied by five different Digits, each of the five Products shall have the nine Digits in it, and

neither more nor lefs; and the Sum of the five Products shall contain the 9 Digits and 0, which are the Characters by which all Numbers whatsoever are expressed.

EXAM-

EXAMPLE.

The Number proposed is \_\_\_\_\_ 123456789

Which mul-? 2 produceth 246913578)

0000

- 6913586247	493827156	These bave
- 493827605	617283945	each just
sysobitrasi	864197523	the 9 Digits,
1975308642	987654312	

3209876514 = Sum,[or 9 Digits and 0.

into 6 and 2. But if the Vumber propounded be multiplied b.II. .9 O .8.9

There is a Number confifting of 9 Digits, as the former, but inverted ; which being multiplied by 5 different Digits, each of the 5 Products will have in it neither more nor lefs than the 9 Digits and Cypher ; or each of the Products will have in it the fame Characters that were in the Sum of the Products in the laft *Proposition*, neither more nor lefs.

will exhibit a Quotients each, having the 9 Digits in it : And the Sum of those two Quotem, A x Hallo just the M Digits, and no more

#### EXAMPLE.

And the Sum of these Products hath the 9 Digits and Cypher, except the 8, which it splits into 6 and 2. But if the Number propounded be multiplied by 9, the Product will be all Eights, only one Nine. And if that last Product be added to the said Sum, that Total will have the 9 Digits again, except the 8, which it divides into 5 and 3.

# PROP. III.

A Number confifting of the 9 Digits naturally afcending, being divided by 2 and by 5, will exhibit 2 Quotients each, having the 9 Digits in it : And the Sum of those two Quotients hath also just the 9 Digits, and no more nor A Mathematical MANUAL. 179 nor lefs (allowing a 0, by way of Decimal, in the Dividend.)

# EXAMPLE.

The Number = 123456789

2) 61728394.5 =firft Quot.

5) 24691357.8 = fecond Quot.

The Sum of which Quotients is = 86419752.3, which is just the 9 Digits : And the like will arise from no other Divisors.

# PROP. IV.

If the 9 Digits naturally afcending, as before, be divided by 4, the Quotient will be the 9 Digits and 0; which is all the Characters that any Number is expressible by, and which will arife from no other Divisor whatever, more or lefs.

## EXAMPLE.

4)123456789(30864197.25 = Quot.

N2

-MA 1. 7 31

ois all the Murpher of Changes that can policity

PROP.

be ranged on a Bolls.

# PROP. V.

If the 9 Digits naturally defcending, be divided by 2 and by 5, the Quotients will each have just the 9 Digits and 0; and the Sum of those two Quotients will also be the 9 Digits and Cypher, or all the Characters by which any Number may be expressed.

Now this is the more strange, because 5 is a prime Number, and no Multiple of any.

#### EXAMPLE.

rom no other Nyifors

2)987654321(4938271605 = 1 Quot.

5) - - - - - 1975308642 = 2 Quot.

be divided by a the cuotient will be the o

Sum of Quotients=6913580247

P.P.OT.

# anon PROP. VI. on mont shine

any Number is expressible by, and which will

And now I am upon the 9 Digits; it may be obferved, that if they be multiplied any way one in another, (or, as one faid, jumbled together) the last Product shall however exhibit all the Number of Changes that can possibly be ranged on 9 Bells.

EXAMPLE.

M

Bells	I
Iultiply'd by 2 gives	2 Changes
2 by 3	6
· · · · · · · · · · · · · · · · · · ·	24 I
~~~ 5 <u> </u>	20
6 - 7	20
7 50	40
8 - 403	20 [Bells
borlai 9 - 3628	80 = Changes on 9

PROP. VII.

By placing 14 Figures to the greatest Advantage, there may be shewed not only the Numbers to be multiplied, but the Products sufficient for any *Multiplication Table*.

This Method, as a Curiofity in Numbers, I contrived about fourteen Years ago; and as follows, do give an

Alfo to fquare or multiply any in the Middle

N 3

EXAM-

of o times 8.

#### EXANPLE.

4	ed.	Bells	of
Multiply 2 of thefe.	Given 2 of thefe to be multiplied.	to a vel l	Add 2 thefe.
Mu of	Giru the mu	9 345 3	Ad
~	ow	pyriser-	ŝ
I	. 9	11.1	40
2	8	. 2.	30
3	•	. 10	20
4		- 7-	10
5	02805 -	- 8 -	

So if it were required to know the Product of 9 times 8.

In the To the Right To the Left.

Againft - - - 9 & 8 is 40 & 30,0170, & 1&2, =72So 9 times 7 - 9 & 7 is 40 & 20=60, & 1&3, =639 times 6 - 9 & 6 is 40 & 10=50, & 1&4, =548 times 7 - 8 & 7 is 30 & 20=50, & 2&3, 016=568 times 6 - 8 & 6 is 30 & 10=40, & 2&4, 018=48

And fo on.

Alfo to square or multiply any in the Middle by it felf, as 9.

s, do give an i

EXAMPL

s the Ratio left 7

In the Middle,

Againft 9 ftands 40, doubled is 80, & the 1 by 1 is 1=818 by 8 - 830,60, & the 2 by 2 is 4=647 by 7 - 720,40,33=9=49

And fo on.

#### PROP. VIII.

The Number 362880 may be continually divided by a different Digit from 1 to 9 inclufive, and no Remainder shall be of any of the Dividends, which cannot be faid of any other Number.

EXAMPLE.

3 : 1 :: 768 : 2%6 = the Sum of the reft .

3) 4) 2)362880(181440(60480(15120

6) 7) 8)9) 5)15120(3024(504(72(9(1 Quot. Rem. o [of all.

#### PROP. IX.

The Sum of an infinite Progression (which may be thought very unaccountable) may be found in Numbers.

 $N_4$ 

EXAM-

Ехамрие of the Series, &c. 768, 192, 48, 12, 3,  $\frac{3}{4}$ ,  $\frac{3}{16}$ ,  $\frac{3}{54}$ ,  $\frac{3}{236}$ , &c. ad infinitum.

Here the Ratio is 4 : Therefore,

As the Ratio lefs 1 :

Is to I :: IIV . TO AA

Canal Canal &

So is the first Term : To the Sum of all the rest of the Terms. Thus,

3: I :: 768 : 256 = the Sum of the reft 768 more the first Term.

1024 == the Sum of all, tho' the Progression had been continued to 10000 Terms lower.

# PROP. X.

A Perfon comes into a Bookfeller's (who was an Accomptant) and asks the Price of a Book, which he was told was 5s.: But he not willing to give it, the Bookfeller told him there were 100 Leaves in it, and if he would give a Pin (of 4 Rows a Penny, and 18 to the Row) for the

# A Mathematical MANUAL. 185 the first Leaf, 2 for the second, &c. to 100 in. clusive, he should have the Book : Which the Buyer willingly accepting, the Value was computed by this Rule in Progression.

Multiply the last (here the 100th Term) by the Ratio 2, and from that deduct the first Term (here 1); divide the Remainder by the Ratio, less 1, and the Quot. is the Sum of all the Terms of the Progression.

Computation of TAXAMPLES AND

By Multiplication, the 100th Term is equal to

World, it would furnifi each with an Effate of

633825300114114700748351602688

Which multiplied by 2, and 1 abated, gives the Sum of all the Terms, equal to

1267650600228229401496703205375 Pins. [Refts 15 Pins.

Which divided by 72, the Pins for 1d. gives equal to

17606258336503186131898655630 Pence. [Refts 2 d.

Which divided by 12, gives 1467188194708598844324887969 Shillings.

Which

Last Chere the Looth Term) by

Which reduced into Pounds, gives the Sum to be paid for the Book by Agreement,

the first Leaf. 2 for the fecond, Sc. to 100 in-

733594097354299422162443981.9s. 2d. 15Pins.

A Sum fo great, that Monfieur Bibliopol. would be content to abate the fifteen Pins, to be informed how he might come at fo much of the reft as would not be inconfiftent with his living out of *M. Fields*: For, according to the Computation of 300,000,000 of People in the World, it would furnish each with an Estate of more than 244,531,365,784,766,474 l. fo wonderfully incredible does this Way of computing increase fmall and inconfiderable Things: As in this Instance, from a Pin to a Sum more than the World is worth.

PROP. XI.

A Row of Decimals infinitely repeated, and, if you pleafe, Integers prefixed, may be multiplied by the like, and the true Product is exhibited by a very few Figures. Thus,

which divided by 12, gives

00344874887069

h & ells R.

Multiply

$$6\frac{2}{3}$$
 is =  $2\frac{0}{3}$ 

Now  $\frac{16}{3}$  by  $\frac{20}{3}$  is = 320

Which  $3\frac{29}{9}$  is = 35  $\frac{5}{3}$ 

Or = 35.5, repeated ad infinitum, as before.

This is a Curiofity which I have but lately contrived, but is yet more briefly done under the next Proposition.

There are three curious Mysteries in the foregoing Proposition.

First, That multiplying only the Prime's Place of the Decimals in each Factor should be made

made fufficient, by adding 2, to give a Number, (as here 320:) Which,

Secondly, Being added from the Right Hand toward the Left, should give the true Product (as here 3 and 5 repeated ;) it being contrary to the general Rules given by all, to add Units to Tens, and those to Figures in the Hundreds Place, &c. And,

Thirdly, That the Sum of the two last Figures in the Line should be a Repeater in the Product.

#### PROP. XII.

If Integers and Decimals are repeating Digits in the Multiplier; and if you multiply by one of the Repeaters, and the Product from the Right Hand toward the Left being added, and the Sum of the two laft having Tens added to Units, the Sum will be the repeating Decimal of that Product. And fo many of that Repeater as there are Integer-Places in the Multiplier, being put toward the Left Hand of the Point, you have the true Product, by making only one Line before it.

That maltiplying only the Frime's

THANK

MAXE the Decimals in each l'actor fibuld be

EXAMPLE.

Multiply 54321 of hum on I find od nod

by 6666.666666666666666666, &c.

325926 Add thefe Units to Tens, Ec.

In this Example, (befides the three Mysteries under the last Proposition mention'd) here is a fourth; *i. e.* That there should always be so many repeating Digits toward the Less Hand from the Point (of the same kind as those toward the Right Hand of it) as there are Repeaters towards the Less-Hand of the Point in the Multiplier.

In like manner the Example under the 11th Proposition might have been done (notwithstanding the great Number of Decimals in each Factor) by making only one Line (instead of three) besides the Product.

shat and there to be true.

The Sum is = 362139999.50

great Brange above, which proves both

Here

#### PROP. XIII.

But if the Multiplier were repeating Integers, then the first Line must be added in another Way to obtain the Product.

EXAMPLE.

54321

by 6666

Add this 325926

362103786 == Product.

PROOF.

The Product of =54321

by

.6 repeated

Is, as fhew'd before = 36213.999, 8c.

To which adding the Product, as in this last Ex-362103786ample, =

The Sum is = 362139999.9999,820

As in the Example above, which proves both that and these to be true.

Here

2

Here to add the Line, I fay 6: Then 6 and 2 is 8 in the Product: Then 6 and 2 is 8, and 9 is 17; 7 put down: Then 1 I carried, and 6 is 7, and 2 is 9, and 9 is 18, and 5 is 23; put down 3, and carry 2: Then, becaufe you have added as many as there are Places in the Divifor, leave out the 6 in Unit's Place, and fay, 2 carried, and 2 is 4, and 9 is 13, and 5 is 18, and 2 is 20; put down 0, and leave 26 out: and fay, 2 carried, and 9 is 11, and 5 is 16, and 2 is 18, and 3 is 21; put down 1, and carry 2: and fay, 2 and 5 is 7, and 2 is 9, and 3 is 12; I put 2 down, and carry 1, and 2 is 3, and 3 is 6; which put in the Product, and 3 is 3 there.

The Procefs here being a little intricate, becaufe new, I have directed you through the whole, proved as in the foregoing Page.

Note, 'That this is done by 18 Figures in 24 fewer than the common Way.

#### PROP. XIV.

How to avoid all unneceffary Figures in an Operation and Product, when there are many decimal Places in one or both Factors to be multiplied together, and yet to give an accurate Rectangle, as by the common Way.

それらいて、

EXAM-

EXAMPLE I.

Multiply 1.23456 by 9.87654, fo that there may be put 4 decimal Places in the Product, and yet they to be as valuable as if the whole Factors had been multiplied in the common Way.

12.1931 = the true Product, with fewer Figures than the common Way, by 20 in 37.

#### EXAMPLE II.

Multiply .12345 by .98765, and to have 4 Decimals only in the Product, which shall have 4 Places next the Point (which in most Cafes are sufficient) as true as if all had been unneceffarily multiplied.

Rectancie, as by the common Way.

.1219 = Product, with 22 [Figures in 30 fewer than the common Way.

- Note, 1. In this Way of Multiplication I revert the Multiplier.
- I put Unit's Place thereof under that decimal Place of the Multiplicand which anfwers to the Number of Decimals that I. would have in the Product.
- 3. I only multiply the Figures which ftand over that Figure I multiply by.
- 4. But I confider what would be carried, if two, or at leaft one of the Figures next the Right Hand of that which I multiply, were multiplied.
- 5. I place the Surplus above 10 of each Figure, which I first multiply, one under another, all next the Right Hand, and

not

not a Place more toward the Left Hand, as in the common Way.

By these Notes any one, I think, may perform Multiplication this Way.

### PROP. XV.

To know the Chances that may be thrown on any Number of Dice, from 1 to 6, is as by this *Table* of 1, 2, 3, *Bc.* to 6.

Die	e					niclatif, add may
I	I	2	3	4	5	6 Roots, or Points [on one Side.
2	I	4	9	16	25	36 Squares.
3	I	8	27	64	125	216 Cubes.
4	I	16	81	256	625	1296 Biquadrates.
5	I	32	243	1024	3125	7776 Surfolids.
6	I	64	729	4096	15625	46656 Squar'd Cubes.

TABLE I.

The uppermost Figures involved, produce the Powers under them.

The

The Right-Hand Column fhews the greatest Number of Chances that is on any Number of Dice from 1 to 6. That under 5 is the Number without a 6; that under 4, the Number without 5 and 6, 8c.

And that this is no more strange than true, I will demonstrate feveral Ways that the greatest Number of Chances on two Dice is 36. = the Square of the greatest Number of Points on one Side of a Dice.

The particular Chances on two Dice are thus:

TABLE II.

a li	6 +	6 +	6 +	6,+	6 +	6 = 36 [in all.
						Statement for Balances
	1,6	2,6	3,6	4,6	5,6	6,6
	1,5	2,5	3,5	4,5	5,5	6,5
	1,4	2,4	3,4	4,4	5,4	6,4
	1,3	2,3	3,3	4,3	5,3	6,3
	1,2	2,2	3,2	4,2	5,2	6,2
	1,1	2,1	3,1	4,1	5,1	6,1

Note, + fignifieth more, and = equal to.

0 2

A

A fecond Way thus :

TABLE III.

and and a state of the state of	1. C.					
1,1	1,2	2,3	3,4	4,5	5,6	
2,2	1,3	2,4	3,5	4,6		
3,3	1,4	2,5	3,6		I	
4,4	1,5	2,6		2	+2	14
5.5	1,6	Lecter A	3		+ 3	10
6,6		4		a Die	+4	
	5				+ 5	
6	0 10100	113 (47.8			+6	
				-		

.L. B. M.

XX I I du

== 21 Sum.

-

19 17

Farther,

As

, + fignificth more, and = equal to.

\$ 0

Chances = 15 + 21 = [36, as before.

TABLE

Ne

# TABLE IV.

A third Way for particular Chances on two Dice.

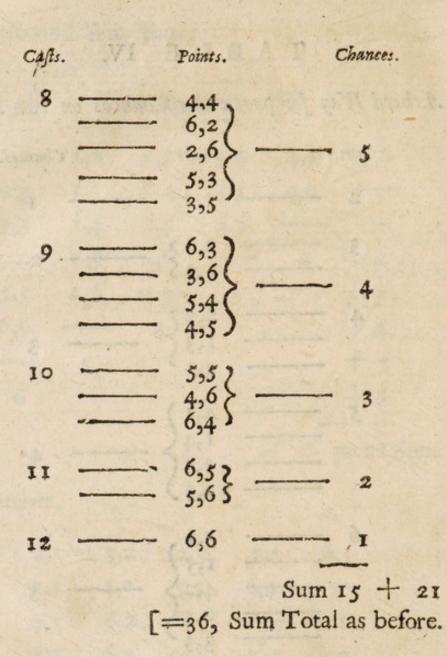
	2 10 5 10	
Casts.	Points.	Chances.
2	- 1,1	- I
3	- 2,I }	2
4	$\begin{array}{c} 2,2\\ 1,3\\ 3,1 \end{array}$	3
5		4
6	5,1 1,5 4,2 2,4 3,3	- 5
7	6,1 1,6 5,2 2,5 4,3 3,4	6 21 == Sun
	a area Chance	

0 3

Cafts.

n

198



Also in farther Use of *Table* I. to demonftrate that the Chances answer to the Number of Points in the uppermost Line, and the Number of Dice in the Left-Hand Column. Thus against 2 Dice, and under 3, stands 9; which shews that there are 9 Chances on 2 Dice, when the greatest Number of Points are but 3 on those Dice.

# Demonstrated thus:

Points. 1 & 1 2, 2 3, 3 1, 2 2, 1 1, 3 3, 1 2, 3 3, 2Sum = 9 Chances. 1, 33, 2

Secondly, That there are but 8 Chances on 3 Dice, when the greatest Number of Points thereon is 2. Thus,

1	Points.		-, <u>cc</u> , <u>cc</u>
18	18	[1]	Authors and a
2,	2,	2	The second states
2,	1,	I	
Ί,	1,	2	Sum = 8 Chances,
1,	2,	I	as by the Table.
2,	1,	2	Carrier and an and
2,	2,	I	
I,	2,	2	
	0	4 -	Thirdly,

Thirdly, That there 27 Chances on 3 Dice, when the greatest Number of Points thereon is 3. Thus,

Points.	Chances.
I, I, I	I State
2, 2, 2	I
3, 3, 3	I
I, 2, 2	2
I, 3, 3	2
I, 2, 3	2 .
I, 2, I	I
I, I, 2	2
I, I, 3	2
I, 3, I	the greates
2, 1, 2	I I Martin
2, 3, 2	I
2, 3, 3	2
2, 1, 3	
2, 3, I	2
3, I, 3	
3, 2, 2	2
3, 2, 3	I

no 200naj

of Points

S Chance

27=Sum Total,

PROP.

### PROP. XVI.

The Unciæ of Powers algebraically involv'd are the Figures which ftand towards the Left Hand of the feveral Members of the feveral Powers: As a + b being multiplied in it felf, gives aa + 2ab + bb; that is, 1a fquared, more 2ab, (or twice a multiplied in b) more 1b fquared.

And where the Unciæ are but 1, they are not put down, but supposed ; and so the Cube, Biguadrate, and Sursolid are as follow :

added in 5 lefs o, divide

#### a+b

Multiplied by -- a+b

Gives aa + 2ab + bb = the Square of a + b. Multiplied by - - - - a + b

Gives aaa + 3aab + 3abb + bbb = the Cube.

ner Bus and

Multiplied by ---- a+b

Gives aaaa + 4aaab + 6aabb + 4abbb + bbbb == the Multiplied by ----- a + b

Gives aaaaa + 5aaaab + 10aaabb + 10aabbb + 5 abbbb + bbbbb = [the Surfolid.

Here-

Here in this Surfolid, or fifth Power of a+b, it is plain the Unciæ are 1, 5, 10, 10, 5, 1. Now there is a Rule to find these Numbers without multiplying the Species, thus:

$$1 \times \frac{5-0}{1} (5 \times \frac{5-1}{2} (10 \times \frac{5-2}{3} (10 \times \frac{5-3}{4} (5 \times \frac{5-4}{5} (10 \times \frac{5-3}{5} (10 \times \frac{5-3}{5}$$

#### That is,

1	multiplied in	5 lef	ŝo	, divided by	1=5
10	the the second	5-	2		3=10
10		5-	3	CARACTER PRO	4 = 5
5		5 -	4	-	5 = I

Secondly, But there is a briefer Way of finding the Unciæ, and only by Addition, which is my own Thought, thus:

1, 1 = the Unciæ of the Root. 1, 2, 1 = that of the Square. 1, 3, 3, 1 = that of the Cube. 1, 4, 6, 4, 1 = that of the Biquadrate. 1, 5, 10, 10, 5, 1 = that of the Surfolid. 1, 6, 15, 20, 15, 6, 1 = that of the fquared [Cube,  $\mathcal{C}c$ .

Here 2 added from the Right toward the Left, gives those in the Middle respectively, and the 1's at each End of a Line put down as they are. Thus for the Unciæ of the Square; 2 in the Middle is the Sum of 1 and 1 above: For the Cube, 2 and I = 3, and 1 and 2 = 3, and 1 and 1 next the Right and Left: And in the Biquadrate from the Unciæ of the Cube, I fay, (1), 3 and 1 is (4), 3 and 3 is (6), 1 and 3 is (4), and (1) always to the Right and Left; those in () being the Unciæ, which are foon found.

Thirdly, But that which I chiefly infift upon as a Curiofity (under this *Proposition*) is the Rule for finding the Unciæ of any Member of any Power, without knowing those of the preceding Powers or Members.

This is also my own Invention: Altho' near feven Years afterward I faw a Rule very near it, used by an ingenious Author on another Occasion, not this.

To find the Unciæ of the fourth Member, or Term, of the fixth Power, put down the Digits to within 1 of the given Member, and multiply them together for a Divifor.

As here 1 by 2 by 3 is = 6, the Divifor. Then

Then put down as many Figures downward from the Power, as here, 6, 5, 4; which multiply together for a Dividend = 120, and the Quotient will be = 20, the Unciæ fought: As appears by the last *Table*.

So also the Unciæ of the 3d Term of the 4th Power will be found 6 :

For, 1 in 2 is 2, the Divifor.

And, 4 in 3 is 12, the Dividend, Quot. = 6 [Anfw.

So also the Unciæ of the 4th Term of the 5th Power is 10:

For, 1 in 2 in 3 = 6, the Divifor.

And, 5 in 4 in 3 = 60, the Dividend.

Quot. is as above.

Then

So, lastly, the Unciæ of the 10th Term of the 15th Power is thus found :

[Divifor. 1 in 2 in 3 in 4 in 5 in 6 in 7 in 8 in 9= And,15 in 14 in 13 in 12 in 11 in 10 in 9 in 8 in 7= [Dividend.

here r hy a by a is set 6, the Dividor.

Thus,

THE IS SHOT WITH

Thus,

For Divisor multiply For Dividend multiply

of own sits open a bit bit bit bit	by 14	1
Curiolicy.	210 by 13	2 by 3
R I Terr Firm	2730 12	6 4
For meding tire Barrel of Berrio	32760 11&1	24
rd amyiquina Bo	3603600	120 6
	32432400	720
	529459200 7	 5040 8
(5005 = Anfw.	81621440.03 181440	40320 9
[or Quot.	= Divifor.	36288.0

So that, according to the new Rule above, the Unciæ of the tenth Term, or Member, of the fifteenth Power, is 5005.

And if the greatest Man that ever was, thought it necessary to give the Rule under and at the End of the first Head of this *Proposition*, I hope the two New Methods under the fecond and third Heads (being much briefer and easier) will be taken as a great Improvement and Curiofity.

#### PROP. XVII.

For finding the Gallons in the Decimal of a Barrel of Beer, I have contrived the following curious and briefer Method than the common of multiplying by 36.

#### EXAMPLE I.

.6543 of a Barrel. 26.172 22.5548 Gallons and P.

23.5548 Gallons and Parts.

EXAMPLE II.

.4321 of a Barrel.

1.7284

15.5556 Gallons and Parts.

hth Power, is soos.

Here

Here I only multiply the given Decimal by 4, and fubtract the Product from it felf, as Units from 0, Tens from Units, &c. having first cut off from the Product one Place less than in the Decimal given.

So that as in former *Propositions* I have given the Answer by adding, so here by subtracting one and the same Line, Tens from Units, &c. A Thing never shewed by any other before, and what may be thought unaccountably curious by an impartial Reader.

# For briefly Valuing Decimals of Money, Weight, or Measure, by Inspection.

#### PROP. XVIII.

To write down, or know the Value of a Decimal of Money by Infpection.

EXAMPLE I.

Value of .1234 *l*. Is = 2s.  $5^{\frac{1}{2}}d$ .

to structure a thir drinker

ExAM-

EXAMPLE II.

Value of 456l. Is = 9 s.  $1\frac{1}{2}d$ . ferè.

EXAMPLE III.

Value of .67891. Is = 13 s. 7 d. prop?.

I have about Thirty-three Years ago publisted this Rule in The Merchant's Magazine, whose Vending hath been a sufficient Indication of its Usefulness.

In Example I. Double the Prime's Place is 2s. and the 23 in the fecond and third Places, are 23 Farthings, lefs 1, because above 13 is 22, or  $5\frac{1}{2}d$ .

In Example II. Double the 4 in Prime's Place is 8; and because the Second's Place amounts to 5, add 1 is = 9s. and the 6 is Farthings: So 9s.  $1\frac{1}{2}d$ . is the Answer.

In Example III. Double the Prime's Place is 12; to which add 1, becaufe the Second's Place is not lefs than 5, makes 13 s. Then the

the 2 above 5 in the Second's Place, and 8 in the Third's Place, I call 28 Farthings; which I should make lefs by 1, (as under the first Ex-ample) but do not, because the fourth Place from the Point is above 6. So 28 Farthings is 7 d.; and 13 s. and 7 d. is the Answer.

Note, I was the first that gave the Reason of this Rule in my Book above.

#### PROP. XIX.

To find the Value of the Decimal of a Pound Troy (mostly) by Inspection.

EXAMPLE I.

add the Digit next the Right Hand to the Pro-

.8765 3 10.5180 Or, 310. dwt.10. gr.9.

 $E_{XAMPLE}$  II. .7654  $\Xi 9.1848$ Or,  $\Xi 9. dwt. 3. gr. 17.$ EXAM-

I doithe E X A M P L E III. I abid I st mould make lefs by 1. (as under the frift Ear-

the a above 5 in the Second's Place, and 8 in

ample) but do not, 25432 the fourth Place ₹ 6.5184 Or, ₹ 6. dwt. 10. gr.9.

Note, I was the first that gave the Reafon of

from the Point is

is rd. ; and ras.

The Penny-weights and Grains found entirely by Infpection ; as follows :

The Answers to the three last Examples are produced thus : To find the Value of

First, Multiply the given Number by 2, and add the Digit next the Right Hand to the Product, &c. and when you come to the Digit next the Left Hand, and have multiplied that, add the Tens carried to that Digit, which in the first Example is 10.51803. And fo of the reft. Or. 310. dat. 16. gr. 9

Secondly, For Penny-weights, double the Prime's Place of the Decimals of an Ounce, and if the Second's Place be 5, or more, add 1; (as in the fecond Example.)

Thirdly, For the Grains, take half what the Second's Place is above or under 5, and the Third's Place, for Grains. So in the faid fecond Example, 8 is 3 above 5; which 30 added

A Mathematical MANUAL. 211 to the Third's Place, 4, is 34; half of which is 17 Grains : And fo of the reft. Which is all new and eafy.

See alfo Prop. XXII. for the Decimal of a Foot by Infpection.

#### PROP. XX.

When the Value of any Integer is 2, the Value of any Number is known, by cutting off Unit's Place with a Point. So those towards the Left Hand are Pounds, and those towards the Right are fo many 2 Shillings.

EXAMPLE I.

1234 at 2 s. each Are, 1231. 8s.

EXAMPLE II.

EXAMPLE.HL

56789 at 2s. Are 56781. 18 s.

This is done by mulciplying the Number of

baos

Integers by III A M P L'E TILL VI angestil Unit's Place with a Point from the Foduct. 8.008 ai 4881 2098765 at 2.5. find orh ni o2 a lo alemicol Are, 98761, 105. of bas al Pound : In the first Example, 165. in the fe-PROP. P 2

Which is all

is' 2, the

# PROP. XXI.

to the Third's Place, 4, is 34; half of which if

If the Value of an Integer is any even Number of Shillings, the Value of the whole is found, without putting down a Figure befides the Anfwer.

EXAMPLE I.

1234 at 14s. Is l. 863.8. Anfwer.

EXAMPLE II.

Right are fo many a Shillings.

Arc, 1231 85.

4567 at 16s. Is 1.3653.6. Anfwer.

EXAMPLE III.

6789 at 18 s. Is 1.6110.1. Anfwer.

Are 56781 185.

This is done by multiplying the Number of Integers by half the Price of 1, and cutting Unit's Place with a Point from the Product. So in the first *Example*, 7 times 1234 is 863.8, Ec. and the Digits cut off are Decimals of a Pound : In the first *Example*, 16s. in the fecond A Mathematical MANUAL. 213 cond, 12 s. Ec. by Prop. XVIII. for valuing a Decimal by Infpection. Vid. Prop. XXIII.

Ways are allo New.

-hhA

# PROP. XXII.

The Value of the Decimal of a Foot in Inches and Quarters is thus found by Infpection cafily.

of those Integers may be found by their three

EXAMPLE I.

.26 Foot. Value = 3 Inches, 0 Quarters.

EXAMPLE H.

.45 Foot. Value = 5 Inches, 2 Quarters.

EXAMPLE III.

.89 Foot.

Value = 10 Inches, 2 Quarters.

The Prime's Place is fo many Inches and fo many Quarters.

The Second's Place is fo many Half-Quarters. But if it be 3, or upward to 6, deduct 1; 6, P 3 or

or upward to 9, deduct 2; 9, 3. Never done before by any other. Two of the following Ways are also New.

# PROP. XXIII.

When the Value of an Integer is any odd Number of Shillings, the Price of any Number of those Integers may be found by these three short Ways.

#### The first Way.

5432 at 135. each.

Add { 1. 3259.2 271-125.

Sum 1.3530 - 16 s. Anfwer.

The fecond Way.

5432 at 13s. each. 7061.6 1.3530 - 16s. Anfwer,

me's Tinde is to many Inches and 19;

The

A Mathematical MANUAL. 215 an initial of a complete of an initial of a complete of the third way.

5432 at 135. each.

Parcels (each 10) non 00 had? Parcels (each 10) no 00 had? I.3530 — 16s. Anfwer.

In the first Way I work for 12s. as is done under Prop. XXI. and to the Product add half the 5432, except Unit's Place.

another, beginning at ap, 6%, downward for

To antwor this, the Number of Parods

In the fecond Way I multiply the 5432 by 3, and add the Figure next the Right Hand as I proceed, &c. As under Prop. XIX. Rule the First.

In the third Way I multiply the given 5432by 65 = the Decimal of 13 s. which is eafily done without making a Digit befides the Anfwer: For I fay, 5 times 2 is 10, 0 and carry 1; 5 times 3 is 15, and 1 is 16, and 6 times 2, or 12, is 28, put 8 down, and carry 2, &c. So that Product is l.3530.80, or l.3530, and the .8, by the Rule under Prop. XXI. is 16 s.

This Way of multiplying by two Figures is very eafy when much ufed. I feldom make P 4 two

-MAX

two Lines for two Figures in the Multiplier, as appears by the next Proposition.

#### PROP. XXIV.

Out of twenty Things, how many different Parcels (each 10) may be had?

To answer this, the Number of Parcels from 1 upward must be multiplied together continually for a Divisor; and so many of the 20 as there are Parcels must be multiplied one in another, beginning at 20, &c. downward for a Dividend. So the Quot. is the Answer.

a, and add the Figure next, the Right Hand as

In the third Way I multiply the given \$432

by 65 = the Decimal of each which is cally

done without making, a Digit belides the An-

face: For Links sectors sizes, o and carry ;;

5 times 3 is 15, and 1 is 16, and 6 times 2, or

-that Product is Largo So, or Largo, and the

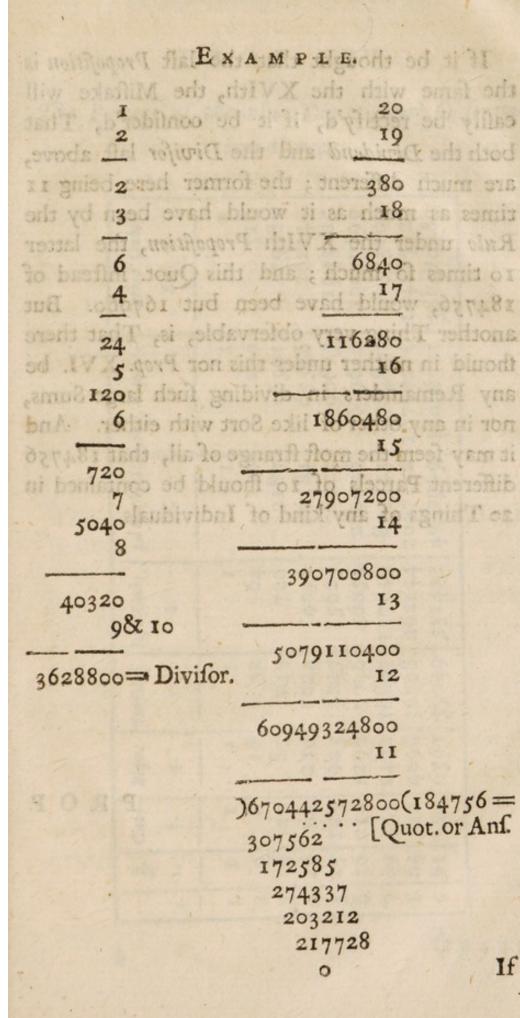
This Way of multiplying by the Pigures is

very early when mach ufed. I feldom make

Is, is 28, put 8 down, and carry a, Sc.

.S. by the Rule under Prop. XXL is 16 r.

EXAM-



If it be thought that the last Proposition is the fame with the XVIth, the Mistake will eafily be rectify'd, if it be confider'd, That both the Dividend and the Divisor last above, are much different; the former here being II times as much as it would have been by the Rule under the XVIth Proposition, the latter 10 times fo much ; and this Quot. instead of 184756, would have been but 167960. But another Thing very observable, is, That there should in neither under this nor Prop. XVI. be any Remainders in dividing fuch large Sums, nor in any other of like Sort with either. And it may feem the most strange of all, that 184756 different Parcels of 10 should be contained in 20 Things of any kind of Individuals.

390700800

0010110400

#### PROP.

#### PROP. XXV.

# The Powers of the nine Digits, with Observations thereon.

are therefore called fighterical or circular

	and the second
Cubed Cube. Exp. 9.	I 512 512 19683 262144 1953125 10077696 40353607 134217728 387420489
Squ. Biquad. 8.	1 256 6561 6561 65536 390625 1679616 5764801 16777216 43046721
zd Swrfolid. 7.	128 128 2187 2187 16384 78125 279936 823543 823543 823543 2097152 2097152
Squ.Cube. 6.	1 64 729 4096 15625 46656 117649 262144 262144 531441
Surfolid. 5.	1 32 243 1024 3225 7776 16807 32768 32768 32768 32768
Biqu. 4.	16 81 81 81 81 81 625 625 625 1296 2401 4096 6561 6561
Cube 3.	125 125 216 343 343 729
mbs a	н 4 6 4 2 6 4 9 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
-2-2-	

OBSER-

II

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filler,

3 1110

s at

#### OBSERVATIONS.

I. That the Unit's Place of all the Powers of 5 and of 6, are 5 and 6 respectively, and are therefore called spherical or circular Numbers.

II. That the Unit's Places of the Powers of 4, are 6 and 4 alternately.

III. And those of 9, are 1 and 9 alternately.

IV. Unit's Place of the Square and fquared Cube	Arejust the
	fame from
V. Unit's Place of the Cube and Surfolid	Top to Bottom;
	and the 2
VI. Unit's Place of the Biqua-	last are
drate and square Biquadrate	the 9 Di-
VII. Unit's Place of the Surfo-	gits each;
lid and cubed Cube, viz. The	which is
Places of the Powers 2d and 6th,	the XIth
3d and 7th, 4th and 8th, 5th	Observa-
and 9th	tion.

VIII. That the Number of Places in the Powers of 8 and 9, are equal to the Roots 8 and 9.

IX. The

 $\mathcal{I}$ 

IX. The Exponents of the Square being 2, of the Cube 3, the Biquadrate 4, the Surfolid 5, Cubed Cube 6, &c. I fay the Sum of the Exponents of any two Powers is equal to the Exponent of the Rectangle of those Powers: So where the Root is 4, and the Exponents 2 and 6; I fay, the Sum of the Exponents 2 and 6 is 8, equal to the Exponent of the Rectangle of the Powers 4096 by 16 = 65536: As by the Table. And Double the Exponent is = that of the Square of the Powers.

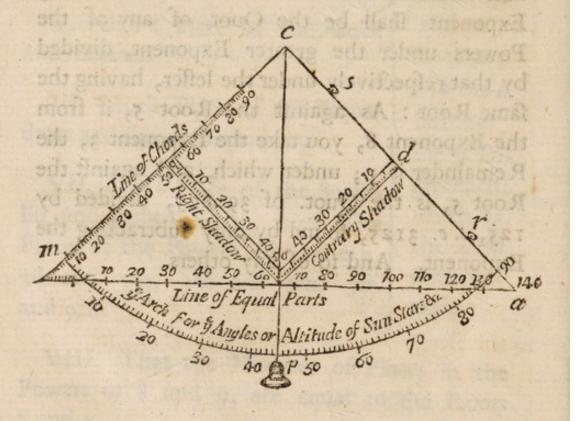
X. and Laftly, If from any Exponent you take another, the Power under the remaining Exponent shall be the Quot. of any of the Powers under the greater Exponent, divided by that respectively under the lesser, having the fame Root : As against the Root 5, if from the Exponent 8, you take the Exponent 3, the Remainder is 5; under which, and against the Root 5, is the Quot. of 390625, divided by 125, *i.e.* 3125, found by only subtracting the Exponent. And fo of any others.



# SECT. VIII.

INSTRUCTIONS how to take Heights, Depths, and Diftances, feveral Ways, great or small.

The QUADRATIC INSTRUMENT.



SEC

I. To

I. To take ALTITUDES.

1. The Use of the Square q, a, d, c, q, and the Line and Plummet c, p.

#### PROPOSITION I.

n measure on equen Ground from

To take the Altitude of a Tower, Steeple, House, Tree, &c.



OOK at the Top of the Object through the Sight r, s, (with rnext your Eye) and go forward or backward, till, at the fame time that you fee the Top of

the Object, the Plumb-Line falls at 50 Parts in the Square : Then measure from your Foot to the Bottom of the Object where it touches the Surface of the Earth, and that Distance, adding the Distance of your Eye from the Ground, is the Altitude of the Object required.

So if I find from my Foot (for Example) to the Bottom of the Object, 91 Foot, more 5 is 96 Foot, the Height required.

to meafine the Diffance () at which

Jeffance looking through the Sights at the Top od ... Object, I find the Plumb-Line cutteth 2

16.2

2. The Use of the Side Right Shadow q, a.

#### PROP. II.

To take the Height of any Object from any Place to which you can measure on even Ground from the Bottom of such Object.

The foregoing Method is for fuch as underftand not the Rule of Proportion : This is for fuch as do.

The Use of the Foreside, or Right Shadow, is for such Distances of the Place where you observe to the Bottom of the Object as exceeds the Height of that Object.

# the Bottom of La J q M A X H at the bottom of La J q M A X H

the Square : Then measure from your Foot to

I will take the Altitude of the foregoing Object from a Station which I will fuppofe 120 Foot from the Botrom (becaufe I cannot come nearer it, by reafon of fome Impediment or Water or Morafs, &c. but can fend one round with a Clue of Packthread, keeping one End in my Hand to meafure the Diftance;) at which Diftance looking through the Sights at the Top of the Object, I find the Plumb-Line cutteth 2 40 Parts A Mathematical MANUAL. 225 40 Parts : Then I fay, by the Rule of Proportion,

As 50, the whole of the Fore-fide, or Right Shadow :

I'm Fin of the cont

Is to 120, the whole Diftance ::

So is 40 Parts cut by the Line :

To 96, the Altitude of the Object required (as before.) Thus,

50 : 120 :: 40

of the foregoing Object but cannot go tartiter

from the Bottom of the Opref than as Foot

(50)480.0(96) = the Altitude, as

svoda] ooking through the light at the Top of

the Lower, Sa the Togad cuts 37.9 in con-

As the Parts cut by the Thread = 27.5 :

Is to the Diffance that Is im from the Bot-

tom of the Tower (more Height of my

trary (or back) Shadow Then I fay,

So is yo, the whole of contrary Shadow

and i do an and a churid A or 3. The

Eye) 72 20 20

3. The Use of the contrary Shadow a, d.

# PROP. III. Wobade

To take the Height of any Object from which you cannot go so far backward as to make the Thread fall at 50 Parts.

#### EXAMPLE.

(as before.) "Fines,

I will fuppofe I were to take the Altitude of the foregoing Object, but cannot go farther from the Bottom of the Object than 72 Foot (by reafon of fome Impediment behind me;) where looking through the Sight at the Top of the Tower, &c. the Thread cuts 37.5 in contrary (or back) Shadow. Then I fay,

As the Parts cut by the Thread = 37.5:

Is to the Diftance that I am from the Bottom of the Tower (more Height of my Eye) 72 ::

So is 50, the whole of contrary Shadow :

To the Altitude as before = 96. Thus,

37.5

37.5 : 72 :: 50

50

antine. " O. 1. 52.8 - : 0, 72.0

37.5)3600.0(96 =the Altitude as [before.

Note, In these Cases it is necessary to take the Altitude of one and the same Object, that so the Agreement of the several Ways may demonstrate the Truth of each; which others on this Subject not having done, have render'd their Answers uncertain.

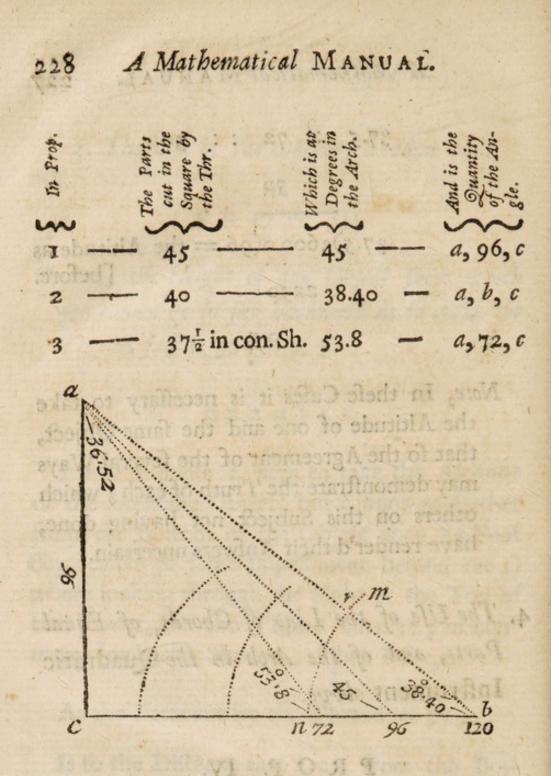
4. The Use of the Line of Chords, of Equal Parts, and of the Arch in the Quadratic Instrument above.

# So without the Square, only by the three

The second Proposition above performed by these Lines geometrically, according to the following Scheme, which is a Demonstration of the Truth of the three first Propositions.

Q 2

Nota



So without the Square, only by the three Lines above, to take the Altitude of ca; I stand at b, because I cannot well come nearer, and looking at a through the Sights, I find the Thread cuts  $38^{\circ} 40'$ ; and measuring the Distance bc, I find it 120 Foot.

0 2

# 5. Now to lay this down upon Paper,

I draw a Line, cb, at Pleafure ; then taking 120 from the Line of Equal Parts on the Inftrument, it extends from c to b; Thirdly, I erect the Perpendicular ca; Fourthly, With 60 Degrees of the Line of Chords, fetting one Foot of the Compasses in b, I describe the Arch n, m; Fifthly, Becaufe the Angle at b (or a b c) is 38.40, I therefore take that from the fame Line of Chords, and fet it from n to r; Sixthly, I lay a Ruler from b to r, and draw a Line from b, till it interfect the Perpendicular c a, which it doth in a; therefore, Seventhly, I take the Diftance ca, and applying it to the faid Line of Equal Parts, I find it 96, == the true Altitude required. And alfo in like manner may you take the Height at the other z, &c. Stations.

And note farther, That by this Way you have also the Hypothenuse ab, by taking it between your Compasses, and applying it to the fame Scale of equal Parts; which is done easier and speedier than by the 47, 1 Euclid, of taking the square Root of the Sum of the Squares of the Base and Perpendicular cband ca.

Q 3

# 6. A third Way to find the Altitude c a, Arithmetically.

Having with the foregoing Inftrument taken the Angle at the Station b, and the Diftance b c; fay,

As Radius — Io.

then taking

6. A

To the Diftance bc = 120, its Log. 2.079181

So is the Tangent of the Angle 9.903199at  $b = 38^{\circ} 40'$ 

To the Log. of ca = 96 - 1.982380

And fo of any other Altitude, and the other Stations for this.

# PROP. V.

To take greater Altitudes, as of the Stars, Sun, or Moon, by the Quadratic Inftrument.

Look through the Sights, with r next your Eye, and when you fee the Star, obferve how many Degrees are cut in the Arch by the Thread from m towards 90; and fo many are the Altitude above the Horizon.

2. Or, for the Sun: You may hold up your Quadrant with s next the Sun, and when the Point of the Sun, fhining through the Hole at s, falls upon the Hole at r, the Degrees then cut by the Thread in the Arch, is the Sun's Altitude above the Horizon.

3. For the Meridian Altitude : Take the Altitude of the Sun, as before, at 12 a-Clock, by fome good Dial that hath Minutes, and making Allowance for the Time in the Table of the Equation of natural Days, the Degrees cut by the Thread shew the Meridian Altitude of the Sun that Day.

# II. To take DEPTHS Several Ways.

#### PROP. I.

How to take the Depth of any Well, or of the Eye of any Coal or Lead-Mine, &c.

-

V

Si Of

51

A TABLE shewing the Feet that an heavy Body falls in any Number of Seconds, not exceeding 12, and to take Depths thereby; and also without the Table, by the 4 of the Ist, and 3 of the IId Prop.

Seconds an heavy Bo- dy falls.	Feet it falls in each Se-	Sums of the Feet that it falls.
I	16 -	16
li læ	481-	64
3	80	144
4	112 -	256
5	144	4.00
6	176 -	576
1 70 7	208 -	784
8	240 -	1024
9	272 -	1296
10	304	1600
II	336	1936
15	368	2304

This

A

#### This Table is made feveral Ways :

1. For if you multiply the first of the Middle Column by 3, it gives the 2d Number; by 5 the 3d, by 7 the 4th, &c. Or,

2. If you add 32 to the 1st, &c. continually, you will have all the Numbers in the fecond Column.

3. If you add the two first Numbers in the middle Column, you have the fecond Number in the third Column; the three first in the fecond gives the third in the third, &c. Or,

4. Without the fecond or third Columns, the Sum of the Feet that any Body falls in any Number of Seconds may be found by confidering that the Diftance is as the Square of the Time. So if you would know how far a heavy Body falls in 5 Seconds, I fay,

As  $I : I6 : : 5^2 = 25 : 400$ . As in the third Column.

Or in 6 Seconds fay;

I : 16 ::  $6^2 = 36$  ; 576 As in Col. 3,  $\mathcal{C}_c$ .

PROP,

the Watch, which is e

#### PROP. II.

# To take a Depth by your Watch and the third Column.

Observe how many Beats of the Watch there are between letting the Body fall, and hearing the Sound of it when it comes to the Bottom, which fuppose 12: Now in 12 Beats, reckoning 4 to 1 Second, is 3 Seconds; against which, in the third Column, is 144 Foot, the Depth.

# For a IId EXAMPLE.

Suppose it 24 Beats of the Watch from the Time it is let fall, to the Time you hear the Sound at the Bottom; that divided by 4 is 6 Seconds; right against which, in the third Column, is 576 Foot, or 192 Yards, the required Depth.

#### EXAMPLE III.

Suppose the Time of falling is 22 Beats of the Watch, which is 5.5 Seconds; then by the 4th Paragraph above,

" F. " Foot. As  $1 : 16 :: 5.5^2 : 484$ , or  $161\frac{1}{3}$  Yards, =the [Depth, without the Table above. So

Time from Int-

12

前屋

AI

E.S.

Dr.

PI

Br.

Time

So much for taking Depths in the Medium of Air. Now for Water.

But note, The Body you let fall may be about 5.25 Inches Diameter, and Round.

Note also, That 5.5<sup>2</sup> is 5 and an half squared or multiplied in it felf; and so 6<sup>2</sup> is 6 squared.

The Depth above being in Air, what follows in this Proposition is in the Medium of Water.

-----

#### PROP. III. 8

13.7 ----

6.3+

5.0 -:-

- Ante

1.9

+ 4.8

0.0

9.5

How to take any Depth at Sea, without a Sounding Line.

In order to which, I shall give the following TABLE.

236		athematical Im-		
fedium	merfion t	E-alique	Fathoms	11.02
	merjion.	iter.	deep.	TA To
the sale	"I	-		
		ly you let		Bat
	DAIRCA.	bus coran	ald muringen	about 3
barreno	- 3	n bua y ai J	1.6-	
· b.borei		Section and the section of the secti	11 12.1 +	tions and
	. Jack		an Nem In In	
and the	Sid	t ur Sund	avoda2.6.+	The
in ofe	6	da <u>ni si (o</u>	3.2-	ia nwoi
and the second second	7		3.7-	Water,
	1.	He line		
	8		4.2+	
in a tang	9	2	4.8-	ilere
	IO	ing Line.	Sound -	
San Marine	Jan Bar		5.3-	
Suimol	11	ovi <del>entin</del>	5.8+	10 61
Supply	12	/	6.3+	Part L
	13		AM AND	
	- 5		6.9-	
	14		7.4	
Aller Marchi	15		7.9+	
Same	16	and the second		
		Fin	8.4+	
stat ca	17		9.0-	with the
	18		9.5	
				Time

- 1

237

Time from Im- mersion to E- mersion.	Fathoms deep.
19.01	10.0+.
2000	- 10.6-
-21 02	· II.I-
22	- 11.6+
23 12	- 12.1+
24 22	- 12.7
25	- 13.2-
26	- 13.7+
27.82	- 14.2+.
28 10	- 14.8-
29	- 15.3+
30.22	- 15.8+
-31 2	- 16.4-
-32.02	- 16.9-
332.00	- 17.4+
34 72	- 17.9+
35.82	- 18.5-
-36:82	- 19.42

2 ime

Time

Time from Im-	Elips from Im-
mersion to E- mersion.	Fathoms deep.
-37.01	
-38.or	
39.11	20.6-
49.11	21.1+
44.21	- 21.6+
42.01	- 22.2 -
-43.81	22.7-
44 81	- 23.2+
45	- 23.8-
-46 pi	- 24.3
47.23	- 24.8 +
48 21	25.3+
49.01	- 25.9
-59.31	26.4
54.7I	26.9+
520.71	- 27.4 +
-532.81	- 28.0
54.ez	- 28.5

Time

28110

\*

Time from Im-	W your De
mersion to E-	Fathoms
mersion.	deep.
II is the second of the	C. Xuyman
55	29.0+
). by the ass, the	n abovefaid
56	29.6-
57	30.1
58	30.6+
e not fo much lefs as.	ad all at -
59	31.1,+
were short a new de	and second
60	31.7 -

-DI STITZ

reconser :

It hath been tried in fhallow Water, that if you take a varnish'd Ball of light Wood, and on that fix a Hook a very little hooked, and to that hang a Weight that will eafily fink it; when the Weight comes plump to the Bottom, the Ball will be difengaged, and come up again; and from the Time the Ball is all covered with the Water, to the Time it appears again, i.e. from its Immersion to its Emersion, being found in the Table (taken by the Beats of a Watch, or rather by a Pendulum, which vibrateth Seconds, to fave the Trouble of dividing the Beats by 4) right against that Time you have the Depth; as hath been found by Experiments. Which Table is grounded on this Proportion, that the Ball will be under Water 6 Seconds, when the Depth is 3 Fathom and I Sixth, or 3.1666666; or, as 36 to 19.

Or if your Depth exceed what is in the Table ; as, admit the Ball is immers'd 285 Seconds : If you multiply .52777, which are the Fathoms answering to I Second (according to the Proportion abovefaid) by the 285, the Product will give the Depth = 150.4 Fathom.

Note, That + in the foregoing Table fignifyeth more, but not fo much more as .05; and that - is lefs, but not fo much lefs as .05 : Or, the Depth to the Time is near I Yard in I Second, being but about 3 Yards over in 60 Seconds; as by the Table.

#### PROP. IV.

It inth been tried in faillow Water, that if

bes in oot, and

Being at the Top of a Tower, &c. how to take the Depth or Length down to the Bottom or Surface of the Earth, by Help of the foregoing Quadratic Instrument. the Water, to the Time

I will inftance in the Diftance under Prop. II. for taking Altitudes. Being at the Top of the Tower ac, (fee the Triangle abc) I order some one to fet up a Mark at b; then I look at that thro' the Sights, with that Sight next my Eye which is next o the Center, and I find the Thread cuts 51° 20', which is the Angle cab, or at a; then I subtract 51° 20' from 90, and the Remainder is 38.4.0. the Angle a b c. Then I fay,

2.0

As the Sine of 51.20 — 9.892536Is to the Log. of the dift. meafur'd 2.079181 cb = 120 — 2.079181So is the Sine of the Angle at b, 39.795733 38.40 — 39.795733To the Log. of the Depth ac = 96 - 1.982278

Or this may be done Geometrically in all Refpects, as under the faid IVth Proposition for taking Altitudes; after you have acquired the Angle abc, or at b, by taking the Complement of 51.20 to 90.

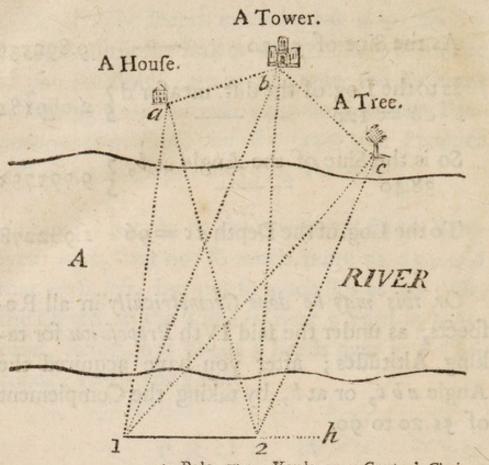
III. To take DISTANCES Several Ways.

#### PROP. I.

To take leffer Distances by the plain Table, and fupposing the Places are inaccessible from the Places where you make your Observations.

As for EXAMPLE.

Admit it were required to take the Diftances following from 1 to a, to b, to c, &c over a River : I place my Inftrument at 1; and applying the Edge of the Index to that End of R the 242



40 Pole, or 220 Yards, or 10 Gunter's Chains.

the flationary Line, I turn it till I can fee the Mark at a, and then draw a Line by the Side of the Index directly towards a, as 1 a; then keeping the Edge to the fame Point, I turn the Index till through the Sights I can fee the Bottom of the Tower at b, and then I draw the Line on the Head of the Table, as 1 b, and then I turn the Index till I fee the Tree at c, and draw the Line 1 c. All the three Lines thus drawn at Pleafure, I put a Mark at Station 1, and meafure from thence to a fecond Station at 2, which fuppofe I find 40 Pole, this I take from the Scale of equal Parts, and fet on a Line drawn at pleafure, as 1 b from I to 2.

Then

Then I remove my Inftrument from 1 to 2, the fecond Station, and laying the Edge of the Index to the Line 2, 1, I turn the Head of the Table, till, through the Sights, I fee the former Station at 1, and then I turn the Index to a, b, and c, as before; and drawing Lines 2 a, 2 b, and 2 c, they will cut the former Lines in a, b, &c. Then any of the Lines above being applied to the fame Scale that the ftationary Diftance 1, 2 was measur'd by, gives its Length. So that by the two Stations forming the Scheme above you have taken eight feveral Diftances; *i. e.* 

The pointed Line	Statute Pole.	Yards.
I, a is	= 94  or  -	- 517
1, b —	= 113	$-621\frac{1}{2}$
1, c —	= 114	- 627
2, a	= 95	$-522\frac{1}{2}$
2,6 -	= 102	- 561
2, 0 -	= 91	- 500 1/2
a, 6 —	= 33	$-181\frac{1}{2}$
b, c	= 37	$-203\frac{1}{2}$

R 2

And

And the River between the two Stations and the Objects is almost a Quarter of a Mile broad.

Note, A Statute Pole is 5 Yards and an half: And I have taken these Distances in Poles measured by the Line of Equal Parts in the foregoing Quadratic Instrument.

#### PROP. II.

### To take a Diftance from a known Height by Help of the faid Quadratic Instrument.

Under Prop. IV. for taking Altitudes, admit I am at the Top of the Tower c a, and would find the Diftance c 72, or any other, (tho' 10 times that) I take the *Quadratic Inftrument*, and looking from a through the Sights, with that next the Center nearest my Eye, I find the Angle at a (or c a 72)  $36^{\circ} 52'$ , whose Complement is 53.8: Therefore to find the Diftance (c72) I fay,

As the Sine of  $53^{\circ} 8' - 9.903108$ Is to the Log. of ca = 96 - 1.982271So is the Sine of 36.52 - 9.778119To the Log. of 72,  $&c. = the \ 1.857282$ Diftance required

Or

Or Geometrically: Draw two Lines at Pleafure, but perpendicular to each other (as cband ca under the faid Prop. IV. for Altitudes;) then from the Scale of equal Parts on the Quadratic Inftrument, fet off the known Height ca, = 96; then at a lay down the Angle, = 36.52, and drawing the Line from a, it will cut cb in 72; which is the Diffance required, = c72.

#### PROP. III.

To take the Distance by Help of your Watch; as, admit it were required to know the Distance to the Place where a Cannon is discharg'd, let it be never so far off, provided you see the Flash of Fire, and hear the Sound.

A very ingenious Perfon tells us, that Sound proceeds 968 Foot in a Second of Time; another fays, more than 1100 Foot: But we will put it at 1000 (being a round Number between them.) Now upon feeing the Flash of a Gun's Powder, I tell the Beats of my Watch, till I hear the Sound or Report of the Difcharge, which suppose 20 Beats or Impulses; I divide that by 4, gives 5 Seconds, which is 5000 Foot, or 1666  $\frac{2}{3}$  Yards, the Answer; which is 1760, or 1 Mile, wanting only 93  $\frac{1}{3}$  Yards.

# EXAMPLE II.

Suppose the Cafe of Thunder : I take the Beats between the Lightning and the Thunder, which suppose 52 Beats of my Watch, or 13 Seconds, which is 13000 Foot, or near 2 Miles and an half.

PROP. III.

FINIS.

the Place where a Cannon is difehered, let

tion : Town A and

after of Fires, and bear the Sound.

as which is the Diffance required,

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