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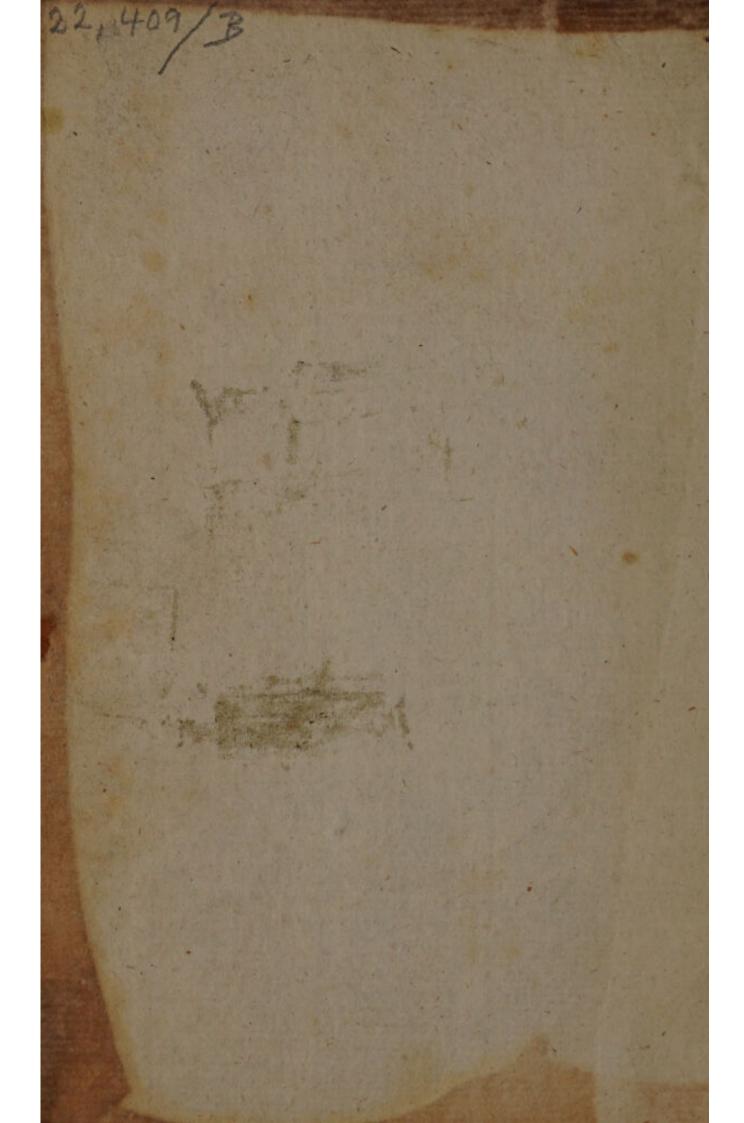
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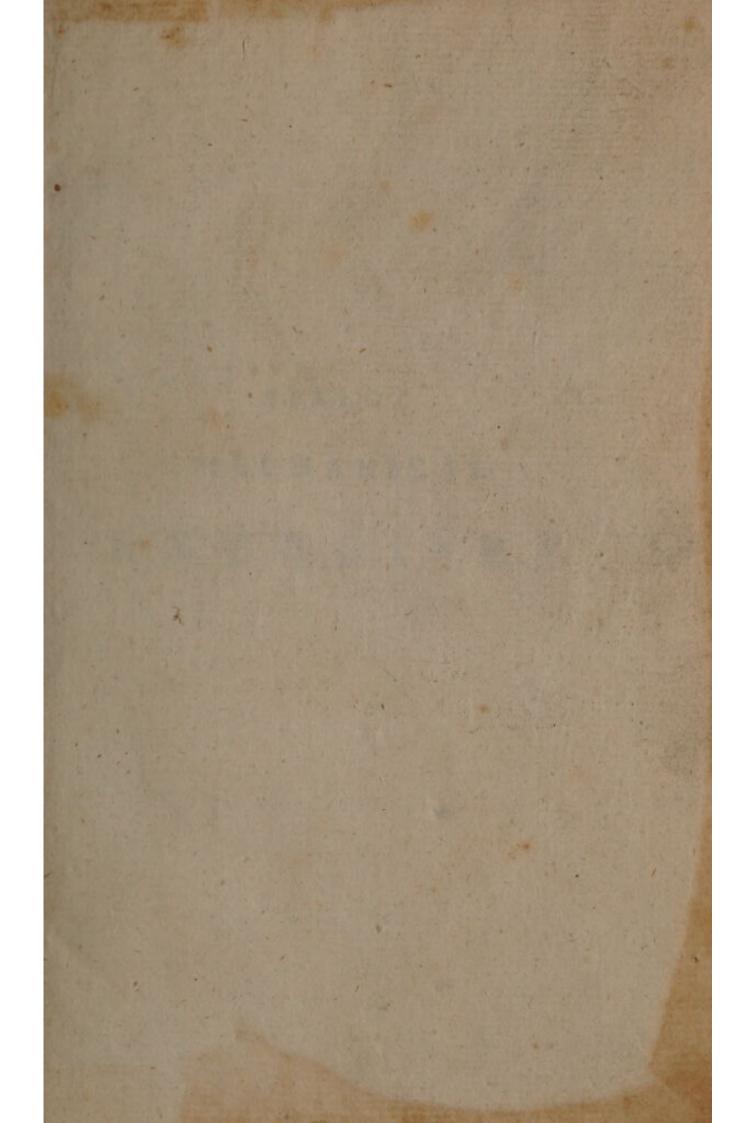
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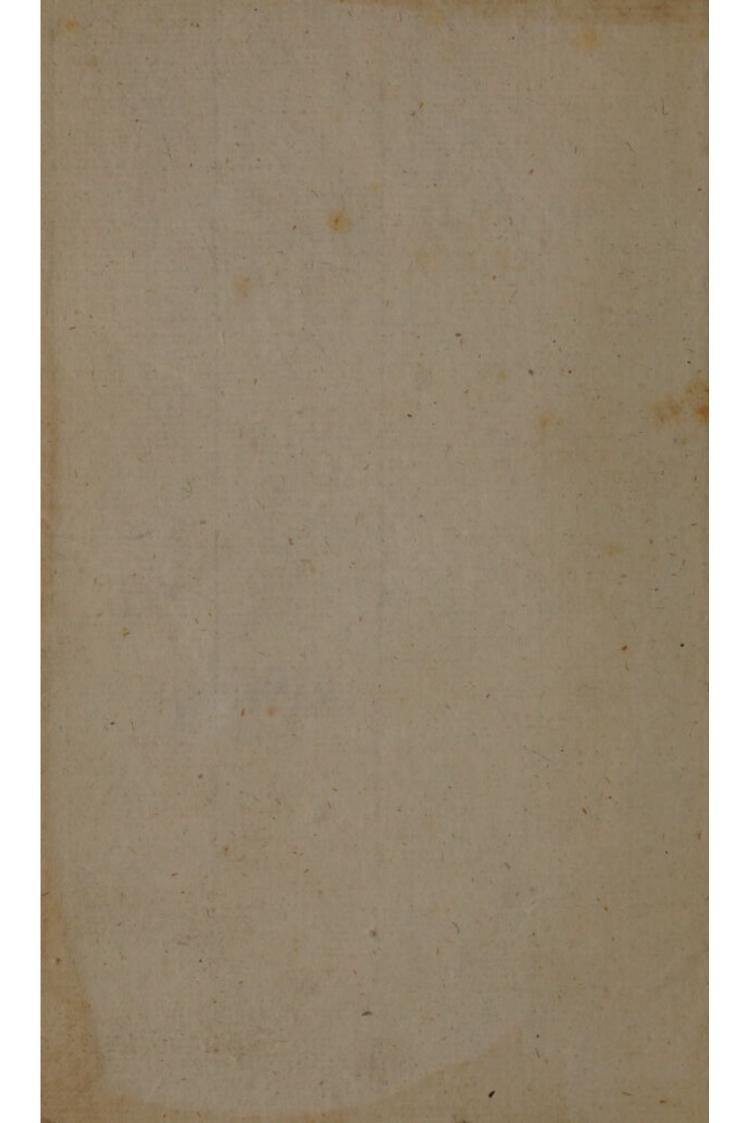


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SELECT MECHANICAL EXERCISES.

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Mechanical Exercises:

Shewing how to confiruct different

CLOCKS, ORRERIES, and SUN-DIALS,
ON PLAIN AND EASY PRINCIPLES.

WITH SEVERAL

MISCELLANEOUS ARTICLES;

AND

NEW TABLES,

- I. For expeditionally computing the Time of any NEW or FULL MOON within the Limits of 6000 Years before and after the 18th Century.
- II. For graduating and examining the usual Lines on the SECTOR, PLAIN SCALE, and GUNTER.

Illustrated with COPPER-PLATES.

To which is prefixed,

A short Account of the Life of the Author.

By JAMES FERGUSON, F. R. S.

THE SECOND EDITION.

LONDON:

Printed for W. STRAHAN: and T. CADELL, in the Strand.



THE

A Short Account of the Life of the Au-
A Short Account of the Life of the Au- thor, Page i.
A Clock Shewing the Hours, Minutes, and
Seconds, having only three Wheels and
two Pinions in the whole Movement.
Invented by Dr. Benjamin Franklin of
Philadelphia, I
Another Clock, Shewing the Hours, Mi-
nutes, and Seconds in a different Way by
the like Movement, 4
A Clock Shewing the apparent daily Motions
of the Sun and Moon, the Age and Phases
of the Moon, with the Time of her coming
to the Meridian, and the Times of High
and Low Water, by having only two
Wheels and a Pinion added to the com-
mon Movement, 11
A An

An Astronomical Clock, Shewing the appa-
rent daily Motions of the Sun, Moon, and
Stars, with the Times of their rifing,
Southing, and Setting, the Places of the
Sun and Moon in the Ecliptic, and the
Age and Phases of the Moon, for every
Day of the Year, - Page 19
Another Clock, Shewing the Same Things, in
a more simple Way of Construction, 31
How to regulate a Clock by the Motion of the
Stars so as to measure mean Solar Time
exactly, 33
To find the Length of a Pendulum that shall
make any given Number of Vibrations in a
Minute, and vice versa, - 36
The Description of a new Machine, called
the Mechanical Paradox, - 44
An Orrery, Shewing the Motions of the Sun,
Mercury, Venus, Earth, Moon, and Nodes
of the Moon's Orbit; the different Lengths
of Days and Nights, the Vicissitudes of
Seasons, Age and Phases of the Moon,
and all the Solar and Lunar Eclipses, 72
Another Orrery 88

A new Geometrical Method of constructing
Sun-Dials, Page 9
A Description of the Hungarian Machine fo
Praising Water from Mines, - 10
Description of a Pump, invented by M. De
la-Hire, which raises Water equally
quick by the Descent as by the Ascent of
the Piston in the Pump-Barrel, 100
The Height of the apparent Level above
the true, at different Distances from the
Levelling Instrument, 115
Of the Velocities acquired by falling Bodies,
and the Spaces they fall through in dif-
ferent Times, 117
A Table Shewing how much the Mercury
would sink in a Barometer at given
Heights above the Earth's plane Surface;
and consequently, how the Heights of Hills
may be found thereby, 121
To divide the Area of a given Circle into
any required Number of equal Parts, by
concentric Circles, by Mr. Hutton, 123
To make two equal Circles, whose Areas
taken together, Shall be equal to the Area
A 2 of
0)

of a given Circle: or four Crescents, the
Sum of whose Areas shall be equal to the
Area of a given Square, - Page 125
Of squaring the Circle, 126
To shew that an Angle may be continually
diminished, and yet never be reduced to
nothing: and consequently, that Matter is
infinitely divisible, 130
A new Experiment in Electricity, shewing
the Motions of the Sun, Earth, and
Moon; by Edward King, Esq; of Lin-
coln's-Inn, 132
Tables and Precepts for calculating (in a
most short and easy Way) the Time of any
New or Full Moon, within the Limits of
6000 Years before or after any given Year
in the present Century, - 137—160
A Table Sheaving the Number of Days be-
tween the Old and New Sile in different
Periods of Time, 161
A Table shewing the Weight of Gold, com-
pared with the Weights of other Materials
of equal Bulk with the Gold, - 162
y cynn Dan transfer

A Table Shewing the Standard Weight, Va-
lue, and comparative View of English
Silver Money, from King William the
Conqueror, A. D. 1066, to A. D. 1765,
Page 163
Prices of Goods between these Dates, 165
Concerning Standard Gold, - 167
The Number of Ways in which all the Let-
ters of the Alphabet might be combined,
or put together, from 1 Letter to 25.
Or, the Number of Changes that might
be rung on any Number of Bells not exceed-
ing the Number of Letters in the Alphabet,
168
The Time it would take to do this, - 169
Concerning the Strength of Steam. From
the Reverend Mr. Mitchell's Treatise on
Earthquakes, 170
Mathematical Tables for dividing the Lines
on Scales and Sectors, - 175—205
Of the Construction of the plain Scale, Sector,
and Gunter's Scale, by the Tables, 206
5 Horo

How to examine the Divisions of the Lines on Sectors and Scales, - Page 232
How to construct these Mathematical Tables, 238
Some Uses of the Plain Scale, Sector, and Gunter's Scale, 240
A short Account of the Logarithms, with Proofs that Lord Nepair was the In-
ventor of them, 244

Generalist of Change that might

be rung on any Number of Beth not exceed-

ing the Number of Letters in the Alphabets

The Time it would take to do this, - - 160

Concerning the Strength of Steams From

the Reverend Mr. Mitchell's Treathe on

Earthquake, - - - - 170

Mathematical Tibles for dividing the Lines

Of the Confirmation of the flain Seale, Selfer,

and Gunter's Scale, by the Tables, 206

on Scales and Sections, " 175-205

201

House

DIRECTIONS to the BINDER.

The Plates must open to the left-hand, fronting the right-hand pages, in the following order:

Plate	I			fronting Page 1		
	II.			-	-	5
	III.	E S	201 9 0 1	· uloqific	120	11
	IV.	11 (4)	Mill.	60 no.	240	19
	V.			1000	300	45
	VI.	- 1		on side	70-1	73
	VII.	9-10-	1250	Separate.	1	75
	VIII.	15 31	17 5	-	-3119	95
	IX.	-		3	STOROL STOR	103

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ASHORT

ACCOUNT

OFTHE

LIFE OF THE AUTHOR.

A sthis is probably the last Book I shall ever publish, I beg leave to prefix to it a short account of myself, and of the manner I sirst began, and have since prosecuted my studies. For, as my setting out in life from a very low station, and in a remote part of the Island, has occasioned some false and indeed very improbable particulars to be related of me, I therefore think it the better way, instead of contradicting them one by one, to give a faithful and circumstantial detail of my whole proceedings, from my first B obscure

obscure beginning to the present time: wherein, if I should insert some particulars of little moment, I hope the good-natured Reader will kindly excuse me.

I was born in the year 1710, a few miles from Keith, a little village in Bamffshire, in the North of Scotland; and can with pleasure say, that my parents, though poor, were religious and honest; lived in good repute with all who knew them, and died with

good characters.

As my father had nothing to support a large family but his daily labour, and the profits arising from a few acres of land which he rented, it was not to be expected that he could bestow much on the education of his children: yet they were not neglected; for, at his leisure hours, he taught them to read and write. And it was while he was teaching my elder brother to read the Scotch Catechism that I acquired my reading.

Ashamed

Ashamed to ask my father to instruct me, I used, when he and my brother were abroad, to take the Catechism, and fludy the lesson which he had been teaching my brother: and when any difficulty occurred, I went to a neighbouring old woman, who gave me fuch help as enabled me to read tolerably well before my father had thought of teaching me.

Some time after, he was agreeably furprifed to find me reading by myself: he thereupon gave me further instruction, and also taught me to write; which, with about three months I afterward had at the grammar-school at Keith, was all the education I ever received.

My taste for mechanics arose from an odd accident.-When about 7 or 8 years of age, a part of the roof of the house being decayed, my father, defirous of mending it, applied a prop and lever to an upright spar to raise it to its former fituation; and, to my

great aftonishment, I saw him, without confidering the reason, lift up the ponderous roof as if it had been a fmall weight. I attributed this at first to a degree of strength that excited my terror as well as wonder: but thinking further of the matter, I recollected that he had applied his strength to that end of the lever which was furthest from the prop; and finding, on enquiry, that this was the means whereby the feeming wonder was effected, I begun making levers (which I then called bars); and by applying weights to them different ways, I found the power gained by my bar was just in proportion to the lengths of the different parts of the bar on either fide of the prop.-I then thought it was great pity that, by means of this bar, a weight could be raifed but a very little way. On this, I foon imagined, that, by pulling round a wheel, the weight might be raifed to any height by tying a rope to the weight,

weight, and winding the rope round the axle of the wheel; and that the power gained must be just as great as the wheel was broader than the axle was thick; and found it to be exactly fo, by hanging one weight to a rope put round the wheel, and another to the rope that coiled round the axle. So that, in these two machines, it appeared very plain, that their advantage was as great as the space gone thro' by the working power exceeded the fpace gone through by the weight: and this property I also thought must take place in a wedge for cleaving wood; but then, I happened not to think of the screw.-By means of a turning lathe which my father had, and fometimes used, and a little knife, I was enabled to make wheels and other things necessary for my purpose.

I then wrote a short account of these machines, and sketched out sigures of them with a pen, imagining it to be the first treatise of the kind that ever was written: but found my mistake when I afterward shewed it to a gentleman, who told me that these things were known long before, and shewed me a printed book in which they were treated os: and I was much pleased when I found, that my account (so far as I had carried it) agreed with the principles of mechanics in the book he shewed me. And from that time my mind preserved a constant tendency to improve in that science.

But, as my father could not afford to maintain me while I was in purfuit only of these matters, and I was rather too young and weak for hard labour, he put me out to a neighbour to keep sheep, which I continued to do for some years; and in that time I began to study the stars in the night. In the day-time I amused myself by making models of mills, spinning-wheels, and such other things as I happened to see.

I then went to ferve a confiderable farmer in the neighbourhood, whose name

name was James Glashan. I found him very kind and indulgent; but he foon observed, that in the evenings, when my work was over, I went into a field with a blanket about me; lay down on my back, and ftretched a thread with fmall beads upon it, at arms' length, between my eye and the flars; fliding the beads upon it till they hid fuch and fuch flars from my eye, in order to take their apparent distances from one another; and then, laying the thread down on a paper, I marked the stars thereon by the beads, according to their respective positions, having a candle by me. My master at first laughed at me; but, when I explained my meaning to him, he encouraged me to go on: and that I might make fair copies in the daytime of what I had done in the night, he often worked for me himfelf. I shall always have a respect for the memory of that man.

One day he happened to fend me with a message to the Reverend Mr.

B 4

John

John Gilchrift, minister at Keith, to whom I had been known from my childhood. I carried my ftar-papers to shew them to him, and found him looking over a large parcel of maps, which I furveyed with great pleafure, as they were the first I had ever feen. He then told me that the Earth is round like a ball, and explained the map of it to me. I requested him to lend me that map, to take a copy of it in the evenings. He chearfully confented to this, giving me at the fame time a pair of compasses, a ruler, pens, ink, and paper; and difmiffed me with an injunction not to neglect my mafter's bufiness by copying the map, which I might keep as long as I pleafed.

For this pleafant employment, my master gave me more time than I could reasonably expect; and often took the threshing-flail out of my hands, and worked himself, while I fat by him in the barn, bufy with my compasses, ruler, and pen.

When I had finished the copy, I asked leave to carry home the map: he told me I was at liberty to do fo, and might flay two hours to converse with the minister.—In my way thither, I happened to pass by the school at which I had been before, and faw a genteel-looking man (whose name I afterwards learnt was Cantley) painting a fun-dial on the wall. I flopt a while to observe him, and the schoolmaster came out, and asked me what parcel it was that I had under my arm. I shewed him the map, and the copy I had made of it, wherewith he appeared to be very well pleafed, and asked me whether I should not like to learn of Mr. Cantley to make fun-dials. Mr. Cantley looked at the copy of the map, and commended it much; telling the school-master (Mr. John Skinner) that it was a pity I did not meet with notice and encouragement. I had a good deal of conversation with him, and found him to be quite affable

ble and communicative; which made me think I should be extremely happy if I could be further acquainted with him.

I then proceeded with the map to the minister, and shewed him the copy of it.-While we were converfing together, a neighbouring gentleman, Thomas Grant, Efq; of Achoynaney, happened to come in; and the minister immediately introduced me to him, shewing him what I had done. He expressed great satisfaction, asked me fome questions about the construction of maps, and told me, that if I would go and live at his house, he would order his butler, Alexander Cantley, to give me a great deal of instruction. Finding that this Cantley was the man whom I had feen painting the fun-dial, and of whom I had already conceived a very high opinion, I told 'Squire Grant, that I should rejoice to be at his house as soon as the time was expired for which I was engaged

gaged with my present master.—He very politely offered to put one in my

place; but this I declined.

When the term of my fervitude was out, I left my good master, and went to the gentleman's house, where I quickly found myself with a most humane good family. Mr. Cantley the butler foon became my friend, and continued fo till his death. He was the most extraordinary man that I ever was acquainted with, or perhaps ever shall see; for he was a complete master of arithmetic, a good mathematician, a master of musick on every known instrument except the harp, understood Latin, French, and Greek, let blood extremely well, and could even prescribe as a physician upon any urgent occasion. He was what is generally called felf-taught; but, I think, he might with much greater propriety have been termed God AL-MIGHTY's fcholar.

He immediately began to teach me decimal arithmetic, and algebra; for I had

I had already learnt vulgar arithmetic, at my leifure hours, from books. He then proceeded to teach me the elements of geometry; but, to my inexpressible grief, just as I was beginning that branch of science, he left Mr. Grant, and went to the late Earl of Fife's, at several miles distance. The good family I was then with could not prevail with me to stay after he was gone; so I left them, and went to my father's.

He had made me a present of Gordon's Geographical Grammar, which, at that time, was to me a great treasure. There is no figure of a globe in it, although it contains a tolerable description of the globes, and their use. From this description I made a globe in three weeks at my father's, having turned the ball thereof out of a piece of wood; which ball I covered with paper, and delineated a map of the world upon it; made the meridian ring and horizon of wood; covered them with paper, and graduated them;

them; and was happy to find, that, by my globe (which was the first I ever faw) I could folve the problems.

But this was not likely to afford me bread, and I could not think of staying with my father, who I knew full well could not maintain me in that way, as it would be of no service to him; and he had, without my assistance, hands sufficient for all his work.

I then went to a miller, thinking it would be a very eafy business to attend the mill, and that I should have a great deal of leisure-time to study decimal arithmetic and geometry. But my master, being too fond of tipling at an ale-house, left the whole care of the mill to me, and almost starved me for want of victuals; so that I was glad when I could have a little oat-meal mixed with cold water to eat. I was engaged for a year in this man's fervice, at the end of which I left him, and returned in a very weak state to my father's.

Soon after I had recovered my former strength, a neighbouring farmer, who practifed as a physician in that part of the country, came to my father's, wanting to have me as a labouring fervant. My father advised me to go to Doctor Young, telling me that the Doctor would instruct me in that part of his business. This he promifed to do, which was a temptation to me. But instead of performing his promise, he kept me constantly to very hard labour, and never once shewed me one of his books. All his fervants complained that he was the hardest master they had ever lived with; and it was my misfortune to be engaged with him for half a year. But, at the end of three months, I was fo much overwrought, that I was almost disabled, which obliged me to leave him: and he was fo unjust as to give me nothing at all for the time I had been with him, because I did not complete my halfhalf-year's fervice; though he knew that I was not able, and had feen me working for the last fortnight, as much as possible, with one hand and arm, when I could not lift the other from my fide. And what I thought was particularly hard, he never once tried to give me the least relief, further than once bleeding me, which rather did me hurt than good, as I was very weak, and much emaciated. I then went to my father's, where I was confined for two months on account of my hurt, and despaired of ever recovering the use of my left arm. And during all that time, the Doctor never once came to fee me, although the distance was not quite two miles .--But my friend Mr. Cantley hearing of my misfortune, at twelve miles diftance, fent me proper medicines and applications, by means of which I recovered the use of my arm; but found myself too weak to think of going into fervice again, and had entirely

AN ACCOUNT OF THE

lost my appetite, so that I could take nothing but a draught of milk once

a-day, for many weeks.

In order to amuse myself in this low state, I made a wooden clock, the frame of which was also of wood; and it kept time pretty well. The bell, on which the hammer struck the hours, was the neck of a broken bottle.

Having then no idea how any timekeeper could go but by a weight and a line, I wondered how a watch could go in all politions; and was forry that I had never thought of asking Mr. Cantley, who could very eafily have informed me. But happening one day to fee a gentleman ride by my father's house (which was close by a public road), I asked him what o'clock it then was: he looked at his watch, and told me. As he did that with fo much good-nature, I begged of him to shew me the inside of his watch: and though he was an entire stranger, he immediately opened the watch, and put

put it into my hands. I faw the fpringbox with part of the chain round it, and asked him what it was that made. the box turn round: he told me that it was turned round by a fteel fpring within it. Having then never feenany other fpring than that of my father's gun-lock, I asked how a spring within a box could turn the box fo often round as to wind all the chain upon it. Heanfwered, that the fpring was long and thin; that one end of it was fastened to the axis of the box, and the other end to the infide of the box; that the axis was fixed, and the box was loofe upon it. I told him I did not yet thoroughly understand the matter: Well, my lad, fays he, take a long thin piece of whalebone, hold one end of it fast between your finger and thumb, and wind it round your finger: it will then endeavour to unwind itself; and if you fix the other end of it to the infide of a small hoop, and leave it to itself, it will turn the hoop hoop round and round, and wind up a thread tied to the outfide of the hoop. -I thanked the gentleman, and told him that I understood the thing very well. I then tried to make a watch with wooden wheels, and made the fpring of whalebone; but found that I could not make the watch go when the balance was put on, because the teeth of the wheels were rather too weak to bear the force of a fpring fufficient to move the balance; altho' the wheels would run fast enough when the balance was taken off. I inclosed the whole in a wooden case, very little bigger than a breakfast teacup: but a clumfy neighbour one day looking at my watch, happened to let it fall; and turning hastily about to pick it up, fet his foot upon it, and crushed it all to pieces; which so provoked my father, that he was almost ready to beat the man; and discouraged me fo much, that I never attempted to make fuch another machine chine again, especially as I was thoroughly convinced I could never make one that would be of any real use.

As foon as I was able to go abroad, I carried my globe, clock, and copies of fome other maps besides that of the world, to the late Sir James Dunbar of Durn (about feven miles from where my father lived), as I had heard that Sir James was a very good-natur'd, friendly, inquisitive gentleman. He received me in a very kind manner, was pleafed with what I shewed him, and defired I would clean his clocks. This, for the first time, I attempted; and then begun to pick up some money in that way about the country, making Sir James's house my home, at his defire.

Two large globular stones stood on the top of his gate: on one of them I painted (with oil colours) a map of the terrestrial globe, and on the other a map of the celestial, from a planisphere of the stars which I copied on

paper from a celestial globe belonging to a neighbouring gentleman. The poles of the painted globes flood toward the poles of the heavens; on each, the 24 hours were placed around the equinoctial, so as to shew the time of the day when the fun shone out, by the boundary where the half of the globe at any time enlightened by the fun was parted from the other half in the shade; the enlightened parts of the terrestrial globe answering to the like enlightened parts of the earth at all times. So that, whenever the fun shone on the globe, one might see to what places the fun was then rifing, to what places it was fetting, and all the places where it was then day or night, throughout the earth.

During the time I was at Sir James's hospitable house, his fister, the Honourable the Lady Dipple, came there on a visit, and Sir James introduced me to her. She asked me whether I could draw patterns for needle-work on aprons and gowns. On shewing me some, I undertook the work, and drew several for her; some of which were copied from her patterns, and the rest I did according to my own fancy. On this, I was sent for by other ladies in the country, and begun to think myself growing very rich by the money I got for such drawings; out of which I had the pleasure of occasionally supplying the wants of

my poor father.

off star-gazing in the nights, and taking the places of the planets among the stars by my above-mentioned thread. By this I could observe how the planets changed their places among the stars, and delineated their paths on the celestial map, which I had copied from the above-mentioned celestial globe.

By observing what constellations the Ecliptick passed through in that map, and comparing these with the starry heaven, I was fo impress'd as sometimes to imagine that I saw the Ecliptic in the heaven, among the stars, like a broad circular road for the sun's apparent course; and fancied the paths of the planets to resemble the narrow ruts made by cart-wheels, sometimes on one side of a plain road and sometimes on the other, crossing the road at small angles, but never going far from either side of it.

Sir James's house was full of pictures and prints, several of which I copied with pen and ink: this made him think I might become a painter.

Lady Dipple had been but a few weeks there, when William Baird, Efq; of Auchmedden, came on a visit: he was the husband of one of that lady's daughters, and I found him to be very ingenious and communicative; he invited me to go to his house and stay some time with him, telling me that I should have free access to his library, which was a very large one; and that

he

he would furnish me with all forts of implements for drawing. I went thither, and flaid about eight months; but was much disappointed in finding no books of aftronomy in his library, except what was in the two volumes of Harris's Lexicon Technicum, altho' there were many books on geography and other sciences: several of these indeed were in Latin, and more in French; which being languages that I did not understand, I had recourse to him for what I wanted to know of these subjects, which he chearfully read to me; and it was as eafy for him, at fight, to read English from a Greek, Latin, or French book, as from an English one. He furnished me with pencils and Indian ink, shewing me how to draw with them: and although he had but an indifferent hand at that work, yet he was a very acute judge; and confequently a very fit person for shewing me how to correct my own work. He was the first who CA

XXIV AN ACCOUNT OF THE

who ever fat to me for a picture, and I found it was much easier to draw from the life than from any picture whatever, as nature was more striking than any imitation of it.

Lady Dipple came to his house in about half a year after I went thither. And as they thought I had a genius for painting, they confulted together about what might be the best way to put me forward. Mr. Baird thought it would be no difficult matter to make a collection for me among the neighbouring gentlemen, to put me to a painter at Edinburgh: but he found, upon trial, that nothing worth the while could be done among them. And as to himfelf, he could not do much that way, because he had but a fmall estate, and a very numerous family.

Lady Dipple then told me that she was to go to Edinburgh next spring, and that if I would go thither, she would give me a year's bed and board

at her house gratis, and make all the interest she could for me among her acquaintance there.-I thankfully accepted of her kind offer; and inflead of giving me one year, she gave me two. I carried with me a letter of recommendation from the Lord Pitsligo (a near neighbour of 'Squire Baird's) to Mr. John Alexander, a painter in Edinburgh; who allowed me to pass an hour every day at his house, for a month, to copy from his drawings; and faid he would teach me to paint in oil-colours, if I would ferve him feven years, and my friends would maintain me all that time: but this was too much for me to defire them to do; nor did I chuse to serve so long. I was then recommended to other painters, but they would do nothing without money. So I was quite at a loss what to do.

In a few days after this, I received a letter of recommendation from my good friend 'Squire Baird to the Reverend rend Dr. Robert Keith at Edinburgh, to whom I gave an account of my bad fuccess among the painters there. He told me, that if I would copy from nature, I might do without their affistance; as all the rules for drawing fignified but very little when one came to draw from the life: and, by what he had feen of my drawings brought from the North, he judged I might fucceed very well in drawing pictures from the life, in Indian ink, on vellum. He then fat to me for his own picture, and fent me with it and a letter of recommendation to the Right Honourable the Lady Jane Douglas, who lived with her mother, the Marchioness of Douglas, at Merchistonhouse, near Edinburgh. Both the Marchioness and Lady Jane behaved to me in the most friendly manner, on Dr. Keith's account, and fat for their pictures; telling me at the fame time, that I was in the very room in which Lord Napier invented and computed the

LIFE OF THE AUTHOR. xxvii

the Logarithms; and that, if I thought it would inspire me, I should always have the fame room whenever I came to Merchiston.-I staid there several days, and drew feveral pictures of Lady Jane; of whom it was hard to fay, whether the greatness of her beauty, or the goodness of her temper and dispositions, was the most predominant. She fent these pictures to adies of her acquaintance, in order to recommend me to them; by which means I foon had as much business as I could possibly manage, so as not only to put a good deal of money in my own pocket, but also to spare what was fufficient to help to fupply my father and mother in their old age .-Thus a bufiness was providentially put into my hands, which I followed for fix and twenty years.

Lady Dipple, being a woman of the strictest piety, kept a watchful eye over me at first, and made me give her an exact account at night of what

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xxviii AN ACCOUNT OF THE

families I had been in throughout the day, and of the money I had received. She took the money each night, defiring I would keep an account of what I had put into her hands; telling me that I should duly have, out of it, what I wanted for clothes, and to fend to my father. - But, in less than half a year, she told me that she would thenceforth trust me with being my own banker; for the had made a good deal of private enquiry how I had behaved when I was out of her fight through the day; and was fatisfied with my conduct.

During my two years' stay at Edinburgh, I fomehow took a violent inclination to fludy anatomy, furgery, and physic, all from reading of books, and converfing with gentlemen, on these subjects; which, for that time, put all thoughts of astronomy out of my mind, and I had no inclination to become acquainted with any one there who taught either mathematics or

aftronomy: for nothing would ferve me but to be a Doctor.

At the end of the fecond year I left Edinburgh, and went to fee my father, thinking myself tolerably well qualified to be a physician in that part of the country; and I carried a good deal of medicines, plaisters, &c. thither. - But to my mortification, I foon found that all my medical theories and study were of little use in practice. And then, finding that very few paid me for the medicines they had, and that I was far from being fo fuccessful as I could wish, I quite left off that business, and began to think of taking to the more fure one of drawing pictures again .- For this purpose I went to Inverness, where I had eight months bufinefs.

When I was there, I began to think of aftronomy again; and was heartily forry for having quite neglected it at Edinburgh, where I might have improved my knowledge by conversing with

with those who were very able to asfift me.- I began to compare the Ecliptic with its twelve figns (through which the fun goes in twelve months) to the circle of 12 hours on the dialplate of a watch, the hour-hand to the Sun, and the minute-hand to the Moon, moving in the Ecliptic; the one always overtaking the other at a place forwarder than it did at their last conjunction before. On this, I contrived and finished a scheme on paper for shewing the motions and places of the Sun and Moon in the Ecliptic on each day of the year, perpetually; and confequently the days of all the New and Full Moons.

To this I wanted to add a method for shewing the Eclipses of the Sun and Moon; of which I knew the cause long before, by having observed that the Moon was, for one half of her period, on the North side of the Ecliptic, and for the other half on the South. But, having not observed her course

course long enough among the Stars by my above-mentioned thread, so as to delineate her path upon my celestial map, in order to find the two opposite points of the Ecliptic in which her orbit crosses it, I was altogether at a loss how and where in the Ecliptic (in my scheme) to place these intersecting points: this was in the year 1739.

At last, I recollected, that when I was with 'Squire Grant of Achoynaney in the year 1730, I had read, that on the 1st of January 1690, the Moon's ascending Node was on the 10th minute of the first degree of Aries; and that her Nodes moved backward thro' the whole Ecliptic in 18 years and 224 days, which was at the rate of 3 min. 11 sec. every 24 hours. But, as I scarce knew in the year 1730 what the Moon's Nodes meant, I took no further notice of it at that time.

However, in the year 1739, I fet to work at Inverness; and after a tedious calculation of the slow motion of the Nodes

xxxii AN ACCOUNT OF THE

Nodes from Jan. 1690 to Jan. 1740, it appeared to me, that (if I was fure I had remembered right) the Moon's afcending Node must be in 23 deg. 25 min. of Cancer at the beginning of the year 1740. And so I added the Eclipse-part to my scheme, and called it The Astronomical Rotula.

When I had finished it, I shewed it to the Reverend Mr. Alexander Mac-Bean, one of the ministers at Inverness, who told me he had a set of almanacks by him for feveral years past, and would examine it by the Eclipses mentioned in them. We examined it together, and found that it agreed throughout with the days of all the New and Full Moons and Eclipses mentioned in these almanacks; which made me think I had conftructed it upon true astronomical principles. On this, Mr. Macbean defired me to write to Mr. Maclaurin, profesfor of the mathematics at Edinburgh, and give him an account of the methods

LIFE OF THE AUTHOR. xxxiii thods by which I had formed my plan, requesting him to correct it where it was wrong. He returned me a most polite and friendly answer (although I had never feen him during my stay at Edinburgh) and informed me that I had only mistaken the radical mean place of the afcending Node by a quarter of a degree; and that, if I would fend the drawing of my Rotula to him, he would examine it, and endeavour to procure me a fubscription to defray the charges of engraving it on copper-plates, if I chose to publish it. I then made a new and correct drawing of it, and fent it to him, who foon got me a very handsome subscription by setting the example himfelf, and fending fubfcription-papers to others.

I then returned to Edinburgh, and had the Rotula-plates engraved there by Mr. Cooper*. It has gone through

^{*} Cooper was master to the justly celebrated Mr. Robert Strange, who was at that time his apprentice.

XXXIV AN ACCOUNT OF THE

feveral impressions, and always sold very well till the year 1752, when the stille was changed, which rendered it quite useless.—Mr. Maclaurin received me with the greatest civility when I sirst went to see him at Edinburgh. He then became an exceeding good friend to me, and continued so till his death.

One day I requested him to shew me his Orrery, which he immediately did. I was greatly delighted with the motions of the Earth and Moon in it, and would gladly have seen the wheelwork, which was concealed in a brass box, and the box and planets above it were surrounded by an armillary sphere. But he told me, that he never had opened it; and I could easily perceive that it could not be opened but by the hand of some ingenious clock-maker, and not without a great deal of time and trouble.

After a good deal of thinking, and calculation, I found that I could contrive

LIFE OF THE AUTHOR. XXXV trive the wheel-work for turning the planets in fuch a machine, and giving them their progressive motions; but should be very well fatisfied if I could make an Orrery to shew the motions of the Earth and Moon, and of the Sun round its axis. I then employed a turner to make me a fufficient number of wheels and axles, according to patterns which I gave him in drawing: and after having cut the teeth in the wheels by a knife, and put the whole together, I found that it answered all my expectations. It shewed the Sun's motion round his axis, the diurnal and annual motions of the Earth on its inclined axis, which kept its parallelism in its whole course round the Sun; the motions and phases of the Moon, with the retrograde motion of the Nodes of her orbit; and confequently, all the variety of feafons, the different lengths of days and nights, the days of the New and Full Moons, and Eclipses.

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XXXVI AN ACCOUNT OF THE

When it was all completed, except the box that covers the wheels, I shewed it to Mr. Maclaurin, who commended it in presence of a great many young gentlemen who attended his lectures. He desired me to read them a lecture on it, which I did without any hesitation, seeing I had no reason to be afraid of speaking before a great and good man who was my friend.—Soon after that I sent it in a present to the Reverend and ingenious Mr. Alexander Irvine, one of the ministers at Elgin in Scotland.

I then made a fmaller and neater Orrery, of which all the wheels were of ivory, and I cut the teeth in them with a file.—This was done in the beginning of the year 1743; and, in May that year, I brought it with me to London, where it was foon after bought by Sir Dudley Rider. I have made fix Orreries fince that time, and there are not any two of them in which the wheel-work is alike: for I could never

bear

LIFE OF THE AUTHOR. xxxvii

bear to copy one thing of that kind from another, because I still saw there was great room for improvements.

I had a letter of recommendation from Mr. Baron Edlin at Edinburgh to the Right Honourable Stephen Poyntz, Efq; at St. James's, who had been preceptor to his Royal Highness the late Duke of Cumberland, and was well known to be possessed of all the good qualities that can adorn a human mind. - To me, his goodness was really beyond my power of expreffion; and I had not been a month in London till he informed me that he had wrote to an eminent professor of mathematics to take me into his house, and give me board and lodging, with all proper instructions to qualify me for teaching a mathematical school he (Mr. Poyntz) had in view for me, and would get me fettled in it. This I should have liked very well, especially as I began to be tired of drawing pictures, in which, I confess, I never D 3 ftrove

ftrove to excel, because my mind was still pursuing things more agreeable. He foon after told me he had just received an answer from the mathematical master, desiring I might be sent immediately to him. On hearing this, I told Mr. Poyntz, that I did not know how to maintain my wife during the time I must be under the master's tuition. What, fays he; are you a married man? I told him I had been fo ever fince May in the year 1739. He faid he was forry for it, because it quite defeated his scheme; as the mafter of the school he had in view for me must be a batchelor.

He then asked me, what business I intended to follow? I answered, that I knew of none besides that of drawing pictures. On this he desired me to draw the pictures of his lady and children, that he might shew them in order to recommend me to others; and told me, that, when I was out of business, I should come to him, and he would

LIFE OF THE AUTHOR, xxxix

would find me as much as he could and I foon found as much as I could execute: but he died in a few years after, to my inexpressible grief.

Soon afterward, it appeared to me, that although the Moon goes round the Earth, and that the Sun is far on the outfide of the Moon's orbit, yet the Moon's motion must be in a line that is always concave toward the Sun: and upon making a delineation reprefenting her absolute path in the Heavens, I found it to be really fo. I then made a fimple machine for delineating both her path and the Earth's on a long paper laid on the floor. I carried the machine and delineation to the late Martin Folkes, Efquire, Prefident of the Royal Society, on a Thursday afternoon. He expressed great fatisfaction at feeing it, as it was a new discovery; and took me that evening with him to the Royal Society, where I shewed the delineation, and the method of doing it.

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xl

When the business of the Society was over, one of the members desired me to dine with him next Saturday at Hackney; telling me that his name was Ellicott, and that he was a watchmaker.

I accordingly went to Hackney, and was kindly received by Mr. John Ellicott, who then shewed me the very fame kind of delineation, and part of the machine by which he had done it; telling me that he had thought of it twenty years before. I could eafily fee, by the colour of the paper, and of the ink lines upon it, that it must have been done many years before I faw it. He then told me what was very certain, that he had neither stolen the thought from me, nor had I from him. And from that time till his death, Mr. Ellicott was one of my best friends. The figure of this machine and delineation is in the 7th Plate of my book of Astronomy.

Soon after the stile was changed, I had my Rotula new engraved; but have

have neglected it too much by not fitting it up and advertifing it. After this, I drew out a scheme, and had it engraved, for shewing all the problems of the Rotula except the Eclipses: and, in place of that, it shews the times of rising and setting of the Sun, Moon, and Stars; and the positions of the Stars for any time of the night.

In the year 1747, I published a Differtation on the Phenomena of the Harvest Moon, with the description of a new Orrery, in which there are only four wheels. But having never had grammatical education, nor time to study the rules of just composition, I acknowledge that I was afraid to put it to the press; and, for the same cause, I ought to have the fame fears still. But having the pleasure to find that this my first work was not ill received, I was emboldened to go on, in publishing my Astronomy, Mechanical Lectures, Tables and Tracts relative to feveral Arts and Sciences, The Young Gentleman

Gentleman and Lady's Astronomy, a small treatise on Electricity, and the following sheets.

In the year 1748, I ventured to read Lectures on the Eclipse of the Sun that fell on the 14th of July in that year. Afterwards I began to read Aftronomical Lectures on an Orrery which I made, and of which the figures of all the wheel-work are contained in the 6th and 7th Plates of this book. I next began to make an apparatus for Lectures on Mechanics, and gradually increased the apparatus for other parts of Experimental Philosophy, buying from others what I could not make for myfelf, till I brought it to its present state. - I then entirely left off drawing pictures, and employed myself in the much pleasanter business of reading Lectures on Mechanics, Hydroftatics, Hydraulics, Pneumatics, Electricity, and Astronomy: in all which, my encouragement has been greater than I could have expected.

The

The best machine I ever contrived is the Eclipsareon, of which there is a figure in the 13th Plate of my Astronomy. It shews the time, quantity, duration, and progress of Solar Eclipses, at all parts of the earth. My next best contrivance is the Universal Dialing Cylinder, of which there is a figure in the 8th Plate of the Supplement to my Mechanical Lectures.

It is now thirty years fince I came to London; and during all that time, I have met with the highest instances of friendship from all ranks of people both in town and country, which I do here acknowledge with the utmost respect and gratitude; and particularly the goodness of our present gracious Sovereign, who, out of his privy purse, allows me fifty pounds a-year, which is regularly paid without any deduction.

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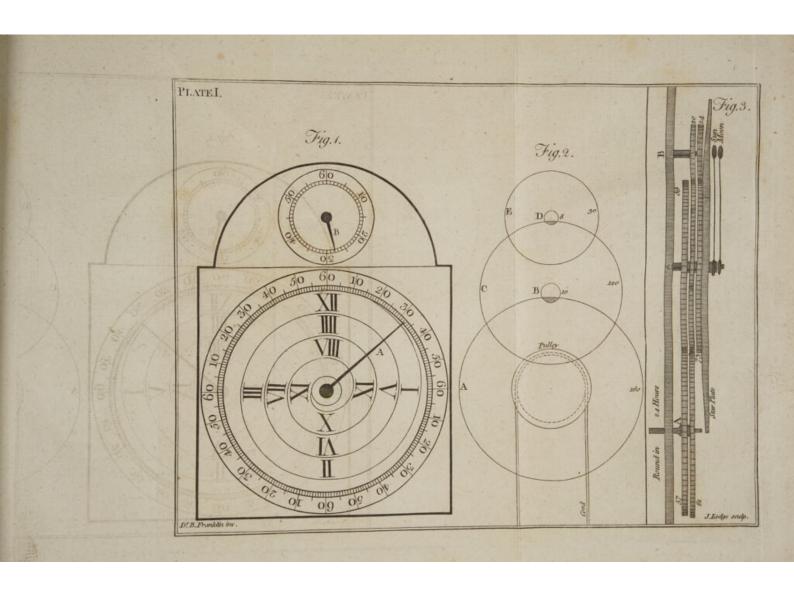
EXERCISES.

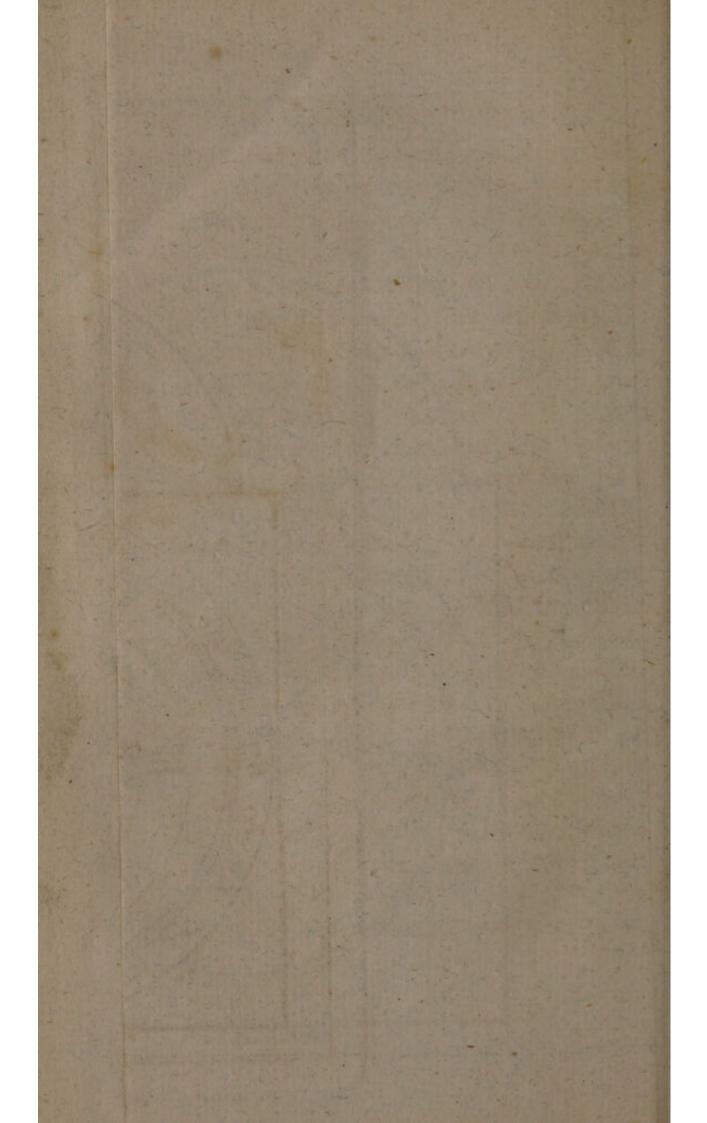
A Clock Shewing the Hours, Minutes, and Seconds, having only three Wheels and two Pinions in the whole Movement. Invented by Dr. FRANKLIN of Philadelphia.

THE dial-plate of this clock is represented by Fig. 1. of Plate I. The hours are engraven in fpiral spaces, along two diameters of a circle containing four times 60 minutes. The index A goes round in four hours, and counts the minutes from any hour it has passed by, to the next following hour. The time, as it appears in the figure, is either 321

minutes past XII, or past IIII, or past VIII; and so on in each quarter of the circle, pointing to the number of minutes after the hours the index last left in its motion. Now, as one can hardly be four hours mistaken in estimating the time, he can always tell the true hour and minute, by looking at the clock, from the time he rises till the time he goes to bed. The small hand B, in the arch at top, goes round once in a minute, and shews the seconds as in a common clock.

Fig. 2. shews the wheel-work of this clock. A is the first or great wheel, it contains 160 teeth, goes round in four hours, and the index A (Fig. 1.) is put upon its axis, and moved round in the same time. The hole in the index is round, it is put tight upon the round end of the axis, so as to be carried by the motion of the wheel, but may be set at any time to the proper hour and minute, without affecting either the wheel or its axis. This wheel of 160 teeth turns a pinion





B of 10 leaves; and as 10 is but a 16th part of 160, the pinion goes round in a quarter of an hour. On the axis of this pinion is the wheel C of 120 teeth; it also goes round in a quarter of an hour, and turns a pinion D, of 8 leaves, round in a minute; for there are 15 minutes in a quarter of an hour, and 8 times 15 is 120. On the axis of this pinion is the fecond-hand B (Fig. 1.) and also the common wheel E (Fig. 2.) of 30 teeth, for moving a pendulum (by pallets) that vibrates feconds, as in a common clock.

This clock is not defigned to be wound up by a winch, but to be drawn up like a clock that goes only 30 hours. For this purpose, the line must go over a pulley on the axis of the great wheel, as in a common 30 hour clock. Several clocks have been made according to this ingenious plan of the Doctor's, and I can affirm, that I have seen one of them, which measures time exceedingly well.—

The

The simpler that any machine is, the better it will be allowed to be, by every man of science.

Another Clock that shews the Hours, Minutes, and Seconds, by means of only three Wheels and two Pinions in the whole Movement.

As Dr. FRANKLIN, whom I rejoice to call my friend, is perhaps the last person in the world, who would take any thing amifs that looks like an amendment or improvement of any fcheme he propofes, I have ventured to offer my thoughts concerning his clock, and how one might be made as fimple as his, with fome advantages. But I must confess, that my alteration is attended with fome inconveniences, of which his are entirely free.—I shall mention both, to the best of my knowledge, that they who chuse to have such simple and cheap

cheap clocks may have them made in either way they pleafe.

The Doctor's clock cannot well be made to go a week without drawing up the weight; and if a person wakes in the night, and looks at the clock, he may possibly be mistaken four hours in reckoning the time by it, as the hand cannot be upon any hour, or pass by any hour, without being upon or passing by four hours at the same time. To avoid these inconveniences, I have thought of the following method.

In Fig. 1. of Plate II. the dial-plate of such a clock is represented; in which there is an opening a b c d below the center. Through this opening, part of a flat plate appears, on which the twelve hours are engraved, and divided into quarters. This plate is contiguous to the back of the dial-plate, and turns round in 12 hours; fo that the true hour, or part thereof, appears in the middle of the opening,

at the point of an index A, which is engraved on the face of the dial plate. -B is the minute-hand, as in a common clock, going round through all the 60 minutes on the dial in an hour; and, in that time, the plate feen thro' the opening a b c d shifts one hour under the fixt engraven Index A. By thefe, you always know the hour and minute, at whatever time you view the dial-plate.-In this Plate is another opening efg h, thro' which the feconds are feen on a flat moveable ring, almost contiguous to the back of the dial plate; and, as the ring turns round, the feconds upon it are shewn by the top-point of a fleurde-lis C, engraved on the face of the dial-plate.

Fig. 2. represents the wheels and pinions in this clock. A is the first or great wheel; it contains 120 teeth, and turns round in 12 hours. On its axis is the plate on which the 12 hours above mentioned are engraved. This plate

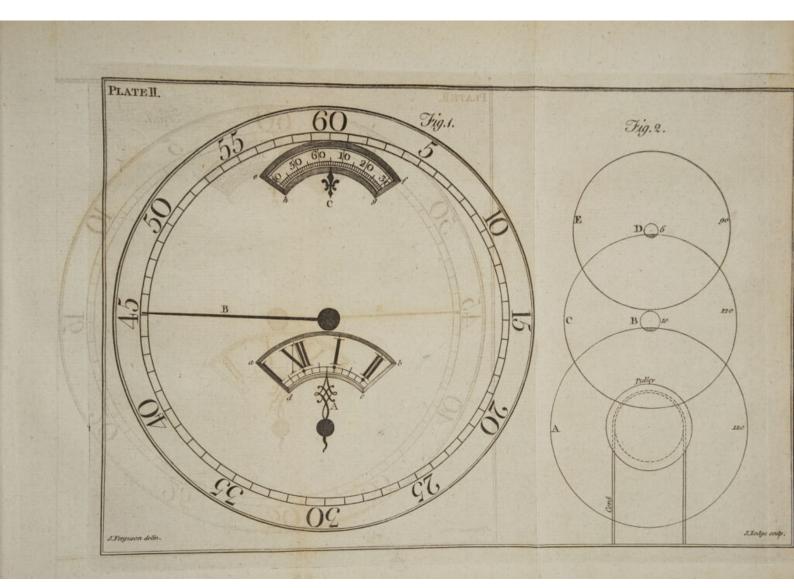




plate is not fixed on the axis, but is only put tight upon a round part thereof, fo that any hour, or part of an hour, may be fet to the top of the fixed index A (Plate I.) without affecting the motion of the wheel. For this purpose, twelve small holes are drilled through the plate, one at each hour, among the quarter divisions: and, by putting a pin into any hole in view, the plate may be fet, without affecting any part of the wheel-work. This great wheel A, of 120 teeth, turns a pinion B of 10 leaves round in an hour; and the minute-hand B (Fig. 1.) is on the axis of this pinion, the end of the axis not being fquare, but round; that the minute-hand may be turned occasionally upon it, without affecting any part of the movement. On the axis of the pinion B is a wheel C of 120 teeth, turning round in an hour, and turning a pinion D of 6 leaves in 3 minutes; for 3 minutes is a 20th part of an hour, and 6

is a 20th part of 120. On the axis of this pinion is a wheel E of 90 teeth, going round in 3 minutes, and keeping a pendulum in motion that vibrates feconds, by pallats, as in a common clock, where the pendulum wheel has only 30 teeth, and goes round in a minute. - But, as this wheel goes round only in 3 minutes, if we want it to shew the seconds, a thin plate must be divided into 3 times 60, or 180 equal parts, and numbered 10, 20, 30, 40, 50, 60; 10 20, 30, 40, 50, 60; 10, 20, 30, 40, 50, 60; and fixed upon the fame axis with the wheel of 90 teeth, fo near the back of the dial-plate, as only to turn round without touching it: and thefe divisions will shew the seconds, thro' the opening efg b in the dial-plate, as they flide gradually round below the point of the fixed fleur-de-lis C.

As the great wheel A, and pulley on its axis over which the cord goes (as in a common 30 hour clock) turns round

round only once in 12 hours, this clock will go a week with a cord of common length, and always have the true hour, or part of that hour, in fight at the upper end of the fixed index A on the dial-plate. These are two advantages it has beyond Dr. Franklin's clock: but it has two difadvantages of which his clock is free. For, in this, although the 12 hour wheel turns the minute-index B, yet, if that index be turned by hand, to fet it to the proper minute for any time, it will not move the 12 hour plate to fet the corresponding part of the hour even with the top of the index A: and therefore, after having fet the minuteindex B right by hand, the hour-plate must be set right by means of a pin put into the fmall hole in the plate just below the hour. 'Tis true, there is no great matter in this; but I have fome fuspicion that the pendulum wheel E having 90 teeth instead of the common number 30, may be fome E 3 difadvantage

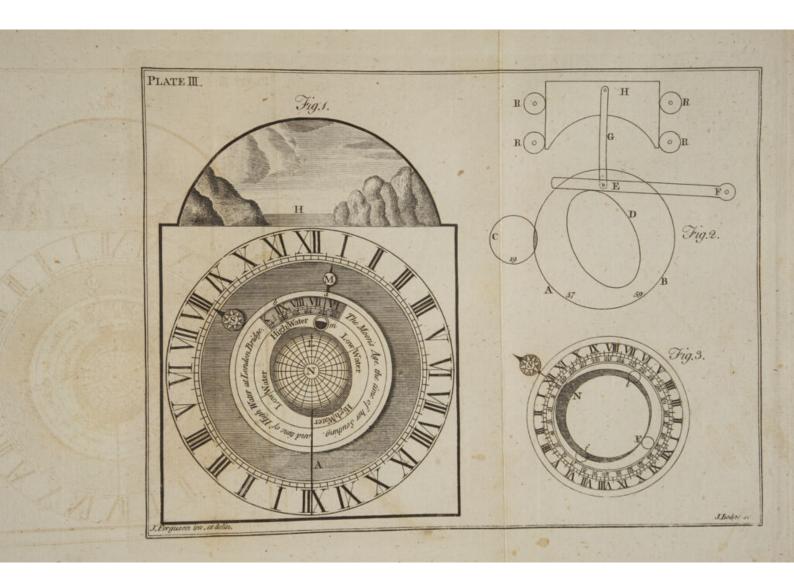
difadvantage to the scapement, on account of the smallness of the teeth; and 'tis certain, that it will cause the pendulum-ball to describe but small arcs in its vibrations. Indeed fome men of science think small arcs are best; but if they really are, I must confess myself ignorant of the reason. For, whether the ball describes a large or a small arc, if the arc be nearly cycloidal, the vibrations will be performed in equal times; the time then depending entirely on the length of the pendulum-rod, not on the length of the arc the ball describes. larger the arc is, the greater is the momentum of the ball; and the greater the momentum is, the lefs will the times of the vibrations be affected by any unequal impulse of the pendulumwheel upon the pallets.

But the worst thing about this clock (and what every one will allow to be a difadvantage) is, that the weight of the flat ring on which the feconds are engraved, engraved, will load the pivots of the axis of the pendulum-wheel with a great deal of friction, which ought by all possible means to be avoided; and yet I have seen one of these clocks (lately made) that goes very well, not-withstanding the weight of this ring. For my own part, I think it might be quite left out; for seconds are of very little use in common clocks not made for astronomical observations; and table-clocks never have them.

A Clock sherwing the apparent daily Motions of the Sun and Moon, the Age and Phases of the Moon, with the Time of her coming to the Meridian, and the Times of High and Low Water, by having only two Wheels and a Pinion added to the common Movement.

The dial-plate of this clock is represented by Fig 1. of Plate III. It

contains all the 24 hours of the day and night. S is the Sun, which ferves as an hour-index, by going round the dial-plate in 24 hours; and M is the Moon, which goes round in 24 hours 501 minutes, from any point in the hour-circle to the fame point again, which is equal to the time of the Moon's going round in the heavens, from the meridian of any place to the fame meridian again. The Sun is fixed to a circular plate (as Fig. 3.) and carried round by the motion of that plate, on which the 24 hours are engraven, and within them is a circle divided into 291 equal parts for the days of the Moon's age, accounted from the time of any new Moon to the next after; and each day flands directly under the time (in the 24 hour circle) of the Moon's coming to the meridian, the XII under the Sun standing for mid-day, and the opposite XII for midnight. - Thus, when the Moon is 8 days old, the comes to the meri-





dian at half an hour past VI in the afternoon; and when the is 16 days old, fhe comes to the meridian at I o'clock in the morning. The Moon M (Fig. 1.) is fixed to another circular plate, of the same diameter with that which carries the Sun; and this Moon-plate turns round in 24 hours 501 minutes. It is cut open, fo as to shew some of the hours, and days of the Moon's age, on the plate below it that carries the Sun, and, across this opening, at a and b are two short pieces of small wire in the Moon-plate. The wire a fhews the day of the Moon's age, and time of her coming to the meridian, on the plate below it that carries the Sun; and the wire b shews the time of high water for that day, on the fame plate. These wires must be placed as far from one another, as the time of the Moon's coming to the meridian differs from the time of high water at the place where the clock is intended to ferve. At London-bridge,

it is high-water when the Moon is two hours and an half past the meridian. .

Above this plate, that carries the Moon, there is a fixed plate N, supported by a wire A, the upper end of which is fixed to that plate, and the lower end is bent to a right angle, and fixed into the dial-plate at the lower-most or midnight XII. This plate may represent the Earth, and the dot at L London, or any other place at which the clock is designed to shew the times of high and low water.

Around this plate is an elliptical shade upon the plate that carries the Moon M: the highest points of this shade are marked High Water, and the lowest points Low Water. As this plate turns round below the fixed plate N, the high and low water points come successively even with L, and stand just over it at the times when it is high or low water at the given place; which times are pointed out by the Sun S, among the 24 hours on the dial-plate: and,

and, in the arch of this plate, above XII at noon, is a plate H that rifes and falls as the tide does at the given place. Thus, when it is high water (fuppose at London) one of the highest points of the elliptical shade stands just over L, and the tide-plate H is at its greatest height: and when it is low water at London, one of the lowest points of the elliptical shade stands over L, and the tide-plate H is quite down, so as to disappear beyond the dial-plate.

As the Sun S goes round the dialplate in 24 hours, and the Moon M goes round it in 24 hours 50½ minutes, the Moon goes fo much flower than the Sun as to make only 28½ revolutions in the time the Sun makes 29½; and therefore the Moon's distance from the Sun is continually changing; so that, at whatever time the Sun and Moon are togeher, or in conjunction, in 29½ days afterward they will be in conjunction again. Consequently, the plate that carries the Moon moves so

much flower than the plate that carries the Sun, as always to make the wire a shift over one day of the Moon's age on the Sun's plate in 24 hours.

In the plate that carries the Moon, there is a round hole m, thro' which the phase or appearance of the Moon is feen on the Sun's plate, for every day of the Moon's age from change to change. When the Sun and Moon are in conjunction, the whole space feen through the hole m is black: when the Moon is opposite to the Sun (or full) all that space is white: when fhe is in either of her quarters, the fame space is half black half white: and different in all other politions, fo as the white part may refemble the visible or enlightened part of the Moon for every day of her age.

To shew these various appearances of the Moon, there is a black shaded space (Fig. 3.) as Nf F l, on the plate that carries the Sun. When the Sun and Moon are in conjunction, the

whole

whole space seen through the round hole is black, as at N: when the Moon is full, opposite to the Sun, all the space seen through the round hole is white, as at F: when the Moon is in her first quarter, as at f, or in her last quarter, as at l, the hole is only half shaded; and more or less accordingly for each position of the Moon with regard to her age; as is abundantly

plain by the Figure.

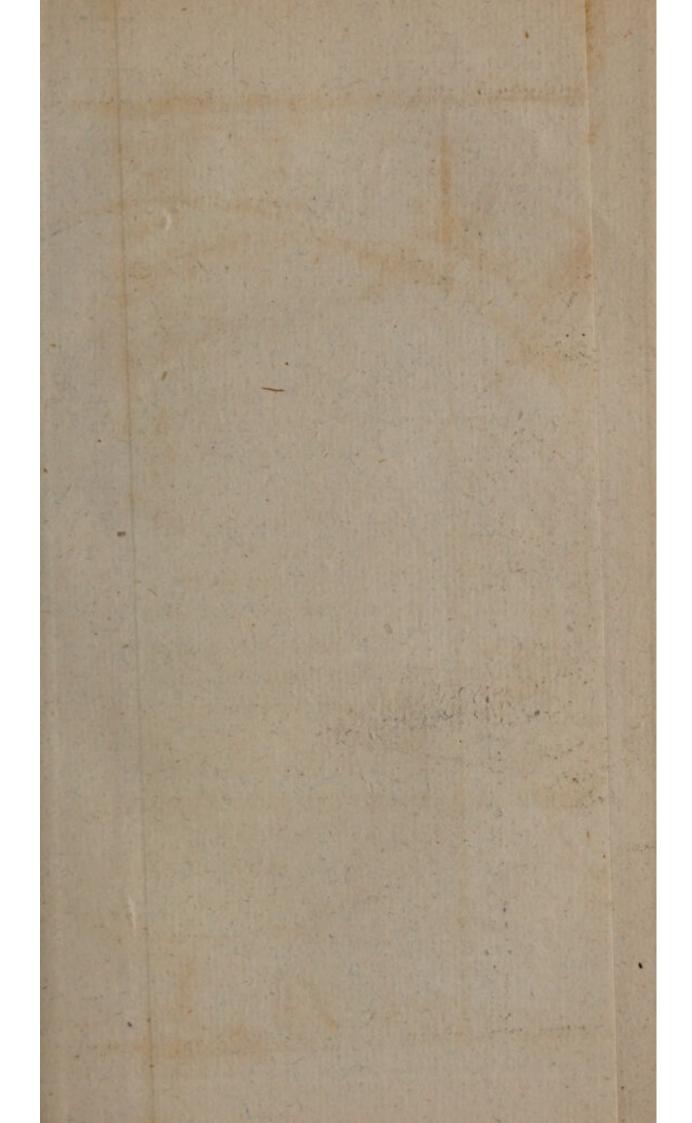
The wheel-work and tide-work of this clock is represented by Fig. 2. in which A and B are two wheels of equal diameters. A has 57 teeth, its axis is hollow, it comes through the dial of the clock, and carries the Sunplate with the Sun (S, in Fig. 1.). B has 59 teeth, its axis is a folid spindle, turning within the hollow axis of A, and carrying the Moon-plate with the Moon (M, in Fig. 1.). A pinion C of 19 leaves takes into the teeth of both the wheels, and turns them round. This pinion is turned round, by the common clock-work, in 8 hours; and,

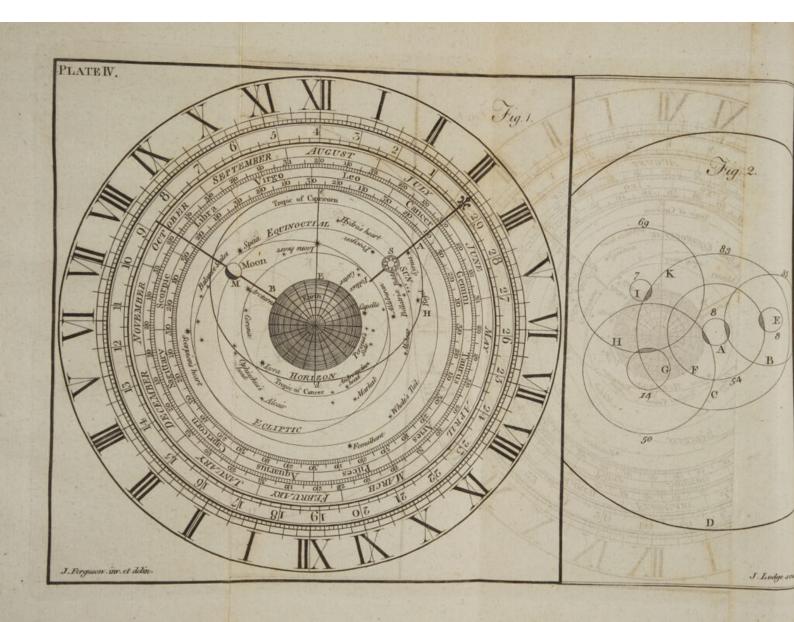
as 8 is a third part of 24, fo 19 is a third part of 57: and therefore the wheel A, of 57 teeth, that carries the Sun, will go round in 24 hours exactly. But, as the fame pinion C (that turns the wheel A of 57 teeth) turns also the wheel B of 59 teeth, this last wheel will not turn round in less than 24 hours 50 ½ minutes of time: for as 57 teeth are to 24 hours, so are 59 teeth to 24 hours 50½ minutes, very nearly.

On the back of the Moon-wheel of 59 teeth is fixed an elliptical ring D, which, as it turns round, raises and lets down a lever E F, whose center of motion is on a pin at F; and this, by means of an upright bar G, raises and lets down the tide-plate H, twice in the time of the Moon's revolving from the meridian to the meridian again. The upper edge of this plate is shewn at H, in Fig. 1. and it moves between four rollers R, R, R, R, in Fig. 2.

I have made one of these clocks to go by the movement of an old watch, in the following manner:

The





The first, or great wheel of a watch, goes round in four hours. I put a wheel of 20 teeth on the end of the axis of that wheel, to turn a wheel of 40 teeth on the axis of the pinion C; by which means, that pinion is turned round in 8 hours, the wheel A in 24 hours, and the wheel B in 24 hours 50; minutes.—I never saw nor heard of any other clock of this kind.

An astronomical Clock, shewing the apparent daily Motions of the Sun, Moon, and Stars with the Times of their rising, southing, and setting, the Places of the Sun and Moon in the Ecliptic, and the Age and Phases of the Moon, for every Day of the Year.

The dial-plate of this clock is reprefented by Fig. 1. of Plate IV. It contains all the 24 hours of the day and night, night, and each hour is divided into 12 equal parts, so that each part anfwers to 5 minutes of time.

Within these divisions of the hour-circle is a flat ring, the face of which is just even (or in the same plane) with the face of the hour-circle. This ring is divided into 29½ equal parts (numbered 1, 2, 3, 4, &c. from the right hand toward the left) which are the days of the Moon's age from change to change: the ring turns round in 24 hours, and has a fleur-de-lis upon it, ferving as an hour-index to point out the time of the day or night in the 24 hour circle.

Within this ring, and about fourtenths of an inch below its flat furface, is a flat circular plate, on which the months and days of the year are engraved; and within these, on the same plate, is a circle containing the signs and degrees of the ecliptic, divided in such a manner, as that each particular particular day of the year stands over the sign and degree of the Sun's place on that day.

Within this circle, on the fame plate, the ecliptic, equinoctial, and tropics, are laid down; and all the stars of the first, second, and third magnitude that are ever feen in the latitude of London, according to their respective right afcentions and declinations; those of the first magnitude being distinguished by eight points, those of the second by fix, and those of the third by five. This plate turns round in 23 hours 56 minutes 4 seconds 6 thirds of time, which is the length of a fydereal day; and confequently it makes 366 revolutions (as the stars do in the heavens) in the time the Sun makes 365; the number of fydereal days in a year exceeding the number of folar days by one.

Over the middle of this plate, and about four tenths of an inch from it, is a fixed plate E, to represent the Earth;

Farth; round which, the Sun, Moon, and Stars move in their proper times, viz. the Sun in 24 hours, the Moon in 24 hours $50\frac{1}{2}$ minutes, and the Stars in 23 hours 56 minutes 4 feconds 6 thirds. The Sun S is carried round by a wire A, which is fixed into the infide of the Moon's age ring, even with the fleur-de-lis; the Moon M is carried round by a wire B, which is fixed to the axis of a wheel below the Earth E, and the Star-plate is turned round by a wheel at the back of the dial-plate.

Over the dial-plate is a glass, as in common clocks. On this glass is an ellipsis H, drawn with a diamond, to represent the horizon of the place for which the clock is to serve, and across this horizon is a straight line e E d (even with the two XII's) to represent the meridian. All the Stars that are seen at any time within this ellipsis are above the horizon at that time, and all those that are without it are then

Star on the Plate comes to the left-hand fide of the horizon (the Stars moving from left to right) the like. Star in the heavens is rifing; when it comes under the meridian line e E, the like Star in the heavens is on the meridian of the place; and when it comes to the right-hand fide of the horizon, the like Star in the heavens is fetting.

When the point of the ecliptic, that the Sun's wire A interfects, comes to the left-hand fide of the horizon, on any day of the year cut by that wire, the fleur-de-lis will be at the time of the Sun's rifing, in the 24 hour circle; and at the time of his fetting when the interfection of the Sun's wire and ecliptic comes to the western side of the horizon.—The like is to be understood with regard to the rising and setting of the Moon, when the point of the ecliptic which her wire B interfects

fects comes to the left and right hand fides of the horizon.

Every 24 hours, the Moon's wire shifts over one day of her age in the circle of 29½ equal parts on the slat ring above mentioned. Each of these day-spaces is divided into four equal parts, for shewing the Moon's age to every sixth hour thereof. Thus, as the Moon's wire B stands in the sigure, it shews the Moon to be 8 days 18 hours old. It shifts quite round the ring, and carries the Moon round from the Sun to the Sun again, in 29 days 12 hours and 45 minutes.

The Sun, on its wire A, goes 365 times round in 365 days; and, in that time, the Star-plate, with the months and days of the year upon it, goes 366 times round. So that, for every revolution of the Sun, the Star-plate advances forward, under the Sun's wire, through the space of one day in the circle of months: and by this means

the Sun's wire shews the day of the month throughout the whole year; and at the same time, for each particular day of the year, it shews the Sun's place in the ecliptic, in the circle of signs.—The Moon's wire B cuts the Moon's place in the circle of signs, for every day of her age, throughout

the year.

The whole circle of figns shifts round, under the Sun's wire A, in 365 days 5 hours 48 minutes 58 seconds, which is the time the Sun takes in going quite round the ecliptic: and the Moon's wire shifts over all the circle of signs in 27 days 7 hours and 43 minutes, which is the time of the Moon's going round the ecliptic. And thus, by these different motions of the Sun and Moon, there are always 29 days 12 hours and 45 minutes between any conjunction of the Sun and Moon, and the next succeeding one.

The moon M is a round ball, half black half white: it turns round its axis,

axis, or wire B, in 29 days 12 hours 45 minutes, and fo shews all the different phases of the Moon, for every day of her age, from change to change. When the Sun and Moon are together, or in conjunction, the white fide of the Moon-ball M is toward the Sun, and the black fide toward the eye of a fpectator looking at the clock, who then can fee no part of the white or (apparently enlightened) fide of the Moon: when the Moon is full, or opposite to the Sun, all the white fide of the ball M is turned toward the spectator's eye: and when the Moon is in either of her quarters, or 90 degrees from the Sun, the spectator sees half the black and half the white fide of the ball; fo that the white part of it then appears like the Moon in her first or last quarter.

Fig. 2. reprefents (what is called) the dial-work of this clock, or the wheels at the back of the dial-plate, between it and the wheels of the common movement, which are contained

between

between two fixed plates, wherein the pivots of their axis turn in holes.

A long pin or fpindle is fixed into the movement-plate next the back of the dial-plate, perpendicular to both these plates. This spindle goes thro' the center of the dial-plate, and has the Earth-plate E (Fig. 1.) fixed on the end of it.

On this spindle, and close to the movement-plate in which it is fixed, is a fixed pinion A of 8 leaves (Fig. 2.) which take into the teeth of a wheel B, and of a wheel C: the number of teeth in B is 35, and the number in C is 50.

These two wheels hang and turn upon a large plate D; which, by the common clock movement, is turned round upon the axis of the fixed pinion A in 24 hours: and consequently, as these wheels are carried round the fixed pinion, and its leaves take into their teeth, each of them will be so far turned round its axis, in 24 hours,

as is equal to 8 of their teeth. The axis of the plate D is hollow, and turns upon the folid fixed fpindle or axis of the pinion A; and the fide of the plate D that is nearest to the clockmovement is almost contiguous to the end of the pinion A next to the dialplate of the clock. Hence it is plain, that the two wheels B and C, which are carried round the pinion A, and are turned by it, must be on that side of the plate D which is almost contiguous to the pinion. All the rest of the wheels and pinions in the figure are on the other fide of the plate D; namely, on the fide of it which is next to the back of the dial-plate.

The axes of the wheels B and C go through the plate D: on the top of the axis B is a pinion E of 8 leaves, which turns a wheel F of 54 teeth. The axis of this wheel is hollow, and turns upon the hollow axis of the plate D; it comes through the center of the dial-plate of the clock, and carries

ries the Moon round by the wire B in Fig. 1. which wire turns round in a piece that goes tight upon the hollow end of the axis of F (Fig. 2.) just under

the Earth-plate E (Fig. 1.).

The hollow axis of the plate D turns round, as the plate does, in 24 hours. On the end of this axis, just under the middle of the Earth-plate E, is a small wheel of 20 teeth, turning a contrate wheel of the fame number, the pivots of whose axis turn in the piece that carries the Moon's wire; and this wheel turns another wheel of the fame number of teeth, fixed on the Moon's wire or axis. By these wheels (which lie concealed under the Earth plate E) the Moon is turned round her axis in 29 days 12 hours 45 minutes, as above mentioned, and shews her different phases. These three last mentioned wheels are not reprefented in Fig. 2. because they could not be put in without confusing it.

On the axis of the wheel C of 50 teeth is a pinion G of 14 leaves, which turns a wheel Hof 69 teeth, on whose axis is a pinion I of 7 leaves, turning a wheel K of 83 teeth: this wheel is pinned fast to the back of the Starplate, which, together with the wheel, turns round in a fydereal day, or in 23 hours 56 minutes 4 feconds 6 thirds of mean folar time; and the abovementioned wheels, which belong to the Moon, will carry her round from the meridian to the meridian again in 24 hours 501 minutes; if the plate D, on which all the wheels hang, be turned round in 24 mean folar hours.

The plate D carries the ring of $29\frac{1}{2}$ equal parts round, within the fixed 24 hour-circle of the dial-plate, in 24 hours, by means of four pillars, whose opposite ends are fixed into the plate D, and into the ring. By this, the Sun is carried round in 24 hours (its wire A being fixed into the ring) and also

also the fleur-de-lis that shews the time, like an index, in the 24 hour-circle.

I contrived this clock above twenty years ago, and made a model of it in wood, which I have still in my cuftody; and fince that time,

Another Clock shewing the Equation of Time, the apparent daily Motions of the Sun, Moon, and Stars; with the Times of their rising, southing, and setting.

The dial-plate of this clock is like the one last described; but the wheelwork at the back of the dial-plate is different, and rather more simple.

Two wheels, one of 57 teeth and the other of 61, are fixed upon an axis A (fee Fig. 3. of Plate I.) and turned round by the common clock-movement in 24 hours.

The wheel of 57 teeth turns a wheel of 59, on the top of whose axis, above (or

(or before the face of) the Star-plate, is a wire that carries the Moon round, from the meridian to the meridian again in 24 hours 50½ minutes.

The wheel of 61 teeth turns another of the same number, whose axis is hollow and turns on the solid axis of the wheel of 59. On the top of this hollow axis, between the Moon's wire and the Star-plate, is a wire that carries the Sun round from the meridian to the meridian again, in 24 mean solar hours.

The last mentioned wheel of 61 teeth (whose axis carries the Sun) turns a wheel of 20 teeth, upon a pin fixed in the immoveable plate B; and to this wheel of 20 teeth is fixed a wheel of 24, by pins put through them, and riveted on their outsides: this wheel of 24 teeth turns a wheel of 73, loose on the hollow axis of the Sun-wheel of 61, and riveted fast to the Star-plate; which,

which, together with the faid wheel, turns 366 times round in 365 days, measured by the Sun's motion. The days of the months, and corresponding Equations of Time are laid down on the Star-plate, and cut by the wire that carries the Sun.

How to regulate a Clock by the Motion of the Stars, so as to measure mean solar Time exactly.

As the Stars make 366 revolutions in 365 days, each Star comes to the meridian 3 minutes 55% feconds on each fucceeding day or night fooner than it did on the day or night before. We shall first give the following table of their revolutions for a year, and then shew its use in regulating clocks and watches, so as to keep mean solar time.

A TABLE for regulating Clocks and Watches to true equal Time, by the daily Revolutions of the Stars.

Rev.	Days	. H.	M.	S.	H.	-M.	s.
I	Name and Address of the Owner, where the Owner, which is the Owner, where the Owner, which is the Owner, where the Owner, which is the Owner, whic	23	56	4.1	0	-	-
2	I	23	52	8.2		3 7	55.9
3		23	48	12.3		11	47.7
4		23	44	16.4	0	15	43.6
		23	40	20.5		119	39.5
56	5	23	36	24.6		23	35.4
	1	23	32	28.7		27	31.3
7 8	7	23	28	32.8		31	27.2
9	7 8	23	24	36.9		35	23.1
10	9	23	20	41.0	0	39	19.0
11	10	23	16	45.1	1000	43	14.9
12	II	23	12	49.2	0	7	10.8
13	12	23	8	53.3	0	51	6.7
14	13	23	4	57-4	0	55	2.6
15	14	23	1	1.5	0	58	58.5
16	15	22	57	5.6	I	2	54.4
17	16	22	53	9.7	I	6	50.3
18	17	22	49	13.8	I	10	46.2
19	18	22	45	17.9	1	14	42.1
20	19	22	41	22.0	1	18	38.0
21	20	22	37	26.1	I	22	33.9
22	21	22	33	30.2	1	26	29.8
23	22	22	29	34.3	1	30	25.7
24	23	22	25	38.4	1	34	21.6
25	24	22	21	42.5	I	38	17-5
26	25	22	17	46.6	I	42	13.4
27	26	22	13	50.7	1	46	9.3
28	27 28	22	9	54.8	1	50	5.2
29		22	5	58.9		54	1.1
30	29	22	2	3.0	1	57	57.0
40	39	21	22	44.0	2	37	10.0
50	49	20	43	25.0	3	16	35.0
THE RESERVE OF THE PERSON NAMED IN	59	20	4	6.0	3	55	54.0
7º 80		19	24.	47.0	4	35	13.0
_	79	18	45	28.0	5	14	32.0
90	99		26	9.0	5	53	51.0
200		17		50.0		33	20.0
300		4	53	30.0	13		30.0
360		0			23	39 35	24.0
365	264	0	24		23		
366		0	4	0.6	22	55 58	3.5
3000	3 3			0.01	-3	20	59.4

The first column denotes the number of revolutions of the Stars, from the meridian to the meridian again, in a common year of 365 days: the next other columns (titled Days H. M. S.) shew the times in which these revolutions are made: and those in the right-hand part of the Table (titled H. M. S.) shew how much any Star gains daily upon the time shewn by a well-regulated clock or watch.

Therefore to know whether the clock goes true or not, observe the time by the clock when any Star disappears behind a chimney (or any other fixed object) as seen through a hole in a thin plate of metal fixed in a window-shutter; and if the same Star disappears on every succeeding night as much sooner by the clock as to agree with the times shewn in the right-hand part of the Table (as suppose 39 minutes 19 seconds in 10 days, or 1 hour 18 minutes 38 seconds in 20 days)

days) the clock goes true: otherwife it does not, and must be regulated accordingly, by screwing up or letting down the ball of the pendulum, as it goes too slow or too fast.

To find the length of a Pendulum that shall make any given number of Vibrations in a Minute, and vice versa.

A pendulum whose length is 39.2 inches, from the point of suspension to the center of oscillation, makes 60 vibrations in a minute; and this is called the standard length. Then, for any other number of vibrations in a minute, say, As the square of the given number of vibrations is to the square of 60, so is the length of the standard to the length sought.—Thus, suppose the given number of vibrations to be 30 per minute: the square of 30 is 900, and the square of 60 is 3600: then,

as 900 is to 3600, fo is 39.2 to 156.8; fo that the length required for 30 vibrations per minute is 156.8 inches.

If the length of the pendulum be given, and the number of vibrations it makes in a minute be required; fay, As the given length is to the standard length (39.2 inches) so is the square of 60 vibrations to the square of the number required: the square root of which shall be the number of vibrations made by the pendulum in a minute. Thus, suppose the given length to be 156.8 inches: As 156.8 is to 39.2, so is 3600 (the square of 60) to 900; the square root of which is 30, the number of vibrations that this pendulum will make in a minute.

The length of a pendulum that would make only one vibration in a minute is 3920 yards, or 141120 inches: and the length of a pendulum that would make 240 vibrations in a minute (or 4 in a fecond) is 2.45 inches.

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In these calculations it is supposed that the weight of the pendulum-rod bears little or no sensible proportion to the weight of the ball. But as this cannot be the case in practice, the center of oscillation will always be further from the point of suspension than the calculation makes it; and this must be found by trial.

To divide the Circumference of a Circle into any given Number of equal Parts, whether even or odd.

As there are very uncommon and odd numbers of teeth in some of the wheels of astronomical clocks, and which consequently could not be cut by any common engine used by clockmakers for cutting the numbers of teeth in their clock-wheels, I thought proper to shew how to divide the circumference of a circle into any given odd or even number of equal parts,

fo as that number may be laid down upon the dividing-plate of a cutting engine.

There is no odd number, but from which, if a certain number be fubtracted, there will remain an even number, easy to be subdivided. Thus, supposing the given number of equal divisions of a circle on the dividing plate to be 69; fubtract 9, and there will remain 60.

Every circle is supposed to contain 360 degrees: therefore fay, As the given number of parts in the circle, which is 69, is to 360 degrees, fo is a parts to the corresponding are of the circle that will contain them: which arc, by the Rule of Three, will be found to be 46 95. Therefore, by the line of chords on a common scale, or rather on a fector, fet off 46,05 (or 46 9) degrees with your compasses, in the periphery of the circle, and divide that arc or portion of the circle into 9 equal parts, and the rest of the circle into

babit

into 60; and the whole will be divided into 69 equal parts, as was required.

Again, suppose it were required to divide the circumference of a circle into 83 equal parts; subtract 3, and 80 will remain.—Then, as 83 parts are to 360 degrees, so (by the Rule of Proportion) are 3 parts to 13 degrees and one hundredth part of a degree; which small fraction may be neglected. Therefore, by the line of chords, and compasses, set off 13 degrees in the periphery of the circle, and divide that portion or arc into 3 equal parts, and the rest of the circle into 80; and the thing will be done.

Once more, suppose it were required to divide a given circle into 365 equal parts: subtract 5, and 360 will remain. Then, as 365 parts are to 360 degrees, so are 5 parts to $4\frac{9}{100}$ degrees. Therefore, set off $4\frac{9}{100}$ (or $4\frac{9}{10}$) degrees in the circle; divide that space into 5 equal parts, and the rest of the circle into 360; and the whole will be divided

vided into 365 equal parts, as was

required.

I have often found this rule or method very useful in dividing circles into an odd number of equal parts, or wheels into odd numbers of equal fiz'd teeth with equal spaces between them: and now I find it just as easy to divide any given circle into any odd number of equal parts, as to divide it into any even number. And, for this purpose, I prefer the line of chords on a fector to that on a plain fcale; because the fector may be opened fo, as to make the radius of the line of chords upon it equal to the radius of the given circle, unless the radius of the circle exceeds the whole length of the fector when it is opened fo as to refemble a straight ruler or scale; and this is what very feldom happens.

Any person who is used to handle the compasses, and the scale or sector, may very easily, by a little practice, take off degrees, and fractional parts of a degree, by the accuracy of his eye, from a line of chords, near enough the truth for the above-mentioned purpose.

Supposing the distance between the Centers of two Wheels, one of which is to turn the other, be given; that the Number of Teeth in one of these Wheels is different from the Number of teeth in the other, and it is required to make the Diameters of these Wheels in such Proportion to one another as their Numbers of Teeth are, so that the Teeth in both Wheels may be of equal Size, and the Spaces between them equal, that either of them may turn the other easily and freely: it is required to find their Diameters.

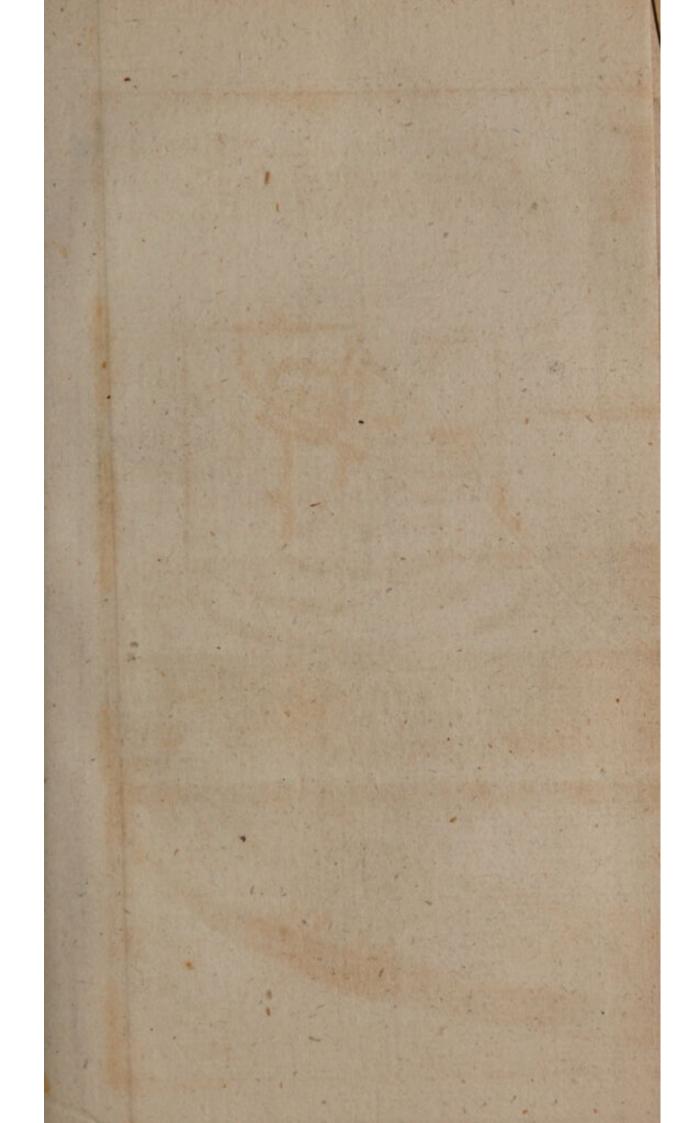
Here it is plain that the distance between the centers of the wheels is equal to the sum of both their radii in the working parts of the teeth.— Therefore, Therefore, as the number of teeth in both wheels, taken together, is to the distance between their centers, taken in any kind of measure, as feet, inches, or parts of an inch; so is the number of teeth in either of the wheels to the radius or semidiameter of that wheel, taken in the like measure, from its center to the working part of any one of its teeth.

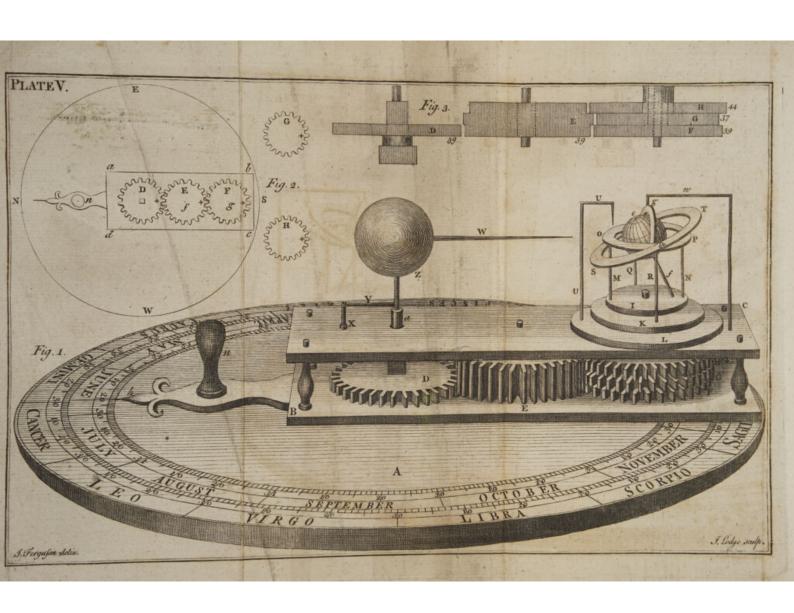
Thus, suppose the two wheels must be of fuch fizes, as to have the distance between their centers 5 inches; that one wheel is to have 75 teeth, and the other to have 33, and that the fizes of the teeth in both the wheels is equal, fo that either of them may turn the other. The fum of the teeth in both wheels is 108; therefore fay, As 108 teeth is to 5 inches, fo is 75 teeth to 3 to 5, fo is 33 to 1 53. So that, from the center of the wheel of 75 teeth to the working part of any tooth in it, is 3 inches and 47 hundred parts of an inch; and, from G 4

from the center of the wheel of 33 teeth to the working part of either of its teeth, is 1 inch and 53 hundred parts of an inch.

The Description and Use of a New Machine called the MECHANICAL PARADOX.

The vulgar and illiterate take almost every thing, even the most important, upon the authority of others, without ever examining it themselves .- Although this implicit confidence is feldom attended with any bad confequences in the common affairs of life. it has nevertheless, in other things, been much abused; and in political and religious matters, has produced On the other hand, fatal effects. knowing and learned men, to avoid this weakness, have fallen into the contrary extreme: fome of them believe every thing to be unreasonable, or impossible, that appears so to their first





first apprehension; not adverting to the narrow limits of the luman understanding, and the infinite variety of objects, with their mutual operations, combinations, and affections, that may be presented to it.

It must be owned, that credulity has done much more mischief in the world than incredulity has done, or ever will do; because the influences of the latter extend only to fuch as have some share of education, or affect the reputation thereof.—And fince the human mind is not necessarily impelled, without evidence, either to belief or unbelief; but may fuspend its affent to, or diffent from, any propofition till after a thorough examination; it is to be wished, that men of literature, especially philosophers, would not hastily, and by first appearances, determine themselves with refpect to the truth or falfehood, possibility or impossibility of things.

A person who has made but little progrefs in the mathematics, though in other respects learned and judicious, would be apt to pronounce it impoffible that two lines, which were no where two inches afunder, may continually approach toward one another, and yet never meet, although continued to infinity: and yet the truth of this proposition may be easily demonflrated. - And many, who are good mechanics, would be as apt to pronounce the fame, if they were told, that although the teeth of one wheel should take equally deep into the teeth of three others, it should affect them in fuch a manner, that in turning it any way round its axis, it should turn one of them the same way, another the contrary way, and the third no way at all.

On a very particular occasion, about eighteen years ago, I contrived a small machine of this fort, which has been shewn

shewn and explained to many; and which I shall here describe, and explain some of the uses it has been applied to.

It is represented to view by Fig. 1. of Plate V. in which A is called the immoveable plate, because it lies still on a table whilst the machine is at work. BC is a moveable frame, to be turned round an upright axis a (fixed into the center of the immoveable plate) by taking hold of the knob n, which is fixed into the index h.

On the faid axis is fixed the immoveable wheel D, whose teeth take into the teeth of the thick moveable wheel E, and turn it round its own axis, as the frame is turned round the fixed axis of the immoveable wheel D; and in the same direction that the frame is moved.

The teeth of the thick wheel E take equally deep into the teeth of the three wheels F, G, and H; but operate on these wheels in such a manner, that whilst

whilst the frame is turned round, the wheel H turns the fame way that the wheel E does; the wheel G turns the contrary way, and the wheel F turns no way at all.

Before we explain the principles on which these three different effects depend, it will not be improper to fix some certain criteria for bodies turning or not turning round their own axes or centers; and to make a distinction between absolute and relative motion.

r. If a body shews all its sides progressively round toward a certain fixed point in the heavens, the body turns round its own axis or center, whether it remains still in the same place, or has a progressive motion in any orbit whatever.—For, unless it does turn round its own center, it cannot possibly have one of its sides toward the west at one time, toward the south at another, toward the east at a third time, and toward the north at a fourth.—

This

This is the cafe with the Moon, which always keeps one fide toward the earth; but shews the same side to every fixed point of the flarry heaven in the plane of her orbit, in the time fhe goes once round her orbit; because in the time that she goes round her orbit, she turns once round her own axis or center .- On the contrary, if a body still keeps one of its fides toward a fixed point of the heaven, the body does not turn round its own axis or center, whether it keeps in one and the fame place or has a progressive motion in any orbit or direction whatever.-This is the case with the card of the compass in a ship, which still keeps one of its points toward the magnetic north, let the ship be at rest, or fail round a circle of many miles diameter.

Both these cases may be exemplified either by a cube or a globe, having a pin fixed into either of its sides to hold it by: we shall suppose a cube, because its sides are flat.—Sit down at a table, and

and hold the cube by the pin, which may be called its axis, and keep one of its fides toward any fide of the room. Whilst you do this, you do not turn the cube round its axis, whether you still keep it in the same place, or carry it round any other fixed body on the table.—But if you try to keep any fide of the cube toward the fixed body, whilst you are carrying it round the same, you will find that you cannot do fo, without turning the pin round (which is fixed into the cube) betwixt the finger and thumb whereby you hold it; unless you rise and walk round the table, keeping your face always toward the fixed body on the table; and then, both yourfelf and the cube will have turned once round; for the cube will have shewn the same fide progressively round to all fides of the room, and your face will have been turned toward every fide of the room, and every fixed point of the horizon.

2. If a ship turns round, and at the fame time a man flands on the deck without moving his feet, he is turned absolutely round by the motion of the ship, though he has no relative motion with respect to the ship .- But if, whilst the ship is turning round, he endeavours to turn himfelf round the contrary way; he thereby only undoes the effect that the turning of the ship would otherwise have had upon himfelf; and is, in fact, so far from turning absolutely round, that he keeps himself from turning at all; and the ship turns round him, as round a fixed axis; although, with respect to the fhip, he has a relative motion.

Fig. 2. is a fmall plan, or flat view of the machine, in which, the fame letters of reference are put to the wheels in it, as to those in Fig. 1. for the conveniency of looking at both the figures, in reading the description of them. WSEN is the round immoveable plate: D the immoveable wheel

wheel on the fixed axis in the center of that plate: E the thick moveable wheel, whose teeth take into the teeth of the wheel D; and F is one of the thin wheels, over which G and H may be put; and then, F, G, and H will make a thickness equal to the thickness of the wheel E, and its teeth will take equally deep into the teeth of them all. The frame that holds thefe wheels is represented by the parallelogram a b c d; and if it be turned round, it can give no motion to the wheel D, because that wheel is fixed on an axis which is fixed into the great immoveable plate.

Take away the thick wheel E, and leave the wheel F where it lies, on the lower plate of the frame. Then turn the frame round the axis of the immoveable plate WSEN (denoted by A in Fig. 1.) and it will carry the wheel F round with it.—In doing this, F will still keep one and the same side toward the fixed central wheel D,

as the Moon still keeps the same side toward the Earth: and although F will then have no relative motion with respect to the moving frame, it will be absolutely turned round its own center g (like the man on the ship whilst he stood without moving his feet on the deck), for the cross mark on its side next S will be progressively turned toward all the sides of the room.

But, if we would keep the wheel F from turning round its own center, and so cause the cross mark upon it to keep always toward one side of the room; or, like the magnetic needle, to keep the same point still toward one sixed point in the horizon; we must produce an effect upon F, resembling what the man on the ship did, by endeavouring to turn himself round the contrary way to that which the ship turned, so as he might keep from turning at all; and by that means keep his face still toward one and the same point of the horizon.—And this

is done, by making the numbers of teeth equal in the wheels D and F (suppose 20 in each) and putting the thick wheel E between them, fo as to take into the teeth of them both. For then, as the frame is turned round the axis of the fixed wheel D, by means of the knob n, the wheel E is turned round its axis by the wheel D; and, for every space of a tooth that the frame would turn the wheel F, in direction of the motion of the frame, the wheel E will counteract that motion, by turning the wheel F just as far backward with respect to the motion of the frame; and so will keep F from turning any way round its own center: and the cross mark near its edge will be always directed towards one fide of the room.-Whether the wheel E has the fame number of teeth as D and F have, or any different number, its effect on F will be still the same.

If F had one tooth less in number than D has, the effect produced on F, by the turning of the frame, would be

be as much more than counteracted by the intermediate wheel E, as is equal to the space of one tooth in F: and therefore whilft the frame was turned once round, suppose in direction of the letters WSEN on the immoveable plate, the wheel F would be turned the contrary way, as much as is equal to the space taken up by one of its teeth. But, if F had one tooth more in number than D has, the effect of the motion of the frame (which is to turn F round in the fame direction with it) would not be fully counteracted by means of the intermediate wheel E; for as much of that effect would remain as is equal to the space of one tooth in F: and therefore, in the time the frame was turned once round, the wheel F would turn, on its own center, in direction of the motion of the frame, as much as is equal to the space taken up by one of its teeth: and here note, that the wheel E (which turns F) always turns in direction of the motion of the frame.

H 2

And

And therefore, if an upright pin be fixed into the lower plate of the frame, under the center of the wheel F, and if the wheel F has the fame number of teeth that the fixed wheel D has, the wheel G one tooth lefs, and the wheel H one tooth more; and if thefe three wheels are put loofely upon this pin, fo as to be at liberty to turn either way; and the thick wheel E takes into the teeth of them all, and also into the teeth of the fixed wheel D; then, whichever way the frame is turned, the wheel H will turn the same way, the wheel G the contrary way, and the wheel F no way at all.—The less number of teeth Ghas, with respect to those of D, the faster it will turn backward; and the greater number of teeth H has, with respect to those in D, the faster it will turn forward; reckoning that motion to be backward which is contrary both to the motion of the frame and of the thick wheel E, and that motion to be forward which is in the fame direction with the motion of the

the frame and of the wheel E.—So that the turning or not turning of the three wheels, F, G, H, or the direction and velocity of the motions of those that do turn round, depends entirely on the relation between their numbers of teeth and the number of teeth in the fixed wheel D, without any regard to the number of teeth in the moveable wheel E.

Having solved the paradox, and described the cause of the different effects which are produced upon the three wheels F, G, and H, we shall now proceed to shew some uses that may be made of the machine.

This machine is so much of an Or-RERY, as is sufficient to shew the different lengths of days and nights, the vicissitudes of the seasons, the retrograde motion of the nodes of the Moon's orbit, the direct motion of the apogeal point of her orbit, and the months in which the Sun and Moon must be eclipsed.

On

On the great immoveable plate A (fee Fig. 1.) are the months and days of the year, and the figns and degrees of the zodiac fo placed, that when the annual index b is brought to any given day of the year, it will point to the degree of the fign in which the Sun is on that day.—This index is fixed to the moveable frame BC, and is carried round the immoveable plate with it, by means of the knob n. The carrying this frame and index round the immoveable plate, answers to the Earth's annual motion round the Sun, and to the Sun's apparent motion round the ecliptic in a year.

The central wheel D (being fixed on the axis a, which is fixed in the center of the immoveable plate) turns the thick wheel E round its own axis by the motion of the frame; and the teeth of the wheel E take into the teeth of the three wheels F, G, H, whose axes turn within one another, like the axes of the hour, minute, and facond

hands

hands of a clock or watch, where the feconds are shewn from the center of the dial-plate.

On the upper ends of these axes are the round plates I, K, L; the plate I. being on the axis of the wheel F, K on the axis of G, and L on the axis of H. So that, whichever way these wheels are affected, their respective plates, and what they support, must be affected in the same manner; each wheel and plate being independent of the others.

The two upright wires M and N are fixed into the plate I; and they fupport the fmall ecliptic OP, on which, in the machine, the figns and degrees of the ecliptic are marked.—This plate alfo fupports the fmall terreftrial globe e on its inclining axis f, which is fixed into the plate near the foot of the wire N. This axis inclines 232 degrees from a right line, supposed to be perpendicular to the furface of the plate I, and 66 to the plane of the small ecliptic H 4

ecliptic OP which is parallel to that

plate.

On the Earth e is the crescent g, which goes more than half way round the Earth, and stands perpendicular to the plane of the fmall ecliptic OP, directly facing the Sun Z: its use is to divide the enlightened half of the Earth next the Sun from the other half which is then in the dark; fo that it represents the boundary of light and darkness, and therefore ought to go quite round the Earth; but cannot, in a machine, because, in fome politions, the Earth's axis would fall upon it.—The Earth may be freely turned round on its axis by hand, within the crescent, which is supported by the crooked wire w, fixed to it, and into the upper plate of the moveable frame B.C.

In the plate K are fixed the two upright wires \mathcal{Q} and R: they support the Moon's inclined orbit ST in its nodes, which are the two opposite points of the

the Moon's orbit where it interfects the ecliptic OP. The afcending node is marked a, to which the descending node is opposite, below e, but hid from view by the globe e. The half a a a of this orbit is on the north side of the ecliptic a a is on the south side of the ecliptic. The Moon is not in this machine: but, when she is in either of the nodes of her orbit in the heavens, she is then in the plane of the ecliptic: when she is at a in her orbit, she is in her greatest north latitude; and when she is at a a, she is in her greatest south latitude.

In the plate L is fixed the crooked wire U U, which points downward to the fmall ecliptic O P, and shews the motion of the Moon's apogee therein,

and its place at any given time.

The ball Z represents the Sun, which is supported by the crooked wire XY, fixed into the upper plate of the frame at X. A straight wire W proceeds from the Sun Z, and points always toward

the center of the Earth e; but toward different points of its surface at different times of the year, on account of the obliquity of its axis, which keeps its parallelism during the Earth's annual course round the Sun Z; and therefore must incline sometimes toward the Sun, at other times from him, and twice in the year neither toward nor from the Sun, but sidewise to him. The wire W is called the solar ray.

As the annual index b shews the Sun's place in the ecliptic for every day of the year, by turning the frame round the axis of the immoveable plate A, according to the order of the months and signs, the solar ray does the same in the small ecliptic OP: for, as this ecliptic has no motion on its axis, its signs and degrees still keep parallel to those on the immoveable plate. At the same time, the nodes of the Moon's orbit ST (or points where it intersects the ecliptic OP) are moved backward,

backward, or contrary to the order of figns, at the rate of 19½ degrees every Julian year; and the Moon's apogeal wire UU is moved forward, or according to the order of the figns of the ecliptic, nearly at the rate of 41 degrees every Julian year; the year being denoted by a revolution of the Earth e round the Sun Z; in which time the annual index b goes round the circles of months and figns on the immoveable plate A.

Take hold of the knob n, and turn the frame round thereby; and in doing this, you will perceive that the north pole of the Earth e is conftantly before the crefcent g, in the enlightened part of the Earth toward the Sun, from the 20th of March to the 23d of September; and the fouth pole all that time behind the crefcent in the dark; and, from the 23d of September to the 20th of March, the north pole is conftantly in the dark, behind the crefcent, and the fouth pole in the light before it:

which shews that there is but one day and one night at each pole, in the whole year; and that, when it is day at either pole, it is night at the other.

From the 20th of March to the 23d of September, the days are longer than the nights in all those places of the northern hemisphere of the Earth which revolve through the light and dark, and shorter in those of the southern hemisphere.—From the 23d of September to the 20th of March, the reverse.

There are 24 meridian semicircles drawn on the globe, all meeting in its poles; and as one rotation or turn of the Earth on its axis is performed in 24 hours, each of these meridians is an hour distant from the other, in every parallel of latitude.—Therefore, if you bring the annual index b to any given day of the year, on the immoveable plate, you may see how long the day then is at any place of the Earth, by counting how many of these meridians

meridians are in the light, or before the crefcent, in the parallel of latitude of that place; and this number being fubtracted from 24 hours, will leave remaining the length of the night.— And if you turn the Earth round its axis, all those places will pass directly under the point of the solar ray, which the Sun passes vertically over on that day, because they are just as many degrees north or south of the equator, as the Sun's declination is then from the equinoctial.

At the two equinoxes, viz. on the 20th of March and 23d of September, the Sun is in the equinoctial, and confequently has no declination. On these days, the solar ray points directly toward the equator, the Earth's poles lie under the inner edge of the crescent, or boundary of light and darkness; and, in every parallel of latitude, there are twelve of the meridians, or hour-circles before the crescent, and twelve behind it; which shews that the days

and nights then are each twelve hours long at all places of the Earth. And, if the Earth be turned round its axis, you will fee that all places on it go equally through the light and the dark hemispheres.

On the 21st of June, the whole space within the north polar circle is enlightened, which is 23½ degrees from the pole, all around; because the Earth's axis then inclines 23½ degrees toward the Sun; but the whole space within the south polar circle is in the dark; and the solar ray points toward the tropic of Cancer on the Earth, which is 23½ degrees north from the equator.—On the 20th of December the reverse happens, and the solar ray points toward the tropic of Capricorn, which is 23½ degrees south from the equator.

If you bring the annual index b to the beginning of January, and turn the Moon's orbit ST by its supporting wires 2 and R till the ascending node (marked

(marked a) comes to its place in the ecliptic O P, as found by an Ephemeris, or by Astronomical Tables, for the beginning of any given year; and then move the annual index by means of the knob n, till the index comes to any given day of the year afterward, the nodes will fland against their places in the ecliptic on that day.-And if you move the index onward, till either of the nodes comes directly against the point of the solar ray, the index will then be at the day of the year on which the Sun is in conjunction with that node. At the times of those new Moons which happen within feventeen days of the conjunction of the Sun with either of the nodes, the Sun will be eclipfed: and at the times of those full Moons, which happen within twelve days of either of these conjunctions, the Moon will be eclipsed. - Without these limits there can be no eclipse either of the Sun or Moon; because, in nature, the Moon's

Moon's latitude or declination from the ecliptic, is too great for the Moon's shadow to fall on any part of the Earth, or for the Earth's shadow to touch the Moon.

Bring the annual index to the begining of January, and fet the Moon's apogeal wire UU to its place in the ecliptic for that time, as found by Aftronomical Tables: then move the index forward to any given day of the year, and the wire will point on the fmall ecliptic to the place of the Moon's

apogee for that time.

The Earth's axis f inclines always toward the beginning of the fign Cancer on the fmall ecliptic O P .- And, if you fet either of the Moon's nodes, and her apogeal wire, to the beginning of that fign, and turn the plate A about, until the Earth's axis inclines toward any fide of the room (fuppose the north fide) and then move the annual index round and round the immoveable plate A, according to the order

order of the months and figns upon it, you will fee that the Earth's axis and beginning of Cancer will still keep toward the fame fide of the room, without the least deviation from it; but the nodes of the Moon's orbit ST will turn progressively towards all the fides of the room, contrary to the order of figns in the fmall ecliptic OP, or from east, by fouth, to west, and so on: and the apogeal wire U U will move the contrary way to the motion of the nodes, or according to the order of the figns in the small ecliptic, from west, by south, to east, and so on quite round.-A clear proof that the wheel F, which governs the Earth's axis and the fmall ecliptic, does not turn any way round its own center; that the wheel G, which governs the Moon's orbit O P, turns round its own center backward, or contrary both to the motion of the frame BC and thick wheel E; and that the wheel H, which governs the Moon's apogeal wire UU, turns

turns round its own center, forward, or in direction both of the motion of the frame, and of the thick wheel E, by which the three wheels, F, G, and H, are affected.

The wheels D, E, and F, have each 39 teeth in the machine; the wheel G has 37, and H 44; as shewn in Fig. 3.

The parallelism of the Earth's axis is perfect in this machine; the motion of the apogee very nearly so; the motion of the nodes not quite so near the truth, though they will not vary sensibly therefrom in one year.—But they cannot be brought nearer, unless larger wheels, with higher numbers of teeth, are used.

In nature, the Moon's apogee goes quite round the ecliptic in eight years and 312 days, in direction of the Earth's annual motion; and the nodes go round the ecliptic in a contrary direction, in eighteen years and 225 days.—In the machine, the apogee goes round the ecliptic OP in eight years

years and four-fifths of a year, and the nodes in eighteen years and a half.

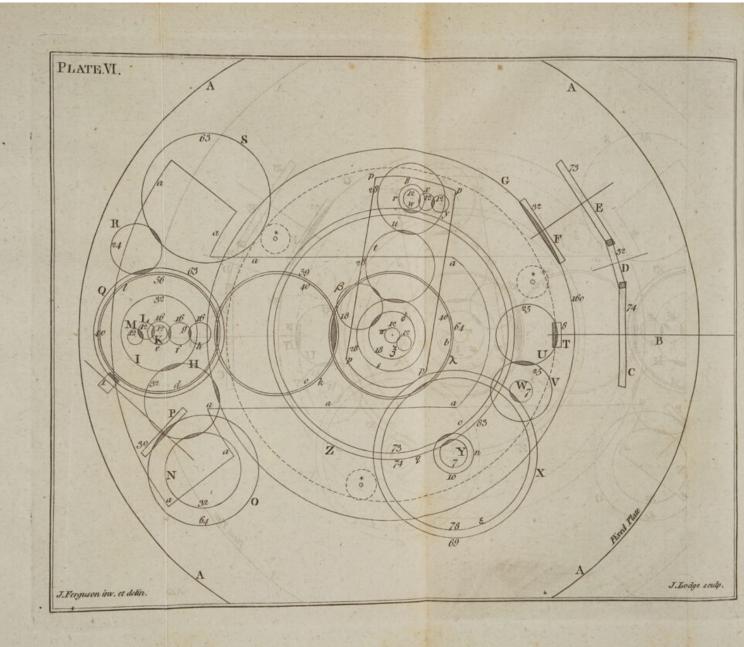
Notwithstanding the difference of the numbers of teeth in the wheels F, G, and H, and their being all of equal diameters, they take tolerably well into the teeth of the thick wheel E, because they are made of soft wood. -But, if they were made of metal, the wheel E in Fig. 1. ought to be made of the shape of E (feen edgewife) in Fig. 3. with very deep teeth: and the wheels F, G, and H, in Fig. 1. of diameters proportioned to their respective numbers of teeth, as F, G, and H, in Fig. 3. And then the teeth of these three wheels would be of equal fizes with those of the wheel E wherein they work: and the motions would be free and eafy, without any pinching or shake in the teeth.

that I can; and do with the 'de(crip-

An Orrery, Shewing the Motions of the Sun, Mercury, Venus, Earth, Moon, and Nodes of the Moon's Orbit; the different Lengths of Days and Nights, the Vicissitudes of Seasons, Age and Phases of the Moon, and all the Solar and Lunar Eclipses.

The use of this Orrery, and the manner of using it, being already defcribed in my Astronomy, I shall not repeat those matters here; but shall only describe the wheel-work of it, which is not done in that book. It is not copied from any other Orrery whatever, and I can truly fay, that it shews the revolutions of the Moon and Planets nearer the truth than any other Orrery does, that has fallen under my examination. I therefore freely give the following account of it to the Public, in the best manner that I can; and do wish the description may be generally understood. To any





any Clock-maker I hope it will be plain, and to every Orrery-maker I believe it will be quite fo.

The fixth Plate is a plan of the wheel-work, in which the diameter of each wheel is equal to the femidiameter or radius thereof in the Orrery I have made: the numeral figures at each wheel shew the number of teeth in that wheel, and the shaded parts shew where the teeth of any one wheel takes into the teeth of another, as the one turns the other.

The feventh Plate is a fection or fideview of all the wheel-work that could be brought into fight. But in this, fome few wheels could not be shewn; for, in the Orrery itself, take a view of the wheels on any fide you pleafe, fome of them will be unavoidably hid from fight by others that are between them and the eye.

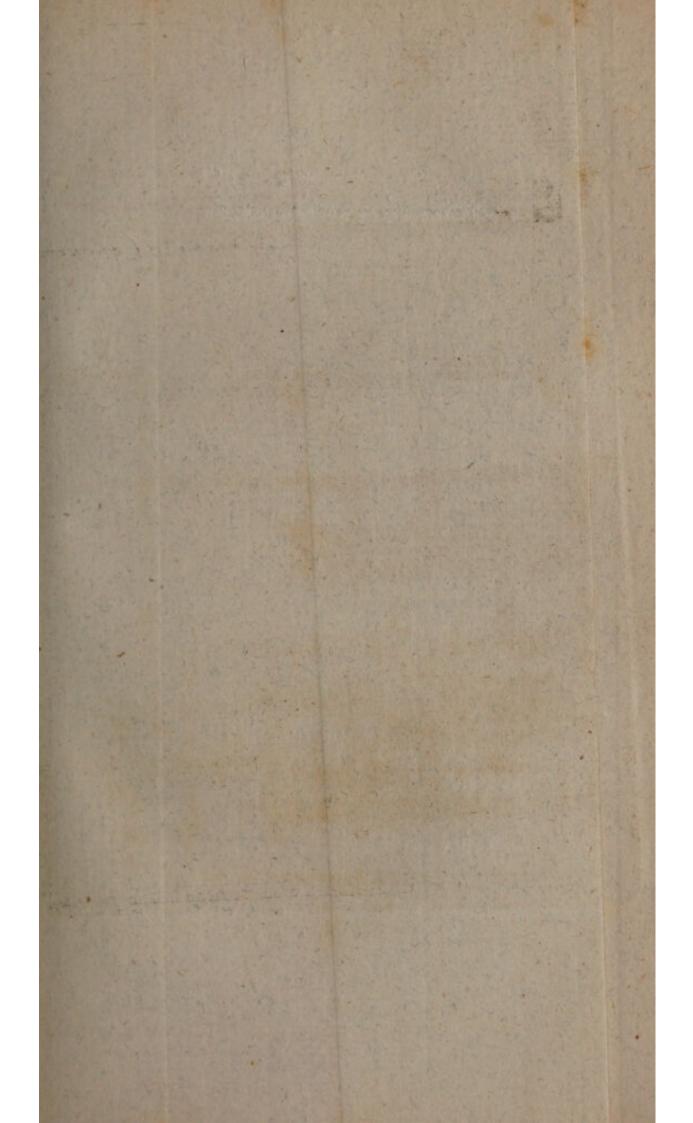
Those in Plate VII. that come in fight have the same numeral figures set to them as the like ones have in Plate VI.

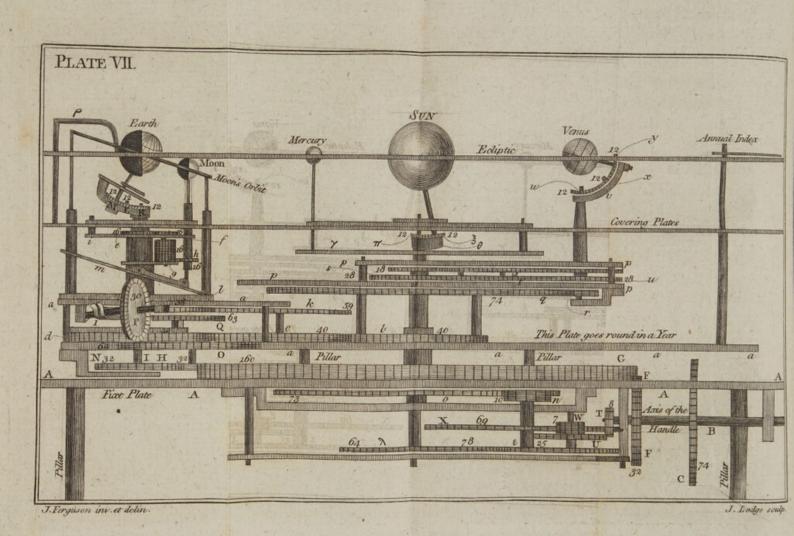
I 3

and also the same letters of reference where there is room to insert them. And therefore, in reading the description of Plate VI. it will be requisite to look first at it, and then at Plate VII.; by which means the Reader will see the position of these wheels with respect to each other, as they are placed higher or lower in the frames which contain them.

AAAA is a round immoveable plate fupported by four pillars; some of the wheels are below it, but the greatest number of them are above it. It supports and bears the weight of them all.

B is the axis of the handle or winch by which all the wheels are turned: on its axis is a wheel C of 74 teeth, which turns a wheel D of 32, and D turns a wheel E of 73 teeth, on whose axis is a wheel F of 32, turning a wheel G of 160 teeth, which turns a wheel H of 32, and H turns a wheel I of the same number, on the top of whose axis





is a small wheel K of 12 teeth (just under the Earth) which turns a wheel L of the same number and fize; and L turns fuch another wheel M of the fame number. The axis of Minclines 232 degrees, and the Earth at the top of it is turned round by it. The wheel Hof 32 teeth turns a wheel N of the fame number, on the top of whose axis is an index which goes round a circle of 24 hours (on the plate that covers the wheel-work), in the time the Earth turns round its axis. - The wheels D and E could not be shewn in Plate VII. because the wheel C of 74 teeth hides them from fight.

On the axis of the wheel N is a wheel O of 64 teeth, turning a contrate wheel P of 30, on whose axis is an endless serew, of a single thread 1, turning a wheel 2 of 63 teeth, which carries the Moon round the Earth in her orbit, from change to change, in 29 days 12 hours 45 minutes. This wheel of 63 teeth turns a wheel R of

24, which turns a wheel S of 63 teeth round in 29 days 12 hours 45 minutes, on whose axis is an index that shews the days of the Moon's age on a circle of 29½ equal parts, on the plate that covers the wheel-work.

On B, the axis of the handle, is a pinion T of 8 leaves, turning a wheel U of 25 teeth, which turns another wheel V of the fame number and fize, on whose axis is a pinion Wof 7 leaves, turning a wheel X of 69 teeth, on whose axis is a pinion Y of 7 leaves, turning a wheel Z of 83 teeth once round in 365 days 5 hours 48 minutes 57 feconds, and carrying the Earth round the Sun in that time. For, in this wheel are four short pillars, whose upper ends are fixed into the lower plate of a moveable frame a a a a a a a (Plate VI.) that turns round on a fixed upright pin in the center of the plate AAAA, and contains the above-mentioned wheels belonging to the Earth and Moon: fo that the whole frame goes round the center pin in the fame time with the wheel Z.

This last wheel cannot be seen in Plate VII. because it lies within the wheel G, which is only a thick ring having 160 teeth on its outside. Its innermost fide is represented by a dotted circle in Plate VI. and it is kept in its place by three rollers, marked * * *, which turn upon pins fixed in the great

immoveable plate AAAA.

As the uppermost edge of the contrate wheel F (see Plate VII.) must come a little way through the plate AAAA, in order to turn the ringwheel G that lies on the upper fide of this plate, and this wheel turns the wheel Hof 32 teeth that belongs to the Earth's diurnal motion; it is plain, that as the wheel H must go round G in a year by the annual part of the work, G must be thick enough to turn Hat fuch a distance from or above the plate AAAA, that H may go over the top of F without touching it: otherwife,

wife, when H came round to F, it could not pass by, but would stop the annual motion.

In the center, just above the upper furface of the moveable frame-plate aaaa, is a fixed wheel b of 40 teeth taking into the teeth of the wheel c, which is also 40 in number; and these take into the teeth of a wheel d, whose number is 40 also. The axis of this last wheel is hollow, and the top of it is fixed tight at K (see Plate VII.) in the piece KL M that carries the Earth.—This part of the work keeps the Earth's inclined axis in a conflant parallelism in its annual course round the Sun. For, as d is connected with the fixed wheel b, by means of the intermediate wheel c, and c rolls or goes round b by the annual work, and as b, c and d have equal numbers of teeth, d must always preserve its parallelism throughout its annual motion. The axis of b is fixed into the immoveable plate AAAA; and it is hollow, to let the the axis of fome wheels below that plate turn within it.

The folid spindle, or axis of the wheel I of 32 teeth, turns within the hollow axis of the wheel d of 40; and on the top of this solid spindle is the small wheel K of 12 teeth, which turns the Earth round its axis by the wheels L and M, of equal number and size with K, as already mentioned.

The hollow axis of the parallelifmwheel d is within an upright focket, whose lowermost end is fixed into the top plate (marked 56 in Plate VII.) of the moveable frame a a a a, and on the top of this focket is fixed a small wheel e of 16 teeth, which take into the teeth of another wheel f of the fame number and fize; on the axis of which is a long pinion g of 16 leaves, which take into the wheel b of 16 teeth, whose axis is hollow, and has a black cap on the top of it, covering just one half of the Moon .--- Now, as the focket, on whose top the wheel e is placed,

placed, is fixed into the annual moving frame, it is plain, that, whichever fide or tooth of the wheel e is once toward the Sun, will always be fo; and therefore, as the wheel f, the pinion g, and the wheel b, go all round the wheel e by the work that carries the Moon round the Earth, and all these have equal numbers of teeth, the wheel h will always keep the Moon's cap facing towards the Sun, and shew her to be always full as feen from the Sun, but continually changing her phases as feen from the Earth in her going round it. For, when the Moon is between the Earth and the Sun (as reprefented in Plate VII.) her cap will hide the whole of her from the Earth: but, when she is opposite to the Sun, all the half or fide of her next the Earth will then appear like a full Moon, before the circular edge of the cap: and when she is mid-way between these positions, or in either of her quadratures, the will appear just half enlightened as feen from the Earth.

The

The axis of the wheel 2, of 63 teeth, which carries the Moon round the Earth, is hollow, and turns round upon the above-mentioned fixed focket. To the top of this axis (just under the wheel e of 16 teeth, Plate VII.) is fixed the bar if, which carries the Moon round the Earth by the motion of the wheel 2.

On the top of the axis of the wheel c of 40 teeth, is a wheel k of 59, turning a wheel l of 56, which cause the nodes of the Moon's orbit to go once round, with a retrograde motion, thro' all the figns and degrees of the ecliptic, in 18 2 years. The axis of 1 is hollow, and turns upon the hollow axis of 2; and on the axis of l is a circular plate m(Plate VII.) fixed obliquely on that axis, and parallel to the Moon's orbit. The work that carries the Moon round the Earth carries also the piece g round upon this oblique plate; and, as the lower end of the Moon's axis (which turns within the hollow axis

of her cap) is fixed into the piece g, it causes the Moon to rise and fall in her oblique orbit, according to her north or south latitude or declination from the ecliptic. As the nodes of her orbit are even with the plane of the ecliptic, one half of her orbit is on the north side, and the other half on the south side of the ecliptic.

On the axis of the wheel X, which has 69 teeth, is a pinion n of 10 leaves, turning a wheel o of 73 teeth, which carries Venus round about the Sun in 224 days 17 hours. The axis of the wheel o is hollow (because another axis turns within it) and on the top of it is fixed the lower plate of the frame pppp, which carries Venus round the Sun, and has wheels within it belonging to Venus and to Mercury.

Under the lowest plate of this frame is a fixed wheel q of 74 teeth, of the same diameter as the wheel Z of 83, which gives the Earth its annual motion; so that, in Plate VI. one and the

fame

A pinion r of 8 leaves takes into the teeth of the fixed wheel q, and is carried round q by the motion of the frame pppp, that carries Venus round the Sun. Confequently, in the time this pinion is carried round the wheel, it will turn 9^{1}_{+} times round its axis, equal to the number of Venus's days and nights in the time she goes round the Sun.

The wheel q of 74 teeth is fixed on the fame (above-mentioned) focket on which the wheel b of 40 teeth is fixed. The top of this focket goes through the lower plate of the frame ppp, and a wheel s of 28 teeth is fixed upon the top of this focket, just above the fame plate. Another wheel t of 28 teeth takes into the teeth of s, and is carried round it by the motion of the frame: and a third wheel u of 28 teeth (which is also carried round by the frame) takes into the teeth of t: the axis of u is hollow, it turns upon the Sec. W

the folid spindle or axis of the pinion r of 8 leaves, and on its top is fixed the curved piece v (Plate VII.) that carries Venus on her inclined axis, which, by means of the three last-mentioned wheels of 28 teeth, is kept in a constant parallelism in going round the Sun.

On the top of the axis of the pinion r of 8 leaves, and just above the curved piece v (Plate VII.) is a small wheel w of 12 teeth, which turns another wheel x of the same number and size; and this last wheel turns a third wheel y of the same number, which is sixed on the axis of Venus, and turns her g^{\perp}_{τ} times round her axis in the time she goes round the Sun; which is just as often as the pinion r turns round in the time it is carried round the fixed wheel q of 74 teeth.

On the top of the axis of the middle wheel t of 28 teeth, is another wheel of the same number and size, which turns a wheel β of 18 teeth; and this wheel

wheel turns another wheel & of the fame number, whose axis is a hollow focket, on which a bar γ (Plate VII.) is fixed; and this bar carries Mercury round the Sun in 87 days 23 hours.

On the axis of the wheel X (already mentioned) of 69 teeth is a wheel ε of 78, which turns a wheel λ of 64 round its axis in 25 days 6 hours. The axis of this wheel turns within the abovementioned hollow arbors in the center; and on its top is the small wheel π of 12 teeth, which turns another wheel ξ of the same number and size: this last wheel is fixed on the Sun's axis, it turns in the fixed piece θ (Plate VII.) and turns the Sun round his axis in 25 days 6 hours.

The Sun's axis inclines 7^t/₂ degrees from a perpendicular to the ecliptic; Venus's axis 75 degrees and the

Earth's axis 231.

The Earth turns round within a black cap, that always covers the half of it which at any instant of time is turned

turned quite away from the Sun: the edge of the cap represents the folar horizon, or circle bounding light and darkness: it is supported by a crooked wire p, whose lower end is fixed into the plate that covers the wheels, and is carried round by the annual motionwork. An index (called the annual index) goes round the ecliptic, by the same work, keeping always opposite to the Sun, and shewing the days of the months, and the Sun's apparent place in the ecliptic as seen from the Earth.

On looking at Plate VI. it may perhaps appear, even to a very ingenious mechanic, that the wheels C, D, and E are supersuous; and that the wheel F, which gives motion to the toothed ring G, might have been upon the axis B of the handle. For, as F has 32 teeth, and H, that is turned by the teeth of G (and turns the Earth round its axis), has also 32 teeth, F and H would turn round in equal times; and conse-

consequently, a turn of the handle would have answered to a turn of the Earth on its axis.—This indeed would have been the case if the Earth had no annual motion: but as H goes round G in a year, the fame way that G turns round, H loses five turns in going round G (for 5 times 2 is 160) the number of teeth in G), and then the handle would have turned 370 times round in the time the Earth made 365 rotations .- To prevent this, and fo make the turns of the Earth and handle agree together, C has 74 teeth, and E only 73. So that the wheel E will turn five times oftener round than the handle does in 365 turns thereof; and confequently make the Earth's daily rotation equal to a turn of the handle, or to 24 hours of mean folar time.

Another Orrery.

This is the Orrery mentioned in my Tables and Tracts (page 169, 2d edition) which I intended to keep for my fon, who was then ferving an apprentice-fhip to a mathematical instrument-maker. But, as it has pleased God to call him from this world to a better, I shall now freely communicate it to the Public.

It shews the length of day and night at all places of the Earth, every day of the year, with the Sun's true place, declination, time of rising and setting, the hour of the day, the Sun's altitude, azimuth, and the variation of the compass at any place. Also the Moon's periodical and synodical revolution, her motion on her axis, her latitude, altitude, azimuth, rising and setting; her mean anomaly and elliptic equation; with the days of all the new and full Moons and eclipses, for 6000 years before

before and after the Christian æra.—
The out-side figure of this Orrery is exactly shewn in the eighth plate of my Astronomy; but the inside work differs much from what is represented in the second figure of that plate: and this inside work is what I shall now describe.

A large wheel of 235 teeth is fixed in the box that contains the work, the center of the wheel being in the center of the box, directly under the Sun's center. On this wheel runs a pinion of 19 leaves, carried round the teeth of the wheel by the annual motion of the Earth; and by this means, the pinion is turned round its own axis for every 19 teeth that it is carried onward, in going round the wheel .-Now, fuppofing this pinion to be carried round the wheel in 365 days, the pinion will be turned round its own axis in 29 days 12 hours 44 minutes 25 feconds, and a bar on the axis of the pinion will earry the Moon round the Earth, from change to change, in that time. This comes so near to the truth, as to vary but one day in the Moon's course in 335 years; and these are the nearest numbers for such simple wheel-work that can possibly be found for mean lunations.

But in nature, the Earth moves unequally round the Sun, so that there
are 8 days more between the vernal
and autumnal equinox, than between
the autumnal and vernal.—And therefore, in common Orreries, where this
circumstance is taken no notice of,
the Earth's position to the Sun cannot
be right at both the equinoctial points.

In order to avoid this error, I first divided the ecliptic into 360 equal parts for degrees; and then, after having put the names of the signs to it, I laid down the days of the year from an ephemeris against the degrees of the Sun's place in the ecliptic, for each day respectively throughout the year. By this means, the daily spaces answer-

answering to the Earth's unequal motion round the Sun, were so divided, as to be continually and gradually lessening from the 30th of December till the first of July; and then as gradually lengthening from the first of July to the 30th of December; as the Earth's progressive annual motion is swiftest of all on the 30th of December, and slowest of all on the first of July.

July.

The days of the months being unequally divided, fo as to answer to the Earth's unequal motion round the Sun, I made these divisions a pattern or scale for dividing the 235 teeth of the above-mentioned wheel into such unequal spaces as would agree with the spaces allotted for the days answering to them. But these gradual inequalities of the teeth were so very small, and the difference so little between the widest and narrowest, that the pinion (whose leaves were all equal, run very smoothly through all the teeth of the wheel; as the leaves

of the pinion were fized to thefe teeth, which were at a mean rate between the greatest and least distances from one another. By this contrivance, the mean lunation was always 29 days 12 hours 44 minutes 25 feconds throughout the whole year; and the pinion was among the least distant teeth of the wheel when the annual index was at the first of July, and among the most distant teeth when the index was at the 30th of December.

For the parallelism of the Earth's axis, a wheel of 59 teeth was fixed in the middle of the work, with its center directly over the center of the wheel of 235 teeth, and the teeth of another wheel of 59 took into the teeth of the former; and those into the teeth of a third wheel of the fame number, on the top of whose axis the piece that carries the Earth on its oblique axis was fixed. And, as the Earth was moved round the Sun, these three wheels kept the parallelism of the Earth's axis, as described in the Mechanical Paradox, and the former Or-

rery.

Above the middlemost wheel of 59, and on its axis, is fixed a wheel of the fame number, which takes into a wheel of 56 teeth: this last wheel is just below the Earth, and turns the nodes of the Moon's orbit quite round backward, in 182 years.

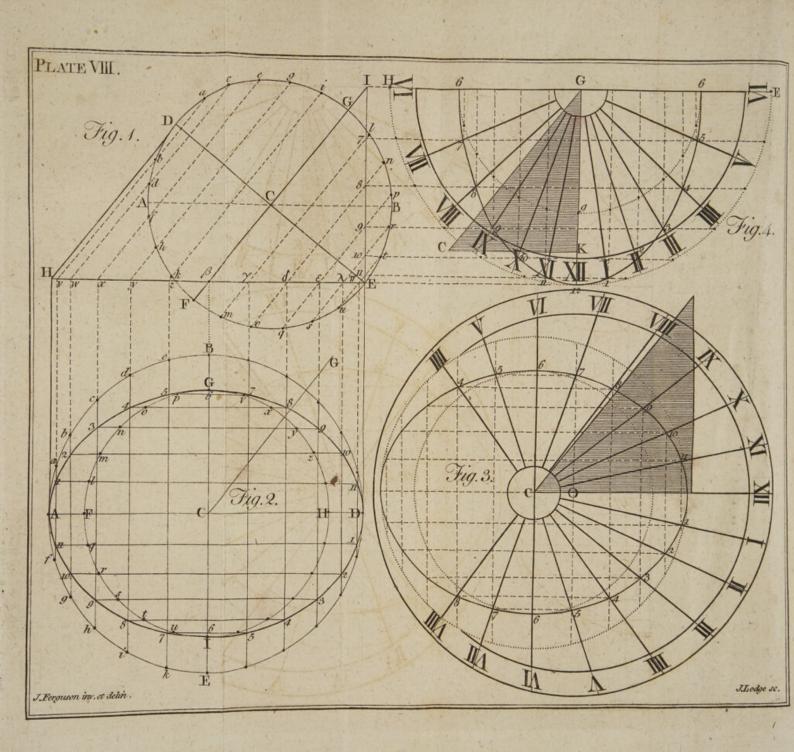
Above the last-mentioned wheel of 59 teeth, and on the fame axis with it, is a wheel of 55, turning a wheel of 62 teeth below the Earth; and this wheel of 62 moves the Moon's apogee plate quite round forward, in 8 years 312 days. And from this plate a wire rifes, and points out the place and motion of the apogee in the Moon's ecliptic.

[By comparing this description with that of the Orrery in the 8th plate of my Astronomy (see § 399.) it will be very easily understood: particularly those parts which shew the parallelism of the Earth's axis, the motion of the Moon's nodes, and apogee.] As As the Moon goes round the Earth, she comes to her mean changes, nodes, and apogee, in the proper times; and, at all intermediate times, her distance from her apogee and nodes are shewn in her ecliptic, orbit, and apogee plate; on which last her mean anomaly and elliptic equation are shewn: by which means her true place in the ecliptic, and her latitude, may be very nearly found for any given time.

The days of the months, throughout the year, are laid down in a diagonal manner, in a spiral line of four revolutions, marked o, 1, 2, 3, for leap year, and the first, second, and third years after. The annual index, in these spirals, being at the given day of any month, for either of these years, all the other motions and phenomena will be right for that day: and, by means of these diagonals, the lunation is brought still nearer the truth than as above specified.

Within this fet of spirals are tables, which shew the places of the Sun, Moon,





Moon, Ascending Node, and Apogee, for the noon of the first day of January, in any year within the limits of 6000 years both before or after the Christian æra. And, by means of these tables, the Orrery may, in less than two minutes of time, be rectified for the beginning of any of these years; and then, all the motions, not only for that year, will be right, but also for 334 years afterward, without needing any rectification.

A New Geometrical Method of constructing Sun-Dials.

Draw at pleasure the horizontal line ACB (Plate VIII. Fig. 1.) and on the point C, as a center, describe the circle DGEF. Draw the diameter DGE, fo as to make an angle (DCA) with ACB equal to the co-latitude of the place for which the dial is to ferve; and draw FCG at right angles (or perpendipendicular) to DCE: then ACB shall represent the horizon of the place, DCE the equinoctial, ECG the axis of the world and stile of the dial, G the north pole, F the south pole, and the arc BG the elevation of the pole above the north point of the horizon; which elevation is equal to the latitude of the place.

From the point E draw the right line E H parallel to the horizon ACB, and from the point D draw D H parallel to CF. So E H shall be equal to the longest diameter of an ellipsis (Fig. 2.) and D E equal to the shortest diameter thereof. Divide the circle DGEF into 24 equal parts, beginning at D; and connect the division-points which are equidistant from D by the straight lines ab, cd, ef, &c. continuing these lines down to the points v, w, x, y, z, in that part of the line HE that falls without the circle.

From the point β , where GCF interfects HE, draw βBCE (Fig. 2.)

perpendicular to $H\beta E$ (Fig. 1.) and draw ACD in Fig. 2. parallel to $H\beta E$ in Fig. 1. So, in Fig. 2. BCE and ACD shall cross each other at right angles in the point C .- On this point, as a center, with the length βH or β E in Fig. 1. as a radius, defcribe the circle ABDE in Fig. 2. and divide it into 24 equal parts, beginning at A, and connect the division-points, which are equidifiant from A, by the straight lines af, bg, cb, di, ek, &c. Then, from Fig. 1. take CD in your compaffes, as a radius; and, with that extent, on C, as a center in Fig. 2. describe the circle FGHI, and divide it into 24 equal parts, beginning at G. Through these division-points p, v, o, x, n, y, &c. which are equidiffant from G, draw the right lines 57, 48, 39, 210, &c. meeting the lines within the former circle at the points 5, 7, 4, 8, 3, 9, 2, 10, I, II, on the fide AGD; and at 7. 5, 8, 4, 9, 3, 10, 2, 11, 1, on the fide AID. Then, through these points of meeting, draw by a fleady hand the ellipfis AT

A 1 2 3 4 5 6 7 8, &c. whose longest diameter AD is equal to $H \beta E$ in Fig. 1. and its shortest diameter GI equal to DCE in the same figure, as above mentioned.

This done (which may be much fooner done than described) lay the edge of a straight ruler to the center C in Fig. 2. and to the above-mentioned division-points 5, 7, 4, 8, &c. in the ellipsis, and draw straight lines from C through these points, as in Fig. 3.; and they will be the true hour-lines on a horizontal dial.

Lastly, from the center C, in Fig. 2. draw the straight line C G parallel to CG in Fig. 1. for the axis of the stile, or edge thereof that casts a shadow on the time of the day; and CG shall be parallel to the axis of the world when the dial is truly set, as the like edge of the stile of every dial must be.

[N. B. Straight lines, parallel to BCE in Fig. 2. being drawn through the ellipsis from the points (Fig. 1.)

 $v, w, x, y, z, \beta, \gamma, \delta, \varepsilon, \lambda, \pi$, will cut the ellipsis in the points 1 11, 2 10, 3 9, &c. through which the hour-lines on the horizontal dial must be drawn from the center C.

The point C (Fig. 3.) from which the hour-lines are drawn, should not coincide with the center O of the dialplate, but be taken at some small distance from it, toward the left-hand from XII in the meridian line, in order to enlarge the spaces between the hours near mid-day, as the angular distances between them are less than those about VI in the morning or afternoon.

From the point E in Fig. 1. draw E I perpendicular to E H, till it meets the axis F C G (produced beyond G) in I. Then, as H β E reprefents a horizontal plane, fo E I will reprefent a vertical one, facing the fouth; and ferve for shewing how to draw the hour-lines on an erect direct fouth dial, as Fig. 4.

From the point I in Fig. 1. draw IHGE perpendicular to EI: and make G H in Fig. 4. equal to E I in Fig. 1. With this extent, as a radius, fet one foot of the compasses in G (Fig. 4.) and with the other foot defcribe the femicircle H 12 E, and divide it into 12 equal parts. Through these points of division, which are equidistant from 12, draw the straight lines 11 1, 10 2, 9 3, 8 4, and 7 5. Make G 6 in Fig. 4. equal to CD in Fig. 1. and with that extent, as a radius, fet one foot of the compasses in G (Fig. 4.) and with the other foot describe the femicircle 6 g 6. Then divide this femicircle into 12 equal parts, and thro' these points of division draw straight lines parallel to Gg, meeting the former straight lines (drawn parallel to HE) in the points 7 5, 8 4, 9 3, &c. and draw the femi-ellipsis 6 7 8 9 10 11 12 1 2 3 4 5 6 through these points. So the longest diameter G 12 of this femi-ellipsis shall be equal to IE in Fig.

Fig. 1. and its shortest diameter 6 G 6 equal to DCE. This done, lay the edge of a ruler to the center G (Fig. 4) and fuccessively to all the divisionpoints 7, 8, 9, &c. in the same ellipsis, and draw straight lines from G thro' these points, as in the Figure, and they will be the true hour lines on the erect direct fouth dial; to which fet the hours, as in Fig. 4. and draw GC therein parallel to GC in Fig. 1. for the hypothenuse or axis of the stile that casts a shadow on the time of the day; and the dial will be finished when the stile GCK is erected upon the 12 o'clock line Gg K 12. And when the dial is truly set, the edge GC of the stile will be parallel to the axis of the world.

[N. B. Straight lines drawn parallel to HGE, thro' the semi-ellipsis 6 12 6, from the points (Fig. 1.) 7, 8, 9, 10, 11, in the perpendicular E I, where the lines lm, no, pq, rs, and tu, cut this perpen-

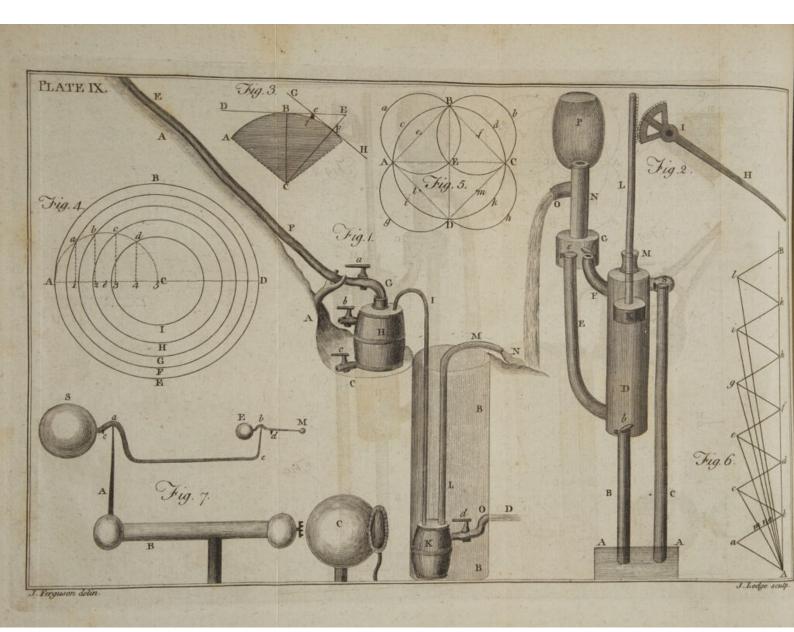
perpendicular, will cut the femi-ellipsis in Fig. 4. in those points through which the hour-lines must be drawn from the center G.]

And thus by means of a circle divided into 24 equal parts, as in Fig. 1. a horizontal dial or erect direct fouth dial may be made for any latitude. The method may perhaps appear tedious, on account of the number of words in the description: but I will venture to say, that whoever puts it in practice, will find it short, easy, and pleasant.

Description of the Hungarian Machine for raising Water from Mines.

In Fig. 1. of Plate IX. A A is the fide of a hill, close by the brink of the shaft or mine-pit B B, which is 104 feet deep below the surface of the ground C at the foot of the hill. In this hill





is a large spring of water, 143 feet above the furface of the ground at C (taken in perpendicular measure) and the fpring affords much more water than what the fpring D, under ground, lets in to the mine.

A pipe EFG lets the water down from the fpring in the hill, into a close air-tight vessel H that stands at the foot of the hill, that contains 572 cubic feet, or 43 gallons in wine meafure. In this pipe is a cock a, which being opened or thut, lets the water of the spring run into H, or stops it, as occasion requires: and in H are two cocks b and c, the uppermost of which is for letting air into H, and the lowermost for letting the water out of it.

A fmall pipe I goes from the veffel Hon the furface of the ground to a veffel K in the bottom of the mine, and terminates in the top thereof. This yeffel is air-tight, and contains 272 cubic feet, or 2053 gallons in wine measure, which is forced up the

afcend-

ascending pipe L M, and runs off to waste, at N, above ground. The lower end of this pipe goes down so far into the vessel K, as almost to touch its bottom.

From this vessel, a pipe O goes to the spring D under ground, which lets water into the mine, and would overslow it if the water was not forced up or raised from the mine, through the pipe LM. The pipe O lets this water into the vessel K when the cock d is turned open, and keeps back the water when the cock is shut.

The Operation is as follows:

The cock b being open, and the cocks a and c shut, and no water in the vessel K, open the cock d to let the vessel K fill with water from the spring in the mine. As this vessel fills, the water will drive the air out of it, up through the small pipe I into the vessel H, and all that air will go out of the

the vessel H by the open cock b, and then H will remain, as it was before, full of air in the same state of density as the common air is on the outfide of H. When K is full of water, thut the cocks b and d, and open the cock a to let water run down from the spring in the hill, by the pipe EF, into the veffel H. As the water rifes in that veffel, the air will thereby be driven out of it, down through the pipe I, into the veffel K: and as this air is compreffed by the weight of the running water in the pipe EF, the compressed air will force all the water out of the vessel K, up through the pipe LM, from which it will run off at N on the surface of the ground; and then the compressed air will rush out, after the water.

When the veffel K in the mine is emptied of water, and the air is heard to begin to rush out, shut the cock a to stop the water from the spring, and open the cocks b and c: then the water that came from the fpring will run

run out of the vessel H by the cock c, and air will go in by the cock b: at the same time, open the cock d in the mine, to let the vessel K fill with water from D the spring in the mine; and as H empties above-ground, K will fill below it; and the air that remained in K will (by the rising of the water in it) be driven back into the vessel H through the pipe I.

When H is empty of water, and K full, shut 'the cocks b, c, and d, and open the cock a: then H will fill with water from the spring in the hill; and this water, as it rises in H, will force the air out of H, down the pipe I, upon the water in K; and the force of the compressed air will drive all the water out of K, up the pipe L M, from which

it will run off at N, as before.

And thus, wherever there is a spring in a hill, near a mine, that affords more water than what slows into the mine from a spring under ground; and the perpendicular height of the spring

fpring in the hill is greater than the depth of the mine; water may thus be raifed from the mine, in a most simple and easy manner, by an engine in which there are neither pumps, pistons, nor valves: and such an engine will not be liable to be out of order, nor need repairs in many years. As this engine is but very little known in Britain, I have made a working model of it, which I always shew in my course of lectures.

But as there are very few mines that have hills near them with high fprings, water cannot then be raifed from them in this manner; and therefore Mr. Blakey proposed another method, which was, to make H an airvessel, with a pipe going from it to another vessel in which is water, kept boiling by a fire under it, and this vessel to have a cock to let out the steam occasionally that rises from the surface of the boiling water. When the cock is shut, the steam will go off from the

boiler into the air-veffel H, and drive the air out of it, down through the pipe I into the veffel K in the mine: and the force of the air compressed by the elasticity of the steam, will raise the water from K, up through the pipe LM, till K be emptied of water. Then the cock in the boiler is to be turned open, to let out the steam, and the cock d to be opened to let the vessel K fill from the spring in the mine: and when it was full, both these cocks are to be shut, and the operation will go on as before.

That Blakey's scheme would do, the Hungarian machine puts beyond all doubt.—In both of them the vessels must be made very strong, because every part of each vessel, equal in surface to the bore of the ascending pipe L M, will sustain an outward pressure equal to the whole weight of water in that pipe.—It will not answer for such depths as the common fire-engine will, nor will it raise so much water;

water; but it may be built for less than a third part of the expence, and would answer very well where the depth is not above 100 feet.

Description of a pump, invented by M. Dela-Hire, which raises Water equally quick by the Descent as by the Ascent of the Piston in the Pump-Barrel.

In Fig. 2. of Plate IX. AA is the well, in which the lower ends of the pipes B and C are placed. D is the pumpbarrel, into the lowermost end of which the top of the open pipe B is soldered, and in the uppermost end the hollow piece S is soldered, which opens into the barrel, and the top of the pipe C is soldered into that piece. Each of these pipes has a valve on its top, and so have the crooked pipes E and E, whose lower ends are open into the pump-barrel, and their upper ends into the box E.

H is the pump-handle, its center of motion is at I; and as it is moved up and down, it moves the folid plunger K up and down in the barrel, by the straight rod or spear L, which moves air-tight in a long collar of leathers in the neck M; and the plunger never goes higher than K, nor lower than D; so that from K to D is the length of the stroke.

As the plunger rifes from D to K, the atmosphere (pressing on the surface of the water A A in the well) forces the water up the pipe B, through the valve b, and fills the pump-barrel with water up to the plunger: and during this time, the valves e and S lie close and air-tight on the tops of the pipes E and C.

When the plunger is up to its greatest height at K, it stops there for an instant; and in that instant the valve b falls, and stops the pipe B at top. Then, as the plunger goes down, it cannot force the water between K and D back through

through the close valve b, but forces all that water up through the crooked pipe E through the valve e, which then opens upward by the force of the water; and this water, after having filled the box G, rises into the pipe N, and runs off by the spout at O.

During the descent of the plunger K, the valve f falls down, and covers the top of the crooked pipe F; and the pressure of the atmosphere on the well AA forces water up the pipe C, through the valve S, which then opens upward by the force of the ascending water; and this water runs from S into the pump-barrel, and fills all the space in it above the plunger.

When the plunger is down to its lowest descent at D, and stops there for an instant, in that instant the valve S falls down, and shuts the top of the pipe C: and then, as the plunger is raised it cannot force the water above it back through the valve S, but drives all that water up the crooked pipe F, through

ward by the force of the ascending water; which water, after filling the box G, is forced up from thence into the pipe N, and runs off by the spout at O.

And thus, as the plunger descends, it forces the water below it up the pipe E; and as it ascends, it forces the water above it up the pipe F; the presure of the atmosphere filling the pump-barrel below the plunger throw the pipe B while the plunger ascends, and filling the barrel with water above the plunger, through the pipe C, as the plunger goes down.

And thus, there is as much water forced up the pipe N to the spout 0 by the descent of the plunger, as by its ascent; and, in each case, as much water discharged at 0 as fills that part of the pump-barrel as the plunger

moves up and down in.

On the top of the pipe 0 is a close air-vessel P. When the water is forced

up above the spout O, it compresses the air in the vessel P; and this air, by the force of its spring acting on the water, causes the water to run off by the spout O in a constant (and very

nearly) equal stream.

Whatever the height of the spout O be above the surface of the well, the top S of the pipe C must not be 32 feet above that surface; because, if that pipe could be entirely exhausted of air, the pressure of the atmosphere in the well would not force the water up the pipe to a greater height than 32 feet. And if S be within 24 feet of the surface of the well, the pump will be so much the better.

As the collar of leathers within the neck M are apt to dry and shrink when the pump is not used, and confequently to let air get into the pumpbarrel, which would stop the operation of the atmosphere in the pipe C, I think collars of old hats might be used instead of leathers, as they would not be liable to that inconvenience.

It matters little what the fize of the pipe N be, through which the water is forced up to the fpout: but a great deal depends on the fize of the pump-barrel; and, according to the height of the fpout O above the furface of the well, the diameter of the bore of the barrel should be as follows.

For 10 feet high, the bore should be 6.9 inches; for 15 feet, 5.6; for 20 feet, 4.9; for 25 feet 4.4; for 30 feet, 4.0; for 35 feet, 3.7 inches; for 40 feet, 3.5; for 45 feet, 3.3; for 50 feet, 3.1; for 55 feet, 2.9; for 60 feet, 2.8; for 65 feet, 2.7; for 70 feet, 2.6; for 75 feet, 2.5; for 80 feet, 2.5 will do; for 85 feet, 2.4; for 90 feet 2.3; for 95 feet, 2.2; and for 100 feet, the diameter of the bore should not exceed 2.1 or 2.2 inches at most.—If these proportions are attended to, a man of common strength may raise water 100 feet high by one pump as eafily as he could raise it 10 feet high by another.

In this pump, the pipes B and C feem to be rather too fmall, which will

SELECT EXERCISES.

will cause the water rising in them to have a great deal of friction, from the quickness of its motion: and whoever makes such a pump, will find it very difficult to make the leathers in the neck M water-tight, so as that no water shall be forced out that way when the piston is drawn up.

The Height of the apparent Level above the true.

In Fig. 3. of Plate IX. let ABF be part of the Earth's spherical surface, C the Earth's center, BC or FC its semidiameter, DBE a tangent to the Earth's surface at B, drawn perpendicular to BC; and GFH a tangent to the Earth's surface at F, drawn perpendicular to FC. The line DBE is a true level at B; but being carried on straight toward D or E, it rises above the Earth's surface: and although it seems to be level as seen from

from B, it is above the true level at F, by the whole height FE; for, at the point F, the tangent GFH is the true level.

At the distance of a geographical mile, or 6094 feet, from the point B, the line BD or BE will be 10.637 inches above the globular furface of the Earth: at two fuch miles from B, the fame line will be four times as high (or 3 feet 6.548 inches) above the Earth's furface: at three miles diftance, nine times as high (or 7 feet 11.733 inches) above the Earth's furface; and fo on, always increasing in height according to the square of the distance: for, if F be twice the distance of f from B, FE must be four times as high as fe, if both their tops touch the right line BeE.

At the distance of an English mile, or 5280 feet, the apparent level is 7.90 inches higher than the true; at two miles distance, it is four times as high, or 2 feet 7.60 inches above the true;

at three miles distance, nine times as high; and so on, increasing in proportion to the square of the distance.

At the distance of a degree or 60 geographical miles, which are equal to 69. English miles, the height of the apparent level above the true is 3191 feet and parts of an inch. And therefore, a hill, whose top was so far above the level of the sea, would be just seen at top by an eye at the surface of the sea, and 69. English miles from the hill.

Of the Velocities acquired by falling Bodies, and the Spaces they fall through in given Times.

In fuccessive equal parts of time, as 1, 1, 1, 1, &c. the spaces thro' which a body falls are as 1, 3, 5, 7, &c. and the acquired velocities are as 1, 2, 3, 4, &c. continually: so that the velocities M are

are as the times, and the spaces are as the squares of the times in falling.

Thus, in the first second of time (from the inflant of beginning to fall) the body will fall through 16 feet; in the next fecond it will fall through three times 16, or 48 feet, which added to the former 16 makes 64 feet, the whole fpace fallen through in 2 feconds of time: in the third second of time, the body falls 5 times 16, or 80 feet; which, added to the above 64, makes 144 feet, the whole space fallen through in 3 feconds: in the fourth fecond it falls 7 times 16, or 112 feet; which, added to the above 144 feet, makes 256, the whole space fallen through in 4 feconds: and fo on continually, increasing as the odd numbers 1, 3, 5, 7, 9, 11, in 1, 2, 3, 4, 5, 6 feconds of time.

Whatever velocity the body acquires at the end of the first second, it will acquire twice as much at the end of the next, three times as much at the end

end of the third, four times as much at the end of the fourth fecond, and fo on continually.

In the following Table, the numbers under T denote the feconds of time, from 1 to 60, in which the body continues to fall: the numbers under S denote the spaces, in feet, through which the body falls in any fecond from 1 to 60: and the numbers under N denote the whole number of feet the body falls through, at the end of any number of feconds from 1 to 60. Thus, between the end of the 59th and 60th fecond, the body falls 119 times 16 feet; and at the end of the both fecond it has fallen through 57600 feet.

In a quarter of a fecond from the instant of beginning to fall, a body would fall one foot: at the end of half that second it will have fallen 4 feet: at the end of three quarters of that fecond it will have fallen through 9 feet: and at the end of that whole fe-

cond, through 16.

The

The whole spaces fallen through being as the squares of the times in which the body falls, Qu. How many feet would it fall through in an hour?

In 60 feconds the space is 57600 feet, and the square of 60 is 3600. But 57600 multiplied by 3600 is 207360000, the number of feet the body would fall through in an hour, in a free or unrefifting space: and this number being divided by 5280, the number of feet in an English mile, quotes 39272.7 for the number of miles.

TABLE of FALLING BODIES.

T.	S.	N. 1	T.	S.	N. 1	T	S. N.	T.	S.	N.
1	1	Feet 10	16	31	4096		61 15376	46	91	33856
2	3	64	17	33	4624		63 16384	47	93	35344
3	5	144	18	35	5184		55 17424		95	36864
4	17	256	119	37	5776		57 18496		97	38416
15	9	400	20	39	6400	35	69 19600	150	99	40000
6	11	576		41	7056	136	71 20736	51	101	41616
17	13	784	22	43	MILES PROPERTY AND ADDRESS.		73 21904	STATE OF THE PARTY NAMED IN	103	43264
8	15	1024		4	Million Co., Co., Co., Co., Co., Co., Co., Co.,	38	75 23104	53	105	44944
9	17	1296	24	47	9216		77 243 36		107	46656
10	19	1600	25	49	10000	40	79 25600	155	109	48400
11	21	A SHAREST PARTY OF THE PARTY OF			10816		81 26896	156	111	50176
12	123	2304			11664		83 28224		113	51984
13	25						85 29584		115	53824
14	27						87 30976			55696
115	129	3600	130	159	14400	145	89 32400	60	110	57600

A TABLE shewing how much the Mercury would sink in a Barometer at given Heights above the Earth's plane Surface; and consequently, how the Heights of Hills may be found thereby.

				3		11/2	9.50			1000		1			100	
1	At the	MI	erc.	At the	IVI	erc.	Atthe	Me	erc.	At the	M	erc.	At the	M	erc.	ı
	height	fir	ks		fir	ks	height	fin	ks	heigh	fir	iles	height	fin	ks	ı
ı	of		-	neight		-	of		=	of		0	of	-		ı
1	01	ne	100	01	Inches.	100	1 01	Inches	00	0,	Inches.	0	0.	Inches.	00	ı
1	Y2 1	nches.	parts		he	Part	100000	he	parts	-	he	par	10.	he	parts	ı
1	Feet.	· ·	rts	Feet.	. 0	7	Feet.	50	SII	Feet		SI	Feet.	1	rts	ı
ı	100	-	-	-	-	20		-	-	10000	9	.87	1450:	12	-37	ı
1	200	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	.11	3700	3	.83	7300	7	.05	11000	_		14000		-	
ı		0	.22	3800	3	.92	7400	7	.22	11100	-	.01	14700		.50	
ı	300	0	.33	3900	4	.02	750	4	1000000	11200	_		14800		.57	
ı	400	0	-44	4000	4	.12	7500	7	.30	A CONTRACTOR OF THE PARTY OF TH			14900			
ı	500	-	-54	410	-		The second second	1	.38	THE RESERVE OF THE PERSON NAMED IN			15000	-	.70	
1	000	0	.65	4200		.30	7800	1	.46	Management American			15100			
1	700 800	0	.76	4300	Marie Co.	-39	7900	7	.55	11600			15200		.83	
1	900	0	INCOME.	440	4	.49	810	7	.71	Service Property	_		15300		.80	
1	1000	0	-98	4500	_	.58	8200	7	.79	Marie Contraction	_		15400		1000000	
1	1100		.09	4000	4	.77	8300	7	.87	11900	-	THE REAL PROPERTY.	15500		.02	
1	1200	-	.19	4700	4	.86	8400	7	.95				15600		.09	
1	1300	-	.30	4500	4	.95	8500	8	.03	12100		-73	15700	_	.15	
ı	The second second		.40	4900	4	10.	8600	8	.11		_		15800		.21	
1	1400		.50	5000	5	.13	8700	8	.19				15900		.28	
1	1500		.72	5100	2	.22	8800	8	.27	THE RESERVE AND DESCRIPTION OF THE PERSON NAMED IN COLUMN TWO	_		16000		•34	
1	1700		.82	5200	5	.31	8900	8	-35	12500	_		16100		.40	
1	1800		1000000	5300	5	.40	9000	8	43	12600	_				-47	
1	1900	2	.93	5400	2	.49	9100	8	.51	12700	_	.15	16300		-53	
1	2000	2	.14	5500	5	.58	9200	8	.58	12800			16400		.59	
1	2100	2	.24	5700	2	.67	9300	8	.66	12900	_		16500		.65	
ı	2200	2	-34	5800	2	.76	9400	8	.74	13000	_		16600		.71	
4	2300	2	ALCOHOLD !	5900	-	.85	9500	8	.82	13100	_	.43	16700		.78	
1	2400	_	·44 •54	100000000000000000000000000000000000000	2	.94	9600	8	_	13200	_					
1	2500	2	.6;			.02	9700	8		13300						
ı	2 00	2	.75	The second second	1000	.11	9800		.05	THE RESERVE OF THE PERSON NAMED IN	11	.63	17000	13	.96	ı
ı	2700	2	.85	6300		.20		9	.12				17100			
ı	2800	2	.95	6400	6	.25	10000	9	.20	13600			17200			
ı	2900	2	.05	6:00	6	.37	10100	9	.27	13700			17300			
ı	3000	3	.15	6600	6	.45	10200	9	.34	13800			17400			
1	3100	2	.25	6700	6	.54	1 1000 1000	9	.42		_		17500			
1	3200	3	.34	6800	6		10:00	9	.50				17600			
1	3300	3	.44	6,00	6		10500	9	-57				17700			
	3400	100000	.54	7000	6		10600	9	.64				17800			
1	3500	3	.63	7100	6		10700	9	.72	and the same			1790		.51	
1	3600	3	.73	7200	6		10800		.79	NAME OF TAXABLE			18000			
	-					100	-	-				-	N. Sandardon	No.	73	1

By this Table, and a common barometer, the height of any hill may be found, if its height, taken in perpendicular measure, be not much above half a mile.—Thus, if the mercury be 2 inches and 95 hundred parts of an inch lower in the tube at the top of the hill, than what it was obferved to be at the bottom, the perpendicular height of the hill is 2800 feet, which is 160 feet more than half a mile.

But as there are many hills much higher than 2800 feet, and the common barometer-scale is only 3 inches long, let a scale 14 inches long, divided into inches, and hundred parts of an inch by diagonal lines, be applied to the tube, and have a sliding index across it in the common way; and this, I apprehend, will do for the highest mountain on the earth.—For, supposing the quicksilver was observed to be 13 inches and 21 hundred parts of an inch lower in the tube when at the

the top of the hill than it was when at the foot: against 13.21 inches in the Table is 15800 feet for the height of the hill, which wants only 40 feet of being 3 miles high.

To divide the Area of a given Circle into any required Number of equal Parts, by concentric Circles.

In Fig. 4. of Plate IX. let ABDE be a circle, whose area is required to be divided into 5 equal parts by concentric circles, as FGHI.

Divide the semidiameter AC into 5 equal parts, as A 1, 1 2, 2 3, 3 4, 4 5; and on the middle point e as a center, with the radius e A, describe the semicircle A a b c d C. From the points of equal division at 1, 2, 3, and 4, and perpendicular to AC, raise the perpendiculars 1 a, 2 b, 3 c, 4 d, till they meet the semicircle in the points a, b, c, and d: through which points, draw M A

the concentric circles F, G, H, I, and the thing will be done.

Supposing that five blacksmiths should agree to buy a grinding-stone among them, each paying an equal share of the price, and that each man should therefore have the use of the stone, to wear off a fifth part of it, till it came to the last man, who was to wear it out: the first man should wear the stone from E to F, the second from F to G, the third from G to H, the fourth from H to I, and the fifth from I to the center or axle C.

By this eafy method, which I learnt of Mr. Hutton, teacher of the Mathematics at Newcastle, the area of any circle may be divided by concentric circles into any required number of equal parts. For, into whatever number of equal parts the radius AC be divided, the area of the circle will be divided into the like number of parts, all equal among themselves.

To make two equal Circles, whose Areas taken together, shall be equal to the Area of a given Circle: or four equal Crescents, the Sum of whose Areas shall be equal to the Area of a given Square.

In Fig. 5. of Plate IX. let c d k i be the given circle. In this circle defcribe the square e f m l; and, on the middle points of any two of its sides, as at e and f as centers, describe the two circles A a B E A and B b C E B: the areas of these two circles, taken together, shall be equal to the area of the given circle c d k i.

Draw the diagonal A E C, which will divide the fquare into two triangles A B C and A D C, right angled at B and D. Now, as the fides A B and B C of the triangle A B C are equal, and fo are the fides A D and D C of the triangle A D C, and the areas of circles being as the fquares of their diameters,

meters, and the hypothenuse AC being squared is equal to the square of the sides AB and BC, or AD and DC; the larger semicircle AcBdC is equal to the two lesser semicircles AaBdC is equal to the two lesser semicircles AaBdC is equal and BdCfB. Consequently, if you subtract the two common portions AcBdA and BdCfB, the two remaining crescents AaBdA and BbCdB will be equal to the two triangles AEBA and BCEB, which make one half of the square efml: and therefore the sum of the areas of all the four outward crescents is equal to the area of the whole square.

Of Squaring the Circle.

Although there has not yet been any method found for doing this to mathematical exactness, yet, by means of the following numbers, it may be brought so very near the truth, as to be within a grain of fand in a square mile,

mile, supposing 100 grains of sand (placed in a straight line, and touching one another) to be equal to the length of an inch; and consequently 401448960000000 to cover a square mile.

If the diameter of a circle be given, and the length of the fide of a square so nearly equal to the circle as to be true to 14 places of sigures be required; say, As 1 is to the diameter of the given circle, so is 0.88622692545276 to the side of the square required, in such measures as the diameter of the circle was taken.

If the length of the fide of a square be given, and the diameter of a circle equal (as nearly as above-mentioned) to the square be required; say, As 1 is to the fide of the given square, taken in any measure, as feet, inches, &c. so is 1.12837916709551 to the diameter of a circle (taken in the same kind of measures) whose area is equal to the area of the given square.

In practice, it is sufficient to take out the decimal parts to four places of figures; for, even by fo fmall a number, we come so near the truth as to be within a ten thousandth part of the whole area of being perfectly true. And this is nearer than any one can pretend to delineate on paper.

Thus, supposing the diameter of a circle to be 12 inches, and that it is required to find the length of the fide of a square (or to make a square) whose area shall be equal to the area of the circle; fay, As 1 is to 12, fo is .8862 to 10.6344 inches, the length of the fide of the fquare required.

Or, supposing the fide of a square to be 12 inches, and that it is required to find the diameter of a circle whose area shall be equal to the area of a square; say, As 1 is to 12, so is 1.1284 (inflead of 1.128379) to 13.5408 inches the diameter of the circle required.

Hence, as a square vessel, just one foot wide and one foot deep, would hold a cubic foot of water; a cylindrical veffel 13.54 inches wide and one foot deep would hold a cubic foot of water

too; at least so near the truth, that no difference could be perceived.

The diameter of any circle is in proportion to its circumference, as 1 is to 3.1415926535897932384626434; or as 1 is to 3.1416, near enough for practice.

Any circle is equal to a parallelogram, whose length is equal to half the circumference of the circle, and breadth equal to half the diameter. Therefore multiply half the circumference by half the diameter, and the product shall be equal to the area of the circle, in square measure. The square root of this area is the side of a square equal to the circle.

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To shere that an Angle may be continually diminished, and yet never be reduced to nothing: and confequently, that Matter is infinitely divisible.

In Fig. 6. of Plate IX. let AB be a straight line, produced to an infinite length beyond B, and straight throughout. On this line let there be an infinite number of equilateral triangles placed, as Aab, bcd, def, fgh, &c. whose bases Ab, bd, df, fb, &c. touch one another upon the right line AB: and let the fide ab of the first triangle be of any given length, as suppose an inch, and each fide of each triangle be of the fame length with ab.

Then, from the point A draw the straight line Ac to the top of the fecond triangle b c d; and A c shall cut

a b in the middle point at m.

From the point A draw the straight line Ae to the top of the third triangle def; and Ae shall cut ab at n, in two thirds

thirds of its length from a, leaving only one third remaining, from n to b.

From the point A draw the right line Ag to the top of the fourth triangle fg b; and Ag shall cut ab at o, in three fourth parts of its length from a; and consequently leave one fourth of it remaining, from o to b.

Here it is plain that every line drawn from A to the top of the next triangle beyond that to which the last preceding line was drawn, will make a less angle with the line AB than the last preceding line did. But no right line drawn from the point A to the top of any triangle placed upon AB, even at an infinite distance from A, could ever coincide with the line AB, although every fucceeding line will make a less angle with AB than the line last drawn before it did: and therefore the angle at A will be continually diminishing, but can never come to nothing. Confequently, the whole

whole line ab will never be exhausted or quite cut off, by any line drawn from A to the top of any triangle: and therefore, a part of it will still remain between a and b; which proves that matter is infinitely divisible.

A new Experiment in Electricity, shewing the Motions of the Sun, Earth, and Moon; by Edward King, Esq; of Lincoln's-Inn.

The Sun and Earth go round the common center of gravity between them in a folar year, and the Earth and Moon go round the common center of gravity between them in a lunar month.—These motions are represented by an electrical experiment, as follows:

In Fig. 7. of Plate IX. the ball S represents the Sun, E the Earth, and M the Moon, connected by bended wires ac and bd: a is the center of gravity between

between the Sun and Earth, and b is the center of gravity between the Earth and Moon. These three balls, and their connecting wires, are hung and supported on the sharp point of a wire A, which is stuck upright in the prime conductor B of the electrical machine; the Earth and Moon hanging upon the sharp point of the wire cae, in which wire is a pointed short pin, sticking out horizontally at c; and there is just such another pin at d, sticking out in the same manner, in the wire that connects the Earth and Moon.

When the globe C of the electrical machine is turned, the above-mentioned balls and wires are electrified: and the electrical fire, flying off horizontally from the points c and d, cause S and E to move round their common center of gravity a; and E and M to move round their common center of gravity b. And, as E and M are light when compared with S and E, there

is much less friction on the point b than upon the point a; fo that E and M will make many more revolutions about the point b than S and E make about the point a .- I had this experiment from my ingenious friend Mr. King; and have adjusted the weights of the balls fo, that E and M go twelve times round b in the time that S and E go only once round a .- It makes a good amusing experiment in electricity; but is fo far from proving that the motions of the planets in the heavens are owing to a like cause, that it plainly proves they are not. For the real Sun and Planets are not connected by wires or bars of metal; and confequently there can be no fuch metallic points as a and b between them. And without fuch points, the electric fluid would never cause them to move: for, take away these points in the above-mentioned experiment, and the balls will continue at rest, let them be ever so strongly electrified.

TABLES

TABLES

FOR

NEW or FULL MOON, from the Creation of the World to A. D. 7800; near enough the Truth for any common Almanack.

ADVERTISEMENT.

In all the British Lunar Tables bitherto published, the time depending upon the Moon's annual equation is subtracted from the mean time of New and Full Moon when the Sun's anomaly is less than fix signs, and added when greater: in the elliptic equation, the time depending on the Moon's anomaly is added to the mean time of New and Full Moon when her anomaly is less than six signs, and fubtracted therefrom when her anomaly is greater. In the following Tables, I have made these equations always additive, which renders the calculations much easier. For this purpose, I have put down all the radical mean times of New and Full Moon 13 hours 59 minutes sooner than in the former Tables; the greatest annual equation being 4 hours II minutes, and the greatest elliptic equation 9 hours 48 minutes; the sum of both these (to the nearest full minute) is 13 hours 59 minutes. The numbers under A are the degrees of the Sun's mean anomaly, and those under B the degrees of the Moon's-I was led to this, by observing that the late eminent M. CLAIRAUT at Paris has made all the equations additive in his Lunar Tables.

TABLE I. The mean Times of New and Full Moon in January, from A. D. 1700 to A. D. 1800, according to the Old Stile.

New Moon. Full Moon.									-		
	11.57	200	Ne	w M	oon.			No. of Concession,	STATE OF THE PARTY OF	CONTROL NO.	
Y	ears.	D.	h.	m.	A	B	D.	h.	m).	A	В
L.	1700	8	0	43	202	1	22	19	5	217	194
Pile	1701	26	22	16	221	336	12	3	54	206	143
	1702	16	7	5	210	286	1	12	43	195	1000
25	1703	5	15	53	199	236		10	15	214	
L.	1704	23	13	26	218	211	8	19	4	203	
7 12	1705	12	22	15	207	161	27	16	37	222	Section 18
	1706	2	7-	3	196	III	17	1	25	211	-
	1707	21	4	36	215	87	6	10	14	200	
L.	1708	9	13	24	203	36	24	7	46	SC 10 2335	229
131	1709	28	10	57	222	12	15	16	35	BIRTON AND ADDRESS OF THE PARTY	179
7	1710	17	19	46	211	322	3	1	24		129
	1711	7	4	34	200	272	21	22	56	100	105
L.	1712	25	2	7	219	247	10	. 7	45	204	The second second
200	1713	14-	10	56	208	197	29	5	18	223	CONTRACTOR
	1714	3	19	44		147	18	4	6	-	340
-	1715	22	17	17	216	122	7	22	55	2000000	290
L.	1716	II	2	. 5	205	72	25	20	27	-	265
	1717	0	10	54	194	22	15	5	16	_	215
	1718	19	8	27	213	358	4	14	5		165
+	1719	8	17	15	202	283	23 11	20	37	100000000000000000000000000000000000000	140
L.	1720	_	14	48	220	THE REAL PROPERTY.	I			205	1000
200	1721	15	23	37	198	183	20	5 2	47	194	
	1722	5		58	217	158	9	11	36	_	325
T	1723	24	5	47	206	108	27	9	9	No. of Column 2	301
L.	1724	12	14	35	195	58	16	17	57	10000000	251
1	1725	_	23	33	214		6	2	46	100000	201
100	The second second	11000000		56	203	1000		0	18		177
L.	1727	28	5 3	20	222	319		9	7	207	126
Lie	1729	17	12	18	211	269	2	17	56	196	76
450	1730		21		200		21	15	28		
239	1731	25	18			194	_	0	16		
L.	1732		3		208		28	21	49		337
The same of	130	-	1000		N	_		SALES OF	-		

TABLE I. (Mean Times of New and Full Moon in January, Old Stile) continued.

			Ne	w M	ооп.	1	100	Full	Mo	on.	
Ye	ars.	D.	h.	m.	A	5	D.	h.	m	A	В
	1733	3	12	16	197	94	18	6	38	212	
	1734	22	9	49	216	69	7	15	27	201	236
300	1735	11	18	37	205	19	26	12	59	220	
L.	1736	0	3	26	194	329	14	21	48	209	162
	1737	19	0	59	213	305	4	6	37	198	
	1738	8	9	47	202	254	23	4	9	217	
	1739	27	7	20	220	230	12	12	58	205	100-000
L.	1740	15	16	9	209	180	0	21	47	194	Section 19
	1741	5	0	57	198	130	19	19	19	213	
1	1742	23	22	30	217	105	9	4	8	202	HOL-Ob-4
	1743	13	7	18	206	55	28	1	40	221	
L.	1744	1	16	-7	195	5	16	20	29	210	THE REAL PROPERTY.
	1745	20	13	40	214	341	5	19	18	199	77100
	1746	9	22	28	203	291	24	16	50	218	THE OWNER OF THE OWNER,
+	1747	28	20	1	222	266	14	1	39	207	
L.	1748	17	4	50	211	216	2	10	28	196	
	1749	6	13	38	200			8	0	215	MONEOUS P
1	1750	25	II	11	218	141	10	16	49	203	DESCRIPTION OF THE PARTY.
4	1751	14	19	59	207	91	10	1	37	192	
L.		3	4	48	196	41	17	23	10	211	_
	1753	22	2	21	215	16	17	7	59	200	_
	1754		11	9	204	326	26	5	31	219	
	1755	0	19	58		276	15	14	20	208	SHIP CO.
L.	1756	18	17	31	212	252	3	23	9	197	
100	1757	8	2	19		202	22	20	41	216	
	1758	26	23	52	220	III DANIE AND	12	5	30	205	No. of Contrast, Name of Street, or other party of the Contrast, Name of Street, Name of Stree
7	1759	16	8	41	209	127	1	14	19		294
L.	1700		17	29	190	77 52	1,3	11		213	
100	1761		15		The second second			20	40	The state of the s	
1	1762		23	50				18			
IT	1763		6	39				3	I		
L.	1764			12	S SECURIO		1 100-00	11	50	THE REAL PROPERTY.	THE REAL PROPERTY.
1	1765		15	0	6 (2) (2) (A)	237		18	11	60 11/30	
1_	1700	120		33	221	1413	1113	10	11	200	-

TABLE I. (Mean Times of New and Full Moon in January, Old Stile) concluded.

77		3	New	/ Mo	on.			Foll	Mo	on.	
Y	ears.	D.	h.	m.	A	В	D.	h.	m.	A	B
	1767	17	21	22	210	16	3	3	0	195	330
L.	1768	6	6	10	199	113	21	0	32	214	306
	1769	25	3	43	218	88	10	9	21	203	255
	1770	14	12	31	207	38	29	6	53	222	231
	1771	3	21	20	196	348	18	15	42	211	181
L.	1772	21	18	53	215	323	7	-0	31	200	131
	1773	11	3	41	204	273	25	22	3	219	106
	1774	0	12	30	193	223	15	6	52	208	56
	1775	19	10	3	212	198	4	15	41.	197	6
L.	1776	7	18	51	201	148	22	13	13	216	341
	1777	26	16	24	220	_	11	22	2	205	291
	1778	16	1	12	209	74	I	6	50	194.	241
	1779	5	10	1	198	24	20	4	23	213	217
L.			7	34	217	359	8	13	12	202	167
7	1781	12	16	22	206	309	27	10	44	221	142
	1782		1	11	195	259	16	19	33	210	92
	1783		22	44	213	234	6	4	22	-	42
L.			7	32	202		24	1	54	217	17
	1785		5	5	221	160	13	10	43	206	327
88	1786		13	54	210	10000000	2	19	32	195	277
16	1787		22	42	199		21	17	4	1000000	100 HOURS
L.	The same time		20	15	218		10	1	53	203	202
	1789	III DOMESTICAL DESIGNATION OF THE PERSON NAMED IN COLUMN 1	5	3	207		28	23	25		178
100	1790		13	52	196	E Buddingson	18	8	14		128
ш	1791		11	25	215	100000000000000000000000000000000000000	7	17	3	200	1 0
L			20	13	204	A RESPONSE	25	14	35	0.0000000	
				2	193		14	23	24	1	
	1793		5 2	35		145		8		197	
			11				23	5	45		
L	1799	26	8	56	S SUSPENSE		11	14		204	
1							0	23		193	20.00
1	179	15	17	44			119	20	55		H III CONTRACTOR
1	179	5	2	33	216	306			23	201	
T		24	8					5 3	16	220	
L	. 1000	12	0	54	120)	1-30	11 -1	3	1	A. Audich	

TABLE II. The Mean Times of New and Full Moon in January, from A. D. 1752 to A. D. 1800, according to the New Stile.

- 37	And I		Ne	w [V]	1		Ful	I Mc	oon.		
Ye	ears.	D.	h	m.	A	В	D.	h.	m.	A	В
	1753	3	13	37	186	350	18	7	59	200	184
	1754	22	11	9	204	326	7	16	47	189	133
36	1755	11	19	58	193	276	26	14	20	208	109
L.	1756	29	17	31	212	252	14	23	9	197	59
	1757	19	2	19	201	201	4	7.	57	186	9
	1758	8	11	8	190	151	23	5	30	205	344
2	1759	27	8	41	209	127	12	14	19	194	294
L.	1760	15	17	29	198	77	0	23	7	183	244
	1761	5	2	18	187	27	19	20	40	202	219
100	1762	23	23	50	206	2	9	5	28	191	169
	1763	13	8	39	195	312	28	3	1	210	145
L.	1,64	I	17	28	184	262	16	11	50	199	95
333	1765	20	15.	0	203	237	5	20	38	188	
100	1766	9	23	49	202	187	24	18	11	206	20
CO.	1767	28	21	22	210	163	14	3	0	195	330
L.	1768	17	6	10	199	113	2	11	48	184	280
202	1769	6	14	59	188	63	21	9	21	203	255
	1770	25	12	31	207	38	10	18	9	192	205
200	1771	14	21	20	196	348	0	2	58	181	155
L.	1772	3	6	9	185	298	18	0	31	200	131
100	1773	22	3	41	204	273	17	9	19	189	80
	1774	11	12	30	193	223	26	6	52	208	56
	1775	0	21	19	182	173	15	15	41	197	6
L.	1776	18	18	51	201	148	4	0	29	186	316
320	1777	8	3	40	190	198	22	22	2	205	191
23.0	1778	27	1	12	209	74	12	6	50	194	241
-	1779	16	10	1	198	24	I	15	39	183	191
L.	1780		18	50	187	334	19	13	Part of	202	167
1000	1781		16	22	200	309		22	100	The second second second	117
10	1782		1	11	195	259		19		210	
4	1783		10	0		209	_	4		198	
L.	1784	20	7	32	203	184	5	13	10	187	352
1	1785	9	16	21	192	134	124	10	43	206	327

TABLE II. concluded. New Stile.

-		75	Ne	v M	oon.		Full Moon.					
Y	ears.	D.	h.	m.	A	В	D.	h.	m.	A	В	
	1786	28	13	54	210	110	13	19	32	195	277	
	1787	17	22	42	199	59	3	4	20	184	227	
L.	1788	6	7	31	188	9	21	1	53	203	202	
	1789	25	5	3	207	345	10	10	41	192	152	
100	1790	14	13	52	196	295	29	8	14	211	128	
	1791	3	22	41	185	245	18	17	3	200	78	
L.	1792	21	20	13	204	220	7	1	51	189	28	
	1793	11	5	2	193	170	25	23	24	208	3	
	1794	0	13	51	182	120	15	8	13	197	313	
2	1795	19	11	23	201	95	4	17	1	186	263	
L.	1796	7	20	12	190	45	22	14	34	204	238	
-	1797	26	17	44	208	21	11	23	22	193	188	
-	1798	16	2	33	197	331	1	8	11	182	138	
2	1799	5	11	22	186	281	20	5	44	201	114	
C.	1800		8	54	205	256	19	14	32	190	63	

TABLE III. Mean Lunations.

Lun.	D.	h.	m.	A	B	Months. Days.
1	29	12	44	29	26	For Subt.
2	59	1	28	58	52	January o
3	88	14	12	87	77	February 31 0
4	118	2	56	116	103	March 31 Days
	147	15	40	146	129	April 90 8
5.	177	4	24	175	155	Mar
7	206	17	8	204	181	June 151
8	236	5	52	233	207	July 181 5
9	265	18	36	262	232	August 212 3
10	295	7	20	291	258	June 151 July 181 August 212 September - 243 October 273
11	324	20	5	320	284	October 273 2
12	354	8	49	349	310	November - 304
13	383	21	33	18	336	December - 334

In Leap years, in January and February, add a day to the time found by these Tables.

No.	TABLE IV. The first Equation. (A)														
A	h.	m.	A	h.	m.	A	h.	m.	A	b.	m.	A	h.	m.	
	4	7	37	1	43	73	0	13	100	0	12	145	I	45	
2	4	2	38	1	39	74	0	12	110	0	14	146	1	48	
3	3	58	39	1	36	75	0	11	111	0	15	147	I	52	
4	3	54	40	1	32	76	0	10	112	0	17	148	1	56	
56	3	50	41	1	29	77	0	9	113	0	18	149	1	59	
THE OWNER OF THE OWNER OWNER OF THE OWNER OWN	3	46	42	I	26	78	0	8	114	0	20	150	2	3	
7 8	3	42	43	1	23	79	0	7	115	0	22	151	2	7	
10000	3	37	44	1	19	80	0	6	116	0	23	152	2	11	
9	3	33	45	I	16	81	0	5	117	0	25	153	2	15	
IC	3	29	46	1	13	82	0	4	118	0	27	154	2	19	
11	3	24	47	1	10	83	0	3	119	0	29	155	2	23	
12	3	20	48		7	84	0	2	120	0	31	156	2	27	
13	3	16	149		4	85	0	2	121	0	34	157	2	31	
14	3	12	50	I	1	86	0	1	122	0	36	158	2	35	
15	3	7	SI	0	58	87	0	1	123	0	38	159	2	39	
16	3	3	52	0	56	88	0	I	124	0	40	100	2	43	
7	2	59	53	0	53	89	0	0	125	0	43	161	2	48	
18	2	55	54	0	51	90	0	0	124	0	45	162	2	52	
19	2	51	55	0	48	91	0	0	127	0	48	163	2	56	
20	2	47	56	0	45	92	0	0	128	0	51	164	3	0	
21	2	43	57	0	43	93	0	0	129	0	53	165	3	5	
22	2	39	58	0	40	94	0	0	130	0	55	166	3	9	
33	2	35	59	0	38	95	0	1	131	0	59	167	3	13	
24	2	31	60	0	36	56	0	1	32	I	2	168	3	18	
25	2	27	61	0	34	97	0	1	133	1	5	169	3	22	
26	2	23	62	0	32	98	0	2	134	I	8	170	200000	27	
27	2	19		0	30	THE RESERVE OF THE PERSON NAMED IN	0	2	135	1	11	171	3	31	
28	2	15	64	0	28	100	100	3	136	1	14	172	3	35	
29	2	12	65	0	26	IOI	0	4	137	1	17	173	3	40	
30	2	8		0	24	102	0	5	138	I	20	174	3	44	
31	2	4	67	0	22	103	0	Name and Address of the Owner, where	139	I	24	175	3	49	
32	2	0		0	20	104	_	7 8	140	I	27	176		53	
33	1	57	69	0	19	105	0	_	141	1	30	177	3	58	
34	1	54	70	0	17	_	0	9	142	1	34	178	4	2	
35	1	50	71	0	15		0	10	143	1	37	179	4	7	
36	I	46	72	0	14	108	0	11	144		411	1180	4	11	

TABLE IV. (Equation A) concluded.

A h. m. A h. m.
182 4 20 218 6 48 254 8 13 290 8 5 326 6 20 183 4 24 219 6 52 255 8 14 291 8 3 327 6 20 184 4 29 220 6 55 256 8 15 292 8 2 328 6 2
182 4 20 218 6 48 254 8 13 290 8 5 326 6 20 183 4 24 219 6 52 255 8 14 291 8 3 327 6 20 184 4 29 220 6 55 256 8 15 292 8 2 328 6 2
183 4 24 219 6 52 255 8 14 291 8 3 327 6 2 184 4 29 220 6 55 256 8 15 292 8 2 328 6 2
1184 4 29 220 0 55 250 8 15 292 8 2 320 0 2
1.0-1: 0-1 2016 -0 2018 0 2016 1
185 4 33 221 6 58 257 8 16 293 8 0 329 6 1
186 4 28 222 7 2 25 8 17 294 7 58 330 0 1
187 4 42 223 7 5 259 8 18 295 7 56 331 6 1
1188 4 47 1 224 7 8 1 200 8 19 1290 7 54 1332 0
180 4 51 225 7 11 261 8 20 297 7 52 333 6
100 4 55 226 7 14 262 8 20 298 7 50 334 5 5
1915 0 227 7 17 263 8 21 299 7 48 335 5 5
192 5 4 228 7 20 264 8 21 300 7 49 330 5 5
193 5 9 229 7 23 265 8 21 301 7 44 337 5 4
194 5 13 230 7 26 26 8 22 302 7 41 338 5 4
195 5 17 231 7 29 267 8 22 303 7 39 339 5 3
196 5 22 232 7 31 268 8 22 304 7 37 340 5 3
197 5 20 233 7 34 209 8 22 305 7 34 34 5 3
198 5 30 234 7 37 276 8 22 306 7 31 342 5 2
199 5 34 235 7 39 27 6 22 307 7 29 343 5 2
200 5 39 236 7 41 272 8 21 308 7 26 344 5 1
201 5 43 237 7 44 273 8 21 309 7 23 345 5 1
202 5 47 238 7 46 274 8 20 310 7 21 346 5 1
203 5 51 239 7 48 275 8 20 311 7 18 347 5
204 5 55 240 7 50 270 8 19 312 7 15 348 5
205 5 59 241 7 53 277 8 19 313 7 12 349 4 5
206 6 3 242 7 55 278 8 18 314 7 9 350 4 5
207 6 7 243 7 57 279 8 17 315 7 6 351 4
208 6 11 244 7 59 280 8 16 316 7 3 352 4
209 6 15 245 8 C 281 8 15 317 7 0 353 4 4 210 6 19 246 8 2 282 8 14 318 6 56 354 4
210 6 19 246 8 2 282 8 14 318 6 56 354 4 211 6 23 247 8 4 283 8 13 319 6 53 355 4
210 6 19 246 8 2 282 8 14 318 6 56 354 4 211 6 23 247 8 4 283 8 13 319 6 53 355 4 212 6 26 248 8 6 284 8 12 320 6 50 356 4
211 6 23 247 8 4 283 8 13 319 6 53 355 4 212 6 26 248 8 6 284 8 12 320 6 50 356 4 213 6 30 249 8 7 285 8 11 321 6 46 357 4 214 6 34 250 8 9 286 8 10 322 6 43 358 4 215 6 37 251 8 10 287 8 9 323 6 39 359 4
213 6 30 249 8 7 285 8 11 321 6 46 357 4
214 6 34 250 8 9 286 8 10 322 6 43 358 4
210 6
212 6 26 248 8 6 284 8 12 320 6 50 356 4 213 6 30 249 8 7 285 8 11 321 6 46 357 4 214 6 34 250 8 9 286 8 10 322 6 43 358 4 215 6 37 251 8 10 287 8 9 323 6 39 359 4 216 6 41 252 8 11 288 8 8 324 6 36 360 4

TABLE	V.	The second	Equation.	(B)
				11 36

B	h. m.	B	h. m.	11 B	jh. m.	B	h. m.	B	h. n	n.
1	9 59	137	16 2	11 73	19 21	100	18 51	145	15	4
2	10 10	138	16 11	1 74	19 23	110	18 47	146	14 5	-
1 3	10 21	139	16 19	1 75	19 25	111	18 43	147		8
4	10 32	40	16 27	75	19 27	112	18 38	148		9
5	10 43	41	16 35	77	19 29	113	18 34	149	14 3	8000
II III COSTI	10 54	42	16 43	78	19 30	114	18 29	150	14 2	3
7 8	11 5	43	16 50	79	19 32	115	18 24	151	14 1	4
8	11 16	44	16 58	80	19 33	116	18 19	152	14	5
19	11 27	45	17 5	81	19.34	117	18 14	153	13 5	7
10	11 38	46	17 12	82	19 35	118	18 8	154	13 4	8
11	11 49	47	17 19	83	19 35	119	18 3	155	13 3	9
112	11 59	48	17 26	84	19 36	120	17 57	156	13 3	1
13	12 10	149	17 33	85	19 36	121	17 51	157	13 2	2
14	12 20	50	17 39	86	19 36	122	17 45	158	13 1	3
15	12 31	51	17 46	87	19 36	123	17 40	159		4
16	12 42	52	17 52	88	19 36	124	BOOK AND DESCRIPTION OF THE PERSON NAMED IN COLUMN 1	160	12 5	
17	12 52	53	17 58	89	19 35	125	17 28	161	12 4	
18	13 2	54	18 4	90	19 35	126	17 22	162	12, 3	м.
119	13 13	155	18 9	91	19 34	127	17 15	163	12 2	
20	13 23	56	18 15	92	19 33	128	17 9	164	12 I	8
21	13 33	57	18 20	93	19 32	129	17 2	165	12	9
22	13 43	58	18 25	94	19 31	130	16 56	166	400	0
23	13 53	59	18 30	95	19 30	131	16 49	167	11 5	
24	14 3	60	18 35	95	19 28	132	16 42	168	LI 4	
25	14 13	61	18 40	97	19 26	133	16 35	159	11 3	
26	14 23	62	18 44	98	19 24	134	16 28	170	11 2	
27	14 32	63	18 48	99	19 22	135	16 21	171	11 1.	4
28	14 42	64	18 52	100	19 20	136	16 14	172		4
29	14 52	65	18 56	101	19 18	137	16 6	173	10 5	_
30	15 1	66	19 0	102	THE PERSON NAMED IN COLUMN 1	138		174		
31	15 10	67	19 4	103	THE RESERVE OF THE PERSON NAMED IN	139	15,51	175	10 30	
32	15 19	68	19 7	104	19 9	140	15 44	176	10 20	
33	15 28	69	19 10	105	19 6	141	15 36	177	10 1	
34	15 37	70	19 12	106	19 2	142	15 28	178	10	7
35	15 45	7-1	19 16	107	18 59	143	15 20	179	9 5	
36	15 5411	721	19 19	108	18 55	144	15 12	180	9 4	8

T	A	R	T.	F	V	(Faunt	ion B'	concluded.
1	77	n	-	-	200.00	(midness)	1412 20	, communicus

		63	Section	44	1000	6 3		11/4	1 1000	100	1000	1	10.74	
В	Б.	m.	B	h.	m.	B	h.	m.	B	b.	m.	B	h.	m.
181	9	38	217	4	16	253	0	38	289	0	20	325	3	51
182	9	29	218	4	8	254	0	35	290	0	23	326	3	59
183	9	19	219	4	0	255	0	31	291	0	26	327	4	8
184	9	10	220	3	52	256	0	27	292	0	29	328	4	17
185	9	0	221	3	45	257	0	24	293	0	32	329	4	26
186	8	51	222	3	37	258	0	21	294	0	36]	330	4	35
187	8	41	223	3	30	259	0	19	295	0	40	331	4	44
188	8	32	224	3	22	200	0	16	296	0	44	332	4	54
189	8	22	225	3	15	261	0	14	297	0	48	333	5	2
190	8	13	226	3	8	262	0	12	298	0	52	334	5	13
191	8	4	227	3	I	263	0	10	299	0	56	335	5	2.3
192	7	55	228	2	54	264	0	8	300	1	1	336	5	33
193	7	45	229	2	47	265	0	6	301	I	6	337	5	43
194	7	36	230	2	40	266	0	=5	302	I	11	338	5	53
195	7	27	231	2	34	267	0	4	303	1	16	339	6	3
196	7	18	232	2	27	268		3	1304	I	22	340	6	13
197	7	8	233	2	21	269	0	2	305	I	27	341	6	23
198	6	59	234	2	14	270	0	1	1306	1	32	342	6	34
199	6	50	235	2	8	271	0	1	307	I	38	343	6	44
200	6	41	236	2	2	272	0	Ball	308	1	44	344	6	54
201	6	32	237	I	56	273	0	0	309	I	50	345	7	5
202	6	23	238	I	51	274	0	0	310	I	57	346	7	16
203	6	14	239	I	45	275	0	0	311	2	. 3	347	7	26
30000 Pag	.5	5	240	I	39	276	0	- 1	312	2	10	348	7	37
205	5	57	241	I	33	277	0	1	313	2	17	349	7	48
206	5	48	242	1	28	278	0	1 2	314	2	24	350	7	58
207	5	39	243	I	22	279	0	3	315	2	31	351	8	2
208	5	31	244	I	17	281	0	14	316	2	38	352	1775	20
209		22	245		U100533	282	10000	12/12/	317	1000	46	353	8	31
210	1000	13	246		7 2		153	7	318		53	354	8	42
211	5	5	247	I	58	283	0.0	11	319		-1	355	8	53
	4	157	248	00		285	0	_	320		9	356	9	4
213	_	49	249	100	53			13	321		17	357	9	15
214	_	40	250	0 0	46	287		14	a common comm	_	25	358	19	26
219		32	251	0	42	288		17	323	3	34	359	9	37
2410	1+	1	1.2.		140	100	17	1/1	344	. 3	42	1300	19	48

TABLE VI. Supplemental to TABLE I. for finding the mean Time of New or Full Moon in January for 6000 Years before or after any given Year in the 18th Century, according to the Julian or Old Stile.

1	10-16-	4084	March.	57/15	9-11		000000000000000000000000000000000000000		11159	13	2.00	Why he was
1	Years.	D.	b.	m.	A	B	Years.	D.	h.	m	A	R
1	100	4	8	11	3	255	3100	16	10	41	347	253
1	200	8	16	22	7	151	3200	20	18	52	351	148
1	300	13	0	33	10	46	3300	25	3	3	354	44
1	400	17	8	43	13	301	3400	29	11	14	357	299
1	500	21	16	54	17	197	3500	4	6	40	332	169
1	600	26	1	5	20	92	3600	8	14	51	335	64
1	700	0	20	32	354	322	3700	12	23	2	338	319
1	800	5	4	43	358	217	3800	17	7	13	342	215
1	900	9	12	54	1	112	3900	21	15	24	345	110
1	1000	13	21	16	4	8	4000	25	23	35	349	6
1	1100	18	5		8	263	4100	0	19	1	323	235
1	1200	22	13	26	11	159	4200	15	3	12	326	130
1	1300	26	21	37	14	54	4300	9	II	23	329	26
I	1400	1	17	4	349	284	4400	13	19	34	333	281
1	1500	6	I	15	352	179	4500	18	3 -	45	336	177
1	1600	10	9	26	355	74	4600	22	II	56	340	72
1	1700	14	17	37	359	330	4700	26	20	7	343	327
1	1800	19	1	48	2	225	4800	1	15	33	317	197
1	1900	23	9	58	5	120	4900	5	23	44	321	92
1	2000	27	18	9	9	16	5000	10	7	55	324	348
1	2100	2	13	36	343	245	5100	14	16	6	327	243
1	2200	6	21	47	346	141	5200	19	- 0	17	331	138
1	2300	11	5	58	350	36	5300	23	8	28	334	34
1	2400	15	14	9	353	291	5400	27	16	39	337	289
1	2500	19	22	20	356	187	5500	2	12	5	312	159
1	2600	24	6	31	0	82	5600	6	20	16	315	54
1	2700	28	14	41	3	337	5700	11	4	27	318	309
1	2800	3	10	8	337	207	5800	15	12	38	322	205
1	2900	7	18	19	341	102	5900	19	20	49	325	100
1	3000	12	2	30	344	358	6000	24	5	0	328	355
-		-			-	-	-		_		-	-

To calculate the true Time of New or Full Moon.

For any proposed year, within the limits of Table II. for Old Stile, or Table II. for New Stile, write out the mean time of New or Full Moon in January, with the numbers or arguments under A and B. With these arguments find the equations in Tab. IV. and V. which being added to the mean time of New or Full Moon in January, will give the true time thereof in that month.

For the time of New or Full Moon in any month after January, add as many lunations from Table III. to the mean time in January, as the given month is after January, and also the numbers A and B for these lunations, to the numbers A and B belonging to the mean time in January. Then, with the respective sums of these numbers, if under 360, find the corresponding

fponding equations in Tab. IV. and V. which added to the mean time will give the true time of the required New or Full Moon, in days, hours, and minutes, from the beginning of January. When either of the fums A or B exceeds 360, fubtract 360 from it; and with the remainder enter the corresponding Table, and take out the equation.

Then, from the number of days made by the lunations added to the New or Full Moon day in January, fubtract the number of days against the given month in Table III. and the remainder will be the day of the required New or Full Moon in that month. If this number of days be equal to the number you fubtract them from, the required New or Full Moon falls not in the given month, but on the last day of the month preceding it: and, when that is the cafe, you must add a lunation to it from Table III. with the equations A and B for

B for that lunation; and then you will have the true time of New or Full Moon in the given month.

If the number of the given month after January be equal to or exceed the number of days accounted from the beginning of January on which the New or Full Moon therein falls, you must take out one lunation more from Table III. than what answers to the number of the given month after January; otherwise you would have the New or Full Moon not in the month you want, but in the month next before it. And this will always be the case in some month or other of the year wherein the New or Full Moon in January falls before the 11th day thereof.

In leap years, in the months of January and February, the Tables give the New or Full Moon a day sooner than it really falls: and therefore, in these years and months, a day must be added to the time found by these Tables. They always begin the day

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150 SELECT EXERCISES.

at noon, and reckon the hours onward from that time to the noon of the following day.

EXAMPLE L. For the true Time of New Moon in June A. D. 1772, New Stile.

	D.	h.	m.	A	B
To New Moon in Jan. 1772, TAB. II	. 3	6	9	185	298
Add 6 lunations from TAB. III	177	4	24	175	155
The fums are	180	10	33	360	453
First equation (A) for 360, TAB. IV.		4		_	360
Second equation (B) for 93, TAB. V.	1	19	32		93
The whole makes	181	10	16	16.	
TABLE III. against June, subtract	151				
Remains the true time, viz. June	30	10	16	1	13/4

So the true time of the required New Moon is the 30th of June, at 16 minutes past X in the evening.

Example II. For the true Time of Full Moon in June A. D. 1772, New Stile.

				A	
To Full Moon in Jan. 1-72, TAB. II.	18	0	31	200	131
Add 5 lunations from TAB. III	147	15	40	146	129
The fums are	165	15	11	346	260
First equation (A) for 346, TAB. IV.		5	10	-	
Second equation (8) for 260, TAB. V.		0	16	1992	
The whole makes	165	21	37	100	
TABLE III. against June, sobtract	151			Sec.	
Remains the true time, viz. June	14	21	37	120	

Namely, the 15th of June, at 37 minutes past IX in the morning.

To calculate the true Time of New or Full Moon in any given Year and Month after the 18th century, which begins with A. D. 1700, and ends with A. D. 1800.

Here we must go by the Old Stile, and then reduce the time to the New, by the Table farther on, shewing the number of days whereby the stiles do differ .- In Tab. I. find a year in the 18th century of the fame number with that in the century proposed: then from that year, in the 18th century, write out the mean time of New or Full Moon in January, with the numbers A and B belonging thereto. This done, find a year in Table VI. which, when added to the faid year in the 18th century, shall make up the number of the given year. Take out the time and numbers A and B for that year in Table VI. and add them to those in January in Table I. and the fums shall be the mean time of 0 2

of New or Full Moon in January for the given year, and the arguments for finding the equations in that month. Then, for any other month in the given year, work as already taught.

When the fum of days for January exceeds 31 (as in the following example) fubtract a lunation (Tab. III.) from the time, and also the numbers A and B for that lunation from the former numbers, and set down the remainders for the mean time in January, and equation-arguments for that month. If either of the numbers A or B to be subtracted be greater than the number you would subtract from, add 360 to the lesser number, and then make the subtraction.

EXAMPLE III. For the true Time of New Moon in May A. D. 1909, Old Stile.

To A. D. 1709 add 200, and the fum will be 1909.

W-244-2419 Carlot 20-23-23-23-23-23-23-23-23-23-23-23-23-23-	D.	h.	m. 1	A	В
To New Moon in Jan. 1709, TAB I.	28	10	57	222	12
Add, for 200 years, from TAB. VI	8	16	36	17	151
The forms are	37	3	19	229	163
Subtract I lunation, TAB. III				29	
Rem. mean New Moon in Jan. 1909	7	14	35	200	137
Add 4 lunations from TAB. III.	118			116	
The fums are	125	17	31	316	240
First equation (A) for 316, TAB. IV.	110	7	3		2001
Second equation (B) for 240, TAB. V.		1	34	1761	
The whole makes	120	2	13	Part of	
TABLE III. against May, subtract	120		13.8	200	
Remains the true time, viz. May	0	2	13	130	
THE RESERVE OF THE PARTY OF THE			11. 3		

So the true time of the required New Moon is the 6th of May, at 13 minutes past II in the afternoon.

There was no difference between the Old Stile and the New in the year of Christ 200.—In any century after that year, to find the difference between the Old and New Stile, divide the number of the given century by 4, and (without regarding the re-O3 mainder

154 SELECT EXERCISES.

mainder when there is any) add 3 to the quotient; then fubtract the fum from the number of the century, and the remainder shall be the number of days which must be added to the Old Stile time, to reduce it to the New. Thus, in the year 1909, the difference will be found to be 12 days: and therefore, in the preceding example, the day of New Moon in May will be the 18th, according to the New Stile. -At the end of these precepts and examples, I shall subjoin a Table of these differences, which I have copied from a certain Author, who has copied much more from my book of Astronomy into one of his, without doing the common justice of acknowledging, in these cases, from whom he copied.

THE COURSE VIOLET AND VIOLETTE SERVICE

To calculate the true Time of New or Full Moon in any given Year and Month betrueen the Christian era and the 18th Century, Old Stile.

Find a year in the 18th century of the fame number with that in the century proposed, and take out the mean time of New or Full Moon in January, from Table I. for the faid year in the 18th century, with its numbers A and B. Then, from Table VI. take out the time and numbers A and B for as many years as, when fubtracted from the above-mentioned year in the 18th century, shall leave the given year remaining. Subtract the times and numbers taken from Table IV. from those taken from Table I. and set down the remainders for the mean time of New or Full Moon in January in the given year, and the arguments A and B for finding the equations in January: and then, for any other month in that year, work as above taught.

When

156 SELECT EXERCISES.

When subtraction of days cannot be made (as in the following example) add a lunation, and its numbers A and B, from Table III. to the first time and numbers taken out: then subtract, and set down the remainders for the mean time of New Moon in January, and the arguments for finding the equations belonging to it.

EXAMPLE IV. For the true Time of Full Moon in April, Old Stile, in the Year of Christ 796.

From A. D. 1796 fubtract 1000, and 796 will remain.

			D.	h.	m.	A	B	
To Full Moon in	Jan. A. D.	1796	·II	14	34	204	238	
Add I lunation fr	om Table	III.	29	12	44	29	26	
The fums are		-	41	3	18	233	264	
From which fubt. TABLE VI.	for 1000 j	years, }	13	21	5	4	8	
Rem. for Full Mo	on, Jan. A.	D. 796	27	6	13	229	256	
Add 3 lunations,	for April, T	AB. III.	88	14	12	87	77	
The fums are	· with the same		115	20	25	310	333	
First equation (A)			1.12	7	3	100		
Second equation (B) for 333,	TAB. V.	13	1 5	2			
The whole makes		101-	116	8	30			
TABLE III. for A	pril, subtrac	2 -	90		3			
Remains the true t	ime, viz.	April	26	8	301		12	
		The same of the same of			20-70 00			

So that, in April A. D. 796, the true time of Full Moon was the 28th day, at 30 min. past VIII in the evening.

To calculate the true Time of New or Full Moon in any given Year and Month before the Christian era, according to the Old Stile.

Find a year in the 18th century, which being added to the given number of years before Christ diminished by one, shall make any number of compleat centuries.

Find this number of centuries in Table VI. and fubtract the time and numbers A and B belonging to it from those in the year of the 18th century; and the remainder will be the mean time of New or Full Moon for January in the given year, and the numbers A and B belonging thereto. Then, for any other month in that year, work as above.

When

When the number of days taken from Tab. VI. exceeds the number taken from Tab. I. add a lunation. And when subtraction cannot be made in the numbers A or B (as is the case in the 3d and 4th lines (A) in the following example) add 360 to the lesser number, and then make subtraction.

EXAMPLE V. For the true Time of New Moon in May, Old Stile, the Year before Christ 585.

The years 584 added to 1716, make 2300, or 23 centuries.

D. h. m.	A	B
To New Moon in Jan. 1716, TAB. J. 11 2 5	205	72
Add I lunation from TABLE III 29 12 44	29	26
The fums ar: 40 14 49	234	98
Subtract from Tab. VI. for 2300 years 11 5 58	350	36
New Moon in Jan. bef. Christ 585 29 8 51	244	62
Add 4 lunations, for April, TAB. III. 118 2 56	116	103
The fums are, for April 147 11 47	300	105
First equation (A) for 360, TAB. IV. 4 11		All .
Second equation (B) for 105, TAB. V. 12 9		
The whole makes 148 4 7	TOTAL	
TABLE III. for May, subtract - 120	1000	
Remains the true time, viz. May 28 4 7	1	

So that the true time was the 28th of May, at 7 minutes past IV in the after-

afternoon.—At that time, a total eclipse of the Sun put an end to the long war between the Medes and Lydians, by frightening both the armies with a sudden darkness, which overspread the field of battle, just as they were ready to begin the decisive engagement.

Some chronologists believe, that the world was created at the time of the autumnal equinox, in October, the year 4007 before the year of Christ's birth, and that the Moon was full upon the third day of the creation week, which must have been Wednesday.—But, by a calculation from these Tables, I find that the said Full Moon was on Tuesday, the 23d of October, at 45 minutes past VI in the morning; and Dr. Halley's Tables make it but one minute sooner. In that year, the autumnal equinox was on Wednesday, October the 24.

These Tables are adapted to the meridian of London; but they will answer

answer for any other, by adding 4 minutes to the time found by them for every degree eastward from the meridian of London, or subtracting 4 minutes for every degree westward. They are as near the truth as can be, by having only two equations; and I have never found them to differ half an hour from Meyer's, which have thirteen.

And thus, by a very short and easy method, the time of any New or Full Moon, within the limits of 6000 years either before or after the Christian æra, may be found, sufficiently near the truth for any common purpose.—I have tried various methods for making such tables as should render the calculations of New and Full Moons from them still shorter, but have hitherto found it impossible, unless I should have contented myself with such as would sometimes vary a whole hour from the truth.

A TABLE shewing the Number of Days between the Old and New Stile in different Periods of Time.

Years beforeChaid. New Stile. Daye foreChrift. Doff. In ter Chrift. Doff. New Stile. Years after Chrift. Doff. New Stile. Years after Chrift. Doff. New Stile. Ter Chrift. Doff. New Stile. Heart Chrift. Doff. Heart Chrift. New Stile. Heart Chrift. Doff. <	1					7 23 3	10
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The days in the columns marked — are to be subtrasted from the Old Stile time to reduce it to the New. All the years in the columns marked + are to be added to the Old Stile, in order to reduce it to the New. All the years in this Table are Leap years in the Old Stile, but only those which are marked L are Leap years in the New. The backward or forward, it varies 3 days in every 400 years.

The Weight of Gold compared with the Weights of other Materials, of equal Bulk with the Gold.

An hundred pound weight of pure fine Gold is equal in bulk to

Pound weight.

90.3 of Guinea Gold.

69.1 of Quickfilver.

58.1 of Lead.

56.5 of pure Silver.

54.1 of coinage Silver.

49.4 of Bilmuth.

45.8 of Copper.

44.1 of hammered Brass.

40.3 of cast Brafs.

40.2 of forged Iron.

39.8 of Spring Steel.

37.2 of Block Tin.

35.7 of Silver Ore.

30.5 of Gold Litharge.

25.5 of Lapis Calaminaris.

24.2 of Loadstone.

21.3 of Copper Ore.

20.8 of Sapphires.

17.9 of Diamonds.

15.2 of Cornelian Stone.

16.0 of Crystal Glass.

15.5 of Lapis Lazuli.

15.0 of Plate Glais.

14.5 of red Coral.

13.8 of Iceland Cryffal,

13.8 of white Marble.

13.4 of Rock Crystal.

13.1 of homogeneal Pyrites.

11.9 of Sulphur.

9.5 of black Lead.

5.4 of Frankincenfe.

5.1 of common Water.

5.0 of Camphire.

4.7 of Proof Spirits.

4.4 of pure Spirits.

3.9 of Oil of Turpentine.

3.7 of Æther.

1.2 of Cork.

An hundred pound weight of coinage Gold is equal in

Pound weight.

110.8 of pure fine Gold.

76.6 of Quickfilver.

64.4 of Lead.

62.6 of pure Silver.

59.4 of c inage Silver.

54.7 of Bismuth.

50.8 of Copper.

48-3 of hammered Brass.

44.6 of call Brafs.

44.5 of forged Iron.

44.0 of Spring Steel. 41.2 of Block Tin.

39.5 of Silver Ore.

33.8 of Gold Litharge.

28.2 of Lapis Calaminaris.

26.8 of Loadstone.

23.0 of Copper Ore.

22,5 of Sapphires. 19.9 of Diamonds.

18.4 of Cornelian Stone.

17.7 of Crystal Glass.

17.2 of Lapis Lazuli.

16.6 of Plate Glafs.

16.1 of red Coral.

15.3 of Iceland Cryffal.

15.3 of white Marble.

15.0 of Rock Crystal.

14.6 of homogeneal Pyrites.

13.2 of Sulphur.

10.5 of black Lead.

6.0 of Frankincente.

5.6 of common Water.

5.5 of Camphire.

5.2 of Proof Spirits.

4.9 of pure Spirits.

4.3 of Oil of Turpentine.

4.1 of Æther.

1.3 of Cork.

		2017				11		1			_	-		
į	0	2000						mber						
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1	5000	1395	II	2	0	18	25	0	8	12	0	8	17	14
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н	1765,	1422	II	2	0	18	30	0	8	0	0	7	8	0
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1	200	1549	•	0	_	0	72	0.000	3	6	16	0	13	_
1	22	1551	3	0	9	0	72	0	_			-		16
1	130 E	1553	* 1	1	0	19	00	0	4	0	0	3	13	16
1	ia.	1,00	11	2	0	18	50	0	4	0	0	3	14	0
1	11	15835	1	1 100			7-	100	456		319	1 30	1	
1	53	16017	1	-	1	1 11 11		3378	10			1738		-
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1	J.	1627		100		133	-	10 10	100			2.30		
1	B	16611	11	2	0	18	52	0	3	17	IO	3	11	15
-	d a	1671		10	10	. 19			3	1	-	3		-
1	TABLE Shewing from King William	1685	1.50	1	1	4-1		Lig-	-		1	-		
1	5.	1720		1	1231	-	1	-						-
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1	the state of the s	-	_	-				_	-	
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1	Dates	7	Value	of		Oun	ce of		he	THE PARTY NAMED IN
1	of the		he fa		Money	the	then	2000		****
1	feveral	_	o Sh		at each	Stan			nce.	Kings and
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1	Indent-		r pre		to that	HEROTO DESCRIPTION	tof		ver	Periods.
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400	ures.		Mone	1.	prefent		THE REAL PROPERTY.	Per	od.	
1	REFERENCE	900		100	Money.		fent			THE PERSON NO
1 1	1000000		-		Transfer at	Mo	ney.	-		
1	A. D.	1.	5.	d.		fh.	d.	fh.	d.	-
1	1066	2	18	15	2.9062	5	2	-	113	Will. Cong.
		1000	2	0	3.1000		2.3			Will. Rufus.
1	1087	3		100000		5			20	Edward I.
	1300	3.	1	23	3.0614		2	1		
1000	1347	2	15	13	2.7557	5	2	2	0-8	Edward III.
110	1354)			-	799	200			10	
2000	1395 }	2	9	73	2.4802	5	2	2	3	Richard II.
	1402	10		1 7	2 610		No.	1	1	Henry IV.
12			.0			1		-	105	
at le	1412	I	18	9	1.9375	5	2	2		Hann VI
17	1422	2	1	4	2.0666	5	2	2	4.00	Henry VI.
concluded.	1422	1	13	03	1.6531	5	2	3	4 1/2	
1 93	1426]	4	1		2.0666	-	2	2	81	SINT RELEASE
1 13	14465	2	1	4	2.0000	5	-	-	2	Edward IV.
田	1461)			BE AN						CONTRACT TO
200000000	1464	100		1						1.23
L		1	-	- 3	. 6	1	-	-	, 3	CONTRACTOR
Semantin Service	1482 >	1	13	04	1.6531	5	2	3	42	21 177
100	1483					900	A 16			Edward V.
1000000	1494									Henry VII.
A		I	17	0	1.5500	1 -	2	3	74	100000000000000000000000000000000000000
10000	1505		**	-	2200	5		3	1000	Henry VIII.
H	1509 }	I	7	65	1.3776	1 5	2	4	05	rienty ville
1	15325		1	10000	Daniel Andrew	13		T	100	
1 00	1543	1	3	31	1.1635	4	77	4 8	95	STATE OF THE STATE
12	THE RESERVE TO SHARE THE PARTY OF THE PARTY	10	13	115	0.6984		91	8	0	10004 - 000
The	1545	10	*3	** \$	0.0904	-	72	1	1	100 100
1	1546)			-		1		3	1	172 J WI
1	15477	0	9	34	0.4656	I	103	12	0	Edward VI.
1-13-	15483	1	1. (2)		19 78	1 - 2		119		7777
1	1549	10	9	33	0.4656	2	91	12	0	1300 15 20
1 37	The state of the s			77	0.2328	I		90000000	0	12-11-11-11
1	1551	0	4	73	0.2320		43	_		Mary T
1 10	1553	I	0	67	1.0286	5	14	5	5 18	Mary L.
1	1560 }	120		0		1		1 -	17	Elizabeth.
1	11583 5	N	0	8	1.0333	5	2	5	47	The state of the s
1	1601	1			17773	1		177		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
1-1		1			1000	1		1		Inmar I
110	1605	1			1 3	1.11-		1		James I.
1	1627	1			The same of	1		1		Charles I.
1	1661	1			1	1		100		Charles II.
1000		1	0	0	1.0000	5	2	1 5	7	A STORY
1 3	1671	1			1 - 10 - 10	1		1		James II
1	1685	1			1-12	1		1		James II.
1	1720	1			1 1/16	10		1-3		George I.
1	1764	1			1	1		1		George III.
	1-1-47	24-	13000	No.		Sec. of	-	1	-	1

Prices of Goods at the above-mentioned.
Times.

From A. D. 1000 to A. D. 1066. A horse 11. 17 s. 6 d. A cow 6 s. An ox 7 s. 6 d. A swine 2 s. A sheep 1 s.

3 d. Wheat per quarter 1 s. 6 d.

From A. D. 1066 to A. D. 1199. A horse 12s. 5d. An ox 4s. 8d. A sow 3s. A colt 2s. 4½d. A calf 2s. 4½d. A sheep 1s. 8d. Wheat per quarter 3s. 1d.

From A. D. 1199 to A. D. 1307. A horse 11. 115. An ox 45. 8 d. A sow 35. A cow 175. $o_{\frac{1}{2}}^{\frac{1}{2}}d$. A lamb 45. A heifer 25. $1\frac{1}{2}d$. A goose 15. $o_{\frac{1}{2}}^{\frac{1}{2}}d$. A cock $4\frac{1}{2}d$. A hen 3 d. Wheat per quarter 11. 35. $2\frac{1}{2}d$.

From A. D. 1307 to 1418. A horse 18 s. 4 d. An ox 2 l. 6 s. 1 d. A cow 7 s. 2 d. A calf 4 s. 2 d. A sheep 2 s. 7 d. A goose 9 d. A cock 3\frac{3}{4} d. A hen 2\frac{3}{4} d. Wheat per quarter 15 s. Ale per gallon 7\frac{3}{4} d. Day labourer's wages 4\frac{1}{4} d.

From A. D. 1418 to A. D. 1524. A horse 21. 4s. An ox 11. 15s. 8; d. A cow 15s. 6d. A colt 7s. 8d. A sheep 5s. A hog 5s. A calf 4s. 1 d. A cock 3 d. A hen 2 d. Wheat per quarter 11 s. 3 d. Ale per gallon 23 d. Day labourer's wages 33 d.

From A. D. 1524 to A. D. 1604. An ox 11. 16 s. 7 d. A sheep 4 s. 3 d. A calf 5 s. 6 d. A lamb 4 s. 4 d. A goose is. A capon is. Beef per stone 11 d. Coals per chaldron 78. 94d.

Wheat per quarter 158.

From A. D. 1624 to A. D. 1646. A pheafant 5 s. 6 d. A turkey 3 s. 9 d. A goose 2s. A partridge 1s. A pullet 1 s. 6 d. A pigeon 6 d.

From A. D. 1730 to A. D. 1760. A horse 101. An ox 81. A cow 71. 7 s. A hog 11. 15 s. A sheep 11. 6 s. A turkey 4 s. A cock 1 s. 3d. Seamens wages per day 9 d. Common labourers 1 s. 8 d.

In the preceding Table, by comparing the number of shillings in the pound pound weight of filver in the former times with the number in the pound weight at prefent, it will be found that the above-mentioned articles were not so cheap as is now generally believed.

Concerning Gold.

The standard for coinage gold is it ounces of pure gold and i ounce of copper.

At the Tower of London, 44 guineas and an half are coined out of a Troy pound, or 5760 grains, of gold. Hence, the standard weight of a guinea is

129 4 3 8 2 grains.

The weight of a cubic foot of fuch gold is 7524921% grains (or 1306 Troy pounds 4 ounces 18 penny-weight 9% grains. Out of this quantity, 58135% guineas may be coined, which is equal in value to 61042 pounds o shillings 3 pence sterling.

A lump of this gold, equal in bulk to 21297, cubic feet, coined into guineas,

would pay the national debt.

The Number of different Ways in which all the Letters of the Alphabet might be combined, or put together, from 1 Letter to 25. Or, the Number of Changes which might be rung on any Number of Bells not exceeding the Number of Letters in the Alphabet.

Thus 2 letters may be put 2 different ways together; 3 letters, 6 different ways; 4 letters, 24 ways; 5 letters, 120 ways; 6 letters, 750 ways; and fo on, as in the following Table:

```
D
        24.
       120
        720
        5040
        40320
        362880
9
        3628800
10
        39916800
        479001600
12
        6227020800
13
        87178291200
14
        1307674368000
        20922789888000
16
        35,687428096000
17
        6402373705728000
    S
        121645100408832000
19
        2432902008176640000
    U
        51090942171709440000
    V
21
        1124000727777607680000
    W
22
        25852016738884976640000
23
        620448401733239439360000
        15511210043330985984000000
```

Now,

Now, supposing all the 25 letters could be put down in 30 seconds of time, or each combination of them made in that time (which might be done) it would require 57461442099517020244 Julian years to make all the various combinations which these letters would admit of. And consequently, if the world had already lasted 6000 years, it would require 9576907016586170 such ages to make all these combinations, without ever stopping for one single second of time.

Supposing a square Cistern to be a Mile wide and a Mile deep, or to contain a Cubic Mile of Water; and that a Cubic Yard of Water should run off from it every Minute until it was quite emptied. Qu. How much Time would all the Water take to run out of the Cistern?

Ans. 5451776000 minutes (for so many cubic yards there are in a cubic mile) or 10365 Julian years 139 days 7 hours 20 minutes.

P 3

Concern-

Concerning the Strength of Steam. From the Reverend Mr. Mitchell's Treatise on Earthquakes.

" There are many effects produced by the vapour of water, when intenfely heated; which make it probable that the force of gunpowder is not near equal to it. The effects of an exceeding small quantity of water, upon which melted metals are accidentally poured are fuch, I think, as could no ways be expected from the like quantity of gunpowder. Founders, if they are not careful, often experience these effects to their cost .-An accident of this kind happened about forty years ago, at the casting of two brass cannon at Windmill-Hill, Morefields. The heat, fays Cranmer, of the metal of the first gun drove so much damp into the mould of the fecond, which was near it, that, as foon as the metal was let into it, it blew up with

with the greatest violence, tearing up the ground some feet deep, breaking down the furnace, untiling the house, killing many spectators on the spot with the steams of the melted metal, and scalding many others in a most miserable manner.

Volcanos prove that there are fires within the earth, far below its furface; and over fome of these fires there may be caverns of water. When any of the water finds its way through the bottom of such a cavern, and falls down into the fire, the water will be immediately rarised into steam; and the elasticity thereof will heave up the ground above it, and make an earthquake. The deeper the fire is, the further will the earthquake be extended."

SELECT EXELUCISES.

swith the granul tome fear, door, later up the granul tome fear, door, later as a down the fantage of the partition of the withing the door, because of the doctor of the meteor makes.

rgirèralde manner.

Voidance prove that rises are determined and trueviolein the carely for bottomy in truethere is not over found out the formal
any of the waterfield in way through a
the bottom of fach a closur, and raise
down time the fach a closur, and raise
to the things in the fact and water with
the things and above it, and make comon the ground above it, and make comon the ground above it, and make comon the ground above it, and make comour inquite. The pleasure prove it.

SHIEM

MATHEMATICAL

TABLES

FOR

Dividing the LINES on SCALES and SECTORS.

In these Tables I have only numbered the whole degrees, the intermediate lines shewing how many parts each of them is divided into: as where there are three such lines, they denote the degree to be divided into quarters; where two, into thirds; and where one, into halves.

-	ALCOHOL: N	 STATE OF THE PARTY
71 -4	A	ords.
IVAL	711201	mras-

Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.				
1 4	4.36	7 4	143.86	4	282.66	14	420.09				
	8.72		148.21	1200	286.98	1 3300	424.35 428.61				
1	13.09	9	152.56	17	291-30	20	432.87				
The state of	21.81	9	161.26	1/	299.93	25	437.13				
300	26,17	300	165.61	Basi	304.24	3567	441.39				
	30.53	STA.	169.96	A.T.	308.55	163.	445.65				
2	34.90	10	174.31	18	312.86	26	449.90				
FOR	39.26	E Bar	178.66	18.	317.17	Till	454.15				
200	43.62	SEL.	183.01	1884	321.48	100	458.40				
1000	47.98	1970	187-35	神安。	325.79	200	462.65				
1 3	52.35	11	191.69	19	330.09	27	466.89				
	56.71	19.45	196.02	1000	334-39	12	471.13				
15.53	61.07	- 577	200.37	233	338.69		475-37				
	65.43	1000	204.71	1000	342.99	1923	479.61				
4	69.79	12	209.05	20	347.29	28	483.84				
18.93	74.15		213.39		351.59	1222	488.07				
188	78.51		217.73		355.88		492.30				
	82.87		222.07		360.18	12.50	496.53				
5	87.23	13	226.40	21	364.47	29	500.76				
Teach	91.59	1000 P	230 74		368.76		504.98				
139	95.95		235.07	235	373.04	TO THE	509.20				
6	100.31		239.40	200	377-33	100	513.42				
10	104.67	14	243.73	22	381.61	30	517.63				
-	109.03	1000	248.06	186	385.89	1000	521.85				
100	113.38	100	252.39	100	390.18	120	526.06				
7	122.00	15	261.05	23	394.46		530.27				
1	126.45	.,	265.38	23	398.73	31	534-47 538.68				
1000	130.80	1000	269.70	- 600	407.28	The state of	542.88				
(Same)	135.16	17861	274.02	PERM	411.55	- Bell	547.08				
8	139.51	16	278.34	24	415.82	32	551.27				
200	333		7 -34		1.3.02	3"	33/				

	Natural Chords.										
Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.				
4	555.46	7	688.19	1 4	817.45 821.43	4	942.79				
33	563.84 568.03 572.21	41	696.37 700.41 704.55	49	825.41 829.38 833.35	57	950.47 954.31 958.14				
34	576.39 580.56 584.74 588.92	42	708.58 712.71 716.73 720.81	50	837.31 841.27 845.23 849.18	58	961.97 965.79 969.61 973.43				
35	593.09 597.25 601.41	43	724.87 728.94 733.00	51	853.13 857.08 861.02	59	977.24 981.04 984.84				
	605.57 609.72 613.88		737.06 741.11 745.16	A STATE	864.96 868.89 872.82	- 100	987.64 992.43 996.22				
36	618.03 622.18 626.32 630.46	44	749.21 753-25 757-29 761.33	52	876.74 880.66 884.57 888.48	6⊚	1000.00* 1003.77 1007.54 1011.31				
37	634.60 638.74 642.87	45	765.36 769.39 773.42	53	892.39 896.29 900.19	61	1015.07				
38	647.00 651.13 655.26	46.	777.44 781.46 785.47	54	904.09 907.98 911.85	62	1026.33				
39	659.38 663.50 667.61	47	789.48 793.49 797.49	55	915.74 919.62 923.49	63	1037.54 1041.27 1044.99				
No.	671.72 675.83 679.94		801.49 805.49 809.48		927.36 931.22 935.08	6	1048.71				
140	684.04	48	813.47	56	938.94	64	1059.83				

Natural Chords.

	Sales and	100		-		-	
Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.	Degrees.	Chord. Parts.
14	1063.52	1 4	1164.95	4	1262.03	1 4	1354-39
65	1070.91	72	1172.03	79	1268.78	86	1360.80
	1078.27		1179.09		1275.51	The state of the s	1367.18
66	1085.61	73	1186.13	80	1282.22 1285.57 1288.91	87	1373.53 1376.70 1379.86
	1092.93		1193.14 1196.64 1200.14		1292.24		1383.02
67	1103.87	74	1203.63	81	1298.89	88	1389:31
	1111.14	150	1210.58	82	1305.51	89	1395.58 1398.70 1401.81
68	1118.38	75	1217.52	02	1315.40	09	1404:92
69	1128.21	76.	1227.88	83	1321.97	90	1411.12
	1136.40	10	1234.75	1	1328.50		
70		77	1241.60	84	1335.01 1338.26 1341.50		
100	1150.72	100	1251.84		1344.73		
71	1161.40	78	1258.64		1351.18	1	

End of the Table of Natural Chords.

	Natural Sines.											
Degrees.	Sine. Parts.	Degrees.	Sine. Parts.	Degrees.	Sine. Parts.	Degrees.	Sine. Parts.					
1 4	4.36	1 4	143.49	1 4	279.83	1 4	410.72					
- Cont	8.72	Chr.	147.81	1	284.02		414.69					
1	13.09	1	152.12	1	288.20		418.66					
199	21.81	9	156.43	17	292.37	25	422.62					
1 - 1%	26.17	130	165.05	1000	296.54	33.9	426.57					
3 5%	30.53	1.30	169.35	1000	304.86	3 3	430.51					
2	34.90	10	173.65	18	309.02	26	438.37					
1	39.26	DIN	177.94	1000	313.16	-	442.29					
700	43.62	1 100	182.23	1870	317.30	11/19	446.20					
3.54	47.98	12/2/2	186.52	To a se	321.44	7.09	450.10					
3	52.34	11	190.81	19	325-57	27	453.99					
3-1-1	56.69	DIN	195.09	1200	329.69	I S	457.87					
10.12	61.05	200	199-37	11.5	333.81	37.6	461.75					
1 1 2	65.40	The same	203.64	Let !	337-92	1	465.61					
4	69.76	12	207.91	20	342.02	28	469.47					
623	74.11	1000	212.18		346.12	No or Bridge	473.32					
7	78.46 82.81	1508	216.44	1000	350.21	10 30 5	477.16					
5	87.16	13	220.70	21	354-29		480.99					
3	91.50	.3	229.20		358.37	29	484.81					
1	95.85	1000	THE LANGE OF THE LOCAL PROPERTY OF		362.44	9008	THE RESERVE OF THE PARTY OF THE					
	100.19	- 100	233.45	2003	370.56	William	492.42					
6	104.53	14	241.92	22	374.61	30	.500,00					
7 3	108.87		246.15	17-12	378.65	3	503.77					
1	113.20		250.38	12-12	382.68	Colta	507.54					
MONEY.	117.54	12/3/	254.60	1	386.71	1000	511.29					
7	121.87	15	258.82	23	390.73	31	515.04					
1	126.20	14.13	263.03	No. 10	394-74	1 70	518.77					
3 1 1 1 L	130.53	all by	267.24	1	398.75	47 8	522.50					
0	134.85		271.44	200	402.75	17.00	526,21					
8	139.17	16	275.64	24	405.74	32	529.92					

Natural Sines.											
Degrees.	Sine. Parts.	Degrees.	Sine. Parts.	Degrees.	Sine. Parts.	Degrees.	Sine. Parts.				
-14	533.61	1 4	646.12	1 4	746.06	* 4	831.47				
	537-30		649.49	1798	748.96		833.86				
	540.97	- Sec.	652.76		751.84		836.29				
33	544.64	41	656.06	49	754.71	57	838.67				
5	548.29	2-0	659.35		757-56		841.04				
	551.94	100	662.62		760.41		843.39				
24	555.57	12	665.88		763.23 766.04	-0	845.73				
34	559.19	4.2	672.37	50	768.84	58	848.05				
13	566.41	400	675.59	663	771.62		850.35				
	569.99	3 (7)	678.80		774-39	1016	852.64 854.91				
35	573.58	43	682.00	51	777.15	59	857.17				
33	577.14		685.18	3	779.88	29	859.41				
-	580.70	130	688.35	70018	782.61		861.63				
L. Pro	584.25	- 3	691.51		785.32		863.84				
36	587.79	44	694.66	52	788.01	60	866.03				
6B	591.31	12.50	697.79	5	790.69		868.20				
21	594.82	131	700.91	BIN	793-35		870.36				
	598.32		704.01	777	796.00		872.50				
37	601.81	45	707.11	53	798.64	61	874.62				
REE !	605.29	1	710.19	7	801.25	13/18	876.73				
PE	608.76	88	713.25		803.86		878.82				
-0	612.22	1	716.30		806.44	,	880.89				
38	615.66	46	719.34	54	809.02	62	882.95				
15	619.09	1336	722.36	10000	811.57	18016	884.99				
10. 155	622.51	TO BE	725·37 728·37	1	814.12	THE REAL PROPERTY.	887.01				
20	629.32	47	The second secon	-	816.64	60	889.02				
39	632.71	47	731.35	55	819.15	63	891.01				
1	636.08	THE PARTY	737.28	39 3	824.13	NO THE	892.98				
13.	639.44	5304	740.22	1000	826.59	1	894-93				
40	642.70	18	743.14	-6	820.04	1.	808.70				

	Natur	res.	yond 70,	han whole needlefs to	
Deorees.	Sine. Parts.	Degrees.	Sine. Parts.	ontain the degrees of the Sines are so very small when they go beyond	e whose line or r in lefs than
4	900.70	1 3	963.63	when	n the nor it was
30	902.59	75 76	965.93	=	d 75,
	906.31	77	974-37	l ji	and and
-	908.14	78	978.15	1 5	ye, o an
1	909.96	79	981.63	Ver	n 70
100	911.76	79 80	984.81	0 1	en
6	913.55	81	987.69	9	lves between
50	915.31	82	990.27	, a	bet
63	917.06	83 84	992.55	seu	quarters without nurting the eye, even g lefs than halves between 70 and 75
7	920.50	85	994.52 996.19	Si	lye
1	922.20	90	1000.00	he	ha
	923.88	100	1 1 2	Je I	WI
22	925.54	SELT		8	T T
8	927.18		nd,	are.	lefs
8	928.81		53	deg	200
	930.42		Sim	pe !	thing
9	933.58	Matural Since	26	1 3	==
9		Tast	e ti	tail	any
25	936.67		ber	no	0 2
100	938.19		402	9	int
0	939.69	7	iin iii	nic.	or o
C CO	942.64	F	de le	1	nou
1	945.52		113	Ses	19.
1	948.32	3	can	pad	lol
2	951.00	-	Se	1 9	ot c
2	0:6.30	Tool of the Trakla of	The Secants begin aubere the Sines	41	fo
3	935.14 936.67 938.19 939.69 942.64 945.52 948.32 951.06 953.72 9,6.30 958.82 961.26	2000		As the spaces which co	was a foot long, nor into
4	961.26	1200		-	was a foot long, nor int

	Natural Tangents.											
Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.					
+	4.36	1 4	144.99	4	291.47	1 4	450.47					
	8.73	1 33	149 45	13.53	296.21	1	455.73					
1	13.09	1	153.91	1	300.97	1	466.31					
1	21.82	9	158 38	17	305.73	25	471.63					
123	26.19		167.34	2300	315.30	100	476.98					
10.1	30 55	19	171.83	1100	320 10	983	482.34					
2	34.92	10	176.33	18	324.92	26	487.73					
	39.29	116	180.83		329.75	1000	493.15					
7.3	43.66	133	185.34	330	334.60	1	498.58					
	48.03	1	189.86		339-45	190	504.04					
3	52.41	11	194.38	19	344.33	27	509.53					
10/2	56.78	12	198.91	1175	349.22	100	515.03					
120	61.16	1000	203.45	4.00	354.12	1257	520.57					
	65.54	10	208.00	20	359.03	0	526.13					
4	69.93	12	217.12	20	363.97 368.92	28	531.71					
	78.70	200	221.69	9.50	373.88	TOP	537.32					
	83.09		226.26	153	378.87	2.3	548.62					
5	87.49	13	230.87	21	383.86	29	55431					
	91.89		235.47	P'	388.88	20	560.03					
	96.29	0.02	240.08	31/3	393.91	300	565.77					
	100.69		244.70	17	398 96		571.55					
6	105.10	14	.249-33	22	404.03	30	577-35					
000	109.52		253.97	19	409.11		583.18					
	113.93		258.62	437	414.21	2020	589.04					
	118.36	1	263.28	130	419.33	1	594.94					
7	122.78	15	267.95	.23	424.47	31	600.86					
	131.65	THE P	277.32	199	429.63	THE REAL PROPERTY.	612.80					
1	136.09	334 3	282.03	7134	434.81	235	618.82					
8	140.54	16	286.74	24	445.23	32	621.87					

	Natural Tangents.										
Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.				
	630 95	1	846.56	14	1120.41	4	1496.61				
1	643.22	-	854.08 851.66		1130.29		1510.84				
33	649.41	41	869.29	49	1150.37	57	1539.86				
177	655.63		876.98 884.73		1170.85		1554.67				
	668.18	120	892.53	1	1181.25	-0	1584.90				
34	680.88	42	900.40	50	1191.75	58	1600.33				
13	587.28		915.33	1	1213.10		1631.85				
1	700.21	43	924.39	51	1223.94	59	1647.95				
35	706.73	13	940.71		1245.97		1680.85				
10	713.29		948.96	1	1257.17		1697.66				
36	719.90	44	965 69	52	1279.94	60	1732.05				
1	733.23		974.16		1291.52		1749 64				
13	739.96	133	982.70	11	1303.23		1767.49				
37	753.55	45	1009.00	53	1327.04	61	1804.05				
1	760.42		1008.76	113	1339.16		1822.76				
	774.28		1026.53	100	1363.83	,	1861.09				
38	781.29	46	1035.53	54	1376.38	62	1880.73				
1	788.34	1	1053.78	119	1401.95	119	1920.98				
13	802.58	1	1063.03	110	1414.97	6.	1941.62				
39	809.78	47	1072-37	55	1428.15	63	1962.61				
1	824.34	133	1091.31	1	1455.01	13	2005.69				
1	831.69	10	1110.61	56	1468.70	64	2027.80				
140	839.10	48	1110.01	130		No.					

Natural Tangents.

		-					
Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.	Degrees.	Tang. Parts.
1 4	2073.21	1 4	2506.52	14	3124.00	1 4	4086.66
65	2120.30 2144.51 2169.17	69	2571.50 2605.09 2639.45	73	3220 53 3270.85 3322.64	77	4246.85 4331.48 4419.36
66	2194.30 2219.92 2246.04	70	2674.62 2710.62 2747.48		3375·94 3430.84	-0	4510.71
	2272.67	70	2785.23	74	3487.41 3545.73 3605.88	78	4704.63 4807.69 4915.16
67	2327.56 2355.85 2384.73	71	2863.56 2904.21 2945.90	75	3667.96 3732.05 3798.27	79	5027.34 5144.55 5267.15
68	2414.21 2444.33 2475.09	72	2988.68 3032.60 3077.68	76	3856.71 3937.51 4010.78	80	5395.52 5530.07 56-1.28
	14/1109	The state of	30//100	101	40.0.70	10	10 1.20

As the Tangents are never laid down further than to 80 degrees on common scales, it would be needless to

carry them further in this Table.

The semi-tangents may be laid down on a scale by taking out the tangents of half the number of degrees in this Table.—Thus, the semi-tangent of a whole degree is the whole tangent of half a degree: the semi-tangent of 2 degrees is the whole tangent of 1 degree: the semi-tangent of 3 degrees is the whole tangent of 4 degrees is the whole tangent of 2 degrees: and so on. They are never subdivided further than to half degrees.

	Natural Secants.										
Degrees.	Sec. Parts.	Degrees.	Sec. Parts.	Degrees.	Sec. Parts.	Degrees.	Sec. Parts.				
0 10 15	1000.00	1 38	1260.47	3 47	1459.46 1466.28 1473.19	3 55	1732.67 1743.45 1754.40				
16 17 18	1040.30 1045.69 1051.46 1057.62	39	1286.76 1295.97 1305.41 1310.22	48	1480.19 1487.28 1494.48 1501.77	56	1765.52 1776.81 1788.29 1799.95				
20 21 22 23	1064.18 1071.14 1078.53 1086.30	41	1315.09 1320.02 1325.01 1330.07	49	1509.16 1516.65 1524.25 1531.96	57	1811.80 1823.84 1836.08 1848.51				
24 25 26 27	1103.38	42	1335.19 1340.38 1345.63 1350.95	50	1539.79 1547.69 1555.72 1563.87	58	1861.16 1874.01 1887.08 1900.37				
28 29 30	1132.57	43	1356.34 1361.80 1367.33 1372.93	51	1572.13 1580.51 1589.02 1597.64	59	1913.88 1927.62 1941.60 1955.82				
31	1166.63	44	1378.56 1384.34 1390.16 1396.06	52	1605.39 1615.26 1624.27 1633.41	60	1970.29 1985.02 2000.00 2015.25				
33	1192.30 1199.20 1206.22	45	1402.03 1408.08 1414.21 1420.42	53	1642.68		2030.77 2046.57 2062.67 2079.05				
35	1228.33	16	1426.72 1433.09 1439.56	54	1681.17	_	2095.74 2112.74 2130.05 2147.70				
37	1244.00		1446.10	1	1722.05		2165.68				

Natural Secants.

-	The second secon										
Deg.	Sec. Paris.	Deg.	Sec. Parts.		Sec. Parts.	Deg.	Sec. Parts.				
63	2184.01		2585.91 2613.13		3193.22	4	4207.23				
	2221.74	68	2640.97		3280.15	77	4362.99				
64			2698.64	73	3372.21		4531.09 4620.22				
	2301.79	_	2759.09	13	3469.86 3520.94	78	4713.03				
65	2344.29 2366.20 2388.57		2822.54	74	3573.61		5015.85				
	2411.42	70	2889.20	_	3684.05	79	5125.83				
66	2458.49		2959.31	75	3863.70		5487.40				
	2507.84		3033.15 3071.55 3111.01		3993-93	80	5619.76				
67	25:9.30		3151.55	76	4133-57	T	he End.				

Natural Rhumbs.

R.1	Parts.	R.	Parts.	R.	Parts.	R.	Parts.
4	49.09	4	438.19	4	810.48	4	1151.62
	98.14		485.96		855.10		1191.40
1	147.12	3	533.42	5	899.22	7	1230.46
	224.82		027.36		985.82		1306.34
	293.46	100	673.78		1028.20	100	1343.12
2	341.92	4	719.80	6	1111.14	8	1379.07

This and all the preceding Tables are fitted to one and the same Radius on the plain scale.

A TABLE shewing in what Parallel of Latitude any given Number of Geographical Miles make a Degree of Longitude, and their Projection on a plain Scale.

Latitudes, for the Dialing Scale.

Deg.	Parts.	Deg.	Parts.	Deg.	Parts.				
1	24.7	31	647.5	61	931.1				
2	49.3	32	662.2	62	936.0				
3	73.9	33	676.4	63	940.8				
4	98.4	34	690.2	64	945.4				
	122.8	35	703.6	65	949.6				
5	147.0	36	716.6	66	953-9				
	171.1	37	729.2	67	957.8				
7 8	194.9	38	741.4	68	961.5				
9	218.6	39	753.2	69	965.1				
10	241.9	40	764.7	70	968.5				
11	265.0	41	775.8	71	971.6				
12	287.9	42	786.5	72	974-5				
13	310.4	43	796.8	73	977.4				
14	332.5	44	806.7	74	980.1				
15	354-3	45	816.5	75	982.5				
16	375.8	46	825.9	76	984.8				
17	396.9	47	834.8	77	986.9				
18	417.6	48	843.6	78	988.8				
19	437.8	49	851.9	79	990.6				
20	457-7	50	860.0	80	992.4				
21	477.3	-51	867.8	85	998.2				
22	496.1	52	875.3	90	1000.0				
23	514.6	53	882.5	can	8e be-				
24	532.8	54	889.5	S C	9				
25	- 550.5	55	896.2	10	nor and				
26	567.8	56	902.6	50.5	tw 5				
27	584.6	57	THE RESERVE OF THE PERSON NAMED IN COLUMN 1	lo Degrees o	85, n en 85 a				
28	601.0	58	914.7	S. S.	le sen				
29	616.9	59	920.3	l be	icale and 8 tween				
30	6325	60	925.8	1					

	Hours and Minutes.	Parts.	Hours and Minutes.	Parts.
	XII o	0.0	III o	707.1
	5	30.3	5	722.5
118	5 10	59.1	10	737-9
ali	15	87.0	15	753-4
0	20	1138	20	769.0
	25	139.6	25	7846
for	3,0	164.5	30	800.2
1	35	188.8	35	816.0
1 5	40	212.0	40	831.9
no	45	2346	45	847.8
ti	. 50	256.7	50	863.8
10	55	278.0	TIT 55	880.1
ed to the preceding Table of Latitudes, for Dialing.	IO	298.8	IIII o	896.5
0	5 10	319.2	10	913.1
126		339.0	The second second second	930.0
1 2	15	358.4	15	947.1 964.5
1	20	377.3	And the second s	982.0
1 80	25	395.9	25	1000.0
di	30	414.2	30	1018.3
600	35	449.7	35	1036.9
12	40	467.1	4° 45	1055.8
0	45	484.2	50	1075.2
12	50	501.1	55	1095.0
2	II 0	517.7	V	1115.4
a.	5	534.1	5	1136.2
	10	550.4	10	1157.5
lat	15	566.4	15	1179.6
aa	20	582.4	20	1202.2
Hours adap	25	598.3	25	1225.4
no	30	614.0	30.	1249.7
H	35	629.6	35	1274.6
The State of	40	645.2	40	1300.4
1 100	45	660.8	45	1327.2
110000	50	676.3	. 50	1355.1
	55	691.7	55	1383.9
1	III o	707.1	VI o	1414-2

Inclination of Meridians.

Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	
1	24.3	31	530.8	61	909.8	
2	47.7	32	543.8	62	923.3	de
3	70.4	33	5568	63	936.9	ita
4	92.4	34	569.7	64	950.6	of Latitudes
5	113.8	35	582.4	65	964.5	f I
_	134.5	36	595.1	66	978.5	
7 8	154.6	37	607.7	67	992.8	Line
_	174.2	38	620.3	68	1007.3	H
9	193.4	39	632.8	69	10220	and
10	212.0	140	645.2	70	1036.9	TO SECURE A SECURE AND ADDRESS OF THE PARTY AN
11	230.1	41	657.7	71	1052.0	Hours,
12	247.9	42	670.0	72	1067.4	no
13	265.3	43	682.4	73	1083.1	. 1
14	282.2	44	694.7	74	1099.1	Jo
15	298.8	45	707.1	75	1115.4	Line
16	315.1	46	719.5	76	1132.0	i i
17	331.1	47	731.8	77	1148.9	00
18	346.8	48	744.2	78	1166.3	preceding
19	362.2	49	756.5	79 80	1184.1	3
20	377.3	50	769.0		1202.2	pre
21	392.2	51	781.4	81	1220.8	0
22	406.9	52	793.9	82	1240.0	the 1
23	421-4	53	806.5	83	1259.6	2
24	435.7	54	819.1	84	1279.7	po
25	449.7	55	831.8	85	1300 4	Adapted
26	403.6	56	844.5	86	1321.8	Ida
27	477.3	57	857.4	87	1343.8	4-
28	490.9	58	8704	88	1366.5	
29	504.4	59	883.4	89	1389.9	
30	517.7	60	896.5	90	1414.2	

The preceding Tables are for graduating the Lines of Natural Chords, Sines, Tangents, and Secants, &c. on common plain Scales and Sectors.—
The following Tables are for laying down Gunter's logarithmic Lines of Numbers, Sines, Tangents, Versed Sines, Meridional Parts, &c. on his Scales.

Numbers. The Logarithm of 1 = 0.

N.	Parts.	N.	Parts.	N.	Parts.					
1.01	4.32	1.31	117.27	1.61	206.83					
1.02	8.60	1.32	120.57	1.62	209.52					
1.03	12.84	1.33	123.85	1.63	212.19					
1.04	17.03	1.34	127.10	1.64	214.84					
1.05	21.19	1.35	130.33	1.65	217.48					
1.06	25.31	1.36	133-54	1.66	220,11					
1.07	29.38	1.37	136.72	1.67	222.72					
1.08	33.42	1.38	139.88	1.68	225.31					
1.09	37-43	1.39	143.01	1.69	227.89					
1.10	41.39	1.40	146.13	1.70	230.45					
1.11	45.32	1.41	149.22	1.71	233.00					
1.12	49.22	1.42	152.29	1.72	235.53					
1.13	53.08	1.43	155.37	1.73	238.05					
1.14	56.90	1.44	158.36	1.74	240.55					
1.15	60.70	1.45	161.37	1.75	243.04					
1.16	64.46	1.46	164.35	1.76	245.51					
1.17	68.19	1.47	167.32	1.77	247.97					
1.18	71.88	1.48	170.26	1.78	250.42					
1.19	75.55	1.49	173.19	1.79	252.85					
1.20	79.18	1.50	176.09	1.80	255.27					
1.21	82.79	1.51	178.98	1.81	257.68					
1.22	86.36	1.52	181.84	1.82	260.07					
1.23	89.91	1.53	184.69	1.83	262.45					
1.24	93.42	1.54	187.52	1.84	264.82					
1.25	96.91	1.55	190.33	1.85	267.17					
1.26	100.37	1.56	193.12	1.86	269.51					
1.27	103.80	1.57	195.90	1.87	271.84					
1.28	107.21	1.58	198.66	1.88	274.16					
1.29	110.59	1.59	201.34	1.89	276.46					
1.30	113.94	1.60	204.12	1.90	278.75					

Gunter's Line of Numbers.

Algorithms.		M			
N.	Parts.	N.	Parts.	N.	Parts.
1.91	281.03	2.42	383.8z	3.05	484.30
1.92	283.30	2.44	387-39	3.10	491.36
1.93	285.56	2.46	390.94	3.15	498.31
1.94	287.80	2.48	394.45	3.20	505.15
1.95	290.03	2.50	397.94	3.25	511.88
1.96	292.26	2.52	401.40	3.30	518.51
1.97	294.47	2.54	404.83	3.35	525.04
1.98	296.66	2,56	408.24	3.40	531.48
1.99	298.85	2.58	411.62	3-45	537-82
2.00	301.03	2.60	414.97	3.50	544.07
2.02	305.35	2.62	418.30	3.55	550.23
2.04	309.63	2.64	421.60	3.60	556.30
2.06	313.87	2.66	424.88	3.65	562.29
2.08	318.06	2,68	428.13	3.70	568.20
2.10	322.22	2.70	431.36	3.75	574.03
2.12	326.34	2.72	434.57	3.80	579.78
2.14	330.41	2.74	437-75	3.85	585.46
2,16	334.45	2.76	440.91	3.90	591.06
2.18	338.46	2.78	441.04	3-95	596.60
2,20	342.42	2.80	447.16	4.00	602.06
2.22	346.35	2.82	450.25	4.05	607.45
2.24	350.25	2.84	453.32	4.10	612.78
2.26	354.11	2.86	456.37	4.15	618.05
2.28	357-93	2.88	459-39	4.20	623.25
2.30	361.73	2.90	462.40	4.25	628.40
2.32	365.49	2.92	465.38	4.30	633.47
2.34	369.22	2.94	468.35	4.35	638.49
2.36	372.91	2.96	471.29	4.40	643.49
2.38	376.58	2.98	474.22	4.45	648.36
2.40	380.21	3.00	477.12	4.50	653.21

Gunter's Line of Numbers.

The second secon								
N.	Parts.	N.	Parts.	N.	Parts.			
4.55	658.01	6.05	781.75	7.55	877-95			
4.60	662.76	6.10	785.33	7.60	880.81			
4.65	667.45	6.15	788.75	7.65	883.66			
4.70	672.10	6.20	792.39	7.70	886.49			
4.75	676.69	6.25	795.88	7.75	889.30			
4.80	681.24	6.30	799.34	7.80	892.09			
4.85	685.74	6.35	802.77	7.85	894.87			
4.90	690.20	6.40	806.18	7.90	897.63			
4.95	694.61	6.45	809.56	7.95	900.37			
5.00	698.97	6.50	81291	8.00	903.09			
5.05	703.29	6.55	816.24	8.05	905.71			
5.10	707.57	6.60	819.54	8.10	908.48			
5.15	711.81	6.65	822.82	8.15	911.16			
5.20	716.00	6.70	826.07	8.20	913.81			
5.25	720.16	6.75	829.30	8.25	916.45			
5.30	724.28	6.80	832.51	8.30	919.08			
5.35	728.35	6.85	835.69	8.35	921.69			
5.40	732.39	6.90	838.84	8.40	924.28			
5.45	736.40	6.95	841.98	8.45	926.86			
5.50	740.36	7.00	845.10	8.50	929.42			
5.55	744.29	7.05	848.19	8.55	931.97			
5.60	748.19	7.10	851.26	8.60	934.50			
5.65	752.05	7.15	854.30	8.65	937.02			
5.70	755.87	7.20	857-33	8.70	939-52			
5.75	759.67	7.25	860.34	8.75	942.01			
5.80	763.43	7-30	863.32	8.80	944.48			
5.85	767.16	7.35	866.29	8.85	946.94			
5.90	770.85	7.40	869.23	8.90	949.39			
5.95	774.52	7.45	872.16	8.95	951.82			
6.00	778.15	17.50	875.06	9.00	954424			

	Gunt	er's L	ine of N	umbers.	
N.	Parts.	N.	Parts.	N. 1	Parts.
9.05	956.65	9.40	973-13	9.75	989.00
9.10	959.04	9.45	975-43	9.80	991.23
9.15	961.42	9.50	977.72	9.85	993-44
9.20	963.79	9.55	980.00	9.90	995.63
9.25	966.14	9.60	982.27	9.95	997.82
9.30	968.48	9.65	984.53	10.00	1000.00
9.35	970.81	9.70	986.77	Th	e End.

All the number of parts into which the double Line of Numbers (from 1 to 10) on a scale two feet long can well be divided, are inserted in this Table.

The Line of Numbers is marked with the numeral figures 1, 2, 3, 4, 5, 6, 7, 8, 9, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10.—The space between 1 and 2 may be divided into 100 parts; from 2 to 3, into 50; but all the others into no more than 20 each, without hurting the eye to look at such small divisions.

But, in common practice, the spaces from the first 1 to the second 1 are divided only into 10 parts each; and after that, from 1 to 2, into 50; from 2 to 5, into 20 each; and from 5 to 10, each space is divided into no more than 10 parts; leaving the intermediate subdivisions to be estimated by the eye, which may be easily done.

In the following Tables, D. stands for Degrees, and M. for Minutes of a Degree.

Gunter's Line of Sines.

The second secon								-
D.	M.	Parts.	D.	M.	Parts.	D.	M.	Parts.
0	20	2235.25	3	15	1246.47	6	10	968.91
	25	2138.34	1981	20	1235-49		15	963.10
	30	2059.16		25	1224.78		20	957-38
	35	1992.21		30	1214.32		25	951.72
	40	1934.22		35	1204.12	300	30	946.14
	45	1883 07		40	1194.15	86	35	940.63
	50	1837.32	775	45	1184.40	197	40	935.19
	55	1795.93		50	1174.87	100	45	929.82
1	0	1758.14	17.00	55	1165.54		50	924.52
	5	1723-39	4	0	1156.42	750	55	919.28
	10	1691.21	200	5	1147.48	7	0	914-11
-	15	1661.25	100	10	1138.72	315	5	908.99
	20	1633.22		15	1130.13		10	903.94
	25	1606.90	4	20	1121.71	23	15	898.84
	30	1582.08	100	25	1115.10	100	20	894.01
100	35	1558.61		30	1105.36	1	25	889.13
200	40	1536.34	100	35	1097.40	533	30	884.30
100	45	1515.15	240	40	1089.60	3	35	879.53
200	50	1494.96	100	45	1081.92	193	40	874.81
0.0	55	.1475.66		50	1074.39		45	-870.15
2	0	1457.18	Con	55	1066.98	237	50	865.53
100	5	1439.46	5	0	1059.70	10	55	860.96
	10	1422.43	100	5	1052.64	8	0	856.44
	15	1406.05		10	1045.50	13.5	5	851.97
201	20	1390.27		15	1038.57	100	10	846.67
1	25	1375.03	138	20	1031.75		15	843.17
130	30	1360.32	1	25	1025.04	100	20	838.84
1	35	1346.09	1	30	1018.43	1	25	834-55
1	40	1332.31		35	1011.92	1	30	830.30
100	45	1318.96	1	40	1005.50	-	35	826.09
	50	1306.00	1 19	45	999.18	1	40	821.93
10	55	1293.42	100	50	992.96		45	817.80
13	0	1281.20	16	55	986.82		50	813.72
	5	1269.31	6	0	980.77	1	55	809.67
	10	1257.74	1	5	974.78	19	0	1,004.07

Gunter's Line of Sines. D. M. D. M. Parts. D. Parts. Parts. M. 801.70 46c.78 611.29 14 10 20 15. 9 5 606.31 455.67 797.77 30 IO 20 450.64 601.40 15 30 45 790.01 596.54 21 445.67 20 40 786.18 591.75 15 440.77 25 50 587.00 782.39 30 435.92 30 15 778.63 IO 582.32 45 4;1.14 35 22 20 426.42 40 774.91 577.68 771.22 573.10 421.76 45 30 15 417.16 568.57 767.56 40. 30 50 50 412.61 564.09 763.93 45 55 16 559.66 408.12 760.33 23 0 0 10 10 555.28 15 403.68 10 753.23 746.24 20 550.95 30 399.30 20 546.66 30 739-37 45 394.97 30 390.69 24 40 732.61 40 542.42 0 386.46 538.22 50 15 50 725.95 534.06 382.27 719.40 30 0 378.14 529.95 10 712.95 10 45 525.88 25 706.60 374.05 20 20 0 521.86 370 OI 700.34 15 30 30 517.87 366.02 694.18 30 40 40 688.11 362.05 513.93 50 50 45 26 510.02 358.16 682.12 18 0 676.22 506.15 10 IO 15 354.29 670.40 350.47 502.32 30 20 20 664.66 346.69 498.52 30 30 45 659.00 494.77 342.95 40 40 653.42 491.04 15 339.25 50 50 647.91 487.36 0 0 30 335.59 642.48 483.71 331.97 10 IO 45 28 637.11 480.09 328.39 20 20 0 631.81 30 30 476.50 15 324.85

40

50

472.95

469.43

465.95

321.34

317.87

314.43

30

45

626.59

621.42

616.32

40

50

14

		Gi	unter's I	ine o	of Sines	D 2 1 1
Deg	Parts.	Deg	. Parts.	1 eg	. Parts.	1 0 1
1 4	311.02	1/4	208,24	12	89.31	
-	307.66	68	205.85	1 55	86.64	-0
1000	304.33	100	203.48	100	84.01	from 1 whole
30			201.13	56	81.43	
1	297.76	13.9	198.80	97.8	78.89	into into
	294-53	-0	196.49	57	76.41	
31	291.33	10	194.20	1	73.97	. 00
13.	285.02	40	191.93	58	71.58	112 to 8
-	281.92	41	187.46	19.5	69.23	into hat t be p
1000	278.84	17	178.73	59	66.93	
32	275.79	42	174.49	60	64.68	1 2 1 2
	272.77		170.32	61	62.47 58.18	be divided o 2; after Degree ca
1980	269.78	43	166.22	62	54.07	be di
-160	266.82	312	162.19	63	50.01	
33	263.89	44	158.23	64	46.34	may l o into 85th I
	260.99		154.34	65	42.72	H 0 00
BHILL	258.11	45	150.51	66	39.27	700
-	255.26		146.76	67	35.97	the to I
34	252.44	46	143.07	68	32.83	the n 40 only
2.7	249.64	DOTAN.	139.44	69	29.85	080
2	246.87	47	135.87	70	27.01	18 t
-	244.13	.0	132.37	71	24.33	יה יהי
35	241.41	48	128.93	72	21.79	an an
The same	238.71	10	125.54	73	19.40	beginning to the into 4; from 4
1	233.40	49	118.95	74	17.16	no e
36	230.78	50		75 76	15.06	from the 20 to 40 between
3	228.18	20	115.75		13.10	om o to
200	225.61	51	109.50	77	11.28	1 2 P
1000	223.06	600 I	106.46	78	9.60	gree from then,
37	220.54	52	103.47	79	8.05	15.05
600	218.03	Will have	100.53	85	1.66	De 6;
2000	215.55	53	97.65	90	0.00	40.
1300	213.09	The same	94.82			Each Degree for into 6; from 2 rees; and then,
38 1	A10.66	54 1	92.04	The	End.	Each 20 into grees;

Gunter's Line of Versed Sines.

10000						Des 1	Parts.
Deg	Parts.	Deg.	Parts.	Deg.	Parts.	Deg.	
0	0	60	124.93	93	324-37	111	493.74
10	3.31	61	129.26	3742	328.38	54.15	499.28
12	4 77	62	133.87	94	332-43	112	504.88
14	6.49	63	138.47	DATE D	336.41	3 - 1 5	510.52
16	8.16	64	143.16	95	340.63	113	516.22
18	10.76	65	147-94	2411.6	344.79	ERAB	521.97
20	13.30	66	152.81	96	348.98	114	527.78
22	16.10	67	157.79	1600	353.20	00,00	533.65
24	19.19	68	162.85	97	357.47	115	539-57
26	22.55	69	168.01	2000	361.77		545.54
28	26.19	70	173.27	98	366.11	116	551.58
30	30.11	71	178.63	THE PERSON	370.49	2017	557.67
32	34.31	72	184.08	99	374.91	117	563.83
34	38.81	73	189.64		379-37	1	570.04
36	43.58	74	195.30	100	383.86	118	576.32
38	48.66	75	201.06	130.00	388.41	E TOWN	582.66
40	54.03	76	206.93	101	392.98	1119	589.06
41	56.82	77	212.91	17.07	397.60	I have been	595-53
42	59.70	78	218.99	102	402.26	120	602.06
43	62.64		225.19	Total !	406.95		608.66
44	65.67	80	231.49		411.70	121	615.32
45	68.77	81	237.90		416.48		622.06
46		82	244.44	market by	421.31	122	628.85
47	75.20	83	251.09		426.19		635.73
48					431.10		642.67
49	The state of the s	85	THE RESERVE OF THE PARTY OF THE	32.8	436.07		649.69
50	A SECTION AND ADDRESS OF THE PARTY OF THE PA	86	OR RESIDENCE TO A SECOND SECOND		441.07	124	
51	All the second second second second	OF REPORTS	The second second	350	446.13	1 25/2	663.95
52	THE RESIDENCE OF A			107	451.22	125	671.19
53		Marie Marie Property Co.		65 8	456.37		678.51
54	20 20 20	-					685.91
55			304.83		466.80		69 .38
50			10 60				
5	112.20	-	312.55		477.4	3	1 708.58
5	Charles and the Control of the Contr	and the second	and the second second		482.82	128	THE RESIDENCE OF THE PARTY OF T
1 3			320.40		1488.20	51	1724.13
-		-				200	The same

Gunter's Line of Versed Sines.

Deg.	Parts.	Deg.	1 Pants	10	. D	-	
				Deg.	Pares.	Deg	Parts.
129	732.03	1 2	901.27	1 2	1106.2	13	13 2.2
1,00	740.02	1000	906.29	1900	1112.7	455	1391.4
130	748.10	139	911.34	148	1119.3	157	1400.6
10000	752.16		916.42	1000	1125.9		1410.0
1	756.27	-	921.55	1000	1132.6		1419.5
131	760.12	Share	926.09	18.8 %	1139.4	1	1429.1
1 31	764.55	140	931.89	149	1146.2	158	1438.8
-	768.52		937.12	-	1153.0	-	144 .6
200	772.91		942.38		1160.0		1458 5
132	781.37		947.67	100	1167.0	599	1468.5
132	785.45	141	953.00	150	1174.0	159	1478.7
63.00	789.93		958.37	220	1181.1	20	1489.0
1520	793.97	3,44	963.78	9.	1188.3	139	1499 4
133	798.60	142	969.21		1195.5	6	1510.0
. 22	803.33	*4*	974.71	151	1202.8	160	1520.6
	807.36		980.23	(233)	1210.1	-31	1531.4
2000	811.18	801	985.80	75	1217.5	100-11	1542.4
134	816.24	7.12	991.39		1225.0	01,11	1553.5
34	820.72	143	997.04	152	1232.6	61	1564.7
1923	825.22		1002.4	をひり	1240.3	2011	1576.1
192.4	829.45	1	1014.2	Marie .	1248.0	23/2	1587.7
135	834.32	144	1020.0		1255.8	-	1599.4
233	838.91	144	1025.9	153	1263.6	162	1611.3
(K) 9	843.52	-	1031.7	223	1271.5	2.75	1623.3
200	848.17	BY	1037.9	9 10	1279.5	25.20	1635.6
136	852.84	145	1043.7	1-1	1287.6		1648.0
000	857.54	147	1049.7	154	1295.8	163	1660.6
250年	862.28		1055.8	27	1304.1	BALL BA	1673.4
1200-3	867.04		1061.9	99.	1312.4	A. I	1686.3
137	871.84	146	1068.1	7	1320.8		1699.6
001	876.67	140	1074.6	155	1329.2	164	1712.9
Ob.	881.53	1 2	1080.6	36	1337.9		1726.5
335	886.40	1	1086.9	388	1346.6	10 Por	1740.3
138	891.34	147	1093.3	1.6	1355-3	.6.	1754.3
2000	896.29	17/	1099.7	156	1364.2	165	1768.6
		-	1999		1373.2		1783.1

Gunter's Line of Versed Sines.

Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	Deg	Parts.
1/2	1797.9		1859.6		1926.2	1	1998.4
166	1828.2		1892.3	168	1961.5	Th	e End.

Gunter's Line of Tangents.

D.	M.	Parts.	D.	M.	Parts.	D.	M.	Parts.
0	30	2059.14	2	45	1318.46	5	0	1058.05
105	35	1992.19		50	1305.47	1999	5	1050.83
2000	40	1934.19		55	1292.86	700	10	1043.73
1	45	1883.04	3	0	1280.60	29	15	1036.75
243	50	1837.27	100	5	1268.68		20	1029.87
1000	55	1795.87	100	10	1257.08	188	25	1023.09
1	0.	1758.08	250	15	1245.77	1	30	1016.42
1750	5	1723.31	2 19	20	1234.75	131	35	1009.85
1768	10	1691.12	933	25	1224.00	920	40	1003.38
392	15	1661.14		30	1213.51	2011	45	996.99
1922	20	1633.11	53	35	1203.27	100	50	990.70
100	25	1606.77	36	40	1193.26	13.5	55	984.50
100	30	1581.93	100	45	1183.47	6	0	978.38
	35	1558.43	303	50	1173.90	17	5	972.34
1115	40	1536.15		55	1164-53	133	10	966.39
THE R	45	1514.95	4	0	1155.36	19	15	960.52
Barre	50	1494.73	1	5	1146.37	933	20	954.72
100	55	1475.41	13 1	10	1137.57	133	25	948.99
2	0	1456.92	1	15	1128.94	13	30	943-34
1000	5	1439.17	La.	20	1120.47	BY BY	35	937.76
1-60	10	1422.12	1879	25	1112.16	1	40	932.25
1000	15	1405.72	3 3	30	1104.02	130	45	926.80
100	20	1389.91	185	35	1096.01	193	50	921.42
100	25	1374.65	100	40	1088.15	4,4%	55	916.11
1.44	30	1359.91	1	45	1080.43	7	0	910.86
13	35	1345.65	1	50	1072.84	193	5	905.66
103	40	1331.84	1	55	1065.38		10	900.53

Gunter's Line of Tangents.

U.	M.	Parts.	D.	M.	Parts.	D.	M.	Parts.	ID.	Parts.
17	15	895.40		30	732.20		30	528.40	34	350.54
111	20	890.44	1000		725.04		75000	523.78		III BOOK CONTRACTOR
1	25	885.48		50	718.14		50			346.34
100	30	880.57		0	711.35		0	514.66	100	341.30
100	35	875.72		10			10	510.16		336.29
	40	BROOK OFFICE AND ADDRESS OF THE PARTY OF THE	100	20	The second second	199	20	505.70	25	331.33
100	45	866.16	200	30		1911	30	NAME AND ADDRESS OF THE OWNER, TH		326.40
	50	861.46	100	40			40			321.50
	55	856.80		50	CONTRACTOR OF THE PARTY OF THE	1		492.54		316.64
8	0	TOTAL CO. LANSING MICH.	12		672.53	18	0	INC. STORY STORY STORY		311.82
1	5	847.64		10	200	1	10			307.03
	10	843.12		20	660.26		20			302.26
	15	838.65		30	654.24		_	475.48		297.53
	20	COLUMN TO STATE OF THE PARTY OF		40			40	100	27	292.83
	25	829.84			642.43			457.15		288.16
	30		13	0		19	0	463.03		283.52
	35	821.20		10				458.94		278.91
133	40			20	625.24			454.88	28	274-33
-	45	812.72			619.65			450.85		269.77
100	50		199		6086	200	40	The second second second		265.24
1	55				608.64		MONTH (1992)	442.88	30	260.73
9	0	796.22	14	0		20	0	438.93	29	256.25
100	5	792.18			597.88	36.0		433.07		251.79
ret some	15	788.18		_	592.58		200	427.26		247.36
1900	20	784.22		30	587.34 582.16	21	100	421.51	-	242.95
1	25	780.29			The state of the s		131	415.82	30	238.56
123	30	1	15	0	571.95			404.60	HE	234.20
1	The same I	772.53	-0		566.92		_	Charles of the last of the las	120	229.85
1000		768.70			561.94	22		399.07	21	225.53
1		764.90		30	557.01			393.59	31	221.23
13/10		761.13			552.13			382.78		216.94
170	_	757-39			547.29		_	377.44	80	208.44
10			16	_	542.50	22		THE RESERVE OF THE PERSON NAMED IN	32	
127		746.35			537.76	and the	73	366.90	3-	204.21
1	_	739.14	1.		533.06			361.70	1	195.81
-				-	R		00	, , , ,	-	95.01

	Gunter's Line of Tangents.									
Deg.	Parts,-	Deg	Parts.	Deg.	Parts.	Deg.	Parts.			
3 4	191.64	36	138.74	4	87.76	1/2	37.95			
33	187.48	1	134.76	177	83.90	1	34-14			
	183.34		130.79	40	76.19	43	30.34			
	179.22	37	122.89	40	72.34	1000	22.75			
34	171.01	1	118.95	1000	68.50	1	18.96			
1	166.93	1	115.02	1	64.67	44	15.16			
1303	162.87	10	111.00	41	60.84	186	7.58			
1 20	158.81	38	107.19	1000	57.01	1	3.79			
35	150.75	1	99.39	100	49.38	45	0.00			
100	142.73	39	95.51	42	45.56	The End.				

On Gunter's Scale, the Tangents begin at o degrees 35 minutes, at the left hand, and are thence numbered on to 45 degrees at the other end of the Scale; and thence backward, at the same divisions, to 89 degrees 25 minutes. For, as the Tangents above and below 45 degrees are equally distant from the Radius, every grand division may be doubly numbered. So that 40 and 50, 60 and 30, 70 and 20, 80 and 10, 85 and 5, are placed at the same grand divisions of the Tangent line.

N. B. The first three numbers (od. 20 m. 25 m. and 30 m.) in the preceding Table of Sines, are superfluous, because they cannot be brought into the Scale.

Gunter's Lines of Rhumbs.

	-	1		1701	1.70
Deg.	M.	Rhumbs.	Sines.	Rhumbs.	Tangents.
0	0	0	Infinite.	0 8	infinite.
2	483	4	1309.21	-	1308.68
5 8	37=		1008.70		1006.60
	264		833.48		828.75
II	15	I	709.76	I 7	701.34
14	34		614.43	No. 1 6.	601.21
16	52 1		537.18	F F 10.1	518.06
19	414		472.51	2 6	446.35
22	30	2	417.16	2 0	382.78
25	183	E Carterior	369.01 326.61	AND FRANCE	325.17 272.04
28	71	33750000	288.95		222.30
30	564		255.26	3 5	175.11
33	45 33 ³ / ₄	3	224.97	3 3	129.80
36	221	STEEL STEEL STEEL	197.64	BIRT ST	85.83
42	111	12000	172.02	ALCOHOLD BY	41.71
45	0	4	150.51	4 4	0.00
47	483	NO STATE	130 21		The Party
50	37		111.81	The T	angents and
53	261	A Property	95.17		nts being e-
55	15	5	80.15	qually d	istant from
59	33	5 (15 C)	66.65	Radius,	they are
61	521	DESCRIPTION OF THE PERSON OF T	54-57	both four	
64	414		43.84	fame poi	
67	30	6	34.38		therefore
70	183		26.16		nd division
73	71	13 3 3	19.11		figured; as
75	564	100	13.21		put to fig-
78	45	7	8.43		one point
18	333		4.73		n points of
84	221	War Best	0.52	on.	pass; and so
87	114	8	0.00	00.	4 4 4
1 90	-			-	-

Gunter's Line of Meridional Parts.

Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	Leg.	Parts.
		16		28		2 3	503.8
0	6.0	10	194.5	20	350.2		508.9
1		1		1 7	354-7	39	
1	12.0	17	207.1	-	359.3		514.1
1276	18.0	-0	213.3	29	363.9		519.3
2	24.0	18	219.6	25	368.2	40	524.5
100	30.0	- Care	225.8	1	373.1		529.7
3	36.0	19	232.3	30	377-7	1000	535.0
7757	42.0	8 2	238.6	1000	382.3	41	540.3
4	48.0	20	245.0	100	387.9		545.6
3 80000	54.1	1 2 3	249.3	31	391.6	1 120	550.9
5	60.1		253.5	1000	396.2	42	556.3
	66.1	21	257.8	1000	400.9	1386	561.7
6	72.1	1000	262.1	32	405.7	10.15	567.1
33	78.2	1	266.4	15000	410.4	43	572.6
7	84.2	22	270.7		415.1	1-19-1	578.1
	90.3	74:00	275.0	33	419.9	7.1	583.6
8	96.3	1000	279.3	200	424.7	44	589.1
1	102.4	23	283.7	40000	429.5	1130	594-7
9	108.4	1000	288.1	34	434.3	0.13	600.3
	114.5	18 18	292.4	1	439.1	45	605.9
10	120.6	24	296.8	17 3	443.9	100	611.6
13.31	126.7	The State	301.1	35	448.8	1 1	617.3
II	132.8	1313	305.5		453.7	46	623.1
	138.9	25	309.9	10,90	458.7	- 500	628.9
12	145.0	1750	314.4	36	463.5	1 . 30	634.7
	151.2	170	318.8	2.53	468.5	47	640.5
13	157-4	26	323.3	10003	473.5	1 100	646.4
1000	163.5	1	327-7	37	478.5	10/18/2	652.3
14	169.7	1	332.2		483.5	48	658.3
1000	175.9	27	336.7	13000	488.5	11/10	664.3
15	182.1	1000	341.1	38	493.6	1 2 00	670.3
1	188.3	1000	345.7		498.7	49	676.4
-			-				

Gunter's Line of Meridional Parts.

Deal	Verte	(Don I	Parts.	Dag	Pares.	Davil	Parts.
Deg.	Parts.	Deg.		Deg.		Deg.	
3	682.5	60.	905.5	68	1126.1	70	1442.0
375	688.7	4	911.5		1134.2		1454-5
50	694.9	200	917.5	UPD 3	1142.3	1	1407.2
	701.1	-	923.7		1150.5	and the	1480.2
200	707.4	61	929.8	69	1158.9	77	1493.4
51	713.7	355	936.0	300	1167.3	30	1506.9
	720.1		942.3		1175.8	103	1520.6
	726.5	,	948.6	1919	1184.4		1534.6
52	733.0	62	954.9	70	1193.1	78	1548.9
	739.5	1000	961.4		1202.0	24	1563.5
1935	746.1	3	967.9	(By	1210.9	1.8	1579-3
53	752.7		974.4		1219.9	-	1593.5
	759.4	63	980.9	71	1229.1	79	1609.0
	766.1		987.6	113	1238.4	100	1625.0
54	772.9	155	994.3	11111	1247.8	1391	1641.3
16.2	779-7	1,1	1.1001	Mel 13	1257.3	1	1657.9
	786.6	64	1007.9	72	121.6.9	80	1675.0
55	793.5		1014.7	3-97.3	1276.7	110	1692.5
SHE	800.5		1021.6	W. Chi	1286.6	15.00	1710.4
11.70	807.6		1028.7		1296.6		1728.8
56	814.7	65	1035.7	73	1306.8	81	1747.8
4 40	821.9		1042.8	1	1317.2	1000	1767.2
SUPP	829.2	21.5	1050.1	1379	1327.7	-	1787.2
57	836.5		1057-3	The said	1338.3	1	1807.8
Total S	849.9	66	1065.7	74	1349.1	82	1829.0
51919	851.3	14865	1072.1	0130	1360.1	1000	1850.9
58	858.8		1079.6	1000	1371.2	199	1873.6
3000	866.4	1	1087.1	LAU I	1382.5	1	1896.9
15/80	874.1	67	1094.8	75	1394.0	83	1921.1
59	881.8		1102.5	13000	1405.7	1	1946.2
311	889.6	100	1110.2	750	1417.6	128 3	1972.2
1	897.5	1	1118.1		1429.7		1999.2

Of the Construction of the plain Scale, Sector, and Gunter's Scale.

As it often happens that these three most useful instruments are badly divided, either through the fault of patterns erroneous in their first construction, or worn out by much use, or by the ignorance or neglect of the divider, it was thought that rules and Tables for graduating them accurately, and examining those which have been already made, might be very acceptable both to the workman and young mathematician desirous of projecting them, or to any person who is obliged to use them.

The foundation of these, and indeed of most other scales, is a line of equal parts, so subdivided as that one of the least of these parts shall scarce take up a visible space, as into thousand parts of an inch, or even more minute; so

that

that an error of one unit in the last place, in taking off any distance, may not affect the graduations of your intended instrument. Furnished with such a scale, and a beam compass with a regulating screw at one end, you may lay down any number, of four, or even sive places of sigures, with great exactness.

The best way of dividing a right line into any possible number of parts, and that which is practised by our best dividers of mathematical instruments, is by help of diagonal lines; both because the smallest diagonal subdivisions are as perceptible on such a scale as the largest, and that this is the most simple method of subdividing, and may be extended further than any other way yet known.

In order to have an exact diagonal fcale, it is absolutely necessary that the parallel lines, through which the diagonal lines are drawn, be equidistant among themselves; that the diagonals

be so likewise; and that, in the two outermost parallels in which the diagonals terminate, the ends of each diagonal must be just even with the opposite ends of those next to it on each side; that is, in a line perpendi-

cular to the parallels.

In one inch, 25 diagonal lines may be very eafily placed, and confequently 50 in two inches: and if these diagonals run through 20 equidiftant parallel lines, they will divide every two inches of length of the diagonal scale into 1000 equal parts, which will be quite fufficient for graduating the lines of Rhumbs, Chords, Sines, Tangents, and Secants, on common plain fcales, where the radius (or 60 degrees of the Chords) takes up only two inches in length of the whole line: and to that line of Chords, the Rhumbs, Sines, Tangents, and Secants, are adapted.

There is generally another line of Chords of 3 inches radius on these scales, fcales, at the right-hand end; and just above that line is a line marked M. Lon. for shewing how many geographical miles are contained in a degree of longitude in any given parallel of latitude. To lay down these two lines, there must be a diagonal scale containing 1000 parts in 3 inches; and these parts or divisions must be continued on to 1420, which will be sufficient for the purpose, as the whole length of each of these two lines takes up only 1414.21 parts.

But, for laying down the abovementioned lines of Rhumbs, Sines, Chords, Tangents, and Secants; where the radius 2 inches contains 1000 equal parts, and the length of the Tangent line (in which there are only 80 degrees laid down) is 11\frac{2}{10} inches, the diagonal parts or equal divisions must be carried to 5760; of which, 5671.28 will be equal to the Tangent of 80 degrees, and 5758.77 to the Secant of the same number of degrees; as shewn by the Tables of Natural Tangents and Secants.

For Gunter's lines of Numbers, Rhumbs, Sines, Versed Sines, Tangents, and Meridional Parts, every one of which takes up 22 ½ inches of his two foot scale, a diagonal scale must be first made, in which 22 ½ inches shall contain 2000 equal parts: and, for this purpose, there will be no need for more than 10 equidistant parallel lines along the scale, and one inch of its length will not include quite 8 equidistant diagonal lines.

For Sectors, of whatever length the radius of the Chords (or of 60 degrees) be, which is generally very near the whole length of the Sector when shut, a diagonal scale must be prepared, in which that length shall contain 1000 equal parts.—The distance between these long parallels should not be less than a tenth part of an inch: otherwise the eye cannot well estimate the decimal parts expressed in the Tables,

which

which are hundredth parts of the fpaces between the long parallel lines, in all except the Dialing Tables of Latitudes, Hours, and Inclination of Meridians, and in the Table of Gunter's Meridional Parts; in which, the fpaces between the parallels are fupposed to contain only ten parts each.

Being thus provided with proper diagonal scales, patterns for graduating all the lines on Scales and Sectors may be made in the following manner.

Having drawn the lines on your intended brafs pattern, analogous to those which must contain the graduations on scales, fix your diagonal scale close by the upper edge of the pattern to be graduated: and then applying one side of a square along the upper edge of the diagonal scale, and the other side directly across both that scale and the pattern, cut the first division of each line on the pattern directly even with the very beginning of the diagonals; "and

and each division after that, against the fame number of parts, found among the diagonals, as answer to the number of parts in the Tables belonging to each degree in the respective lines: and, where the lines are long enough to admit of the quarters of degrees, these may be put in, according to the numbers in the Tables-But, in the common plain scales, where the length of the radius of the Chord line is only two inches, the spaces taken up by the degrees are too fmall to allow of fubdivisions, except in the Tangents and Secants after the 50th degree.

Thus, in the Tables of Natural Chords, Sines, Tangents, and Secants, against the first degree is 17.45 parts both for the Chords and Sines, and 17.46 for the first degree of the Tangents. Therefore, finding those parts among the diagonals, and laying the cross edge of the square to them, cut the first degree of these lines on the pattern,

pattern, close by the said edge of the square: and proceed on in the same manner with all the rest of the degrees in the several lines, cutting them right against the same number of parts found among the diagonals which the Tables shew to belong to them respectively. Thus, the 20th degree in the line of Chords must be cut even with 347.29 parts among the diagonals; the like degree of the Sines even with 342.02 parts; and the same degree of the Tangents even with 363.97 parts in the diagonal scale.

Where the Sines end on the plain scale, the Secants begin; namely, even with 1000 parts among the diagonals. But the Secant degrees are so small at first, that there can be no putting in any of them less than the 10th, which answers to 1015.43 parts among the diagonals; and the next that can be put in is the 15th, which answers to 1035 28 parts: after which, all the degrees as far as 80 may be put

into the line of Secants, cutting them even with the fame numbers of parts found among the diagonals as fland against them in the Table of Natural Secants.

On Sectors, there are two Tangent lines on each leg. The first of these goes only to 45 degrees, the length of the leg admitting of no more: and the others begin at 45 degrees, at a fourth part of the length of the leg from the center of the joint to that part near the end of the leg where the 45th degree of the former line stands, and goes on generally to 76 degrees. The first of these which goes from o degeees to 45, is called the lower Tangents; and the last, which goes from 45 to 76, is called the upper Tangents.

The lower Tangent degrees are laid down by the diagonal fcale according to the numbers found against them in the Table of Natural Tangents; 1000 parts of the diagonal fcale taking up just as much length as the whole 45

degrees

degrees of these Tangents do. as the radius of the upper Tangents is only a fourth part of the length of that of the lower ones, in order to lay them down on the Sector-pattern, all the numbers in the Table of Natural Tangents above 45 degrees must be divided by 4, and their quotients fought for, among the diagonals, for laying down the respective degrees of these Tangents. To fave the operator this trouble, I have taken it, and made the following Table, which confifts of these quotients, and consequently contains the number of parts (to be found among the diagonals) for dividing the line of upper Tangents, the 76th degree of which is even with 1002.69 parts of the diagonal scale.

Supplemental Table, for laying down the Line of upper Tangents on Patterns for dividing the Lines on Sectors.

	and the contract of		1254 3	4110	AL RIDO	ELL	50-001
Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	Deg.	Parts.
45	250.00	3 4	328.77	1 0	441.87	4	626.33
	252.19	53	331.76	1357	446.41	SEC.	634.46
8000	254.40		334.79	61	451.01		642.87
	256.63	34.7.3	337.85		455.69	69	651.27
46	258.88	138	340.36	1023	460.44	WE ST	659.86
10.70	261.15	54	344.09	1200	465.27		668.65
1515	263.44	-	347.27	62	470.18	10120	677.65
12.53	265.51	19.	350.49		475.17	70	686.87
47	268.09		353-74	1000	480.24	100	696.31
35.15	270.45	55	357.04		485-40	7.31	705.98
	272.83		360.37	63	490.65	-	715.89
	275.23	1972	363.75	HIE	495.99	71	726.05
48	277.73	1	367.17	No.	501.42	16/5	736.47
J. 1	280.10	56	370.64		506.95	41.5	747-17
194 (2)	282.57	-	374-15	64	512.57	33 348	758.15
19976	285.07	100	377.71		518.30	72	769.42
49	287.59	1	381.31	13.5	524.13	17	781.00
2570	290.14	57	384.95	1	530.07	11990	792.70
1000	292.71	1000	388.67	65	536 13	133	805.13
137	295.31	1000	392.42		542.29	73	817.71
50	297.94	-0	396.22		548.57	1	830.66
1000	300.59	58	400.08	1	554.98	1 13	843.98
200	303.27	18 335	403.99	66	561.51	1 366	857.71
100	305.98	1000	407.96	1000	568.17	74	871.85
51	308.72		411.99	1 35	574.96	1-30	886.43
1000	311.49	59	416.07	1	581.89	1	901.47
16187	314.29	1000	420.21	67	588.96	1000	916.99
1	317.12	100	424.41		596.18	75	933.01
52	319.98	160	428.68	100	603.55		949.57
100	322.88	60	433.01	100	611.08	1.10	966.68
-	325.81	1	437-41	68	618.77	1	984.38

The

The diagonal scale remaining where it did, for dividing the line of lower Tangents, [See the Remark farther on] cut the 45th degree by the square against 250 parts found among the diagonals, having put the cross side of the square to it: so this second line of Tangents shall begin just at a fourth part of the length of the former line from the center of the joint; and then proceed with the rest of the degrees from 45 to 76, cutting them in the pattern even with the same number of parts found among the diagonals as belong to them in the preceding Table.

The Secants on the Sector begin also at a fourth part of the length of the leg from the center of the joint; and therefore, to lay down the degrees of the Secants on the Sector pattern, all the numbers in the Table of Natural Secants from o to 75½ must be divided by 4, and their quotients taken among the parts on the diagonal scale. The following Table, for this purpose, is the quotients of the numbers in the Table of Natural Secants divided by 4.

The Secants of 75³ degrees would reach to 1015.55, which is 15.55 parts more than the diagonal scale contains.

Supplemental Table, for dividing the Line of Secants on Sector Patterns.

Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	Deg.	Parts.
0	250.00		315.12		304.85		433-17
10	253.86	38	317.25	47	366.57	55	435.86
15	258.82	1700	319.44	-	368.30	100	438.00
16	260.07	39	321.69	323	370.05	700	441.38
17	261.42	10000	323.99		371.82	1	444.20
18	262.86	40	326.25	48	373.62	56	447.07
19	264.40	1200	327.55	11,653	375.44	10 33	449.99
20	266.01		328.77	100	377-29	10000	452.95
21	267.78		330.00		379.16	-	455.96
22	269.63	41	331.25	49	381.06	57	459.02
23	271.59		332.52		382.99	1000	462.13
24	273.66	1	333.80	1,330	384.95	1 113	465.29
25	275.84		335.09	1000	386.92	0	468.50
26	278.15	42	336.41	150	388.93	58	471.77
27	280.58	650	337.74	THE OW	392.79	-313	475.09
28	283.14	1	339.08		393.03		478.47
29	285.84	12 135	340.45	1115	395.13		481.90
30	288.67	43	341.83	51	397-23	59	485.40
No.	290.15	-10	343.23	1	399.41	1	488.95
31	291.66	2000	344.64	1 Delle	401.60	1	492.57
	293.21		346.08	1 1 100	403.81	1	496.25
32	294.79	1 44	347-54	52	406.07	60	500.00
	296.42	1000	349.01	100	408.35	1 - 17	503.81
33	298,09	22.00	350.51	1000	410.67	1300	507.69
	299.80	13.0	352.02	137754	413.02	1	511.64
34	301.55	45	353-55	53	415.41	61	515.67
San San	393.35	100	355.10	392	417,83	14 92	519.76
35	305.19		356.68	100	420.29	1	523.93
1	307.08	1,	358.25	9.19	422.79	1	528.18
36	309.02	46	359.89	54	425.32	62	532.54
	311.00	100	361.52	1	427.90	1	536.92
37	313.03	1	363.18	1	430.51	1000	541.43

E TO	The	Supp	lementai	Tabi	le conclu	ded.	
Deg.	Parts.	Deg.	Parts.	Deg.	Parts.	Deg.	Parts.
6 ₃	546.00 550.67 555.42 560.29 565.24 570.29 575.45 580.70 586.07 591.55 597.14 602.85 608.69	66 67 68	614.62 620.74 626.96 633.32 639.82 646.48 653.28 660.24 667.35 674.66 682.12 689.77 697.61	70 71 72	705.63 713.86 722.30 730.95 739.83 748.93 758.29 767.89 777.75 787.89 798.30 809.02 820.01	73 74 75	831.38 843.05 855.07 867.46 880.23 893.40 906.99 921.01 935.49 950.46 965.92 981.93 998.48

On Sectors, the line of Lines (which is divided into equal parts) and the lines of Chords, Sines, Tangents, and Secants, are laid down on both the legs. They are all drawn from the center of the joint, and ought to be strictly at equal angular distances from each other, at the other ends of the legs. So that, whether the Sector be open or shut, the same opening of the compasses that reaches cross-wise from 10 on the line of Lines on one S 4

leg to 10 on the other (at the ends furthest from the joint) should reach from 60 to 60 degrees of the Chords, from 90 to 90 of the Sines, from 45 to 45 of the lower Tangents, from end to end of the upper Tangents, and likewise from end to end of the lines of Secants. I generally find all these very well laid down, except the lines of upper Tangents and Secants; which, for want of this precaution, are troublesome to use on most Sectors.

I apprehend that Sectors would be much more convenient than they now are, if their lines of Chords contained all the degrees of o to 90. For then, in laying down an angle of any number of degrees less than 90, one opening of the compasses would do; whereas, as they now are, it requires two operations to lay down an angle of any number of degrees above 60. And besides, if the line of Chords contained all the 90 degrees, the lower Tangents, instead of ending at 45 degrees,

grees, would go on to 55, by carrying them out a very fmall space beyond the end of the Chords: and also, the line prolonged on which the Sines are laid down (they going no further than 60 degrees of the Chords) would receive thereon all the Secants. as far as 45 degrees; fo that, all these Tangents and Secants might be taken off without a fecond opening of the Sector, as is customary in common ones; which would be a very great convenience to those who use it. And then, beginning the line of upper Tangents at 55 degrees, and of upper Secants at 55, with a fourth part of the Tabular numbers from the center of the joint, both Tangents and Secants might be carried on to 80 degrees.-For these purposes, the diagonal scale must be so divided, as that 1414.2 of its equal parts shall be equal in length to the whole line of Chords; and then, 1440 of these parts would extend but a very little further. And the

the line of Lines (which is a line of equal parts) must be so divided, as that ten of its grand divisions, to which the numeral figures are set, shall be precisely equal in length to so degrees of the line of Chords.—In common Sectors, s inches long when shut, each grand division of the line of Lines is subdivided into 20 equal parts, every one of which is supposed to be subdivided into 5; by which means, the 10 grand divisions of that line are supposed to contain 1000 equal parts, viz. the tabular number answering to the Radius, or so degrees of the Chords.

The annexed small Table is for laying down the line of Polygons on Sectors where the line of Chords goes on to 90 degrees. Thus the figure (or number) 4 must stand even with

No	Parts.
4	1414.21
5	1175-57
0	1000,00
7	867.89
8	765.36
9	684.04
10	618.03
11	563.47
12	517.63

1414.21 parts of the diagonal scale; the figure 5 against 1175.57 parts; the figure 6 against 1000.00 parts; and so on to 12, as in the Table.-But, by these numbers, the line of Polygons could be laid down only from 6 to 12 on common Sectors, where the line of Chords goes no further than 60 degrees.

But, for those who chuse to make Sectors in the common way, the hereannexed Table shews the

numbers in the diagonal fcale by which the line of Polygons is to be laid

No l	Parts.	Ì
4	1000,00	
5	831.25	į
6	707.11	1
7	613.69	i
8	541.19	į
9	483.69	1
10	437.01	١
11	402.73	۱
12	366.02	ı

down. Thus, the figure 4 must anfwer to 1000.00 parts of the diagonal scale, the figure 5 to 831.25 parts, the figure 6 to 707.11 parts, the figure 7 to 613.69, and fo on to the last division

REMARK.

d down only from 0 to 12.

As all those lines which are properly called Sectoral Lines *, terminate in an arch whose center is the center of the joint, the diagonal scale ought to be fo placed, as that the long parallel lines upon it may be firictly parallel to each sectoral line on the pattern to be divided from the scale: and also, that when one fide of the fquare is laid close to the upper edge of the diagonal scale, and the other side of the fquare (that lies across the scale and pattern) to the center of the joint, that fide of the fquare may then be at the beginning of the diagonal divisions on the scale. Then all the divisions cut by that fide of the fquare will be true, and each division at right angles to its own respective line. Without this precaution, the innermost fectoral lines

^{*} The lines which are drawn from the center of the joint almost to the other ends of the legs.

would not be divided to their whole proper lengths: and so they would not all have the same radius, and consequently the measures taken off from them by the compasses would not

agree together.

But, when the Sector pattern is truly divided according to this method, it may be applied close to the fide of the Sector to be divided from it; because, as the lines on the intended Sector will be parallel to the like lines on the pattern, one fide of a square may be applied to the upper edge of the pattern, and the other fide will lie across both the pattern and Sector at right angles: and then, by applying that fide to each division of the pattern, and cutting each fuch division close by it on the Sector, all the divisions on the Sector lines will be true, although they be not cut at right angles to those lines to which they belong respectively.

As the dialing lines of Latitudes, Hours, and Inclinations of Meridians, have no dependence on the radius of any of the above-mentioned lines, and are indifcriminately put upon Sectors and plain Scales, they may be made of any convenient length where there is fufficient room. But, as they depend upon one another, they must be all laid down from one scale of equal parts. The lines of Hours and Inclination of Meridians are of equal length, which ought to be six inches at least; and the length of the line of Latitudes is equal to that of four hours and an half, in the line of Hours.

To lay down these lines, you must have a diagonal scale of such a length, as that 1414.2 of its equal parts shall contain as great a length as the line of Hours is intended to be of. And then, the same number of parts, which stand in the Tables against the degrees of Latitudes, Inclination of Meridians, Hours and parts of an Hour, must be found among the diagonals; and the respective divisions in the lines cut by the

the fide of a square applied to these parts in the diagonal scale, after it has been fixed close to the edge of that on which these lines are to be divided.— Thus, 10 degrees in the line of Latitudes (reckoned from the beginning thereof, which must be even with the beginning of the diagonal divisions) must stand even with 241.9 parts among the diagonals: 10 degrees of the line of Inclination of Meridians must be even with 212 parts of the diagonals, the hour of I against 298.8 parts; and so on, as in the Tables.

Gunter's Lines, of Rhumbs, Numbers, Sines, Versed Sines, Tangents, and Meridional Parts (on the scale that goes by his name) are all laid down by one diagonal scale of equal parts; and 2000 of these parts must include a length equal to the whole length of the line of Numbers, which consists of 18 grand divisions of different lengths, marked with the numeral sigures 1, 2, 3, 4, 5, 6, 7, 8, 9,

1, 2, 3, 4, 5, 6, 7, 8, 9, 10; the first grand division being the space between the first 1 and the first 2, and the last between the fecond 9 and the 10.-On this scale, the grand divisions from the first 1 to the second 1 are generally fubdivided into 10 parts each, althor they might bear four times that number from 1 to 3; 20 divisions each from the first figure 3 to the figure 7, and after that, only 10 divisions each, to the fecond figure 1, which is at the middle of the line. The grand divifions in the other half of the line are. of the same lengths with those in the former half; but in the latter half of the line, each grand division from the figure 1 to 3 is fubdivided into 50 parts; from 3 to 7, into 20 parts each; and from 7 to 10 at the end of the line, each grand division is also subdivided into 20 parts only, on account of the shortness of the spaces.

Being provided with a diagonal scale of 2000 equal parts, which include a length

length equal to the intended length of the like of Numbers, fix the lower edge of it close to the upper edge of the scale intended to be divided, and applying one fide of the square to the upper edge of the diagonal scale, and the other fide to the beginning of the diagonal divisions, cut the first cross line in the line of Numbers (where the first 1 is to stand) close by that side of the square; and then, moving the square onward till the same side of it comes to the number of parts among the diagonals which answer in the Table of Gunter's Numbers to the intended subdivisions between 1 and 2, cut these divisions accordingly, in the line of Numbers, close by the fide of the fquare which was fet to the parts in the diagonals answering to these fubdivisions; and so on till the whole line be divided.

Thus, the Tables shew, that the figure 2, at the end of the first grand division (marked in the Table 2.00)

must answer to 301.03 parts found among the diagonals; the divisionline for the figure 3 must answer to (or fland even with) 477.12 parts, the division-line for 4 against 602.60 parts; and fo.on, to the end of the first half of the line, where the fecond figure 1 stands against 1000. The other half of the line is divided the fame way, by the other 1000 diagonal parts of the scale.—The subdivisions which the operator chuses to put into this line must be cut even with the like number of parts found among the diagonals as answer to them in the Table.

In order to divide the lines of Rhumbs, Sines, Versed Sines, Tangents, and Meridional Parts, on Gunter's Scale, the diagonal scale must be placed the contrary way to what it was for dividing the line of Numbers, because all these lines are divided backward, or from the right hand toward the left. Therefore, turn the diagonal

diagonal scale, and placing its contrary edge to the upper edge of the scale to be divided, fix it so, as that, when the square is applied, the beginning of the diagonal divisions shall stand just even with the end of the line of Numbers: and then, applying the cross side of the square to the same number of parts among the diagonals which answer to the degrees, half degrees, Sec. in the Tables of Rhumbs, Sines, Versed Sines, Tangents, and Meridional Parts, cut these divisions in the proper lines close by that side of the square.

As Tables of this kind were never all in print before (at least so far as I ever heard of) and they serve not only for dividing the lines accurately on Scales and Sectors, but also for examining and proving whether the Scales and Sectors which are sold at shops be accurately divided or not, I hope they will be acceptable, not only to the makers of these instruments in

T 2 general,

232 SELECT EXERCISES.

general, but also to those who use them.

How to examine the Divisions of the Lines on Sectors and Scales.

If the line of Lines (which is a line of equal parts) on the Sector be accurately divided, which may be easily tried with a pair of compasses, it will serve for examining all the other lines which are drawn from the center of the joint; for all their divisions ought to answer to the equal parts of that line, as they do to the like equal parts of a diagonal scale from which they are supposed to be laid down according to the preceding directions.

Whatever the length of the Sector be, if the line of Chords upon it goes no further than 60 degrees, the line of Lines contains 10 grand divisions, marked 1, 2, 3, 4, 5, 6, 7, 8, 9, 10: but if the Chords go on to 90, the line of

Lines

Lines ought to contain 1414.2 equal parts, supposing each grand division to be subdivided into 100.

On Sectors fix inches long, each grand division of this line is subdivided into 20 equal parts; and if each of these parts be supposed to be subdivided into 5 (which is left to be estimated by the eye), each grand division will contain 100 parts; and confequently the whole ten will contain 1000.

On Sectors 12 inches long, these grand divisions are seldom subdivided into more than 20 parts each, althor there might very well be 50, and then each part could be easily divided into two by estimation of the eye; and confequently the whole line would contain 1000 equal parts.

This being understood, set one foot of the compasses in the center of the joint, and extending the other foot to the same number of parts in the line of Lines as agree with the tabular number

number of parts for any degree of the Chords, Sines, Tangents, or Secants, turn that foot to the line of degrees you want to examine; and if it falls into the degrees answering respectively to the tabular numbers, the line is

truly divided; otherwise not.

But if the Sector be too long for the points of the compasses to take in the whole length of the line of Lines between them, open it so far, as that the compasses may reach conveniently across the Sector from 10 in the line of Lines on one leg to 10 in the line of Lines on the other: and then, taking the tabular numbers of parts in the compasses across the Sector, in each line of Lines which answer to the tabular number of parts for each degree of the line of Lines, Chords, Tangents, or Secants, apply that extent across the Sector to the like degrees of these lines: and if the points of the compasses fall directly into these graduations, the lines are accurately diyided; otherwise not,

To examine the lines on plain Scales or Gunter's Scales, open the Sector fo, as that the length of the radius of the Chords, or whole length of the line of Lines, taken in the compasses, their points shall then reach from 10 in one line of Lines on the Sector to 10 on the other: and then, taking the tabular numbers for the degrees of the Chords, Sines, or Tangents, across the Sector from one line of Lines to the other, fet one foot of the compasses in the beginning of the line to be examined, and the other foot forward among the degrees of that line; and if it falls just into each given degree, the line is truly divided; but falfely if it does not.

Thus you may examine the whole line of Lines, the line of Chords to 60 degrees, and the Tangents to 45: but, in order to examine the degrees of the Tangents above 45, and all the degrees of the Secants, you must take the following method.

T 4

The

The Sector remaining at the same opening as before, take the supplemental tabular numbers in your compasses across the Sector from one line of Lines to the other, which answer to the respective degrees of the Tangents and Secants, and apply that extent across the Sector to the like degrees in these lines: if the compasspoints fall exactly into them, the lines are truly graduated.

For Gunter's lines of Numbers, Rhumbs, Sines, Versed Sines, Tangents, and Meridional Parts, set one foot of the compasses in the beginning of the line of Numbers (at the first sigure 1) and open the compasses till the other foot falls into the second 1 at the middle of the line. Then open the Sector so, as that the same opening of the compasses shall reach from 10 in the line of Lines on one leg to 10 in the like line on the other. Then, taking the tabular numbers in your compasses across the Sector in these

fwer to the divisions of the lines you want to examine, apply that extent forward from the left-hand end of the line of Numbers, but backward from the right-hand end of the other lines; and if these divisions or graduations are found by the compasses to agree with the tabular numbers belonging to them, the lines are truly divided; otherwise not.

N. B. In the Sectoral Lines, which proceed from the center of the joint, each has three parallel straight lines drawn for limiting the greater and lesser divisions: in each of these, it is the innermost line to which the points of the compasses must be applied; as that is the only line of the three that proceeds directly from the center of the joint.—I have dwelt the longer on this subject, because these instruments are in the hands of every Mathematician, and it is of the utmost importance to have them rightly divided.

Having

Having shewn how to divide and examine the Lines on Scales and Sectors, it is natural to suppose that the divider would be willing to know, not only how to examine the Tables themselves, but also how to construct them.

The Tables of Natural Sines, Tangents, and Secants, are copied from those in Sherwin's Tables thereof.

The right Sine of an Arc is half the Chord of double that Arc. Therefore, double the Natural Sine of half the given Arc (or number of degrees) and that will be the Chord of the whole Arc, or number of degrees required; which, in the Tables, is carried no further than to 90.

The construction of the Table of Natural Rhumbs is the same as that of the Chords.

The Table of Numbers is only the logarithms of these Numbers. The logarithm of unity (or 1) being nothing, is not inserted in the Table: the logarithm of 1.01 (the same as that of

which may be put down 4.32; the logarithm of 1.02 is 86002, which may be put down 8 60; and fo on, for laying down the line of Numbers on Gunter's Scale.

For the same scale, the Sines are the respective logarithmic Sines subtracted from radius, or the Co-secants less radius.

The Tangents (for the same scale) are the logarithmic Tangents, rejecting radius.

The Versed Sines are double the logarithmic Secants of half the given number of degrees.

For the Meridional Parts, divide the Meridional Parts in any Table thereof by 60.

For the Sine Rhumbs, having found the degrees in every point and quarter-point of the Mariner's Compass, find the logarithmic Sines thereof, and take their complements arithmetical from radius, or from 8 points.

The

The same holds good for Tangent Rhumbs, remembering they extend only to 4 points on the scale, and that both the Rhumb and its complement stand on the same point of the line; a logarithm and its reciprocal being equally distant from radius on the opposite sides.

By these rules I have made the foregoing Tables from the now common Tables of Logarithms, Sines, Tangents, Secants, and Versed Sines, with all the care and accuracy that I possibly could, without regarding the time and pains required to construct

them.

Of the plain Scale, Sector, and Gunter's Scale.

The lines on the plain Scale are useful in most branches of the mathematics, and its use in each of them is to be found in almost every treatise of the practical mathematics.

The

The Sector is principally useful as a universal plain Scale, sitted to any radius within the compass of its opening; only observing that the equal Parts, Sines, Chords, and Tangents under 45 degrees, are not taken along one line, as on the plain Scale, but across the Sector from any degree on one leg to the same degree of the same line on the other.

The Gunter's lines are for readily working proportions; in which, regard must be had to the terms, whether arithmetical or trigonometrical; that the first and third term may be of the fame name, and the fecond and fourth of the same name likewise: then, raifing your proportion according to these rules, take the extent on their proper line, from the first term to the third, in your compasses; and applying one point of the compaffes to the fecond, the other applied to the right or left according as the fourth term is to be more or less than the the second, will reach to the fourth, Three examples will explain this.

If 4 yards of cloth cost 18 shillings,
Then 32 yards
will cost?

2.

As radius
to the hypothenuse 120,
So the sine of the angle opposite the base 30° 17'
to the base.

As the co-fine of the latitude 51° 30'

(= the fine of 38° 30')

is to radius,

So is the fine of the Sun's declin. 20° 14'

to the fine of the Sun's amplitude.

Note, The Line of Numbers (on Gunter's Scale or on the Sector) is intended to supply the Table of Logarithms. Those of Sines, Tangents, (and Secants, which are found in the same place with their Co-sines) and the Versed Sines, supply the places where their logarithms are necessary in calculation.

Now,

Now, in the first question, on the Line of numbers take in your compasses the distance between 4 and 32; apply one foot thereof on the same line at 18, and the other will reach to 144, the shillings required.

In the fecond, the distance between radius (or the Sine of 90°) and the Sine of 30° 17', taken from the Line of Sines, and one foot applied to the hypothenuse 120 on the Line of Numbers, and the other applied to the left (as the legs of a right lined and right angled triangle are less than the hypothenuse) that foot will reach to 60°, the length of the base required.

The third is wrought wholly on the Line of Sines. The distance between the Sines of 38° 30′ and 20° 14′ taken in your compasses, set one foot on the radius or Sine of 90°, and the other will reach to 33° 4, the Sun's amplitude required.

In the fame manner are used the Tangents, Secants, and Versed Sines,

in proportions where they are required: though fometimes the Versed Sine is taken when the other foot stands on the Line of Sines, as in finding the azimuth, &c. which is eafily performed when the art of raising the proportion is known.

A Short Account of the Logarithms.

The invention of Logarithms, fays the great Dr. Halley, is justly esteemed one of the most useful discoveries in the art of numbers. This affertion is corroborated by the united testimonies of every learned mathematician who has made mention of them, from the time of their first publication to this day.

Lord Nepair, of Merchiston in Scotland, in the year 1614, published the first specimen of these useful numbers, under the title of Mirifici Logarithmorum Canonis Descriptio; a book which was received with transport in the mathematical world. And tho' the author had referved the method of conftructing his Table, till the sense of the learned upon his invention should be known; yet Kepler, Speidell, and others, abroad and at home, laboured at the computation of Logarithms, and constructed small tables thereof, conformable to the plan of Lord Nepair.

The description and use of the Canon being in Latin, induced Mr. Edward Wright, a learned mathematician of those times, and to whom we owe the principles of that falfely called Mercator's Sailing, to translate it for the benefit of fuch of his pupils and others, who not understanding the original, were yet defirous of being acquainted with fo valuable a performance. This he effected with great care; but unhappily dying before the publication, that office devolved to his fon, Samuel Wright, who, with the " before affiftance

affistance of Mr. Briggs, then Geometry Professor at Gresham College, and whose name shines with great lustre in a history of Logarithms, published it in the year 1616 or 1618 *.

This translation was dedicated by the publisher to the East India Company, who, it feems, had employed Mr. Edward Wright in mathematical affairs: in which dedication he fays, " his father's care to make the tranf-" lation bear a true refemblance of " the original was fo great, that he " procured the author's perufal of it; who, after great pains taken therein, " gave approbation to it. And it is " apparent enough that he (Edward " Wright) esteemed it, and intended " to have recommended it as a book " of more than ordinary worth, espe-" cially to feamen. But shortly after " he had it returned out of Scotland, it pleased God to call him away,

My copy is printed at London for Simon Waterson, " before affiftance

" before he could publish it." Thus we see that the edition of Edward Wright had fome advantages over the first edition, from the revisal of the inventor, who also wrote a preface to the same; which, as it sets forth the purfuits that led to this discovery, and as the book is very rare, I shall insert in the words of its noble author, together with a specimen and description of the work itfelf.

" The Author's Preface to the admirable " Table of Logarithms.

" Seeing there is nothing, right " well beloved students in the mathe-" matics, that is fo troublesome to " mathematical practice, nor that doth " more molest and hinder calculators, " than the multiplications, divisions, " fquare and cubical extractions of " great numbers, which, besides the " tedious expence of time, are for the " most part subject to many slippery " errors, I began therefore to confider " in

Delina to a

" in my mind, by what certain and " ready art I might remove those hin-" drances; and having thought upon " many things to this purpose, I found " at length some excellent brief rules, " to be treated of (perhaps) hereafter. " But amongst all, none more profit-" able than this, which, together with " the hard and tedious multiplica-" tions, divisions, and extractions of " roots, doth also cast away from the " work itself even the very numbers " themselves that are to be multi-" plied, divided, and refolved into " roots, and putteth other numbers " in their places, which perform as " much as they can do, only by ad-" dition and fubtraction, division by " 2 or division by 3: which secret in-" vention being, as all other good " things are, fo much the better as it " shall be the more common, I thought " good heretofore to fet forth in Latin " for the public use of mathemati-" cians. But now, fome of our coun-" trymen

" trymen in this Island, well affected " to these studies, and the more pub-" lic good, procured a most learned " mathematician to translate the same " into our vulgar English tongue; " who, after he had finished it, sent " the copy of it to me, to be feen and " confidered of by myfelf. I having " most willingly and gladly done the " fame, find it to be most exact, and " precisely conformable to my mind, and the original. Therefore, it may " please you who are inclined to these " fludies, to receive it from me and " the translator with as much good-" will as we recommend it unto you. " Fare ye well."

And in his dedication to Prince Charles (afterwards King Charles I.) he fays, "This his new invention "doth clean take away all the diffi-"culty that heretofore hath been in mathematical calculation; and is fo fitted to help the weakness of me-"mory, that, by means thereof, it is U 3 "eafy

" eafy to refolve more mathematical

" questions in one hour's space, than

" otherwise by that wonted and com-

" monly received manner of Sines,

" Tangents, and Secants, can be done

" even in a whole day."

The following is a specimen of the first page of the Canon, in which I have, however, corrected the typographical errors.

reprecisely conformable to my mind,
the elegenal. Therefore, it may
the please you sone are incheed to these

findies, to receive it from me and

to the transferon with as much good.

" Fare ye well."
And in his dedication to Prince

Charles (alterwards King Charles I.) he fays "This his new invention

doth clean take away all the diffi-

" culty that herejofore hath been in

* mathematical calculation pand is for

" fitted to help the weakness of piece

" more, that, by means thereof, it is

Tes h

	Sines.	Logarith.	Differen.	Logar.	Sines.	1
0 1 2	0 291 582	Infinite. 8142568 7449421	Infinite. 8142568 7449421	.0	1000000.0	60 59 58
3 4 5	873	7043956	7043956	·4	999999.6	57
	1164	6756275	6756274	·7	999999.3	56
	1454	6533131	6533130	1.1	999998.9	55
6 7 8	1745	6350810	6350808	1.6	999998.6	54
	2036	6196659	6196657	2.2	999998.7	53
	2327	6063129	6063126	2.8	999997.4	52
9 10 11	2618 2509 3220	5945345 5839986 5744676	5945342 5839982 5744671	3·5 4·3 5·2	999995.9 999995.0	51 50 49
12	3491	5657665	5657659	6.2	999994.0	48
13	3781	5577622	5577615	7.3	999992.8	47
14	4072	5303514	5503506	8.4	999991.7	46
15	4363	5434523	5434513	9.6	999990.5	45
16	4654	5369984	5369973	10.9	999989.2	44
17	4945	5309360	5309348	12.3	999987.8	43
18	5236	5252202	5252188	13.8	999986.3	42
19	5527	5198136	5198121	15.4	999984.7	41
20	5818	5146843	5146826	17.0	999983.1	40
21	6109	5098054		18.7	999981.3	39
22	6199	5051534		20.5	999979.5	38
23	6690	5007083		22.4	999977.6	37
24 25 26	6981 7272 7563	49 ⁶ 45 ² 4 49 ² 37 ⁰ 3 48844 ⁸ 3	4923676	26.5	999975.6 999973.6 999971.4	36 35 34
27 28 29	7854 8145 8436	4846743 4810376 4775286	4810343	33.2	999969.2 999965.8 999964.4	33 32 31
30	8726	4741385	4741347	38.1	999961.9 Deg.	[.Vin

The columns marked Sines are the natural fines answering to the degree and minute of the first and last columns; the adjoining ones their logarithms, and the middle one the differences between the logarithms. The Author explains every one of these columns; but I shall only infert, in his words, what relates to those containing the logarithms.

" § 11. The 3d column containeth " the logarithms of the arches and

" fines towards the left hand.

" § 13. And they are also the loga-" rithms of the complements of the " arches and fines towards the right " hand, which we call Antilogarithms.

" § 14. The fifth column containeth

" the logarithms of the arches and

" fines towards the right hand.

" § 16. They are also the antiloga-" rithms of the arches and fines to-

" wards the left hand, or the loga-

" rithm of the complements.

" § 17. Laftly, the 4th or middle " column containeth the differences " between " between the logarithms of the 3d

" and 5th columns; and fo this co-

" lumn is twofold, abounding and

" defective.

"§ 18. Those differences are abound-

" ing which arise out of the subtrac-

" tion of the logarithms of the fifth

" column from the logarithms of the

" third column.

" § 19. But the differences arifing

" by fubtraction of the logarithms of

" the third column out of the loga-

" rithms of the fifth column, are de-

" fective; which therefore are less

" than nothing.

" § 20. The abounding differences

" are called the differential numbers

" of the arches towards the left hand.

" § 22. And are also the logarithms

" of the tangents of the left hand

" arches.

" § 23. But the defective differences

" are called the differential numbers

" of the right hand arches.

" § 25. And are also the logarithms " of

" of the tangents of the right hand " arches."

And as admonitions, amongst others, he gives the following:

" if you make the logarithms of the 3d column defective, fetting before

" them this mark -, they shall be

" made the logarithms of the hypo-

" thenuses or secants of the right hand

arches of the feventh column.

"30. And if you make the loga-

" rithms of the fifth columns defec-

" tive, they shall be the logarithms of

" the hypothenuses, or of the secants

" of the left hand arches of the first

" column."

Thus the nature of the Canon required some knowledge of algebraic addition and subtraction; and it was besides troublesome thereby to find the intermediate numbers; the logarithms being only given for such numbers

bers as were equal to the natural fines of each minute. The latter inconvenience E. Wright endeavoured to remove by a scale, of which a draught and description is given in the translation of the admirable Canon, but which Mr. Briggs performed much better in the fame work, by means of a fubfidiary table of fimple application.

The first of these inconveniencies was well removed by John Speidell, who was a very ingenious man, and first completed the Canon for trigonometrical use, by adding three other columns, which were the complements arithmetical of Lord Nepair's, to wit, Secant, and Co-fecant and Cotangent less radius. By this means he faved the application of the plus and minus, and rendered the calculus of triangles more eafy. This he published in the year 1619, under the title of New Logarithms; and to the fixth impression thereof in 1624, is added ly licent

added a Table of the Logarithms of Natural Numbers to 1000, in which the logarithm of 1 is nothing, and that of one thousand, 690775.—Kepler too, in the year 1724, published at Marpurg his Chilias Logarithmorum ad totidem Numeros rotundos; in which his logarithm of 1 was 1611809.59, and of 100000, nothing; which also answered to the logarithm of 90°. And as Nepair had given the logarithms to every degree and minute of the quadrant, so Kepler gives the nearest corresponding degree and minute, answering to each of his logarithms.

But of all that bestowed their labour on the first fort of logarithms, Benjamin Ursinius is most worthy of mention, who calculated a table of such logarithms to every 10 seconds, which was printed at Cologne in 1625, and to which Vlaac must have been much obliged in constructing his Canon Magnus.

These attempts served to facilitate and enlarge the use of Nepair's sirst system

fystem of logarithms, but were all nevertheless subject, in some measure, to its inconveniencies. The perfection of those noble numbers was referved as an additional honour to their first inventor; and the present system, than which there can scarcely be hoped for a better, is likewise the invention of Lord Nepair.

Mr. Henry Briggs, at the time when the Canon Mirificus appeared, was Geometry Professor at Gresham College. This man joined to a great genius and wonderful fagacity in mathematical affairs, a most indefatigable industry, with fingular purity of manners, candour, and generofity. Inflamed by this truly admirable work, he writes, on the 10th of March 1615, to Mr. (afterwards Archbishop) Usher, " that " he was wholly taken up and em-" ployed about the noble invention of " logarithms, then lately discovered." And again, "Nepair Lord of Markin-" fton hath fet my head and hands at " work

" work with his new and admirable " logarithms; I hope to fee him this "Summer, if it please God; for I " never faw a book which pleafed me " better, and made me more wonder." And we find he actually computed new logarithms, wherein he made o the fine total, as in the Canon, but made 10000000000 the logarithm of one-tenth part of the whole fine, or of 5 degrees 44 minutes 21 feconds, judg+ ing them more commodious than those of Nepair; which, in the Summer of 1616, he carried with him to Edinburgh, where he was received by the Baron with great kindness, and staid down, and generothrom a mid driw

by Mr. Briggs's account, that Lord Nepair communicated to him his intended alteration of the Canon; and that he had caused it to be printed in its present form, till his health and leisure should permit him to calculate another, wherein he intended to make o the logarithm of unity, and 10 that of the fine total. Briggs, greatly pleased with that suggestion, which he confessed was much more eligible than his own, threw aside those he had begun, and, as well from his own inclination as the earnest entreaty of Lord Nepair, on his return to London, fet about the calculation of new ones, after that form: of which having computed 1000 to 8 places of figures, befides the index, he carried them, in the Summer of 1617, to the Baron, who was highly pleased therewith, and pressed his beloved friend Briggs, as he stiles him, to continue the work. Which injunction he afterwards more flrongly enforced, by the public teftimonies he gave of both the capacity and industry of his friend; and the expectations the world might form from his continuing the great work, of which his Lordship, in regard to thefe improved logarithms, challenged little more than the invention and mode of construction.

Nor were the sentiments of Briggs in regard to Lord Nepair less lively than those of the latter for him; he mentions him every where with the utmost veneration, warmth, and affection; and seems perfectly enraptured by the nobleness and utility of the great invention. And indeed nothing less could have sustained him through the immense labour of such computations, as he underwent in

bringing it into practice.

On his return to London, he printed the Chilias Prima; and seven years after, in 1624, he produced his Arithmetica Logarithmica, wherein he gives the logarithms of 31000 natural numbers to 14 places of sigures, besides the index; a work which will appear stupendous to any one who, by the same method, will take the trouble to compute the logarithms of only two or three such numbers; which method he may find in the said work, in Malcolm's Arithmetic, Keil's Euclid, Ward's Mathematics, and several other

writers; and of which an idea may be formed from the account of Dr. Halley, who fays, that to have his logarithm true to 14 places of figures, Mr. Briggs, by continual extraction, was obliged to find the root of more than the 140 million of millioneth power. Euclid Speidell fays, he was told, that only finding the logarithm of 2 true to 15 places, for the aforesaid Table, was the work of eight persons a whole year; and Pardies, in his Geometry, praises God, who, for the public good, has raifed up perfons to whom he had given fufficient patience to furmount the fatigue of a labour feemingly insupportable: "for," fays he, " we know that more than 20 per-" fons, employed for that purpose, " fpent upwards of 20 years with in-" defatigable affiduity in the calcula-"tion." This last testimony, which fome have thought an infinuation that the logarithms were first invented in France, rather proves the genius and ability

ability of our excellent countryman Briggs, who, in eight years, with fcarce as many perfons, performed a much greater work than 20 Frenchmen in thrice the time: for the largest French tables of those times were carried to only 11 places of figures, and these are supposed to have been taken from Vlaac.

Though the Chilias Prima was printed in the latter end of the year 1617, it was nevertheless not published till after the death of Nepair, which happened on the 3d of April, 1618; for, in the preface thereto, Briggs says, why these logarithms differ from those set forth by their most illustrious inventor, of ever worshipful memory, in his Canon Mirisicus, it is to be hoped his posthumous book will shortly make appear."

In 1620, two years after the Chilias

Prima of Briggs was published, Mr.

Edmund Gunter set forth a Canon of
Sines and Tangents, adapted to these
loga-

logarithms, which was the first of that kind, and to which he gave the name of Artificial Sines and Tangents. This must have cost Gunter some labour, though he appears to have been much beholden to the Chilias, which consists of 8, and these only of 7 places, besides the index, of which the last place is anomalous, when compared with those which Briggs and Vlaac afterwards computed. These he republished in his book De Sectore et Radio, in 1623, together with the Chilias Prima of his old colleague.

But Briggs himself lived to complete a Table of logarithmic Sines and Tangents, to the one hundredth part of every degree, and to 14 places of sigures, besides the index; to which he intended to have written a full description and use, when death put an end to his labours, at the age of 74, on the 26th January, 163%, thirteen years after his beloved Nepair.

It is remarkable of these two great men, that they both undertook these X 2 mighty mighty labours at rather an advanced age. The Compendium of Honour mentions Nepair to have died in his 67th year; and as it is generally fupposed the logarithms were invented by him about 1610, he must have been near 60 years of age, and, as himfelf informs us, weak and infirm of body, when he began the calculation of his Canon; and in 1614, when Briggs first applied his thoughts that way, he must have been upwards of 57: which may teach us, there is no time of our life too late to acquire honest fame, when we are obedient to the voice of genius, and keep our ease in due subjection to industry.

Briggs, when dying, recommended his last-mentioned work to the care and completion of Henry Gellibrand, then Astronomy Professor at Gresham College, who added thereto the defcription and use of the Canon, and published it at London *, in 1633, un-

^{*} At Gouda, according to some writers.

der the title of Trigonometria Britan-

Thus were these numbers completely planned by the wisdom of the ingenious Lord of Merchiston, and the great building rear'd, in nice conformance thereto, by the most industrious and learned Henry Briggs, in a few years; and it is difficult to determine in these two great men, which is the most admirable; the sagacity of the inventor, or the indefatigable

application of the calculator.

In the Arithmetica Logarithmica, Mr. Briggs had calculated the logarithms of all the natural numbers from 1 to 20000, and from 90000 to 101000; leaving the interval to be filled by the ingenious; to any of whom, in his preface, he offers paper properly ruled, and necessary instructions, he purposing, in the mean time, to employ himself on his Triangular Canon, and having left no labour which an ordinary skill might not perform. But Adrian Vlaac, of Targou, or Gouda

in Holland, completed the 70000 intermediate numbers with fuch expedition, that, in 1628, he published the fecond edition of the Arithmetica Logarithmica, wherein was contained all the logarithms from 1 to 100000 to 10 places of figures, together with a Table of Artificial Sines, Tangents, and Secants (as Gunter had called them) to every minute of the quadrant.

Confidering also that the usual method of angular supputation was by minutes and feconds, Vlaac, in the fame year with the Trigonometria Britannica, published his Trigonometria Artificialis; wherein is contained the logarithmic Sines and Tangents to every 10 feconds, and the logarithms from 1 to 20000: which shews Vlaac to have been a very affiduous and ingenious man; though Dr. Newton, Norwood, and also Wingate, feem to censure both him and others, who rashly published new editions of Briggs's Logarithmica Arithmetica without his leave; thereby preventing the additions he intended

intended to give it when republished, and for making mutilated translations of that and his Trigonometria Britannica, to the discredit as well as disadvantage of the author. Be this as it will, Vlaac's editions are in great esteem, for having the intermediate Chiliads, for his Sexagenary Notation, and for the exactitude of his Tables.

These Tables have been reduced into a more compendious form by the Reverend Nathaniel Roe, of Binacre in Suffolk, in 1633; by Dr. Newton in 1658; and the finishing hand seems to be given to them, in point of disposition and fulness, by Sherwin, in 1706; in whose Mathematical Tables are contained, to 7 places of sigures besides the index, the logarithms of numbers from 1 to 100000, with natural and logarithmical Sines, Tangents, Secants, and versed Sines, to every minute of the quadrant.

The honour of this noble and useful invention has been almost universally attributed to the Great Man to whom

it is due; yet there have been some found who have, through envy, prejudice, or want of confideration, attempted to lessen or transplant it. And, first, Wood, in his Athena Oxonienses, tells it as a report of Oughtred's, that one Dr. Craig first gave Lord Nepair an intimation that fuch numbers were invented by Longomantanus; which fet him about calculating his first Canon. Now this story refutesitself; first, by Oughtred's own acknowledgment of Lord Nepair as the inventor; and by Longomantanus never claiming the invention, though he lived many years after the honour thereof was attributed to Nepair. Wingate, who carried this invention into France, in his publications, afferts, " the fecond fort of logarithms " were jointly schemed by Briggs and " Nepair;" contrary to the fense of the very passage he quotes from Briggs himself. And, I presume, following, or rather willing to improve upon him, Saunderson, in his Algebra, afferts,

ferts, "that Briggs was undoubtedly the "first that thought of this (the pre-"fent) fystem:" which affertion could be contradicted by Lord Nepair's claim in Wright's Translation of his Canon, and that of his son for him, in the preface to his father's Posthumous Works, 1619, both printed under the inspection of Briggs, if even the positive testimony of Briggs himself were not against it.

And it may be observed of this ingenious man, that every attempt to lessen his reputation has only served to establish or increase it: the trivial, and often ridiculous arguments of his opponents; the testimonies of his honest and candid coadjutors Briggs and Wright, as well as of those best acquainted with mathematical history, foreigners as well as Britons, uniting to fix the invention of Logarithms in their first and present form to Lord John Nepair of Merchiston.

The logarithmic Canon ferves to find readily the logarithm of any af-

4

figned

figned number; and we are told by Dr. Wallis, in the 2d volume of his mathematical works, that an antilogarithmic Canon, or one to find as readily the number corresponding to every logarithm, was begun by Mr. Harriot the algebraist (who died in 1621) and completed by Mr. Walter Warner, the editor of Harriot's works, before 1640; which ingenious performance it seems was lost, for want of encouragement to publish it.

A small specimen of such numbers was published in the Philosophical Transactions, for the year 1714, by Mr. Long of Oxford; but it was not till 1742 that a complete antilogarithmic Canon was published, by Mr. James Dodson, wherein he has computed the numbers corresponding to every logarithm from 1 to 100000, to eleven places of figures.

The logarithmic numbers were difposed on straight lines by Gunter in 1623, and hence the Gunter's Scale:

by Wingate, 1627; on two rulers fliding against

against each other, to save the use of compasses in working, and also on circles, by Oughtred, about 1627; in a special form by Mr. Milburne of Yorkshire, about 1650; and lastly, on the present sliding Gunter, by Seth Partridge, in 1657.

The errors of the press are never more numerous than in books of Mathematics, especially Tables; the calculift, compositor, examiner, and even the printer, all being liable to produce them. Warmth and precipitancy are the means which occasion them in the former; and the printer's ink-balls will fometimes pull out a letter or figure, which he has not always the knowledge of, and when he has, does not perhaps take the pains to repair the injury properly: a figure fnatched up in hafte, often fupplying, at a venture, the deficiency. From hence it feems next to impossible to be affured that a whole impression is alike, or that it is free from error. Now, as the present series of logarithms requires

quires nothing but correctness to make it perfect, I cannot help concluding this short discourse with a wish, that our public-spirited noblemen and gentlemen would unite in producing a national edition of this most excellent BRITISH INVENTION, in a manner

worthy themselves.

If Gardiner's Logarithms, freed from errors, were deeply engraved on strong copper-plates, they would endure for ages; would be free from typographical lacune; and, as the errors occasionally found therein might be continually increasing in value. Also, as by national or private generosity, in defraying part of the sirst expense, the work might be fold reasonable enough to come within the purchase of most mathematicians, it would be a universal benefit, and will immortalize his name who sirst promotes it.







