Mr. Wingate's arithmetick: containing a plain and familiar method, for attaining the knowledge and practice of common arithmetick.

Contributors

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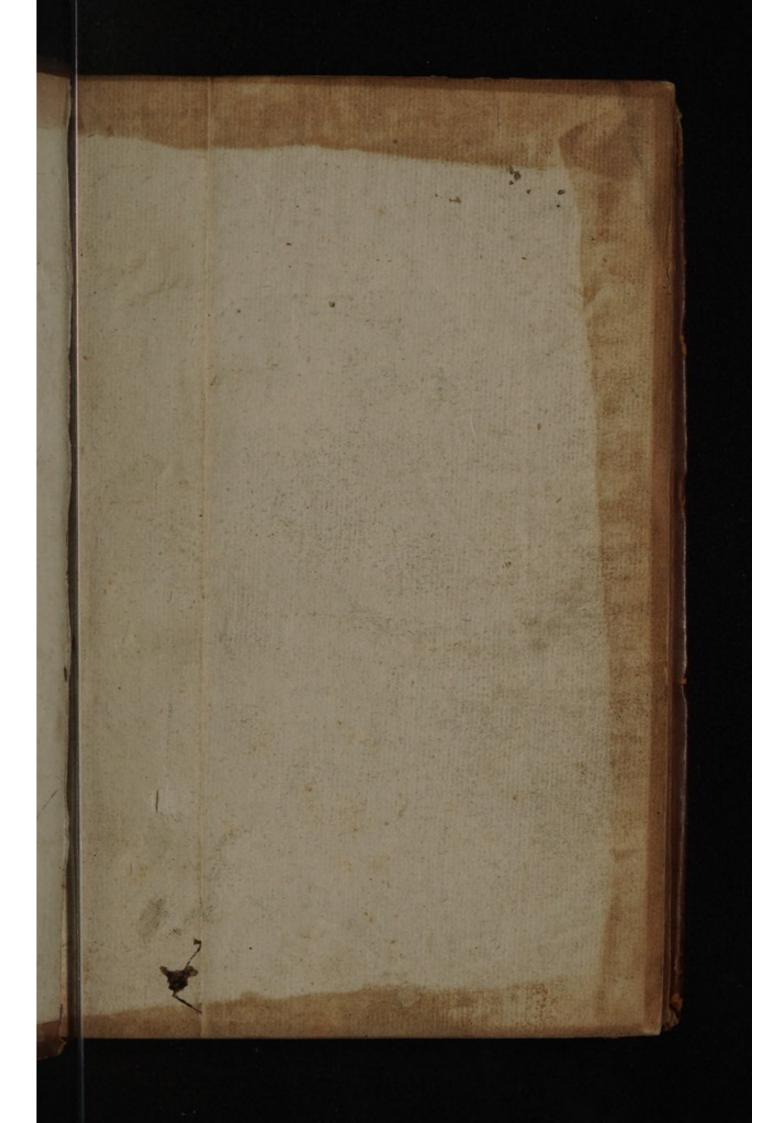


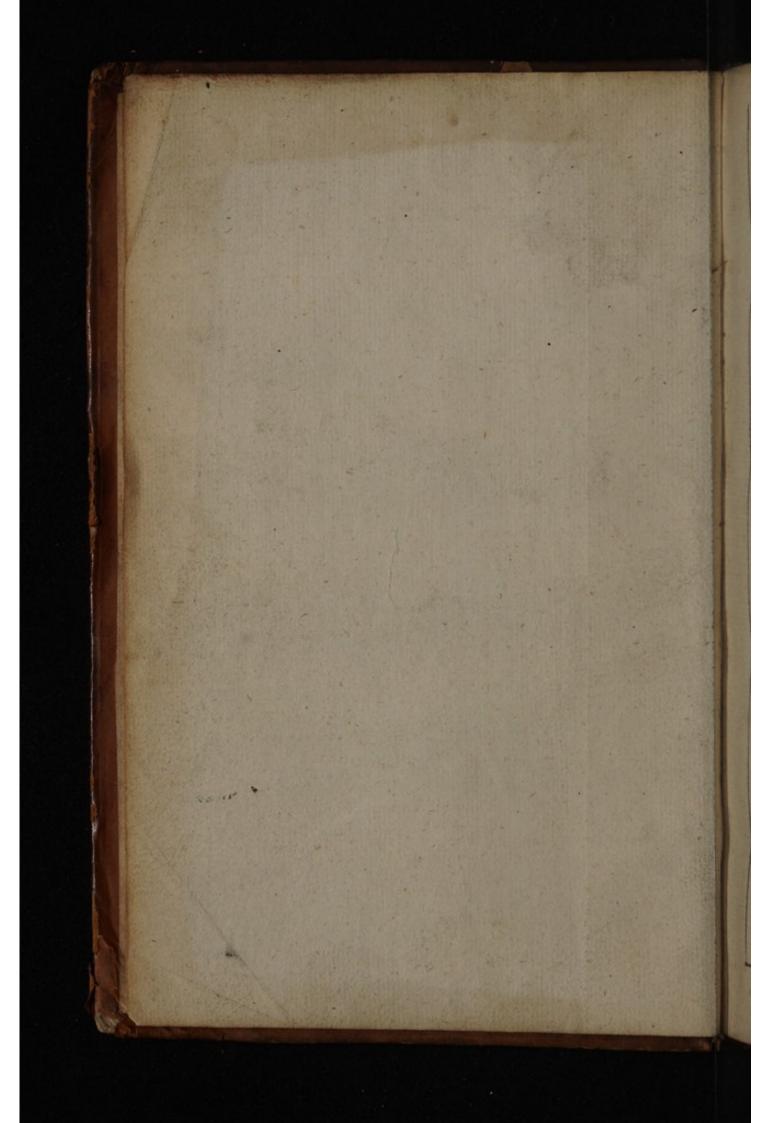






WINGATE KENYON Peel Efg!





Mr. Wingate's Arithmetick,

Containing

A PLAIN AND FAMILIAR METHOD,

For attaining the

KNOWLEDGE and PRACTICE

Of

COMMON ARITHMETICK.

The Seventh Edition, very much enlarged.

First composed by Edmund Wingate late of Grayes-Inne Esquire.

Afterwards upon Mr. Wingate's request, enlarged in his life time: Also since his decease carefully revised, and much improved, as will appear by the Preface and Table of Contents.

By JOHN KERSET, Teacher of the Mathematicks, at the Sign of the Globe in Shandois-street in Covent-Garden.

Boetius Arith.lib. 1. cap. 2.

Omnia quæcunque á primæva rerum natura constructa sunt, Numerorum videntur ratione formata: Hoc enim suit principale in animo Conditoris Exemplar.

LONDON,

Printed by S. R. for R. S. and are to be fold by J. williams at the Sign of the Crown in St. Paul's Churchyard. 1678.

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HISTORICAL

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Sine Cerere & THE Street Venus ,

RIGHT HONOURABLE

THOMAS

Earl of Arundel and Surrey,

Earl Marshal of ENGLAND, &c.

Right Honourable,



He good affection you bear to all kind of Learning, and in particular to the Mathematicks, makes me adven-

ture to present your Lordship with this Tractate of Arithmetick, because that Art, compared with other Mathematical

A 2 Sciences

The Epistle Dedicatory,

Sciences is as the Primum Mobile, in respect of the other inferiour Orbs: For as
the Poets used in times past to say of Venus,
Sine Cerere & Baccho friget Venus,
so may I also considertly averr of them,
without Arithmetick they are poor, and
without motion. Presuming therefore that
your Lordship, loving the Art, cannot
disaffect the Artist, nor his intention to do
good in that kind, I am bold to shelter this Treatise under your Lordships protection, bumbly intreating Tour gracious
acceptation, and earnestly desiring for ever
to remain

Your Honours, in all

- fervice affectionately

to prefent your Lordship with this abis

EDM. WINGATE.



THE

PREFACE

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JOHN KERSEY.



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Bout the year 1629 our learned Countryman Edmund Wingate Esquire, published a Treatise of Arithmetick divided into two Books, the one intitu-

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led Natural Arithmetick, the other Artificial Arithmetick; and in regard his principal design in that Treatise was, to remove the difficulties which ordinarily arise in the practice of Common Arithmetick, by the help of artificial, or borrowed numbers, called Logarithmes (whose proper work is to perform Muliplication by Addition; Division by Substraction, &c.)

The Preface

he did then in his faid first Book omit divers pieces of Common or Practical Arithmetick, which for the perfect and univerfal understanding thereof, were necessary to have been inserted. But after the first impression of both those Books was spent, our raid Author being importuned to take care of the second Edition, he promised his affistance therein; yet his other necessary employments not permitting him to pursue his said purpose, he was pleased to impart his thoughts concerning the same unto me, together with his request, that I would peruse the said first Book, and supply it with such pieces of Practical Arithmetick, which for the reasons aforesaid were wanting in the first Edition.

In pursuance of which request, I have contributed my Talent towards perfecting this Tractate, upon our Authors foundation, partly in his life time to his good liking, and partly since his decease, in several Editions committed to my care to be prepared for the Press: wherein I have used my best endeavours, as well to preserve this Book as a Monument of our said Authors worth, as also to make it a compleat Store-house of Common Arithmetick; from

The Preface

from whence the ingenious may be furnish'd with the excellencies of that Art, in reference both to common affairs, as also to the practical parts of the Mathematicks. And in order to those ends I have made thefe following alterations and Additions, namely, s ne oven for

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First, for the ease and benefit of fuch Learners, who defire only fo much skill in Arithmetick, as is useful in Accompts, Trade and fuch like ordinary employments the Doctrine of whole Numbers, (which in the first Edition was intermingled with Definitions and Rules concerning broken Numbers commonly called Fractions) is now entirely handled apart. And to the end the full knowledge of Practical Arithmetick in whole Numbers might more clearly appear, I have explained divers of the old rules in the first five Chapters, and framed anew the Rules of Division, Reduction, and the Golden Rule in the fixth, feventh, eighth, and minth Chapters; fo that now Arithmetick in whole Numbers is plainly and fully handled before any entrance be made into the craggy paths of Fractions, at the fight whereof some Learners are so dis-A 4 couraged,

The Preface.

discouraged, that they make a stand, and cry out, non plus ultra, there's no progress further.

Secondly, to affift such young Students as desire to lay a good foundation for the attaining of a general knowledg in the Mathematicks, I have in a familiar method delivered the entire Doctrine of Fractions, both Vulgar and Decimal, which was omitted in the first Edition; and have also newly framed the Extraction of the Square and Cube roots, in a method which by experience is found to be much easier than that commonly used heretofore, and is exactly suitable to the Construction or Composition of Square and Cube numbers.

Lastly, I have added an Appendix, which is furnished with variety of choice and delightful knowledge in numbers, both Practical and Theoretical. In all which performances I have earnestly aimed at truth, perspicuity, and exact correction both of the Text and Numbers; so that I hope this Book is now supplied with all things necessary to the full knowledge and practice of Common Arithmetick, the use-tulness whereof is so generally known, that

The Preface.

that there will be no need of Arguments to excite any one that defires his own or the publick good, to be acquainted with fo excellent an art.

But if the more curious Artist, after he is well excercis'd in vulgar Arithmetick, defires further inspection into the Mysteries of Numbers, his best Guide is the admirable Art called Algebra; the Elements whereof I have expounded at large in a Treatife lately published you. A. f bist och

The Doctrine of whole numbers is contained in the first 15 chapters, the titles whereof are these lollowing. Oncerning the Netation of Numbers -11

CF The double Rule of T OF The double Rule of Lorce inverfe. The Rule of Three compound of five Numbers, 12 The Rule of Fellowship. -The Rule of Alligation. The Rale of Falle. -

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The Table of Contents.

is well excercised in vulgar Arithmetick.

Where those Chapters of Mr. Wing ates, that have been altered and framed anew by John Kersey, are distinguished by this mark of, and those chapters that have been entirely composed by the said J. K. may be discovered by this Asterisk *.

The Doctrine of whole numbers is contained in the first 15 chapters, the titles whereof are these following.

Chap. Pag. Oncerning the Notation of Numbers -1! Concerning English Moneys, Weights, 2 Measures, &c. 16 Addition .-23 Subtraction . -Multiplication .-Division .-58 TReduction -The Rule of Three direct. ---The Rule of Three inverse. ---82 The double Rule of Three direct. _____10 The double Rule of Three inverse. -- 11 The Rule of Three compound of five Numbers. 12 The Rule of Fellow(hip. -----13|102 The

The Contents of the Appendix. The Doctrine of Fractions both vulgar and deci-mal, is contained in the 16 chap next following,

ALCOHOL: NAME OF TAXABLE PARTY.	spike on the latest		ASSESSMENT OF THE PARTY NAMED IN	
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7. Pag. -1 I 22 8 -3 16 -4 23 5 31 -6 38 -7 58 -9 82 -10 87 -11 94 -12 98

-13 102 -14 108 -15 125 The

Concerning vulgar Fractions.	The state of
Keels and the substitution of south of	Chap. Pag.
* Notation.	-16/133
* Reduction.	-17 137
* Addition.	-18 151
* Subtraction.	-19 154
* Multiplication.	-20 160
* Division. Was 199 star and to	-21/164
Concerning Decimal fractions.	and a most
* Notation.	-22 167
* Reduction.	-23 172
* Addition.	24 211
* Subtraction.	-25 214
* Multiplication.	-26215
* Division.	-27 226
In volgar and decimal Fractions.	omex N. W.
* The Rule of Three Direct	
* The Rule of Three inverse	-20 345
* The double Rule of Three	201247
* The Kule of False	21250
	A STATE OF THE PARTY OF THE PAR
The Extraction of Roots is containe	Note to the same of
in the two Chapters next following	NAME OF TAXABLE PARTY.
The extraction of the square root	-32/257
The extraction of the Cube root-	-33 270
The Relation of Numbers in quanti	THE RESERVE OF THE PARTY OF THE
quality is contained in the two	ly and
quality is contained in the two f	01-
lowing Chapters.	
The Relation of Numbers in Quantity-	34/290
The Relation of Numbers in Quality; when	rel.
of Arithmetical and Geometrical proportion	H 5331205
	The

The Contents of the Appendix.

The Comence of the Tippendia.
Chap. Page
Oncerning Contractions in the Rule 3 1300
+ of Three \ 1 309
A CONTRACTOR OF THE PROPERTY O
* Exchanges of Coins, Weights, and Measures 3 339
*Practical Questions about lare, 1ret, 7
*Practical Questions about Tare, Tret, Loss, Gain, Barter, Factorship, and measu- } 4 360
ring of Tapeltry
* Interest of money, with Tables to value)
Annuities, &c, at any rate per centum
from 41.to 121. and the manner of making 51368
those Tables
* A Demonstration of the Rule of Three 6 440
* A Demonstration of the double Rule of !
* A Demonstration of the double Rule of \ 7443
Fellowship.
* A demonstration of the rule of alligation; 3 81446
with its use in the composition of medicines?
* A Demonstration of the Rule of False 9 461
* A Collection of Subtil Questions to exer-
cise all the parts of Vulgar Arithmetick;
to which also are added various practical
Questions, about the mensuration of Su-(191475
perficial Figures and Solids, with the
Gaging of vessels.
Spores and pastimes

The Relation of Numbers in quantity and quality is contained in the two-fol-

The Relation of Numbers in Duskies where the Rushing and Sometrical propertion?

The



Common Arithmetick.

The First Book

CHAP. I.

Concerning Notation of Numbers.

ided, with proper Characters in their de



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A Pag

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2/315

3 339

4360

5/368

6 440

71443

8 446

9 461

10/475

11 528

Rithmetick is the art of accompting by Number. As magnitude or greatnesse is the subject of Geometry, fo multitude or number is that of Arithmetick.

II Number is that by which every thing is numbered; or that which an-

lwcrs

fwers this question, how many? (unless it be anfwered by nothing:) So if it be asked how many dayes are in a week, the answer is seven, which is called Number.

The Characters which Number is ordinarily expression ber is expressed fed, are these; tone, 2 two, 3 three, 4 tour, 5 sive, 6 six, 7 seven, 8 eight,

9 nine, o nothing.

IV. These Notes or Characters are either figni-

ficant figures, or a Cypher.

V. The fignificant figures are the first nine; viz. 1,2,3,4,5,6,7,8 9. The first whereof is more particularly called an Unit, or Unity, and the rest are said to be composed of Unities: so 2 is composed of two unities, 3 of three Unities, &c.

VI. The Cypher is the last, which though of it self it signifies nothing, yet being annexed after any of the rest, it increases their value: As will ap-

pear in the following Rules.

VII. Arithmetick hath two parts, Notation and

Numeration.

VIII. Notation teacheth how to express read, or declare, the signification or value of any number written, and also to write down any number propounded, with proper Characters in their due places.

IX. A Number is said to have so maderes of any places or degrees, as there are Characters in the number; viz. when divers figures, whether they be intermixt with a Cypher or Cyphers or not, are placed together like letters in a word, without any point, comma, line, or other note of distinction interposed.

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XVI

The Order of

posed, all those Characters make but one number, which confiss of so many places as there are Characters fo placed together: fo this number 205 confifts of 3 places, and this 30600 of five places, &c.

X. Notation confifts in the knowledge of two things; viz: the order of places, and the value of

every place in any number.

XI. The order of the places is from the right hand towards the left : So in this number 465, the figure 5 standeth in the number. places in any first place,6 in the second, and 4 in the

third; likewise in this number 7560, a Cypher stands in the first place, 6 in the second, 5 in the

third, and 7 in the fourth.

XII. The first place of a Number, 6which as before is the outermost to-The values of wards the right hand) is called the place places in aof Units or Unities; in which place any number. ny figure fignifieth its own simple value: fo in this number 465, the figure 5 standing in the first place. lignifieth five Unities, or five.

XIII. The second place of a number is called the place of Tens; in which place any figure fignifieth fo many Tens as the figure containeth unities: fo in this number 465, the figure 5 in the first place fignifieth simply five, but the figure 6 in the second

place signifieth fix tens, or fixty.

XIV. The third place of a number is called the place of Hundreds: in which place any figure fignifieth fo many hundreds as there are unities contain'd in the figure : So in this number 465, the fr gure 4 in the third place fignifieth four Hundreds : wherefore if it be required to read or pronounce this number 465, you are to begin on the left hand,

and according to the aforefaid rules to pronounce it thus, four hundred fixty five; likewife this number 315 is to be pronounced thus, three hundred and tifteen: and this number 205, two hundred and five; also this number 500, five hundred. Whence it is manifest, that although a Cypher of it felf signifies nothing, yet being placed on the right hand of a figure it increaseth the value thereof, by advancing such figure to a higher place than that wherein it would be feated, if the Cypher were absentati ni a bas , haccol si

The true reading or pronouncing the value of any number written, as also the writing down any number propounded, depends principally upon a right understanding of the three first places before mentioned, and therefore I shall advise the Learner to be well exercis'd therein , before he proceeds to the following Rules. " at a spitted to shirtly to

XV. The fourth place of a number is called the place of Thousands (that's, any number of Thoufands under ten thousand;) the fifth place tens of thousands, the fixth place Hundreds of thousands; the seventh place Millions (a Million being ten hundred thousand;) the eighth place tens of Millions; the ninth place hundreds of Millions; the tenth place thousands of Millions; the eleventh place tens of thousands of Millions; the twelfth place hundreds of thousands of Millions : And in that order you may conceive places to be continued infinitely from the right hand towards the left, each following place being ten times the value of the next preceding place; but to give names to them would be both a troubleforn and an unnecefhis number 465, you are to begin on the later was

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XVI. From the rules aforegoing, an easie way may be collected to read or express the vilue of a Number propounded, Viz. Let it be Abreif way of re-quired to read or pronounce this

nnmber 52 1426341, First, Distinguish by a Comma, or point, every three places, beginning at the right hand, and proceeding towards the left, so will the aforesaid number be distinguished into

parts, which may be called Periods, and stand thus 521, 426, 341. where APeriod

you may note the first period towards
the right hand to consist of these figures 341, the
second of these 426. and the third of these 521. Secondly, read or pronounce the figures in every Period as if they stood apart from the rest, so will the
first Period be pronounced three hundred forty
one, the second sour hundred twenty six: and the
third sive hunnred twenty one. Thirdly, to every
Period except the first towards the right hand, a peculiar denomination or sirname is to be applyed, Viz.
the sirname of the second Period is Thousands; of the
third, Millions; of the sourth, Thousands of Millions, &c. Therefore beginning to pronounce at
the highest Period, which in this Example is the
third, and giving every Period its due sirname,

Thousands, three hundred forty one.

Note, When a number is distinguished into Periods, as before, the highest Period will not always compleatly consist of three places, but sometimes of one place, and sometimes of two, nevertheless after such Period is pronounced as if it stood apart, the due sirname is to be annexed; so this

the faid number will be pronounced thus, Five

bundred twenty one Millions, four bundred twenty fix

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number 3204689, after it is divided into Periods, will stand thus, 3,204,689, and to be pronounced thus, Three Millions, two bundred and four thou-

Sands fix bandred eighty nine.

XVII. The aforefaid Rules for the right pronouncing or reading of a Number which is written down, being well understood, will sufficiently inform the Reader how to write down any number propounded to be written.

The Table of Notation.

	. the first period cowerly	OUT-HOUSE
201 112	Twelfib place 3 Hundreds of Thousand Millions. Tenth place 2 Tens of Thousand Millions. Tenth place 1 Thousand Millions. Ninth place 9 Hundreds of Millions. Eighth place 8 Tens of Millions. Seventh place 7 Millions. Sixth place 6 Hundreds of Thousands. Fifth place 5 Tens of Thousands. Fifth place 5 Tens of Thousands. Third place 4 Thousands.	ed the lat
-42	16 42 62 and the third wife	oud of the
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The values of Places.	Sc. Hundreds of Thousand! Thens of Thousand Millions. Thousand Millions. Hundreds of Millions. Millions. Millions. Thousands. Hundreds.	190 Kg Loir
5	&c. Hundreds Trens of Trens of Trens of Trens of Millions. Millions. Millions. Hundreds Trens of Tr	many Trail
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a s	nir of the state o	200
P	Twelfib place Tento place Tento place Ninto place Ninto place Eighto place Sixto place Fifth place Fifth place Third place	Second place First place
of o	h Period, Eleventh place 3 Hundreds of Thousand Millions. Tenth place 1 Thousand Millions. Ninth place 9 Hundreds of Millions. Registe place 8 Tens of Millions. Sevemb place 7 Millions. Seventh place 6 Hundreds of Thousands. Sixth place 6 Hundreds of Thousands. Fourth place 5 Tens of Thousands. Third place 3 Hundreds.	S
Salara Po	- 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1	20 30 500
2 de la constante	Caralle and Cindo	0 10 190
5000	and Lone in Santan and I have	Hosla one
The order of Places.	Terried of the second second	200
2000	ii.	= 0
1	Fourth Period, Third Period, Second Period.	First Period,
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Notation of Numbers by Latin Letters.

Land exchange Waret	21	Concerning E IXX
2 II.	30	XXX.
3 111.	40	XL.
4 IIII. or thus IV.	49	XLIX.
5 V.	50	Edward Comment
6 VI. to fire sprils all	59	LVIIII. or thus LIX.
VIII. VOODS ESCHOLA	60	LX. Similare state
8 VIII. or thus IIX.	89	the divertity XIXXX
9 VIIII. or thus IX.	100	which they are offer
io X. orotaroniw cohe	200	CC. Malben drod salw
ach. Moneys W.IX 11	300	CCC. ser or send been
12 XII. mind with Wald	400	GCCC 8 to walk of
18 XVIII.or thus IIXX.	500	D. or thus 100 vigo
19 XVIIII, or thus XIX.	600	DC. or thus IC.
20 XX. Lambifridi som	700	DCC, or thus IOCC.

10000 CIO. or thus M. 20000 CIO. CIO. CIO. 50000 CCIOO.

100000 CCCIDDD. or thus CM.
1000000 CCCCI. DDDD.
10000000 CCCCI. DDDD.
16771 CIDDCLXXVII. or
MDCLXXVII.

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CHAP.

Faribing

12. Pence

20.Shillin

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CHAP. II.

Concerning English Moneys, Weights, Measures, &c.

Money, Weight, Measue, Time, and things accompted by the dozen: Of the three first of these, there are infinite kinds and varieties according to the diversity of the several Common-wealths in which they are used, all which here to produce were both endlesse and needlesse: wherefore we intend here to treat only of such Moneys, Weights, Measures, &c. as are used in this Nation, being indeed only necessary for our present purpose.

II. The least piece of money used in English Moland is a Farthing, from whence this followneys.

ing Table is produced.

1. Farthing
4. Farthings
12. Pence
20. Shillings

1. Farthing
1. Peny.
1. Shilling.
1. Pound.

English (or sterling) Money is ordinarily written down with Figures after this manner,

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The first Rank of the said Numbers signifies thirty four pounds, thirteen shillings, five pence, two farthings: the fecond Rank expresseth nine pounds, five shillings, ten pence, one farthing: the third Rank, fix pounds, no shillings, fix pence, three farthings, &c.

III. The smallest Weight used in England is a grain, that is, the weight Vide Statide of a grain of Wheat well dried and compositione gathered out of the middle of the ear, whereof thirty two make another weight called a Peny-weight, Peny-weight make an Ounce Troy.

ponderum. 51 Hen. 3.

and twenty

Here observe, That by the Statutes quoted in the Margent, the weight of two and thirty grains of .Wheat make a peny weight, which weight being once discovered by two and thirty

31 E . I. v. Roft weights 7 49 8. 12 Hen. 75.

fuch grains, the said peny weight (being the twentieth part of an ounce Troy) is usually subdivided into four and twenty parts only, called also Grains, as appears by the ensuing Table.

A Table of Troy Weights. Troy weight. 32 Grains of Wheat (24 Artificial Grains. 24 Grains make I Peny Weight.
I Ounce.

20 Peny Weight 12 Ounces (1 Pound Troy.

Troy Weight is ordinarily written down with Figures after this manner.

> p.w. -05-- 13--13 -II-- 07 --06 -00 --- 05 --- 20

The first rank of the said numbers expresseth seventeen pounds, five ounces, thirteen peny weight, thirteen grains, of Troy weight: the second rank, no pounds, eleven ounces, seven peny weight, six grains: and the third, no pounds, no ounces, sive peny weight, and twenty grains.

Now this Troy weight serveth only to weigh

Malynes lex Mercat.p. 49. Malynes ib. pag. 252. Bread, Gold, Silver, and Electuaries. And here observe also by the way, that Troy weight regulateth and prescribeth a form how to keep the Money of England at a certain Stan-

dard. For about two hundred years before the Conquest, Osbright a Saxon, being then King of England, canfed an ounce Troy of Silver to be divided into 20 pieces, at the same time called Pence; and so an Ounce of Silver at that time was worth no more than twenty pence, or one shilling eight pence, which continued at the same value until the time of Henry the fixth, who (in regard of the enhancing of Moneys in Forein parts) valued the fame at thirty pence, so that then there were accordingly thirty pieces made out of the Ounce, and the old pieces went then for three half pence, until the time of Edward the fourth, who valued the Ounce at forty pence, and then the old pieces went for two pence apiece. After this, Henry the eight valued the Ounce of sterling Silver at forty five pence, which value continued until Queen Elizabeths time, who valued the same Old pence at Three-pence the piece, fo that all Three-pences coined by the same Queen weighed but a peny weight, and every Six pence two peny weight; and so in like manner the Shilling and other pieces accordcl.

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accordingly; which made the Ounce Troy of Silver to be valued at fixty pence or five shillings, as it now remains at this day without alteration.

IV. The weights used by Apothecaries are derived from a pound Troy, Apothecaries which is subdivided as in the follow- Weights. ing Table:

A Table of Apothecaries Weights.

the A pound Troy

An Ounce (is equal) 8 Drams.

A Dram (unto) 3 Scruples.

A Scruple (20 Grains.)

So that if you were to express in Figures 12 pounds 10 ounces, five drams, two Scruples, and 16 grains: also three pounds, five ounces, seven drams, one scruple, and two grains, the ordinary way to write them down is briefly thus,

V. Besides Troy weight before-mentioned, there is another kind of weight used in England, called Averdupois weight, a pound whereof is equal unto 14 Ounces, twelve peny weight Troy. This Averdupois weight serveth to weigh all kind of Grocery-ware, as also Butter, Malynes ib. Cheese, Flesh, Tallow, Wax, and every page 49. other thing which beareth the name of Garbel, and whereof issued a resuse or waste.

VI. Averdupois weight is either greater or less.
VII. The greater is, when one hundred and twelve pounds Averdupois Averdupois are considered as one entire weight greater weight.

commonly called an hundred weight, and then such hundred weight is subdivided first into sour quarters, and each quarter into eight and twenty pounds: again, each pound into sour quarters, or (if you will be more exact) into 16 Ounces, and if you please each Ounce into sour quarters. But ordinarily a pound is the least quantity that is taken notice of in Averdupois gross weights.

A Table of Averdupois greater weight.

So that if you were to express by Figures eight hundred, three quarters, and five pounds; like-wise, seven hundred, one quarter, and seventeen pounds: the ordinary way to write them down is briefly thus,

Awardupois is, when a pound is the highest name or Integer, each pound being subdivi-

ded into sixteen ounces, and each ounce again into 16 drams, and if you please, each dram into 4 quarters, as by the subsequent Table is manisest.

A Table of Averdupois lesser Weight.

4 Quarters of a Dram make I Dram.
16 Drams
16 Ounces
17 Dram.
18 Pound.

So that if you were to express by Figures eighteen pounds, twelve ounces, five drams, and three quarters of a dram; likewise five pounds, no ounces twelve drams, and one quarter of a dram, the ordinary way to write them down is briefly thus.

18—12—05—3

IX. The measures used in England are either of

Capacity or Length.

X. The measures af Capacity are those which are produced from Weight, and they are either

Liquid or Dry.

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XI. The Liquid measures are those, in which all kind of Liquid Substances Liquid Meaare measured, and they are expressed in the Table following.

	A Table of Li	quid 1	Measures.
1	Pound of Wheat?	1015	TI. Pint.
	Troy weight \$	1	
2	Pints	1 13	1 Quart.
200	Quarts	1-11	I Pottle.
	Pottles	15 15	I Gallon.
	Gallons	1	I Firkin of Ale,?
	Get in some of the state	1 5	Sope, Herring,
0	Gallons	> K	I Firkin of Beer.
-	Gallons and an	ma	I Firkin of Salmon
	balf	lie!	or Eels.
2	Firkins	heed.	1 Kilderkin.
	Kilderkins	and a	CONTRACTOR OF THE PARTY OF THE
	Gallons	4	I Barrel.
100	Gallons	- Burn	I Tierce of Wine.
			I Hogshead.
	Hogsheads P.	27 24 44	1 Pipe or But.
-	Pipes or Buts	3	I Tun of Wine.
220	Inc. IIV		XII. Dry

14

Quarters

XII. Dry Measures are those, in Dry Measures. which all kind of dry substances are meted, as Grain, Sea-coal, Salt, and the like; their Table is this that follows:

	A Table of Dry Measures.					
I	Pinte -		-1	Pinte.		
2	Pintes	-	1	Quart.		
2	Quarts	ni bi		Pottle. nonT XI		
2	Pottles		I	Gallon. to with the		
2	Gallons	1 sk		Peck. II SAT .X		
4	Pecks	B	1	Bushel land-measure.		
5	Pecks		I	Bushel water-measure.		
8	Bushels	RETER	I	Quarter.		
4	Quarters	Bien		Chalder. Salsania		
100-00	The state of the s	10/11/11/11/11	THE OWNER OF THE OWNER, THE OWNER			

Long Mea- XIII. Long Measures are exprest in this Table following.

3 Barley Corns in		I In	ch.	23
length	-			. 2848
12 Inches	題器	I Fo	ot.	125
3 Foot		1 Ta	rd.	1100
3 Foot nine Inches	ke	I El	1.	
6 Foot	SE Y	I Fa	thom.	
5 Tards and an balf			le or Pe	rcb.
40 Poles or Perches		I Fu	erlong.	200
8 Furlongs			iglish m	

Note, That a Yard, as also an Ell, is usually subdivided into four Quarters, and each Quarter into four Nails.

XIV. Super-

Chap. II. Weights, Measures, &c.

IS

of Land, are such as are express in the Land Mea-Table following:

or Perches Smake an Acre.

4 Roods Acre.

So that if you would express by Figures these quantities of Land, viz. Thirty six Acres, three Roods, twenty Perches: also seven Acres, no Roods, thirty two Perches; the ordinary way to write them down is thus,

A. R. P. 36—3—20 7—0—32

XV.A Table of Time is this that follows. Time

I Minute

60 Minutes

24 Hours

7 Daies

4 Weeks

1 Month of twenty eight

1 days.

1 Day, and

6 Hours

But in ordinary computations of time, the whole year confissing of three hundred fixty five days, is divided either into twelve equal parts or months, each month then containing thirty daies and ten hours: or else into twelve unequal Kalendar months, according to the ancient Verse:

Thirty days bath September, April, June, and No-

February hath twenty eight alone, and each of the rest thirty one.

Note.

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Note, That every Leap-year (which happeneth once in four years) containeth three hundred fixty fix days, and in such year February containeth twenty nine dayes.

XVI. Of things accounted by the of things accounted by the ing of twelve dozen, each dozen containing again twelve particulars: so that if you would express in Figures, seven Gross four dozen, and sive particulars; also four Dozen and eight particulars, they may be briefly

written thus.

CHAP. III.

Addition of whole Numbers.

1. Concerning notation of Numbers; and how thereby the quantities of things are usually exprest, a sull Declaration hath been made in the preceding Chapters; Numeration ensueth, which comprehends all manner of operations by Numbers.

II. In Numeration, the four primary or fundamental operations (commonly called Species) are these, Addition, Subtraction, Multiplication,

and Division.

III. Addition is that by which divers Numbers are added together, to the end that their fum, aggregate, or total, may be discovered:

IV. In Addition, place the Numbers given,

One

ten or any number of tens, write down the excess

under fuch Rank, and for every ten contained in

the fum of any Rank, referve an Unite or I in your mind, and add fuch Unit or Units to the Fi-

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gures of the next Rank towards the left hand, fo the Numbers 4937, 9878, and 394 being given

to be added together, the operation will be thus, viz. beginning with 4937 the rank of Units, I fay 4, 8 and 7 9878 make 19, wherefore I write down 9, 394 the excess above 10, and carrying 1 15209 in mind instead of the ten con-

tained in the faid 19. I fay 1 and 9 (9 being the lowermost figure of the second rank) make 10. which added to 7 and 3, the other figures of the fame rank, the whole fum of them is 20, wherefore fetting down a Cypher under the line in that rank (because the excess above the two tens is nothing) I carry 2 to the third rank, and fay 2 and 3 (3 being the lowermost figure of the third rank) make 5, which being added to 8 and 9 (the other figures of the same rank) the sum of them is 22, wherefore writing down 2 (being the excefs above the two tens) under the line, in the third rank, I carry 2 in mind (because there were two tens in 22) to the fourth rank, and fay 2 and 9 make 11, which added to 4 makes 15, this 15 because it is the sum of the last rank I write totally down under the line, on the left hand of the Figures before subscribed; so the sum of the three Numbers given is found to be 15209, as in the Kanks amounts unto ten, or any t Example.

VII. When numbers given to be Addition of min- added, do express things of dibers of div es vers Denominations; first write Benominations. them down orderly (according to the Examples in Chap. 2.) then after a line is drawn under them all, begin to add the numbers 水1.

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of the least Denomination, and if the sum of them amounts to one Integer, or many Integers of the next greater Denomination, with some excess of the less Denomination, write down that excess, or a Cypher when there is no excess, under the line, so as it may stand under the least Denomination, and keep the faid Integer or Integers in mind, to be added to those of the next greater Denomination on the left hand: But when the fum of the numbers of the least Denomination amounts not to one Integer of the next greater Denomination, fet down the fum it self under the line; then add the Integer or Integers kept in mind (when any happens) to the numbers of the next greater Denomination on the left hand, and proceed to add them, as also those of every greater Denomination, in like manner as above is directed, until you come to the numbers of the greatest (or highest) Denomination, which are to be added according to the foregoing Rules V. and VI. of this Chapter. So these several sums 24 l. - 13 s. - 5 d. - 3 f. Alfo 121.-05.-8 d. and 51.-185.-2f. being propounded to be added, their total furn is 42 1. ___ 12 s. ___ 2 d. ___ 1f. For having written them down orderly according to the second Rule of the Second Chapter, and drawn a line underneath; I begin with the Farthings first, and fay, two Farthings and

three Farthings make five 1. s. d. f.

Farthings, that is, one Peny 24—13—05—3
with a Farthing over and 12—00—08—0
above; wherefore setting 05—18—00—2
down I under the denomination of Farthings, I 42—12—02—I

carry

carry one Peny to the denomination of Pence. then I fay 1, 8, and five Pence make 14 Pence, which contain one shilling and two Pence, wherefore writing two under the denomination of Pence, I likewise carry I shilling to the denomination of shillings: Then adding the said I shilling unto 18 shillings and 13 shillings, the sum will be found I pound and 12 shillings, wherefore setting down 12 under the denomination of shillings, I carry I pound in mind unto the denomination of pounds faying, I pound in mind, together with 5,2, and 4 pounds which stand in the first Rank of pounds, make 12 pounds, wherefore (according to the fixth Rule of this Chapter) I write 2, the excess above 10, underneath the faid first rank of pounds, and carry 1 in mind for the faid 10 to the fecond. Rank of pounds, then faying in like manner, I in mind, together with I and 2 which stand in the fecond Rank of pounds make 4, which I write underneath the line, that done, I find the total of the three sums propounded to be 42 l .-- 12 s .-- and -- 1 f.

In like manner 3 lb. -05 oz--19 p.m. 15 gr. Also
2 lb. -0 oz. - 3 p.m. - 7 gr. Also o lb. - 10 oz.

-6 p. m. And o lb. - 9 oz. - 0 p.m. - 17 gr.
being given to be added together, their sum will
be sound 7 lb. - 1 oz. - 9 p. m. - 15 gr. and
the work will stand thus.

1b. 6z. pm. gr.

03 — 05 — 19 — 15

02 — 00 — 03 — 07

00 — 10 — 06 — 00

00 — 09 — 00 — --17

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Note, In adding together the Numbers in the last Example, it must be remembred that 24 grains make one Peny weight; 20 Peny weight, one ounce; and 12 ounces one pound Troy (as before is declared in the third Rule of the second Chapter;) And then you are to proceed according to Rule VII. of this Chap.

More Examples of Rule VII. are these following, which presuppose the Learner to be well exercised in the Tables of Chap. 2. that he may readily know, what Integers are to be carried from every lesser Denomination to the next greater.

Addition of English Money.

		625 655 5 T	0,	- 17 17 0		
16.	s.	d.	·f.	1.	s	d.
230-	-17-	-10-	-1	0-	-13-	-05
175-	<u> </u>	-11-	-3	0-	-17-	-08
052-	-05-	-06-		0-	-00-	-10
009-	-00-	08-	-1	0-	-10-	-03
506-	-13-	00-	2	0-	-15-	-06
.br.		I Meala	Derfice.	HOF SH	ALLE TO	
974	-10-	-00-	-3	2	17	-08
The same	COLUMN TO SERVICE	530	-	-	-	

Addition of Troy Weight.

1b. oz. pw. ogr.	02.	o pw.	gr
23-07-16-13	Con later of	-13-	1
17-10-15-07	208-	-11-	0179
325-06-19-20	063-	-10-	-05
49—11—07—12		00-	
417-00 70			
417-00-19-04	907	15	-19

CHAP

kI.

dr. -12

-17

-13

-36 -10 -36

HAP

Subtraction of whole Numbers.

I. Subtraction is that by which one number is taken out of another, to the end that the remainder, or difference, between the two numbers given man believe.

bers given may be known.

II. The number out of which the Subtraction is to be made, must be greater, or at least, equal with the other. As you may Subtract, 4347 or 9478 out of 9478, so bers of one can you not subtract 9478 out of denomination.

numbers one under the other as in Addition, with this caution, that the number placed uppermost may exceed, or at least be equal unto the other: So if the number 4347 be given to be subtracted from 9478, I order them as in the Margent: then proceeding to the subtraction, I say, 7 taken out of 8, there remains one.

which I place in the same rank under the line. In like manner 4 being taken out of 7, the remainder is 3, which likewise I set under the line in the 5131

likewise I set under the line in the 5131 next rank; again taking 3 from 4, the remain der is I, which I likewise place under the third rank; lastly subtracting 4 from 9, there will remain 5, which I subscribe under the sourth rank; so the whole operation being sinished, I find, that if 4347 be taken out of 9478, the remainder is 5131, or (which is the same) the difference between the numbers 9478 and 4347 is 5131, as in the Example.

C 2

remainder will be found 2750; for after the numbers are orderly ranked, 2856 106 I begin at the place of Units, and fay

6 from 6, there remains nothing, 2750 wherefore I subscribe o. then proceeding to the second rank I say, if o

(or nothing) be taken from 5, there will remain 5 which I also subscribe under the line; again I from 8, there remains 7; lastly o from 2, there re-

mains 2, See the work in the Margent.

24

IV. When any of the figures of the number given to be subtracted is greater than the upper figure out of which it is to be subtracted, you must borrow 10 of the next rank towards the left hand, and add the faid 10 to the faid upper figure, then from the fum of fuch Addition subtract the lower figure, and fet down the remainder: In this case the tigure of the next rank which is to be subtracted, must be esteemed an unite greater than it is; wherefore, keeping one in your mind add it to the next figure of the number given to be subtracted, and deducting all out of the figure above it, proceed in like fort till you have finished the whole operation. Example, let it be required to subtract 374 out of 8023. Having ranked them as before, I fay four out of 3, that cannot be, wherefore borrowing ten of the next rank, and adding the fame to the faid 3, I say 4 out of 13, there remains 9; then writing 9 under the line, and carrying 1 in my mind,

I say 1 and 7 make 8, 8 out of 2 that can-8023 not be, but 8 out of 12(12, because 10 be-374 ing borrowed, and added to 2, makes 12) there remains 4, which I subscribe under the 7649 2 x 12 201 11 20 1 3 1 7 12 21 74 24 bos 6742 2120 line II.

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line; again 1 in my mind being added to 3 makes 4, 4 out of nothing, that cannot be, but 4 out of 10 there remains 6, which I likewise subscribe under the line; laftly I in my mind being taken out of 8 there remains 7. Thus you see that the remainder after 374 is subtracted from 8023 is 7649. Note diligently, that as often as 10 is borrowed, 1 must be kept in mind to be added to the figure standing in the next place of the lower number, and the sum of such Addition must be subtracted from the vpper place; but if it happen that there is no figure in the next place of the lower number, then the 1 in mind must be subtracted from the upper place, (as in the last rank of the last Example.) Another Example. Let it be required to subtract 92 from 62801. Having placed the greater number uppermost and the lesser orderly underneath, I begin at the place of units, and say, 2 from r I cannot take, but 62801 borrowing 10, and adding it to the faid 1, I fay 2 from 11, there remains 9, which I subscribe under the 62709 line; then I proceed and fay, I in mind with 9 makes 10, 10 out of 0 I cannot take, but borrowing 10 I fay 10 out of 10 and there remains o. wherefore I subscribe o under the line; again, I in mind out of 8, there remains 7; then because there are no more Figures in the lower number, I say o out of 2 there remains 2; lastly, o

V. If the numbers propounded have divers denominations, place them as before, and beginning with

Subtraction of numbers of divers denominations

C 3

out of 6 there remains 6; therefore I conclude

the least denomination first, subtract the lower number from the upper when it may be subtracted, and place the remainder underneath; but if it happen that the lower number cannot be taken out of the upper, you must borrow an integer of the next greater denomination on the left hand; which in teger, after it is converted into the same denomination with the faid upper number, must be added to it: then from the fum of fuch Addition, you are to subtract the lower number, and write down the remainder, keeping I (that is the integer borrowed) in your mind, to be added to the next place of the number given to be subtracted, as before: so gol.—14s.—10d.—3 f. being subtracted from 1241.-11s.-7d.-1 f. the remainder is 331. -16s. -8d. -2 f. For beginning with the farthings, I fay, 3 farthings out of

1. s. d. f. I farthing I cannot take, where124—11—07—1 fore borrowing 1 peny (that
90—14—10—3 is an integer of the next grea33—16—08—2 ter denomination) and having

converted this peny into four farthings, I add them to the aforesaid I farthing, so the sum is five farthings, out of which subtracting 3 farthings, there remains 2 farthings, which I place underneath the denomination of farthings; then I proceed to the next denomination, and say, I peny which I borrowed and Iod. make IId. this IId. out of 7d. I cannot take, wherefore borrowing I shilling or I2d. and adding I2d. to the said 7d. the sum is 19 d. from which I subscribe under the denomination of pence; again I shilling which I borrowed being added to 14s. makes

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makes 151, which I cannot subtract out of 115, and therefore I borrow I pound or 20s. which being added to the faid 111. makes 31s. from which Subtracting 15s. there remains 16s. which I subscribe under the denomination of shillings; then carrying I pound which I borrowed to the lower place of pounds, I fay I in mind with o makes I, which taken out of 4, there remains 3; again 9 out of 2, I cannot take, but 9 out of 12 (10 being borrowed and added to the faid 2, according to the fourth Rule of this Chapter) and there remains 3. lastly I (for the to that was borrowed) being taken out of I, there remains nothing; and so at last I find, that if A. being indebted to B. in 1241 .- 115: 7d. - I f.hath paid in part thereof 901-14s. 10d. -3 f, there remains yet undischarged'331. -16s. -8d. -2f.

VI. When many numbers are given to be subtracted from a number propounded, you must first add those numbers together, according to the rules of the third Chapter, and then

Subtraction of many numbers from one numher.

the sum sound is to be subtracted from the number first propounded. Example, A being indebted to B. in 3240l. paid thereof at one time 700l. at a second payment 1236 l. and at a third 305 l. the question is how much of the debt

question is how much of the debt remained undischarged? First, I add together the several sums paid, and find the total to be 2241 l. this I subtract from 3240l. so there remains 999 l. undischarged as you see by the-operation in the Margent.

1. 32.40 The debt.

700 | Payments 305 |

2241 Total payd 999 rest unpayd

TO BOOK IS
l. s. d. Another Example of
The Debt 50000 oo like nature. A. being
indebted to B.in 500l
\$340-12 06 paid in part thereof
Payments 2 13-18 - 03 at one payment 340 l
2 1716 10 121 06 d. at
- a second payment 131
Paid in all 372-07 07 18s 3d. at a
Rest unpaid 127-12-05 third 17 116s.
- rod. the question is, how much was in arrear?
Here if the operation be prosecuted as before, it
will appear that there was 127 l 125 05 d.
unpaid: see the work in the Margent:
VII. Addition is proved by fubtra-
The proof Air and Colon Air A 11:1
and fut- For having added divers numbers to
Berner's 1. Journal one of thefit
out of the sum, the remainder must be
equal to all the rest, as you may observe by the
Example following, viz. supposing these 4 num-
bers are given to be added viz.
236, 452, 29, 217. and that
their sum is found to be 934
452 934 (by the Rules of the 3d. Chap.)
29 236 it is required to prove whe-
217 698 ther the faid sum be true or
934 not; to perform this I draw a
698 line under the uppermost num-
ber 236, to seperate it from the
rest, and seek the sum of all the numbers given, ex-
cept that uppermost, which sum I find to be 698.
Then I subtract the said uppermost number 236
from 934 (the total fum of all the numbers first
found) and because the remainder 698 is the same
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with the sum of all the numbers excluding the uppermost, I conclude that the sum of all the numbers first found was truly computed.

In like manner is Subtraction proved by Addition, for if you add the remainder, and the number given to be subtracted together, the sum must be equal to the

number out of Example 1. Example 2. which the Subtra- 1. s. d. Ction is made, so if out of 9478 24—13—07 4347 be subtracted subtr. 4347 19—15—08 from 9478 the re- Kest 5131 04—17—11 mainder is \$131, Proof 9478 24—13—07 for if \$131 be added

to 4347, the sum is 9478, which is the same with the number out of which the Subtraction was made. Again, if a Servant receive 241.——131.

-7 d. and lay cut or disburse 191.——15s. ——08d. there must remain in his hands—41.

17 s.——11d. for this being added to 19 l.—
15 s.——08d. which was the Money he expended, the furn will be equal to 24 l.—
13 s.——07 d. (being the Money wherewith he

was first charged.)

More Examples of Subtraction are these that follow.

Subtraction of English Money.

1. s. d. f.	1.	5.	d. f.
l. s. d. f. Rec. 309010071	24 -	- 00	0
paid 0099-14-08-3	05-	17	11 3
reft 2990-15102			100
proof 309010071	24-	- 00 -	0
April 1	ATTORES.		Sub-

Subtraction

Book I.

n drive

Subtraction of Troy weight.

+MUA	1b. oz. pw. gr.	0%.	pro.	gr.
Bough	# 352-10-13-15	205-	-13-	-19
Sold	019-11-16-18	118-	16-	20
Rest	332-10-16-21	86-	_16_	23
Proof	352-10-13-15	205-	-13 -	19

Subtraction of Averdupois Weight.

C. q. 1b.	lb. oz. dr.
Bought 256-2-23	25-13-12
Sold 079-3-26	00-14-13
Rest 176-2-25	24—14—15
Proof 256-2-23	25—13—12

Subtraction of Superficial Measures of Land.

	Acres, B	Loods, Per	ches.	A.	R.	P.
Bough.	t 780 -			2040-		
Sold	090 -	3	-36	919-	-3-	30
Rest	689 —		-39	1120-	-1-	-30
Proof	780-		-35	2040-	-1-	-20

Questions to exercise Addition and Subtraction.

Quest. 1. Two persons, A. and B. owe several debts, the lesser debt being that of A. is 30451. the difference of their debts is 104 l, what is the debt of B? Answer, 3149 l. Quest

Quest. 2. Two persons A. and B. are of several ages, the age of the elder, being that of A. is 70, the differences of their ages is 19, what is the age of B? Answer, 51.

Quest. 3. What number is that which being ad-

ded to 168 maketh the fam to be 205? Anf.37.

Quest. 4. The sum of two numbers is 517, the

lesser is 40, what is the greater? Ans. 477.

Quest. 5. A certain person born in the year of our Lord 1616, desired to know his age in the year

1676, what was his age? Ans. 60.

Quest. 6. The greater of two numbers is 130, their difference is 49, what is the lesser number?

Answ. 81.

CHAP. V.

Multiplication of whole numbers.

I. Ultiplication teacheth how by two numbers given to find a third, which shall contain either of the numbers given so many times as the other contains I or unitie.

II. Of the two numbers given in Multiplication, one (which you will) is called the Multiplicand, and the other the Multiplicator, (or both are called Fa-

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III. The number fought, or arising by the multiplication of the two numbers given, is called the product, the Fact, or the Rectangle: so if 5 be given

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given to be multiplied by 3, or 3 by 5, the product is 15, that is 3 times 5, or 5 times 3 makes 15: and here 5 may be called the Multiplicand, and 3 the Multiplicator, or 3 may be called the Multiplicand, and 5 the Multiplicator; and as 3 (one of the two numbers given) containeth 1 or unity thrice, so 15 the product containeth 5 (the other given number) thrice; likewise as 5 (one of the given numbers) contains unity 5 times, so 15 (the product) contains 3 (the other given number) five times.

IV. Multiplication is either single or compound.

Single multiV. Single Multiplication is, when plication the Multiplicand and Multiplicator consist each of them of one only figure, as in the last Example; In like manner if you multiply 9 by 5, the product is 45, this is likewise single multiplication: now the several varieties of single multiplication are well express in the Table following, usually called Pythagorus bis Table.

The Table of Multiplication.

To a series	THE REAL PROPERTY.	11331	100000	0.00	N III	1 1 1 1 1 1	00	-
1	2	3	4	5	6	7	8	9
2	4	6	8	10	12	14	16	18
3	6	9	12	15	18	21	24	27
4	8	12	16	20	24	28	32	36
5	10	15	20	25	30	35	40	45
.6	12	18	24	30	36	42	48	54
7	14	21	28	35	42	49	56	63
8	16	24	32	40	48	56	64	
9	18	27	136	45	54	63	72	81

The use of the Table is this, having one figure given

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given to be multiplied by another to know the product of them, find the multiplicand in the top of the Table, and the multiplicator in the first Column thereof towards the left hand; this done, in the angle of position just against those two figures you shall find the product. So 9 being given to be multiplied by 5, I find 9 in the top of the table, and 5 in the first column towards the left hand, then carrying my eye from 5 in a right line equidistant to the upper side or top line of the Table, until I come to that square which is directly under 9, I find 45, which is the Product required. The particular varieties of this Table ought to be learned by heart, (that is, a man must be able to give the Product of any fingle multiplication, without the least pause or stay) before he can readily work compound multiplication, as will further appear hereafter.

when the multiplicator and multiplication is, Multiplication and either one or both confift of more

figures than one.

VII. In compound Multiplication, when the numbers given do end with fignificant figures, place them as in Addition and subtraction. So 134 being given to be multiplied by 2, place them thus: then proceeding to the multiplication 134 fay thus: two times 4 is 8, which write under the line in the rank of your multiplying 268 figure, again, say two times 3 is 6, which likewise write under the line in the next rank; Lastly, two times 1 is 2, which being likewise written down under the line in the next rank, the Product is discovered to be 268, and the work will stand as in the Margent.

VIII. When the Multiplicator confists of more figures than one, as many figures as it hath, so many several products must be subscribed under the line, which at last being added into one sum, gives you the total product of all. So 1232 being given

to be be multiplyed by 23, the operation 1932 thereof will stand thus, for 1232 being

23 multiplied by 3, (according to the 3696 last rule) the product is 3696. Again,

2464 1232 being multiplied by 2, the pro-28336 duct is 2464, which several products,

after they are placed in their due or-

3963 tiplying figure) and added together,

2642 produce 28336, the product required:

multiplied by 123, the product is 162483, and the operation will stand

as you fee in the Margent.

IX. When the product of any of the particular figures exceeds ten, place the excess under the line as before, and for every ten that it so exceeds, keep one in mind to be added to the next Rank.

Example, 3084 being given to be 3084 multiplyed by 36, the work will stand 36 thus; for 6 times 4 being 24, I write 18504 4 under the line, and reserve 2 in mind 9252 for the two tens; then I say 6 times 8 111024 is 48, unto which if I add 2 kept in mind, the whole is 50, wherefore subscribing 0 in the next rank under the line (0 because there is no excess of 50 above 5 tens) I reserve 5 in mind for the 5 tens; again, I say 6 times nothing

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times thing nothing is nothing, to which adding 5 that I kept in mind, the whole will be but 5, which I likewise subscribe under the line in the next rank; again 6 times 3 is 18, which (in regard 3 is the last figure of the multiplicand) I write wholly down; so that the particular product arising from the multiplying figure 6 is 18504: in like manner proceeding with the multiplying figure 3, the particular product arising will be 9252. Lastly, these several products being placed in due order, and added together (after the manner of the 8th. Rule of this Chapter) will give 111024, which is the total product arising from the multiplica-

tion of 3084 by 36, and the operation will stand as in the Margent. After the 256 same manner if 5073 be given to be 30438 multiplied by 256, the product will be 25365 found to be 1298688, and the operation will stand as you see in the example.

be multiplyed, do one or both of them end with a Cypher or Cyphers towards the right hand, multiply the fignificant figures in both numbers, one by the other, neglecting such Cyphers, and when the multiplication of the fignificant figures is finished, annex on the right hand of the number produced by the multiplication, the Cy-

pher or Cyphers with which one or both of the numbers first given did end fo will the whole give you the true 2155 product demanded: Example, 43100 431

being given to be multiplied by 646500000 15000 the product will be found 646500000 for omitting the Cyphers which stand; -23

in the last places towards the right hand as well in the multiplicand as the multiplicator, I multiply the significant sigures 431, by the sigures 15 (according to sormer rules,) so there will arise 6465, to which annexing on the right hand all the Cyphers before omitted, the true product will be 646 500000: more Examples hereof are these following.

43125	5108000
43125	25540 Hwy 10216 Snill
64687500	5108
ac and a said	638500000

XI. When in the multiplicator Cyphers are included between fignificant figures, multiply by the faid fignificant figures, neglecting such Cyphers or Cypher, but observe diligently to set the particular products of the fignificant figures in their due places, according to the 8th rule of this

Chapter. So if 56324 be given to be multiplied by 20006, I first multiplied by 20006, I first multiplied by 6, and place the product orderly underneath the line, then passing over the three Cyphers, I multiply 56324 by 2 and place 8 (which is

the first excess of this particular product) directly under the multiplying figure 2, and the rest in their order, so at last the true product will be found 1126817944, and the work will stand as you see in the Example.

More

More Examples hereof are thefe that follow.

	23765
3094	10302
104	d 10 47530
12376	71295
3094	23765
321776	244827030

Note, That one of the principal cautions to be observed in Multiplication, is the due placing of the particular products arising by each multiplying figure: and that may be performed either by taking care to place the first figure or Cypher which ariseth in each product under the respective multiplying figure; or at least the first place arising in the second product must stand under the second place of the first product, and the first place of the third particular Product under the third place of

the first, &c.

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XII. When a number is given to be multiplied by a number that confists of 1 (or an unit) in the first place towards the lest hand, and a Cypher or Cyphers on the right hand of such unit (such are 10, 100, 1000, 10000, &c. the multiplication is performed by annexing the Cypher or Cyphers of the multiplicator at the end (to wit on the right hand) of the multiplicand; so if 326 be given to be multiplied by 10, the product is 32600; if by 100, the product is 326000; in like manner if 170 be multiplied by 10, the product is 1700; if by 100, 17000, &c.

two are given to be multiplied one by the other, that kind of Multiplication tion.

D

is called Continual, and is thus performed, Viz. first multiply any two of the numbers given one by the other, then multiply the product by another of the numbers given, and this product by the fourth number given (if there be so many) and in that or-

der till every one of the given numbers hath been made a Multiplicator, so the last product is the true product required. Example, If 4, 18, and 22 were given to be multiplyed continually, first 18 multiplyed by 4 produceth 72, which multiplied by 22 (the third number) produceth 1584, the last product or

number required, see the work in the Margent.
The proof of Multiplication is by Division as will

appear by the next Chapter.

CHAP. VI.

Division by whole numbers.

I. I Ivision is that by which we discover, how often one number is contained in another, or (which is the same) it sheweth how to divide a number propounded into as many equal parts as you please.

II. In Division there are always three remarkable numbers which are commonly called by these names, the Dividend, the Divisor, and the Quotient.

III. The Dividend is the number given to be divided into equal parts.

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IV. The Divisor is the number by which the Dividend is to be divided; that is, it is the number which declareth into how many equal parts the dividend must be divided.

V. The Quotient is the number arising from the division, and sheweth one of the equal parts required: so if 15 were given to be divided by 5, or into 5 equal parts, the number arising, or one of the equal parts will be 3, for 5 is found three times in 15: And here 15 is the Dividend, 5 the Divisor, and 3 the Quotient.

VI. Division being the hardest lesfon in Arithmetick, must be heedfully fingle figure.

intended by the Learner, for whose ease I shall use my utmost endeavours to make the way smooth by Rules and Examples, beginning with the easiest first, which will be in that case when the Divisor consists of one figure only; for example, Let it be required to divide 192 by 8, or 192 pounds into 8 equal parts or shares; here 192 is the Dividend, 8 is the Divisor, and the Quotient or one of the equal parts is sought.

vil. Place a crooked line at each

VII. Place a crooked line at each end of the Dividend, that on the left hand serving for the place of the Divisor, and that on the right for the Quotient; then if the Divisor be a single figure, subscribe a point under the first figure of the Dividend towards the left hand, if such first figure be either equal unto, or greater than the Divisor,

but if such first figure be less than the Divisor, put a point under the next place of the Dividend; which number so distinguished by the point may be called the Dividual; so in the example

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given in the 6 Rule, 192 being the Dividend, and 8 the Divisor, I subscribe a point under 9, not under 1, because it is less than the Divisor. This done the Dividual, or number whereof the question must

be asked, is 19.

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VIII. Having thus prepared the numbers, ask how often the Divisor is contained in the Dividual, and write the number which answers the question in the Quotient; then multiply the Divisor by the number placed in the Quotient, and subscribe the product underneath the Dividual. Lastly, having drawn a line under the product, subtract it from the Dividual, and subscribe the remainder orderly

underneath the line. So demanding 8) 192 (2 how many times the Divisor 8 is found in the Dividual 19, the answer is two times, wherefore I write 2 in the Quotient; then multiplying the Divisor 8

by 2 (the number placed in the Quotient) the product is 16, which I subscribe orderly under the Dividual 19; and after a line is drawn underneath the product 16, I subtract it from the Dividual 19, and

place the remainder 3 underneath the line.

IX. Put another point under the next place of the Dividend towards the right hand, and bring down the Figure or Cypher standing in that place to the remainder; that is, fet it next after it, fo the whole will be a new Dividual: Thus a point,

being placed under 2 which stands in 8) 192 (2 the next place of the Dividend, I write 2 next after (to wit, on the righ hand 16 of) the remainder 3, so is 32 a new Dividual, or number whereof the fecond question must be asked, and the work will stand as you see in the example.

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X. A new Dividual being set apart, renew the question and proceed according to the 8th. Rule of this Chapter. Thus demanding how often the Divisor 8 is found in the Dividual 32, the answer is four times; wherefore I write 4 in the Quotient, then multiplying the Divisor 8 by four (the figure last placed in the Quotient) the product 8)192(24 is 32, which I subscribe under the Dividual 32, and after a line is drawn underneath, I subtract the product 32 32 from the Dividual 32, and there being no remainder, I subscribe o under the line, so the whole work being finisht, the Quotient is found to be 24, and the operation stands as you see in the Example; wherefore I conclude, if 192 pounds be equally divided amongst 8 perfons, the share of each person will be 24 pounds.

A second Example. Let it be required to divide 936 pounds into 9 equal parts; having distinguished the first Dividual by a point, (according to the 7th. Rule of this Chapter) I demand how often the Divisor 9 is found in the Dividual 9, and finding it once contained in it, I write 1 in the Quotient; then multiplying the Divisor 9 by 1, the product

plying the Divisor 9 by 1, the product o is 9, which I subscribe under the Dividual 9; after this, a line being drawn under the product

duct 9, I subtract it from the Dividual 9, and there being no remainder, I place a 0 underneath the line, as you see in the Example.

Again, placing a point under 3 which stands in the next place of the Dividend, I tranfcribe the said 3 next after the remainder 0 for a new Dividual, then asking

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how

how often the Divisor 9 is contained in the Dividual 3, and not finding it once contained therein, I write 0 in the Quotient, and now because the product which ought to arise from the Multiplication of the Divisor by 0 (the Cypher last placed in the Quotient,) amounts to 0, the Dividual 3, out of which that product should have been subtracted, remains the same without alteration; wherefore after a point is subscribed under 6 the next place

9 (936 (104

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of the Dividend, I annex 6 to the Dividual 3, so there will be a new Dividual, to wit, 36; then demanding how often the Divisor 9 is found in the Dividual 36, the 2n-swer will be 4 times, wherefore I place 4 in the Quotient, and multi-

plying the Divisor 9 by 4, the product is 36, which I subscribe under, and subtract from the Dividual 36, so the remainder is 0, thus the whole work being finisht, the Quotient is found to be 104, as you see in the Example; wherefore I conclude, if 9361. be divided equally amongst 9 persons, the share of each will be 1041. In like manner if 296163 be divided by 7 the Quotient will be 42309

The substance of The whole work of Division is division by what briefly contained in this following method for ver. Verse.

Die quot, mutiplica, subdue, transferque secundum. Or thus,

First you must ask how oft, in Quotient answer make; Then multiply, subtract, a new Dividual take.

A compend cus XI. When in the Division the reay of dividing Divisor consists of a single Figure by a single figure onely, the Quotient may be written down,

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down, and all the operation performed in mind, without writing down any part thereof; so \$2506 being given to be halfed or divided into two equal parts, the work will be thus, The Divisor 2 is found 2) \$2506 (41253 in 8 four times; in 2 once; in 5 twice; and there will remain 1, which 1 being supposed to stand before (to wit, on the lest hand of) the Cypher makes 10, then I say 2 is found in 10 five times; and last of all in 6 three times; so that the true Quotient or one half of the given number \$2506 is found to be 41253

In like manner if 82506 be given to be divided by 3, or into 3 equal parts, the work will be thus, the Divisor 3 3)82506(27502

is found in 8 twice, & there will remain 2, which 2 being supposed to stand before (to wit, on the lest hand of) the following 2 makes 22, then I say 3 is found in 22 7 times, in 15 5 ti nes, in 0 not at all, and lastly in 6 twice; so that the true quotient or one of the 3 equal parts required is 27502. After the same manner may division be wrought by any single figure, without much charge to the memory.

Note, here the Learner may ask Anote, concerning what shall be done with the last the remainder after temainder, if any happen, when the Division is sinished? For a full ded, if any happen. answer to this, I refer the Reader to the Note in

propound an example where the said case happens, viz. Let it be required to divide 351 by 8, or 351 pounds equally amongst 8 persons; now if the opera-

former rules, the Quotient will be

found to be 43, and after the Division 8)351 (43

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is finisht, there will remain 7, that is, each person must have 43 pounds, and there will be an overplus of 7 pounds, which must be also divided equally among the 8 persons, but that cannot be done till the 7 pounds be reduced into shillings, and then those shillings must be divided by 8 to give every person his due share of the shillings contained in the faid 7 pounds; again, if there yet remain any surplusage of shillings, they must be reduced to pence, which must also be divided by 8, to give every person his due share of pence: so that when this question is fully answered each persons share will appear to be 43 l.—17 s.—6 d. But how the before mentioned Reduction is performed will be made manifest in the fifth rule of the next Chapter. XII. When the divisor confifts of Division by two or more figures, two, three, or how many places soever the first and ea- the operation is more difficult than steft method. theformer, but depends upon the fame grounds, and therefore the learner being well vers'd in the preceding method of dividing by a fingle figure, will the more readily understand these that follow, which are two, whereof the first is the easier, but the later more expeditious, and that which indeed is principally to be aimed at: For an example of the former, let it be required to divide 4112772 by 708, or (which is the same) to divide 4.112772 into 708 equal parts.

First, a Table is to be made to shew at first sight any Multiple or product of the Divisor, it being taken twice, thrice, or any number of times under ten, so having first written down the Divisor it self 708, and drawn a line on the right hand thereof, I place I on the right hand of the line directly

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against the Divisor; then un- The Divisor	r. 708 1
fcribe the double thereof,	21243
which is 1416, and place the	1416 2 2124 3 2832 4
figure 2 directly against the	3540 5
	4248 6
ther fide of the line. Again	4956 7
adding 1416 (to wit the dou-	5664 8
ble of the Divisor) to the Divi-	4956 7 5664 8 6372 9
for it felf 708, the fum is 2124	

for the triple of the Divisor, this triple I subscribe under the double and place 3 on the other side of the line right against the triple; Again adding 2124 (the triple of the Divisor) to the Divisor, which quadruple of the quadruple of the Divisor, which quadruple I subscribe under the triple, and proceeding in like manner, at last the table is finisht, which readily shews the Divisor, with the duple, triple, quadruple, quintuple, sextuple, septuple, octuple, and noncuple of the Divisor.

Now for a proof of the said Table, adding the last number thereof, to wit, 6372 (which was sound to be nine times the Divisor) to the Divisor 708, I find the sum to be 7080, which (by the 12th. Rule of the sisth chap.) is evident ten times the Divisor; wherefore I conclude that the Table is true, in regard that the last number thereof is derived from

all the fuperiour numbers.

The Table of Multiples or Products of the Divisor being thus prepared, write down the dividend on the right hand of the Divisor; then distinguish by a point so many of the foremost places of the Dividend towards the lest hand as are either equal in value (being considered apart) to the Divisor, or which

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708 1416 2124 2832 3540 4248	3 3540 4 5727	yet come nearest to the yet come nearest to the value thereof, thus I subscribe a point under 2, thereby setting apart 4112, being the sewess
4956 5664	6372	of the foremost places which will contain the
63729	0	Divisor 708, so is 4112

the dividual (or num. ber whereof the first question must be asked;) then demanding how often the Divisor 708 is contained in the dividual 4112, the answer will be found by the Table to be five times, for looking in the Table I cannot finde the dividual exactly, but I fee the 5 times the Divisor is the next greater than the dividual 4112, and five times is the next leffer; wherefore I write 5 in the quotient, and the number in the Table which stands against 5, to wit, 3540 I subscribe under the dividual 4112, then baring drawn a line underneath, I subtract 3540 (which is five times the Divisor) from the dividual 4112; and subscribe the remainder 572 underneath the line; that done, I put a point under the next place of the dividend towards the right hand, and because the figure 7 stands in that place, I transcribe 7 next after the remainder 572, so there is 5727 tor a new dividual.

Then demanding how often the Divisor 708 contained in the dividual 5727, the answer will be found by the Table to be 8 times, for looking in the Table I find that 9 times the Divisor is the next greater, but 8 times is the next leffer than the devidual, wherefore I write 8 in the quotient, and

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the number in the Table which stands against 8, to wit, 5664 I subscribe under, and subtract from the dividual 5727, placing the remainder 63 underneath the line.

Again, I put a point under the next place of the dividend, where I find the figure 7, and therefore transcribing 7 next after the remainder 63, the new dividual will be 637 then demanding how often the Divisor 708 is contain'd in the dividual 637; and not finding it once contain'd therein, I write o in the quotient, and fince in this case (that is, when a Cypher answers the question) the dividual remains the same without alteration, the figure or cypher standing in the next place of the dividend is to be transcribed after the dividual for a new dividual, so writing 2 next after 637, the new dividual is 6272, wherefore demanding how often the Divifor 708 is contain'd in 6372, I find by the Table it is contain'd in it 9 times, wherefore writing 9 in the Quotient, and placing the number which stands against 9 in the Table, to wit, 6372 under the dividual 6372, and subtracting it from the dividual there will remain o. Wherefore I conclude if 41 12772 be divided by 708, or into 708 equal parts, the true Quotient or one of the equal parts required is 5809. Divisor. 1881)

In like manner if 20304 be divided by 188, that is into 188 equal parts, the quotient arifing or one of those equal parts will be 108, and the operation will stand you see.

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	376	2	20304 (108
Divisor	564	3	
Dia	752	-	188
W. Street	940		1504
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The preceding method of Division by the help of a Table of the Multiples or Products of the Divisor, as it is most easie, so in some Cases (namely, where the Divisor is great, and a Quotient of many places is required, as in calculating Tables of Interest, Astronomical Tables, and such like it excells all other ways of Division, both in respect of certainty and expedition, but for common practice it is too tedious, and therefore I shall proceed to the choisest practical method.

XIII. I now come to the last and principal method of

The latter and choifest practical method of Division, when the Divisor confists of many places. Division, when the Divisor consists of many places, which to such as have the Table of Multiplication by heart will not be difficult; for example, let 56304 be a number given to

be divided by 184, that is, into 184 equal parts, and the Quotient or one of the equal parts is required.

First, distinguish by a point (as before) so many of the formest places of the dividend towards the lest hand, as are either equal in value (when they are consider'd apart) to the Divisor, or else which being greater, yet come nearest unto it, thus I subscribe a point under the figure 3, thereby setting apart 563, being the sewest of the soremost 184) 56304 (places which will contain the Divisor; so is 563 the dividual, or number whereof the first question must be asked. Having thus prepar'd the numbers, I demand how often the Divisor 184 is contained in the dividual 563; and since to answer this question and such like, there is a necessity of tryal, it will be requisite to shew how this tryal may fitly be made: first, there-

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fore compare the number of places in the dividual with the number of places in the Divisor, and when the number of places is the same in both, let it be asked how often the first or extream figure of the Divisor towards the left hand is contained in the first figure of the dividual towards the fame hand; so here demanding how often I is contained in 5, the answer is 5 times, whence I infer that the Divisor 184 is not contained oftner than 5 times in the dividual 563 (for 6 times 184 is manifestly greater than 563) but whether it be contained 5 times in it or not, examination must be made either by multiplying (in some by-place) the Divifor 184 by the faid 5, and comparing the product with the dividual 563; or else thus, saying 5 times I (to wit the I in the Divisor!) is contained in 5. to wit, the first figure of the dividual 563, 5 times, but then 8, the following figure of the Divisor. cannot be found 5 times in 6, the following figure of the dividend, and consequently the Divilor 184 is not contained 5 times in the dividual 563; wherefore I make another tryal to see whether it may be contained 4 times in it or not, faying 4 times 1 is 4. which is found in 5, and there will remain 1, but then 4 times 8, which is 32, cannot be had in 16, (for the 1 before remaining being supposed to stand on the left hand of 6 maketh 16) hence I conclude again, that the Divisor 184 is not contained 4 times in the dividual 563; wherefore I make another tryal to see whether it may be contained 3 times in it or not, faying 3 times I is 3, which is found in 5, and there will remain 2, again, 3 times 8 is 24, which is found in 26 (for the 2 before remaining being supposed to stand before the 6 in. the

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the dividual makes 26) and there will remain 2:lastly, 3 times 4 is 12, which is likewise found in 23, (for the 2 remaining being supposed to stand before the 3 in the dividual makes 23) whereby I see that the Divisor 184 is contained 3 times in the dividual 563, wherefore I write 3 in the Quotient, and proceeding according to the 8th Rule of this Chap-

184) 56304(3 ter, I multiply the Divisor 184 by 3 (the figure placed in the Quotient)

fo the Product is 552; which I subscribe orderly underneath the divi-

dual 563, then having drawn a line underneath the faid Product, I subtract it from the dividual, and subscribe the remainder which is II under the line.

Again, according to the 9th Rule of this Chapter, I bring down o which stands in the next place of the dividend, to the remainder 11, so there is 110 for a new dividual, then demanding how often the Divisor 184 is sound in the dividual 110, and not sinding it once contained in it, I write o in the Quotient (which is to be done as often as the question is answered by nothing;) now because the Producti arising from the multiplication of the Divisor by 0 (the Cypher last placed in the Quotient)

184)56304(306

552 1104 1104 0 amounts to of the dividual 110 out of which that Product should be subtracted, remains the same without alteration; wherefore after a point is subscribed under 4 the following place of the dividend, I annex

4 to the last dividual 110, so there will be a new dividual, to wit, 1104; and here the question at larg is to know how often 184 is found in 1104; but to lessen

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the tryal, because the dividual confists of one place more than is in the Divisor, it must be asked how often the first figure of the Divisor on the left hand is contained in the two foremost places of the dividual towards the left hand, viz. I demand how often 1 is contained in 11, and although it may be had II times, yet I need never begin the tryal above 9 times, therefore I make tryal with 9, faying 9 times I is 9, which is found in II, and there will remain 2; but then 9 times 8 which is 72 cannot be found in 20 (20 because the 2 remaining being supposed to stand before o in the dividual makes 20) therefore I make tryal with 8, faying 8 times 1 is 8, which is found in 11, and there will remain 3, but then 8 times 8 cannot be had in 30 (30 because the 3 remaining being supposed to stand before the o or Cypher makes 30) therefore I make tryal with 7, faying 7 times I is 7, which is found in 11, and there will remain 4; but then 7 times 8 cannot be had in 40, therefore I make tryal with 6, faying 6 times 1 is 6, which is found in 11, and there will remain 5; also 6 times 8 is 48, which is found in 50, and there will remain 2; laftly, 6 times 4 is 24, which is found in 24, whereby at length I fee that the Divisor 184 is contained 6 times in the Dividual 1104, wherefore I write 6 in the Quotient, and proceeding according to the 8th. Rule of this Chapter, I multiply the Divisor 184 by 6 (the figure last placed in the Quotient) so the Product is 1104, which being subscribed under and subtracted from the dividual 1104, the Remainder is o, fo at last I conclude that the Quotient fought is 306.

Note, if the figure assumed for the Quotient holds

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holds good upon tryal, as aforesaid, by two or three of the foremost places of the dividual, it will for the most part hold throughout the dividual; but this must be a perpetual Rule, that whensoever the Product of the multiplication of the Divisor by the figure placed in the Quotient happens to be greater than the dividual, from which it ought to be subtracted, such Product must be struck out of the work, and a leffer figure is to be placed in the Quotient.

For a second Example, let it be required to divide 15114220 by 2987, or into 2987 equal parts.

First, the Divisor 2987 being greater than 1511, (to wit, the four foremost places of the Dividend) I fet a point under 4, thereby fetting apart 15114 for a Dividual; then because the Dividual confists of

14935

one place more than the Di-2987) 15114220 (\$ vifor, I ask how often 2 (the first figure of the Divisor towards the left hand) is contained in 15 (the two fore

179 most places of the dividual) and finding the answer to be 7 times, I infer thence that the Divisor 2987 cannot be contained more than 7 times in the dividual 15114; but whether it will be contained 7 times in it or not, examination must be made, either by multiplying 2987 by 7 (in some by-place) and comparing the Product with the dividual 15114, or else by the manner of tryal before delivered in the last Example : so at length it will be difcovered, that the Divisor 2987 will not be found above 5 times in the dividual 15114; wherefore (according to the 8th. Rule of this Chapter) writing 5 in the Quotient, and multiplying 2987 by 5, I fubk I.

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I subscribe the product of that multiplication, which is 14935, under the dividual 15114, then drawing a line underneath the said Product, and subtracting it from the dividual 15114, I subscribe the remainder 179 under the line.

Again (according to the 9th. Rule of this Chapter) I bring down 2, the next place of the Dividend, to 2987) 15114220(50 the faid Remainder 179, 14935 fo the new Dividual will 1792 be 1792; that done, asking how often the Divisor 2987 is contained in the dividual 1792, and not

finding it once contained in the aividual 1792, and not finding it once contained in it, I write o in the Quotient; and here because the question is answered by o, the next place of the dividend, to wit 2,

is to be brought down to the dividual 1792, fo the new dividual is 17922. Then renewing the question, and proceeding as before, at length the Division be-

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14935 17922 17922 00

ing finisht, the Quotient will be found 5060 exactly, without any Remainder; but if any Remainder had hapned after the subtraction of the last Product, it must have been prosecuted according to the note before given in the example at the latter end of the 11th. Rule of this Chapter.

In like manner if 1208939550 be divided by 19999, or into 19999 equal parts, the quotient, or one of those equal parts, will be found 60450, and the work will stand as here you see.

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This latter method of Divition is to be prefer'd before any of the common ways of dividing by dashing out of figures, where the steps of the Division are

fo confounded (besides the burden upon the memory by a promiscuous Multiplication and Divifion) that if any errour happen, it can hardly be corrected without beginning the work anew; But in the way before explained, the particular Multiplications, Subtractions, and Remainders, which belong to every figure of the Quotient, are fo diflinctly and clearly exprest, that if an errour happen, the work may eafily be reformed.

XIV. So often as the question is repeated in Division, so many places there must How the numbe in the quotient (which may be diber of places in scovered by the number of Points the Quotient placed under the dividend) and fo mamay be discony times is one and the same kind of

operation repeated, the substance whereof is contained in the Verse before mentioned at the end

of the 10th. Rule of this Chapter.

XV. When the Divisor consists of I or an unit A compendious in the extream place towards the left hand, and nothing but Cyphers to way of divis wards the right, the division is perding by 10, 100,1000:190. formed by cutting off with a line fo many places of the Dividend towards the right hand as the Divisor hath Cyphers; so the figures which okI

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which stand on the left hand of the line, give the Quotient, and those cut off to the right (if they be significant sigures) are to be proceeded with as a surplusage or overplus remaining, according to the Note at the end of the eleventh Rule of this

Chapter. So if 4720 l. were given to be divided equally a- 10) 472 0 (472 mongst 10 persons, the share 100) 47 20 (47 of each would be 472 l. also if 1000) 4 1 720 (4

the faid 4720 l. were to be di-

vided equally amongst 100 persons, the share of each would be 47 l. and there would be a surplusage or remainder of 20 l. to be also subdivided amongst them, after the said 20 l. are converted into shillings, according to the fifth Rule of the next Chapter. Lastly, if the said 4720 l. were to be divided amongst 1000 persons, the share of each would be 4 l. and there would be a remainder of 720 l. to be also divided as aforesaid. See the form of the Work in the Margent.

XVI When the Divisor consists of any fignisi-

cant figure or figures in the first or foremost place or places towards the left hand, and nothing but a Cypher or Cyphers towards the right, cut off

Another Compendium in Division.

by a line so many places of the Dividend towards the right hand as the Divisor hath Cyphers towards the right; then divide the figures of the Dividend, which stand on the lest hand of the line, by the figures in the Divisor which remain, when the said Cypher or Cyphers are omitted, remembring after the division is finished, to write down next after the last remainder the places of the Dividend which were first cut off: So if 36732 were given to be

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divided by 20, the Quotient will be 1836, and there will remain 12, viz. if you cut off one place from the Dividend towards the right hand (because the Divisor ends, with one Cypher) and then di-

vide the rest, to wit, 3673

by 2 (according to the 11th.

Rule of this Chapter) there

will arise in the Quotient 1836, and the last remainder, after such division is finisht, will be 1, unto
which if 2 (the figure first cut off from the Dividend) be annexed, the total remainder is 12.

In like manner if 7456787 were given to be divided by 304000, the Quotient will be 24, and there will remain 160787; viz. If you cut off 3 places from the Dividend towards the right hand

(3 places because the 304 000) 7456 787 (24 Divisor ends with 3 Cyphers) and then divide 7456 by 304, there will arise in the Quotient 24, and the last remainder, after

such division is sinisht, will be 160, unto which if 787 (the places first cut off from the Dividend) be annexed, the total remainder or surplusage is 160787, which is to be proceeded with, as is directed in the Note at the latter end of the eleventh Rule of this Chapter.

XVII. Division and Multiplication do interchangeably prove one another; for in Division if you multiply the Divifor by the Quotient, the Product will be equal to the Dividend: So in the

Example of the 13th Rule of this Chapter; if 184

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the Divisor be multiplyed by 306 the Quotient, the Product is 56304, which is the same with the Dividend; but when after the whole Division is finished, any figures remain of the last Subtraction, add them likewise to the Product : So in the last Example of the 16th. Rule of this Chapter, the Divifor 304000 being multiplyed by the Quotient 24, produceth 7296000, unto which if you add the number remaining, to wit, 160787, the fum is 7456787, which is the same with the Dividend. Again, in Multiplication, if the Product be divided by the Multiplicator, the Quotient will give you the Multiplicand, or if the Product be divided by the Multiplicand, the Quotient will give you the Multiplicator : So in the first Example of the 9th. Rule of the last Chapter. if the Product. 111024 be divided by the Multiplicand 3084, the Quotient gives the Multiplicator 36.

There is also of Multiplication a Common proof argued from the Multiplicand, the Multiplicator and the Product, by casting away nines, but by that way of proof (though rightly used) a false Product will be affirmed to be true: Example, if 3462 be multiplyed by 786, the true Product is 2721132; but if I say 4953132 or 3153132 is the Product (or many others which may be given) the proof by nines will confirm them to be true Products, though they are false, as will be evident to such as know the Rule, which I mention here only to set a brand upon it, that it may be avoided

by all lovers of Truth.

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CHAP VII.

Reduction.

I Orasimuch as in Money, there are diversities of kinds, viz. in England, Pounds, Shillings, Pence, and Farthings; also divers kinds of Weights, Measures, &c. as hath been sully declared in the second Chapter; and because it is often times required to find how many pieces of one kind of Money are equal in value to a given number of another (and so likewise of Weights, Measures, &c.) it will be convenient in this place to shew how that is performed, since thereby the Rules of Multiplication and Division before delivered will be exercised; This kind of operation is called Reduction.

II. Reduction is either descending or ascending.

III. Reduction descending is, when some Integers of a number of greater denomination being given, it is required to find how many Integers of a lesser denomination are equal in value to that given number of the greater: As when it is required to find how many shillings are contained in 30l. Likewise how many pence in 320 s. or how many bours in

IV. Reduction ascending is, when some Integers of a number of lesser denomination being given, it is required to find how many Integers of a greater denomination are equal in value to that given number of the lesser: As when it is required to find how many pence are contained in 500 farthings: likewise how many shillings in 348 pence: or how many days in 864 hours: &c. V. Re-

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V. Reduction decending is performed by Multiplication, for if the given number of InReduction detegers of a greater denomination be feending is
multiplied by a number, which expressfeth how many Integers of the lesser are Multiplication
equal to one of the Integers given, the Product is the
number of Integers of the lesser denomination required.

So 230 l. of English Money will be reduced into 4600 s. for if 230 be multiplied by 20 (the number of shillings which are equal to 1 pound) the

product is 4600; in like manner 4600 s. will be reduced into 55200 d. for if 4600 be multiplied by 12 (the number of pence contained in 1 shilling) the product is 55200. Also 55200 pence being multiplied by 4 (because 4 farthings make a penny) are reduced into 220800 Farthings, as by the operation in the Margent is evident.

The like method is to be observed in Weights, Measures, &c. So 345 Ounces Troy are reduced into 6900 Peny weights, and 6900 Peny weights to 2165600 Grains, as by the operation in the Margent you may 138 see.

Note, By this Rule the Learner is furnished with skill to resolve that case in Division, when the Dividend is less than the Divisor:

Compare this with the Note upon the last Example of The 1 1th Rule of the 6th.Chapter.

Example.

Example, Let it be required to divide 7 pounds of English Money equally amongs 8 Persons; here it is evident that the Dividend 7 is less than the Divisor 81; that is, the number of pounds is less than the number of Persons, and consequently each there must be less than a Pound; so that in effect it is required to find how many Shillings and Pence belong to each Person for his share: First, therefore reduce the 7 Pounds into Shillings, which will be 140, these divided by 8 give 17 Shillings to each Person, and there will yet be a remainder of 4 Shillings to be also equally divided into 8 parts, but these 4 Shillings must be first reduced into Pence, which will be 48, then dividing 48 by 8, the Quotient will give 6 Pence more to every Person: so at last it appears that if 7 Pounds of English Money be equally divided into 8 parts, the entire Quotient (or one of the equal shares) will be 17 Shillings and 6 Pence.

In like manner, if 354 Pounds of English Money be given to be divided equally amongst 125 Persons, the share of each will be sound to be 2 Pounds, 16 Shillings, 7 Pence, 2 Farthings, and somewhat more, but the parts of a Farthing being of no moment (and not properly to be handled

in this place) are neglected.

Compare these two Examples with the last Example of the eleventh Rule of the sixth Chapter.

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Pottles Quarts 61

5. Of Dry Measures.

Quarters	7-(8)	(Bushels.
Bushels	12/4/	Pecks.
Pecks	12/2	Gallons.
Gallons	1552	Pottles.
Pottles	1 2 /2 (2 Quarts.
Quarts) \(\big(\frac{7}{2} \)	(Pints.

6. Of Long Measures.

English miles	12(8 .	1	(Furlongs.
Furlongs	ed	220		Yards.
Tards	>=<	3	B.	Feet.
Feet	1	12	Pro	Inches.
Inches) ()	3 -) (Barley Corns.

Also,

7. Of Superficial Measures of Land.

Acres	Z=S4Z=SRoods
Roods	SE 240 E Perches or Poles.
Weeks	8. Of Time.
Dayes Hours	The Stayes. The Stayes of Stayes. The Stayes of Stayes

To reduce Integers of divers denominations of those denominations.

VI. Integers of divers denominations may be reduced into the last of into the lowest those denominations according to the fifth Rule aforegoing, by descending orderly to the next inferiour denomi-

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nation, and adding to each Product such Integers (if there be any) which are of the same name.

So 12 Pounds, 13 Shillings, and 10 Pence may be re-

duced into 3046 Pence in this	l. s. d.
manner, viz. 12 l. multiplied	12 -13-10
by 20 (because 20 s. make one 1.) produce 240 Shillings, un-	20
to which adding 13 s. the fum	240
is 253 Shillings: Again, 253 s.	add 13
multiplied by 12 (because 1	253 Shillings.
shilling is equal to 12 Pence)	12
produce 3036 Pence, unto	506
which if 10 Pence be added,	253
the sum is 3046 Pence, as by	3036
the operation in the Margent	add 10
is manifest.	3046 Pence.

But after that general Method is well understood the work of the last Example, and such like may be contracted thus; viz. To convert 12 Pounds

13 Shillings, 10 Pence, all into Dence, First 12 multiplied by O, 12--13--10 (which stands in the units place 20 of 20) produceth 0, but instead 253 Shillings. of o, I write down 3 under the line (to wit, the 3 that stands 12 in the units place of the 13 shil-516 lings in the fum propounded;) 253 Then I proceed to multiply 12 3046 Pence. by 2, faying twice 2 is 4, to

which adding I (for the ten in the said 13 Shillings) it makes 5, which I set on the lest hand of 3 before written; Lassly, twice I is 2, which I set on the lest hand of 5; And so 12 Pounds 13 Shillings are converted into 253 Shillings.

It remains to multiply the said 253 by 12 (because 12 Pence makes 1 Shilling) and toadd 10 to the Product, which may be done thus; First, twice 3 is 6, to which adding 10 (to wit, 10 pence in the Sum first propounded) it makes 16, wherefore (according to the Rule of Multiplication) I set 6 under the line, and keep 1 in mind; Again, twice 5 with 1 in mind making 11, I write down 1, and keep 1 in mind; Likewise twice 2 and 1 in mind making 5, I write down 5; Then 253 multiplied by 1 makes 253, which I set orderly under \$16; Lastly, those two Products added together makes 3046, which is the number of Pence contained in 12 l.—13 s.—10 d. as before was found out by the general method.

So35 Ounces, 16 Peny Weights, and 12 Grains

Troy will be reduced into 17196 Grains.

VII. Reduction ascending is performed by Direduction of vision, for if the number of Integers
given be divided by such a number
of the same Integers, as are equal to
one of the Integers required, the

Quotient is the number of Integers fought.

So 220800 Farthings being divided by 4 (the number of Farthings in a Peny) give 55200 Pence in the Quotient; In like manner if 55200 Pence be divided by 12 (the number of Pence in a Shilling) the Quotient is 4600 Shillings. Lastly 4600 Shillings being divided by 20 (because 20 s. make a Poundsterling) the quotient is 230 Pounds sterling) which are equal to 220800 Farthings first given. The operation is as solloweth.

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In like manner, 34268 Grains Troy will be reduced to 5 l. 11 Onnces, 7 Peny Weight, and 20 Grains. This kind of Reduction may be made the easier to the Learner by the following Tables.

1. Of English Money.

Farthings 3 5 4 7 Spence.

Pence
Sbillings. Schillings.
Pounds.

2. Of Troy Weight.

Grains
Peny W.
Ounces

12

24

Counces.

Ounces

Pounds Troy.

Also in Apothecaries Weights.

Grains Scruples.
Scruples Scruples.
Drams Sala Solunces Troy.

3. Of Averdupois Weight.

Drams
Ounces
Ounces
Pounds
Pounds
Quarters
Quarters

A
Of

Ounces.

Pounds.

Quarters of C.

Hund. Weight.

4. Of

4. Of Liquid Measures.

Pints	120	2) (Quarts.
Quarts	(2)	2	(a)	Pottles.
Pottles	\ a.	2	5:50) Gallons.
Gallons) Ä(63) (Hogheads.

5. Of Dry Measures.

Pints	7 (2	1 (Quarts.
Quarts	121	121		Pottles.
Pottles	(2)	12	10	Gallons.
Gallons	15	21	1:20	Pecks.
Pecks	10	14	\	Bushels.
Bushels) (8.) (Quarters.

6. Of Long Measures.

Barley C.	121	7. 3-	1	Inches:
Inches	100	12		Feet.
Feet	200	3	33	Yards.
Yards	(5)	220	8:	Furlongs
Furlongs) A (8) (English miles

Also,

Of Superficial Measures of Land.

and the	337	8. (Of Time.
Minutes	つかく	60	Houres.
Houres	534	24	>.25 Dayes.
Dayes	1	-7	Weeks.

Note,

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Note, that if after Division is finisht in Reduction ascending there be any remainder, it is of the same denomination with the Dividend.

Note also, that Reduction descending and ascending do mutually prove one another, by inverting the question; for as in 56 Pounds sterling, there will be found 53760 Farthings, by Reduction descending; So for Proof thereof, 53760 Farthings will be reduced to 56 Pounds, by Reduction ascending.

Queftions to exercise Reduction.

1. In 257 1. how many shillings? Answer, \$140.

2. In 3076 l. how many shillings? Answ.61520.

3. In 902 shillings how many pence? An. 10824.

4. In 2179 shillings how many farthings? Answer, 104592.

5. In 49 1.—13 s.—7 d. how many pence? An-

Swer, 11923.

6. In 2053 l. —14s.—9 d.— 2f. how many farthings? Answ. 1971590.

7. In 354 lb. of Troy weight how many grains

(of Gold-smiths weight?) Answ.2039040.

8. In 300 English miles how many yards? Answer, 528000.

9. In I English mile, how many barley corns

length? Answ. 190080.

10. In 560 Acres how many Perches? Answer 89600.

11. In 225 Acres, 3 Roods, and 30 Perches, how

many Perches? Answ.36150.

In 11923 pence how many pounds? Answer 49 1.—13 s.—7 d.

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13. In 5764684 farthings, how many pounds?

Answ. 6004 l.—17 s.—7 d.

14. In 234678 Perches, how many Acres? An-

fwer, 1466 Acres, 2 Roods, and 38 Perches.

15. In 525960 minutes of an houre, how many days? Answ. 365 days and 6 houres (or I year very near.)

16. In 10080 Pints, how many Hogsheads?

Answ. 20.

17. In 34678 grains of Apothecaries weight, how many ounces Troy? Answ. 72 Ounces, 1 Dram, 2 Scruples, and 18 Grains:

18. In 106735 Pints of wheat, how many Quarters? Answ. 208 Quarters, Bushels, 2 Pecks,

I Gallon, I Pottle, I Quart, I Pinte.

Miles? Answ. 20 Miles, 7 Furlongs, 12 Yards, 2 Feet, 4 Inches, and 1 Barley corns length.

7. In zea lb. of I roy weight how meny grains

o. In a English mile, how many barley corns

ro. In 500 Acres how many Parches? Anlien'

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20. In 1900800 Barley corns length, how ma-

(of Gold-finishs weight?) Ansmy zogono.

ny Miles? Answ. 10.

. CHAP. 225 Acres B Roods, and 30 Perches, how

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CHAP. VIII.

Of the Rule of Three Direct.

THE Rule of Three is fo called, because by three numbers known or given, it teacheth to find a fourth unknown; it is also called the Golden Rule for the excellency thereof; Lastly, it is called the Rule of Proportion for the reason hereafter declared.

II. The Rule of Three is either fingle or com-

pound.

III. The fingle Rule is, when three terms or numbers are propounded, and a fourth pro- The Rule portional unto them is demanded. of Three

IV. Four numbers are said to be proportionals, when the first containeth the second, or is contained by the second in the same manner as the third containeth the fourth, or is contained by the fourth : so these 4 numbers are said to be Proportionals, 8, 4, 12,6, for as 8 containeth 4 twice; for doth 12 contain 6 twice, and therefore 8 is faid to have such proportion to 4 as 12 hath to 6; likewise these are Proportionals, 4, 8, 6, 12. For as 4 is the half of 8, so is 6 the half of 12; and therefore 4 is said to have such proportion to 8 as 6 hath to 12.

V. The terms or numbers of the Rule of Three (to wit, the three numbers given, and the fourth fought) confift of two different denominations, viz. two of the three given terms have one name, and the other given term with the term

The divers denominations of the terms in the Rule of Three.

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required have another: so this question being demanded, if sour Students spend 19 pounds in certain moneths, how much money will serve 8 Students for the same time, and at the same rate of expence? Here Students and pounds are the two denominations of the terms in the question, viz. 4 and 8 (being two of the terms propounded) have the denomination of Students, and 19 the other term given, together with the term required, have the denomination of pounds.

VI. In the Rule of Three, two of the three given terms imply a supposition, and the third moves a question: so in the aforementioned question a supposition is made, that 4 Students spend 19 pounds, and a question is moved with the number 8, to wit, how many pounds will 8 Students

fpend.

VII. In the Rule of Three, the numbers given must be so ranked, that the known The right ordering of the number, or term upon which the queftion is moved, must possess the third germs given. place in the Rule; also of the other two that which hath the same denomination with the third, must be in the first place: lastly, the other known term, which is of the same denomination with the fourth term fought (or answer of the question) must possels the fecond place: fo in the question before mentioned, the terms 4, 19, and 8, are to be thus placed, viz. 8 is the term upon which the question is moved, and therefore to possess the third place in the Rule; 4 is of the same denomination with 8, viz. of Students, and therefore to be in the first place; Lastly, 19 being of the same denomination with the term fought, viz. of money, is to be in the fecond Chap.VIII. of Three Direct 71
second place: and so they will be placed in the Rule thus.

Students. Pounds. Students.

If 4——————————————————————8

That is to say, if 4 Students spend 19 pounds, what will 8 Students spend? And here for the better discerning of the term or number upon which the question is moved, you may observe, that for the most part it is the known number in the question which immediately solloweth these or such like words; viz. How many? How much? What will? How long? How far? &c.

VIII. The Rule of Three is either Direct or

Inverse.

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IX. The Rule of Three Direct is, when the fense or tenour of the question requireth, The Rule of that the fourth number fought must Three Direct. have fuch proportion to the fecond, as the third number hath to the first ; so in the afore-mentioned question, if 4 Students spend 19 pounds, how many pounds will 8 Students spend at the same rate of expence? It is evident that the thing required is to find a number which may have fuch proportion to 19, as 8 hath to 4; that is, as 8 is the double of 4, so ought the fourth number to be the double of 19; for if 19 pounds be required to maintain 4 Students a certain time, as much more must needs be required for the maintenance of 8 Students the same time; and therefore in this case we may fay in a direct proportion, as 4 is to 8, fo is 19 to a number which ought to be as much more as 19:

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X. In the direct Rule of Three, if you multiply the second term by the third, or (which is all one) the third term by How to work the second, and then divide the Product by the first, the quotient will give

the Rute of Three Direct, the three given terms beingfingle nambers.

nal required: so in the question before propounded, if you multiply 19 by &, the product

the fourth term or fourth proportio-

is 152, which if you divide by 4, the quotient will give you 38 the fourth term demanded, and the work will

stand thus.

Stud. l. Stud. l. 4) 152 (38 pounds 12

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A fecond Example may be this, if 8 yards cost 9 pounds, how much will 3 yards coft? Answer, 3 1,-

This question being stated according to the se-0

-(3:7:6 8)27 (3 pounds 3 the remainder. 20 8) 60 (7 Shillings. 56 4 the remainder

8)48(6 pence

venth Rule of this Chapter, will stand as here you see; then multiplying (asbefore) the second term 9 by the third term 3, the Product is 27, which being divided by the first term 8, the quotient is 3 pounds, and there is a remainder of three pounds, which must be reduced into 60 shillings, and after those shillings are divided by 8, and the rest of the workprofecuted according to the ok I

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Note at the latter end of the 11th Rule of the 6th. Chapter, at length the entire quotient or answer of the question is 3 1. - - 7 s. - 6 d.

A third Example, if 51 ounces of filver plate be fold for 13 pounds sterling, what is the price

of I ounce of that plate? Anf.5 s .-- I d. and fomewhat more. The operation is thus: After the three known terms of this question are rightly ordered, they will stand as here you fee in the Example; 51)260 (5 shillings. then multiplying the fecond term 13 by the third term 1, the product will be also 13 (for multiplication by I makes no alteration;) which 13 being divided by 51, after the manner of operation

03. 1. 02. 501113 No. 4161-1100 20 1 Sharpage of 255 51) 60 (1 peny.

delivered in the note upon the 5th Rule of the 7th Chapter, the entire Quotient or answer of the question will at length be found to be 5 s .- I d. and somewhat more, but the surplusage being less

than a farthing is omitted as useless.

Example 4. What must be paid to a labourer for his wages for 27 weeks at the rate of 4 s. for 1

week? Answer, 51.-8 s. After the three given terms are rightly placed inthe

Rule, they will stand as you fee in the Example; then multiplying the third term 27 by the fecond term 4, the product is 108, which I

should divide by the first term 1, but in regard F 3 · divition

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division by 1 makes no alteration, the Quotient is also 108, so that the fourth term sought is 108 shillings, which being reduced to pounds, according to the seventh Rule of the seventh Chapter, give 5 1.8 s. for the answer of the question.

XI. In the Rule of Three, if after the question

divers denomi nations.

is stated according to the seventh To prepare the Rule of this Chapter, any of the 3 Rule of Three, given terms be a compound term conwhen they are fifting of divers denominations, as compounded of pounds, shillings, and pence; or weeks, days, hours, &c. such compound term must first be reduced into the lowest

of those denominations (by the fixth Rule of the feventh Chapter) to the end that the three given terms may be three fingle numbers; also of these three fingle numbers the first and third must always be of one and the same denomination: for if it happen that they express things of different names, fuch of the two which hath the greater name (or denomination) is to be reduced into the same name with the leffer (by the 5th Rule of the feventh Chapter:) These preparations being obferved, the rest of the work is to be prosecuted according to the tenth Rule of this Chapter. ample, what will 48 ounces, 17 peny weight, and 20 grains of filver plate amount unto at the rate of 5 s .- 6 d. the ounce? Answer, 13 l. 8s.—10d.—3 f.very near.

This question oz. d. 1-5-6-48-17-20 being stated according to the 20 12 feventh Rule of this Chapter, will 24 24 stand in the Rule as you fee in the 1954 Example, to wit, 23468 grains. if I ounce cost

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will 48 oz.—17 p.m.—20 gr. cost? Here because the third term is compounded of divers denominations, it must be reduced into the lowest of those denominations, to wit, grains; so by the sixth Rule of the seventh Chapter there will be found 23468 grains for the third term: likewise, because the second term 5 s.—6 d. is a compound term, whose lowest name is pence, it must be reduced into pence (by the asoresaid rule;) so there will be sound 66 pence for the second term: moreover because the first term hath the name ounce and the third term the name grain, the first term 1 ounce must be converted into 480 grains (which are equal to 1 ounce;) then will the three terms or single numbers stand in the

rule, as here you see, viz. gr. pence. gr. if 480 grains cost 66 480-66-23468

pence, how many pence will

23468 grains cost? Now proceeding according to the tenth Rule of this Chapter, there will arise in the quotient 3226 pence, besides a remainder of 408 pence, which being reduced to 1632 farthings, and those

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those divided by the first term 480 the quotient will be 3 farthings, so that the entire quotient is 3226 pence, 3 farthings, and somewhat more (but the parts of a farthing being of no moment, may be neglected.) Lastly, the said 3226 pence being reduced according to the seventh Rule of the seventh Chapter, give 13 l.—8 s.—10 d.—3 f. so that 13 l.—8 s.—10 d.—3 f. and somewhat more, will be the Answer of the Question:

XII. For the proof of the Direct Rule of Three The proof of the multiply the fourth term by the first, Rule of Three which done, if that Product be equal direct. to the Product of the second term multiplyed by the third, the work is right, otherwise it is erroneous: so in the first Example, 38 the fourth term, being multiplyed by the first term 4, the Product is 152, which is also the Product of 19 multiplied by 8. But if it happen that after the fourth term, or answer of the question is found in the same denomination with the second term, there is yet a remainder, such remainder must be added to the Product of the first term, multiplyed by fuch fourth term, and then the fum must be equal to the Product of the second and third terms (the fecond term confisting of the same denomination with the fourth:) so in the last Example the fourth term is 3226, and there happens to be a remainder of 408, which being added to the Product of the multiplication of the faid 3226 by the first term 480, gives 1548888, which is the same with the Product of the third term 23468 multiplyed by the second term 66 as will appear by the work.

When the first of the three given numbers in the Rule of three Direct, Acompendious operatis I or unity, the question may of tion in the Rule of tentimes be answered more spee-three direct, when the dily than by the Rule of Three, first term is I or unity even by those who have but little skill in Arithmetick, as will partly appear by the following Examples, viz.

1. At 17 5.—9 d. the yard, what will 84 yards cost? Answer, 74 l.—11 s. For reason sheweth that 84 yards must (at the said rate) cost 84 Angels, 84 Crowns, 84 half Crowns, and 84 Three pences, all which being compueded added together, will give the sull value of 84

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84 Angels make-	42	-00-	-00
84 Crowns———	2]	-00-	-00
84 half Crowns	10-	-10-	-00
84 Three-Pences	1-	-01-	-00
San Transfer to the contract and	Sum 74-	-11-	-00

2. At the rate of 9 s. the Bushel of Wheat, what will 51 Quarters amount unto? Answer, 183 l.—12 s.—0 d.

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It is evident that the price of 1 Quarter (which confifts of 8 Bushels) will be 8 Angels wanting 8 Shillings; therefore

of Three, full services and or main	stort lein wise de vd.
	4-00-00
Subtract -	0-08-00
And the second s	Thought the same

remains the price of 1 Quarter --- 3 -- 12 --- 00

Then the value of 51 Quarters, at the rate of 3 l.—12 s.—od. the Quarter, may be found in manner following. Viz.

to as onest not our said man	I.	5.	d.
Street or commission of the last terms	151-	-00-	-00
51 times 3 l. or 3 times 51 l. is	>51-	-00-	-00
00-00-404		-00-	-00
51 Angels make	-25-	-10-	-00
51 Shillings doubled make	- 5	-02-	-00
the price of 51 Quarters	183-		-00

3. What is a Chest of Sugar worth, that weighthere is that wherein subtracted) 7 C. 3 q. 7 lb. at any thing is put, as a the rate of 6l.—3s.—4 d. Bug for Pepper, a Chest for I C? Answer, 48l.—3s.—6 d.—2 f.

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Practical rules of this nature cannot be compleatly understood without some skill in fractions, as will hereaster appear in the second Chapter of the Appendix: and therefore I shall conclude this Chapter with the following Questions, whose Answers are annexed to them, and may be found out by the preceding Rules; but the operations are purposely omitted, and left as an exercise for the Learner.

Questions to exercise the Rule of Three direct.

1. If 17 yards of Cloth cost 19 l.2 s.6 d.what will 35 yards cost at that rate? Answer, 39 l.7 s.6 d.

2. If 35 yards cost 39 l. 7 s. 6 d. how many yards may be bought at that rate for 19 l. 2 s. 6 d. Answer, 17 yards.

3. If 35 yards cost 39 l. 7 s. 6 d. what are 17 yards worth at that rate? Answer, 19 l. 2 s. 6 d.

4. If 17 yards be fold for 191. 2 s.6 d. how many yards will 39 l. 7 s. 6 d. buy at that rate? Answ. 35 yards. 5. What

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5. What must I pay for the carriage of 17 hundred weight, 3 quarters, and 11 pounds Averdupois, at the rate of 7 shillings the hundred weight? Answ. 6 l.—4 s.—11 d.—1 farth.

6. If 61.—4 s.—11 d.—1 f. be pay'd for the carriage of 17 hundred weight, 3 quarters, and 11 pounds, what was pay'd for the carriage of 1

pound weight? Answ. 3 Farthings.

7. What must I pay for 39 ounces, 7 peny weight, and 18 grains of white plate at the rate of 5 s. and 5 d. the ounce? Answ. 10 l.—13 s.—4 d. and three quarters of a farthing.

8. What must 1 l. (or 20 s.) pay towards a Tax, when 326 l.—6s.—8d. is affessed at 41l.—16 s.—

2 d.-3 f? Answ. 2 s.-6 d.-3 f.

9, What will the Interest of 8761.—17 s.—6d. amount unto for 1 year at the rate of 61. for 1001. for the same time? Answ. 52 l.—12 s.—3 d.

10. If 3 yards in length of English measure be equal to 4 ells Flemish; how many Flemish ells are contained in 120 yards English? Answer 160 Flemish ells.

11. If 4 Flemish ells in length, be equal to 3 English yards; how many English yards in 300 Flemish ells? Answ. 225 English yards.

12. If 3 ells in length of English measure, be equal to 5 Flemish ells; how many Flemish ells in

120 English ells? Answ. 200 Flemish ells.

13. If 5 Flemish ells in length, be equal to 3 English ells; how many English ells in 145 Flemish

ells? Answ. 87 English ells.

14. If 3 Ounces of Silk weight, be equal to 4 ounces of Venice weight; how many ounces Venice are equal to 60 ounces of Silk weight? Answer 80 ounces Venice.

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15. A Merchant delivered at London 120 %. sterling, to receive 207 l. Flemish at Amsterdam; what was I 1. sterling valued at in Flemish money? Answ. 11,-14s.-6d.

16. If a Bill of Exchange be accepted at London, for payment of 400l. sterling, for the value diliver'd at Amsterdam, at 1 1 .- 13 s .- 6 d. Flemish for I l. sterling; how much Flemish money was deliver'd at Amsterd im? Answ. 6701. Flemish.

17. When the Exchange from Antwerp to London is at 11 .- 4s .- 7 d. Flemish for 1 l. sterling; how much sterling must I pay at London to receive 236 l. Flemish at Antwerp ?. Answ. 192 l. sterling.

18. A Merchant deliver'd at London 370 l. fferling by Exchange for Roan at 74 d. Sterling for 50 s. Tournois; how much Tournois ought he to receive at Roan? Answ. 60000 s. Tournois.

19. In 370 Ducats, at 4 s .- 2 d.the Ducat; how many French Crowns at 6s .- 2 d. Answ. 250 Crowns; For if 74 d. give I Crown, 18500 d.(or

370 Ducats) will give 250 Crowns.

20. In 516 Dollers, at 4 s .- 5 d. the Doller; how many Guinneys at 1 l.-1 s.-6 d. the piece? Answ. 106 Guinneys; For if 258 d.give I Guinney, 27348 d. (or 516 Dollers) will give 106 Guinneys.

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CHAP IX.

Of the Inverse Rule of Three.

HE Rule of Three Inverse is, when the fourth term required ought to proceed from the fecond term, according to the same rate or proportion that the first proceeds from the third: fo this question being propounded, if 8 Horses will be maintained 12 dayes with a certain quantity of Provender, how many dayes will the same quantity maintain 16 Horses? Here as 8 is half 16, so ought the fourth term required to be half 12; for if certain bushels of Provender serve 8 Horses 12 dayes, 16 Horses will eat up as much Provender in half that time: and therefore you cannot say here in a direct proportion (as before in the Rule of Three direct) borses dayes borses as 8 to 16, so is 12 to ano-8-12-16 ther number which ought to be in that case as great again as 12; but contrariwife by an inverted Proportion, beginning with the last term first, as 16 is to 8, so is 12 to another number, which ought to be in this case half 12. And by the due observation of this definition, together with that of the Rule of Three Direct (propounded in the ninth Rule of the eight Chapter) when any question belonging to the fingle Rule of Three is propounded, you may readily discern by which of those Rules it ought to be refolved; for if the three terms given look for a fourth

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fourth in a direct proportion as they stand ranked in the Rule, you must resolve the question by the direct Rule; contrariwise when the proportion is inverted or turned backwards, it ought to be resolved by the Inverse Rule of Three, which here followeth.

II. In the Inverse Rule of Three, after the three given terms are rightly placed in the Rule, and reduced (if there How to work be need) according to the eleventh the Inverse Rule of Three. Rule of the eighth Chapter, multiply

the first term by the second, or (which is the fame) the second term by the first , and then divide the Product by the third term, fo the quatient will give you the fourth term required, or answer of the question; thus in the question premised in the last Rule, if you multiply 12 by 8, the Product is 96, which if you divide by 16, the Quotient gives you 6, the fourth term required, as by the subsequent operation is manifest.

borses dayes borses dayes 16)96 (6 96

III. For the more ready discovering, whether a question propounded belongs to the Rule of Three Direct, or to the Rule Inverse, observe the directions following, Viz. 1. By resolved by the Rule the sense and tenour of the question consider, whether more be

How to discern when ther a question in the Rule of Three is to be Direct, or by the Rule

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required or less; that is, whether the number fought must be greater or less than the second term: Secondly, esteeming the first and third terms as extreams inrespect of the second, this will be a general Rule; namely, When more is required, the leffer extream is the Divisor ; but when less is required, the greater extream is the Divisor. Lastly, the Divisor being found out, it will be apparent whether the Rule be direct or Inverse, for when the Divifor is the first term, it is a Rule Direct; but when the Divisor is the third term, the Rule is Inverse. Another Example of the Rule Inverse may be this; If 12 Mowers do mow certain Acres in 4 dayes, in what time will 23 Mowers perform the same work? Answer, 2 dayes, 2 hours, and

22) 48 (2 dayes 23) 48 (2 bours.

somewhat more. Here, D. M. the 3 known terms being rightly placed in the Rule, will stand as you fee in the Example; and tince it is evident that 23 men will require less time than 12 men to finish the fame work, therefore (by the Rule aforegoing) the greater of the two extream numbers 23 and 12 must be the Divisor; and because the Divisor 23

stands in the third place, this question is to be wrought by the Rule Inverse; wherefore multiplying the first term 12 by the second term 4, the product is 48, which being divided by the first term 23, the Quotient gives 2 dayes, and there is a remainder kl.

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mainder of 2 dayes, which being reduced to hours, and those divided by 23, the Quotient will be 2 hours, and there is yet a remainder of 2 hours to be subdivided into 23 parts if you please; so that the fourth term fought, or answer of the question

is 2 dayes, 2 hours, and somewhat more.

Again, take this for a third Example, If I lend my Friend 356 pounds for one year and 35 dayes (the year being supposed to consist of 365 dayes.) how long time ought he to lend me 500 pounds to require my courtesse? Answer, 284 dayes and fomewhat more, there being a remainder, to wit 400, after the Division is finish'd, as by the subsequent operation is manifest.

multiply \$400 5100)1424100 (284 dayes.

IV. The proof of the Inverse Rule of Three is this, multiply the third term by the fourth, then if this Product be e-The proof of the Rule qual to the Product of the first term Three Inverse. multiplyed by the second, the work is true, otherwise erroneous; so in the Example of the second Rule, the Product of 16 and 6 is equal to the Product of 8. and 12 But if it happen

happen that after the fourth term, or answer of the queltion, is found in the fame denomination with the second term, there is yet a remainder, such remainder must be added to the Product of the third term multiplyed by the fourth, and then the fum must be equal to the Product of the first and fecond terms (fuch fecond term being of the same particular denomination with the fourth:) fo in the last Example, the fourth term is 284 dayes, and there remains 400 after the division is finisht, this 400 being added to the Product of the Multiplication of the third term 500, by the fourth term 284 gives 142400, which is equal to the Product of the first term 356, multiplyed by the second tetm 400 dayes.

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The double Golden Rule Direct, performed by two single Rutes. dering of the terms of supposition, which of

HE Compound Golden Rule is, when more than 3 terms are propounded.

them hath the lame denomination

II. Under the Compound Golden Rule, is comprehended the double Golden Rule, and divers Rules of plural proportion. have the fame denomination with

III. The double Golden Rule is, when five terms being propounded, a fixth proportional unto them is deman- The double Golden Rule. ded: as in this question, If 4 Students spend 19 pounds in 3 moneths, how much will serve 8 Students 9 moneths? Or this, if 9 Bushels of Provender serve 8 Horses 12 dayes, how many dayes will 24 Bushels last 16 Horses?

IV. The five terms given in this Rule confift of two parts , Viz. A supposition expressed in the three first terms and a The parts into which the terms demand propounded in the two last: of the Same rule So in the first Example of the last are distributed. Rule, this Clause (if four Students spend 19 pounds in 3 moneths.) is the supposition, and this (how much will ferve 8 Students nine G 2 moneths)

The double Rule Book 888 moneths) is the demand : likewise in the other Example of the same Rule, this clause (if nine Bushels of Provender Serve 8 Horses 12 dayes) is the supposition, and this (How long, or how many dayes will 24 Bushels last 16 Horses) is the demand propounded: The slds V. Here for ranking the terms propunded in their due order, first observe amongst the terms of supposition, which of The right orthem hath the fame denomination dering of the terms. with the term required; then referving that term for the second place, write the other two terms of supposition one above another in the first place; and lastly the terms of demand likewise one above another in the third place of the Rule, in such fort that the uppermost may have the same denomination with the uppermost of those in the first place : Example, if 4 Students spend 19 pounds in 3 moneths, how much will ferve & Students 9 moneths? Here the three terms of supposition are 4, 19, and 3, and of these terms 19 hath the same denomination with the term required, Viz. of Pounds, for you are to enquire how much Money is requilite for the maintenance of 8 Students 9 moneths; wherefore referving 19 for the fecond place I write 4 and 3 one above another thus; then drawing a line upon the right hand of 4, I write 19 in the second place; this done, the work will stand as in the Margent; Last of all, the terms of

demand being 8 and 9, and 8 having the denomination of Students, I place it in the fame line with 4 and 19, and write 9

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under it; all this performed, the terms in this question rank themselves as followeth : 1000 300 of the laft place to the term required.

So in this Example, and P. siveited

28 to ment tova term of the figit place as a common number in the fift proportion , widt to. I. If 4 Studente frender or preside (in three moments | wast will ferve 845tudents (the

In like manner, if the fecond question of the third Rule of this Chapter were propounded, the terms thereof ought to be disposed and distant direct (by the third Rule of the ninth Chapter;)

therefore the flerth proportional adledding

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Again, to had the term required, ann sudseio, the

nominos a comentario ten common a common de la common de Number in this lader opertion fay 8 followers.

II. Win three moneths 38 pounds are spent (by Q MI. Questions belonging to the double Golden Rule may be resolved by two single Rules of Three, or by the Golden Rule Compound offive Numbers od bliwalil like and Tho day and war

VII. When Questions of The Proportions of the this nature are resolved by double Golden Rule, two fingle Rules, the propor- when it is performed by tions are as followeth: 100 fingle Rules.

before recited) to be it to, for 38 being multiply-L As the uppermost term of the first place, is to the middle term; So is the uppermost term of the last place to a fourth months, 144 pounds v.radmun 8 butdents

II.

The double Rule Book I. 90 II. As the lower term of the first place is to that fourth Number; so is the lower term of the last place to the term required. So in this Example before recited, 4-19-8 using tacitly the lower term of the first place as a common number in the first proportion, say thus, I. If 4 Students spend 19 pounds (in three moneths) what will ferve 8 Students (the fame time ?) Orthus, If 4 Students spend 19 pounds, what third Rule of this Chapter wers brigh Bollist, the Which Rule of Three will be discovered to be direct (by the third Rule of the ninth Chapter;') therefore the fourth proportional proceeding from the faid three given numbers 4,19, and 8 is 38 (by the 10th Rule of the 8th Chapter aforegoing.) Again, to find the term required, uling tacitly the uppermost term of the third place as a common Number in this last proportion, Say as followeth. II. If in three moneths 38 pounds are spent (by Students) how much will ferve them for 9 Rule may be resolved by two sis edtagomles of ordorthus, If 3 give 38, what will 9 yield you dir Which Rule of Three will likewise be discovered to be direct (by the third Rule of the minth Chapters) therefore the fourth proportional proceeding

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Which Rule of Three will likewise be discovered to be direct (by the third Rule of the minth Chapter) therefore the sourth proportional proceeding from the said 3 numbers, 3,38, and 5 year shall likewise find (by the 10th Rule of the 8th Chapter before-recited) to be 114, for 38 being multiplyed by 9, the Product is 342, which divided by 3 yields you in the Quotient 114: So that I conclude, If sour Students spend nineteen pounds in three moneths, 114 pounds will serve 8 Students

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101 32 1 84 flos	of 8 C. weight 12 8 miles
	how much may 12 Lve 4 C.
	cording to the hoh Rule

In like manner if two single Rules of Three be formed (according to the preceding 7th Rule) out of the five numbers given in the last mentioned question, the same being ranked according to the latter manner of ordering the said numbers in the fifth Rule, each of the said two Rules of Three will be a Rule direct, and the same answer of the squession, to wit, 114 pounds will be discovered, as you may see by the subsequent operation.

Here it is cate to differ that the fewer miles less motey will pay for 4-157-8-(1144) 19-9-(157 number fought &v the faid Kule of Three must be les than 411) 324 (4 be 25 30) 1710(574 th Chapter, Then less casa (whetherett ne the is required, the proster t be the Diving; therefirst or third number) mu the Dividos and con-100176 above propounded is a 11 Th enus drauol adi tuo so

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VIII. The double Golden Rule is either Direct

IX. The double Golden Rule Direct is, when both the fingle Rules do each of them look for a fourth term in a direct proportion: As in the ExThe double Gol- ample of the seventh Rule, where each den Rule Direct. of the two single Rules of Three is a Rule Direct.

For another Example take this, if the carriage of 8 C. weight 128 miles, cost 48 shillings, for how much may I have 4 C. weight carried 32 miles after the same rate? The terms of this question according to the fifth Rule of this Chapter, rank themselves in this order:

Now taking tacitly the lower term of the first place as a common number, I form the first Rule of Three according to the seventh Rule, saying.

1. If the carriage of a certain weight (to wit, 8 C.) 128 miles will cost 48 shillings, what will the carriage of the same weight 32 miles cost?

Here it is easie to discern, that the sewer miles any weight is carried, the less money will pay for the carriage of that weight; therefore the fourth number sought by the said Rule of Three must be less than the second number 48: And sorasmuch as by the third Rule of the ninth Chapter, when less is required, the greater extream (whether it be the first or third number 128 is the Divisor; therefore the first number 128 is the Divisor, and consequently the Rule of Three above propounded is a Rule direct; wherefore finding out the fourth number

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CHAP.

ber by the tenth Rule of the eighth Chapter to be 12 shillings, I proceed to the second proportion, and say:

II. If the carriage of 8 C (32 miles) cost 12 shillings, how much must I give to have 4 C, carried the same distance:

And here likewise finding a sourth number to be looked for in a direct proportion, I discover that sourth, by the said tenth Rule of the eighth Chapter, to be 6 s. which is the term domanded, and the answer to the question propounded: so that at last I conclude, If the carriage of 8 C. 128 miles cost 48 s. the carriage of 4 C. 32 miles will cost 6 s. according to the same rate: see the whole Work.

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And then work by two lingle Rules of Three,
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of Three will be inverte, and the latter directs
of Three will be inverted and the latter directs, for faying first, if 8 horse maintained an dayes
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answer 6 dayes will 1875 and out by the Rule of
Three inverte: Second 25 faying, if 9 bullels of
Provender be catenupo by 16 horfes) in 6 dayes, in
how many dayes will a 4 bullels be fpent? here the
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The Double Golden Rule Inverse, performed by two single Rules.

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THE Double Golden Rule Inverse is, when one of the single Rules looks for a fourth term the double Gol. in an inverted proportion: As in the den Rule In- last Example propounded in the fifth Rule of the last Chapters. For if you rank the terms of that question, according to the said fifth Rule, thus.

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And then work by two single Rules of Three, formed according to the seventh Rule of the last Chapter, you shall find by the third Rule of the ninth Chapter, that the first of the said two Rules of Three will be inverse, and the latter direct; for saying first, is horses be maintained 12 dayes (by 9 bushels of Provender) how many dayes will 16 horses be kept by so much Provender? Here the answer 6 dayes will be found out by the Rule of Three inverse: Secondly, saying, if 9 bushels of Provender be eaten up (by 16 horses) in 6 dayes, in how many dayes will 24 bushels be spent? here the answer 16 dayes will be found out by the Rule of Three direct.

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And then work by two single Rules of Three; formed according to the seventh Rule of the last Chapter, you shall find by the third Rule of the ninth Chapter, that the first of the said two Rules of Three will be Direct, and the latter Inverse for saying first, It 9 bushels of Provender will last 12 dayes (to maintain 8 horses) how many dayes will 24 bushels serve the same number of horses? The answer 32 dayes will be found out by the Rule of Three direct. Secondly, saying, It 8 horses will be maintained 32 dayes (by 24 bushels of Provender) how long will 16 horses be kept by the same quantity of Provender? Here the answer 16 dayes will be found out by the Rule of Three direct.

Wherefore, whenfoever a question belonging to the double Rule of Three is severed into two single Rules of Three (according to the preceding Rules) if one of them happens to be a Rule inverse, that double Rule is called the double Rule inverse.

Now the Resolution of the Question propounded being ranked after the first manner, is as solloweth.

Again, The Refolution of the fame Questionbeing ranked after the last manner, is this:

venth Rule of the laft Chapter, you that find by the time nuise of the ninth Chapter, that the fifth of the faid two Rules of Three will be Direct 12 dayes (to maintain 8 herfes) how many dayes will 24 buthels ferve the fame number of hories? The answer a dayes will be found out by the Rule maintained as dayes (by 24 bulbels of Provender) holl lo 45 170 holl or 180 by the fame quantity of Provender ? Here the antwer 16 dayes will be found out by the Rule of Three direct, Where He then Cer a queltion belonging to the double Kull of Three is levered into two fingle Rules of Three (according to the preceding Rules) if one of then happens to be a Rule inverfithat double Rul # called the double Rule inverte Now the Relatedon of the Question propositded being ranked after the first manner, is as tolloweth.

Again, The Resolution of the same Question, being ranked after the last manner, is this:

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HE Golden Afte compound of five numfore, inflead of \$10 design tended, as bee'thens we use their produde, and then proce ?? to find the term required by one fingle Rule of hree.

If. Here when the Caefiton proposaded ought to be performed by the double Rule to be performed by the double Rule to be performed by the double Rule. to be performed by the double Rule direct, multiplying the terms of Rule compound the first place, the one by the other, of feve numper formed terro, the middle number for thefeown odn to 18 org 32 16 (16 Borth share laft terms for the third toen, this done, baving

found by the Rule of T ee direct, a fourth proof mrst de 16) 256 (16) one fancting found is the number you lotte tot; to this quefish being again propounded, if a Students found

ry hing moneths how muck will firve 8 Students o moneche? and the verms Secret being ranked as be lore vire thur.

So that at last I say, If 9 Bushels of Provender serve 8 Horses 12 dayes, 24 Bushels will last 16 Horses 16 dayes, which is the resolution of the Question propounded, CHAP.

98 The Rule of Three compound Book I.

CHAP. XII.

The Golden Rule compounded of five Numbers.

42

I. THE Golden Rule compound of five numbers is, when the terms being ranked, as before, instead of the double terms we use their products, and then proceed to find the term required by one single Rule of Three.

II. Here when the Queftion propounded ought

to be performed by the double Rule The Golden direct, multiplying the terms of Rule compound the first place, the one by the other, of five numtake their product for the first bers performed by one single term, the middle number for the fe-Rule direct. cond, and the product of the two last terms for the third term; this done, having found by the Rule of Three direct, a fourth proportional unto those three? that fourth term fo found is the number you look for: fo this question being again propounded, if 4 Students spend

19 l. in 3 moneths, how much will serve 8 Students

9 moneths? and the terms thereof being ranked as before, viz. thus,

The product of a multiplyed by 3 is 12, and the product of 8 multiplyed by 9 is 72; wherefore I fay, As 12 to 19, so 72 to the term required, which I find by the single Rule of Three direct to be 114.

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So that if 4 Students spend 19 1. in three moneths. 114 l. will be requisite for the maintenance of 8 Students 9 moneths, see the whole operation, as followeth,

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term by which it is prod 84 verse proportion be tour 84 in find the term required by the tingle Rule of Three

direct : But in cafe you had

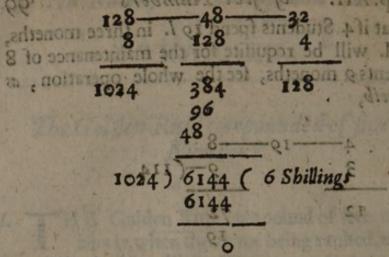
In like manner this being the Question as before (in the last Rule of the tenth Chapter) if the carriage of 8 C. 128 miles, cost 48 s. what will the carriage of 4 C. 32 miles stand me in? the Answer thereunto will be 6 s, as appears by the Work.

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tivil line, as is observed in the last

And therefore having subferibed the

100 The Rule of Three compound Book I.



III. When the Question propounded ought to

The Golden Rule compound af five Numbers performed by one fingle inver fe.

be resolved by the double Rule Inverse, having multiplyed the double terms a crois, that is, the uppermost term of the first place by the lower Rale diret or of the last, and the uppermost of the fast place by the lower of the first, write each product under the lower

term by which it is produced: and then if the inverse proportion be found in the uppermost line, using those products as single terms, proceed to find the term required by the tingle Rule of Three direct : But in case you find the Inverse proportion in the lower line, perform the Work by the fingle Rule of three Inverse.

So in the Example above mentioned, if 9 bushels of Provender serve 8 horses 12 dayes, how long will 24 bushels last 16 horses? Here -16 if you rank the terms thus , you shall 24 find the Inverse proportion in the

first line, as is observed in the last Chapter: And therefore having subscribed the

products

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Chap.XIII. The Rule of Three compound 101

products according to the direction given you in this Rule, I proceed to satisfie the demand of this question by the fingle Rule of Three direct, asap-

pears by the Work following.

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But the terms of this Question being ranked zbus, the Inverse proportion is

found in the lower line, as you 9-12may observe likewise by the last 8

Chapter: whereupon in this cafe,

to resolve the Question, I proceed by the single Rule of Three Inverse, as appears by the Work hereunto annexed : howfoever therefore you work the Question, you shall find the term required to be 16; fo that at last I conclude, as before in the laft Chapter, IF 9 bushels of Provender seive 8 horses 12 dayes, 24 bushels will last 16 horses 16 dayes on cantingmoles at the molestic aminopol s of grand Hargings and then ones on

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CHAP. XIII.

The Rule of Fellowship.

I. THE Rules of plural proportion are those,
by which we resolve Questions, that are
discoverable by more golden Rules
Rules of plural than one, and yet cannot be perproportion. formed by the double golden Rule
mentioned before in the three last
Chapters. Of these Rules there are divers kinds
and varieties, according to the nature of the question propounded; for here the terms given are
sometimes sour, sometimes sive, sometimes more, and
the terms required sometimes more than one, &c.

II.

Chap.XIII. The Rule of Fellowship. 103

II. Two particular Rules of plural proportion are these, the Rule of Fellowsbip, and the Rule

of Alligation.

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III. The Rule of Fellowship is that, by which in accompts amongst divers men (their several stocks together with the whole Fellowship. gain or loss being propounded) the

gain or loss of each particular man may be discovered: As in this Example, A and B were tharers in a parcel of Merchandize, in the purchase of which A laid out 7 l. and B 11 l. and they having fold this Commodity, find that their clear gains amounts to 54s. Now here the Question to be resolved by this Rule is, what part of that 54 s. accrews to A, and what to B, according to the rate of the several sums or stocks which they adventured? Again, A, B, and C, fraight a Ship from the Canaries for England, with 108 Tuns of Wine, of which A had 48, B 36, and C 24, the Mariners meeting with a florm at Sea, were confrained for the fafety of their lives, to cast 45 Tun thereof over-board; here the Question to be refolved is, How many of the 45 Tun each particufar Merchant hath loft, according to the rate of his Adventure?

IV. The Rule of Fellowship is either single or double.

V. The single Rule is, when the stocks propounded do continue in the Adventure (or common Bank) equal times, to wit, one stock as long time as another.

VI. In the fingle Rule of Fellowthip, take the total of all the stocks for the fingle Rule the first term, the whole gain or lose,

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The Rule of Fellowship Book I 104 1 for the fecond, and the particular flocks for the third terms; this done, repeating the Rule of Three so often, as there are particular stocks in the Question, the fourth terms produced upon those several operations, are the respective gains or losses of those particular stocks propounded: So in the first Example above-mentioned 7 l.and 1 1 l. are the flocks propounded, whose total is 18 1. which I take for the first term: Again, 54 s. the common gain, is the second term, and 7 1. the first particular stock ; is the third term of the first proportion; whereupon I fay, as 181. to 54 s. for 7 1. to another number, which by the direct Rule of Three kind to be 2 rive vize the part of the gain due to A, that expended the 7 1. flock. Then for the second proportion, I say, as 18 1. to 540. so 11 l. to another number, which I likewise find by the Rule of Three direct to be 33 s. viz. the part

of the gain due to B, for his II I flock to an W

Again, in the other premised Example, the particular loss that happens to A, is 20 Tun, to B 15, and to C 10 Tun.

VII. The double Rule of Fellowship
2. Double. is, when the stocks propounded are
double numbers, viz. when each stock
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Chap. XIII. The Rule of Fellowship 105 hath relation to a particular time: Example, A, B, and C, hold a pasture in common, for which they pay 45 l. per annum. In this Passure A had 24 Oxen went 32 dayes, Bhad 12 there 48 dayes, and C fed 16 Oxen there 24 dayes; now the Question to be resolved by this Rule is, what part each of these Tenants ought to pay of the 45 1. rent? and here you may observe, that the stocks propounded are double numbers, viz. each flock of Oxen hath reference to a particular time; for the respe-Cive stock of A is 24 Oxen, and its particular time is 32 dayes; again, the flock of B is 12 Oxen, and the respective time is 48 dayes; and lastly, the stock of C is 16 Oxen, and its peculiar time is 24 dayes, which as you see are double numbers.

VIII. In the double Rule of Fellowship, mul-

tiply each particular stock by its respective time, and take the total of How to work their Products for the first term, the Rule.

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whole gain or loss for the second, and the faid particular Products of the double numbers for the third term: This done, repeating, as before, the Rule of Three, fo often as there are Products of the double numbers; the fourth terms produced upon those several operations, are the numbers you look for: So in the Example of the last Rule, the Product of 24 and 32 is 768, the Product of 12 and 48 is 576, and the Product of 16 and 24 is 384, the fum of these Products is 1728, which is the first term in the Question, then 45 l. the rent, is the fecond term, and 768 the first Product, is the third term of the first proportion. Wherefore I say, as 1728 to 45 1. so 768 to another number, which I find by the di-H 3

106 The Rule of Fellowship. Book I. rect Rule of Three to be 20 l. viz. the part of the rent that A ought to pay: Then for the fecond proportion I Jay, as 1728 to 45 1. fo 576 to 15 1. which is the part that B ought to pay: And laftly, as 1728 to 45 1. fo 384 to 10 1. viz. the part that C must pay.

A second Example of the eighth Rule. Three Merchants, A, B, and C enter Partnership, and agree to continue in a joynt Adventure 16 moneths; A puts into the common flock at the beginning of the faid term 100 pounds, at 8 moneths end he takes out 40 pounds, and 4 moneths after such taking out he puts in 140 pounds. B puts in at first 200 pounds, at 6 moneths end he puts in 50 pounds more, and 4 moneths after the putting in of the 50 pounds, he takes out 100 pounds. C puts in at first 150 pounds, at four moneths end he takes out 50 pounds, and 8 moneths after fuch taking out puts in 100 pounds. Now at the end of the faid 16 moneths they had gained 357 pounds, the Question is how much of the faid gain belongs to each Merchant for his share.

In Questions of this nature, two things are principally to be observed. I The whole time of partnership. 2. The respective time belonging to each mans particular flock; fo here, it is evident that the whole time is 16 moneths, and the particular ftocks and times belonging to each Merchant will

be as followeth, viz.

A had

100

Chap. XIII. The Rule of Fellowsh	ip -107
A had 100 l. in the common flock for 8 moneths, therefore 100 multiplied by 8 produceth-	1
Also 60 l. for 4 moneths, therefore 60 multiplied by 4 produceth-	§ 240
Alfo 200 1. for 4 moneths, therefore	3 800
The total of the products of money and time for A, is	31840
B had 200 l. in the common stock for 6 moneths, therefore 200 multiplied by 6 produceth -	\$1200
Also 250 l. for 4 moneths, therefore 250 multiplied by 4 produceth-	-51000
Also 150 l. for 6 moneths, therefore 150 multiplied by 6 produceth- The total of the products of money and	5 900
time for B, is————	3
Chad 1501. in the common stock for a moneths, therefore 150 multiplied by a produceth————————————————————————————————————	\$ 600
Also 100 1. for 8 moneths, therefor	\$ 800
Also 200 l. for 4 moneths, therefore	3800
Also 200 l. for 4 moneths, therefore 200 multiplied by 4 produceth The total of the products of money and time for C, is	\$ 2200
Then adding the said three totals toge wit, 1840, 3100 & 2200, the sum is 7140, we proceeding as in the last Example, I saw Rule of three direct, as 7140 is to the total H 4	ther, to therefore y by the

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108 The Rule of Alligation Book

pounds; so is 1840 to 92 pounds the gain of A: again, As 7140 is to 357; fois 3100 to 155 the gain of B: Lastly, as 7140 is to 357; fo is 2200 to 110 the gain of C:

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1X. The Rule of fellow (hip is proved The proof. by Addition of the terms required, whose sum ought to be equal to the fecond term in the Question, otherwise the whole Work is erroneous: so in the first Example of the fixth Rule afore-going, 21 s. and 33 s. being added together are equal to 54 s. the second term in that Question: likewise in the last Example of the same Rule, as also in the first Example of the last Rule, the sum of 20,15, and 10, the terms required, are equal to 45, the second term propounded.

CHAP. XIV.

The Rule of Alligation.

I. HE Rule of Alligation is that, by which we refolve Questions, that concern the mixing of divers simples together.

II. Alligation is either Medial or Alternate.

III. Alligation Medial is, when having the feveral quantities and rates of divers Alligation fimples propounded, we discover the Medial mean rate of a mixture compounded of those simples. So 10 bushels of wheat at 4 s. or (which is all one) 48 d. the bullel; 40 bullels of rye at 3 s. or 36 d. the bushel; and 50 bushels of barley at 2 s. or 24 d. the bushel; being mixed £4:

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with 20 bushels of Oats at 12 d. the bushel, the Rule of Alligation medial sheweth you the mean price of that missling.

IV. In Alligation medial, first The operations sum the given quantities, then find and proportions the total value of all the simples: this done, the proportion will be as folfoweth.

of the same

As the sum of the quantities is to the total value of the simples:

So is any part of the mixture propounded to the required mean rate or price of that part.

Repeating again the premised Example of the third Rule, I demand how much one bushel of that missling is worth? Now the sum of 10, 40, 50, 20 (the given quantities) is 120 bushels, and the value of the 10 bushels of wheat at 48 d. the bushel, amounts to 480 d. for 48 being multiplied by 10. the product is 480: again, the value of the 40 buthels of rye at 36 d. the bushel, is 1440 d. The value of the 50 bushels of barley at 24 d. the bushel, is 1200 d. And the value of 20 bulhels of Oats at 12d. the bulhel is 240d. All these values being added together, their total is 3360 d. I say then by the Rule of Three Direct, if 120 bushels give 3360 d. what will I bushel yield? The Rule presently an-Iwers me 28 d. whereupon I conclude, that a bushel of that missling may be afforded for 28 d. that is, 2 s. 4 d. which is the resolution of the Question propounded.

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In like manner if it be demanded what 8 Bushels or a Quarter of that Missling is worth? The Answer will be 224 d. which being divided by 12, and by that means reduced into spillings; is 18 s. 8 d.

V. In Alligation Medial, the trial of the Work is by comparing the total value of the The proof. several simples with the value of the whole mixture: For when those sums accord, the operation is perfect; so in the first Example of the last Rule.

190	Bushels of Wheat at 4 s. the	1. s. d.
Valve of	40 Bushels of Rye at 3 s. the Bushel is	-6-0-0
The Va	50 Bushels of Barley at 2 s. the Bushel is-	-5-0-0
06.	And 20 Bushels of Oats at 12 d. the Bushelis	-1-0-0

veral rates of divers Simples given, we discover such quantities of them, as are necessary to make a mixture, which may bear a certain rate propounded.

Example: A man b ing determined to mix 10 Bushels of Wheat at 4 s. or 48 d. the Bushel, with Rye book I.

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with Ryc Ryc of 3 s. or 36 d. the Bushel, with Barley of 2 s. or 24 d. the Bushel, and with Oats of 1 s. or 12 d. the Bushel, the Rule of Alligation Alternate will discover unto you how much Rye, how much Barley, and how much Oats he ought to add unto the 10 Bushels of Wheat; in such fort that the mixture of them altogether may bear a certain rate or price propounded.

VII. In Questions of Alligation Alternate, you

must rank the terms in such fort, that the given rate of the mixture may represent the root, and the several rates of the Simples may stand as branches

The right ordering of the Terms.

iffuing from that root: So the Example of the last Rule being propounded, I demand how much Rye, Barley, and Oats, ought to be added to the 10 Bushels of Wheat, that the mixture of all together may bear the rate or price of 28 d. or 2 s. 4 d. the Bushel: And therefore drawing a line of connexion, I place 28 d. the given rate of the mixture, upon the left hand thereof by it felf representing the Root, and likewise write the other rates propounded, viz. 48 d. 36 d. 24 d. and 12 d. one above another upon the right hand of that line 24 of Connexion, which rates are con-

ceived to issue from 28 d. as branches from the Root, the fabrick hereof appears plainly in the Margent.

VIII. Having ranked the terms in their due order, link the branches together by How to couple certain Arks, in such fort, that one the Termis . that is greater than the Root or rate

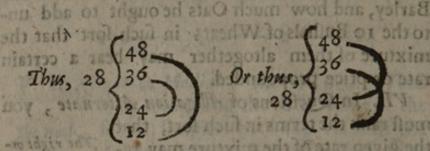
of the mixture, may always be coupled with ano-

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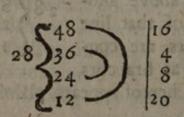
both distribution of the state of the state

ther that is less than the same ! So in the premited Example, 48 may be linked with 12, and 36 with 24, or otherwise 48 may be coupled with 24, and 36 with 12, and then the Work will fland



IX. Having alligated the branches, and found the difference betwixt them and the How to order Root, write the differences of each the differenbranch just against his respective yokefellow. So the branches of the example

afore-going being linked after the first manner, and the difference between 28 and 48 (by the third or fourth Rule of the fourth Chapter of this Book) being 20, I place 20 just against 12, the respective yoke-fellow of 48. Again, 16 being the difference betwixt 28 and 12, I write it just against 48. In like manner 8 being the diffe-



rence between 28 and 36, I place it right against 24. And lastly, 4 the difference betwixt 28 and 24, I write just against 36: In the end the whole Fabrick of the Work (as the branches are thus linked) will fland as in the Example.

Chap.XIV. The Rule of.

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But the branches being linked after the other manner, the Work will be thus disposed to the billion and the base of the base o

the Question now is How much the Railey and Oats ought to be the cought to de the cought to de the cought to de the cought to the bushelves Here of the cought to the cought

For in this case 48 hath 24 for his yoke-sellow, and the respective Comerado of 36 is 12; and here the interchangeable placing of the differences (as in the premised Examples) is that which is more

particularly termed Alternation.

X. When one branch is linked to divers other branches, and not to one alone, the differences ought to be as often transcribed, as it is so diversly linked. So in the premised Example, you may (if you please) conceive 12 to be coupled both with 48 and 36; likewise 24 may be conceived to be linked with the same 48 and 36; wherefore the difference betwixt 28 and 12 being 16, I write it both just against 48 and 36: In like manner the difference between 28 and 24 being 4, I write it likewise over against the same numbers 48 and 36. Again, 20 being the difference betwixt 28 and 48,

I place it just against 24 and 12; and 8 being the difference between 28 and 36, I write it likewise over against the same numbers 24 and 12: All

8 36 36 16.4 16.4 20.8 20.8

this performed, the whole frame of the Work will stand as in the Margent.

2. Take this for another Example: It is required

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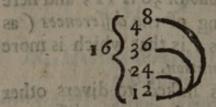
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Oats

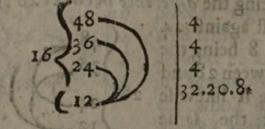
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red to mix 10 bushels of Wheat at 48 d. the bushel with Rye of 36 d. the bushel, with Barley of 24 d. the bushel, and with Oats of 12 d. the bushel, and the Question now is, How much Rye, Barley, and Oats ought to be added to the 10 bushels of Wheat, that the entire mixture may be afforded at 16 d. the bushel? Here the branches of this Question (according to the eighth Rule of this Chapter) ought to be linked thus,



And as for the Alternation of the differences, it is evident (by the present Rule) that the difference between 16 and 12 being 4, ought to be thrice transcribed, viz. first just against 48, then against 36, and last of all against 24. Again, 32 the difference betwixt 16 and 48, as also 20 the difference between 16 and 36; and lastly, 8 the difference betwixt 16 and 24, ought all to be placed just against 12.



3. I determining to mix 10 bushels of Wheat at 48 d. the bushel, with Rye of 36 d. the bushel, with Barley of 24 d. the bushel, and with Oats

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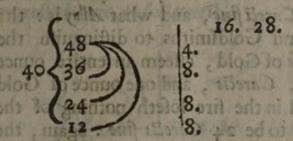
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of 12 d. the Bushel, desire to know how much of each I ought to take, that I might afford the whole mixture at 40 d. the bushel: Here the whole Work being ordered according to the Rules aforegoing, it will stand as followerb.



4. A man intending to mix 10 bushels of Wheat at 48 d. the bushel, with Rye of 36 d. the bushel, with Barley of 24 d. the bushel, with Pease of 16 d. the bushel, and with Oats of 12 d. the bushel, defires to know how much Rye, Barley, Pease, and Oats he ought to add to the 10 bushels of Wheat, that the whole mass of Corn so mixed might be afforded at 20 d. the bushel. This Question being thus propounded, the terms thereof (by the Rules aforegoing) may be Alligated, and the differences of the terms Alternated, as followeth.

5. Lastly, A Goldsmith hath some Gold of 24 Caretis, other of 21 Caretis, and other some of 19 Caretis sine, which he would so mix with Alloy, that 192 Ounces of the entire mixture might bear

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What a Carect fine, and what Alloy 850

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can well understand this Question, it will be necessary to explain what a Carect fine, and what Alloy is: the

Mint-Masters and Goldsmiths to distinguish the different fineness of Gold, esteem an entire ounce to contain 24 Carecis, and one ounce of Gold that being tryed in the fire lofeth nothing of the weight, is said to be 24 Careds fine: again, the ounce that being tryed loseth one four and twentieth part of the weight, is faid to be 23 Carecis fine: In like manner that which lofeth two four and twentieth parts of the ounce, is effected to be 22 Caretis fine, and fo confequently of the rest: And as for Alloy, it is filver, copper, or some other baser metal, with which the Goldsmiths use to mix their Gold, to the intent they may moderate, or abate the fineness thereof. Here you may also observe, that as the fineness of Gold is meafured by Carecis, so is the fineness of Silver estimated by ounces: In such fort, that a pound of Silver, which being tryed a certain time in the fire, loseth nothing of the weight, is said to be 12 onnces fine. But a pound, that being tryed loseth somewhat of the weight, is said to be the remainder of the weight fine. Example; a pound of Silver, that lofeth in the fire one ounce 8 p. is estimated to be 10 ounces 12 p. fine; and that which loseth 2 ounces 8 p. 10 grains, is said to be 9 ounces 11 p. 14 grains fine, &c. Now to rank the terms of the last mentioned Question, as also the differences of the terms in their due order, because the three given branches (viz. 24 Carecis.

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Carells, 21 Carells, and 19 Carells) are all greater than 17 Carells the root or rate of the mixture. I add o as another branch, which I conceive to be less than the root, and then proceed as in the former operations; the whole frame of the Work is expressed here, as followeth:

$$17 \begin{cases} 24 \\ 21 \\ 19 \end{cases} \qquad \begin{vmatrix} 17 \\ 17 \\ 17 \\ 7.4.2. \end{vmatrix}$$

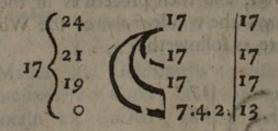
XI. When in one and the same line there are found more differences than one, add them together and write the sum just How to add

them together, and write the sum just against the same differences before a straight line drawn towards the

right hand of the Work.

So the first Example of the last Rule being propounded, the sum of 16 and 4 (the differences placed just against the first branch) being 20, I write it over against the same differences, before the new line drawn upon the right hand of the Work, and so consequently the rest in their due order, as appears by the Example hereunto annexed.

In like manner the last Example of the last Rule being offered, the whole Fabrick of the Work will stand, as followeth:



XII. Alligation Alternate is, either Partial or Total.

Alternation Partial is, when having the feveral rates of divers Simples, and the quantity of one of them given, we discover the feveral quantities of the rest, in such fort that a mixtue of those

Simples being made according to the quantity given, and the quantities so found, that mixture may bear a certain rate propounded: Of this kind is the Example of the fixth Rule, as also all the Examples of the tenth Rule, except the last.

The proportions XIV. In Questions of Alternation used in this Partial, the proportion is as followers.

As the difference annexed to the first branch is to the several differences of the rest:

So is the quantity propounded to the feveral

quantities required.

So the Example of the fixth and seventh Rules of this Chapter being again repeated, and the terms thereof, as also the differences of the terms being ordered after the first manner (shewed you in the ninth Rule asoregoing) it is evident that

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for every 16 Bushels of Wheat that
I take in the mixture, I ought to
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Rye, 8 Bushels of

Barley, and 20 bushels of Oats; and therefore I

Say,

I. As 16 the difference annexed to the first branch (being the rate of the Wheat) is to 4 the difference annexed to the next, being the rate of the Rye; so is 10 the given quantity of the Wheat to another number, which being sound by the Rule of Three direct, to be two bushels and an half (or two pecks) is the quantity of Rye necessary in the mixture.

II: As 16 to 8, so is 10 to another number, which being likewise sound by the Rule of Three to be five bushels, is the quantity of

Barley necessary in the mixture.

III. As 16 to 20, so is 10 to another number, which being in like fort sound by the Rule of Three to be 12 bushels, and half of a bushel, is the quantity of Oats requisite in the mixture.

So that at last I conclude, a heap of Corn being composed of 10 bushels of Wheat, 2 bushels and a half of Rye, 5 bushels of Barley, and 12 bushels and an half of Oats (when those several Grains bear the prices aforesaid) may be afforded at 2 s. 4 d. the bushel.

The same Example being ordered after the second manner (expressed likewise in 2 Case. the 9th Rule of this present Chapter) I say

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I. As 4 the difference annexed to the rate of the wheat, is to 16 the difference annexed to the rate of the Rye; so is 10 the given quantity of the wheat, to 40 bushels the required quantity of the Rye.

The Rule of

II. As 4 to 20, so is 10 to 50 bushels, the re-

quisite quantity of the barley.

III. As 4 to 8, so is 10 to 20 bushels, the quantity of the oats necessary in the mixture.

$$28 \begin{cases} 48 \\ 36 \\ 24 \end{cases}$$

So that I conclude again, a mass of Corn being compounded of 10 bushels of wheat, 40 bushels of rye, 50 bushels of barley, and 20 bushels of oats, (when those Grains bear the prices propounded in this Example) may be afforded at 25.4 d. the bushel as before.

3. Cuse the third manner (expressed in the tenth and eleventh Rules of this Chapter) I say

I. As 20 the sum of the differences annexed to the rate of the wheat, is to 20 the sum of the differences annexed to the rate of the rye; so is 10 the given quantity of the wheat, to 10 bushels the required quantity of the rye.

II. As 20 to 28, so is 10 to 14 bushels the re-

quifite quantity of the barley.

111. As 20 to 28, fo is 10 to 14 bushels, the quantity of oats demanded in the mixture.

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Whereupon this third time likewise I conclude, that (those Grains still retaining the given rates) to bushels of Wheat, 10 bushels of Rye, 14 bushels of Barley, and 14 bushels of Oats being all mixed together, will constitute a mass of Corn, that may

be afforded at 28 d. or 2 s. 4 d. the bushel.

By this Example thus diversified it plainly appears, that the quantities required may be altered as often as the Question given will admit divers Alligations, and yet the mixture produced will still hold the rate propounded; but when the Question propounded will admit but one only way of Alligation, the quantities required to make the mixture, cannot be varied; so the second Example of the tenth Rule of this Chapter, being again produced, and ordered according to the direction of the eleventh Rule aforegoing, I say,

I. As 4 to 4, so 10 to 10 bushels of Rye.

II. As 4 to 4, so 10 to 10 bushels of Barley.

III. As 4 to 60, so 10 to 150 bushels of Oats.

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So that for this Question I conclude, to 10 bushels of wheat you ought to add 10 bushels of Rye, 10 bushels of barley, and 150 of oats, to the end that a mixture of Corn might be made, which may be sold at 16 d. the bushel: And here the quantities found (viz. 10, 10, and 150) cannot be altered, because the terms of this Question will not admit any other variety of Alligation.

XV. In Alternation Partial, the proof is likewise

by comparing the total value of the The Proof. several simples, with the value of the whole mixture: So in the second example of the last Rule, the total value of the 10 bushels of wheat, 40 bushels of rye, 50 bushels of barley, and 20 bushels of oats amounts to 14 l. which is also the value of the whole mixture at 2 s. 4 d. the bushel, as appears by the example of the fifth Rule of this present Chapter.

XVI. Alternation total is, when having the total quantity of all the simples, toge-Alternation ther with their several rates, we produce their several quantities, in such fort, that a mixture of them be-

ing made according to the quantities so found, that mixture may bear a certain rate propounded: Of this sort is the last example of the tenth Rule aforegoing; as also this, a Goldsmith having divers sorts of Gold, viz. some of 24 Carects, other of 22 Carects, some of 18 Carects, and other some of 16 Carects fine, is desirous to melt of all these sorts so much together, as may make a mass containing 60 ounces of 21 Carects fine: Now this Rule of Alternation total sheweth you how much you are to take of each fort, to the end the whole mass

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may contain just 60 ounces of 21 Carects, the fineness propounded.

XVII. In Questions of Alternation total the proportion is, as fol-

As the sum of all the differences is to the total quantity of all the simples: So is the correspondent difference of each rate to the respective quantity of the same rate.

So the last example of the last Rule being propounded, Isav.

I. As 12 the sum of the differences is to 60 ounces the total quantity of all the simples: so is 5 the correspondent difference of 24 Carects the first rate, to 25 ounces, viz. the required quantity of the Gold of the same rate, which may be taken to make the mixture propounded.

II. As 12 to 60, so is 3 the correspondent difference of 22 Carects the second rate, to 15 ounces, viz. the quantity of the Gold of 22 Carects, that ought to be used in the mixture. III. As 12 to 60; so is 1 to 5 ounces of the

Gold of 18 Carects fine.

IV. As 12 to 60, so is 3 to 15 ounces of the Gold of 16 Carecas fine, which are requisite to be taken for the mixture propounded.

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Whereupon I conclude, that 25 ounces of 24 Carects fine, 15 ounces of 22 Carects, 5 ounces of 18 Carects, and 15 ounces of 16 Carects fine, being all melted together will produce a mass of Gold containing 60 ounces of 21 Carects fine, which is the resolution of the Question propounded.

Again, the lift Example of the tenth Rule being here repeated, and ordered according to the di-

rection of the eleventh Rule, Isav,

I. As 64 to 192, fo is 17 to 51 ounces of 24 Carects fine.

11. As 64 to 192, so is 17 to 51 ounces of 21 Carects fine.

III. As 64 to 192, so is 17 to 51 ounces of 19 Carects fine.

IV. As 64 to 192, so is 13 to 39 ounces of Alloy.

And therefore for conclusion I say, that 51 ounces of Gold, 24 Carects fine, 51 ounces of 21-Carects fine, 51 ounces of 19 Carects fine, and 39 ounces of Alloy being all mixed together, will produce a mass containing 192 ounces of Gold, 17 Carects fine, which is the satisfaction of the question premised

And here observe (as before in the Exposition of the fourteenth Rule of this Chapter) that the operations of the first of these Examples may be varied according to the divertity of the Alligations which k I.

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igation White which it will admit, whereas the last Example is not subject to any variety, the Alligations thereof remaining always the fame.

XVIII. Here the operation is perfect, when the fum of the quantities found agrees with the total quantity propounded The Proof. So in the first Example of the last Rule, 25, 15, 5, and 15 (the quantities found) being all added together amount to 60, which is the total quantity propounded.

CHAP. XV. LaAs 24 10 26, 6 in 610 of is the part chies

The Rule of False.

THE Rule of False is always performed by false and supposititial numbers taken at pleafure after the Proposition is made, and the question propounded; for things are said to be found out by the Rule of False, when by false terms supposed, we discover the true terms required.

II. The Rule of False, is either of single or

double position.

III. The Rule of fingle position is, when at once, viz. by one falle polition, The Rule of we have means to discover the true re- fingle Position folution of the Question propounded.

For Example : A, B, and C, determining to buy together a certain quantity of Timber, that should cost them 36 1. agree amongst themselves that B shall pay of that sum a third part more than A, and that C shall pay a fourth more than B. Now the Question is, What particular sum each of these parties

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parties ought to pay of the 36 l. To resolve this Question; first, put the case that A ought to pay 6 l. of the 36 l. and then B must pay 8 l. because he pays one third part more then A. And lastly, C ought to pay 10 l. because he is to lay out one sourth part more then B. This done, although by addition of these three sums, viz. 6, 8, and 10, I find that I have made a wrong Position (their total amounting onely to 24 l. which ought to have been 36 l.) nevertheless by those suppositial Numbers, I have means to discover the true sums which the several parties ought to pay: for I say by the Rule of Three Direct.

I. As 24 to 36, so is 6 to 9 l. the part that A must pay.

II. As 24 to 36, so is 8 to 12 l. the part that B ought to pay.

III. As 24 to 36, so is 10 to 15 1. the part of the

36 l. that C must pay.

IV. Here for trial of this Rule the total of the sums found ought to accord with the sum given: So in the Example of the last Rule, 9, 12, and 15 being all added together a-

mount to 36, the sum propounded.

V. The Rule of double Position is, when two The Rule of false Positions are supposed for the double Position. resolution of the question propountion. ded. As in this, A Workman having thresht out 40 quarters of Grain (part thereof being Wheat, and the rest Barley) received for his labour 28 s. being paid after the rate of 12 d. for every quarter of Wheat, and 6 d. for each quarter of Barley: Now here the question is, how many of those 40 quarters were Wheat, and how

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how many Barley? Here therefore I first suppose at random, that there was 26 quarters of Wheat. and 14 of Barley, and then to discover whether I have gueffed right or wrong, I find how much money is due unto the Workman at the rate of 12 d. the Quarter of Wheat, and 6 d. the Quarter of Barley, which I find to be 33 s. (viz. 26 s. for the 26 Quarters of Wheat, and 7 s. for the 14 Quarters of Barley) which he ought to have received, if my supposition had been right; but because it differs from 28 s: the true fum that he received, I perceive I have mist the mark, and therefore discovering how much I have err'd by finding the difference betwixt 28 s. and 33 s. I keep in mind 5 their difference, which is called the first errour, or the errour of the first Position: Again, I propound for the second Position, that there was 30 quarters of Wheat, and 10 quarters of Barley; and then the second errour I find to be 7; for there is then due to the Workman for the 30 quarters of Wheat 30 s. and for the 10 quarters of Barley 5 s. in all 35 s. which differs from 28 s. the true fum that he received, by 7 s. and here by these two false Positions, together with their errours, you may discover how many quarters of Wheat, and how many of Barley the Workman thresht, as shall be further explained by the Rule following.

VI. In the Rule of double Position having drawn two lines a cross, and The operation.

placed the terms of the false Position (viz. those that have the same Denomination) at the uppermost end of that Cross, as also each errour under his respective Position at the lower end of the

fame Cross, multiply each errour by the contrary

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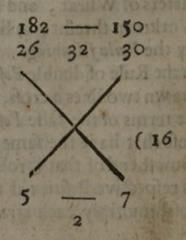
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Position; that is, the second errour by the first Positions and the first errour by the second Position; this done when both the errours are of one and the same kind (viz. both excesses or both desects) subtract the less Product out of the greater, and then the remainder is your Dividend; but if the errours be of differing kinds, (viz. one of them an excess, and the other a desect) add those Products together, and then the sum will be your Dividend, which if you divide by the difference of the errours, (when they are of one and the same kind) or by their sum (when they are of different kinds) the Quotient will give you a number you look for, having the same Denomination with the salse Positions placed at the upper end of the Cross.

again propounded, I place these terms, viz. 26 (having the Denomination of the Quarters of Wheat in the first Position) and 30 (having the same Denomination in the second Position at the upper end of the Cross: As also 5 and 7 the two errours respectively under them at the lower end of the same Cross, as you may see it exemplified by

the Pattern following.

Note that this Charaster—
fignifies that the lesser of the two Numbers, betwixt which it is found, cught to be subtrated from the greater.



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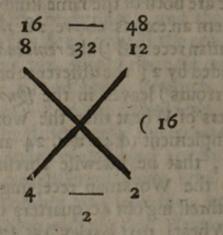
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This done, having multiplyed 26 by 7, the product is 182, and likewise 30 by 5, the product is 150, which being deducted out of 182 (because the errours here are both of the same kind, that is, are each of them an excess above 28 s. the sum that the workman received) the remainder is 32, which being divided by 2 (the difference betwixt 5 and 7 the two errours) leaves in the Quotient 16, for the quarters of Wheat that the workman thresht, whose complement to 40 viz. 24 are the quarters of Barley, that he likewise thresht; so at last I conclude; the Workman receiving 28 s. for his wages in threshing out 40 quarters of Grain (being part Wheat, part Barley) at 12 d. the quarter of Wheat: and 6 d, the quarter of Barley, threshed in all 16 quarters of Wheat, and 24 quarters of Barley.

2. Example. The fame Question being again propounded, I suppose for my first Position that there are 8 quarters of Wheat, and 32 quarters of Barley, and then the first errour will be 4 s. for 8 s. being accounted for the 8 quarters of Wheat, and 16 s. for the 32 quarters of Barley, make in all 24 s. which wants 4 s. of 28 s. the fum received: Again, Supposing that there are 12 quarters of Wheat, and 28 quarters of Barley, the fecond errour will be 2 s. for 12 s. being allowed for the 12 quarters of Wheat, and 14 s. for the 28 quarters of Barley, the fum is 26 s. which comes 2 s. short of 28 s.the right sum: now then 8 being multiplyed by 2, the Product is 16; likewife 12 by 4 produceth 48, out of which if you deduct 16 (because the errours in this case happen to be both desects under 28 s. the sum received) the remainder is 32, which being 130

being divided by 2 (the difference of the errours)
gives you in the quotient 16, viz. the quarters of
Wheat, as before.



3 Example. The same demand being the third time produced, I take for my first Position 10 quarters of Wheat, and 30 quarters of Barley, and then proceeding as before, the first errour will prove 3 s. which upon that Position I want of 28 s. the right fum: Again here for the fecond Position I take 26 quarters of Wheat, and 14 quarters of Barley, and then the fecond errour will be 5 s. which upon that Position I have exceeded 28 s. the true sum: now then multiplying 10 by 5, the Product is 50, and 26 by 3, the Product is 78: And here (because the errours are of different kinds, one of them being a defect, and the other an excess of 28 s. the true fum) you are to add 50 and 78 the two Products together, whose sum is 128, which being divided by 8, the fum of 3 and 5 the two errours, gives you in the quotient 16 for the quarters of Wheat, as before in the former resolutions. So that what Positions soever you take in this Question you shall always find, that the Workman threshed 16 quar-

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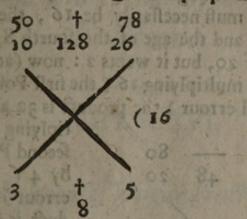
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ters of Wheat, and 24 quarters of Barley, which is the resolution of the Question propounded.

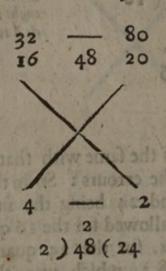


Note that this Character & imtimates that the Numbers, betwixt which it is found, ought to be added together.

VII. Here the trial is the same with that which is used in sinding out the errours: So in the Example premised 16 and 24 being the numbers found, and 16 s. being allowed for the 16 quarters of Wheat, likewise 12 s. for the 24 quarters of Barley, their sum is 28 s. which was the sum received by the Workman.

4. Example. A certain man being demanded what was the age of each of his 4 Sons? Answered, that his eldest Son was 4 years elder than the second; his second Son was 4 years elder than the third; his third Son was 4 years elder than the fourth or youngest; and his sourth or youngest, was half the age of the eldest; the Question is, what was the age of each Son? Here I guesse the age of the eldest Son to be 16, then it may be inferr'd from the Question, that the age of the second Son was 12, the age of the third 8, and the age of the sourth or youngest 4, this 4 should be half 16 (for the Question saith, that the age of the youngest was half the age of the eldest) but it wants 4 of what it ought

ought to be; wherefore I make a fecond Position, and take 20 for the age of the eldest, then the age of the second must necessarily be 16, the age of the third 12, and the age of the fourth 8, which should be half 20, but it wants 2: now (according to the Rule) multiplying 16 (the first Position) by 2 (the second errour) the product is 32, also mul-



tiplying 20 (the second Position) by 4 (the sirst errour) the Product is 80, and because the errours are both of one kind, to wit, both desertive; I subtract the lesser Product from the

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greater, so the remainder is 48 for a Dividend, also subtracting the lesser errour from the greater, the remainder is 2 for a Divisor: Lastly, dividing 48 by 2, the quotient is 24, and such was the age of the eldest Son, therefore the age of the second was 20; the age of the third 16, and the age of the fourth 12, which is half the age of the eldest, as was declared by the Question.

elder Son to be 16 , then it may be intered

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Chap. XVI. Notation of Vulgar &c. 133

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The Doctrine of Vulgar Fractions.

CHAP. XVI.

Notation of Vulgar Fractions.

Thus far of Arithmetick in whole numbers, only the doctrine of Fractions ensueth, which depends upon this supposition, that Unity, or at least one whole thing, whatsoever it be, may in mind be conceived divisible into any number of equal parts: some will not allow 1 or unity to be a number, when it is considered in the abstract, and separated from matter, but for smuch as that Prince of Arithmeticians Diophantus of Alexandria, in divers of his subtil Problemes doth mention unity as a number, and propounds it to be divided into numbers, I shall take the like liberty to esteem 1 or unity as a number, and likewise suppose it divisible into any number of equal parts.

II. A broken number, otherwise called a Fraction, is only part of an In- A Fraction; teger or whole thing, as if you would express in figures the length of a piece of cloth, that contains three fourths, or (which is all one) three quarters of a yard, you are to write it thus \frac{1}{4}, that is, an entire yard being supposed to be divided into source qual parts, the length of the piece propounded

III. A Fraction confists of two parts, the Numerator and the Denominator, which are placed one above the other, and separated by a little line.

IV. The Numerator is the number placed above

the line, and the Denominator is the number placed underneath:

4 Denominator. fo in the aforementioned Fradion \(\frac{1}{4} \) the number 3 placed a-

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bove the line is the Numerator, and the number 4 placed underneath is the Denominator. Also in this Fraction $\frac{6}{12}$, the Numerator is 6, and the Denominator is 12. The Denominator is so called, because it denominates or declares into how many equal parts the Integer or whole thing is supposed to be divided, and the Numerator is so called, because it numbreth or expresses how many of those equal parts of the Integer are signified by the Fraction.

V. A Fraction is either proper or improper.

VI. A proper Fraction is that whose Numerator is less than the Denominator, such are the Fractions before-mentioned $\frac{3}{4}$ $\frac{6}{12}$ $\frac{25}{120}$ and the like.

VII. A proper Fraction is either single or com-

pound.

Asingle : VIII. A single Fraction is that which Fraction. consists of one Numerator, and one Denomi-

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Denominator; such are \$\frac{3}{4} \frac{-6}{12} \frac{25}{100}\$ and the like. 1X. A single Fraction doth often arise in Division of whole numbers, for when Division is finisht, if any number remain, it is to be esteemed as the Numerator of a Fraction, which hath the Divisor for a Denominator, and is to be annexed to the Integer or Integers in the quotient as part of the quotient; which Fraction doth always express certain parts (or at least a part) of an Integer or entire unity, which hath the same Denomination with one of the Integers in the quotient; fo if 17 pounds be given to be divided equally amongst 5 persons, there will arise 3 entire pounds in the quotient, and there will be a 5) 17 (3 3 remainder or furplufage of 2 pounds which 2 is to be placed, as the Numerator of a Fra-Gion, over the Divisor 5 as a Denominator; so will the Fraction be 3, and the compleat quotient will be 3 3, that is, 3 pounds and 2 fifth parts of a pound

A fingle Fraction doth likewise arise, when a lesser whole number is given to be divided by a greater, for in such case the Dividend is to be made the Numerator of a Fraction, and the Divisor the Denominator; which Fraction is the true quotient, and doth always express certain parts (or at least a part) of an Integer, which hath the same name with the Dividend: so if 3 pounds sterling be given to be divided equally amongst 4 Persons, the share of each, that is, the quotient will be 1, to wit, three fourth parts of a pound. In like manner, if 5 be given to be divided by 8, the quotient is 1, so that the Numerator of a Fraction is always a Dividend, the Denominator is a Divisor, and the Fraction it felf is the quotient. K 2

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Fraction.

Denominators than one, and may be discovered by the word [of] which is interpos'd between the parts of such compound Fraction: so 3 of 1 is a Fraction of a Fraction, or compound Fraction, and expresseth two thirds of three fourths of an Integer, viz. a pound sterling being supposed the Inreger, and first divided into four parts, three of those four parts are equal to 15 s. Again, if the faid 15 s. be divided into three parts, two of those three parts are equal to 10 s. therefore the compound Fra-Clion 3 of 4 of a pound sterling doth express 10 s. In like manner the compound Fraction 4 of 4 of 4 of a pound sterling, that is, one fourth of three fourths of four fifths of a pound sterling doth express 3 s.as will be farther manifest by the fixteenth and ninth Rules of the seventeenth Chapter.

XI. An improper Fraction is that, Animproper whose Numerator is either greater, or Fraction. at least equal unto the Denominator: so this Fraction 16 that is 16 fourths, is called an Improper Fraction, and so is this 4; for indeed 2 Fraction of this kind may well be furnamed Improper, because it will not admit the definition of a true Fraction, lince it is always greater than an entire unity, or at least equal unto it; so sixteen Farthings, or 16 of a peny are equal to 4 entire pence; and 4 Farthings, or 4 of a peny are equal to 1 peny; therefore when the Numerator is greater than the Denominator, such improper Fraction lignifieth more than I or an Integer, but when the Numerator is equal to the Denominator Chap.XVII. Reduction of &c.

(be it what number soever) such improper Fraction

is alwayes equal to unity, or I Integer.

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XII. A mixt number confifts of entire A mixt unities (or Integers) or at least of unity number. (or I Integer) and a Fraction annexed: So 511, 13, and fuch like; are called mixt num-

bers; So that if a piece of Timber be five feet and eleven inches in length, you are to write that length thus, 511; In like manner, one mile and three quarters or fourths of a mile are to be written thus, I 1.

CHAP. XVII.

Reduction of Vulgar Fractions.

I. THe same parts of Numeration, as have been wrought in whole Numbers in the preceding Chapters, are likewise to be performed in fractions, but first of all Reduction of Fractions in divers kinds must be known, which being the principal skill in the doctrine of Fractions, must be diligently ob-

ferved by the Learner.

II. A number is said to be a common Measure or Divisor unto two or more numbers given, when it will measure or divide every one of the numbers given, and leave no remainder; so 4 is a common measure unto the numbers 12 and 20; for if 12 be divided by 4, the Quotient will be exactly 3, without any remainder or furplulage, allo if 20, be divided by the same Divisor 4, the quotient will be precisely

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To find the greatest common mea ure unto any two numbers.

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138

III. Two numbers being given, their greatest common Divisor, that is, the greatest number which will measure or divide each of the numbers given without leaving any remainder, may be found out in this

manner viz. Divide the greater number by the less, then divide the Divisor by the remainder (if there be any) and so continue dividing the last Divisors by the remainders, until there be no remainder (neglecting the quotients;) so is the last Divisor the greatest common Divisor unto the numbers given.

Thus, if the greatest common Divisor unto the numbers 91 and 117 be fought, divide the greater

91) 117 (1 9 I 26)91(3 78 13)26(2 26

number 117 by 91, the remainder is 26, by which dividing 91, the remainder is 13, by which dividing 26, the remainder is 0; fo is 13 the greatest common Divisor unto the numbers 117 and 91, as is manifest in dividing each of them by 13; for 13 is found in 91 precifely 7 times, and in 117 precifely 9 times. In like manner, 29 will be found a

common Divisor unto 116 and 145; And SIa common Divisor unto 561 and 612.

To reduce a Fra-Hion into the leaft Berms. VIZ. I Ey & general Rules

IV. A fingle fraction may be reduced into the least terms, by dividing the Numerator and Denomi-

Chap.XVII. Vulgar Fractions.

139

nator by their greatest common measure (or Divifor;) for the quotients will be the Numerator and Denominator of a fraction equal to the former, and in the least terms.

So if the fraction - 21 be given to be reduced into the least terms, search out the greatest common Divisor unto 91 and 117 by the last Rule, which will be found 13, and then dividing 91 by 13, the quotient will be 7 for a new Numerator; also dividing 117 by 13, the quotient will be 9 for a new Denominator: so the fraction - 21 is reduced into the least terms, viz. into the fraction 2. In like manner 146 will be reduced unto \(\frac{4}{5}\); And \(\frac{561}{612}\) unto \(\frac{11}{12}\): But here you are to observe, that if the greatest common Divifor unto the Numerator and Denominator be I, fuch Fraction is in its leaft terms already: fo the fra-Ction 151 cannot be reduced into lower terms, because the greatest common Divisor will be found 1, (by the third Rule of this Chapter;) the like may happen of infinite others: and although the last be a general Rule for the Reduction of Fractions into their least terms, yet there are other practical Rules, which in some cases will be more ready (especially unto beginners) viz.

V. When the Numerator and De- 2. By particunominator are even numbers, they lar Rules.

may be measured or divided by 2.

Therefore in such case you may (as is taught in the Rules of the 6th Chapter) take the half of the Numerator for a new Numerator, also the half of the Denominator for a new Denominator. So

if $\frac{16}{64}$ be given, draw at length the line which separates the Numerator from the Denominator, and $\frac{16|8|4|2|1}{64|32|16|8|4}$

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cross the same with a downright stroke near the Fra Ction, as you may fee in the Margent ; then take the half of 16, which is 8, for a new Numerator, also the half of 64, which is 32, for a new Denominator; Again, the half of 8 is 4, for a new Numerator, also the half of 32 is 16, for a new Denominator, and proceeding in like manner, there will be found 1, equivalent unto 16

VI. When the Numerator and Denominator do each of them end with 5, or one of them ending

with 5, and the other with a Cypher, 225 45 9 they may be both measured or divided by 5. So 225 will be reduced in-475 95 19 to $\frac{-2}{19}$ and $\frac{50}{425}$ into $\frac{-2}{17}$ as by the opera-50/10/ 2

tion in the Margent is manifest. 425 85 17 VII. Whenfoever you can elpy any

other number, which will exactly divide the Numerator and Denominator (although it be not the greatest common Divisor) you may divide the

Numerator and Denominator by fuch number as before: So 384 may be first reduced into -1 by 4, and -1 may be re-84 21 3 duced into 1/3 by 7, as by the operation

is manifest.

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VIII. When the Numerator and Denominator do each of them end with a Cypher or Cyphers, cut off equal Cyphers in both, 5|00 and the fraction will be reduced into leffer 7100 terms: So 400 is reduced into 5, and 9000 into 90.

IX. The value of a fingle To find the value of afingle fraction in the known fraction in the known parts parts of the Integer.

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of the Integer, may be found out in this manner, viz. multiply the Numerator of the fraction propounded by the number of known parts of the next inferiour denomination which are equal to the Integer, and divide that product by the Denominator, so is the quotient the value of the fraction in that inferiour denomination, and if there happen to be any fraction in the quotient, you may find the value thereof in the next inferiour denomination, by the same Rule, and so proceed till you come to the least known parts.

So the value of $\frac{9}{16}$ of a pound sterling will be found 20 11 s. 3 d. viz. multiply the Numerator 9, by 20 (the number 16) 180(11-4 of shillings which are equal to 16 is 180, which being divided 20 by the Denominator 16, the 16 Quotient is 11 74 shillings. In like manner, the value of 14 of a shilling will be found 3 pence, for multiplying the -Numerator 4 by 12 (the num- 16) 48(3 ber of pence in a shilling) the 48 product is 48, which being divided by the Denominator o 16, the quotient is 3 pence.

Also the value of 13 of a pound sterling, will be found 10 s. 9 -3 d. And 36 of a pound Troy will be found equivalent unto 3 ounces 17 peny weight and 12 grains.

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To reduce a mixt number into an improper fractirn

X. A mixt number may be reduced into an improper fraction equivalent unto the mixt number,

in this manner, viz. Multiply the Integer or Integers in the mixt number by the Denominator of the fraction annexed to the Integer or Integers, and unto the Product add the Numerator of the faid fraction; so is the sum the Numerator of an improper fraction, whose Denominator is the same with that of the said fraction annexed.

So 4 11 will be reduced into the improper fra-Ction 12; for 4 being multiplyed by 12, the Product is 48, unto which adding the Numerator 11, the fum is 59 for a new Numerator, which being placed over the Denominator 12, gives the improper fraction $\frac{59}{12}$, which is equivalent unto $4\frac{11}{12}$ (as will appear by the 13 Rule of this Chapter.) In like

manner 7 ½ will be reduced into 15.

XI. A whole number is reduced To reduce a whole into an improper fraction, by planumber into an improper fraction cing the whole number given as a Numerator, and I as a Denominator.

So 14 Integers will be reduced into the improper fraction 14, and one Integer into the improper fraction +.

XII. A whole number is reduced into an improper fraction which shall have any Denominator affigned, in multiplying the whole number given by the Denominator affigned, and placing the Product as a Numerator over the said Denomina-

As if 13 be given to be reduced into an improper fraction whose Denominator shall be 4, multiply 13

by 4, the Product is 52, which being placed over 4, gives the improper fraction 52 equivalent unto 13 (as will appear by the next Rule.) In like man-

ner 13 may be reduced into 21.

XIII. An improper fraction may be reduced into its equivalent whole number or mixt number in this manner, viz. divide the Numerator by the Denominator, and the quotient will give the whole number or

Te reduce an improper fra-Hion into its equivalent whole or mixt number.

mixt number fought; So the improper fraction 12 will be reduced into this mixt number 411, for if 59 be divided by 12, the quotient is 411 Alfo this improper fraction 12 will be reduced into the whole

number 13.

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XIV. Fractions having unequal Denominators may be reduced into fractions of the same value, which shall have equal Denominators, by this Rule and the next following, viz. when two fractions

To reduce fractions to a common denominator ; viz. I. When two fractions are propounded.

having unequal Denominators are propounded to be reduced into two other fractions of the same value, which shall have a common Denominator, multiply the Numerator of the first fraction (that is, either of them) by the Denominator of the fecond, and the Product shall be a new Numerator (correspondent unto the Numerator of that first fra-Ction;)also multiplying the Numerator of the second fraction by the Denominator of the first, the Product is a new Numerator (correspondent unto the Numerator of the second fraction; lastly, multiply the Denominators one by the other, and the

Product

Product is a common Denominator to both the new Numerators.

Thus, if the fractions & and & be propounded, multiply 2 by 5, the product 10 is a new Numerator correspondent unto 2: also multiply 4 by 3, the product 12 is a new Numerator correspondent unto 4: lastly, multiply 3 by 5, and the product 15 shall be a common Denominator unto the 15 15 new Numerators. so the fractions 13 and are found out which have equal Denominators, and each of these new fractions is equal unto its correspondent fraction first given, viz. 10 is equal unto 3 and 13 is equal unto 4 (as will be manifest by the 4th Rule of this Chapter.)

XV. When three or more Fractions having un-

2. When three or Fractions areto be reduced into others that Shall have a Common Denominatur.

144

equal Denominators, are given to be reduced into other Fractions of the fame value with those given, but fuch as shall have one common Denominator; multiply continually (according to the thirteenth Rule of the fifth Chap-

ter)the Numerator of the first Fraction into all the Denominators, except the Denominator of that first Fraction; and reserve the last Product for a new Numerator instead of that first Numerator : In like manner, multiply continually the Numerator of the second Fraction into all the Denominators, except the Denominator of the second Fraction, and referve the last Product for a new Numerator, instead of the second Numerator; Proceed in like manner to find out new Numerators for the rest of the given Fractions: Lastly, multiply continually

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Chap. XVII. Vulgar Fractions 145 all the Denominators one into another, and the last Product shall be a common Denominator to all the new Numerators.

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iencly all As for Example, if these three Fractions, $\frac{2}{8}$, $\frac{2}{5}$, having unequal (or different) Denominators, be given to be reduced into three other Fractions of the same value, which shall have equal Denominator (or one common Denominator) First,

I multiply continually the first Numerator 3 into the second and third Denominators 5 and 7, saying 3 times 5 makes 15, which

multiplyed by 7 produceth 105, For a new Numerator instead of the first Numerator 3; Secondly, I multiply continually the second Numerator 2 into the first and third Denominators 8 and 7, saying, twice 8 is 16, which multiplyed by 7 produceth 112, for a new Numerator instead of the fecond Numerator 2; Thirdly, I multiply continually the third Numerator 5 into the first and fecond Denominators 8 and 5, faying 8 times 5 makes 40, which multiplyed by 5 produceth 200, for a new Numerator instead of the third Numerator 5; Fourthly and lastly, I multiply continually all the Denominators 8, 5 and 7 one into another, faying, 8 times 5 makes 40, which multiplyed by 7 produceth 280 for a Denominator to each of the three new Numerators 105, 112 and 200 before found out; And so these three Fractions 101, 112, and 200, are discovered, which have one common Denominator 280, and each of them is equal in value unto its correspondent Fraction first given, viz. 101 is equal unto 3; Also 112 is equal unto 3; and 200 is equal unto 1; as may eafily be proved by the Fourth Rule of this Chapter.

After the same manner, these four Fractions $\frac{2}{3}$, $\frac{2}{4}$, $\frac{4}{3}$, and $\frac{1}{6}$ are reducible into these, $\frac{240}{360}$, $\frac{270}{360}$, $\frac{280}{360}$ and $\frac{100}{360}$, which have 360 for a common Denominator, and are equal in value respectively to the sour Fractions given to to be reduced.

Note, Although by the foregoing fourteenth and fifteenth Rules, any multitude of Fractions may be reduced to a common Denominator; yet because Fractions in their least Terms are fittest for use, I shall shew how lesser Denominators, than those that will be discovered by the said Rules, may often times be found out, viz.

I. When the unequal Denominators of two Fra-Ctions have a common Divisor greater than 1, divide the Denominators severally by their greatest common Divisor (found out by the fore-going third Rule of this Chapter;) and then multiply cross-wise in this manner, viz. The Numerator of the first Fraction by the latter Quotient, and the Numerator of the latter Fraction by the first Quotient, and reserve the Products for new Numerators; Lastly, multiply the Denominator of the first Fraction by the latter Quotient (or the Denominator of the latter Fraction by the first Quotient,) fo shall the Product be a common Denominator to the faid new Numerators: As for example, if 12 and The proposed to be reduced to a common Denominator, I divide each of the Denominators 12 and 18 by their greatest common Divisor 6, and

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the Quotients are 2 and 3; then I multiply 5 the Numerator of the first Fraction by 3 the latter Quotient, also 7 the Numerator of the latter Fraction by 2 the first Quotient, and the Products 15 and 14 I reserve for new Numerators instead of 5 and 7; Lastly, I multiply 12

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36	36

the Denominator of the first Fraction by 3 the latter Quotient (or 18 the Denominator of the latter Fraction by 2 the first Quotient,) and the Product 36 is a Denominator to each of the new Numerators 15 and 14: so \frac{1}{36} and \frac{1}{36} are found out, which have the least common Denominator unto which the given Fractions \frac{1}{2} and \frac{1}{8} can be reduced;

Also $\frac{15}{36}$ is equal to $\frac{5}{12}$, and $\frac{14}{36}$ to $\frac{7}{18}$.

II. Whensoever the Denominator of a Fraction can be divided by the Denominator of a second Fraction, without any Remainder; then if by the Quotient you multiply severally the Numerator and Denominator of such second Fraction, a third will arise, having the same value with the second, and the same Denominator with the first Fraction: By this Rule three or more Fractions may often times be reduced to a lesser common Denominator, than that which will be discovered by the foregoing Rule XV. As for Example, Let these six sollowing Fractions be given to be reduced to a common Denominator, viz.

$\frac{13}{36}$, $\frac{11}{18}$, $\frac{7}{12}$, $\frac{4}{9}$, $\frac{5}{6}$, $\frac{2}{3}$.

Because 36 the Denominator of the first Fraction, being divided by the five other Denominators severally.

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rally will give these Quotients 2, 3; 4, 6, and 12 without any Remainder, I multiply the Numerator and Denominator of each of the five latter Fractions, by its correspondent Quotient, viz. 11 and 18 by 2 the first Quotient; Also 7 and 12 by 3 the second Quotient, and in like manner the rest; So instead of those five latter Fractions, sive others (hereunder placed after the first of those six) are produced, viz.

$\frac{13}{36}$, $\frac{22}{36}$, $\frac{21}{36}$, $\frac{16}{36}$, $\frac{30}{36}$, $\frac{24}{36}$.

All which Fractions last express have a common Denominator 36, and are equal in value respective-

ly to those given to be reduced.

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pound fraction
to a fingle fraction. See continual
multiplication in
the last Rule of
the 5th Chapter.

XVI. A compound fraction (otherwise called a fraction of a fraction on) may be reduced into a single fraction in this manner, viz. Multiply all the Numerators continually, and take the Product for a new Numerator, also multiply all the

Denominators continually, and the Product shall

be a new Denominator.

Thus, if the compound fraction of the given to be reduced into a single fraction, multiply the Numerators 2 and 3, one by the other, so is the Product 6 a new Numerator. Also multiplying

the Denominators 3 and 4 one by the

other, the product 12 is a new Denominator, so 76 (or 1/2 is the single
fraction sought, being equivalent unto
of 1/4 the compound fraction given to be reduced.

Chap. XVII. Vulgar Fractions. 149
In like manner, this compound Fraction 2 of 2

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In like manner, this compound Fraction $\frac{2}{3}$ of $\frac{4}{4}$ of $\frac{4}{5}$ will be reduced unto $\frac{24}{60}$, or $\frac{2}{5}$; For the Numerator 2, 3, 4 being multiplyed continually produce the new Numerator 24, And the Denominators 3, 4, 5 multiplyed continually produce the new Denominator 60; Lassly, the new Fraction $\frac{24}{60}$ (by the fourth Rule of this Chapter) will be reduced unto $\frac{2}{5}$, which is equal to $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{4}{5}$: But to make the meaning hereof more evident, Suppose the Integer to be one poind of English money; Then

\$\frac{1}{5}\$ of 1 l. (viz. of 20s.) is—16s.

\$\frac{3}{4}\$ of those \$\frac{4}{5}\$ (viz. of 16s.) is—12s.

\$\frac{2}{3}\$ of those \$\frac{2}{4}\$ (viz. of 12 s.) is \to 8 s. or \$\frac{2}{5}l\$. whereby 'tis manifest that \$\frac{2}{3}\$ of \$\frac{3}{4}\$ of \$\frac{4}{5}l\$ l.is equal to \$\frac{2}{5}l\$.

By this Rule a fraction or mixt number of a lesser name may be reduced to a fraction of a greater name. As if $3\frac{1}{2}$ pence be propounded to be reduced into an improper fraction of a pound sterling, the operation will be in this manner, viz. $3\frac{1}{2}$ or $\frac{7}{2}$ of a peny is $\frac{7}{2}$ of $\frac{1}{12}$ of $\frac{1}{20}$ of a pound sterling, which compound fraction will (by the aforesaid Rule) be reduced to $\frac{1}{480}$ l. In like manner $42\frac{7}{16}$ minutes of an hour are equal to $\frac{45}{64}$ of an hour, for $\frac{67}{16}$ (that is $42\frac{7}{16}$) of $\frac{1}{60}$ are equal to $\frac{67}{260}$ (or in its least terms) $\frac{45}{64}$.

Here you may also observe, that when a compound fraction is one of the given terms in any question, it is first of all to be reduced to a single

fraction by the aforesaid sixteenth Rule.

XVII. Two or more fractions being given, there may be whole numbers found, which shall have the same reason or proportion as the

To find whole numbers, which shall have the same reason as any fra-. Elions or mixt numbers given.

fractions

fractions given, viz. When the fractions given have unequal denominators, reduce them into equivalent fractions which shall have a common denominator (by the 14th or 15th Rule of this Chapter;) then rejecting the common denominator, the Numerators shall have the same reason or proportion

as the fractions first given.

So 3 and 5 being given, will first of all be reduced into their equivalent fractions 24 and 25; then rejecting the common denominator 40, the Numerators 24 and 25 have the same reason with 3 and 5 viz. As 3 is to 5 fo is 24 to 25: also if the fractions 1/4 and 1/2 were given, there will be found 8, 16, and 32, which are in the same proportion one to the other as the fractions given: In like manner, if mixt numbers be given, there may be whole numbers found which thall have the fame reason or proportion, as the mixt numbers; so 5 3 and 3 5 being given, will be first reduced into the improper fractions 17 and 29 (by the tenth Rule of this Chapter:) also the said 17 and 22 will be reduced into 126 and 87 sthen rejecting the common Denominator 24, the Numerators 136 and 87 will have the fame reason as 5 3 and 3 2, viz. As 136 is to 87, so is 5 3 to 3 5 : also 16 2 and 18 being given, there will be found 33 and 36, which being divided by their common Divisor 3 (found out by the third Rule of this Chapter) will give 11 and 12 which have the same reason as 16 1 and 18.

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CHAP. XVIII.

Addition of Vulgar Fractions and mixt Numbers.

I. VV Hen the numbers given to be added are fingle fractions, and have equal denomi-

nators, add all the Numerators together, so is the sum the Numerator of a fraction, whose denominator is the same with the common denominator; which new fraction is the sum of the

To all single fractions, viz

1. when they have equal denominators

fractions given to be added.

So $\frac{1}{9}$ and $\frac{2}{9}$ being given to be added, their sum will be sound $\frac{1}{9}$ viz. the sum of the numerators, 3 and 2, is 5, which being placed over the common denominator 9, gives $\frac{5}{9}$: In like manner the sum of these fractions $\frac{2}{8}$ $\frac{1}{8}$ and $\frac{2}{8}$ will be sound $\frac{12}{8}$, which (by the 13 Rule of the seventeenth Chapter) will be sound equivalent unto $2\frac{12}{8}$; so that $2\frac{1}{8}$ is the sum of the fractions given to be added.

II. When the fractions given to be added have unequaldenominators, they are first to be reduced into fractions of the same value, which shall

2. When they have uniqual denominators?

have a common Denominator (by the fourteenth or fifteenth Rule of the seventeenth Chapter;) and then they may be added by the first Rule of this Chapter.

So if \(\frac{1}{3} \) and \(\frac{1}{3} \) were given to be added, their fum will be found 1 \(\frac{1}{25} \); for (by the fourteenth Rule of

and $\frac{2}{13}$, which having equal Denominators may be added according to the first rule of this Chapter, and for the sum will be found $1 \frac{4}{13}$. In like manner the sum of these fractions $\frac{1}{13}$ that is $1\frac{4}{13}$ ons $\frac{1}{2}\frac{3}{8}$ and $\frac{3}{4}$ will be found $1\frac{5}{8}$. Also the sum of these six Fractions, $\frac{1}{3}\frac{3}{6}$

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11/8 , π², 15 , 2 , after they are reduced to a common Denominator (according to the latter Example in the note at the end of the fifteenth Rule of the feventeenth Chapter) will be found 12%, that is, 3 ½.

III. When any of the fractions given to be added is a compound fraction, such the Addition of compound fraction is furth of all to be reduced into a single fraction (by the sixteenth Rule of the seventeenth

Chapter) and then you may proceed as before.

So \(\frac{2}{3}\) and \(\frac{2}{3}\) of \(\frac{1}{3}\) being given to be added, their (um will be found \(\frac{2}{3}\) for the compound fraction \(\frac{2}{3}\) of \(\frac{1}{3}\) will (by the tixteenth Rule of the 17th Chapter) be reduced to \(\frac{1}{2}\) (or in its least terms) \(\frac{1}{6}\) which added to the single fraction \(\frac{1}{3}\) (according to the second rule of this Chapter) gives \(\frac{2}{3}\). Here you may observe, that the fractions given to be added in all the sormer cases, are supposed to be fractions

etion is means fame particular denomination, viz. if the name of one of the fractions given to be adans Integer or ded, be a fraction of a pound sterling: all the rest ought to be fractions of a

pound

Chap.XVIII. Vulgar Fractions.

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pound sterling; and the like is to be understood of other denominations.

of different denominations are given to be added, they are first of all
to be reduced into fractions of Inte-

gers which shall have one and the same particular denomination (by the sixteenth Rule of the seventeenth Chapters) and then they may be added by

the first or second Rule of this Chapter.

So if $\frac{2}{9}$ of a pound sterling, $\frac{3}{5}$ of a shilling, and $\frac{5}{8}$ of a peny were given to be added, reduce the two latter into fractions of a pound sterling (by the sixteenth Rule of the seventeenth Chapter) viz. $\frac{1}{5}$ of a shilling is $\frac{3}{5}$ of a pound sterling, which compound fraction being reduced into a single fraction, gives $\frac{1}{100}$ li. Likewise $\frac{5}{8}$ of a peny, is $\frac{3}{4}$ of $\frac{1}{100}$ of a pound sterling, which compound fraction being reduced, gives $\frac{3}{384}$ li. Lastly, $\frac{3}{5}$ li. $\frac{1}{100}$ li. and $\frac{3}{384}$ li. being added according to the second Rule of this Chapter, their sum will be sound $\frac{2}{3}$ li. $\frac{3}{4}$ li. So on in its least terms, $\frac{2}{2}$ lies furn will be sound

find first of all the sum of the fra-Gions (by the first and the second Rule numbers. of this Chapter;) then add the Integer

or Integers (if there be any found) in the fum of the fractions, unto the whole numbers, and collect the fum of them as you were taught by the Rules of the third Chapter.

So if 3 \(\frac{1}{2}\) 4 \(\frac{1}{3}\) and 16 \(\frac{1}{3}\) were given to be added, their furn will be found $24\frac{1}{2}\frac{1}{4}$ wiz. the furn of the fractions \(\frac{1}{2}\) \(\frac{1}{3}\) and \(\frac{1}{3}\) will be found (by the second Rule of this Chapter) to be $1\frac{1}{2}\frac{1}{4}$ and the sum of the

L 3 whole

whole numbers 3, 4, and 16, is 23, unto which adding I (the Integer found in the fum of the fractions) the fum is 24; so that 24 11 is the fum of the mixt numbers given to be added.

CHAP. XIX.

Subtraction of Vulgar Fractions and mixt Numbers.

Hen the numbers given are both fingle fractions and have equal denominators,

fingle frallions, viz. I. When they have a common denominator

subtract the lesser numerator The subtrattion of from the greater, and place the remainder over the common denominator, so is such new fraction the difference between the

fractions given.

Thus the difference between the fractions -? and 77 is 77, which is found by subtracting the lesser numerator 7 from the greater denominator 9, and placing the remainder 2 over the common denominator II; also the difference between the fractions 11 and 17 is 21, that is, the fraction 17 exceeds 11 by -6.

II. When the numbers given are both fingle fractions, and have not a common 2. When they denominator, reduce them into frabave unequal ctions of the same value which shall denominators have a common Denominator (by

the fourteenth or fifteenth Rule of the seventeenth Chapter,) and then find their difference by the last Rule.

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So the difference between the fractions $\frac{6}{7}$ and $\frac{2}{8}$ will be found $\frac{1}{36}$ viz. reducing the fractions given into their equivalent fractions $\frac{43}{36}$ and $\frac{49}{36}$ which have a common denominator, the difference fought will be found $\frac{1}{36}$ by the first Rule of this Chapter. Likewise $\frac{12}{12}$ being subtracted from $\frac{11}{13}$, there will remain $\frac{41}{136}$.

III. When one of the numbers given is a whole number or a mixt number, also when both of them are mixt numbers, reduce such whole, or mixt numbers into an

The subtraction of mixt numbers, viz. 1. By uze-neral Rul.

improper Fraction or Fractions by the tenth or eleventh Rule of the seventeenth Chapter, and then the operation will be according to the first or se-

cond Rule of this Chapter.

So 7 \(\frac{3}{5}\) being given to be subtracted from 12, the remainder will be sound 4 \(\frac{2}{5}\); viz. First 7 \(\frac{3}{5}\) will be reduced into the improper Fraction \(\frac{18}{5}\), also 12 will be reduced to \(\frac{12}{1}\), then these two improper fractions \(\frac{18}{5}\) and \(\frac{12}{1}\) will be reduced into their equivalent fractions \(\frac{18}{8}\) and \(\frac{60}{5}\) (which have a common Denominator.) Lastly, the difference between \(\frac{18}{5}\) and \(\frac{60}{5}\) is \(\frac{22}{5}\), or 4\(\frac{2}{5}\). In like manner 9\(\frac{1}{2}\) being given to be subtracted from 12\(\frac{1}{5}\), the remainder will be found 2\(\frac{70}{10}\); as by the subsequent operation is manifest.

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#2 that is 4 2	1 27 that is 2 70.	44
by the lait Rule is to m	L4 Alsh	nough

the Integers confift of many places, as will be manifest by the operation, viz.

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IV. When a whole number is given to be fub-

will be more expeditious in the fubtraction of mixt numbers, or whole and mixt, especially when

tracted from a mixt number, lubtract the faid whole number from the 2. By payticular Kutes viz. Integer or Integers of the mixt num-I. A whole ber (as is taught by the Rules of the number from fourth Chapter) and unto the rea mixt nummainder annex the fractional part of

the mixt number given, fo is the mixt number thus found, the remainder or difference lought.

As if 7 be given to be subtracted from 24 \$, the remainder 17 80 as by the operation feit.

V. When a fraction is given to be subtracted from an Integer, subtract the Nume-2. A Fraction rator from the Denominator, and from an Inte. place that which remains over the ger all sty Denominator, which new fraction

thus found, is the remainder or difference fought.

So } being subtracted from an Integer, or 1, the remainder is 3: Also 13 being subtracted from 1, the remainder is 7%.

- VI. When a fraction is given to be subtracted

from a whole number greater 3. A Fragion from than I, subtract the faid fraa whole number great ction from one of the Integers ger than I. given (by the last Rule;) so the Althurated

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remaining fraction being annexed to the number of Integers lessened by unity or 1, gives the remainder or difference sought.

Thus \(\frac{1}{7}\) being subtracted from 17, the remainder is 16\(\frac{1}{7}\): also \(\frac{1}{2}\) being subtracted from 39, the re-

mainder is 38 -5.

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id frantegers) fo the naining VII. When a mixt number is given to be subtracted from a whole number, subtract first of all (by the sisth Rule of 4 A mixe this Chapter) the fractional part of number from the mixt number from an Integer ber borrowed from the whole number

given, and fet down the remaining fraction, then adding the Integer borrowed unto the Integer or Integers of the mixt number, subtract the said sum from the whole number given (as is taught in sub-

from the whole number given (as is taught in subtraction of whole numbers;) so that which remains, together with the remaining fraction before found, is the remainder or difference sought.

So if $9\frac{7}{12}$ be subtracted from 50, the remainder is $40\frac{7}{12}$, as by the operation is $9\frac{7}{12}$ manifest.

fubtracted from a mixt number, and the faid fraction is less than the fractional part of the mixt number, subtract the lesser fraction from the greater by the first 5. A fraction from a mixt

or second Rule of this Chapter, then from a mixt number by this the remaining fraction being annex- and the next ed to the Integer or Integers of the Rule.

or difference fought.

X. When a mixt number is given to be subtra-

cted from a mixt number, and the fractional part of the mixt number 6. A mixt number from a mixt to be subtracted, is less than the franumber by this ctional part of the mixt number and the next from which you are to subtract, sub-Rule. tract the said lesser fraction from

the greater (by the first or second Rule of this Chapter) and set down the remaining Fraction : also subtract the Integers of the leffer mixt number from the Integers of the greater (as in Subtraction of whole numbers;) fo is the mixt number thus found, the remainder or difference fought.

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Chap. XIX. Vulgar Fractions 159

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So if 17 % be given to be subtracted from 20 5, the remainder will be found 20 5 3 19, viz. Subtracting 1 from 5, the remainder is 12; also subtracting 17 from 20, the remainder is 3.

XI. When a mixt number is given to be subtracted from a mixt number, and the fractional part of the mixt number to be subtracted is greater than the fractional part of the mixt number from which you are to subtract, subtract the faid greater Fraction from an Integer borrowed from the greater mixt number (by the fifth Rule of this Chapter) and add the remaining fraction unto the fractional part of the greater mixt number (by the first or second Rule of the 18th Chapter;) so is the fum to be referved as the fractional part of the remainder fought; then add the Integer borrowed unto the Integer or Integers of the leffer mixt number, and subtract the sum from the Integers of the greater mixt number (as in subtraction of whole numbers;) fo that which remains, together with the fraction before referved, is the remainder or difference fought.

Thus if 20 % be given to be subtracted from 35% the remainder will be found 14 22, viz. subtracting ? from an Integer or 1, the 35 \$ remainder is \$, which added to \$ gives 20 \$ then adding the Integer borrowed unto 14 29 20, it will be 21, which subtracted from 35, the remainder is 14, fo the remainder or difference sought is 14 22. when the west of the west of when

When you cannot clearly discern which is the greater of two fractions, having unequal denominators, reduce them into fractions of the same value which shall have a common Delication the nominator (by the fourteenth Rule greater of two

fractions. of the seventeenth Chapter) and then it will be apparent which of the two fractions is the greater. As, if it be desired to know which of these two fractions 7 and 11/3 is the greater, after they are reduced to 28/2 and 27/2, it is evident that the former exceeds the latter by 21/2.

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entroping company CHAP. XX.

Multiplication of Vulgar Fractions and mixt numbers.

Hen the numbers given to be multiplyed are both fingle fractions, multiply the Numerators one by the other and take the Product for a new numerator; also multiply the denominators one by the other and take the product for a new numerator;

by the other, and the product is a new denominator,

which new traction is the product fought.

so $7\frac{1}{2}$ and $\frac{5}{8}$ being given to be multiplied, the product will be found $\frac{5}{9}\frac{5}{6}$, for 7 multiplied by 5 produceth 35 for a new Numerator, and 12 multiplied by 8 produceth 96 for a new Denominator: also $\frac{5}{7}$ and $\frac{3}{7}$ being multiplied one by the other, the product will be found $\frac{1}{4}\frac{5}{9}$. Here you may observe that in the multiplication of proper Fractions, the product is always less than either of the terms given, For in multiplication such proportion

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Chap.XX. Vulgar Fractions 161; as unity or 1 hath to either of the terms given, the same proportion hath the other term to the pro-

the first Rule of this Chapter: As forexample-flub

II. When one of the numbers given is a whole number or a mixt number; also To multiply mixe when both of them are mixt num numbers. bers reduce such whole number or

mixt number or numbers into an improper fraction or fractions by the tenth or eleventh Rule of the seventeenth Chapter, and then the operation

will be the fame as in the last Rule. To Bulle There

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So 8 \(\frac{2}{3}\) being given to be multiplied by 5, the product will be found 43 \(\frac{1}{3}\); viz. 8 \(\frac{2}{3}\) being reduced into the improper fraction \(\frac{26}{3}\); also 5 unto \(\frac{1}{3}\); multiply 26 by 5, the product is 130 for a new Numerator: also multiplying 3 by 1, the product is 3 for a new Denominator, which new Fraction \(\frac{13}{3}\) being reduced (according to the thirteenth Rule of the seventeenth Chapter) will be 43 \(\frac{13}{3}\) the product sought. In like manner 7 \(\frac{1}{2}\) being multiplied by 5 \(\frac{1}{3}\), the product will be found 42. Here observe, that when either of the terms given is a compound fraction, it is first of all to be reduced into a single fraction, and then the operation is as before.

Note 1. Sometimes the work of Multiplication in Fractions may be very usefully contracted by this

following Rule, viz.

When two Fractions propos'd to be multiplyed (whether they be proper or improper) are such, that the Numerator of the one, and the Denominator of the other, may be severally divided by some common Divisor without a remainder; you may

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and Denominator, and then multiply as before in the first Rule of this Chapter: As for example, if be to be multiplyed by $\frac{5}{12}$; because 6 the Numerator of the first, and 12 the Denominator of the latter Fraction, being severally divided by their common Divisor 6 give the Quotients 1 and 2, I set these (or imagine them to be set) in the places of and 12; by which exchange there arise $\frac{1}{7}$ and $\frac{1}{2}$, these multiplyed one by the other (according to the first Rule of this Chapter) produce $\frac{1}{14}$ the desired Product of $\frac{1}{7}$ into $\frac{1}{12}$, in the smallest terms.

Again, to multiply $\frac{16}{48}$ by $\frac{3}{16}$; because the Numerator of the first Fraction and the Denominator of the latter, being each divided by 16 give the Quotients 1 and 1, I set 1 and 1 in the places of 16 and 16; likewise because 48 the Denominator of the first, and 3 the Numerator of the latter Fraction, being each divided by their common Divisor 3, give 16 and 1, I take 16 and 1 instead of 48 and 3; so by those exchanges there arise $\frac{1}{16}$ and $\frac{1}{1}$, which multiplyed one by the other produce $\frac{1}{16}$, which is the Product in the smalless terms made by the multiplication of 16 into (archiv) $\frac{1}{16}$

tiplication of \(\frac{16}{48} \) into (or by) \(\frac{1}{6} \).

2. To take any part or parts of a number propounded, is nothing else but to multiply the said number by the Fraction which declareth what part is to be taken: so if you defire to know what is \$\frac{1}{8}\$ of 320, multiply \$\frac{120}{2}\$ by \$\frac{1}{8}\$, or \$\frac{40}{1}\$ by \$\frac{1}{1}\$, and the product will be 200. In like manner \$\frac{1}{3}\$ of 45 \$\frac{3}{8}\$ is \$30\frac{1}{4}\$. Also \$\frac{1}{4}\$ of 120 is 30.

^{3.} Som etimes the work of multiplication in mixt numbers

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numbers may be compendiously performed after the manner of these following examples. viz.if it be required to multiply 120 \(\frac{1}{4}\) by 48 \(\frac{1}{2}\), first multiply the whole numbers mutually, to wit, 120 by 48, and place the particular products orderly one un-

der the other as in Multiplication of whole numbers; then multiply the said whole numbers first given by the fractions alternately, viz. take \(\frac{1}{4}\) of 48 which is 12, also take \(\frac{1}{2}\) of 120 which is 60, and place the said 12 and 60 orderly to be added to the former particular products: Lastly, addalltogether, and to the sum annex the product of the

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two fractions, to wit in this example, the product of the Multiplication of $\frac{1}{4}$ by $\frac{1}{2}$, which is $\frac{1}{8}$, so the total product required will be $5832\frac{1}{8}$, as you see by the example in the Margent. In like manner, if $18\frac{1}{2}$ be multiplied by $40\frac{1}{3}$, the product will be $746\frac{1}{6}$; and if $29\frac{1}{2}$ be multiplied by 50, the product will be 1475, as you see by the examples following.

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403	50
720	1450
20	25
6	1475
746 %	La single at the Management

4. When a fraction is to be multiplyed by a number which happens to be the same with the Denominator, take the Numerator for the product; so if this fraction \(\frac{1}{4} \) be propounded to be multiplied by the Denominator 4, the product will

and place the particular products orderly one un-

whole numbers: then multiply t

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CHAP. XXI.

Division of Vulgar Fractions and mixt numbers.

Hen the numbers given are both fingle fractions, multiply the Denominator of the Divisor by the numerator of the The Division of Dividend, and take the product Tingle fractions. for a new numerator: also multiply the numerator of the Divisor by the denominator of the Dividend, and the product is a new denominator; which new fraction is the quotient fought. So if & be given to be divided by &, the quotient will be found 27; vig. multiplying 5 by 4 the product is 20 for a new numerator, also multiplying 3 by 9, the product is 27 for a new denominator, to is 20 the quotient fought; in like manner if & begiven to be divided by the quotient will be found 16 that is 2 16, as you fee in the Exam-12) (15) ple: here you may observe, that in Disan die som vision by proper tractions, the quotient

for in Division, as the divisor is in proportion to I

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II. When one of the numbers given is a whole number or a mixt number; also when both are mixt numbers, reduce such whole number or mixt number or numbers into an improper fraction or fractions, by the tenth or eleventh Rule of the feventcenth Chapter, and then the operation will be the same as in the last Rule.

So if 42 be divided by 7 1, the quotient will be found 5 3, for 7 1 and 42 will be reduced into these improper fractions 14 and 47, then multiplying 42 by 2, the product is 84 for a new

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Numerator, also multiplying 15 by 1, the product is 15 for a new denominator, fo is \$4 the quotient fought, which is equal to 5 3 (as is evident by the thirteenthRule of the seventeenthChapter.) In like manner, if 6 1 be divided by 3 2, the quotient will be 1 31. Also if 5 1 be divided by 12 1

the quotient will be 33.

Note, Sometimes the work of Division in Fractions may be very usefully contracted by this following Rule, viz. When either the two Numerators, or the two Denominators of the Fractions propofed, can be divided feverally by some common Divisor without a remainder, you may take the Quotients instead of the said Numerators or Denominators, and then divde by the first Rule of this Chapter: as for example, if 12 be to be divided by s, because the Numerators 12 and 8 being each divided by their common Divisor 4 will give the Quotients 3 and 2, I take these instead of 12 and 8, by which exchange there arise 17 and 3 the former of which being divided by the latter, (according to the first Rule of this Chapter) gives 34, which is the Quotient in the least terms that ariseth

by dividing 17 by 8. dw

Again, to divide \$\frac{2}{8}\$ by \$\frac{1}{8}\$; because the Numerators 25 and 15 being severally divided by their common Divisor 5 give the Quotients 5 and 3, likewise because the Denominators 8 and 8 being each divided by 8 give the Quotients 1 and 1, I set 5 and 3 in the places of the Numerators 25 and 15, also 1 and 1 in the places of the Denominators 8 and 8, whence arise \(\frac{1}{2}\) and \(\frac{1}{2}\); Lastly dividing \(\frac{1}{2}\) by \(\frac{1}{2}\), that is 5 by 3, there ariseth \(\frac{1}{3}\), that is 1\(\frac{1}{3}\), which is the defired Quotient of \$\frac{1}{8}\) divided by \$\frac{1}{8}\.

Fractions before delivered.

Quest. 1. The difference of two numbers is $1\frac{13}{24}$, the lefter number is $2\frac{1}{3}$, what is the greater? Answ. $3\frac{2}{3}$, (found by Addition.)

2.2. What number is that, which if added to 3 \frac{1}{8} gives the sum 8\frac{1}{8}? Answ.4\frac{1}{1} (found by Subtraction.)

Quest. 3. There is in three bags the sum of 121-21. viz. in the first bag 50 \(\frac{1}{3} \) l. in the second 40 \(\frac{1}{3} \) l. what is in the third bag? Answ. 30 \(\frac{1}{3} \) l. (found by Addition and Subtraction.)

Quest. 4. Two Merchants A and B, have certain there in a Ship, the share of A is 70 of the Ship, that of B 73, what is the difference between their parts? Answ. the share of A exceeds the share of B by 730 (found by Subtraction.)

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Chap. XXII. Notation of &c. 167 Quest. 5. What is \(\frac{5}{8} \) of 130 \(\frac{2}{3} \)? Answ. 81\(\frac{2}{3} \)

(found by Multiplication.)

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Quest. 6. What number is that, which being multiplied by \(^3\) produceth 25 \(^3\)? Ans. 42 \(^1\) (found by Division.)

Now followeth the doctrine of Decimal Fractions.

The Doctrine of Decimal Fractions.

CHAP. XXII.

Notation of Decimal Fractions.

I. I T is hard to determine, who was the first that brought Decimal Arithmetick to light, though it be a late Invention; but without doubt it hath received much improvement within the compass of a few years, by the industry of Artists, and now seems to be arrived at persection. The excellency thereof is best known to such as can

apply it to the practical part of the Mathematicks, and to the Constru-Ction of Tables, which depend upon

standing or constant proportions, such are Trigonometrical Canons, Tables for computing of compound
Interest, &c. in which cases decimal operations do
afford so great help, that (in my opinion) many ages have not produced a more usefull invention.
But it may be objected, that Decimal Arithmetick
for the most part gives an impersect solution to

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a question. This I grant, yet the answer so given may be as usefull as that which is exactly true; for in common affairs, the loss of Toos part of a grain, or of an inch,&c. to wit, any quantity which cannot be seen, is inconsiderable: but I could not be mistaken, for inextolling Decimals I do not cry

down Vulgar Fractions, fince experience sheweth that Decimal Fractions Decimal Fraare commonly abused, by being apctions Some times abufed. plyed to all manner of questions a-

bout money, weight, &c. when indeed many questions may be refolved with much more facility by Vulgar Arithmetick, as may partly appear by this Example, viz. at 91. -6 s. -8 d. the hundred weight of Tobacco, what will 987 hundred weight cost? Answ. 9212 l. which by the common Rule of Practice by Aliquot parts is found out in a quarter of the time, that will necessarily be required to work it by Decimals, which at last will give an imperfect answer; I might instance the like inconvenience divers wayes, were it not for loss of time; fo that the right use of Decimals depends upon the discretion of the Artist.

II. When a fingle Fraction hath for its denominator a number confisting of 1 or of a Decimal Unity in the extream place towards the left hand, and nothing but a Cy-Fraction pher or Cyphers towards the right, it is more particularly called a Decimal: of this kind are these that follow, To, that is five tenths, 100, five hundredth parts; likewise these are decimalfractions, 1000, 10000, 10000, &c.

III. A Decimal traction may be exprest with-

out

Decimal Fractions. Chap.XXII. 169 out the denomonator, by prefixing a point or comma before (to wit, on the left hand of) the numerator, fo -5 may be written thus, .5 or thus ,5 and Too thus, .25 or thus ,25.

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IV. In Decimals when the Numerator confists not of so many places as the Denominator hath Cyphers, fill up the void places in the Numerator with Cyphers perfixed on the left hand: fo - is written thus .05; likewise 7000 thus, .050; and 10000, thus, .0205, likewise 1000, thus, .006.

V. In Decimals thus exprest, the Denominator is discoverable by the places of the Numerator: for if the Numerator confists of one place, the Denominator confifts of 1 or unity with one Cypher; if of two places, the Denominator confists of 1 with two Cyphers annexed; if of three, the Denominator confilts of 1 or unity with three Cyphers annexed: so the Denominator of .25 is 100, the Denominator of .050 is 1000, and the Denominator of .096 is 1000.

VI. Cyphers at the end of a Decimal do neither augment or diminish the value thereof: fo.2, .20, .200, .2000 are decimals, which have one and the fame value, for 700 being abbreviated by the eighth Rule of the feventeenth Chapter, will be made -2

and fo will -200 or -2000

VII. Wherefore Decimal fractions are easily reduced to a common Denominator (which is a troublesome work in Vulgar Fractions;) for if all the Numerators of as many decimal fractions as are given, be made to confist of the same number of places, by annexing a Cypher or Cyphers at the

as are defective, they will all be reduced to a common Denominator, fo these Decimals .2, .03, .027 (which fignifie 12, 100, 1000) may be reduced into these, .200, .030, .027, which have a 1000

for a common Denominator.

VIII. The order of places in any Decimal proceedeth from the left hand to the right, contrary to the order of places in Integers, which is from the right hand to the left: so in this Decimal .247, the figure 2 standeth in the first place (being the outermost towards the left hand, and next to the point,) the figure 4 standeth in the second place , and 7 in the third. Also in this Decimal .0245, a Cypher stands in the first place, 2 in the second

in the third, and 5 in the fourth.

IX. Every place in the Numerator of a Decimil Fraction hath a peculiar Denominator or proper value, viz. the Denominator of the first place is 10; of the fecond, 100; of the third, 1000, &c fo that the first place of a Decimal signifies tenth parts of an unite or Integer; the second place, hundredth parts of an Integer; the third place, thoulandth parts of an Integer, &c. Hence it is manifest, that this Decimal 3254 (every place thereof being confidered apart by it felf) confifts of .3, .02, .005, .0004 (viz. 10, 100, 1000, 1000, which being rednced to a common denominator (by the seventh Rule of this Chapter) will give these, .3000, .0200, 0050, .0004 (to wit, 10000, 10000, 10000, 10000) all which collectively make .3254 (or 10000)

X. In whole numbers, the first place above (that is on the left hand of) the place of unities figni-

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Chap. XXII. Decimal Fractions.

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fies Tens of unities; but the first place beneath, (that is on the right hand of) the place of unities fignifies tenth parts of 1 or unity, and is called the first place of Decimal parts, or place of Primes; likewise the second place above the place of Unities, fignifies hundreds of Unities, but the fecond place beneath the place of Unities fignifieth hundredth parts of I or unity, and is called the Second place of Decimals, or place of seconds; so that as the values of the places in Integers do ascend in a decuple proportion from the place of Units towards the left hand, so the values of the places of Decimals do descend in a subdecuple proportion beneath the place of units towards the right hand : viz. Among the places of Integers, every following place towards the left hand, is ten times the value of the next preceding place; But among the places of Decimal parts, every following place towards the right hand is one tenth part of the value of the next preceding place: all which will be evident by the following Table.

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A Table for the Notation of Integers and Decimals.

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In the foregoing Table you may observe, that the places of Integers or whole numbers are separated from the places of Decimal parts of 1 (or unitie) by a point; so the number on the lest hand of the Chap. XXII. Decimal Fractions.

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the point expresseth 73285 Integers or unities, but the number on the right hand of the point express feth only 8237 parts of I (or an Integer) Support fed to be divided into 10000 equal parts. In like manner this number 5 . 8 fignifies 5 Integers and eight tenth parts of an Integer, and this number 285 .82 fignifies 285 Integers (or Unities) and parts of an Integer, and laupo moto mot osni from much be supposed or imagined when it, cannot

acteany he made.) I his feet in length to divided, ecing applied to the fides of faperficial figures, or of

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Concerning the Reduction of Vulgar Fra-Etions to Decimal Fractions.

vulgarly divided will thew you how many feer

and how much this excels the vulgar may of thall I. F E the greatest Integer of money, as also of weight; measure. &c. were subdivided decimally, to wit, a pound of English money into ten equal pieces of coyn, and every one of these into ten other equal pieces, &cc. and weights, measures, &c. after the same manner; the doctrine of Arithmetick would be taught with much more ease and expedition than now it is; but it being improbable that fuch a reformation will ever be brought to pass, I shall proceed in directing a course to the studious for obtaining the frugal use of such Decimal fractions as are in his power. The second of the borne of the street

II. Forasmuch as in Arithmetical questions, some of the given numbers do for the most part happen to be fractions, a way must be shewd how to reduce a Vulgar Fraction to a Decimal Fraction ; yet in -111/1 E

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some cases there is no need of this Reduction; for example, a foot in length is vulgarly subdivided into 12 inches, an inch into 4 quarters, and each quarter into 2 half quarters; but a foot may as eafily, and a great deal more commodiously be divided, first into ten equal parts, and then each of those into ten other equal parts, and each of these into ten other equal parts ; (or at least such divifion must be supposed or imagined when it cannot actually be made.) This foot in length fo divided, being applyed to the fides of Superficial figures, or of folids will at first fight give the quantities of lines in feet and decimal parts of a foot (as readily as a foot vulgarly divided will shew you how many feet, inches, quarters, and half quarters are contained in any line) from whence the Superficial or folid content may be found in feet by multiplication only; and how much this excels the vulgar way, I shall partly manifest in the fifth Rule of the 26th Chapter. The like fubdivision I would have to be made of a Yard, Pereb &count your Miland to be

I I I. A fingle fraction, which is no decimal fraction, may be reduced into a deHow to reduce i cimal of the fame value, or infinitely a vulgar fractions cannot mal fraction. be exactly reduced to decimals) by

Denominator of any single fraction whatsoever, is to the Numerator thereof, so is any other Denominator to his correspondent Numerator: Example, let it be required to reduce into a Decimal, whose Denominator is assigned to be 1000, say by the Rule of three, if the Denominator 8 hath 5 for a Numerator, what will the Denominator 1000 require for a Numerator, what will the Denominator 1000 require for a Numerator, what will the Denominator 1000 require for a Numerator.

Chap. XXIII. to Decimal Fractions. a Numerator? Multiply and divide as the Rule of Three direct doth require, fo will the fourth proportional be found to be 625, which is the Numerator Sought; therefore -625 or .625, is a decimal fraction equal in value to 1. Another Example, let it be required to reduce 240 into a decimal fraction, whose Denominator shall be 100000, say by the Rule of three, if 240 the Denominator give 7 for a Numerator, what will the Denominator 100000 require for a Numerator? Answ. 2916 and somewhat more, but that which the faid 2916 wants of being a true Numerator is less than Tooooo part of an Integer, therefore the decimal fraction - 2916 is almost equal to 240, which 240 cannot be exactly reduced into a decimal fraction. The like will happen in the reduction of most vulgar fractions todecimals; in which case, the Denominator of the decimal must be affigned to be fo great, that what is wanting in the Numerator may be an inconfiderable value.

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IV. Upon the aforesaid ground; the known of accustomary parts of Money, Weight, Measure, Time, &c. may be reduced to decimals: for if you desire to know what decimal fraction of a pound sterling is equal in value to one shilling, consider first that a pound is the Integer, and that 20 shillings are equal to that Integer, therefore I shilling is \(\frac{1}{2} \) of a pound; now if we conceive one pound to be divided into 100000 parts, viz. if we assign 100000 for the Denominator of a decimal fraction, the Numerator will be sound by the last Rule to be 5000, so that \(\frac{1}{100000} \) or \(\frac{1}{2} \) of a decimal fraction of a decimal are of no use, as hath been shewn in the 6th Rule of the 22 Chapter is a decimal fraction of a pound, and is exactly

176 Reduction of Vulgar Fractions Book I.

actly equal to I s. or 20 part of a pound sterling. In like manner forasmuch as 240 pence are equal to a pound of English money, 7 pence are 240 parts of a pound, which fraction will be reduced into this decimal.02916 l.which is is very near equal to = 210 for it wants not Toogoo part of a pound. Moreover fince 960 farthings are equal to a pound English, one farthing is 760 part of a pound, which will be reduced into this decimal .00104 l. very near; but if you please to proceed near to the truth, you will find this decimal .00104166 &c. to answer a farthing, and so by augmenting the Denominator with Cyphers, you may proceed infinitely near, when you cannot attain unto the truth it felf. After the same method may the vulgar Sexagenary fractions used in Astronomy be reduced to decimals, for fince a degree is usually subdivided into fixty parts called minutes or primes; a prime or minute into fixty parts called feconds; a fecond into fixty thirds; a third into fixty fourths, &c. and consequently a degree is equal unto 60 minutes (or Primes) or unto 3600 seconds, or 216000 thirds or 12960000 fourths, &c. It is evident that 7 minutes (or Primes) are - parts of a degree, which by the third Rule of this Chapter may be reduced into the Decimal .1166, &c. Also 29 shirds are 216000 parts of a degree which may be reduced into the decimal .000134, &c. Moreover,

58:33:14:12, that is, 58 Primes, 33 seconds, 14 thirds, and 12 fourths may be reduced to a decimal in this manner, viz. reduce them all into fourths (according to the fixth Rule of the seventh Chapter) so will you find 12647652 fourths, which

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Chap. XXIII. to Decimal Fractions. 177

are 12642612 parts of a degree, which vulgar fraction
may be reduced into this decimal of a degree, to wit,
.975899,&c. (by the third Rule of this Chapter.)

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This to the ingenious will be a sufficient light for the sinding of the Decimals congruent to the shillings, pence, and farthings which are under a pound sterling; also the decimals of the known parts of Weight, Measure, Time, &c. as they are express in the following Table, wherein you may observe, that most of the decimals consist of 7 or 8 sigures, yet in ordinary practice, you shall have occasion to use only the first five, and sometimes sewer.

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0020833	184 142057	.0375
1. Tarin0010416	v abonable	.0354166
TABLET II.	16	0333333
Of Troy weight, the In-	77815	.03125
teger being an Ounce.	1787114	.0291666
Attended	10000120	.0270833
Peny Decimals of	141700112	.025
weights an Ounce	4111215821	.0229166
19.95	101115857	.0208333
18.90	16.133958	.01875
17.85	18.125	.0166666
16.8	11.0911-21	.0145833
15.75	19:102142	.0125
14227		=

200	- 22
5101041661	87280.111.0982142
0083333	10.0892857
3.00625	278150 9.0803571
22.0041666	8 .07 14285
Committee of the Commit	7.0625
TABLET III.	6.0535714
Of Averdupois great	077710. 5.0446428
HIT MUETONBUONS COM	000010. 4.0357142
Mobeld by Pur Tirre	3.0267857
an bundred weight, to	2 .0178571
wit, 112 pounds.	147810 11:0089285
auarters up accentions	decimals of
i bundred. I bundred.	Ounces. I bundred.
3 75	15 .0083705
21.5	"""
1,25	
CACCITICALS OF A	The American Control of the Control
Pounds bundred	THE RESIDENCE OF THE PARTY OF T
	Canna III
26 2321428	AND THE RESERVED OF THE PARTY O
25 2222142	water and the state of the stat
25 .2232142	CO. S. W. WILLIAM T. T.
24 2142857	
23 1061285	6.0033482
8 2 1964285	4.0022321
21 .1875	4.0022321
0801010 40 11/05/14	3.0016741
19.1696428	2.0011160
18,1607142	1,0005580
17:1517857	quarters of decimals of
8 28000 16 1428571	1 Ounce. I bundred
73.0 15.1339285	000418
8 14.125	3 .0004185
8 82410. 13 .1160714	2 0002790
121.1071428	11.0001395
2	TABLET

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mate of undered 04185 02790 01395

	of Manuellon. 201
TABLET IV	
Of Averdupois liti	118 5 01052125
weight, the Integer b	7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7
a pound.	THE RESIDENCE OF THE PROPERTY OF
10000	3.01171875
decimal	THE RESERVE OF THE PROPERTY OF THE PERSON OF
Ounces. a pou	-
15 .9375	quarters of decimals of
14.875	a dram. I pound.
13.8125	3 .0029296
12 .75	2 .0019531
11.6875	1 - 0000565
10.625	1 .0009765
9.5625	TABLETV.
8 5	Of liquid measures, the
8.5	Integer being a gallon.
7.4375	decimals of
6.375	Pints. I gallon.
5 -3125	THE RESERVE TO SERVE THE PARTY OF THE PARTY
4.25	7 .875
3.1875	CAN THE PROPERTY OF THE PROPERTY OF THE
2 .125	5 .625
1.0625	4 .5
decimals	3 .375
Drams. a pound.	of
	9 2502102 .25
	2 .25
15,.058593	75 quarters of decimals of
15.058593	75 quarters of decimals of a pint.
15.058593 14.054687 13.050781	75 quarters of decimals of a pint. agallon.
15.058593 14.054687 13.050781 12.046875	75 quarters of decimals of a pint. a gallon.
15.058593 14.054687 13.050781 12.046875	2 .25 1 .125 75 quarters of decimals of a pint. a gallon. 15 3 .09375 2 .0625
15.058593 14.054687 13.050781 12.046875 11.042968	2 .25 1 .125 75 quarters of decimals of a pint. agallon. 31.09375 2 .0625 1 .03125
15.058593 14.054687 13.050781 12.046875 11.042968 10.039062	2 .25 1 .125 75 quarters of decimals of a pint. agallon. 31.09375 2 .0625 1 .03125
15.058593 14.054687 13.050781 12.046875 11.042968 10.039062	2 .25 1 .125 75 quarters of decimals of a pint. agallon. 31.09375 2 .0625 1 .03125
15.058593 14.054687 13.050781 12.046875 11.042968 10.039062 9.035156 8.03125	2 .25 1 .125 75 quarters of decimals of a pint. a gallon. 31.09375 2 .0625 1 .03125
15.058593 14.054687 13.050781 12.046875 11.042968 10.039062	2 .25 1 .125 75 quarters of decimals of a pint. a gallon. 3 .09375 2 .0625 1 .03125

TABLET VI.	TABLET VII.
Of dry measures, the In-	Of long measures, one
teger being a Quarter.	Tard or one Ell being the
decimals of	Integer.
Bushels. \ a quarter.	quarters of dicimals of
71.875	I yard or 1 yard or 1
The state of the same of the s	ell. ell.
5 .625	3 .75
41:)	2 .5
3 .375	\decimals of
1 .125	Nails. I ya.or I ell
decimals of	The state of the s
Pecks a quarter.	2 .125
3 .09375	1 .0625
2 .0625	quarters of decimals of
1 .03125	I nail. [ya. or I ell]
quarters of decimals of	31.046875
a Peck. a quarter.	2 .03125
3 .0234375	1 .015625
2.015625	TABLET VIII.
11.0078125	Of the Reduction of in-
decimals of	ches,&c.to decimals,the
Pints. a quarter.	Integer being a foot in
3.005859	length.
2.003906	Inches. a foot.
1,100,755	11.9166666
19 11 55 6 5	10 .83333333
	9 .75
The state of the s	
The state of the s	8

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1	203
8,.6666666	parts of a decimals of
7.58333333	dozen. a gross.
2.648350, 6.5	11.076388
5 .4166666	10.069944
4.3333333	9.0625
3.25	8.055555
2.1666666	7.048611
1 .08333333	6.041666
quarters of decimals of	5.034722
an inch. a foot.	41.027777
3.0625	3 020833
2 .0416666	2.013888
1.0208333	1.006944
balf a quarter .0104166	TABLET X.
of an inch.	Of Time, a day being the
I A D L ET IX.	Integer.
Of dozens, the Integer be-	decimals of
ing a gross.	Hours. a day.
decimals of	23.9583333
dozens. a gross.	22 .9166666
11.9166666	21 .875
10.8333333	20.8333333
9.75	19 7916666
8.6666666	18.75
7.5833333	17.70833333
0.5	16.6666666
5,4166666	15.625
4-3333333	14.58333333
The state of the s	
3.25	13.5416666
2,1666666	12.5
2,1666666	12 .5
	12.5

-04	
91.375	38.0263888
8 3333333	37 .0256944
2916666	36.0249999
6.25	35 .0243055
	34.0236111
-116166	33.0229166
	32.0222222
3.125	31.0215277
2.0833333	30.0208333
1.0416666	29.0201388
decimals of	28.0194444
Minutes. a day.	27.01875
59.0409722	26.0180555
58 .0402777	20.0100555
57 .0395833	25 .0173611
56 0388888	24.0166666
55 .0381944	23.0159722
54.0375	22 .0152777
53.0368055	21 .0145833
	20/.0138888
52.0361111	19 .013 1944
51.0354166	18.0125
56.0347222	17.0118055
49.0340277	16 .0111111
491.0355555	15.0104166
47 .0326388	14.0097222
46 .0319444	13.0090277
45 .0312500	12 .0083333
44 .0305555	11 .0076388
43 .0298011	10.0069444
42 .0291000	9.00625
41 .0284722	8.0034722
40.0277777	7 .0048611
39 .0270833	6.0041666
11 10 10 10 10	5 .0034722

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	THE RESERVE	BEED DONAL
	.4	.0027777
Huera	3	:0020833
che in	2	.0013888
in ben	11.	0006944

V. This Table aforegoing consists of ten several

des lot a sound

Tablets, of which the first intituled of the same English money) contains in the first Tublet 1. of column thereof the particular Fra- English money.

Ctions (viz. the Shillings, pence, and farthings) of a pound sterling; and in the other column the decimals, unto which they may be respe-Crively reduced: So in the same Tablet .65 is the decimal, answerable to 13 s. . 0208333 to 5 d. and .003125 to 3 f.Likewife, .0489583 is the decimal of 11 d. together with 3 farthings; Alfo .03 125 is the decimal of 7 pence half peny.

VI The next Tablet (intituled Try weight)con-

tains in the first column thereof the particular Fractions (viz. the Peny 2. Of Troy weights, and Grains) of an ounce Troy, weight.

and in the other their respective deci-

mals: so .6 is the correspondent decimal of 12 peny weight, and .0020833 of I grain. Likewise .025 is the decimal of 12 grains.

VII. The third Tablet (intituled Averdupois great weight) contains in the first co-3. Of Averlumn thereof the Fractions (viz. the dupois great Quarters, Pounds, Ounces, and the weight. Quarters of an Ounce) of an Hundred

according to Averdupois weight, and in the other their proper decimals: so .5 is the decimal of two quarters or half a hundred, 1517857 of 17 pounds: .0033482

206 Reduction of Vul. Fract. Book I. .0033482 of 6 Ounces, and .0004185 the decimal of 3 quarters of an Ounce. VIII. The fourth (intituled Averdupois little weight) theweth you the fractions(viz. the Ounces, drams, and quarters of a 4. Of Averdupois little dram) of a pound Averdupois, togeweight. ther with their respective decimals: fo the decimal of 3 Ounces is .1875, the decimal of 9 Drams is.03515625, and the decimal of one quarter of a Dram is .0009765. IX. the fifth (intituled Liquid measures) hath the fractions (viz. the Pints and quar-5.0f Liquid ters of a pint) of a Gallon, and likewise their several decimals: so the demal of 5 Pints is .625, and the decimal of two quarts or half a pint is .0625. X. The fixth (intituled Dry measures) gives you the fractions (viz. the Bushels , Pecks. 6. of Dry quarters of Pecks and pints) of a quarter, together with their peculiar decimeasures. mals: so .375 is the decimal of three Bushels, .03125, of one Peck, .0234375 of 3 of a peck, and .003906 of two pints. XI. The seventh (intituled Yards and Ells) offers you the fractions (viz. the Quarters, Nails, and quarters of Nails) of 7. Of Long Yards or Ells, and their respective demea fures. cimals: fo .25 is the decimal of one quarter of a Yard or Ell, .125 of two Nails, and .046875 of three quarters of a Nail. XII. The eighth (intituled Reduction of inches,

&c. to decimals of a foot) presents unto you the

fractions (to wit, the Inches, quarters and

half quarter of an Inch) of a foot, together

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of,

Chap. XXIII. to Decimal Fractions 207 with their correspondent decimals: so .4166666 is the decimal of 5 Inches, .0625 of \(\frac{1}{4} \) of an Inch, and .0104166 of \(\frac{1}{8} \) or half a quarter of an Inch.

XIII. The ninth Tablet (intituled Dozens)

yields you the Fractions (viz. the Dozens and particulars) of a Gross, as also their respective decimals: so

8. Of things accompted by the Dozen.

.25 is the decimal of 3 Dozen, and .048611 of 7 particulars.

XIV. The tenth and last Tablet (intituled Time)

gives you the Fractions (viz. the Hours

and Minutes) of a Day: so .625 is the 9 of Time. decimal of 15 hours, .0375 of 54 mi-

nutes, and .0006944 of one minute.

XV. When a fingle Fraction of any of the pre-

mised Tablets is propounded to be reduced to a decimal, find it in the first Column of the Tablet, unto which it belongs; this done, just against that Fraction so sound, you shall have the decimal required: so

The use of the same Table for the Reduction.

1. Of single fractions to decimals.

13 s. being propounded, taking the

first premised Tablet, I find 13 s. in the first Column of the Tablet of money, and just against the same thirteen shillings, I observe .65, before which having prefixed a point, and by that means signed it for a decimal (according to the third Rule of the 22 Chapter of this Book) I conclude the same .65 so ordered, to be the correspondent decimal of thirteen shillings the fraction propounded: In like manner .0229166 is the decimal of 11 grains in the Tablet of Troy weight; and .0357142 the decimal of 4 lb. in the Tablet of Averdupois great weight, &c.

XVI. When

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208 Reduction of Vul. Fract. Book I.

pounded, and it is required to find a decimal equivalent unto the sum of them, find the decimal of each of the Fractions given according to the last Rule; then adding together the decimals so sound, that intire sum is the decimal sought: so 13 s. 5 d. being reduced to a decimal, is .670833; for the decimal of 13 s. is .65, and the decimal of 5 d. .020833, which being added together (by the second Rule of the 24th Chapter of this Book) amount to .670833, viz. the decimal which represents 13 s. 5 d. the Fraction propounded: In like manner the decimal of 9 peny weight, and 13 Grains is .4770833, and the decimal of ½ C. 19 lb. 7 Ounces is .67354, &c.

13 5. 5 d.	.65
A spanor of	.670833
9 p. w. 13 gr.	.027083
non , sand juli	-477083
12 C. 19 lb. 7 ounc.	.16964
o lymbolichic	.67354

And here as you see meer Fractions reduced, so likewise may the Fractions of mixt numbers be reduced to decimals. for example, these numbers 97

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Chap. XXHI. to Decimal Fractions. 209

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1b. 7 ounces 13 \(\frac{1}{4}\) drams. Item of 67 Gallons, 5\(\frac{2}{4}\) pints. Item 28 Quarters, 0, Bushels and 2\(\frac{1}{2}\) Pecks, after reduction are 97 .4891, 67 .7187, and 28 .0781.

97.4375	67.625	28.0625
0507 500	liwalil.093713vi	g lemin.01561c
.000900	of the book less	A CONTRACTOR OF THE PARTY OF TH
0111	10 67 .7187 3230	28.0781

Again 22 ½ yards, 3 ½ Nails; Item 36 Gross, 3
Dozen and 5 particulars, being reduced, are 22
7031, 36.2847.

22.5 .1875 .0156 .0347 .22.7031 .36.2847

What Fraction it represents, fearch

the same decimal in the second Co- 3. of Decimals to single Fra-

longs, where if you find it expressly,
the number just against it in the first Column is the
fraction you look for: so .65 (representing the
fraction of a pound sterling) being given, I find
it in the second Column of the Tablet of Money,
and over against it in the first Column I find 13 s.
which is the fraction represented by .65, the decimal propounded. In like manner 3 .025 (representing 3 ounces and .025 of an ounce Troy) being propounded, the number represented by it, is
3 Ounces, o p.m. 12 grains.

XVIII. When in the second Column of the Tablet.

210 Reduct. of Vulg. Fractions Book I.

Tablet, unto which you are directed, you cannot precifely find the decimal propounded, search that which being less, comes nearest unto it, and take the number that answers unto it in the first Column for the greatest fraction of the number required: then deducting the decimal so found out of the decimal given, find likewise the remainder, as another decimal, and take his correspondent number for the next fraction of the number required: and so proceed in that order, till you have discovered the intire number represented by the

decimal propounded.

Example: .6739 being propounded, I demand the fraction of a pound sterling represented by it; the decimal in the Tablet of money, which being less comes nearest to .6739 is .65, whose correspondent number in that Tablet is 13, which are the shillings of the number required; then subtracting (by the 1 Rule of the 25 Chapter of this Book) .65 out of .6739, the remainder is .0239, and the nearest decimal in the same Tablet to .0239 is .0208, whose correspondent number is 5, which are the pence of the number required: last of all deducting .0208 out of .0239, the remainder is .0031, which gives you in the first Column 3, being the farthings of the number required: So that I conclude the intire fraction represented by the decimal. .6739, is 13 s. 5 d. 3 f.

day) & so. & romant	.6739 l. sterling.	
Subtract 13 s	65	
the representation of the	.0239	
Subtratt 5 d.	0208	
3 f.	003 ¥	

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Chap. XXIV. Addit. of Decim. Fract. 211

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In like manner 7.359 C. being reduced by the Tablet of Averdupsis great weight is 7\frac{1}{4} C. 12 lb. 4 ounc. And 94.58 lb. reduced by the Tablet of Averdupsis little weight is 94 lb. 9 ounces and 6 drams.

01. 9	7.359 C.
Subtract I quarter-	-25
'MUL 2017	.109
Subtract 12 lb.	107
4 0%.	002
character and the second	94.58 lb.
Subtract 9 02.	56
6 Drams.	.02 10 2

CHAP. XXIV.

Addition of Decimal Fractions.

I. To such as well understand the Notation of Decimal fractions, all the varieties of their Nume ration, to wit, Addition, Subtraction, &c. will be as easie as the operations by whole numbers; therefore he that would be a good Prosicient in Decimal Arithmetick, must throughly understand the 22 and 23 Chapters asoregoing.

II. When divers decimal fractions are given to be added together, they must first of all be orderly placed one under another according to the doctrine of their Notation. So if these Decimal fractions, to wit, .125, .39 and .7 were given to be added, they must be written down thus;

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or if you will have the same number of places to be in all the decimals given, without altering their values, they may be written thus, 82. 10 bit A Danso

> dispose tittle menghi .390 .700 Trang I tranten Not thus, .125 di cr

For the Figures or Cyphers, which are of like degrees or places must be subscribed directly one under another, viz. tenth parts or primes must be written down directly underneath tenths; also bundredth parts or seconds must be placed under bundredth parts, as you see in the first Example, where .3 or three tenth parts in the second decimal stands directly under . I or one tenth part in the first decimal; likewise .7 or seven tenths in the third decimal stands directly under the tenths in the former, and fo of the rest.

In like manner, when mixt numbers, which confift of Integers and decimal parts are given to be added, due respect must be had of their subscription one under another: so if these mixt numbers, to wit, 32 .056, 7 .07, and 1 .9 were given to be added, they must be written down thus,

d of mayin staw r. bns .32 .056 ma awob man 7 .07 dum vall

III. Having placed the decimals and drawn a line underneath in manner aforesaid, add them together, ok L

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12WD | em to gether gether, beginning with the outermost rank towards the right hand (as hath been taught in Addition of whole numbers of one denomination in the third Chapter:) fo if the decimals in the first Example of the second Rule of this Chapter were given to be added, I first subscribe 5, which is all that stands in the first rank towards the right hand, then pro-

ceeding to the fecond rank, I fay 9 and .125 2 make II, wherefore I write down I. .39 which is the excess of II above 10, and for the 10 I carry 1 in mind to the 1.215 next rank, faying I in mind added to

7 makes 8, which added to 3 and 1 make 12, wherefore I write 2 which is the excess of 12 above 10 under the line, referving I in mind for the 10, then I prefix a point before 2, which stands in the first place of decimals; and on the left hand of the point, to wit in the place of Units or first place of Integers, I write down I (being the I in mind) which done, I find that the furn of the Decimals given is 1.215, that is, one Integer (whether it be a Perch. Yard, Foot, &c.) and -215 parts of an Integer, as you fee in the Example. In like manner these mixt num-

bers 32.056; 7.07 and 1.9 being given to be added, their fum will be found to be 32.056 41.026, that is, 41 Integers and -26 parts 7.07 of an Integer, as you fee in the Margent; 1.9 more Examples for the learners exercise 41,026 are thefe.

.65	24.7	503.75
.025	0.35	0.32
.03	5.26	0.12
.705	30.31	504.19
	many of A Shin Sin	CHAP.

214 Subtract. of Decimal Fract. Book I.

CHAP. XXV.

Subtraction of Decimal Fractions.

Aving first written down the greater of the I two numbers given (whether it be a whole number, mixt number, or decimal) and the lesser underneath the greater, according .784 to the directions in the second Rule of the 24th Chapter, Proceed as you are taught in Subtraction of whole numbers (by the Rules of the 4th Chapter:) fo if this decimal fraction . 784 were given to be subtracted from this decimal .837, the remainder will be .053, that is 1000 parts of an Inte-295.094 ger; in like manner if this mixt number 78.919 were given to be subtracted 78.919 from 295.094, the remainder will be 216.175 216 175 in each of whichexamplesyou may observe that 10 is borrowed as often as need requires, according to the Rules of Subtraction of whole numbers of one denomination: Note also, when the decimals in both the numbers given confift not of the same number of places, that decimal which is defective in places towards the right hand. must have the void places filled up with cyphers, or at least cyphers must be supposed to be annexed : so if this decimal .04338 be given to be subtracted from this .65, the remainder will be .65000 found to be .60662, and the Work will .04338

found to be .60662, and the Work will frand as in the Margent, where you fee the three void places are supplied with cyphers, and then the operation is as in whole numbers, by borrowing to as often as the lower fig.

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Chap. XXVI. Multip. of Dec. Fract. 215 gure cannot be subtracted from the upper. More Examples of Subtraction of Decimals are these following.

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24.04338	37.	-394
.65	0.104	-35
23.39338	36.896	.044

CHAP. XXVI.

Multiplication of Decimal Fractions.

7 Hen two numbers are given to be multiplied, and are both mixt numbers, or both decimal fractions, or one of them a whole number, and the other a decimal or mixt number (which are all the cases that can happen) there is no necessity of writing them down precisely one under the other as in Addition and Subtraction, for the product or number sought in Multiplication depends not upon any regular placing of the two numbers given: so if this mixt number 56.3 were given to be added to this mixt number 1.30526 1. 30526, they ought to be written one under the other, as you see (according to the second Rule of the 24th Chapter;) but if they are to be multiplied one by the other, they may be written thus,

1.30526

II. In any of the Cases which may happen in Multiplication of Decimals, multiply the numbers given as if they were whole numbers, then cut off always from the product by a point, comma, or line

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line, so many places towards the right hand, as there are places of decimal parts in both the numbers given to be multiplied; that done, the figure or figures (if any happen to be) on the left hand of the faid point or line of separation doth declare the Integer or Integers in the the product, and those on the right hand of the point are decimal parts of an Integer: fo if this mixt number 56 .3 (that is, 56 Integers and 70 of an Integer) be given to be multiplied by this mixt number 1 .30526, the product will be found 73 .486138, that is, 73 Integers and 7486138 parts of an Integer; for having chosen that to be the Multiplicator, which will cause least work, and subscribed it under the Multiplicand (to wit, 56 .3 underneath 1.30526) I proceed according to the Rules of Multiplication of whole numbers, viz. having drawn a line underneath the numbers given, I multiply all the Multiplicand, to wit, 1.30526, as if it were a whole number, by 3 the first multiplying figure, and sub-

1.30526 scribe the product thereof, which is 56.3 391578 underneath the line, and 391578 proceeding in like manner with the 783156 other multiplying figures 6 and 5, at last I find the total of the particular 73|486138 cause there be 73486138; and beparts in both the numbers given (to wit, 5 places of parts in the multiplicand, and I place in the multiplicator) I cut off 6 places to the right hand from the total before produced, so will it stand thus 73|486138: wherefore I conclude that the true product is 73 7000000 or 73.486138, that is, 73 Integers and almost 1 of an Integer In

Chap. XXVI. Decimal Fractions. 217

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In like manner, if this mixt number 246.25 (that is 246 125) were given to be multiplied by 35 Integers, the true product will be found 8618.75, that is 8618 Integers and 125 parts of an Integer, as you see by the operation in the Margent, where you may observe that 246.25 two places are cut off from the total number produced of the multiplication, towards the right hand, because 123 125 there are two places of decimals in the 73875 multiplicand (the multiplicator consisting of Integers only;) but if there 8618175 had been decimal parts also in the multiplicator, so many more places should have been cut off, as was shewed in the first Example.

Again, if these two decimals. 87 and .9 (to with 100 and 100) were given to be multiplied one by the other, the true product will be found to be: 783 that is 100 parts of an Integer, as you see in the Example, where you may observe that the product is a fraction only; for after 3 places (being the number of places of decimals in both the numbers given to be multiplied) are cut off to the right hand, there remains no Integer on the lest hand.

III. When the Muitiplication is finisht, if there arise not so many places in all as ought to be cut off by the second Rule of this Chapter (which may often happen when the product is a fraction;) in such case, as many places as are wanting, so many cyphers must be prefixed to the product on the less hand thereof, and then a point must be prefixed

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which declareth how many known parts are equal to the Integer, the Product gives the number of known parts-required: So this decimal fraction of a pound sterling, to wit, .8687 1. being propounded, I multiply it first by 20 (the number of shillings contained in a pound) and the product gives 17 shillings and .3740 parts of a Chillings;

the Integer.

Chap. XXVI. Decimal Fractions. 219 shilling; which decimal 3740 being multiplied

by 12 (the number of pence in a shilling) produceth 4

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pence, and .488 parts of a peny; lastly, multiplying .488 by 4 (the number of farthings, which make a peny) the product gives a farthing and .952 parts of a farthing, which are very near in value to another farthing, so it appears that .8687 parts of a pound sterling are 17 s. 4 d. 2 f. very near. After the same manner, a decimal fraction of any

Shill. 17|3740 12 7480 3740 Pence 4|4880 4 Farth. 19520

Integer whatfoever may be reduced into the known

or accustomed parts of fuch Integer.

A briefer way to value any decimal part of a

pound of English money, without loss of a farthing may be this, viz. the figure (if any happen) in the first place of the decimal being doubled gives shillings; also if there be 5, or a figure greater than

Abrief way to find the value of any decimal fraction of a pound of English moneys.

(when

5 in the second place, one shilling more is to be added to the sormer; lastly, when 5 is taken from the sigure in the second place, if every unit in the remainder be accounted as ten, and the sigure in the third place as unities, these tens and units taken as one number and lessened by 1 give the number of farthings, which with the shillings before sound declare the value of the decimal propounded; likewise if the sigure in the second place

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(when any happens) be less than 5, every unit in fuch figure is to be acounted ten as before: so in the decimal before mentioned, to wit, . 8687 1. the figure 8 in the first place being doubled gives 16 shillings, also because 5 is contained in 6 which stands in the second place, one shilling more is to be added to the aforefaid 16 shillings, which will now be made 17 s. that done, the remainder of the faid 6 after 5 is subtracted, to wit, I being esteemed as 10, and added to 8 (which stands in the third place, and to be effeemed as units) gives 18, from which abating 1, the remainder is 17 farthings or 4 pence and a farthing; fo that the value of the faid decimal .8687 1. is found as before to be 17 thillings 4 pence I farthing. After the fame manner this decimal of a pound of English money, to wit, .319 1. will be reduced to 6 shillings and 18 farthings or 6 shillings 4 pence 2 farthings, which wants less than a farthing of the exact value of the decimal .319 l.

V. Having explained all the cases in Multiplica-

tion of Decimals; I shall here give the learner a taste of their excellent See the queffiuse, by some familiar questions, ons from 49 to 73 in the 10th whereby it will be evident, that Chapter of the what is often times performed by Appendix. many tedious Multiplications and

Divisions in the vulgar way, is effected for the most part by one or two Multiplications in Decimals.

The first Example may be this: suppose there is a certain piece of Wainscot in form a rectangled parallelogram commonly called a long square, whose breadth is 3 yards, 3 of a yard, I nail and 4 of a nail; and the length 6 yards, and 1 of a yard, the question is to know

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know how many square yards are contained in that piece of Wainscot; here because it is desired that the superscial content may be given inyards, the parts of a yard as well in the breadth as in the length of the Wainscot, which are before express by the accustomed parts of quarters, nails, &c. must be reduced into decimal parts of a yird, which are as easie to be found by a yard subdivided decimally, as the common parts of quarters and nails are found by a yard vulgarly subdivided: but for want of a yard subdivided decimally, this Reduction may be performed by the seventh Tablet of the precedent Table of Reduction, viz. looking into the said Tablet, right against 4 of a yard, I find 2 this decimal

Also the decimal correspondent to 2,0625

And the decimal of 4 of a nail?.015625

The fum of those three decimals 3.828125

Wherefore the breadth of the Wainscot in yards and decimal parts 3.828125

Again, the decimal of half a yard is .5, wherefore the length of the 6.5

Wherefore I conclude that 24 square yards and somewhat more are contained in that piece of Wainscot,

Wainfoot; and it is evident by the first place of the decimal, that what is above 24 yards is more than 5, but less than 70 of a square yard; or more strictly, it is more than -8.8, but less than -8.2 of a square yard: but by taking all the places in the decimal you have the exact answer to this question, because the common parts of quarters, nails, and quarters of mails may be always exactly reduced into decimals, but that feldom happens in other things; nevertheless, albeit by decimal operations you cannot always hit the mark, yet you may come as near it as is possibly to be imagined, and that with much more eafe than by vulgar computations in queilions of this nature, as will appear by com-

y. q. 3-3 4	n. q. n.
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6,1	Soit to 6

245 quarters of nails.

paring the precedent operation with the common way of working here in your view, viz. the 3 yards, 3 quarters of a yard, I nail, and 1 of a nail (which express the breadth before mentioned) must all be reduced into quarters of nails by the fixth Rule of the feventh Chapter; fo there will be found 245

quarters of Nails, as you see by the operation,

Again the 6 yards and half which express the length aforesaid, must likewise be reduced into quarters of Nails by the aforefaid Rule; fo there will be found 416 quarters of nails of a yard, as you fee by the operation.

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416 quarters of nails.

Then multiplying the breadth and length one by the other, to wit, 245 by 416, the product will give 101920 for the superficial content of the piece of Wainscot in square quarters of nails of a yard; now these square quarters of nails of a yard must be reduced to square yards, and the readiest way to perform that, is to find first of all how many quarters of nails of a yard are contained in one yard in length, viz. fince there are 16 nails in a yard, there are consequently 4 times 16 quarters of nails, to wit, 64 quarters of nails in a yard in length; therefore 64 multiplied by 64 produceth 4096 square quarters of nails in a yard square; lastly, I say by the Rule of three, if 4096 square quarters of nails of a yard give 1 yard square, how many yards square will 101920 square quarters of nails give? So will the answer be found 24 3616 yards, which is the same with 24.8828125 before found by the decimal operation (for \(\frac{3616}{4096} \) is equal to the decimal .8828125, as will appear by reducing them to a common denominator by the fourteenth .04

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teenth Rule of the seventeenth Chapter.) Now I leave it to the Reader to judge, which of these two wayes is the more expeditious, and so let him take which liketh him best.

Example 2. There is a squared piece of Timber terminated at both ends with equal long squares, viz. the breadth of the piece of Timber is I foot 5 inches 3 quarters of an inch, and a half quarter of an inch; the depth or thickness is I foot 3 inches I quarter of an inch, and i or half a quarter of an inch, and the length of the piece is II feet 10 inches, and 3 quarters; the question is how many folid or cubical feet are contained in that piece of Timber? The Answer may be found by decimal Multiplication in manner following, viz. Foralmuch as it is defired that the folid content may be given in feet, the parts of a foot as well in the breadth, depth, and length, which are before exprest by the accustomed parts of inches, quarters, and half quarters must be reduced into the decimal parts of a foot, which are as ealie to be found by a foot subdivided decimally, as the other common parts by a foot vulgarly fubdivided; but for want of a foot subdivided decimally, this Reduction may be performed by the eighth Tables of the precedent Table of Reduction. 212.

The decimal correspondent to 5 in-	-416
	ARCHITECTURE DE L'ANNE DE
The decimal of a of an inch is The decimal of half a quarter of an inch is	
The sum of those 3 decimals is Wherefore the breadth of the piece	200
of Timber is	In.405

Chap. XXVI. Decimal Fractions. 225

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In like manner the common parts of inches, &c. in the depth or thickness of the piece of Timber will be reduced by the said Tablet, into these decimals, viz.

The decimal correspondent to 3 inches i	5-25
The decimal of a of an inch is	02
The decimal of half a quarter of an inch	is01
The sum of these 3 decimals is -	- 28
Wherefore the depth or thickness is	-1.28
Again, the accustomed parts of inches, &	e in the
ength of the piece of Timber will be rea	duced to
hese decimals, viz.	THE PARTY OF THE P

Now if the breadth depth and length be multiplied continually, the last product is the solid content required, viz. 1.488 multiplied by 1.28 produceth 1.90464, which multiplied by 11.895 produceth 22.65, &c. wherefore I conclude that 22 solid Feet, half a soot, and somewhat more than half a quarter of a soot are contained in that piece of Timber:

Example 3. How many Equinodial degrees are correspondent unto 136 dayes, 21 hours, and 40 minutes? The Answer is found by multiplying the time given by 360, for as 1 day is to 360 degrees, so 136 dayes, 21 hours, and 40 minutes, to the Equinodial degrees required; but first the 21 hours and 40 minutes must be reduced to decimal parts of a day, by the tenth Tablet, thus.

The

The decimal of 2 1 hours is-The decimal of 40 minutes is ----The fum of thef: 2 decimals is-

Therefore the time propounded is -136.90277

Which being multiplied by 3602 49284.99 &c. produceth-

Wherefore I conclude, that 49284.99 or very near 49285 Equinoctial degrees are correspondent unto 136 dayes, 21 bours, and 40 minutes, which was required by the question.

CHAP. XXVII.

Division by Decimal Fractions.

I. I N any of the Cases which may happen in Di-· I vision, if the Dividend be greater than the Divisor, the quotient will be either a whole number or else a mixt number. but when the Dividend is less than the Divisor, the quotient must necessarily be a fraction; for a lesser number is contained in a greater once at the least, but a greater is not contained once in a leffer.

II. Sometimes the Dividend, whether it be a whole number, mixt number, or decimal fraction, is to be prepared by annexing a competent number of cyphers thereunto, to make room for the Divifor: To if 32 .5 were given to be divided by 17 .325 the Dividend 32 .5 must be increased with cyphers at pleasure after this manner 32 . 50000, &c. Likewife if I were given to be divided by 360, the Di-

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chap. XXVII. Decimal Fractions. 227 vision cannot be made till the Dividend I be increased with cyphers, which being annexed, the Dividend will stand thus I.000000,&c. Here note, that the cyphers annexed in manner aforesaid do supply places of decimal parts, and will be usefull in discovering the quality of the quotient according to the sourth Rule of this Chapter.

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III. After the Dividend is prepared by annexirg cyphers, when occasion requires (as in the last Rule,) all the places thereof must be esteemed as one whole number (to wit confisting of unities or Integers:) and so is the Divisor to be esteemed whether it be a decimal fraction or mixt number; for in all cases the Division must be performed in every respect according to the Rules of Division of whole numbers in the fixth Chapter. So if this mixt number 326.25 were given to be divided by this mixt number 12.3, you must divide in the same manner, as when you divide 32625 Integers by 123 Integers. Also if this decimal .8356 were given to be divided by this decimal .05, you are to divide in the same manner, as when you divide 8356 Integers by 5 Integers; and after the quotient is found, the degree or place of the first figure which ariseth in the quotient must be inquired after; viz. you must know how far such first figure is diflant from the place of units, to the end that the point or line which is used to separate between the place of unities (or first place of Integers) and the first place of decimals may be duly placed: This is the only knot in decimal Division, and may be resolved by the following Rule, viz. the place of Units to the Divitor will be placed

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IF. In any of the Cases which may happen in Di-

Ageneral Rule to discover the quality of the quotient in all cases of Divifion by decimal Fractions.

vision of decimals, the first figure which ariseth in the Quotient, will be always of the same place or degree with that figure or cypher of the Dividend, which at the first question standeth over, or at least belongeth unto the place of units in

the Divifor. To illustrate this Rule I shall give Examples in all the principal cases; and firstflet a mixt number be given to be divided by a mixt number, viz. Let it be required to divide 172 .5 by 3 .746: here (according to the second Rule of this Chapter) the Dividend must be increased with cyphers at pleasure, so will it stand thus 172 .500000, &c. then Division being made according to the Rules of Division of whole numbers in Chapter 6, the Quotient arising will be 46049, &c.

3.746) 172.500000 (46049, &c.

Now it remaineth to separate the Integers in this quotient from the decimal parts; to perform which, I subscribe the Divisor 3 .746 orderly underneath tound, the segme or place or the first figure

3.746) 172 .500000 (46,049, &c." you mall a now how ear such interests

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the first Dividual 172 .50 (being that part of the Dividend whereof the first question must be asked) or at least I imagin the Divisor to be so subscribed, and fo I find that the figure 3 which frands in the place of Units in the Divisor will be placed under ook L

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under 7, which is the place of tens (or fecond place of Integers) in the Dividend; wherefore by the fourth Rule before given, I conclude that the first figure arifing in the quotient must likewise stand in the place of tens (or fecond place of Integers) and confequently the next place on the right hand must be the place of Units; so it is evident that the separating point or line must be placed between the figure 6 and 0 in the quotient, that done, the true quotient is found to be 46 .049, &c. to wit, 46 Integers and 1000 parts of an Integer, and fornewhat more: for 46 7000 is less than the true quotient, but 46 1000 is greater than it; and therefore albeit, after the aforesaid Division of 172, 500000 by 3.746 is ended, there will be a remainder, to wit 446 which feems to be greater, yet here it is less in value than Tooopart of an Unit or Integer, and if to that remainder you annex another cypher and continue the Division, you will proceed nearer the truth and not miss Tooos part of an unit of the true quotient, and in that order you may proceed infinitely near, when you cannot obtain the quotient exactly by Division of Decimals.

Example 2. Suppose this mixt number 2 .34 be given to be divided by this mixt number 52 .125 (where you may observe that the Dividend is less than the Divisor;) first (as before) annex cyphers at pleasure to the Dividend, to make room for the Divisor, then the division being prosecuted as in whole numbers, at length these figures will arise in

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the quotient, to wit, 448: and to the end the degree or quality of the first figure 4 may be discovered, I subscribe the Divisor 52 .125 under the first dividual 2.34000 (for so far the first question did extend in the Division)and thereby I find that the figure 2 which stands in the place of units in the divisor will be seated under 4, which is in the fecond place of decimals; wherefore I conclude that the first figure arising in the quotient must also stand in the second place of decimals, and consequently the first place of decimals (which is next on the left hand to the second) must be supplied with a cypher; fo that if a cypher be prefixed on the left hand of 4, and then a point placed before that cypher, the quotient will at length be discovered to be. 0448,&c.or -448 and somewhat more that is to fay, 10000 is less than the true quotient, but 10000 is greater than it; and if you will proceed nearer the truth, you may continue the division, as is directed in the first Example of this Rule.

Example 3. Where a whole number is divided by a decimal fraction, viz. suppose 82 Integers were given to be divided by this decimal .056; After cyphers are annexed to the dividend at pleasure, and

true quotient, and in that order von men pre

.e56) 82.00000 (146428, &c.

Chap. XXVII. Decimal Fractions. 231

the division prosecuted as in whole numbers (to wit, 8200000 being divided by 56) these figures 146428 will arise in the quotient: now to the end the degree or seat of 1, the first figure in the quotient may be known, I subscribe the Divisor. 056 under the first dividual 82 (for so sar did the first question in the division extend;) and because the divisor is less than unity, I supply the place of units by a cypher or o prefixed on the lest hand of the point of separation in the divisor; also I pre-

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fix cyphers before (to wit on the left hand of) the Integers in the dividend to represent a succession of places of Integers (for the order of places in Integers is from the right hand towards the left;) then I find that the cypher or o which represents the place of units in the divisor, doth stand under that cypher, which represents the fourth place of Integers in the dividend (as you fee by the Example ;) wherefore I conclude that the first figure arifing in the quotient must also be seated in the fourth place of Integers, and consequently the 4 first places in the quotient will be Integers, and the rest a decimal, so that the true quotient is 1464 Integers, and 700 parts of an Integer, and fomewhat more, viz. 1464.28 is less than the true quotient, but 1464.29 is greater thanit.

Example 4. Suppose this decimal .0125 be given

to be divided by this decimal .5;

after division is finished accor- .5) .0125 (25

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Chap. XXVII. Decimal Fractions. plieth the place of units in the divisor, doth stand under the cypher which is seated in the third place of Integers in the dividend; wherefore I conclude by the Rule, that the first figure arising in the quotient must be also in the third place of Integers, and consequently the three first places in the quotient will be Integers, and the rest a decimal, so that the true quotient is 107 .05 or 107 Too.

Example 6. Let it be required to divide this decimal fraction .73952 by this .32; first dividing 73952 by 32 as it they were whole numbers, the figures arising in the quotient will be 2311. Now to discover the quality or value of the said figures I subscribe the Divisor .32 under the first dividual

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as aforesaid, to represent the place of units in each of them, I find the cypher or o, which supplieth the place of units in the divisor, to stand under the o which represents the place of units in the dividend; wherefore I conclude by the preceding fourth Rule, that the first figure arising in the quotient will stand in the place of units, and confequently the following places of the quotient will be a decimal fraction, so that the true quotient is 2:311 or 27111

The reason of the foregoing fourth Rule will appear from the following Considerations.

Chap

I If the Product of the Multiplication of two numbers be divided by one of them, the quotient is the same with the other number: As, if 269.0625, the productof 14.35 multiplyed by 18.75, be divided by 14.35, the quotient will give 18.75.

II. If the Divisor be multiplied by the first figure in the quotient, the Product is the first number to be subtracted from the Dividend (being the same with the last particular product in the multiplication of the two numbers that produced the Dividend:) and every particular place of that product is of the same degree with that figure or cypher of the Dividend, which stands over such particular place when the subtraction is made; For a figure of one degree (or place) cannot be subtracted from a figure of a different degree: As in the last mentioned Example, the work whereof is here in view; the divisor 14.35 being taken as in a whole number and multiplied by I, the first figure in the quotient produceth 1435, which must be conceived to confilt of the same degrees as are in 269.0 in the Dividend, from which the said product is to be subtracted, and therefore the said product 1435 is really but 143.5, as you may fee by the last particular product, in the multiplication of the mixt number 14.35 by 18.75.

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14.35) 269.0	625 (18.75
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III. And therefore to discover the degree of the first figure in the quotient, is nothing else but to find out the degree of that figure, which multiplying the figure or cypher in any particular place of the Divisor, will produce the same degree as that figure or cypher in the Dividend is of, which stands over, or at least belongs unto such particular place of the Divisor, at the first question; because the degree produced must be subtracted from the like degree above it.

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IV. Now among many Rules that might be given to discover the degree of the first figure in the quotient, and consequently the degrees of all the rest, the preceding fourth Rule of this Chapter is sufficient, namely, The first figure which ariseth in the quotient, is always of the same place or degree with that figure or cypher in the Dividend, which at the first question stands over, or at least belongs unto the place of units in the Divisor: The reason is, because if a figure standing in the units place of the Divisor be multiplied by (or doth multiply) a figure of the same degree with that degree in the Dividend, which at the first question belongs to the faid units place of the Divisor, the first place in the product shall be of that degree also, whether it be of Integers or decimal parts; and consequently the rest of the places in the said product shall be of the same degrees with their correspondent degrees (or places in the Dividend, as they ought to be, to the end that due Subtraction may be made (according to observ. 2.)

So in the Example before given, the first figure 1 in the quotient, shall be of the degree or place of Tens, because if the figure 4 standing in the units place of the Divisor 14.35 be multiplied by Ten, to wit, the degree which the figure 6 in the Dividend is of that belongs to the said 4 at the first question, it will produce four Tens, to be subtracted from the said six Tens: In like manner if a figure in the place of units be multiplied by units, the first place in the product shall be units; if by tenth parts of an unit, or Integer, the first place in

the product shall be Tenths, &c.

Having explained all necessary Rules in Division concerning

Chap. XXVII. Decimal Fractions. 23

conceening decimal fractions, I shall give a tast of their excellentuse, by the two following questions.

and then conclude this Chapter.

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into min Quest. 1. A Merchant bought of gold Plate 356 ounces, 13 peny weight, and 15 grains for 1160 pounds sterling, the question is what he paid for an ounce? Answer 31.—5s.—½ divery near. The operation by decimals may be after this manner, viz.

By the second Tablet of Reduction 3.65 the decimal of 13 peny weight is ______ 3.65

The decimal of 15 grains is - 03125

The sum of those 2 decimals is -. . 68125

Wherefore the quantity of Plate)
in ounces and decimal parts of an ounce 356.68125

Then by the Rule of three I say, if 356.68125 ounces cost 1160 pounds, what 1 ounce? Here 'tis evident that if I divide 1160 by 356.68125, the quotient will give the value of an ounce, to wit, 3 252 pounds, or 3 pounds, 5 shillings and ½ d. very near.

356.68125) 1160.0000000 (3.252,&c.

Quest. 2. Suppose the length of the Tropical year (or the space of time wherein the Sun running through the whole Ecliptick circle, consisting of 360 degrees, is returned to the same Equinoctial or Solstitial point from whence he departed) to confist of 365 dayes, 5 hours, and 49 minutes, the question is to know the Suns mean or equal motion for 1 day, to wit, what part of 360 degrees the Sun moveth in a whole day? The operation by decimals, thus,

P 3

By the tenth Tablet of Reduction? the decimal correspondent to 5 bours > . 2083333

The decimal of 49 minutes is -0340277 The sum of those decimals is _____.24236.0

Wherefore the time given, in days 3365.2423610 and decimal parts of a day is -

Then by the rule of three, if 365.242361 dayes give 360 degrees (or a total circumference;) what will 1 day give? Here if I divide 360 by 365 .242361, the quotient will give the diurnal motion required, which will be found very near .98564, &c.or -28564 parts of a degree, which decimal being reduced into the common Sexagenary parts (by the

fourth Rule of the 26 Chapter) will give 59-8, &c. and fuch is the Suns diurnal motion very near, according to the aforesaid supposition of the length of the Tropical year.

I shall here add the vulgar Sexagenary resolution of this question, that by comparing both wayes together, the excellency of decimal Arithmetick in calculations of this nature may be the more perspicuous.

The aforefaid question being stated according to the Rule of three will stand thus,

dayes bours degrees If 365 : 5: 49-360-

The first term in the Rule must be reduced into minutes (by the fixth Rule of the seventh Chapter;) so there will be found 525949 minutes:

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Likewise the third term 1 day must be reduced into minutes, which will be found to be 1440, as you see by the following operation.

1 Day or 24 hours.
60
1440 minutes

Then multiplying the third term by the second, to wit 1440 by 360, the product is 518400, which being divided by the first term 525949 (according to the note in the ninth Rule of the 16th Chapter) the quotient will give $\frac{518400}{525949}$ parts of a degree, which sraction being reduced into the accustomed Sexagenary parts (by the ninth Rule of the seven-

teenth Chapter) will give as before 59:8, &c. for the Suns mean diurnal motion; now which of these two wayes is the more expeditious I leave to him who is verst in both to determine.

P 4

CHAP.

CHAP. XXVIII.

The Rule of three direct in Fractions.

declared in reference to the definition of this Rule, as also to the due placing of the 3 given numbers, would be superfluous; and if respect be had to the Rules of Multiplication and Division in fractions. delivered in the 20, 21, 26 and 27 Chapters, the working of he Rule of three direct in fractions as well vulgar as decimal, is the same with that in whole numbers, viz. multiply the second number by the third (or the third by the second,) and divide the product by the first number, so the quotient is the sourth number sought; to wit, the answer of the question.

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Otherwise thus in Vulgar Fractions.

Multiply the Denominator of the first number by the Numerator of the second, also multiply that product by the Numerator of the third number, and reserve this last product for a new Numerator; again multiply the Numerator of the first number by the denominator of the second, also multiply this product by the Denominator of the third number, so shall this last product be a new Denominator; lastly, the new fraction (whose Numerator and Denominator is sound as aforefaid, is the sourth number sought, which, if it be a proper

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it be a proper proper fraction; may (if occasion require) be reduced into the known parts of the Integer (by the ninth Rule of the seventeenth Chapter;) if an improper fraction, it is to be reduced into its equivalent whole number or mixt number, by the thirteenth Rule of the seventeenth Chapter.

Example, If 4 of a yard of Velvet be fold for 2 of a pound sterling, what shall is of a yard cost? Anfwer 40 1.or 14 s. 92 d. For according to the Rule I multiply the Denominator 4 by the Numerator 2,

and the product is 8, this 8 I a-

gain multiply by the Nu- y. 1. y. 1. merator 5, and the product 3 4 3 6 (40)

gives 40 for a new Nume-

rator: moreover I multiply the Numerator 3 by the Denominator 3, and the product which is 9 I again multiply by the Denominator 6, so the last product is 54 for a new Denominator; wherefore I conclude that 40 is the fourth number fought, wich if it be reduced (according to the ninth Rule of the seventeenth Chapter) gives 14 s. 912 d. (or

9 d.) for the Answer of the question.

II. When any of the three given numbers is a whole number or mixt number, such number must first of all be reduced into an improper fraction by the tenth or eleventh Rule of the seventeenth Chapter) to the end that all the three given numbers may be 3 fractions: moreover if after fuch Redu-Ction, the first and third numbers be not fractions of Integers of the same particular denomination, fuch of the said numbers which is of the leffer denomination, must be reduced to a fraction of the greater (by the fixteenth Rule of the feventeeners Chapter;) which preparations being performed, the

rest of the Work is to be prosecuted according to the first Rule of this Chapter. An Example of this second Rule here followeth. If a quantity of Ambergreece weighing 1 \frac{5}{7} lb. Troy be sold for 60 l. sterling, what are 19 \frac{5}{8} grains worth at that rate? Answer = \frac{6.5.2 \div 0}{2.9.60} l. or 2 s. 4 \frac{1}{1.92} d.

But fince the third number $\frac{1}{3}\frac{7}{8}$ grains Troy is not a fraction of an Integer of the same name with the first (which is a fraction of a pound Troy,) it must be reduced into a fraction of a pound Troy, thus, $\frac{157}{8}$ gr. is $\frac{157}{8}$ of $\frac{1}{24}$ of $\frac{1}{20}$ of $\frac{1}{12}$ of a pound Troy, which compound traction will be reduced (by the 16 Rule of the 17 Chapter) into this single fraction, to wit, $\frac{1}{46080}$ lb. Troy and so the 3 numbers will at length stand thus in the Rule.

Then working as in the first Example of this Chapter, the Answer will be found $\frac{65940}{552960}$ l. which being reduced (according to the 9 and 4 Rules of the 17 Chapter) is found equal unto 2 s. $4\frac{119}{192}$ d.

Another Example. When the \(\frac{2}{3}\) of \(\frac{2}{4}\) of a Ship is valued at 147 \(l.\)—11 s.—3 \(d.\) how much is the whole Ship worth? Answ. 491 \(l.\)—17 s.—6 \(d.\)

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Note, when in any question whatsoever a compound fraction, to wit, a fraction of a fraction, is one of the given numbers, such compound fraction must first of all be reduced to a single fraction (by the 16 Rule of the 17 Chapter;) so here, the compound fraction \(^2_5\) of \(^3_4\) being reduced into a single fraction gives \(^6_0\) or \(^3_{-0}\); then say is \(^3_{-0}\) be worth 147 l.11 s. 3 d. what is 1 or the

ting the 147 l. 113. 3 d. into pence, and that number of pence, as also the third number 1. into improper fractions, the 3 numbers will stand in the Rule thus,

Ship pence Ship

Lastly, proceeding as in the first Rule of this Chapter, the fourth number will be found to be ^{3 141 23}d. which being reduced first by the 13 Rule of the 17 Chapter, and then by the 7 Rule of the 7 Chapter, the Answer at length is 491 l.—17 s.—6 d.

An Example of the Rule of three direct in Decimals may be this that follows. If 19 ounces, 3 peny weight, and 5 grains of Gold, be worth 621.—10s.—6 d. what is the value of 1 ½ ounce? Answ. 4 l.—17 s.—10 ¾ d. very near.

244 The Rule of Three Direct	Book I.
By the 2. Tablet in the Table of Re-	15 16 STOVE
duction in the 23 Chapter, the decimal	POLITICAL PROPERTY.
fraction correspondent to 3 peny	Salasto
weight is	10 Harring
Also, the decimal of 5 grains is-	
The sum of those 2 decimals is -	
Wherefore the first number in the Zo	z.
Rule of three is	19.160416
Again, by the first Tablet of the)	
aforementioned Table the decimal of	5
10 Millings is-	An and the said
Also the decimal of 6 pence is—.	
The sum of these two decimals is-	525
Wherefore the second number in 21.	To Britain
the rule of three is	2.525
Moreover by the said Tablet 2.the)	
decimal of \frac{1}{2} of an ounce or 10 peny	0%.
weight is.5, wherefore the third num-	1.)
ber in the Rule of three is)	initht the 2
So that after the faid reduction is f	hue
given numbers will stand in the Rule t	1103
examine the state of the state of	oun.
19.160416 — 62.525-	1.5
19.100410 02.727	THE REAL PROPERTY.

Lastly, multiplying the second number by the third, and dividing the product by the first number (according to the Rules of Multiplication and Division of Decimals delivered in the 26 and 27 Chapters) the fourth number will be this, to wit, 4.8948, &c. that is four pounds sterling and \(\frac{3.24.3}{100.00} \) parts of a pound, which decimal being reduced according to the fourth Rule of the 26 Chapter) gives 17 s.—10 d.—3 far.

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The proof of the Rule of three direct in Fractions is the same as in whole numbers, respect being had to the Rules of Multiplication in Fractions.

CHAP. XXIX.

The Inverse Rule of three in Fractions-

I. A Fter a question belonging to this Rule is duly stated (according to the seventh rule of the eighth Chapter) and prepared if need require, according to the fecond Rule of the 28 Chapter; The operation will be the same as in the Rule of three Inverse in whole numbers, respect being had to the Rules of Multiplication and Division in Fractions, viz multiply the first number by the second, and divide the product by the third; the quotient is the fourth number fought, to wit, the answer of the question.

Orthus, in Vulgar Fractions;

Multiply the Denominator of the third fraction by the Numerator of the second, also multiply that product by the Numerator of the first fraction, and referve the last product for a new Numerator: again multiply the numerator of the third fraction by the denominator of the second, also multiply this product by the denominator of the first fraction, so is the last product a new denominator; laftly, this new fraction is the fourth number fought, or answer of the question.

Example,

246 The Inverse Rule of Three Book I.

Example, if of cloth, which is 1\frac{1}{4} yard in breadth, 3\frac{1}{2} yards in length will make a Cloak, how much in length of stuff which is \frac{5}{8} yard in breadth will make a Cloak of the same bigness with the former? Answer 9\frac{4}{5} yards.

The 3 numbers being duly 3 brea. leng. brea. placed will stand thus - 1 \frac{1}{4} y. -3 \frac{1}{2} y. -\frac{5}{8} y.

Lastly, 8, 7 and 7 being multiplied continually give 392 for a numerator; also 5, 2 and 4 being multiplied continually give 40 for a denominator, whereby this improper fraction $\frac{392}{40}$ ariseth, which (by the thirteenth rule of the seventeenth Chapter) will be found to be $9\frac{32}{40}$, or (the fraction being reduced into its least terms) $9\frac{4}{5}$, which is the Answer of the question.

Ex.2. Suppose when Wheat is at 2 l.—001.—6d. the Quarter, the peny white loaf ought to weigh 8 ounces and $1-\frac{1}{2}$ peny weight of Troy weight; what ought it to weigh when Wheat is at 36 shillings the Quarter? Answer 9 ounces and $1-\frac{1}{2}$ pe.

ny weight.

The 3 given numbers being pence p.w. pence duly placed in the rule and reduced will fland thus,

And if the operation be profecuted according to the rule before given, the Answer will be found 181 = 3296 peny weight, or 9 ounces, 1 = 37 peny weight.

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CHAP. XXX.

The Double Rule of Three in Fractions.

I. THe Double Rule of Three is so called, because it is composed of two fingle Rules, and may either be resolved at one Work by the Rule compound of 5 numbers, or else by two distinct single Rules of three; which latter way, to fuch as understand the Rule of three in fractions is (as I conceive) less troublesome in the stating, and (in the method whereby I intend to profecute it) the same in operation with the former. This I shall manifest first in whole numbers, then in fractions.

Example 1. If I pay 28 shillings for the carriage of 3 C.weight for 50 miles, how much ought I to pay for the carriage of 17 C. for 84 miles? Answer 13 l. - 6 s. - 6 d. 18

Of the 5 given numbers I make choice of three fuch which will make a fingle rule of three, and fay,

Which rule I find (by the third rule of the ninth Chapter) to be direct, and therefore I multiply the third number 17 by the second 28, and the product which is 476 I place as a numerator over the divifor as denominator. Then with this fraction (whether it happen to be a proper or improper fraction) and the remaining two numbers in the question, which have not yet been used, I form a second rule of Three, and say,

miles

248 The double Rule of Three Book I.

Which being a rule of three direct, I work as a rule of three in fractions, according to the first rule of the 28 chapter, and fo find the fourth number to be 19984 s. or 13 l. 6 s. 6 18 d.

Or the first fingle rule being varied, the opera-

tion will be thus,

C. sh. C. sh.

2. By a rule direct,
$$\frac{1}{84}$$
: $\frac{28}{1}$: $\frac{12}{1}$: $(\frac{19984}{150})$

Otherwise thus,

Thus you see the two fingle rules to be varied three manner of wayes in refolving the question propounded, and each way produceth the same Anfwer ; the like diversity may be found in all questions resolvable by the double rule of three, or rule compound of 5 numbers.

Example 2. if 403 l.in 3 of a year gain 21 l.what will 100 l. gain after that rate in 72 of a year?

Answ. 52500 l. or 5 l. -75. - 9 29 d.

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By 2 Single rules of three, thus,

l. L. L. I. I. By a rule direct, 223; 5: 100; (2500

2. By a rule direct, 3: 2500: -12: (

Kale of the Figure Print Or by these two single rules,

year l. year l.

1. By a rule direct, \(\frac{2}{1} : \frac{5}{2} : \frac{7}{12} : \((\frac{105}{48}) \)

2. By a rule direct, 203: 105: 100 : (52500)

Otherwise thus,

1. By a rule inverse, $\frac{201}{5}$: $\frac{2}{3}$: $\frac{100}{1}$: $(\frac{406}{1500})$

ion year 2. By arule direct, 1426 : 1 : 12 : (\$2500 9744)

Thus by 2 fingle rules of three varied three feveral ways, you see the Answer of the question to be \$2,500 l. to wit, 5 l. - 7 s. - 9 7 d. by comparing the refults at

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utes of three grants CHAP. XXXI.

The Rule of False in Fractions. The traine days

X 7. Hen a question propounded cannot readily beapplyed to the Rule of three, or any of the vulgar Rules in Arithmetick; the best refuge for fuch as are not acquainted with Algebra is the Rule of two false Positions, which, for that it hathalready been handled in whole numbers, I shall the more briefly touch upon in Fractions.

II. When a number is fought by a question, you are to feign or suppose some number taken by guess to be the number fought, and to make tryal whether that feigned number will answer the conditions in the question or not, by comparing the number resulting at the end of the Work, wirn the given number resulting from the true number fought; and if you find both those results to be the same, then is the number which you first took by guess the true number or answer of the question; but if the number resulting from the suppofititious number be either greater or less than the given refult, with which it ought to be compared (to see whether you have hit the mark or not) fuch excess or defect must be noted for the Error of the first Position, to wit, an excess must be signified by this note +; and a defect by this --

III. In like manner a second number must be feigned, and after tryal is made therewith, to fee whether it will perform the conditions prescribed in the question, by comparing the results as afore-

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faid, the error of this fecond Position, if too much is to be noted by t, if too little by —, as before.

IV. After the errors of both Politions are difcovered, the two numbers before supposed or feigned to be the number fought, must be multiplied by the altern errours, that is, the first Position by the second errour, and the second Polition by the first errour; then if the notes of the errours be unlike, to wit, one of them +, and the other , the sum of the said products is to be taken for a dividend, and the sum of the errours for a divisor; but it the notes of the errours be both alike, to wit, both of them +, or both ----, the difference of the said products is to be taken for a dividend, and the difference of the errours for a divifor; laftly, the quotient arifing from the division made by the said dividend and divisor, gives the true number sought, or answer of the question, if it be solvable by the Rule of False. These Rules are the same in substance with those delivered in the 15 Chapter, and may be farther illustrated by the following Questions.

Quest. 1. A Gentleman hired a servant for a year for 6 pounds sterling, and a livery Cloak valued at a certain rate, but it happened that $\frac{1}{12}$ of the year being expired they fell at variance, and the Gentleman put away his servant, giving him the Cloak together with 50 shillings in mouey, which was the servants sull due for the time of his service, the question is to find what the Cloak was valued

at? Answ. 21. -- 8 s. -- 0 d.

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fervant, faying, if one year give 3 l. how much 1-3---- (1/4 l. -7 of the year? Auf. 1/2 l. 2. I likewise find what part of the 6 pounds was due to the fervant at the end of $\frac{1}{12}$ of the

 $-\frac{1}{12}$ — $(\frac{1}{2}1.$ year, faying, if I year give 6 pounds, how

much - of the year? Answer, 21.

3. For as much as the Cloak together with the money which the servant received ought to be equal to the part of the Cloak, together with the part of the 6 pounds wages due to him at the end of -2 of the year, therefore 3 1. (the supposed value of the Cloak) together with 2 1/2 l. (the money which the servant received) should be equal to 2 of a pound (the value of part of the Cloak due to the servant at the end of 12 of the year) together with 2 1. (the wages due for the fame time) that is to fay, 11 l. (the sum of 3 l. and 2 1 l.) should be equal to $\frac{21}{4}l$. (the sum of $\frac{7}{4}l$. and $\frac{7}{2}l$.) but it is greater by 1, wherefore the first Polition for the value of the Cloak being 3 pounds, the errour is found to be 1 too much.

4. I make a second Supposition guesting the value of the Cloak to be 2 pounds, and proceeding in every respect as with the first supposition I find the errour to be too little; fo that the two Pofi-

tions with their errours will be as you fee :

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Now in regard the errours are fractions, I may take in their stead whole numbers in the same proportion, to wit, multiplying the Numerator of the sirst fraction (or first errour) by the Denominator of

the fecond, I take the product which is 6 instead of the first errour \(\frac{1}{4}\); likewise multiplying the Numerator of the second fraction by the Denominator of the first, I take the product

Pos. Er. $\frac{3}{4} + \frac{1}{6} = \frac{6}{3} = \frac{1}{6} = \frac{1}{4} = \frac{2}{6} = \frac{1}{6} = \frac{1}{4} = \frac{2}{6} = \frac{1}{6} = \frac{1}{4} = \frac{1}{$

5) 12 (23 poun.

which is 4 instead of the second errour \$\frac{1}{6}\$, Or instead of the said 6 and 4 1 may take 3 and 2 which are in the same proportion with 6 and 4, (or with \$\frac{1}{4}\$ and \$\frac{1}{6}\$:) Then multiplying the Positions and new errours crosswise, and adding the products together (because the signs are unlike) the sum is 12 for a Dividend, and the sum of the errours 3 and 2 is 5 for a Divisor, so the quotient will be sound to be 2 \$\frac{2}{5}\$ l. so much therefore was the value of the Cloak, as will easily appear if tryal be made with 2 \$\frac{2}{5}\$ l. in the same manner as with the first seigned number.

Quest. 2. Vitruvius (in lib. 9. cap. 3.) reporteth that King Hiero having given commandment for the making of a Crown of pure Gold, was informed that the Workman had detained part of the Gold, and mixt the rest with as much Silver, as he had stole of Gold; The King being much displeased at the deceit, recommended the examination of the business to the samous Archimedes of Syracuse, who without desacing the Crown discovered the cheat in this manner; viz. Experience telling him that a quantity of Gold would possess less roome or space than the same quantity of Sil-

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ver, and consequently that a mixt mass of Gold and Silver of the same quantity would take up some mean space between the two sormer, he made a mass of pure Gold of the same weight with the Crown, likewise another mass of Silver of the same weight, then having put the Crown as also the other two Masses severally into a vessel filled up to the brim with water, he diligently reserved the water slowing over into another vessel, and from those 3 several quantities of water so expeld, he sound out the quantity of Gold and of Silver in the Crown: But torasmuch as Virruvius delivers not the practical operation, I shall here shew the same after the manner of Cardanus, Gemma Frisius, and other Arithmeticians.

Let us therefore suppose the weight of the Crown as also of the two several Masses to have been 5 l. Suppose also that by putting of the mass of Gold into the vessel, 3 l. of water was expeld; by putting in of the Crown, 3 ½ l. and by putting in of the mass of Silver, 4½ l. The question therefore is to know how much Gold and how much Silver the Crown was composed of. This may be resolved after this manner. Suppose 3 l. of Gold to be in the Crown,

then there remained 2 l.

5-3-3-(1 $\frac{4}{5}$ of Silver, now say by

5-4 $\frac{1}{2}$ -2-(1 $\frac{4}{5}$ the Rule of 3, if 5 l. of

Gold expel 3 l. of water

how much 3 l. of Gold? Answer 1 \(\frac{1}{5}\) l. Also if 5 l. of Silver expel 4 \(\frac{1}{2}\) l. of water, how much 2 l. of Silver? Answer, 1 \(\frac{1}{5}\) l. of water, add therefore the water of the Silver and of the Gold together, to wit, 1 \(\frac{1}{3}\) and 1 \(\frac{1}{5}\), so there will arise 3 \(\frac{1}{3}\) l. of water; this ought to have been 3 \(\frac{1}{4}\) l. (for so much overflowed

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Vitt. With flowed by putting in of the Crown;) but it is too much by -2, wherefore -2 is to be noted with + for the errour of the first Position 3 1. Again, seign another quantity of Gold to have been in the Crown, to wit , 2 l. therefore there remained 3 l. of Silver,

then fay if 5 1. of Gold expel 3 1. of water, how much 2 l.of Gold? Anfw. 1 1 l. of water: Alfo if

5 l. of Silver expel 4 1 l. of water, how much 3 l. of Silver? Answer, 2 72; then add 1 4 unto 2 72, the fum will be 3 72 1. of water : this ought to have been 3 4 L but it is too much by 11 wherefore 11 is to

be noted with + for the errour of the second Position 2 l. Here because the errours are fractions having a common Denominator, I take their Numerators 7 and 13 instead of the errours; then multiplying crof-

Pos. 39 14 6)25 (4 to lb. of Gold.

wife, to wit, 3 by 13 the product is 39, also 2 by 7 the product is 14, which subtracted from the former Product 39 because the errours are like Heaves 25 for a Dividend; also the difference between the errours 7 and 13 is 6 for a Divisor; Lastly, dividing 25 by 6, the quotient is 4 1; fo much Gold therefore was in the Crown, and consequently (because the weight of the Crown was 5 l.) there was 5 l. of Silver which may be proved thus; Say if 5 1. of Gold, expel 3 1. of water, how much 4 1 l. of Gold? Answer, 2 1 l. of water; again if 5 l. of Silver ex256 The Rule of False &c. Book I.

Pel $4\frac{1}{2}$ of water, how much $\frac{5}{6}$ of Silver? Answer, $\frac{3}{4}l$. of water, which being added to $2\frac{1}{2}l$. the sum is $3\frac{1}{4}l$. of water, to wit, as much as flowed over

when the Crown was put into the veffel.

Here note, that in making a tryal of this nature, there is no necessity that the mass of Gold or of Silver be of the same weight with the Crown, or whatsoever thing is to be examined, but of what notable part of weight you please.

Note also, that for the more easie discovering of the Dividend and Divisor by the notes of t and — according to the sourth Rule of this Chapter, the sollowing verse may be a help, to

wit.

Addito dissimiles, subtrabitoque pares.

Or thus,

Notes being unlike, Addition make; If like, lesser from greater take.

The Reader may see more questions to exercise the Rule of False in the tenth Chapter of the Appendix, and the demonstration thereof in the ninth Chapter of the same.

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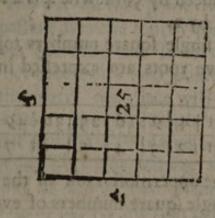
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CHAP, XXXII.

The Extraction of the Square (or Quadrate) Root.

I He Extraction of the Square root is that, by which having a number given, we find out another number, which being multiplied by it felf, produceth the number given.



II. In the Extraction of the Square-root, the number propounded is alwayes conceived to be a quare number, that is, a certain number of little quares comprehended within one intire great quare, and the root or number required is the fide of that great square, as will readily appear by this Diagram, where you see 25 little squares contained within one great square; now it the said content 25 be given, and the side or root of the square containing the said 25 little squares is required, the invention of such side or root is called the extraction of the square root; which root must

be

258

be such, that is it be squared, that is, multiplied by it self, the product must be equal to the square content sirft given: So 5 is the square root of 25, for 5 times 5 is 25. Likewise this square number 49 being propounded, his root is 7.

III. Square numbers are either fingle or com-

pound.

ing produced by the multiplication of one single figure by it self, is alwayes less than 100: so 25 is a single square number produced by 5; likewise 4 is a square num-

V. All the single square numbers together with their respective roots are expressed in the Table

following.

Squares. 1 | 4 | 9 | 16 | 25 | 36 | 49 | 64 | 81 | Roots. 1 | 2 | 3 | 4 | 5 | -6 | 7 | 8 | 9

Here in the uppermost rank of the Table are placed the single square numbers of every particular sigure, and in the other their respective roots; and therefore if it were demanded what is the square root of 36, the answer will be 6. So the square root of 16 is 4, the square root of 9 is 3 &c. And contrarily the square of the root 6 is 36, Also the square of 3 is 9.

VI. When a square number is given, that exceeds not 100, and yet is none of the square numbers mentioned in the Table, for his root you are to take the root of the square number that being less, yet comes nearest unto it: so 45 being given, the root that belongs unto it is 6, and 10 being given,

his correspondent root is 3. wall and la

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Chap. XXXII. the Square Root 259

VII. A compound square number is that, which being produced by a number (that consists of more places then one) multiplied by it self, is never less than ber.

number produced by the multiplication of 32 mul-

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VII. A

VIII. To prepare any square number given for extraction, put a point over the first place thereof on the right hand (being the place of Units;) then proceeding towards the lest hand, pass over the second place, and put another point over the third place; also passing over the fourth place put another point over the fifth, and so forward in such manner that between every two points which are next one to the other, one place will be intermitted: so if the square root of 1024 be required, the first point is to be placed over 4, and the second over 0 as you see, and 1024 so many points as are in that manner placed, of so many figures the root demanded will consist.

IX. Having thus prepared your number, you may see it distributed by the points into several squares: so in the last Example, 10 is the first square and 24 the second, likewise if this number 144 were propounded for extraction, after points are duly placed according 144 to the last Rule, you will see 1 to be the first square and 44 the second.

X. Having drawn a crooked line on the right hand of the number propounded for extraction (after the same manner as is usually done in Division to denote the place of the quotient,) find the

root

The Extraction of Book I.

root of the first square, and place it in the quoti-

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ch bei 00 0 left hand of the Refolvend 124, the work will stand as you fee.

XV. Let the whole Refolvend, except the first place thereof on the right hand (being the place of units) be alwayes efteemed as a Dividend; then demanding how often the Divisor before found, is contained in the faid Dividend, and observing in that behalf the Rules before taught in Divition,

write the answer in the quotient, and also on the right hand of the Divifor, to wit, between the Divifor and the crooked line : fo if you ask how often the Divisor 6 is found in the Dividend 12, the answer is 2, wherefore I write 2 in the quotient, and also after the

62) 124

Divisor 6, as you see in the Margent.

XVI. Multiply all the number which standeth on the left hand of the Refolvend, (to wit, before the crooked line) by the figure last placed in the quotient, and write the product orderly under-

neath the Refolvend (to wit, units under units, tens under tens, &c.) then having drawn a line under the faid product, fubtract it from the Resolvend, and subscribe the remainder under the line: fo 62 being multiplied by 62) 124 2, the product is 124, which if I fubtract out of the Resolvend 124, the remainder is 0; and thus

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	1000	200	SECTION .

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the whole Work being finished, the square root of 1024 (the number propounded) is found to be

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Note 1. When the product before mentioned exceeds the Refolvend placed above it, the work is erroneous, and then you are to reform it by placing

a leffer figure in the quotient.

Note 2. For every one of the particular squares (diffinguished by the points) except the first on the left hand, a Refolvend is to be fet apart, by bringing down to the remainder the congruent particular square, as is directed in the 13 Rule; and as often as a Resolvend is set apart, so often a new divisor is to be found by doubling or multiplying by 2 all the root in the quotient (confisting of what number of places soever.)

Note 3. The Work of the 10,11, and 12 Rules for finding of the first figure in the root, is but once ufed in the extraction of the root of a number confifting of what number of places foever; but the Work of the 13,14, 15, and 16 Rules is to be repeated for the finding of every place in the root ex-

cept the first.

The practice of these 3 Notes will be seen in the following Examples. in or) broyloted and dispra

Example 2. Let it be required to extract the

square root of 43623.

Having distributed the number propounded into several squares by points, as is directed in the eighth Rule of this 43623 (2 Chapter, I demand the square root of 4 the first square, which I find by the 4 ACT 5 rule of this Chapter to be 2; wherefore placing 2 in the quotient, and the square thereof, which is 4, under

the first square 4, I draw a line, and subtracting 4 from 4 the remainder is o, which I subscribe underneath derneath the line. This is alwayes the first Work. which is no more repeated in the whole Extraction (as was intimated in the third Note aforegoricer; and alto effer the division up state de . gni

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Then bringing down the next square, which is 36, and placing it next after the remainder o, the Resolvend is 36; and doubling the root 2 in the quotient, the product is 4 for a Divisor (by the 13 and 14 Rules) and the Dividend will be 3 (by the 15

Rule;) wherefore I demand how often the Divisor 4 is contained in the dividend 3, and not finding it once contained in it, I place o in the quotient, and al-Io next after the Divisor 4; and because the product of 40 multiplied by of the last Character 32 and sont

43623 (20

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in the quotient) is o, the resolvend 36, from which the faid product ought to be deducted, remains the fame without alteration, therefore I bring down 23 the next square, and place it after the remainder 36, so will 3623 be a new refolvend; then doubling the whole root in the quotient, which is 20, the

divifor will be 40 (according to the second Note before men-banden. . 61 318 tioned,) and the dividend will be 43623000 362 (to wit, all the resolvendexcept the first place on the right hand by Rule 15.) wherefore 1 40)03623

demand how often the divisor some six so 40 is contained in the divided 362, or how often 4 in 36, & though it be 9 times in it, yet (according to the first Note aforegoing) Ican can take but 8, (for if I should take 9, and proceed according to the 15

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and 16 Rules, a number would arise greater than the resolvend, from which such number arising ought to be subtracted;) wherefore I write 8 in the quotient, and also after the divisor 40; this done, I

the left hand of the resolvend)
by 8 the figure last placed in the quotient, and the product, to wit, 3264 I subscribe under, and subtract from the resolvend
359, thus the work being finished I find 208 to be the num-

ber of unities contained in the root fought; and because after the extraction is ended there happens to be a remainder, to wit, 359, I conclude that the root sought is greater than the said 208, but less then 209, yet how much it is greater then 208, no rules of Art hitherto known will exactly discover, although we may proceed infinitely near, as in the

next Rule will be manifest.

very near, a competent number of pairs of cyphers, to wit,00,0000,000000,0r 0000000,&c. are to be annexed to the number first propounded, then esteeming the number propounded with the cyphers annexed to be but one entire number, the extraction is to be made according to the precedent Rules, and look how many points were placed over the number first given, so many places of Integers will be in the root, the rest of the root towards the right hand will be the Numerator of a decimal fraction, which Numerator consistes of the root places as there were points over the cyphers

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cyphers annexed: so if 43623 were given as before, to find the root thereof (according to this rule) annex cyphers in this manner, and then if you extract it according to the Rules aforegoing, you

43623.000000 (208.861, &c.

will find the root arising in the quotient to be 208.861, that is 208 \(\frac{861}{1000} \); and because after the extraction is finisht there happens to be a remainder, I conclude that 208 \(\frac{861}{1000} \) is less than the true or exact root, but 208 \(\frac{862}{1000} \) is greater than it; so that by annexing three pairs of cyphers to the number propounded, you will not miss \(\frac{1}{1000} \) part of an unit of the true root; also by annexing 4 pairs of cyphers, you will not miss \(\frac{1}{10000} \) part of an unit, and in that order you may proceed infinitely near, when you cannot obtain the true root. The whole operation of the said \(Example \) here followeth.

43623.000000 (208.861, &c, 4 The root. 408) 03623 3264 4168) 35900 33344 41766) 255600 250596 417721 82679 R Again 266

Again if to were propounded to be extracted, you must prepare it thus,

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And then the root thereof 2 1622776, &c. being extracted will bewhich (according to the third) Rule of the 22 Chapter) may be 3.1622776, &c. written thus -

See here part of the Work in the extraction of the root of 10, which may give you a light and understanding of the rest.

10.00000000000000 (3.16227, &c.

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XVIII. The extraction of the The Proof. square root is proved by multiply-

ing the root by it felf, for that done, the product 1 in such case when there is no remainder after the extraction is finished) will be equal to the number whose square root was enquired; so in the first Example of this Chapter, the root 32 being multiplyed by it felf produceth 1024 the number propounded: but when after the extraction is finithed there happeneth to be a remainder, and that the root is found as near as you please, in a mixt number of integers and decimal parts (by annexing cyphers as in the 17. Rule) then fuch mixt number being multiplyed by it felf must produce a mixt number less than the number first propounded for extraction, yet so near unto it, that if the figure standing in the last place of the Numerator of the decimal fraction in the root be made greater by I, and then the mixt number fo increased be multiplyed by it self, the product must be greater than the number first propounded: so in the Example of the 17. Rale, if 208.861 be multiplyed by it felf, it produceth 43622 .917, &c. which is less than the propounded number 43623, but if 208.862 be multiplyed by it self, the product will be 43623.335,&c. which is greater than 43623.

XIX. The square root of a Fra-Ction is found in this manner, viz. To extract the Square root of extract the root of the Numerator a Frattion. (by the precedent Rules of this

Chapter) which root shall be a new Numerator. Also the root of the denominator is to be taken for a new denominator, so the new Fraction shall be the square root of the Fraction first propound-

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ded: thus the square root of 72 is 3, viz the root of 9 is 3 for a new numerator, also the root of 16 is 4 for a new denominator. In like manner the square root of 1 is 1. But here note diligently, that if the Fradion whole fquare root is required be not in its leaft terms, it must first of all be reduced by the 4. Rule of the 17. Chapter before any extraction be made; for oftentimes it happens that the Fraction first given hath not a perfect root, but when such Fra-Gion is reduced into its least terms, the root thereof may be extracted: foin this Fraction 78, each term is incommensurable to its square root, viz. neither 8 nor 18 hath a Square root expressible by any true or rational number; but the faid 78 being reduced to its least terms +, the root of this may be extracted, for the root of 4 is 2 for a new Numerator; also the root of 9 is 3 for a new Denominator; fo that 3 is found to be the fquare root of \$ (equivalent unto 78.

XX. When either the Numerator or Denominator of a Fraction hath not a perfect square root, such root is usually express by prefixing this Character, $\sqrt{\text{or }}\sqrt{q}$, before the Fraction given: so the square root of $\frac{1}{16}$ is signified thus $\sqrt{\frac{1}{16}}$, or thus \sqrt{q} , $\frac{13}{16}$, because the root of $\frac{13}{16}$ cannot be express by any true or rational number whatsoever, yet it

may be found very near as in the next Rule.

To extract the

Square root

near, of a

fraction in
commensurable to its

Square root.

which is in commensurable to its root, may be found near, in this manner, viz reduce the fraction proposed into a decimal by the third Rule of the 23. Chapter: the more places are in the decimal, the nearer will the root be

found, but the decimal must consist of an even

number of places, viz. either of two, four, fix, eight or ten, &c. places; then extract the square root of that decimal, as if it were a whole number, according to the Rules aforegoing, which root found shall be a decimal expessing near the square root of the fraction proposed.

So if the square root of 13 be required near, reduce the said 13 into a decimal (by the 3d Rule of the 23. Chapter) which will be found \$1250000, &c. Then extracting the square root thereof as if it were a whole number, it will be found .9013 very

near.

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number commensurable to its root, To extract the is sound in the same manner as in square root of the 19. Rule of this Chapter, the ber, mixt number being first reduced in-

to an improper fraction by the 10. Rule of the 17

Chapter. on the ag anothe

So the square root of 34 34 will be sound 5 7, viz. 34 34 being reduced into the improper Fraction 2203 4, the square root of the Numerator 2209 will be 47 for a new Numerator; also the square root of the Denominator 64 i 8, for a new Denominator; so is found 47, which (by the 13. Rule of the 17. Chapter) is 5 1/8 the square root sought. And here the same caution is to be observed as in the 19. Rule of this Chapter; viz. the fractional part of the mixt number, or the improper fraction equivalent unto the mixt number, must be in the least terms before any extraction be made.

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To find the Square root ear, of a mixt number incommenfurable to its root.

XXIII. When the mixt number given is incommensurable to its Square root, prefixing this Character before it, viz. I or Iq. So the square root of 73 will be thus expressed: 17 3 or /q. 73: but if you desire to find

the square root near of a mixt number incommensurable to its root, reduce the fractional part of the mixt number into a Decimal of an even number of places, as in the 21. Rule of this Chapter, and annex the Decimal fo found unto the whole part of the mixt number; then esteeming the said whole number and Decimal as one entire number, extract the fquare root thereof according to the aforegoing Rules of this Chapter, and from the root found, cut off alwayes to the right hand, fo many places as there are points over the Decimal annexed, which number so cut off shall be a Decimal, shewing the fractional part of the root, and that on the left hand shall be the whole part of the root; so the square root of 7 3 will be found 2 .7688 very near.

CHAP. XXXIII.

The Extraction of the Cube Root.

HE Extraction of the Cube Root is that, by which having a number given, we find another number, which being first multiplyed by it felf, and then by the product, produceth the number given.

II.

II. In the Extraction of the Cube root, the number propounded is alwayes conceived to be a Cube num-

A Cubical

ber, that is a certain number of little Cubes, comprehended within one entire great Cube, and the root or number required is the fide of that great Cube: what a Cube is may be well exprest by a Die, which indeed is a little Cube it felf; wherefore if you place four Dice in a square form, that is, laying two and two in a rank, you shall have a square containing four Dice, upon which if you yet erect such another square of Dice, you shall have a great entire Cube comprehending two times 4, that is 8 Dice or little Cubes; and here 8 is the Cube number given, and two is the root, or number required: In like manner if you rank 25 Dice in a square form, viz. laying 5 in a rank, you have a square containing 25 Dice, now upon this square of Dice if you erect four other fuch squares one up. on another, you shall have a great entire Cube comprehending 5 times 25, that is 125 little Cubes, and in this case 125 is the Cube number propounded, and 5 the root or number required.

III. A Cube number is either fingle or com-

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IV. A fingle Cube number is that, which being produced by the Multiplication of one fingle figure first by it self, and then by the product, is alwayes less than 1000. So 125 is a fingle Cube number produced by 5 multiplyed first by it self, and then by 25 the product; for 5 times 5 is 25, and 5 times 25 is 125.

V. All the single Cube numbers, and square numbers

bers, together with their respective roots, are ex-

Cubes									
Squares							49	64	81
Roots.	1	21	3	4	51	6	7	1 8	9

Here, in the uppermost rank of the Table are placed the single Cube numbers of the particular singures 1,2,3,4,5,6,7,8.9. in the next the squares of those sigures, and in the lowest rank the sigures themselves being the respective roots of the Cubes and squares in the uppermost ranks; and therefore the Cube root of 125 being demanded the answer is 5, and the Cube root of 216 being required, the Table will give you 6, and so of the rest.

VI. When a Cube number is given that exceeds not 1000, and yet is none of the Cube numbers mentioned in the Table; for his root you are to take the root of the Cube number, that being less comes nearest unto it. So 157 being given, the

root that belongs unto it is 5.

A. compound Gube number is that, which being produced by a number (that confifts of more places than one) first multiplyed by it self, and then by the product is never less than 1000. So 157464 is a compound Gube number, being produced by 54 multiplyed first by it self, and then by 2916 the product, for 54 times 54 is 2916, and then 54 times 2916 is 157464, the compound Cube number propounded.

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VIII. To prepare a Cube number for extraction, put a point over the first place thereof towards the right hand (to wit the place of units;) then passing over the second and third places, put another point over the sourch; and passing over the fifth and sixth put another point over the seventh, and in that order (to wit two places being intermitted between every two adjacent points) place as many points as the number will permit: so 157464 being given, you are to place the points as in the Margent, and so many points as are in that manner placed, of so many figures the rost demanded will consist.

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May see it distributed by the points into several Cubes: so in the same example

157 is the first Cube, and 464 the second.

157464
In like manner if this number 7464 were propounded for extraction, after points are duly placed as before, you will see 7

to be the first Cube, and 464 the second.

X. Having drawn a crooked line on the right hand of the number propounded to fignific a quotient, find the Cube root of the first Cube and place it in the quotient: so . .

I finding (by the fixth Rule of this 157464(5) Chapter) 5 to be the correspondent

root of 157, I write 5 in the quotient, and then the work will stand as you see in the Margent.

AI. Subscribe the Cube of the root
placed in the quotient, under the first
Cube of the number given: so 125
being the Cube of 5 the root (by the

fifth

first Cube of the number given, as you fee in the example. XII. Draw a line under the Cube subscribed as aforesaid (to wit the Cube of the root placed in the quotient) and subtract this Cube from the first . . Cube of the number propounded, 157464 (5 placing the remainder orderly underneath the line: fo 125 the Cube of 5 being subtracted from 157, the remainder is 32, and the Work will 32 stand as you see. XIII. To the faid remainder bring down the next Cube of the number propounded (to wit the figures or cyphers that frand in 157464 (5 the 3 next places) placing the said Cube next after, to wit, on -- the right hand of the remainder, 32464 reselv. so the next Cube 464 being placed after the remainder 32, there will be found this number 32464, which may be called the Refolvend. XIV. Having drawn a line underneath the Refolvend, square the root in the quotient, that is, multiply it by it felf, and subscribe the triple of the said square or product under the 157464 (5 resolvend in such manner, that the first place (to wit, the place of t-- nits) of the faid triple square 32464 resolv.may stand directly under the third place (or place of hundreds) in the resolvend: so the square of the root 5 is 25, the triple whereof is 75, which I subscribe under the Resolvend

The Extraction of Book I.

fifth Rule of this Chapter) Iwrite it under 157 the

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vend in such manner, that the figure 5 which is in the first place (to wit the place of units) in the triple product 75, may stand under 4 which is feated in the third place of the resolvend, as you fee in the Margent.

XV. Triple the root or number in the quotient, acd subscribe this triple number in such manner that the first place thereof (to wit the place of units) may stand directly under the second

place (to wit the place of tens) in the Refolvend: fo the triple of the root 5 is 15, which I 157464 (5 subscribe in such manner, that 125 the figure 5 which is in the first place(to wit the place of units) 32464 Refolv. in the faid triple number, doth fland directly under 6, which is 75 5000 w feated in the fecond place of the 15 resolvend, and the Work will

stand as in the Margent.

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XVI. The triple square of the root, and the triple of the root being placed

one under the other, as is directed in the 14. and 15. Rules 157464 (5 aforegoing, draw a line un- 125 derneath, and add them together in such order as they are 32464 Resolv. seated, and let the sum be efleemed as a divisor : so the triple square 75, and the triple number 15, being added together as they are ranked in 765 Divisor. the Work, the fum will be 765 for a Divisor.

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XVII. Let

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276 XVII. Let the whole Refolvend, except the first place thereof towards the right hand (to wit the place of units) be esteemed as a Dividend, then

demanding how often the first figure (towards the left hand) 157464 (54 of the Divisor is contained in 125 the correspondent part of the - dividend, and observing in that 32464 Refolv. behalf the Rules before taught - in Divition, write the answer in the quotient : fo if I ask how often 7 (the first figure of the - Divisor towards the left hand) 765 Divisor. is contained in 32 (the corre-Spondent part of the Dividend placed above) the answer will be 4, wherefore I write 4 in the quotient, as you

fece in the Example. It to bail a fee and a fe miolyend, and the twork will fland as in the Mandenty

XVIII. Having drawn another line under the Work, multiply the triple square before subscribed (as is

Margent.

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157464 (54 directed in the 14. Rule) by the figure last placed in the quotient, and subscribe this product 32464 Resolv. under the said triple square; (to wit units under units, tens under tens, &c.) fo75 being multiplyed by 4, the product - is 300 which I subscribe under 765 Divifor. 75 (the triple square) and the work will stand as you see in the

XIX. Multiply

XIX. Multiply the figure last placed in the quotient first by it self, and then the product by the criple number before subscribed (as is directed in the 15. Rule of this Chapter;) this done, fubscribe the last product under the faid triple number (to wit , units under units , tens under tens, &c.) so 4 being squared or multiplyed by i felf, the product is 16, which being multiplyed by the triple number 15, the product is 240, this therefore I subscribe under the aforesaid triple number 15, and the Work will stand as you see.

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XX. Subscribe the Cube of the figure last placed in the quotient, under the resolvend, in such manner that the first place of this 157464 (54 Cube (to wit, the place of u- 125 nits) may fland under the place of units in the resol- 32464 Resolvend. vend: So 64 being the Cube of 4, I write it under the re- 75 folvend 32464, in fuch man- 15 ner that the figure 4, which is in the place of units in the 765 Divisor. Cube 64, may stand under the figure 4 which is feated in the place of units of the refol- 240 vend: observe the Work in 64 the Margent.

s	Ser.
-	157464 (54
5	32464 Resolvend.
on t	75 minute 201.
t	765 Divisor.
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XXI. 157464		
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work, add the three last numbers together in the same order as they are feated, and fubtract the fum of them from the resolvend, placing the remainder orderly underneath: fo the fum of the three last numbers, as they are ranked in the Work, is 32464, which if you subtract out of the resolvend 32464, the remainder is o. Thus the whole Work being finished, the Cube root of 157464 (the number propounded) is found to be 54.

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Note 1. When the sum of the three last numbers before mentioned is greater than the resolvend, the Work is erroneous, and then you are to reform it by placing a lesser figure in the quotient.

Note 2. For every one of the particular Cubes (distinguished by the points) except the first Cube on the lest hand, a resolvend is to be set apart, by bringing down to the remainder the next Cube (as is directed in the 13. Rule.) And as often as a resolvend is set apart, so often is a new Divisor to be sound, by adding the triple of all the root in the quotient (consisting of what number of places soever) to the triple of the square of such root, after they are orderly placed according to the 14. Note

Note 3. The Work of the 10, 11, and 12. Rules for finding of the first figure in the root is but once used in the extraction of the root of any number whatsoever, but the Work of all the sollowing Rules is to be used for the finding of every place in the root, except the first.

The practice of these 3 Notes will be seen in the

following Examples.

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he 14 Note Example 2. Let it be required to extract the

Cube root of 8302348.

Having distributed the number given into several Cubes by points, as is directed in the eighth Rule of this Chapter, I demand the Cube root of 8 (the first Cube on the left hand) which I find by the fifth Rule of this Chapter

to be 2, wherefore placing . . .

2 in the quotient, and 8 the 8302348 (2

Cube thereof under 8 the first 8

Cube, I draw a line, and fubtracting 8 out of 8 the o

remainder is o, which I fub-

fcribe under the line. This is alwayes the first Work, and is no more repeated in the whole extraction (as was intimated in the 3. Note aforegoing;) then bringing down the next Cube (to wit, the figures standing in the three sollowing places of the number propounded) which is 302, I place it after the remainder 0, so is 302 the resolvend; this done, having drawn a line underneath the resolvend, I seek for the triple of the square of the root, viz. the root in the quotient is 2, which multiplyed by it self produceth the square 4, the triple whereof is 12, this I subscribe under the resolvend, in such manner that the figure 2

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in the units place of this triple square 12, may stand directly under the figure 3, which is seated third place of the

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A min II a lo also W	resolvend, (to wit, the place
8302348 (2	of hundreds) according to
8	the 14. Rule aloregoing;
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Again I triple the root 2,
0302 Resolvend.	which produceth 6, and sub-
0,000	fcribe this triple number 6
12	under the second place (or
06	place of tens) in the resol-
The state of the s	- vend, to wit, under o (ac-
126 Divisor.	cording to the 15. Kule of
	- this Chapter;) then drawing
a saint	a line under the Work, and

adding together the said two numbers last subscribed, as they are ranked, the sum of them is 126 for a divisor (according to the 16. Rule afore-

going.)

That done, esteeming 30, to wit, all the places except the first or place of units in the refolvend, as a Dividend, I demand how often the divisor 126 is contained in 30, and not finding it once contained therein, I write o in the quotient, and now because the sum of the three numbers which ought to have been produced (according to the 18, 19, and 20. Rules of this Chapter) by the multiplication of o (which was last placed in the quotient) amounts to 0, the resolvend 302 out of which the faid fum should have been subtracted, remains the same without alteration, wherefore having drawn a line under the Work, I write down anew the old refolvend 302, and bringing down the next Cube 348. I annex it to the faid 302

Chap.XXXIII. the Cube Root.

302; so there will be a new resolvend, to wit. 302348.

Then squaring the root 20 (that is, multiplying of it by it felf) the product is 400, which I

triple or multiply by 3, and subscribe the product 1200 underneath the new refolvend in fuch manner, that the place of units in this triple quadrate 1200 may stand under the place of hundreds, or third place of the resolvend 302348, to wit, under 3 (according to the 14. Rule.) Again I Subscribe the triple of the root 20, which is 60, in such manner that the place of units in this triple root 60 may stand under the place of tens or fecond place of the refolvend, to wit, under 4, then adding together the two numbers last subscribed, to wit, 1200 and 60, in fuch order as they are ranked in the Work, the sum is 12060 for a

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Again, esteeming the whole resolvend, except the sust place (or place of units) as a dividend, to wit; 30234, I demand how often I (the sirst figure of the divisor towards the left hand) is contained in 3 the correspondent part of the Dividend; and though it be three times contained in it, yet (according to the first Note at the end of the 21 Rule of this Chapter) I dare take but 2, for it I should take 3, and proceed according to the 18, 19, 20, and 21 Rules of this Chapter, a number would arise greater than the resolver d (from which such number arising ought to be substracted,) wherefore I write 2 in the quotient.

Then multiplying the triple square 1200 before subscribed, by 2 (the figure latt placed in the quotient,) the product is 2400, which I subscribe under the faid 1200 (to wit, units under units, and tens under tens, &c.) Also multiplying the triple root 60 before subscribed, by 4 (the quadrate of 2 the figure last placed in the quotient) the product is 240, which I subscribe under the faid triple root 60; last of all I subscribe 8 the Cube of the faid new root 2, under the place of units or first place of the resolvend, to wit, under 8, and having added together those three numbers last subscribed, to wit 2400, 240 and 8 as they thand in ranks in the Work, the fum of them is 242408, which being subducted from the resolvend 302348, there will remain 59940. Wherefore the Work being finished, I find 202 to be the number of unities contained in the Cube root of 8302348 the number propounded: and because after the extraction is ended there happens.

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to be a remainder, to wit 59940, I conclude that the Cube rost fought is greater than the said 202, but less than 203; yet how much it is greater than 202, no Rules of Art hitherto known wilexactly discover, although wee may proceed infinitely

near, as by the next Rule will be manifest.

XXII. To find the fractional part of the root very near, ternaries of cyphers, to wit, ooo, oocooo, or oocoocooo, &c. are to be annexed to the number first propounded; then esteeming the number propounded with the cyphers annexed to be but one entire number, the Extraction is to be made according to the preceding Rules of this Chapter, and look how many points were placed over the number first given, so many of the foremost places in the Quotient are the Integers or unities contained in the Cube root fought, and the rest of the places in the quotient are to be esteem'd as the Numerator of a Decimal fraction, which Numerator confifteth of so many places as there were points over the cyphers first annexed: fo if 8302348 were given as before, to find the Cube root thereof (according to this Rule) annex cyphers in this manner,

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And then if you profecute the extraction according to the Rules aforegoing, you shall find the Cube root fought to be 202. 48, &c. that is, 202 \(\frac{4}{100} \) and more; wherefore you may conclude that 202 \(\frac{4}{100} \) is less than the true root, but 202 \(\frac{4}{100} \) is greater

greater than it: fo that by annexing two ternaries of cyphers, to wit, 6 cyphers, to the number propounded, you will not miss 100 part of an unit of the true root; also by annexing 3 ternaries of cyphers, to wit 9 cyphers, you will not miss Tood part of an unit of the true root, and in that order you may proceed infinitely near, when you cannot obtain the true root. The whole operation of the faid Example here followeth, where you may observe, that for the more certain and easie placing, as well of the numbers which constitute the feveral Divisors, as of those which constitute the Ablatitious numbers to be subtracted from the feveral and respective resolvends, down-right lines are drawn between the particular Cubes of the number propounded, first distinguished by points as before.

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In like manner the Cube root of 2 will be found to be near equal to 1, 25992, &c. that is, 1 = 25992 and more.

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XXIII. The extraction of the Cube root is proved by multiplying the root cubically,

The Proof. to wit, the root being first multiplied by

it felf, and then the product multiplied by the root, the number arifing or last product (incife there be no remainder after the extraction is finished) will be equal to the number propounded: so in the first Example of this Chapter, the Cube root 54 being multiplied first by it felt produceth 2916, which being multiplied again by 54 produceth 157464, to wit, the number whose Cube root was inquired. But when after the Extraction is finished, there happeneth to be a remainder, and that the root is found as near as you please in Integers and decimal parts (by annexing cyphers as in the 22 Rule of this Chapter,) then such mixt number expressing the root, being multiplied cubically, must produce a mixt number less than the number first propounded, yet so near unto it, that if the figure standing in the last place of the decimal fraction in the root be made greater by 1, and the mixt number so increased be multiplied cubically, the product must be greater than the number first propouuded : so in the Example of the 22 rale of this Chapter, if 202.48 be multiplied cubically it produceth 8301305.49, &c. which is less than the propounded number 8302348, but if 202.49 be multiplied cubically, there will arise 8302535.49, &c. which is greater than the faid given number.

this manner, viz. extract the Cube root of the Numerator

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Numerator (according to the Foregoing Rules,)

which root referve for a new Numerator; also the Cube root of the De- Toextrollibe neminator shall be a new Denomina-

tor; lastly this new Fraction shall be fraction.

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the Cube root of the Fraction first propounded: fo the cube root of - s is 3 for the cube root of 8 is 2 for a new Numerator, also the cube root of 27 is 3 for a new Denominator. In like manner the cube root of is is . But here note diligently, that the fraction whose cube root is required, must be in its least terms before any Extraction be made; for oftentimes it happens that the fraction first given hath not a perfect root, albeit, when such fraction is reduced into its least terms, the root thereof may be extracted : fo in this fraction 15 neither the numerator nor denominator bath a perfect cube root, yet the faid 16 being reduced to its leaft terms 27 by the fourth Rule of the 17 Chapter) the cube rom of this may be extracted, for the cube root of 8 is 2 for a new numerator, also the cube root of 27 is 3 for a new denominator, so that the cube root of -8 (which ise. qual to 16) is found to be 31 s ton the boriops at

XXV. The Cube root of a fraction which hath not a perfect Cube root may be found near in this manner, viz reduce the Fraction given into a Decimal fraction, by the third Rule of the 23 Chapter, the more places are in the Decimal, the nearer will the root be found, but the decimal must confut of ternaries of places, to witheither of three, fix, nine, or twelve, &c places; then extract the Cube root of the Numeraror of that Decimal, as if it were a whole number (according to the Rules before given,) which root found shall be a De imal

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expressing near the Cube root of the Fraction pro-

pounded.

MXVI. The Cube root of a mixt number commensurable to its root may be found in the same manner as in the 24 Rule of this Chapter, the mixt number being first reduced into an improper fra-

Ction (by the 10 Rule of the 17 Chapter.

So the cube root of $12\frac{19}{27}$ will be found to be $2\frac{1}{3}$, viz. reducing $12\frac{12}{27}$ into this improper fraction $\frac{3+3}{27}$ the cube root of $\frac{3+3}{27}$ will be found $\frac{7}{3}$ or $2\frac{1}{3}$. And here the same caution is to be observed as in the 24 Rule of this Chapter, viz. the fractional part of the mixt number, or the improper fraction equivalent unto the mixt number, must be expressed by a Numerator and Denominator in the least terms be-

fore any extraction be made.

is required, hath not a perfect cube root, this character, Jc. is usually prefixed before such mixt number; so the cube root of 2 \frac{3}{8} is thus expressed, Jc. 2\frac{3}{8}. Likewise Jc. \frac{5}{8} denotes the cube root of \frac{5}{8} which is a fraction, whose cube root is inexpressible by any true or rational number: but if you desire to know the cube root near of a mixt number which hath not a perfect cube root, reduce the fractional part of the mixt number into a decimal (as in the 25 Rule of this Chapter) and annex the decimal so sound unto the Integers of the mixt number; then esteeming the said Integers with the decimal so annexChap. XXXIII. the Cube Root. 289

thereof, and from the root found cut off alwayes to the right hand so many places as there were points over the said decimal annexed, which places so cut off shall be the fractional part of the root, and those remaining on the lest hand shall be the Integers of the root: so the cube root of 2 \frac{3}{8} will be found 1.334, and more.

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Etion of the roots of the Biquadrate (or fourth Power,) the fifth Power, &c. but their operations being exceeding tedious, and hardly intelligible without the knowledge of Algebra; I shall only in this place touch upon the Extraction of the Biquadrate-root, because it may be extracted by the Rules delivered in the 32 Chapter, and refer the more curious Arithmetician for further satisfaction in this matter, to my Treatise of the Elements of Algebra.

XXIX. A quadrate or square number multiplyed

by it self produceth a Biquadrate number: So 4 multiplied by it self produceth the Biquadrate 16. Therefore if a root.

drate root thereof be required, first extract the quadrate or square root of the number propounded, and then extract the square root of that root for the Biquadrate root sought. Thus if 20736 be a number propounded, the Biquadrate root thereof will be found 12: for the square root of 20736 is 144, and the square root of 144 is 12. When the number given hath not a persect Biquadrate root, you are to annex quaternaries of cyphers, to wit, either 4,8,12, or 16, &c. cyphers, and then proceed as before; so will you find the root near, whose fractional part will be a decimal. Thus the Biquadrate root of 7 will be found near 1.62.

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The Relation of Numbers in quantity.

FILE might here proceed to thew the extra-I. Hus far fingle Arithmetick: Comparative Arithmetick infues, which is wrought by numbers, as they are confidered to have Relation one to another. I glass He A To and all depoch stores a set

II. This Relation confifts in quan-Bretius Ari.b.

LI cap:21 tity, or quality.

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III. Relation in quantity is the reference or respect, that the numbers themselves have one unto another: As when the comparison is made between

6 and 2, or 2 and 6: 5 and 3, or 3 and 5.

IV. Here the Terms or Numbers propounded are alwayes two, whereof the first is called the Antecedent, and the other the Consequent: So in the first eximple, 6 s the Antecedent, and 2 the Consequent: and in the second, 2 is the Antecedent, and 6 the Confequent.

V. Relation in Quantity consists either in the difference, or else in the rate or reason that is

found betwixt the Terms propounded.

CHAP.

VI. The difference of two numbers is the remainder, which is left after subtraction of Difference. the less out of the greater : so 6 and 2 being the terms propounded, 4 is the difference betwixt them : for if you subtract 2 out of 6, the remainder is 4.

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Chap. XXX. Numbers in Quantity 291

the quotient of the Antecedent divided by the Consequent: So if it be Rate or Reason demanded what rate or reason 6 hath to 2, I answer, Triple reason: for if you divide 6 the Antecedent, by 2 the Consequent, the quotient is 3, 2 being contained just 3 times in 6. In like manner is there subtriple reason betwixt 2 and 6, for if you divide 2 by 6, the quotient is $\frac{2}{6}$, or (which is all one) $\frac{1}{3}$, because 6 being not once found in 2, there remains 2 for the Numerator, 6 the Divisor being the Denominator of the Fraction given you in the Quotient, according to the 9 Rule of the 16 Chapter asoregoing.

VIII. This rate or reason of numbers is either

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1X. Equal reason is the Relation that equal numbers have unto one another:

as 5 to 5, 6 to 6, 7 to 7, &c.

Equal Reason.

X. Here the one being divided by the other, the quotient is alwayes an Unit: for if it be deman-

ded how often 5 is in 5, the answer is 1.

Qual numbers have one unto ano-

ther: and this is either of the grea- unequal reason.

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XII. Unequal reason of the greater to the less, is when the greater Term is Antecedent: as of 6

to 2, 5 to 3, and the like.

vided by the Consequent is always greater than an Unit; So 6 divided by 2, the Quotient is

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3, and 5 divided by 3, the quotient is 1 \(\frac{2}{3}\).

XIV. Unequal reason of the less to the greater, is when the lesser Term is Antecedent: as of 2 to 6, 3 to 5, &c.

ded by the consequent is alwayes less than an unit: So 2 divided by 6, the quotient is $\frac{2}{6}$ or $\frac{1}{3}$; and 3 di-

vided by 5, the quotient is 3.

XVI. Each of these kinds of unequal reason is again subdivided into five other kinds or varieties, whereof the three first are simple, and the other two are mixt.

XVII. The simple kinds of unequal reason are 1. Manifold. 2: Superparticular. 3. Super-

partient.

Manifold Reatained in the Antecedent divers
times without any part remaining:
as 4 to 2, 8 to 4, 16 to 8, which is

called Double reason, because the less is contained twice in the greater; so 6 to 2 is triple reason,

8 to 2 fourfold reason, &c.

vided by the consequent is always a whole number: so 8 divided by 2, the quotient is 4.

XX. The opposite of this kind, viz. of the less to the greater, is called submanifold:

Submanifold. Examples hereof are 2 to 4, 4 to 8, 8 to 16, &c. Likewise 2 to 6, 2 to 8,

2 to 10, &c.

XXI. Superparticular is, when the Antecedent contains the confequent once, and besides an aliquot part of the confeder.

Superparticular.

chap. XXXIV. Numbers in Quantity 293 quent; that is, an half, a third, a fourth, or a fifth part, &c. of the consequent, as 3 to 2, 4 to 3, 5 to 4, 6 to 5, and the like; here three divided by 2, the quotient is 1½, and 4 being divided by 3, the quotient is 1⅓. In like manner 5 divided by 4, the quotient is 1¼, and 6 divided by 5 the quotient is 1⅓; wherefore I say 2 and half 2 (that is 1) constitute 3: So likewise 3 and one third part of 3 (viz. 1) constitute 4, and so of the rest.

XXII. Here the quotient of the Antecedent divided by the Consequent is a mixt number, whose whole part, as also the numerator of the fraction annexed, is alwayes an unit: as is observable in

the examples last mentioned.

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XXIII. The opposite reason of Subsuperparti-

to 3, 3 to 4, 4 to 5, 5 to 6, &c.

XXIV. Superpartient is, when the Antecedent contains the Consequent once, and besides divers parts of the conse-

quent: as 5 to 3, 7 to 5, 7 to 4,

8 to 5, 9 to 5, 11 to 7, &c. here 5 divided by 3, the quotient is 1 \(\frac{2}{3}\), and therefore 5 contains 3 once, and \(\frac{2}{3}\) of 3; for 3 and two thirds of 3 (viz.

2) constitute 5.

vided by the consequent is a mixt number, whose whole part being an unit, hath alwayes for the Numerator of the fraction annexed unto it a number composed of more units than one: so the conference being made betwixt 5 and 3, and 5 the Antecedent being divided by 3 the consequent, the quotient is 1 \frac{2}{3}.

fuperpartient : Examples hereof are 3 to 5, 5 to 7, 4 to 7, 5 to 8, 5 to Subsuperparti-9, 7 to 11, and the like. XXVII. The mixt kinds of unequal reason are Manifold Superparticular, and mainfold superpartient. XXVIII. Manifold Superparticular reason is, when the Antecedent contains the consequent divers times, and besides Manifold Superparticular. an aliquot part of the consequent : as 5 to 2, 10 to 3, 17 to 4,21 to 5, and the like. XXIX. Here the quotient of the Antecedent divided by the consequent is a mixt number, whose whole part confifting of more units than one, hathalwayes an unit for the Numerator of the Fraction annexed unto it; fo 5 divided by 2, the quotient is 2 1, and 21 divided by 5, the quotient is 4 1. XXX. The opposite of this Reason Submanifold is Submanifold Superparticular; as Superparticu-2 to 5, 2 to 7, 3 to 7, 4 to 9, &c. XXXI. Manifold Superpartient is, when the antecedent contains the consequent divers times, and besides divers parts Manifold Superpartient. of the consequent; as 8 to 3, 17 to 5, 19 to 4, 28 to 5, &c. XXXII. Here the quotient of the Antecedent divided by the Consequent is a mixt Number, whose whole part as also Submanifold the Numerator of the Fraction an-Sup expartient. nexed unto it, is alwayes a Number composed of more units than one: so 8 divided by 3, the quotient is 2 2, and 28 divided by 5, the XXXIII. The quotient is 5 ?

294 The Relation of Book r

XXVI. The opposite of this reason is Sub-

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Chap. XXXV. Numbers in Quality 295

XXXIII. The Opposite here is Submanisold Superpartient: as 3 to 8, 5 to 17, 4 to 19, 5 to

28, and the like.

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And these are the several kinds or varieties of the Rates or Reasons that are sound amongst Numbers, so that no two Numbers whatsoever can be named, but the rate or Reason betwixt them is comprehended under one of these sive kinds.

CHAP. XXXV.

The Relation of Numbers in Quality, where of Arithmetical and Geometrical Proportion.

I. P Elation in quality (otherwise called Proportion) is either the reservence or respect that the Reasons of Vide Euclide 1 Numbers have one unto another, or else which the differences of numbers have one to another.

II. Therefore here the Terms propounded ought alwayes to be more than two, for otherwise there cannot be a comparison of Reafons or differences in the Plural number.

III. This proportion is either Arithmetical, or

Geometrical.

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IV. Arithmetical proportion is, when divers numbers differ according to an equal difference, as 2, 4, 6, 8, 10,&c. here Arithmetical 2 is the common difference betwixt 2 Profortion. and 4, 4 and 6, 6 and 8, 8 and 10, &c. So 1, 2, 3, 4, 5, 6, 7, &c. differ by Arithmetical Proportion, a being the common difference betwixt

them. V. Arithmetical Proportion is either continu-

ed or interrupted.

VI. Arithmetical Proportion continued is, when divers numbers are linked together by a continual progression of I. Continued. equal differences. Such are the ex-

amples last propounded, as also these 1, 3, 5, 7, 9, 11, 13. &c. And 100000, 200000, 300000,

400000, &c.

VII. In a rank of numbers that differ by Arith--metical Proportion continued, the fum of the first and last Terms being multiplyed by half the number of the Terms, the Product is the total fum of all the Terms: so it being demanded, how many strokes the Clock strikes betwixt midnight and noon; the Terms of the Progression in this question are Twelve, viz. 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12. for in that order the Clock strikes, wherfore if I multiply 13 the fum of 12, and 1 (the first and last Terms) by 6 (being half the number of the Terms) the Product is 78, which is the total fum of all the Terms propounded being added tegether.

VIII. Or thus, Multiply the number of the Terms by the half fum of the first and last Terms,& then likewise the Product will give you the total Chap. XXXV. Numbers in Quality. 297

of all the Terms: so 13, 11, 9, 7, 5, 3, being given, their total is 48, for 8 the half sum of 13 and 3, the first and last Terms being multiplyed by 6, the

number of the terms, the product is 48.

IX. Three numbers being given, that differ by Arithmetical proportion continued, the mean being doubled, is equal to the sum of the extreams: so 5, 6, 7, being given, 6 being doubled is equal to the sum of 5 and 7 the two extreams.

X. Arithmetical Proportion may be continued either upwards or down- Upwards.

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XI. Upwards, when the Terms of the Progreffion increase, as these, 2, 4, 6, 8, 10, 12, &c. or these, 1, 2, 3, 4, 5, 6, &c. And this last rank is more particularly termed Natural Progres-

fion.

XII. Here when the first term is also the common difference of the terms, the last term being divided by the number of the terms, the quotient will give you the first term of the rank: again in this case the first term multiplyed by the number of the terms produceth the last term: so this rank 3, 6, 9, 12, 15, 18, 21, being propounded, wherein 3 is both the first term as also the common difference of the terms; I say 21 the last term being divided by 7 the Number of the terms, the quotient is 3 the first term; contrariwise 3 the first term multiplyed by 7, produceth 21 the last terms

XIII. Arithmetical proportion continued

downwards is, when the terms of the

progression decrease: such as are 35, Downwa

32, 29, 26, 23, 20: And 40, 35, 30,

25, 20, 15, 10, 5.

This Rule is in the inverse of t'e 12. Rute aforegoing.

XIV. Here when the last term is also the common difference of the terms, the first term being divided by the Number of the terms, the quotient will give you the last term: Again, the last Ch

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term multiplyed by the number of the terms, produceth the first term of the rank.

For example, this rank 40, 35, 30, 25, 20, 15, 10, 5 being propounded, in which 5 is both the last term, and likewise the common difference of the terms, I fay, 40 the first term being divided by 8 the number of the terms, the quotient is 5 the last term: on the other tide 5 the last term being multiplyed by 8, the product is 40 the first term.

XV. Arithmetical Proportion interrupted is, when the Progression is discontinu-

ed: as in these numbers 2,4,8,10; 2. Interrupted. here 2 and 4 being compared with 8

and 10 differ according to Arithmetical proportion, but so do not 4 and 8 differ, for 2 is the common difference betwixt 2 and 4, 8 and 10, whereas the difference betwixt 4 and 8 is 4. In like manner 8, 14, 17, 23, differ by Arithmetical

proportion interrupted.

XVI. Four numbers being given, that differ by Arithmetical proportion either continued or interrupted, the fum of the two means is equal to the fum of the two extreams: fo 5, 6, 7, 8, being given, the fum of 6 and 7, the two mean numbers, is equal to the fum of 5 and 8, the two extreams: and 8, 14, 17, and 23, being propounded, the fum of 14 and 17 being added together is equal to the fum of 8 and 23.

XVII.Geo-

Chap. XXXV. Numbers in Quality. 299

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XVII. Geometrical proportion is, when divers numbers differ according to like
Rate or reason: that is, when the reafons of numbers, being compared to-

gether, are equal. So 1, 2, 4, 8, 16, 32, &c. which differ one from another by double reason, are said to differ by Geometrical proportion, for as one is half 2, so 2 is half 4, 4 half 8, 8 half 16, 16 half 32, &c.

XVIII. Geometrical proportion is either continued or interrupted.

XIX. Geometrical proportion continued is, when divers numbers are linked together by a continued progression of the like reason: of this sort is the example last given: for as 1 is to 2, so is 2 to 4, 4 to 8, 8 to 16, 16 to 32, &c. So likewise the numbers 3, 9, 27, 81, 243, 729, &c. diff r by Geometrical proportion continued, viz. by triple reason, each of them being contained three times in the next number that sollows it.

XX. In numbers continually proportional from 1, the first number from 1 is the root or first power, the second is the square or second power, the third the cube or third power, the fourth the Biquadrate or sourth power, the fifth the fifth power, the sixth the sixth power, &c. So in this rank of numbers, 1,3,9,27,81,243,729, &c. 3 is the root, 9 the square, 27 the cube, 81 the biquadrate, 243 the fifth power, 729 the sixth power, &c.

XXI. The root being multiplyed by it self produceth the square, which being again multiplyed by the root produceth the cube, and so each proportional.

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given for the root, multiplyed by it self, the product is 4, which being again multiplyed by it self produceth 16, then 16 in like manner squared produceth 256, which likewise multiplyed by it self produceth 65536, I say then that 2, 4, 16, and 256 are continual means betwixt 1 and 65536.

XXIII. The continual means comprehended betwixt any number given and I, are discovered
by a continued extraction of the square roots; for
example, 65536 being given, the root thereof extracted is 256, whose root is 16, then the root of
16 is 4, and the root of 4 is 2; so that at last I
find 256, 16, 4, and 2 to be continual means intercepted betwixt 65536 and I as before.

cal proportion continued, if you multiply the last term by the quotient of any one of the terms divided

Chap. XXXV. Numbers in Quality. 301 divided by another term, which being less is next unto it, and then deducting the first term out of that product, divide the remainder by a number that is an unit less than the quotient, the last quotient will give you the total of all the terms propounded in the progression; so this rank 2, 6, 18, 54, 162, 486, 1458, being propounded, wherein the proportionals differ by subtriple proportion, I first take 2 and 6 the two first terms, and dividing 6 by 2, I find the quotient 3, wherefore multiplying 1458 the last term, by 3 the quotient, the product is 4374, out of which if I deduct 2 the first term, the remainder is 4372, which being divided by 2 (viz. a number which is an unit less than 3 the quotient) the last quotient gives me 2186, which is the total fum of the proportionals propounded admin by prod.

XXV. Three proportionals being given, the square of the mean is equal to the product of the extreams: so 4, 8, and 16 being propounded, 8 times 8 being 64, is equal to 4 times 16, which is

likewise 64.

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XXVI. Geometrical proportion interrupted is, when the progression of like rea-

son is discontinued, in such sort 2. Interrupted.

that four numbers being given, the
like reason is not found betwixt the second and
third, that is betwixt the first and second, and the
third and sourth; of this sort are these numbers
2, 4, 16, 32. here as 2 is to 4, so is 16 to 32, for
they differ by double reason; but as 2 is to 4, so
is not 4 to 16, for 4 and 16 differ by sourfold reason, 4 being contained 4 times in 16: so likewise
4, 8, 8, 16, differ according to Geometrical proportion interrupted.

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XXVII.

302 The Relation of &c. Book I.

Division are proportional; for in Multiplication, as I is to the Multiplicator, so is the Multiplicand to the product, or as I is to the Multiplicand, so is the Multiplicator to the product: Again, in Division as the Divisor is to I, so is the Dividend to the Quotient: or as the Divisor is to the Divisor is to the Divisor is to the Dividend, so is I to the Quotient.

ever being given, the product of the two means is equal to the product of the two extreams: So 2, 4, 16, 32, being propounded, 4 times 16 (which is 64) is equal to 2 times 32, which is likewife 64.

Here endeth the first Book, which containeth all that is absolutely necessary, for the sull understanding of common or practical Arithmetick. Such as desire to see how the same is performed by artificial, or borrowed numbers, called Logarithmes, may peruse Mr. Wingates Second Book, being a distinct Treatise of artificial Arithmetick.

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APPENDIX.

CONTAINING

Choice knowledge in Arithmetick, both Practical and Theoretical; the Contents whereof
are exprest in the following Page.

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Composed by John Kersey.

Teacher of the

MATHEMATICKS.

At the Sign of the Globe in Shandois-Street in Covent-Garden.

Vox audita perit, litera Scripta manet.

Choice knowledge in Arithmetick, both Prastical and Thio." terical; the Contents whereof + are express in the follow-

At the Sign of the Globe in Shandois-Street in Covert Garden.

Fax andits perit, letera Stripen manet.

The Contents of the

APPENDIX.

CHAP.

I. F Contractions in the Rule of Three.

2. Of Rules of Practice by aliquot parts.

3. Of Exchanges of Coins, Weights, and Mea-

4. Practical questions aboute Tare, Tret, Loss, Gain, Barter, Factorship, and measuring of Tapestry.

5. Of Interest of Money, and the construction of Tables to value Annuities, &c:

6. A demonstration of the Rule of Three.

7. A demonstration of the Double Rule of Fellow-

8. A demonstration of the Rule of Alligation: where also of the composition of Medicines.

9. A demonstration of the Rule of False.

the parts of vulgar Arithmetick, to which also are added various practical Questions, about the Mensuration of Superficial Figures and Solids, with the Gaging of Vessels.

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An Explication of such Notes or Characters, which for brevity sake are used in this AP-PENDIX.

Hist is a note of Addition, fignifying that the number which followeth such fign is to be added to the number preceding it; so 3 + 4 imply that 4 is to be added to 3: sometimes also, when no number is placed next after the said note, it implies that the number preceding is not exactly express; so the square root of 2 is 1.414 to or 1.414, &c. that is, 1.7000 and somewhat more.

This—is a fign of Subtraction, fignifying that the number which followeth fuch fign is to be subtracted from the number preceding it; so 6—2 signifiesh the difference between 6 and 2, or 2 to

be subtracted from 6.

This * is a fign of Multiplication, fignifying that the number which precedeth such sign is to be multiplyed into, or by the number following the sign: so 4 implies that 3 is to be multiplyed by 4; likewise by 3 * 4 * 8 is understood the continual multiplication of the numbers 3, 4, and 8; viz. 3 is to be multiplyed by 4, and the product is to be multiplyed by 8. Sometimes also the said sign hath reference to as many of the preceding or following numbers as have a little line placed over them; so 3 * 2 † 6 or 2 † 6 * 3 signifieth that 3 is to be multiplyed by the sum of 2 and 6. Likewise

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wise 8—5 × 3, or 3 × 8—5 implieth that 3 is to be multiplied by the difference between 8 and 5: Moreover if A and B represent two numbers, then A × B or A B implieth the product of the multiplication of those numbers: Likewise B—C × A signifieth the product arising from the multiplication of the excess of the number B above the number C, by (or into) the number A. Again, if A B and A C represent two lines, then A B × A C implieth a rectangular Figure or long square made of the lines A B and A C.

Numbers placed as you fee in the 3) 18 (6

Margent denote a Divisor, a Dividend

and a Quotient, to wit, 3 the Divisor, 18 the Dividend, and 6 the Quotient; the like is to be under-

flood of ether numbers fo placed.

Numbers placed after the manner of a fraction denote a quotient, which ariseth from dividing the 2 x 5 x 6

Numerator by the Denominator; fo-is equal

3 × 4

to the Quotient, which ariseth from dividing the product of the continual multiplication of 2, 5 and 6 by the product of 3 multiplied by 4.

Four numbers placed as you fee in 2.4 :: 6.12

the Margent are Geometrical proporti-

onals, viz. As 2 is to 4; so is 6 to 12: or if 2 give 4, then 6 will give 12. Sometimes also they are

placed thus, 2 4 6 12.

This = is a note of equality or equation; so by 3 † 4=5 † 2 is signified that the sum of 3 and 4 is equal to the sum of 5 and 2: also 7—3=9—5 signifieth that the difference between 7 and 3 is equal to the difference between 9 and 5; that is, 7 lessened lessened by 3 leaves the same remainder, as 9 lesfened by 5. Also 4 * 3 = 12 implieth that the product of the multiplication of 4 by 3 is equal to 12.

> This is a fign of majority, fignifying that the number on the left hand of fuch fign is greater than the number on the right hand thereof; fo 5 > 3 implieth that 5 is greater than 3.

< This is a fign of minority, fignifying that the number on the left hand of fuch fign is left than the number on the right hand thereof; fo 3 < 5 implieth that 3 is less then 5. A ban & A contact

This Character J or J q. signifies the square root of the number which follows it, fo / 144 im-

plies the square root of 144, to wit 12.

Also this Jc. fignifies the cube root of the number which follows it, So Jc. 1728 fignifies the cube root of 1728, which cube root will be found to be 12 goldivib woil at Sking stolilw angityup a ston

Numerator by the Teaminatur Committee is requal

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the Margent are Generalizated proportion or account endersize As a is to a sign to it a saint alien

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This = is a note of equality or counting a for by a the state is figuited that the famous and A is

equal to the fum of ganda; along -3 = 9-5 fignifieth that the difference between and 3 is co-

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APPENDIX.

CHAP. I.

Of Contractions in the Rule of Three.



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of Arithmetick, which have been fully laid open in the precedent Book, and are mindfull of the Notes or Symbols before explained, will find no difficulty in the 1, 2, 3, 4, 5, and 10. Chapters of this Appendix,

wherein divers compendious operations no less delightful than useful are methodically handled, and the rest will be as easie to such as are but meanly acquainted with Geometrical demonstration.

II. To repeat the breif wayes of Multiplication set forth in the 10,11, and 12 Rules of the fifth Chapter, or those of Division, in the 11, 15, and 16 Rules of the

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the fixth Chapter aforegoing, would be a superfluous work, and therefore I shall presuppose the Reader to be throughly acquainted with them, as also with competent knowledge in the operations of fractions both vulgar and decimal.

III.It will be no small advantage to the Practical Arithmetician, to have by heart not only the com-

	mon Table of Multiplication,
27	24 but this also in the Margent,
3	36 to the end that when a num-
41	48 ber is given to be multiplied
5!	60 or divided by 12, (which
6 x 12 =	72 happens in the Reduction of
7	84 shillings to pence and the con-
81	96 verse)the product or quotient
93	108 may be writen down in one
	line only, as in the Examples
(3243 F. 1 - 3)	following.

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3472	fully h	4736

IV. When a whole number is given to be divided by a Divisor, which is equal to the product of the Multiplication of two single figures, instead of dividing by that Divisor you may first divide by one of those single figures, and then divide the quotient by the other, so will the last quotient be the same as if the Division had been finish by the Divisor first given: thus if 3466 farthings be given to be reduced to shillings, because $8 \times 6 = 48$ I first divide 3466 by

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8, so there will arise 433 for a new Dividend, and 2 farthings remain; then I divide the said 433 by 6,

) 3466 6) 433 (72 .. 2 1

fo there will arise 72 1, or

72 Shillings 2 pence, which with the 2 farthings remaining of the first Division make in all 72 s.: 2 1 d. which is the very quotient, when 3466 farthings are divided by 48. Note that you are to referve a farthing for every unit remaining of the first Division by 8, and two pence for every unit remaining of the second Division by 6. The reason of the operation is evident, for $\frac{1}{6}$ of $\frac{1}{8} = \frac{1}{48}$.

In like manner, if 7136 pence are given to be reduced into pounds, because 240 d. = 1 l. also 6 x 40 =240, therefore if 7136 pence be first divided by 6. the quotient will give 1189 fix pences, and 2 pence remain; then if 1189 be divided by 40, (that is by 4, after 9 the last place of the Dividend towards

the right hand is cut off)

6) 7136

the quotient will be 29 1. and there will remain 29

fix pences, or 14 s. 6 d. 40)118 9)29:14:8

which together with the

2 pence remaining of the first Division, and the faid 29 1. makes in all 29 1.: 14 s.: 8 d. which is the same with the quotient, when 7136 pence are divided by 240, for -1 of 1 = 240.

Again, suppose 3463 pence are given to be reduced into shillings; for a sinuch as 4 × 3 = 12, I first divide 3463 by 4, so there will arise 865 for a new Dividend and 3 penceremain: then I divide the faid 865 by 3 fo there will arise 288 1 or 288 s.

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4 d. which with the 3 4) 3463 pence before remaining s. d. make 288 s. 7 d. which 3) 865 (288...7 is the fame with the quotient, when 3463

pence are divided by 12, for 1 of 1 = 11.

V. In the Rule of Three as well direct as inverse, when the Divifor with either of the other two given numbers may be feverally divided by fome common measure, without leaving any remainder, the quotients may be taken for new terms and proceeding in like manner as often as is possible, the operation according to the tenth Rule of the eighth Chapter, or the second Rule of the ninth Chapter, will be much contracted : so if it be demanded what 52 yards of Cloth will cost at the rate of 21 1. for 14 yards; the Auswer will be found 78 pounds, in manner following.

> 1. y. 14 ... 21 ... 52 2 ... 3 ... 52 ... 3 ... 26 .. (78

In the first rank you may observe, that the Divifor 14 and the second term 21, being severally divided by their common measure 7, (the three new terms in the fecond rank) will be 2,3, 52. Again in the fecond rank the Divisor 2 and the third term 52 being feverally divided by their common meafure 2, the three new terms (in the third rank) will be 1, 3, 26. Laftly, working with these according to the Rule of Three direct, the Answer to the question (or fourth term) will be found to be 78.

Another

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Another Example, If 21 men will finish a work in 16 dayes, what time must be allowed to 12 men for the finishing of such a work? Answer , 28 dayes.

> men dayes 21 ... 16 ... Bomb 10 7 ... 4 ... I (28 dayes

In the first rank you may observe, that the Divifor 12 (for the rule is inverse) and the first term 21 being severally divided by their common measure 3, the three new terms (in the second rank) will be 7, 16, 4. Again, in the second rank, the Divisor 4, and the fecond term 16, being severally divided by their common measure 4, the three new terms in the third rank will be 7, 4, 1. Lastly, working with these as the Rule of three inverse requires, the Answer to the question (or fourth term) will be found 28.

VI. In the Rule of three, as well direct as inverse, when the Divisor and either of the other two terms are fractions having a common denominator, the said denominators may be rejected, and their numerators retained as new terms: fo if it be demanded what is the value of 2 of an Ell, when 3 of an Ellare worth 66 pence, the Answer will be found 154 pence, and the Work will stand as you

> one yard in breadth will be buildient 3 .. 66 ., 2 3 .. 66 .. 7 1 .. 22 .. 7 (154

Another

Another Example. If 3 \(\frac{1}{4}\) yards of Scarlet cloth cost 8 l. 15 s. what is the price of one yard at that rate? Answer 2 l. 6 s. 8 d.

$$\frac{15}{4} \cdots \frac{35}{4} \cdots 1$$
 $15 \cdots 35 \cdots 1$
 $3 \cdots 7 \cdots 1 \cdots (2\frac{1}{3}l \cdots 1)$

VII. In the Rule of three as well direct as inverse, when the Divisor only is a fraction, either of the other two terms may be reduced to a fraction of the same Denominator, and then the Denominators may be rejected, as before in the fixth Rule; also when one of the three given terms is a fraction, and is not the Divisor, the Divisor may be reduced to a fraction of the same Denominator with the fraction first given, and then the common Denominators may be likewise cancelled.

An Example of the first Case may be this, if \(\frac{7}{8} \) of a yard cost 14 s. what is the price of 1 yard? Answer 16 shillings.

An Example of the second Case; if of suff which is \(\frac{1}{4} \) of a yard in breadth, 7 yards in length will make a Garment; how much of that stuff which is one yard in breadth will be sufficient for the same purpose? Answer 5\(\frac{1}{4} \) yards.

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Chap. II. Rules of Pract. by Aliq. parts 315

Rules of 3 $\begin{cases} \frac{1}{4} & \cdots & 7 & \cdots & 1 \\ \frac{1}{4} & \cdots & 7 & \cdots & \frac{4}{4} \\ 3 & \cdots & 7 & \cdots & 4 \end{cases}$ (). $\frac{21}{4}$ or $5\frac{1}{4}$.

CHAP. II.

Rules of Practice by Aliquot parts.

IV. Any even number of failings is either 7 of

I. A Naliquot part takes its name from the Latine word aliquoties, for (according to Euclid) an aliquot part is of a greater number such a part, which being taken (aliquoties or) certain times doth precisely constitute that greater number; so 3 is an aliquot part of 12, for 3 taken sour times doth exactly make 12, without any excess or defect; in like manner 4 is an aliquot part of 20, because 4 taken 5 times doth precisely make 20; but 7 is not an aliquot part of 20, for 7 taken twice doth want of 20, and being taken thrice doth exceed 20; this kind of part last mentioned is by Kuelid called pars aliquanta, of which there will be no use in this place.

II. When the Rule of Three direct hath I or an Integer for the first time, it is commonly called a Rule of Practice, either from the great use and practice thereof in common affairs, or else for that questions of this nature, may be resolved by operations more speedy and practical than those of the

Rule of Three.

III. The

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316 Rules of Practice Appendix III. The choicest of these Rules of Practice may be reduced to 5 Cafes, viz.

(1. Of shillings under 20. When the price 2. Of pounds and (hillings. of 1 or an In- 3. Of pence under 12. teger consists. 4. Of shillings and pence. 15. Of pounds, shillings, pence, .II with parts of a peny.

All which cases with others of the like nature

are handled in their order.

IV. Any even number of thillings is either To of a pound (that is 2 shillings,) or elle is composed of 10 1. (to wit 2 s.) taken certain times: fo 8 s. is composed of 10 l. (or 2 shillings) taken four times, in like manner 18 s. is composed of 10 l. taken nine times.

V. When the price of I, or an integer of what name foever, is 2 thillings, the price of as many Integers as one will of that name is discoverable at hist fight, to wit by accounting the double of the figure which stands in the first place (towards the right hand) of the faid number of Integers, as shillings and the rest of the said number as pounds : so 345

yards at two shillings the yard shill. yards yard will coll 34 1. 10 s. for 1 . . 2 . . 345 the double of 5 is 10, which I write down apart as shil-Answer 34 l. 10 s. lings, then esteeming the remaining figures towards the 152 Gil

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left hand, to wit 34, as an entire number of pounds, the Answer will be 34 1. 10 s. This contraction is nothing elfe, but dividing the number

Chap. II. by Alignot parts. ber of Integers, whose price is required by 10; More examples hereof are these;

> and fifth Eules aloregoine. oz. Shill, cz. and to esigment I ... 2 ... 2057

> > Answ. 205 .. 14

shill. yards

Answ. 12 .. 0

VI. When the given price of I or an Integer is any even number of shillings greater than two shillings, multiply the number of Integers, whose price is required, by half the given number of thillings, with this caution, that the double of the figure which arifeth, in the first place of the product be written apart as shillings, and the rest of the product as pounds: so if it be demanded what 218 yards at 8 thillings the yard will amount unto, the Answer will be found

87 1. 4. s. for I multiply 218 by 4 (which is half 8 the given number of shillings) faying, 4 times 8 is

32, here the double of 2 (to wit, of that figure

which is to possess the first place in the product) is 4, which I fet apart as shillings, keeping 3 in mind for the three tens, again 4 times I is 4, which

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The second of	l. s. Answ. 3054
yar 1	d s. yards 18 230
count of to the	1. s. Answ. 207.0

VII. Any odd number of (hillings is either compos'd of $\frac{1}{10}$ l. (or 2 s.) and of $\frac{1}{20}$ l. (or 1 s.) or else it is compos'd of $\frac{1}{10}$ l. (or 2 s.) taken certain times, and of $\frac{1}{20}$ l. (or 1 s.) So 3 s. is compos'd of 2 s. and 1 s. Also 7 s. is compos'd of 2 s. taken three times and of 1 s. Likewise 13 s. is compos'd of 2 s. taken fix times and of 1 s.

VIII. When the given price of 1 or an Integer is an odd number of shillings, work for the greatest even number of shillings contained in that odd number, according to the fifth or sixth Rule aforegoing; then for the odd shilling remaining, take $\frac{1}{20}$ of the number of Integers, whose price is required (by the 16 Rule of the sixth Chapter of the preceding Book.) These two refults added together give the Answer to the question;

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question: so is it be demanded what 2344 ounces at 13 s. the ounce will cost, the answer will be found 1523 l. 12 s. For if (according to the sixth

Rule of this Chapter) I multiply 2344 by 6, 02. (to wit, by half the 2344 remainder, when one is abated from 13 the given number of thillings) there will arise 1406..8 14061.8 s. Then ta-117 .. 4 king -1 of 2344, there . will arise 117 1. 4 s. which being added to 1523..12 the former product

gives 1523 1. 12 s. for the auswer to the question.

Note, When 5 shillings is the given price of r or an Integer, the breisest way will be to take \(\frac{1}{4}\) of the number of Integers, whose value is required, for such quotient will give the pounds and shillings, which answer the question: so 2347 ounces at 5 s. the ounce amount unto 586 l. 15 s. for \(\frac{1}{4}\) of 2347 is 586\(\frac{3}{4}\) or 586 l. 15 s. But when the given price of 1 is any other odd number of shillings, this eighth Rule will be as compendious as any other whatsoever.

More examples of this Rule are these following.

yard	Shill.	yards		
10.	19 .	739		
2.	1, 101	1.	5.	
8		665.	2	
		36.	19	3-11-4
91.	Anfw.	702.	. I	
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yard I	Shill 17	yards 345	
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IX. When the given price of 1 or an Integer consists of pounds and shillings, first multiply the number of Integers whose price is required, by the number of pounds in the said given price, and subscribe the product as pounds; then proceed with the shillings in the said given price, according to the sixth or eighth Rule of this Chapter, and having subscribed that which ariseth under the aforesaid product of pounds, add them all together for the answer of the question: so if it be demanded what 328 hundred weight will amount unto at 21. 17 s. per C. (or one hundred weight) the answer will be found to be 9341 163. as by the operation is evident.

C. l. s.	C. 328 - de la 120
apack	1. 5.
	656 0
	16 :. 8
Answ.	934:16

More

Chap. II. by Aliquot parts. 321

More Examples to illustrate this Rule are these following:

C. 1. s. 17:12	
(110 (110))	1. s. 3528 3028
Answ.	3830 8
C. 1. s. 1 5 : 7	C. 129
	1. s. 645 3814 6 9
Anfw	690 3

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X. Any number of pence under 12 is either an Aliquot part of a shilling, or else compos'd of Aliquot parts, thereof; so 3 pence is an Aliquot part, to wit, \(\frac{1}{4}\) of a shilling. Likewise 4 is \(\frac{1}{3}\) of 12; moreover 5 pence are compos'd of 2 Aliquot parts, to wit, of 3 pence Which is \(\frac{1}{4}\) of a shilling, and of 2 pence which is \(\frac{1}{6}\) of a shilling; all which will readily appear by the sollowing Table.

More Exempler to illustrate this Kule are thefe

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Pence	Aliquot parts of a shilling.
1 1 ± 1	$-\frac{1}{12}$ (or $\frac{1}{3}$ of $\frac{1}{4}$)
3	
5	4 + 16
7 8	$\frac{1}{4} + \frac{1}{3}$ $\frac{1}{3} + \frac{1}{3}$ $\frac{1}{2} + \frac{1}{4}$
10	1 + 1 3 1 + 1 3 + 1 4

XI. When the given price of 1 or an Integer is an Aliquot part of a shilling, divide the number of Integers whose value is required by the denominator of such aliquot part; so will the quotient be the number of shillings which answer the question, which number of shillings (when there is occasion) may be reduced to pounds by the brief way of dividing by 20: so if it be required to know what 2686 ounces at 4 pence the ounce will amount

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ce will mount amount unto; the answer will be found 44 1. 15 1. 4 d. for fince 4 d. is an aliquot part, to wit, \ of a thilling, I divide 2686 by 3, so will the quotient be 895 3 s. or 895 s. 4 d. which shillings being divided by 20, give 44 l. 15 s. 4 d. for the answer to the question, as you see by the following operation

> ... 4 2686 s. d.
> 20) 89 5 · 4
>
> Answ. 44 · 15 · 4

More Examples of this Rule are these following.

yard d. yards 1 ... 6 ... 759 Answ. 18 .. 19 ..

> yard d. yards Arfw. 17 shillings.

XII. When the given price of an Integer is compos'd of aliquot parts of a shilling, divide the number of Integers, whose price is required, by the several denominators of the aliquot parts contained in the given number of pence, then add the quoti-

ents together, and the sum shall be the number of shillings which answer the question: so if it be demanded what 2347 yards of linnen cloth will cost at 9 pence the yard, the answer will be found 88 l. o s. 3 d. For since 9 d. is composed of 6 d. and 3 d. to wit, of the aliquot parts \frac{1}{2} and \frac{1}{4} of a shilling, I first divide 2347 by 2 (the denominator of the aliquot part \frac{1}{2}) so there

yard d. yards
1....9...2347

s. d.
1173:6
586:9
20)176|0:3

Answ. 88:6:3

the said 2347 by 4(the denominator of the other aliquot part) there
will arise 5863, or 586

s.9 d. which two quotients being added tod. gether give 1760 s.
3 d. or 88 l. os. 3 d.
which is the answer

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s. 6 d. Again, dividing

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of the question. More Examples to illustrate this Rule are these.

yard d. yards

s. d. 260 ... 8 260 ... 8

20) $52 \mid 1 \dots 4$ 1. s. d.
Answ. 26 .. 1 .. 4

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0%. d. 0%. I ... II ... 540

Mel Examples 081 kind are the li

942 135 135 20) 4915 s. d. Answ. 24 ... 15:0

XIII. When the given price of an Integer confifts of shillings and pence, first multiply the number of Integers whose value is required by the said given number of shillings, and subscribe the product as shillings, then divide the said number of Integers by the feveral denominators which are correspondent to the aliquot parts contained in the given number of pence, and subscribe the quotient or quotients underneath the aforesaid product of shillings, all which being added together give the number of shillings which answers the question: fo if it be demanded what 347 yards of cloth will cost at the rate of

7 s. 10 d. the yard, yard s. d. yards the answer will be I ..7: 10.. 347 found 135 1.18 1.2d. for first 347 being

multiplied by 7 (the 7 * 347 = | 2429 : given number of 2) 347(.. 173:6 thillings) produceth 3) 347(.. 115: 8 2429 (hillings, then dividing 347 by 2 20) 271 8: 2 and 3 feverally, (because 10 d. is com- Answ. 135: 18: 2

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	4)	540(135	of Integers
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Anjw. 226.. 18:6

XIV. When the price of an Integer confifs of shillings and pence, and that such shillings and pence joyntly considered do make an aliquot part of a pound, it will oftentimes be a briefer way than that in the last Rule, to divide the number of Integers, whose value is required, by the denominator of such aliquot part, so will the quotient give the answer

answer to the question in pounds and known parts of a pound. Thus if it be demanded what 767 yards will cost at the rate of 6 s. 8 d. the yard, the answer will be sound 255 l. 13 s.4 d. For since 6 s.8 d is an aliquot part, to wit, \frac{1}{3}
of a pound, I divide
767 by 3, so there ariseth in the quotient
255 \frac{2}{3}, or 255 l: 13 s.
24 d which is the answer of the question. Note that the Aliquot parts of a pound convenient for this Rule are these express in the following Table.

Sh. d.	Aliquot parts of a pound.
6 8	1 1000
3 . 4	fore Examples of this Rule as th
1 8	7½ & a A , 3
I 4	824 8: 81 . 5 1

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XV. When the given price of 1 or an Integer confilts of pounds, shillings and pence, reduce the said pounds and shillings all into shillings, then proceed according to the 13 Rule of this Chapter: So 517C-at 3l.: 171.5d-per C. will be sound to amount unto 2001 l. 4 s. 5 d. for having reduced 3 l. 17 s. into 77 s. I multiply 517 by 77, and write down the particular

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particular products; then for the 5 pence which is compos'd of the aliquot parts 4 and 6 of a shilling, I take 1 and 6 of 517, and subscribe the quotients orderly underneath the aforesaid products: Lastly, adding all together the fum is 400245.5 d. or 2001 l. 4 s. 5 d. for the answer of the question.

C. t. s. d. -ine and ol & yd ror 1 ... 3: 17: 5 .. 517

77 * 517= 4) 517 (.. 129:34. 6) 517 (.. 86:2

> 20)4002 4:5 bound a to ent. composit d. Anfro. 2001: 4: 5

More Examples of this Rule are thefe following.

C. l. s. d. C. 1 ... 5 : 13:8 ... 108

3) 108 (.. 36 -org coll agolliel orgi la exagell o

settos mor bruth ad liter 20) 1227 6: A TE A Showhar surveil las is a de A 1002 oton

Anfw: 613: 16: 0 10 10

Chap.II. by Aliquot parts. 329 1 ... 2: 10 :6 ... 84 50 × 84=4200 20) 424 2 (212:2 1. s. d. C. I ... I : 12 : 41 ... 306 20) 990 0: 4 1/2 Answ. 495: 0: 41

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Note, when the given price of an Integer confifts of certain pence together with 2 d.or 4 d.it will be convenient to take due aliquot parts of the number of Integers propounded for all the given price of an Integer except 1 d. and the said \(\frac{1}{2} \) d. or \(\frac{3}{4} \) d. then for that peny, and \(\frac{1}{2} \) d. take \(\frac{1}{8} \) of the faid Integers propounded, and if there be yet a farthing, take tof the faid quotient which ariseth by taking ; both which quotients give the value in shillings correspondent to 1 3 d. this will be evident by the following Examples. yard X

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yard d. 1 8½	
	81 6
20	$\frac{1}{1}$ $\frac{23 7 \cdot 8 \frac{1}{2}}{1}$ $\frac{1}{5}$ $\frac{1}{6}$

s. d.
$$1 \dots 3 : 6^{\frac{1}{2}} \dots 720$$

Answ. 11: 17:8 1/2

XVI. When the price of an Integer is given, and the price of many Integers of the same name together with 4 or 2 or 4 of an Integer is required, the value of those Integers may be first found by some of the precedent Rules, and then for the price of 1 of an Integer, take 1 of the given price of

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of an Integer; likewise for $\frac{1}{4}$ of an Integer, take $\frac{1}{4}$ of the said given price, also for $\frac{3}{4}$ of an Integer take the composed of $\frac{1}{2}$ and $\frac{1}{4}$ of the said given price: So if it be demanded what $34 \, C. \, 3 \, qu.$ (to wit, 34 hundred weight, and $\frac{3}{4}$ of an hundred weight) of Sugar will cost at $41.16 \, s. \, 3 \, d. \, per \, C.$ the Answer will be found $167 \, l. \, 4 \, s. \, 8 \, \frac{1}{4} \, d.$ as by the subsequent operation is manifest.

An example of Averdupois greater weight, where the quantity whose price is sought consists of entire hundred weights, quarters of an hundred, and of some number of pounds, which is not an aliquot part of 28 or \(\frac{1}{4}\) C.

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5. d.

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The example last mentioned being (of those questions which ordinarily happen in trade) one of the hardest to be resolved by the Rule of Practice, I shall touch upon the aforegoing operation, where you may observe the price of 218 C. 3 qu. to be sound after the manner of sormer Examples; then for 14 lb. part of the 24 lb. in the question, I take 1/2 of the price of 1/4 lb. and so there yet remains 3 lb. whose price is sound by taking 1/3 of the price of 7 lb. vize the price of 7 lb. being very near 7 s. 2 1/2 d.or 861/2 d.

I multiply 86 1/2 by 3, and divide the quotient by 7. so there ariseth 37 d. or 3 s. 1 d. very near; lastly, all being added together, the sum is sound to be

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r 861 d.

ent by 7.

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be very near 25322 s. 3 1 d. or 1266 l. 2 s. 3 1 d.

Note that a quarter of a farthing (or 76 of a penny) is the smallest money express in the example, and where any thing ariseth less than a quarter of a farthing it is omitted, but it is supposed to sollow this note †, for which surplusages some respect ought to be had in adding all together: now albeit, in resolving questions after this practical manner there will be some error, yet the loss for the most part will be less then a farthing, which is inconsiderable.

XVII. When the price of 1 or an Integer confitts of divers denominations, as pounds, shillings, pence; and the price of a certain number of Integers, which exceeds not a single figure, is required, work as in the following Example, viz. If it be required to find what 8 C. must cost at 3 l. 135.7 ½d. per C. it is evident that 8 C. must cost 8 times 3 l.

C. 1. s. d. C.
$$1. \cdot 3 : 13 : 7\frac{1}{2} ... 8$$

Answ. 29:9:0

13 s.7 ½ d.therefore I multiply ½ by 8, faying, 8 half pence make 4 pence, which I referve in mind; again, 8 times 7 pence make 4 s. 8 d. (to wit, 8 fix pences make 4 s. and there are 8 pence besides) to which adding 4 pence in mind, there will arise 5 s. which I reserve in mind, and subscribe a cypher under the place of pence; again, I say 8 times 13 shillings make 5 l. 4 s. (to wit, 8 Angels make 4 l. and 8 times 3 s.make 1 l.4 s.) to which adding 5 s.

in mind, the sum will be 5 l. 9 s. wherefore I subscribe 9 s. (the excess above the pounds) under the
shillings, and keep 5 lin mind; lastly, I say 8 times
3 pounds make 24 pounds, which with 5 pounds in
mind make 29 pounds; so that the total product
or answer of the question is sound to be 29 l. 9 s.

More Examples of this kind are these.

C. 1. s. d. C. 1 . . 17: 15:
$$5\frac{1}{4}$$
 . . . 7

Anjw. 124:8:0 $\frac{3}{4}$

Answ. 149:00:6

**XVIII. When the price of 1 lb. weight is known, and the price or value of 1 C. (to wit 112 lb.) is required, the answer may sometimes be given more speedily than by any of the sormer Rules, by this Rule which sollows, viz. Find the number of sarthings contained in the given price of 1 lb. weight, then take twice that number of shillings, and once that number of groats, and having added them together the sum will give the value of 1 C. to wit 112 lb. weight: So it it be demanded what 1 C, or 112 lb. weight of Cheese will cost at the rate of 3 \frac{1}{4} pence the pound weight, the answer will be 1 l.10 s. 4 d.

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gain of 246 l. 18 s. 10 d.) Answer 7 l. 8 s. $1-\frac{25}{0.0}d$. First I multiply 246 l. 18 s. 10 d. by 3 (the second term) after the manner delivered in the 17 Rule of this Chapter, and write down the product which is 740 l. 16 s.6 d. Then I divide the said product by 100 (the first term in this Rule of Three) in this manner, viz. I divide 740 pounds by 100, which is personmed by cutting off towards the right hand

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the two last places of 740, so the quotient gives 7 pounds, and there will be a remainder of 40 pounds, which 40 pounds I reduce into shillings, so there will arise 800 s. to which adding the 16 s. which stand in the place of shillings, the sum will be 816 shillings; these are also to be divided by 100 (by cutting off two places as before,) so the quotient will give 8 shillings, and there will remain 16 shillings, which being reduced to pence, and unto them 6 pence being added (to wit the 6 pence which stands in the place of pence) there will arise 198 pence; these also are to be divided by 100 (by cutting off two places to the right hand as before,)

so the quotient gives I peny, and there will remain 98 pence; so the exact quotient or Answer of the question is found to be 7 l. 8 s. I = 28 d.

More Examples of this Rule are these following.

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After the same manner may this sollowing quesion and such like be resolved, viz. When 100 Ells of Linen cloth cost 30 l. 18 s.9 d. what is the price of 1 Ell? Answer 6 s. 2 d. 1 farth.

Ells

XX. When the given gain of (or allowance for) 100 Integers consists of some number of pounds not exceeding 10, together with fome Aliquot part or parts of a pound, the operation will be little different from the last mentioned Examples, as may appear by the resolution of the subsequent question, viz. What must be allowed for 2156 1. 13 s. 4 d. at the rate of 6 l. 15 s. for 100 l.? Answ. 145 l. 11 s. 6 d. thus found; first I multiply the faid 2156 l. 13 s. 4 d. by 6 (the number of pounds in the given allowance 6 l. 15 s.) after the manner of the last Examples, and subscribe the product which is 12940 l. underneath the line as you fee, then since 15 s. are equal to 1 l. together with 1 l. I take \(\frac{1}{2}\) of 2156 \(l.13\) s.4 \(d.\) which is 1078 \(l.6\) s.8 \(d.\) likewise & of the said 2156 l. 13 s. 4 d. to wit, 5391. 3 s. 4 d. and having subscribed these quotients underneath the product first found, and added them all together, I find 14557 1. 10 s. o d.for the total product, with which I proceed as in the former Examples; and so at length the Answer is found to be 145 l. 115.6 d. View diligently the operation.

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1. 1. 1. s. d. 100 .. 61 .. 2156:13 : 4 tonin (ask, tagish toning) a 61 tryle 12940:00 : 0 1078:06:8 539:03:4 1. 145 57:10:0 20 5. 1150 sids 12 iw goirron by d. 56 00

CHAP. III.

Concerning Exchanges of Coins, Weights, and Measures,

He rate or proportion between Coins, Weights, &c. of different kinds being known, either from fome good Author, or rather by experience; it will not be difficult, to fuch as understand the Rule of Three, to know how to exchange a given quanty of one kind, for a quantity of the same value in another kind. But since in some cases, the common way of working may be much contracted,

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pendious wayes to perform this business.

II. In exchanging of things of different kinds (whether they be Coins or Weights, &c.) when two things of different kinds are compared together, the question may be resolved by one single Rule of Three, as will be evident by the subsequent Examples, viz.

Quest. 1. How many Riders at 21 s. 2½ d. sterling the piece, ought to be received for 251 l. 6 s. 4½ d. of sterling money? Answer, 237 Riders. For the first and third terms in the Rule of Three, which arise from this question, being converted into half

pence, the proportion will be this,

509 . 1 : : 120633 . 237

Quest.2. If 100 Ells of Antwerp make 75 yards of London, how many yards of London measure will 27 Ells of Antwerp make? Answer 20 1/4 yards.

100 . 75 :: 27 . 20 4

III. When more than two different Coins, Weights, Measures, &c. are compared together, viz. when one kind of Coin is compared with a second of another kind; that second with a third; the third with a sourth; the fourth with a fifth, &c. two different cases are ordinarily raised from such comparison, viz.

1. How many pieces of the first Coin are equal in value to a given number of

It may be pieces of the last coin: or required to pieces of the last coin:

know.

2. How many pieces of the last Coin are equal in value to agiven number of pieces of the sirst kind of coin.

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An Example of the first case.

If 35 ells of Vienna make 24 ells at Lyons; 3 ells of Lyons 5 ells of Antwerp; and 100 ells of Antwerp 125 ells at Frankfort; how many ells of Vienna are equal unto 50 ells at Frankfort? Answer, 35 ells of Vienna.

For the more easie understanding of the resolution of this question and others of like nature, Let a represent an ell at Vienna; b an ell at Lyons; c an ell at Antwerp, and d an ell at Frankfort; then may the given terms in the question be stated in the sollowing order.

Suppositions
$$\begin{cases} 35 & a=24 & b \\ 3 & b=5 & c \\ 100 & c=125 & d \end{cases}$$
The question $50 & d=?a$

Which order of placing the said given numbers (or terms) being observed, it appears that if 35 a be accounted to stand in the first place; 24 b in the second; 3 b in the third; 5 c in the sourth; 100 c in the fifth, &c. then all the terms which stand in odd places, to wit, in the first, third, fifth, and seventh places, will necessarily fall under the first row or column on the lest hand, and all the terms which stand in even places, to wit, in the second, fourth, and sixth places, will fall under the latter column.

These things premised, all questions which fall under Case 1. before mentioned may be resolved by this Rule, viz.

Rule

Multiply all the given terms which stand in odd places (to wit, in the first column) according to the rule of continual multiplication, and reserve the last product for a dividend: Again multiply continually all the terms which stand in even places, so shall the product be a divisor, and the quotient arising from the said Dividend and Divisor shall be the answer of the question.

So in the last mentioned question, if all the numbers in the first column, to wit 35, 3, 100, and 50 be multiplyed continually; the product will be 525000 for a Dividend; also if all the numbers in the latter column, viz. 24, 5 and 125 be multiplied continually, the last product will be 15000 for a Divisor, and the quotient arising from the said Dividend and Divisor will be 35, which is the number of ells of Vienna required.

35 | 24 3 | 5 100 | 125 50 |

525000: 15000) 525000 (35

The reason of the said Rule I. will be manifest by solving the question propounded by three single Rules of three, thus,

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I. 24b. 35a:: 3b. $\frac{35 \times 3}{24}a (= 5c.$

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II. $\frac{5035 \times 3}{124} a :: \frac{100}{1} c. \frac{35 \times 3 \times 100}{5 \times 24} a (= 125d.$

III. 125 d: 35 × 3 × 100 a:: 50 d. 35 × 3 × 100 × 50 a.

wstich fourth proportional last sound, to wit, $35 \times 3 \times 100 \times 50$ being well viewed and compared with the before mentioned order of placing the terms given in the question gives the very Rule I. before express in words.

An Example of the latter of the two Cases before mentioned.

If. 10 lb. of Averdupois weight at London be equal to 9 lb. of Amsterdam; 45 lb. at Amsterdam, 49 lb. at Bruges; and 98 lb. at Bruges equal to 116 lb. at Dantzick; how many lb. of Dantzick are equal to 112 lb. of Averdupois weight at London? Answer, 129. 92 lb. of Dantzick.

That the operation may be the more clear, let a represent one pound of Averdupois weight; b one lb. of Amsterdam; e one lb. of Bruges, and d one lb. of Dantzick; then let the question be stated after the order in the first Case, viz.

Suppositions

Suppositions $\begin{cases} 10 & a = 9 & b \\ 45 & b = 49 & c \\ 98 & c = 116 & d \end{cases}$ The question 112 a = ? d

These things premised, all questions which fall under Case 2. before mentioned may be solved by this Rule, viz.

Rule II.

Multiply all the given terms which stand in even places (to wit in the latter column) and the last odd term in the first column according to the rule of continual multiplication, and reserve the last product for a Dividend; again, multiply continually the rest of the terms which stand in odd places (to wit in the first column) for a Divisor, so shall the quotient arising be the answer of the question.

Or in this latter case if you place the last of the given terms in the same column with the even terms, the rule for solving questions, which fall under the latter case will be this which solloweth,

viz.

Multiply continually all the numbers in the latter column for a Dividend; also multiply continually all the numbers in the first column for a Divisor, so shall the quotient arising be the answer of the question. Thus the answer of the last mentioned question will be found 129.92, to wit, 129 100 lb. of Dantzick, as is evident by the subsequent operation.

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The reason of the said Rule II. will be manifest by folving the question propounded, by three fingle Rules of three, thus,

II.
$$\frac{49}{1}c.\frac{45*10}{9}a::\frac{98}{1}c.\frac{45*10*98}{49*9}a (=116 d.$$

$$111.\frac{45 \times 10 \times 98}{49 \times 9} a. \frac{116}{1} d:: \frac{112}{1} a. \frac{49 \times 9 \times 116 \times 112}{45 \times 10 \times 98} d.$$

Which fourth proportional last found, to wit, 49 × 9 × 116 × 112 being well viewed and compa-45 × 10 × 98

red with the before mentioned order of placing the terms given in the question discovers the very

Rule II. before exprest in words.

Note, when the same numbers happen to be Multiplicators in the Dividend, and also in the Divisor, such Multiplicators may be cancelled in both, and thereby much labour will oftentimes be spared. Y

Such

Such which have much practice in calculating Exchanges, and do exactly know the rate or proportion between two different weights or meafures or coins, which they would compare together, may by the Rule of Three frame Tables of proportions for the more speedy reducing of a given quantity of one kind of weight, measure, &c. into a quantity of the same value in another kind of weight, &c. In the expressing of which proportions it will be very convenient that the first number or Antecedent of each proportion be made I or unity, and the second term or consequent a Decimal, or else a mixt numb r whose Fractional part is a Decimal, for then the Coin, Weight, &c. of the one place (whose term is 1) may be reduced into that of the other place, by help of those Tables and of Multiplication of Decimals without sensible error: For Example, It hath been observed by some ingenious Merchants that 100 lb. of Averdupois weight at London, are equal unto 89 lb.in Paris by the Kings beam, and consequently Tlb. Averdupois is equal to -89 lb or . 89 lb. at Paris (for if 100 give 89, then I will give . 89;) therefore any number of pounds Averdupois being multiplied by .89 (with respect unto Multiplication of Decimals, explained in the 26 Chapter of the preceding Book) will produce pounds of Paris: Again, if 89 lb. of Paris be equal to 100 lb. Averdupois, then I lb.of Paris will be near equal to 1 .1235 lb. of Averdupois; therefore any number of pounds of Paris being multiplied by 1.1235 will produce pounds Averdupois very near.

Upon this ground I have collected the proportions in the following Tables, wherein I would not have any to confide further than they shall know

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Chap.III. Weights and Measures. 347

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ATable for the Reduction of Averdupois weight at London, to the weights of divers foreign Cities and remarkable places.

-2014 ter A 124.	of mark	ngr am ma ke
		lb.
A PRODUCTION OF	Antwerp,	.9615
S. Marine	Amsterdam,	.9
M de succes	Abbeville,	.91
Secient Cont.	Ancona,	1 .282
Mary mary	Avignon,	1 .12
	Burdeaux,	.91
MARINES TO	Burgoyne,	.91
of Familia	Bollonia,	1 .25
SCHOOL DECIME	Bridges,	.98
One pound	Callabria,	1 .3698
of Averdu-	Callais,	1 .07
pois weight	Constan- (.8474
at London,	tinople, \$	Loder;
makes at	Deepe,	· .91
79.5455	Dansik,	1 .16
	Ferrara,	I -3333
	Florence,	1 .282
	Flanders ?	1 .06
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	Geneva,	.9345

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		25 C redi dr. 10
		1.16,6 will 0188.
	istm Zilell.	.07 common weight.
	Lyons,	.98 filk weight.
		.9 customers weight.
	Legborn, L	
	Millan, OI II	
	Mirandola, Norimberg,	88
	Naples, 00 1	.4084
One pound	Paris, OSE	The second secon
of Averdu-	Prague, -	.83
pois weight	Placentia, 11	3888
at London, makes at	Rotchel, I	
makes at	Rome, 1	.27
The state of the s	Rouan,	.875 by vicont.
	Disease of the second	.9017 common weight
1 700		.08
		.2195
-	7 1	.5625 Suttle.
	Venetia, }	.9433 gross.
Mary Control	Vienna,	.813
	San	10 m 10 m 17 m
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350 Of Exchanges, &c. Appendix.

The use of the preceding Table will be manifest

by the subsequent example, viz.

How much weight at Dansick do 320 lb. Averdupois make? Answer, 371.2 lb. Seek in the precedent Table for Dansick, and right against it you shall find 1.16, which shews that 1 lb. Averdupois is equal to 1.16 lb at Dansick, therefore multiply 320 by 1.16, so will the product be 371.2 lb. of Dansick, as by the Operation is manifest.

Aver. Dans. Aver. Dans. 1:1.16::320:371.2

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ATable for the Reduction of the weights of divers foreign Cities and remarkable places to Averdupois weight at London-

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The state of the s	Antwerp		1.04
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E981 . 11	Abbeville !	1 91201	1.0989
14.	Ancona	1	.78
1.1235	Avignon	20	.8928
8402.1	Burdeaux	N I	1.0989
.E.	Burgoyne	Sic	1.0989
8558:	Bollonia	dn	8 8
eig +	Bridges	rd	1.0204
8181114	Callabria	Siv sal	-73
Po	Callais	1 4	-9345
OS OF I	Deep	dumen.	1.0989
658	Danfick	do	.862
ouc.	Ferrara	207	1 -75
181	Florence	1 3	.78
. NO.	Flanders in	Phillips S	9433
	general	1 Age	1124313
00. I	Geneva	(Boroll)	1.07
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43/42	Holland	F3.154	1.0526
100	Lixborn	SALKS	1.135
	S common weight.	II TERRE	.9345
	Lyons Silk weight.	44 16	1.0204
48 69	(custom, weight		I.IIII
	Leghorn	ight	.75
	Millain	Vei	-7
One pound weight in	Mirandola	5	-75
ghi	Norimberg	odi	1.1363
vei	Naples	du	.71
Pos	Paris	The second	1.1235
nn &	Prague	123	1.2048
000	Placentia	0.4	.72
ne	Rotchel	don	.8928
90	Rome	No.	.7874
	Sby Vicont,	CTI's	1.1428
245	Rouans	Sa	
1 680	Sivill Commonweight.	- Ke	1.1089
52	Tholousa	Dank	.9259
7	Turin	Eerran	.8928
, 8	Cfuttle,	nerol 3	.64
433	Venetia)	Sur 1.1	.04
	2gross,	Renera	1.06
7	Vienna	12311317	1 22
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		Cenous	1.207.63
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		2112121	-

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Chap. III. Weights and Measures. 452

The use of the last mentioned Table, will be manifest by this example, viz.

In 224 lb. weight at Hamburg, how many pounds
Averdupois?

Answ. 243.376 lb.

Higi &

Seek in the Table for Hamburg, and right against it you will find 1.0865, which sheweth that 1 lb.of Hamburg makes 1.0865 lb. Averdupois; therefore if 1.0865 be multiplied by 224 the product will be pounds Averdupois.

Jorimberg 1 ... 1 .0865 ... 224 224 43460 21730 Vienus 21730 **然为好这样** 243 3760 Lions! Callais Feniece, TanbahT Elorence Braces Millon Legborn Maderd

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A Table for the Reduction of English Ells to the Measures of divers fo-reign Cities, and remarkable places.

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1 1 1501	Amsterdam	1.6949	bod With uny
intida :	Antwerp	1.6666	
Dibbot	Bridges	1.64	a .osos hen
The state of	Arras	1.65	
No. of the last of	Norimberg	1.74	
100	Colen	2.08	Ells
at	Lifle	1.66	
S	Maffrich	1.57	-
lak	Frankford	2.0866	
=	Danfick	1.3833	The state of
at London, makes	Vienna	1.45	
nd	Paris	.95	
Lo	Rouan	1.03	
34	Lions	1.0166	Aulnes.
	Callais	1.57	
One ell	1 Pline	1,8, 1	
On	Venice Sline	7.06	
	2		1184 1.
Carlotte and	Lucques	2.	
	Florence	2.04	Braces
	Millan	2.3	1100-1
	Legborn	2.	
	Madera }	1.0328	
	Isles \$	3	
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s at	Sivil Lisbone	1.35	ात रेजारेश
nako	Castilia	1.3875	Vares
n n	Andoluzia	1.3625	3,40,345,4
мори	Granado	1.3625)	Dalma
Lon	Genoa Saragofa	4.8083	Palms
at	Rome	.55	
EII	Barselona	.7125	Canes
One	Valentia	1.2125	ए' त्रिशंब ए' त्रिशंब
-	L PRINCE	The second is	CONTRACTOR OF THE PARTY OF THE

The use of the aforesaid Table will be manifest by the subsequent example, viz.

In 325 ells of London, how many ells at Antwerp?
Answ. 541.645 ells: Seek in the Table for Antwerp, and right against it you shall find 1.6666 which being multiplied by 325 produceth 541.645 ells of Antwerp, as by the operation is manifest.

 A Table for the Reduction of the Measures of divers foreign Cities, and remarkable places to English Ells.

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1		Amfterdam ?	* Ffelia	59	
	at	Antwerp ?	A 500 500	.6	3
-	EII	Bridges 191	Selona	.6097	
1	ne I	Arras 2515.1	entra de c	606	3
1	o -	Norimberg	-	.5747	-
-	1	Colen	34084	.4807	10
11	lla sa	Lifte 111W Sids 1	e atoreian	.6024	*
		Mastrich	nt examp	.6369	ris ye
3	at	Frankford	H women	.4792	91
	ala.	Danfick	don	.7228	The same
0	A	Vienna	0000	.6896	S
2	ne (Paris Porq 758	a panatri	1.0526	E
B	0	Rouan	Sales	.9708	O. SIT
1		Lions	32	.9836	100
	at	Callais	E .	6369	100
K	One Brace at	Venice Slinen	75.0	-5555	1000
K	3ra) 21114.	8223	.5102	
R	le I	Lucques	22222	-5	A THE
8	0 (Florence	80004	.4901	
1) Millan	103	-4347	Ser Ser
1		Leghorn	1 4 1 645U	1.5	2 33
7		Madera Isles		1.9681	No. 19
	Maria Company				

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One	Palm at Genoa	Sat	1.8181	Ells
nucand	Rome Barfelona	make	1.7857	Tap o
e Co	(Valentia	ne Tables and	.8247	erisla
O	Cardina .	1000	dern.	on birt

The use of the said Table will be manisest by the subsequent example, viz.

In 730 Aulnes at Lions, how many ells at Lon-

don?

Sinil

Answ. 718.028. Seek in the Table for Lions, and right against it you shall find .9836, which being multiplied by 730 produceth 718.028 ells of London, as by the operation is manisest.

358 Exchanges of Coins, &c. Appendix.

Note, that one and the same kind of Weight or Measure doth seldom or never alter from its peculiar quantity, in the Kingdom or Common wealth, where such weight or measure was first established; but one and the same kind of money doth often rise and fall in its value in foreign parts: for which cause I have spared the pains of calculating Decimal Tables for Coins, yet to give some light to such as read modern relations, and want experimental knowledge in this matter I shall here insert a Table, in the same estate as I find it in the aforesaid Map of Commerce, and refer the Reader, for surther satisfaction, to the Tables in Riders Distionary, concerning Coins, Weights, and Measures, both ancient and modern.

The ide of the faid Table will be manifelt by the

ing a Anines at Liour, how many clear Lon

Antic. 718.028. Seek in the Table for Land, and

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Of Exchanges of London, with divers foreign Cities.

Pence

Placentia sterl. for 64 Crown 64 Crown for Lyons Rome 66 for Ducat 65 Crown Genoa 641 for 1 Millan Crown 50 for Ducat Venice 53 2 for I Ducaton Florence Ducat Naples for 50 Lecchia in & for Ducat Callabria for I Ducat Barri 572 for I Ducat < Palermo 561 for I Ducat Mesina (hill. Antwerp 1 l.fterl. flem. & Colen Ducat Valentia Ducat Saragosa Barfelona 64 Ducat Ducat Lixborn for 1 Ducaton 53 2 Bollonia I Ducaton Bergamo Florin 59= for Frankfort for Crown Genoa

London

459 Questions of Tare, Appendix.

Lendon exchangeth in the denomination of pence sterling with all other Countries, Antwerp and those neighbouring Countries of Flanders and Holland excepted, with which it exchangeth by the entire pound of 20 shillings English (or sterling.)

CHAP. IV.

Practical Questions about various things; viz. Tare, Tret, Loss, Gain, Barter, Fractorship, and Measuring of Tapestry.

of abatements and allowances in Traffick, viz. 1. Of Tare. In the trade of Merchandize there are in use various allowances, and abatements, known by the names of Tare, Tret, &c. concerning which I shall give a few examples, whereby

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II.

the practical Arithmetician will easily see, that there is more difficulty in the name than in the thing; for the rate, or proportion agreed upon, in any allowance or abatement (be it called by what name soever) being once known, the Arithmetical work will quickly be dispatcht by the Rule of Three, or else by that and some of the former rules mixtly used, as will partly appear by the sollowing questions.

Gross weight is compesed of the neat weight of the commodity, and also of the Tare, to wit, the Chest, Bag, But, Gree which containeth the commodity.

Quest. I. A Factor buyeth 4 Chests of Sugar marked A.B.C.D. The gross weight of each Chest in Ave. dupois greater weight is as

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C. C. q. Ib).
A. 11 1 15	9
B 10 3 20)
C. 11 2 13	
D. 1 10 17	

The total grofs weight 44 ... 1 ... 13

Now supposing the Tare or weight of each Chest, when it is empty, to be 37 lb. the question is what neat weight of Sugar will remain, when the total Tare is subtracted? Answ. 43 G. oq. 4 lb.

from 44 . 1 . 13 the total gross weight Subtr. 1 . 1 . 08 the total Tare.

Rem. 43 .. 0 :. 05 the neat weight of sug.

Quest. 2. If from 990 C. 3 qu. 21 lb. gross weight, Tare is to be subtracted after the rate of 14 lb. per C. (or 112 lb.) of gross weight, how many C. neat will remain? Answ. 867 C. 0 qu. 7 3 lb.

I. The gross weight being converted into pounds by the 6th. rule of the 7th. Chapter of the preceding Book, will give 110985 lb.

II. Then by the Rule of Three.

or 8 . 1 :: 110985 : 13873 \$

sin 2012:401.001 III. From

III. From 110985 the gross weight: Subtr. 13873 the total Tare.

C. qu. lb.
Rest neat 971112=867..0..73

Note, when the number of lb.to be abated per C. for Tare, is an aliquot part of 112, as in the last mentioned example, where 14 = \frac{1}{8} of 112, the operation may be thus;

C. C. C. q. lb. C. qn lb. $1 \cdot \frac{1}{8} :: 990 : 3 : 21 \cdot (123 : 3 : 13\frac{1}{8})$

 $\begin{cases}
990 \text{ c.=} 123 : 3 : 00 \\
3 \text{ q'=} 00 : 0 : 10\frac{4}{8} \\
21 \text{ lb} = 00 : 0 : 02\frac{5}{8}
\end{cases}$

Total Tare 123: 3: 13\frac{1}{8}

Kest neat 867: 0: 07\frac{1}{8}

Quest. 3. Suppose at some City, there is of Tret. a custom in selling of certain Merchandize by weight, to allow or cast in as an overplus to the buyer, 4 lb. weight for every 100 lb. weight that is bought, and in that proportion for a greater or lesser quantity. Now if a Merchant buy 1175 lb. weight of some commodity, and is to be allowed thereupon after the aforesaid rate, the question is, how many lb. weight ought he to receive in all? Answ. 1222 lb. weight.

100.104::1175.1222

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This kind of allowance is commonly called Tret Quest. 4. Suppose a Merchant hath 1222 lb. weight of a certain commodity, part whereof he bought at a certain rate per lb. and the rest was allowed to him or cast in as an overplus, after the rate of 4 lb. weight for every 100 lb. weight which he bought; the question is, to know how many pounds neat weight he bought? Answ. 1175 lb. weight.

104. 100:: 1222. 1175

This question is the converse of the former, and

sheweth how to make abatement for Tret.

Quest. 5. If from 55 C. 1 qu. of gross weight, Tare is to be subtracted after the rate of 16 lb. per C. and from the remainder Tret is to be abated after the rate of 4 lb. per 104 lb. the question is, what the neat weight is worth in money after the rate of 8 l.8s. for every C. (or 112 lb?) Answ. 382 \frac{1}{2} l.

I. The gross weight in lb. is 6188 l.

II 112 . 16 :: 6188 . 884

or 7 . 1 :: 6188 . 884

III. 6188--884=5304

IV. 104. 100 :: 5304 . 5100

V. 112 . 82 :: 5100 . 3822

Quest. 6, A Merchant hath bought of loss and Linen cloth at 11 s. per ell, which pro- gain. ving worse than he expected, he is willing to sell it at such a price that he may lose precisely after the rate of 1 \frac{2}{3} l. for every 20 l. that he laid out; the question is to know at what price he eught to sell the ell, that the proportion in the

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faid

364 Of Loss, and Gain, Appendix. faid loss may be observed? Answ. 10 s. 1 d. per ell.

I. $20-1\frac{2}{3}=18\frac{1}{3}$ II. $20\cdot 18\frac{1}{3}$: 11: $10\frac{1}{2}$ pence

Otherwise,

I. 20 · 1 $\frac{1}{3}$:: 11 · $\frac{11}{12}$ II. 11 — $\frac{11}{12}$ = 10 $\frac{1}{12}$

Quest. 7. If 100 lb. weight of any commodity cost 30 s. at what price must 1 lb. weight of that commodity be sold to gain after the rate of 10 l. for every 100 laid out? Answ. 3 24 d. per lb. weight.

I. 100.110 :: 30.33II. $100.33 :: 1.\frac{31}{100}s$. (or $3\frac{24}{25}d$.)

Quest. 8. A Merchant selleth a parcel of Jewels which cost him 250 l. ready money, for 559 l. payable at the end of 6 moneths; the question is (his security being supposed to be good) what his gain was worth in ready money upon rebate of interest at the rate of 6 l. for 100 l. for an year? Answ. 300l.

559-250 = 309 103 · 100:: 309 · 300

Quest. 9. How much Sugar at 8 d. per of Barter. 1b. weight may be bought for 20 G. of Tobacco at 3 l.per C.? Answ. 1800 lb. weight of Sugar.

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Quest. 10 A. hath 100 pieces of Silks, which are worth but 3 1. per piece in ready money, yet he barters them with B. at 4 lb. per piece, and at that rate takes their value of B. in Wools at 7 1. 100. per C. which are worth but 6 l. per C. in ready money, the question is to know what quantity of Wools payes for the Silks, and which of the two A. or B. is the gainer, and how much? Answ. \$3 \$ C. of Wools payes for the Silks, and A. gaineth 20 1. by the barter. A se boulev zew salvest enofo

7 2. 1 :: 400. 53 3 3 5 6 1 00 1 5 5 miles. $\begin{cases} 1 & .6:: 53\frac{1}{3}. 320 \\ or 7\frac{1}{2}. 6:: 400. 320 \end{cases}$

So it is evident that the true worth of the Wool which B. delivered was 320 1. for which he received only of A. the worth of 300 l. in Silks, and therefore B. lofeth 201. by the birter.

Quest. 11. A Merchant delivered to his Factor

600 l. upon condition that if the Factor add to it 250 1. of his own money, and bestow his pains in managing the whole flock, he Thall then have 3 parts of the total gain. The question is to know what stock the Factors service was estimated at? Answ. 150 l.

Of Factor (hip. See brief rutes for computing of Factors allowances in the 19 and 20 rules of the second chapter of this Appen-

I. The Faffors part of the gain being 3, the Merchant must necessarily have the remainder, which

length, hath such proportion to IS 3. 3 . 3 :: 600 . 400 III. 400 - 250 = 150 Z 3

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Quest. 12. A Merchant delivereth to his Factor 320 1. and permitteth him to add to it 64 1. of his own money, to be employed in traffick; and by agreement between them the Factors fervice is estimated equivalent to a certain stock; which is such, that if the total gain be divided proportionably according to those three stocks, the Factor is to receive ; of the total gain, in consideration of the faid imaginary flock (being the value of his fervice;) the question is to know the full part of the gain belonging to each, and what stock the Factors service was valued at? Answ. the Merchant of the gain, and the Factor 1, whose service was valued at 96 l. stock.

320 + 64 = 384 \$. 1::384.96. 0071000320 - III. 64 320.

Quest. 13. If a piece of Arras hangings, in the form of a long square, hath for its length 64 yards English, and breadth Of Measuring of Tupe Stry 4 yards; how many square ells, or flicks Flemish are contained in that piece, when the length of a Flemish ell is equal to 3 yard English? Answer, 44 & square ells or flicks Flemish.

Forasmuch as by supposition, a Flemish ell in length, hath such proportion to an English yard in length, as 3 to 4, and consequently the square of the one to the square of the other, as 9 to 16.

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Therefore in a direct proportion, as 9 is to 16; so is any given number of square yards English to a number of square ells Flemish, which will take up equal space with the said square ells English. Also in a direct proportion, as 16 is to 9, so is any given number of square ells Flemish to a number of square yards English, which will take up an equal space with the said Flemish ells: therefore to resolve the aforesaid question, first find the number of square yards English contained in the said piece of Arras, by multiplying the length and breadth in yards mutually one by the other, then proceed according to the aforesaid proportion; so the work will stand thus,

I. 6\frac{1}{4} \times 4 = 25 square yards English.

II. 9.16::25.44\frac{4}{5} square ells Flemish.

Otherw se,

6 4 yards English in length give 38 1 length. by the Rule of Three in Flemish ells 3 1 length.

Also 4 yards English give in Fle. 5 \frac{1}{3} breadth.

Therefore the product of the said

8 \frac{1}{3} \text{ multiplyed by \$\frac{1}{3}\$, gives for the superficial content as before }

44 \frac{4}{9}

Quest. 14. If a piece of Tapettry in the form of a long square be in length 15 \(\frac{1}{4}\) ells Flemish, and in breadth 4\(\frac{1}{3}\) ells Flemish, how many square yards English are contained in that piece, when 4 ells Flemish in length are equal to 3 yards English? Answ. 37\(\frac{1}{64}\) square yards English.

I. $15\frac{1}{4} \times 4\frac{1}{3} = 66\frac{1}{12}$.

II. $16 \cdot 9 :: 66\frac{1}{12} \cdot 37\frac{11}{64}$.

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CHAP.

Concerning the Interest of Money, and the Construction of Tables to that purpose.

I. N resolving questions concerning interest of money, four things are to be well observed, to wit, first, the Principal, or money lent for gain or interest; secondly, the time for which the faid Principal is lent; thirdly, the rate or proportion which the Principal bears to the fum of the principal and interest; and fourthly the interest it self: So if 100 l. be lent upon condition that 106 l. shall be repaid at the end of a year, the faid 100 1. is called Principal; the time for which the faid principal is lent is one year; the proportion which the principal bears to the fum of the principal and interest is such as 100 hath to 106; lastly, the intereft it self is 6 l.

Il. Interest is either Simple or Compound.

III. Simple Interest is that which ariseth or is computed from the principal only: So if 100 1. be lent for two years, the simple Interest thereof after the rate of 6 pounds for 100 pounds for 1 year will be 12 pounds, viz. 6 pounds due at the first years end, and 6 pounds due at the second years end.

IV. Compound Interest is that which ariseth from the principal, and also from the interest thereof, and therefore it is called interest upon interest: So if roopounds be lent and forborn 3 years 'and compound interest thereof is to be com-

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(DO)puted puted after the rate of 6 pounds for 100 l. for one year; there will arise besides the simple interest of the principal for three years, the interest of 6 pounds (due at the first years end) for 2 years, and the interest of 6 pound (due at the second years end)

for one year following.

V. Rebate or discompt of money is, when a sum of money due at any time to come, is satisfied by the payment of fo much present money, which if it were put forth at a certain rate of interest for the faid time, would become equal to the fum first due: So if 100 pounds be due at the end of two years, and is to be satisfied by the payment of present money upon rebate, after the rate of 6 pounds per centum, per annum, simple interest, there ought to be fo much ready money paid, which in two years after the said rate of interest would be augmented unto 100 l. In like manner if the rebate or difcompt were to be made after any rate of compound interest, so much ready money ought to be paid, which at such rate of compound interest, for the time agreed on would become equal to the fum first due Examples of the manner of computation by rebate may be feen in the tenth and fourteenth Rules of this Chapter.

VI. In the taking of interest, or use money, for

the loan or forbearance of money lent, respect must be had to the rate limited by Act of Parliament, which now restraineth all persons from taking more than 6 l. for the interest or use of 100 l. lent for a year , but grounded. what part of 6 l. may be taken for

The foundation upon which the Miles for computing simple interest are

the interest of 100 l. lent for half a year, a quarter

of a year, a moneth, or any other part of a year, is not exprest in the Act; In this case therefore we must observe custom and daily practice, so we shall find that 3 l. is usually taken for half a years interest of 100 l. and 30 s. for a quarter of a year, &c. by which practice, this following Analogy (which is the ground or reason of the common sules for computing simple interest) seems to be assumed for a safe exposition of the Statute, viz. That fuch proportion as the whole year (supposed to confist of 305 dayes) hath to any propounded space of time more or less than a year, such proportion any interest (not exceeding the rate limited by the Act) for any Principal lent for a year, ought to have to the interest of the same Principal for the time propounded: This Analogy being granted, the manner of computing simple interest, for any Principal lent and forborn any time propounded, will be such as is exprest in the two next Sections.

Interest.

vII. The interest or gain of 100 l. principal money forborn for a year being known, the interest of any other principal money for the same time may be found out by one single Rule of Three; for as 100 l. principal is in proportion to the interest thereof, so is any other principal to its interest: So if it be demanded what 270 l. will gain in a year at the rate of 6 l. for 100 l. for one year, the Answer will be found to be 16 l. 4s. For,

1. 1. 1. 1. 1. 1. 5. d.
100 . 6::270 . 16, 2 (or 16:4:0

A second Example, What is the interest of 175 l.
18 s. 11 d. for a year, at the rate of 6 l. for 100 l.
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for a year? Answ. 101.11 s. 1-62 d. as by the following operation (which is performed after the practical manner delivered in the nineteenth Rule of the second Chapter of this Appendix) is evident

1. 1. 1. s. d. 1. s. d.

100.6:: 175: 18: 11 (10:11:1762

multiply by .. 6

1..... 10 55 : 13 : 6

s. 11 13

d. 1 62

VIII. If the interest of 100 1. principal for one whole year, or 365 dayes be known, the simple interest of any other principal, for any number of dayes more or less than 365, may be found out by the following Rule, viz.

Multiply these three numbers according to the

Rule of continual Multiplication, to wit, the given interest of 100 l. for a year, the principal, whose interest is required, and the number of dayes prescribed, reserving the last product for a Dividend: Also mul-

A Rule for computing simple interest for any number of dayes.

tiply 365 by 100 and reserve this product for a Divisor; Lastly finish Division, so shall the quotient be the interest or gain sought.

Note here, that the two principals, to wit 100 l.
and the other propounded, are supposed to be of
one and the same denomination: Also the interest
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required will be of the same denomination with

the given interest of 100 %.

For an example of this Rule, let it be required to find out the interest of 400 l. for a week, or 7 dayes at the rate of 6 1. for 1001. for a year, or 365 dayes; First multiplying these three numbers 6, 4000, and 7 continually (viz. multiplying 6 by 400. and the product thence ariling by 7) the last product will be 16800 for a Dividend; also multiplying 365 by 100, the product is 36500 for a Divifor; laftly, dividing 16800 by 36500 (after cyphers at pleasure are added to 16800) the quotient (according to the fourth Rule of the 27th. Chapter of the preceding Book) will be discovered to be this decimal .4602, which is equal to 9 s. 2 d. I farth. (as will appear by the brief way of valuing a decimal fraction in the fourth Rule of the 26th. Chapter. Jonal ad saveb 205 to my along

The reason of the above mentioned rule for the computing of interest for dayes, will be manifest by this following way of solving the same question

by two fingle Rules of Three, viz.

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I.
$$100.6:1400.\frac{6 \times 400}{100}$$

II. $\frac{365}{100}.\frac{6 \times 400}{100}:\frac{7.6 \times 400 \times 7}{1.365 \times 100}$

Which fourth proportional in the latter Rule of Three, to wit, $\frac{6 \times 400 \times 7}{365 \times 100}$, being well viewed the truth of the rule before delivered will be manifest.

Hence one vulgar errour in computing interest

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is discovered, for some argue thus, 61. is the interest of 1001. for a year, therefore 101. (or $\frac{1}{12}$ of 61.) is the interest for a moneth, and consequently 21.6 d. for a week or seven dayes, and so the interest of 4001. for 7 dayes, computed after that manner would be 105. which exceeds the Answer sound by the preceding Rule by $9\frac{3}{4}$ d. very near, which fallacy hath its rise from the taking, (or rather mistaking) of 28 dayes for $\frac{1}{12}$ part of the number of dayes in a year, when indeed the just $\frac{1}{12}$ part of 365 dayes consists of 30 $\frac{1}{12}$ dayes.

Moreover, by the help of this decimal fraction

of a pound, to wit, .000164383, which is very near the interest of one pound for a day at the rate of 6 per cent.per annum (as will appear by the preceding rule) the interest of

Auother Rule for computing fimple Interest for dayes.

any principal (supposed to be pounds or decimal parts of a pound) for any number of dayes propounded, at the said rate of interest, may be found out by multiplication only, viz. First multiply the faid decimal .000164383 by the principal whose interest is required, then multiply that product by the number of dayes propounded, so thall this last product be the interest required; (but in these multiplications respect must be had to the cutting off of places in the products, according to the second and third rules of the 26th. Chapter of the preceding Book;) for example, if it be required to find the interest of 1000 1.for 131 dayes, at the rate of 6 per cent. per ann. the Ans. will be found 21.534 t, or 21 l. 10 s. 8 d. t for according to the rule last given.

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.000164383 x 1000 x 131 = 21.534 t

Interest.

But at another rate of interest, a peculiar decimal instead of the said .000164383 (which serves only for 6 per cent. per annum) must be found out by the first rule aforegoing, before the latter rule can take place, the reason of which latter rule doth also evidently arise from two single rules of three.

IX. When an Annuity payable yearly is in ar-

The manner of fumming up Annuities in arrear with allowances of fimple interest.

rear for any number of years, and it is required to know what the same will amount unto, simple interest being computed for each particular yearly payment, from the time it became due, until the end of the term of years, the work will be as in this

following example, viz. If an Annuity, or yearly rent of 134 l. 10 s. 6 d. be all forborn till the end of 4 years, what will it then amount unto, simple interest being allowed at the rate of 6 per cent. per annum for each years rent, from the time on which it was due, until the end of the said term of sour

years? Answ. 586 l. 105. 6 - 26 d.

It is evident by the question, that at the rate of interest propounded, there must be computed the interest of 134 l. 10 s. 6 d. (due at the third years end) for one year (to wit, the sourth year;) also the interest of the like sum due at the second years end, for two years (to wit, the third and sourth years;) likewise the interest of the same sum due at the first years end, for three years (to wit, the second, third and sourth years:) all which interest being added to the sum of the sour years rent, the total sum will shew what the said Annuity will amount

Chap. V. Interest. 375; mount unto at the end of the said term of 4 years.

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The interest of 134 1.51 is... 8:1:5.16

10 s.6 d. at 6 per cent. per 2 is... 16:2:10.32

annum, for 3 is... 24:4: 3.48

The sum of the 4 years

rent (to wit, 4 times is... 538:2:0

134 l. 10 s. 6 d.)

All which added together give the Answer of the question, to wit,

X. When it is required to find out how much ready money will satisfie a Debt due at the end of any space of time to of rebate or

at the end of any space of time to discompt of come, by rebating or discompting at money at simagiven rate of simple interest, it may ple interest.

be effected by this rule, viz. First find out the interest of 100 l. at the given rate of interest, sor the time which the ready money is to be paid beforehand, then adding the interest so found to 100 l. make alwayes the sum of that addition the first term in a rule of three; 100 l. the second term; and the debt propounded to be satisfied the third term; lastly, the sourth proportional sound out by the said Rule of Three shall be the ready money which ought to be paid in satisfaction of the debt propounded.

Example 1. If a debt of 100 l. be payable at the end of a year to come, how much ready money will discharge that debt by rebating or discompting at the rate of 6 per cent. per annum? Answ.94 l.

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106. 100::100, 94.3396+

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That is to fay, if 106 l. (which is compos'd of 100l. principal and 6 l. interest) proceeds from 100 l. principal forborn for a year, from what principal forborn for a year doth 100 l. (compos'd of principal and interest) proceed from? Answ. 94.3396 l. t (or 94 l. 6 s. $9\frac{1}{2}$ d. very near) principal money: therefore $94 l. 6 s. 9\frac{1}{2}$ d. in ready money, is of equal value with 100 l. due at the end of a year to come; for if the said $94 l. 6 s. 9\frac{1}{2}$ d. be put forth at interest for a year, at the rate of 6 per cent. per annum, it will gain $5 l. 13 s. 2\frac{1}{2}$ d. very near, which together with the said $94 l. 6 s. 9\frac{1}{2}$ d. makes the 100 l. the debt first propounded to be discharged by rebate.

Example 2. If 150 l. 10 s. be payable at the end of 73 dayes to come, how much present money will discharge the said debt, by rebating after the rate of 6 per cent. per annum? Answ. 148 l. 14s. 3 ½ d. + as by the following operation is manifest.

dayes 1. dayes 1. I. 365.6:: 73.1.2

1. 1. i. 1.

II. 101.2. 100:: 150.5. 148.7154†

That is to fay, First I seek by a single Kule of Three the interest of 100 l. for 73 dayes, at the rate of interest propounded, saying if 365 dayes (or a year) gain 6 l. what will 73 dayes gain? Answ. 172 l. or 1.2 l. Then adding the said 1.2 to 100, I say, by

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by a second Rule of Three, if 101.2 1. principal and interest, payable at the end of 73 dayes to come, be equivalent to 100 l. ready money, what ready money is 1501. 10 s. (or 150.5) payable at the end of 73 dayes to come equivalent unto? fo by multiplying and dividing (according to the rules of Decimal Multiplication and Division explained in Chapter 26 and 27 of the preceding Book) the quotient or answer of the question will befound 148.7154 +, that is, 1481. 145. 31d. + for the decimal .7154 being valued according to the brief way at the end of the fourth rule of the 26th Chapter, will by inspection only be discovered to be 14 s. 3 2 d. which rule I shall here once for all, advise the Learner to be well acquainted

The proof.

Seek (by the Rule of Three) what the ready money found as aforesaid will gain, in so much time as it is paid before hand at the rate of interest propounded; then having added this gain to the faid ready mony, if the fum be equal to the debt first propounded to be fatisfied by rebate, the ready money was rightly found out. So the last example will be thus proved.

> 1. 1001 1. 601 1. 611 1. 18 100 , 1.2 : : 148.7154 . (1.7845

Which fourth proportional 1.7845 being added to 148.7154, the sum will be 150.4999 t, which doth not want a farthing of 150 l. 10 s. the debt first propounded.

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of the present worth of an Annuity, by rebating or discompting at a given rate of simple interest, the operation will be as in the following example, viz. How much present money is equivalent to an Annuity or rent of 100 l.

per annum to continue five years, rebate being made at the rate of 6 l. for 100 l. for one year, at simple interest? Answ. 425 l. 18 s. $9\frac{1}{2}$ d. very near.

It is manifest that there must be computed the present worth of 100 l. due at the first years end; also the present worth of 100 l. due at the second years end, and in like manner for the third, fourth and fifth years; all which particular present worths being added together, the agreggate or sum will be the total present worth of the Annuity, to wit 8286150

in the example above propounded, 425 88212671.

that is, 425 l. 18 s. 91 d. very near.

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The operation by decimals (which will come near enough to the truth) will be as followeth viz.

l. l. l. l.

1. | 106 . 100::100 . 94,33962 †

2. | 112 . 100::100 . 89,28571 †

3. | 118 . 100::100 . 84,74576 †

4. | 124 . 100::100 . 80,64516 †

5. | 130 . 100::100 . 76,92307 †

Answ: 425,93933 +

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Here by the way, from the manner of resolving the last mentioned question, rhat Rule commonly called Equation of payments, which is insisted on by divers Arithmetical Writers, will be sound errone-

ous, which I thus prove.

dayes of payment, upon which particular sums of money are due, unto a mean time upon which the aggregate or total of those particular sums ought to be paid, without damage to the Debitor or Creditor, there must be necessarily some rate of interest implied; for otherwise why may not any day at pleasure be assigned for one intire payment.

2. If some rate of interest be implied, then equity requires that the present worth of the total sum payable at one entire payment, rebate or discompt being made according to that rate of interest, may be equal to the sum of the present worths of the particular sums of money, rebate being made at

the same rate of interest.

3. In regard the said Rule doth mention no particular rate of Interest, it ought to be true at any

rate of interest whatsoever.

4. Let us therefore examine the said Rule according to the rate of 6 per centum, per annum, simple interest, by taking the last mentioned question for an example, which (according to the accustomed manner) will be thus stated, viz. If 500l. ought to be paid by five equal yearly payments, to wit, 100l. at each years end, what time ought to be given for the payment of the said 500 l. at one entire payment, without loss either to the Debitor or Creditor.

5. By proceeding according to the faid rule of Equation of payments (which faith, If the sum of the A2 2 products

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products, ariling from the multiplication of each particular fum of money by its respective time, be divided by the fum or aggregate of the faid particular sums of money, the quotient will be the mean time to be affigned for one intire payment) there will be found three years, which time (according to the said rule)ought to be given for the payment

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of the whole 500 1.

6. Now it 500 1. due at the end of three years to come be worth as much in present money, as is the present worth of an Annuity of 100 l. to continue five years, then the faid Rule of Equation is true; otherwise false; but the present worth of 500l.due at the end of three years to come, rebate being made at the rate of 6 per centum, per annum, simple interest, will be found (by the tenth rule of this Chapter) to be 423 1.14 s. 6 d. 3 f. very near; also the prefent worth of the faid Annuity, rebate being made as before, is found (as appeareth by the resolution of the last mentioned quettion) to be 425 1. 18 s, 91 d. very near; wherefore it is evident that the Creditor lofeth 21.45.23d. very near, by receiving the whole 500l. at three years end: moreover at 6 percentum, per annum, compound interest, he would lose 11.85.6 d. very near, as will be manifest by the Tables of compound interest hereaster expressed: so that the loss will be either more or less according as the rate of interest doth differ; and therefore I conclude the faid Rule (as also all other rules or resolutions of questions which have dependance thereon) to be erroneous.

Although questions of this nature seldom come into practice, yet he that will take the pains, may find out such a mean time as is required by the said Rule

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Rule of Equation of payments, at any rate of simple

interest by this following rule, viz.

First, by the preceding tenth Rule of this Chapter find out the present worth of every particular furn in the question payable at a time to come, by rebating at the rate of interest agreed on; then find in what time the fum of those present worths will be augmented unto the total of all the particular furns payable at times to come, according to the first agreement, so shall the time found out be the mean time for the payment of the whole debt : thus the mean or equated time in the last example will be found to be 2.8979, &c. years (not three years, as the faid Rule of Equation of payments would have it) for by rebating at 6 per cen. per annum, simple interest, 500 l. payable at the end of 2.8979 &c. years to come (that is 2 years and 328 dayes very near) is worth in ready money 425 1. 18 s.of divery near, and the fame ready money is also the present value of 100 l. Annuity for 5 years, at the fame rate of interest, as before hath been manifested. But to return to the path from which I have made a digression.

From the preceding tenth rule of this Chapter the following Tables I. and II. are deduced, whose

construction and use are afterwards declared.

sight againfi the sumpers of years 1,2,3,4,5,6,and Transdecimal fractions, one pound of English money being the lureger, and are time found (accor-

ding to the preceding reach Rule or this Chapter)

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Years	Table I. Which sheweth in decimal parts of a pound, the present worth of one pound due at the end of any number of years to come, not exceeding 7 years, at the rate of 6 per centum, per annum, simple interest.	Years	Table II. Which sheweth in pounds and decimal parts of a pound, the present worth of one pound Annuity, to continue any number of years not exceeding 7, at the rate of 6 percentum, per annum, simple interest.
I 2 3 4 5 6 7	.847457	1 2 3 4 5 6 7	4 - 259393

The Construction of Table I.

The numbers in the first Table which are placed right against the numbers of years 1,2,3,4,5,6,and 7, are decimal fractions, one pound of English money being the Integer, and are thus found (according to the preceding tenth Rule of this Chapter)

106 . 100 :: 1 . ,943396 † 112 . 100 :: 1 . ,892857 † 118 . 100 :: 1 . ,847457 †

whereby

whereby it appears, that 11. due at the end of a year to come, is worth in ready money .943396 +, that is, 18 s. 10 d. 1 f. and somewhat more. Also 11. due at the end of two years to come, is worth in ready money .892857 +, or 17 s. 10 d. rebate being made at the rate of 6 per centum, per annum, simple interest the like is to be understood of the rest of the numbers in Table I. which may be continued to more years, and other Tables also of rebate may be framed upon the same ground, for moneths, or dayes, by the ingenious Artist.

The use of Table I.

The practical use of the said first Table will be manifest by solving this sollowing question; viz. How much ready money will discharge 345 l. 15 s. 6d. due at the end of five years to come, by rebating simple interest at the rate of 6 per centum, per annum Answer, 265 l. 19 s. 7½ d. which is thus found out; viz. In the preceding Table I. right against 5 years, I find the decimal .76923, which shews that 1l. due at the end of five years to come is worth in ready money .76923 (that is, 15 s. 4½ d.) then instead of 15 s. 6 d. mentioned in the question propounded, taking the decimal .775 which is equal to 15 s. 6 d. (the same being reduced according to the fifth rule of the 23 chapter of the preceding book) I say, by the Rule of Three.

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1. ,76923:: 345.775. (265.9805 †
That is to fay if 1 l. give.76923 l. what will 345.775 l. give? Answ.265.9805 l. tor multiplying 345.775 by .76923, according to the second Rule of the 26 Chapter of the preceding Book, the product will be 265.9805, that is, 265 l. 19 c. 7 d.

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The Construction of Table II.

The numbers in the second Table are found out by the addition of those in the first, viz the first number in the latter Table is the same with the first number in the former, the second in the latter is the fum of the first and second in the former; the third in the latter is the fum of the first, second and third in the former, and in that manner the rest are found ; (the reason of which composition is manifest from the example of the eleventh rule aforegoing;) otherwise, the numbers in Table II.may be found more easily thus, viz. the first number in the faid Table II. is the same with the first number in Table I. the second number in the latter Table is compos'd of the second number in the former and the first in the latter, the third number in the latter Table is compos'd of the third number in the former and the second in the latter, the fourth in the latter is compos'd of the fourth in the former and the third in the latter; the like is to be understood of the rest of the numbers in Table II. which might be continued to more years, and fitted to other rates of interest, but I shall spare that labour, in regard a more equal way of finding out the present worth of an Annuity, agreeable to the accustomed and practical rates of buying and felling Annuities or Rents, for terms of years, is grounded upon a computation of interest upon interest, as will hereafter be made manifest, for at simple interest an Annuity will be overvalued.

The use of Table. II.

The use of Table II. will appear by this follow-

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ing example; viz. What is the present worth of an Annuity of 100 l. per annum payable yearly during the term of five years, discompt or rebate being made at the rate of 6 per centum, per annum, simple interest? Answer, 425 l. 18 s. 9½ d. very near which is thus found out, viz. In the preceding Table II. right against five years, I find this number 4.259393, which shews that an Annuity of 1 l. payable yearly during sive years, is worth in ready money 4.259393 l. (that is 4 l. 5 s. 2 d. and somewhat more) therefore, I say, by the Rule of Three;

1. 1. 1. 1.

That is to fay, if 1 l. give 4.259393 l. what will 100 l. give? Answer 425 l. 18 s. 9½ d. very near, for by multiplying 4.259393 by 100, the product (according to the second rule of the 26 Chapter of the preceding Book) is 425.9393, that is, 425 l. 18 s. 9½ d. very near. Which operation being compared with the manner of solving the same question before mentioned in the eleventh Rule of this Chapter, the great benefit of Tables of this kind in point of expedition will be apparent.

XII. When it is required to know, unto what sum of money any propounded principal forborn any number of years will at the end of such term be augmented unto, interest up-

Of the forbearance of money at compound interest.

on interest being computed at a given rate, there must be found a rank of continual proportionals, more in number by one than is the number of years in the question; of which proportionals the first is the principal assigned, the second must increase

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or proceed from the first, the third from the second, &c. in such manner or rate, as 106 proceeds fro 100 (or as 108 from 100, if the rate of interest be 8 per centum) then will the last proportional be the Answer of the question: So if 300 pounds principal money be put forth at interest upon interest, at the rate of 61. for 100 l. for one year, and all sorborn until the end of 4 years, there will then be due 378.743088, or 378 l. 141. 10½ d.very near, as by the sour following Rules of Ibree is manisess.

For the said 300 l. will at the first years end be augmented unto 318 l. which 318 l. being put forth as a principal for 1 year, will (at the second years end) be augmented unto 337.08, again this 337.08 being put forth as a principal for 1 year, will (at the third years end) be augmented unto 357.3048, in like manner 357.3048 being put forth as a principal for 1 year, will (at the sourth years end) be augmented unto 378.743088, which is the number required by the question. And if the work be well examined, it will appear (as was before declared) that the principal sirst assigned, to wit 300 l. and the numbers resulting successively at the ends of the several years are continual proportionals, viz. these sive numbers are so qualified, that if the second be mul-

300 | 318 | 337.08 | 357.3048 | 378.743088

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tiplied by it self, the product will be equal to the product of the first and third; also if the third be multiplied by it self, the product will be equal to the product of the second and sourth; in like manner, if there were more continual proportionals in a rank, if any one proportional which is placed between two next on each side of such one, be multiplied by it self, the product will be equal to the product of those two extreams (which is a property peculiar to continual proportionals.)

Note here by the way, that if any Two numbers two numbers be propounded, suppose being given to 300 and 318, and it be required to find a third, a find to them a third, a fourth, a fifth, forc. in continual proportion, multi
we. in continual proportion, multi
must proporti-

ply the second proportional 318 by on.

it self, and divide the product
101124 by the first proportional 300, so shall the
quotient 337.08 be a third in continual proportion; In like manner if you multiply the third proportional 337.08 by it self, and divide the product
113622.9264 by the second proportional 318 the
quotient 357.3048 shall be a sourth in continual
proportion, and after the same manner a fifth, a
sixth, or as many as you please may be sound out.

From what hath been said by way of explication of the preceding twelfth Rule, the following Table III. is deduced, the construction and use

whereof is afterwards declared.

Interest.

Chap.	V						In	ter	rel	7.			Mil.		,	89
The Table	12	020	60	0	1276	629	100	0031	234	862	900	10	8	386	993	-
rhe in	1	6 6.13	9 6.86	5 7.68	1 8.612	1 9.646	6,10.80	712.10	6,13.55	5.1	7.0	619.04	421.32	023.883	26.7	39.5
of the	111	801	5.8950	5.5435	7.2633	m	8.94910	335	1.02626	2.239151	3.585461	5.07986	86	90	.62369	89229
TH.	IO I	164	447	160	290	2749 8	1	M. P.	-	973 1	104	8171	1 666	-	.8630920	1940133
Table	1	4.59	3 5.05	2 5.55	6 6.11	6.7	0 7.4	8.1.	00	8 9.8		16.11	8 13.10	3 14.42	15	1.7.4
be preceding Table III	6	3.9703	4.3276	47171	5.1416	\$.60441	6,1088	6586	7.25787	0116	8.62308	9.39919	0.24508	1.16713	2.17218	3.26767
of the pr	8	2594	1000	10966	1570	6005	338	3654	7146	4	4847	9635	1 9088	627101		265 1
ation	12	6 3.42	3.7	3.5	2 4.31	8 4.66	6 5.0	5.4	11	6 6.3	30 6.8	5 7.3	36.2	00	5 9.3	3 10.06
сонтии	7	2.9521	3.1588	3-3799	.6165	.8696	-1405	1.43040	1-7405	3.0723	1 4274	.8073	.2138	.648	中日	7.6122
7	9	54035	69277	854333	02559	207133	39956	60353	81975	24893	18167	549385	822346	11168	415387	74349
Aufa Aufa	10 m	32872.)20r 2.	1990	695 3	13293.	35963.	\$ \$263.	71523	\$ 608 8	36354	55674	33454	20125.	16135	21945.
100.1		8 2.18	0 2.29	1 2.40	4 2.52	2 2.6	6 2.78	1 2.92	13.07	0 3.2	33.3	6 3.5	63.7	03.9	54.5	9343
ALCO A	4	1.8729	1.9479	2.0258	2.1068	2.1911	2.2787	5.3699	2.4647	2.5633	2.6698	2.7724	2.8833	2.9987		3.2433
Tea	rs.	191	17	18	19	20	717	22	23	54	25	50		28	0	130

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The Construction of the preceding Table III.

The numbers 1,2,3,4,&c. to 30, in the first column on the left hand signific years; the numbers 4,5,6,7,8,9,10,11,and 12, placed at the head of the rest of the colums signific rates of interest, for 100 1. lent for a year, and the numbers placed in the several columns underneath those rates of interest, are sound out by the Rule of Three in decimals, in manner sollowing; viz.

I. | 100 . 104 :: 1 :: (1.04 II. | 100 . 104 :: 1.04 :: (1.0816 III. | 100 . 104 :: 1.0816 :: (1.12486

That is to say, First, if 100 l. put forth at interest for a year be augmented to 104 l. at the years end, what will 1 l. be then augmented unto at the same rate? Answ. 1.040 l. (that is 1l.0s.9d. 2f. and somewhat more) which 1.04 (or 1.04000, the cyphers after the 4 being of no value in decimals) is the first number in the second column belonging to 4 per centum, and is placed right against 1 year in the first column.

Secondly, say if 1001, lent for a year be augmented to 1041. at the years end, what will 1.041. be then augmented unto at the same rate? Answ. 1.08161. (that is 1 l. 1 s. 7 d. 2 f. +) which 1.0816 is the second number in the said column of 4 per cent. and is placed right against 2 years in the first column.

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Thirdly, as 100 is to 104, so is 1.0816 to 1.124864 (or 1 l.2s.5d.2 f.t) which 1.12486 is the third number in the column of 4 per centum, and is placed right against 3 years in the first column. Hence it appears, that 1 l. at 4 per centum, per annum compound interest, will at the end of 3 years be augmented unto 1.124864 l. (that is, 1 l.2s.5d.2f. and some what more.)

After the same manner the rest of the numbers in the second column, as also in the other columns are sound out (mutatis mutandis.)

The use of the preceding third Table.

Quest. 1. What will 1361.15 s.6d.be augmented unto, being forborn 20 years, interest upon interest being computed at the rate of 6 per centum per annum? Answ. 4381. 13 s. 1 d. very near, which is thus found out.

First, looking into the fourth column of the said third Table, to wit, that column which hath the sigure 6 placed at the head of it, I find right against 20 years the number 3.20713, which shews that 11. being continued 20 years at 6per centum, per annum, compound interest, and all scrborn until the end of the said term will be augmented unto 3.20713 1. (that is 31.41.1d.2f. and somewhat more) therefore after the 15 1.6 d. in the question is reduced to the decimal .775 (by the sixteenth rule of the 23 Chapter of the preceding book) I multiply the said tabular number 3.20713 by 136.775 (the sum propounded in the question) according to the second rule of the 26th Chapter, so the Product is found

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found to be 438.665,&c. that is,438 1.13 s.1d.for the Answer of the question. View the operation here following.

1 . 3.20713 :: 136.775 . (438.665 + 136.775

1603565 2244991 1924278 962139 320713

438 65520575

Queft. 2. If 320 1. be forborn 11 years, at interft upon interest at 5 per centum, per annum, what will be due at the end of those eleven years for principal and interest? Answer, 547 l. 6s. 1 d. t. For in the third column of the third Table, under the figure five at the head of the column and right against 11 years you will find this number 1.71033, which shews that I l. at the end of II years will at five per centum, per annum, compound interest, be augmented to 1.71033 (that is 1 1. 14 s. 2 d. 1 f. and fomewhat more) wherefore by multiplying the faid 1.71033 by 320 the number of pounds propounded in the question) the product will be 547 .305, &c. that is 547 l. 6s, 1 d. f for the answer of the question. See the following operation: hid tabular number 2,2 of 13 by 136,775 (sintfam)

propounded in the question) according to fire to

cond rule of the 26th Chapter, to the Product is

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After the same manner the numbers belonging to any of the other rates of interest mentioned in the third Table are to be used.

XIII. When an Annuity payable The manner of yearly is in arrear for any number summing up Anof years, and it is required to know nuities in arwhat the same will amount unto, lowances of incompound interest being computed terest upon infor each particular Annuity from tereft.

the time it became due until the end of the term of years, the work will be as in the following example; viz. Suppose an Annuity of 3001. payable at yearly payments be forborn, and all unpaid untill the end of four years, the question is, what will then be due, compound interest being computed at the rate of 6 per centum, per annum, for each yearly payment from the time it becomes due to the end of the faid term of four years? Answer 1312 l. 7 s. 8 d. very near.

It is evident by the question, that there must be computed what 300 l. due at the third years end will be augmented unto in one year (to wit the fourth year)at 6 per centum; Also what 3001.due at the second years end will be augmented unto in two years (to wit the third and fourth years;) like-

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wise what 300 l. due at the first years end, will be augmented unto, in the three following years (to wit the second, third and sourth years) all which sums being added to 300 l. (the payment due at the end of the sourth year, which is incapable of any improvement) the aggregate or sum will be the total money in Arrear at the end of the sourth year, to wit, $1312\frac{1114}{10000}$ l. as may appear by the following operation, viz.

The last payment of the Annuity due at the end of the fourth year 300.

Again, the 300 l. due at the third years end, will in one year after the rate of 6 per centum, be augmented unto

Also 300 l. due at the second years end, will in two years at the rate of 6 per centum, per annum, compound interest, be augmented unto (as appears by the first example of the twessth Rule asoregoing.)

In like manner; 300 l. due at the first years end, will in three years 357.3048 be augmented unto

The fum due at four years 31312.3848

The invention of the numbers before mentioned being well examined, it will appear, that if an Annuity or Rent payable at yearly payments be improved the f

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proved to the utmost at interest upon interest, and all forborn or respited unto the end of certain years, the total then due will be the sum of a rank of continual proportionals as many in number as there are yearly payments, the first of which proportionals is the first (or any one) years rent, and the second proportional proceeds from the first in the same rate as 106 proceeds from 100, if the rate of interest be 6 per centum, (or as 108 proceeds from 100, if the rate of interest be 8 per centum, &c.) and so likewise the third from the second, the sourth from the third, &c. (after the manner of the operation in the first example of the twelsth Rule of this Chapter.)

Otherwise.

Find a principal which may have such proportion to 300 as 100 hath to 6, and say by the Rule of Three,

6 . 100 :: 300 . 5000

That is to say, as 61. interest hath 1001. for a principal, so 3001. interest hath 50001. for a principal, then seek what 50001. will be augmented unto, being sorborn sour years at 6 per centum, per annum, compound interest (after the manner of the first example of the twelfth rule asoregoing;) so will you find 6312.3848, from which substracting the said principal 50001. the remainder (as before) is 1312.3848 1. being the sum which 3001. Annuity will be augmented unto at the end of sour years, according to the said rate of interest, the Annuity being payable at yearly payments.

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The reason of the latter Rule.

If a principal be put forth at interest upon interest payable by yearly payments, and all be forborn until the end of certain years, the total then due is equal to the aggregate or sum of these three numbers, to wit, the said principal sirst put forth; the sum of the annual simple interests of that principal; and the utmost improvement of those simple interests by computing interest upon interest; wherefore if from the said aggregate the sirst principal be subtracted, the remainder must necessarily consist of the sum of the annual simple interests, (which are in the nature of an Annuity) and the utmost improvement of those simple interests (or Annuity) by computing interest upon interest.

The Construction of the following Table IV.

Upon the aforesaid grounds, the following Table IV. is calculated, to shew what one pound Annuity, payable at yearly payments, and sorborn any number of years under 31, will amount unto by computing interest upon interest at any of the rates exprest at the head of the said Table.

But the same Table may be more easily composed by the addition of the numbers in the preceding Table III. in this manner, viz. the first number in each of those columns in the following Table IV. at the head whereof are placed the numbers 4, 5, 6, 7, 8, 9, 10, 11, and 12, signifying rates of interest 10

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ceding ber in ble IV. 45 of ID terett terest per centum, is 1 or unity; the second number in each of these columns in the latter Table is compos'd of I or unity, and the first number in the respective columns of the said preceding Table III.

Also the third number in each of the faid columns of this latter Table is compos'd of 1, and the fum of the first and second numbers of the respe-Ctive columns of the former Table, and in that order the rest are found out; or more easily thus, the third number in the latter Table is compos'd of the second number in the latter, and of the second in the former; the fourth number in the latter is compos'd of the third in the latter, and of the third in the former, &c. But you are to observe that according to either of hefe wayes of composing the fourth Table by Addition, the numbers in the preceding Table III. ought to be continued to more places then are there exprest to prevent error which may happen by adding of defective decimal fractions.

Table

100000	1000					100	-	-			-	0	0	
umber of sputed at	12	1,00000	O.	3.37440	6.35284	8.15118	10.08901	12.29969	14.77565	17.54073	24.12212	28.0291	32.39260	21:4/91
and forborn any number of interest being computed at rannum.	11	1,00000	2.11000	3.34210	6.22780	7.91285		20.00				4. 5227126.21163	30.09491	34.40232
0.1	101	1.00000	2.10000	3.31000	4.04100	7.71561	9.48717	11.43588	11.97798 12.48755 13.02103 13.57947 14.16397	15.03742	7164 15.7835916.64548 17.5602918.53116 19.50142 20.0545	24.52271	150622.5504824.2149226.0191827.9749830.09491	759625.1290227.1521129.3609131.7724834.4033315/12/9/1
arly paymen		1.00000	2.09000	3.27810	5 08471	Marie Co.	9.20043	0.63662 11.02847 11.43588	13.02103	15.19292	17.56029	821220.1406421.4952922.953382	36.01918	29.36091
I A B L E and Annuity, payable by yearn unto, at the end of the to	8	I.00000	2.08000	3.24640	4.50611			10.63662	12.48755	14 48656	16.64548	21.49529	24.21492	27.15211
T huity, pay 10, at the e	1	1.00000	2.07000	3.21490	4.43994	7 1 5 5 2 2 0	8.65402	9.89746 10.259801	86179.11	13.81644	15.78359	17.00045	22.55048	25.12902
pound Anname un	10	1.00000	2.06000	3.18365	4.37461	\$.03709	8.20282		11.49131	13.18079	14.97164	16.8699417	21.01506	23.27596
sich heweth what one pound Annui years under 31, will amount unto,	2 2	1.000000	2.05000	3.15250	4.31012	5.52503	8 14200	0.64010	11.02656	12.57789	14.20678	15.91712	19.59863	21.57856
Which sheweth what one pound Annuity, payable by yearly payments, years under 31, will amount unto, at the end of the term, compound	ANY OF SING	100000	2.04000	2.12160	4.24646	5.41632	0.03297	1.09029	10,5827011.0265611.49131	1012.00610 12.57789 13.18079 13.81644 14 48656 15.19292 15.93742 10.72200	11,13.48635 14.20678 14.9	12 15.02 580 15.9 1712 16.8	14 18.29191 19.59863 21.0	1520.0235821.5785623.2
	ear.	5.	- 0	1 "	4	5	0 1	100	0	10	11	12	12	115

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41	42.75328 48.88367 55.74971 63.43968 72.05244 81.69873 92.50289 104.60289 118.15524 150.33393 169.37400 190.69888 214.58275
	7.8880530.3242833.0033935.9497239.18994 42.75328 9.8402133.7302236.9737040.5447044.50084 48.88367 3.9990337.4502441.3013345.5991750.39593 55.74971 7.3789641.4462646.0184551.1590956.93948 63.43968 9.9954945.7619651.1601157.2749964.20283 72.05244 4.8051750.4229256.7645364.0024972.26514 81.69873 9.0057355.4567562.8733371.4027481.21430 92.5028 3.4361460.8932969.5319379.5430291.14788 104.60289 8.1766766.7647576.7898188.49732102.17415118.15524 3.2490373.1059384.7008998.34705114.41330 133.333387 8.6764679.9544193.32397 109.1817612799877 150.333393 4.4838287.35076102.72313 21.0599414307863109.37400 9.6976995.33882112.9682113420993159.81728 190.695888 7.3465210396593 24.1353514863092178.39718 214.58278
e. IV.	\$7 27.88805 30.32428 33.0033935.94972 39.18994 87 30.84021 33.77022 36.97370 40.54470 44.50084 65 33.9990337.45022 41.30133 45.59917 50.39593 99 37.37896 41.4462646.01845 51.15909 56.93948 59 40.99549 45.76196 51.16011 57.27499 64.20283 72 44.86517 50.42292 56.76453 64.00249 72.26514 38 49.00573 55.45675 62.87333 71.40274 81.21430 82 53.43614 60.89329 69.53193 79.54302 91.14788 151 63.24903 73.10593 84.70089 98.34705 114.41330 153 68.67646 79.95441 93.32397 109.18 176 127.9877 170 74.48382 87.35076 102.72313 21.05994 14307863 170 50.6976 95.33882 112.96821 13420993 159.81728 10 80.6976 95.33882 112.96821 13420993 159.81728 18 94.46078 113.28 221 12630753 64494021 199022087
A continuation of the preceding Table.	242833.00339 \$02236.97370 \$022441.30133 462646.01845 6196 \$1.16011 2292 \$6.7645 \$6475762898 6475767898 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 1647576789 16476789
n of the pre	\$30.32428 33.75022 337.45024 641.44626 945.76196 750.42292 750.42292 766.76475 355.45675 460.89329 766.76475 373.10593 679.95441 287.35076 295.33882 210396593 8113.28321
continuatio	14 www 4 4 4 N N D 10 100 00 0
Y	25.672 28.212 3 30.905 33.759 5 39.992 7 46.995 5 50.815 6 58.528 1 73.639
	23.6574 25.8403 28.1323 28.1323 30.5390 35.7192 36.5052 44.4304 44.77270 44.5019 64.6691 54.6691 54.6691 54.6691 54.6691 54.6691
igs is	25.6975 25.6975 25.6454 27.6712 27.6712 31.9692 34.2479 36.6178 36.6178 36.6178 36.6178 36.6178 36.6178 36.6178 36.6178 37.0826 47.0842 47.0842 47.0842
Tear	W w w w w w w w w w w w w w w w

13 16.62683 17.7 1290 12.01506 22.58048 24.1140 20.3600131.77248 34.40835 137.15211 29.3600131.77248 34.40835 137.15311 29.3600131 27.15311 29.3600131 27.15311 29.3600131 27.15311 29.3600131 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.15311 29.360013 27.150013 2

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The use of the preceding Table IV.

The use of the said fourth Table will be manifest by the manner of solving this Question, viz. if an Annuity of 20 1. payable by yearly payments for 15 years, be all forborn or unpaid until the end of the faid term, what will it then amount unto, upon a computation of interest upon interest, at the rate o! 6 per centum per annum? Answ.4651.10 s.4d.2f. very near, as by the following operation is evident; For in the column belonging to 6 per centum (to wit, that column which hath the figure 6 placed at the head of it) right against 15 years, you will find 23.27596, which shews that an Annuity of 11. payable at yearly payments for 15 years will at the end of the faid term (compound interest being computed at 6 per cent. per annum) amount unto 23.27596 l.(or 231.55.6d.+) Therefore multiplying the faid tabular number 23.27596 by 20. (20 because the Annuity propounded is 20 1.) the product will be 465.519 +, that is 465 l. 10 s. 4 d.2f. which is the answer of the question; view the following operation.

> 23.27596 :: 20 : (465.519+ 465 51920

In the same manner the numbers in the other column are to be used.

XIV. When a fum of money is due of rebate at at a time to come, and it is required compound inte- to know what it is worth in ready money, rebate being made at a given reft. rate

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rate of compound interest, the work will not be much different from the 12 Rule of this Chapter, viz. there must be found a feries or rank of continual proportionals more in number by one, than is the number of years in the question; of which proportionals, the first is the money propounded to be rebated, the second must decrease or lessen from the first, the third from the second, &c. in such manner or rate as 100 decreafeth from 106 (or as 100 from 108, if the rate of interest be 8 per centum) then will the last proportional be the answer of the question: So if 378 - 2410 88 l.be due at the end of four years wholly to come, it will be found to be worth in ready money 300 l. rebate being made at compound interest at 6 per centum, as by the four following Rules of Three is manifest, which may be proved by the preceding twelfth rule, where it will appear that 3001. being forborn four years, will at the faid rate of compound interest be augmented unto 378.743088 1.

1. 1. 1. 1. (378.743088 · 357.3048) 357.3048 · 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 | 337.08 |

Upon this ground the following Table V. is calculated, to shew what one pound due at the end of any number of years to come, is worth in present money, rebate being made at the rates of compound interest, mentioned in the said Table; by the help whereof and of Multiplication, questions of rebate for any sum propounded may be performed without considerable error.

Table

Table

02	Interest.	Appendix.
nder 31,is fe rates,to terest.	22.797193 91.711780 31.635518 51.567426 40.506631 26.403883 24.360610	.287476 .287476 .256675 .229174 .204619
which sheweth what one pound, payable at the end of any term of years to come under 31, is north in ready money, discompt or rebate being yearly computed at any of these rates, to wit, 4, 5, 6, 7, 8, 9, 10, 11, and 12 per centum, per annum, compound interest.	\$ 6	352184 317283 285840 257514 231994 269004
m of years mputed at nnum, com	25925.917431.909090 25925.917431.909090 57338.841680.826446 93832.772183.751314 35029.708425.683013 80583.649931.620921 30169.596267.564474 83490.547034.513158 40268.501866.466507	22410 385543 87532 350494 55534 318630 26178 289664 99246 263331 74538 239392
l of any ter	9 1.917431 1.917431 1.772183 1.649931 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267 1.596267	13.558391.508349.463193.422410.3 79.526787 475092.428882.387532.3 37.496989.444012.397113.355534.3 21.468839.414964.367697.326178.2 67.442300.387817.340461.299246.2 17.417265.362446.3152411.274538.2
able at the end or rebate bein nd 12 per cent	96.934579 .925925.9 19.816297 .793832.7 93.762895 .735029.7 93.762895 .735029.7 93.762895 .735029.7 93.762895 .735029.7 93.762895 .735029.7 98.543933 .500248.4	.463193 .428882 .397113 .367697 .367697 .340461
d, payable ompt or r. 11, and 1	6 7 89996.934579 89996.873438 39619.816297 92093.762895 47258.712986 04960.666342 65057.622749 27412.582009	1.508349 475092 444012 414964 387817 5.362446
noney, dife	1.943396.934579.925925 9.889996.873438.857338 7.839619.816297.793832 2.792093.762895.735029 6.747258.712986.680583 6.747258.712986.680583 5.704960.666342.630169 1.665057.622749.583490 9.627412.582009.540268	3.558391. 79.526787 77.496989 21.468839 57.442300
ich sheweth what worth in ready 1	\$ 8638 8638 8237 7402 7404 6768	5846 55568 55568 55503 155503 155503
which shen worth i	888899 888899 884455 884899 82192 73069 73069	1. 649580 · 584 2. 624596 · 556 3. 600573 · 530 4. 577474 · 505 5 · 555264 · 481
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Chap.	v.	Interest.	403,
W. W.	12	.163121 .145644 .130039 .116106 .103666 .082642 .082559 .073787 .058823 .058823 .058823	037383
edanin obsodet	11	188292 169632 152822 137677 124034 100668 090692 081705 066313	053821
c V.	10	217629 197844 179858 163508 148643 148643 1122840 1122840 111678 101525 092296	.069343
of the preceding Table	6		548
the preces	8	291890 270269 250249 231712 214548 198655 170315 157699 146018	115913
ration of	1.1	338734. 316574. 295864. 276508. 241513. 225713. 210947. 197146.	150402
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The Construction of the preceding Table V.

The numbers 1,2,3,4, &c. to 30, in the first column on the left hand, signific years; the numbers 4,5,6,7,8,9, 10,11, and 12, placed at the head of the rest of the columns signific rates of interest for 100 l. lent for a year, and the numbers placed in the several columns underneath those rates of interest are sound out by the Rule of Three in decimals, in manner following viz.

I. | 104.100:: 1 . (,9615384615,&c. II. | 104.100::,9615384615†.(,9245562,&c. III. | 104.100::,9245562,&c. (,888996 †

That is to fay, First, if 104 decrease to 100, or if 104 l. payable at the end of a year to come be worth 100l. ready money, what ready money is 1 l. due at the end of a year to come worth? Answer, .9615384615 + (or 19 s. 2 d. 3 f. very near) So that .961538 is the first decimal in the second column belonging to 4 per centum, in Table V. and is placed right against 1 year in the first column.

Secondly, say in like manner if 104 decrease to 100, what will .9615384615, &c. (the decimal found by the first rule of three) decrease unto? Answer, .9245562,&c. the first 6 places whereof, to wit, .924556 are the second decimal in the said column of 4 per cent. which is placed right against

two years.

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Thirdly, as 104 is to 100; fo is ,9245562,&c. (the decimal found by the second Rule of Three) to .888996 + (or 17s.9d. 1f. +) which is the third decimal in the column of 4 per centum. Hence it appears that I l. due at the end of 3 years to come is worth .888996+ (or 175.9d. if and some what more) in ready money, rebate being made at the rate of 4 per centum, per annum, compound intereft.

After the same manner the rest of the decimal fractions in the faid fecond column, as also in the other columns are found out (mutatis mutandis)

The use of the preceding Table V.

To exemplifie the faid fifth Table, let it be required to find out how much ready money wil difcharge a debt of 356 l. payable at the end of feven years to come, by rebating at the rate of 7 per centum, per annum, compound interest? Answ.2211.135. 11d.3f. very near. For in the fifth column, at the head whereof is placed 7, fignifying 7 per centum. right against 7 years, I find .622749, which shews that 11. due at the end of 7 years to come is worth in present money .622749 decimal parts of a pound, rebate being made at the faid rate of compound interest. Therefore multiplying the said tabular number . 622749 by the faid 3561. (the debt propounded) the product (according to the fecond rule of the 26th. Chapter) will be 221.698, &c.that is,2211. 13s. 11d. 3f. which is the Answer of the question. See the subsequent operation.

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In the same manner the numbers in the other co. lumns are to be used.

Fofind the prefint worth of computation of compound intezofta

XV. The finding out the prefent worth of an Annuity is grounded Anmittes by a upon this foundation, to wit, if the present money which is paid for the purchase of an Annuity, to continue any term of years, be put forth at any

rate of compound interest, and all forborn untill the end of the faid term, and that the total money then due be put into one Scale : also if the total sum of the utmost improvements of the annual payments of the Annuity, put forth at the same rate of compound interest, from the time those annual payments become due until the end of the term, be put into the other Scale, the Scales must be even viz. the faid two total fums of money must be equal one to the other.

Now to find out such a present worth of an Annuity, there are divers wayes, some of which I shall

here explain by emamples:

First therefore let it be required to find the prefent worth of an Annuity of 378.73088 1. to cons time three years compound interest being compused at 6 per cent. per ann. Answer, 1012.38481.

If

It is evident by the question, that there must be computed (after the manner of the Example upon the fourteenth Rule aforegoing) the present worth of 378 -241088 l. due at the first years end, also the present worth of the like sum due at the second years end, and in like manner for the third year; all which particular present values being added together, the aggregate or sum will be the total present worth of the Annuity propounded, viz.

378.743088 l. payable at the end) l.

of one year is worth in ready money
(as is evident by the fourteenth rule)
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Also the like sum payable at the?
end of 2 years to come is worth in 337.08
ready money

Again, the like fum payable at the end of three years to come, is 318.

of an Annuity of 378.743088 1. to 1012.3848 continue 3 years is

Find a principal which may be in such proportion to the propounded Annuity 378.743088 1. as 100 is to 6. Which will be exactly 9312.38481. for

6. 100 :: 378.743088 : 6312,3848

Then supposing this principal so sound to be a sum due at the end of three years to come, find what it will be worth in ready money, by diminishing it according to the sourteenth Rule of this Chapter, so you will find \$3001. for the ready money equivalent to the said 6312.3848 1. due at the end

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end of three years, which ready money 53001. be ing fubtracted from the faid 6312.3848 1. leaves (as before) to12.3848 l. for the present worth of the faid Annuity of 378.7430881. to continue three years, compound interest being allowed at 6 per centum, per annum. which particular profess values,

The reason of the latter Rule.

It will not be difficult to apprehend, that if 6312.3848 1. ready money be put forth as a Principal at interest upon interest, it will at three years end be augmented unto an Aggregate or fum compos'd of these three numbers, to wit, the said Principal 6312.3848; the sum of the annual simple interests of that Principal, and the utmost improvement of those simple interests by interest upon interest: And because (by the operation aforegoing) 5300l. ready money (part of the faid ready money 6312.38481) will at three years end be augmented unto 6312.38481. part of the faid Aggregate, therefore 1012.3848 l. the complement or remaining part of the faid ready money 6312.38481. must neceffarily be augmented unto the complement or remaining part of the faid Aggregate, which remaining part last mentioned is composed of the sum of the aforefaid simple interests, and of their utmost improvement at interest upon interest, that is, the said remainder is the utmost improvement of an Annuity of 378.7430881. to continue three years, compound interest being allowed at 6 per centum, per annum.

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The Construction of the following Table VI.

Upon the aforesaid grounds the following Table VI. is calculated, to thew how much ready money an Annuity of one pound to continue any number of years under 31. and payable at yearly payments, is worth, upon a computation of compound interest at any of the rates per centum, mentioned at the head of the faid Table. But the faid Table VI.may more easily be composed by the help of the preceding Table V. in this manner, viz. the first number in every of the Columns (except the Column of years) in the following Table V! is the fame with the first number in the like Columns respectively in the preceding Table V. the second number in each of the faid Columns of the fixth Table is the fum of the first and second numbers in the respective Columns of the fixth Table, the third number in the faid Columns of the fifth Table is the fum of the first, second and third numbers in the respective Columns of the fifth Table: Or yet more eafily thus, the third number in the fixth Table, is composed of the third in the fifth Table and of the second in the fixth; the fourth number in the fixth Table is composed of the fourth in the fifth and of the third in the fixth; the like is to be understood of the rest. But you are to observe that according to this way of composing the fixth Table by Addition, the numbers in the tifth Table must be continued to more places then are there expres, to prevent error arising by the addition of desective Decimal fractions.

Table

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410	Interest.	Appendix.
Which sheweth the present worth of one pound Annuity, to continue any term of years under 31, and payable by yearly payments, compound interest being computed at any of these rates, to wit, 4,5,6,7,8,9,10,11, and 12 per centum, per annum.	5238 5238 5238 4595 7569 7569 6321 6321	38 10.37965 9.71224 9.10791 8.55947 8.06068 7.19087 6.81086
-		

13 9.98964 9.3935/ 0.29498 8.74540 0.24423 7.75014 7.500087 2.5087 6.81081

yd as que- n An- year-	11. 12.	717.37916	7.548797.11	7.701617.249	12 7.83929 7.3057	107.903327.4	598.07507 7.5620	548.175747.044	8.266437.718	8.348137.7043	04 8.42174 7.0	248.488057.8	780	102 7.984	0118.0218	691,8.69379,8.05518
ng Table. VI.	9. 10.	1255 7.8	54363	75562 8.2	95011 8.3	12854	29224	9.44242 8.771	\$8020	70661	9.822579.077	79.1	0.026579.23	10.11612 9.30650	12.27767 11.15840 10.19828 9.36960 8.65	10.273659.42
continuation of the preceding T	- 8	\$.85136	2 9.12163	8 9.37188	9.60359	9.81814	10.01680	10.20074	8 10.37105	-	\sim	7 10.80997	1 10.935161	1 11.05107	7 11.15840 1	111.2 \$77811
ntinuation	7.	9.4466	9.7632	10.0590		_	7 10.83557	11.0612	11.2721	11.4693	11.6535	6 11.8257	-	16 12:1371	71 12.2776	2112,4000
A CO	.9	10.10589	10	8 10.82760	111.15811	0 1 1.46992	5 11.76407	012.04158	7 12.30337	4 12.5503	4 12.78335	13.0031	1.3.210	13.406		413.764821
	5	10.83776	11.2740	95	93 12.0853	12.4622	512,82115	13.1630	200	613.7986	7 14.09394	614-37518	8 14.64303	-	115.141	215.3924
2	4 ars	16 11.65229	12.165	18 12.65929	1913.13393	06	21 14.02915	22 14.45111	23 14.88683	24 15.24696	25 15.62207	26 15.9827	27 16.32958	28 16.6630	29 16.9837	3017.29202
The same of										14/16					-	-

The use of the preceding Table VI.

The use of the said sixth Table will appear by the manner of solving these two subsequent que-

flions, viz.

Quest. I. What is the present worth of an Annuity or rent of 56 l. per annum payable by yearly payments for 21 years, accompting interest upon interest at the rate of 6 per centum, per annum? Answer, 658 1. 151.9d. very near, thus found out; In the fourth Column of the preceding Table VI. under the figure 6 at the head, and right against 21 years, I find 11.76407, which shews that an Annuity of 1 l. payable by yearly payments for 21 years, is worth in present money 11.764071. (or II l. 15 s. 3 d. 1 f. and formewhat more) interest upon interest being computed on both fides at the rate of 6 per centum, per annum; therefore multiplying the faid tabular number 11.76407 by 56, (56 because the Annuity propounded is 56 pound) the product (according to the fecond rule of the 26th. Chapter of the preceding Book) will be found to be 658.787, &c. that is 658 l. 15 s. 9d. very near; Wherefore I conclude that the Anfwer of the question is 658 l. 15 s. 9 d. view the following operation.

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Quest. 2. What is the present worth of an annual rent of 45 l. payable by yearly payments for 21 years, interest upon interest being computed at 10 per centum, per annum? Answ. 389 l.35.10d. very near; for in the Column of 10 per centum, in the said sixth Table, right against 21 years, and under 10 at the head I find this number 8.64869; which shews that at 10 per centum, compound interest, an Annuity or rent of 1 l. payable by yearly payments for 21 years, is worth in ready money 8.64869 l. that is 8 l. 125.11 d. 3 f. therefore multiplying the said tabular number 8.64869, by 45 (the rent propounded) the product will be 389.1914, that is 3891.35.10d. very near, which is the Answer of the Question.

1 . 8.64869 :: 45 . (389.191 +

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389 19105

purchase

In the same manner the numbers in the other Columns of Table VI, are to be used.

Cc 3

Moreover

numbering the Column

To find how many years purchase an Annuity or a Lease foryears is worth.

at first fight shew how many years purchase an Annuity to continue any number of years under 31 is worth, to be sold for present money, compound interest being computed on both sides, at any of the said rates 4, 5, 6, 7, 8, 9, 10, 11

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and 12 per centum: so if you desire to know how many years purchase an Annuity issuing out of Lands for 21 years, to begin presently, is worth, if it were to be fold for ready money, when the current rate of interest is 6 per centum; Seek in the first Column of Table VI. for 21 years, and carry your eye from thence equidiffant to the head-line of the Table till you come under 6, which (as before hath been faid) fignifies 6 per centum. So in the fourth Column you will find 11.76407, whereof you need only confider 11.76, which shews that the said Annuity is worth 11 years purchase, (or 11 times one years rent whatever it be) and 76 parts of one years purchase divided into 100 parts, or a 113 years purchase and a The same annuity when money was little more. at 8 per centum was worth 10 years purchase and about 100 part of a years purchase more, as the number in the Column of 10 per centum right against 21 years will discover.

In like manner supposing 10 per centum to be a fit rate to be allowed in the valuation of Leases of houses, the Lease of a house for 21 years will be found by the said Table to be worth 8 years purchase and 700 parts of a years purchase, or 8 years purchase

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purchase and an half, and half a quarter of a years purchase, and somewhat more; But note here, that in valuing of Leases, the rate per centum is to be set higher or lower according to the goodness of the thing leased, and the certainly or uncertainty of the rent.

XVI. When a sum of money is propounded,

and it is required to know what Annuity (to continue any number of years, and according to any given rate) that fum will buy, you may prefuppose at pleasure an Annuity for

Of the purchase of Annuities at compound in-

the term of years propounded, and find the value of that Annuity in ready money (according to the fifteenth Rule aforegoing) at the rate assigned; then will the proportion be as followeth.

As the value found is in proportion to the supposed Annuity; so is the sum of money propounded, to the Annuity required.

So if it be required to find what Annuity to begin presently, and to continue three years, 500l.in present money will purchase, compound interest being computed at 6 per centum, per annum: The Answer will be 187 l. 1 s. 1 d. very near.

wit, 378.7430881.payable yearly for 3 years, the value thereof in present money will (by the fifteenth Rule of this Chapter) be found to be 1012.38481. Therefore by the Rule of proportion fav.

1012.3848 . 378,743088 :: 500 : 187,054

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That is to say, if 1012.3848 l. in ready money will buy an Annuity of 378.743088 l. (to continue three years) then 500 l. in present money will purchase an Annuity (to continue the same term of years, and at the same rate of interest) of 187.054, &c. that is 187 l. 1 s. 1 d. very near.

The Construction of the following Table VII.

Upon this ground the following Table VII. is calculated to shew what Annuity (to continue any term of years under 31, and at any rate of interest mentioned at the head of that Table) one pound will purchase, by which Table, and by the help of Multiplication, questions concerning the purchase of Annuities, Rents or Pensions, by any sum of ready money propounded, may be resolved without considerable error. But a more ready way to make the said Table VII. may be this following viz.

Forasmuch as it is evident by the construction of the third Table aforegoing, that one pound ready money is equivalent unto 1.06 l. payable at the end of a year to come, at the rate of 6 per centum, per annum; therefore this 1.06 is to be the first number in the Column intituled 6 per centum in the subsequent Table VII. Again, the present value of one pound Annuity to continue two years at the said rate will be sound by the preceding Table VI. to be near 1.833391. Therefore by the Rule of

Proportion, fay, an ydayobank . 1848 s.

1.8339

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1.83339 . 1 :: 1 : 54543,&c.

That is, if 1,833391. ready money will purchase an Annuity of 11. (to continue two years;) what Annuity to continue the same time will I !. in present money purchase? Answer, an Annuity of .54543 l. that is 10 s. 11 d. very near, to continue two years; therefore the faid Decimal .54543 1. is to be placed as the second number in the fourth Column of the Subsequent Table VII. Hence it follows, that if I or unity be divided by every one of the numbers in all the Columns of Table VI. except the first Column of years, the quotients will give the respective numbers to be placed in the like Columns of the following Table VII. In which operation it will be requisite, that the numbers in the preceding Table VI. be continued to more places than are there exprest, to prevent error that will arise by adding of defective decimals.

Table

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-	12.	1.12000	916	163	.32923	774	-	.21911	13	.18767	17698	.16841	.16143	.15567	0	.14682
e any term need at an nnum.	8.08	1.11000	.58393	·40921	.32232	70	-23637	22	194	.18060	.16980	16112	.15402	.14815	.14322	13906
ents, to continue any term of years of being computed at any of the centum, per annum.	IO.	1.10000	194	02 I	154	637	.22960	54	874	736	527	.15396	-	.14077		.13147
payments, to continue any term of years interest being computed at any of these 2 per centum, per annum.	9.	1.09000	.56846	.39505	0	.25709	.22291	69861.	18067	62991.	.15582	146941	.139651	20	.12843	.12405
le by yearly payment compound interest	8.	0	.56076	200	.30192	.25045	m	076	17401	1,16007	.14902	14007	32	0	12129	.11682
T payab	7.	1,000/0,1	530	810	.29519	2438	7602	1855	1674	534	423	00	.12590	96	-F1434	62601.
pound will pur 4, 5, 6, 7, 8,5	6.	1.06000	454		00	.23739		.17913	.16103	.14702	.13586	12079	.11927	96701.	.10758	10296
weth what 31, one pou to wit, 4,	5. (0	.53780	.36720	.28209	.23097	10791.	.17281	.15472	14069	.12950	.12038	.11282	.10645	.10102	.09634
Which (heweth wh under 31, one p	1-4	1.04001	.53019	.36034	.27549	.22462	19076	09991.	14852	.13449	.12329	11414	.10655	.10010	994600	16680
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The use of the preceding Table VII.

Quest. I. What Annuity or yearly rent issuing out of Lands, to begin prefently, and to continue 14 years, wil 320 l. purchase, compound interest being reckoned on both fides, at the rate of 6 per contum, per annum? Answ. 341.85.6d. very near, which is thus found out, viz. In the fourth Co-Jump of the preceding Table VII. under 6 at the head of that Column, and right against 14 years. you will find this decimal .10758, which shews that I l. ready money will purchase an Annuity of .10758 1. (that is 2 s. 1 d. 2 f. +) therefore multiplying the faid decimal .10758 by the faid 320; the product (according to the fecond Rule of the 26th. Chapter of the preceding Book) will be found to be 34.425, &c. that is 34 1.8 s. 6d. very near, which is the Answer of the question.

1.,10758 :: 320 . (34.425 +

32274

34 42560

In like manner, if 10 per centum be thought a fit rate of interest to be allowed in purchasing Leases of houses, 500 l. will buy a present yearly rent of 63 l. 18 s. 1 d. payable for 16 years out of a house. For underneath 10 at the head of the 8th Column, and right against 16 years (in the preceding Table VII.) you will find this decimal .12781, which be-

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ing multiplied by 500, (the number of pounds propounded to purchase the Lease) the product will be found to be 63.90500, that is, 631.181.1d. + as by the subsequent operation is manifest.

. ,12781 : : 500 . (63.905

63190500

XVII Upon the same foundations which have

been laid in the 12, 13, 14, 15 and 16 Rules of this Chapter, for the ma- The moking of king of Tables which respect yearly payments; Tables may be made for half yearly and quarterly payments, ments.

Tables for half yearly. quarterly pay-

num-

the interest of 1001. for 1 year, and likewise for 4 year being first agreed upon : For if we suppose that at the rate of 6 l. for 100 l. for a year, the interest of 1001. for 1 year is 31. the numbers 100 and 103 are to be used in the same manner to calculate Tables for half yearly payments, as the numbers 100 and 106 have been before used to form Tables for yearly payments. But if at the rate of 6 per centum per annum, the interest of 1001. for 1 year ought to be such, that being added to the faid principal 100 land the whole put forth at interest for the next half year, at the said rate, the fum then due (to wit, at the years end) must exa-Aly amount unto 106 l. In this case a Geometrical mean proportional number between the extreams 100 and 106 must be sought, which mean will (by the following 18th. Rule) be found to be near 102.956301 +, And then the numbers 100 and 102.956301, &c. are to be used instead of the

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numbers 100 and 106 in manner aforefaid. In like manner, if it be supposed that at the rate of 6 per centum, per annum, the interest of 1001.for + year is 1 l. 10 s.or 1.5 l. the numbers 100 and 101.5 are to be used for the calculating of Tables for quarterly payments, in the fame manner as the numbers 100 and 106 for yearly payments. But if at the rate of 6 per centum, per annum, the interest of 100l for year ought to be fuch, that being added to the faid 100 l. and the whole put forth at the same rate of interest for the next 1 year, and in that manner for the third and fourth quarters, and that the fum due at the years end must exactly amount unto 106 l. In this case a series or rank of five numbers in Geometrical proportion continued must be considered, viz: the principal 1001. (which is the leffer of the two extream proportionals;) the three sums (composed of principal and interest) due at the end of the first, second and third quarters of the year, (which are the three mean proportionals) and 1061. due at the years end (which is the greater of the two extream proportionals;) now between the faid extreams 100 and 106, the first (to wit the least) of the faid three mean proportionals is to be fought, which (by the following 20th.Rule of this Chapter) will be found to be near 101.4673 +. And then the numbers 100 and 101.4673, &c. are to be used instead of the numbers 100 and 106 in manner aforesaid.

metrical mean preportional number tween two mumbers given

To find a Geo. XVIII. Two numbers being given to find a Geometrical mean proportional between them; multiply the two given numbers one by the other and extract the faguare root of the

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product, so is such square root the mean proportional sought: for example, if 8 and 18 are two numbers given, and it is required to find a mean number Geometrically proportional between them, multiply 18 by 8, so is the product 144, whose square root is 12 for the mean proportional sought; so that 8, 12 and 18, are three numbers in Geometrical proportion continued, viz. As 8 is in proportion to 12, so is 12 to 18. In like manner a Geometrical mean proportional between the extreams 100 and 106 will be found near 102.956301.

XIX. Two numbers being given, to find the first

of two Geometrical mean proportionalnumbers between the extreams given, multiply the square of the leffer extream by the greater, and extract the cube root of the product, so is such cube root the lesser of the two mean proportionals required: for example, if 8 and 27 are assigned

to other sels and Afford

To find the first of the Geometrical mean proportional numbers be tween two extream numbers given.

for two extreams, the leffer mean will be found 12; for according to the rule, the square of 8 the leffer extream is 64, which being multiplyed by 27 (the greater extream) produceth 1728, whose cube root is 12 the leffer mean sought, then may the greater mean be sound more easily by the Rule of Three, for 8. 12:: 12. 18, so that 12 and 18 are two means Geometrically proportional between the extreams 8 and 27, viz. these four numbers are in geometrical proportion continued, to wit, 8. 12. 18 and 27.

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To find the first of three Geometrical mean proportionals between two extream numbers given. XX. Two numbers being given to find the first of three Geometrical mean proportionals between the extreams given, multiply the cube of the lesser extream by the greater, and extract the Biquadrate root of the product, so is such Biquadrate root

the first (to wit, the least) of the three mean proportionals required: for example, if 2 and 32 are two extreams given, the first and least of three Geometrical mean proportionals will be found to be 4, for (according to the Rule) the cube of 2 (the lesser extream given) is 8, which being multiplied by 32 (the greater extream) produceth 256, the Biquadrate root whereof being extracted (according to the 29 Rule of the 33 Chapter of the preceding Treatise) gives 4 for the first and least of the three means sought, the other means may be easily found by the Rule of Three for,

12 . 4 :: 4 . 8 :: 8 . 16 :: 16 . 32

So that these five numbers will appear to be in Geometrical proportion continued, to wit,

2 . 4 . 8 . 16 . 32.

In like manner the first and least of three Geometrical mean proportionals between the extreams 100
and 106, will be found to be near 101.4673, &c.
Thus have I shewed the most easie wayes (raised from clear grounds) to make Tables for the resolution of the usual questions, which depend upon the computation of interest, by the help of Multiplication only.

Questions

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end upon Multi-Guestion Questions to exercise the precedent Tables, with their use in solving Questions of the same nature, when the number of years exceeds 30.

Quest. 1. If the Lease of a house be worth 153 l.

Fine, and 16l. yearly rent, payable yearly for 21
years, and the Lessee be desirous to bring down the
Fine to 50l. and so to pay the more Rent, the question is, what rent the Tenant shall pay, accompting
compound interest at the rate of 10 per centum, per

annum? Answer, 27 l. 18 s. 11 d. near.

First find the difference between the Fines, which is 103 l. Then after the manner of the examples of the use of the preceding Table VII. seek what Annuity or rent to continue 21 years, 103 l. ready money will purchase at 10 per centum, so will you find 11 l. 18s. 13 d. which being added to the old rent 16 l. gives 27 l. 18s. 13 d. which the Tenant must pay to the end that the Fine may be diminished unto 50 l.

Quest. 2. There is a Lease of certain Lands to be let for 14 years for 2501. Fine, and 441. Rent per annum, payable yearly, but the Tenant is defirous to pay less Rent, viz. 20 pounds per annum, and to give a greater Fine; the question is what Fine ought to be paid to bring down the rent to 201. per annum, accompting compound interest, at the rate of 6 per cent. per annum? Answer, 4731. 15.7 d.

First find the difference between the Rents, which will be 24 pounds per an. Then by the help of the preceding Table VI. seek what Annuity or Rent of 241. per annum, to continue 14 years, is worth in ready money at 6 per centum, per annum, so will you

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find 223 l. 1 s. 7 d. which being added to the first Fine 250 pounds, gives 473 l. 1 s. 7 d. which the Tenant must pay, to the end the rent may be brought

down to 201. per annum.

Quest.3. There is a Lease of certain Lands worth 321.per annum, more than the rent paid to the Lord for it, of which Lease seven years are yet in being, and the Lessee is desirous to take a Lease in reversion for 21 years, to begin when his old Lease is expired, the question is, what sum of money is to be paid for this Lease in reversion, accompting compound interest at the rate of 6 per centum, per annum Answer. 2501.75.2d. †

First by adding the 7 years of the Lease in being to the 21 years you would have in reversion after those seven are expired, the sum is 28. Then by the

preceding Table VI.

The present worth of 1 l. An- nuity for 28 years at 6 per centum	13.40616
Likewise the present worth of 11.3 Annuity for 7 years is ——————————————————————————————————	5.58233
Therefore the difference of those present worths, shall be the pre- sent value of 11. Annuity for 21	7.82383
which multiplied by 32 (the yearly rent propounded) gives the Answer of the question.	

of realizable as Otherwife thus. In all ad yd yat

First by the help of the said Table VI. find out how much 32 l. yearly rent for 21 years is worth in ready money, as if the 21 years were to begin presently, at the rate of 6 per centum, which ready money will be found 376.450241. Then by Table V.find what 376.45024 l. due at the end of 7 years to come, is worth in ready money; so will it be 2501. 7s.2d. which agrees with the Answer before found.

Quest. 4. One would bestow 6301. to purchase a present yearly rent or Annuity of 60 l. to be paid by yearly payments, the question is to know how many years the faid Annuity must continue, compound interest at 6 per centum, per annum, being allow'd on both fides. Answ. 17 years, and 23 dayes,

very near.

First I divide 630 by 60, the quotient is 10.5, which shews that 10 years purchase and an half are given for the Annuity; then fearthing for 10.5, in Table VI. in the Column of 6 per centum, I find it not exactly, but the nearest less then it, is 10 .47725, standing right against 17 years, and the next greater than 10.5is 10.82760 which is placed against 18 years, Whence I infer that the Annuity must continue 17 years and more, yet less then 18 years. Now the proportional part of a year to be added to 17 years, may be found out near enough for use, thus, viz. subtract the said lesser tabular number 10.47725 from the greater 10.82760, fo the remainder will be found .35035: Also subtracting the faid 10.47725 from 10.5 (the quoti-

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ent first found) the remainder will be 02275; then fay by the rule of three in decimals, as 35035 the greater remainder is to .02275 the lesser; so is I year (the difference between 17 and 18 years) to .0649 parts of a year, or 23 dayes † (as will appear by the fourth Rule of the 26 Chapter of the preceding Book;) therefore the number of years sought by the question is 17 years, 23 dayes.

Queit. 5. If an Annuity of 961. payable by yearly payments for 14 years be fold for 8261, what rate of interest per centum, is implied in that bargain

Anfw. 71. 55. 7 1 d. near.

First, dividing 826 by 96, the quotient is 8,60146, which shews how many years purchase was given for the Annuity; then fearthing for 8.60416 in Table VI. in a right line passing from 14 years, equidistant to the head line of the Table, I find it not exactly, but the neareft less than it is 8.24423 (which stands in the Column of 8 per cent.) and the nearest greater is 8.74546 (which stands in the Column of 7 per cent.) whence I infer, that the rate of interest required is between 7 and 8 per cent.) and the proportional part of 11. to be added to 71. may be found out near enough for practice thus, viz. Subtract the said leffer tabular number 8.24423 from the greater 8.74546, the remainder will be .50123. Also subtract 8.60416 (the quotient first found, which falls between the faid tabular numbers from the faid greater tabular number 8.74546, the remainder will be 14130; then fay by the rule of three in decimals, as 50123 the greater remainder (or difference between the two tabular numbers)is to 14130 the lesser remainder; so is 11. (the difference between 7 per ceut. and 8 per cent.) to .2819,

&c.or \$5.7d.2f. which added to 71. gives 71. \$5.7d. 2f. which is near the rate of interest p. c. required.

Quest. 6. If a years rent (or one years purchase) be paid as a Fine, for renewing or adding 7 years to 14 years yet to come of an old Leafe for 21 years, and accordingly a new Leafe be taken for 21 years to begin presently (which proportion is ordinarily observed by Bishops, Deans, and Chapters, Heads and Fellows of Colledges in letting Leafes of their Lands) what rate of interest per centum is implied in that Agreement? Answ. 111.11s. 8d. 1f. and fomewhat more.

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To folve this Question, first I search in the preceding Table VI. to find out two numbers to scated in some one Column of interest, that one of them may stand right against 14 years, and the other against 21 years; and so qualified that the difference between them may be exactly I or unity ; but not finding any two numbers precifely answering those conditions, I take those numbers that come nearest, which will be found in the Columns of 11 and 12 per cent. for the difference between the numbers 6 98186 and 8.07507, which stand in the Column of 11 per centum, right against 14 years and 21 years, is 1.09321, which exceeds 1 (that is I years purchase) by .09321; Also the difference between 6.62816 and 7.56200, which stand in the Column of 12 per cent. right against 14 years and 21 years, is . 92384, which wants .06616 of 1; therefore I divide 11. (the difference between 111. and 121. per cent.)into two parts, in such proportion one to the other, as the faid decimals .09321 and .06616 are one to the other; fo I find the faid parts of 11, to be near .5848 and .4151; or 11 s. 8 d. if. t and 8s. 3 de

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3 d. 2 f. t; the former of which being added to 11 per centum, or the latter being subtracted from 121.

per cent. gives 11.58481. or 111. 111. 8d. 1ft, which is very near the rate of interest required by the question.

Quest, 7. What is the present worth of 11. per ann. payable yearly for 10 years, compound interest being computed at the rate of 11.5848 1. per cent. An. 51.15 st o d. very near, which is found out by the help of the preceding Table VI. in this manner, viz.

The tabular number for 10 years?	5.88923
The tabular number for 10 years?	5.65022
Their difference is	0.23901

Then say by the Rule of Three in decimals, as 11. (the difference between 11 and 12 per cent.) is to .5848 1. (to wit, the decimal by which the given rate in the question exceeds 11 per cent.) so is .23901 (the difference found out as above) to .13977 +, which being subtracted from 5.88923 (the greater of the two tabular numbers above mentioned) there will remain 5.74946, or 5 1.15 s. od. which is near the present worth, of one pound yearly rent to continue 10 years, at the proposed rate of 11.5848 1. per centum.

After the same manner the present worth of 11.
yearly rent payable for 21 years, at the same rate of
interest, will be found to be 7.77503 l.or 7 l. 15 s.
6d. very near, from which if you substract 5.74946
(being the afore-mentioned present worth of 11.
yearly rent for 10 years) there will remain 2.02557

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or 21.01.6d. which is near the present worth of a Lease of 11. rent per annum, for 11 years in reversion, to begin after 10 years yet to come in a Lease are expired; Hence it is evident, that if a Tenant to a Colledge hath 10 years yet to come in a Lease, at 11. rent per annum, and desires to have 11 years renewed, or added to those 10, and so take a new Lease for 21 years, to begin presently at the same rent, he must give 21.01.6d. or two years purchase and $\frac{1}{40}$ part of a years purchase, very near (according to the sundamental proportion before assumed in the sixth question.) The like may be done for any other term of years under 30, by the help of the said Table VI.

But yet by a Table calculated pur- Concerning the posely for the said rate of 11.5848 1. renewing of a per centum, (according to the fifteenth of Lands.

Rale of this Chapter) questions of the same kind with the two last, may be more easily answered, and therefore (for that they come often in practice) I shall here insert such a Table, as I find it ready calculated to my hand by Doctor Newton, in his Scale of Interest lately published, which Table is to be used in every respect like to the preceding Table VI. and will be very ready and useful, for the proportioning of Fines, in the renewing of Leases held from Cathedral Churches and Colledges, as will be manifest by the manner of solving the two sollowing questions.

TABLE VIII

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Quest. 8. If a Colledges
Tenant hath 7 years yet to
come or unspent in a Lease
of lands for 21 years, at 11.
yearly rent, and defires to
have 14 years renewed or
added to those seven years,
and so to take a new Lease for
21 years to begin presently,
what must be pay for a Fine?
Answ. 31. 35. od.

The rule for finding out the answer of the question proposed, and such like, is this; viz.

From 7.77507 (being the number which answers to 21 years in this Table VIII.) subtract alwayes the tabular number which belongs to the number of years to come or unspent in the old Lease, so the remainder will shew what Fine must be paid for the years to be renewed or added, to make those unspent years in the old Lease to be 21 years compleat again, at 1 l. yearly rent.

So to solve the question proposed.

Shewing the	present
worth of one	pound
Annuity)	
number of under 22,	
rate of 111.1	2
1-1 f. per	
compound	Inte-

Tears	present worth
TINI	0.90034
2	1.69938
3	2.41922
4	3.06438
5	3.64262
6	4.16088
7 113	4.62540
8	5.04176
9	5.41496
10	5.74948
II	6.04934
12	6.31819
13	6.55907
14	6.77507
15	6.96868
16	7.14226
17	7.29786
18	7.43737
19	7.56243
20	7.67455
21	7.77507

From

From the present worth of 11. 3
yearly rent for 21 years, which is 3
Subtract the present worth of the fame rent for 7 years (that were unspent in the old Lease.)

And there will remain the Fine 3.14967

That is to say, 3.14967 l. or 3l. 3s. od. (very near) must be paid as a Fine, for renewing or adding 14 years to 7 years, that were unspent in the old Lease, the yearly rent being 1 l. Also the said 3.14967 shews, that such a renewal is worth 3 years purchase, and near $\frac{1}{100}$ parts of a years purchase (what ever the rent be.)

Quest. 9. If a Tenant that hath 17 years yet to come, in a Lease of lands held of a Colledge for 21 years, at 50 l. yearly rent, be desirous to renew 4 years, and so make those 17 years to be 21 years compleat again at the same rent, what must he give for a sine? Answ.23l.17 s. 2 d. 1f. For, according to the rule before given,

From the present worth of 1 l.

yearly rent for 21 years

Subtract the present worth of the

fame rent for 17 years (that were unfpent in the old Lease.)

And there will remain

Which multiplied by the rent

The product will be the Fine

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fought, to wit, 23 l.17 s. 2 d. 1 f.

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Oestions of this nature may be readily solved without the loss of one fixteenth part of a years Purchase by the help of the following Table IX, which I have drawn from the foregoing Table VIII for the benefit of such as understand not Decimal fractions: for example, if a Colledge-Tenant defireth to have 10 years added to 11 years that are to come or unspent in a Lease of Lands that he may have a new Lease for the term of 21 years to begin presently the following Table IX. shews that he must give for a Fine 1 years Purchase, and 2 quarters of a years Purchase, and 3 quarters of a quarter of a years Purchase, viz. one years rent, and half a years rent, and three quarters of a quarter of a years rent: Supposing then the rent to be 48 1. per annum, the Fine may be computed thus.

One years rent is	1. s. d.
The first term of the second s	24:00:00
The fum is the Fine required	81:00:00

Whence it appears that the Tenant must give 81 1. as a Fine, for adding of 10 years to 11 years that were unexpired in his old Lease, to the end he may

have a new Leafe for 21 years in being.

In like manner the following Table IX. shews that the Fine for renewing or adding 7 years to 14 years that are unspent in a Lease of lands, to the end there may be a new Lease for 21 years in being, is valued at 1 years Purchase precisely, which is the fundamental proportion assumed in calculating the fore2 going Table VIII, as before was said.

TABLE IX:

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Service will the property acts as	Tears-	og k shop shod	Years-	ing so the process for the five by the l	quarter gear
	1 2 3 4 5	to to to to	20 19 18 17 16	is valued at	\[\begin{array}{cccccccccccccccccccccccccccccccccccc
ng or adding	6 7 8 9	to to to to	15 14 13 12 11	is valued at	0:3:0 1:0:0 1:0:3 1:1:3 1:2:3
Fine for renewing	11 12 13 14 15	to to to to	10 98 76	is valued at	2:0:0 2:1:1 2:2:3 (3:0:2 3:2:1
The F	17	to	46	is valued a	16 4 0 3
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The like may be done for renewing any oother term of years under 21, at any rent proposed.

But because it may sometimes happen, that the

Of finding out tabular numbers for any term of years above 30. number of years in questions beloning to the preceding 3, 4, 5, 6 and 7 Tables may exceed 30, I shall by the five following questions shew, how by the help of those Tables the answer to any question of that na-

ture may be found out near the truth, when the

term of years is above 30.

Quest. 10. If 340 l. be put forth at 4 per centum, compound interest, and both principal and interest be forborn until the end of 45 years, what will then be due? Auswer, 1986 l. very near.

To resolve this question and the like, observe this rule, viz. First make choice of such numbers of years in Table III. that if they be added together will make the number of years proposed in the question, as 17 and 28, or 15 and 30, each of which pairs make 45, then looking into Table III. in the Column belonging to 4 per centum, you will find right against 17 and 28 years these numbers, 1.94790 and 2.99870, which being multiplyed one by the other will produce 5.84116 t. or 51.16s.10d. which shall be the increase of 11. sorborn 45 years at 4 per centum, compound interest; therefore multiplying the said 5.84116 by 340, the Product will give 1985.994, &c. or 1986 l. very near for the Answer of the question.

The reason of the said Rule will be manisest by this Theorem, viz. If there be a rank of numbers in Geometrical proportion continued, beginning

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car. observe with 1 or unity, as 1,2,4, 8, 16, 32, 64, 128,&c. Also if the first term t be cast away, and over or under all the rest of the terms there be placed another rank of numbers, beginning at 1 and proceeding according to the natural order of numbers, as 1,2,3,4,5,6,7,&c. which may be called the Indices of those in the first rank, after the first term 1 is cast away; I say if any two of those remaining Geometrical proportionals be multiplyed one by the other, the product shall be a proportional correspondent to that Index, which is equal to the sum of the Indices answering to the two proportionals that were multiplyed one by the other.

Proport. 2 . 4 . 8 . 16 . 32 . 64 128
Indices. 1 . 2 . 3 . 4 . 5 . 6 7

So if 4 and 32, which are the second and fifth proportionals in the upper rank, be multiplyed one by the other, the product is 128, which shall be the feventh proportional, because the sum of the Indices 2 and 5, which answer to the faid 4 and 32, is 7. In like manner because the sum of the Indices 3 and 4 is 7, therefore if the third and fourth proportionals, to wit, 8 and 16, be multiplyed one by the other, the product shall also give the feventh proportional 128. Now forasmuch as the numbers in every one of the Columns, except the first Column of years in the preceding Table III. are continual proportionals whose first term is 1, but 'tis excluded out of the faid Columns, as appears by the Construction of that Table, and for that the numbers of years 1, 2, 3, 4, 5, &cc. are placed

Appendix. placed as Indices thewing the order or feat of those proportionals inferted in the Columns, therefore the rule before given for continuing that Table to Char

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any numbers of years is manifest.

Quest. 11. If one pound be due or payable 50 years hence, what is it worth in ready money, by rebating at 5 per centum per annum, compound interest? Answ. .08720, &c. or 1 s. 9 d. twhich is found out by the help of Table V. in the same manner as the Answer to the last Question; (respect being had to the second and third rules of the 26th. Chapter of the preceding Book concerning

the multiplication of decimal fractions.)

Quest. 12. If an Annuity of one pound payable yearly for 40 years, be all forborn until the end of that term, what will it then amount unto, compound interest being computed at 5 per centum per annum? Answ. 1201.16s od. thus found out: First, according to the second way of calculating the fourth Table in the thirteenth Section of this Chapter, find out a Principal, which may have such proportion to the proposed Annuity 11. as 100 l. hath to 5, faying, if 51. interest hath 100 1. for a principal, what principal must 11. interest have? Answer, 201. Secondly, seek (after the manner of the preceding tenth question) what 20 1. will be augmented unto being forborn 40 years, at the rate of 5 per centum, per annum, compound interest, so you will find 140.798 +, from which subtracting the faid principal 201, the remainder will be 120. 798 +, or 120 l. 16 s. which is the answer of the question.

Quest. 13. If an Annuity of one pound payable yearly for 37 years, be to be fold for prefent mo-

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ney, what is it worth, compound interest being computed on both fides at 6 per centum, per annum? Answer, 141. 145.9 d. which is found out thus: First, according to the second way of calculating the fixth Table in the fifteenth Section of this Chapter, find out a principal in such proportion to one pound (the proposed Annuity) as 100 is to 6, fo will such principal be found 16.66666+, then after the manner of the preceding eleventh question find out the ready money which is equivalent to 16.66666, due 37 years hence, fo will fuch ready money be found to be 1.92988 + (or 11.18 s. 7 d.) which being subtracted from the faid principal 16.66666, the remainder will be 14.73678 to or 141.14 s. 9 d. which is the Answer of the Question propounded.

Quest. 14. What Annuity payable by yearly payments to continue 37 years will one pound Purchase, at 6 percentum, per annum, compound interest? Answ. 1 s. 4 d. near, which is found out thus; First find out the present worth of one pound Annuity to continue 37 years, which present worth (by the last question) will be found 14.73678 l. Then say by the Rule of Three, if 14.73678 l. will purchase an Annuity of one pound, (to continue 37 years) what Annuity to continue the same term will 1 l. purchase? Answer, .06785+, or 1 s. 4 d. which is the answer of the

By the proceding Definition in 1. thefall

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A Demonstration of the Rule of Three, or Rule of Proportion.

I. F Our numbers are said to be proportionals, when the first containeth the second so often as the third containeth the sourth; likewise when the first is such part of the second, as the third is of the sourth: So these numbers sollowing are called proportionals, viz.

That is to say, 4 times 6 (or 24) is said to have such proportion to 6, as 4 times 9 (or 36) hath to 9. In like manner, \(\frac{2}{3}\) of 12 (or 8) hath such proportion to 12; as \(\frac{2}{3}\) of 15 (or 10) hath to 15.

II. When four numbers are proportionals, the product arising from the multiplication of the two extreams is equal to the product of the two means.

Demonstration.

By the preceding Definition in 1. these four numbers are proportionals, viz.

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Chap. VI. the Rule of Three 441

The product of the \(\frac{2}{4} \times 6 \times 9 \)

two extreams is \(---- \)

Ex C x D

The product of the 3 6 x 4 x 9 two means is — C x B x D

But $\left\{ \begin{array}{l} 4 \times 6 \times 9 \\ B \times C \times D \end{array} \right\} = \left\{ \begin{array}{l} 6 \times 4 \times 9 \\ C \times B \times D \end{array} \right\}$

Therefore the Prop. is manifest,

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Likewise.

By the preceding definition these four numbers are proportionals, viz.

3 x 12 . 12 :: 3 x 15 . 15

The product of the 2 2 x 12 x 15 baA

The product of the 2 12 x 3 x 15 w 2 15

But $\frac{2}{3} \times 12 \times 15 = 12 \times \frac{2}{3} \times 15$

Wherefore the proposition is every way pro-

III. From the last proposition ariseth the Rule of Proportion commonly called the Rule of Three, or Golden Rule, which teacheth by three numbers given to find a fourth proportional number in this manner, viz. Multiply the second and third numbers mutually one by the other, & divide the product by the sirst number; so the quotient shall be the fourth proportional number sought, in a direct proportion. This Rule hath been sully exemplified in the 8th. Chapter of the preceding Book, and the truth of the Ee

faid Rule may be thus demonstrated, viz. Let there be three numbers given to find a fourth in direct proportion, viz. if 24 gives 6, what shall 36 give? Or as 24 is in proportion to 6, so is 36 to a fourth proportional number sought, which sourth proportional (whatsoever it be) we may suppose to be Q, and then these four numbers will be proportionals, viz.

Therefore by the second proposition of this Chapter.

And because if equal plane numbers be severally divided by one and the same number, the quotients will necessarily be equal between themselves, therefore

Whereby it is manifest that the fourth proportional number is equal to the quotient that ariseth by dividing the product of the multiplication of the second and third proportionals by the first, which was to be proved.

Note, that every Rule of Three inverse may be made a Rule of Three direct, by making the third term the first, and by proceeding forward to the other two terms; therefore one and the same demonstration serveth for both rules.

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longs to A must have such proportion to the gain

Stock of sol. sight moneths a I lay (according to

A Demonstration of the Double Rule of Fellowship.

He Double Rule of Fellowship Commonly called the Rule of Fellowship with time) presuppoleth two things, viz. 1. That the particular Stocks of Merchants in company, have continued unequal spaces of time in the common Stock, 2. That at the end of their Partnership, the total gain or loss is to be divided amongst them, in fuch manner, that their shares shall have such proportion between themselves, as those sums of interest money have one to another, which at any rate per centum, simple interest only being computed, might be gained by the particular Stocks, within the respective times of their Continuance in the common Stock: Now for the effecting of fuch a proportional partition, the faid Double Rule of Fellowship gives this direction, viz. Divide the total gain or loss into fuch parts, which hall have the fame proportion one to the other, as is between the products arifing out of the multiplication of each particular Stock by its S. Thus it appears, that the trabnoglarion

to be partners in Traffick, for a certain time first Ee 2 agreed

A Demonstration of Appendix. agreed on between them, and that A doth permit his Stock of 100 l. to be employed in their joynt Traffick three moneths, and that B forbears his Stock of 501. eight moneths; I say (according to the faid Kule of Fellow(hip with time) what ever the total gain or loss be, that part thereof which belongs to A must have such proportion to the gain or loss of B, as 100 x 3 (or 300) hath to 50 x 8 (or 400.) This rule bath been fully exemplified in the 13 Chapter of the preceding Book, and the truth thereof, taking the two premised Suppositions for granted, may be thus demonstrated. 1. Suppoling 1001. (the Stock of A) to gain in 3 moneths any certain fum of money, as two pounds; I feek how much 501. (the Stock of B) will gain in the fame time, and at the faid rate : fo I find 2 x 50 2. That at the end of their Pertugion I. the rotal proportion between themselves, as those sums of interest monty have one to another, which at gov rate per centum, fimple interest only being Having found what 501. will gain in 3 moneths, I feeck how much the faid 501 will gain in 8x 07x See in the common Stock : Now for the & moneths, at the same rate, and so I find -Ex 1001/2 Kale of Fellowskip gives ships direction, sie, Divide the total gainer lots into fuch , roles; on or on 3 min 2 x 50 ml 8 over 2 x 50 x 8 between the products willing out of Etx: QOI riplication to coclook ricular Brock by its 3. Thus it appears, that if 100 1. in 3 moneths

doth gain 2 1. then 50 1, in 8 moneths will gain at

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Chap. VII. the Rule of Fellowship. 445

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monets ill grint 4. If both the terms (to wit, the Antecedent and Confequent) of the said proportion be severally multiplied by the said Denominator 100 x 3, the products will be in the same proportion with the numbers or terms multiplied, (by 17 è 7. Euclid) viz. the gain of A will be to the gain of B,

As 2 x 100 x 3 is to 2 x 50 x 8

5. Lastly, because 2 (the supposititious gain first assumed) is a Multiplicator as well in the Antecedent as in the Consequent of the last mentioned proportion, it may be expunged out of both, and so the gain of A will be to the gain of B in this proportion (which was to be proved) to wit,

As 100 x 3 is to 50 x 8

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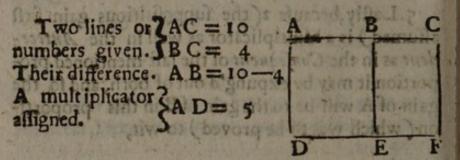
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CHAP. VIII.

A Demonstration of the Rule of Alligation alternate, and the use of the said Rule in the Composition of Medicines.

IN order to the Demonstration of the said Rule, I shall premise this Lemma, viz. if the difference of any two numbers given, be multiplied by a number assigned, the product will be equal to the difference between the products which arise from the multiplication of those two numbers severally by the number assigned.

Suppositions.



Which suppositions, and the Diagram being well viewed, the truth of the said Lemma will be evident, viz.

II. To

Chap. VIII. the Rule of Alligation.

II. To add the more light to the following Demonstration of the rule of Alligation alternate, I shall propound a question which properly belongs to the faid rule, viz. Suppose a Vintner having Frenchmines at 5 d, the quart, and at 10 d, the quart, would make a mixture of them in fuch minner, that he might fell the mixt quantity at 7 p. the quart, and so make as much money of the mixture, as if he should sell each quantity of wine at its own price; the question is to know what proportion the quantities of both forts of mine in the mixture must bear one to another. Here according to the Rule of Alligation alternate, I take the differences between the mean price affigued for the mixture, and the two other given prices, and place those differences alternately, viz. the difference between 7 and 10 being 3, I write 3 against 5, likewise 2 being the difference between 7 and 5, I write 2 against 10; so I 72 conclude, that the quantity to be taken of that fort of wine of 10 d. the quart, must have such proportion to the quantity of 5d. the quart, as 2 to 3. That is to fay, if 2 quarts at 10d. the quart be mixed with 3 quarts at 5d. the quart, the total mixture 5 quarts being fold at 7d. the quart, will yield as much money as the faid 3 quarts at 5 d. the quart, together with the said 2 quarts at 10 d. the quart; as is evident by the subsequent work.

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II.	1.	+ 20	:: 2 = 7×5	= 35

From the premisses it appears, that when two things are given to be mixt in such manner as the Rule of alligation alternate requires, the proposition

to be demonstrated will be this, namely,

Three numbers A.B.C. being given in such fort that A.is less than B. but greater than C. if the difference between A. and B. be multiplied by C. and the difference between A. and C. be multiplied by B. the sum of those products will be equal to the product arising from the multiplication of A. by the sum of the said differences,

Demonstration.

Products

A SE A C BA BC

CB CA

B—C BA—CA B—C A

The difference between B. and A. is B—A. which multiplied by C produceth (as is evident by the Lemma

Chap. VIII. The Rule of Alligation. 449

Lemma aforegoing in the first Section of this Chapter) CB—CA. Also the difference between A and C is A—C. which multiplied by B produceth BA—BC. Then the sum of those two produces is BA—CA. (for † CB and — CB expunge one the other) which sum is manifestly the same with the product arising from the multiplication of A the mean price, by B—C the sum of the aforesaid differences (to wit, the sum of A—C and B—A) for † A and —A expunge one another.

When more than two things of different prices are given to be mixt as aforesaid, the Demonstration will not be otherwise: for if the sum of every two products arising from the multiplication of two alternate differences by their respective prices, be equal to the product of the mean price multiplied by the sum of the said differences; the sum of all the said products will also be equal to the product of the mean price multiplied by the sum of all the differences; as will clearly appear by view of the subsequent work.

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Moreover, because if equal numbers be severally divided by one and the same number, the quotients will be equal between themselves, therefore from the premisses this Corollary will arise.

COROLLARY.

In the Rule of Alligation alternate, if the aggregate of the products ariling from the multiplication of the several alternate differences by their respective prices, be divided by the sum of the said differences, the quotient wil be equal to the main price. This may be a proof of any example of the said rule of Alligation.

OF THE COMPOSITION OF MEDICINES.

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See more of this in Mr. J. Dee his Mathematical preface, also Tom. 2. of P. Herigon and Master Mores Arithmetick.

I. Medicines and Simples in respect of their qualities are considered in some of these five wayes, viz. either as they are hot or cold, moist or dry, or as they are temperate; so that such Simples or Medicines which work heat in our bodies, are said to be, hot such cold which; are the cause

of coldness, &c.

II. The mean or middle between the extream qualities of Heat and Coldness, also between Dryuess and Moisture, is called Temperate or the Temperature;

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perature; from which each of the said qualities hot, cold, moist and dry, doth differ in sour degrees, so that a Medicine or Simple is said to be either temperate, or else hot, cold, moist, or dry, in the sirst, second,

third or fourth degree.

III. If the numbers 1,2,3,4,5,6,7, 8,9, be placed as you see from A to B, the differences between 5 (the middle number) and the superiour numbers 6,7,8,9, will be 1,2,3,4, which may represent the 4 degrees of the qualities hot and dry; likewise the differences between 5 and the inferiour numbers 4,3,2,1, will be 1,2,3,4, which may represent the 4 degrees of the qualities cold and moist, the temperature represented by 0. being the mean or middle from whence the said degrees do swerve.

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7	I	and dry. Temperature.
4	- COMMISSION OF	THE OWNER OF THE PERSON OF
A I	3	Qualities cold and moist.
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IV. Since the Rule of Alligation alternate requires that of two things miscible, the one must exceed the mean

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mean propounded and the other be less, therefore the questions of Alligation in this kind are to be wrought with the numbers in the aforesaid Column AB, for by them the degrees and qualities are discovered, being placed as you see in the Column adjacent to AB, and for distinction sake, those numbers in the said Column AB, may be called the Indices or Exponents of the degrees, which Indices are to be used in the same manner as the prices of Merchandizes in the questions of Alligation alternate in Chapter 14 of the preceding Book, and therefore those examples may be compared with these.

Prop. I.

Having divers Simples whose qualities are known, to make a composition or mixture of them, in such manner that the quality of the medicine may be some mean amongst the qualities of the simples, and the quantity thereof any quanti-

ty affigned.

Example 1. An Aposhecary hath four forts of Simples, A, B, C, D, whose qualities are as solloweth, viz. A is hot in the sourth degree, B is hot in the second, C is temperate, and D is cold in the third degree; the question is to know what quantities of each ought to be taken, to make a Medicine, whose quantity may be 12 ounces, and the quality in the first degree of heat? Seek in the aforesaid column AB, for the Indices or exponents of the qualities of the Simples given, viz. for A which is hot in the second, take 7; for C which

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which is temperate, take 5; and for D which is cold in the third degree, take 2; that done, rank those numbers in the same manner as the prices of Merchandizes in the questions of the 14 Chapter, viz. descend from the highest degree of heat unto the temperature, and so proceed downwards to the degrees of cold, fetting 6 the Index or exponent of the mean quality propounded, which is 1 degree of heat, as common to them all: then by crooked lines or otherwise connect two such Indices, whereof one may be greater than the mean, and the other less, and proceeding according to the Rule of the fourteenth Chapter you will find that to make a Medicine of 9 ounces, and the quality refulting to be in the first degree of heat, you must take I ounce of A (being that Simple which was hot in 4) 4 ounces of B, 3 ounces of C, and 1 ounce of D, as will be manifest by the proof,

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A 8 41 = 1 X 3 = 2	9	ID	1 2		54	(6

Lastly, by the rule of proportion you may increase the Medicine to the quantity of 12 ounces, and yet the quality to continue in the first degree of heat, according to the following operation.

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9. I 9. 4 9. 3 9. I	:: 12	1 50	of B
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The quantity assigned 12 ounces.

By other connexions of the qualities, other quantities of each Simple would arise, but that hath been sufficiently manifested in the questions of the

fourteenth Chapter.

Example 2. Suppose there are five Simples, A, B, C, D, E, whose qualities are as followeth, viz. A is hot in 3°. B is hot in 2°. C is hot in 1°. D is cold in 1°. E is cold in 3°. and it is required to mix four ounces of B, with such quantities of the rest, that the quality of the Medicine may be temperate?

200	* 4 × × × × × × × × × × × × × × × × × ×	4 B 7	Simp	The proof.
S	3	3	A B B	$8 \times i = 8$ $7 \times 3 = 2i$
s)sono			A D	$6 \times 1 = 6$ $4 \times 4 = 16$ $2 \times 2 = 14$
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= 6

4 = 16

= 14

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Proceed

Proceed as before, so will you find that to make a Medicine of 11 ounces, and the quality of the Form resulting to be temperate, you must take 1 ounce of A, 3 ounces of B, 1 ounce of C, 4 ounces of D, and 2 ounces of E; then since the quantity of B, in the composition propounded is limited, viz. 4 ounces, find numbers which may be in such proportion to 4 (the quantity of B assigned) as the numbers 1, 1, 4, 2, (the quantities of A, C, D, E, in the aforesaid Composition of 11 ounces) are unto 3 (the quantity of B in the said Composition) in manner following:

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fach proportion oners the other, as the respective

A Medicine being compounded of divers Simples whose qualities and quantities are known, to find the degree of the Form refulting, viz. the exact

temperament of the Medicine.

Example 1. Suppose a Medicine to be compounded of two Simples, viz. 6 ounces of B hot in 4°. and 3 ounces of C hot in 3°. and it is required to find the temperament of the Medicine, viz. the degree and quality resulting from such mixture? Seek in the aforesaid Column AB for the Indies of

of the respective degrees and qualities of the Simples given, and dispose them orderly in ranks right against their respective quantities; then multiply each Index by its respective quantity, and divide the sum of the products by the sum of the quantities: so will the quotient be the Index of the degree and quality of the Medicine.

So in the said example the Quotient will be found $8\frac{2}{3}$, which is the Index of $3\frac{2}{3}$ degrees of heat, and therefore the said Medicine is hot in $3\frac{2}{3}$ de

grees.

Forasmuch as any two quantities miscible according to the Rule of Alligation alternate, are in such proportion one to the other, as the respective alternate differences between the mean quality of the mixture and the qualities correspondent unto the said quantities, the demonstration of the aforesaid rule will be manifest by the Corollary aforegoing in this Chapter.

ded of 4 Simples, whose qualities and quantities are known, viz. 2 ounces of A hot in 3°. 3 ounces of B hot in 2°. 4 ounces of C temperate, and 5 ounces of D cold in 4°. and let it be required to

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find the mean quality refulting from fuch mixture. According to the aforesaid rule, I multiply each Index by its respective quantity, and divide the fum of the products by the fum of the quantities, fo the quotient is 41, which is the Index of # degrees of cold (for the difference between 5 the Index of the temperarure, and 4 ? the Index tound, is # degrees of cold) which is the quality of the faid Medicine.

> 1 x 5 = 5 14) 62 (47

Example 3. Suppose a medicine to be compounded of several Simples, whose qualities and quantities are as followeth, viz. 4 ounces of a Simple which is cold in 20. and moist in 10. 5 ounces hot in 30. and (in respect of dryness and moisture) temperate; 3 ounces hot in 2°. and dry in 2°. 6 ounces hot in 10. and moift in 40. 4 ounces cold in 30. and moist in 20. the question is to know the temper refulting? bald a diministers thomans of

In the resolution of this question there must be two distinct operations, each of them like to that -in the last example; viz. of enisibed a sloqque

loweth, viz. I dram of a Simple hot in 40,2 drams

1. Find in the same manner as before, the degree and quality resulting from the commixture of the qualities hot and cold; so will you find $5\frac{-2}{2}$ which is the Index of $\frac{-2}{2}$ degrees of heat (for the difference between 5 the Index of the temperature and $5\frac{-2}{2}$ the Index found, is $\frac{-2}{2}$ degrees of heat.)

Prod. Oun. Ind.	Prod. Oun. Ind.
3 × 4 = 12	4 × 4 = 16
8 × 5 = 40	5 × 5 = 25
7 × 3 = 21	7 × 3 = 21
6 x 6 = 36	1 x 6 = 6
$2 \times 4 = 8$	3 × 4 = 12
22) 117 (5-2	22) 80 (377

2. Find in the same manner, the temper resulting from the mixture of the qualities dry and moist; so will you find $3\frac{7}{1}$ which is the Index of $1\frac{4}{1}$ degree of moisture, so the quality of the said Medicine is $\frac{7}{2}$ degree of heat, and $1\frac{4}{1}$ degree of moisture, as by the operation is maniscit.

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To augment or diminish a Medicine in quality ac-

Suppose a Medicine to be compounded as solloweth, viz. I dram of a Simple hot in 4°.2 drams hot in 3°. 2 drams hot in 2°. I dram hot in 1°, I dram

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dram cold in 1°. and 1 dram cold in 2°. Then will the quality of the faid Medicine be in 11 degree of heat (as will be manifest by the second Proposition.) Now let it be required to augment the faid Medicine in quality, viz. to add such a quantity of some one of the Ingredients (or some other fimple) which may raise the quality of the Medicine 1 degree; so that the temperament of the Medicine after it is increased in quantity, may be in 2°. of heat. Make choice of such a simple, the Index of whose quality may exceed the Index of the quality affigned, viz. make choice of that simple which is hot in 3°. whose Index is 8, then proceed according to the I example of the first Proposition; so will you find that if I dram of the aforesaid Medicine be mixed with 1 dram of that simple which is hot in 30. the temper resulting from fuch mixture will be in 2°. of heat.

Lastly, by the Rule of Three, say, if i dram require dram, what shall 8 drams (the quantity of the

the Medicine first given) require?

Answ. 4. drams: So that if 4 drams of a simple which is hot in 3°. be mixed with 8 drams of a Medicine which is hot in 1½ degree, the the temper resulting will be in 2°, of heat, as by the operation is manifest.

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The proof.

61 x 8 = 52 8 × 4 = 32 12.) 84 (7

If it be required to diminish a Medicine in quality, you are to make choice of fuch a Simple, the Index of whose quality may be less than the Index of the quality assigned, and then to proced as before.

Here observe, that if in questions of this nature, the quantities of the Simples be exprest by weights of divers denominations, they are to be reduced to that weight which is of the lowest denomination in the question, according to the fixth rule of the seventh chapter of the preceding Book.

The augmenting or diminishing of a Medicine in respect of quantity; Also the finding of the value of any quantity of a Medicine, the prices of the ingredients being known, will be familiar to fuch as understand the Rule of Proportion, and there-

fore I shall not insist upon them.

CHAP.

CHAP. IX.

A Demonstration of the common Rule of False by two Positions.

I. What the ordinary double Rule of False is, and how to be used in resolving such questions which cannot be readily applied to any of the other rules of Arithmetick, hath been sully declared in the 15 and 31 Chapters of the preceding book; it remains that to shew what kind of operation is presupposed before the said Rule can be applied to the resolution of a question, and then to demonstrate the truth of the Rule it self.

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II. In the said Rule of False, look what operation the question requires to be performed with the number sought and some given number or numbers, the same kind of operation in every respect is to be made with each of the two seigned numbers (commonly called positions) and the said given number or numbers; which threefold process being sinisht (whether it be by any one, or all of these rules, to wit, Addition, Subtraction, Multiplication, and Division) there will arise three remarkable numbers or results, to wit, one resulting from the true number sought, and two others resulting from

the two feigned numbers; then from these three results, the errors are collected, which are nothing else but the differences between the true result, and

each of the two falle refults.

III. After the faid errors or differences are difcovered, the Rule of False will be of no force, unless this Analogy or proportionality doth arife, name-Jy, the first error must have the same proportion to the second, as the difference between the number fought and the first feigned number harh to the difference between the faid number fought and the second seigned number; here therefore it may be demanded, what kind of operation will produce the faid Analogy? To this I answer, when the question requires the number sought to be increased, lessened, multiplied or divided by some given number, or the number arising from such operation to be increased, lessened, multiplied or divided by some given number; in any of those cases, the aforesaid Analogy will necessarily arise, as I shall here manifest in all the said cases. First, therefore I say when unto each of three numbers (namely the number fought by the Rule of False and the two seigned numbers) one and the same number is added, the faid Analogy will ensue, for in this case the difference between the first sum and the second will b? equal to the difference between the first and second of the faid three numbers; likewise the difference between the first sum and the third will be equal to the difference between the first number and the third, which may be proved in manner following.

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Therefore the first of the 12 dies of the 2 dies of the 2

Suppose also that the first number A is greater

than either of the numbers B and C,

Suppose also, some number as D (3) to be added to each of the faid three numbers, fo will the three fams be,

C + D

The Proposition to be demonstrated is, that the difference between the first sum and the second is equal to the difference between the first number and the second; also that the difference between the first sum and the third is equal to the difference between the first number and the third.

Demonstration.

The difference between the first number and the fecond is, likewife enfire as may Be chare payed.

The difference between the first sum and the fecond is,

A + D-B-D 8 . EF 66 4

464 A Demonstration of Appendix.

But the latter difference is manifestly equal to the former (for + D and —D expunge one the other) to wit,

$$A + D - B - D = A - B$$

Therefore the first part of the proposition isproved.

Again, the difference between the first number and the third is,

A-C

The difference between the first sum and the third is,

A + D - C - D

But the latter difference is manifestly equal to the former, for + D and —D expunge one the other, viz.

 $A \dagger D - C - D = A - C$

Wherefore the proposition is fully proved.

The like property might be proved after the same manner, when one and the same number is subtracted from three numbers severally.

Secondly, when three numbers (namely the number fought by the rule of False and the two seigned numbers) are severally multiplied by one and the same number; the aforementioned Analogy will likewise ensue, as may be thus proved.

Let there be three numbers, to wit,

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the Rule of False. 465 Chap. IX.

Suppose also that the first number A is less than

either of the numbers B and C.

Suppose also, each of those three numbers to be multiplied by one and the same number as D (4) and the three products to be thefe,

DA | 12 DB | 20 DC 32 cd salamon bornest

non of a la box religion reporting bles The Proposition to be demonstrated is, that the difference between the first product and the second hath fuch proportion to the difference between the first product and the third, as the difference between the first number and the second hath to the difference between the first number and the third, viz. white a morning a made

$$DB-DA \cdot DC-DA :: B-A \cdot C-A$$
8 · 20 :: 2 · 5

Demonstration

Forasmuch as (by the 17th. Prop. of the seventh book of Euclids Elem.) if a number (D) multiplying two numbers (B-A and C-A) produceth other numbers (DB-DA and DC-DA) the numbers produced by the multiplication shall be in the same proportion as the numbers multiplied are, therefore

DB_DA . DC_DA : : B_A . C_A

which was to be demonstrated.

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Likewise when 3 numbers are divided by one and the same number, the demonstration will not be other wife;

A Demonstration of 466 Appendix. otherwise; and because by the second Section of this Chapter, the errors in the Rule of False are the differences between the true refult and the two falle results, therefore from the precedent demonstrations it is evident, that the aforementioned Analogy or proportionality (namely, when the first error hath fuch proportion to the fecond, as the difference between the number fought and the first feigned number hath to the difference between the faid number fought and the second feigned number) will succed from such operation, as is before declared in the beginning of the third Section of this Chapter.

ther a question be resolvable by the Rule of Falle or not.

IV. Now to discern what kind of To know when operation will not produce the faid Analogy, observe this note, viz. when a question requires some given number to be divided by the number fought or any part thereof, al fo

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when the number fought or some part thereof is to be squared, cubed, &c. likewise when some parts of the number fought are to be multiplied one by the other; I say from such operations the aforementioned Analogy will not arise, and in those cases, the ordinary rule of False will be useles: as may partly appear by the two following examples, viz.What number is that by which if 360 be divided the quotient will be 24? Here if two positions or feigned numbers be taken, and 360 be divided by each of them, the errors will not be in the same proportion with the differences between the true number fought and the 2 feigned numbers, and therefore the rule of False will be used in vain : yet if it be asked what number is that, which being multiplied OLDON WINCS

by 24, the product will be 360, the Answer to this latter question is the same with the answer to the tormer, and may be found by the rule of False; but such kind of interpretations and inferences are not alwayes obvious, and therefore since the preparative work of the rule of False (after the number is taken by guess for the number sought) proceeds gradually from one condition in the question to another, it will for the most part be eatie to determine whether the ordinary rule of False will take place or not, by comparing the conditions of a question with the note before given.

Another Example; a certain person being demanded what number of years he had lived, answered if 10 of that number were multiplied by 14 of the same number, the product would thew the number, or his age: here it will be in vain to search the number sought (which is 40) by the rule of False; for the aforementioned Analogy or proportionality will not succeed, and the question cannot easily be

resolved without Algebra.

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Now from this supposition, that after the preparative work of the rule of False is finisht, the errors will be in such proportion as aforesid, I shall make it manifest that the Rule of False will discover the

V. In the Rule of two false Positions there are 3 cases, viz. the errors are either both excesses and noted with t, or else both desects and noted with —, or lastly one of the errors is noted with t, and

the other with -.

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In the two first cases the Rule is this, Multiply the Positions or seigned numbers by the altern errors, viz. the first Position by the second error,

A Demonstration of Appendix. the second Position by the first error, and reserve those products; then dividing the difference of the faid products by the difference of the faid errors, the quotient shall be the number fought by the queflion.

The demonstration of the faid Rule here followeth.

Case I. When the errors are both excesses and noted with +.

Suppositions.

1. Let some number unknown and sought &A by the rule of False be represented by 2. Let the first Position (or feigned num- 3B

ber) be

3. And the second feigned number . . . 4. Suppose also that B is greater then C, and

each of them greater then A.

5. Moreover suppose the error of the first? Polition to be

6. And the error of the second Position to be .

7. Suppose also that this Analogy will be found in the faid numbers, viz.

B-A . C-A :: F . G

8. The proposition to be demonstrated.

$$A = \frac{FC - GB}{F - G}$$

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Demonstration.

9 Forasmuch as by supposition in 7%.

B-A . C-A :: F . G

10. Therefore by comparing the rectangle of the extreams to the rectangle of the means.

GB-GA=FC-FA

11. And by equal addition of FA.

FA + GB-GA =FC

12. Again, forasmuch as by supposition in 40:

B>C

13. And consequently out of 40. and 120.

B-A > C-A

14. Therefore out of 9° and 13°.

F > G

15. Therefore

A

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FA > GA

16. Therefore

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FA-GA > 0

17. There-

in the faid mimberspring.

470 A Demonstration of Appendix.

17. Therefore by equal subtraction of GB from the equation in 11°.

FA-GA = FC-GB

18. Wherefore by dividing both parts of the last equation by F-G, equal quotients will arise, viz.

which was to be demonstrated.

Case II. When the errors are both defects, and noted with —

Suppositions.

by the rule of False be represented by A

2. Let the first position (or seigned num- B ber) be

3. And the second position, C 4. Suppose also that B is less then C, and each of them less then A.

5. Moreover, suppose the error of the first? F

6. And the error of the second Position .. G
7. Suppose also that this Analogy will be found in the said numbers viz.

A-B. A-C :: F . G

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Chap. IX. the Rule of False.' 471

8. The Proposition to be demonstrated.

Demonstration.

9. Forasmuch as by supposition in 7%.

A-B . A-C :: F . G

10. Therefore by comparing the rectangle of the means to the rectangle of the extreams:

FA-FC = GA-GB

11. Any by equal addition of FC

FA = FC + GA-GB

12. Again, forasmuch as by supposition in 406

B > C

13. And confequently out of 4°. and 12°.

A-B > A-C

14. Therefore out of bo. and 13°.

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A Demonstration of Appendix. 16. Therefore nebed or not logor I all .3

FA-GA > 0

17. Therefore by equal subtraction of GA from the equation in 11°.

18. Wherefore by dividing both parts of the last equation by F-G, equal quotients will arise, viz.

$$A = \frac{FC - GB}{F - G}$$

which was to be demonstrated.

Case III. When one of the errors is an excess (to wit, noted by t) and the other a defect (noted by-)

In this third Case the Rule of False is this, viz.

Multiply the Politions by the altern errors, to wit the first Position by the second error, also the fecond Polition by the first error, and referve those products; then dividing the fum of the faid products by the fum of the faid errors, the quotient shall be the number sought by the question.

The Demonstration of this latter Rule here fol-Suppositions.

loweth.

1. Let some number unknown and sought by ? the rule of False be represented by 2. Let the first Position be 3. And

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Chap. IX. the Rule of False. 473

3. And the second Position.... C

4. Suppose also that B is greater than C, and also greater than A, and that C is less than A.

5: Moreover, suppose the error of the sirst F

Position to be

6. And the error of the second Position to be. G

7. Suppose also that this Analogy will be sound in the said numbers, viz.

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B-A. A-C :: F . G

8. The Proposition to be demonstrated.

Demonstration.

9. Forasmuch as by supposition in 70.

B-A . A-C :: F . G

10. Therefore by comparing the rectangle of the means to the rectangle of the extreams.

$$FA-FC = GB-GA$$

11. And by equal addition of FC and GA to the last equation, this will arise.

FA + GA = GB + FC

Wherefore by dividing both parts of the last

474 A Demonstration of, &c. Appendix. equation by F x G, equal quotients will arise, viz.

$$A = \frac{GB + FC}{F + G}$$

which was to be demonstrated.

The learned Herigonius (in cap. 13. Tom.2. of his Cursus Mathematicus) hath delivered another way of resolving the rule of False, namely by the two sollowing rules, viz.

When the signs of the Errors are unlike.

Rule I. As the sum of the errors is to the first error, so is the difference of the supposed numbers to a sourth proportional, which being added to the first supposed number, when the said first supposition is less than the second, or subtracted from it when it exceeds the second; the sum or remainder will be the true number sought.

When the figns of the Errors are unlike.

Rule III As the difference of the errors is to the first error, so is the difference of the Supposed numbers to a fourth proportional, which being added to the first supposed number when the signs are—or subtracted from it when the signs are +; the sum or remainder will be the number sought.

Both which rules the said Herigonius demonstrateth geometrically by lines, upon a supposition of the Analogy or proportionality before mentioned in the third Section of this Chapter, and the same may likewise be easily demonstrated according to the precedent method by letters.

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CHAP. X.

A Collection of pleasant and subtil Questions, to exercise all the parts of Vulgar Arithmetick. To which also are added various practical Questions about the mensuration of Superficial Figures and Solids.

Examples of the Rule Of Three mixtly nsed Gold weighing 173 lb. with other rules. Of Troy weight be worth 679 lb. sterling, what is the value of 1-3 grain of that Gold? Answ. 2 pence.

I.
$$I_{\frac{1}{3}}^{\frac{3}{3}}$$
 (or $\frac{16}{13}$) of $\frac{1}{24}$ of $\frac{1}{20}$ of $\frac{1}{12} = \frac{1}{4680}$
II. $\frac{122}{7} \cdot \frac{4258}{7} : \frac{4680}{4680} \cdot \frac{1}{120}$

Quest. 2. A man dying gave to his eldest Son \(^3\) of \(^1\) of his estate to his second Son \(^1\) of \(^1\) of his estate and when they had counted their Portions, the one had 401. more than the other; the remainder of the estate was given to the wise and younger children. The question is, what was the portion of the eldest Son, also of the second, and how much did belong to the wise and younger children?

Answ. The eldest Sons portion 1001. the second Sons portion 601. and 4401. for the wife and younger children.

The fractions being reduced, it will be manifest that the eldest Son bad to, and the second to also the Gg 2 dif-

115 · 40 · 10 · 60	
CHAP X	1.
The second Sons portion	60
The difference of their portions	40
The eldest Sons portion	100

Lastly,600 - 160 = 440 for the wife and younger children.

-1 · 40 :: 1 · 000

Quest. 3. A young man received $66\frac{2}{3}l$. which was $\frac{2}{3}$ of $\frac{1}{2}$ of his elder brothers portion, and $3\frac{1}{2}$ times of his elder brothers portion was $1\frac{1}{4}$ times of his fathers estate, the question is, what was the fathers estate? Answ. 560l.

 $\frac{1}{3}$. $66\frac{2}{3}$:: I. 200 200 × $3\frac{1}{2}$ = 700 $1\frac{1}{4}$. 700 :: I. 560

Quest. 4. If A can finish a work in 20 dayes, and B in 30 dayes; in what time will the work be finished by A and B working together? Answer 12 dayes.

First find what quantity of the work will be done by each workman in one and the same time; then it will be, as the sum of those quantities is in proportion to the said time, so is I or the whole work to the time wherein such work will be finished by both workmen working together.

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Hence it appears that A and B working together 20 dayes, will finish that work once, together with 3 of the same work; therefore say again by the Rule of Three,

work dayes work dayes

Quest. 5.

Æreus adsto leo, tubuli mibi lumina bina,
Osque etiam, dextrisic quoque planta pedis.
Binis dextro oculo, ternis lacus iste diebus
Impletur levo, sed pede bis geminis.
Orisufficiunt sex bora. Dic simul ergo,
Quo spatio os, oculi, pesque replere valent?

The sence is this. A brazen Lyon being placed in an artificial fountain, conveyeth water into a Cistern by two streams issuing from his eyes, also by one from his mouth, and by another at the bottom of his right soot. Now the Pipes through which these streams pass, are of different capacities, in such sort, that by the right eye set open alone, the rest of the streams being stopt, the Cistern will be filled in two dayes (the length of a day being supposed to be 12 hours;) by the lest eye alone in three dayes; by the soot alone in sour dayes; and

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by the mouth alone in fix hours. The question is, to find in what time the Ciftern will be filled, if all those streams be set open at once ?

Answer, 17 day,

dayes	4	Cift	Par	dayes	•	Cift.
2		THE WATER		3		I 1/2
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The sum is 94 Cisterns that will be filled in three dayes by all the four streams running together: Then say by the rule of Three.

Cist. Dayes Cist. day
$$9\frac{1}{4} \cdot 3 : 1 \cdot \frac{12}{37}$$

Quest. 6. A Ciftern in a certain Conduit is sup. plied with water by one pipe of fuch bigness, that if the cock A at the end of the pipe be let open, the Cistern will be filled in \frac{1}{2} hour; moreover at the bottom of the Ciftern two other cocks B and C are placed, whose capacities are such, that by the Cock B set open alone (all the rest being stopt) the Ciftern supposed to be full) will be emptied in 13 hour; also by the cock C set open alone the Cistern will be emptied in 21 hour : now because more water will be infused by the cock A, than can be expelled by both the cocks B and C in one and the same time; the question is to find in what time the Cistern will be filled if all the said three cocks be set open at once? Answ. 1-2 hour.

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Chapter, find how many times the Cistern will be emptied in one and the same space of time, by the cocks B and C running together; also how much of the Cistern will be filled by A in the same time; then will the difference shew how much of the Cistern is gained by the filling cock in the said time: Lastly, as the Cisterns or parts gained are in proportion to the correspondent time; so is the whole Cistern, to the time wherein it will be gained or filled.

bou. cist. bou. cist.

I.
$$2\frac{1}{3} \cdot I :: 1\frac{3}{7} \cdot \left(\frac{20}{49}\right) \begin{cases} \frac{1}{2} \\ \frac{1}{49} \end{cases} \begin{cases} \frac{1}{2} \\ \frac{1}{2} \end{cases} \begin{cases} C \\ B \\ \frac{1}{2} \end{cases} \begin{cases} B \\ B \end{cases} \begin{cases} C \\ B \end{cases} \end{cases}$$

bou. cist. bou.

II. $\frac{1}{2} \cdot I :: I\frac{3}{7} \cdot \left(2\frac{6}{7} \text{ filled by } A\right)$

$$1\frac{1}{49} \text{ gained by } A \end{cases}$$

cist. bou. cist. bou.

III. $1\frac{1}{49} \cdot I\frac{3}{7} :: I : 1\frac{9}{61}$.

Quest.7. Suppose a Dog, a Wolf and a Lion, were to devour a Sheep, and that the Dog could eat up the sheep in an hour, the Wolf in \(\frac{3}{4} \) hour, and the Lion in \(\frac{1}{2} \) hour; now if the Lion begin to eat \(\frac{1}{8} \) hour before the other two, and afterwards all three eat together, the question is, in what time the sheep would be devoured? Answ. \(\frac{3}{104} \) hour.

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$$\frac{1}{2}$$
 . I :: $\frac{1}{8}$. $\frac{1}{4}$ Gg 4

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Thus it appears that \(\frac{1}{4}\) of the sheep would be exten by the Lion, before the Dog and Wolf began to eat.

11. Proceed according to the fourth question, so will you find the remaining $\frac{3}{4}$ to be eaten by them all in $\frac{3}{12}$ hour, which added to $\frac{1}{8}$ gives $\frac{3}{104}$ hour, in

which time the sheep would be devoured.

Quest. 8. If 12031. be to be distributed amongst three persons A,B,C, in such fort, that as often as A takes 5, B shall take 4, and as often as B takes 3, C shall take 2; what shall be the share of each?

Answ. A 5141. B41-21.C27-51.

Find three Numbers which may express the proportions of their shares, by the Rule of Three, or (to avoid fractions) thus,

$$5 \cdots 4$$

$$3 \cdots 2$$

$$15 \cdot 12 \cdot 8$$

$$15 \cdot 12 \cdot 8$$

$$5 \times 3 = 15$$

$$3 \times 4 = 12$$

$$4 \times 2 = 8$$

$$35 \cdot 120\frac{1}{3} :: \begin{cases} 15 \cdot 51\frac{1}{7} \\ 8 \cdot 27\frac{51}{70\frac{5}{7}} \end{cases}$$

Quest. 9. A Governour of a certain Garrison, being desirous to know how much money the Port or passage of the Garrison did amount unto in

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certain moneths, made choice of a loyal fervant, giving him order to receive of every coachman passing with a coach 4d. of every horsman 2 d. and of every footman ½ d. Now at the years end, the servant making his accompt to the Governour, giveth him 94l. 15s. 10d. and lets him know that as often as 5 passed with coaches, 9 passed on horsback; and as often as 6 passed on horseback, 10 passed on foot; the question is how many coaches, horsemen, and sootmen passed? Answer, 2500 coaches, 4 500 horsmen, 7500 sootmen.

Find three proportional numbers after the manner of the 8 question, which will be 5, 9, 15, then

proceed as followeth,

d.
5 Coaches .. 20
9 Horsemen 18
15 Footmen : $7\frac{1}{2}$ If $45\frac{1}{2} \cdot 22750 :: \begin{cases} 5 \cdot 2500 \\ 9 \cdot 4500 \\ 15 \cdot 7500 \end{cases}$

Quest. 10. A Factor would exchange 780l.sterling for double Ducats, Dollars, and French Crowns, the Ducats at 7s. 6d. the piece, the Dollars at 4s. 4d. and the French Crowns at 6s. the piece, to be in such proportion, that ½ of the number of Ducats may be equal to ¾ of the number of Dollars, and ¼ of the Dollars equal to ¼ of the Crowns, the question is, how many pieces of each coin he shall receive for his 780 pounds.

Answ. 600 Ducats, 900 Dollars, 1200 Crowns. Find three proportional Numbers (after the

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manner of the eighth question) which will be 6, 4,3,

$$\frac{\frac{1}{2} \cdot \dots \cdot \frac{1}{3}}{\frac{1}{4} \cdot \dots \cdot \frac{3}{16}}$$

$$\frac{\frac{1}{8} \cdot \frac{1}{12} \cdot \frac{1}{16}}{6 \cdot 4 \cdot 3}$$

Thus it appears that fix times the number of Ducats must be equal to four times the number of Dollars, also equal unto three times the number of Crowns. Then make choice of three numbers to answer those proportions, such are these, 2, 3, 4, (for $6 \times 2 = 4 \times 3 = 3 \times 4$) with which numbers proceed as followeth,

Quest. 11. Twenty Knights, 30 Merchants, 24 Lawyers and 24 Citizens, spent at a dinner 64 pound, which was divided amongst them in such manner, that 4 Knights paid as much as 5 Merchants, 10 Merchants as much as 16 Lawyers; and 8 LawTi

8 Lawyers as much as 12 Citizens; the question is, to know the sum of money paid by all the Knights, also by the Merchants, Lawyers and Citizens.

Answer, The 20 Knights paid 20 pounds, the 30 Merchants 24 pounds, the 24 Lawyers 12 pounds,

and the 24 Citizens 8 pounds.

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Mer-; and Laws Find four numbers to express the proportions of their payments, by the Rule of Three, or (to avoid fractions) in manner following, so will the proportional numbers be 4, 5,8,12, viz. 4 Knights paid as much as 5 Merchants, or 18 Lawyers, or 12 Citizens.

4
320.400.640.960
thus found,
4 x 10 x 8=320
10 x 8 x 5 = 400
8 x 5 x 16=640
5 x 16 x 12=960

Then presupposing that a Knight is to pay 4 s. proceed as followet's, viz.

fay, if $12\frac{4}{5}$. 64: $\begin{cases} 4 \cdot 20 \\ 4\frac{4}{5} \cdot 24 \\ 2\frac{2}{5} \cdot 12 \\ 1\frac{3}{5} \cdot 8 \end{cases}$

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Quest. 12. A certain man with his wise did usually drink out a vessel of Beer in 12 dayes, and the husband found by often experience, that his wise being absent, he drank it out in 20 dayes; the question is, in how many dayes the wise alone could drink it out? Answer 30 dayes.

Note, it is to be supposed that the husband in 12 of the 20 dayes wherein he drank alone, did drink as much as in the 12 dayes wherein he drank with his wife; hence it followeth, that in the remaining 8 of the said 20 dayes, he drank as much as his wife did in 12 dayes. Therefore by the Rule of Three say, If 8 give 12, what 20? Answ. 30. view the following form of the work.

Frem 20 Subtract 12

Then if 8 . 12 :: 20 . 30

Quest. 13. If a house be to be built by three Carpenters, A, B, C, working in such fort, that A, alone will mish it in 30 dayes B in 40 dayes and

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and A, B, C, together in 15 dayes, in what time could Calone build the house? Answ. 120 dayes.

I. After the manner of the fourth question, find in what time A and B working together will finish the house; Answ. 177 dayes.

dayes work dayes work

40 · I · 30 · 34

add I

fum 11/4

mork dayes mork dayes.

II. Supposing the work of A and B to be performed by one person, as D, the house will be built by D in 17¹/₇ dayes, but by D and C together in 15 dayes; Then find (according to the 12th. question) in what time C will build the same; Answ. 120 dayes.

From 17¹/₇
Substract 15

Then if 21/7 . 15 :: 171/7 . 120

The proof may be wrought according to the

fourth or fifth questions.

Quest. 14. Two Travellers A and B perform a journey to one and the same place in this manner, viz. A travels 14 miles every day, and had travelled 8 dayes before B began; upon the ninth day B sets forward, and travels 22 miles every day; the

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the question is, to find in what time B shall overtake A? Answ. at the end of 14. dayes:

I. Find how many miles A had travelled before

B set forward? Answ. 112 miles; For

day miles dayes miles
1 . 14 :: 8 . 112

II. Find how many miles B gains of A in a day;
Answ. 8 miles; For

22-14 = 8

miles day miles dayes
III. Is 8 . I :: 112 . 14

Quest. 15. There is an Island which is 36 miles in compass. Now if at the same time, and from the same place, two footmen A and B set forward to travel round about the said Island, and follow one another in such manner that A travelleth every day 9 miles, and B 7 miles; the question is to find in what space of time they will again meet, also how many miles, and how many times about the Island each footman will then have travelled?

Answer, They will meet at the end of 18 days from their first parting; and then A will have travelled 162 miles (or 4½ times the compass of the Island) and B will have travelled 126 miles (or

3 times the compais of the Island.)

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36) 162 (4½ | 36) 126 (3½

Quest. 16. Two footmen A and B depart at the same time from London towards Tork, travelling at this rate, viz. A goeth 8 miles every day, B goeth 1 mile the first day, 2 miles the second day, 3 miles the third day, and in that progression he goeth sorward, travelling in every following day one mile more than in the preceding day; the question is to know in how many dayes B will overtake A?

Answer, 15 dayes.

To resolve this and such like questions, double 8 (the number of miles which A travelleth daily) which make 16, from which subtract 1, the re-

mainder is 15 the number of dayes fought.

Quest. 17. If Execter be distant from London 140 miles, and that at the same time one footman A departed from London towards Exceter, travelling every day 8 miles, and another B from Exceter towards London, travelling every day 6 miles the question is in how many dayes they will meet one another, and how many miles each footman will have then travelled?

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Answer, They will meet at the end of 10 dayes, and then A will have travelled 80 miles, and B 60 miles.

add \ 8 miles travelled daily by A. 6 miles travelled daily by B.

Jum 14 miles which A and B together did travel daily.

m. da. miles da.

14.1:: 140. 10 in which time A and
B will meet each other.

10 x 8 = 80 miles travelled by A.

10 x 6 = 60 miles travelled by B.

Quest. 18. A certain sootman A departeth from London towards Lincoln, and at the same time another sootman B departeth from Lincoln towards London; also A travelleth every day 2½ miles more then B. Now supposing those two Cities to be 100 miles distant one from the other, and that those two sootmen do meet one another at the end of 8 dayes after the beginning of their journeys; the question is, how many miles each will have then travelled, as also how many miles each travelled daily?

Answer, A 60 miles, B 40 miles. Also A travelled 7 miles every day, and B 5 miles.

day miles dayes miles
1 . 2: :: 8 . 20

Hence it appears that at the time of their meeting A had travelled 20 miles more than B, which lik

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B 60

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travelled, therefore A had travelled 60 miles.

Now to find how many miles each travelled dai-17: 17: 12. 68 miles mavelled. val

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Therefore \{\begin{array}{c} A \\ B \end{array} \travelled \{\begin{array}{c} 7\\ 2 \end{array} \} \frac{1}{2} \quad \text{daily}. : the quemonts, in what time they will be a-

Queft. 19. There is an Island which is 134 miles in compass; now at the same time, and from the same place, two footmen A and B begin a journey round about the faid Island, but they travel towards contrary parts, at this rate, viz. A travelleth II miles in every 2 dayes, and B 17 miles in 3 dayes: the question is to find in what space of time A and B will meet one another; and how many miles each will then have travelled ?

Answer, They will meet at the end of 12 dayes and then A will have travelled 66 miles, and B 68 ference only in the fame time's therefore miles.

After the manner of the fourth question of this chapter the time fought will be found 12 dayes.

miles dayes miles misv mi supo so 142 add 17

dayes miles dayes

To die : sine puro con 331 13 1 3 1 134 . 12

of Sugar? Aufar. 21d.

2 . 11:: 12 . 66 miles travelled by A. 3 : 17:: 12 . 68 miles travelled by B.

Quest. 20. If a Clock hath two Indices (or hands) one of which (to wit A) is carryed twice round the whole circumference of the Dyal in one day; and the other (B) once in 30 dayes, and that both at once shewing the same point begin to be moved; the question is, in what time they will be again conjoyned?

Answer, 10 day or 12 hours and alagrams at

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dayes: the quellon is to find in what frace of

Hence it appears, that in 30 dayes A will have run through 60 circumferences, and B one circumference only in the same time; therefore A gains of B 59 circumferences in 30 dayes therefore say.

circum. dayes circum. day

Quest. 21. If 6 lb. of Sugar be equal in value to 7lb. of Raisins; 5lb. of Raisins to 2lb. of Almonds; 3lb. of Almonds to 5 lb. of Currants; 2lb. of Currants to 18d. how many pence are the value of 3lb. of Sugar? Answ. 21d.

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Quest. 22. If 3 dozen pair of Gloves be equal in value to 2 pieces of Ribbon; 3 pieces of Ribbon to 7 dozen of points; 6 dozen of points to 2 yards of Flanders-lace; and 3 yards of Flanderslace to 81 shillings; how many dozen pair of Gloves may be bought for 28 shillings?

Answ. 2 dozen pair of Gloves.

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Quest. 23. Suppose a Graybound to be coursing a Hare, in such fort that the Hare takes five leaps for every four leaps of the Graybound, and that the Hare is one hundred of her own leaps distant from the Graybound; now if three of the Graybounds leaps be equal to four leaps of the Hares, the question is to know how many leaps the Grayhound must take before he obtain his prey?

Answer, 1200 leaps.

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I. If 3 . 4:: 4 . 51

Thus it appears, that 4 of the Graybounds leaps are equal to 5\frac{1}{3} of the Hares leaps; and because by the question the Graybound takes 4 leaps for every 5 of the Hares, therefore the Graybound in every four of his leaps gains \frac{1}{3} of one of the Hares leaps; therefore say by the Rule of Three,

II. If \(\frac{1}{3} \cdot 4 \div 100 \cdot 1200 \)

Quest.24. There is a certain room whose Basis is a long square, which is incircuit 50½ feet, and the height of the walls or sides of the room is 8¼ feet; all which walls of the room except a space taken out for a window in the form of a long square, whose height is sive feet, and breadth sour feet, are to be surnished with Hangings of ell-broad stuff at 35.4d. the yard, the question is to know how much money the stuff will cost?

Answer, 51. 175. 63d.

 $50\frac{1}{2} \times 8\frac{1}{4} = 416\frac{5}{8}$ Square feet. $5 \times 4 = 20$ Subtract

Queft. 23. Suppole a Grayhanna to be courling a Flare, in flich forts 18 fibe flare takes five leaps

3½ × 3 = 11½ square feet in one yard of fuff.

feet d. feet d. If 111/4 . 40 :: 3968 . 14109

Quest. 25. There is a certain Walk which is a long

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long square, whose length is 40 yards, and breadth 7 yards, to be paved with stones, each of which being in form of a long square is 28 inches in length, and 24 inches in breadth: the question is to know how many fuch stones will be requisite to pave the faid Walk?

Answer, 540.

Inches Inches

1440 × 252 = 362880 Square Inches. 28 × 4 = 672 Square Inches. 672 · I :: 362880 · 540 Stones.

with 28. A Marchant wrond

Quest. 26. Suppose a piece of Tapestry to be 53 yards English in length, and 32 yards in breadth, the question is, how many square ells Flemish are contained in that piece of Tapestry, when the length of I ell Flemish is equal to 3 of a yard English?

Answer, 3736 square ells Flemish.

53 × 33 = 1133 Square yards.

Then because 12 of a square yard is equal to I ell fquare of Flemish measure (for \(\frac{3}{4} \times \frac{3}{4} = \frac{2}{16}\) say, If 75 . 1

Quest. 27. A Workman hath performed a piece of Tiling bearing the form of a long square, whose length is 273 feet, 7 inches; and breadth 21 feet 5 inches; now when Tiles are fold at the rate of 11s. 103d.for 1000 Tiles, and every square of tiling confifting of 10 feet as well in length as in breadth doth take up 1000 Tiles, what doth the said piece of Tiling amount nnto?

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Answer

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Answer, 341. 17 1. 0-4001d.

I. $273\frac{7}{12} \times 21\frac{1}{12} = \frac{841711}{144}$. Square feet d.

II. $100 \cdot 142\frac{3}{4}$:: $\frac{841711}{144} \cdot 8364\frac{4001}{7600}$

Quest. 28. A Merchant would bestow 2201. in Cloves, Mace and Nutmegs, the Cloves being at 5 s. the pound; the Mace at 11 s. the pound, and the Nutmegs at 6s. the pound; now he would have of each fort an equal quantity, the question is how many pounds he may have of each sort?

Answer, 200 lb.

22 · I :: 4400 .200

The Proof.

16.	5.	7.301) STUTTED WAY	l.
200 2	it 5	amounts unto	. 50
		amounts unto	
200 2	it 6	amounts unto	60
1043	beard	fuer 7 inches and	7.0 21.0

220

Quest. 29. A Factor is to receive a sum of money, and is offered Dollars at 4s. 4d. which are worth but 4s. 3d. or French Crowns at 6s. 1\frac{1}{2}d. which

are

are worth but 6s. the question is by which coin he shall sustain the least loss?

Answer, the Dollars.

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That is, in receiving the Dollars every 61. 1½ d. loseth 1-41/04 but in receiving the Crowns 65.1½ d. loseth 1½ d. which is a greater loss than 1-41/04 d.

Quest. 30. A Butcher agrees with a Grasier, for the seeding of 20 Oxen, during the space of 12 equal moneths, but at 2 moneths end, the Butcher adds 5 Oxen more, and 63 moneths after that, he added 10 Oxen more, and then it is agreed between them, that the Grasier shall feed them all, so long time as will be equivalent to the keeping of the first twenty during 12 moneths; the question is how long time he shall feed them all, after the putting in of the last 10?

Answer, I moneth.

Consider, that as he receives more Oxen to feed he ought to keep them all the less time; therefore work as the question imports by the Rule of Three inverse.

Oxen	mon. 12 2	Onen. 20 5	mon.	Oxen
If 20			· (8	25 10
	off a	5	13 .0	35 (I mon.

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Examples of Quest. 31. Two Merchants, viz. A she Rule of and B, have entred Company; A puts in 500l. and at 4 moneths end takes out a certain sum, leaving the remainder to continue 8 moneths longer. B puts in 250l. and at five moneths end puts in three hundred pounds more, and then his whole sum continues seven moneths longer. Now at the making of their Accompt A sindeth that he hath gained 1063 pounds, and B gained 1333 pounds; the question is to know how much A took out of the bank at 4 moneths end?

- Answer, 2401. A galant maxO os Manthastant

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guel monocine frat as a monethe end, the Britches

5100 5100 5100 $500 \times 4 = 2000$ (fubtract

8)2080 (260 Lastly, 500-260 = 240 taken out by A.

The Proof.

l. mon.
500 x 4 = 2000
Subtract 240

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260 x 8= 2080

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Quest. 32. Five Merchants, viz. A, B, C, D, and E have gained 2025l. which they divide in such fort that $\frac{1}{2}$ of the share of A is equal severally to $\frac{1}{4}$ of the share of $B, \frac{1}{5}$ of $C, \frac{1}{6}$ of $D, \frac{1}{8}$ of E. The question is, what was the share of each Merchant?

Answer, A 1621. B 3241. C 4051. D 4861. E 6481.

Divide a number at pleasure into such parts which may be in such proportion as the shares required, and proceed according to the subsequent operation.

2025

Quest. 33. Two merchants A and B are in company, the sum of their stocks is 3001. the money of A continuing in company 9 moneths, the money of B 11 moneths, they gain 2001. which they divide equally, the question is to know how much each Merchant did put in?

Answer, A 1651. B 1351.

Divide 300 into two such parts which may be in proportion as 11 to 9, so will the greater part be the stock of A, and the lesser the stock of B, which stocks being multiplied by their respective times, the products will be equal.

9 (II . 165 for 1

9 . 135 for B

Appendix.

Quest. 34c Two Merchants, viz. A and B, are in company, A did put in 3251 more then B, and the stock of A continued in company 7½ moneths; B put in a certain sum which is unknown, and it continued in company 10¾ moneths: after a certain time they divide the gain equally; the question is, what each Merchant did put in?

Answer, B 7501. and A 10751.

Divide the product of the difference of their stocks multiplied by the time of A, by the difference of their times, so will the quotient be the stock of B, which added to 3251 gives the stock of A

 $325 \times 7\frac{1}{2} = 2437\frac{1}{2}$ $3\frac{1}{4}$) $2437\frac{1}{2}$ (750 stock of B add 325

1075 Hock of A

Examples of the Rule of Alligation, How the fineness of gold and situated, were is estimated, v.p. 111.

Quest.35. A Goldsmith hath some Gold of 24 Carects, others of 22 Carects, and another sort of 18 Carects sine; he would so mix these together that the mass mixed might be 60lb. and that the whole mixture might bear 20 Carects sine. How much of each sort must be take? We

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S12 of 24 Carells.

Answer, \$12 of 22 Carells.

36 of 18 Carells.

10 : 60 :: \\ 2 . 12 \\ 6 . 36

Note; some may think that questions of Atligation are capable only of fo many feveral anfwers as there are different wayes to connect the mean rate or price with the extream rates or prices; yet it is most certain, that any or dinary question of Alligation, where three or more things are propounded to be mixt in such manner as that rule requires, is capable of infinite answers, if fractions be admitted, and sometimes of many answers in whole numbers, which are not discoverable by the common rule of Alligation: fo albeit to the last mentioned question, the said rule of Alligation can find but one answer only, which is before given; yet there are eight other answers in whole numbers, which are these that follow (the invention whereof I have shewn in the 19th. Question of the thirteenth chapter of my second Book of the Elements of Algebra.)

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Of 24 Careds Of 22 Careds Of 18 Careds	3	16	0	115	4-
Of 24 Careds Of 22 Careds	18	6	4	2	(a-)
Of 18 Careds					

see chap. 8. of Quest. 36. An Apothecary hath sethis Appendix. veral Simples, viz. A hot in 3°. B hot in 2°. C temperate, D cold in 2°. and E cold in 4°. Now he desires to make a Medicine of

E cold in 4°. Now he desires to make a Medicine of those Simples, in such fort that the temper thereof in respect of quality may be in 1°. of heat, and the quantity 8½ Drams, the Demand is what quantity of each Simple he must take?

Answer, 4½ Drams of A, ½ Dram of B, 1½ Dram of C, 1 Dram of D, and 1 Dram of E.

Drams $0 \cdot 4\frac{1}{2} \mid A.$ $17 \cdot 8\frac{1}{2} :: \begin{cases} 9 \cdot 4\frac{1}{2} \mid A. \\ 1 \cdot 0\frac{1}{2} \mid B. \\ 3 \cdot 1\frac{1}{2} \mid C. \\ 2 \cdot 1 \mid D. \\ 2 \cdot 1 \mid E. \end{cases}$

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Queft.

Queft. 37. A Merchant buyeth 2 forts of Clothes, viz. of blacks and Examples of whites for 681. 21. after the rate Falfe Pofition: of 21s, the yard for the blacks, and

the Rule of

125. the yard for the white, and he taketh so much of each fort, that & of the number of yards of the black, are equal to 7 of the white; the demand is

how many yards he bought of each fort?

Ansmer, 42 yards of black, and 40 yards of white. Quest. 38 A certain person A payeth unto the use of B for ever 2500l. in present money, upon this condition, that B shall pay unto A an Annuity or yearly rent to be continued four years, the equality of their agreement being thus grounded, viz. the faid 2500l. is supposed to be put forth at interest for a year (to commence from the time of their agreement) at the rate of 8 per centum, per annum. Then from the sum of that principal and interest (arising due at the years end) the first payment of the Annuity being subtracted, the remainder is likewise supposed to be put forth at the same rate of interest for the second year; then from the composed of this principal and interest (due at the second years end) the second payment of the Annuity being subtracted, the remainder is likewife supposed to be put forth at the same rate of interest for the third year; then from this principal and interest the third payment of the Annuity being subtracted, the remainder is in like manner supposed to be put forth at the same rate of interest for the Fourth year ! lastly from this principal and interest the fourth and last payment of the Annuity being subtracted, there must be nothing left: the question is, what sum of money must be vearly certain

I. 100 . 108 :: 2500 . 2700

Subtract the first payment 75414117

II. 100 . 108 :: 1945 - 3485 . 2100 1760 2

Subtract the second payment 754 1411 25

III. 100 . 108 :: 1346 - 208 . 1453 12 124 Subtract the third payment 754 14 117 602

IV. 100 . 108 :: 698\frac{1}{1}\frac{6}{1602} \cdot 754\frac{1}{17602} \cdot 754\frac{1}{17602}

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Mule, Asineque duos imponit servulus utres
Impletos vino; segnemque ut vidit Asellam
Pondere desessam vestigia sigere tarda,
Mula rogat; quid chara parens cunciare, gemisque?
Unam ex utre tuo mensuram si mihi reddas,
Duplum oneris tunc ipsa seram; sed si tibi tradam
Unam mensuram, sient equalia utrique
Pondera; mensuras dic docte Geometer istas?

The sence is this. A Mule and an Ass carried two unequal quantities of Wine, each consisting of a certain

標 of a certain number of measures, in such fort, that if the Als inparted one of her measures to the Mule, then the Mules number of measures so increased would be the double of those which the Ass had remaining; but if the Mule gave one measure to the Afs, then the Asses measures with that increase would be equal to the Mules remaining measures. The question is, how many measures each carried? Answer, the Mule 7 and the Afi 5.

and a Dollars for a 5 shillings sheetle

mother time lie deli-04s AnD ch Crowins and Es, ferrum,fannum miscens, aurique metallum, Sexaginta minas penfantem finge coronam. As aurumque duos simul efficiento trientes. Ternos quadrantes franno mixtum impleat aurum. At totidem quintas auri vis addita ferro. Ergo age die fulvi quantum tibi conjicis auri Miscendum: die quantum eris stannique requiras: Die quoque sufficiant duri quet pondera ferri: Prescriptam ut valeas rite efformare coronam.

The sense is this, Suppose a Crown that shall weigh 601. is to be made of Gold, Brass, Iron, and Tin, mixed together in such proportion, that the weight of the Gold and of the Brass together may be 401. the joynt weight of the Gold and of the Tin 451b, and the joynt weight of the Gold and of the Iron, 36lb. The question is how much of every one of those four metals must be taken?

(302 of Gold. Answer, \$ 9\frac{1}{2} of Brass. 142 of Tin.

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present hour of the day, answered, that the time then past from noon was equal to \(\frac{1}{3}\) of the time remaining until midnight. The question is, what a clock it was? (supposing the time between noon and midnight to be divided into twelve equal parts or hours.)

Answer, 36 hour after noon,

Quest. 42. A Factor delivers 6 French Crowns and 2 Dollars for 45 shillings sterling; also at another time he delivers 9 French Crowns and 5 Dollars (at the same rate with the former) for 76 shillings. The question is to know the value of a French Crown, also of a Dollar?

Answer, A Crown was valued at 6 s. rd. and a

Dollar at 4s. 3d. a tre rise to the man deshine the

Quest. 43. A certain Usurer received 36 Dollars for the simple interest of 1861. lent for a certain time unknown; also he received 90 Dollars for the gain of 3601 at the same rate of interest for a certain time unknown; now the sum of the moneths wherein both the said numbers of Dollars were gained was twenty moneths. The question is to know in what time as well the 36 Dollars as the 90 Dollars were gained?

Answer, The 36 Dollars were gained in 871 moneths, and the 90 Dollars in 1171 moneths, as may be proved by the Double Rule of Three.

Which answer may be discovered by the follow-

ing Canon found out by the Algebraick art.

Multiply the Dollars first gained, the latter Principal, and the given time, according to the rule of continual Multiplication, for a dividend; then multiply the first principal by the Dollars last gained;

alfo multiply the latter Principal by the Dollars first gained, and reserve the sum of these two last products for a Divisor; lastly, divide the Dividend first found by the said Divisor, so shall the quotient be the time wherein the first number of Dollars was gained, which subtracted from the time given in the question discovers the time wherein the latter number of Dollars was gained,

> 36 x 360 x 20 = 259200 186 × 90, + 300 × 36, = 29700

And consequently 20 - 87 = TITE

2 44. If 3481 Souldiers are to Examples of the Extraction of be placed in asquare battel, how many are to be fet in rank or in File ?

Answ. 59 (for the square root of 3481 is 59) Quest. 45. If 4050 Souldiers are to be fet in battel in a figure, which beareth the form of a long square in such manner, that the number in File may be to the number in Rank as 1 to 2; how many Souldiers are to be placed in rank and how many in File?

Answer, 90 in rank and 45 in File (found by this

Canon or general rule) viz:

As the greater term of the proportion given is to the leffer, so is the number of men to be placed in battel to a fourth proportional, whose square root is the leffer number fought (whether it be for the rank or File:)also as the leffer term of the given proportion is to the greater; fo is the number of men to be set in battel to a fourth proportional, whole

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whose square root is the greater number sought (whether it be for the rank or File.)

I. | 2 . 1 :: 4050 . 2025

II. | /q . 2025 = 45 (men in File

III. | 1 . 2 :: 4050 . 8100

IV. | /q . 8100 = 90 (men in Rank.

The proof.

45 x 90 = 4050 Also 45 . 90 :: 1.2

Or when one of the numbers fought (whether it be for the rank or File) is found, the other may be discovered by Division, viz.

45) 4050 (90

Quest. 46. Suppose the wall of a Garrison to be in height 21 feet, and the breadth of the Moat surrounding the said wall to be 28 feet; the question is, what length must a scaling ladder have to reach from the outermost side of the Moat to the top of the Wall?

Answer, 35. (to wit, the square root of the sum

of the squares of 21 and 28.)

21 x 21 = 441 28 x 28 = 784

/q. 1225 35

Quest. 47. If 1001. being put forth for interest at a certain rate, will at the end of two years be augmented unto 112761. (compound interest, or interest upon interest being computed) what principal and interest will be due at the first years end?

Answer, 1061. (composed of 1001. principal and 61. interest) which 106 is a mean Geometrically proportional between 100 and 112.36 (and may be found by the eighteenth rule of the fifth Chapter of this Appendix.)

100 × 112.36 = 11236 (106

Quest. 48. If 1001. being put forth for interest at a certain rate, will at the end of three years be augmented unto 115.7625 1. (compound interest being computed) what principal and interest will be due at the first years end?

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Answer, 105 l. (composed of 100 l. Principal, and 5 % interest) which 105 is the first of two mean proportional numbers between 100 and 115, 7625 1. (See the nineteenth rule of the fifth Chapter of this Appendix.)

Various Practical Questions to exercise Decimal Arithmetick, in the mensuration of Sua perficial Figures and Solids.

See the second Quest. 49. If the fide of a square Section of the Superficies be 3 feet, what is the area 23 chapter of or content of that Superficies? Or the preceding (which is the same thing) how many Book. CA squares, each of which is a foot in tike tr square, are contained in that Superficies? Answer,

Answer, 9 square feet, which content is found out by multiplying the given side 3 by it self, viz.

3 multiplyed by 3 produceth 9. 1 oran bergaman

In like manner, if the side of a square pavement of stone be 15.7 seet, the superficial content of that pavement will be 246.49 seet, that is 246 seet and an half very near, (for 15.7 multiplied by it self produceth 246.49.)

Likewise, a square piece of Wainscot whose side is 3.24 yards, will be found to contain 10.49 t yards, or 10 yards and an half almost; for, 3.24 multiplied by it self, to wit, by 3.24 will produce

10.49 +

Also if the side of a square piece of Land be 37.25 perches, the content in square perches (neglecting the fraction in the product) will be found 1387, which being reduced (according to the seventh Tablet in Rule 4, chapter 7 of the preceding book) will give 8 acres, 2 roods, and 27 perches for the content of that square piece of land.

Quest. 50. If a long square be 8 seet in length and 5 seet in breadth, what is the superficial con-

tent?

Answer, 40 feet; which content is found out by multiplying the length by the breadth, viz. 8 multiplyed by 5 produceth 40. So if one of the lights of a glass window supposed to be in the form of a long square, hath for its length 3.06 feet, and breadth 1.47 feet, the content of that glass will be 4.4982 feet, or 4 feet and an half almost, (for 3.06 multiplied by 1.47 produceth 4.4982.)

In like manner if there be a piece of Wainfcot, Plastring, or any other superficies in the form of Ch

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a long square, which is in length 6. 325 yards and in breadth 3.214 yards; the superficial content will be found 20. 32 t yards, that is 20 yards, one quarter of a yard, and somewhat more, for, 6.325 multiplied by 3.214 produceth 20.32 +.

Likewise a piece of Tiling in the form of a long square whose length is 18.5 feet, and breadth 11.7 feet will be found to contain 216.45 square feet, which will be reduced to 2.1645 squares of Tiling by allowing (according to custom) 100 square feet

to one square of Tiling. to shall make month boundager

Also if a piece of land in the form of a long square be 48.75 perches in length, and 36.25 in breadth, the area or content in perches will be found 1767.18 +, which 1767 perches being reduced will give it acres and 7 perches for the content of that piece of ground.

Queff. 51. If it be required to set forth in 2 Meadow one acre of grass to ly in the fashion of a long square, and that the length thereof be limited or agreed to be 20 perches, what must the

breadth be?

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Answer, 8 perches, which breadth is found out by dividing 160 (the number of square perches contained in an acre) by the given length 20. If two acres were required, then 320 (to wir, twice 160) must be divided by the given side, whether it be the length or breadth; fo if 7. 25 perches be prescribed for the breadth of two acres, the length must be 44. 13 + percheseds to tostoro to sais and

In like manner, if the breadth of a Board be 1.32 foot, and it be demanded how far one ought to measure along the side thereof to have a superticial foot, or a foot square of that Board; divide

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I by the given breadth, so you will find in the quotient this decimal traction .757 †, which represents three quarters of a toot or nine inches and somewhat more, and so much in length ought to be measured along the side of that Board to make a superficial soot. Likewise if the breadth of a board be given in inches, then 144 (the number of square inches contained in a superficial soot square) being divided by the given breadth, the quotient will shew how many inches ought to be measured along the side of that board to make a superficial soot; so the breadth of a board being 9 inches, the length forward to make a superficial soot will be sound 16 inches.

Quest. 52. If the three sides of a piece of land that lyes in the form of a triangle be 15 perches, 14 perches, and 13 perches, what is the area or number of square perches contained in that triangle?

Answer, 84 perches, or half an acre and four perches, which content is found out by this Rule

From half the sum of the three sides of any plane triangle subtract each of the three sides severally, and note the three remainders; then multiply the said half sum and those three remainders one into the other (according to the rule of continual Multiplication;) that done, extract the square root of the last product, so shall such square root be the area or content of the triangle.

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The 3 sides of a triangle	214
or or other contraction of the c	NEWS OF
The sum of the 3 sides	42
The half of that sum	- 21
The 3 remainders found out by sub- tracting each side from the half sum—	3 7 8
The product arising from the con tinual multiplication of the four la	A\$7056
The square root of which product the content required, to wit,	is {84
Another Example.	Perches
The 3 sides of a triangle	$ \begin{cases} 120.5 \\ 112.6 \\ 90.3 \end{cases} $
The fum of the 3 fides	323 . 4
The half of that sum The 3 remainders found by subtr	- 161 · 7
Aing each fide from the half fum-	- 71.4
The product arising from \$ the continual multiplication 233553	80 . 1096
The square root of that product—4	Wherefore

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Wherefore I conclude that the content of a plane triangle, whose three sides are 120.5 perches 112.6 perches, and 90.3 perches, is 4832.7 † perches, which reduced give 30 acres and 32 perches

(the traction of a perch being neglected.)

Now forasimuch as every irregular piece of ground may be divided into triangles, for a fourtided field will be divided into two triangles by one imaginary fireight line leading overthwart from corner to corner called a Diagonal line; a five-fided field into three triangles by two Diagonals; a fix-fided ground into four triangles by three Diagonals, &c., the rule before given will be of excellent use to find out the Contents of large fields, especially if the land be of a dear value, as also when any controversie ariseth by the reason of the different admeasurements of Surveyors of land: for if the fides of those triangles be mealured in the field, and their lengths be agreed on, all Artifls to whom the reason of the rule before givenis known, will agree in one and the same content. But yet this way of measuring presupposeth that there is no obstacle, as Water, Wood, or other impediment, to hinder the measuring of the fides of those triangles into which the field is divided as aforefaid.

Queft. 53. If the diameter of a Circle be 28.25,

what is the circumferrence ? shriemer a an I

Answer, 88,749 ten for as 113 is in proportion to 355 v or as 1 is to 3.14159, so is the diameter to the circumference. Therefore multiplying alwayes the diameter given by the said 3.14159 the product shall be the circumference required.

Quest. 54. If the diameter of a Circle be 28.25,

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what is the superficial content of that Circle?

Answer, 626.79 †: for as I is in proportion to .78539, so is the square of the diameter to the superficial content. Therefore multiplying alwaies the said decimal fraction .78539 by the square of the given diameter (which square is the product of the multiplication of the diameter by it self) the product shall be the superficial content required.

Quest. 35. If the diameter of a Circle be 28.25. what is the side of a square which may be inscri-

bed within the fame Circle?

Answer, 19.975 + for the square root of half the square of the diameter, or the square root of the double of the square of the semidiameter, shall be the side of the inscribed square sought. Otherwise, as 1 is to 707 roo, so is the diameter to the side required. Therefore if you multiply (alwayes) the said .707 roo, by the diameter given, the product will be the side of the inscribed square required.

Queft. 56. If the Circumference of a Circle be

88.75 what is the diameter ?

Answer, 28.249 + for as 355 is to 113, or as 1 is to .318309, to is the Circumference to the Diameter. Therefore if .318309 be multiplied alwayes by the given Circumference, the productshall be the diameter required.

Quest. 57. If the Circumserence of a Circle be 88.73, what is the superficial content of that Cir-

Answer, 626.801 t; for as 1 is to .079578. so is the square of the Circumference to the superficial content. Therefore if .079578 be alwayes multiplyed by the square of the given circumference, the product shall be the superficial content sought.

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Quest. 58. If the circumference of a Circle be 88.75. what is the side of a square that may be inscribed within the same Circle?

Answer, 19.975 †; for as 1 is to .225078, so is the circumference to the side required. Therefore if .225078 be alwayes multiplied by the circumference given, the product will be the side of the inferibed square sought.

Quest. 59. If the superficial content of a Circle

be 626.8, what is the diameter?

Answer, 28.25 †; for as 1 is to 1.27324, so is the content to the square of the diameter. Therefore multiplying alwayes 1.27324 by the given content, the square root of that product shall be the diameter required.

Quest. 60. If the superficial content of a Circle

be 626.8, what is the circumference?

Answer, 88.75 t, for as 1 is to 12.5664, so is the content to the square of the circumference. Therefore if 12.5664 be alwaies multiplied by the given content, the square root of the product shall be the circumference required.

Quest. 61. If the superficial content of a Circle be 626.8, what is the side of a square equal to the

fame Circle?

Answer, 25.035 +, for the square root of the gi-

Quest. 62. If the side of a Cube be 12 inches, how many cubical inches are contained in that Cube?

Answer, 1728. What a Cube is may be well represented by a Dye, which is a little cube it self being a rectangular or square solid, that hath an equal length, breadth and depth, and is comprehended

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hended under fix equal squares; now if the side of one of those equal squares (which is also the side of the Cube) be 12 inches, the superficial content of that square will be 144 square inches (for according to the preceding 49th question, 12 multiplied by 12 produceth 144) which multiplied by the depth 12 inches, produceth 1728 cubical inches, and such is the solid content of that Cube whose side is 12 inches: so that by one soot of timber or stone in whatsoever kind of solid it be sound, is understood a Cube, containing 1728 cubical or dye-square inches, and consequently half a soot solid contains 864 cubick inches, and a quarter of a foot solid contains 432 cubick inches.

In like manner, it the side of a Cube of stone be 2.53 feet, the solid content of that Cube will be sound 16.194† feet, for 253 being multiplied by it self produceth 6.4009 superficial feet, which product being multiplied by the said 2.53 will pro-

duce 16.194 + folidf eet.

Also if the side of a Cube of stone or wood be 6 inches, or .5 soot, the solid content will be found 216 cubick inches or .125 parts of a foot solid (for 6 multiplyed cubically produceth 216, likewise.5 multiplyed cubically produceth .125;) whence it may be inser'd, that 8 little cubes of stone or wood, each of which is half a foot or 6 inches square, are contained in a foot of stone or timber; for 8 times 216 produceth 1728 (being the number of cubick inches contained in a foot solid) likewise 8 times .125 produceth 1 (to wit one entire foot solid.)

Quest. 63. If the breadth of a squared piece of timber, supposed to be streight and terminated at both

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both ends by two equal squares, be 1.55 soot, the depth also 1.55 soot, and the length 17.33 seet, how many cubick feet are contained in that piece of timber?

Answer, 41.635 feet, that is, 41 feet and an half, and about half a quarter of a foot. Which solid content is found out by this rule, viz. multiply the breadth 1.55 by the depth 1.55 the product will be 2.4025 superficial feet, which is the content of the Base (that is, the Area of either of the two equal squares at the ends of the pieces) lastly multiplying the said Base 2.4025 by the length 17.33 the product will be 41.635 +, which is the solid content required.

In like manner if the breadth of a squared piece of timber, supposed to be streight and terminated at both ends by two equal long squares (which are called the Bases) be 2.34 seet, the depth 1.61 soot, and the length 17.58 seet, the folid content will be 66.23 t, seet; for (as before) multiplying the breadth by the depth, and that product by the length, the last product shall be the solid content

arequired on a last parts of a foodbard

Quest. 64. If the breadth, as also the depth of a squared piece of timber having equal square Bases, the 1.55 foot, how far ought one to measure along the length of that piece of timber to make a foot solid?

near; which decimal is thus found, viz. First and the superficial content of the Base, which will be 2.4025 (for 1.55 multiplied by 1.55 produceth 2.5025;) Then dividing I (to wit I solid foot) by the Base 2.4025 the quotient will be .416 +

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or 1000 parts of a foot, or five inches almost, and so far ought to be measured along the length of the piece to make a foot solid. In like manner, if the breadth be 2.34 feet, and the depth 1.61 feet, the length sorward along the piece to make one solid foot will be found .265 parts of a foot, or three inches and almost 1 part of an inch.

Quest. 65. If a streight squared piece of timber be terminated by unequal Bases, whereof one contains 1.92 superficial soot, the other .85 soot, and the length of that piece of timber be 17.4 seet; what is the solid content, or how many Cubical seet are

contained in that piece of timber?

Answer, 23.474 + feet (found out by one of Mr. Oughtreds Rules for measuring a segment of a Pyramid in Problem 21. Chapter 19. of his Clavis Ma-

themat.) The rule is this.

Multiply the greater Base by the less, and extract the square root of that product, then multiply the sum of the two Bases and that square root by one third part of the length of the solid propounded, so shall the last product be the solid content required.

duling agaget t feet: for if the area of the

Este of a Pyramid, be multiplied by one third pays of the beight thereof, the product fall last berthe falld

content of the Pyramid a shorefore 5.756 * 475 = 27.3 & feet the folidity of the Pyramid pro-

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equal Bafes, for the meaturing of which latter feg-

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The product of the multiplication 5
of those two Bases ———————————————————————————————————
The square root of that product 1 . 2774
the sum of that square root and \ -4.0474
AND THE RESIDENCE OF THE PARTY
One third part of the length is 5 . 8
The product of the multiplication
of the two last numbers is the solid 2-23 . 474†
content required

Quest. 66. A Pyramid is a solid comprehended under plane furfaces, and from a triangular, quadrangular, or any multangular Bafe, diminisheth equally less and less till it finish in a point at the top; now if the superficial content of the Base of a Pyramid be 5.756 feet, and the height thereof 14.25 feet (which height is the length of the perpendicular line that falleth from the top of the Pyramid to the Base) what is the solid content of that Pyramid?

Answer, 27.341 + feet: for if the Area of the Base of a Pyramid, be multiplied by one third part of the height thereof, the product shall be the folid content of the Pyramid; therefore 5.756 x 4.75 = 27.341 feet = the folidity of the Pyramid propounded.

Note, If a Pyramid be cut into two fegments by a Plane parallel to the Base, one of those segments will be a Pyramid, and the other will have two unequal Bases, for the measuring of which latter seg-

ment

ment, a rule hath been already given in the fixty fifth question, the Area of each Base being known.

Quest. 67. A Cone is a solid, which hath a Circle for its Base, from whence it grows equally less and less (like a round Steeple of a Church) till it finish in a point at the top; now if the Area of the Base of a Cone be 5.756 feet, and the height thereof be 14.25 feet, what is the solid content of that Cone?

Answer, 27 341 feet: for if the Area of the Base of a Cone be multiplyed by one third part of the height thereof, the product shall be the solid con-

tent of the Cone.

Note, If a Cone be cut into two segments by a Plane parallel to the Base, one of those segments will be a Cone, and the other segment will have 2 unequal Bases which are Circles, the solidity of which latter segment may be sound out by the rule before given in the 65 question, the Area of, each Base (or circle) being known.

Quest. 68. A Cylinder is a folid which may be well represented by a Stone-roll, such as are used in Gardens for the rolling of Walks. Now if the circumference of a Cylinder be 4.57 seet, and the length 3.25 seet, what is the solid content of that

Cylinder?

Answer, 5.4 + feet, thus found out: First by the help of the given circumference 4.57, find out the superficial content of that Circle) being the Base of the Cylinder) which content (by the preceding 57th question) will be sound 1.6619 + soot, then multiplying the said 1.6619 by the given length 3.25, the product will be 5.4008 which is the solid content required.

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Answer, .601 parts of a foot; For I (to wit. I folid foot) being divided by the base 1.6619, gives in the quotient the decimal .601 for the length required. . . or A odt li won a got odt te

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Quest. 70. A Globe is a perfect round body contained under one Plane; in the midle of the Globe there is a point called the Center, from whence all fireight lines drawn to the outfide are of equal length, and called Semidiameters, the double of any one of which is equal to the Diameter of the Globe; now if the Diameter of a Globe of Stone be 1.75 feet, how many feet solid are contained in that Globe?

Answer, 2.807 + feet, for as 21 is in proportion to 11. or as 1 is to .5238, so is the Cube of the Diameter to the folid content of the Globe: Therefore, multiplying alwayes the Cube of the Diameter by the faid decimal .5238, the product shall be the folid content required: So the Diameter 1.75 being first multiplied by it felf, the product will be 3.0625, which multiplied by the faid 1.75, gives in the product 5.359375, to wit, the cube of the diameter, which being multiplied by .5238, the product thence arising will be 2.807 t, which is the folidity of the Globe propounded.

Quest. 71. What is the Diameter of a Globe of

Stone which contains 4 cubical or solid feet?

Answer, 1.96 + foot for as a 11 is in proportion to 21, or as 1 is to 1.9090909 fo is 4 (the folid content given) to a fourth proportional, to wit, 7.636363 + whose cubick root is 1.96 + the diame-Con ter required .

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Concerning the gaging of Vessals.

callons and about a quart more (found out by the

ere laid to agree very near with thole of an English veffel called a pipe) what is the content of that

rule above given, is will be granifelt by the follo The easiest and aptest wayes for practice in gaging, are those which are perform'd by the help of Tables, or Gaging rods purposely compos'd: Nevertheless to give the Reader of this Treatise some light in this matter, I shall here insert one rule to find out the number of Gallons contained in a full Tun, Pipe, Hogshead, Barrel, or such like veffel, according to Mr. Wingate's way of reducing a Veffel to a Cylinder. The Rule is this;

Having found the difference of the two diameters at the bung and head of the veffel, take 70 of that difference and add it to the leffer diameter; then square that sum and reserve the product; that done, if the content be required in Wine gallons multiply the product reserved, this decimal traction .0034, and the length of the veffel, one into the other (according to the Rule of continual Multiplication) fo thall the last product be the number of Wine gallons required : but if the content be required in Ale gallons, multiply the product before reserved, this decimal fraction .0027, and the length of the veffel, one into the other continually, so shall the product be the content in Ale gallons: This Rule I shall first explain by two questions, and then shew how it is raised.

Quest. 72. If the diameter at the bung of a vessel be 32 inches, the diameter at the head 28.2 inches, and the length 39 inches (which dimensions

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are said to agree very near with those of an English vessel called a pipe) what is the content of that

vessel in Wine gallons ?

Answer, 126.278 Wine gallons, that is 126 Wine gallons and about a quart more (found out by the rule above given, as will be manifest by the following operation.) of saysw flates bas it also said are thole which are perfered.

Explication.

The Diameter at the bung32.0
The Diameter at the head28
Their difference
Which multiplied by 72, that is, -0.7
The product will be 2. 66
Which adddd to the leffer diame-?
Which adddd to the leffer diame-
Which mean diameter being?
fquared (that is, multiplied by it 952 3396
felt) produceth
Which product multiplied by 0 . 0024
The product thence arising will be -3 . 2379+
Which multiplyed by the length of ?
the veffel
The product is the number of \$126.278†
Wine gallons fought, viz

reletived, this countilitation to. Quest. 73. If the diameter at the bung of a barrel be 23 inches, the diameter at the head 19.9 inches, and the length 27.4 inches; what is the content of that barrel in Ale gallons?

Answer, 36.031 Ale gallons, that is 36 gallons and about a quarter of a Pint more (found out by the preceding Rule.) and or alternal and bas a

Explication.

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Explication.

The diameter at the bung	-22 . 0
The diameter at the head	-10.9
Their difference	-3.1
Which multiplied by 72, that is-	-0.7
The product will be	2 . 17
Which added to the leffer diame-7	TO TO THE PARTY OF
ter gives the mean diameter	7-22 . 07
Which mean diameter being	Contenting
fourred (that is . multiplyed by it	487.0849
felf) produceth ————	al agrave again
Which product multiplyed by -	0.0027
The product thence ariting is -	1 . 315+
Which multiplied by the length	10 10 11 2 2 2 2
of the veffel	274 1011
The product is the number of	2 26 22 14
Ale gallons fought, to wit-	30.0311
quated (vor sor other) dismerse com	DOLLAR DIEUPI

The reason of the Rule.

Two things are taken for granted in the said Rule, viz. First, it is supposed that if 7% of the difference of the two diameters at the bung and head, be added to the lesser diameter, the sum shall be an equated or mean diameter (near enough for practical use though it be not exact) viz. If there be a Cylinder whose diameter is equal to that mean diameter, and whose length is equal to the length of the vessel, that Cylinder shall be equal to the capacity of the vessel very near. Secondly

the said Rule presupposeth that 231 cubick inches are equal to a Wine gallon, and 282 equal to an Alegallon; concerning which equalities (efpecially the latter) Artists differ somewhat in their experiments; but according to any equality which in that particular shall be agreed on, from this that follows a rule may be framed, and Tables thence calculated for gaging a full veffel without confiderable error.

Taking then those two things above mentioned for granted, we may rightly infer that if a Cylinder hath for its Base a Circle whose superficial content is 23 1 inches, every inch in length of that Cylinder will contain 231 cubick inches, or one intire Wine gallon; Now forasmuch as all Circles are in such proportion one to the other as the squares of their diameters, it shall be as 294.11844, (to wit, the square of the diameter of that Circle whose superficial content is 231) is to I (to wit, the superficial content 231 considered as the Base of one Wine gallon;) or as I is to .0034; So is the square of the equated (or any other) diameter, to the superficial content of that Circle in Wine gallons and parts of a gallon, which content multiplied by the length of the veffel will produce its folidity or capacity in Wine gallons: Therefore the first part of the preceding rule for finding of the number of Wine gallons contained in a full veffel is manifest: And after the same manner, suppoling as before 282 cubick inches are equal to an Ale gallon, the decimal .0027 prescribed in the faid rule will be found out.

Upon those grounds Mr. Wingate compos'd his Gaging rod; Mr. Oughtred also in his circles of

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os'd his clas of portion Proportion hath delivered another rule for Gaging, from whence his Gaging rod is deduced; but the particular constructions of those rods, and likewise the making of Tables for the same purpose, being handled by several Artists, I shall not

infift upon them.

Now if the industrious and more curious Arithmetician, after he is well exercis'd in vulgar Arithmetick, desires surther knowledge in finding out the Answer of subtil Questions about numbers, his best Guide will be the admirable Algebraical Art, which discovers rules for the solving of Problems, as well Arithmetical as Geometrical, that are above the reach of any of the rules of common Arithmetick, or practical Geometry, as may partly appear by the two rules in the aforegoing 52 and 65 Questions, as also by the two following Questions, with which I shall conclude this Chapter.

Quest. 74. To find two numbers in a given proportion, suppose the lesser to the greater as 2 to 3 and such, that if the lesser number be added to the square of the greater, also if the greater number be added to the square of the lesser, the two sums shall be square numbers whose roots are expressible by rational or true numbers (fractions being admitted for numbers.)

Answer, 70 and 20.

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The Proof.	
The square of -1 (the greater num-?	sdoz.
ber) is —	400
To which adding the leffer number —	-1
The fum in its leaft terms will be	-42
Which is a square number, whose?	400
root is	20
Again, the square of 10 (the lesser?	
number) is	Too
To which adding the greater num-	Jam
ber — — Greater hum-	-3
The fum in its least terms will be -	AN
Which is a Course week of 2	25
Which is a square number whose root?	2
Samuel Sa	12 242

Also the said numbers $\frac{1}{10}$ and $\frac{3}{20}$ are one to the other as 2 to 3, wherefore the question is solved. Which numbers $\frac{1}{10}$ and $\frac{3}{20}$ are found out by this following

Theoreme.

If the fraction 4 be divided into any two parts; either of those parts being increased with the square of the other part shall give a fraction having a rational square root.

Wherefore by dividing \(\frac{1}{4}\) into the two fractions \(\frac{1}{10}\) and \(\frac{1}{20}\), which are in the prescribed proportion of 2 to 3, those fractions will satisfie the conditions

in the question propounded.

Likewise these two fractions $\frac{70.80}{10.80}$ and $\frac{10.81}{10.080}$ will answer the question, and are found out without extracting any root; but the manner of finding out the said Theorem and last mentioned fractions, I have shewn in the 24th question of my third book of the Elements of Algebra.

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Quest. 75. To find 3 numbers, such that the square of any one of them being added to the other two numbers, the sum of such addition shall be a square number, whose root is a rational number.

Answer, 1, 3, and 16.

The proof.

First, the square of the first number?	I part
To which adding the second and? third numbers \(\frac{3}{3} \) and \(\frac{16}{3} \), the sum will be \(\frac{5}{3} \) Which is a square number whose \(\frac{5}{3} \)	9
Secondly, the square of the second?	64
To which adding the first and third? numbers 1 and 16/3, the sum in its least? terms will be	121
Which is a square number whose	111011 113011
Thirdly, the square of the third num-2	256.
numbers 1 and \$ the fum in its least	227
which is a square number whose root is—	12 3

Wherefore it is manifest that the three numbers 1, \frac{8}{3} and \frac{16}{3} will satisfie the conditions in the question, which may be solved also by other numbers, but the manner of finding them out I have shewn in the 32 Question of my third Book of the Elements of Algebra.

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Of Sports and Pastimes.

Probl. I.

To discover a number which any one shall have in his mind, without requiring him to reveal any part of that or any number what soever.

A Fter any one hath thought upon a number at pleasure, bid him double it, and to that double bid him add any such even number which you please to assign, then from the sum of that addition let him reject one half, & reserve the other half: Lastly from this half bid him to subtract the number which he first thought upon, then may you boldly tell him what number remaineth in his mind after that subtraction is made, for it will alwayes be half the

number which you affigned him to add.

For example suppose he thought upon 6, the double thereof is 12, to which bid him add some even number at your pleasure, suppose 4, so will the sum be 16, whereof the halt is 8, from which if he subtract 6 (the number first thought on) the remainder is 2 (to wit, half the number 4, which was by you assigned to be added;) which remainder you discover, notwithstanding all the operation was performed in his mind, without his making known of any number whatsoever. Note that the adding of an even number as aforesaid is not of necessity, but only to avoid a fraction which will arise by taking the half of an odd number.

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The reason of the Rule.

If to the double of any number (which number for distinction sake I call the first) a second number be added, the half of the sum must necessarily confist of the said first number, and half the second; therefore it from the said half sum the first number be subtracted, the remainder must of necessity be half of the second number which was added.

Probl. II.

Two numbers, the one even and the other odd, being propounded unto two persons, to the end they may (out of your sight) severally chuse one of those numbers; to discover which of these numbers each person shall have chosen.

Suppose you have propounded unto Peter and John two numbers, the one even and the other odd, as 10 and 9, and that each of those persons is to chuse one of the said numbers unknown to you. Now to discover which number each person shall have chosen, you must take two numbers, the one even and the other odd, as 2 and 3; then bid Peter multiply that number which he shall have chose, by 2; and cause John to multiply that number which he shall have chosen by 3; that done, bid them add the two products together, and let them make known the fum to you, or else demand of them whether the said sum be even or odd, or by any other way more secret endeavour to discover it, by bidding them to take the half of the faid fum, for

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for by knowing whether the said sum be even or odd, you do obtain the principal end to be aimed at, because if the said sum be an even number, then infallibly he that multiplied his number by your odd number(to wit, by 3) did chuse the even number (to wit, 10;)but if the faid fum happen to be an odd number, then he whom you caused to multiply his number by your odd number (to wit, by 3) did infallibly chuse the odd number (to wit, 9.)

For example, if Peter had made choice of 10, and John o, suppose you willed Peter to multiply his number 10 by 2, and John, to multiply his number 9 by 3; the products will be 20 and 27, whereof the sum is 47, which being an odd number, you may thence conclude that John whom you caused to multiply his number by 3, did chuse the odd number 9, and therefore Peter did chuse 10. But if you had willed John to have multiplied his number 9 by 2, and Peter to have multiplyed his number 10 by 3, the products would have been 18 and 30, whereof the sum is 48, which is an even number, from whence you may infer that he that multiplyed his number by 3 did chuse the even number, and therefore Peter had chose 10, and John 9.

Demonstration.

The reason of the said rule is very easie, and dependeth principally upon the 28 and 29 propositions of the 9th book of Euclid; for one may infer from the 21 of the same book, that an even number multiplied by any number whatfoever produceth an even number, but an odd number is of a different nature, for if it be multiplied by an even num-

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ber, the product is an even number (by the said 28 proposition;) and if it be multiplied by an old number, the product is odd (by the said 29 proposition.) Therefore if in making this sport it happeneth that the even number be multiplied by your odd number, both the products shall be even, and consequently the sum shall be infallibly an even number (by the said 21 proposition.) But if it happen that you cause the odd number to be multiplied by your odd number, that product will be odd, and the other product even, therefore the sum of these two products shall be an odd number (as Clavius hath demonstrated upon the 23. of the 9th. of Euclid.

Probl. 3.

A certain number of distinct things being propounded, to dispose them in such an order, that casting away alwayes the ninth, or the tenth, or any other that shall be assigned, unto a certain number, those remaining may be such as were first intended to be left.

This Problem is usually propounded in this manner, viz. fifteen Christians and fifteen Turks being at Sea in one and the same Ship in a terrible storm, and the Pilot declaring a necessity of casting the one half of those persons into the Sea, that the rest might be saved; they all agreed that the persons to be cast away should be set out by lot after this manner, viz. the thirty persons should be placed in a round form like a Ring, and then beginning to count at one of the Passengers, and proceeding circularly, every ninth person should be cast into the Sea, until of the thirty persons

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there remained only fifteen. The question is, how those thirty persons ought to be placed, that the lot might infallibly fall upon the fitteen Turks, and not upon any of the fifteen Christians? For the more easie remembring of the rule to resolve this question, I shall presuppose the five vowels, a,e,i,o,u to signific five numbers, to wit, (a) one, (e) two. (i) three, (o) four, and (u) five; then will the rule it self be briefly comprehended in these two solutioning verses.

From numbers, aid and art Never will fame depart.

In which verses you are principally to observe the vowels, with their correspondent numbers before assigned, and then beginning with the Christians, the vowel o (in form) signifieth that sour Christians are to be placed together; next unto them, the vowel u (in num) signifieth that sive Turkes are to be placed; In like manner e (in bers) denoteth 2 Christians, a (in aid) 1 Turk, i (in aid) 3 Christians, a (in and 1 Turk, a (in art) 1 Christian, e (in ne) 2 Turkes, e (in ver) 2 Christians, i (in will) 3 Turkes, a (in fame) 1 Christian, e (in fame) 2 Turkes, e (in de) 2 Christians, a (in part) 1 Turk.

The invention of the said Rule, and such like, dependeth upon the subsequent demonstration, viz. if the number of persons be thirty, let thirty figures or ciphers be placed circularly, or else in a right

line as you fee,

That done, begin to count from the first, and mark

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mark the ninth (or what other shall be assigned) by putting a point or cross over it; then count forward from that which you have marked, and place another point over the next ninth; and continue to do the same, beginning again when you shall be at the end (if the cyphers are placed in a right line) and paffing over those, which you shall have already marked, until you have marked the number required, as in the example propounded, untill you have marked fifteen, for then all the cyphers marked shall be those which must be cast away, and the others those which shall remain. Hence it is evident, that if you observe how those cyphers which are marked, are disposed amongst those which are not marked, you will easily make a rule for any number whatfoever.

By this invention (as some do conjecture) the famous Historian Josephus the Jew, preserved his life very fubtily in the Cave, to which himself and forty of his Countreymen had fled from the furious and conquering Romans at the Seige of Fotapata: for his faid Countreymen having most wickedly refolved to kill one another, rather than yield to their enemies, he at length (when no arguments that he could use would disswade them from so horrid an act) prevailed with them to execute their tragical design by lot; and so by the help of the aforefaid artifice (as we may suppose) himself with one other person only remaining alive, after the rest were inhumanly murthered, they agreed to put an end to the lot, and thereby fave their lives. This ftory you may see at large in the fourteenth Chapter of the third book of the History of Fosephus of the Warrs of the Jews. Probl.

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Probl. 4.

Many numbers which proceedfrom I or unity in a progression, according to the natural order of numbers, (such as these, 1,2,3,4,5,6,&c.) being placed in a round form like a Ring; to discover which of those numbers any one shall have thought upon.

Let any multitude of numbers in the aforesaid progression, suppose these 10, to wit, 1.2.3.45.6.7.8.9.10. be written upon 10 ivory counters (or for want thereof upon 10 small pieces of paper) which may be represented by these 10 letters, A. B.C.D.E.F.G.H.I.K.L.viz. suppose 1 to be written upon the counter A, 2 upon B, 3 upon C, &c. Then having placed those Counters circularly as you see (with their blank saces uppermost, and the figures underneath, that the subtilty of the sport

STARKE SE	A A gains
L 10 K 9	2 B 3 C
H 8	4 D 5 E
	6 bas poly

may the better be concealed) let any one think upon any number of unities which doth not exceed 10; that done bid him touch one of those Counters at pleasure, and to the number on the backside of the counter touched (which you cannot be ignorant of, having noted well the place of 1 or

A)

A) add fecretly in your mind, the just number of all the counters, and reserve the sum; then bid him imagine in his mind the counter touched to be the number which he thought; and from that counter to count backwasds, until he shall have made up the aforesaid sum, which you reserved, so will his computation infallibly end upon the counter upon which the number thought upon is written.

For example, suppose that he thought 7 or G, and that he touched B, to wit, 2 Add to 2 the number of all the counters, to wit, 10, so the sum will be 12; then bid him to count unto 12 beginning at B and going backwards, and esteeming B to be the number thought, to wit 7, so will 8 fall upon A, 9 upon L, 10 upon K, 11 upon H, and lassly, 12 upon the counter G, which being turned up will shew 7 the

number thought, multiple of laupe of the

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The reason of this rule is not difficult to be apprehended, two principles being presupposed, the one is this, to wit, many counters or things whatfoever being disposed orderly one after the other, in one continued line, whether it be right or circular; if you value or name the first counter to be some number of unities at pleasure, and continue to count forward according to their natural order of numbers, untill another number be named which falleth upon the last counter; or if you imagine or name the last counter, to be the same number of unities as before you put upon the first, and contitinue to count backwards unto the first counter; I fay, that the same number will be named at the end of both those computations: for example, in these 9 letters A.B.C.D. E.F. G.H.K. if the letter A be effeemed

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esteemed to be 4, and from thence you count forwards unto K, according to the natural order of numbers, the letter K will fall upon the number 12. In like manner, if you esteem K to be 4, and count backwards from K to A, the letter A will likewise fall upon 12.

4.	5.	6.	7.	8.	9.	10.	II.	12,
A.	B.	C.	D.	E.	F.	10. G.	H.	K.
						6.		

The other principal is this, to wit, many counters being disposed in a round manner like a Ring, if you esteem any one of those contents to be some number at pleasure, and then from that counter if you count circularly, until you end upon the counter where you began, the number last named will be equal to the sum of the number of all the counters, and of the number which you put upon the sirst counter; for example; If D be one of 10 Letters placed in a circumference, and that imagining D to be 7, you begin with it, and count round the whole circumference, according to the natural progression of numbers, till

to count terward accord A c to cheir

L 10 K 9		B 3 C
H 8 G 7	5	4 D E
and topics and	-	dines :

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You end with D where you began; the number 17 which is composed of 10 and 7 will necessarily fall upon D; for 9 (which is the number of letters in the circumference besides D) being added to 7 (which was first put upon D) makes 16, to which 1 being added (because D doth end as well as begin the circumference) the fum is 17.

Now these two principles being presupposed, it will not be difficult to appehend the reason of the aforesaid rule in all cases that can happen ; for imagine that one hath thought upon 7, or the counter G, then that counter which he shall touch must either be the same counter G or some other

that proceedeth or followeth G. dw as danger as fort

First therefore supposing the counter or number touched to be the same with the number thought the truth of the rule will be then evident, for by the rule given, he shall begin to count from the same G unto 17, putting 7 upon G, therefore by the fecond presupposition the number 17 will fall fame G. And because G being supposed to E.D noqu

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Secondly imagine that he touched a counter or number following G the number thought, as L or 10. then according to the rule adding 10 (the multitude of all the counters placed circularly) unto 10; or L (the counter touched) bid him count backwards unto 20 by beginning at L, and esteem L to be 7. Now because by beginning to count at G which is 7, and proceeding to count forward, the number 10 will fall upon L; therefore by the first presupposed principle, if we esteem L tobe 7 and count backwards, the number 10 will infallibly fall upon G, and then the number 20 (hall also fall upon the same G by the second presupposed principle. Laftly.

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Laftly, imagine he touched forme number or counter which precedeth 7 the number fought, as B or 2; then adding 10 to 2, you are to bid him count unto 12, he having first imagined B to be the number thought 7, and going backwards to A,L, K, &c. Now because by proceeding to count at B, which is 2, and beginning to count forward to C, Dies the number 7 falleth upon G; therefore if one imagine that Gis 2, and from thence count backwards towards F.E. &c. the number 7 will fall upon Bo (by the first presupposed principle;) therefore when one affumeth B to be 7, and counteth towards A, L, &c. to any affigued number, it is in effect as much as when one imagineth G to be 2, and counteth towards F.E. &c. unto the faid affigned number, for each of those computations will end in the fame point; but it is manifest (by the second presupposed principlen) that effeeming G to be 2, and counting towards F.E.D. &c. round the whole circumference, the number 12 will fall upon the same G. And because G being supposed to be 2, and counting on the same coast as before, the number 7 falls upon B; therefore if the computation be continued on the same coast from B 7 unto 12, the number 12 will fall upon the fame G. So that the practice of this sport in all its cases is fully demonfirated. I to guinaigad yel os otatu abray

Note, that to the number of the counter touched you may not only add the number of all the counters once (as the rule directs) but twice, thrice or more times: for example, B being touched, you may cause him to count unto 12, or unto 22, or to 32, 42, &c. the reason whereof is evident from the second presupposed principle.

Probl.

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you fee in the feconizh, idor from A towards B;

then place a underneath x , and 5 after 3 f in the Many numbers being shewed by pairs, to wit, two by two, unto any one, that be may think upon any one of those pairs at pleasure; to discover the pair that was thought upon. Q whom all sould mit. toher in the rank CD. and tal under va. Mirelovex

Let 20 numbers, suppose these, 1.2.3.4.5.6.7. 8.9.10.11.12.13.14.15.16.17.18.19.20. be written upon Ivory counters (or for want thereof upon smal pieces of paper) to wit, I upon one counter, 2 upon another, 3 upon a third, &c. Then difpose them into pairs as you see, viz. suppose 1 and 2 to be one pair, 3 and four to be another

	THE RESERVE THE PERSON NAMED IN	State Street
2 2	16	2
12 1 13	3.	4
1 24 91	5.	6
0.5 0.1	7-	8
DEEC	9. 1	0
	11. 1	2
n tripugiti	13. 1	4
ad illiali a	15. 1	6
CO boost	17.	8
, manualit	19. 2	0
DIES DES COLUMN	De 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	The same of

pair, &c. and of these pairs let any one think upon which pair he pleaseth. That done you are to difiribute the faid 20 numbers in ranks, in the form of a long square, until there be 5 numbers in length, and 4 in breadth, after this manner. vize lay

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lay the three first numbers 1, 2, and 3 in a rank (as you see in the second figure) from A towards B; then place 4 underneath 1, and 5 after 3 (in the said rank AB.) Again place 6 under 4, and 7 after 5 (in the said rank AB.) Then place 8 under 6, al-10 9.10.11 on the right hand of 4 in the rank CD. Again place 12 under 9, and 13 on the right hand of 11 in the rank CD. and 14 under 12. Moreover place 15.16.17. on the right hand of 12 in the rank EF. Lastly, place 18.19.20. on the right hand of 14 in the rank GH, so will all the numbers be ranked as you fee in the Table. That done, you are to demand of him that thought upon two numbers as aforesaid, in what rank or ranks the said numbers do happen to be found, viz.

A	1	2	3	5	7	B
C	4	9	10	II	13	D
E	6	12	15	16	17	F
G	8	14	18	19	20	H

in which of the ranks AB, CD, EF, GH, or in which two of the said ranks: now if he answer that the two numbers which he first thought upon are in the first rank AB. then I and 2 shall be the numbers thought upon; if in the second CD, then 9 and 10 shall be the numbers thought; if in the third rank EF, then I5 and 16 shall be the numbers thought: if they are in the sourth rank GH, then 19 and 20 shall be the numbers thought; but if he shall say that the numbers thought are in different ranks, then you are heedfully to mark the said numbers I and 2, 9 and 10, 15 and 16, 19 and 20, which

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which may be called the keys of the sport, in regard they ferve not only to discover the two numbers thought, when they are both in one and the fame rank (as aforesaid) but also when they are in two different ranks, for in this latter case as soon as it hath been declared to you in which two ranks the two numbers thought are placed, you must take the key of the highest of those two ranks, and descending in a down right line from the first number of that key unto the lower of the faid two ranks, you shall there find one of the two numbers thought, and upon the right hand of the second number of the said key, at the same distance fidewife from the second number of the key, as one of the numbers thought was distant from the first number of the key, you shall find the other number thought.

For example, suppose the two numbers thought are 7 and 8, and that it shall be declared unto you that they are in the sirst and sourth ranks; take then the key of the highest of these two ranks, to wit of the sirst, which is 1 and 2, and descending down right from 1 unto the sourth rank, you shall there find 8 one of the numbers thought; then seek side wise on the right hand of 2 (the second number of the key) a number as far separated from 2, as 8 is distant from 1, and you will find 7 the other

number thought.

Again, suppose he saith that the numbers thought are in the second and third ranks; take then the key of the second rank which is 9 and 10, and descending downright from 9 to the third rank, you shall there find 12 which is one of the numbers thought; then seek sidewise on the right hand

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hand of 10 (the second number of the key) a number as far distant from 10 as 12 is from 9, and you shall find II which is the other number thought.

The reason of this will be apparent from a serious consideration of the placing of the numbers according to the rules before given, for it is thereby evident that of the two numbers coupled two by two, there can never be found more then one pair in one and the same rank, and of all the other pairs one number is alwayes found in one rank, and the other number in an other rank.

Note also, that this sport may be practifed with divers persons at once, and not only with 20 numbers, but with any such multitude of numbers which is produced by the multiplication of any two numbers which differ by I or unity; as 30, which is the product of 5 multiplied by 6, and 42 which is the product of the multiplication of 6 and 7. That which is chiefly to be regarded is the placing of the numbers in ranks according to the directions before given : and for the more easie comprehending of that order, I have in the following Table ranked 30 numbers in their due places. which being compared with the former Table, and well viewed, will be a clearer illustration than can be exprest by many words.

I	2	3	5	7	9
41	11	12	13	115	17
				21	COLUMN TWO IS NOT THE OWNER.
8 4	16	22	25	26	1 27
10	18 1	24 1	28 1	29	30

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Three jealous bushands with their wives, being ready to pass by night over a river, do find at the river side a boat which can cary but two persons at once, and for want of a Boatman they are necessitated to row themselves over the river at the several times: the question is how these 6 persons shall pas 2 by 2, so that none of the 3 wives may be found in the company of 1 or of 2 men unless her husband be present.

They must pass in this manner, viz. First two women pass, then one of them bringeth back the boat and repasseth with the third woman; that done, one of the three women bringeth back the boat, and sitting down upon the ground with her husband permitteth the other two men to pass over to find their wives; then one of the said men with his wife bringeth back the boat, and placing her upon the ground he taketh the other man and repasseth with him; lastly, the woman which is found with the three men entereth into the boat, and at twice goeth to setch over the other two women.

Probl. 7. mi from sell as a seld

Two merry companions are to have equal shares of 8 Gallons of wine, which are in a vessel containing exactly 8 Gallons, now to make this equal partition they bave only two other empty vessels, whereof one containeth 5 Gallons, and the other 3; the question is, how they shall exactly divide the wine by the help of those three vessels.

First, from the vessel which containeth 8 gallons and

and is full of wine, let 5 gallons be poured into the empty veffel of 5, and from this veffel fo filled let 3 be poured into the empty veffel of three, so there will remain 2 gallons within the veffel of 5. Then let the three gallons which are within the veffel of 3 be poured into the vessel of 8, which will now have 6 gallons within it, that done let the 2 gallons which are in the veffel of 5, be put into the empty veffel of 3, then of the 6 gallons of wine which are within the veffel of 8 fill again the five, and from those 5 pour out I gallon into the veffel of 3, which wanted only I gallon to fill it, fo there will remain exactly 4 gallons within the veffel of \$ and 4 gallons within the other two veffels. question may be resolved in another way, but I leave that as an exercise to the wit of the ingenious Reader.

Now albeit at first sight it may be thought by some, that the two last mentioned Problems cannot be resolved by any certain Rule, but only by many trials, yet by infallible argumentation and discourse, the solution of those questions may be sound out or else the impossibility of them, if by chance they should have been propounded impossible; as the most ingenious Gasper Backet hath manifested in a little Book in the French Tongue, intituled Problemes plaisans & delectables qui se font par les nombres, from which book I have extracted the Contents of this Chapter.

Soli Deo Gloria.

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