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ELEMENTARY LESSONS

IN

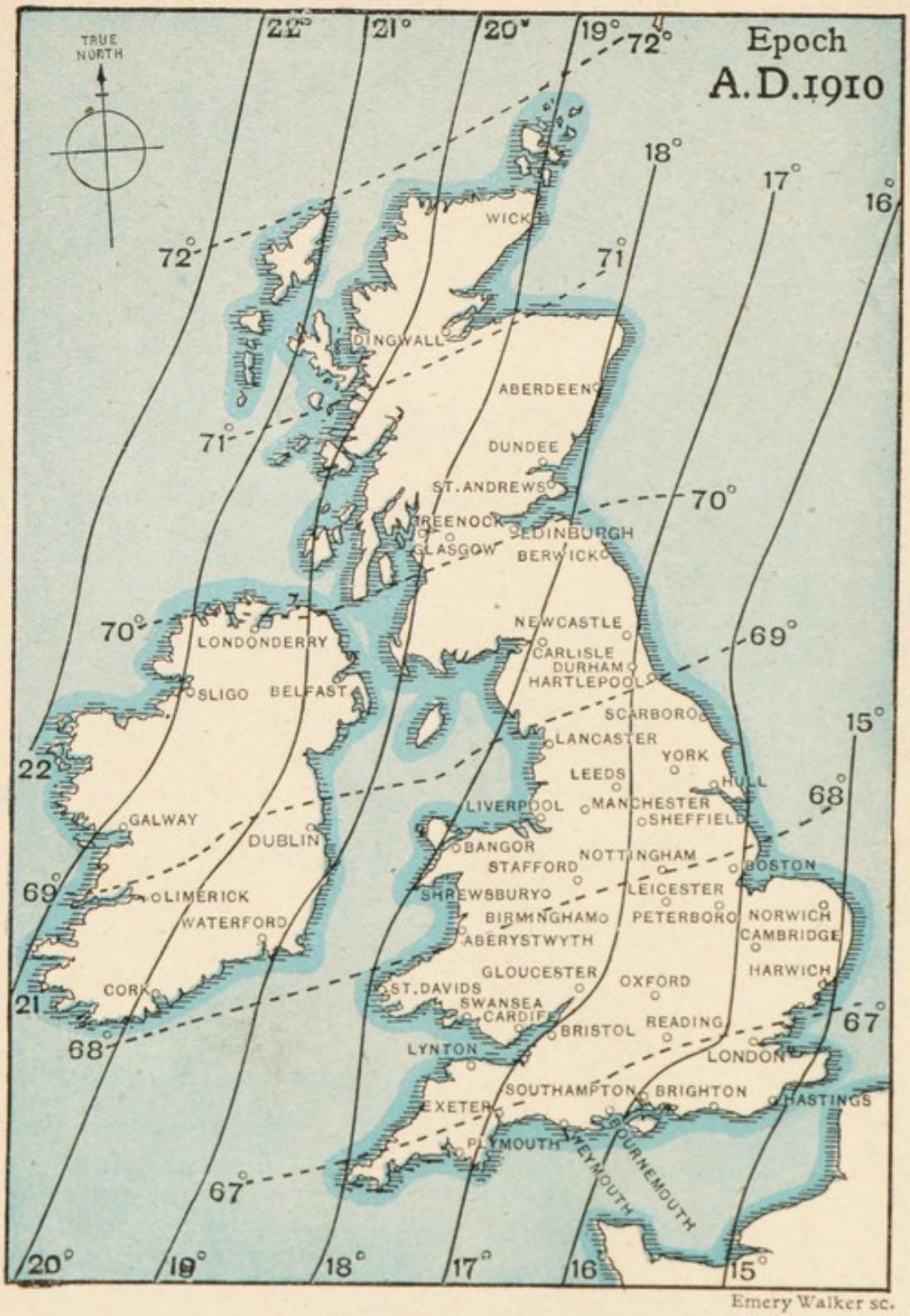
ELECTRICITY AND MAGNETISM



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ELEMENTARY LESSONS

IN

ELECTRICITY & MAGNETISM

BY

SILVANUS P. THOMPSON

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PREFACE

For the purpose of the present edition the entire work has been completely revised, and in many parts re-written. Progress in the development of the industrial applications of electricity has been so great in the past decade as to necessitate the remodelling of the latter half of the book. A new chapter has been added on Wireless Telegraphy, and another on the modern conception of the Electron.

The author returns cordial thanks to various professional friends and electrical engineers who have aided him with information. He has to thank Dr. C. Chree, F.R.S., of the Kew Observatory, for sundry magnetic data, and Professor L. A. Bauer, of Washington, for material used in preparing the magnetic map of North America.

He is indebted for help in the revision to his daughter, Helen G. Thompson, B.Sc., and to his assistant, Mr. Richard Gosden, who has been indefatigable with checking numerical calculations, and with proof-reading.

SILVANUS P. THOMPSON.

July 1915.

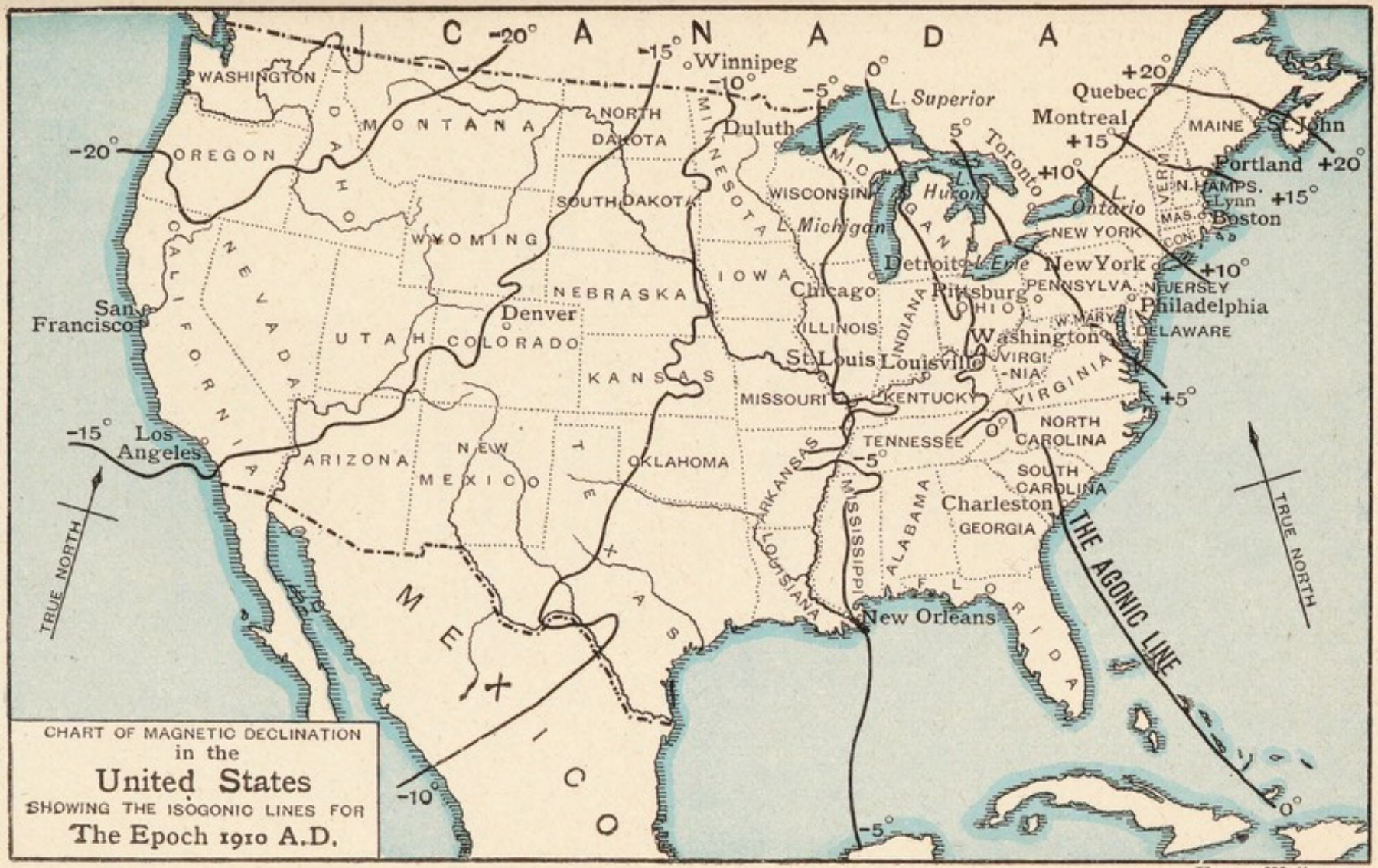


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ELEMENTARY LESSONS

IN

ELECTRICITY & MAGNETISM

Part First

CHAPTER I

FRICTIONAL ELECTRICITY

LESSON I.—*Electric Attraction and Repulsion*

1. Electricity.—*Electricity* is the name given to an invisible agent known to us only by the effects which it produces and by various manifestations called *electrical*. These manifestations, at first obscure and even mysterious, are now well understood, though little is yet known of the precise nature of electricity itself. Electricity is neither matter nor energy; yet it apparently can be associated or combined with matter; and energy can be spent in moving it. Indeed its great importance to mankind arises from the circumstance that by its means energy spent in generating electric forces in one part of a system can be made to reappear as heat or light or work at some other part of the system; such transfer of energy taking place even to very great distances at an enormous speed. Electricity is apparently as indestructible as matter or as

energy. It can neither be created nor destroyed, but it can be transformed in its relations to matter and to energy, and it can be moved from one place to another. In many ways its behaviour resembles that of an incompressible liquid; in other ways that of a highly attenuated and weightless gas. It appears to exist distributed nearly uniformly throughout all space. Many persons consider it as having to do with the luminiferous *ether*. There is an intimate relation between the two. That this must be so, is a necessary result of the great discovery of Maxwell —the greatest scientific discovery of the nineteenth century—that light itself is an electric phenomenon, and that the light-waves are merely electric, or, as he put it, electromagnetic waves. Electricity is now regarded as consisting of immense numbers of excessively minute atomic quantities, equal amongst themselves, each such atomic quantity being called one *electron*. The modern doctrine of electrons is stated in Art. 630, p. 668.

2. The Science and its Subdivisions.—The name *electricity* is also given to that branch of science which deals with electric phenomena and theories. The phenomena, and the science which deals with them, fall under four heads. The manifestations of electricity when standing still are different from those of electricity moving or flowing along: hence we have to consider separately the properties of (i.) statical *charges*, and those of (ii.) *currents*. Further, electricity whirling round or in circulation possesses properties which were independently discovered under the name of (iii.) *magnetism*. Lastly, electricity when in a state of rapid oscillation manifests new properties not possessed in any of the previous states, and causes the propagation of (iv.) *waves*. These four branches of the science of electricity are, however, closely connected. The object of the present work is to give the reader a general view of the main facts and their simple relations to one another.

In these first lessons we begin with charges of

electricity, their production by friction, by influence, and by various other means, and shall study them mainly by the manifestations of attraction and repulsion to which they give rise. After that we go on to magnetism and currents, and the relations between them. The subject of electric waves is briefly discussed at the end of the book.

3. Electric Attraction.—If you take a piece of

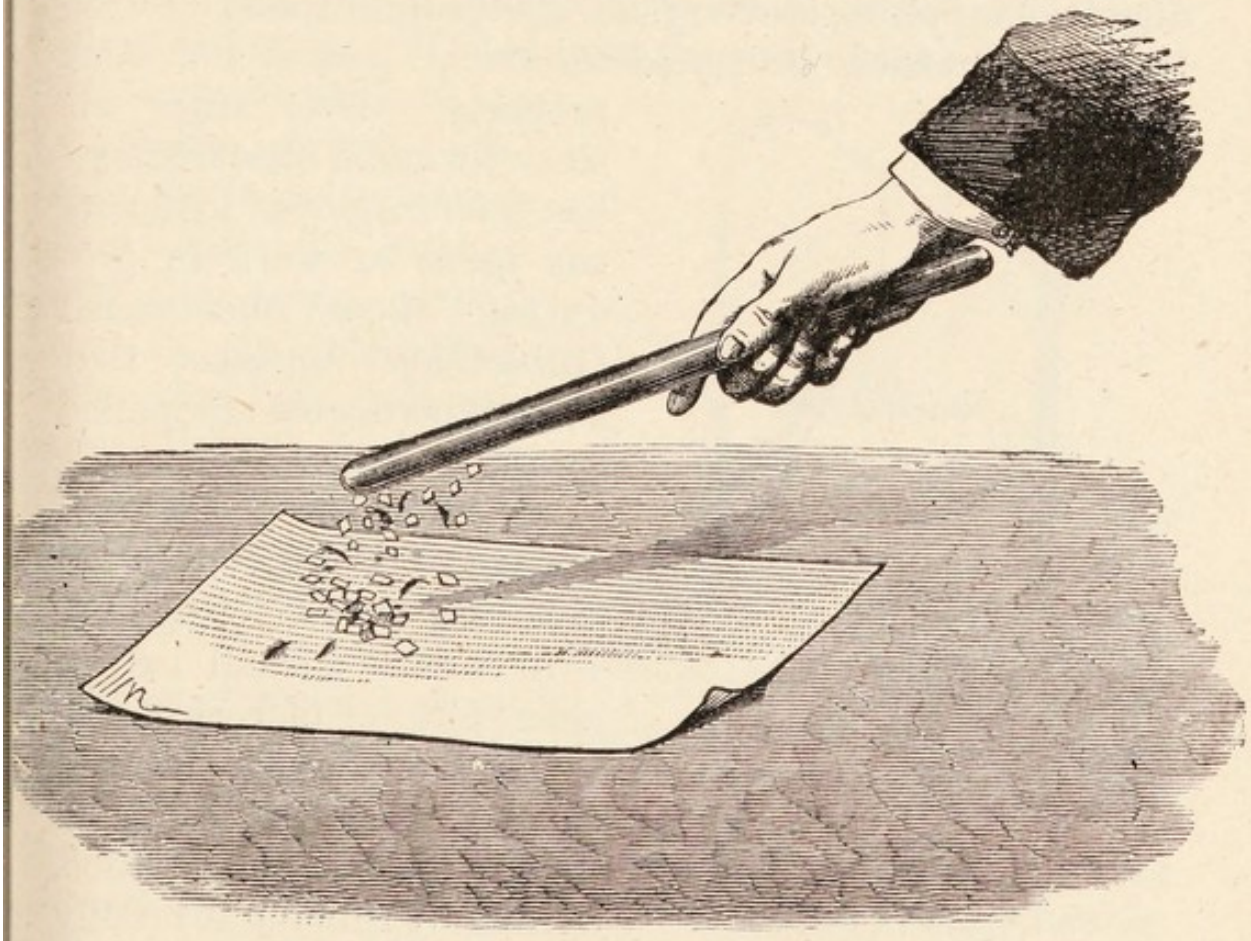


FIG. 1.—Electric Attraction of Light Bodies.

sealing-wax, or of resin, or a glass rod, and rub it upon a warm, dry piece of flannel or silk, it will be found to have acquired a property which it did not previously possess: namely, the power of attracting to itself such light bodies as chaff, or dust, or bits of paper (Fig. 1). This curious power was originally discovered to be a property of **amber**, or, as the Greeks called it, ἤλεκτρον (*elektron*), which is mentioned by Thales of Miletus (B.C. 600), and by Theophrastus in his treatise on Gems, as attracting light bodies

when rubbed. Although an enormous number of substances possess this property, amber and jet were the only two in which its existence had been recognised by the ancients, or even down to so late a date as the time of Queen Elizabeth. About the year 1600, Dr. Gilbert of Colchester discovered by experiment that not only amber and jet, but a very large number of substances, such as diamond, sapphire, rock-crystal, glass, sulphur, sealing-wax, resin, etc., which he styled *electrics*,[1] possess the same property. Ever since his time the name **electricity**[2] has been employed to denote the agent at work in producing these phenomena. Gilbert also remarked that these experiments are spoiled by the presence of moisture.

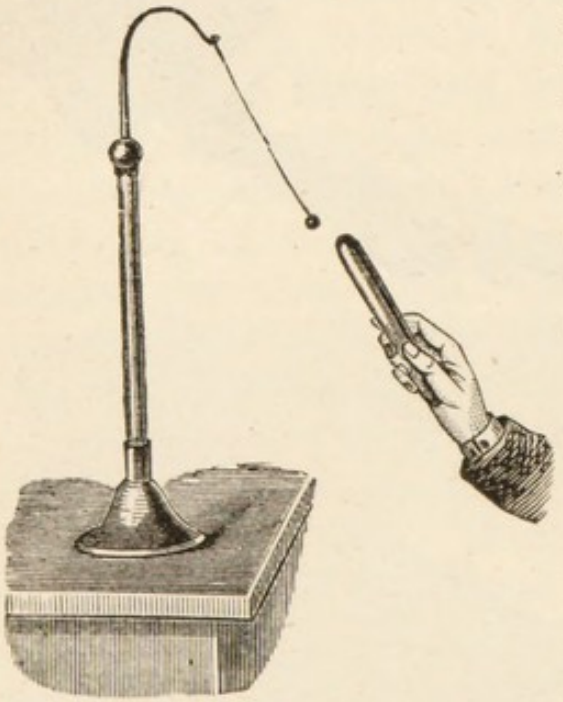


FIG. 2.—Attraction of Pith-Ball.

4. Further Experiments.—A better way of observing the attracting force is to employ a small ball of elder pith, or of cork, hung by a fine thread from a support, as shown in Fig. 2. A dry warm glass tube, excited by rubbing it briskly with a silk handkerchief, will attract the pith-ball strongly, showing that it is highly *electrified*. The most suitable rubber, if a stick of sealing-wax is used, will be found to be flannel, woollen cloth, or, best of all, fur. Boyle discovered that an electrified body is itself attracted by one that has not been electrified. This may

[1] "*Electrica*: quae attrahunt eadem ratione ut electrum" (Gilbert).

[2] The first work in which this term was used is that of Dr. Thomas Browne, *Enquiries into Vulgar and Common Errors*, published in London, 1646; the oldest book devoted to electricity is Robert Boyle's *Experiments and Notes about the Mechanical Origine or Production of Electricity*, printed at Oxford, 1675.

be verified (see Fig. 3) by rubbing a stick of sealing-wax, or a glass rod, and hanging it in a wire loop at the end of a *silk* thread. If, then, the hand be held out towards the suspended electrified body, the latter will turn round and approach the hand. So, again, a piece of silk ribbon, if rubbed with warm indiarubber, or even if drawn between two pieces of warm flannel, and then hung up by one end, will be found to be attracted by objects presented to it. If held near the wall of the room it will fly to it and stick to it.

With proper precautions it can be shown that *both* the rubber and the thing rubbed are in an electrified state, for both will attract light bodies; but to show this, care must be taken not to handle the rubber too much. Thus, if it is desired to show that when a piece of fur is rubbed upon sealing-wax the fur becomes also electrified, it is better not to take the fur in the hand, but to cement it to the end of a glass rod as a handle. The reason of this precaution will be explained toward the close of this lesson, and more fully in Lesson IV.

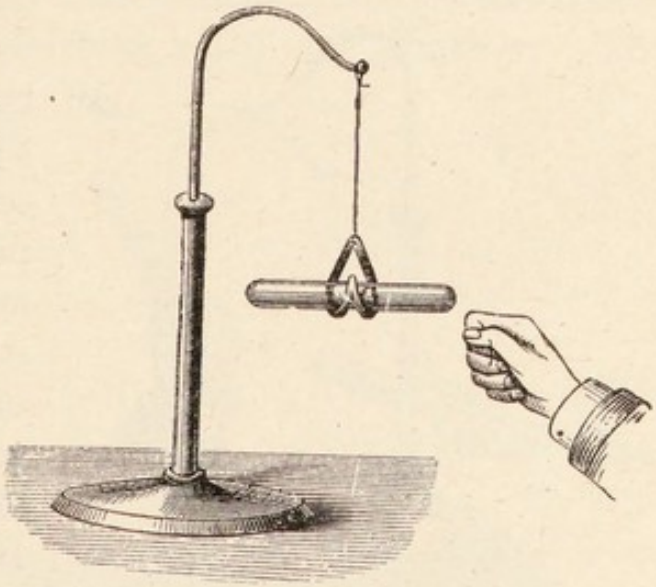


FIG. 3.—Rubbed Glass Rod attracted by the Hand.

A large number of substances, including iron, gold, brass, indeed all the metals, and stony substances such as slate and marble, and ordinary woods, when held in the hand and rubbed, exhibit no sign of electrification—that is to say, do not attract light bodies as rubbed amber and rubbed glass do. Such bodies were, on that account, formerly termed *non-electrics*; but the term is erroneous, for if they are mounted on glass handles and then rubbed with silk or fur, they behave as electrics.

5. Electric Repulsion.—When experimenting, as in Fig. 1, with a rubbed glass rod and bits of chopped paper, or straw, or bran, it will be noticed that these little bits are first attracted and fly up towards the excited rod; but that, having touched it, they are speedily repelled and fly back to the table. To show this repulsion better, let a small piece of feather or down be hung by a silk thread to a support, and let an electrified glass rod be held near it. It will dart towards the rod and stick to it, and a moment later will dart away from it, repelled by an invisible force (Fig. 4), nor will it again dart towards the rod. If the experiment be repeated with another feather, and a stick of sealing-wax rubbed on flannel, the same effects will occur. But, if now the hand be held towards the feather, it will rush toward the hand, as the rubbed body (in Fig. 3) did. This proves that the feather, though it has not itself been rubbed, possesses the property originally imparted to the rod by rubbing it. In fact, it has become electrified, by having touched an electrified body which has given part of its electricity to it. It would appear then that two bodies electrified with the same electrification repel one another. This may be confirmed by a further experiment. A rubbed glass rod, hung up as in Fig. 3, is repelled by a similar rubbed glass rod; while a rubbed stick of sealing-wax is repelled by a second rubbed stick of sealing-wax. Another way of showing the repulsion between two similarly electrified

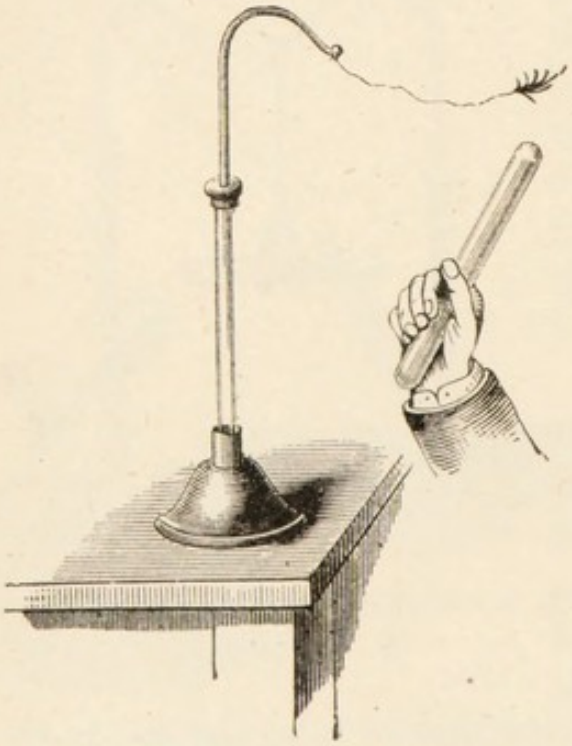


FIG. 4.—Repulsion of Feather.

bodies is to hang a couple of small pith-balls, by thin linen threads, to a glass support, as in Fig. 5, and then touch them both with a rubbed glass rod. They repel one another and fly apart, instead of hanging down side by side; while the near presence of the glass rod will make them open out still wider, for now it repels them both. The self-repulsion of the parts of an electrified body is beautifully illustrated by the experiment of electrifying a soap-bubble, which *expands* when electrified.

6. Two Kinds of Electrification. — Electrified bodies do not, however, always repel one another. The feather which (see Fig. 4) has been touched by a rubbed glass rod, and which in consequence is repelled from the rubbed glass, will be *attracted* if a stick of rubbed sealing-wax be presented to it; and conversely, if the feather has been first electrified by touching it with the rubbed sealing-wax, it will be attracted to a rubbed glass rod, though repelled by the rubbed wax. So, again, a rubbed glass rod suspended as in Fig. 3 will be attracted by a rubbed piece of sealing-wax, or resin, or amber, though repelled by a rubbed piece of glass. The two pith-balls touched (as in Fig. 5) with a rubbed glass rod fly from one another by repulsion, and, as we have seen, fly wider asunder when the excited glass rod is held near them; yet they fall nearer together when a rubbed piece of sealing-wax is held under them, being attracted by it. Symmer first observed such phenomena as these, and they were independently discovered by Du Fay, who

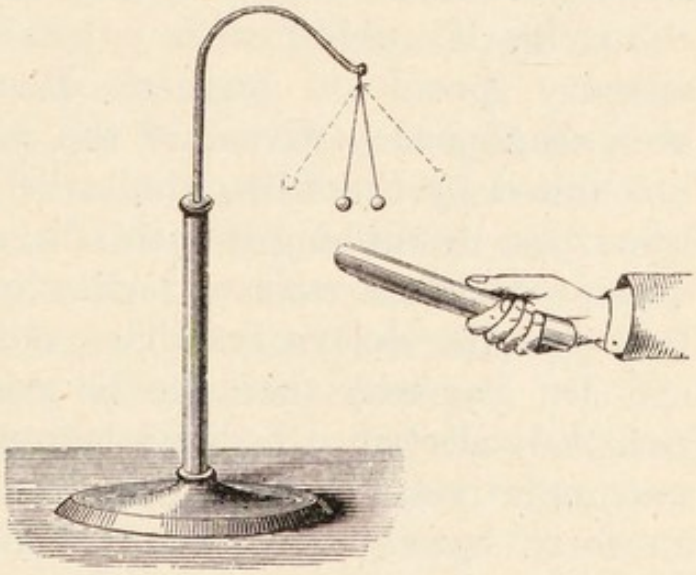


FIG. 5.—Repulsion between Pith-Balls.

suggested in explanation of them, that there were two different kinds of electricity which attracted one another, while each repelled itself. The electricity produced on glass by rubbing it with silk he called *vitreous* electricity, supposing, though erroneously, that glass could yield no other kind; and the electricity excited in such substances as sealing-wax, resin, shellac, indiarubber, and amber, by rubbing them on wool or flannel, he termed *resinous* electricity. The kind of electricity produced is, however, found to depend not only on the thing rubbed but on the rubber also; for glass yields "resinous" electricity when rubbed with a cat's skin, and resin yields "vitreous" electricity if rubbed with a soft amalgam of tin and mercury spread on leather. Hence these names have been abandoned in favour of the more appropriate terms introduced by Franklin, who called the electricity excited upon glass by rubbing it with silk, *positive* electricity, and that produced on resinous bodies by friction with wool or fur, *negative* electricity. The observations of Symmer and Du Fay may therefore be stated as follows:—Two positively electrified bodies apparently repel one another: two negatively electrified bodies apparently repel one another: but a positively electrified body and a negatively electrified body apparently attract one another. It is now known that these effects which appear like a repulsion and an attraction between bodies at a distance from one another, are really due to actions going on *in the medium* between them. The positive charge does not really attract the negative charge that is near it; but both are urged toward one another by stresses in the medium in the intervening space.

7. Simultaneous Production of both Electrical States.—Neither kind of electrification is produced alone; there is always an equal quantity of both kinds produced; one kind appearing on the thing rubbed and an equal amount of the other kind on the rubber. It is possible in certain cases to give clear proof that these

amounts are *equal*. For it is found that if both the electricity of the rubber and the electricity of the thing rubbed be imparted to a third body, that third body will show *no electrification at all*, the two equal and opposite electrifications having exactly neutralized each other. A simple experiment consists in rubbing together two disks, one of sealing-wax, and the other of wood covered with flannel, both being held by handles of glass or ebonite. To test them an insulated pot and an electroscope are required as in Fig. 28. If, after being rubbed together, either disk be inserted in the pot the leaves of the electroscope will diverge; but if both are inserted at the same time the leaves do not diverge, showing that the two charges on the disks are equal and of opposite sign.

In the following list the bodies are arranged in such an order that if any two be rubbed together the one which stands earlier in the series becomes positively electrified, and the one that stands later negatively electrified:—*Fur*, *wool*, *ivory*, *glass*, *silk*, *metals*, *sulphur*, *indiarubber*, *guttapercha*, *collodion* or *celluloid*.

8. **Theories of Electricity.**—Several theories have been advanced to account for these phenomena. Symmer proposed a "**two-fluid**" **theory**, according to which there are two imponderable electric fluids of opposite kinds, which neutralize one another when they combine, and which exist combined in equal quantities in all bodies until their condition is disturbed by friction or otherwise. A modification of this theory was made by Franklin, who proposed instead a "**one-fluid**" **theory**, according to which there is a single electric fluid distributed usually uniformly in all bodies, but which, when they are subjected to friction, distributes itself unequally between the rubber and the thing rubbed, one having more of the fluid, the other less, than the average. Hence the terms *positive* and *negative*, which are still retained. That body which is supposed to have an excess being said to be charged with positive electricity (usually

denoted by the *plus* sign +), while that which is supposed to have less is said to be charged with negative electricity (and is denoted by the *minus* sign −). These terms are, however, purely arbitrary, for in the present state of science we are not certain which of these two states really means more and which means less; but apparently it follows from recent researches (see Art. 630) that the kind of electrification called resinous or negative is that in which there is an excess of electrons. In many ways electricity behaves as a weightless substance as incompressible as any material liquid. It is, however, quite certain that *electricity is not a material fluid*, whatever else it may be. For while it resembles a fluid in its property of apparently flowing from one point to another, it differs from every known fluid in almost every other respect. The electrons, or atoms of electricity, repel one another and thus differ fundamentally from the particles of matter, which are mutually attractive. It is, moreover, quite impossible to conceive of two fluids whose properties should in every respect be the precise opposites of one another. For these reasons it is misleading to speak of an electric fluid or fluids, however convenient the term may seem to be. In metals and other good conductors electricity can apparently move and flow quite easily in *currents*. In transparent solids such as glass and resin, and in many transparent liquids such as oils, and in gases such as the air (if still, and not rarefied), electricity apparently cannot flow. Even a vacuum appears to be a non-conductor. In the case of all non-conductors (except when they are disrupted or pierced by a discharge) electricity can only be moved by an action known as *displacement* (see Art. 58).

It appears then that in metals electricity can easily pass from molecule to molecule, and from atom to atom; but in the case of non-conductors the electricity is in some way stuck to the molecules, or associated with them. Some electricians, notably Faraday, have regarded the

electrical states as being the result of certain peculiar conditions of the molecules of the surfaces that have been rubbed. Another view is to regard the state of electrification as related to the *ether* (the highly attenuated medium which fills all space, and is the vehicle by which light is transmitted), which is known to be associated with the atoms of matter. Some indeed hold that the ether itself is electricity; and that the two states of positive and negative electrification are due to displacement of the ether at the surfaces of the charged bodies. In these lessons we shall avoid as far as possible all theories, and shall be content to use the term **electricity.**

9. Charge.—The quantity of electrification of either kind produced by friction or other means upon the surface of a body is spoken of as a **charge,** and a body when electrified is said to be *charged.* It is clear that there may be charges of different amounts and they may be of either kind. The word charge implies that the electricity is in the *static* condition, that is, is *at rest* on the surface of the body. When the charge of electricity is removed from a charged body, the body is said to be *discharged.* A charge given to a conductor, such as a piece of metal, will not be retained by it, unless the conductor be insulated, that is, held on some non-conducting support. Conductors of electricity are instantaneously discharged if touched by the hand or by any conductor in contact with the ground, the charge thus finding a means of escaping to earth or to surrounding walls. A charged non-conductor such as a rubbed rod of glass or ebonite may be readily and completely *dis-electrified* by passing it through, or even holding it near to, a flame. (See also Art. 334, p. 311.)

Electricity may either reside upon the surface of bodies as a *charge,* or flow through their substance as a *current.* That branch of the science which treats of the laws of the charges, that is to say, of electricity at rest upon the surface of bodies, is termed **electrostatics,**

and is dealt with in Chapter IV. The branch of the subject which treats of the flow of electricity in currents is dealt with in Chapter III., and other later portions of this book.

10. Modes of representing Electrification.— Several modes are used to represent the electrification of surfaces. In Figs. 6, 7, and 8 are represented two disks—A covered with woollen cloth, B of some resinous body—which have been rubbed together so that A has become positively, B negatively, electrified. In Fig. 6 the surfaces are marked with *plus* (+) and *minus* (−) signs. In Fig. 7 dotted lines are drawn just outside the positively electrified surface and just within the negatively electrified surface, as though one had a surplus and the other a deficit of electricity. In Fig. 8 lines are drawn across the intervening space from the positively electrified surface to the opposite negative charge. The advantages of this last mode are explained in Art. 14.

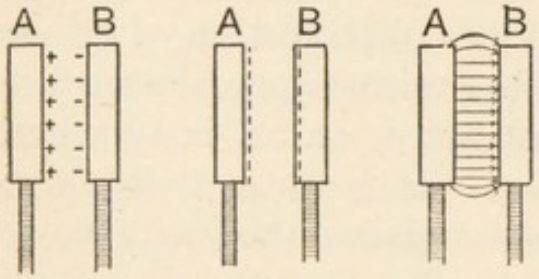


FIG. 6. FIG. 7. FIG. 8.

Modes of Representation of Electrification.

11. Conductors and Insulators. — The term "conductors," used above, is applied to those bodies which readily allow electricity to flow through them. Broadly speaking, bodies may be divided into two classes—those which conduct and those which do not; though very many substances are partial conductors, and cannot well be classed in either category. All the metals conduct well; the human body conducts, and so does water. On the other hand glass, porcelain, sealing-wax, silk, shellac, guttapercha, indiarubber, resin, oils and fatty substances generally, and the air, are **non-conductors**. On this account these substances are used to make supports and handles for electrical apparatus where it is important that the electricity should not leak away; hence they are

sometimes called **insulators** (see Arts. 30 and 437). Faraday termed them **dielectrics**, Art. 25. We have remarked above that the name of *non-electrics* was given to those substances which, like the metals, yield no sign of electrification when held in the hand and rubbed. We now know the reason why they show no electrification; for, being good conductors, the electrification flows away as fast as it is generated. The observation of Gilbert that electrical experiments fail in damp weather is also explained by the knowledge that water is a conductor; the film of moisture on the surface of damp bodies causing the charges produced by friction to leak away as fast as they are generated.

12. Other Electrical Effects.—The production of electricity by friction is attested by other effects than those of attraction and repulsion, which hitherto we have assumed to be the test of the presence of electricity. Otto von Guericke first observed that sparks and flashes of light could be obtained from highly electrified bodies at the moment when they were discharged. Such sparks are usually accompanied by a snapping sound, suggesting on a small scale the thunder accompanying the lightning flash, as was indeed remarked by Newton and other early observers. Pale flashes of light are also produced by the discharge of electricity through tubes partially exhausted of air by the air-pump. Other effects will be noticed in due course.

13. Sources of Electrification.—But *friction* is by no means the only source of electrification. The other sources, percussion, compression, heat, chemical action, physiological action, contact of metals, etc., will be treated of in Lesson VII. We will simply remark here that friction between two different substances *always* produces electrical separation, no matter what the substances may be. Symmer observed the production of electrification when a silk stocking was drawn over a woollen one, though woollen rubbed upon woollen, or silk rubbed

upon silk, produces no electrical effect. If, however, a piece of rough glass be rubbed on a piece of smooth glass, electrification is observed ; and indeed the conditions of the surface play a very important part in the production of electrification by friction. In general, of two bodies thus rubbed together, that one becomes negatively electrical whose particles are the more easily removed by friction. Differences of temperature also affect the electrical conditions of bodies, a warm body being usually negative when rubbed on a cold piece of the same substance. The quantity of electrification produced is, however, not proportional to the amount of the actual work expended on mechanical friction ; hence it appears doubtful whether friction is truly the cause of the electrification. When the surfaces of two different substances are brought into intimate contact something certainly happens, which has the result that when they are drawn apart they are found (provided at least one of them is a non-conductor) to have acquired opposite charges of electrification ; one surface having apparently taken some electricity from the other. But these opposite charges attract one another and cannot be drawn apart without there being mechanical work done upon the system. The work thus spent is stored up in the act of separating the charged surfaces ; and as long as the charges remain separated they constitute a store of potential energy. The so-called frictional electric machines are therefore machines for bringing dissimilar substances into intimate contact, and then drawing apart the particles that have touched one another and have acquired electric charges.

If the two bodies that are rubbed together are both good conductors, they will not become strongly electrified, even if held on insulating handles. It is quite likely, however, that the heat produced by friction, as in the bearings of machinery, is due to electric currents generated where the surfaces meet and slip.

14. Electric Field. — Whenever two oppositely

charged surfaces are placed near one another they tend to move together, and the space between them is found to be in a peculiar state of stress, as though the medium in between had been stretched. To explore the space between two bodies one of which has been positively and the other negatively electrified, we may use a light pointer (Fig. 9) made of a small piece of very thin paper pierced with a hole through which passes a long thread of glass. It will be found that this pointer tends to point across from the positively electrified surface to the negatively electrified surface, along invisible *lines of electric force.* The space so filled with electric lines of force is called an *electric field.* In Fig. 8 A and B represent two bodies the surfaces of which have been electrified, the one positively, the other negatively. In the field between them the electric lines pass across almost straight, except near the edges, where they are curved. Electric lines of force start from a positively charged surface at one end, and end on a negatively charged surface at the other end. They never meet or cross one another. Their direction indicates that of the resultant electric force at every point through which they pass. The stress in the medium thus mapped out by the lines of force acts as a tension along them, as though they tended to shorten themselves. In fact in Fig. 8 the tension in the medium draws the two surfaces together. There is also a pressure in the medium at right angles to the lines, tending to widen the distance between them. Fig. 10 represents a ball which has been positively electrified, and placed at a distance from other objects;

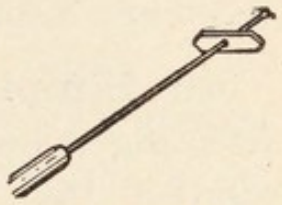


FIG. 9. — Paper Pointer to explore Field.

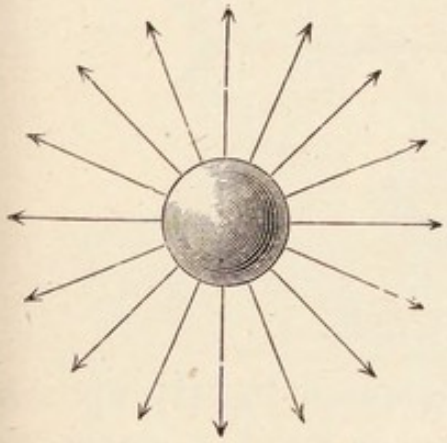


FIG. 10. Electric Forces around Charged Ball.

the lines in the field being simply radial. Curved lines of force are found in the electric fields between two electrified sources as in Fig. 15, p. 23.

LESSON II.—*Electroscopes*

15. Simple Electroscopes.—An instrument for detecting whether a body is electrified or not, and whether the electrification is positive or negative, is termed an **Electroscope.** The feather which was attracted or repelled, and the two pith-balls which flew apart when electrified, as we found in Lesson I., are in reality simple electroscopes. There are, however, a number of pieces of apparatus better adapted for this particular purpose, some of which we will describe.

16. Needle Electroscope.—The earliest electroscope was that devised by Dr. Gilbert, and, as is shown

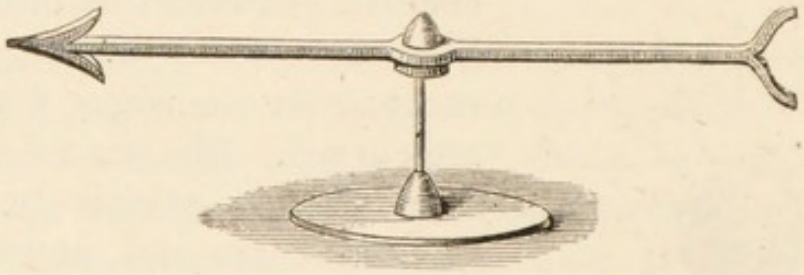


FIG. 11.—Needle Electroscope.

in Fig. 11 consists of a stiff strip balanced lightly upon a sharp point. A thin strip of brass or wood, a straw, or even a goose quill, balanced upon a sewing needle, will serve equally well. When an electrified body is held near the electroscope it is attracted and turned round, and will thus indicate the presence of electric charges far too feeble to attract bits of paper from a table.

17. Gold-Leaf Electroscope.—A still more sensitive instrument is the **Gold-Leaf Electroscope** invented by Bennet, and shown in Fig. 12. We have seen how two pith-balls when similarly electrified repel one another and stand apart, gravity being partly over-

come by the force of the electric repulsion. A couple of narrow strips of the thinnest tissue paper, hung upon a support, will behave similarly when electrified. But better results are obtained with two strips of gold-leaf, which, being excessively thin, is much lighter than the thinnest paper. Aluminium leaf is even better. The Gold-Leaf Electroscope is conveniently made by suspending the two leaves within a wide-mouthed glass jar, which

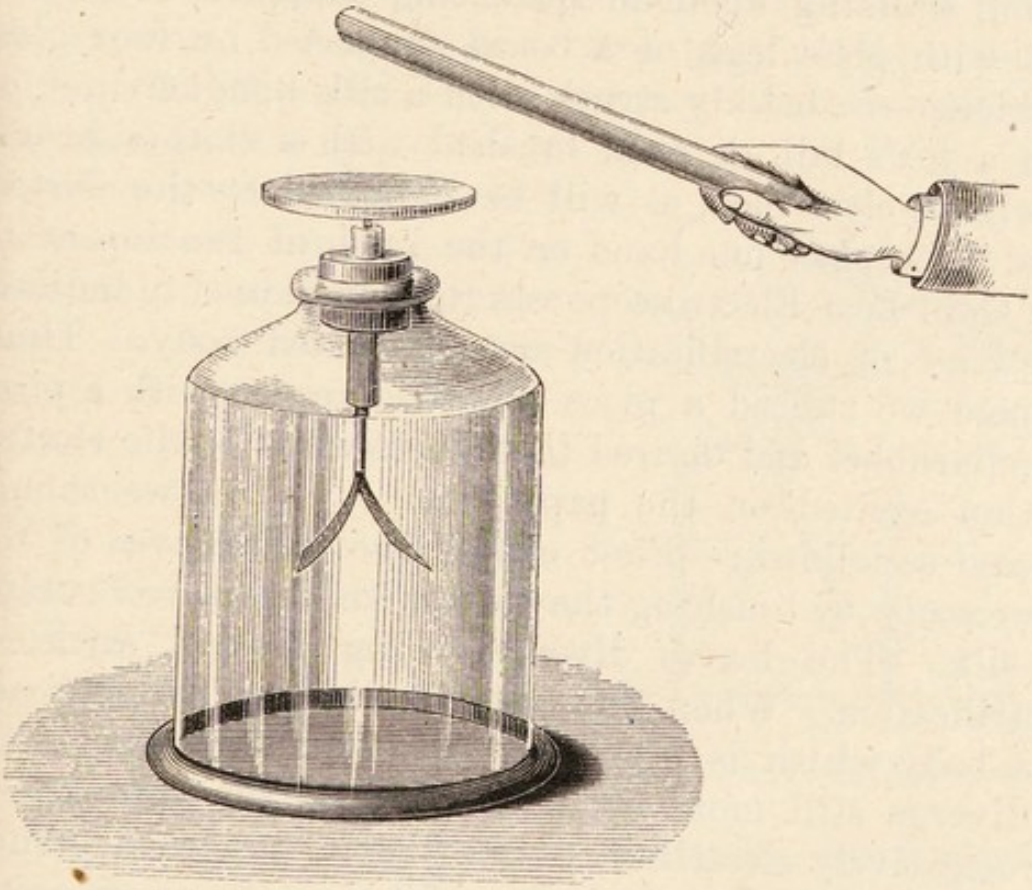


FIG. 12.—Gold-Leaf Electroscope.

serves both to protect them from draughts of air and to support them from contact with the ground. The mouth of the jar should be closed by a plug of paraffin wax, through which is pushed a bit of varnished glass tube. Through this passes a stiff brass wire, the lower end of which is bent at a right angle to receive the two strips of gold-leaf, while the upper supports a flat plate of metal, or may be furnished with a brass knob. When kept dry and free from dust this instrument will indicate

excessively small quantities of electrification. A rubbed glass rod, even while two or three feet away, will cause the leaves to repel one another. The chips produced by sharpening a pencil, falling on the electroscope top, are found to be electrified. If the knob be brushed with a small camel's-hair brush, even this slight friction produces a perceptible effect. With this instrument all kinds of friction can be shown to produce electrification. Let a person, standing upon an insulating support—such as a stool with glass legs, or a board supported on four glass tumblers,—be briskly struck with a silk handkerchief, or with a fox's tail, or even brushed with a clothes' brush, he will be electrified, as will be indicated by the electroscope if he place one hand on the knob at the top of it. The Gold-Leaf Electroscope can further be used to indicate the *kind* of electrification on an excited body. Thus, suppose we rubbed a piece of brown paper with a piece of indiarubber and desired to find out whether the electrification excited on the paper was + or −, we should proceed as follows:—First charge the gold leaves of the electroscope by touching the knob with a glass rod rubbed on silk. The leaves diverge, being charged with + electrification. When they are thus charged the approach of a body which is positively electrified will cause them to diverge still more widely; while, on the approach of one negatively electrified, they will tend to close together. If now the brown paper be brought near the electroscope, the leaves will be seen to diverge more, proving the electrification of the paper to be of the same kind as that with which the electroscope is charged, or positive. Sometimes the outer surface of the glass jar containing the gold leaves is covered with wire gauze or strips of foil to shield the leaves from the influence of external bodies. A preferable way is to use glass of a kind that conducts.

The part played by the surrounding medium in the operation of the electroscope is illustrated by Fig. 13. Of

the electric lines in the field surrounding the rubbed rod a number will pass into the metal cap of the electroscope and emerge below, through the leaves. The nearer the rod is brought, the greater will be the number of electric lines thus affecting the instrument. There being a tension along the lines and a pressure across them, the effect is to draw the gold leaves apart as though they repelled each other.

The Gold-Leaf Electroscope will also indicate roughly the amount of electrification on a body placed in contact with it, for the gold leaves open out more widely when the charge thus imparted to them is greater. For exact measurement, however, of the amount of charge recourse must be had to the instruments known as *Electrometers*, described in Art. 304, pp. 280-288.

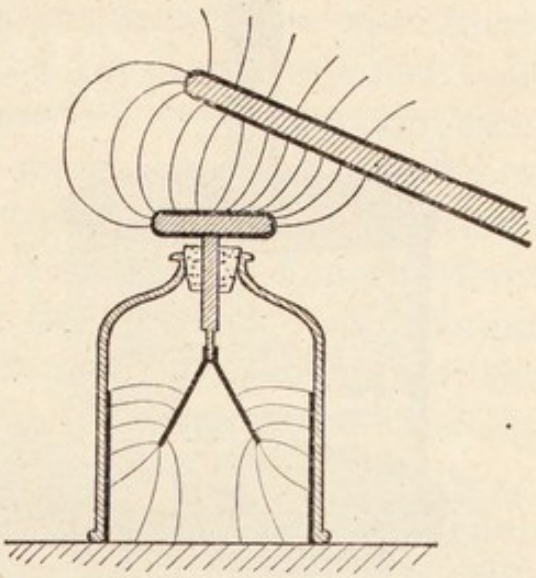


FIG. 13.—Action of Electroscope.

In another form of electroscope (Bohnenberger's) a single gold leaf is used, and is suspended between two metallic plates, one of which can be positively, the other negatively electrified, by placing them in communication with the poles of a "dry pile" (Art. 203). If the gold leaf be charged positively or negatively it will be attracted to one side or the other, according to the law of attraction and repulsion mentioned in Art. 5.

18. The Torsion Balance.—Although more properly an *Electrometer* than a mere *Electroscope*, it will be most convenient to describe here the instrument known as the Torsion Balance (Fig. 14). This instrument, once famous, but now quite obsolete, serves to measure the force of the repulsion between two similarly electrified bodies, by balancing the repelling force against the force

exerted by a fine wire in untwisting itself after it has been twisted. The torsion balance consists of a light arm or lever of shellac suspended within a cylindrical glass case by means of a fine silver wire. At one end this lever is furnished with a gilt pith-ball *n*. The upper end of the silver wire is fastened to a brass top, upon which a circle, divided into degrees, is cut. This top can be turned round in the tube which supports it, and is called the torsion-head. Through an aperture in the cover there can be introduced a second gilt pith-ball *m*, fixed to the end of a vertical glass rod *a*. Round the glass case, at the level of the pith-balls, a circle is drawn, and divided also into degrees.

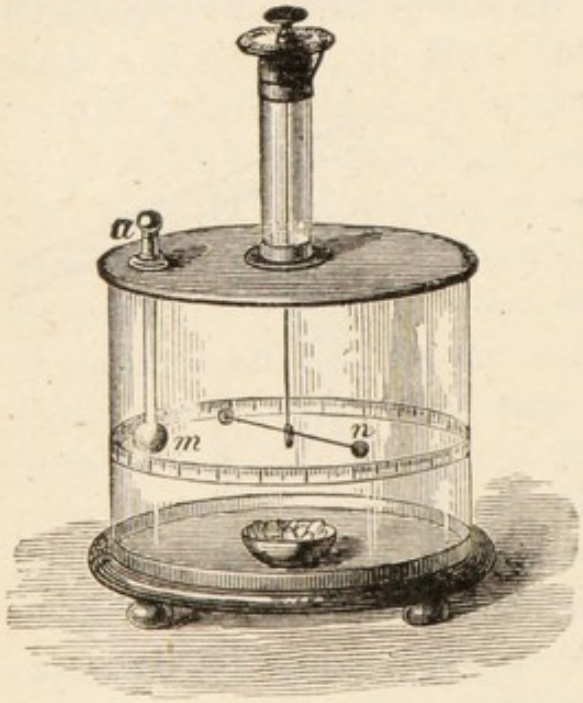


FIG. 14.—Torsion Balance.

In using the torsion balance to measure the amount of a charge of electricity, the following method is adopted:— First, the torsion-head is turned round until the two pith-balls *m* and *n* just touch one another. Then the glass rod *a* is taken out, and the charge of electricity to be measured is imparted to the ball *m*, which is then replaced in the balance. As soon as *m* and *n* touch one another, part of the charge passes from *m* to *n*, and they repel one another because they are then similarly electrified. The ball *n*, therefore, is driven round and twists the wire up to a certain extent. The force of repulsion becomes less and less as *n* gets farther and farther from *m*; but the force of the twist gets greater and greater the more the wire is twisted. Hence these two forces will balance one another when the balls are separated by a certain distance, and it is

clear that a large charge of electricity will repel the ball *n* with a greater force than a lesser charge would. The distance through which the ball is repelled is read off in angular degrees of the scale. When a wire is twisted, the force with which it tends to untwist is precisely proportional to the amount of the twist. The force required to twist the wire ten degrees is just ten times as great as the force required to twist it one degree. In other words, *the* **force** *of torsion is proportional to the* **angle** *of torsion.* The angular distance between the two balls is, when they are not very widely separated, very nearly proportional to the actual straight distance between them, and represents the force exerted between electrified balls *at that distance* apart. The student must, however, carefully distinguish between the measurement of the **force** and the measurement of the actual **quantity** of electricity with which the instrument is charged. For the force exerted between the electrified balls will vary at different distances according to a particular law known as the "law of inverse squares," which requires to be carefully explained.

19. The Law of Inverse Squares.—Coulomb found, by means of the Torsion Balance, that the force exerted between two small electrified bodies varies inversely as the square of the distance between them when the distance is varied. Thus, suppose two small electrified bodies 1 inch apart repel one another with a certain force, at a distance of 2 inches the force will be found to be only one quarter as great as the force at 1 inch; and at 10 inches it will be only $\frac{1}{100}$ part as great as at 1 inch. This law is demonstrated by the following experiment with the torsion balance. The two scales were adjusted to 0°, and a certain charge was then imparted to the balls. The ball *n* was repelled round to a distance of 36°. The twist on the wire between its upper and lower ends was also 36°, or the force tending to repel was thirty-six times as great as the

force required to twist the wire by 1°. The torsion-head was now turned round so as to twist the thread at the top and force the ball *n* nearer to *m*, and was turned round until the distance between *n* and *m* was halved. To bring down this distance from 36° to 18°, it was found needful to twist the torsion-head through 126°. The total twist between the upper and lower ends of the wire was now 126° + 18°, or 144°; and the force was 144 times as great as that force which would twist the wire 1°. But 144 is four times as great as 36; hence we see that while the distance had been reduced to one *half*, the force between the balls had become *four times* as great. Had we reduced the distance to *one quarter*, or 9°, the total torsion would have been found to be 576,° or *sixteen* times as great; showing the force to vary **inversely as the square of the distance.**

In practice it requires great experience and skill to obtain results as exact as this, for there are many sources of inaccuracy in the instrument. The balls must be very small, in proportion to the distances between them. The charges of electricity on the balls are found, moreover, to become gradually less and less, as if the electricity leaked away into the air. This loss is less if the apparatus be quite dry. It is therefore usual to dry the interior by placing inside the case a cup containing either chloride of calcium, or pumice stone soaked with strong sulphuric acid, to absorb the moisture.

Before leaving the subject of electric forces, it may be well to mention that the force of *attraction* between two oppositely electrified bodies varies inversely as the square of the distance between them, provided they are so small compared with the distance between them. And in every case, whether of attraction or repulsion, the force at any given distance is **proportional to the product of the two quantities** of electricity on the bodies. Thus, if we had separately given a charge of 2 to the ball *m* and a

charge of 3 to the ball n, the force between them will be $3 \times 2 = 6$ times as great as if each had had a charge of 1 given to it. It must be remembered, however, that the law of inverse squares is only true when applied to the case of bodies so small, as compared with the distance between them, that they are mere points. For flat, large, or elongated bodies the law of inverse squares does not hold good. The attraction between two large flat disks oppositely electrified with given charges, and placed near together, does not vary with the distance.

20. Field between two Balls.—The electric field (Art. 14) between two oppositely electrified balls is found (Fig. 15) to consist of curved lines. By the principle laid down in Art. 14, there is a tension along these lines so that they tend not only to draw the two balls together, but also to draw the electrifications on the surfaces of the balls toward one another. There is also a lateral pressure in the medium tending to keep the electric lines apart from one another. One result of these actions is that the charges are no longer equally distributed over the surfaces, but are more dense on the parts that approach most nearly.

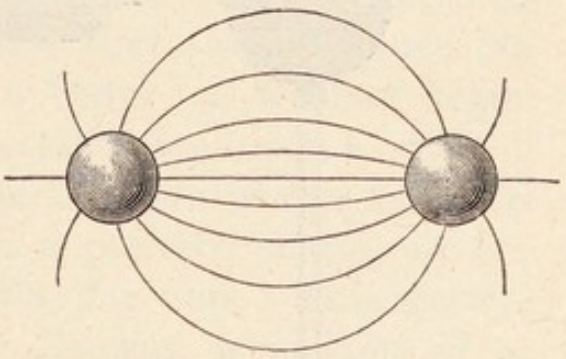


FIG. 15.—Field between Balls.

21. Unit Quantity of Electricity.—In consequence of these laws of attraction and repulsion, it is found most convenient to adopt the following definition for that quantity of electricity which we take for a **unit** in terms of which to measure other quantities of electricity. *One (electrostatic) Unit of Electricity is that quantity which, when placed at a distance of one centimetre in air from a similar and equal quantity, repels it with a force of one dyne* (see Art. 277). If instead of air another medium occupies the space, the force will be

different. For example, if petroleum is used the force exerted between given charges will be about half as great (see Art 57). Further information about the measurement of electrical quantities is given in Arts. 279 and 317.

LESSON III.—*Electrification by Influence*

22. Influence.—We have learned how two charged bodies may apparently attract or repel one another by virtue of the charges they carry, and will now consider

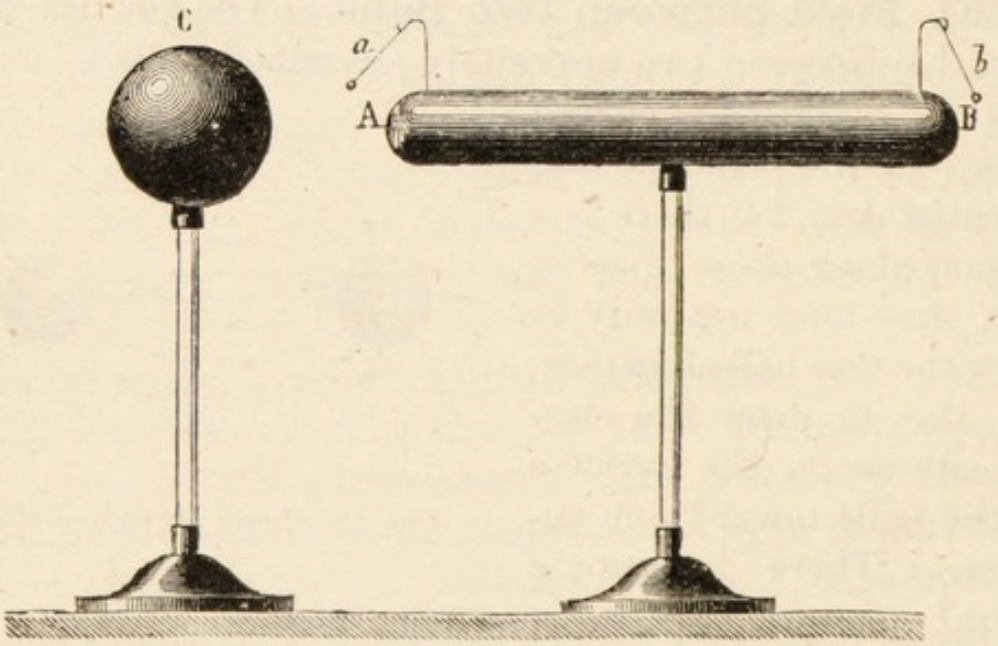


FIG. 16.—Experiment on Electric Influence.

the electric influence exerted by an electrified body upon one that has not been electrified.

Suppose we electrify positively a ball C, shown in Fig. 16, and hold it near to a body that has not been electrified, what will occur? We take for this experiment the apparatus shown on the right, consisting of a long sausage-shaped piece of metal, either hollow or solid, held upon a glass support. This "conductor," so called because it is made of metal which permits electricity to pass freely through it or over its surface, is supported on glass to prevent the escape of electricity to the earth, glass being a non-conductor. The influence of the positive charge

of the ball placed near this conductor is found to *induce* electrification on the conductor, which, although it has not been rubbed itself, will be found to behave at its two ends as an electrified body. The ends of the conductor will attract little bits of paper; and if pith-balls be hung to the ends they are found to be repelled. It will, however, be found that the middle region of the long-shaped conductor will give no sign of any electrification. Further examination will show that the two electrifications on the ends of the conductor are of opposite kinds, that nearest the excited glass ball being a negative charge, and that at the farthest end being an equal charge, but of positive sign. It appears then that a positive charge attracts negative and repels positive, and that this influence can be exerted at a distance from a body. If we had begun with a charge of negative electrification upon a stick of sealing-wax, the presence of the negative charge near the conductor would have induced a positive charge on the near end, and negative on the far end. This action, discovered in 1753 by John Canton, is spoken of as **influence**, or **electrostatic induction**.[1] It will take place across a considerable distance. Even if a large sheet of clean dry glass be placed between the charged body and the conductor, the effect will be produced. When the electrified body is removed both the charges disappear from the conductor, leaving no trace behind, and the glass ball is found to be just as much electrified as before; it has parted with none of its own charge. It may be noted that, according to the electron theory (see Art. 630),

[1] The word **induction** originally used was intended to denote an action at a distance, as distinguished from **conduction**, which implied the conveyance of the action by a material conductor. But there were discovered other actions at a distance, namely, the induction of currents by moving magnets, or by other currents, and the induction of magnetism in iron in the presence of a neighbouring magnet. As the term **induction** has now been officially adopted for the *induction of electromotive-forces*, its use in other senses ought to be dropped. Hence the preference now given to the term **influence** for the induction of charges by charges.

a body charged positively is regarded as having fewer free electrons than the things round it, while one with a negative charge is regarded as having more. According to this view it would appear that when a body (such as the + electrified glass ball) having fewer electrons than things around it is placed near an insulated conductor, the uniform distribution of electricity in that conductor is disturbed, the electrons flowing up to that end which is near the + body, a greater number than usual accumulating at that end, and fewer than usual remaining at the other end. This view of things will account for the disappearance of all signs of electrification when the electrified body is removed, for then the distribution of electrons in the conductor recovers its uniformity; and the conductor being neither more nor less electrified than all the objects around on the surface of the earth, will show neither positive nor negative charge. The action is not, however, a mere action at a distance; it is one in which the intervening medium takes an essential part. Consider (Fig. 17) what takes place when an insulated, non-electrified metal ball B is brought under the influence of a positively electrified body A. At once some of the electric lines of the field that surrounds A pass through B, entering it at the side nearer A, and leaving it at the farther side. As the ball B has no charge of its own, as many electric lines will enter on one side as leave on the other; or, in other words, the induced negative charge on one side and the induced positive charge on the other will be exactly equal in amount. They will not, however, be quite equally distributed, the negative charge on the side nearer A being more concentrated, and the lines in the field on that side denser.

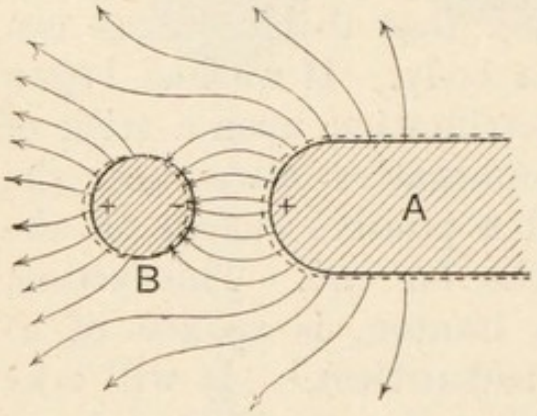


FIG. 17.—Charging by Influence.

23. Effects of Influence.—If the conductor be made in two parts, which, while under the influence of the electrified body, are separated, then on the removal of the electrified body the two charges can no longer return to neutralize one another, but remain each on its own portion of the conductor.

If the conductor be not insulated on glass supports, but placed in contact with the ground, that end only which is nearest the electrified body will be found to be electrified. The repelled charge is indeed repelled as far as possible into the walls of the room; or, if the experiment be performed in the open air, into the earth. One kind of electrification only is under these circumstances to be found, namely, the opposite kind to that of the excited body, whichever this may be. The same effect occurs in this case as if an electrified body had the power of attracting up the opposite kind of charge out of the earth. This is easily explained by the electron theory (see Art. 630). According as the charge of the body be + or −, the electrons in the earth are attracted up into the conductor, making it −, or they are repelled into the earth from the conductor, leaving it +.

The quantity of the two charges separated by influence on a conductor in the presence of a charge of electricity, depends upon the amount of the charge, and upon the distance of the charged body from the conductor. A highly electrified glass rod will exert a greater influence than a less highly electrified one; and it produces a greater effect as it is brought nearer and nearer. The utmost it can do will be to induce on the near end a negative charge equal in amount to its own positive charge, and a similar amount of positive electrification at the far end; but usually, before the electrified body can be brought so near as to do this, something else occurs which entirely alters the condition of things. As the electrified body is brought nearer and nearer, the charges of opposite sign on the two opposed surfaces attract one

another more and more strongly and accumulate more and more densely, until, as the electrified body approaches very near, a spark is seen to dart across, the two charges rushing together to neutralize one another, leaving the induced charge of positive electricity, which was formerly repelled to the other end of the conductor, as a permanent charge.

In Fig. 18 is illustrated the operation of gradually lowering down over a table a positively electrified metal ball. The nearer it approaches the table, the more does the electric field surrounding it concentrate itself in the gap between the ball and the table top; the latter becoming negatively electrified by influence. Where the electric lines are densest the tension in the medium is greatest, until, when the ball is lowered still farther, the mechanical resistance of the air can no longer withstand the stress; it breaks down and the layer of air is pierced by a spark. If oil is used as a surrounding medium instead of air, it will be found to withstand a much greater stress without being pierced.

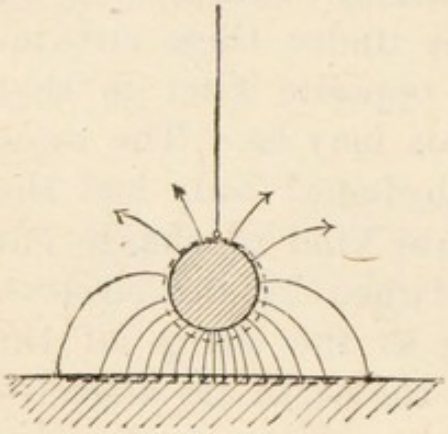


FIG. 18.—Charged Ball over Table.

24. Attraction due to Influence.—We are now able to apply the principle of influence to explain why an electrified body should attract things that have not been electrified at all. Fig. 17, on p. 26, may be taken to represent a light metal ball B hung from a silk thread presented to the end of a rubbed glass rod A. The positive charge on A produces *by influence* a negative charge on the nearer side of B and an equal positive charge on the far side of B. The nearer half of the ball will therefore be attracted, and the farther half repelled; but the attraction will be stronger than the repulsion, because the attracted charge is nearer than the repelled.

Hence, on the whole, the ball will be attracted. It can easily be observed that if a ball of non-conducting substance, such as wax, be employed, it is not attracted so much as a ball of conducting material. This in itself *proves* that influence really precedes attraction.

Another way of stating the facts is as follows:—The tension along the electric field on the right of B will be greater than that on the left, because of the greater concentration of the electric lines on the right.

25. Dielectric Action.—We have pointed out several times what part the intervening medium plays in these actions at a distance. The air, oil, glass, or other material between does not act simply as a non-conductor; it takes part in the propagation of the electric forces. Hence Faraday, who discovered this fact, termed such materials *dielectrics*. Had oil, or solid sulphur, or glass, been used instead of air, the influence exerted by the presence of the electrified body at the same distance would have been greater. The ability of a non-conducting substance to transmit the influence of an electrified body across it is called its inductivity (or was formerly called its *specific inductive capacity*, see Art. 57 and Lesson XXIII.).

26. The Electrophorus.—We are now prepared to explain the operation of a simple and ingenious instrument, devised by Volta in 1775, for the purpose of procuring, by the principle of influence, an unlimited number of charges of electricity from one single charge. This instrument[1] is the **Electrophorus** (Fig. 19). It consists of two parts, a round cake of resinous material cast in a metal dish or "sole," about 12 inches in diameter, and a round disk of slightly smaller diameter made of metal, or of wood covered with tinfoil, and provided with a glass handle. Shellac, or sealing-wax, or a mixture of resin, shellac, and Venice turpentine, may

[1] Volta's electrophorus was announced in 1775. Its principle had already been anticipated by Wilcke, who in 1762 described to the Swedish Academy of Sciences two "charging-machines" working by influence.

be used to make the cake. A slab of sulphur will also answer, but it is liable to crack. Sheets of hard ebonized indiarubber are excellent; but the surface of this substance requires occasional washing with ammonia and rubbing with paraffin oil, as the sulphur contained in it is liable



FIG. 19 —Volta's Electrophorus.

to oxidize and to absorb moisture. To use the electrophorus the resinous cake must be beaten or rubbed with a warm piece of woollen cloth, or, better still, with a cat's skin. The disk or "cover" is then placed upon the cake touched momentarily with the finger, then removed by taking it up by the glass handle, when it is found to be powerfully electrified with a positive charge, so much so

indeed as to yield a spark when the knuckle is presented to it. The "cover" may be replaced, touched, and once more removed, and will thus yield any number of sparks, the original charge on the resinous plate meanwhile remaining practically as strong as before.

The theory of the electrophorus is very simple, provided the student has clearly grasped the principle of influence explained above. When the resinous cake is first beaten with the cat's skin its surface is negatively electrified, as indicated in Fig. 20. When the metal disk is placed down upon it, it rests really only on three or four points of the surface, and may be regarded as an insulated conductor in the presence of an electrified body.

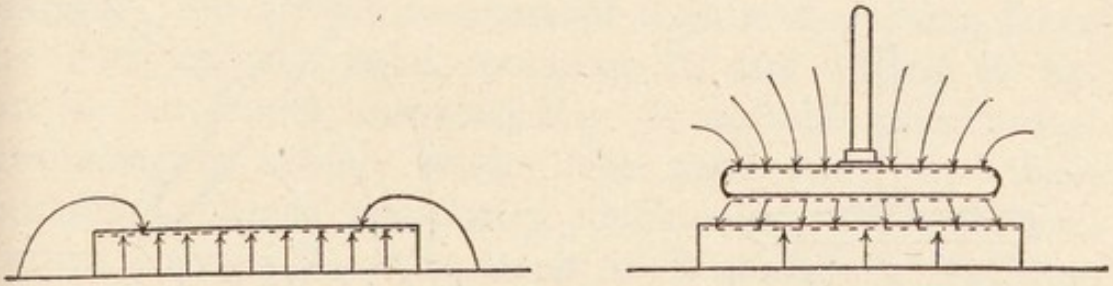


FIG. 20. FIG. 21.

Action of Electrophorus.

The negative electrification of the cake therefore acts by influence on the metallic disk or "cover," the electrons in it being displaced upwards, causing the upper side to become negatively electrified, and leaving a positive charge on the under side. This state of things is shown in Fig. 21. If now the cover be touched for an instant with the finger, the negative charge of the upper surface will flow away to the earth through the hand and body of the experimenter. The attracted positive charge will, however, remain, being bound as it were by its attraction towards the negative charge on the cake. Fig. 22 shows the condition of things after the cover has been touched. If, finally, the cover be lifted by its handle, the remaining positive charge will be no longer "bound" on the lower surface by attraction, but will distribute itself on both

sides of the cover (Fig. 23), and may be used to give a spark, as already said. It is clear that no part of the original charge has been consumed in the process, which may be repeated as often as desired. As a matter of fact, the charge on the cake slowly dissipates—especially if the air be damp. Hence it is needful sometimes to renew the original charge by afresh beating the cake with the cat's skin. The labour of touching the cover with the finger at each operation may be saved by having a pin of brass or a strip of tinfoil projecting from the metallic "sole" to the top surface of the cake, so that it touches the plate

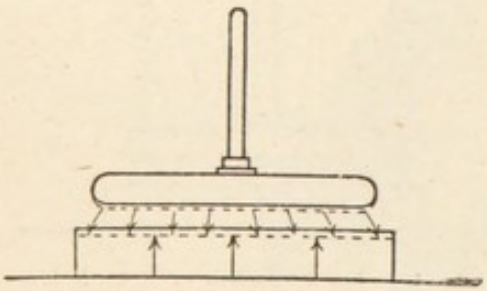


FIG. 22.

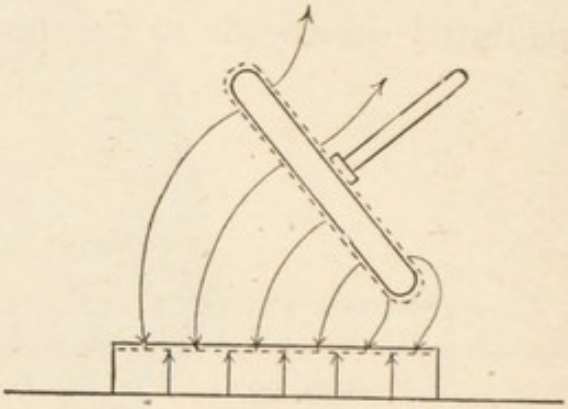


FIG. 23.

Action of Electrophorus.

each time, and thus neutralizes the negative charge by allowing electrons to flow away to the earth.

The principle of the electrophorus may then be summed up in the following sentence. *A conductor if touched while under the influence of a charged body acquires thereby a charge of opposite sign.*[1]

Since the electricity thus yielded by the electrophorus

[1] Priestley, in 1767, stated this principle in the following language :— "The electric fluid, when there is a redundancy of it in any body, repels the electric fluid in any other body, when they are brought within the sphere of each other's influence, and drives it into the remote parts of the body ; or quite out of the body, if there be any outlet for that purpose. In other words, bodies immerged in electric atmospheres always become possessed of the electricity, contrary to that of the body in whose atmosphere they are immerged."

is not obtained at the expense of any part of the original charge, it is a matter of some interest to inquire what the source is from which the energy of this apparently unlimited supply is drawn; for it cannot be called into existence without the expenditure of some other form of energy, any more than a steam-engine can work without fuel. As a matter of fact it is found that a little more work is required to lift up the cover when it is charged than if it were not charged; for, when charged, there is the tension of the electric field to be overcome as well as the force of gravity. Slightly harder work is done at the expense of the muscular energies of the operator; and this is the real origin of the energy stored up in the separated charges. The purely mechanical actions of putting down the disk on the cake, touching it, and lifting it up, can be performed automatically by suitable mechanical arrangements, which render the production of these inductive charges practically continuous. Of such continuous electrophori, the latest is Wimshurst's machine, described in Lesson V.

27. "Free" and "Bound" Electrification.—We have spoken of a charge of electricity on the surface of a conductor, as being "bound" when it is attracted by the presence of a neighbouring charge of the opposite kind. The converse term "free" is sometimes applied to the ordinary state of electricity upon a charged conductor, not in the presence of a charge of an opposite kind. A "free" charge upon an insulated conductor disappears instantaneously if a conducting channel to the earth be provided. It is immaterial what point of the conductor be touched. In the case represented in Fig. 17, lines of force run out in all directions from the + electrified body to the surrounding objects. Some lines encounter the metal ball, inducing a − charge where they enter, and a + charge on the other side where they pass out. If the metal ball be touched with the hand and thus put in connection with the surroundings, these

latter lines vanish, and with them the + charge on the ball; but the − charge remains as if it were "bound." The + charge is "free" to be removed, no matter what part of the metal ball is touched.

28. Method of charging the Gold-Leaf Electroscope by Influence.—The student will now be prepared to understand the method by which a Gold-Leaf Electroscope can be charged with the opposite kind of charge to that of the electrified body used to charge it. In Lesson II. it was assumed that the way to charge an electroscope was to place the excited body in contact with the knob, and thus permit, as it were, a small portion of the charge to flow into the gold leaves. A rod of glass rubbed on silk being + would thus obviously impart + electrification to the gold leaves.

Suppose, however, the rubbed glass rod to be held a few inches above the knob of the electroscope, as is indeed shown in Fig. 13. Even at this distance the gold leaves diverge, and the effect is due to influence. The gold leaves, and the brass wire and knob, form one continuous conductor, insulated from the ground by the glass jar. The presence of the + charge of the glass acts inductively on this "insulated conductor," inducing − electrification on the near end or knob, and inducing + at the far end, *i.e.* on the gold leaves, which diverge. As is shown in Fig. 13, p. 19, lines of force pass from the glass rod to the knob, and continue from the gold leaves to the floor and walls of the case, and through them to the earth. If now, while the excited rod is still held in position, the knob be momentarily touched with the finger, and thereby put in electrical connection with the earth, the lines of force between the earth and the gold leaves disappear, and the leaves collapse together. After removing the finger, let the glass rod be taken right away; the lines of force will be dragged after it, and as they increase in length they repel one another more strongly, until, when the rod is so far away that it becomes

part of the surroundings, lines of force run in from all sides to the electroscope, some entering the gold leaves, which again diverge. And now the charge upon them is of the same sign as the charge upon the knob, namely negative.

29. The "Return-Shock."—It is sometimes noticed that, when a charged conductor is suddenly discharged, a discharge is felt by persons standing near, or may even affect electroscopes, or yield sparks. This action, known as the "return-shock," is due to influence. For in the presence of a charged conductor a charge of opposite sign will be induced in neighbouring bodies, and on the discharge of the conductor these neighbouring bodies may also suddenly discharge their induced charge into the earth, or into other conducting bodies. A "return-shock" is sometimes felt by persons standing on the ground at the moment when a flash of lightning has struck an object some distance away.

LESSON IV.—*Conduction and Distribution of Electricity*

30. Conduction.—Toward the close of Lesson I. we explained how certain bodies, such as the metals, conduct electricity, while others are non-conductors or insulators. This discovery is due to Stephen Gray; who, in 1729, found that a cork, inserted into the end of a rubbed glass tube, and even a rod of wood stuck into the cork, possessed the power of attracting light bodies. He found, similarly, that metallic wire and moist pack-thread conducted electricity, while silk did not.

We may repeat these experiments by taking (as in Fig. 24) a glass rod, fitted with a cork and a piece of wood. If a bullet or a brass knob be hung to the end of this by a linen thread or a wire, it is found that when the glass tube is rubbed the bullet acquires the property of attracting light bodies. If a dry silk thread is used, however, no electricity will flow down to the bullet.

Gray even succeeded in transmitting a charge of electricity through a hempen thread over 700 feet long, suspended on silken loops. A little later Du Fay succeeded in sending electricity to no less a distance than 1256 feet through a moistened thread, thus proving the conducting power of moisture. From that time the classification of bodies into *conductors* and *insulators* has been observed.

This distinction cannot, however, be entirely main-

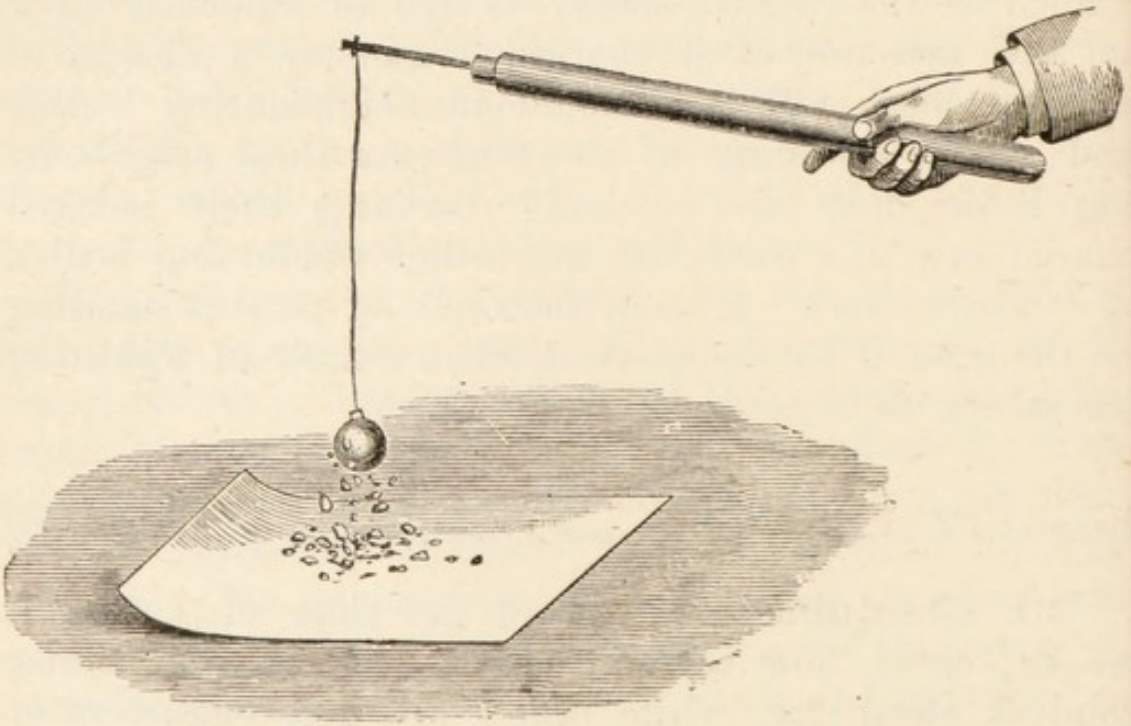


FIG 24.—Conduction of Electrification by a Thread.

tained, as a large class of substances occupy an intermediate place as partial conductors. For example, dry wood is a bad conductor and also a bad insulator; it is a good enough conductor to conduct away the high-potential electricity obtained by friction, but it is a bad conductor for the relatively low-potential electricity of small voltaic batteries. Substances that are very bad conductors are said to offer a great **resistance** to the flow of electricity through them. There is indeed no substance so good a conductor as to be devoid of resistance. There is no substance of so great a resistance as

not to conduct a little. Even silver, which conducts best of all known substances, resists the flow of electricity to a small extent; and, on the other hand, such a non-conducting substance as glass, though its resistance is many million times greater than that of any metal, does allow a very minute quantity of electricity to pass through it. In the following list, the substances named are placed in order, each conducting better than those lower down on the list.

Silver	Good Conductors.	Pure water	Non-Conductors or Insulators.
Copper		Oils	
Aluminium		Porcelain	
Other metals		Wool	
Carbon		Silk	
Liquid acids		Resin	
Liquid alkalis		Indiarubber	
Salts in solution		Guttapercha	
Water (impure)		Shellac	
		Ebonite	
Cotton	Partial Conductors.	Paraffin Wax	
Dry wood		Glass	
Marble		Quartz (fused)	
Paper		Air and gases	

A simple way of observing experimentally whether a substance is a conductor or not, is to take a charged gold-leaf electroscope, and, holding the substance to be examined in the hand, touch the knob of the electroscope with it. If the substance is a conductor the electrons can flow away through it and through the body to (or from) the earth, and the electroscope will be discharged. Through good conductors the rapidity of the flow is so great that the discharge is practically instantaneous. Further information on this question is given in Lesson XXXIII., p. 425.

31. Distribution of Charge on Bodies.—If electrification is produced at one part of a non-conducting body, it remains at that point and does not flow over the surface, or at most flows over it exceedingly slowly.

Thus if a glass tube is rubbed at one end, only that one end is electrified. Hot glass is, however, a conductor. If a warm cake of resin be rubbed at one part with a piece of cloth, only the portion rubbed will attract light bodies, as may be proved by dusting upon it through a piece of muslin fine powders such as red lead, lycopodium, or verdigris, which adhere where the surface is electrified. The case is, however, wholly different when a charge of electricity is imparted to any part of a *conducting* body placed on an insulating support, for the charge *instantly* distributes itself all over the surface, though in general not uniformly over all parts of the surface.

32. The Charge resides on the Surface.—A charge of electricity resides on the surface only of conducting bodies. This is proved by the fact that it is found to be immaterial to the distribution what the interior of a conductor is made of; it may be solid metal, or hollow, or even consist of wood covered with tinfoil or gilt; but, if the shape be the same, the charge will distribute itself precisely in the same manner over the surface. There are also several ways of proving by direct experiment this very important fact. Let a hollow metal ball, having an aperture at the top, be taken (as in Fig. 25), and set upon an insulating stem, and charged by sending into it a few sparks from an electrophorus. The absence of any charge in the interior may be shown as follows:—In order to observe the nature of the electrification of a charged body, it is convenient to have some means of removing a small quantity of the charge as a sample for examination. To obtain such a sample, a little instrument known as a **proof-plane** is employed. It consists of a little disk of sheet copper or of gilt paper fixed at the end of a small glass rod. If this disk is laid on the surface of an electrified body at any point, part of the charge flows into it, and it may be then removed, and the sample thus obtained may be examined with a gold-leaf electroscope in the ordinary way. For some

purposes a metallic bead, fastened to the end of a glass rod, is more convenient than a flat disk. If such a proof-plane be applied to the *outside* of our electrified hollow ball, and then touched on the knob of an electroscope, the gold leaves will diverge, showing the presence of a

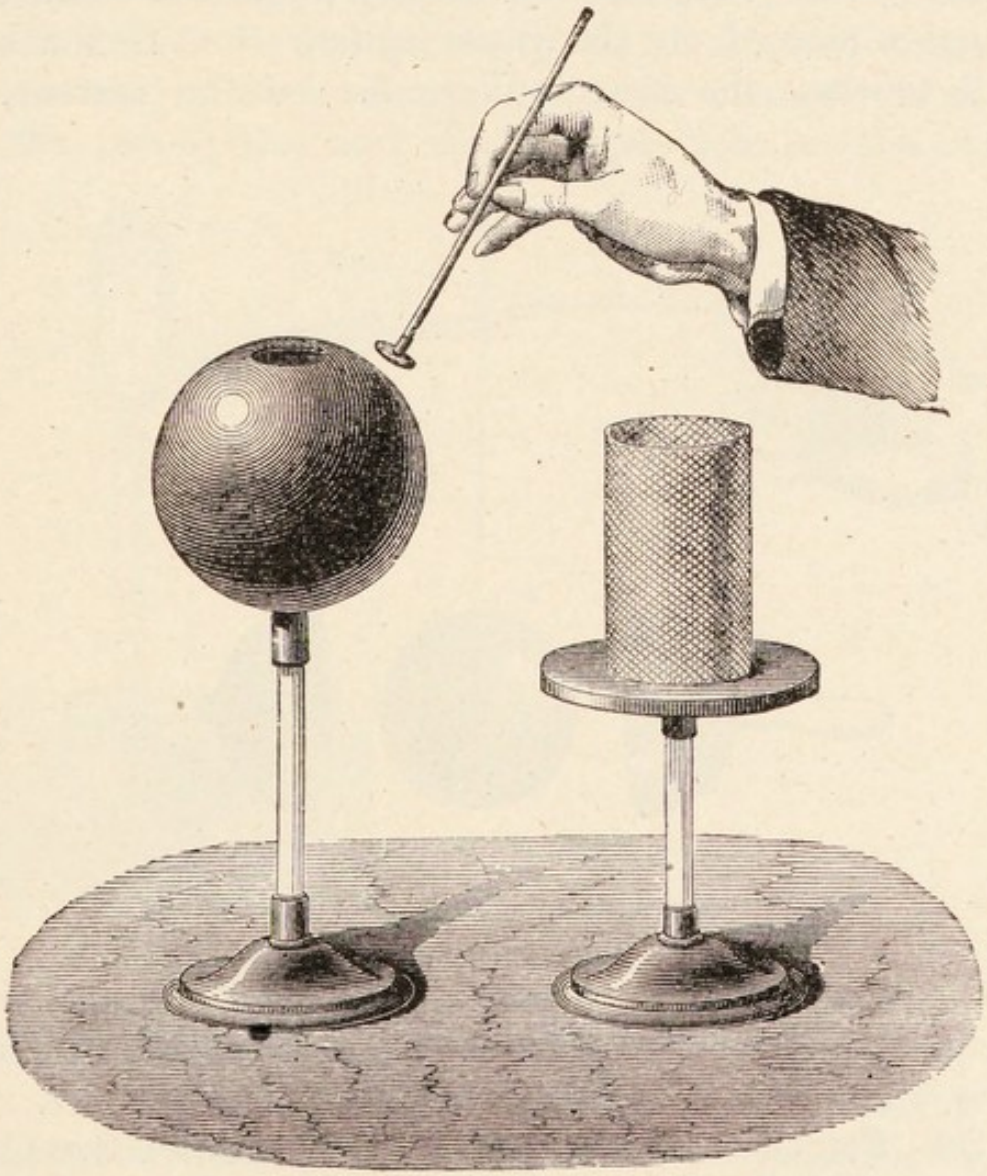


FIG. 25.—Examining Charges by a Proof-plane.

charge. But if the proof-plane be carefully inserted through the opening, and touched against the *inside* of the globe and then withdrawn, it will be found that the inside is destitute of electrification. An electrified pewter mug will show a similar result, and so will even a cylinder of wire gauze.

33. Experiment with Hollow Sphere.—Cavendish and Coulomb proved the same fact in another way. A copper ball was electrified and insulated. Two hollow hemispheres of copper, of a larger size, and furnished with glass handles, were then placed together outside it (Fig. 26). So long as they did not come into contact the charge remained on the inner sphere; but if the outer shell touched the inner sphere for but an instant, the

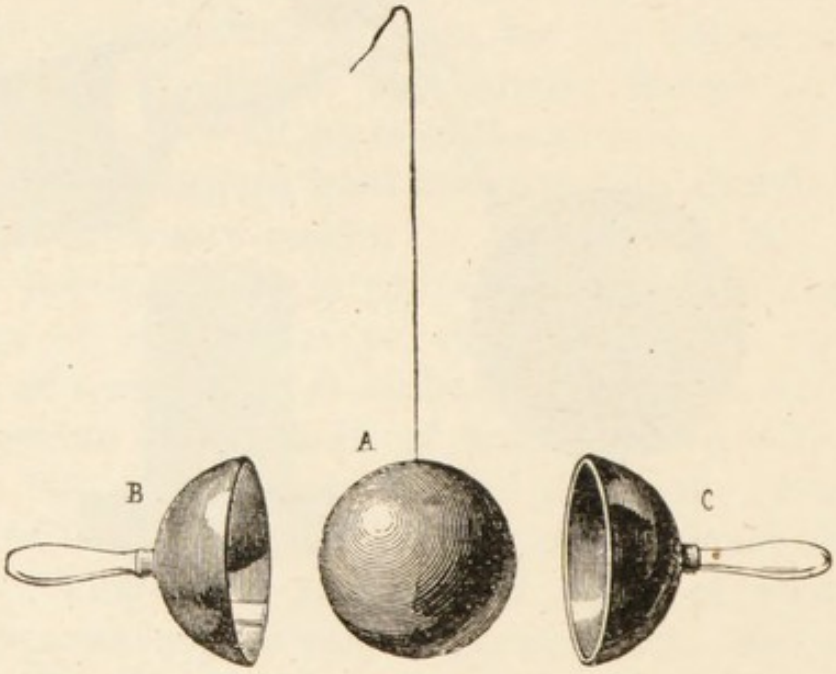


FIG. 26.—Experiment with Hollow Hemispheres.

whole of the charge passed to the exterior; and when the hemispheres were separated and removed the inner globe was found to be completely discharged.

34. Further Explanation.—Doubtless the explanation of this behaviour of electricity is to be found in the property previously noticed as possessed by either kind of electrification, namely, that of repelling itself; hence it retreats as far as can be from the centre and remains upon the surface. An important proposition concerning the absence of electric force within a closed conductor is proved in Lesson XXI.; meanwhile it must be noted that the proofs, so far, are directed to demonstrate the absence

of a free charge of electricity in the interior of hollow conductors. Amongst other experiments, Terquem showed that a pair of gold leaves hung inside a wire cage could not be made to diverge when the cage was electrified. Faraday constructed a conical bag of linen-gauze, supported as in Fig. 27, upon an insulating stand, and to it silk strings were attached, by which it could be turned inside out. It was charged, and the charge was shown by the proof-plane and electroscope to be on the outside

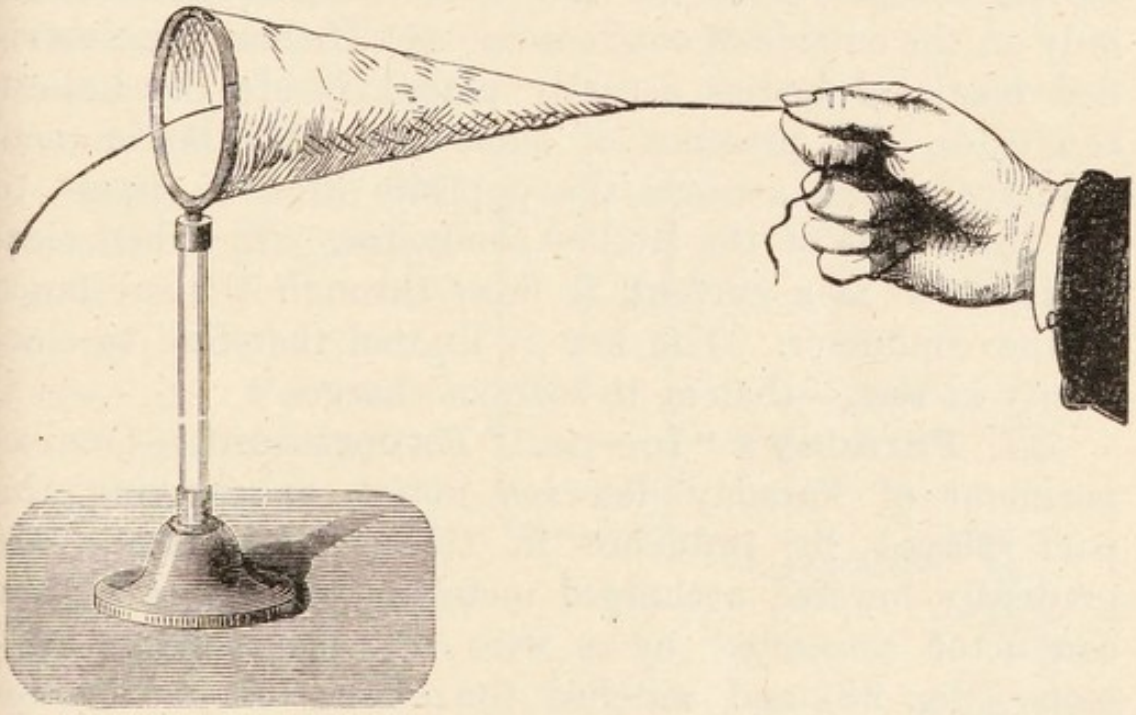


FIG. 27.—Faraday's Conical Bag.

of the bag. On turning it inside out the electricity was once more found *outside*. Faraday's most striking experiment was made with a hollow cube, measuring 12 feet each way, built of wood, covered with tinfoil, insulated, and charged by a powerful machine, so that large sparks and brushes were darting off from every part of its outer surface. Into this cube Faraday took his most delicate electroscopes; but once within, he failed to detect the least effect upon them.

35. Applications.—Advantage is taken of this in the construction of delicate electrometers and other in-

struments, which can be effectually screened from the influence of electrified bodies by enclosing them in a cover of thin metal, closed all round, except where apertures must be made for purposes of observation. Metal gauze answers excellently, and is nearly transparent. It was proposed by the late Professor Clerk Maxwell to protect buildings from lightning by covering them on the exterior with a network of wires.

36. Apparent Exceptions.—There are two apparent exceptions to the law that electrification resides only on the outside of conductors. (1) If there are electrified insulated bodies actually placed inside the hollow conductor, the presence of these electrified bodies acts inductively and attracts the opposite kind of charge to the inner side of the hollow conductor. (2) When electricity flows as a current, it flows through the substance of the conductor. The law is limited therefore to electricity at rest,—that is, to *statical* charges.

37. Faraday's "Ice-pail" Experiment.—One experiment of Faraday deserves notice, as showing the part played by influence in these phenomena. He gradually lowered a charged metallic ball into a hollow conductor connected by a wire to a gold-leaf electroscope (Fig. 28), and watched the effect. A pewter ice-pail being convenient for his purpose, this experiment is continually referred to by this name, though any other hollow conductor—a tin canister or a silver mug, placed on a glass support—would of course answer equally well. The following effects are observed:—Suppose the ball to have a + charge: as it is lowered into the hollow conductor the gold leaves begin to diverge, for the presence of the charge acts inductively, and attracts a − charge into the interior and repels a + charge to the exterior. The gold leaves diverge more and more until the ball is right within the hollow conductor, after which no greater divergence is obtained. On letting the ball touch the inside the gold leaves still remain diverging as before,

and if now the ball is pulled out it is found to have lost all its electrification. The fact that the gold leaves diverge no wider after the ball touched than they did just before, proves that when the charged ball is right inside the hollow conductor the induced charges are each of them precisely equal in amount to its own charge, and the interior negative charge exactly neutralizes the charge on the ball at the moment when they touch, leaving the equal exterior charge unchanged. An *electric cage*, such as this ice-pail, when connected with an electroscope or electrometer, affords an excellent means of examining the charge on a body small enough to be hung inside it. For without using up any of the charge of the body (which we are obliged to do when applying the method of the proof-plane) we can examine the induced charge repelled to the outside of the cage, which is equal in amount and of the same sign. If two equal charges of opposite kinds are placed at the same time within the cage no effects are produced on the outside.

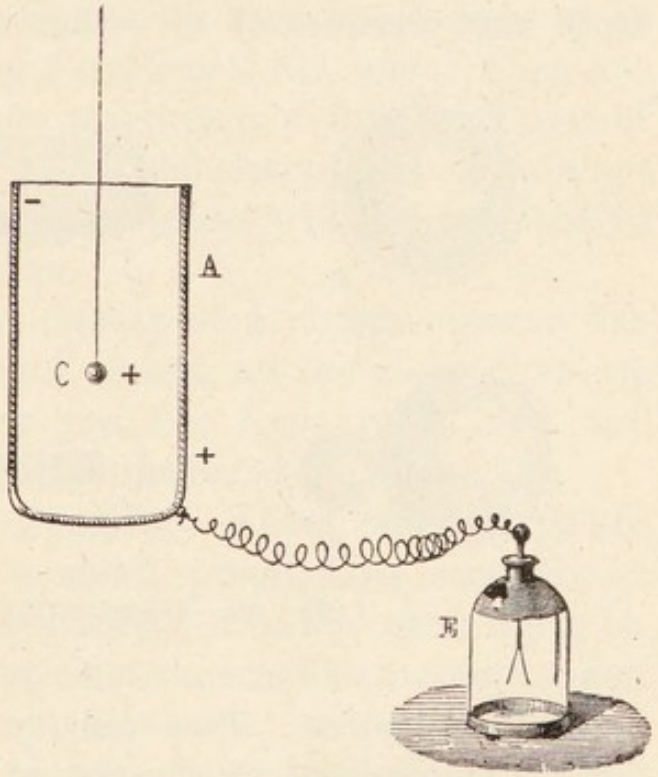


FIG. 28.—Faraday's Ice-pail Experiment.

38. Distribution of Charge.—A charge of electricity is not usually distributed uniformly over the surfaces of bodies. Experiment shows that the charge is denser on the edges and corners of bodies than upon their flatter parts. This distribution can be deduced from the theory laid down in Lesson XXI., but mean-

time we will give some of the chief cases as they can be shown to exist. The term **Electric Density** is used to signify the amount of electricity at any point of a surface; *the electric density at a point is the number of units of electricity per unit of area* (*i.e.* per square inch, or per square centimetre), the distribution being supposed uniform over this small surface.

(*a*) **Sphere.**—The distribution of a charge over an insulated sphere of conducting material is uniform, provided the sphere is also isolated, that is to say, is remote from the presence of all other conductors and all other

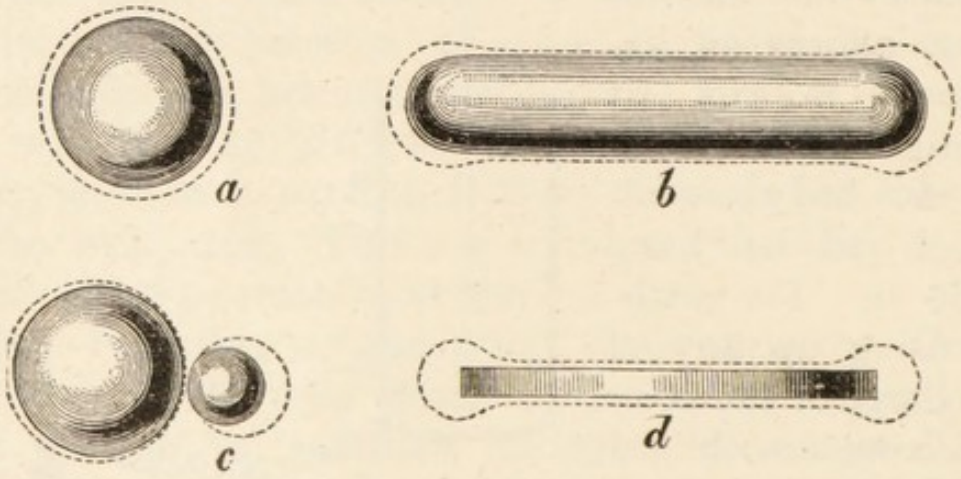


FIG. 29.—Distribution of Charges.

electrified bodies. The density is uniform all over it. This is symbolized by the dotted line round the sphere in Fig. 29 *a*, which is at an equal distance from the sphere all round, suggesting an equal thickness of charge at every point of the surface. It must be remembered that the charge is not really of any perceptible thickness at all; it resides on or at the surface, but cannot be said to form a stratum upon it.

(*b*) **Cylinder with rounded Ends.**—Upon an elongated conductor, such as is frequently employed in electrical apparatus (Fig. 29*b*), the density is greatest at the ends where the curvature of the surface is the greatest.

(*c*) **Two Spheres in contact.**—If two spheres in

contact with each other are insulated and charged, it is found that the density is greatest at the parts farthest from the point of contact, and least in the crevice between them. If the spheres are of unequal sizes the density is greater on the smaller sphere, which has the surface more curved (Fig. 29*c*). On an **egg-shaped** or **pear-shaped** conductor the density is greatest at the small end. On a **cone** the density is greatest at the apex ; and if the cone terminate in a sharp point the density there is very much greater than at any other point. At a **point**, indeed, the density of the collected electricity may be so great as to electrify the neighbouring particles of air, which then are repelled (see Art. 47), thus producing a continual loss of charge. For this reason points and sharp edges are always avoided on electrical apparatus, except where it is specially desired to set up a discharge.

(*d*) **Flat Disk.**—The density of a charge upon a flat disk is greater, as we should expect, at the edges than on the flat surfaces ; but over the flat faces away from the edge the distribution is fairly uniform (Fig. 29*d*).

39. Experimental Proofs.—These various facts are ascertained by applying a small proof-plane successively at various points of the electrified bodies and examining by means of an electroscope or electrometer the amount taken up by the proof-plane. Coulomb, who investigated mathematically as well as experimentally many of the important cases of distribution, employed the torsion balance (Art. 18) to verify his calculations. He investigated thus the case of the ellipsoid of revolution, and found the densities of the charges at the extremities of the axes to be proportional to the lengths of those axes. He also showed that the density of the charge at any other point of the surface of the ellipsoid was proportional to the length of the perpendicular drawn from the centre to the tangent at that point. Riess found the density at the middle of the edges of a cube to be nearly two and a half times as great as the density at the middle of a face ;

while the density at a corner of the cube was more than four times as great.

If any portion of the charge of an insulated conductor be removed, the remainder of the charge will immediately redistribute itself over the surface in the same manner as the original charge, provided it be also *isolated*, *i.e.* that no other conductors or charged bodies be near to perturb the distribution by complicated effects of influence.

40. Distribution of Charge between several Bodies.—If a conductor be charged with any quantity of electricity, and another conductor of the same size and shape (but uncharged) be brought into contact with it for an instant and then separated, it will be found that the charge has divided itself equally between them. In the same way a charge may be divided equally into three or more parts by being distributed simultaneously over three or more equal and similar conductors brought into contact and symmetrically placed.

If two equal metal balls, suspended by silk strings, charged with unequal quantities of electricity, are brought for an instant into contact and then separated, it will be found that the charge has redistributed itself fairly, half the sum of the two charges being now the charge of each. This may even be extended to the case of charges of opposite signs. Thus, suppose two similar conductors to be electrified, one with a positive charge of 5 units and the other with 3 units of negative charge, when these are made to touch and separated, each will have a positive charge of 1 unit; for the algebraic sum of $+5$ and -3 is $+2$, which, shared between the two equal conductors, leaves $+1$ for each.

41. Capacity of Conductors.—If the conductors be unequal in size, or unlike in form, the shares taken by each in this redistribution will not be equal, but will be proportional to the respective *capacities* of the conductors. The definition of **capacity** in its relation to electric quantities is given in Lesson XXI., Art. 289. We

may, however, make the remark, that two insulated conductors of the same form, but of different sizes, differ in their electrical *capacity*; for the larger one must have a larger amount of electricity imparted to it in order to electrify its surface to the same degree. The term *potential* is employed in this connection, in the following way:—A given quantity of electricity will electrify an isolated body up to a certain "potential" (or its ability to do electric work) depending on its capacity. A large *quantity* of electricity imparted to a conductor of small *capacity* will electrify it up to a very high *potential*; just as a large quantity of water poured into a vessel of narrow capacity will raise the surface of the water to a high level in the vessel. The exact definition of Potential, in terms of energy spent against the electrical forces, is given in the lesson on Electrostatics (Art. 280), p. 260.

It will be found convenient to refer to a positively electrified body as one electrified to a *positive* or *high potential*; while a negatively electrified body may be looked upon as one electrified to a *low* or *negative potential*. And just as we take the level of the sea as a zero level, and measure the heights of mountains above it, and the depths of mines below it, using the sea level as a convenient point of reference for differences of level, so we take the potential of the earth's surface (for the surface of the earth is always electrified to a certain degree) as *zero potential*, and use it as a convenient point of reference from which to measure differences of electric potential.

LESSON V.—*Electric Machines*

42. Frictional Machines.—For the purpose of procuring larger charges of electricity than can be obtained by the rubbing of a rod of glass or shellac, **electric machines** have been devised. Electric machines are of

two[1] kinds: (1) *Frictional Machines*, (2) *Influence Machines*. All frictional machines consist of two parts, one for producing, the other for collecting, the electric charges. Experience has shown that the quantities of + and − electrification developed by friction upon the two surfaces rubbed against one another depend on the amount of friction, upon the extent of the surfaces rubbed, and also upon the nature of the substances used. If the two substances employed are near together on the list of electrics given in Art. 7, the electrical effect of rubbing them together will not be so great as if two substances widely separated in the series are chosen. To obtain the highest effect, the most positive and the most negative of the substances convenient for the construction of a machine should be taken, and the greatest available surface of them should be subjected to friction, the moving parts being pressed against one another with a sufficient pressure.

The earliest form of electric machine was devised by Otto von Guericke of Magdeburg, and consisted of a globe of sulphur fixed upon a spindle, and pressed with the dry surface of the hands while being made to rotate; with this he discovered the existence of electric sparks and the repulsion of similarly electrified bodies. Sir Isaac Newton replaced Von Guericke's globe of sulphur by a globe of glass. A little later the form of the machine was improved by various German electricians; Von Bose added a collector or "prime conductor," in the shape of an iron tube, supported by a person standing on cakes of resin to insulate him, or suspended by silken strings; Winckler of Leipzig substituted a leathern cushion for the hand as a rubber; and Gordon of Erfurt rendered the machine more easy of construction by using a glass cylinder instead of a glass globe. The electricity was led from the excited cylinder or globe to the prime

[1] Machines for generating *currents*, known as dynamo-electric, or magneto-electric machines, are not here considered. For these see Art. 507.

conductor by a metallic chain which hung over against the globe. A pointed collector was not employed until after Franklin's famous researches on the action of points. About 1760 machines having glass plates instead of cylinders were devised. All frictional machines are, however, now obsolete, having in recent years been quite superseded by the modern *Influence Machines.*

43. The Cylinder Frictional Machine.—The Cylinder Frictional Machine consists of a glass cylinder mounted on a horizontal axis capable of being turned by

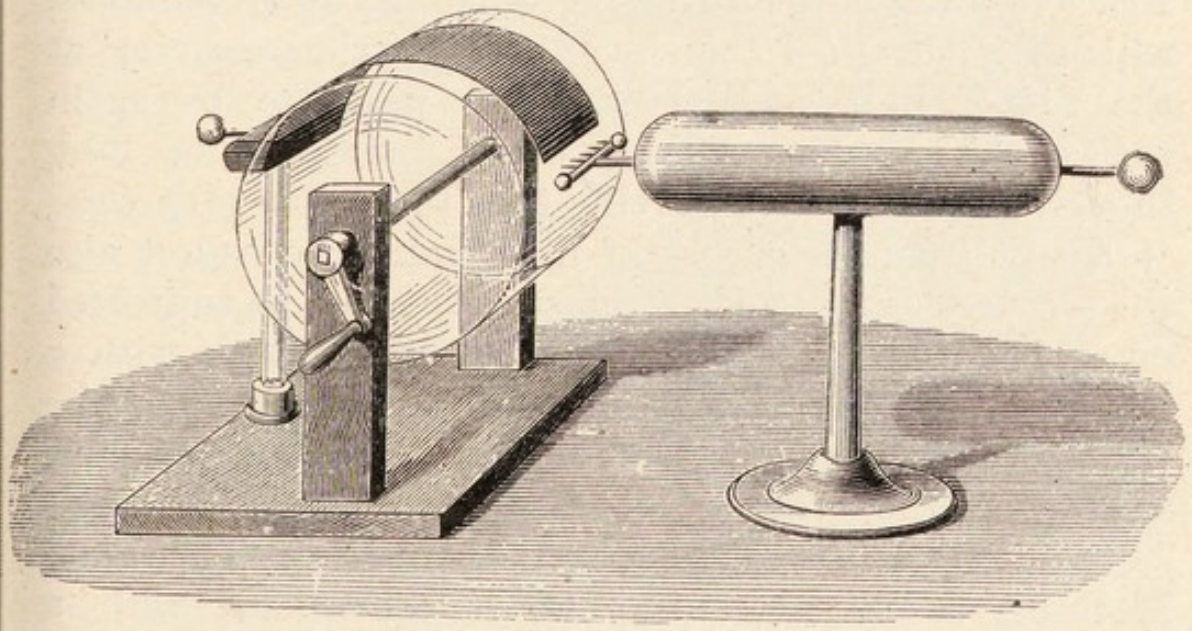


FIG. 30.—Cylinder Frictional Electrical Machine.

a handle. Against it is pressed from behind a cushion of leather stuffed with horsehair, the surface of which is covered with a powdered amalgam of zinc or tin. A flap of silk attached to the cushion passes over the cylinder, covering its upper half. In front of the cylinder stands the "prime conductor," which is made of metal, and usually of the form of an elongated cylinder with hemispherical ends, mounted upon a glass stand. At the end of the prime conductor nearest the cylinder is fixed a rod bearing a row of fine metallic spikes, resembling in form a rake; the other end usually carries a rod terminated in a brass ball or knob. The general aspect of the machine

is shown in Fig. 30. When the handle is turned the friction between the glass and the amalgam-coated surface of the rubber produces a copious electrical action, electricity appearing as a + charge on the glass, leaving the rubber with a – charge. The prime conductor collects this charge by the following process: The + charge being carried round on the glass acts inductively on the long insulated conductor, repelling a + charge to the far end; leaving the nearer end – ly charged. The effect of the row of points is to emit a – ly electrified wind (see Art. 47) towards the attracting + charge upon the glass, which is neutralized thereby; the glass thus arriving at the rubber in a neutral condition ready to be again excited. This action of the points is sometimes described, though less correctly, by saying that the points collect the + charge from the glass. If it is desired to collect also the – charge of the rubber, the cushion must be supported on an insulating stem and provided at the back with a metallic knob. It is, however, more usual to use only the + charge, and to connect the rubber by a chain to "earth," so allowing the – charge to be neutralized.

44. The Plate Frictional Machine.—The Plate Machine, as its name implies, is constructed with a circular plate of glass or of ebonite, and is usually provided with two pairs of rubbers formed of double cushions, pressing the plate between them, placed at its highest and lowest point, and provided with silk flaps, each extending over a quadrant of the circle. The prime conductor is either double or curved round to meet the plate at the two ends of its horizontal diameter, and is furnished with two sets of spikes, for the same purpose as the row of points in the cylinder machine. A common form of plate machine is shown in Fig. 31. Its advantages are that a large glass plate is more easy to construct than a large glass cylinder of perfect form, and that the length along the surface of the glass between the collecting row of points and the edge of the rubber cushions is greater

in the plate than in the cylinder for the same amount of surface exposed to friction; for, be it remarked, when the two charges thus separated have collected to a certain extent, a discharge will take place along this surface, the length of which limits therefore the ability of the machine to give a long spark.

It is usual to smear the surface of the rubber with an *electric amalgam*, consisting of equal parts of tin and zinc, mixed while molten with twice their weight of mercury. Such amalgams are applied to the cushions with a little stiff grease. They serve the double purpose of conducting away the negative charge separated upon the rubber during the action of the machine, and of affording as a rubber a substance which is more powerfully negative (see list in Art. 7) than the leather or the silk of the cushion itself.

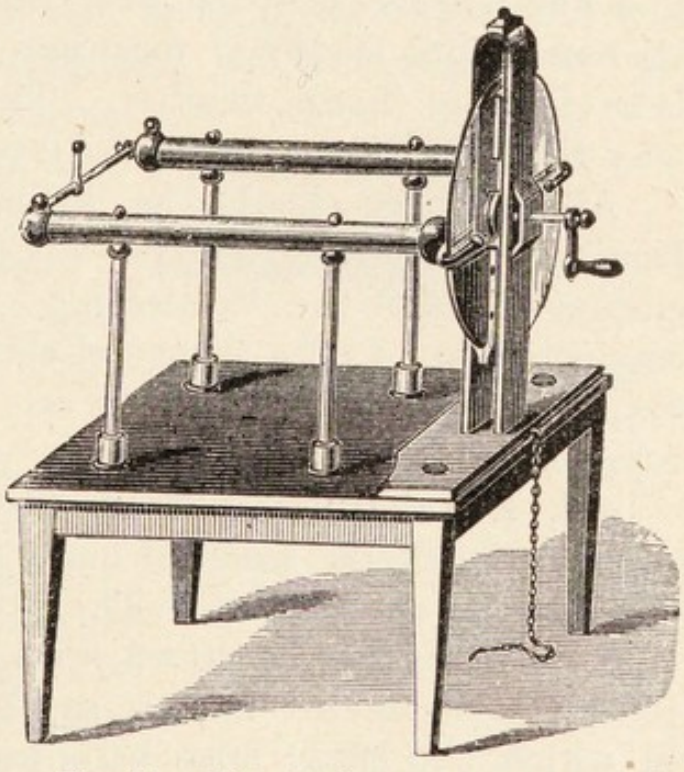


FIG. 31.—Plate Frictional Electrical Machine.

45. Precautions in using Frictional Machines.—Several precautions must be observed in the use of electrical machines. Damp and dust must be scrupulously avoided. The surface of glass is hygroscopic; hence, except in the driest climates, it is necessary to warm the glass surfaces and rubbers to dissipate the film of moisture which collects. Glass stems for insulation may be varnished with a thin coat of shellac varnish, or with paraffin (solid). Anhydrous paraffin (obtained by

dropping a lump of sodium into a bottle of paraffin oil), applied with a bit of flannel to the previously warmed surfaces, hinders the deposit of moisture. A frictional machine which has not been used for some months will require fresh amalgam on its rubbers. These should be cleaned and warmed, a thin uniform layer of tallow is spread upon them, and the amalgam, previously reduced to a fine powder, is sifted over the surface. In spite of all precautions frictional machines are uncertain in their behaviour in damp weather. This is the main reason why they have been superseded by influence machines.

All **points** should be avoided in apparatus for frictional electricity, except where they are expressly employed, like the "collecting" spikes on the prime conductor, to let off a charge of electricity. All the rods, etc., in frictional apparatus are therefore made with rounded knobs.

46. Experiments with the Electric Machine. —With the electric machine many pleasing and instructive experiments are possible. The phenomena of *attraction and repulsion* can be shown upon a large scale. Fig. 32 represents a device known as the **electric chimes**,[1] in which two small brass balls hung by silk strings are set in motion and strike against the bells between which they are hung. The two outer bells are hung by metallic wires or chains to the knob of the machine. The third bell is hung by a silk thread, but communicates with the ground by a brass chain. The balls are first attracted to the electrified outer bells, then repelled, and, having discharged themselves against the uninsulated central bell, are again attracted, and so vibrate to and fro.

By another arrangement small figures or dolls cut out of pith can be made to dance up and down between a metal plate hung horizontally from the knob of the

[1] Invented in 1752 by Franklin, for the purpose of warning him of the presence of atmospheric electricity, drawn from the air above his house by a pointed iron rod.

machine, and another flat plate an inch or two lower and communicating with "earth."

Another favourite way of exhibiting electric repulsion is by means of a doll with long hair placed on the machine; the individual hairs stand on end when the machine is worked, being repelled from the head and from one another. A paper tassel will behave similarly if hung to the prime conductor. The most striking way of showing this phenomenon is to place a person upon a glass-legged stool, making him touch the knob of the machine; when the machine is worked, his hair, if dry, will stand on end. Sparks will pass freely between a person thus electrified and one standing upon the ground.

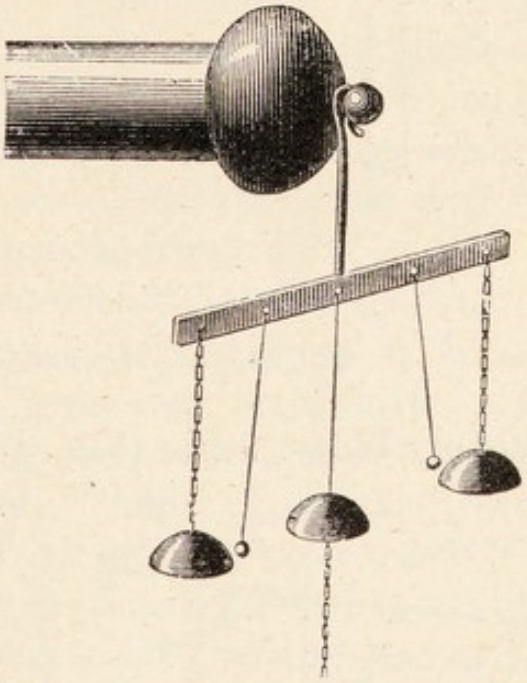


FIG. 32.—Electrical Chimes.

The sparks from the machine may be made to kindle spirits of wine or ether, placed in a metallic spoon, connected by a wire with the nearest metallic conductor that runs into the ground. A gas jet may be lit by passing a spark to the burner from the finger of the person standing electrified, as just described, upon an insulating stool.

47. Effect of Points; Electric Wind.—The *effect of points* in discharging electricity from the surface of a conductor may be readily proved by numerous experiments. If the machine be in good working order, and capable of giving, say, sparks 4 inches long when the knuckle is presented to the knob, it will be found that, on fastening a fine-pointed needle to the conductor, it discharges the electricity so effectually at its point that only the shortest sparks can be drawn at the knob, while a fine jet or brush

of pale blue light will appear at the point. If a lighted taper be held in front of the point, the flame will be

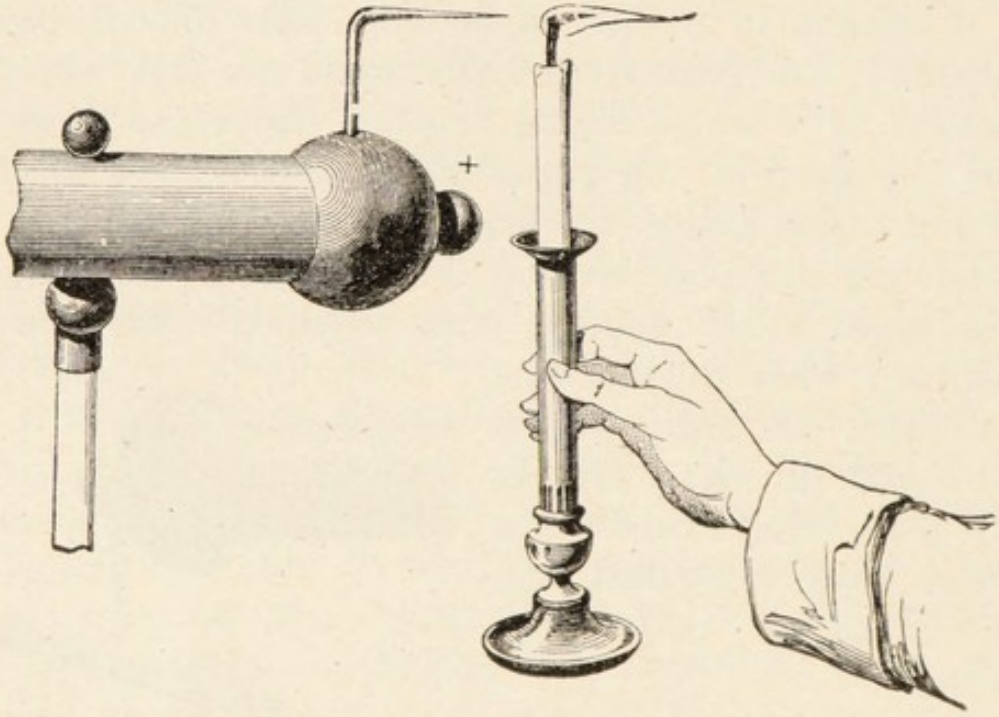


FIG. 33.—Wind produced by Discharge at a Point.

visibly blown aside (Fig. 33) by the streams of electrified air repelled from the point. These air-currents can be felt with the hand. They are due to a mutual repulsion between the electrified air particles near the point and the electricity collected on the point itself. That this mutual *reaction* exists is proved by the **electric fly** or **electric reaction-mill** of Hamilton (Fig. 34), which consists of a light cross of brass or straw, suspended on a pivot, and having the pointed ends bent round at right angles. When placed on the prime conductor of the machine, or joined to it by a chain, the

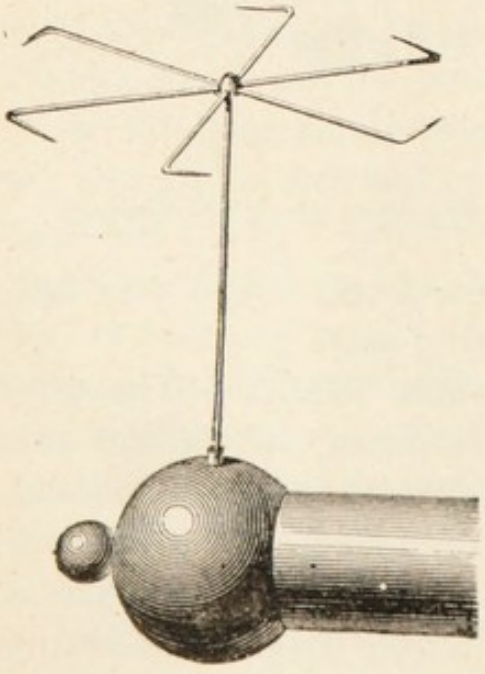


FIG. 34.—Hamilton's Mill.

force of repulsion between the charge on the points and that on the air immediately in front of them drives the mill round in the direction opposite to that in which the points are bent. It will even rotate if immersed in turpentine or petroleum. If the points of the fly are covered with small round lumps of wax it will not rotate, as the presence of the wax prevents the formation of any wind or stream of electrified particles.

The electric wind from a point will produce a charge upon the surface of any insulating body, such as a plate of ebonite or glass, held a few inches away. The charge may be examined by dusting red lead or lycopodium powder upon the surface. If a slip of glass or mica be interposed between the point and the surface against which the wind is directed, an electric *shadow* will be formed on the surface at the part so screened.

48. Armstrong's Hydro-Electrical Machine.— The friction of a jet of steam issuing from a boiler, through a wooden nozzle, generates electricity. In reality it is the particles of condensed water in the jet which are directly concerned. Lord Armstrong, who investigated this source of electricity, constructed a powerful apparatus, known as the **hydro-electrical machine**, capable of producing extraordinary discharges, yielding sparks 5 or 6 feet long. The collector consisted of a row of spikes, placed in the path of the steam jets issuing from wooden nozzles. It was supported, together with a brass ball which served as prime conductor, upon a glass pillar.

49. Influence Machines. — The second class of electrical machines comprises those that depend upon the principle of *influence*. They also have been termed *convection-induction machines*, because they depend upon the employment of a minute initial charge which, acting by influence, *induces* other charges, which are then *conveyed* by the moving parts of the machine to some other part, where they can be used either to increase the

initial charge or to furnish a supply of electrification to a suitable collector. Of such instruments the oldest is the *Electrophorus*, explained fully in Lesson III. Bennet, Nicholson, Erasmus Darwin, and others devised pieces of apparatus for accomplishing by mechanism that which the electrophorus accomplishes by hand. Nicholson's *revolving doubler*, invented in 1788, consists of a revolving apparatus, in which an insulated carrier can be brought into the presence of an electrified body, there touched for an instant while under influence, then carried forward with its acquired charge towards another body, to which it imparts its charge, and which in turn acts inductively on it, giving it an opposite charge, which it can convey to the first body, thus increasing its initial charge at every rotation.

In the modern influence machines two principles are embodied: (1) the principle of *influence*, namely, that a conductor touched while under influence acquires a charge of the opposite kind; (2) the principle of *reciprocal accumulation*. This principle must be carefully noted. Let there be two insulated conductors A and B electrified ever so little, one positively, the other negatively. Let a third insulated conductor C, which will be called a *carrier*, be arranged to move so that it first approaches A and then B, and so forth. If touched while under the influence of the small positive charge on A it will acquire a small negative charge; suppose that it then moves on and gives this negative charge to B. Then let it be touched while under the influence of B, so acquiring a small positive charge. When it returns towards A let it give up this positive charge to A, thereby increasing its positive charge. Then A will act more powerfully, and on repeating the former operations both B and A will become more highly charged. Each accumulates the charges derived by influence from the other. This is the fundamental action of the machines in question. The modern influence machines date from 1860, when C. F.

Varley produced a form with six carriers mounted on a rotating disk of glass. This was followed in 1865 by the machine of Holtz and that of Toepler, and in 1867 by those of Lord Kelvin (the "replenisher" and the "mouse-mill"). The influence machine in widest use is that of Wimshurst.

50. Typical Construction. — Before describing some special forms we will deal with a generalized type

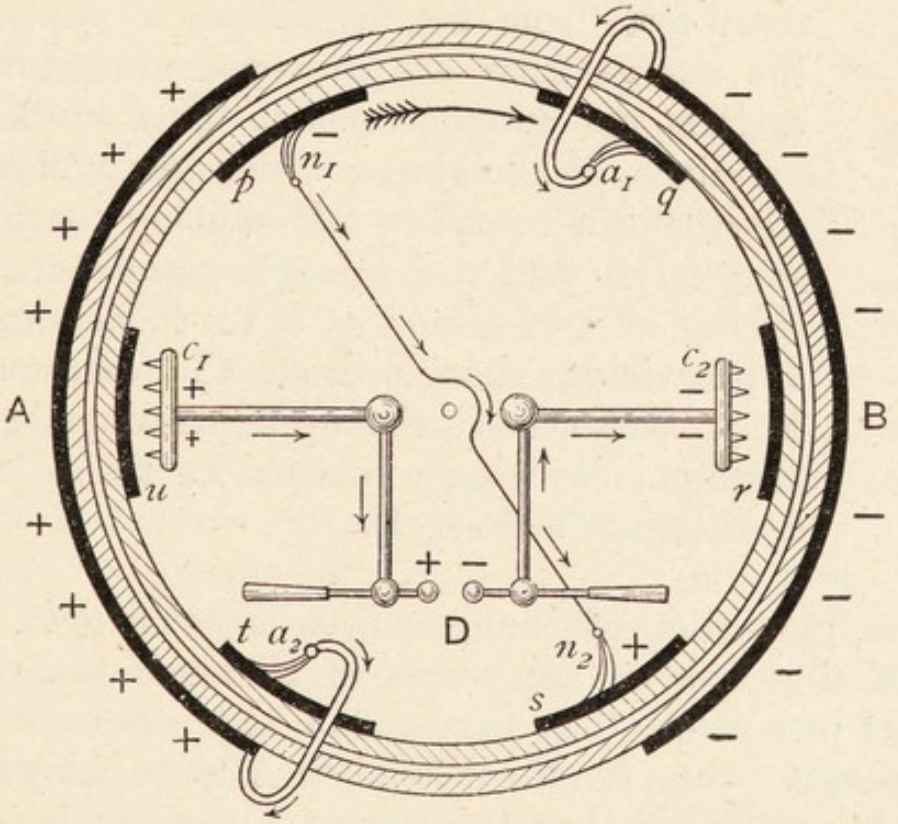


FIG. 35.—Diagram of Typical Influence Machine.

of machine having two fixed *field-plates*, A and B, which are to become respectively + and −, and a set of *carriers*, attached to a rotating disk or *armature*. Fig. 35 gives in a diagrammatic way a view of the essential parts. For convenience of drawing it is shown as if the metal field-plates A and B were affixed to the outside of an outer stationary cylinder of glass; the six carriers *p*, *q*, *r*, *s*, *t*, and *u* being attached to the inside of an inner rotating cylinder. The essential parts then are as follows:—

(i.) A pair of *field-plates* A and B.

(ii.) A set of *rotating carriers* p, q, r, s, t, and u.

(iii.) A pair of *neutralizing brushes* n_1, n_2 made of flexible metal wires, the function of which is to touch the carriers while they are under the influence of the field-plates. They are connected together by a *diagonal conductor*, which need not be insulated.

(iv.) A pair of *appropriating brushes* a_1, a_2, which reach over from the field-plates to appropriate the charges that are conveyed around by the carriers, and impart them to the field-plates.

(v.) In addition to the above, which are sufficient to constitute a complete self-exciting machine, it is usual to add a *discharging apparatus*, consisting of two *combs* c_1, c_2 to collect any unappropriated charges from the carriers after they have passed the appropriating brushes; these combs being connected to the adjustable discharging balls at D.

The operation of the machine is as follows. The neutralizing brushes are set so as to touch the moving carriers just before they pass out of the influence of the field-plates. Suppose the field-plate A to be charged ever so little positively, then the carrier p, touched by n_1 just as it passes, will acquire a slight negative charge, which it will convey forward to the appropriating brush a_1, and will thus make B slightly negative. Each of the carriers as it passes to the right over the top will do the same thing. Similarly each of the carriers as it passes from right to left at the lower side will be touched by n_2 while under the influence of the $-$ charge on B, and will convey a small $+$ charge to A through the appropriating brush a_2. In this way A will rapidly become more and more $+$, and B more and more $-$; and the more highly charged they become, the more do the collecting combs

c_1 and c_2 receive of unappropriated charges. Sparks will snap across between the discharging knobs at D.

The machine will not be self-exciting unless there is a good metallic contact made by the neutralizing brushes and by the appropriating brushes. If the discharging apparatus were fitted at c_1, c_2 with contact brushes instead of spiked combs, the field-plates of the machine would be liable to lose their charges, or even to have the charges reversed in sign, whenever a large spark was taken from the knobs.

It will be noticed that there are two thicknesses of glass between the fixed *field-plates* and the rotating *carriers*. The glass serves not only to hold the metal parts, but prevents the possibility of back-discharges (by sparks or winds) from the carriers to the field-plates as they pass.

The essential features thus set forth will be found in Varley's machine of 1860, in Lord Kelvin's "replenisher" (which had only two carriers), and in many other machines.

51. Toepler's Influence Machine. — In this machine, as constructed by Voss, are embodied various points due to Holtz and others. Its construction follows almost literally the diagram already explained, but instead of having two cylinders, one inside the other, it has two flat disks of varnished glass, one fixed, the other slightly smaller rotating in front of it (Fig. 36). The *field-plates* A and B consist of pieces of tinfoil, cemented on the back of the back disk, each protected by a coating of varnished paper. The *carriers* are small disks or sectors of tinfoil, to the number of six or eight, cemented to the front of the front disk. To prevent them from being worn away by rubbing against the brushes a small metallic button is attached to the middle of each. The neutralizing brushes n_1, n_2 are small whisps of fine springy brass wire, and are mounted on the ends of a diagonal conductor Z. The appropriating brushes a_1, a_2 are also of thin brass wire, and are fastened to clamps

projecting from the edge of the fixed disk, so that they communicate metallically with the two field-plates. The collecting combs, which have brass spikes so short as not to touch the carriers, are mounted on insulating pillars and are connected to the adjustable discharging knobs D_1, D_2. These also communicate with two small Leyden jars J_1, J_2, the function of which is to accumulate the charges before any discharge takes place. These jars are separately depicted in Fig. 37. Without them, the dis-

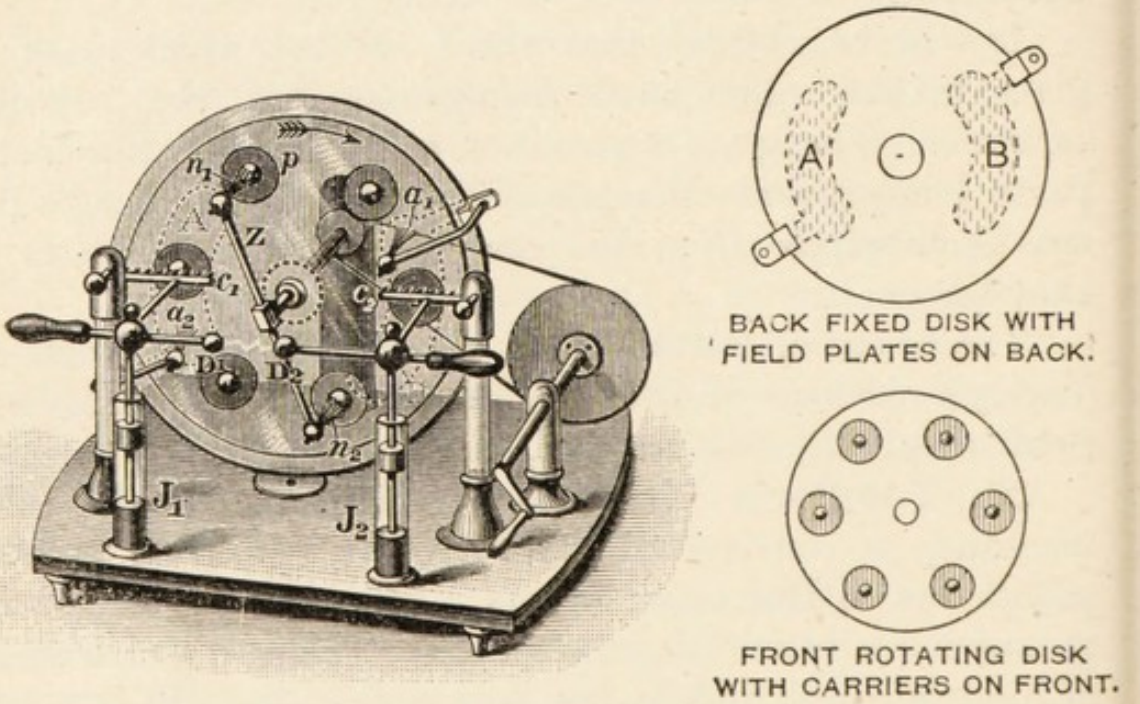


FIG. 36.—Toepler (Voss) Influence Machine.

charges between the knobs take place in frequent thin blue sparks. With them the sparks are less numerous, but very brilliant and noisy.

To use the Toepler (Voss) machine first see that all the four brushes are so set as to make good metallic contact with the carriers as they move past, and that the neutralizing brushes are set so as to touch the carriers while under influence. Then see that the discharging knobs are drawn widely apart. Set the machine in rotation briskly. If it is clean it should excite itself after a couple of turns, and will emit a gentle hissing

sound, due to internal discharges (visible as blue glimmers in the dark), and will offer more resistance to turning. If then the knobs are pushed nearer together sparks will pass across between them. The jars should be kept free from dust. Sometimes a pair of terminal screws are added at S_1, S_2 (Fig. 37), connected respectively with the outer coatings of the jars. These are convenient for attaching wires to lead away discharges for experiments at a distance. If not so used they should be joined together by a short wire, as the two jars will not work properly unless their outer coatings are connected.

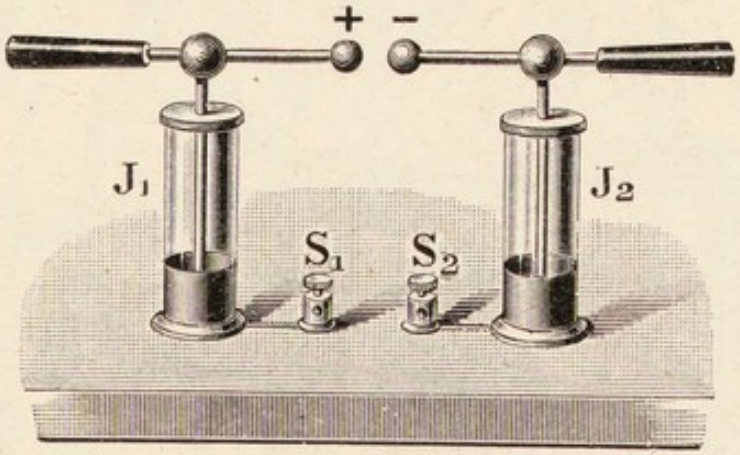


FIG. 37.—Leyden Jars, with Spark Discharge-gap.

52. Wimshurst's Influence Machine.—In this, the most widely used of influence machines, there are no fixed field-plates. In its simplest form it consists (Fig. 38) of two circular plates of varnished glass, which are geared to rotate in opposite directions. A number of sectors of metal foil are cemented to the front of the front plate and to the back of the back plate; these sectors serve both as carriers and as inductors. Across the front is fixed an uninsulated diagonal conductor, carrying at its ends neutralizing brushes, which touch the front sectors as they pass. Across the back, but sloping the other way, is a second diagonal conductor, with brushes that touch the sectors on the hinder plate. Nothing more than this is needed for the machine to

excite itself when set in rotation; but for convenience there is added a collecting and discharging apparatus. This consists of two pairs of insulated combs, each pair having its spikes turned inwards toward the revolving disks, but not touching them; one pair being on the right, the other on the left, mounted each on an insulat-

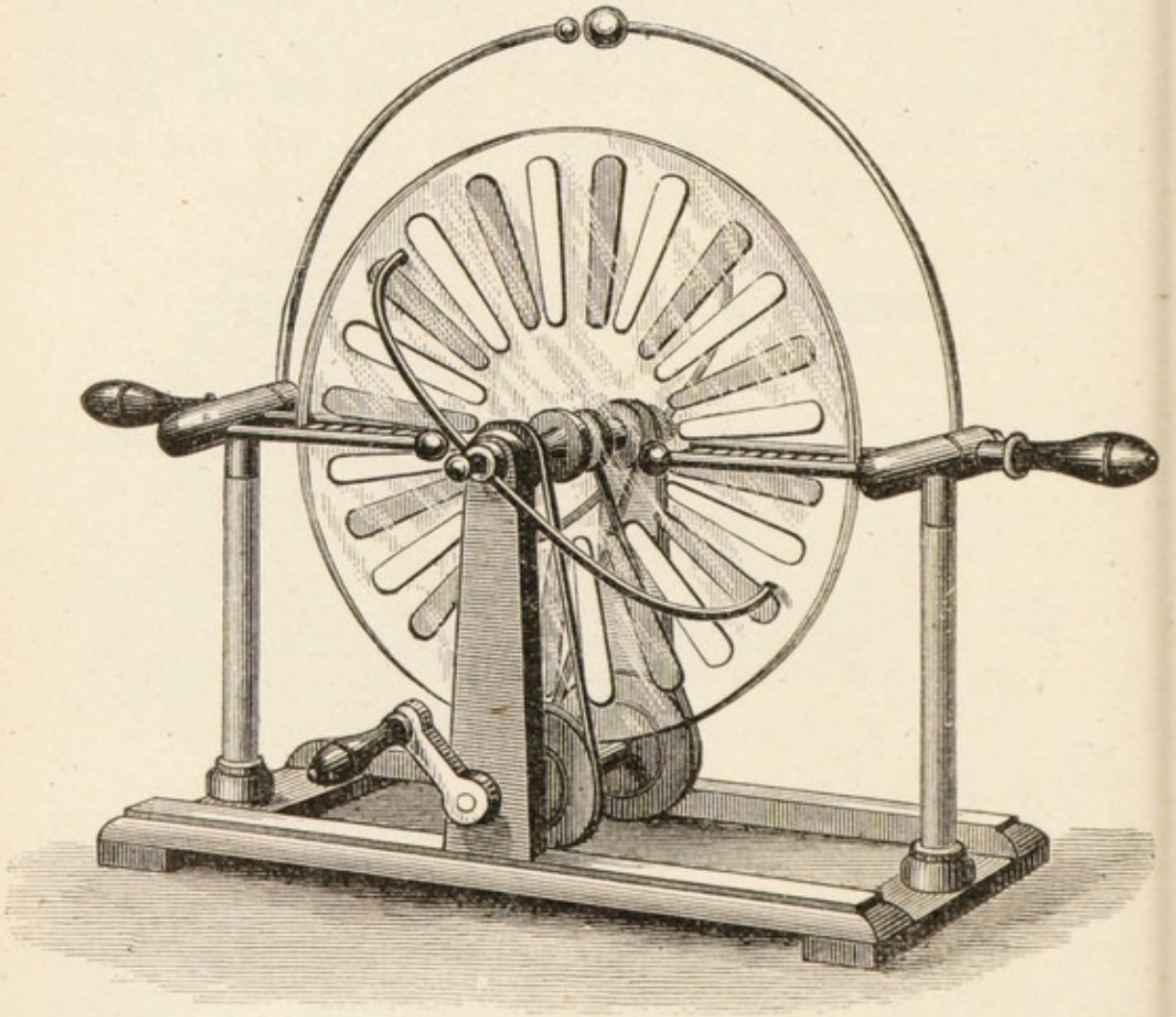


FIG. 38.—Wimshurst's Influence Machine.

ing pillar of ebonite. These collectors are furnished with a pair of adjustable discharging knobs overhead; and sometimes a pair of Leyden jars are added, to prevent the sparks from passing until considerable quantities of charge have been collected.

The processes that occur in this machine are best explained by aid of a diagram (Fig. 39), in which, for

greater clearness, the two rotating plates are represented as though they were two cylinders of glass, rotating opposite ways, one inside the other. The inner cylinder will represent the front plate, the outer the back plate. In Figs. 38 and 39 the front plate rotates right-handedly, the back plate left-handedly. The neutraliz-

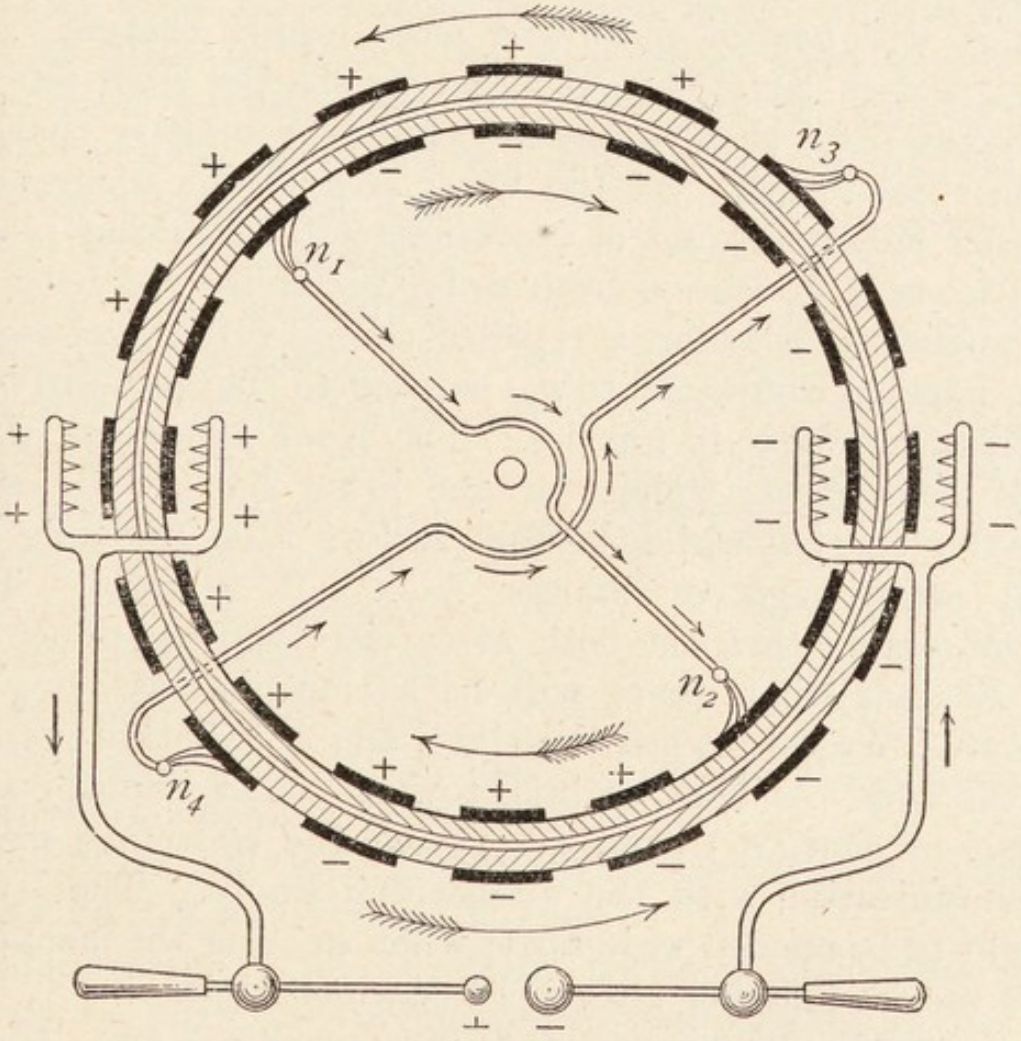


FIG. 39.—Diagram of Wimshurst's Influence Machine.

ing brushes n_1, n_2 touch the front sectors, while n_3, n_4 touch against the back sectors.

Now suppose any one of the back sectors represented near the top of the diagram to receive a slight positive charge. As it is moved onward toward the left it will come opposite the place where one of the front sectors is moving past the brush n_1. The result will be that the

sector so touched while under influence by n_1 will acquire a slight negative charge, which it will carry onwards toward the right. When this negatively-charged front sector arrives at a point opposite n_3 it acts inductively on the back sector which is being touched by n_3; hence this back sector will in turn acquire a positive charge, which it will carry over to the left. In this way all the sectors will become more and more highly charged, the front sectors carrying over negative charges from left to right, and the back sectors carrying over positive charges from right to left. At the lower half of the diagram a similar but inverse set of operations will be taking place. For when n_1 touches a front sector under the influence of a positive back sector, a repelled charge will travel along the diagonal conductor to n_2, helping to charge positively the sector which it touches. The front sectors, as they pass from right to left (in the lower half), will carry positive charges, while the back sectors, after touching n_1, will carry negative charges from left to right. The metal sectors then act both as carriers and as inductors. It is clear that there will be a continual carrying of positive charges toward the right, and of negative charges to the left. At these points, toward which the opposite kinds of charges travel, are placed the collecting *combs* communicating with the discharging knobs. The latter ought to be opened wide apart when starting the machine, and moved together after it has excited itself.

In larger Wimshurst influence machines two, three, or more pairs of oppositely-rotating plates are mounted within a glass case to keep off the dust. If the neutralizing brushes make good metallic contact these machines are all self-exciting in all weathers. Machines with only six or eight sectors on each plate give longer sparks, but less frequently than those that have a greater number. Mr. Wimshurst designed many influence machines, from small ones with disks 2 inches across up to that at South Kensington, which has plates 7 feet in diameter.

53. Holtz's Influence Machine. — The Holtz machine in its typical form had the following peculiarities. There were no metal carriers upon the rotating plate, hence another mode of charging it had to be adopted in lieu of touching conductors while under influence, as will be seen. The field-plates A and B (Fig. 40) were of varnished paper—a poor conductor—fastened upon the back of the fixed disk. In the fixed disk of glass, on which the field-plates were mounted, there were cut two windows or openings, through which there projected from the field-plates two pointed paper tongues, which took the place of appropriating brushes. The discharging knobs were inserted in the neutralizing circuit which united two metal combs with pointed spikes, situated in front of the rotating front disk, opposite the two field-plates. There was no diagonal conductor. Fig. 40 is a view of the machine from behind. The machine was not self-exciting, but required to be excited by giving it a small initial charge.

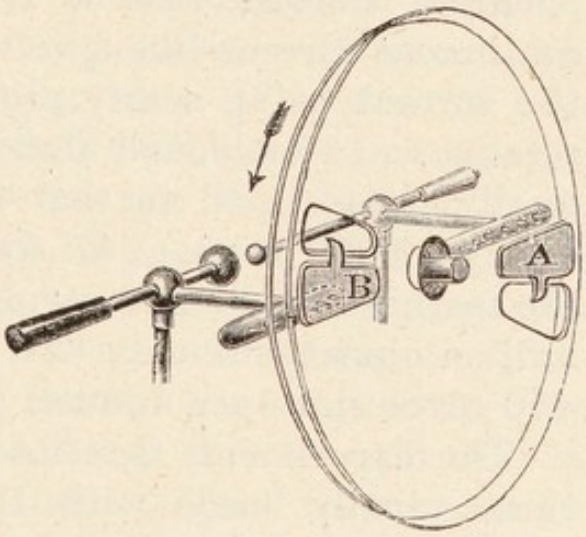


FIG. 40.—Holtz's Influence Machine.

The action of the machine depends upon the circumstance that the surface of a non-conducting body, such as glass, can be electrified by letting off against it an electric wind from a point placed near it (see Art. 47).

The defects of the Holtz machine were that it was so sensitive to damp weather as to be unreliable, that it was apt suddenly to reverse its charges, and that the electric winds by which it operated could not be produced without a sufficiently great initial charge. Holtz constructed many forms of machine, including one with thirty-two

plates, besides machines of a second kind having two glass plates rotating in opposite directions.

54. Experiments with Influence Machines.—Every kind of influence machine is *reversible* in its action; that is to say, that if a continuous supply of the two electricities (furnished by another machine) be communicated to the carriers, the movable plate will be thereby set in rotation and, if allowed to run quite freely, will run *as a motor*, turning in the opposite direction to that in which it would have to be turned in order to make it work as a generator.

Righi showed that a Holtz machine can yield a continuous current like a voltaic battery, the strength of the current being nearly proportional to the velocity of rotation. It was found that the electromotive-force of a machine was equal to that of 52,000 Daniell's cells, or nearly 53,000 volts, at all speeds. The resistance when the machine made 120 revolutions per minute was 2810 million ohms; but only 646 million ohms when making 450 revolutions per minute.

The experiments described in Art. 46, and indeed all those usually made with the old frictional machines, including the charging of Leyden jars, can be performed by the aid of influence machines. In some cases it is well to connect one of the two discharging knobs to the earth by a wire or chain, and to take the discharge from the other knob. To illuminate small vacuum tubes they may be connected by guttapercha-covered wires to the two discharging knobs, or to the terminals S_1, S_2 of Fig. 37.

55. Dispersal of Fog.—The electric discharge from a point possesses the curious property of collecting *dust* or *fumes* from the air. This is readily shown by connecting one pole of an influence machine by a wire to a sharp-pointed needle which is introduced into a bell-jar of glass. The latter is filled with fumes by burning inside it a bit of magnesium wire or brown paper. Then on turning

the handle of the influence machine the fumes are at once deposited, and the air left clear. Sir Oliver Lodge has proposed this as a method of clearing away fogs.

LESSON VI.—*The Leyden Jar and other Condensers*

56. Action across a Dielectric.—It was shown in previous lessons that the opposite charges of electricity attract one another; that electricity cannot flow through glass; and that yet electricity can *act across* glass by influence. Two suspended pith-balls, one electrified positively and the other negatively, will attract one another across the intervening air. If a plate of glass be put between them they will still attract one another, though neither they themselves nor the electric charges on them can pass through the glass. If a pith-ball electrified with a − charge be hung inside a dry glass bottle, and a rubbed glass rod be held outside, the pith-ball will rush to the side of the bottle nearest to the glass rod, being attracted by the + charge thus brought near it. If a pane of glass be taken, and a piece of tinfoil be stuck upon the middle of each face of the pane, and one piece of tinfoil be charged positively, and the other negatively, the two charges will attract one another across the glass, and will no longer be found to be free. If the pane is set up on edge, so that neither piece of tinfoil touches the table, it will be found that hardly any electricity can be got by merely touching either of the foils, for the charges are "bound," so to speak, by each other's attractions; each charge is inducing the other. In fact it will be found that these two pieces of tinfoil may be, in this manner, charged a great deal more strongly than either of them could possibly be if it were stuck to a piece of glass alone, and then electrified. In other words, *the capacity of a conductor is greatly increased when it is placed near to a conductor electrified with the opposite kind of charge.*

If its capacity is increased, a greater quantity of electricity may be put into it before it is charged to an equal degree of potential. Hence, such an arrangement for holding a large quantity of electrification may be called a **condenser** of electricity.

57. Condensers.—Next, suppose that we have two brass disks, A and B (Fig. 41), set upon insulating stems, and that a glass plate is placed between them. Let B be connected by a wire to the knob of an electrical machine, and let A be joined by a wire to "earth." The + charge upon B will act inductively across the glass plate on A, and will draw electrons out of the earth, making the nearest face of A negatively electrified. This − charge on A will attract the + charge of B to the side nearest the glass, and a fresh supply of electricity will come from the machine. Thus this arrangement will become a condenser.

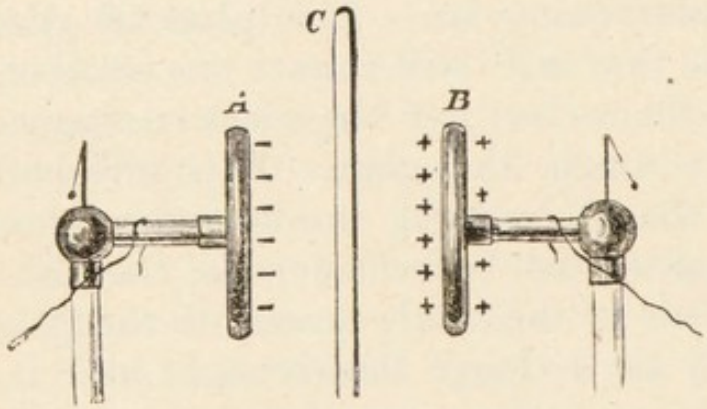


FIG. 41.—Condenser made of two Metal Plates.

If the two brass disks are pushed up close to the glass plate there will be a still stronger attraction between the + and − charges, because they are now nearer one another, and the inductive action will be greater; hence a still larger quantity can be accumulated in the plates. We see then that the capacity of a condenser is increased by bringing the plates near together. If now, while the disks are strongly charged, the wires are removed and the disks are drawn backwards from one another, the two charges will not hold one another bound so strongly, and there will be more *free* electrification than before over their surfaces. This would be rendered evident to the experimenter by the little pith-ball electroscopes fixed to them

(see the Fig.), which would fly out as the brass disks were moved apart. We have put no further charge on the disk B, and yet, from the indications of the electroscope, we should conclude that by moving it away from disk A it has become electrified to a higher degree. The fact is, that while the conductor B was near the – charge of A the *capacity* of B was greatly increased, but on moving it away from A its capacity has diminished, and hence the same quantity of electricity now electrifies it to a higher degree than before. The presence, therefore, of an earth-connected plate near an insulated conductor increases its capacity, and permits it to accumulate a greater charge by attracting and *condensing* the electricity upon the face nearest the earth-plate, the surface-density on this face being therefore very great; hence the appropriateness of the term *condenser* as applied to the arrangement. It was formerly also called an **accumulator**; but the term *accumulator* is now reserved for the special kind of battery for storing the energy of electric currents (Art. 572).

The stratum of *air* between the two disks will suffice to insulate the two charges one from the other. The brass disks thus separated by a stratum of air constitute an **air-condenser**, or **air-leyden.** Such condensers were first devised by Wilcke and Aepinus. In these experiments the sheet of glass or layer of air acts as a *dielectric* (Art. 315) conveying the inductive action through its substance. All dielectrics are insulators, but equally good insulators are not necessarily equally good dielectrics. Air and glass are far better insulators than ebonite or paraffin in the sense of being much worse conductors. But influence acts more strongly across a slab of glass than across a slab of ebonite or paraffin of equal thickness, and better still across these than across a layer of air. In other words, glass is a better **dielectric** than ebonite, or paraffin, or air, as it possesses a higher inductive capacity.

It will then be seen that in the act of charging a

condenser, as much electricity flows out at one side as flows in at the other.

58. Displacement.—Whenever electric forces act on a dielectric, tending to drive electricity in at one side and out at the other, we may draw lines of force through the dielectric in the direction of the action, and we may consider tubular spaces mapped out by such lines. We may consider a tube of electric force having at one end a definite area of the positively charged surface, and at the other end an area of the negatively charged surface. These areas may be of different size or shape, but the quantities of + and − electrification over them will be equal. The quantity of electricity which has apparently been transferred along the tube was called by Maxwell "the *displacement*." In non-conductors it is proportional to the electromotive-force. In conductors electromotive forces produce currents, which may be regarded as displacements that increase continuously with time. In certain crystalline media the displacement does not take place exactly in the direction of the electric force: in this case we should speak of tubes of influence rather than tubes of force. A unit tube will be bounded at its two ends by unit charges + and −. We may consider the whole electric field between positively and negatively charged bodies as mapped out into such tubes.

59. Capacity of a Condenser.—It appears, therefore, that the capacity of a condenser will depend upon—

(1) The size and form of the metal plates or coatings.
(2) The thinness of the stratum of dielectric between them; and
(3) The dielectric capacity of the material.

60. The Leyden Jar.—The Leyden Jar, called after the city where it was invented, is a convenient form of condenser. It usually consists (Fig. 42) of a glass jar coated up to a certain height on the inside and outside with tinfoil. A brass knob fixed on the end of a stout

brass wire passes downward through a lid or top of dry well-varnished wood, and communicates by a loose bit of brass chain with the inner coating of foil. To charge the jar the knob is held to the prime conductor of an electrical machine, the outer coating being either held in the hand or connected to "earth" by a wire or chain. When a + charge of electricity is imparted thus to the inner coating, it acts inductively on the outer coating, attracting a − charge into the face of the outer coating nearest the glass, and repelling a + charge to the outside of the outer coating, and thence through the hand or wire to earth. After a few moments the jar will have acquired its full charge, the outer coating being − and the inner +. If the jar is of good glass, and dry, and free from dust, it will retain its charge for many hours or days. But if a path be provided by which the two mutually attracting electricities can flow to one another, they will do so, and the jar will be instantaneously discharged. If the outer coating be grasped with one hand, and the knuckle of the other hand be presented to the knob of the jar, a bright spark will pass between the knob and the knuckle with a sharp report, and at the same moment a convulsive "shock" will be communicated to the muscles of the wrists, elbows, and shoulders. A safer means of discharging the jar is afforded by the **discharging tongs** or **discharger** (Fig. 43), which consists of a jointed brass rod provided with brass knobs and a glass handle. One



FIG. 42.—Leyden Jar.

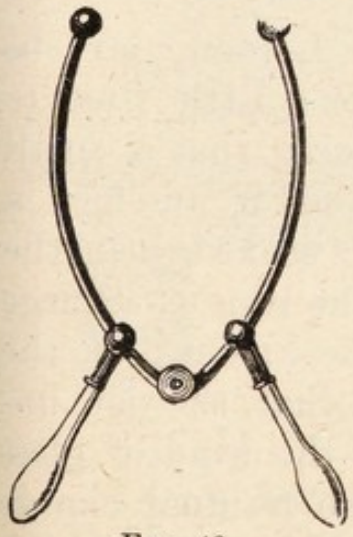


FIG. 43.
Discharging Tongs.

knob is laid against the outer coating, the other is then brought near the knob of the jar, and a bright snapping spark leaping from knob to knob announces that the two accumulated charges have flowed together, completing the discharge. Sometimes a jar discharges itself by a spark climbing over the top edge of the jar. Often when a jar is well charged a hissing sound is heard, due to partial discharges creeping over the edge. They can be seen in the dark as pale phosphorescent streams.

61. Discovery of the Leyden Jar.—The discovery of the Leyden jar arose from the attempt of Musschenbroek and his pupil Cuneus[1] to collect the supposed electric "fluid" in a bottle half filled with water, which was held in the hand and was provided with a nail to lead the "fluid" down through the cork to the water from the electric machine. Here the water served as an inner coating and the hand as an outer coating to the jar. Cuneus on touching the nail received a shock. This accidental discovery created the greatest excitement in Europe and America.

62. Residual Charges.—If a Leyden jar be charged and discharged and then left for a little time to itself, it will be found on again discharging that a small second spark can be obtained. There is in fact a **residual charge** which seems to have soaked into the glass or been absorbed. The return of the residual charge is hastened by tapping the jar. The amount of the residual charge varies with the time that the jar has been left charged; it also depends on the kind of glass of which the jar is made. There is no residual charge discoverable in an air-leyden after it has once been discharged.

63. Batteries of Leyden Jars.—A large Leyden jar will give a more powerful shock than a small one, for a larger charge can be put into it; its capacity is

[1] The honour of the invention of the jar is also claimed for Kleist, Bishop of Pomerania.

greater. If it is desired to accumulate a very great charge of electricity, a number of jars must be employed, all their inner coatings being connected together, and all their outer coatings being united. This arrangement is called a **battery of Leyden jars**, or Leyden battery (Fig. 44). As it has a large capacity, it will require a

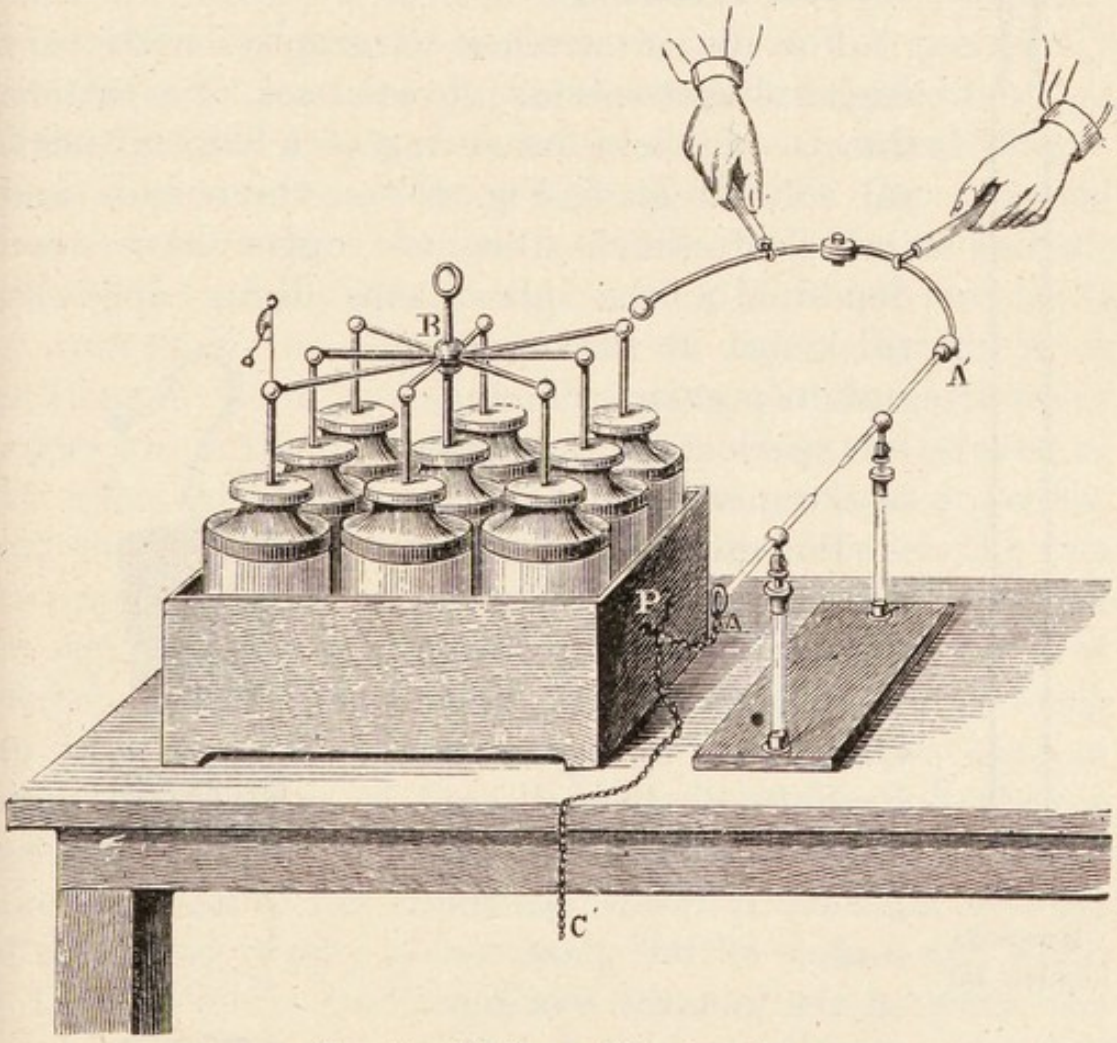


FIG. 44.—Battery of Leyden Jars.

large quantity of electricity to charge it fully. When charged it produces very powerful effects; its spark will pierce glass readily, and every care must be taken to avoid a shock from it passing through the person, as it might be fatal. A Leyden jar made of *thin* glass has a greater capacity as a condenser than a thick one of the same size; but if it is too thin it will be destroyed when powerfully charged by a spark actually piercing the glass.

To prevent jars from being pierced by a spark, the highest part of the inside coating should be connected across by a strip of foil or a metallic disk to the central wire.

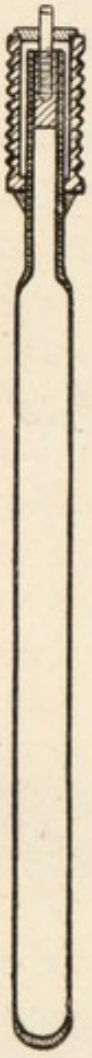


FIG. 45. Moscicki Leyden Jar.

64. High Voltage Jars.—If a jar is desired to give *long sparks*, there must be left a long space of varnished glass above the top of the coatings.

For use in wireless telegraphy, with very high voltages special jars are used, of a pattern due to Moscicki, consisting of a long cylindrical tube of glass, Fig. 45, on the outside and inside of which films of copper have been deposited; the glass tube being specially thickened at the upper end to prevent piercing by a spark at the top edges of the metal coatings.

For the forms of condensers used in telegraphy see Art. 322, p. 300.

65. Seat of the Charge.—Benjamin Franklin discovered that the charges of the Leyden jar really reside on the surface of the glass, not on the metallic coatings. This he proved by means of a jar whose coatings could be removed (Fig. 46). The jar was charged and placed upon an insulating stand. The inner coating was then lifted out, and the glass jar was then taken out of the outer coating. Neither coating was found to be electrified to any extent, but on again putting the jar together it was found to be highly charged. The charges had all the

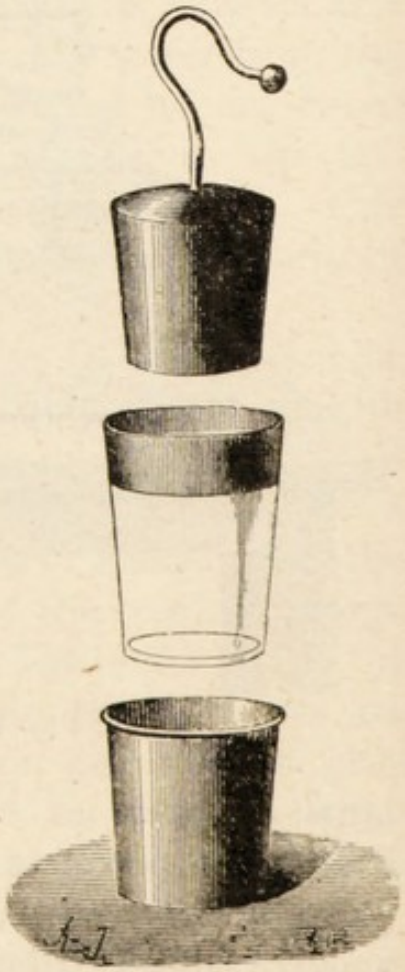


FIG. 46.—Dissectable Leyden Jar.

time remained upon the inner and outer surfaces of the glass dielectric.

66. Dielectric Strain.—Faraday proved that the medium across which influence takes place really plays an important part in the phenomena. It is now known that all dielectrics across which inductive actions are at work are thereby *strained*.[1] Inasmuch as a good vacuum is a good dielectric, it is clear that it is not necessarily the material particles of the dielectric substance that are thus affected; hence it is believed that electrical phenomena are due to stresses and strains in the so-called "ether" (the thin medium pervading all matter and all space), the highly elastic constitution of which enables it to convey to us the vibrations of light, though it is millions of times less dense than air. As the particles of bodies are intimately surrounded by ether, the stresses in the ether are also communicated to the particles of bodies, and they too suffer a strain. The glass between the two coatings of tinfoil in the Leyden jar is actually strained or squeezed, there being a tension along the lines of electric force. When an insulated charged ball is hung up in a room an equal amount of the opposite kind of charge is attracted to the inside of the walls, and the air between the ball and the walls is **strained** (electrically) like the glass of the Leyden jar. If a Leyden jar is made of thin glass it may give way under the stress; and when a Leyden jar is discharged the layer of air between the knob of the jar and the knob of the discharging tongs is more and more strained as they are approached towards one another, till at last the stress becomes too great, and the layer of air gives way, and is perforated by the spark that discharges itself across. The existence of such stresses enables us to understand the residual charge of Leyden jars in which the glass does not recover itself all

[1] In the exact sciences a *strain* means an alteration of form or volume due to the application of a stress. A *stress* is the force, pressure, or other agency which produces a strain.

at once, by reason of its viscosity, from the strain to which it has been subjected. It must never be forgotten that **electric force acts across space in consequence of the transmission of stresses and strains in the medium with which space is filled.** In every case we store not electricity but *energy*. Work is done in pushing electricity from one place to another against the forces which tend to oppose the movement. The charging of a Leyden jar may be likened to the operation of bending a spring, or to pumping up water from a low level to a high one. In charging a jar we pump exactly as many electrons into the negative side as we pump out of the positive side, and we spend energy in so doing. It is this stored energy which afterwards reappears in the discharge.

LESSON VII.—*Other Sources of Electrification*

67. Other Sources.—It was remarked at the close of Lesson I. (p. 13) that **friction** was by no means the only means of electrification. Some of the other sources will now be named.

68. Percussion.—A violent blow struck by one substance upon another produces opposite electrical states on the two surfaces. It is possible indeed to draw up a list resembling that of Art. 7, in such an order that each substance will take a + charge on being struck with one lower on the list.

69. Disruption and Cleavage.—If a card be torn asunder in the dark, sparks are seen, and the separated portions, when tested with an electroscope, will be found to be electrical. The linen faced with paper used in making strong envelopes and for paper collars, shows this very well. Lumps of sugar, crunched in the dark between the teeth, exhibit pale flashes of light. The sudden cleavage of a sheet of mica also produces sparks, and both laminæ are found to be electrified.

70. Crystallization and Solidification.—Many substances, after passing from the liquid to the solid state, exhibit electrical conditions. Sulphur fused in a glass dish and allowed to cool is violently electrified, as may be seen by lifting out the crystalline mass with a glass rod. Chocolate also becomes electrical during solidification. When arsenic acid crystallizes out from its solution in hydrochloric acid, the formation of each crystal is accompanied by a flash of light, doubtless due to an electrical discharge. A curious case occurs when the sulphate of copper and potassium is fused in a crucible. It solidifies without becoming electrical, but on cooling a little further the crystalline mass begins to fly to powder with an instant evolution of electricity.

71. Combustion. — Volta showed that combustion generated electricity. A piece of burning charcoal, or a burning pastille, such as is used for fumigation, placed in connexion with the knob of a gold-leaf electroscope, will cause the leaves to diverge.

72. Evaporation.—The evaporation of liquids is often accompanied by electrification, the liquid and the vapour assuming opposite states, though apparently only when the surface is in agitation. A few drops of a solution of sulphate of copper thrown into a hot platinum crucible produce violent electrification as they evaporate.

73. Atmospheric Electricity.—The atmosphere is found to be always electrified relatively to the earth: this is due, in part possibly, to evaporation going on over the oceans. The subject of atmospheric electricity is treated of separately in Arts. 353 to 361.

74. Compression.—A large number of substances when compressed exhibit electrification on their surface. Thus cork becomes + when pressed against amber, gutta-percha, and metals; while it takes a − charge when pressed against spars and animal substances.

75. Pyro-electricity.—There are certain crystals which, while being heated or cooled, exhibit electrical

charges at certain regions or poles. Crystals thus electrified by heating or cooling are said to be **pyro-electric.** Chief of these is the **Tourmaline,** whose power of attracting light bodies to its ends after being heated has been known for some centuries. It is alluded to by Theophrastus and Pliny under the name of *Lapis Lyncurius.* Tourmaline is a hard mineral, semi-transparent when cut into thin slices, and of a dark green or brown colour, but looking perfectly black and opaque in its natural condition, and possessing the power of polarizing light. It is usually found in slightly irregular three-sided prisms which, when perfect, are pointed at both ends. It belongs to the "hexagonal" system of crystals, but is only hemihedral, that is to say, has the alternate faces only developed. Its form is given in Fig. 47, where a general view is first shown, the two ends A and B being depicted in separate plans. These two ends differ slightly in shape. Each is made up of three sloping faces terminating in a point. But at A the edges between these faces run down to the corners of the prism, while in B the edges between the terminal faces run down to the middle points of the long faces of the prism. The end A is known as the **analogous** pole, and B as the **antilogous** pole. While the crystal is rising in temperature A exhibits + electrification, B − ; but if, after having been heated, it is allowed to cool, the polarity is reversed; for during the time that the temperature is falling B is + and A is −. If the temperature is steady no such electrical effects are observed either at high or low temperatures; and the phenomena cease if the crystal be warmed above 150° C. This is not, however, due to the crystal becoming a conductor at that temperature; for its resistance at even higher temperatures is still so great as to make it practically a non-conductor. A heated crystal of tourmaline suspended by a silk fibre may be attracted and repelled by electrified bodies, or by a second heated

tourmaline; the two similar poles repelling one another, while the two poles of opposite form attract one another. If a crystal be broken up, each fragment is found to possess also an analogous and an antilogous pole.

Many other crystals beside the tourmaline are more or less pyro-electric. Amongst these are silicate of zinc ("electric calamine"), boracite, cane-sugar, quartz, tartrate of potash, sulphate of quinine, and several others. *Boracite* crystallizes in the form shown in Fig. 48, which represents a cube having four alternate corners truncated. The corners not truncated behave as analogous poles, the

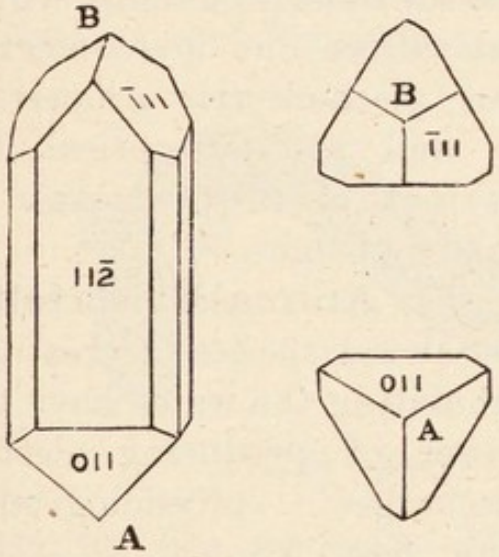


FIG. 47.—Crystal of Tourmaline.

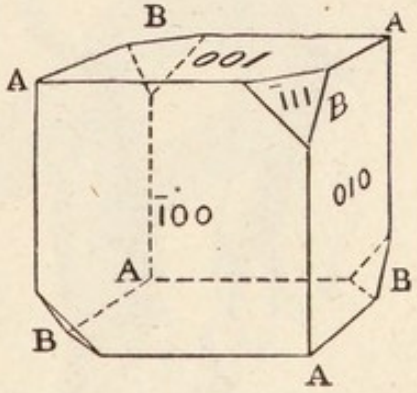


FIG. 48.—Crystal of Boracite.

truncated ones as antilogous. When a natural hexagonal prism of quartz is heated, its six edges are found to be + and – in alternate order.

76. Piezo-electricity.—In certain crystals pressure in a particular direction may produce electrification. Haüy found that a crystal of calcspar pressed between the dry fingers, so as to compress it along the blunt edges of the crystal, became electrical, and that it retained its electricity for some days. He even proposed to employ a squeezed suspended crystal as an electroscope. A similar property is alleged of mica, topaz, and fluorspar. If two opposite edges of a hexagonal prism of quartz are pressed

together, one becomes +, the other −. Pressure also produces opposite kinds of electrification at opposite ends of a crystal of tourmaline, and of other crystals of the class already noticed as possessing the peculiarity of skew-symmetry or hemihedry in their structure. *Piezo-electricity* is the name given to this branch of the science. It is known that skew-symmetry of structure is dependent on molecular constitution; and it is doubtless the same peculiarity which determines the pyro-electric and piezo-electric properties, as well as the optical behaviour of these crystals in polarized light.

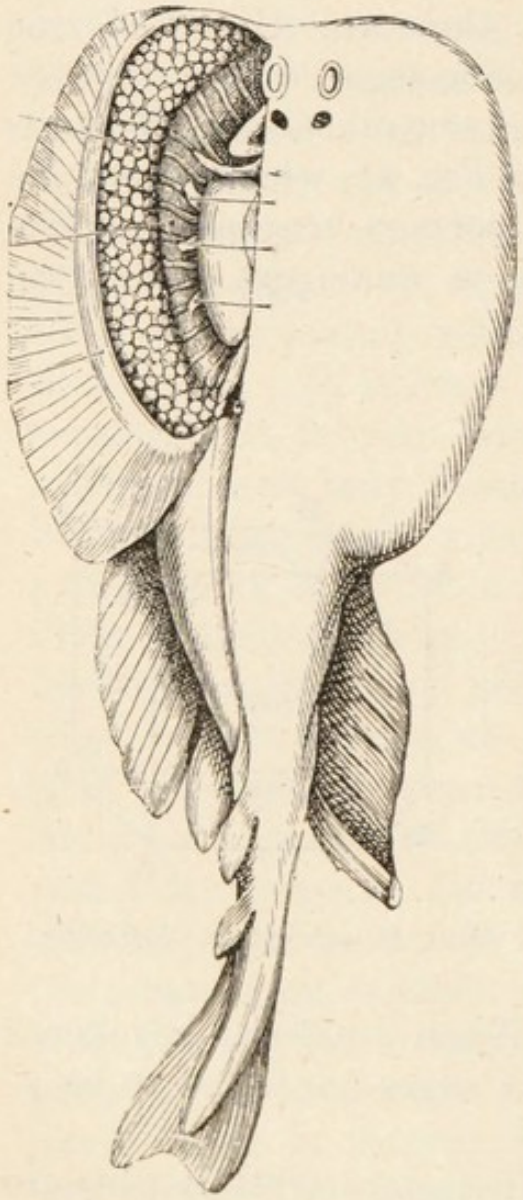


FIG. 49.—Torpedo or Raia.

77. Animal Electricity.—Several species of creatures inhabiting the water have the power of producing electric discharges physiologically. The best known of these creatures are the *Torpedo*, the *Gymnotus*, and the *Silurus*. The **Raia Torpedo**,[1] or electric ray, of which there are three species inhabiting the Mediterranean and Atlantic, is provided with an electric organ on the back of its head as shown in Fig. 49. This organ consists of laminæ composed of polygonal cells to the number of 800

[1] It is a curious point that the Arabian name for the torpedo, *ra-ad*, signifies *lightning*. This is perhaps not so curious as that the *Electra* of the Homeric legends should possess certain qualities that would tend to suggest that she is a personification of the *lightning*. The resemblance between the names *electra* and *electron* (amber) cannot be accidental.

or 1000, or more, supplied with four large bundles of nerve fibres; the under surface of the fish is −, the upper +. In the **Gymnotus electricus**, or Surinam eel (Fig. 50), the electric organ goes the whole length of the body from tail to head. Humboldt gives a lively account of the combats between the electric eels and the wild horses, driven by the natives into the swamps inhabited by the Gymnotus. It is able to give a most terrible shock, and is a formidable antagonist when it has attained its full length of 5 or 6 feet. In the **Silurus** the current flows from head to tail.

Nobili, Matteucci, and others have shown that nerve-excitations and muscular contractions of human beings

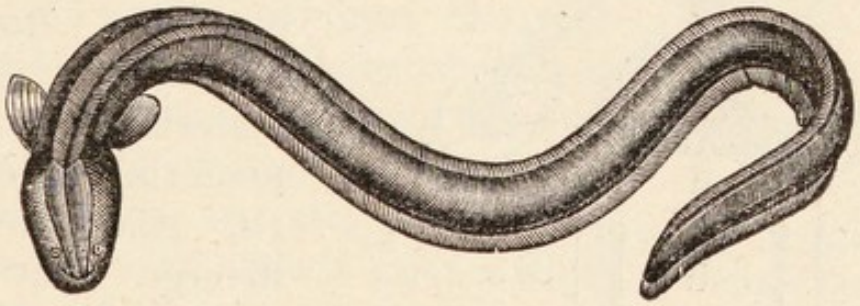


FIG. 50.—Electric Eel or Gymnotus.

also give rise to feeble discharges of electricity. The beating of the heart creates a rhythmical electromotive force.

78. Electricity of Vegetables.—Buff thought he detected electrification produced by plant life; the roots and juicy parts being negatively, and the leaves positively, electrified. The subject has, however, been little investigated.

79. Thermo-electricity.—*Heat* applied at the junction of two dissimilar metals produces a flow of electricity across the junction. This subject is discussed in Arts. 471 to 480 on *Thermo-electric Currents*.

80. Contact of Dissimilar Metals.—Volta showed that the contact of two dissimilar metals in air produced opposite kinds of electrification, one becoming positively,

and the other negatively, electrified. This he proved in several ways, one of the most conclusive proofs being that afforded by his *condensing electroscope*. This consisted of a gold-leaf electroscope combined with a small condenser. A metallic plate formed the top of the electroscope, and on this was placed a second metallic plate furnished with a handle, and insulated from the lower one by being well varnished at the surface (Fig. 51). As the capacity of such a condenser is considerable, a very feeble source may supply a quantity of electricity to the condenser without materially raising its potential, or causing the gold leaves to diverge. But if the upper plate be lifted, the capacity of the lower plate diminishes enormously, and the potential of its charge rises as shown by the divergence of the gold leaves.[1] To prove by the condensing electroscope that contact of dissimilar metals does produce electrification, a small compound bar made of two dissimilar metals—say zinc and

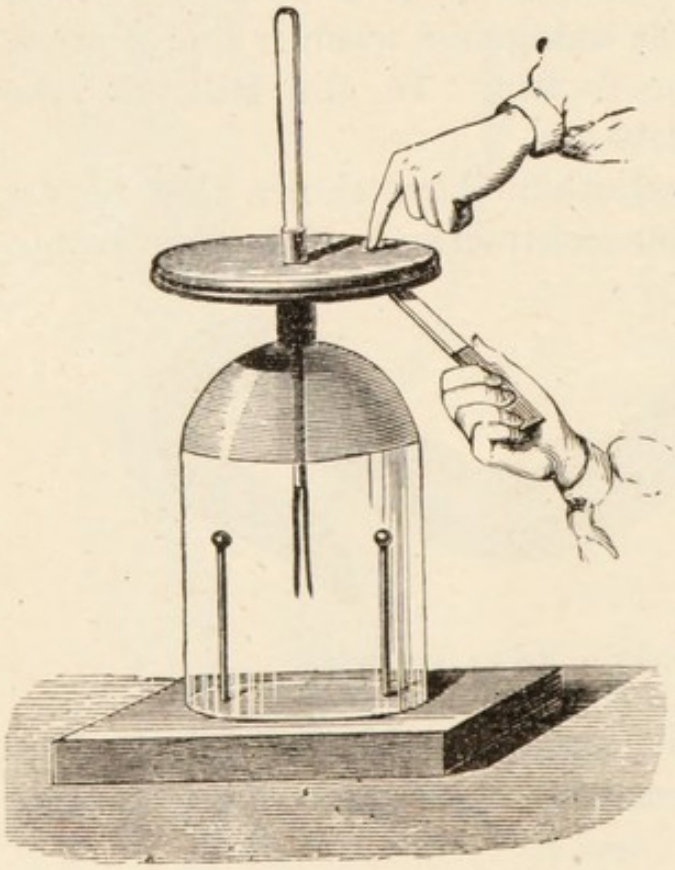


FIG. 51.—Experiment showing Electrification by Contact.

[1] Formerly, this action was accounted for by saying that the electricity which was "bound" when the plates of the condenser were close together, becomes "free" when the top plate is lifted up; the above is, however, a more scientific and more accurate way of saying the same thing. The student who is unable to reconcile these two ways of stating the matter should read again Articles 41 and 56, on pp. 46 and 67. A much more sensitive apparatus to show the effect is the quadrant electrometer (Art. 307).

copper—soldered together, is held in the moist hand, and one end of it is touched against the lower plate, the upper plate being placed in contact with the ground or touched with the finger. When the two opposing charges have thus collected in the condenser the upper plate is removed, and the diverging of the gold leaves shows the presence of a free charge, which can afterwards be examined to see whether it be + or − . Instead of employing the copper-zinc bar, a single voltaic cell may be connected by copper wires to the two plates. For a long time the existence of this electrification by contact was denied, or rather it was declared to be due (when occurring in voltaic combinations such as are described in Lesson XIII.) to chemical actions going on; whereas the real truth is that the electricity of contact and the chemical action are both due to transfers of electrons between the substances under the actions of forces about which very little is known with certainty. Later experiments, especially those made with the modern delicate electrometers of Lord Kelvin, put beyond doubt the reality of Volta's discovery. One simple experiment explains the method adopted. A thin strip or needle of metal is suspended so as to turn about a point *C*. It is electrified from a known source. Under it are placed (Fig. 52) two semicircular disks, or half-rings of dissimilar metals. Neither attracts or repels the electrified needle until the two are brought into contact, or connected by a third piece of metal, when the needle immediately turns, being attracted by the one that is oppositely electrified, and repelled by the one that is electrified similarly with itself.

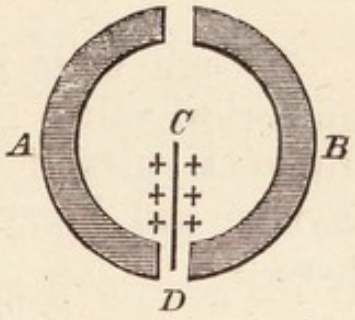


FIG. 52.—Kelvin's Proof of Contact Electricity.

81. Contact Series of Metals (in Air).—Volta found, moreover, that the differences of electric potential between the different pairs of metals were not all equal. Thus, while zinc and lead were respectively + and − to

a slight degree, he found zinc and silver to be respectively + and − to a much greater degree. He was able to arrange the metals in a series such that each one enumerated became positively electrified when placed in contact in air with one below it in the series. Those in italics are added from observations made since Volta's time—

Sodium	Iron
Magnesium	Copper
Zinc	Silver
Hydrogen	Gold
Lead	*Platinum*
Tin	*Graphite* (Carbon).

Though Volta gave rough approximations, the actual numerical values of the differences of potential in air for different pairs of metals were subsequently measured by Ayrton and Perry, a few of whose results are tabulated here—

	Difference of Potential (volts).
Zinc } Lead	0·210
Lead } Tin	0·069
Tin } Iron	0·313
Iron } Copper	0·146
Copper } Platinum	0·238
Platinum } Carbon	0·113

The difference of potential between zinc and carbon is the same as that obtained by adding the successive differences, or 1·09 volts.[1] Volta's observations may therefore be stated in the following generalized form, known as **Volta's Law.** *The difference of potential between any two metals is equal to the sum of the differences of potentials between the intervening metals in the contact-series.*

It is most important to notice that the order of the

[1] For the definition of the *volt*, or unit of difference of potential, see Art. 381, p. 362.

metals in the contact-series *in air* is almost identical with that of the metals arranged according to their electro-chemical power, as calculated from their chemical equivalents and their heat of combination with oxygen (see Table, Art. 568). From this it would appear that the difference of potentials between a metal and the air that surrounds it measures the tendency of that metal to become oxidized by the air. If this is so, and if (as is the case) the air is a bad conductor while the metals are good conductors, it ought to follow that when two different metals touch they equalize their own potentials by conduction but leave the films of air that surround them at different potentials. All the exact experiments yet made have measured the difference of potentials not between the metals themselves, but between the air near one metal and that near another metal. Mr. John Brown showed that while in air iron is positive to copper, but in an atmosphere of sulphuretted hydrogen, iron is negative to copper. He also demonstrated the existence on freshly cleaned metal surfaces of *films* of liquid or condensed gases; also that polished zinc and copper, when brought so near that their films touch, will act as a battery.

82. Contact Actions.—A difference of potential is also produced by the contact of *two dissimilar liquids* with one another.

A *liquid and a metal* in contact with one another also exhibit a difference of potential, and if the metal tends to dissolve into the liquid chemically there will be an electromotive force acting from the metal toward the liquid.

The thermo-electric difference of potential at a junction of two metals is a true contact difference. It is measured by the amount of heat produced (see *Peltier-effect*, Art. 472) by passing a current of electricity in the reverse direction through the junction.

A *hot* metal placed in contact with a *cold* piece of the same metal also produces a difference of potential,

electrical separation taking place across the surface of contact.

Lastly, it has been shown by Sir Joseph J. Thomson that the surface of contact between two non-conducting substances, such as sealing-wax and glass, is the seat of a permanent difference of potentials.

83. Magneto-electricity.—Electric currents flowing along in wires can be obtained mechanically by moving closed conducting circuits in the neighbourhood of magnets. This source is dealt with in Art. 240.

84. Summary.—We have seen in the preceding paragraphs how almost all conceivable agencies may produce electrification in bodies. The most important of these are friction, heat, chemical action, magnetism, and the contact of dissimilar substances. We noted that the production of electricity by friction depended largely upon the molecular condition of the surfaces. We may here add that the difference of potentials produced by contact of dissimilar substances also varies with the temperature and with the nature of the medium (air, vacuum, etc.) in which the experiments are made. Doubtless this source also depends upon the molecular conditions of dissimilar substances being different; the particles at the surfaces being of different sizes and shapes, and vibrating with different velocities. Moreover, they are associated with the electrons in ways that differ in different elements and compounds. There are (see Art. 11) good reasons for thinking that the electricity of friction is really due to electricity of contact, excited at successive portions of the surfaces as they are moved over one another. Péclet found rolling contact and sliding contact to produce equal effects. Apparently those substances stand higher in the list which most readily part with their electrons. See Art. 632, p. 672.

CHAPTER II

MAGNETISM

LESSON VIII.—*Magnetic Attraction and Repulsion*

85. Lodestones or Natural Magnets. — The name **Magnet** (*Magnes Lapis*) was given by the ancients to certain hard black stones found in various parts of the world, notably at *Magnesia* in Asia Minor, which possessed the property of attracting to them small pieces of iron. This magic property, as they deemed it, made the magnet-stone famous; but although the Chinese seem to have known the directive power of the magnet since A.D. 121, yet it was not until the tenth or eleventh century that it was known in Europe that this stone possessed the remarkable property of pointing north and south when floating on a wooden raft on water or hung up by a thread. This property was turned to advantage in navigation, and from that time the magnet received the name of **Lodestone**[1] (or "leading-stone"). The natural magnet or lodestone is an ore of iron, known to mineralogists as *magnetite* and having the chemical composition Fe_3O_4. This ore is found in quantities in Sweden, Spain, the Isle of Elba, Arkansas, and other parts of the world, though not always in the magnetic condition. It frequently occurs in crystals; the usual form being the regular octahedron.

[1] The common spelling *load*stone is due to misapprehension.

86. Artificial Magnets.—If a piece of hard iron be rubbed with a lodestone, it will be found to have also acquired the properties characteristic of the stone; it will attract light bits of iron, and if hung up by a thread it will point north and south. Figs. 53 and 54 represent a natural lodestone and an artificial magnet of steel, each of which has been dipped into iron-filings; the filings are attracted and adhere in tufts at the ends.



FIG. 53.—Piece of Lodestone.

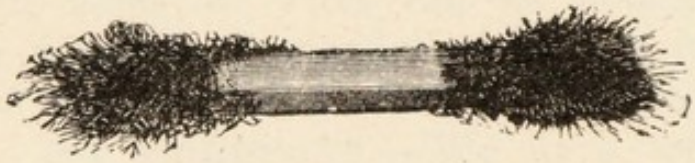


FIG. 54.—Steel Bar Magnet.

87. The earliest Book on the Magnet.—Beside a few stray references to the attractive power of lodestones, the classic authors had little to say of the magnet. Lucretius described how iron rings could hang as in a chain from a magnet; and Pliny, the historian, narrated a number of fabulous stories about the power of the magnet. The first real book on the subject was the *Epistle on the Magnet* of Peter Peregrinus, a Picard knight, written in 1269. He calls the active parts of the magnet its *poles*, and tells how to distinguish them by exploring the surface of the magnet with a needle of iron or steel. He called one the *north* pole (that which turns toward the north), and the other the *south* pole. He showed that while two north poles will repel one another, and two south poles will repel one another, there is attraction between a north pole and a south pole. He found that if a lodestone be cut or broken into two parts, each part will have a north and a south pole. He also described a primitive *mariners' compass*, having a lodestone supported to turn on pivots, and placed in a circular box, surrounded with a fixed circle divided into 360 degrees, and furnished with sights for taking observations at sea or on land.

About the beginning of the fourteenth century some unknown inventor, probably a navigator in Southern Italy, improved the compass by adding a movable "*card*" on which were painted the eight chief winds or "*points*" of the compass, the card being mounted upon a magnetized needle, and turning with it on a pivot.

88. Writings of Dr. Gilbert.—This was all, or nearly all, that was known of the magnet until 1600, when Dr. Gilbert published a large number of magnetic discoveries in his famous work *De Magnete*. Using small compass needles to explore the distribution of magnetism in a magnet, he found that the portion of the magnet which lies between its two poles seems less magnetic. It scarcely attracts iron filings; and all round the magnet, half-way between the poles, there is no attraction at all. This region Gilbert called the **equator** of the magnet, and the imaginary line joining the poles he termed the **axis**. Dr. Gilbert also discovered that the power of a lodestone was increased by arming its poles with caps or pole-pieces of soft iron.

89. Magnetic Needle. — To investigate magnetic forces a **magnetic needle** is employed. This consists (Fig. 55) of a light needle cut out of steel, and fitted with a little cap of brass, glass, or agate, which can be poised upon a sharp point, so as to turn with very little friction. It is rendered magnetic by being rubbed upon a magnet;

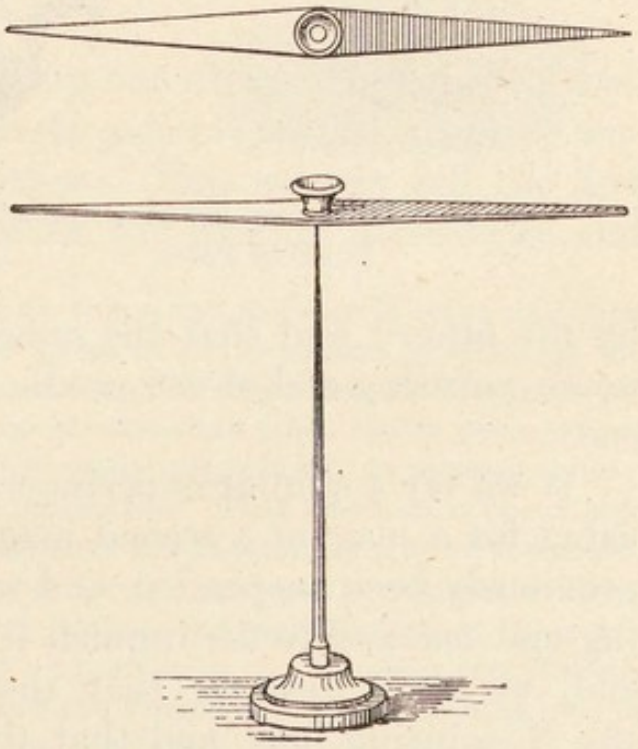


FIG. 55.—A Magnetic Needle.

and when thus magnetized it will turn into the north-and-south position, or, as we should say, will set itself in the "magnetic meridian" (Art. 157), p. 144. The *compass* sold by opticians for use on land consists of such a needle balanced above a fixed card marked with the "points of the compass"; in the *mariners' compass* the card goes round with the needle.

90. Magnetic Attractions and Repulsions.— If we take a magnet (either natural or artificial) in our hand and present the two "poles" of it successively to the north-pointing end of a magnetic needle, we shall observe that one pole of the magnet *attracts* it, while the other *repels* it (Fig. 56). Repeating the experiment on the south-pointing end of the magnetic needle, we find that it is *repelled* by one pole and *attracted* by the other; and that the same pole which attracts the north-pointing end of the needle repels the south-pointing end.

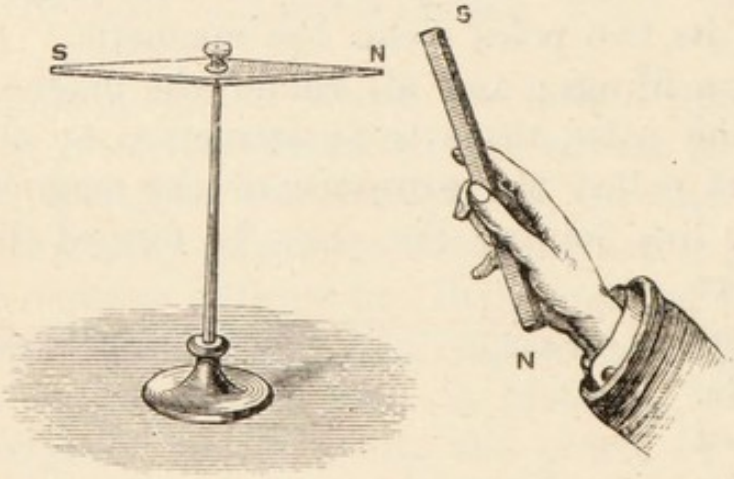


FIG. 56.—Attraction between opposite kinds of Poles.

If we try a similar experiment on the magnetic needle, using for a magnet a second magnetized needle which has previously been suspended, and which has its north-pointing end *marked* to distinguish it from the south-pointing end, we shall discover that the N-pointing pole repels the N-pointing pole, and that the S-pointing pole repels the S-pointing pole; but that a N-pointing pole attracts and is attracted by a S-pointing pole.

91. Two Kinds of Magnetic Poles. — There appear to be two opposite kinds of magnetism, or two

opposite kinds of magnetic poles, which attract or repel one another in very much the same fashion as the two opposite kinds of electrification do; and one of these kinds of magnetism appears to have a tendency to move toward the north and the other to move toward the south. It has been proposed to call these two kinds of magnetism "north-seeking magnetism" and "south-seeking magnetism," but for our present purpose it is sufficient to distinguish between the two kinds of poles. In common parlance the poles of a magnet are called the "North Pole" and "South Pole" respectively, and it is usual for the makers of magnets to mark the N-pointing pole with a letter N. It is therefore sometimes called the "marked" pole, to distinguish it from the S-pointing or "unmarked" pole. We shall, to avoid any doubt,[1] call that pole of a magnet which would, if the magnet were suspended, tend to turn to the north, the "North-seeking" pole, and the other the "South-seeking" pole.

We may therefore sum up our observations in the concise statement: *Like magnetic poles repel one another; unlike poles attract one another.* This we may call the first law of magnetism. As with the electric attractions and

[1] It is necessary to be precise on this point, as there is some confusion in the existing text-books. The cause of the confusion is this:—If the north-pointing pole of a needle is *attracted* by magnetism residing near the North Pole of the earth, the law of attraction (that *unlike poles attract*) shows us that these two poles are really magnetically of opposite kinds. Which are we then to call north magnetism? That which is at the N pole of the earth? If so, we must say that the N-pointing pole of the needle contains south magnetism. And if we call that north magnetism which points to the north, then we must suppose the magnetic pole at the north pole of the earth to have south magnetism in it. In either case there is then a difficulty. The Chinese and the French call the N-pointing pole of the needle a south pole, and the S-pointing pole a north pole. Lord Kelvin called the N-pointing pole a "True South" pole. But common practice goes the other way, and calls the N-pointing pole of a magnet its "North" pole. For experimental purposes it is usual to paint the two poles of a magnet of different colours, the N-seeking pole being coloured *red* and the S-seeking pole *blue*.

repulsions of rubbed bodies, so with these magnetic attractions and repulsions the effects are due, as we shall see, to stresses in the intervening medium.

92. The two Poles inseparable.—It is impossible to obtain a magnet with only one pole. If we magnetize a piece of steel wire, or watch spring, by rubbing it with one pole of a magnet, we shall find that still it has two poles—one N-seeking, the other S-seeking. And if we break it into two parts, each part will still have two poles of opposite kinds.

93. Breaking a Magnet.—If we take a thin strip of hard steel, magnetized so that one end is a N pole

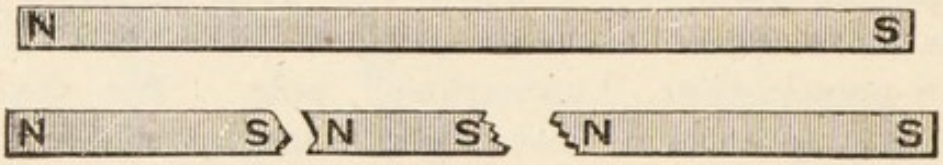


FIG. 57.—Experiment on breaking a Magnet.

and the other a S pole, and break it into two or more pieces, each piece will be found to have a pole at each end. Fig. 57 shows this. If the broken parts be closely joined these adjacent poles neutralize one another and disappear, leaving only the poles at the ends as before. If a magnet be ground to powder each fragment will still act as a little magnet and exhibit polarity. A magnet may therefore be regarded as composed of many little

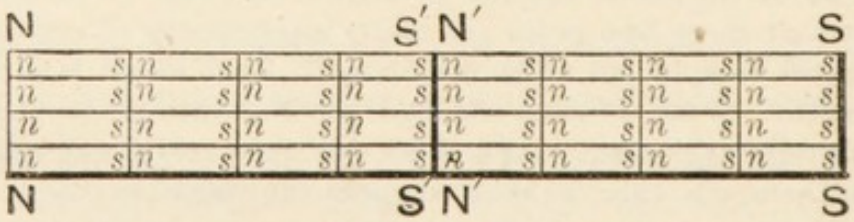


FIG. 58.—Bar Magnet built up of small Bars.

magnets put together, so that their like poles all face one way. Such an arrangement is indicated in Fig. 58, from which it will be seen that if the magnet be broken asunder across any part, one face of the fracture will

present only N poles, the other only S poles. This would be true no matter how small the individual particles.

94. The Earth a Magnet.—The greatest of Gilbert's discoveries was that of the inherent magnetism of the earth. *The earth is itself a great magnet*, whose "poles" coincide nearly, but not quite, with the geographical north and south poles, and therefore it causes a freely suspended magnet to turn into a north-and-south position. Gilbert had some lodestones cut to the shape of spheres to serve as models of the globe of the earth. Such a globular magnet he called a *terrella*. He found that small magnets turned toward the poles of the terrella, and dip, as compass needles do, toward the earth.

The subject of *Terrestrial Magnetism* is treated of in Lesson XII. It is evident from the first law of magnetism that the magnetic condition of the northern regions of the earth must be the opposite to that of the north-seeking pole of a magnetized needle. Hence arises the difficulty of language alluded to on page 91.

95. Magnetic Force.—The force with which a magnet attracts or repels another magnet, or any piece of iron or steel, we shall call *magnetic force*.[1] The force exerted by a magnet upon a bit of iron or on another magnet is not the same at all distances, the force being greater when the magnet is nearer, and less when the magnet is farther off. (See Art. 131, p. 117, on law of magnetic force.)

Whenever a force acts thus between two bodies, it acts on both of them, tending to move both. A magnet will attract a piece of iron, and a piece of iron will attract a magnet.

Fix a magnet upon a piece of cork and float it in a basin of water (Fig. 59); it will move across the basin when a piece of iron is held near. A compass needle

[1] See footnote on "Force," Art. 177, p. 163.

thus floated turns round and points north and south; but it does not rush towards the north as a whole, nor towards the south. The reason of this will be explained later, in Art. 131, p. 117.

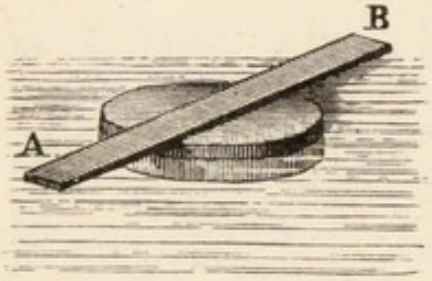


FIG. 59.—Floating Bar Magnet.

Gilbert suggested that the force of a magnet might be measured by making it attract a piece of iron hung to one arm of a balance, weights being placed in the scale-pan hanging to the other arm; and he found, by hanging the *magnet* to the balance and placing the *iron* beneath it, that the effect produced was the same. The action and reaction are then equal for magnetic forces.

96. Magnetic Substances.—A distinction was drawn by Gilbert between *magnets* and *magnetic substances*. A magnet attracts only at its poles, and they possess opposite properties. But any part of a lump of soft iron will attract either pole of the magnet. It has no distinguishable fixed "poles," and no magnetic "equator." A true magnet has poles, one of which is *repelled* by the similar pole of another magnet.

97. Other Magnetic Materials.—In addition to iron (and steel) the metals nickel and cobalt are recognized as magnetic as they are attracted by a magnet. It has also been supposed that chromium and manganese are slightly magnetic, but practically they are non-magnetizable (Art. 396, p. 382). Only nickel and cobalt are at all comparable with iron and steel in magnetic power, and even they are far inferior. Some of the alloy steels (see Art. 396) are magnetic, for example, nickel steel, chrome steel, and tungsten steel. Manganese steel is non-magnetic; yet the alloy of manganese with aluminium and copper, and the alloy of manganese with bismuth, are both highly magnetic. Other bodies, sundry salts of iron and other metals, paper, porcelain,

and oxygen gas are also very feebly attracted by a powerful magnet. Liquid oxygen is attracted to the poles of magnets.

98. Diamagnetism.—A number of bodies, notably bismuth, antimony, phosphorus, and copper, are apparently repelled from the poles of a magnet. Such bodies are called *diamagnetic bodies*; a fuller account of them will be found in Arts. 398 to 402, p. 384.

99. Induction of Magnetism.—Magnetism may be communicated to a piece of iron without actual contact with a magnet. If a short, thin unmagnetized bar of iron be placed near some iron filings, and a magnet be brought near to the bar, the presence of the magnet will *induce* magnetism in the iron bar, and it will now attract the iron filings (Fig. 60). This inductive action



FIG. 60.—Magnetization by influence of a Bar Magnet.

is very similar to that observed in Lesson III. to take place when a non-electrified body was brought under the influence of an electrified one. The analogy, indeed, goes further than this, for it is found that the iron bar thus magnetized by induction will have two poles; the pole nearest to the pole of the inducing magnet being of the opposite kind, while the pole at the farther end of the bar is of the same kind as the inducing pole. Those bodies in which a magnetizing force produces a high degree of magnetization are said to possess a high *permeability*. It will be shown presently that magnetic influence takes place along certain directions called *lines of magnetic force*, which may pass either through iron and other magnetic media, or through air, vacuum, glass, or other non-magnetic media: and, since induction goes on most freely in bodies of high magnetic permeability,

the magnetic lines are sometimes (though not too accurately) said to "pass by preference through magnetic matter," or, that "magnetic matter conducts the lines of force."

100. Attraction across Bodies.—If a sheet of glass, or wood, or paper, be interposed between a magnet and the piece of iron or steel it is attracting, it will still attract it as if nothing were interposed. A magnet sealed up in a glass tube still acts as a magnet. Lucretius found a magnet put into a brass vase attracted iron filings through the brass. Gilbert surrounded a magnet by a ring of flames, and found it still to be subject to magnetic

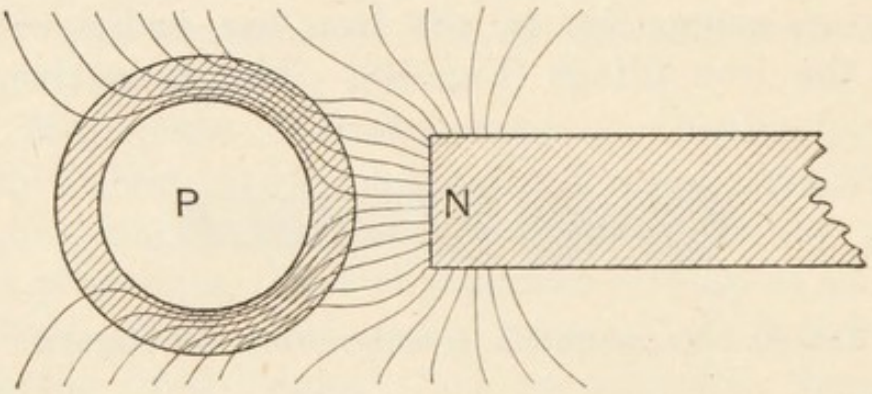


FIG. 61.—Magnetic Screening.

attraction from without. Across water, vacuum, and all known substances, the magnetic forces will act; with the single apparent exception, however, that magnetic force will not act across a *screen of iron* or other magnetic material, if sufficiently thick. If a small magnet is suspended inside a hollow ball made of iron, no outside magnet will affect it. The reason being that the magnetic lines of force are conducted off laterally through the iron instead of penetrating through it. A hollow shell of iron therefore acts as a **magnetic screen**, and shields the space inside it from magnetic influences.

Fig. 61 illustrates the way in which a cylinder of soft iron screens the space interior to it from the influence of an external magnet. A compass needle placed at P inside

the cylinder is not affected by the presence of the magnet outside, for its lines of magnetic force are drawn off laterally. Similarly a magnet inside is screened from affecting outside space.

Although magnetic induction takes place at a distance across an intervening layer of air, glass, or vacuum, there is no doubt that the intervening medium is directly concerned in the transmission of the magnetic force, though the true medium is probably the "ether" of space surrounding the molecules of matter, not the molecules themselves.

We now can see why a magnet should attract a not-previously-magnetized piece of iron; it first magnetizes it by induction and then attracts it: for the nearest end will have the opposite kind of magnetism induced in it, and will be attracted with a force exceeding that with which the more distant end is repelled. But *induction precedes attraction.*

101. Retention of Magnetization. — Not all magnetic substances can become magnets permanently. Lodestone, hard steel, and nickel retain permanently the greater part of the magnetism imparted to them. Pieces of really soft iron and of soft mild steel, though they can be temporarily highly magnetized, lose their magnetism directly the magnetizing force is removed. Cast-iron and many impure qualities of wrought iron also retain magnetism imperfectly. The softer and purer a specimen of iron is, the more lightly is its residual magnetism retained. The following experiment with a bar magnet illustrates the matter:—Let a few pieces of soft iron rod, or a few soft iron nails be taken. If one of these (see Fig. 62) be placed in contact with the pole of a permanent

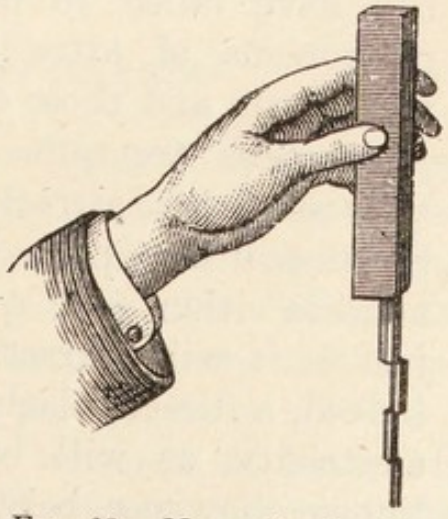


FIG. 62.—Magnetic Chain.

steel magnet, it is attracted to it, and becomes itself a temporary magnet. Another bit of iron may then be hung to it, and another, until a chain of four or five pieces is built up. But if the steel magnet be removed from the top of the chain, all the rest drop off, and are found to be no longer magnetic. A similar chain of steel needles may be formed, but they will retain permanently most of their magnetism.

It will be found, however, that a hard steel rod is more difficult to magnetize than an iron rod of the same dimensions. It is harder to get the magnetism *into* hard steel than into soft iron, and it is harder to get the magnetism *out* of steel than out of iron; for the hard steel retains the magnetism once put into it. This power of resisting magnetization, or demagnetization, is called **retentivity**, and it is measured by the *coercive force* (see Art. 394). The retentivity of hardened steel is great; that of soft steel or wrought iron is very small. The harder the steel, the greater its retentivity. Form affects retentivity. Elongated forms and those shaped as closed or nearly closed circuits retain their magnetism better than short rods, balls, or cubes.

102. Theories of Magnetism.—The student will not have failed to observe the analogies between the phenomena of attraction, repulsion, induction, etc., of magnetism and those of electricity. Yet the two sets of phenomena are quite distinct. A positively electrified body does not attract either the North-pointing or the South-pointing pole of the magnet as such; in fact, it attracts either pole quite irrespective of its magnetism, just as it will attract any other body. There does exist, indeed, a direct relation between magnets and *currents* of electricity, as will be later explained. There is none known, however, between magnets and stationary *charges* of electricity.

Formerly it was the fashion to speak of a **magnetic fluid** or fluids; it is, however, *absolutely certain that*

magnetism is not a fluid, whatever else it may be. The term is a relic of bygone times. A magnet when rubbed upon a piece of steel magnetizes it *without giving up or losing any of its own magnetism.* A fluid cannot possibly propagate itself indefinitely without loss. The arguments to be derived from the behaviour of a magnet on breaking, and from other experiments narrated in Lesson X., are even stronger. No theory of magnetism will be propounded until these facts have been placed before the student.

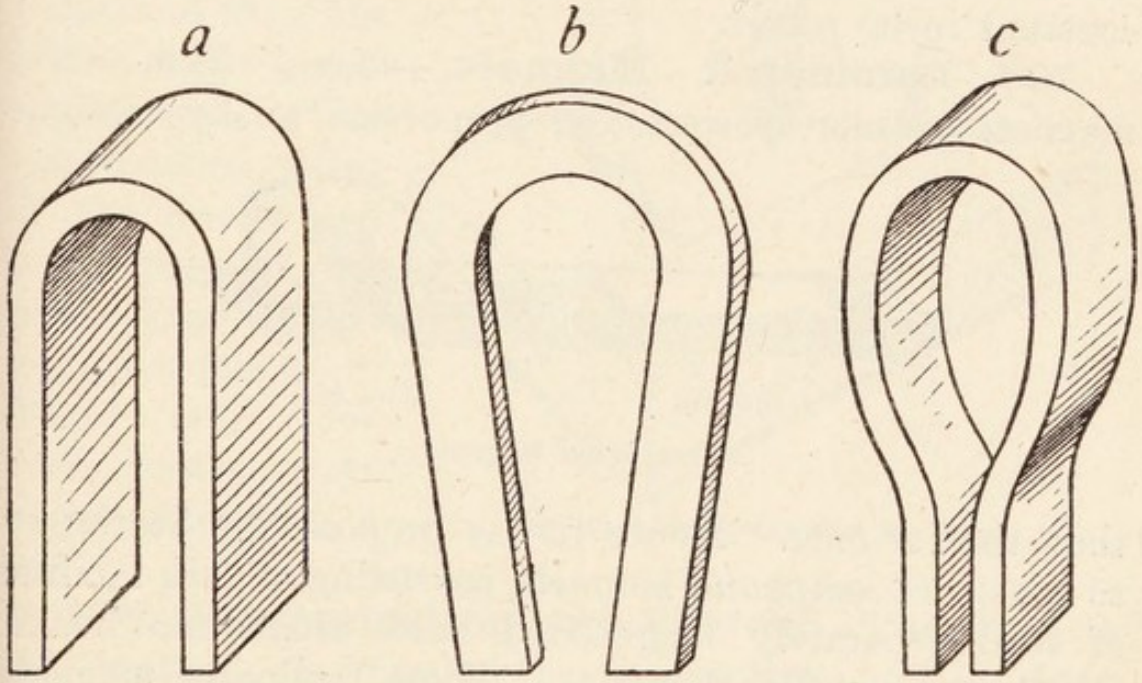


FIG. 63.—Horseshoe Magnets: three forms.

103. Forms of Magnets.—Natural magnets are usually of irregular form, though they are sometimes reduced to regular shapes, such as rods or spheres, by cutting or grinding. Formerly it was the fashion to mount rectangular blocks of lodestone with soft iron cheeks or "armatures" to serve as pole-pieces.

For scientific experiments *bar magnets* of hardened steel are commonly used; but for many purposes the *horseshoe* shape is preferred. In the horseshoe magnet the poles are bent round so as to approach one another, the advantage here being that so both poles can attract

one piece of iron. The "armature," or "keeper," as the piece of soft iron placed across the poles is named, is itself rendered a magnet by induction; hence, when *both* poles magnetize it, the force with which it is attracted to the magnet is the greater. A horseshoe magnet will lift three or four times as heavy a piece of iron as that which can be lifted by a bar magnet of equal weight. Fig. 63 shows three forms of horseshoe magnet. Fig. 63 *b* is the ordinary Sheffield pattern. Fig. 63 *c*, which is of a form more nearly constituting a closed circuit, is more constant in its power.

104. Laminated Magnets. — Long thin steel magnets are more powerful in proportion to their weight

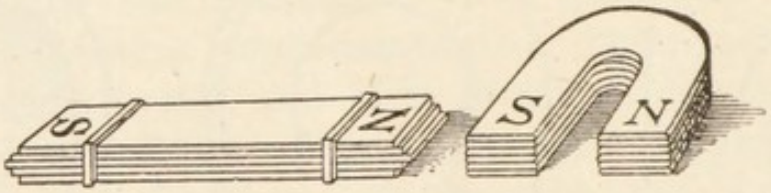


FIG. 64. FIG. 65.

Laminated Magnets.

than thicker ones. Hence it was proposed by Scoresby[1] to construct *compound magnets*, consisting of thin laminæ of steel separately magnetized, and afterwards bound together in bundles (Fig. 64). These laminated magnets have little advantage over simple bars of steel. Compound horseshoe magnets are sometimes used: the plates, separately magnetized, are assembled as in Fig. 65.

LESSON IX. *Methods of Making Magnets*

105. Magnetization by Touch.—It has been so far assumed that bars or needles of steel were to be magnetized by simply touching them, or stroking them from end to end with the pole of a permanent magnet of

[1] A similar suggestion was made by Geuns of Venlo in 1768, using horseshoe magnets. Similar magnets were constructed later by Jamin.

lodestone or steel. A more certain effect is produced if the needle or strip of steel is drawn from its middle to its end, as in Fig. 66, over the pole of a powerful magnet; one half of the needle being drawn across one of the poles, and then the other half across the other pole. The last-touched point of the needle will be a pole of opposite kind to that used to touch it. There are, however, better ways of magnetizing a bar.

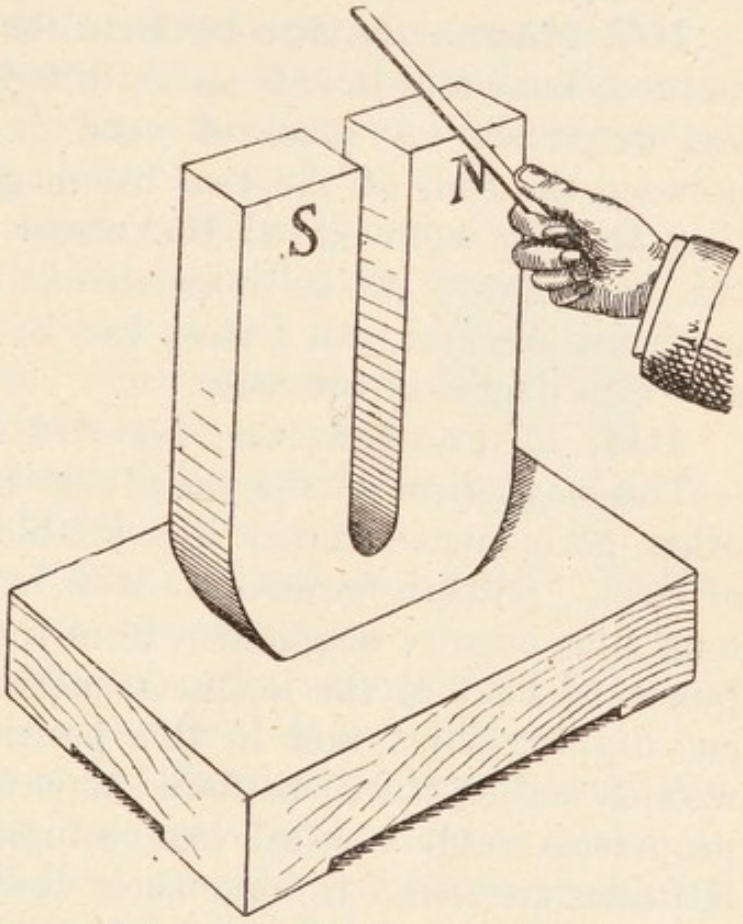


FIG. 66.—Magnetization by Touch.

106. Magnetization by Divided Touch.—In this method the bar to be magnetized is laid down horizontally; two bar magnets are then placed down upon it, their opposite poles being together. They are then drawn asunder from the middle of the bar towards its ends several times, stroking always towards the ends. The bar is then turned over, and the operation repeated, taking care to leave off at ends (see Fig. 67). The process is more effectual if the ends of the bar are meantime supported on the poles of other bar magnets, the poles

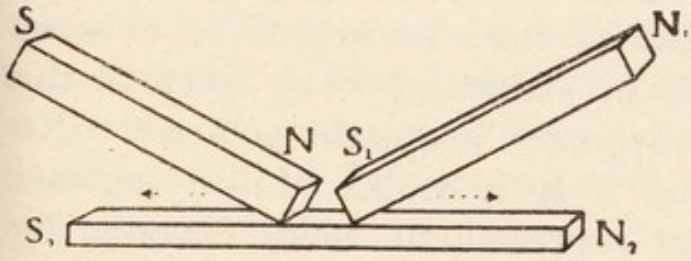


FIG. 67.—Method of Divided Touch.

being of the same names as those of the two magnets above them used for stroking the steel bar.

107. Magnetization by Double Touch.—Another method, known as *double touch*, differs slightly from that last described. A piece of wood or cork is interposed between the ends of the two bar magnets employed, and they are then both moved backwards and forwards along the bar that is to be magnetized. By none of these methods, however, can a steel bar be magnetized beyond a certain degree of intensity.

108. Magnetization derived from the Earth.—The magnetism of the earth may be utilized where no other permanent magnet is available to magnetize a bar of steel. Gilbert found that iron bars set upright for a long time acquire magnetism from the earth. If a steel poker be held in the magnetic meridian, with the north end dipping down, and in this position be struck with a wooden mallet, it will be found to have acquired magnetic properties. All vertical iron columns in our northern latitudes are found to have their lower ends N-poles and their upper ends S-poles. In Australia and the southern hemisphere the tops of iron columns are N-poles. Wires of steel subjected to torsion, while in the magnetic meridian, are also found to be thereby magnetized.

109. Magnetization after Heating.—Gilbert discovered also that if a bar of steel be heated to redness, and cooled, either slowly or suddenly, while lying in the magnetic meridian, it acquires magnetic polarity. No such property is acquired if it is cooled while lying east and west. It has been proposed to make magnets by placing hot bars of steel to cool between the poles of very powerful electromagnets; or to cast magnets of iron in moulds lying in an intense magnetic field. These plans are not recommended.

110. Magnetization by Currents of Electricity.—A current of electricity circulating in a spiral wire wound around a core of iron or steel magnetizes it

more powerfully than any of the preceding methods. In the case of a soft iron core, it is only a magnet while the current continues to flow. Such a combination is termed an **Electromagnet**; it is fully described in Lesson XXXI. Fig. 68 depicts a common form of electromagnet having two coils of insulated copper wire wound upon bobbins that are placed upon the limbs of a soft iron core. The armature is also of soft iron of sufficient thickness. Steel bars may be magnetized by drawing them over the poles of such an electromagnet while the latter is excited by the circulation of the electric current. Steel horseshoes are best magnetized by placing their poles in contact with the poles of a very powerful electromagnet, the current of which is then switched on.

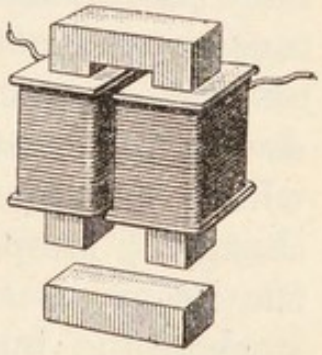


FIG. 68.—Electromagnet.

111. Hardening and Tempering of Steel for Magnets.—There are two ways of hardening steel: (1) by suddenly cooling it from a bright red temperature; (2) by compressing it under hydraulic pressure while it cools slowly. If rods of steel are heated brilliantly red, and then quenched in water, oil, or mercury, they become intensely brittle and *glass-hard*. To temper hard steel it is then gently reheated to near a very dull red heat, when in a few moments it softens slightly while acquiring a *straw tint*. If let down still further by continuing the reheating it becomes a *blue tint*, and is springy and flexible. Short bar magnets retain most magnetism if left glass-hard without tempering. But steel magnets whose length is more than twenty times their thickness retain their magnetism better if tempered down to a straw or even to a blue tint.

112. Destruction of Magnetism.—A steel magnet loses its magnetism partially or wholly if subjected to rough usage, or if purposely hit or knocked about. Newly magnetized magnets lose more strength by rough

treatment than those which have been long magnetized. A magnet loses its magnetism, as Gilbert showed, on being raised to a bright red heat. The slightest vibration will destroy any magnetism remaining in annealed soft iron.

113. Magnets of Unvarying Strength.—Ordinary steel magnets have by no means a permanent or constant magnetism. They soon lose a considerable percentage of their magnetism, and the decay continues slowly for months and years. Every shock or jolt to which they are subjected, every contact with iron, every change of temperature weakens them. Every time that the keeper is slammed on to a horseshoe magnet it is weakened; but sudden detachment of the keeper strengthens the magnet. For the purpose of making magnetic measurements, and for use as controlling magnets of galvanometers, magnets are, however, required that shall possess the utmost constancy in their strength. Magnets of unvarying strength may be made by attention to following points. Select a good tungsten steel or molybdenum steel. Choose a form either of a nearly closed circuit or of a very long rod. Let the steel be hardened as much as possible (see Art. 111 above), then boiled or placed in steam at 100° for twenty or thirty hours or more. Then magnetize as fully as possible, and then heat again for five hours in steam. Magnets of a shape constituting a nearly closed circuit are more constant than short straight magnets.

114. Effects of Heat on Magnetization.—If a permanent steel magnet be warmed by placing it in hot or boiling water, its strength will be thereby lessened, though it recovers partially on cooling. Chilling a magnet increases temporarily its strength. Iron and steel cease to be attracted by a magnet at a bright red heat. Pure iron is transformed at 760° C. to an almost non-magnetic state; the transformation point of nickel is 320° C., that of cobalt 1075° C. On cooling down to the transformation point the metal regains its magnetiz-

ability. It has been surmised that other metals would become magnetic if cooled to a low enough temperature. Dewar observed that the magnetic susceptibility of iron, when cooled to near − 180° C. in liquid oxygen, is nearly twice as high as at 0° C.

If steel at a bright red heat be cooled slowly, a point is reached at which there is a sudden molecular change accompanied by a rapid evolution of heat sufficient to arrest the darkening tint and causing the metal to glow red again. This phenomenon is called *recalescence*; it marks the transition to the magnetizable state. Steel quenched in cold water above the temperature of recalescence is very hard, and capable of great magnetic retentivity. The magnetic metals at high temperatures do not become diamagnetic, but are still feebly magnetic; their susceptibility at temperatures above the transformation point varying inversely as the absolute temperature.

115. Magnetic Saturation.—A magnet to which as powerful a degree of magnetization as it can attain to has been given is said to be relatively *saturated.* A recently magnetized magnet will occasionally appear to acquire a higher degree of magnetism than it is able to retain permanently. Thus a horseshoe-shaped steel magnet will support a greater weight immediately after being magnetized than it will do after its armature has been once removed from its poles. Even soft iron after being magnetized retains a small amount of magnetism when its *temporary magnetism* has disappeared. This small remaining magnetic charge is spoken of as *residual magnetism.*

116. Strength of a Magnet.—The "strength" of a magnet does not mean the same thing as its "lifting power." Its lifting power is a very uncertain quantity depending not only on the shape of its polar surfaces, but on the shape and quality of the mass of iron used as load. Consequently the "strength" of a magnet pole must be measured by the magnetic force which it exerts

at a distance on other magnets. Thus, suppose there are two magnets, A and B, whose strengths we compare by making them each act upon the N-pole of a third magnet C. If the N-pole of A repels C with twice as much force as that with which the N-pole of B placed at the same distance would repel C, then we should say that the "strength" of A was twice that of B. Another way of putting the matter is to say that the "strength" of a pole is the amount of free magnetism at that pole. By adopting the unit of strength of magnet poles as defined in Art. 142, we can express the strength of any pole in numbers as so many "units" of strength.

117. Lifting Power.—The lifting power of a magnet (also called its *portative force*) depends both upon the form of the magnet and on its magnetic strength. A horseshoe magnet will lift a load three or four times as great as a bar magnet of the same weight will lift. A long bar magnet will lift more than a short bar magnet of equal strength. A bar magnet with a rounded or chamfered end will lift more than a similar bar with a flat or expanded end, even though both are equally magnetized. Also the lifting power of a magnet grows in a very curious and unexplained way by gradually increasing the load on its armature day by day until it bears a load which at the outset it could not have done. Nevertheless, if the load is so increased that the armature is torn off, the power of the magnet falls at once to its original value. The attraction between a powerful electromagnet and its armature may amount to 230 lbs. per square inch, or 16,000 grammes per square centimetre of contact surface (see Art. 415); while that of a permanent steel magnet seldom reaches a quarter of that amount. Small magnets lift a greater load in proportion to their own weight than large ones,[1] because the lifting power is proportional to the polar surface, other things being

[1] James Hamilton, in 1729, discovered that the lifting power of a magnet is proportional to the square of the cube-root of its weight; and

equal. A good steel horseshoe magnet weighing itself 1 lb. ought to lift 25 lbs. weight. Sir Isaac Newton is *said* to have possessed a little lodestone mounted in a signet ring which would lift a piece of iron 200 times its own weight.

LESSON X.—*Distribution of Magnetism*

118. Magnetic Field.—*The space all round a magnet pervaded by the magnetic forces is termed the "field" of that magnet.* It is most intense near the poles of the magnet, and is weaker and weaker at greater distances away. At every point in a magnetic field the force has a particular strength, and acts in a particular direction. It is possible at any point in a magnetic field to draw a line in the direction of the *resultant magnetic force* acting at that point. The whole field may in this way be mapped out with magnetic lines (Art. 121). For a horseshoe magnet the field is most intense between the two poles, and the lines of magnetic force are curves which pass from one pole to the other across the field. A practical way of investigating the distribution of the magnetic lines in a field is given in Art. 121, under the title "Magnetic Figures." When the armature is placed upon the poles of a horseshoe magnet, the force of the magnet on all the external regions is weakened, for the induction now goes on through the iron of the keeper, not through the surrounding space. In fact a *closed system* of magnets —such as that made by placing four bar magnets along the sides of a square, the N-pole of one touching the

---

Bernoulli gave the following rule for finding the lifting power p of a magnet whose weight was w :—

$$p = a\sqrt[3]{w^2},$$

where a is a constant depending on the goodness of the steel and the method of magnetizing it. In the best steel horseshoe magnets made at Haarlem by Van Wetteren this coefficient was from 19·5 to 23, the weights being expressed in kilogrammes.

S-pole of the next—has no external field of force. A *ring* of steel may thus be magnetized so as to have neither external field nor poles; or rather any point in it may be regarded as a N-pole and a S-pole, so close together that they neutralize one another's forces.

119. Normal Distribution.—In an ordinary bar magnet the poles are not quite at the ends of the bar, but a little way from it; and it can be shown that this is a result of the way in which the surface magnetism is distributed in the bar. A very long, thin, uniformly magnetized bar has its poles at the ends; but in ordinary thick magnets the "pole" occupies a considerable region, the "free magnetism" falling off gradually from the ends of the bar. In each region, however, a point can be generally determined at which the resultant magnetic forces act, and which may for most purposes be considered as the "pole." In certain cases of irregular magnetization it is possible to have one or more poles between those at the ends. Such poles are called *consequent poles* (see Fig. 72). Sometimes the two poles of a magnet do not seem to be equally strong. This is due to irregularities in the shape of the magnet or to inequalities in the hardening or magnetizing of the steel. Actually the total quantity of magnetism in one half is always exactly equal to that in the other half.

120. Lamellar Distribution of Magnetism. Magnetic Shells.—Up to this point the ordinary distribution of magnetism along a bar has been the only distribution considered. It is theoretically possible to have magnetism distributed over a thin sheet so that the whole of one face of the sheet shall have one kind of magnetism, and the other face the other kind of magnetism; such distribution is, however, unstable. If an immense number of little magnets were placed together side by side, like the cells in a honeycomb, all with their N-seeking ends upwards, and S-seeking ends downwards, the whole of one face of the slab would be one large flat

N-seeking pole, and the other face S-seeking. Such a distribution as this over a surface or sheet is termed a **lamellar** distribution, to distinguish it from the ordinary distribution along a line or bar, which is termed, for distinction, the **solenoidal**, or **circuital**, distribution. A lamellarly magnetized magnet is sometimes spoken of as a **magnetic shell.**

121. Magnetic Figures.—Gilbert showed [1] that if a sheet of paper or card be placed over a magnet, and iron

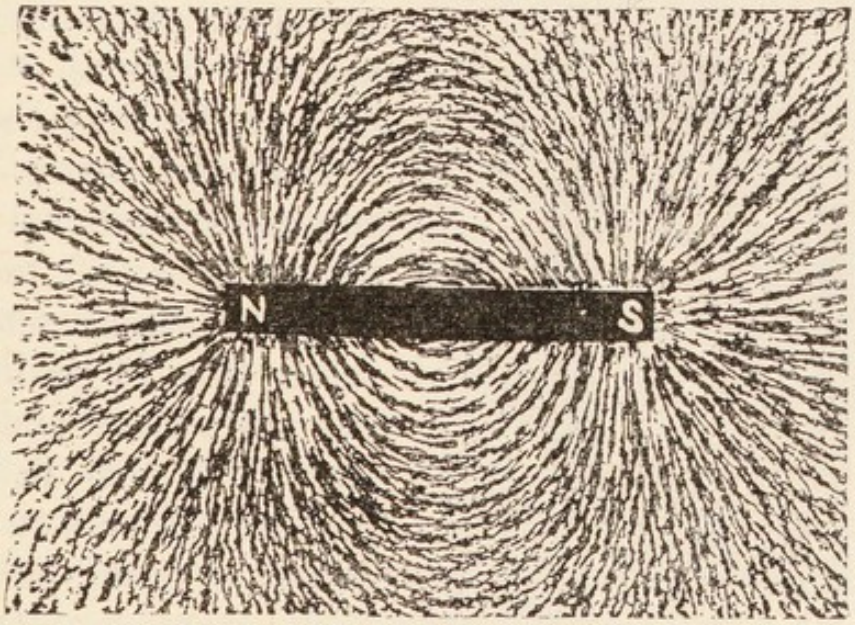


FIG. 69.—Lines of Force delineated by Iron Filings.

filings are dusted over the paper, they settle down in curving lines, forming a *magnetic figure*, the general form of which for a bar magnet is shown in Fig. 69. The filings should be fine, and sifted through a bit of muslin; to facilitate their settling in the lines, the sheet of paper should be lightly tapped. The figures thus obtained can be fixed permanently by several processes. The best of these consists in employing a sheet of glass which has been previously gummed and dried, instead of the sheet of paper; after this has been placed above the magnet the filings are sifted evenly over the surface, and then

[1] The magnetic figures were known to Lucretius.

the glass is tapped ; then a jet of steam is caused to play gently above the sheet, softening the surface of the gum, which, as it hardens, fixes the filings in their places. Inspection of the figure will show that the lines diverge nearly radially from each pole, and curve round to meet these from the opposite pole. Fig. 70, produced from a horseshoe magnet, shows how the magnetic field is most intense between the poles, but spreads beyond them in wide curves. Faraday, who made a great use of this method of investigating the distribution of magnetism in various "fields," gave to the lines the name of **lines of force**. They represent, as shown by the action on little magnetic particles which set themselves thus in obedience to the attractions and repulsions in the field, the resultant direction of the forces at every point ; for each particle tends to assume the direction of the force jointly due to the simultaneous action of both poles ; hence the curves of filings may be taken to represent visibly the invisible *lines of magnetic force*.[1] Faraday pointed out that these "lines of force" map out the magnetic field, showing by their position the direction of the magnetic force, and by their number its intensity. If a small N-seeking pole could be obtained alone, and put down on any one of these lines of force, it would tend

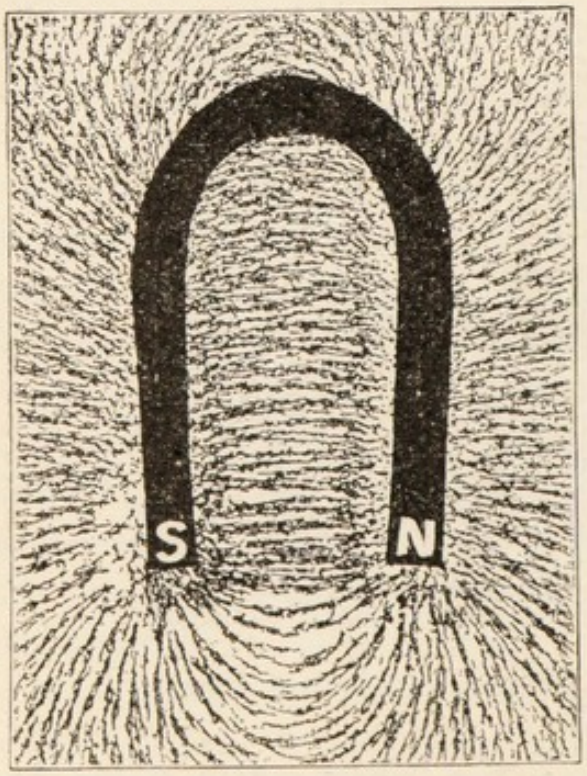


FIG. 70.—Field of Horseshoe Magnet.

[1] Or rather the component part of the magnetic force resolved into the plane of the figure ; which is not quite the same thing, for above the poles the filings stand up nearly vertically to this plane.

to move along that line from N to S; a single S-seeking pole would tend to move along the line in an opposite direction. In Fig. 71, which is the field about one end of a bar magnet, the magnetic lines are simply radial. Faraday also pointed out that the actions of attraction or repulsion in the field are always related to the directions in the field of the magnetic lines. He assigned to these lines of force certain physical properties (which are, however, only true of them in a secondary sense), viz. that they tend to shorten themselves from end to end, and that they repel one another as they lie side by side. The modern way of stating the matter is, that in every magnetic field there are certain stresses, consisting of a tension along the lines of force, and a pressure across them.

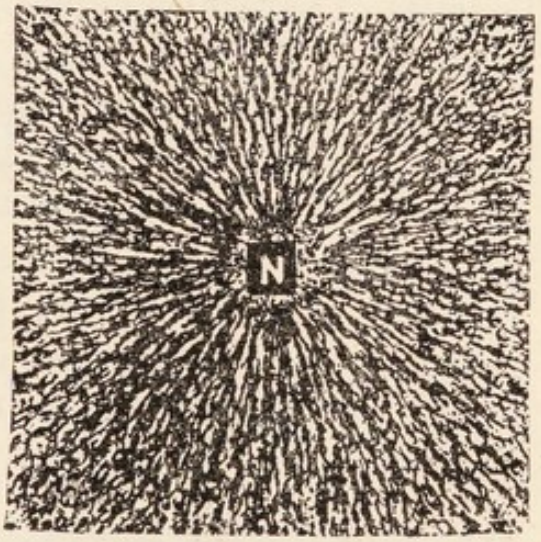


FIG. 71.—Field of a Single Pole.

122. Consequent Poles.—The method of sprinkling filings may be applied to ascertain the presence of

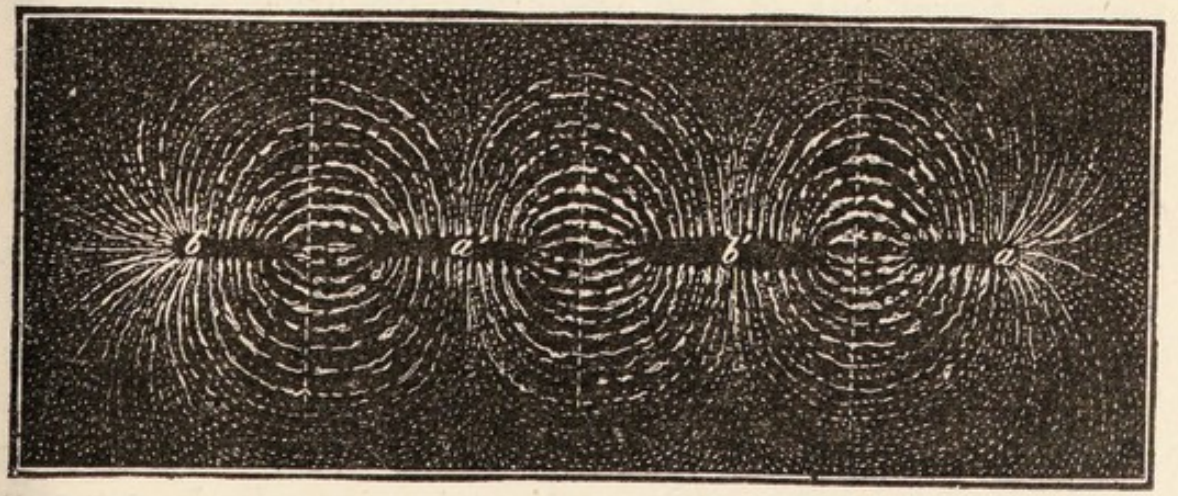


FIG. 72.—Consequent Poles.

consequent poles in a bar of steel, the figure obtained resembling that depicted in Fig. 72. Such a state of things

is produced when a strip of very hard steel is purposely irregularly magnetized by touching it with strong magnets at certain points. A strip thus magnetized virtually consists of several magnets put end to end, but in reverse directions, NS, SN, etc. Consequent poles can also be produced in an electromagnet by reversing the direction in which the wire is coiled around part of the core.

123. Fields mapped by Filings. — The forces producing attraction between unlike poles, and repulsion between like poles, are beautifully illustrated by the magnetic figures obtained in the fields between the poles in the two cases, as given in Figs. 73 and 74. In Fig. 73 the poles are of opposite kinds, and the lines of force

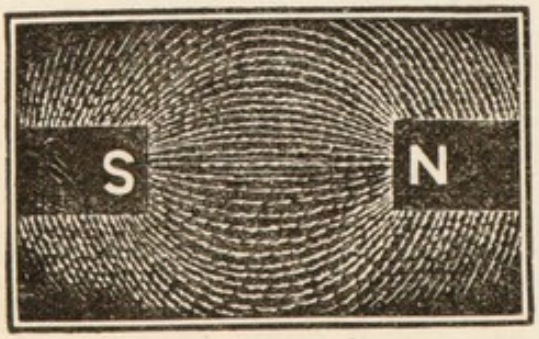


FIG. 73.—Field due to Opposite Poles.

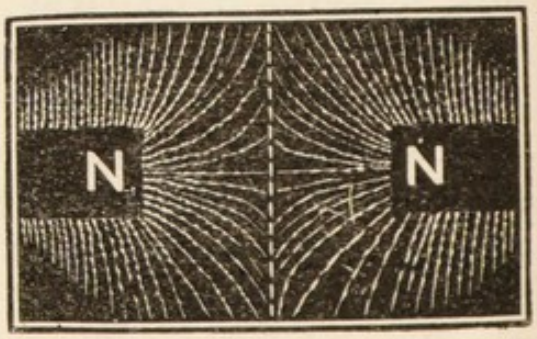


FIG. 74.—Field due to Similar Poles.

curve across out of one pole into the other; while in Fig. 74, which represents the action of two similar poles, the lines of force curve away as if repelling one another, and turn aside at right angles.

124. Magnetic Writing.—Another kind of magnetic figures was discovered by De Haldat, who wrote with the pole of a magnet upon a thin steel plate (such as a saw-blade), and then sprinkled filings over it. The writing, which is quite invisible in itself, comes out in the lines of filings that stick to the magnetized parts; this magic writing will continue in a steel plate many months. See also Art. 599 on the Telegraphone.

125. Mechanical Effects of Magnetization.—Joule found an iron bar to increase by $\frac{1}{720000}$ of its

length when strongly magnetized. Bidwell found that with still stronger magnetizing forces iron contracts again; and rods stretched by a weight contract more when magnetized than unstretched rods do. Barrett observed that nickel shows a slight contraction when magnetized. These are proofs that magnetization is an action affecting the arrangement of the molecules. This supposition is confirmed by the observation of Page, that at the moment when a bar is magnetized or demagnetized, a faint metallic clink is heard in the bar. Sir Wm. Grove showed that when a tube containing water rendered muddy by stirring up in it finely divided magnetic oxide of iron is magnetized, the liquid becomes clearer in the direction of magnetization, the particles apparently setting themselves end-on, and allowing more light to pass between them. A twisted iron wire tends to untwist itself when magnetized. A piece of iron, when powerfully magnetized and demagnetized in rapid succession, grows hot, as if magnetization were accompanied by internal friction (Art. 395).

126. Action of Magnetism on Light.—Faraday discovered that a ray of polarised light passing through certain substances in a powerful magnetic field has the direction of its vibrations changed. This phenomenon, which is sometimes called "The Magnetization of Light," is better described as "The Rotation of the Plane of Polarization of Light by Magnetism." The amount of rotation differs in different media, and varies with the magnetizing force. A ray of polarized light is also rotated by reflexion at the end or side of a powerful magnet. Further mention is made of these discoveries in the section on Electro-optics, Arts. 611 to 616, p. 651.

127. The Act of Magnetizing.—All these various phenomena point to a theory of magnetism very different from the old notion of fluids. It appears that every particle of a magnet is itself a magnet, and that the magnet only becomes a magnet as a whole by the particles being so turned as to point one way. The act of

magnetizing consists in turning the molecules more or less into one particular direction. If a glass tube full of iron filings is magnetized, the filings can be seen to set themselves endways, and that, when thus once set, they act as a magnet until shaken up. It appears to be harder to turn the individual molecules of solid steel than those of soft iron; but, when once so set, they remain end-on unless violently struck or heated. As Weber, who propounded this notion of molecular magnetism, pointed out, it follows from this theory that when all the particles are turned end-on the limits of possible magnetization would have been attained. Some careful experiments of Beetz on iron deposited by electrolysis entirely confirm this conclusion. Fig. 75 may be taken to represent a non-magnetized piece of iron or steel in which the arrangement of the particles is absolutely miscellaneous, in little groups: they do not point in any one direction more than another



FIG. 75.—Molecular State of Unmagnetized Bar.

When magnetized slightly, there will be a greater percentage pointing in the direction of the magnetizing force. When fully magnetized —if that were possible—they would all point in the same direction as in Fig. 76.

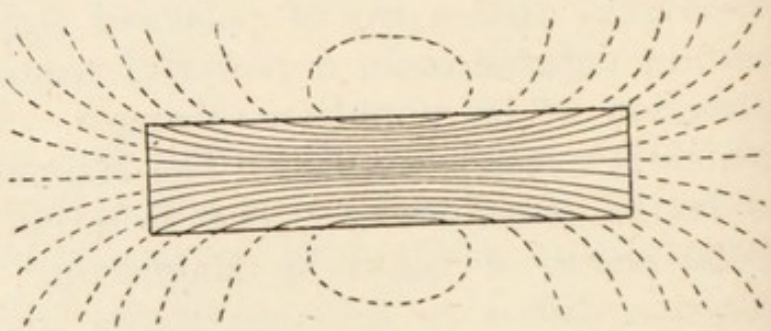


FIG. 76.—Molecular State of Magnetized Bar.

In very few cases, however, is the magnetization uniform throughout the whole length of a bar: the particles are more fully completely turned into line at the middle part of the bar than at the ends.

If the intrinsic magnetization of the steel at every part of a magnet were equal, the free poles would be

found only at the end surfaces; but the fact that the free magnetism is not at the ends merely, but diminishes from the ends towards the middle, shows that the intensity of the intrinsic magnetization must be less towards and at the ends than it is at the middle of the bar. In Fig. 76 an attempt is made to depict this. It will be noticed that the magnetic lines run through the steel and emerge into the air in curves. Some of the lines do not run all the length of the bar, but leak out at the sides. If the bar were uniformly magnetized the lines would emerge at the ends only. It is clear that the middle piece is more thoroughly magnetized than any other part. Magnetism in fact consists of a sort of grain or structure conferred upon the steel. Wherever this structure comes up at a surface, there the surface properties of magnetism are found. A pole is simply a region where the magnetic lines pass through the surface of the steel or iron.

The optical phenomena led Clerk Maxwell to the further conclusion that these longitudinally set molecules are rotating round their long axes, and that in the "ether" of space there is also a vortical motion along the magnetic lines; this motion, if occurring in a perfect medium (as the "ether" may be considered), producing tensions along the lines of the magnetic field, and pressures at right angles to them, would afford a satisfactory explanation of the magnetic attractions and repulsions which apparently act across empty space.

128. Magnetism a Form of Energy.—Though we speak freely of magnetic "force" and, later in the book, of magnetic "flux," it should be pointed out that the magnetic field represents a form of potential energy, and that in treating it as a flux or flow of intangible agent issuing from a N-seeking pole and returning into a S-seeking pole, we are following what is merely a convention instituted to facilitate calculations. If we pull a N-seeking pole to a short distance away from a S-seeking pole, so that there is a magnetic field between

them, we have to exert force, and therefore do some work in producing that field. This energy we have thus expended is stored up as potential energy in the field. When a piece of steel is magnetized by means of a magnet, the magnet is not thereby weakened; and the necessary energy is supplied by the mechanical effort of the person who applies the magnet.

129. Theory of Molecular Magnetism.—The magnetism of iron and steel is intimately connected with the molecular rigidity of the material. Apparently each molecule of a magnetic metal has an absolutely constant inherent magnetic polarity. When a piece of iron or steel is apparently neutral, its molecules are internally arranged

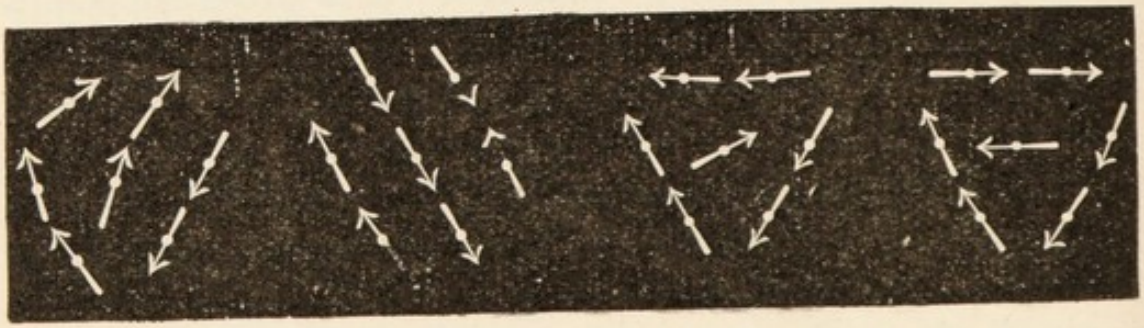


FIG. 77.—Molecular Groupings according to Ewing.

so as to satisfy each other's polarity, forming closed magnetic circuits amongst themselves.

Weber supposed that there was in hard steel some sort of friction which prevented the molecules when once magnetized from turning back into higgledy-piggledy positions. Ewing, however, showed that a complete explanation was afforded by supposing the particles to be subject to mutual forces. In any group not subjected to an external magnetizing force the particles will arrange themselves so as to satisfy one another's polarity. Of the possible groupings some are, however, unstable. Four possible stable groupings of six pivoted needles are shown in Fig. 77. Ewing constructed a model consisting of a large number of pivoted magnetic needles arranged in one layer. When these needles were simply agitated and

allowed to come to rest they settled down in miscellaneous groups; but when acted upon by a gradually increasing magnetic force they turned round, the operation showing three stages—(i.) with very small magnetizing force the needles merely turned through a small angle; (ii.) when a certain force was applied the groupings became unstable, some of the needles suddenly swinging round to a new position, with the result that the majority of the needles point nearly but not quite along the direction of the force; (iii.) a further increase of the magnetizing force cannot produce much more effect: it can only pull the needles a little more perfectly into line. All these things correspond to the three stages observed (see Art. 391) in the gradual magnetization of iron or steel.

LESSON XI.—*Laws of Magnetic Force*

130. Laws of Magnetic Force.

FIRST LAW.—*Like magnetic poles repel one another; unlike magnetic poles attract one another.*

SECOND LAW.—*The force exerted between two magnetic poles is proportional to the product of their strengths, and is inversely proportional to the square of the distance between them, provided that the distance is so great that the poles may be regarded as mere points.*

131. The Law of Inverse Squares.—The second of the above laws is commonly known as the law of *inverse squares*; it is essentially a law of point-action, and is not true for poles of elongated or extended surface. The similar law of electrical attraction has already been explained and illustrated (Art. 19). This law furnishes the explanation of a fact mentioned in an earlier lesson,

Art. 95, that small pieces of iron are drawn bodily up to a magnet pole. If a small piece of iron wire, a, b (Fig. 78), be suspended by a thread, and the N-pointing pole A of a magnet be brought near it, the iron is thereby inductively magnetized; it turns round and points towards the magnet pole, setting itself as nearly as possible along a line of force, its near end b becoming a S-seeking pole, and its farther end a becoming a N-seeking pole. Now the pole b will be attracted and the pole a will be repelled. But these two forces do not exactly equal one another, since the distances are unequal. The repulsion will (by the law of inverse squares) be proportional to $\frac{1}{(Aa)^2}$; and the attraction will be proportional to $\frac{1}{(Ab)^2}$. Hence the bit of iron a, b will experience a pair of forces, turning it into a certain direction, and also a total force drawing it bodily toward A. Only those bodies are attracted by magnets in which magnetism can thus be induced; and they are attracted only because of the magnetism induced in them.

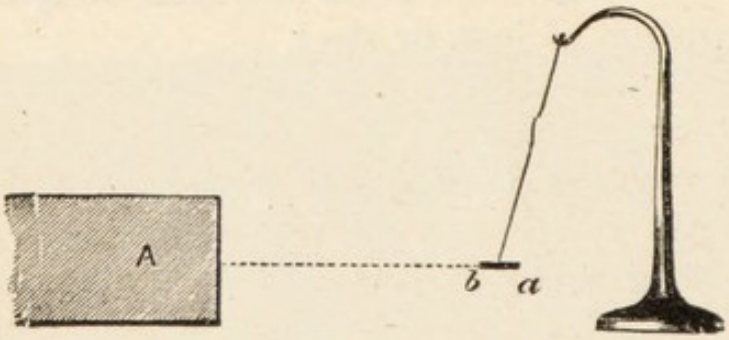


FIG. 78.—Magnetic Force on Short Needle.

We mentioned, Art. 95, that a magnet needle floating freely on a bit of cork on the surface of a liquid is acted upon by forces that give it a certain direction, but that, unlike the last case, it does not tend to rush as a whole either to the north or to the south. It experiences a rotation, because the attraction and repulsion of the magnetic poles of the earth act in a certain direction; but since the magnetic poles of the earth are at a distance enormously great as compared with the length from one pole of the floating magnet to the other, we may say that, for all practical purposes, the poles of the magnet are at

the same distance from the N-pole of the earth. The attracting force on the N-pointing pole of the needle is therefore practically no greater than the repelling force acting on the S-pointing pole, hence there is no motion of translation given to the floating needle as a whole; it is *directed*, not *attracted*.

132. Measurement of Magnetic Forces.—The law of inverse squares can be demonstrated by experiment. But this implies that we have some means of measuring accurately the amount of the magnetic forces of attraction or repulsion. Magnetic force may be measured in any one of the four following ways: (1) by observing the time of swing of a magnetic needle oscillating under the influence of the force (Art. 135); (2) by observing the deflexion it produces upon a magnetic needle which is already attracted into a different direction by a force of known intensity (Art. 133); (3) by balancing it against the torsion of an elastic thread (Art. 134); (4) by balancing it against the force of gravity as brought into play in attempting to deflect a magnet hung by two parallel strings (called the *bifilar* suspension), for these strings cannot be twisted out of their parallel position without raising the centre of gravity of the magnet.

133. Deflexion Experiment.—Fig. 79 shows an apparatus in which a compass needle can be deflected by one pole of a magnet made of a long thin bar of steel, so mounted that its upper pole is always over the centre of the needle, and therefore has no tendency to turn it. So set, it acts as a one-pole magnet, the acting pole of which can be placed at different distances from the compass needle. It is found, using a proper tangent-scale (see Art. 225) for the compass needle, that when the distance is doubled the

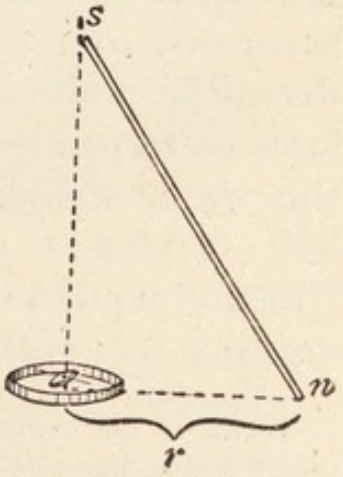


FIG. 79.—Deflexion by one Pole.

deflecting force is reduced to one quarter, and so forth. See Art. 130.

134. The Torsion Balance.—Coulomb applied the Torsion Balance to the measurement of magnetic forces. The main principles of this instrument (as used to measure forces of electrostatic repulsion) were described on p. 13. Fig. 80 shows how it is arranged for measuring magnetic repulsions.

To prove[1] the law of inverse squares, Coulomb made the following experiment :—The instrument was first adjusted so that a magnetic needle, hung in a copper stirrup to the fine silver thread, lay in the magnetic meridian without the wire being twisted. This was done by first putting in the magnet and adjusting roughly, then replacing it by a copper bar of equal weight, and once more adjusting, thus diminishing the error by repeated trials. The next step was to ascertain through what number of degrees the torsion-head at the top of the thread must be twisted in order to drag the needle 1° out of the magnetic meridian. In the particular experiment cited it was found that 35° of torsion corresponded to the 1° of deviation of the magnet; then a magnet was introduced through the lid, that pole being downwards which repelled the pole of the suspended needle. It was found (in this particular experiment) to repel the pole of the needle through 24°. From the preliminary trial we know that this directive force corresponds to 24° × 35° of the torsion-head, and to this we must add the actual torsion on the wire, viz. the 24°, making a total of 864°, which we will call the "torsion equivalent" of the repelling force when the poles are thus 24° apart. Finally, the torsion-head was turned

[1] This is the common way of stating the matter; but what Coulomb really tested was *whether his magnet poles acted as points.* Had they acted exactly as if the magnetism was concentrated at points, the geometric condition of the law of inverse squares could not but have been fulfilled. Robison showed that if a steel needle is provided with two little soft iron spheres on its ends, the effective poles are exactly at the centres of the spheres.

round so as to twist the suspended magnet round, and force it nearer to the fixed pole, until the distance between the repelling poles was reduced to half what it was at first. It was found that the torsion-head had to be turned round 8 complete rotations to bring the poles to 12° apart. These 8 rotations were an actual twist of $8° \times 360°$, or

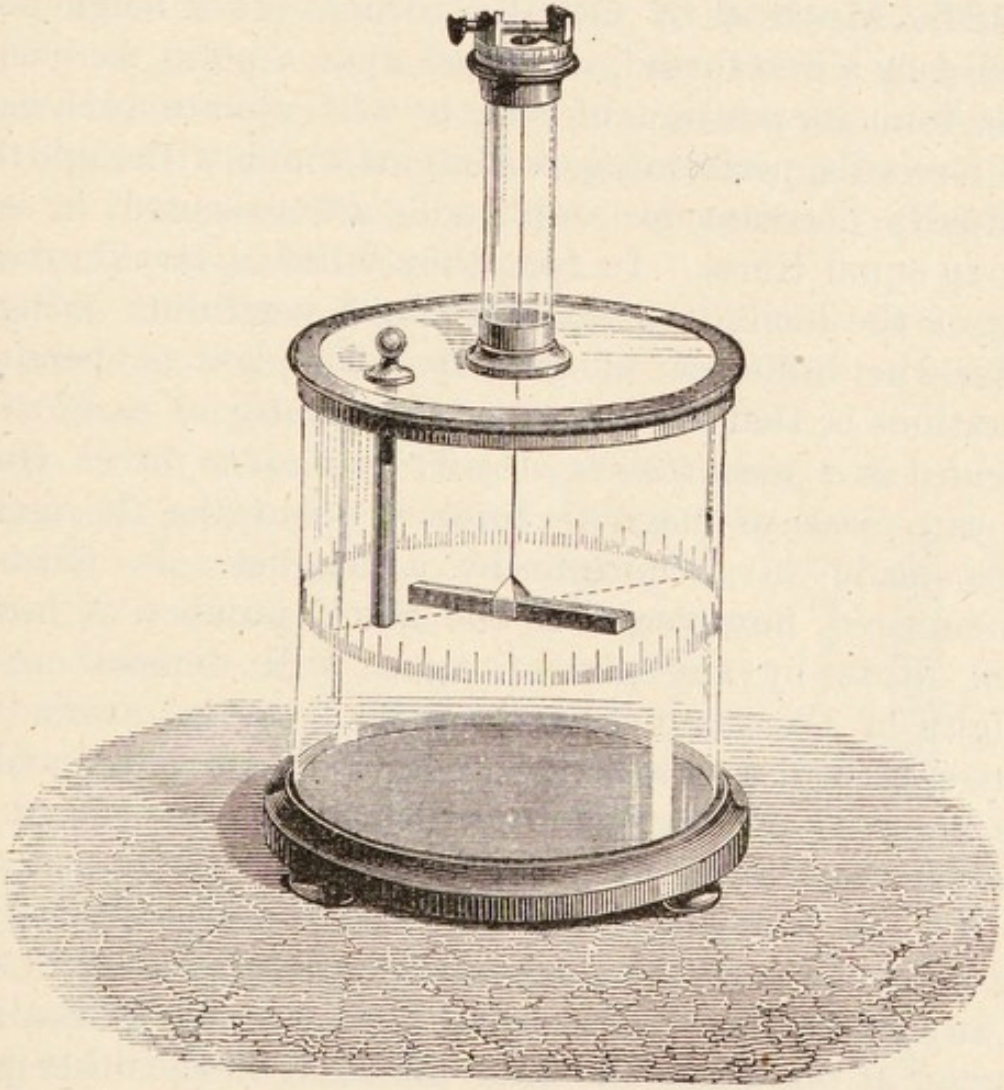


FIG. 80.—Magnetic Torsion Balance.

2880°. But the bottom of the torsion thread was still twisted 12° as compared with the top, the force producing this twist corresponding to 12×35 (or 420°) of torsion; and to these the actual torsion of 12° must be added, making a total of $2880° + 420° + 12° = 3312$. The result then of halving the distance between the magnet poles was to increase the force *fourfold*, for 3312 is very

nearly four times 864. Had the distance between the poles been reduced to one-third the force would have been nine times as great.

We may also, assuming this law proved, employ the balance to measure the strengths of magnet poles by measuring the forces they exert at known distances.

135. Method of Oscillations.[1]—If a magnet suspended by a fine thread, or poised upon a point, be pushed aside from its position of rest, it will vibrate backwards and forwards, performing oscillations which, although they gradually decrease in amplitude, are executed in *very nearly* equal times. In fact, they follow a law similar to that of the oscillations executed by a pendulum swinging under the influence of gravity. The law of pendular vibrations is, that *the square of the number of oscillations executed in a given time is proportional to the force.* Hence we can measure magnetic forces by counting the oscillations made in a minute by a magnet. It must be remembered, however, that the actual number of oscillations made by any given magnet will depend on the weight of the magnet and on its leverage around its centre, as well as upon the strength of its poles, and on the intensity of the field in which it may be placed (see calculations, Art. 388).

We can use this method to compare the intensity of the force of the earth's magnetism[2] at any place with that at any other place on the earth's surface, by oscillating a magnet at one place and then taking it to the other place and oscillating it there. If, at the first, it makes a oscillations in one minute, and at the second b oscillations a minute, then the magnetic forces at the two places will be to one another in the ratio of a^2 to b^2.

1 It is possible, also, to measure *electrical* forces by a "method of oscillations"; a small charged ball at the end of a horizontally suspended arm being caused to oscillate under the attracting force of a charged conductor near it, whose "force" at that distance is proportional to the square of the number of oscillations in a given time.

2 Or, more strictly, of its *horizontal component.*

Again, we may use the method to compare the force exerted at any point by a magnet near it with the force of the earth's magnetism at that point. For, if we swing a small magnetic needle there, and find that it makes m oscillations a minute under the joint action [1] of the earth's magnetism, and that of the neighbouring magnet, and that, when the magnet is removed, it makes n oscillations a minute under the influence of the earth's magnetism alone, then m^2 will be proportional to the joint forces, n^2 to the force due to the earth's magnetism, and the difference of these, or $m^2 - n^2$ will be proportional to the force due to the neighbouring magnet.

136. Surface Distribution.—We will now apply the method of oscillations to measure the relative quantities of surface magnetism at different points along a bar magnet. The magnet to be examined is set up vertically (Fig. 81). A small magnet, capable of swinging horizontally, is brought near it and set at a short distance away from its extremity, and then oscillated, while the rate of its oscillations is counted. Suppose the needle were such that, when exposed to the earth's magnetism alone, it would perform 3 complete oscillations a minute, and that, when vibrating at its place near the end of the vertical magnet it oscillated 14 times a minute, then the force due to the magnet will be proportional to $14^2 - 3^2 = 196 - 9 = 187$. Next, let the oscillating magnet be brought to an equal distance opposite a point a little away from the end of the vertical magnet. If, here, it oscillated 12 times a minute, we know that the force will be pro-

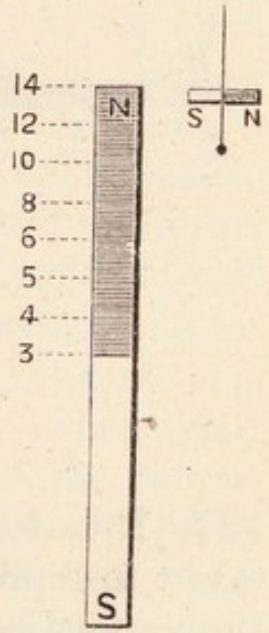


FIG. 81.—Surface Distribution of Magnetism.

[1] We are here assuming that the magnet is so placed that its force is in a line with that of the earth's magnetism at the point, and that the other pole of the magnet is so far away as not to affect the oscillating needle.

portional to $12^2 - 3^2 = 144 - 9 = 135$. So we shall find that as the force falls off the oscillations will be fewer, until, when we put the oscillating magnet opposite the middle of the vertical magnet, we shall find that the number of oscillations is 3 per minute, or that the earth's force is the only force affecting the oscillations. In Fig. 81 we have indicated the number of oscillations at successive points, as 14, 12, 10, 8, 6, 5, 4, and 3. If we square these numbers and subtract 9 from each, we shall get for the forces at the various points the following :—

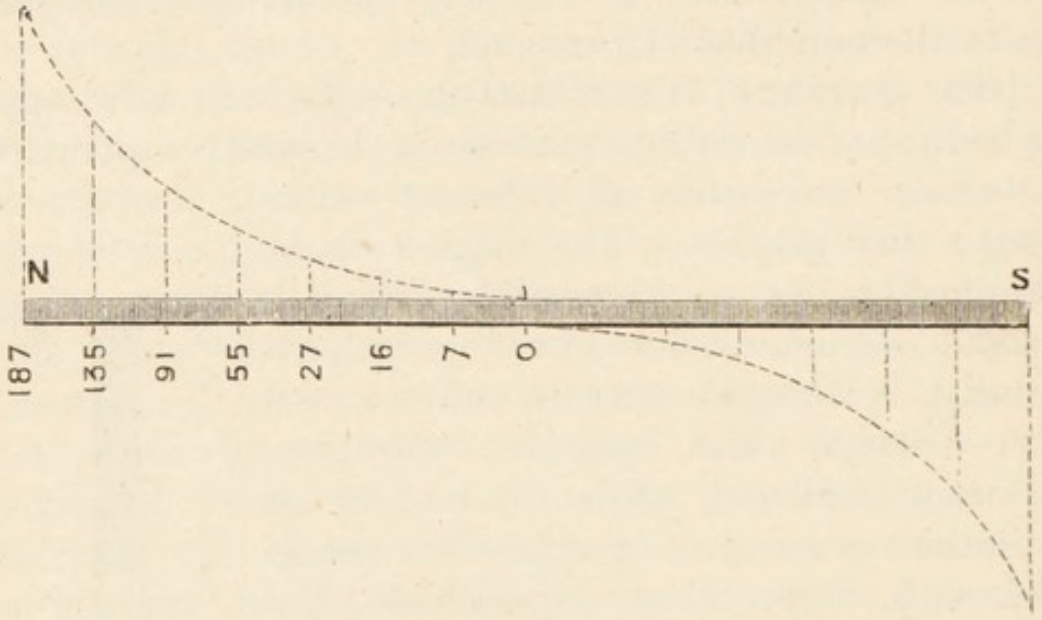


FIG. 82.—Exploration by Oscillations.

187, 135, 91, 55, 27, 16, 7, 0. These forces may be taken to represent the strength of the free magnetism at the various points, and it is convenient to plot them out graphically in the manner shown in Fig. 82, where the heights of the dotted lines are chosen to a scale to represent proportionally the forces. The curve which joins the tops of these ordinates shows graphically how the force, which is greatest at the end, falls off toward the middle. On a distant magnet pole these forces, thus represented by this curvilinear triangle, would act as if concentrated at a point in the magnet opposite the "centre of gravity" of this triangle ; or, in other words, the "pole,"

which is the centre of the resultant forces, is not at the end of the magnet. In thin bars of magnetized steel it is at about $\frac{1}{10}$ of the magnet's length from the end.

Another way to explore the surface distribution is to take a small spherical or ellipsoidal bullet of iron, and to hang it by a wire to a spring balance. The force required to detach such a bit of iron from various parts of the surface of a magnet may be taken as a measure of the distribution, the forces being approximately proportional to the square of the surface density.

137. Magnetic Moment.—It is found that the tendency of a magnet to turn or to be turned by another magnet depends not only on the *strength* m of its poles, but the *length* l between them. The product of these two quantities $m \times l$ is called the **magnetic moment** of the magnet, and is sometimes denoted by the symbol M. As the exact position of a magnet's poles is often unknown, it is easier to determine M than to measure either m or l separately.

138. Method of Deflexions.—There are a number of ways in which the deflexion of a magnet by another magnet may be made use of to measure magnetic forces.[1] We cannot here give more than a glance at first principles. When two equal and opposite forces act on the ends of a rigid bar they simply tend to turn it round. Such a pair of forces form what is called a "couple," and the *torque*, or tendency to turn (formerly called the "moment" of the couple), is obtained by multiplying one of the two forces by the perpendicular distance between the directions of the forces. Such a couple tends to produce a motion of rotation, but not a motion of translation. Now a magnetic needle placed in a magnetic field across the lines of force experiences a torque, tending to rotate it round into the magnetic meridian, for the N-seeking pole is urged northwards, and the S-seeking pole is urged southwards,

[1] The student desirous of mastering these methods of measuring magnetic forces should consult Professor Andrew Gray's *Absolute Measurements in Electricity and Magnetism*.

with an equal and opposite force. The force acting on each pole is the product of the strength of the pole and the intensity of the "field," that is to say, of the horizontal component of the force of the earth's magnetism at the place. We will call the strength of the N-seeking pole m; and we will use the symbol H to represent the force which the earth's magnetism would exert in a horizontal direction on a unit of magnetism. (The value of H is different at different regions of the globe.) The force on the pole A (see Fig. 83) will be then $m \times H$, and that on pole B will be equal and opposite. We take NS as the direction of the magnetic meridian: the forces will be parallel to this direction. Now, the needle AB lies obliquely in the field, while the magnetic force acting on A is in the direction of the line PA, and that on B in the direction QB, as shown by the arrows. PQ is the perpendicular distance between these forces; hence the "moment" of the couple, or torque, will be got by multiplying the length PQ by the force exerted on one of the poles. Using the symbol Y for the torque, we may write

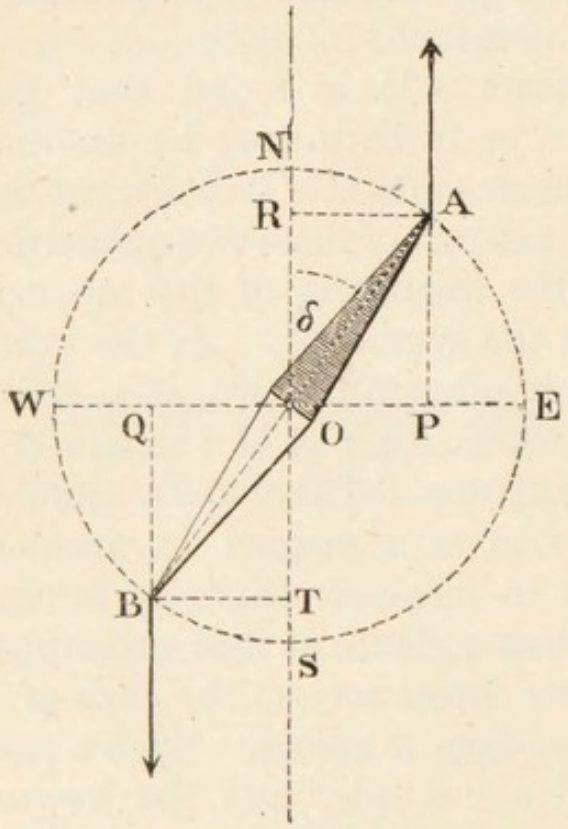


FIG. 83.—Force-couple.

$$Y = PQ \times m \cdot H.$$

But PQ is equal to the length of the magnet multiplied by the sine[1] of the angle AOR, which is the angle of

[1] If any reader is unacquainted with trigonometrical terms he should consult the note at the end of this lesson, on "Ways of Reckoning Angles," p. 137.

deflexion, and which we will call δ. Hence, using l for the length between the poles of the magnet, we may write the expression for the moment of the couple:

$$Y = mlH \cdot \sin \delta.$$

In words this is: the torque acting on the needle is proportional to its "magnetic moment" $(m \times l)$, to the horizontal force of the earth's magnetism, and to the sine of the angle of deflexion.

The reader will not have failed to notice that if the needle were turned more obliquely, the distance PQ would be longer, and would be greatest if the needle were turned round east-and-west, or in the direction EW. Also the torque tending to rotate the magnet will be less and less as the needle is turned more nearly into the direction NS.

139. Law of Tangents.—Now, let us suppose that the deflexion δ were produced by a magnetic force applied at right angles to the magnetic meridian, and tending to draw the pole A in the direction RA. The length of the line RT multiplied by the new force will be the leverage of the new couple tending to twist the magnet into the direction EW. Now, if the needle has come to rest in equilibrium between these two forces, it is clear that the two opposing twists are just equal and opposite in power, or that the torque due to one couple is equal to that of the other couple. Hence the force in the direction WE will be to the force in the direction SN in the same ratio as PQ is to RT, or as PO is to RO.

Or, calling this force f,

$$f : H = PO : RO.$$

Or

$$f = H\frac{PO}{RO}.$$

But $PO = AR$, and $\frac{AR}{RO} = \tan \delta$, hence

$$f = H \tan \delta;$$

or, in other words, *the magnetic force which, acting at right angles to the meridian, produces on a magnetic needle the deflexion* δ, *is equal to the horizontal force of the earth's magnetism at that point, multiplied by the tangent of the angle of deflexion.* Hence, also, two different magnetic forces acting at right angles to the meridian would severally deflect the needle through *angles whose tangents are proportional to the forces.* [See the Table of *Tangents of Angles* on page 682.]

This very important theorem is applied in the construction of certain galvanometers (see Art. 225, p. 206).

140. Magnetometers. — The name **Magnetometer** is given to any magnet specially arranged as an instrument for the purpose of measuring magnetic forces. The methods of observing the *absolute* values of magnetic forces in *dyne-units* (units in the "C.G.S." system) will be explained in Art. 388 at the end of Lesson XXVII. Very simple magnetometers, consisting of small needles pivoted, or suspended by a fibre, are commonly used for measuring the *relative* values of magnetic forces. One very sensitive form (Fig. 84), to be used, like the reflecting galvanometer (Art. 228), with a beam of light as a pointer, consists of a small thin silvered glass mirror, a half-inch or less in diameter, having two or three very light magnets cemented at its back, suspended by a single thread of cocoon silk, and enclosed in a suitable case. Another useful form (Fig. 85) consists of a short compass needle poised on a pivot having a light index of aluminium long enough to move over a scale divided into tangent values (see Art. 225).

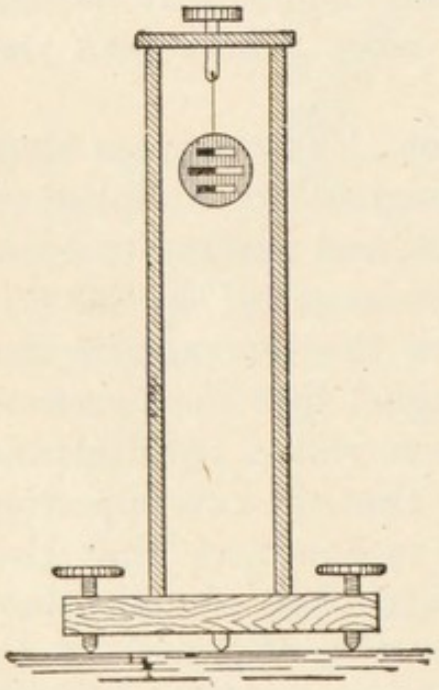


FIG. 84.—Magnetometer.

A convenient deflexion magnetometer for comparing the magnetic moments (Art. 137) of two magnets is afforded by such a tangent compass placed in the middle of a graduated platform (Fig. 86). There are two methods of using this apparatus.

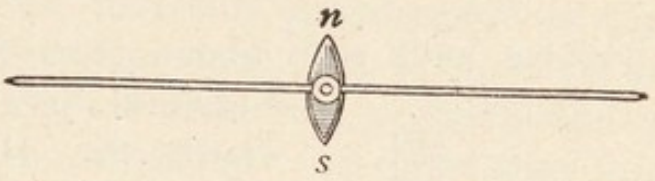


FIG. 85.—Magnetometer Needle.

First Position: End-on Method.—The platform being set to lie magnetically east and west, the deflecting magnet is set *end-on*. In these circumstances the force is found to vary directly as the magnetic moment (Art. 137), and approximately *inversely as the cube* of the distance between the centres of the magnets, or in symbols:—

$$f = 2M/r^3.$$

This formula is deduced as follows. Let the half-length of the deflecting magnet be called $\frac{1}{2}l$, and let the

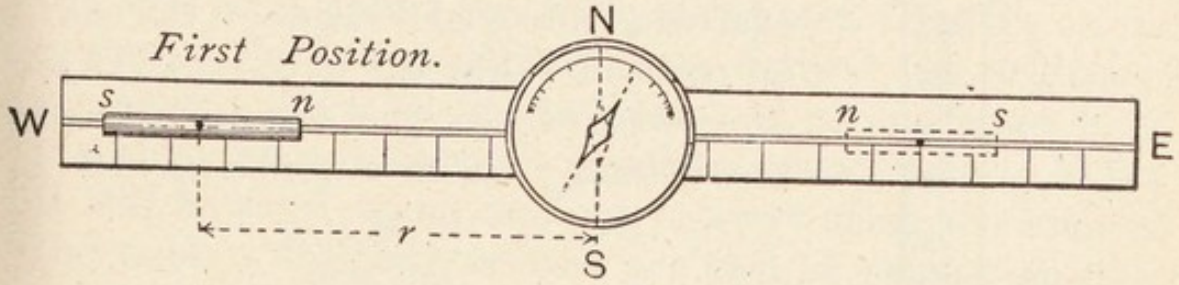


FIG. 86.—End-on Position.

strength of either pole of the magnet be called m, and let r be the distance of the centre of the magnet from the compass needle. Then if a unit pole were situated at the compass centre, its distance from the nearer pole of the deflecting magnet would be $r - \frac{1}{2}l$, and from the further pole would be $r + \frac{1}{2}l$. Hence, applying the law of inverse squares, the resultant force on the unit pole at the centre would be the difference between the two forces $m/(r - \frac{1}{2}l)^2$ and $m/(r + \frac{1}{2}l)^2$, which equals

$$\frac{2lmr}{r^4 - \frac{1}{2}l^2r^2 + (\frac{1}{2}l)^4}.$$

So that, if r is great compared with $\frac{1}{2}l$, we may write as an approximation,

$$\frac{2lmr}{r^4}, \text{ which is } \frac{2M}{r^3}.$$

But we have seen above that where magnetic force is measured by a deflexion δ at a place where the H is earth's horizontal magnetic force, f is equal to H tan δ; so that

$$2M/r^3 = H \tan \delta,$$

whence

$$M = \tfrac{1}{2}r^3 H \tan \delta.$$

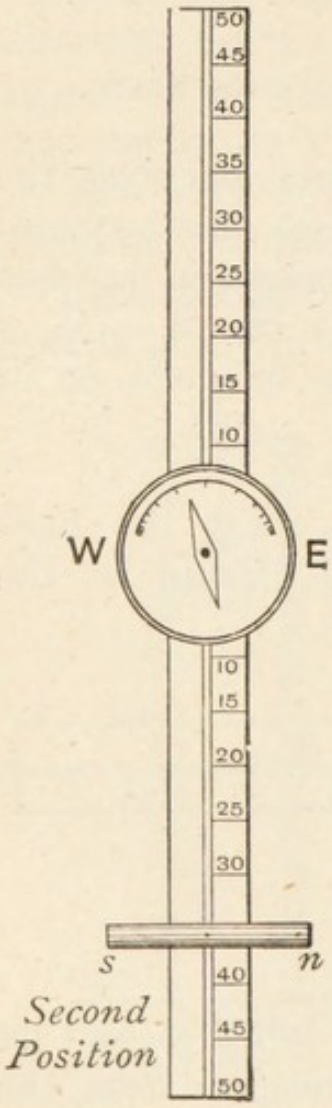


FIG. 87.—Broadside-on Position.

Second Position: Broadside on.—The platform being turned into the north-south position, the deflecting magnet is set *broadside on* (see Fig. 87). In this case the magnet deflects the needle in the other direction and with half the force that it would have exerted at an equal distance in the end-on position. But the force still varies *approximately as the inverse cube* of the distance; the formula being now

$$f = \frac{M}{(r^2 + \frac{1}{4}l^2)^{\frac{3}{2}}};$$

or, if $\frac{1}{2}l$ is small compared with r,

$$f = M/r^3,$$

whence

$$M = r^3 H \tan \delta.$$

141. Balance Methods. — In either position of the magnetometer platform two magnets can be placed on the two sides of the board so as to balance one another's effects by adjusting them to proper distances. This gives a comparison of their magnetic moments in terms of their respective distances, or

$$M_1 : M_2 = r_1^3 : r_2^3.$$

142. Unit Strength of Pole.—The Second Law of Magnetic Force (see Art. 130, p. 117) stated that the force exerted between two poles was proportional to the product of their strengths, and was inversely proportional to the square of the distance between them. It is possible to choose such a strength of pole that this proportionality shall become numerically an equality. In order that this may be so, we must adopt the following as our unit of strength of a pole, or unit magnetic pole: *A Unit Magnetic Pole is one of such a strength that when placed at a distance of one centimetre from a similar pole of equal strength it repels it with a force of one dyne* (see Art. 379, p. 360). If we adopt this definition we may express the second law of magnetic force in the following equation:—

$$f = \frac{m \times m'}{d^2},$$

where f is the force (in dynes), m and m' the strengths of the two poles, and d the distance between them (in centimetres). From this definition is derived the arbitrary convention about magnetic lines. If at any place in a magnetic field we imagine a unit magnetic pole to be set it will be acted upon, tending to move along the lines of the field. The force exerted per unit of magnetism (*i.e.* $f \div m$) is a measure of the strength of the field; so that $\mathcal{H} = f \div m$, and $f = \mathcal{H}m$. Then if at that place we find the force on unit pole to be $\mathcal{H}$ dynes, we may conceive that there are $\mathcal{H}$ lines drawn per square centimetre. For example, if we describe the field as having 50 lines side by side per square centimetre, we mean that a unit pole placed there will be acted on with a force of 50 dynes. Or we may say simply: the intensity of the field is 50 dynes per unit pole, or the flux density is 50 *gausses* (see Art. 365, p. 347).

143. Theory of Magnetic Figures.—We saw (Art. 121) that magnetic figures are produced by iron filings setting themselves in certain directions in the field of

force around a magnet. We can now apply the law of inverse squares to aid us in determining the direction in which a filing will set itself at any point in the field. Let NS (Fig. 88) be a long thin magnet, and P any point in the field due to its magnetism. If the N-seeking pole of a small magnet be put at P, it will be attracted by S and repelled by N; the directions of these two forces will be along the lines PS and PN. The amounts of the forces may be represented by certain

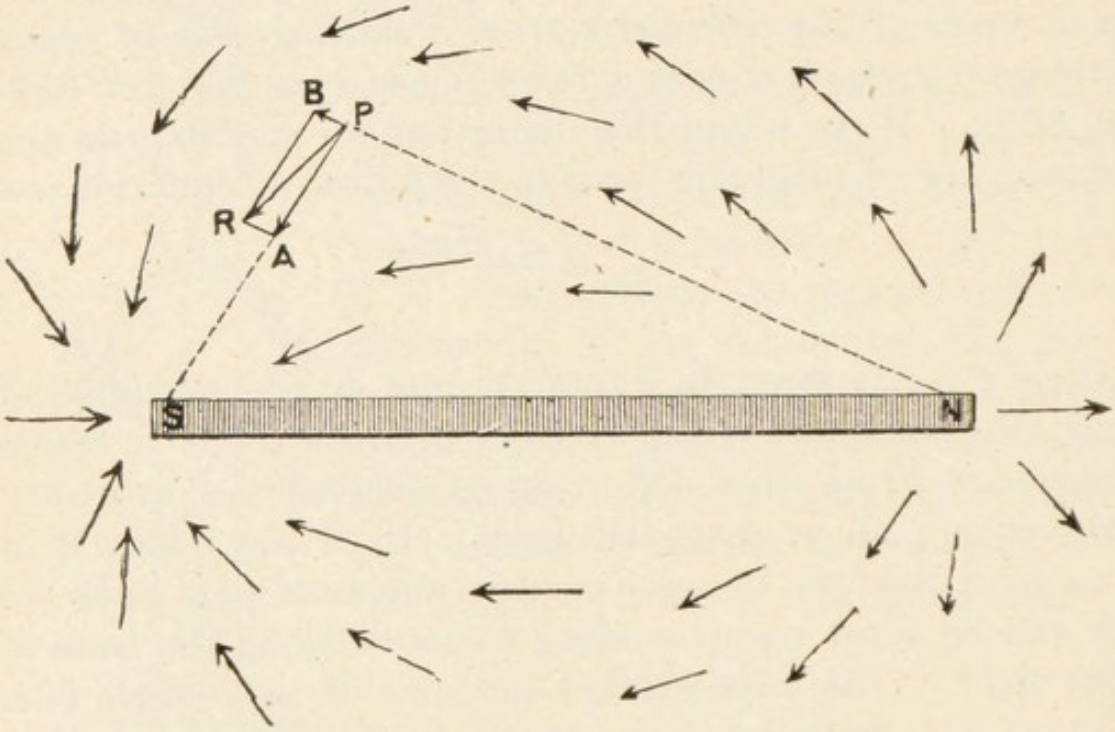


FIG. 88.—Theory of Magnetic Curves.

lengths marked out along these lines. Suppose the distance PN is twice as great as PS, the repelling force along PN will be $\frac{1}{4}$ as strong as the attracting force along PS. So measure a distance out, PA towards S four times as long as the length PB measured along PN away from N. Find the resultant force in the usual way of compounding mechanical forces, by completing the parallelogram PARB; the diagonal PR represents by its length and direction the magnitude and the direction of the resultant magnetic force at the point P. In fact the line PR represents the line along which a small magnet or an

iron filing would set itself. In a similar way we might ascertain the direction of the lines of force at any point of the field. The little arrows in Fig. 88 show how the lines of force start out from the N-pole and curve round to meet in the S-pole. The student should compare this figure with the lines of filings of Fig. 69 (p. 109). Henceforth we must think of every magnet as being permeated by these magnetic lines which extend out into the surrounding space. The whole number of magnetic lines which run through a magnet is termed its *magnetic flux* (Art. 364). It must be remembered, in making such experimental curves, that they are liable to be distorted by the presence of the earth's magnetic field.

144. Superposition of Magnetic Fields.—The

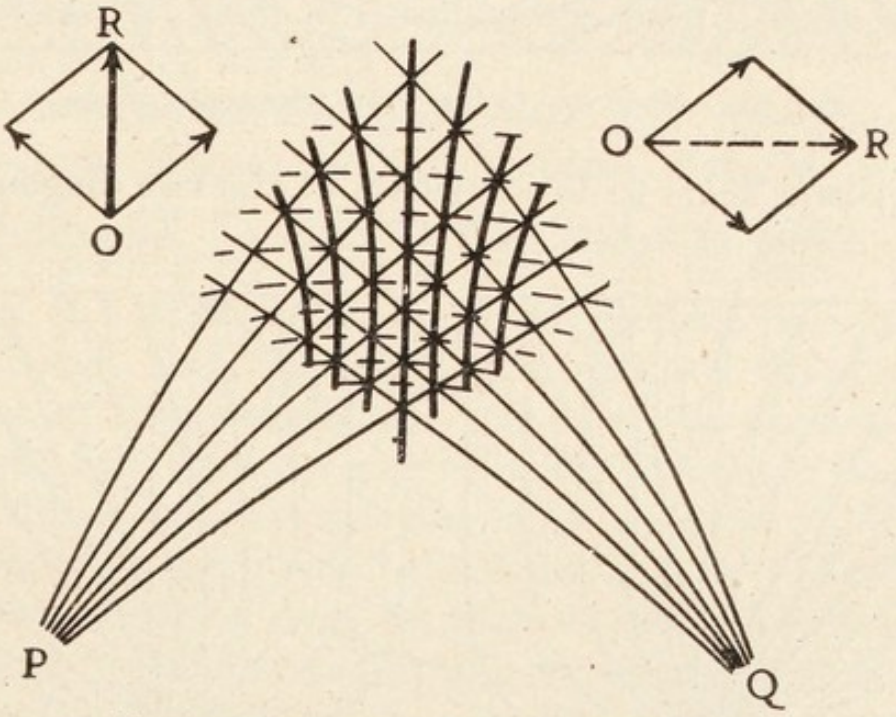


FIG. 89.—Superposition of Magnetic Fields.

process of finding resultants used above may be generalized for the study of the superposition of magnetic fields. When the lines of force of two separate magnetic fields are separately drawn, and then superposed, they present varied patterns of intersecting lines. Fig. 89 represents such a case. The lines of the resultant field formed by the superposition of these two fields may be drawn with sufficient

accuracy by merely joining the diagonals of the little quadrilaterals, regard being had to the initial directions of

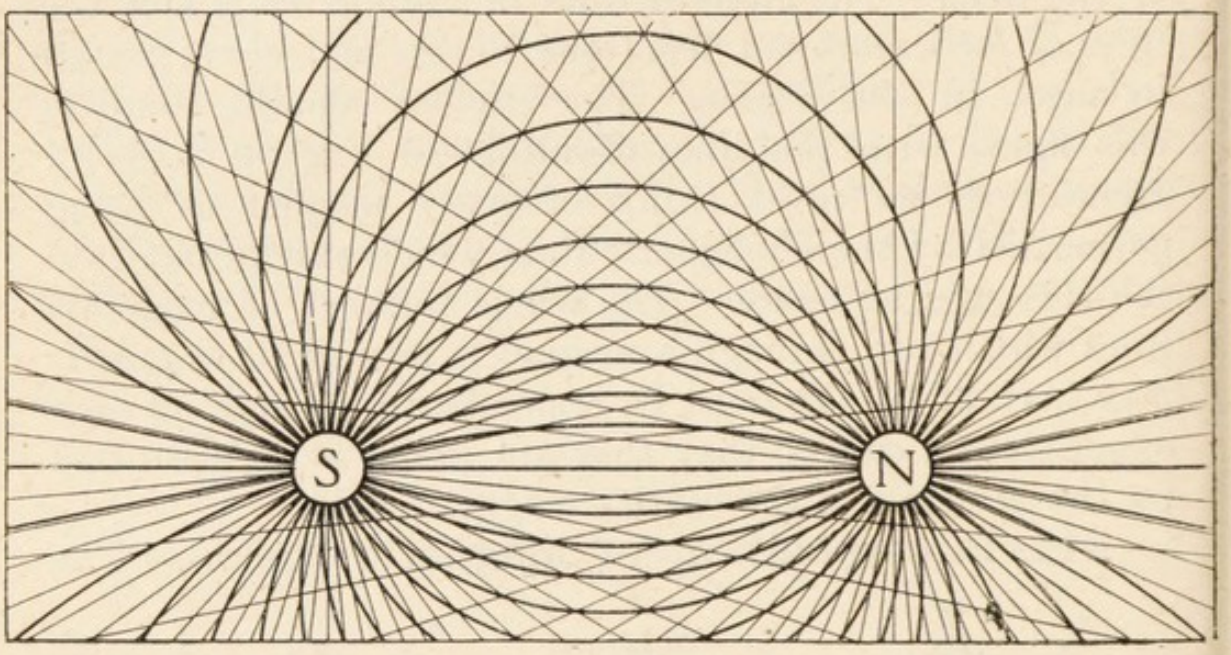


FIG. 90*a*.—Field due to two Poles of opposite kinds.

the separate fields to decide which of the two diagonals (as in the corner sketches) shall be drawn. As examples of

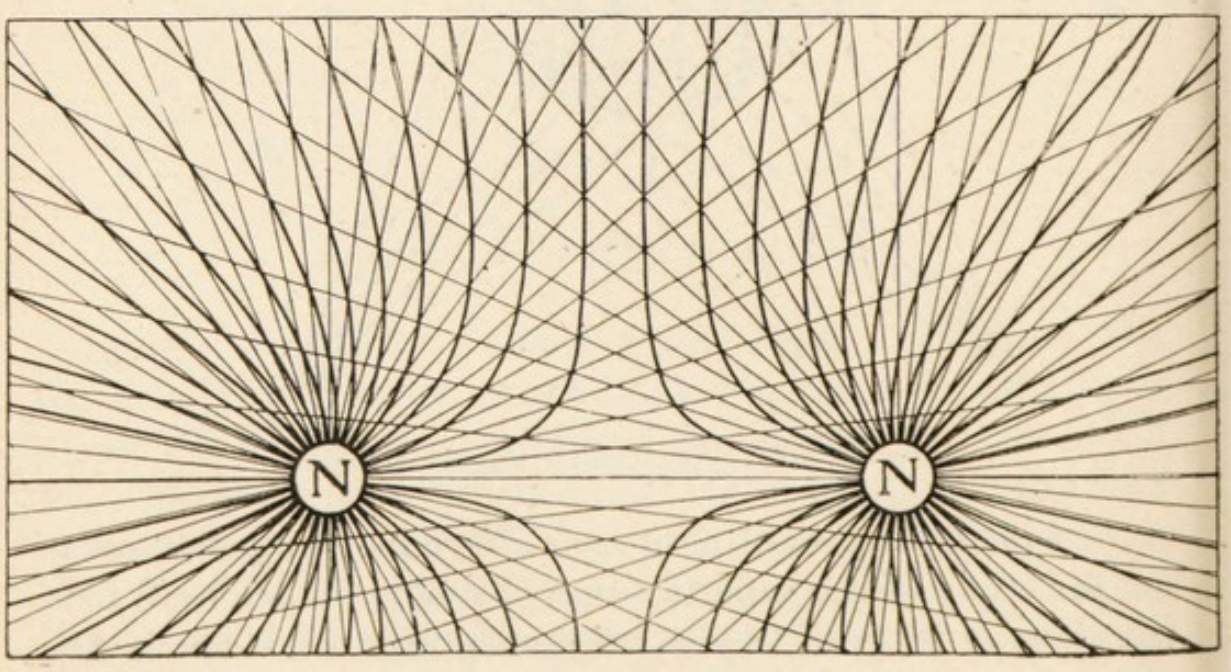


FIG. 90*b*.—Field due to two Poles of similar kinds.

this plan of superposition are given Fig. 90*a* and Fig. 90*b*, representing respectively the field between two equal

poles of opposite kinds, and two equal poles of the same kind. They should be compared with Figs. 73 and 74, p. 112. The same principle is used in Figs. 220 and 221, p. 411, for ascertaining the resultant magnetic field between two wires carrying currents, and in Fig. 190 for drawing the resultant field when a wire carrying a current is placed between the poles of a magnet. The superposition of two electric fields (Art. 420, p. 410) can be graphically treated in the same way.

145. Neutralizing Action of Opposite Poles.—That poles of opposite name can neutralize one another may be shown by the familiar experiment of hanging a steel ring or key to the N-pole of a bar magnet. On bringing the S-pole of another bar magnet to touch the first, the two poles will neutralize each other's actions, and the ring or key will drop.

A Magnetic Paradox.—If the N-seeking pole of a strong magnet be held at some distance from the N-seeking pole of a weak magnet, it will repel it; but if it is pushed up quite close it will be found now to *attract* it. This paradoxical experiment is explained by the fact that the magnetism induced in the weak magnet by the powerful one will be of the opposite kind, and will be attracted; and when the powerful magnet is near, this induced magnetism may overpower and mask the original magnetism of the weak magnet. The student must be cautioned that in most of the experiments on magnet poles similar perturbing causes are at work. The magnetism in a magnet is not quite *fixed*, but is liable to be disturbed in its distribution by the near presence of other magnet poles, for no steel is so hard as not to be temporarily affected by magnetic induction. For instance, it is possible for the polarity of a compass needle to be accidentally, or purposely, reversed by suddenly bringing a powerful magnet close to it; the magnetism being reversed by influence before the steel needle has had time to turn round.

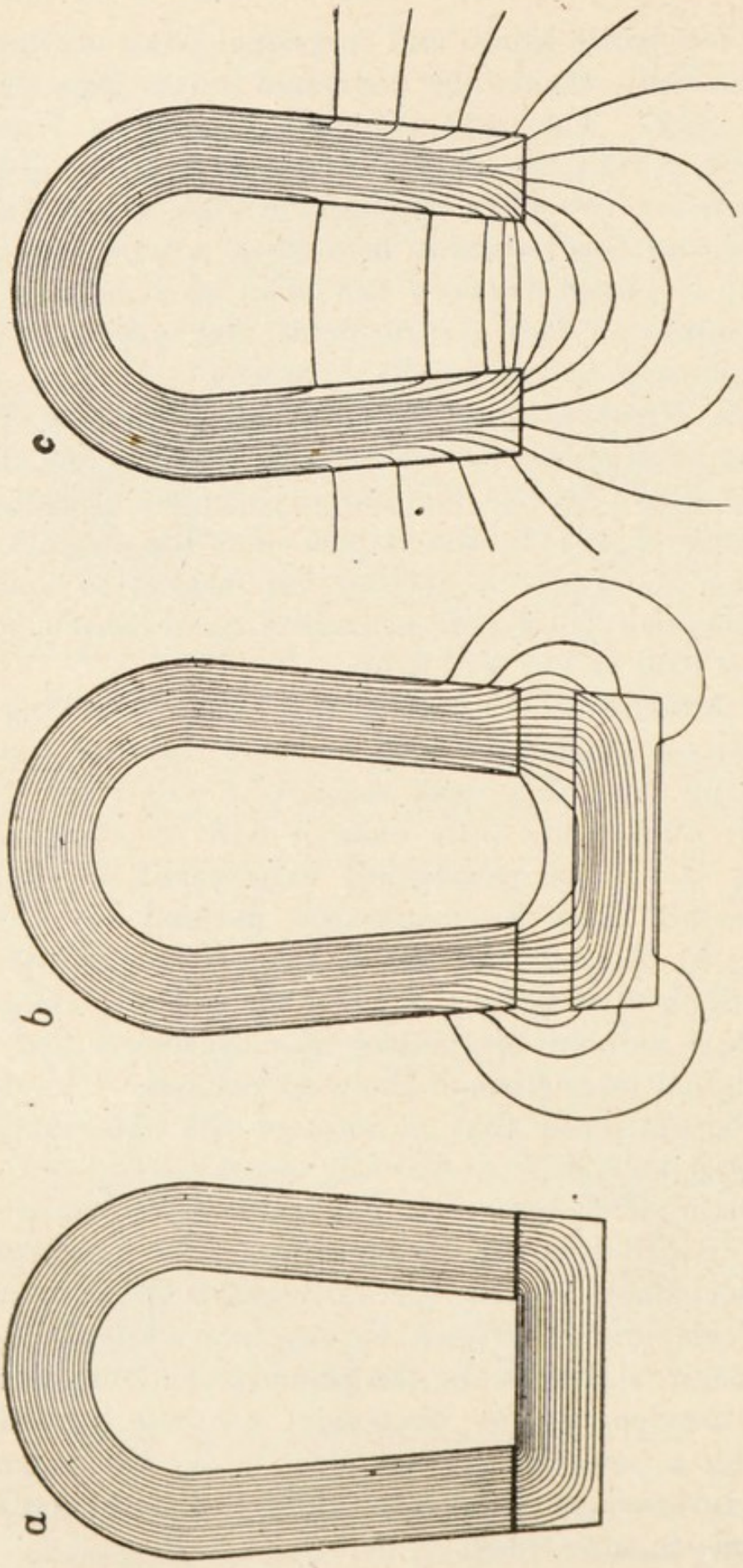


FIG. 91.—Magnetic Field of Permanent Horseshoe Magnet.

146. Pull of Permanent Magnets at Varying Distances.—When a permanent magnet is in contact with its keeper, the whole flux of magnetic lines goes through the keeper and pulls it (Fig. 91 *a*). But if the keeper be removed to a short distance, though the total number of lines of the magnet is unaltered, the pull is smaller because now a part only of the flux passes through the keeper, as in Fig. 91 *b* and *c*. The greater the width of the air-gap, the fewer the number of lines that reach the keeper. The pull does not vary inversely as the square of the distance.

Note on Ways of Reckoning Angles and Solid Angles

147. Reckoning in Degrees.—When two straight lines intersect one another they form an *angle* between them; and this angle may be defined as the amount of rotation which one of the lines has performed round a fixed point in the other line. Thus we may suppose the line CP in Fig. 92 to have originally lain along CO, and then turned round to its present position. The amount by which it has been rotated is clearly a certain fraction of the whole way round; and the amount of rotation round C we call "the angle which PC makes with OC," or more simply "the angle PCO." But there are a number of different ways of *reckoning* this angle. The common way is to reckon the angle by "degrees" of arc. Thus, suppose a circle to be drawn round C, if the circumference of the circle were divided into 360 parts each part would be called "one degree" (1°), and the angle would be reckoned by naming the number of such degrees along the curved arc OP. In the figure the arc is about $57\frac{1}{4}°$, or $\frac{57\frac{1}{4}}{360}$ of the whole way round, no matter what size the circle is drawn.

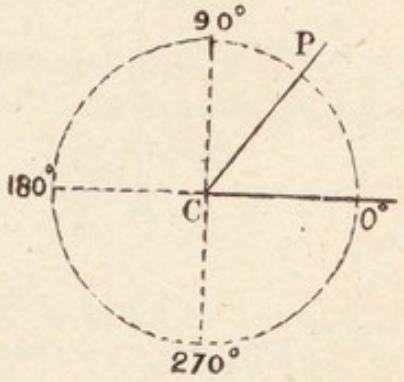


FIG. 92.

148. Reckoning in Radians.—A more sensible but less usual way to express an angle is to reckon it by the ratio between the length of the curved arc that "subtends" the angle and the length of the radius of the circle. Suppose we have drawn round the centre C a circle whose *radius* is *one* centimetre, the *diameter*

will be *two* centimetres. The length of the circumference all round is known to be about $3\frac{1}{7}$ times the length of the diameter, or more exactly 3·14159 . . . This number is so awkward that, for convenience, we always use for it the Greek letter π. Hence the length of the circumference of our circle, whose radius is one centimetre, will be 6·28318 . . . centimetres, or 2π centimetres. We can then reckon any angle by naming the length of arc that subtends it on a circle one centimetre in radius. If we choose the angle PCO, such that the curved arc OP shall be just one centimetre long, this will be the angle *one*, or unit of angular measure, or, as it is sometimes called, the angle PCO will be *one "radian."* In degree-measure one radian $= \frac{360^\circ}{2\pi} = 57^\circ\ 17'$ nearly. All the way round the circle will be 2π radians. A right angle will be $\frac{\pi}{2}$ radians.

149. Reckoning by Sines or Cosines.—In trigonometry other ways of reckoning angles are used, in which, however, the angles themselves are not reckoned, but certain "functions" of them called "sines," "cosines," "tangents," etc. For readers not accustomed to these we will briefly explain the geometrical nature of these "functions." Suppose we draw (Fig. 93) our circle as before round centre C, and then drop down a plumb-line PM, on to the line CO; we may, instead of reckoning the angle by the curved arc, reckon it by the length of the line PM. It is clear that if the angle is small PM will be short; but as the angle opens out towards a right angle, PM will get longer and longer (Fig. 94). The ratio between the length of this line and the radius of the circle is called the "*sine*" *of the angle*, and if the radius is 1 the length of PM will be the value of the sine. It can never be greater than 1, though it may have all values between 1 and −1. The length of the line CM will also depend upon the amount of the angle. If the angle is small CM will be nearly as long as CO; if the angle open out to nearly a right angle CM will be very short. The length of CM (when the radius is 1) is called *the "cosine" of the angle.* If the angle be called θ, then we may for shortness write these functions:

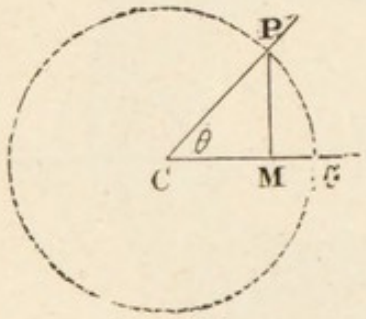


Fig. 93.

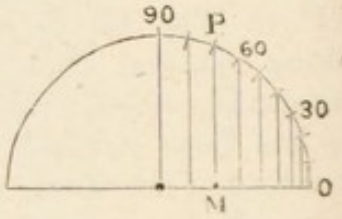


Fig. 94.

$$\sin\theta = \frac{PM}{CP}$$

$$\cos\theta = \frac{CM}{CP}.$$

150. Reckoning by Tangents.—Suppose we draw our circle as before (Fig. 95), but at the point O draw a straight line touching the circle, the *tangent line* at O; let us also prolong CP until it meets the tangent line at T. We may measure the angle between OC and CP in terms of the length of the tangent OT as compared with the length of the radius. Since our radius is 1, this ratio is numerically the length of OT, and we may therefore call the length of OT *the "tangent" of the angle* OCP. It is clear that smaller angles will have smaller tangents, but that larger angles may have very large tangents; in fact, the length of the tangent when PC was moved round to a right angle would be infinitely great. It can be shown that the ratio between the lengths of the sine and of the cosine of the angle is the same as the ratio between the length of the tangent and that of the radius; or the tangent of an angle is equal to its sine divided by its cosine. The formula for the tangent may be written:

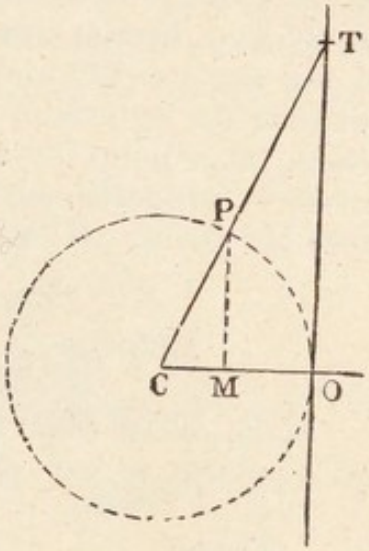


FIG. 95.

$$\tan\theta = \frac{TO}{OC} = \frac{PM}{MC}.$$

A table of radians, sines, tangents, etc., is given at the end of this book as Appendix A, p. 682.

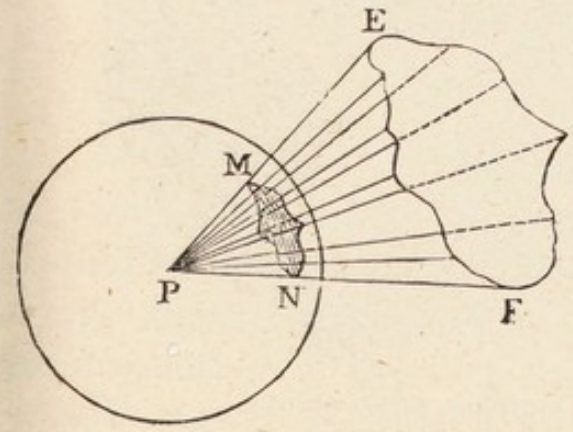


FIG. 96.

151. Solid Angles.—When three or more surfaces intersect at a point they form a *solid angle*: there is a solid angle, for example, at the top of a pyramid, or of a cone, and one at every corner of a diamond that has been cut. If a surface of any given shape be near a point, it is said to subtend a certain solid angle at that point, the solid angle being mapped out by drawing lines from all points of the edge of this surface to the point P (Fig. 96). An irregular cone will thus be generated whose solid angle is the solid angle subtended at P by

the surface EF. To reckon this solid angle we adopt an expedient similar to that adopted when we wished to reckon a plane angle in radians About the point P, with radius of 1 centimetre, describe a *sphere*, which will intercept the cone over an area MN : the area thus intercepted measures the solid angle. If the sphere have the radius 1, its total surface is 4π. The solid angle subtended at the centre by a hemisphere would be 2π. The ratio between the area of the surface EF and the area of the surface MN is the ratio between the squares of the lines EP and MP. The solid angle subtended at a point by a given surface (other things being equal) is inversely proportional to the square of the distance of that surface from the point. This is the basis of the law of inverse squares.

LESSON XII.—*Terrestrial Magnetism*

152. The Mariners' Compass.—It was mentioned in Art. 89, p. 89, that the compass sold by opticians con-

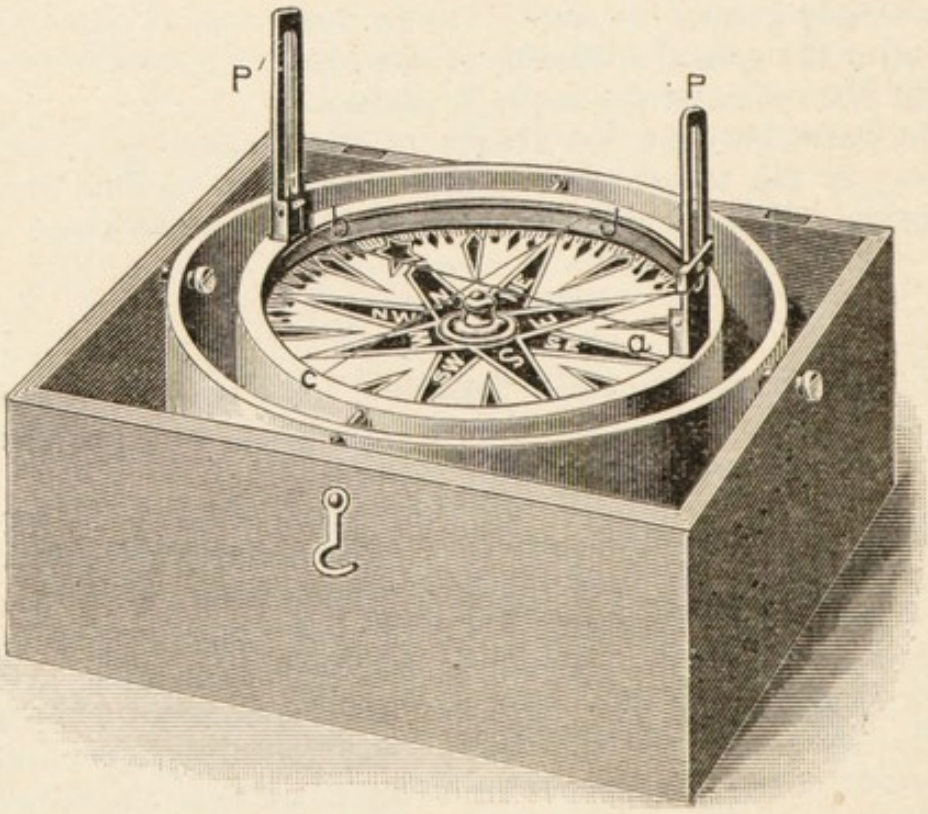


FIG. 97.—Mariners' Compass, with Sights.

sists of a magnetized steel needle balanced on a fine point above a card marked out N, S, E, W, etc. The **Mariners' Compass** is, however, somewhat differently arranged.

In Fig. 97 one of the forms of a Mariners' Compass,

used for nautical observations, is shown. Here the card, divided into the 32 "points of the compass," is itself attached to the needle, and swings round with it so that the point *marked* N *on the card* always points to the magnetic north. The bowl containing the compass is swung on gimbals to keep it level when the ship rolls or pitches. The iron hull and iron fittings of ships affect

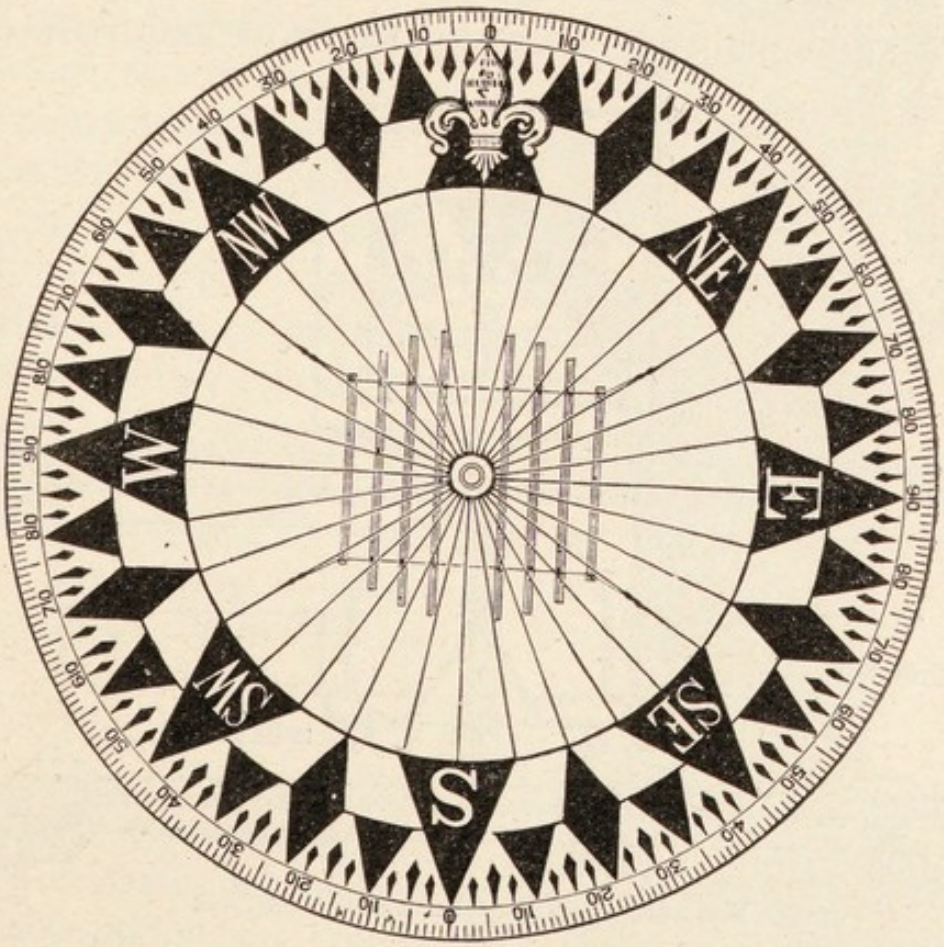


FIG. 98.—Kelvin Compass Card.

the compass, which has therefore to be corrected by placing correcting masses of iron near it, or by fixing it high upon a mast. The error of the compass due to the magnetism of the ship itself is called *the deviation.*

153. Lord Kelvin's Compass.—Lord Kelvin introduced many improvements. To reduce friction on the pivot, and to make the horizontal oscillations of the card slow, he reduced the weight, making the card light by cutting away the middle part, and substituting for the

usual long heavy needle a set of six or eight short light steel needles slung by silk threads below the card. A 10-inch card with its needles weighs only 180 grains ($11\frac{1}{2}$ grammes). To damp the swinging of the bowl it was partly filled with stiff castor oil. The shortness of the needles enabled corrections to be made for the deviation.

154. Floating Compasses.—Recently a further step has been taken by filling the entire compass with liquid, which helps to buoy up the card and reduce its

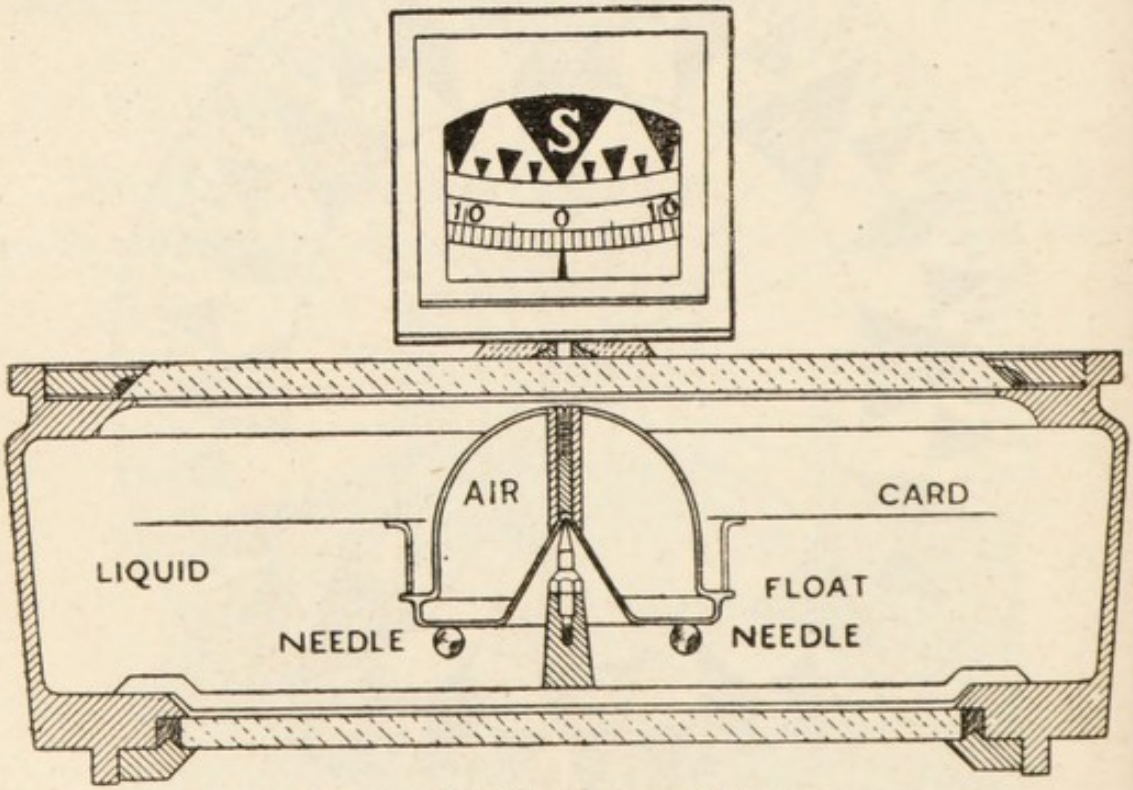


FIG 99.—Kelvin-Chetwynd Compass

effective weight on the pivot. Fig. 99 shows a section of the Kelvin-Chetwynd compass, from which the way in which the float attached below the compass card may be seen. The weight of card and float is actually 82·9 grammes; but, being buoyed up by the spirit in which it is immersed, the actual weight on the pivot is only 7 grammes. Fig. 100 depicts the compass complete in its binnacle. The card is illuminated by two lamps, and is viewed by an optical contrivance so that the card itself appears vertical.

155. Correction of Compass Errors.—The iron hull of a ship is always magnetic; there is a permanent part of the magnetism depending on the direction in which she lay when being built, and a temporary part due to the earth inducing in her a temporary polarity which varies according to the direction in which she is heading. There is a third error, called the *heeling error*, due to the vertical component of the magnetism, which, when a ship rolls, or heels over, tends to set the compass swinging. The permanent part of the ship's magnetism manifests itself by causing the deviation, while the ship is "swung" right round, to become a maximum twice; hence it is called the *semicircular* error. The temporary or induced part causes the deviation to become a maximum four times while the ship is swung round; hence it is called the *quadrantal error*. The semicircular error is compensated by putting below the compass two horizontal sets of correcting steel magnets: one set fixed fore and aft to correct the error that is found when the ship's head lies east or west; the other set is fixed athwart-ships to compensate the error when the ship's head points north or south. A third group of steel magnets is set vertically to correct the heeling error. The

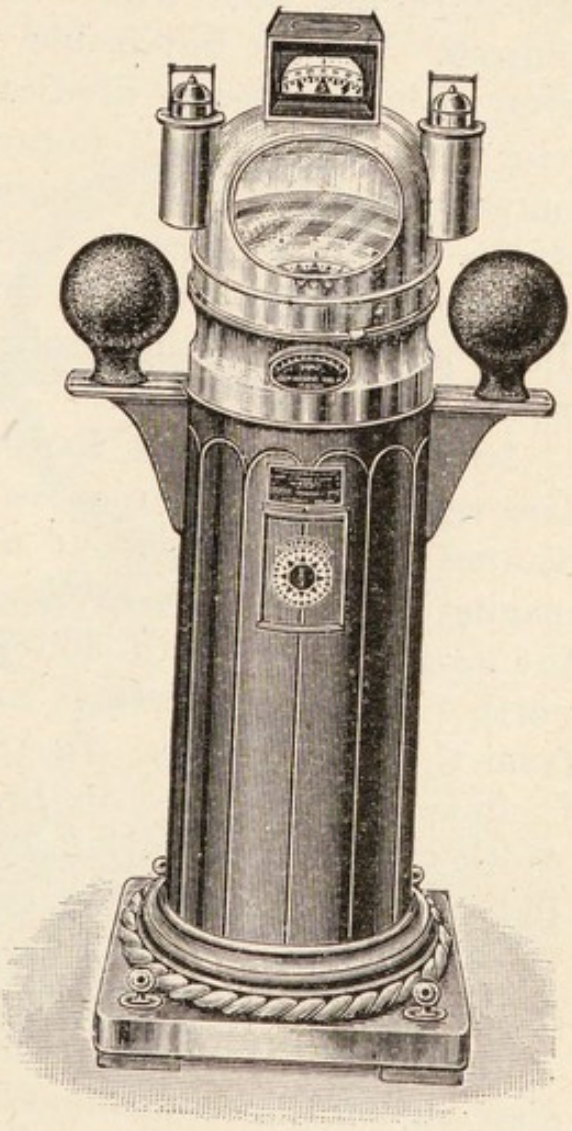


FIG. 100.—Kelvin-Chetwynd Compass.

quadrantal error is corrected by placing two large balls of soft iron at the sides of the compass, athwart-ship, to correct for the masses of iron of the hull which lie fore and aft. They must be of suitable size and be set at suitable distances apart. In Fig. 100 the two spherical correctors are seen supported right and left of the compass. It was impossible to correct the quadrantal error when long heavy needles were used for the compass prior to Lord Kelvin's improvements. As the vertical component of the earth's magnetism varies from one part of the earth's surface to another (Art. 158), a further correction for errors due to this is made by placing under the compass a vertical soft-iron bar, called, from its inventor, a Flinders bar.

156. The Earth's Poles.—Gilbert made the great discovery that the compass-needle points north and south because *the earth is itself also a great magnet.* The magnetic poles of the earth are, however, not exactly at the geographical north and south poles. The magnetic north pole of the earth is more than 1000 miles away from the actual pole. In 1831 it was found by Sir J. C. Ross to be situated in Boothia Felix, just within the Arctic Circle, being in lat. 70° 5′ N., and long. 96° 46′ W. The south magnetic pole of the earth was reached in 1909 by Sir Ernest Shackleton's expedition. It is situated in lat. 72° 25′ S., long. 155° 16′ E.

157. Declination.—In consequence of this natural distribution the compass-needle does not at all points of the earth's surface point truly north and south. Thus, in 1894, the compass-needle at London pointed at an angle of about 17° west of the true north; in 1910 it was 16° 5′. This angle between the *magnetic meridian* [1] and the geographical meridian of a place is called the magnetic

[1] The *Magnetic Meridian* of any place is an imaginary plane drawn through the zenith, and passing through the magnetic north point and magnetic south point of the horizon, as observed at that place by the pointing of a horizontally-suspended compass-needle.

Declination of that place. The existence of this declination was discovered by Columbus in 1492, but may have been previously observed. The fact that the declination differs at different points of the earth's surface, is the undisputed discovery of Columbus.

In order that ships may steer by the compass, magnetic charts (Art. 161, p. 149) must be prepared, and the declination at different places accurately measured. The upright pieces P, P′, on the "azimuth compass" drawn in Fig. 97, are for the purpose of sighting a star whose position may be known from astronomical tables, and thus affording a comparison between the magnetic meridian of the place and the geographical meridian, and of measuring the angle between them.

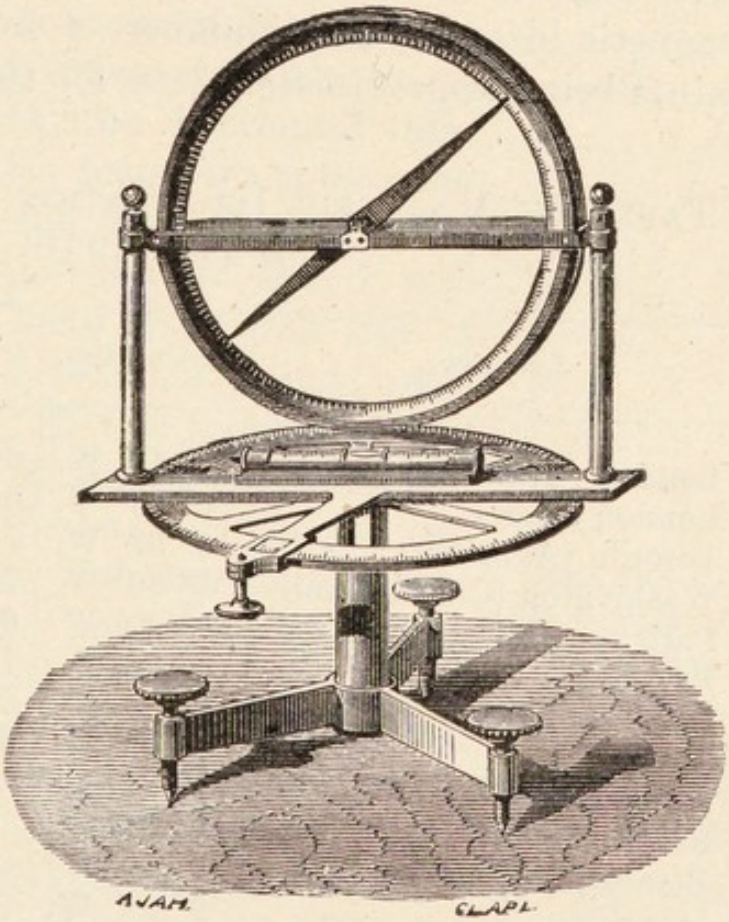


FIG. 101.—Dipping-Needle.

158. Inclination or Dip.—Norman, an instrument-maker, discovered in 1576 that a balanced needle, when magnetized, tends to dip downwards toward the north. He therefore constructed a **Dipping-Needle**, capable of turning in a vertical plane about a horizontal axis, with which he found the dip to be (at London) an angle of 71° 50′. A simple form of Dipping-needle is shown in Fig. 101. The dip-circles used in the magnetic observatory

at Kew are much more exact and delicate instruments. It was, however, found that the dip, like the declination, differs at different parts of the earth's surface, and that it also undergoes changes from year to year. The dip in London for the year 1910 was 66° 59′; in 1915 it is about 66° 55′. In 1910 it was 70° 5′ at Edinburgh, and 70° 45′ at Aberdeen. At the north magnetic pole the needle dips straight down. The following Table gives particulars of the Declination, Inclination, and horizontal magnetic intensity at a number of important places, the values being approximately true for the year 1910.

TABLE OF MAGNETIC DECLINATION AND INCLINATION
(for Year 1910)

Locality.	Declination.	Dip.	Horizontal Force H.
London (Greenwich)	15° 41′ W.	66° 57′ N.	0·1851
London (Kew)	16° 5′ W.	66° 59′ N.	0·1850
Toronto (Agincourt)	5° 59′ W.	74° 40′ N.	0·1630
Washington (Cheltenham)	5° 36′ W.	70° 31′ N.	0·1990
Paris	14° 20′ W.	64° 53′ N.	0·1998
Pavlovsk	1° 22′ E.	70° 39′ N.	0·1648
Potsdam	9° 3′ W.	66° 21′ N.	0·1881
Athens	4° 35′ W.	52° 11′ N.	0·2620
Hong-Kong	0° 1′ E.	30° 59′ N.	0·3706
Rio Janeiro	9° 31′ W.	14° 25′ S.	0·2473
Bombay (Alibag)	0° 59′ E.	23° 35′ N.	0·3684
Mauritius	9° 31′ W.	53° 37′ S.	0·2330
Tokio	4° 58′ W.	49° 7′ N.	0·3001
Christchurch (New Zealand)	16° 37′ E.	67° 59′ S.	0·2251

159. Intensity.—Three things must be known in order to specify exactly the magnetic conditions at any place; these three elements are:

The Declination;
The Inclination or Dip; and
The Intensity of the Magnetic Force.

The magnetic force is measured by one of the methods mentioned in the preceding Lesson. Its direction is in the line of the dipping-needle, which like every magnet, tends to set itself along the lines of force. It is, however, more convenient to measure the force not in its total intensity in the line of the dip, but to measure the horizontal component of the force,—that is to say, the force in the direction of the horizontal compass-needle, from which the total force can be calculated if the dip is known.[1] If in the triangle of Fig. 102 the horizontal line H is drawn to scale to represent by its length the horizontal component of the earth's magnetic force, and the vertical line V, the vertical component of the force, then the oblique line I will represent the total force down the line of dip; and the angle θ between H and I will be the angle of dip. If the horizontal and vertical components of the force are known, the total force and the angle of the dip can both be calculated.[2] The horizontal component of the force, or "horizontal intensity," can be ascertained either by the method of Vibrations or by the method of Deflexions.

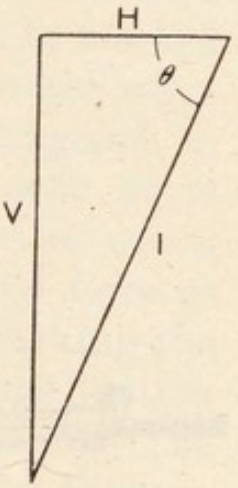


FIG. 102. Components of Earth's Magnetic Force.

The mean horizontal force of the earth's magnetism at London in 1915 is 0·1848 *gausses*, the mean vertical force 0·4332, the total force (in the line of dip) was 0·4710 *gausses*. The distribution of the magnetic force at different points of the earth's surface is irregular, and varies in different latitudes according to an approximate law, which, as given by Biot, is that the force is proportional to $\sqrt{1+3\sin^2 l}$, where l is the magnetic latitude.

160. Kew Pattern Magnetometer. — For the precise measurement of the declination and of the

[1] For if H = Horizontal Component of Force, and I = Total Force, and θ = angle of dip, $I = H \div \cos\theta$.

[2] For $H^2+V^2=I^2$, where V = Vertical Component of Force.

horizontal force a magnetometer of fine construction is

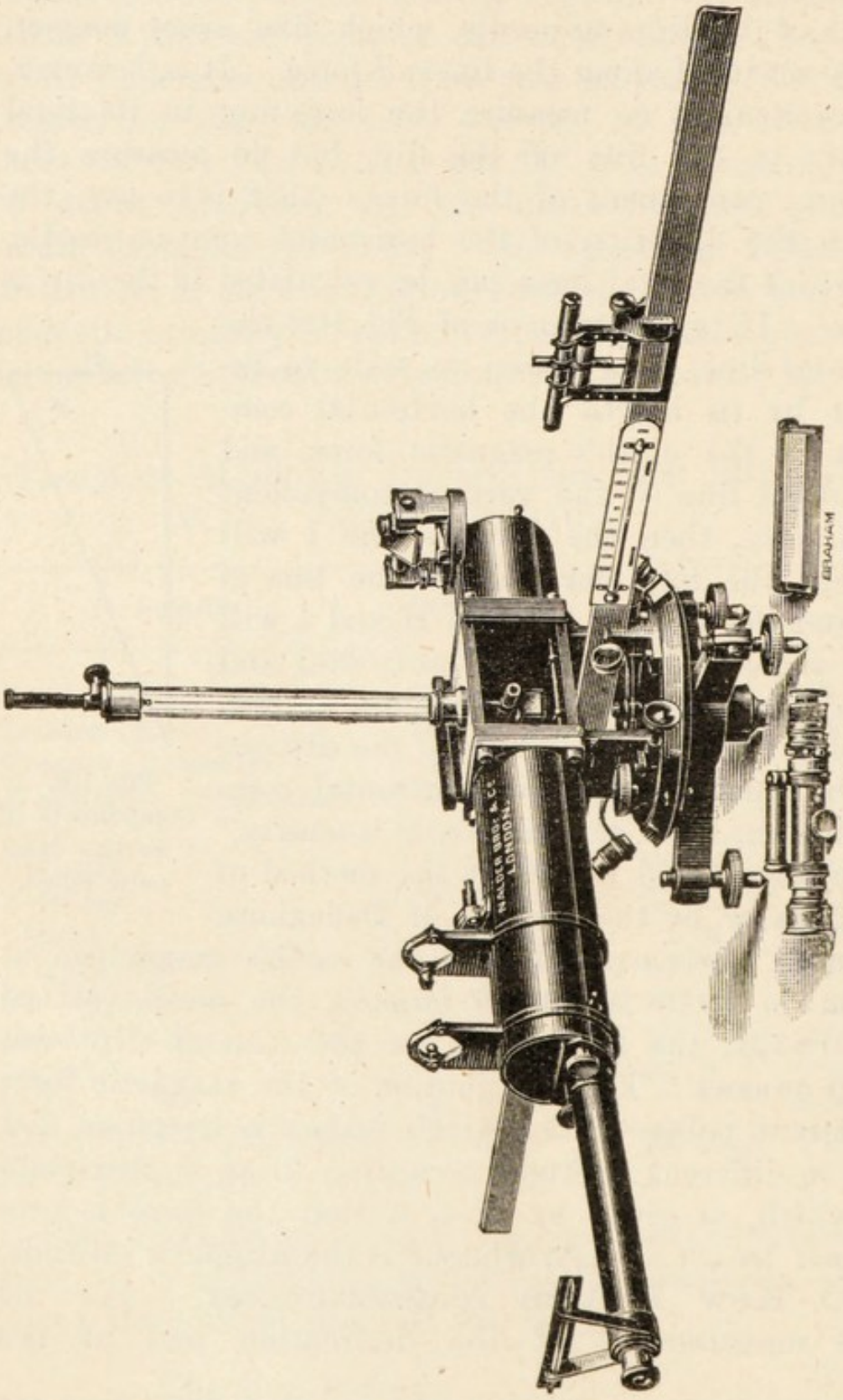


Fig. 103.—Kew Pattern Magnetometer.

employed, as shown in Fig. 103. The magnets are small hollow cylinders which can be suspended in order to observe

their times of oscillation, and which can also be placed on supports M at known distances on a cross bar XY, to serve as deflecting magnets in an end-on position. The tubular magnets are provided with a scale S at one end, and a lens at the other to facilitate observation. Art. 140 gives the method of calculating from such observations the value of H at the place of observation.

161. Magnetic Maps.—For purposes of convenience it is usual to construct magnetic maps, on which such data as those given in the Table on p. 146 can be marked down. Such maps may be constructed in several ways. Thus, it would be possible to take a map of England, or of the world, and mark it over with lines such as to represent by their direction the actual direction in which the compass points; in fact to draw the lines of force or magnetic meridians. A more useful way of marking the map is to find out those places at which the declination is the same, and to join these places by a line. The Magnetic Map of Great Britain, which forms the Frontispiece to these Lessons, is constructed on this plan from the magnetic survey lately made by Rücker and Thorpe as corrected by the latest observations of Kew Observatory and of the Admiralty. At Plymouth the compass-needle in 1910 pointed 17° to the west of the geographical north. The declination at Bristol and at Durham was in this year the same as at Plymouth. Hence a line joining these towns may be called a *line of equal declination*, or an **Isogonic line.** It will be seen from this map that the declination is greater in the north-west of England than in the south-east. We might similarly construct a magnetic map, marking it with lines joining places where the *dip* was equal: such lines would be called **Isoclinic lines.** In England they run across the map from west-south-west to east-north-east. For example, in 1910 the needle dipped about 68° at Nottingham and at Aberystwyth. Through these places then the isoclinic of 68° may be drawn for that epoch. On the globe the isogonic

lines run for the most part from the north magnetic pole to the south magnetic polar region, but, owing to the irregularities of distribution of the earth's magnetism, their forms are not simple. The isoclinic lines of the globe run round the earth like the parallels of latitude, but are irregular in form. Thus the line joining places where the north-seeking pole of the needle dips down 70° runs across Scotland and the north of Ireland; then crosses the Atlantic in a south-westerly direction, traverses the United States, swerving northwards, and just crosses the southern tip of Alaska. It drops somewhat southward again as it crosses China, but again curves northwards as it enters Russian territory. Finally it crosses the southern part of the Baltic, and reaches Scotland across the German Ocean. The magnetic chart of the United States, which is also given at the front of this book, is for the year 1910. It has been prepared from data furnished by Dr. L. A. Bauer of the U.S. Geodetic Survey. It will be noticed that in the year 1910 the magnetic declination was zero at Pittsburg (Ohio), and near Charleston (S. Carolina).

The line passing through places of no declination is called the *agonic* line. It passes across both hemispheres, crossing Russia, Persia, and Australia. There is another agonic line in eastern Asia enclosing a region around Japan, within which there is a westerly declination.

162. Variations of Earth's Magnetism. — We have already mentioned that both the declination and the inclination are subject to changes; some of these changes take place very slowly, others occur every year, and others again every day.

Those changes which require many years to run their course are called *secular changes.*

The variations of the *Declination* previous to 1580 are not recorded; the compass at London then pointed 11° *east* of true north. This easterly declination gradually decreased, until in 1657 the compass pointed true north. It then moved westward, attaining a maximum of 24°

27′ about the year 1816, from which time it has slowly diminished to its present value (15° 19′ in 1915); it diminishes (in England) at about the rate of 9′ per year. At about the year 1976 it will again point truly north, making a complete cycle of changes in about 640 years.

The *Inclination* in 1576 was 71° 50′, and it slowly increased till 1720, when the angle of dip reached the maximum value of 74° 42′. It has since steadily diminished to its present (1915) value of 66° 55′. The period in which the cycle is completed is not known, but the rate of variation of the dip is less at the present time than it was fifty years ago. In all parts of the earth both declination and inclination are slowly changing. The following table gives the data of the secular changes at London.

TABLE OF SECULAR MAGNETIC VARIATIONS

Year.	Declination.	Inclination.
1576		71° 50′
1580	11° 17′ E.	
1600		72° 0′
1622	6° 12′	
1634	4° 0′	
1657	0° 0′ min.	
1676	3° 0′ W.	73° 30′
1705	9° 0′	
1720	13° 0′	74° 42′ max.
1760	19° 30′	
1780		72° 8′
1800	24° 6′	70° 35′
1816	24° 30′ max.	
1830	24° 2′	69° 3′
1855	23° 0′	
1868	20° 33′	68° 2′
1878	19° 14′	67° 43′
1880	18° 40′	67° 40′
1890	17° 26′	67° 23′
1900	16° 16′	67° 9′
1910	15° 3′	66° 56′
1920	14° 20′	66° 49′

The *Total Magnetic force*, or "Intensity," also slowly changes in value. As measured near London, it was equal to 0·4791 *gausses* in 1848, 0·4740 in 1866, in 1880 0·4736 *gausses*, in 1890 0·4741.[1] In 1915 it is 0·4710. Owing to the steady decrease of the angle at which the needle dips, the horizontal component of this force (*i.e.* the "Horizontal Intensity") is slightly increasing. It was 0·1716 *gausses* in 1814, 0·1797 *gausses* at the beginning of 1880, and 0·1823 *gausses* in 1890. In 1915 it is 0·1848.

163. Daily Variations.—Both compass and dipping-needle, if minutely observed, exhibit slight daily motions. About 7 A.M. the compass-needle begins to travel westward with a motion which lasts till about 1 P.M.; during the afternoon and evening the needle slowly travels back eastward, until about 10 P.M.; after this it rests quiet; but in summer-time the needle begins to move again slightly to the west at about midnight, and returns again eastward before 7 A.M. These delicate variations—never more than 10′ of arc—appear to be connected with the position of the sun; and the moon also exercises a minute influence upon the position of the needle.

164. Annual Variations.—There is also an annual variation corresponding with the movement of the earth around the sun. In the British Islands the total force is greatest in June and least in February, but in the Southern Hemisphere, in Tasmania, the reverse is the case. The dip also differs with the season of the year, the angle of dip being (in England) less during the four summer months than in the rest of the year.

165. Eleven-Year Period.—General Sabine discovered that there is a larger amount of variation of the declination occurring about once every eleven years. Schwabe noticed that the recurrence of these periods

[1] That is to say, a north magnet pole of unit strength is urged in the line of dip, with a mechanical force of a little less than half a dyne.

coincided with the eleven-year periods at which there is a maximum of *spots* on the sun. Professor Balfour Stewart and others have endeavoured to trace a similar periodicity in the recurrence of **auroræ**[1] and of other phenomena.

166. Magnetic Storms.—It is sometimes observed that a sudden (though very minute) irregular disturbance will affect the whole of the compass-needles over a considerable region of the globe. Such occurrences are known as magnetic storms; they frequently occur at the time when an aurora is visible. It is suggested that they are due to the emission by the sun of invisible radiations resembling kathode rays, which alter the conductivity of strata of the upper air, and thus augment the electric currents that circulate in the atmosphere.

167. Self-recording Magnetic Apparatus.—At Kew and other magnetic observatories the daily and hourly variations of the magnet are recorded on a continuous register. The means employed consists in throwing a beam of light from a lamp on to a light mirror attached to the magnet whose motion is to be observed. A spot of light is thus reflected upon a ribbon of photographic paper prepared so as to be sensitive to light. The paper is moved continuously forward by a clockwork train; and if the magnet be at rest the dark trace on the paper will be simply a straight line. If, however, the magnet moves aside, the spot of light reflected from the mirror will be displaced, and the photographed line will be curved or crooked. Comparison of such records, or *magnetographs*, from stations widely apart on the earth's surface, promises to afford much light upon the *cause* of the changes of the earth's magnetism, to which hitherto no reliable origin has been with certainty assigned. Schuster has shown that these changes generally come from without, and not from within.

168. Theory of Earth's Magnetism.—The phe-

[1] See Lesson XXV., on Atmospheric Electricity (p. 340).

nomenon of earth-currents, observed to occur spontaneously in long telegraph lines, and flowing generally in directions from the poles towards the Equator, appears to be connected with that of the changes in the earth's magnetism. They are of daily occurrence, but feeble except whenever there is a display of aurora, and during a magnetic storm; but it is not yet determined whether these currents are due to the variations in the magnetism of the earth, or whether those variations are due to the currents. It is believed that the evaporation (see Art. 72) always going on in the tropics causes the ascending currents of heated air to be electrified positively relatively to the earth. Probably the ionizing action (Art. 632) of ultra-violet light in the upper regions has also some share. The air-currents travel northward and southward toward the colder polar regions, where they descend. These streams of electrified air will act (see Art. 429) like true electric currents, and as the earth rotates within them it will be acted upon magnetically. The author has for many years upheld the view that this thermodynamic production of polar currents in conjunction with the earth's diurnal rotation affords the only rational means yet suggested for accounting for the growth of the earth's magnetism to its present state. The action of the sun and moon in raising tides in the atmosphere might account for the variations mentioned in Art. 162. It is important to note that in all magnetic storms the intensity of the perturbations is greatest in the regions nearest the poles; also, that the magnetic poles coincide very nearly with the regions of greatest cold; that the region where auroræ (Art. 361) are seen in greatest abundance is a region lying nearly symmetrically round the magnetic pole.

CHAPTER III

CURRENT ELECTRICITY

LESSON XIII.—*Simple Voltaic Cells*

169. Flow of Currents.—It has been already mentioned, in Lesson IV., how electricity flows away from a charged body through any conducting substance, such as a wire or a wetted string. If, by any arrangement, electricity could be supplied to the body just as fast as it flowed away, a continuous **current** would be produced. Such a current always flows through a conducting wire, if the ends are kept at different electric potentials. In like manner, a current of heat flows through a rod of metal if the ends are kept at different temperatures, the flow being always from the high temperature to the lower. It is convenient to regard the electricity as flowing from positive to negative. The natural direction of an electric current is from the high potential to the low; such a flow tends to equalize the potential. In order that a continuous flow may be kept up there must be a **circuit**[1]—that is, a conducting path—provided. The "current" has sometimes been regarded as a double transfer of positive electricity in one direction,

[1] The conductors connected with a source of electrical supply are collectively called the "circuit." When they form a closed path through which a current circulates there is a "closed circuit." When the path is not closed and no current circulates there is an "open circuit."

and of negative electricity in the opposite direction. The only evidence to support this very unnecessary supposition is the fact that, in the decomposition of liquids by the current, some of the elements are liberated at the place where the current enters, others at the place where it leaves the liquid. Another notion is that the "current" consists in swarms of electrons (or negative particles) flowing along the circuit from negative to positive. No final evidence exists as to the direction in which the current in a wire really "flows."

The quantity of electricity conveyed by a current is proportional to the current and to the time that it continues to flow. The practical unit of current is called the *ampere* (see Arts. 220 and 381). The quantity of electricity conveyed by a current of one *ampere* in one second is called one *ampere-second* or one *coulomb*. One *ampere-hour* equals 3600 *coulombs*. If i is the number of amperes of current, t the number of seconds that it lasts, and Q the number of coulombs of electricity thereby conveyed, the relation between them is expressed by the formula:—

$$Q = i \times t.$$

Example.—If a current of 80 amperes flows for 15 minutes the total quantity of electricity conveyed will be $80 \times 15 \times 60 = 72{,}000$ coulombs. This is equal to 20 ampere-hours.

170. Continuous and Alternating Currents.—Currents are called *continuous* if they flow, without stopping, in one direction. They are called *alternating currents* if they continually reverse in direction, in a regular periodic manner, flowing first in one direction round the circuit and then in the other.

Continuous currents of electricity are produced by *voltaic cells*, and *batteries* of such cells, or else by *dynamos* driven by power, though there are other sources of currents hereafter to be mentioned. Alternating currents are produced by special alternating current dynamos or *alter-*

nators, and are separately treated of in Art. 534 (p. 548).

171. Discoveries of Galvani and of Volta.—The discovery of electric currents originated with *Galvani*, a physician of Bologna, who, about the year 1786, made a series of curious and important observations upon the convulsive motions produced by the "return-shock" (Art. 29) and other electric discharges upon a frog's leg. He was led by this to the discovery that it was not necessary to use an electric machine to produce these effects, but that a similar convulsive kick was produced in the frog's leg when two dissimilar metals, iron and copper, for example, were placed in contact with a nerve and a muscle respectively, and then brought into contact with each other. Galvani imagined this action to be due to electricity generated by the frog's leg itself. It was, however, proved by *Volta*, Professor in the University of Pavia, that the electricity arose not from the muscle or nerve, but from the contact of the dissimilar metals. When two metals are placed in contact with one another in the air, one becomes positive and the other negative, though the charges are very feeble. Volta, however, proved their reality by two different methods.

172. The Voltaic Pile.—The second of Volta's proofs consisted in showing that when a number of such contacts of dissimilar metals could be arranged so as to add their electrical effects together, those effects were more powerful in proportion to the number of the contacts. With this view he constructed the apparatus known (in honour of the discoverer) as the **Voltaic Pile** (Fig. 104). It is made by placing a pair of disks of zinc and copper in contact with one another, then laying on

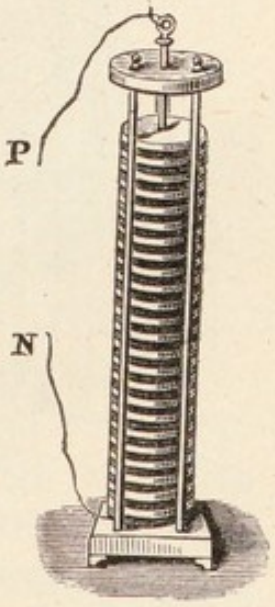


FIG. 104.—Volta's Pile.

the copper disk a piece of flannel or blotting-paper moistened with brine, then another pair of disks of zinc and copper, and so on, each pair of disks in the pile being separated by a moist conductor. Such a *pile*, if composed of a number of such pairs of disks, will produce electricity enough to give quite a perceptible shock, if the top and bottom disks, or wires connected with them, be touched simultaneously with the moist fingers. When a single pair of metals are placed in contact, one becomes + ly electrical to a certain small extent, and the other − ly electrical, or, in other words, there is a certain difference of electric potential (see Art. 283) between them. But when a number are thus set in series with moist conductors between the successive pairs, the difference of potential between the first zinc and the last copper disk is increased in proportion to the number of pairs; for now all the successive small differences of potential are added together.

173. The Crown of Cups.—Another combination devised by Volta was his *Couronne de Tasses* or *Crown of*

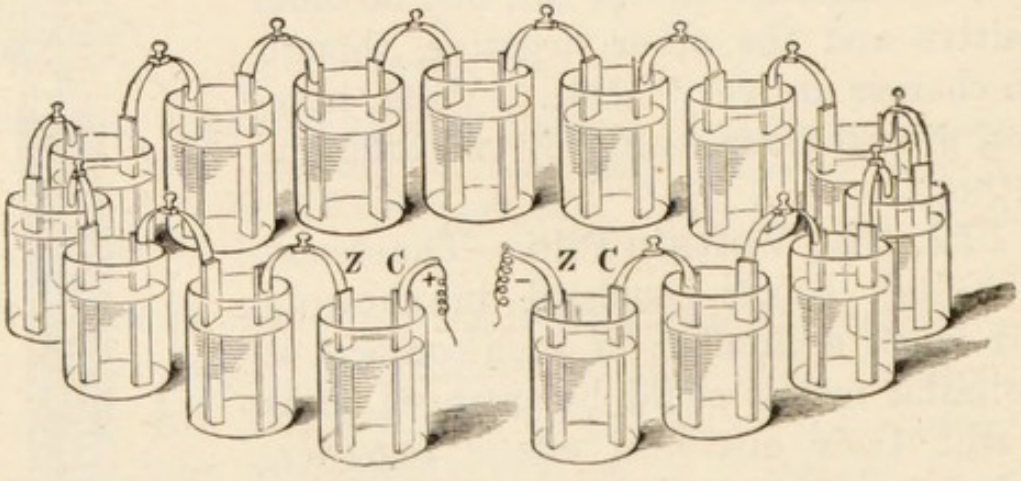


FIG. 105.—Crown of Cups.

Cups. It consisted of a number of cups (Fig. 105), filled either with brine or dilute acid, into which dipped a number of compound strips, half zinc half copper, the zinc portion of one strip dipping into one cup, while the copper portion dipped into the other cup. The

difference of potential between the first and last cups is again proportional to the number of pairs of metal strips. This arrangement, though badly adapted for such a purpose, is powerful enough to ring an electric bell, the wires of which are joined to the first zinc and the last copper strip. The electrical action of these combinations is, however, best understood by studying the phenomena of one single cup or *cell*.

174. Simple Voltaic Cell.—Place in a glass jar some water having a little sulphuric acid or any other oxidizing acid added to it (Fig. 106). Place in it separately two clean strips, one of zinc Z, and one of copper C. This cell is capable of supplying a continuous flow of electricity through a wire whose ends are brought into connexion with the two strips. When the current flows the zinc strip is observed to waste away; its consumption in fact furnishes the energy required to drive the current through the cell and the connecting wire. The cell may therefore be regarded as a sort of chemical furnace in which fuel is consumed to drive the current. The zinc is the fuel,[1] the acid is the aliment, whilst the copper is merely a metallic hand let down into the cell

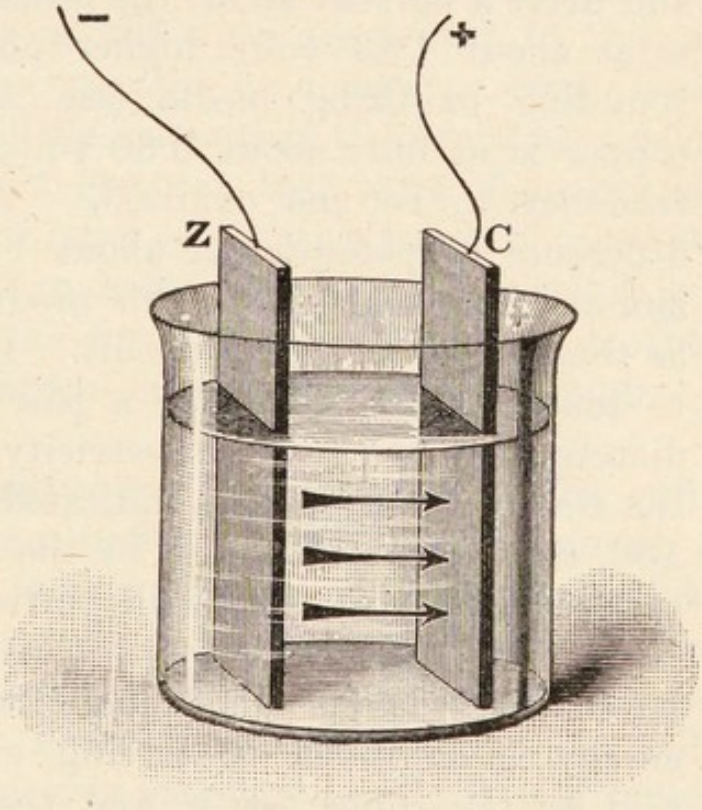


FIG. 106.—Voltaic Cell.

[1] Zinc, as is well known, will burn with a blue flame in air or oxygen, giving out heat. Zinc foil is easily kindled.

to pick up the current, and takes no part chemically. So long as no metallic contact is made with either of the metals no appreciable difference of potential between the copper and the zinc will be observable, even by using a delicate electrometer, because the electrometer merely measures the potential at a point in the air or oxidizing medium outside the zinc or the copper, not the potentials of the metals themselves. The zinc is trying to dissolve and send a current across to the copper; while the copper is trying (less powerfully) to dissolve and drive a current across the other way. The zinc itself is at about 1·83 volts higher potential than the surrounding oxidizing media (see Art. 568); while the copper is at only about 0·80 volts higher, having a less tendency to become oxidized. There is then a latent difference of potential of about 1·03 volts between the zinc and the copper; but this produces no current as long as there is no metallic circuit. If the strips are made to touch, or are joined by a pair of metal wires, immediately there is a rush of electricity through the acid from the zinc to the copper, as indicated by the arrows in Fig. 106, the current returning by the metal circuit from the copper to the zinc. A small portion of the zinc is at the same time dissolved away; the zinc parting with its latent energy as its atoms combine with the acid. This energy is expended in forcing electricity through the acid to the copper strip, and thence through the wire circuit back to the zinc strip. The copper strip, whence the current starts on its journey through the external circuit, is called the *positive pole*, and the zinc strip is called the *negative pole*. If two copper wires are united to the tops of the two strips, though no current flows so long as the wires are kept separate, the wire attached to the zinc will be found to be negative, and that attached to the copper positive, there being still a *tendency* for the zinc to oxidize and drive electricity through the cell from zinc to copper. This state of things is represented

by the + and − signs in Fig. 106; and this distribution of potentials led some to consider the junction of the zinc with the copper wire as the starting point of the current. But the real starting point is in the cell at the surface of the zinc where the chemical action is furnishing energy; for from this point there are propagated through the liquid certain electrochemical actions (more fully explained in Chap. XIII.) which have the result of constantly renewing the difference of potential. At the same time it will be noticed that a few bubbles of hydrogen gas appear on the surface of the copper plate. Both these actions go on as long as the wires are joined to form a complete circuit. The metallic zinc may be considered as a store of energy. We know that if burned as a fuel in oxygen or air it will give out that store of energy as heat. If burned in this quiet chemical manner in a cell it gives out its store not as heat—any heat in a cell is so much waste—but in the form of electric energy, *i.e.* the energy of an electric current propelled by an electromotive-force.

175. Effects produced by Current.—The current itself cannot be *seen* to flow through the wire circuit; hence to prove that any particular cell or combination produces a current requires a knowledge of some of the *effects* which currents can produce. These are of various kinds. (i.) A current flowing through a thin wire will heat it; (ii.) flowing near a magnetic needle it will cause it to turn aside, or circulating in a coil around a rod of iron will magnetize it; (iii.) flowing through water and other liquids it decomposes them; (iv.) and, lastly, flowing through the living body or any sensitive portion of it, it produces certain sensations. These effects, thermal, magnetic, chemical, and physiological, will be considered in special lessons.

176. Voltaic Battery.—If a number of such simple cells are united in series, the zinc plate of one joined to the copper plate of the next, and so on, a greater differ-

ence of potentials will be produced between the copper "pole" at one end of the series and the zinc "pole" at the other end. Hence, when the two poles are joined by a wire there will be a more powerful flow of electricity than one cell would cause. Such a combination of Voltaic Cells is called a Voltaic **Battery**.[1] There are many ways of grouping a battery of cells, but two need special notice. If the cells are joined up in one row, as in Fig. 105 or Fig. 107, they are said to be *in series*.

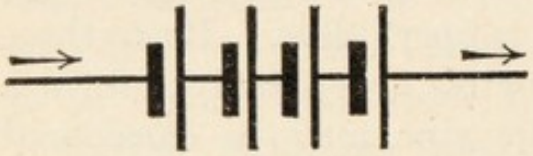


FIG. 107.—Cells in Series.

Electricians often represent a cell by a symbol in which a short thick line stands for the zinc and a longer thin line for the copper (or carbon). Thus Fig. 107 represents four cells joined in series. So joined they can not yield more current (more *amperes*) than a single cell would yield, but they yield that current with a fourfold electromotive-force (*i.e.* with more *volts* of pressure).

The other chief way of grouping cells is to join all the zincs together and all the coppers (or carbons) together; and they are then said to be *in parallel*, or are joined "for quantity." So joined they have no greater electromotive-force than one cell. The zincs act like one big zinc, the coppers like one big copper. But they will yield more current. Fig. 108 shows the four cells grouped *in parallel*;

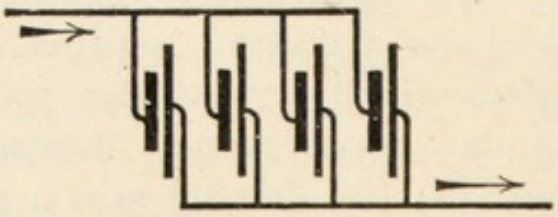


FIG. 108.—Cells in Parallel.

[1] By some writers the name *Galvanic* Battery is given in honour of Galvani; but the honour is certainly Volta's. The electricity that flows thus in currents is sometimes called *Voltaic Electricity*, or *Galvanic Electricity*, or sometimes even *Galvanism* (!), but, as we shall see, it differs only in degree from Frictional or any other Electricity, and both can flow along wires, and magnetize iron, and decompose chemical compounds. The word *Battery* means an arrangement of two or more cells; just as in warfare a battery of guns means an arrangement of two or more guns.

they would yield thus a current four times as great as one cell alone would yield.

177. Electromotive-Force.—The term *electromotive-force* is employed to denote that which moves or tends to move electricity from one place to another.[1] For brevity we sometimes write it E.M.F. In this particular case it is obviously the result of the difference of potential, and proportional to it. Just as in water-pipes a *difference of level* produces a *pressure*, and the pressure produces a *flow* so soon as the tap is turned on, so *difference of potential* produces *electromotive-force*, and electromotive-force sets up a *current* so soon as a circuit is completed for the electricity to flow through. Electromotive-force, therefore, may often be conveniently expressed as a difference of potential, and *vice versâ*; but the student must not forget the distinction. The unit in which electromotive-force is measured is termed the *volt* (see Art. 381). The terms *pressure* and *voltage* are sometimes used for difference of potential or electromotive-force.

178. Volta's Laws.—Volta showed (Art. 80) that the difference of potential between two metals in contact (in air) depended merely on what metals they were, not on their size, nor on the amount of surface in contact. He also showed that when a number of metals touched one another the difference of potential between the first and last of the row is the same as if they touched one another directly. A quantitative illustration from the researches of Ayrton and Perry was given in Art. 81. But the case of a series of cells is different from that of

[1] The beginner must not confuse *Electromotive-force*, or that which tends to move electricity, with *Electric "force,"* or that force with which electricity tends to move charged matter. Newton has virtually defined "force," once for all, as that which moves or tends to move matter. When matter is moved by a magnet we speak rightly of *magnetic force*; when electricity moves matter we may speak of *electric force*. But E.M.F. is quite a different thing, not "force" at all, for it acts on electricity, and tends to make it move round the circuit.

a mere row of metals in contact. If in the row of cells the zincs and coppers are all arranged in one order, so that all of them set up electromotive-forces in the same direction, *the total electromotive-force of the series will be equal to the electromotive-force of one cell multiplied by the number of cells.*

Hitherto we have spoken only of zinc and copper as the materials for a cell; but cells may be made of any two metals. The effective electromotive-force of a cell depends on the *difference* between the two. If zinc were used for both plates in a cell it would give no current, for each plate would be trying to dissolve and to drive a current across to the other with equal tendency. That cell will have the greatest electromotive-force, or be the most "intense," in which those materials are used which have the greatest difference in their tendency to combine chemically with the acid, or which are widest apart on the "contact-series" given in Art. 81 (p. 84). Zinc and copper are convenient in this respect; and zinc and silver would be better but for the expense. For more powerful batteries a zinc-platinum or a zinc-carbon combination is preferable. That plate or piece of metal in a cell by which the current enters the liquid is called the *anode*; it is that plate which dissolves away. The plate or piece of metal by which the current leaves the cell is called the *kathode*; it is not dissolved, and in some cases receives a deposit on its surface.

179. Resistance.—The same electromotive-force does not, however, always produce a current of the same *strength*. The amount of current depends not only on the electromotive-force tending to drive the electricity round the circuit, but also on the **resistance** (see Art. 432) which it has to encounter and overcome in its flow. If the cells be partly choked with sand or sawdust (as is sometimes done in so-called "Sawdust Batteries" to prevent spilling), or, if the wire provided to complete the circuit be very long or very thin, the action will be partly stopped, and the

current will be weaker, although the E.M.F. may be unchanged. The analogy of the water-pipes will again help us. The pressure which forces the water through pipes depends upon the difference of level between the cistern from which the water flows and the tap to which it flows; but the amount of water that runs through will depend not on the pressure alone, but on the resistance it meets with; for, if the pipe be of very small bore, or choked with sand or sawdust, very little water will run through.

Metals in general conduct well: their resistance is small. The *longer* wires are, and the *thinner* they are the more will they resist; thus permitting a smaller current to flow through the circuit. The liquids in the cell do not conduct nearly so well as the metals, and different liquids have different resistances. Pure water will hardly conduct at all, and is for the feeble electromotive-force of the voltaic battery almost a perfect insulator; though for the high-potential electricity of the frictional machines it is, as we have seen, a fair conductor. Salt and sal-ammoniac dissolved in water are good conductors, and so are dilute acids, though strong sulphuric acid is a bad conductor. The resistance of the liquid in the cells may be reduced, if desired, by using larger plates of metal and putting them nearer together. Gases are bad conductors; hence the films of hydrogen gas which are given off at the copper plate during the action of the cell, and which stick to the surface of the copper plate, increase the internal resistance of the cell by diminishing the effective surface of the plates. Some of the rare earths are found to be good conductors when hot. Such an earthy oxide is used in the Nernst lamp (Art. 485).

LESSON XIV.—*Chemical Actions in the Cell*

180. Chemical Actions.—The production of a current of electricity by a voltaic cell is *always* accom-

panied by chemical actions in the cell. One of the metals at least must be readily oxidizable, and the liquid must be one capable of acting on the metal. Zinc and the other metals which stand at the electropositive end of the contact-series (see Art. 81) are oxidizable; whilst the electronegative substances—copper, silver, gold, platinum, and graphite—are less oxidizable, and the last three resist the action of every single acid. There is no proof that their electrical behaviour is due to their chemical properties; nor that their chemical behaviour is due to their electrical properties. Probably both result from a common cause (see Art. 81, and also Art. 568). A piece of quite pure zinc when dipped alone into dilute pure sulphuric acid is not attacked by the liquid. But the ordinary commercial zinc is not pure, and when plunged into dilute sulphuric acid dissolves away, a large quantity of bubbles of hydrogen gas being given off from the surface of the metal. Sulphuric acid is a complex substance, in which every molecule is made up of a group of atoms—2 of Hydrogen, 1 of Sulphur, and 4 of Oxygen; or, in symbols, H_2SO_4. The chemical reaction by which the zinc enters into combination with the radical of the acid, turning out the hydrogen, is expressed in the following equation:—

Zn	+	H_2SO_4	=	$ZnSO_4$	+	H_2
Zinc	and	Sulphuric Acid	produce	Sulphate of Zinc	and	Hydrogen.

The sulphate of zinc produced in this reaction remains in solution in the liquid.

When a plate of pure zinc and a plate of some less easily oxidizable metal—copper or platinum, or, best of all, carbon (the hard carbon from gas retorts)—are put side by side into the cell containing acid, no appreciable chemical action takes place until the circuit is completed by joining the two plates with a wire, or by making them touch one another. Directly the circuit is completed a current flows and the chemical actions begin, the

zinc dissolving in the acid, and the acid giving up its hydrogen in streams of bubbles. But these bubbles of hydrogen are evolved *not* at the zinc plate, nor yet throughout the liquid, but *at the surface of the copper plate* (or the carbon plate if carbon is employed). This invisible transfer of the hydrogen gas through the liquid from the surface of the zinc plate to the surface of the copper plate where it appears is very remarkable. The ingenious theory framed by Grotthuss to account for it is explained in Art. 570 (p. 594).

These chemical actions go on as long as the current passes. The quantity of zinc used up *in each cell* is proportional to the amount of electricity which flows round the circuit while the battery is at work; or, in other words, is proportional to the current. The quantity of hydrogen gas evolved is also proportional to the amount of zinc consumed, and also to the current. After the acid has thus dissolved zinc in it, it will no longer act as a corrosive solvent; it has been "killed," as workmen say, for it has been turned into sulphate of zinc. The battery will cease to act, therefore, either when the zinc has all dissolved away, or when the acid has become exhausted, that is to say, when it is all turned into sulphate of zinc. Stout zinc plates will last a long time, but the acids require to be renewed frequently, the spent liquor being emptied out.

181. Local Action.—When the circuit is not closed the current cannot flow, and there should be no chemical action so long as the battery is producing no current. The impure zinc of commerce does not remain quiescent in the acid, but is continually dissolving and giving off hydrogen bubbles. This **local action**, as it is termed, is explained in the following manner:—The impurities in the zinc consist of particles of iron, arsenic, and other metals. Suppose a particle of iron to be on the surface anywhere and in contact with the acid. It will behave like the copper plate of a battery towards the zinc particles

in its neighbourhood, for a local difference of potential will be set up at the point where there is metallic contact, causing a local or parasitic current to run from the particles of zinc through the acid to the particle of iron, and so there will be a continual wasting of the zinc, both when the battery circuit is closed and when it is open.

182. Amalgamation of Zinc.—We see now why a piece of ordinary commercial zinc is attacked on being placed in acid. There is local action set up all over its surface in consequence of the metallic impurities in it. To do away with this local action, and abolish the wasting of the zinc while the battery is at rest, it is usual to **amalgamate** the surface of the zinc plates with mercury. The surface to be amalgamated should be cleaned by dipping into acid, and then a few drops of mercury should be poured over the surface and rubbed into it with a bit of linen rag tied to a stick. The mercury unites with the zinc at the surface, forming a pasty amalgam. The iron particles do not dissolve in the mercury, but float up to the surface, whence the hydrogen bubbles which may form speedily carry them off. As the zinc in this pasty amalgam dissolves into the acid the film of mercury unites with fresh portions of zinc, and so presents always a clean bright surface to the liquid.

A newer and better process is to add about 4 per cent of mercury to the molten zinc before casting into plates or rods. If the zinc plates of a battery are well amalgamated there should be no evolution of hydrogen bubbles when the circuit is open. Nevertheless there is still always a little wasteful local action during the action of the battery. Jacobi found that while one part of hydrogen was evolved at the kathode, 33·6 parts of zinc were dissolved at the anode, instead of the 32·5 parts which are chemically the equivalent of the hydrogen.

183. Polarization.—The molecules of hydrogen gas liberated at the surface of the copper plate stick to it in

great numbers, and form a film over its surface; hence the effective amount of surface of the copper plate is very seriously reduced in a short time. When a simple cell, or battery of such cells, is set to produce a current, it is found that the current after a few minutes, or even seconds, falls off very greatly, and may even be almost stopped. This immediate falling off in the current, which can be observed with any galvanometer and a pair of zinc and copper plates dipping into acid, is almost entirely due to the film of hydrogen gas sticking to the surface of the copper pole. A battery which is in this condition is said to be "**polarized.**"

184. Effects of Polarization.—The film of hydrogen bubbles affects the strength of the current of the cell in two ways.

First, it weakens the current by the increased *resistance* which it offers to the flow, for films of gas are bad conductors; and, worse than this,

Second, it weakens the current by setting up an opposing *electromotive-force*; for hydrogen is almost as oxidizable a substance as zinc, especially when it is being deposited (or in a "nascent" state), and is electropositive, standing between lead and iron in the series on p. 84. Hence the hydrogen itself produces a difference of potential, which would tend to start a current in the opposite direction to the true zinc-to-copper current. No cell in which the polarization causes a rapid falling off in power can be used for continuous working. It is therefore a very important matter to abolish this polarization, otherwise the current furnished by batteries does not remain constant.

185. Remedies against Internal Polarization.—Various remedies have been practised to reduce or prevent the polarization of cells. These may be classed as mechanical, chemical, and electrochemical.

1. *Mechanical Means.*—If the hydrogen bubbles be simply brushed away from the surface of the kathode,

the resistance they caused will be diminished. If air be blown into the acid solution through a tube, or if the liquid be agitated or kept in constant circulation by siphons, the resistance is also diminished. If the surface be rough or covered with points, the bubbles collect more freely at the points and are quickly carried up to the surface, and so got rid of. This remedy was applied in **Smee's Cell**, which consisted of a zinc and a platinized silver plate dipping into dilute sulphuric acid; the silver plate, having its surface thus covered with a rough coating of finely divided platinum, gave up the hydrogen bubbles freely; nevertheless, in a battery of Smee Cells the current diminishes greatly after a few minutes.

2. *Chemical Means.*—If a highly-oxidizing substance be added to the acid it will destroy the hydrogen bubbles whilst they are still in the nascent state, and thus will prevent both the increased internal resistance and the opposing electromotive-force. Such substances are bichromate of potash, nitric acid, chlorine, and the peroxides.

3. *Electrochemical Means.*—It is possible by employing double cells, as explained in the next lesson, to so arrange matters that some solid metal, such as *copper*, shall be liberated instead of hydrogen bubbles, at the point where the current leaves the liquid. This electrochemical exchange entirely obviates polarization.

186. Simple Laws of Chemical Action in the Cell.—We will conclude this section by enumerating the two simple laws of chemical action in the cell.

I. *The amount of chemical action in the cell is proportional to the quantity of electricity that passes through it*—that is to say, is proportional to *the current* while it passes, and to the *time* during which it is passing.

A current of one ampere flowing through the cell for one second causes 0·00033873 (or $\frac{1}{2952}$) of a gramme of zinc to dissolve in the acid, and liberates 0·00001044 (or $\frac{1}{95785}$) of a gramme of hydrogen. (See Art. 256, p. 239.)

II. In a battery consisting of cells joined in series, *the amounts of chemical action are equal in each cell.*

The first of these laws was thought by Faraday, who discovered it, to disprove Volta's contact theory. He foresaw that the principle of the conservation of energy would preclude a mere contact force from furnishing a continuous supply of current, and hence ascribed the current to the chemical actions which were proportional in quantity to it. How the views of Volta and Faraday are to be harmonized has been indicated in the last paragraph of Art. 81. These laws relate only to the useful chemical action, and do not include the waste by "local" actions (Art. 181) due to parasitic currents set up by impurities.

LESSON XV.—*Voltaic Cells*

187. A good Voltaic cell should fulfil all or most of the following conditions :—

1. Its electromotive-force should be high and constant.
2. Its internal resistance should be small.
3. It should give a constant current, and therefore must be free from polarization, and not liable to rapid exhaustion, requiring frequent renewal of the acid.
4. It should be perfectly quiescent when the circuit is open.
5. It should be cheap and of durable materials.
6. It should be manageable, and, if possible, should not emit corrosive fumes.

No single cell fulfils all these conditions, however, and some cells are better for one purpose and some for another. Thus, for telegraphing through a long line of wire a considerable internal resistance in the battery is no great disadvantage; while, for producing an electric arc, much internal resistance is absolutely fatal. The

electromotive-force of a battery depends on the materials of the cell, and on the number of cells linked together; a high E.M.F. can therefore be gained by choosing the right substances and by taking a large number of cells. The resistance within the cell can be diminished by increasing the size of the plates, by bringing them near together, so that the thickness of the liquid between them may be as small as possible, and by choosing liquids that are good conductors. Cells are sometimes classified into two groups, according as they contain one or two fluids, or electrolytes, but a better classification is that adopted in Art. 185, depending on the means of preventing polarization.

188. Cells of Class I.—With Mechanical Depolarization

The simple cell of Volta, with its zinc and copper plates, has been already described. The larger the copper plate, the longer the time which it takes to polarize. Cruickshank suggested to place the plates vertically in a trough, producing a more powerful combination. Dr. Wollaston proposed to use a plate of copper of double size, bent round so as to approach the zinc on both sides, thus diminishing the resistance, and allowing the hydrogen more surface to deposit upon. Smee, as we have seen, replaced the copper plate by platinized silver, and Walker suggested the use of plates of hard carbon instead of copper or silver, thereby saving cost, and at the same time increasing the electromotive-force. The roughness of the surface facilitates the escape of hydrogen bubbles. By agitating such cells, or raising their kathode plates for a few moments into the air, their power is partially restored. The Law cell, used in the United States for open-circuit work, is of this class: it has a small rod of zinc and a cleft cylinder of carbon of large surface immersed in a solution of sal-ammoniac.

189. Cells of Class II.—With Chemical Depolarization

In these cells, in addition to the dilute acid or other *excitant* to dissolve the zinc, there is added some more powerful chemical agent as a *depolarizer.* Amongst depolarizers the following are used :—Nitric acid, solutions of chromic acid, bichromate of potash, bichromate of soda, nitrate of potash, or ferric chloride ; chlorine ; black oxide of manganese, sulphur, peroxide of lead, red lead, oxide of copper. Most of these materials would, however, attack the copper as well as the zinc if used in a zinc-copper cell. Hence they can only be made use of in zinc-carbon or zinc-platinum cells. Nitric acid also attacks zinc when the circuit is open. Hence it cannot be employed in the same single cell with the zinc plate. In the **Bichromate Cell**, invented by Poggendorff, bichromate of potash is added to the sulphuric acid. This cell is most conveniently made up as shown in Fig. 109, in which a plate of zinc is the anode, and a pair of carbon plates, one on each side of the zinc, joined together at the top serve as a kathode. As this solution would attack the zinc even when the circuit is open, the zinc plate is fixed to a rod by which it can be drawn up out of the solution when the cell is not being worked.

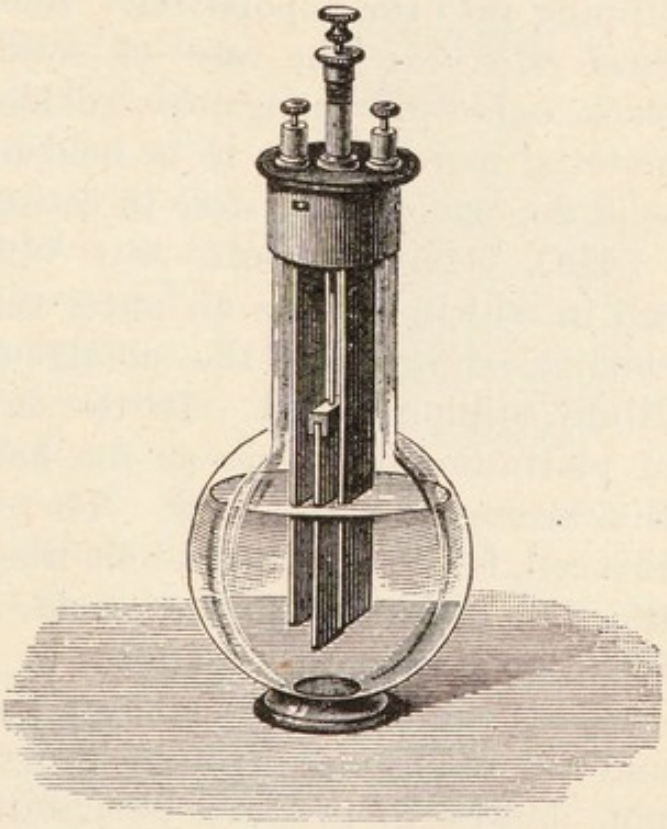


FIG. 109.—Bichromate Cell.

To obviate the necessity of this operation the device is adopted of separating the depolarizer from the excitant liquid into which the zinc dips. In the case of liquid depolarizers this is done by the use of an internal *porous cell* or partition. Porous cells of earthenware or of parchment paper allow the electric current to flow while keeping the liquids apart. In one compartment is the zinc anode dipping into its aliment of dilute acid : in the other compartment the carbon (or platinum) kathode dipping into the depolarizer. Such cells are termed *two-fluid cells.* In the case of solid depolarizers such as black oxide of manganese, oxide of copper, etc., the material merely needs to be held up to the kathode. All solid depolarizers are *slow* in acting.

190. Grove's Cell.—Sir William Grove devised a cell in which there is an outer cell of glazed ware or of ebonite, containing the amalgamated zinc plate and dilute sulphuric acid. In the inner porous cell a piece of platinum foil serves as the kathode, and it dips into the strongest nitric acid. There is no polarization in this cell, for the hydrogen ions liberated by the solution of the zinc in dilute sulphuric acid, in passing through the nitric acid in order to appear at the platinum pole, decompose the nitric acid and are oxidized, producing water and the red fumes of nitric peroxide gas. This gas does not, however, produce polarization, for as it is very soluble, it does not form a film upon the face of the platinum plate, nor does it, like hydrogen, set up an opposing electromotive-force with the zinc. Grove cells may be made of a flat shape, the zinc being bent up so as to embrace the flat porous cell on both sides. This reduces the internal resistance, which is already small on account of the good conducting powers of nitric acid. A Grove's cell will furnish for three or four hours continuously a current of 12 to 15 amperes. The E.M.F. of one cell is about 1·9 volts, and its internal resistance is very low (about 0·1 ohm for the quart size). A single

cell will readily raise to a bright red heat two or three inches of thin platinum wire. Years ago, to produce an arc light, it was usual to employ a battery of fifty Grove's cells joined in series, the platinum of one cell being clamped to the zinc of the cell next to it.

191. Bunsen's Cell.—The cell which bears Bunsen's name is a modification of that of Grove. In the Bunsen cell the expensive[1] platinum foil is replaced by a rod or slab of hard gas carbon. A cylindrical form of cell, with a rod of carbon is shown in Fig. 110. The voltage for a zinc-carbon combination is a little higher than for a zinc-platinum one, which is an advantage; but the Bunsen cell is troublesome to keep in order, and there is some difficulty in making a good contact between the rough surface of the carbon and the copper strap which connects the carbon of one cell to the zinc of the next. The top

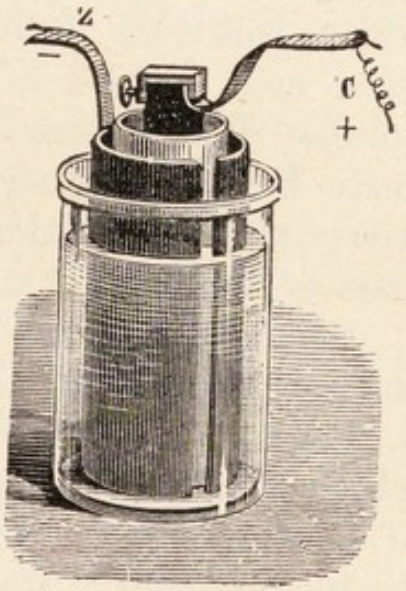


FIG. 110.—Bunsen Cell.

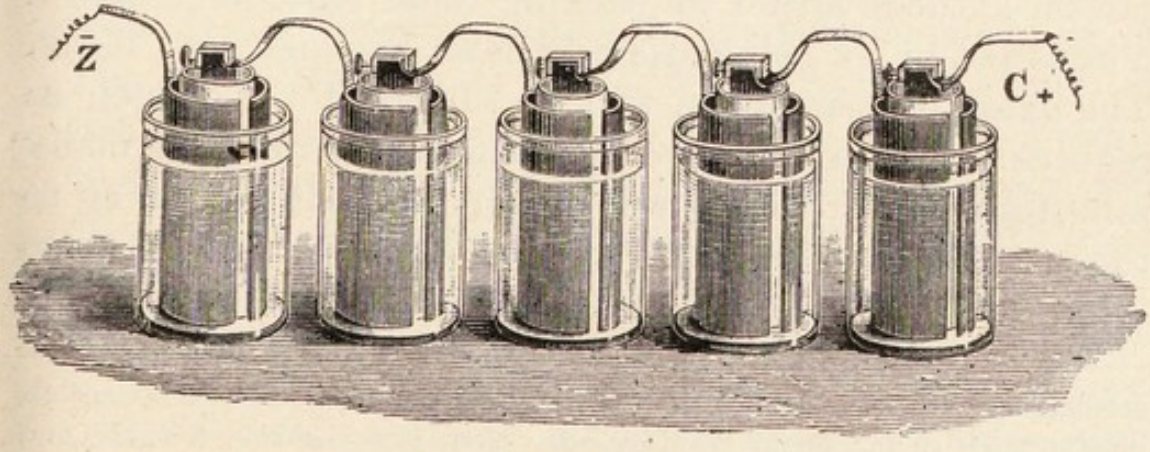


FIG. 111.—Battery of Five Bunsen Cells in Series.

part of the carbon is sometimes impregnated with paraffin

[1] Platinum costs about 240 shillings an ounce—nearly thrice as much as gold; while a hundredweight of the gas carbon may be had for a mere trifle, often for nothing more than the cost of carrying it from the gasworks. An

wax to keep the acid from creeping up, and electrotyped with copper. Fig. 111 shows the usual way of coupling up a series of five such cells. Bunsen's battery will continue to furnish a current for a longer time than the flat Grove's cells, on account of the larger quantity of acid contained by the cylindrical pots.[1]

Chromic solutions, formed by adding strong sulphuric acid to solutions of bichromate of potash or of soda, are often used instead of nitric acid, in cells of this form. Soluble depolarizers in the form of chromic powders are made by heating strong sulphuric acid and gradually stirring into it powdered bichromate of soda. The pasty mass is then cooled and powdered.

192. Leclanché's Cell.—For working electric bells and telephones, and also to a limited extent in telegraphy, a zinc-carbon cell invented by Leclanché is employed, in which the exciting liquid is not dilute acid, but a solution of sal-ammoniac. In this the zinc dissolves, forming a double chloride of zinc and ammonia, while ammonia gas and hydrogen are liberated at the carbon pole. The depolarizer is the black dioxide of manganese, fragments of which, mixed with powdered carbon, are held up to the carbon kathode either by packing them together inside a porous pot or by being attached as an agglomerated block. The oxide of manganese will slowly yield up oxygen as required. If used to give a continuous current for many minutes together, the power of this cell falls off owing to the accumulation of the hydrogen bubbles; but if left to itself for a time the cell recovers itself, the dioxide

artificial carbon prepared by grinding up gas carbon with some carbonaceous matter such as tar, sugar residues, etc., then pressing into moulds, and baking in a furnace, is used both for battery plates and for the carbon rods used in arc lamps.

[1] Callan constructed a large battery in which *cast iron* formed the positive pole, being immersed in strong nitric acid, the zincs dipping into dilute acid. The iron under these circumstances is not acted upon by the acid, but assumes a so-called "passive" state. In this condition its surface appears to be impregnated with a film of magnetic peroxide, or of oxygen.

gradually destroying the polarization. As the cell is in other respects perfectly constant, and does not require renewing for months or years, it is well adapted for domestic purposes. It has the advantage of not containing corrosive acids. Millions of these cells are in use on "open-circuit" service—that is to say, for those cases in which the current is only required for a few moments at a time, and the circuit usually left open. Three

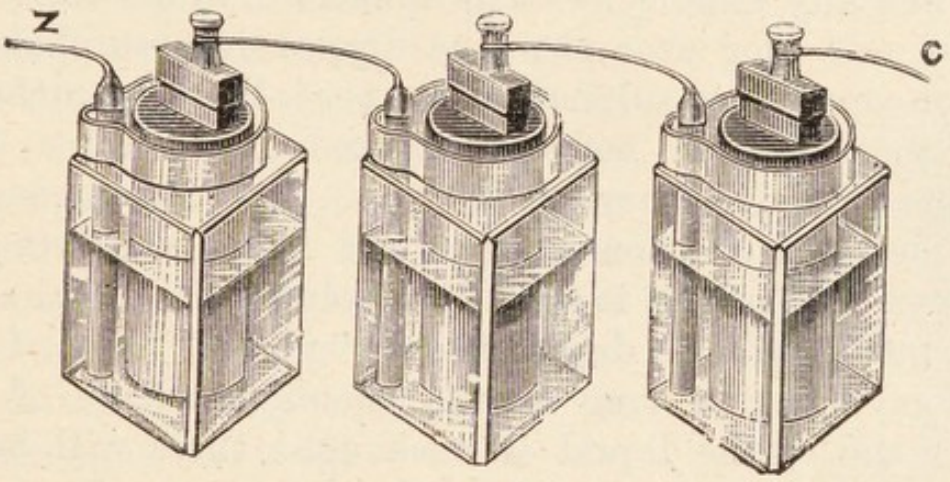


FIG. 112.—Battery of three Leclanché Cells in Series.

Leclanché cells are shown joined in series, in Fig. 112. Common salt may be used instead of sal-ammoniac.

193. Dry Cells.—This name is given to modifications of the Leclanché cell in which the excitant cannot be spilled. The space between the zinc, which forms the case, and the interior depolarizing mass is filled up with a porous or gelatinous paste of sawdust, paper-pulp, or flour, often mixed with plaster of Paris, and impregnated with a solution of sal-ammoniac, with a little chloride of zinc to keep the mass moist, then covered with a layer of pitch or bitumen. The chemical action is the same as in the Leclanché cell, and the voltage is about 1·4 volts, slowly falling as the cell is used.

194. Lalande's Cell.—The anode is zinc, and the exciting liquid is a 30 per cent solution of caustic potash into which the zinc dissolves (forming zincate of potash), whilst the kathode consists of a compressed cake of the

red oxide of copper which becomes gradually reduced to metallic copper. It is mechanically held to a frame of copper or iron. The cell has only 0·8 to 0·9 volts of E.M.F., but is capable of yielding a large and constant current.

195. Cells of Class III.—With Electrochemical Depolarization

When any soluble metal is immersed in a solution of its own salt—for example, zinc dipped into sulphate of zinc, or copper into sulphate of copper—there is a definite electromotive-force between it and its solution, the measure of its tendency to dissolve. If a current is sent from metal to solution some of the metal dissolves; if, however, the current is sent from solution to metal some more metal will be deposited (or "plated") out of the solution. But as long as the chemical nature of the surface and of the liquid is unchanged there will be no change in the electromotive-force at the surface. It follows that if a cell were made with two metals, each dipping into a solution of its own salt, the two solutions being kept apart by a porous partition, such a cell would never change its electromotive-force. The anode would not polarize where it dissolves into the excitant; the kathode would not polarize, since it receives merely an additional thickness of the same sort as itself. This electrochemical method of avoiding polarization was discovered by Daniell. It is the principle not only of the Daniell cell, but of the Clark cell and of others. For perfect constancy the two salts used should be salts of the same acid, both sulphates, or both chlorides, for example.

196. Daniell's Cell.—An element of a Daniell's battery (Fig. 113) consists of an outer cell, usually of copper, which serves as kathode, and an inner cylindrical cell of unglazed porous ware (a cell of parchment, or even of brown paper, will answer), within which is placed a rod of amalgamated zinc as anode. The liquid in the

inner cell is dilute sulphuric acid or dilute sulphate of zinc; that in the outer cell is a saturated solution of sulphate of copper ("blue vitriol"), some spare crystals of the same substance being contained in a perforated shelf at the top of the cell, in order that they may dissolve and replace that which is used up while the battery is in action.

When the circuit is closed the zinc dissolves in the dilute acid, forming sulphate of zinc, and liberating hydrogen; but this gas does *not* appear in bubbles on the surface of the copper cell, for, since the inner cell is porous, the molecular actions (by which the freed atoms of hydrogen are, as explained by Fig. 336, handed on through the acid) traverse the pores of the inner cell, and there, in the solution of sulphate of copper, the hydrogen atoms are exchanged for copper atoms, the result being that pure copper, and not hydrogen gas, is deposited on the outer common plate. Chemically these actions may be represented as taking place in two stages.

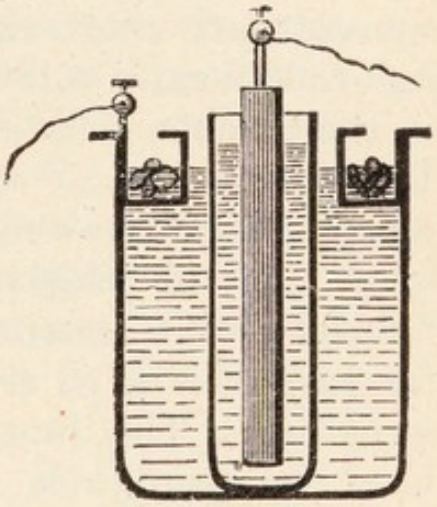


FIG. 113.—Daniell's Cell.

$$Zn + H_2SO_4 = ZnSO_4 + H_2$$

Zinc and Sulphuric Acid produce Sulphate of Zinc and Hydrogen.

And then

$$H_2 + CuSO_4 = H_2SO_4 + Cu.$$

Hydrogen and Sulphate of Copper produce Sulphuric Acid and Copper.

The hydrogen is, as it were, translated electrochemically into copper during the round of changes, and so while the zinc dissolves away the copper grows, the dilute sulphuric acid gradually changing into sulphate of zinc, and the sulphate of copper into sulphuric acid. In the case in which a solution of sulphate of zinc is used

there is no need to consider any hydrogen atoms, copper being exchanged chemically for zinc. There is therefore no polarization so long as the copper solution is saturated; and the cell is very constant, though not so constant in all cases as Clark's standard cell described in Art. 200, owing to slight variations in the electromotive-force as the composition of the other fluid varies. When sulphuric acid diluted with twelve parts of water is used the E.M.F. is 1·178 volts. The E.M.F. is 1·07 volts when concentrated zinc sulphate is used; 1·1 volts when a half-concentrated solution of zinc sulphate is used; and, in the common cells made up with water or dilute acid, 1·1 volts or less. Owing to its constancy, this battery, made up in a convenient flat form (Fig. 116), has been much used in telegraphy. It is indispensable in those "closed circuit" methods of telegraphy (Art. 583), where the current is kept always flowing until interrupted by signalling. The function of the porous partition is to keep the two fluids from mixing; for the solution of sulphate of copper must not be allowed to come into contact with the zinc, otherwise there would be deleterious local action.

197. De la Rue's Battery.—De la Rue constructed a constant cell belonging to Class III., in which zinc and silver are the two metals, the zinc being immersed in chloride of zinc, and the silver embedded in a stick of fused chloride of silver. As the zinc dissolves away, metallic silver is deposited upon the kathode, just as the copper is in the Daniell's cell. De la Rue constructed an enormous battery of over 11,000 little cells. The difference of potential between the first zinc and last silver of this battery was over 11,000 volts.

198. Gravity Cells.—Instead of employing a porous cell to keep the two liquids separate, it is possible, where one of the liquids is heavier than the other, to arrange that the heavier liquid shall form a stratum at the bottom of the cell, the lighter floating upon it. Such arrange-

ments are called *gravity cells*; but the separation is never perfect, the heavy liquid slowly diffusing upwards. Daniell's cells arranged as gravity cells have been contrived by Meidinger, Minotto, Callaud, and Lord Kelvin.

199. Effect of Heat on Cells. — If a cell be warmed it yields a stronger current than when cold. This is chiefly due to the fact that the liquids conduct better when warm, the internal resistance being thereby reduced. A change is also observed in the E.M.F. on heating; thus the E.M.F. of a Daniell's cell is about $1\frac{1}{2}$ per cent higher when warmed to the temperature of boiling water, while that of a bichromate battery falls off nearly 2 per cent under similar circumstances.

200. Standard Cells.—For purposes of standardization and testing a cell is required the E.M.F. of which is constant and independent of all local conditions. A form of Daniell's cell designed by Fleming answers this purpose for ordinary use. A standard cell whose E.M.F. is even more constant than that of the Daniell was suggested by Latimer Clark. The **Clark Cell**, which was at one time adopted as the international standard, consists of an anode of pure zinc in a concentrated solution of zinc-sulphate, whilst the kathode is of pure mercury in contact with a paste of mercurous sulphate. Fig. 114 shows, *in actual size*, the form of the Clark cell. Its E.M.F. is 1·434 volts at 14° C., but it drops slightly if the temperature rises. Its E.M.F., at any temperature of θ° C., may be calculated by the formula

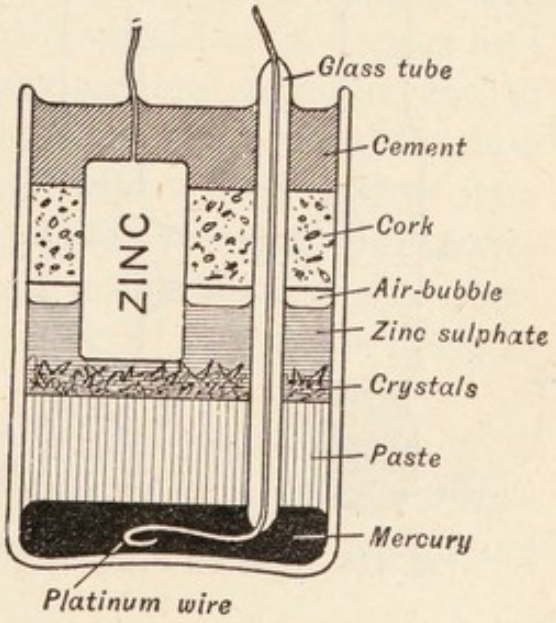


FIG. 114.—Clark Standard Cell.

$$\text{E.M.F.} = 1{\cdot}434\ [1 - 0{\cdot}00077\ (\theta^\circ - 14)] \text{ volt.}$$

Lord Rayleigh suggested a modification known as the "H-form," in which the materials are contained in a glass vessel in the form of the letter H. Zinc amalgam is contained in one limb, and the mercury and mercurous sulphate in the other; the whole being filled with a saturated zinc sulphate solution. One electrode is introduced through the bottom of each limb. This type of cell has the advantage that the position of the electrodes is definitely fixed so that there is no liability to local action. Von Helmholtz proposed to substitute mercurous chloride (calomel) and zinc chloride, in place of sulphates, but the combination has no advantages.

201. The Weston Normal Cell.—This cell resembles the Clark, save in having cadmium instead of zinc. Fig. 115 shows it as made up in the H-pattern. One limb contains cadmium amalgam, the other mercury covered with a paste of mercurous sulphate. The whole is filled with a solution of cadmium sulphate kept saturated by inserting in each limb some crystals of cadmium sulphate which crust together and form as it were plugs below the constrictions of the tubes. Its E.M.F. is 1·0183 volts at 20° C. The voltage falls by 0·00004 for a temperature rise of one centigrade degree.

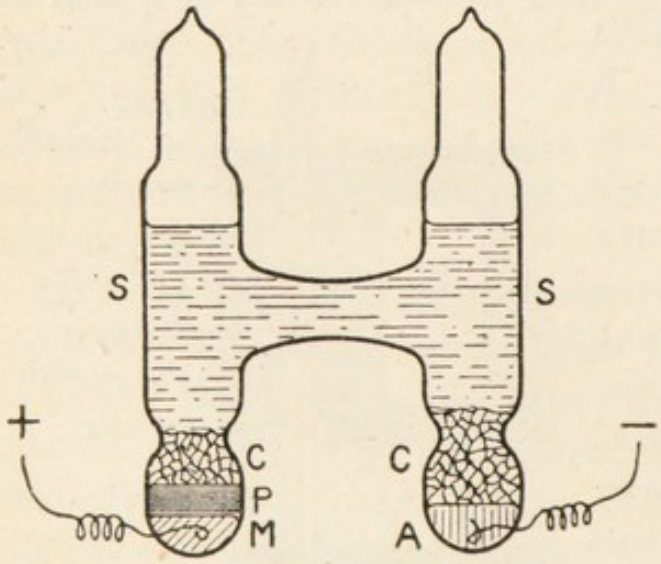


FIG. 115.—Weston Normal Cell.

Within the range 0° to 40° C., the E.M.F. at temperature t° C., is:—

$$E_t = E_{20} - 0{\cdot}0000406(t-20) - \{9{\cdot}5 \times 10^{-7}(t-20)^2\}.$$

202. Other Cells. — Numerous other forms of

battery have been suggested by different electricians. There are three, of theoretical interest only, in which, instead of using two metals in one liquid which attacks them unequally, two liquids are used having unequal chemical action on the metal. In these there is no contact of dissimilar metals. The first of these was invented by Napoleon III. Both plates were of copper dipping respectively into solutions of dilute sulphuric acid and of cyanide of potassium, separated by a porous cell. The second of these combinations, due to Wöhler, employs plates of aluminium only, dipping respectively into strong nitric acid and a solution of caustic soda. In the third, invented by Dr. Fleming, the two liquids do not even touch one another, being joined together by a second metal. In this case the liquids chosen are sodium persulphide and nitric acid, and the two metals copper and lead. A similar battery might be made with copper and zinc, using solutions of ordinary sodium sulphide and of dilute sulphuric acid in alternate cells, a bent zinc plate dipping into the first and second cells, a bent copper plate dipping into second and third, and so on; for the electromotive-force of a copper sodium-sulphide zinc combination is in the reverse direction to that of a copper sulphuric-acid zinc combination.

The Fitch cell, used in the United States, is a zinc-carbon cell with an excitant composed of sal-ammoniac solution to which the chlorates of potash and soda have been added to deplorize.

Jablochkoff described a battery in which plates of carbon and iron are placed in fused nitre; the carbon is here the electropositive element, being rapidly consumed in the liquid.

Planté's and Faure's *Secondary Batteries*, and Grove's *Gas Battery*, are described in Arts. 572, 574.

203. Zamboni's Dry Pile.—The so-called **Dry Pile** of Zamboni consists of a number of paper disks, coated with zinc-foil on the side and with dioxide of manganese

on the other, piled up on one another, to the number of some thousands, in a glass tube. Its internal resistance is enormous, as the internal conductor is the moisture of the paper, and this is slight; but its electromotive-force is very great, and a good dry pile will yield sparks. Many years may elapse before the zinc is completely oxidized or the manganese exhausted. In the Clarendon Laboratory at Oxford there is a dry pile, the poles of which are two metal bells: between them is hung a small brass ball, which, by oscillating to and fro, slowly discharges the electrification. It has now been continuously ringing the bells since the year 1842.

204. Statistics of Cells.—The following table gives the electromotive-forces of the various batteries enumerated:

Name.	Anode.	Excitant.	Depolarizer.	Kathode.	Approximate Volts.
Class I.		(Solution of)			
Volta (Wollaston, etc.).	Zinc	H_2SO_4	none	Copper	1·0 to 0·5
Smee . . .	Zinc	H_2SO_4	none	Platinized silver	1·0 to 0·5
Law . . .	Zinc	NH_4Cl	none	Carbon	1·0 to 0·5
Class II.					
Poggendorff (Grenet, Fuller, etc.).	Zinc	H_2SO_4	$K_2Cr_2O_7$	Carbon	2·0
Grove . . .	Zinc	H_2SO_4	HNO_3	Platinum	1·9
Bunsen . . .	Zinc	H_2SO_4	HNO_3	Carbon	1·9
Leclanché . .	Zinc	NH_4Cl	MnO_2	Carbon	1·4
Lalande . . .	Zinc	KHO	CuO	Carbon	0·8
Fitch . . .	Zinc	NH_4Cl	$KClO_3$+ $NaClO_3$	Carbon	1·1
Class III.					
Daniell (Meidinger, Minotto, etc.).	Zinc	$ZnSO_4$	$CuSO_4$	Copper	1·07
De la Rue . .	Zinc	$ZnCl_2$	AgCl	Silver	1·42
Marié Davy . .	Zinc	$ZnSO_4$	Hg_2SO_4	Carbon	1·4
Von Helmholtz .	Zinc	$ZnCl_2$	Hg_2Cl_2	Mercury	1·0
Clark (Standard) .	Zinc	$ZnSO_4$	Hg_2SO_4	Mercury	1·434
Weston (Standard)	Cadmium	$CdSO_4$	Hg_2SO_4	Mercury	1·0183
Class IV.					
Accumulators.					
(Planté, Faure, etc.)	Lead	H_2SO_4	PbO_2	Lead	2·1 to 1·85
Edison . . .	Iron	KHO	NiO	Steel	1·35 to 1·25

The E.M.F. of the single-fluid cells of Volta and Smee is marked in the table as doubtful, for the opposing E.M.F. of polarization sets in almost before the true E.M.F. of the cell can be measured. The different values assigned to other cells are accounted for by the different degrees of concentration of the liquids. Thus in the Daniell's cells used in telegraphy, *water* only is supplied at first in the cells containing the zincs; and the E.M.F. of these is less than if acid or sulphate of zinc were added to the water.

205. Strength of Current.—The definition of the **strength** of a current is as follows: *The strength of a current is the quantity of electricity which flows past any point of the circuit in one second.*[1] Suppose that at the end of 10 seconds 25 *coulombs* of electricity have passed through a circuit, then the average current during that time has been $2\frac{1}{2}$ *coulombs per second*, or $2\frac{1}{2}$ *amperes*. The usual currents employed in telegraphing over main lines are only from five to ten thousandths of an *ampere*.

If in t seconds a quantity of electricity Q has flowed through the circuit, then the average current i during that time is represented by the equation

$$i = \frac{Q}{t}.$$

This should be compared with Art. 169.

The student must remember that the strength of current which the various batteries will yield depends (Art. 179) on the internal *resistance* of the cells and on that of their circuit, as well as on their E.M.F. The E.M.F. of a cell is independent of its size, and is determined solely by the materials chosen and their condition. The resistance depends on the size of the cell, the conducting qualities of the liquid, the thickness of the liquid which the current must traverse, etc.

[1] The phrases "strength of current," "intensity of current," "quantity of current," are old-fashioned, and mean no more than "current" means —that is to say, the number of *amperes* that are flowing.

The *internal resistance* of cells varies greatly. The maximum current which a cell will give *on short-circuit* through a stout wire, or when short-circuited by an amperemeter, can be found by dividing the E.M.F. by the internal resistance, as in the following cases :—

Name.	E.M.F. (*volts*).	Internal Resistance. (*ohms*) (approximately).	Current on Short-circuit. (*amperes*).
Bichromate .	2·0	0·2	10
Grove } Bunsen } .	1·9.	0·15	12·6
Leclanché .	1·4	0·5	2·8
Lalande . .	0·8	0·1	8·0
Gassner (dry) .	1·4	0·2	7·0
Daniell . .	1·07	1·0	1·07

206. Ohm's Law.—The laws which determine the strength or quantity of a current in a circuit were first enunciated by Dr. G. S. Ohm, who stated them in the following law :—*The current varies directly as the electromotive-force, and inversely as the resistance of the circuit*; or, in other words, anything that makes the E.M.F. of the cell greater will increase the current, while anything that increases the resistance (either the internal resistance in the cells themselves or the resistance of the external wires of the circuit) will diminish the current.

In symbols this becomes

$$\frac{E}{R} = i,$$

where E is the number of *volts*, R the number of *ohms* of the circuit, and *i* the number of *amperes* of current.

Example.—To find the current that can be sent through a resistance of 5 *ohms* by an E.M.F. of 20 *volts*. $20 \div 5 = 4$ *amperes*.

(See further concerning Ohm's Law in Lesson XXXIII., p. 425.) Ohm's Law says nothing about the energy or

power conveyed by a current. The *power* of a current is proportional both to the current and to the electromotive-force which drives it (see Art. 454).

207. Resistance and Grouping of Cells.—The internal resistances of the cells we have named differ very greatly, and differ with their size. Broadly speaking, we may say that the resistance in a Daniell's cell is about five times that in a Grove's cell of equal size. The Grove's cell has indeed both a higher E.M.F. and less internal resistance. It would in fact send a current about eight times as strong as the Daniell's cell of equal size through

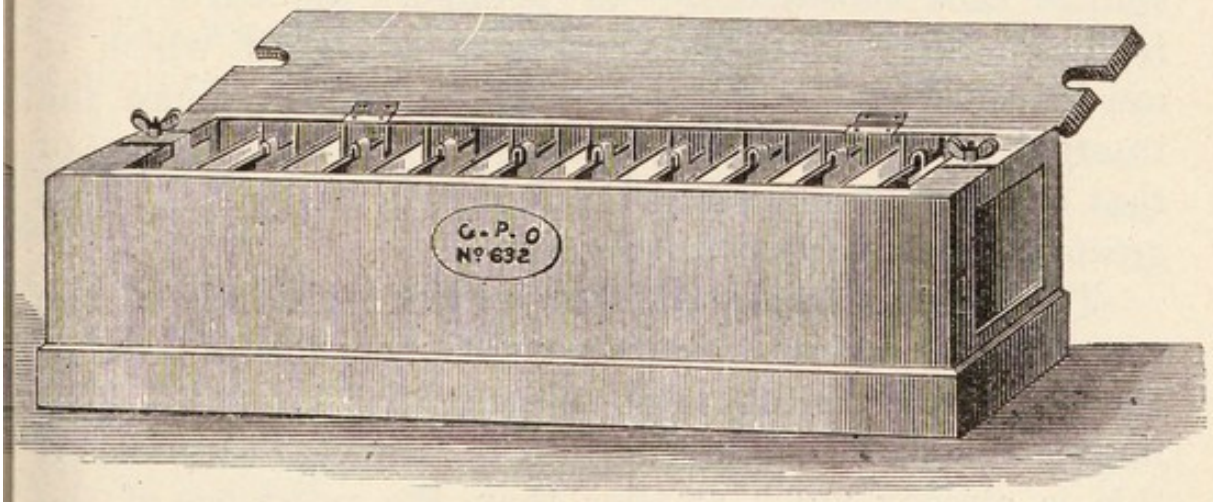


FIG. 116.—Battery of Ten Daniell Cells in Series.

a short stout wire of negligible resistance. The Lalande cell has a remarkably small internal resistance.

We may then increase the strength of a battery in two ways:

(1) By increasing its E.M.F.

(2) By diminishing its internal resistance.

The electromotive-force of a cell being determined by the materials of which it is made, the only way to increase the total E.M.F. of a battery of given materials is to increase the number of cells joined "in series." It is frequent in the telegraph service to link thus together two or three hundred of the flat Daniell's cells; and they are usually made up in trough-like boxes, containing a series of 10 cells, as shown in Fig. 116.

To diminish the internal resistance of a cell the following expedients may be resorted to :

(1) The plates may be brought nearer together, so that the current shall not have to traverse so thick a stratum of liquid.

(2) The size of the plates may be increased, as this affords the current, as it were, a greater number of possible paths through the stratum of liquid.

(3) The zincs of several cells may be joined together, to form, as it were, one large zinc plate ; the coppers being also joined to act as one large copper plate. Suppose four similar cells thus joined "in parallel," the current has four times the available number of paths by which it can traverse the liquid from zinc to copper ; hence the internal resistance of the whole group will be only $\frac{1}{4}$ of that of a single cell. But the E.M.F. of them will be no greater thus than that of one cell.

The current is also affected by the resistances of the wires of the *external* circuit ; and if the external resistance be already great, as in telegraphing through a long line, it is of little use to diminish the internal resistance if this is already much smaller than the resistance of the line wire. It is, on the contrary, advantageous to increase the number of cells in series, though every cell adds a little to the total resistance.

Example.—If the line has a resistance of 1000 *ohms*, and five cells are used each of which has an E.M.F. of 1·1 *volt* and an internal resistance of 3 *ohms*, by Ohm's Law the current will be $5{\cdot}5 \div 1015$; or 0·0054 *ampere*. If now eight cells in series are used, though the total resistance is thereby increased from 1015 to 1024 *ohms*, yet the E.M.F. is increased from 5·5 to 8·8 *volts*, and the current to 0·0085 *ampere*.

208. Keys, Switches, and Reversers.—Various forms of *keys* and *switches* are used for making and breaking the connection of a battery to a circuit. A **key** is an appliance consisting essentially of a lever carrying a contact or contacts, generally used in signalling

and in testing. It is not advisable to leave a battery supplying current longer than the period of actual use because of the rapid action of polarization (Art. 183). The simplest key (shown in Fig. 144, p. 223) consists of a brass arm fixed at one end, the other end being sprung so as not to make circuit with a contact placed underneath. On depressing the arm the circuit is made, while in its normal position it is broken. The Morse key (Fig. 343) is a lever, held up by a spring, which on depressing disconnects receiving instruments and transmits current to the line. **A plug switch** consists of two contacts separated by a small space which can be connected by the insertion of a plug. **A circuit breaker** (Art. 561) is a switch which is opened automatically when the current or the pressure exceeds (or falls below) a certain limit.

It is sometimes necessary to reverse the direction of the current in a circuit when carrying out special tests (*e.g.* Art. 393 *b*). One form of **reverser** operating with a rotary motion is depicted in Fig. 152. Another form consists of a rocking contact piece, operating in mercury cups, which either connects the battery direct to the circuit or cross-connects it according to the position of the rocking contacts.

LESSON XVI.—*Magnetic Actions of the Current*

209. Oersted's Discovery.—A connexion of some kind between magnetism and electricity had long been suspected. Lightning had been known to magnetize knives and other objects of steel; but almost all attempts to imitate these effects by powerful charges of electricity, or by sending currents of electricity through steel bars, had failed.[1] About 1802 Romagnosi, of Trente, vaguely

[1] Hitherto in these lessons magnetism and electricity have been considered separately; no connexion between them has been apparent. The student who cannot remember whether a *charge* of electricity does or does not affect a magnet, should turn back to what was said in Art. 102, p. 98.

observed that a voltaic pile affects a compass-needle. The true connexion between magnetism and electricity remained, however, to be discovered.

In 1819, Oersted, of Copenhagen, showed that a magnet needle tends to set itself at right angles to a wire carrying an electric current. He also found that the way in which the needle turns, whether to the right or the left of its usual position, depends upon the position of the wire that carries the current—whether it is above or below the needle—and on the direction in which the current flows through the wire.

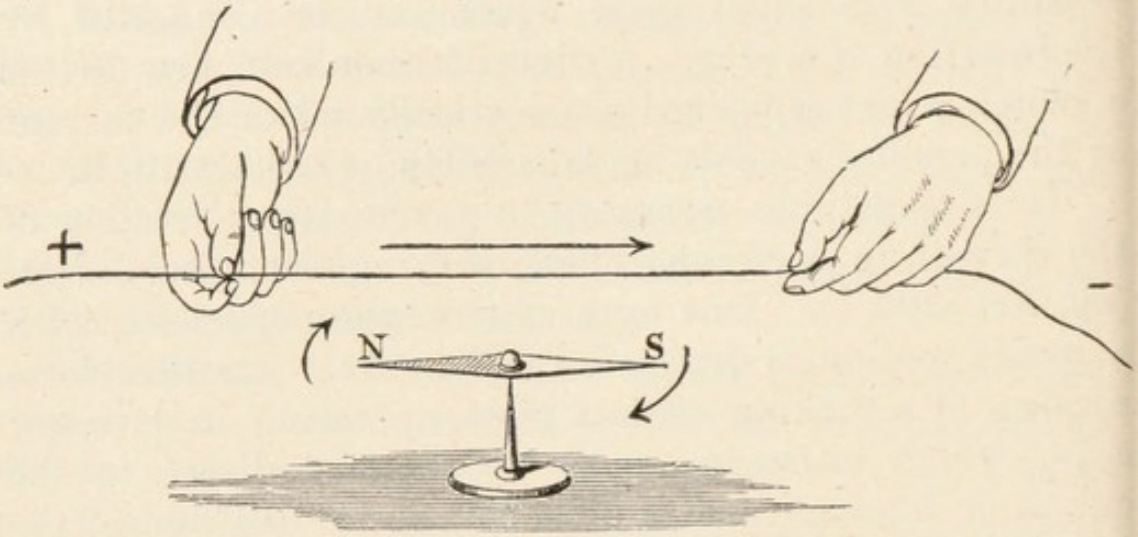


FIG. 117.—Oersted's Experiment: Deflexion of Needle by Current.

His chief experiment is this:—Let a magnetic needle be suspended on a pointed pivot, as in Fig. 117. Above it, and parallel to it, is held a stout copper wire, one end of which is joined to one pole of a battery of one or two cells. The other end of the wire is then brought into contact with the other pole of the battery. As soon as the circuit is completed the current flows through the wire and the needle turns briskly aside. If the current be flowing from South to North along the wire, Over the needle, the north-seeking pole of the needle will turn Westwards. [The letters in capitals—SNOW—will help the memory.] If, as in Fig. 117, the current flows from North to South, Over the needle, the needle will be

deflected Eastwards. If the wire is, however, *below* the needle, the motions will be reversed; a current flowing from North to South, Under the needle, will cause a deflexion Westwards.

210. Ampère's Rule.—To keep these movements in memory, Ampère suggested the following fanciful but useful rule. *Suppose a man swimming in the wire with the current, always facing the needle, then the N-seeking pole of the needle will be deflected towards his* **left** *hand.*

For certain particular cases in which a *fixed* magnet pole acts on a *movable* circuit, the following *converse to Ampère's Rule* will be found convenient. Suppose a man swimming in the wire with the current, and that he turns so as to look along the direction of the lines of force of the pole (*i.e.* as the lines of force run, *from* the pole if it be N-seeking, *towards* the pole if it be S-seeking), then he and the conducting wire with him will be urged *toward his left.*

211. Corkscrew Rule.—The following rule was suggested by Maxwell. *The direction of the current and that of the resulting magnetic force are related to one another, as are the rotation and the forward travel of an ordinary* (right-handed) *corkscrew.* In Fig. 118, if the circle represents the circulation of current, the arrow gives the direction of the resulting magnetic force. One advantage of this rule is, that it is equally applicable in the other case. If the arrow represents the direction of the current along a straight wire, the circle will represent the direction of the resulting magnetic force around it.

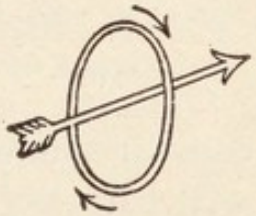


FIG. 118.—Corkscrew Rule.

212. Galvanoscope.—A little consideration will show that if a current be carried *below* a needle in one direction, and then back in the opposite direction *above* the needle, by bending the wire round, as in Fig. 119, the forces exerted on the needle by both portions of the

current will be in the same direction. For let *a* be the N-seeking, and *b* the S-seeking, pole of the suspended needle, then the tendency of the current in the lower part of the wire will be to turn the needle so that *a* comes towards the observer, while *b* retreats; while the current flowing above, which also deflects the N-seeking pole to its left, will equally urge *a* towards the observer, and *b* from him. The needle will not stand out completely at right angles to the direction of the wire conductor, but will take an oblique position. The directive forces of the earth's magnetism are tending to make the needle point north-and-south. The electric current is acting on the needle, tending to make it set itself west-and-east. The *resultant* force will be in an oblique direction between these, and will depend upon the relative strength of the two conflicting forces. If the current is very strong the needle will turn widely round; but could only turn completely to a right angle if the current were infinitely strong. If, however, the current is feeble in comparison with the directive magnetic force, the needle will turn very little.

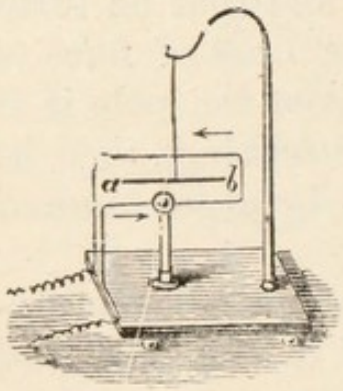


FIG. 119.—Galvanoscope.

This arrangement will, therefore, serve roughly as a **Galvanoscope** or indicator of currents; for the movement of the needle shows the direction of the current, and indicates whether it is a strong or a weak one. This apparatus is too rough to detect very delicate currents. To obtain a more sensitive instrument there are two possible courses: (i.) increase the effective action of the current by carrying the wire more than once round the needle; (ii.) decrease the opposing directive force of the earth's magnetism by some compensating contrivance.

213. Schweigger's Multiplier.—The first of the above suggestions was carried out by Schweigger, who

constructed a *multiplier* of many turns of wire. A suitable frame of wood, brass, or ebonite, is prepared to receive the wire, which must be "insulated," or covered with silk, or cotton, or indiarubber, to prevent the separate turns of the coil from coming into contact with each other. Within this frame, which may be circular, elliptical, or more usually rectangular, as in Fig. 120, the needle is suspended; the frame being placed so that the wires lie in the magnetic meridian. The greater the number of turns the more powerful will be the magnetic deflexion produced by the passage of equal quantities of current. But if the wire is thin, or the number of turns of wire numerous, the resistance thereby offered to the flow of electricity may very greatly reduce the strength of the current. The student will grasp the importance of this observation when he has read the chapter on Ohm's Law. Cumming, of Cambridge, appears to have been the first to use a coil surrounding a pivoted needle to *measure* the current. To him we owe the term *Galvanometer*.

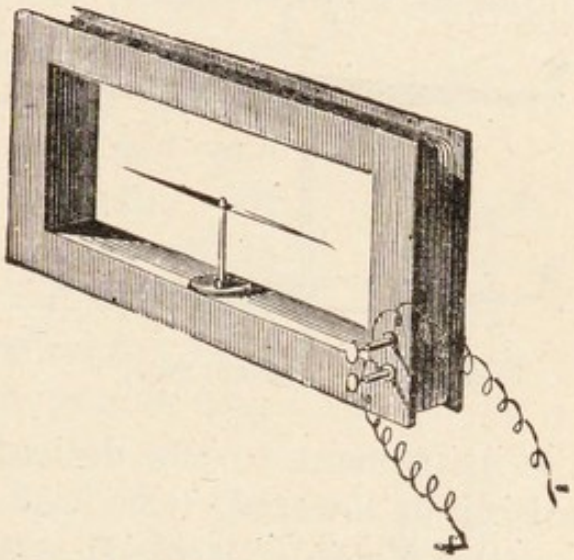


FIG. 120.—Schweigger's Multiplier.

214. Astatic Combinations of Magnets.—The directive force exercised by the earth's magnetism on a magnetic needle may be reduced or obviated by one of two methods:

(*a*) [*Haüy's Method*]. By employing a *compensating magnet*. An ordinary long bar magnet laid in the magnetic meridian, but with its N-seeking pole directed towards the north, will, if placed horizontally above or below a suspended magnetic needle, tend to make the needle set itself with its S-seeking pole northwards. If

near the needle it may overpower the directive force of the earth, and cause the needle to reverse its usual position. If it is far away, all it can do is to lessen the directive force of the earth. At a certain distance the magnet will just compensate this force, and the needle will be neutral. This arrangement for reducing the earth's directive force is applied in the reflecting galvanometer shown in Fig. 134, in which the *controlling magnet* at the top, curved in form and capable of adjustment to any height, affords a means of adjusting the instrument to the desired degree of sensitiveness by raising or lowering it.

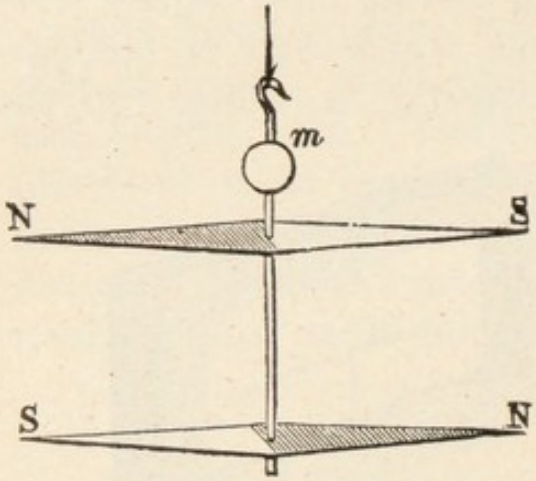


FIG. 121.—Astatic Pair.

(*b*) [*Nobili's Method*]. By using an *astatic pair* of magnetic needles. If two magnetized needles of equal strength and size are bound together by a light wire of brass, or aluminium, in reversed positions, as shown in Fig. 121, the force urging one to set itself in the magnetic meridian is exactly counterbalanced by the force that acts on the other. Consequently this pair of needles will remain in any position in which it is set, and is independent of the earth's magnetism. Such a combination is known as an **astatic pair.** It is, however, difficult in practice to obtain a perfectly astatic pair, since it is not easy to magnetize two needles exactly to equal strength, nor is it easy to fix them perfectly parallel to one another. Such an astatic pair is, however, readily deflected by a current flowing in a wire coiled around one

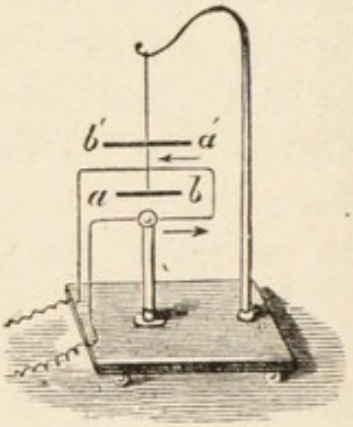


FIG. 122.—Astatic Pair.

of the needles; for, as shown in Fig. 122, the current which flows above one needle and below the other will urge both in the same direction, because they are already in reversed positions. It is even possible to go further, and to carry the wire round both needles, winding the coil around the upper in the opposite sense to that in which the coil is wound round the lower needle. Several other astatic combinations are possible. For example, two needles may be lightly braced together vertically, as in Fig. 123, with poles reversed and suspended to turn. Or the astatic combination (Broca's) of Fig. 124, with consequent poles (Art. 122) at the middle points, may be used.

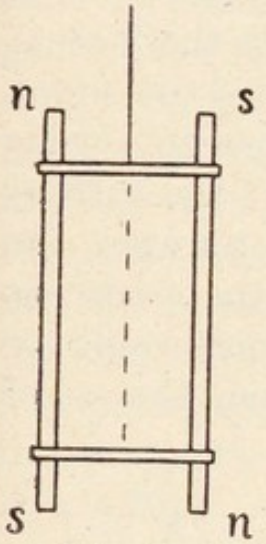


FIG. 123.—Vertical Astatic Pair.

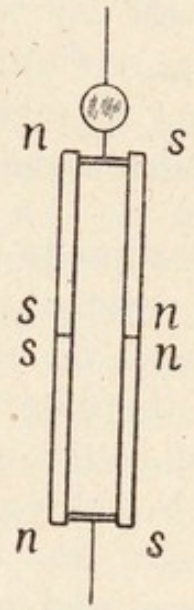


FIG. 124.—Broca's Astatic Pair.

Nobili applied the astatic arrangement of needles to the multiplying coils of Schweigger, and thus constructed a very sensitive instrument, the *Astatic Galvanometer*, shown in Fig. 131. The special forms of galvanometer adapted for the commercial measurement of currents are described in the next Lesson.

215. Magnetic Field due to Current: Magnetic Whirls.—Arago found that if a current be passed through a piece of copper wire it becomes capable of attracting iron filings to it so long as the current flows. These filings set themselves tangentially to the wire, and cling around it, but drop off when the circuit is broken. There is, then, a magnetic "field" around the wire which carries the current; and it is important to know how the lines of force are distributed in this field.

Let the central spot in Fig. 125 represent an imagined cross-section of the wire, and let us suppose the

current to be flowing *in* through the paper at that point. Then, by the corkscrew rule, a magnet needle placed near the side of the wire will tend to set itself at right angles to the current, in positions such as those shown in the figure, with the N-pole pointing in the clockwise direction.[1] In fact the tendency would be to urge the N-seeking pole round the conductor in the same way as the hands of a clock move; while the S-seeking pole would be urged in the opposite cyclic direction to that of the hands of a clock. If the current is reversed, and is regarded as flowing towards the reader, *i.e.* coming up *out* of the plane of the paper, as in the diagram of Fig. 126, then the motions would be just in the reverse sense. It would seem from this as if a N-seeking pole of a magnet ought to revolve continuously round and round a current; but as we cannot obtain a magnet with one pole only, and as the S-seeking pole is urged in an opposite direction, all that occurs is that the needle sets itself as a tangent to a circular curve surrounding the conductor. The field surrounding the conductor consists in fact of a sort of enveloping *magnetic whirl* all along it, the whirl being strong near the wire and weaker farther away. This is

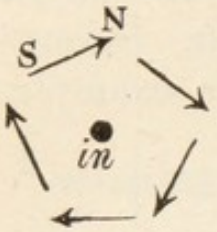


FIG. 125.

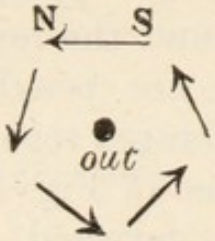


FIG. 126.

Action of Vertical Wire on Needles.

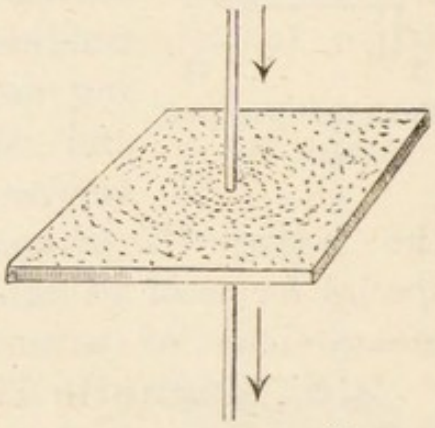


FIG. 127.—Field due to Vertical Wire.

[1] The student may apply Ampère's rule to this case, and to others which follow. Thus, supposing himself to dive head foremost into the page at the point marked *in*, and to turn round so as to face each of the magnets in succession, he will find each N-pole directed to *his* left. In diagram 126 he must conceive himself as coming up *out* of the spot where the current is flowing out.

what Oersted meant when he described the electric current as acting "in a revolving manner" upon the magnetic needle. The field of force, with its circular lines surrounding a current flowing in a straight conductor, can be examined experimentally with iron filings in the following way: A card is placed horizontally and a stout copper wire is passed vertically through a hole in it (Fig. 127). Iron filings are sifted over the card (as described in Art. 121), and a strong current from three or four large cells is passed through the wire. On tapping the card gently the filings near the wire set themselves in concentric circles round it. It is because of this surrounding field that two conductors can apparently act on one another at a distance. If both currents are flowing in the same direction, their magnetic fields tend to merge, and the resulting stress in the medium tends to drag them together with an apparent attraction. If the currents are flowing in opposite directions the stresses in the intervening magnetic field tend to thrust them apart (see also Art. 420).

It is known that energy has to be spent in producing any magnetic field. When a current is turned on in a wire the magnetic field grows around the wire, some of the energy of the battery being used during the growth of the current for that purpose. One reason why electric currents do not *instantly* rise to their final value (Art. 505) is the reactive effect of this surrounding magnetic field. No current can exist without this surrounding magnetic field. Indeed it is impossible to refute the proposition that what we measure as an electric current *in* a wire really is this external magnetic whirl.

216. Equivalent Magnetic Shell: Ampère's Theorem.—For many purposes the following way of regarding the magnetic action of electric currents is more convenient than the preceding. Suppose we take a battery and connect its terminals by a circuit of wire, and that a portion of the circuit be twisted, as in Fig. 128,

into a looped curve, it will be found that the entire space enclosed by the loop possesses magnetic properties. In our figure the current is supposed to be flowing round the loop, as viewed from above, in the same direction as the hands of a clock move round; an imaginary man swimming round the circuit and always facing towards the centre would have his left side down. Then by the corkscrew rule a N-seeking pole would be urged downwards through the loop, while a S-seeking pole would be urged upwards. In fact the space enclosed by the loop of the circuit behaves like a *magnetic shell* (see Art. 120),

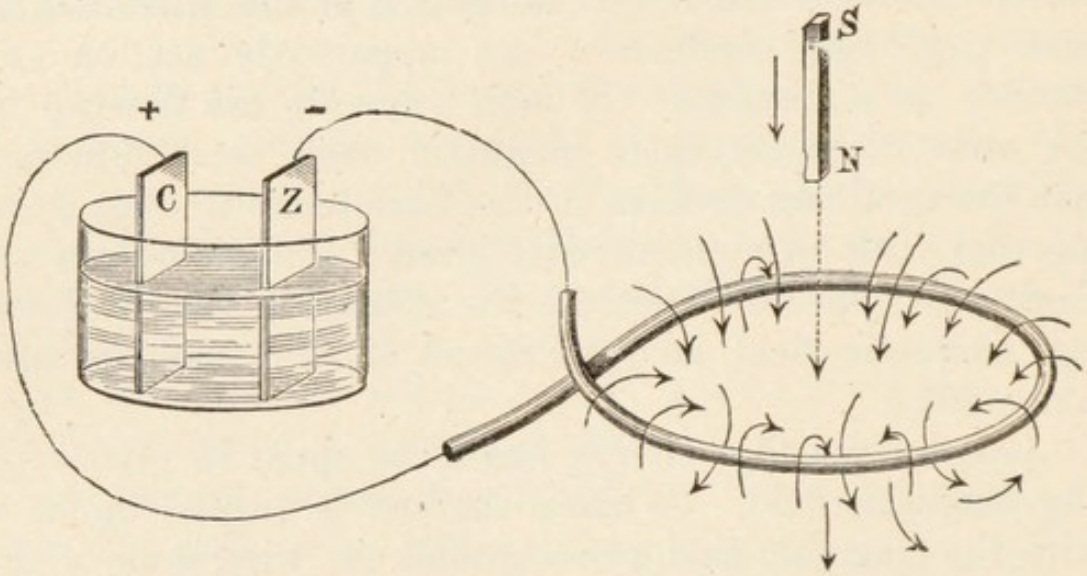


FIG. 128.—Magnetic Properties of Conductor.

having its upper face of S-seeking magnetism, and its lower face of N-seeking magnetism. *A closed voltaic circuit is equivalent to a magnetic shell whose edges coincide in position with the circuit*, the shell being of such a strength that the number of its lines of force is the same as that of the lines of force due to the current in the circuit. The circuit acts on a magnet attracting or repelling it, and being attracted or repelled by it, exactly as its equivalent magnetic shell would do. Also, the circuit itself, when placed in a magnetic field, experiences the same force as its equivalent magnetic shell would do.

217. Maxwell's Rule.—Clerk Maxwell gave the following rule for determining the mutual action of a circuit and a magnet placed near it. *Every portion of the circuit is acted upon by a force urging it in such a direction as to make it enclose within its embrace the greatest possible number of lines of force.* If the circuit is fixed and the magnet movable, then the force acting on the magnet will also be such as to tend to make the number of lines of force that pass through the circuit a maximum (see also Art. 376).

This is but one case of the still more general law governing every part of every electromagnetic system, viz.: *Every electromagnetic system tends so to change the configuration of its parts as to make the interlinkage of magnetic lines with the exciting circuit a maximum* (Art. 409).

218. De la Rive's Floating Coil.—The preceding remarks may be illustrated experimentally by the aid of a little floating circuit. A plate of zinc and one of copper (see Fig. 129) are fixed side by side in a large cork, and connected above by a coil of several turns of covered copper wire. This is floated upon a dish containing dilute sulphuric acid. If one pole of a bar magnet be held towards the ring it will be attracted or repelled according to the pole employed. The floating circuit will so move as to make the flux of magnetic lines through the coil a maximum. If the S-pole of the magnet be presented to that face of

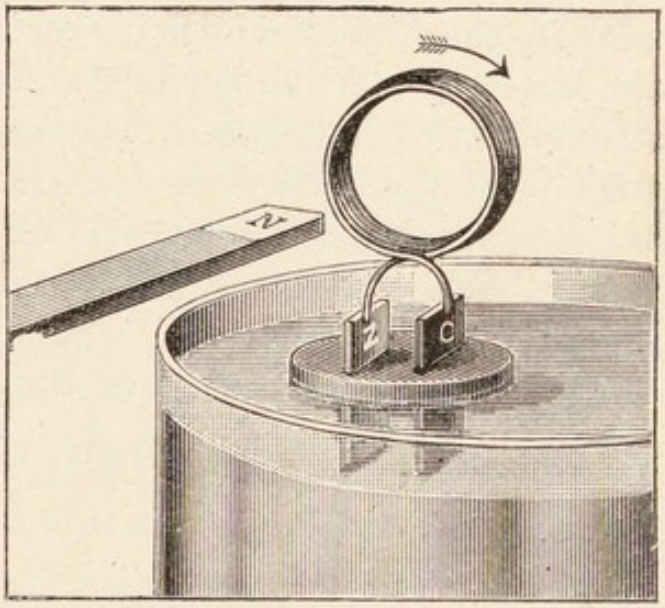


FIG. 129.—De la Rive's Floating Coil.

the ring which acts as a S-seeking pole (viz. that face round which the current is flowing in a clockwise direction), it will repel it. If the pole be thrust right into the ring, and then held still, the battery will be strongly repelled, will draw itself off, float away, turn round so as to present toward the S-pole of the magnet its N-seeking face, will then be attracted up, and will thread itself on to the magnet up to the middle, in which position as many magnetic lines as possible traverse the area of the ring, and link themselves with the current.

Two circuits traversed by currents attract and repel one another just as two magnetic shells would do.

A piece of iron or steel can be magnetized by causing a current to circulate around it in a spiral wire. This introduces the subject of **electromagnets,** which is dealt with in Arts. 411 to 417, p. 398.

219. Strength of the Current in Magnetic Measure.—When a current thus acts on a magnet pole near it, the force f which it exerts will be proportional to the strength i of the current, and proportional also to the strength m of the magnet pole, and to the length l of the wire employed: the force exerted between *each element of the circuit* and the pole will also vary inversely as the square of the distance r between them. If the wire is looped into a circular coil with the magnet pole at the centre, so that each portion of the circuit is approximately at the same distance from the pole, $f = \frac{ilm}{r^2}$ dynes. Suppose the wire looped up into a circle round the magnet pole, then $l = 2\pi r$, and $f = \frac{2\pi i}{r} m$ dynes. Suppose also that the circle is of *one* centimetre radius, and that the magnet pole is of strength of *one* unit (see Art. 379), then the force exerted by the current of strength i will be $\frac{2\pi i}{1} \times 1$, or $2\pi i$ dynes. In order, therefore, that a current of strength i should exert a force of i dynes on

the unit pole, one must consider the current as travelling round only $\frac{1}{2\pi}$ part of the circle, or round a portion of the circumference equal in length to the radius.

220. Unit of Current.—A current is said to have a strength of one "absolute" unit when it is such that if one centimetre length of the circuit is bent into an arc of one centimetre radius, the current in it exerts a force of one dyne on a magnet-pole of unit strength placed at the centre of the arc. The practical unit of "one *ampere*" is only $\frac{1}{10}$ of this theoretical unit (see also Art. 381).

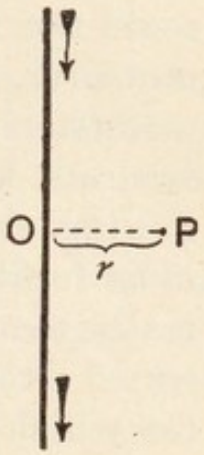


FIG. 130.

If the wire, instead of being looped into a coil, is straight and of indefinite length, the force which the current in it exerts upon a pole of strength m placed at point P near it will be found to vary inversely as the simple distance (not as the square), and the pole will tend to move at right angles both to the wire and to the line OP. In Fig. 130 the descending current will (according to the cork-screw rule above) tend to drive a N-pole at P towards the spectator. If the current is i amperes the force (in dynes) on the pole of m units will (see Art. 371) be

$$f = 2mi/10r.$$

EXAMPLE.—The force exerted by a current of 60 amperes in a long straight conductor upon a pole of 200 units placed 2 centimetres away from it will be 1200 dynes, or (dividing by $g = 981$) about 1·22 grammes' weight.

LESSON XVII.—*Galvanometers*

221. The term **Galvanometer** is applied to an instrument for measuring the strength of electric currents by means of their electromagnetic action. There are two general classes of Galvanometers: (1) those in which the current flowing in a fixed coil of wire causes the

deflexion of a pivoted or suspended magnetic needle; (2) those in which the current flowing in a movable coil suspended between the poles of a fixed magnet causes the coil to turn. There is a third kind of instrument (called for distinction *electrodynamometer*, see Art. 425), in which both the moving part and the fixed part are coils. These last are used chiefly for alternating-currents (see Lesson XLIV. p. 537).

The simple arrangement described in Art. 212 was termed a "galvanoscope," or current *indicator*, but it could not rightly be termed a "galvanometer" or current *measurer*, because its indications were only qualitative, not quantitative. The indications of the needle did not afford accurate knowledge as to the exact strength of current flowing through the instrument. A good galvanometer must fulfil the essential condition that its readings shall really *measure* the strength of the current in some certain way. It should also be adapted to the sort of current for which it is to be used. The galvanometer adapted for measuring very small currents (say a current of only one or two millionth parts of an *ampere*) will not be suitable for measuring strong currents, such as are used in electric lighting or electro-plating. Large currents need thick wires; and a coil of few turns will suffice. If very small currents are to turn the needle they must circulate hundreds or thousands of times around it; for these, therefore, a coil of many turns is appropriate, and the wire may be a very fine one. Moreover, if the current to be measured has already passed through a circuit of great resistance (as, for example, some miles of telegraph wire), a galvanometer whose coil is a short one, consisting only of a few turns of wire, will be of no use, and a long-coil galvanometer must be employed with many hundreds or even thousands of turns of insulated wire round the needle. The reason of this is explained hereafter (Art. 440). Hence it will be seen that different styles of instrument are needed for different kinds of

use; but of all it is required that they should afford quantitative measurements, that they should be sufficiently sensitive for the current that is to be measured, and carry that current without overheating.

222. Methods of Control.—In all instruments, whether the moving part be a magnet or a coil, some controlling force is needful, otherwise the very smallest current would turn the index completely about. If small currents are to produce a small deflexion, and larger currents a larger, there must be forces tending to control. Several means of control may be used. These are :—

(*a*) *Earth's Magnetic Force.*—When the needle is hung on a pivot or fibre, the earth's magnetic force tries to bring it back into the magnetic meridian. This is the usual method in galvanometers with moving needles.

(*b*) *Torsion of Wire.*—The moving part in turning twists the suspending wire, which then tries to untwist, with a force which increases as the angle of deflexion. This method is usual in galvanometers with suspended coils. In some instruments a coiled hair-spring is used.

(*c*) *Gravity.*—If the needle is pivoted on trunnions to move in a vertical plane, it may be weighted at one end.

(*d*) *Permanent Magnet Control.*—To render a needle instrument independent of position, it may be arranged with a powerful external steel magnet to bring the needle back to zero. No "absolute" measurements are possible with these instruments, as their readings depend on the strength of the controlling magnet.

(*e*) *Bifilar Suspension.*—A needle or coil hung by two parallel threads tends by gravity to return to its initial position.

To make an instrument very sensitive the control must be weakened as much as possible.

223. Methods of Observation.—There are the following methods of using galvanometers in making observations :—

(i.) *Deflexion Method.*—The angle through which the moving part (whether needle or coil) is deflected is read off on a scale, by pointer or reflected beam of light, when the moving part has come to rest. This is the most usual method.

(ii.) *Torsion Method.*—The moving part is suspended by a wire from a torsion head, which is turned round until the index is brought back to zero; the controlling force then balancing the deflecting force. In this case one reads off the angle through which the torsion head has been turned (see Torsion Balance, Art. 134, p. 120). This very accurate method, due to Ohm, is used in Siemens' electrodynamometer (Art. 426).

(iii.) *First Swing Method.*—Instead of waiting for moving part to come to rest the *first swing* may be observed. This method, which is the only one practicable for sudden discharges, or for transient currents, is called the *ballistic* method (see Art. 234). If the moving part is not damped in its motion the first swing on turning on a battery current is exactly twice the angle at which the deflexion settles down.

(iv.) *Oscillation Method.*—Instead of observing deflexion, the time of oscillation of the needle may be observed, the coil being in this method set at right angles to the magnetic meridian. Allowance must be made, as in Art. 135, for the earth's magnetism.

(v.) *Cumulative Method.*—For very minute currents a method is sometimes adopted to get up a measurable swing by reversing the current (by hand) as the needle swings through zero. Sometimes a rotating commutator of special construction is employed to produce, and accumulate, the successive impulses.

(vi.) *Null Methods.*—In many cases connexions are used (Wheatstone's "Bridge," "Differential Galvanometers," etc.) of such a kind that when the conditions of electrical equilibrium are attained no current will flow through the galvanometer in the circuit. Such methods, which are generally exceedingly accurate, are known as *null methods.* For such methods sensitive galvanometers are applicable, but the graduation of their scale is unimportant.

224. Nobili's Astatic Galvanometer. — The instrument constructed by Nobili, consisting of an astatic pair of needles delicately hung, so that the lower one lay within a coil of wire wound upon an ivory frame (Fig. 131), was for long the favourite form of sensitive galvanometer. The needles of this instrument, being independent of the earth's magnetism, take their position in obedience to the torsion of the fibre by which they are hung. The frame on which the coil is wound must be set carefully parallel to the needles; and three screw feet serve to adjust the base of the instrument level. Protection against currents of air is afforded by a glass shade. When a current is sent through the wire coils the needles move to right or left over a graduated circle. When the deflexions are *small* (*i.e.* less than 10° or 15°) they are very nearly proportional to the strength of the currents

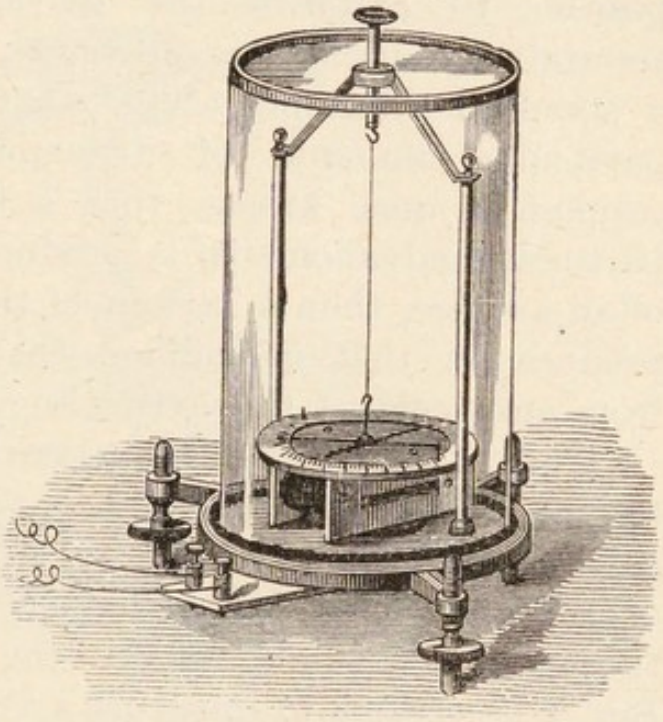


FIG. 131.—Nobili's Astatic Galvanometer.

that produce them. Thus, if a current produces a deflexion of 6° it is known to be approximately three times as strong as a current which only turns the needle through 2°. But this approximate proportion ceases to be true if the deflexion is more than 15° or 20°; for then the needle is not acted upon so advantageously by the current, since the poles are no longer within the coils, but are protruding at the side, and, moreover, the needle being oblique to the force acting on it, part only of the force is turning it against the directive force of the fibre; the other part of the force is uselessly pulling or pushing the needle along its length. It is, however, possible to *calibrate* the galvanometer — that is, to ascertain by special measurements, or by comparison with a standard instrument, to what strengths of current particular amounts of deflexion correspond. Thus, suppose it once known that a deflexion of 32° on a particular galvanometer is produced by a current of $\frac{1}{100}$ of an ampere, then a current of that strength will *always* produce on that instrument the same deflexion, unless from any accident the controlling force has been altered.

225. The Tangent Galvanometer.—It is not—for the reasons mentioned above—possible to construct a galvanometer in which the *angle* (as measured in degrees of arc) through which the needle is deflected is proportional throughout its whole range to the strength of the current. But it is possible to construct a very simple galvanometer in which the *tangent*[1] of the angle of deflexion shall be accurately proportional to the strength of the current. The essential feature of all tangent galvanometers is that while the coil is a large open ring the needle is relatively very small. Fig. 132 shows a form of **Tangent Galvanometer** suitable for large currents. The coil of this instrument consists of a simple circle of stout copper wire from 10 to 15 inches in diameter. Other tangent galvanometers, intended to measure small currents, have

[1] See note on "Ways of Reckoning Angles," p. 137.

many turns of fine wire wound upon a large open wooden ring. At the centre is delicately suspended a magnetized steel needle less than an inch in length, and usually furnished with a light index of aluminium. The instrument is adjusted by setting the coil in the magnetic meridian, the small needle lying then in the plane of the coil.

The magnetic field due to a current passing in the

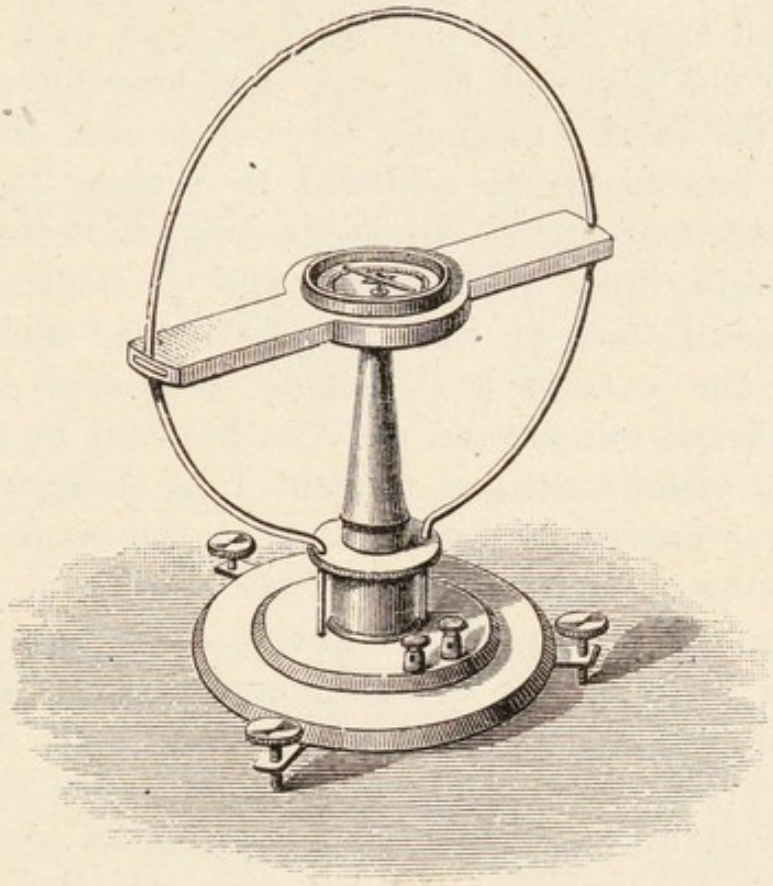


FIG. 132.—Tangent Galvanometer.

coil is not uniform and normal to the plane of the coil except in the region near the centre of the coil; and a considerable error may be introduced if the needle is so long that its ends are in the irregular parts of the field. If the radius of the circle is large and the needle short, its ends will never be far from the centre of the coil, and the needle may be considered as being always in a uniform field, the direction of which is normal to the plane of the coil.

Several devices have been adopted to ensure greater

uniformity of field. Helmholtz designed an instrument with two equal circular coils placed parallel to one another at a distance apart equal to their common radius; the needle being suspended symmetrically between them. A yet more exact result is attained by placing three coils parallel to each other, so that all three lie on the surface of a sphere at the centre of which the needle is suspended.

Whatever the magnetic force which the current in the coil can exert on the needle, it will act in a direction normal to the plane of the coil, and therefore at right angles to the earth's magnetic force (provided the instrument has been properly adjusted by setting the coil in the magnetic meridian). Since the two magnetic forces—the controlling force of the earth and the deflecting force of the current—act at right angles to one another, the action of the current will not be measured by equal degrees marked out around a circle, but will be measured by equal divisions along a tangent line, as shown below. Now, it was proved in Art. 139 that the magnetic force which, acting at right angles to the meridian, produces on a magnetic needle the deflexion δ is equal to the horizontal force of the earth's magnetism at that place multiplied by the *tangent* of the angle of deflexion. Hence a current flowing in the coil will turn the needle aside through an angle such that *the tangent of the angle of deflexion is proportional to the strength of the current.*

EXAMPLE. —Suppose a certain battery gave a deflexion of 15° on a tangent galvanometer, and another battery yielding a stronger current gave a deflexion of 30°. The strengths currents are *not* in the proportion of 15 : 30, but in the proportion of tan 15° to tan 30°. These values must be obtained from a table of natural tangents like that given in Appendix A, from which it will be seen that the ratio between the strengths of the currents is ·268 : ·577, or about 10 : 22.

Or, more generally, if current i produces deflexion δ, and current i' deflexion δ', then

$$i : i' = \tan \delta : \tan \delta'.$$

To obviate reference to a table of figures, the circular scale of the instrument is sometimes graduated into tangent values instead of being divided into equal degrees of arc. Let a tangent OT be drawn to the circle, as in Fig. 133, and along this line let any number of equal divisions be set off, beginning at O. From these points draw back to the centre. The circle will thus be divided into a number of pieces, of which those near O are nearly equal, but which get smaller and smaller away from O. These unequal pieces correspond

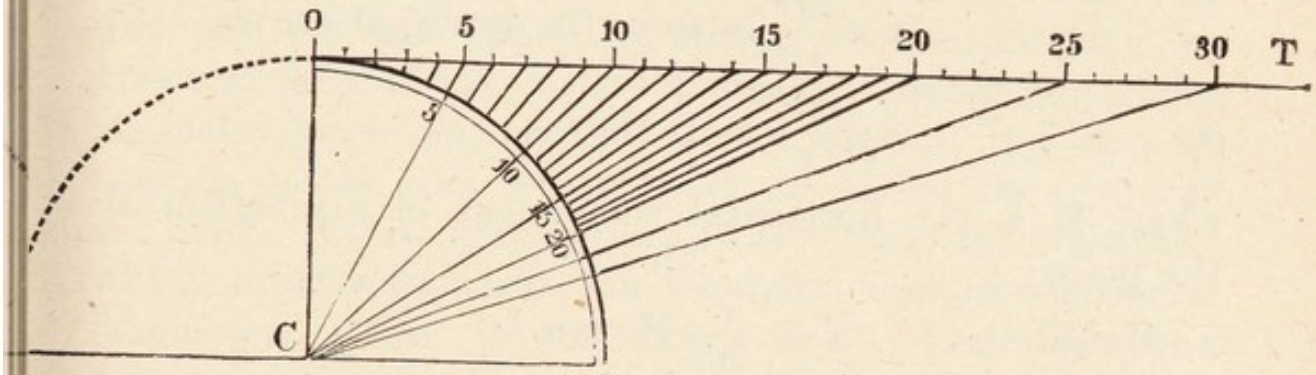


FIG. 133.—Tangent Scale.

to equal increments of the tangent. If the scale were divided thus, the readings would be proportional to the tangents. It is, however, harder to divide an arc into tangent lines with accuracy than to divide it into equal degrees; hence this graduation, though convenient, is not used where great accuracy is needed.

226. Absolute Measure of Current by Tangent Galvanometer.—The strength of a current may be determined in "absolute" units by the aid of the tangent galvanometer if the "constants" of the instrument are known. The tangent of the angle of deflexion represents (see Art. 139) the ratio between the magnetic force due to the current and the horizontal component of the earth's magnetic force. Both these forces act on the needle, and depend *equally* upon the magnetic moment of the needle, which, therefore, we need not know for this purpose. We know that the force exerted by the current at centre

of the coil is proportional to the horizontal force of the earth's magnetism multiplied by the tangent of the angle of deflexion. These two quantities can be found from the tables, and from them we calculate the absolute value of the current as follows :—Let r represent the radius of the galvanometer coil (measured in centimetres); its total length (if of one turn only) is $2\pi r$. The distance from the centre to all parts of the coil is of course r. From our definition of the absolute unit of current (Art. 220), it follows that

$$i \times \frac{2\pi r}{r^2} = \text{force (in dynes) at centre,}$$

or

$$i \times \frac{2\pi}{r} = \mathrm{H} \cdot \tan \delta,$$

where H is the horizontal component of magnetism at the place.

Hence

$$i = \frac{r}{2\pi} \cdot \mathrm{H} \cdot \tan \delta.$$

The quantity $2\pi/r$, or $2\pi n/r$ if the coil has n turns, is sometimes called the "constant" or the "principal constant" of the galvanometer and denoted by the symbol G. Hence the value of the current in absolute (electromagnetic) units [1] will be expressed as

$$i = \frac{\mathrm{H}}{\mathrm{G}} \cdot \tan \delta.$$

The constant G represents the strength of field produced at the centre of the coil by unit current.

227. Sine Galvanometer.—The disadvantage of the tangent galvanometer just described is that it is not very sensitive, because the coil is necessarily very large as compared with the needle, and therefore far away from it. A galvanometer with a smaller coil or a longer needle cannot be used as a *tangent* galvanometer, though it would be more sensitive. *Any* sensitive galvanometer

[1] The student will remember (Arts. 220 and 381) that the practical unit of current which we call "one *ampere*" is only $\frac{1}{10}$ of one "absolute" unit of the centimetre-gramme-second system.

in which the needle is directed by the earth's magnetism can, however, be used as a **Sine Galvanometer**, provided the frame on which the coils are wound is capable of being turned round a central axis. When the instrument is so constructed, the following method of measuring currents is adopted. The coils are first set parallel to the needle (*i.e.* in the magnetic meridian); the current is then sent through it, producing a deflexion; the coil itself is rotated round in the same sense, and, if turned round through a wide enough angle, will overtake[1] the needle, which will once more lie parallel to the coil. In this position two forces are acting on the needle: the directive force of the earth's magnetism acting along the magnetic meridian, and the force due to the current passing in the coil, which tends to thrust the poles of the needle out at right angles; in fact there is a "couple" which exactly balances the "couple" due to terrestrial magnetism. Now it was shown in the Lesson on the Laws of Magnetic Force (Art. 138) that when a needle is deflected the "moment" of the couple is proportional to the sine of the angle of deflexion. Hence in the sine galvanometer, when the coil has been turned round so that the needle once more lies along it, *the strength of the current in the coil is proportional to the sine of the angle through which the coil has been turned.*[2]

[1] Provided the current is not too strong; for with a sine galvanometer the largest current which can be measured is numerically equal to $H \div G$.

[2] Again the student who desires to compare the strength of two currents will require the help of a table of natural sines, like that given in Appendix A. Suppose that with current i the coils had to be turned through an angle of θ degrees; and that with a different current i' the coils had to be turned through θ' degrees, then

$$i : i' = \sin\theta : \sin\theta'.$$

It is of course assumed that the instrument is provided with a scale of degrees on which to read off the angle through which the coils have been turned. It is possible here also, for rough purposes, to graduate the circle not in degrees of arc, but in portions corresponding to equal additional values of the sine. The student should try this way of dividing a circle after reading the note on "Ways of Reckoning Angles," p. 137.

228. The Mirror Galvanometer.—When a galvanometer of great delicacy is needed, the moving parts must be made very light and small. To watch the movements of a very small needle an *index* of some kind must be used; indeed, in the tangent galvanometer it is usual to fasten to the short stout needle a delicate stiff pointer of aluminium. A far better method is to fasten to the needle a very light mirror of silvered glass,

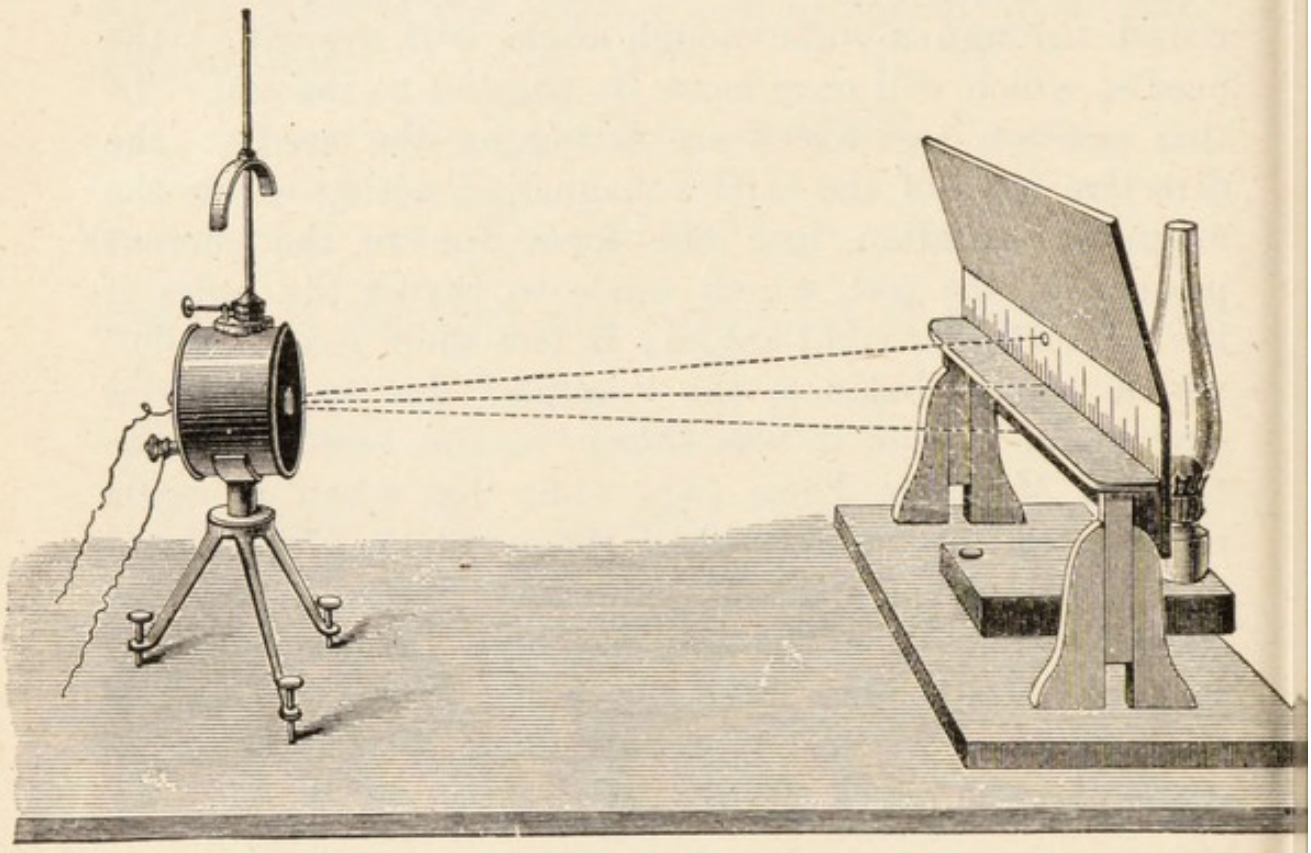


FIG. 134.—Kelvin's Mirror Galvanometer.

by means of which a beam of light can be reflected on to a scale, so that every slightest motion of the needle is magnified and made apparent. The *mirror galvanometers* devised by Sir W. Thomson (Lord Kelvin) for signalling through submarine cables are admirable examples of this class of instrument. In Fig. 134 the general arrangements of this instrument are shown. The body of the galvanometer, consisting of a bobbin on which is wound the coil, is supported on three screw

feet by which it can be adjusted. The magnet consists of one or more small pieces of steel watch-spring attached to the back of a light concave silvered glass mirror about as large as a threepenny piece, weighing altogether only two or three grains. This mirror is hung by a single fibre of cocoon silk within the coil; and a curved magnet, which serves to counteract the magnetism of the earth, or to direct the needle, is carried upon a vertical support above. Another view of the suspended mirror and magnets is shown in Fig. 135. Opposite the galvanometer is placed the scale. A beam of light from a paraffin lamp passes through a narrow aperture under the scale and falls on the mirror, which reflects it back on to the scale. The mirror is slightly concave, and gives a well-defined spot of light if the scale is adjusted to suit the focus of the mirror. The controlling magnet enables the operator to bring the reflected spot of light to the zero point at the middle of the scale. The feeblest current passing through the galvanometer will cause the spot of light to shift to right or left. The tiny current generated by dipping into a drop of salt water the tip of a brass pin and a steel needle (connected by wires to the terminals of the galvanometer) will send the spot of light swinging right across the scale. If a bright beam of light is used, the movement of the needle can be shown to a thousand persons at once. For still more delicate work an astatic pair (Art. 214, p. 193) of needles can be used, each being surrounded by its coil, and having the mirror rigidly attached to one of the needles. Such a form, with two bobbins, wound so

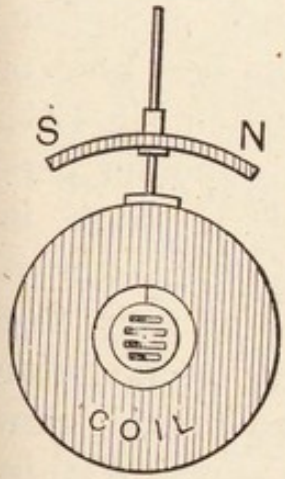


FIG. 135.—Mirror Galvanometer.

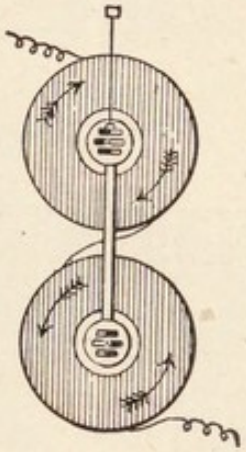


FIG. 136. — Astatic Mirror Galvanometer.

as to be traversed by the current in opposite senses, is represented diagrammatically in Fig. 136. Such an instrument, made with four bobbins, two in front and two behind the suspended needle system, and having on each bobbin about 2 miles of a wire about $\frac{1}{1000}$ inch in thickness, insulated by a coating of silk, is capable of showing by a deflexion of one millimetre on its scale an exceedingly minute current, even down to one fifty-four thousand millionth part of one ampere.

229. Suspended Coil Galvanometers. — These have been used by Sturgeon (1836), Varley (1860), and others, and the principle was also applied in Lord Kelvin's "Siphon Recorder" (Fig. 350). The best known is that of d'Arsonval depicted in Fig. 137. Between the poles of a compound permanent steel magnet of U-shape is suspended by very thin hard-drawn silver wires an open coil of very fine wire wound on a light rectangular frame. The current is led to and from the coil by the suspending wires. Within the suspended coil is a cylinder of soft iron, supported from behind, to concentrate the magnetic field. The vertical parts of the coil then hang freely in the two narrow gaps where the magnetic field is very intense. The force tending to turn the coil is proportional to the current, to the number of windings, and to the intensity of the magnetic field, so that by making the magnet very powerful the instrument becomes very sensitive. The elasticity of the suspending wires controls the position of the coil and tends to bring it back to its initial position. These galvanometers are independent of the earth's magnetic field, and are not affected by magnets in their neighbourhood, so that they can be used

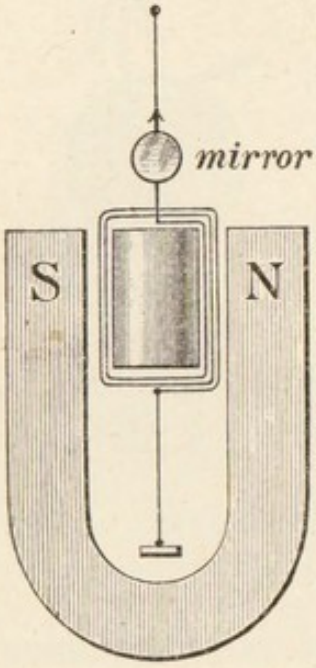


FIG. 137.—Suspended Coil Galvanometer.

$\frac{1}{9} + \frac{1}{10} = \frac{10+9}{90} = 1$

in many places where other galvanometers could not. They are also remarkably dead-beat. Some are provided with a pointer and a horizontal dial; others more usually have a mirror attached to the coil to reflect a spot of light. In some the moving coil is supported on a pivot, the current being introduced through delicate flexible springs.

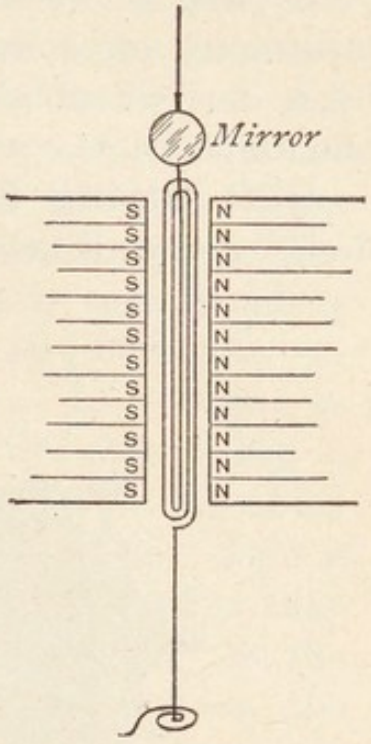


FIG. 138.—Ayrton-Mather Galvanometer.

More recent is the suspended-coil galvanometer of Ayrton and Mather (Fig. 138). Here the suspended coil is formed as an elongated loop with no wide aperture between its sides. Consequently the poles of the magnets may be brought very close together; and these are made up of a number of flat steel magnets of nearly circular form piled up on one another. One of these instruments with mirror and scale, at a standard distance of one metre, will show a deflexion of one millimetre on the scale, with a current less than one ninety-millionth part of 1 ampere.

230. Galvanometer Shunts. — Strong currents must not be passed through very sensitive galvanometers, for, even if they are not spoiled by overheating, the deflexions of the needle will be too large to give accurate measurements. In such cases the galvanometer is used with a *shunt*, or coil of wire arranged so that the greater part of the current shall flow through it, and pass by the galvanometer, only a small portion of the current—say $\frac{1}{10}$, or $\frac{1}{100}$, or $\frac{1}{1000}$—actually traversing the coils of the instrument. The resistance of the shunt must be a small fraction—say $\frac{1}{9}$, or $\frac{1}{99}$, or $\frac{1}{999}$—of the resistance of the instrument, according to the principle laid down in Art. 441 about branched circuits.

231. Broca's Galvanometer.—In this instrument

the special astatic combination depicted in Fig. 124, p. 195, is used. The astatic needles, attached to a mica slip, and hung on a quartz fibre, are suspended so that the central poles hang between two fixed coils. A deflexion of one millimetre on a scale at one metre distance is produced by a current of about one thousand millionth part of one ampere.

232. String Galvanometer.—In this instrument, designed by Einthoven of Leyden, the moving coil is

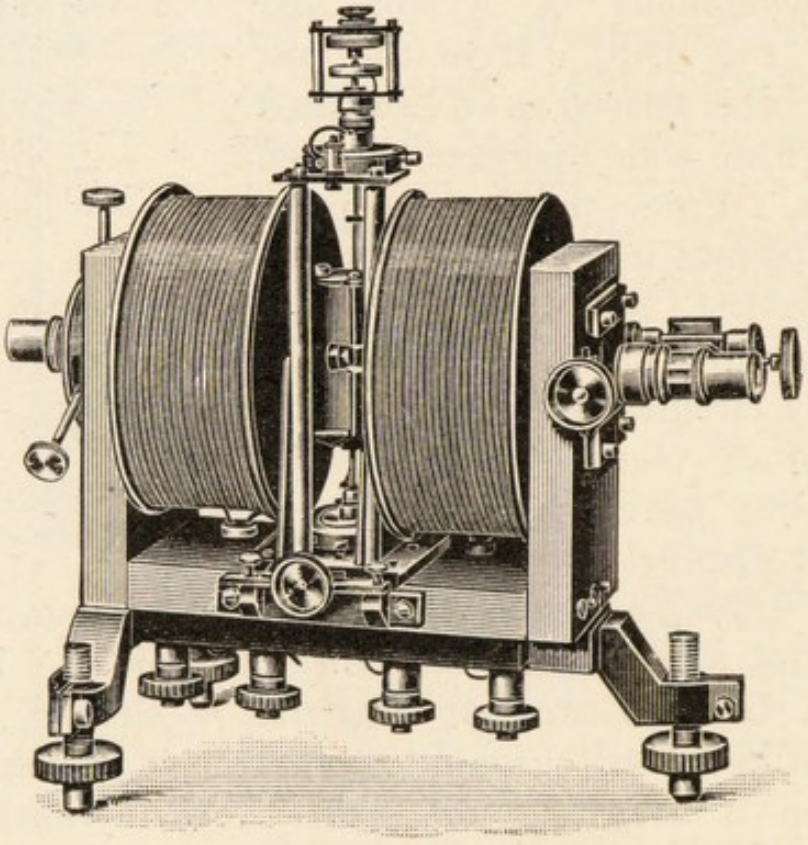


FIG. 139.—String Galvanometer.

reduced to a single "string" or fibre of silvered glass, stretched from supports along a narrow gap between the poles of a special electromagnet. As the "string" thus lies in a very strong magnetic field, when a current passes through it, it is dragged sideways across the magnetic lines (see Art. 367, p. 349), and its deflexion, which is proportional to the current, is observed by a microscope which passes through a hole bored in the pole-pieces (Fig. 139). As the "string" weighs about $\frac{1}{1,000,000}$ gramme, the instru-

ment is extraordinarily sensitive, as well as dead-beat. It will detect a current less than one sixty-thousand millionth of an ampere.

233. Differential Galvanometer.—For the purpose of comparing two currents a galvanometer is sometimes employed, in which the coil consists of *two* separate wires wound side by side. If two equal currents are sent in opposite directions through these wires, the needle will not move. If the currents are unequal, then the needle will be moved with an intensity corresponding to the *difference* of the strengths of the two currents.

234. Ballistic Galvanometer. — In order to measure the strength of currents which last only a very short time, galvanometers are employed in which the needle takes a relatively long time to swing. This is the case with long or heavy needles; or the needles may be weighted by enclosing them in leaden cases. As the needle swings slowly round, it adds up, as it were, the varying impulses received during the passage of a transient current. *The sine of half the angle of the first swing is proportional to the quantity of electricity that has flowed through the coil.* The charge of a condenser may thus be measured by discharging it through a ballistic galvanometer (see Art. 451*b*). The needle must not be damped.

235. Methods of Damping: Aperiodic Galvanometers.—To prevent the needle from swinging to and fro for a long time devices are used to *damp* the motion. These are :—

(*a*) *Air Damping.*—A light vane attached to needle beats against the air and damps the motion. In mirror instruments the mirror itself damps, particularly if confined in a narrow chamber.

(*b*) *Oil Damping.*—A vane dips into oil.

(*c*) *Magnetic Damping.*—If the needle swings close to or inside a mass of copper or aluminium, it will soon come to rest by reason of the eddy-currents (Art. 500) induced in the copper. Eddy-currents damp the motion

of the suspended coil in instruments of that class, particularly if the coils are wound on a metal frame.

The period of swing can be reduced by diminishing the weight and leverage of the moving parts so as to lessen their moment of inertia. It can also be lessened (at the expense of the sensitiveness of the instrument) by increasing the controlling forces. An instrument so well damped as to come to rest without getting up a periodic swing is called an *aperiodic* or *dead-beat* instrument.

236. Oscillographs.—For the purpose of studying exceedingly rapid changes of current, or rapidly alternating currents, instruments called *Oscillographs* have been devised by Blondel, and by Duddell. In Duddell's Oscillograph, a skeleton diagram of which is given in Fig. 140, the current is sent through two thin parallel wires forming a single loop stretched vertically in a narrow gap between the poles of an excessively strong electromagnet, or permanent magnet. The loop tends to turn and moves a light mirror. The movement is damped by immersion in oil of the lower part of the moving system. As its moment of inertia is excessively small it can respond to currents that oscillate with a frequency of several hundreds or even thousands per second. With this apparatus it is usual to combine a rotating or vibrating mirror for the study of periodic currents, and a moving photographic plate or film to record the deflexions of the beam of light, the instantaneous value of the current being proportional to the displacement of the luminous spot.

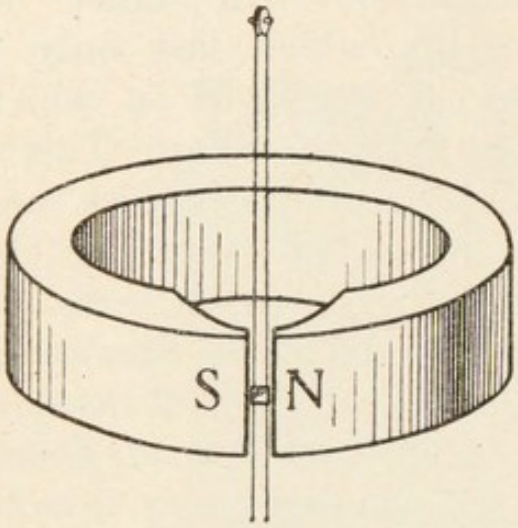


FIG. 140.—Duddell's Oscillograph.

237. Voltmeters, or Potential Galvanometers.—If any galvanometer be constructed with a

very long thin wire of high resistance as its coil, or included in the circuit of its coil, very little current will flow through it, but what little current flows will be exactly proportional to the potential difference that may be applied to the two ends of its circuit. Such a galvanometer, suitably provided with a scale, will indicate the number of *volts* between its terminals. Many forms of voltmeter-galvanometers exist, but they all agree in the essential of having a coil or circuit of a high resistance

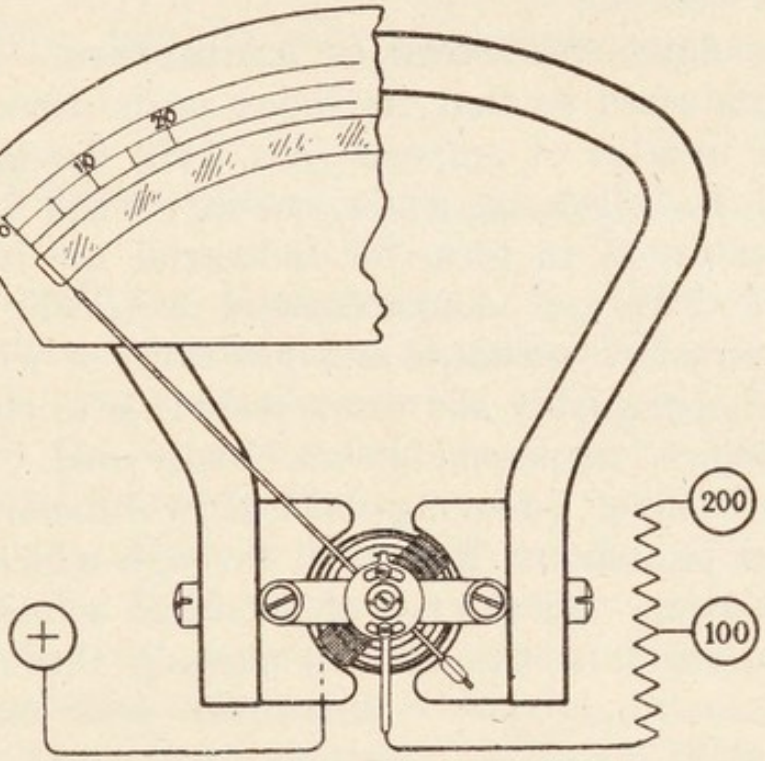


FIG. 141.—Weston's Voltmeter.

—sometimes several thousand ohms. The suspended-coil galvanometers described in Art. 229, with an auxiliary high resistance, make excellent voltmeters. Weston's voltmeter, Fig. 141, is of this class, the coil being delicately pivoted, and controlled by a spiral spring. Any sensitive mirror galvanometer can be used as a voltmeter by simply adding externally to its circuit a resistance sufficiently great. There are also *electrostatic voltmeters* that depend on the repulsion between charged surfaces; they are a species of *electrometer* and are described in Art. 309. *Hot-wire*

voltmeters, of which Cardew's (Art. 465, p. 473) was the earliest, differ from the above class of instrument. The essential feature of these instruments consists in a long thin wire of high resistance, which expands by heating when it is connected across a circuit. All voltmeters are placed across *as shunts* between the two points the potential difference of which is to be measured. They are never joined up *in circuit* as amperemeters are. The range of a voltmeter may be increased by adding resistance in series with it.

238. Amperemeters, or Ammeters.—A galvanometer graduated so that its index reads directly on the scale the number of amperes (Art. 220) flowing through the coil is called an *Amperemeter*. Such instruments were introduced in form for industrial use in 1879 by Ayrton and Perry. Amperemeters are made with short coils of very low resistance and few turns of wire, as they must not appreciably add extra resistance to the circuit.

Moving-coil amperemeters are chiefly used. They consist essentially of a moving-coil milli-voltmeter (Fig. 141) connected to a shunt (Art. 230) through which the main current passes. As the fall of potential across the shunt is proportional to the current passing through it, the instrument scale may be calibrated to read direct in amperes for that particular shunt.

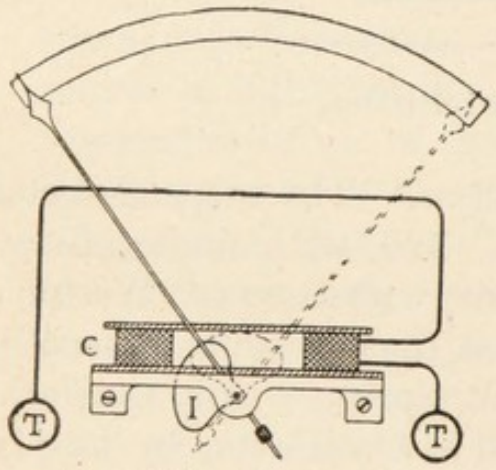


FIG. 142.—Moving-iron Amperemeter

Among the innumerable forms of amperemeter in commerce there are a number in which there is neither magnet nor iron, but which depend upon the mutual force between a fixed and a movable coil traversed by the current. These are dealt with in Art. 425, and are suitable for alternate currents as well as continuous currents. Of

this kind are Siemens' electrodynamometer and the Kelvin balances.

Other instruments depend upon the magnetic properties of iron under the influence of the current. An instrument of the moving-iron type is depicted in Fig. 142. It consists of a coil C of thick wire or strip with a narrow rectangular opening in its centre. A piece of soft iron, of oval shape I attached to a pointer, is pivoted, so that, when the current passes around the coil, the iron is sucked into the coil by forces depending on the strength of the current. Gravity is here the controlling force.

LESSON XVIII.—*Currents produced by Induction*

239. Faraday's Discovery.—In 1831 Faraday discovered that currents can be induced in a closed circuit by moving magnets near it, or by moving the circuit across the magnetic field; and he followed up this discovery by finding that a current whose strength is changing may induce a secondary current in a closed circuit near it. Such currents, whether generated by magnets or by other currents, are known as **Induction Currents.** And the action of a magnet or current in producing such induced currents is termed **magneto-electric** (or electromagnetic) **induction,**[1] or simply induction. Upon this principle are based the modern *dynamo machines* for generating electric currents mechani-

[1] The student must not confuse this electromagnetic induction with the phenomenon of the electrostatic induction of one *charge* of electricity by another *charge*, as explained in Lesson III., and which has nothing to do with *currents*. Formerly, before the identity of the electricity derived from different sources was understood (Art. 262), electricity derived thus from the motion of magnets was termed *magneto-electricity*. For most purposes the adjectives *magneto-electric* and *electro-magnetic* are synonymous. The production of electricity from magnetism, and of magnetism from electricity, are, it is true, two distinct operations; but both are included in the branch of science denominated *Electromagnetics*.

cally, as well as *induction coils*, alternating-current *transformers*, and other appliances.

240. Induction of Currents by Magnets.—If a coil of insulated wire be connected in circuit with a sufficiently delicate galvanometer, and a magnet be inserted rapidly into the hollow of the coil (as in Fig. 143), a momentary current is observed to flow round the circuit while the magnet is being moved into the coil. So long as the magnet lies motionless in the coil it induces no currents. But if it be rapidly pulled out of the coil another momentary current will be observed to flow, and in the opposite direction to the former. The induced current caused by inserting the magnet is an *inverse current*, or is in the opposite direction to that which would magnetize the magnet with its existing polarity. The induced current caused by withdrawing the magnet is a *direct* current.

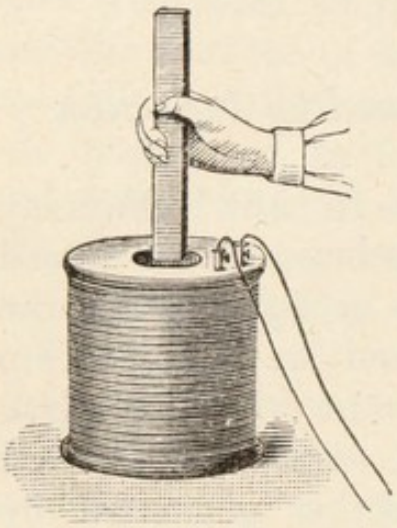


FIG. 143. — Induction of Electric Current by a Magnet.

Precisely the same effect is produced if the coil be moved towards the magnet as if the magnet were moved towards the coil. The more rapid the motion is, the stronger are the induced currents.

The magnet does not grow any weaker by being so used, for the real source of the electrical energy generated is the mechanical energy spent in the motion.

If the circuit is not closed, no currents are produced; but the relative motion of coil and magnet will still set up electromotive-forces, *tending* to produce currents.

Faraday discovered these effects to be connected with the magnetic field surrounding the magnet. He showed that no effect was produced unless the circuit cut across the invisible magnetic lines of the magnet.

241. Induction of Currents by Currents.—

Faraday also showed that the approach or recession of a current might induce a current in a closed circuit near it. This may be conveniently shown as an experiment by the apparatus of Fig. 144.

A coil of insulated wire P is connected in circuit with a battery B of two or three cells, and a key K to turn the current on or off. A second coil S, entirely unconnected with the first, is joined up with wires to a sensitive galvanometer G. We know (Art. 215) that a coil of wire in which a current is circulating acts like a magnet. And we find that if, while the current is flowing in P,

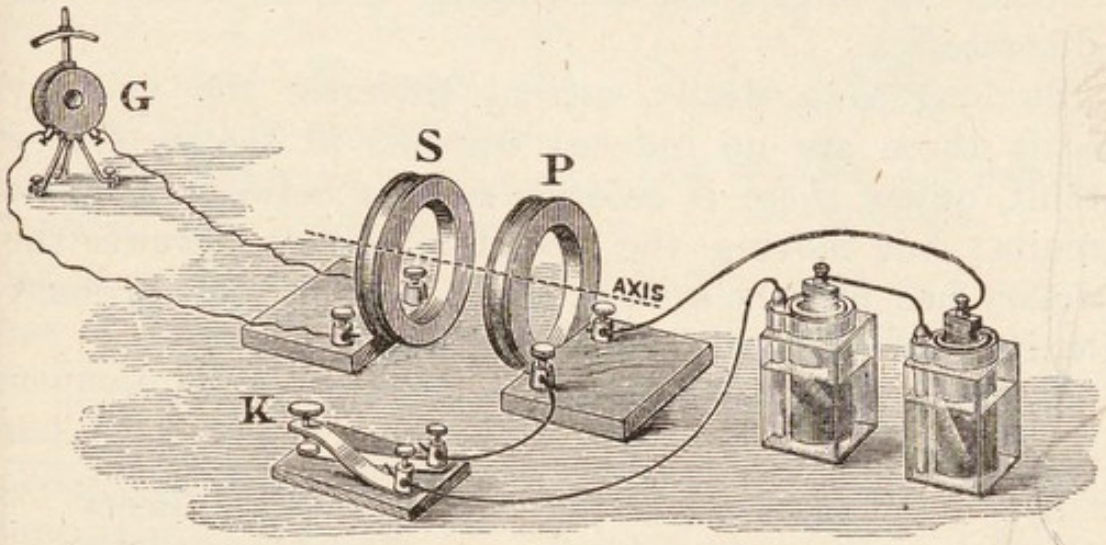


FIG. 144.—Induction of a Current by a Current.

the coil is suddenly moved up toward S, a momentary current will be induced in S. If P is suddenly moved away from S another momentary current will be observed in the second circuit. The first of these two momentary currents is an "inverse" one, while the second one is found to be a "direct" one (*i.e.* one which runs the same way round the coil S as the battery current runs round the coil P). The coil P is called the *primary* coil, and the current in it the *primary current.* The other coil S is called the *secondary* coil, and the momentary currents induced in it are sometimes called *secondary currents.*

Let P now be placed close to S, no current flowing in

either coil. Then on pressing the key K to switch on the primary current, it will be noticed that during the moment while the current in P is growing there will be a transient inverse current in S. The effect of turning on the current is just as if the current had been turned on while P was far away and then P suddenly brought up to S. *Breaking* the battery circuit while the primary coil lies close to the secondary coil produces the same effect as if the primary coil were suddenly removed to an infinite distance. *Making* the battery circuit while the primary coil lies close to the secondary produces the same effect as bringing it up suddenly from a distance.

So long as a steady current traverses the primary circuit there are no induced currents in the secondary circuit, unless there is *relative motion* between the two circuits; but moving the secondary circuit towards the primary has just the same effect as moving the primary circuit towards the secondary, and *vice versa*.

We may tabulate these results as follows:—

By means of	Momentary Inverse currents are induced in the secondary circuit	Momentary Direct currents are induced in the secondary circuit
Magnet	while *approaching*.	while *receding*.
Current	while *approaching*, or *beginning*, or *increasing* in strength.	while *receding*, or *ending*, or *decreasing* in strength.

242. Direction of Induced E.M.F.—It is convenient to have rules for remembering the relations in direction between the magnetism, the motion, and the induced electromotive-force. Of such rules the following, due to Fleming, is most useful: *Let the forefinger of the right hand* (Fig. 145) *point in the direction of the magnetic lines; then turn the thumb in the direction of the motion:*

the middle finger bent at right angles to both thumb and forefinger will show the direction of the induced E.M.F.

Another rule often given is an adaptation of Ampère's: *Suppose a figure swimming in any conductor to turn so as to look along the (positive direction of the) lines, then if he and the conductor be moved towards his right hand he will be swimming with the current induced by this motion*; if he be moved towards his left hand, the current will be against him.

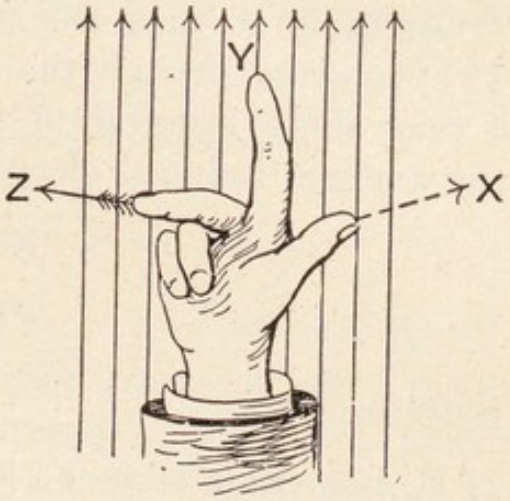


FIG. 145.—Fleming's Rule of the Right Hand.

243. Fundamental Laws of Induction. — When we reflect that every circuit traversed by a current has a magnetic field of its own in which there are magnetic lines running through the circuit (Arts. 215 and 420), we shall see that the facts tabulated in the preceding paragraph may be summed up in the following fundamental laws:—

(i.) *A decrease in the number of lines which pass through a circuit induces a current round the circuit in the positive direction* (i.e. *produces a "direct" current*); *while an increase in the number of lines which pass through the circuit induces a current in the negative direction round the circuit* (i.e. *an "inverse" current*).

Here we suppose the *positive* direction along lines to be the direction along which a free N-pole would tend to move, and the positive direction of the current that in which the current must flow to increase the magnetic flux. Compare the "corkscrew" rule given on p. 191.

(ii.) *The total induced electromotive-force acting round a closed circuit is equal to the rate of decrease in the number of lines which pass through the circuit.*

Suppose at first the number of magnetic lines (Art. 121) passing through the circuit to be F_1, and that after a very short interval of time t the number becomes F_2, the average induced electromotive-force E is

$$E = \frac{F_1 - F_2}{t}$$

By Ohm's law, $$i = E \div R,$$

therefore $$i = \frac{F_1 - F_2}{tR}.$$

If F_2 is greater than F_1, and there is an *increase* in the number of lines, then $F_1 - F_2$ will be a negative quantity, and i will have a negative sign, showing that the E.M.F. is an *inverse* one. A coil of 50 turns of wire cutting 1000 lines will produce the same effect as a coil of 5 turns cutting 10,000 lines, or of one turn cutting 50,000 lines.

To induce an electromotive-force equal to that of a single Daniell's cell would require that 110,000,000 lines should be cut in one second. As such large numbers are inconvenient to express the facts, the unit of E.M.F., the *volt*, has been chosen to correspond to the cutting of 100,000,000 lines per second.

Example.—Suppose the number of magnetic lines to diminish from 800,000 to 0 in the $\frac{1}{50}$ of a second, the rate of diminution is 40,000,000 lines per second. And since 1 volt is taken as 10^8 lines per second, the average induced E.M.F. during that time will be 0·4 volt.

A reference to Fig. 146 will make this important law clearer. Suppose ABCD to be a wire circuit of which the piece AB can slide along DA and CB towards S and T. Let the vertical arrows represent vertical lines of force in a uniform magnetic field, and show (as is the case with the vertical components of the earth's lines of force in the

northern hemisphere) the direction in which a N-pointing pole would move if free. The positive direction of these magnetic lines is therefore vertically downwards through the circuit. Now if AB slide towards ST with a uniform velocity it will cut a certain number of lines every second,

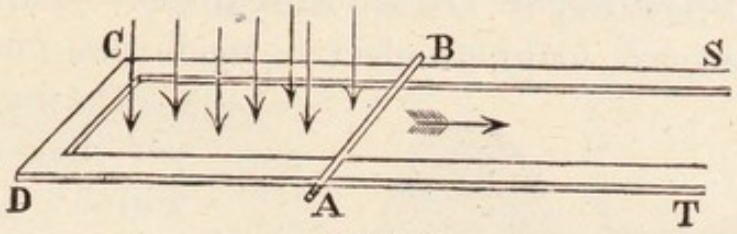


FIG. 146.

and a certain number will be added during every second of time to the total number passing through the circuit. If F_1 be the number at the beginning, and F_2 that at the end of a circuit, $F_1 - F_2$ will be a negative quantity, and there will be generated an electromotive-force whose direction through the sliding piece is from A towards B.

The electromotive-force generated is directly proportional to the strength of the field $\mathcal{H}$, to the velocity v of the movement, and to the length l of the slider; or in symbols:

$$E = \mathcal{H} \times l \times v.$$

Example.—Suppose the strength of the field to be $\mathcal{H} = 6000$ lines per square centimetre, l to be 10 cm., and v to be 50 cm. per second; then E, which is the rate of cutting of magnetic lines, will be 3,000,000 lines per second; or (see Art. 381, p. 362) 0·03 volt.

It is important to note that *all* these inductive operations are really magnetic. In the experiment (Art. 241) with the two coils P and S it is the magnetic lines of coil P which pass through coil S and set up the induced E.M.F. This is proved by the following further experiment. Take a bar of iron—a poker, or better still, a bundle of iron wires—and lay it along the dotted line so that its ends pass through P and S. It will by its great magnetic permeability help to conduct the magnetic lines from P through S. And when it is so placed it will be

found greatly to intensify the actions. In fact if P is many inches away from S, and the iron core is present, the inductive effects of turning the current on and off may be as great as if, in the absence of the core, P were pushed up close to S.

244. Faraday's Disk Machine.—Faraday constructed several magneto-electric machines, one of them consisting of a copper disk (Fig. 147) which he rotated between the poles of a steel magnet or electromagnet. The current flowed from shaft to rim, or *vice versa*, according to the sense of the rotation. It was conducted away by wires having sliding contacts. In other machines copper wire coils were spun so as to cut magnetic lines. This is the principle applied in modern *dynamo-electric machines* (Lesson XLII.). In all cases power, whether of arm or of engine, must be employed to produce the motion. They are all contrivances for converting mechanical energy into electrical energy.

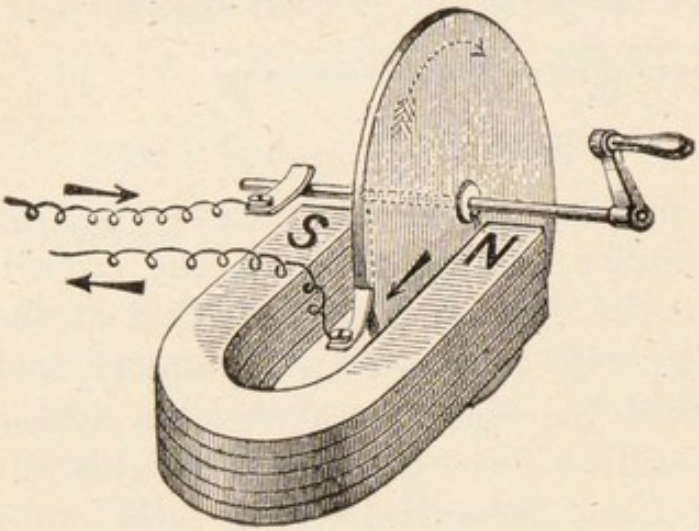


FIG. 147.—Faraday's Simple Disk Magneto-electric Machine.

245. Faraday's Ring: Principle of Transformation.—Amongst Faraday's earliest experiments he took an iron ring about 8 inches in diameter (Fig. 148) and wound upon it two insulated coils of wire P and S, each of many turns. When coil P was connected to a battery circuit, and coil S to a galvanometer, he found that whenever a current was turned on or off in coil P, secondary currents were generated in coil S. In fact the currents in P magnetized the iron ring, and the magnetic lines created by P passed through S, setting up induction

currents. If S is used as the primary then P will work as secondary; in fact the induction between P and S is *mutual*. The Faraday ring, with its two coils wound upon a closed circuit of iron, may be regarded as the type of all *transformers* or *induction coils*. Faraday also employed some induction-coils in which the two coils A

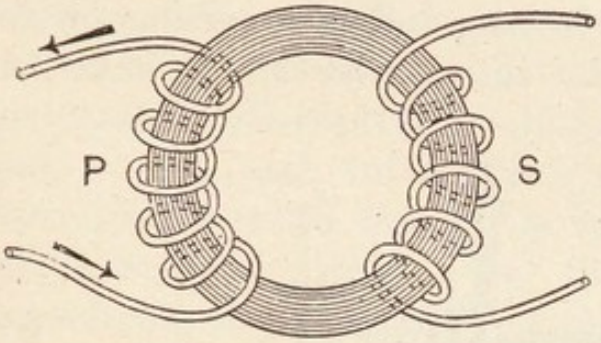


FIG. 148.—Faraday's Ring.

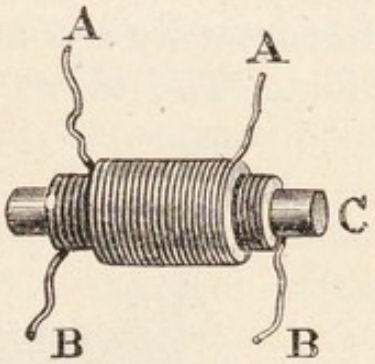


FIG. 149.—Faraday's Transformer.

and B (Fig. 149) were wound cylindrically outside one another upon a straight core C of iron.

In all transformers the electromotive-forces generated in the secondary circuit are, to those employed in the primary circuit, nearly in the same proportion as the relative numbers of turns in the two coils. For example, if the primary coil has 100 turns and the secondary has 2500 turns, the electromotive-force in the secondary circuit will be nearly twenty-five times as great as that used in the primary. By choosing the proper number of turns, the electromotive-force can be transformed either up or down.

246. The Induction Coil.—In order to generate enormously high electromotive-forces which shall be able to send sparks across air spaces that ordinary batteries working at less than 100 volts could not possibly pierce, advantage is taken of the transformer principle. To produce spark discharges there is used the apparatus depicted in Fig. 150, as improved by Callan, Sturgeon, Masson, Ruhmkorff, Apps, and others, and termed the **Induction Coil** or **In-**

ductorium. The induction coil consists of a cylindrical bobbin having a central iron core surrounded by a short inner or "primary" coil of stout wire, and by an outer "secondary" coil consisting of many thousand turns of very fine wire, very carefully insulated between its different parts. The primary circuit is joined to the terminals of a few cells, and in it are also included an interrupter (or automatic break), and a reversing switch or key. The object of the interrupter is to make and

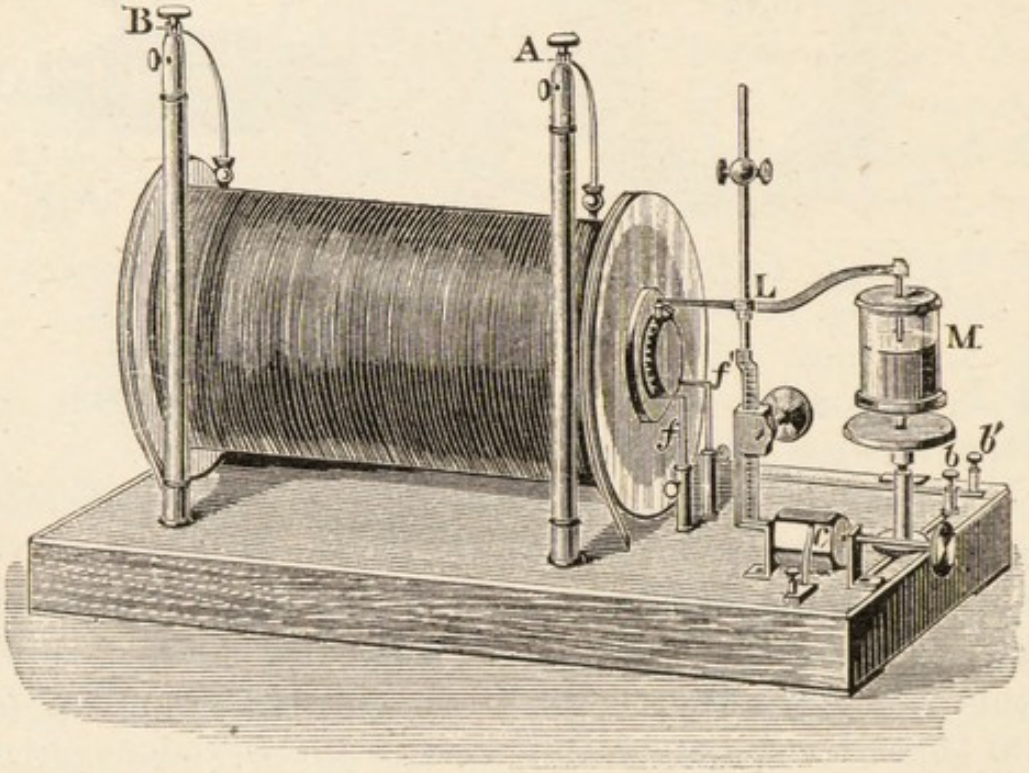


FIG. 150.—Induction Coil.

break the primary circuit in rapid succession. The result of this is at every "make" to induce in the outer "secondary" circuit a momentary inverse electromotive-force, and at every "break" a powerful momentary direct electromotive-force. As the number of magnetic lines created and destroyed at each "make" and "break" is the same, the two electromotive impulses are equal; but by the use of a condenser the current at "make" is caused to take a considerable fraction of time to grow, whilst at "break" the cessation is instantaneous. The *rate* of

cutting of the magnetic lines is therefore much greater at "break" than at "make." The induced electromotive-forces at "make" last longer, but are feebler, and do not suffice to send sparks. The currents at "break" manifest themselves as a brilliant torrent of sparks between the ends of the secondary wires when brought near enough together. The sparks are longer and only pass one way, but they differ merely in degree from those furnished by friction machines and by Leyden jars (Arts. 330, 333). For studying disruptive discharge and discharge through glass vessels and tubes from which the air has been partially exhausted the coil is very useful. The primary coil is made of stout wire, that it may carry strong magnetizing currents, and consists of few turns to keep the resistance low, and to avoid self-induction of the primary current on itself. The central iron core is for the purpose of increasing, by its great magnetic permeability, the number of lines of force that pass through the coils: it is usually made of a bundle of fine wires to avoid the induced currents which, if it were a solid bar, would be set circulating in it, and which would retard its rapidity of magnetization or demagnetization. The secondary coil is made with many turns, in order that the coefficient of transformation may be large; and as the induced electromotive-force will be thousands of volts, the resistance of this coil will be immaterial, and it may be made of the thinnest wire that can conveniently be wound. In Mr. Spottiswoode's giant Induction Coil (which yields a spark of 42½ inches' length in air, when worked with 30 Grove's cells), the secondary coil contains 280 miles of wire, wound in 340,000 turns, and has a resistance of over 100,000 ohms.

247. Interrupters.—The interrupters of induction coils are usually self-acting. That of Foucault, shown with the coil in Fig. 150, consists of an arm of brass L, which dips a platinum wire into a cup of mercury M, from which it draws the point out, so breaking circuit,

in consequence of its other end being attracted toward the core of the coil whenever it is magnetized; the arm being drawn back again by a spring when, on the breaking of the circuit, the core ceases to be a magnet. A more common interrupter on small coils is a "break," consisting of a piece of thin steel which makes contact with a platinum point, and which is drawn back by the attraction of the core on the passing of a current; and so makes and breaks circuit by vibrating backwards and forwards just as does the hammer of an ordinary electric bell.

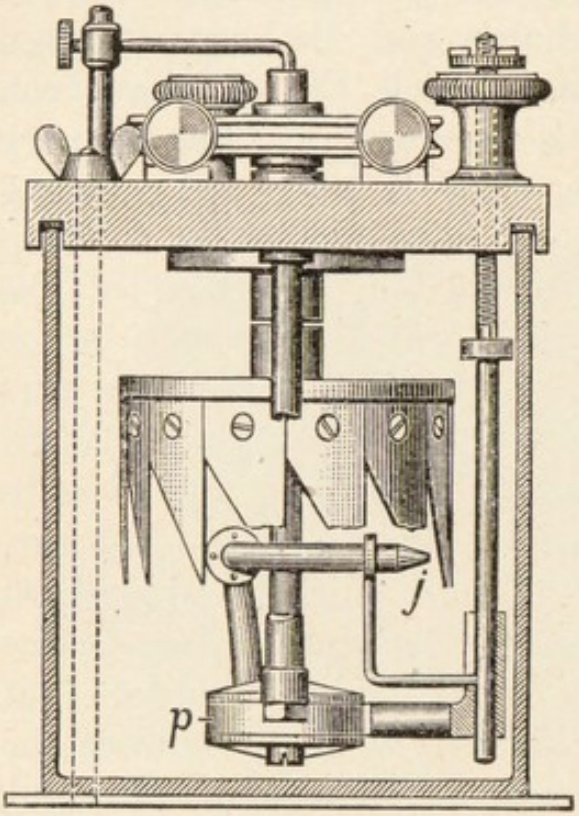


FIG. 151.—Mercury Break or Interrupter.

When an induction coil is required to supply an X-ray tube, a switch of the sprung contact type (Art. 207) connected in the primary circuit and rapidly operated by hand will act as a suitable interrupter. Rotary breaks or interrupters are largely used because of their high rate of interruption and the regularity of the contact periods. A small centrifugal pump p suitably rotated dips in mercury. The pump supplies a jet j with mercury which is directed on to a contact rod opposite, Fig. 151, but rotating on the same shaft as the pump are pointed sectors which periodically intercept the jet of mercury and thus break contact. The jet can be raised or lowered and so the time of contact varied. An electrolytic interrupter devised by Wehnelt consists of two electrodes dipping into a solution of sulphuric acid. The kathode is a lead plate, and the anode is a platinum

point on which bubbles of gas form, and escape, when a current is supplied to it; and so the current is broken by the bubbles and made again when they escape.

Associated with the primary circuit of a coil is usually a small *condenser* (see Art. 322), made of alternate layers of tinfoil and paraffined paper, into which the current flows whenever circuit is broken. The effect of the condenser is, as stated above, to suppress the "inverse" current at "make" and to increase greatly the "direct" electromotive force at "break." The condenser does this by the action known as electric *resonance* (see Art. 529). The sparks are longer, and only pass one way.

248. Ruhmkorff's Reverser.—In order to cut off or reverse the direction of the battery current at will,

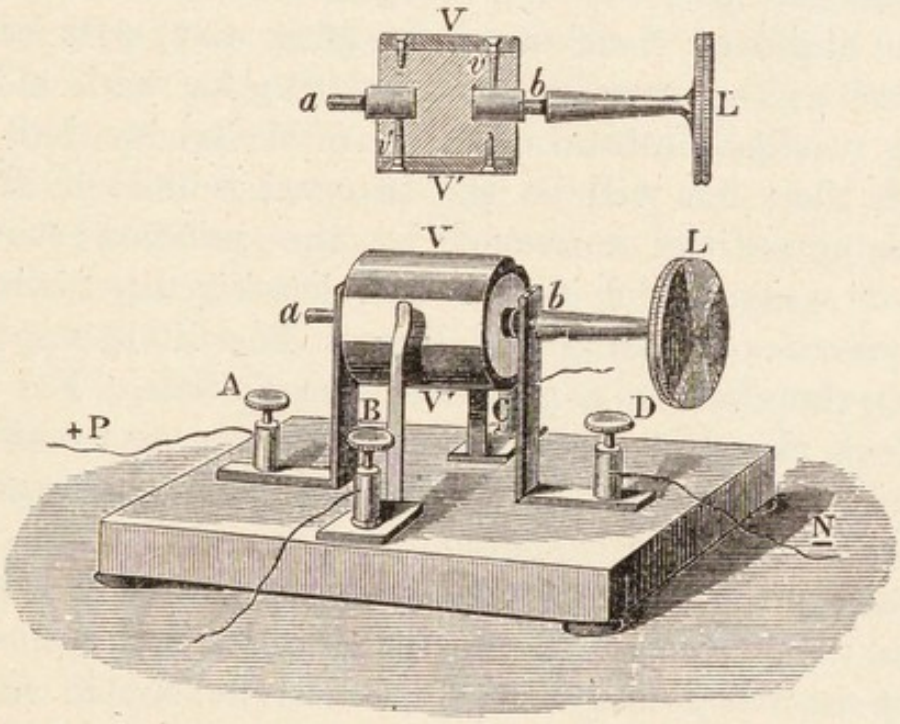


FIG. 152.—Ruhmkorff's Reverser.

Ruhmkorff applied the **current-reverser**, or reversing-switch ("commutator") shown in Fig. 152. In this instrument the battery poles are connected through the ends of the axis of a small ivory or ebonite cylinder to two cheeks of brass V and V′, which can be turned so as to place them either way in contact with two vertical

springs B and C, which are joined to the ends of the primary coil. Many other forms of reversing-switch have been devised; one, much used as a key for telegraphic signalling, is drawn in Fig. 343.

249. Induction Currents from Earth's Magnetism.—It is easy to obtain induced currents from the earth's magnetism. A coil of fine wire joined to a sensitive galvanometer, when suddenly inverted, cuts the lines of the earth's magnetism, and induces a current.

Faraday, indeed, applied this method to investigate the direction and number of magnetic lines. If a small wire coil be joined in circuit with a suitable galvanometer having a heavy needle, and the little coil be suddenly inverted while in a magnetic field, it will cut twice all the lines that pass through its own area, and the sine of half the angle of the first swing (Art. 451) will be proportional to the number of lines cut; for with a slow-moving needle, the total quantity of electricity that flows through the coils will be the integral whole of all the separate quantities conveyed by the induced currents, strong or weak, which flow round the circuit during the rapid process of cutting the lines. The little exploring coil acts therefore as a *magnetic proof-plane*. For small deflexions the first swing may be taken as a sufficient approximation instead of the sine of half the angle (see Art. 234).

If the circuit be moved parallel to itself across a uniform magnetic field there will be no induction currents, for just as many magnetic lines will be cut in moving ahead in front as are left behind. There will be no current in a wire moved parallel to itself along a line of force; nor if it lie along such a line while a current is sent through it, will it experience any mechanical force.

LESSON XIX.—*Chemical Actions of Currents*

250. Conducting Properties of Liquids.—In addition to the chemical actions inside the cells of the battery, which always accompany the production of a current, there are also chemical actions produced outside the battery when the current is caused to pass through certain liquids. Liquids may be divided into three classes—(1) *those which do not conduct at all*, such as turpentine and many oils, particularly petroleum; (2) *those which conduct without decomposition*, viz. mercury and other molten metals, which conduct just as solid metals do; (3) *those which are decomposed when they conduct a current*, viz. the dilute acids, solutions of metallic salts, and certain fused solid compounds.

251. Decomposition of Water.—In the year 1800 Carlisle and Nicholson discovered that the voltaic current could be passed through water, and that in passing through it decomposed a portion of the liquid into its constituent gases. These gases appeared in bubbles on the ends of the wires which led the current into and out of the liquid; bubbles of *oxygen* gas appearing at the place where the current entered the liquid, and *hydrogen* bubbles where it left the liquid. It was soon found that a great many other liquids, particularly dilute acids and solutions of metallic salts, could be similarly decomposed by passing a current through them.

252. Electrolysis.—To this process of decomposing a liquid by means of an electric current Faraday gave the name of **electrolysis** (*i.e.* electric analysis); and those substances which are capable of being thus decomposed or "electrolysed" he termed **electrolytes**.

The ends of the wires leading from and to the battery are called **electrodes**; and to distinguish them, that by which the current enters is called the **anode**, that by which it leaves the **kathode**. The vessel in which a

liquid is placed for electrolysis is termed an *electrolytic cell.*

253. Electrolysis of Water.—Returning to the decomposition of water, we may remark that perfectly pure water appears not to conduct, but its resistance is greatly reduced by the addition of a few drops of sulphuric or hydrochloric acid. The apparatus shown in Fig. 153 is suitable for this purpose. Here a battery of two cells (those shown are circular Bunsen's cells) is seen

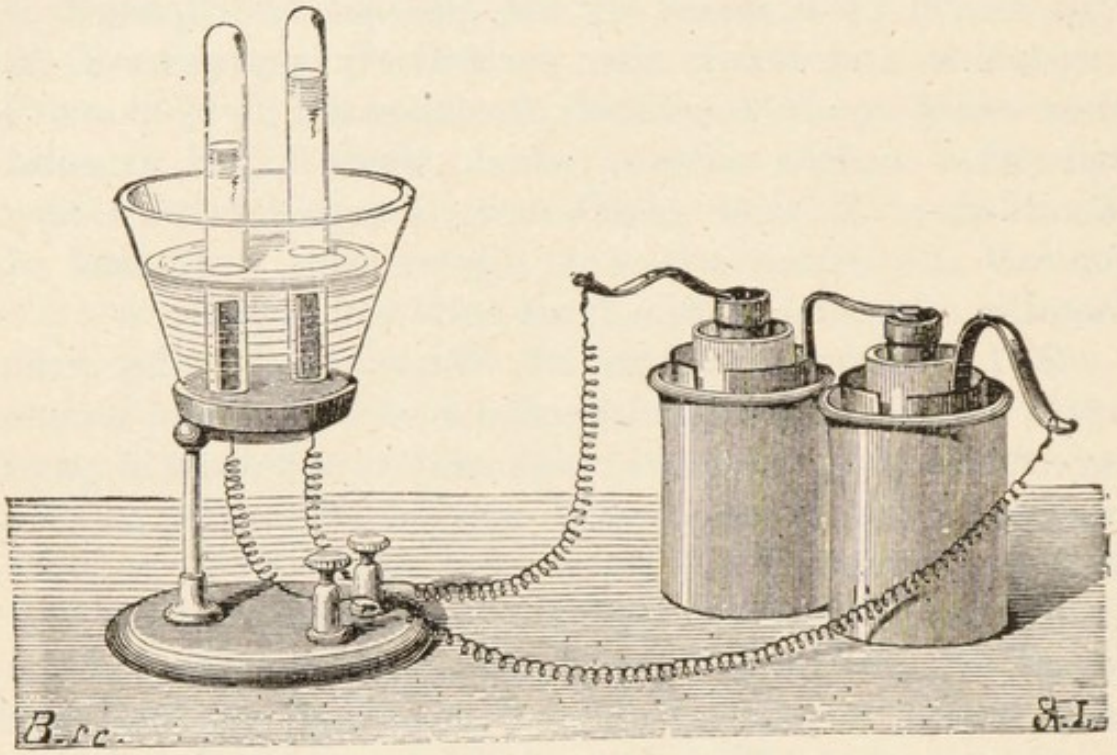


FIG. 153.—Water Voltameter.

with its poles connected to two strips of metallic platinum as electrodes, which project up into a vessel containing the acidulated water. Two tubes closed at one end, which have been previously filled with water and inverted, receive the gases evolved at the electrodes. Platinum is preferred to other metals such as copper or iron, for electrodes, since it is less oxidizable and resists every acid. It is found that there is almost exactly *twice* as much hydrogen gas (by volume) evolved at the kathode as there is of oxygen at the anode. This fact corresponds with the known chemical composition of water, which is

produced by combining together these two gases in the proportion of two volumes of the former to one of the latter. The proportions of gases evolved, however, are not *exactly* two to one, for at first a very small quantity of the hydrogen is absorbed or "occluded" by the platinum surface, while a more considerable proportion of the oxygen—about 1 per cent—is given off in the denser allotropic form of *ozone*, which occupies less space and is also slightly soluble in the water. When a sufficient amount of the gases has been evolved and collected they may be tested; the hydrogen by showing that it will burn, the oxygen by its causing a glowing spark on the end of a splinter of wood to burst into flame. If the two gases are collected together in a common receiver, the mixed gas will be found to possess the well-known explosive property of mixed hydrogen and oxygen gases. The chemical decomposition is expressed in the following equation:

H_2O	=	H_2	+	O
Water	yields	2 vols. of Hydrogen	and	1 vol. of Oxygen

254. Electrolysis of Sulphate of Copper.—We will take as another case the electrolysis of a solution of the well-known "blue vitriol" or sulphate of copper. If a few crystals of this substance are dissolved in water a blue liquid is obtained, which is easily electrolysed between two electrodes of platinum foil, by the current from a single cell of any ordinary battery. The chemical formula for sulphate of copper is $CuSO_4$. The result of the electrolysis is to split it up in two parts. Metallic copper is carried forward by the current and deposited in a film upon the kathode, leaving behind at the anode "sulphion," an easily decomposed compound of sulphur and oxygen, which is immediately acted upon by the water forming sulphuric acid and oxygen. This oxygen is liberated in bubbles at the anode. The chemical changes are thus expressed:

$CuSO_4$		=	Cu	+	SO_4
Sulphate of Copper		becomes	Copper	and	Sulphion;

SO_4	+	H_2O	=	H_2SO_4	+	O
Sulphion	and	water	produce	Sulphuric acid	and	Oxygen.

In this way, as the current continues to flow, copper is continually withdrawn from the liquid and deposited on the kathode, and the liquid gets more and more acid. If copper electrodes are used, instead of platinum, no oxygen is given off at the anode, but the copper anode itself dissolves away into the liquid at exactly the same rate as the copper of the liquid is deposited on the kathode.

255. Anions and Kations.—The atoms which thus are severed from one another and carried invisibly by the current to the electrodes, and there deposited, are obviously of two classes; some are carried backward or left behind at the anode, others are carried forward to the kathode. Faraday gave the name of **ions**[1] to these wandering atoms or groups of atoms; those going to the anode being **anions**, and those going to the kathode being **kations**. Anions are sometimes regarded as "electronegative," because they move as if attracted toward the + pole of the battery, while the kations are

[1] The term *ions*, as introduced by Faraday, was used by him in a wider sense than that adopted to-day by most electrochemists, to denote not only the single electrically charged atoms or groups of atoms, but also the substances so acting. In Art. 824 of his *Experimental Researches* he wrote: "Then, again, the substances into which these [the decomposable substances or electrolytes] divide, under the influence of the electric current form an exceedingly important general class. . . . I have proposed to call these bodies generally *ions*, or particularly *anions* and *cations*, according as they appear at the *anode* or *cathode*; and the numbers representing the proportions in which they are evolved *electrochemical equivalents*. Thus hydrogen, oxygen, chlorine, iodine, lead, tin, are ions." Or again, Art. 829, "A body decomposable by the electric current, *i.e.* an *electrolyte*, must consist of two *ions*, and must also render them up during the act of decomposition." Nowadays electrochemists do not call the *substance* hydrogen an ion: they would say one atom of hydrogen plus its atomic charge is one hydrogen ion.

regarded as "electropositive." Hydrogen and the metals are kations, moving apparently *with* the direction assumed as that of the current, and are deposited where the current leaves the electrolytic cell. The anions are oxygen, chlorine, etc. When, for example, chloride of tin is electrolysed, metallic tin is deposited on the kathode, and chlorine gas is evolved at the anode.

256. Quantitative Laws of Electrolysis.

(i.) *The amount of chemical action is equal at all points of a circuit.* If two or more electrolytic cells are placed at different points of a simple circuit the amount of chemical action will be the same in all, for the same quantity of electricity flows past every point of the circuit in the same time. If all these cells contain acidulated water, the quantity, for example, of hydrogen set free in each will be the same; or, if they contain a solution of sulphate of copper, identical quantities of copper will be deposited in each. If some of the cells contain acidulated water, and others contain sulphate of copper, the weights of hydrogen and of copper will not be *equal*, but will be in chemically *equivalent* quantities.

(ii.) *The amount of substance liberated at an electrode in a given time is proportional to the strength of the current.* A current of two *amperes* will cause just twice the quantity of chemical decomposition to take place as a current of one *ampere* would do in the same time.

(iii.) *The amount of substance liberated at an electrode in one second is equal to the strength of the current multiplied by the "electro-chemical equivalent" of that substance.* It has been found by experiment that the passage of one *coulomb* of electricity through a solution of silver nitrate liberates 0·0011183 gramme of silver. Hence a current of i amperes will liberate $i \times 0{\cdot}0011183$ gramme of silver per second. The number 0·0011183 is called the *electrochemical equivalent* of silver. The "electrochemical equivalents" of other elements can be easily calculated if their chemical "equivalent" is known. Thus the chemical

"equivalent" of hydrogen is 1·008, while that of silver is 107·88. Hence the electrochemical equivalent of hydrogen will be $0{\cdot}0011183 \times 1{\cdot}008 \div 107{\cdot}88 = 0{\cdot}00001044$. Hence to liberate 1·008 grammes of hydrogen, or 107·88 grammes of silver, or the corresponding gramme-equivalent of any other element[1] will require the passage of 96550 coulombs. This number is sometimes called "the Faraday" number.

The chemical *equivalent* must not be confounded with the *atomic weight*. The atomic weight of copper is 63·57, that is to say, its atoms are 63·57 times as heavy as atoms of hydrogen. But in chemical combinations one atom of copper replaces, or is "worth," *two* atoms of hydrogen; hence the weight of copper *equivalent* to 1 of hydrogen is $63{\cdot}57 \div 2 = 31{\cdot}78$. In all cases the chemical "equivalent" is the quotient $\frac{\text{atomic weight}}{\text{valency}}$. The following table gives full statistical information.

All atoms that are uni-valent carry exactly the same minute quantity of electricity: all atoms that are divalent carry exactly twice that amount; all trivalent atoms carry three times the amount. Hence the inference that electricity itself exists in definite atomic quantities. Every atom conveys a quantity of electricity proportional to its valency, not to its weight.

[1] Faraday's remark in 1833 (*Experimental Researches*, Art. 869) was: "If we adopt the atomic theory or phraseology, then the atoms of bodies which are equivalents to each other in their ordinary chemical action, have equal quantities of electricity naturally associated with them." Maxwell, in 1873 (in his *Treatise on Electricity and Magnetism*, Art. 260), wrote:—"We may therefore assume that the number of molecules in an electrochemical equivalent is N, a number unknown at present, but which we may hereafter find means to determine. Each molecule, therefore, on being liberated from the state of combination parts with a charge whose magnitude is $1 \div N$. . . . This definite quantity of electricity we shall call the molecular charge. If it were known it would be the most natural unit of electricity."

[TABLE

TABLE OF ELECTROCHEMICAL EQUIVALENTS, ETC.

Substance.	Symbol.	Atomic Weight.	Valency.	Chemical Equivalent.	Electrochemical Equivalent (grammes per *coulomb*).
Kathionic—					
Hydrogen	H	1·008	1	1·008	0·00001044
Potassium	K	39·1	1	39·1	0·00040527
Sodium	Na	23·0	1	23·0	0·00023839
Gold	Au	197·2	3	65·73	0·00068129
Silver	Ag	107·88	1	107·88	0·0011183
Copper (Cupric)	Cu	63·57	2	31·78	0·00032945
,, (Cuprous)	Cu″	63·57	1	63·57	0·00065890
Mercury (Mercuric)	Hg	200	2	100	0·0010365
,, (Mercurous)	Hg″	200	1	200	0·002073
Tin (Stannic)	Sn	119	4	29·75	0·00030836
,, (Stannous)	Sn″	119	2	59·5	0·00061672
Iron (Ferric)	Fe	55·85	3	18·61	0·00019289
,, (Ferrous)	Fe″	55·85	2	27·92	0·00028934
Nickel	Ni	58·68	2	29·34	0·00030411
Zinc	Zn	65·37	2	32·68	0·00033873
Cadmium	Cd	112·4	2	56·2	0·00058251
Lead	Pb	207·1	2	103·5	0·00107278
Ammonium	NH_4	18·04	1	18·04	0·00018698
Anionic—					
Oxygen	O	16	2	8	0·00008292
Chlorine	Cl	35·46	1	35·46	0·00036754
Iodine	I	126·92	1	126·92	0·00131552
Bromine	Br	79·92	1	79·92	0·00082837
Cyanogen	CN	26·01	1	26·01	0·00026959
Hydroxyl	OH	17·01	1	17·01	0·00017631
Sulphion	SO_4	96·07	2	48·03	0·00049783

257. Weight of Element deposited.—The following equation embodies the rule for finding the weight of any given ion disengaged from an electrolytic solution during a known time by a current of known strength. Let i be the current (reckoned in *amperes*), t the time (in seconds), z the electrochemical equivalent, and w the weight (in grammes) of the element liberated; then

$$w = zit,$$

or, in words, *the weight* (in grammes) *of an element deposited by electrolysis is found by multiplying its electrochemical equivalent by the strength of the current* (in amperes), *and*

by the time (in seconds) *during which the current continues to flow.*

EXAMPLE.—A current from five Daniell's cells was passed through two electrolytic cells, one containing a solution of silver, the other acidulated water, for ten minutes. A tangent galvanometer in the circuit showed the strength of the current to be 0·5 *ampere*. The weight of silver deposited will be 0·0011183 × 0·5 × 10 × 60 = 0·3355 gramme. The weight of hydrogen evolved in the second cell will be 0·00001044 × 0·5 × 10 × 60 = 0·003132 gramme.

258. Voltameters.—The second of the above laws, that the amount of substance liberated in a given time is proportional to the current, is sometimes known as *Faraday's Law*, from its discoverer. Faraday pointed out that it affords a chemical means of measuring currents. He gave the name of **voltameter** to an electrolytic cell arranged for the purpose of measuring the current by the amount of chemical action which it effects.

259. Water-Voltameter.—The apparatus shown in Fig. 153 might be appropriately termed a Water-Voltameter, provided the tubes to collect the gases be graduated, so as to measure the quantities evolved. The weight of each measured cubic centimetre of hydrogen (at the standard temperature of 0° C., and pressure of 1 atmosphere) is known to be 0·00008988 gramme. Hence, if the number of cubic centimetres liberated during a given time by a current of unknown strength be ascertained, the mean strength of the current can be calculated by first reducing the volume to weight, and then dividing by the electrochemical equivalent, and by the time. Each *coulomb* of electricity liberates in its flow 0·1162 cubic centimetres of hydrogen, and 0·0581 c.c. of oxygen. If these gases are collected together in a *mixed-gas voltameter* there will be 0·1743 c.c. of the mixed gases evolved for every *coulomb* of electricity which passes. To decompose 9·008 grammes of water, liberating 1·008 grammes of H and 8 grammes of O, requires 96550 *coulombs* to

be sent through the liquid with an electromotive force of at least 1·47 *volts* (see Art. 566).

260. Copper and Silver Voltameters.—As mentioned above, if sulphate of copper is electrolysed between two electrodes of copper, the anode is slowly dissolved, and the kathode receives an equal quantity of copper as a deposit on its surface. One *coulomb* of electricity will cause 0·0003291 gramme to be deposited ; and to deposit one gramme weight requires a total quantity of 3038 *coulombs* to flow through the electrodes. A current of one *ampere* deposits in one hour 1·185 grammes of copper, or 4·0259 grammes of silver.

By weighing one of the electrodes before and after the passage of a current, the gain (or loss) will be proportional to the quantity of electricity that has passed. In 1879 Edison applied this method for measuring the quantity of electricity supplied to houses for electric lights in them ; a small copper voltameter being placed in a branch of the circuit which supplied the house, to serve as a meter. (For *supply meters* see Art. 460, p. 465).

261. Comparison of Voltameters with Galvanometers.—It will be seen that both *Galvanometers*

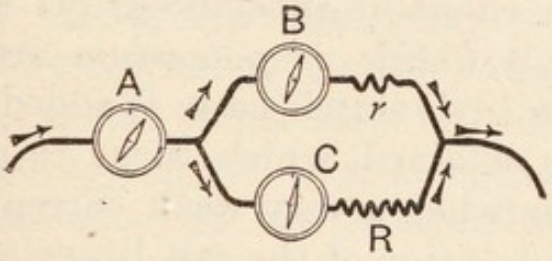


FIG. 154*a*.

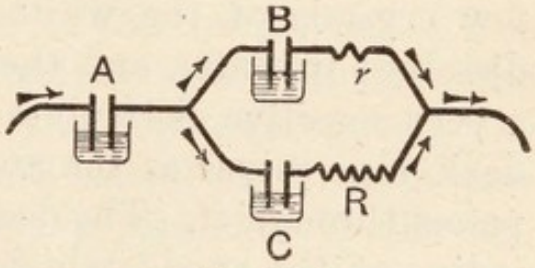


FIG. 154*b*.

and *Voltameters* are intended to measure the strength of currents, one by magnetic, the other by chemical means. Faraday demonstrated that the magnetic and the chemical actions of a current are proportional to one another. In Fig. 154*a* is shown a circuit that is branched so that the current divides, part going through a branch of small resistance r and part through a branch of larger resistance

R. The current will divide, the greater part going by the path of lesser resistance. Three amperemeters are used. It will be found that the number of *amperes* in the main circuit is equal to the sum of the *amperes* in the two branches. In Fig. 154*b* the three amperemeters have been replaced by three copper voltameters. The weight of copper deposited in the voltameter A in the main circuit will be found to be equal to the sum of the weights deposited in B and C in the two branches. A galvanometer shows, however, the strength of the current at any moment, and its variations in strength from one moment to another, by the position of the needle. In a voltameter, a varying current may liberate the atoms of copper or the bubbles of gas rapidly at one moment, and slowly the next, but all the varying quantities will be simply added together in the total yield. In fact, the voltameter gives us the "time integral" of the current. It tells us *what quantity of electricity* has flowed through it during the experiment, rather than *how strong the current was* at any one moment.

262. Chemical Test for Weak Currents.—A very feeble current suffices to produce a perceptible amount of change in certain chemical substances. If a few crystals of the white salt *iodide of potassium* are dissolved in water, and then a little starch paste is added, a very sensitive electrolyte is obtained, which turns to a dark blue colour at the anode when a very weak current passes through it. The decomposition of the salt liberates iodine at the anode, which, acting on the starch, forms a coloured compound. White blotting-paper, dipped into the prepared liquid, and then laid on the kathode and touched by the anode, affords a convenient way of examining the discoloration due to a current. A solution of ferrocyanide of potassium affords when using an anode of iron the well-known tint of Prussian blue. Bain proposed to utilize this in a Chemical Writing Telegraph, the short and long currents transmitted along the line

being thus recorded in blue marks on a strip of prepared paper, drawn along by clockwork under an iron stylus joined to the positive wire. Faraday showed that chemical discoloration of paper moistened with starch and iodide of potassium was produced by the passage of electricity from sources of all different kinds—frictional, voltaic, thermo-electric, and magneto-electric,—even by that evolved by the Torpedo and the Gymnotus (see Art. 77). In fact, he relied on this chemical test as one proof of the identity of the different kinds of electricity.

263. Internal and External Actions.—In an earlier lesson it was shown that the quantity of chemical action inside the cells of the battery was proportional to the current. Hence, Law (i.) of Art. 256 applies both to the portion of the circuit within the battery and to that without it.

Suppose 3 Daniell's cells are being employed to decompose water in a voltameter. Then while 1·008 gramme weight (11,620 cub. centims.) of hydrogen and 8 grammes (5810 c.c.) of oxygen are set free in the voltameter, 31·57 grammes of copper will be deposited in each cell of the battery, and (neglecting loss by local action) 32·5 grammes of zinc will be dissolved in each cell.

264. Reversibility.—It will be evident that the electrolytic cell is the *converse* of the voltaic cell. The chemical work done in the voltaic cell furnishes the energy of the current which that cell sets up in the circuit. In the electrolytic cell chemical work is performed, the necessary energy being furnished by the current of electricity which is sent into the cell from an independent battery or other source. It is important to note the bearing of this with respect to the energy of the circuit. Suppose a current of strength i to flow through a cell of which the electromotive-force is E, and which acts in the same direction as the current. The energy given to the circuit per second by this cell will be (Art. 454) the product of i and E; the chemical energy of the voltaic cell entering the circuit at the place where the

chemical action is going on. In Fig. 155 the current is indicated by the arrows with thick shafts, the electromotive-force by the feathered arrow. For example, if 10 amperes flow through a Daniell cell acting with 1·1 volts of electromotive-force, the power given out by the cell is 11 *watts* (Art. 454). But if the cell be so connected into the circuit, as in Case II. of Fig. 155, that the E.M.F. of the cell opposes the current that is being driven along the circuit, then the energy per second will be the product of i and $-E$, or $-iE$, the negative sign indicating that the circuit is losing energy, part of its energy being absorbed in the cell in doing chemical work.

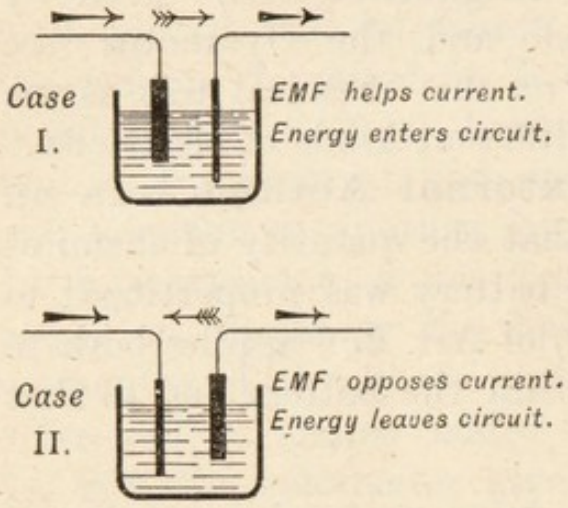


FIG. 155.

If the current is sent backwards through a Daniell cell the chemical processes are reversed, copper is dissolved and zinc is deposited. But all cells are not reversible in their chemical action.

The modern theory of electrolysis, and some examples of its application, are given in Art. 567 on Electrochemical Energy.

LESSON XX.—*Physical and Physiological Effects of the Current*

265. Molecular Actions.—Metal conductors, when subjected to the prolonged action of currents, undergo slow molecular changes. Wires of copper and brass gradually become brittle under its influence. During the passage of the current through metallic wires their cohesion is temporarily lessened, and there also appears to be a decrease in their coefficient of elasticity.

266. Electric Osmose.—Porret observed that if a strong current is led into certain liquids, as if to electrolyse them, a porous partition being placed between the electrodes, the current mechanically carries part of the liquid through the porous diaphragm, so that the liquid is forced up to a higher level on one side than on the other. This phenomenon, known as *electric osmose*, is most manifest when badly-conducting liquids, such as alcohol and bisulphide of carbon, are used. The transfer through the diaphragm takes place in the direction of the current; that is to say, the liquid is higher about the kathode than round the anode.

267. Electric Distillation.—Closely connected with the preceding phenomenon is that of the *electric distillation* of liquids. It was noticed by Beccaria that an electrified liquid evaporated more rapidly than one not electrified. In a bent closed tube, containing two portions of liquid, one of which is made highly + and the other highly −, the liquid passes over from + to −. This apparent distillation is not due to difference of temperature, nor does it depend on the extent of surface exposed, but is effected by a slow creeping of the liquid along the interior surface of the glass tubes. Bad conductors, such as turpentine, do not thus pass over.

268. Diaphragm Currents.—Quincke discovered that a current is set up in a liquid when it is forced by pressure through a porous diaphragm. This phenomenon is the converse of electric osmose. The E.M.F. so produced varies with the pressure and with the nature of the diaphragm. When water was forced at a pressure of one atmosphere through sulphur, the difference of potential was over 9 volts. With diaphragms of porcelain and bladder the differences were only 0·35 and 0·01 volts respectively.

269. Electro-Capillary Phenomena.—If a horizontal glass tube, turned up at the ends, be filled with dilute acid, and a single drop of mercury be placed at

about the middle of the tube, the passage of a current through the tube will cause the drop to move along towards the negative pole. The electrification of a surface modifies those properties which, like surface-tension depend on the condition of the surface. A charge of potential at the boundary surface between two liquids alters the electrification; and thus a movement results from the capillary forces. Lippmann, Dewar, and others have constructed upon this principle *capillary electrometers*, in which the pressure of a column of liquid is made to balance the electro-capillary force exerted at the surface of contact of mercury and dilute acid, the electro-capillary force being nearly proportional to the electromotive-force

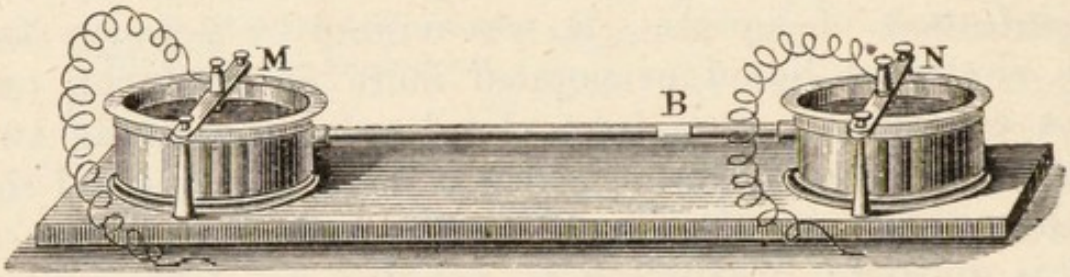


FIG. 156.—Capillary Electrometer.

when this does not exceed one volt. Fig. 156 shows the capillary electrometer of Dewar. A glass tube rests horizontally between two glass dishes in which holes have been bored to receive the ends of the tube. It is filled with mercury, and a single drop of dilute acid is placed in the tube. Platinum wires to serve as electrodes dip into the mercury in the dishes. An E.M.F. of only $\frac{1}{300}$ volt suffices to produce a measurable displacement of the drop. The direction of the displacement varies with that of the current.

270. Physiological Actions.—Currents of electricity passed through the limbs affect the nerves with certain painful sensations, and cause the muscles to undergo involuntary contractions. The sudden rush of even a small charge of electricity from a Leyden jar

charged to a high potential, or from an induction coil (see Fig. 150), gives a sharp and painful *shock* to the system. The current from a few strong Grove's cells, conveyed through the body by grasping the terminals with moistened hands, gives a very different kind of sensation, not at all agreeable, of a prickling in the joints of the arms and shoulders, but not producing any spasmodic contractions, except it be in nervous or weakly persons, at the sudden making or breaking of the circuit. The difference between the two cases lies in the fact that the tissues of the body offer a very considerable resistance, and that the difference of potential in the former case may be many thousands of volts; hence, though the actual quantity stored up in the Leyden jar is very small, its very high E.M.F. enables it at once to overcome the resistance. The battery, although it might, when working through a good conductor, afford in one second a thousand times as much electricity, cannot, when working through the high resistance of the body, and particularly of the skin, transmit more than a small fraction, owing to its limited E.M.F.

After the discovery of the *shock* of the Leyden jar by Cunæus in 1745 many experiments were tried. Louis XV. of France caused an electric shock from a battery of Leyden jars to be administered to 700 Carthusian monks joined hand in hand, with prodigious effect. Franklin killed a turkey by a shock from a Leyden jar.

In 1752 Sulzer remarked that "if you join two pieces of lead and silver, and then lay them upon the tongue, you will notice a certain *taste* resembling that of green vitriol, while each piece apart produces no such sensation." This **galvanic taste**, not then suspected to have any connexion with electricity, may be experienced by placing a silver coin on the tongue and a steel pen under it, the edges of them being then brought into metallic contact. The same taste is noticed if the two wires from the poles of a single voltaic cell are placed

in contact with the tongue. The saliva acts as an electrolyte.

Ritter discovered that a feeble current transmitted through the eyeball produces the sensation as of a bright *flash of light* by its sudden stimulation of the optic nerve. A stronger current flowing between the forehead and the hand gave a sensation of blue and green *colours*. Von Helmholtz, repeating this experiment, observed only a wild rush of colour. Dr. Hunter saw flashes of light when a piece of metal placed under the tongue was touched against another which touched the moist tissues of the eye. Volta and Ritter heard musical sounds when a current was passed through the ears; and Humboldt found a sensation to be produced in the organs of smell when a current was passed from the nostril to the soft palate. Each of the specialized senses can be stimulated into activity by the current. Man possesses no specialized sense for the perception of electrical forces, as he does for light and for sound; but there is no reason for denying the possibility that some of the lower creatures may be endowed with a special electrical sense.

The following experiment shows the effect of feeble currents on cold-blooded creatures. If a copper (or silver) coin be laid on a piece of sheet zinc, and a common garden snail be set to crawl over the zinc, directly it comes into contact with the copper it will suddenly pull in its horns, and shrink in its body. If it is set to crawl over two copper wires, which are then placed in contact with a feeble voltaic cell, it immediately announces the establishment of a current by a similar contraction.

271. Muscular Contractions.—In 1678 Swammerdam showed to the Grand Duke of Tuscany that when a portion of muscle of a frog's leg hanging by a thread of nerve bound with silver wire was held over a copper support, so that both nerve and wire touched the copper, the muscle immediately contracted. More than a century later Galvani's attention was drawn to the subject by

his observation of spasmodic contractions in the legs of freshly-killed frogs under the influence of the "return-shock" experienced every time a neighbouring electric machine was discharged. Unaware of Swammerdam's experiment, he discovered in 1786 the fact (alluded to in Art. 171 as leading ultimately to the discovery of the Voltaic Pile) that when nerve and muscle touch two

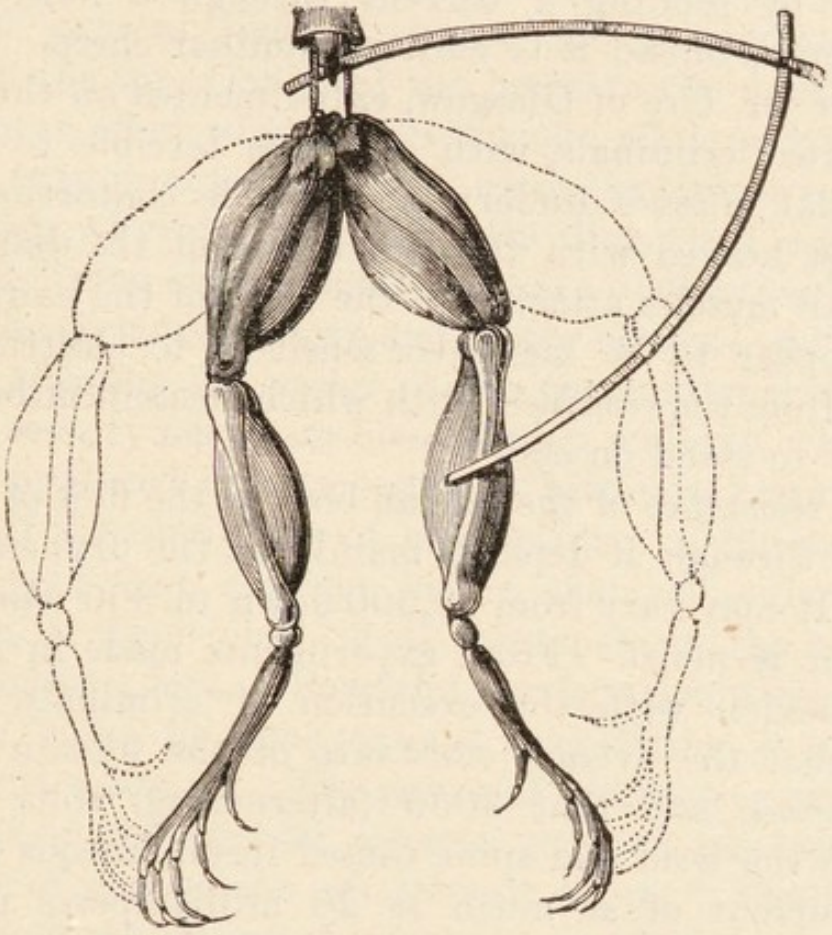


FIG. 157.—Muscular Contraction of Frog's Leg.

dissimilar metals in contact with one another a contraction of the muscle takes place. The limbs of the frog, prepared as directed by Galvani, are shown in Fig. 157. After the animal has been killed the hind limbs are detached and skinned; the crural nerves and their attachments to the lumbar vertebræ remaining. For some hours after death the limbs retain their contractile power. The frog's limbs thus prepared form an excessively delicate galvanoscope; with them, for example, the excessively

delicate induction-currents of the telephone (Lesson LVII.) can be shown, though the most sensitive galvanometers barely detect them. Galvani and Aldini proved that other creatures undergo like effects. With a pile of 100 pairs Aldini experimented on newly-killed sheep, oxen, and rabbits, and found them to suffer spasmodic muscular contractions. Humboldt proved the same on fishes ; and Zanotti, by sending a current through a newly-killed grasshopper, caused it to emit its familiar chirp. Aldini, and later Dr. Ure of Glasgow, experimented on the bodies of executed criminals, with a success terrible to behold. The facial muscles underwent horrible contortions, and the chest heaved with the contraction of the diaphragm. The small muscles attached to the roots of the hairs of the head appear to be markedly sensitive to electrical conditions from the readiness with which electrification causes the hair to stand on end.

The resistance of the human body to the flow of electric current through it depends mainly on the dryness of the skin. It may vary from 10,000 down to 300 *ohms* when the skin is moist. From experiments made in America in connexion with the execution of criminals, it was found that the average resistance of the human body is 2500 *ohms*, and that 3000 (alternating) volts applied between the head and spine caused instantaneous death.

A current of as much as 20 milliamperes produces terrible muscular contractions, whilst a current of 2 amperes traversing a vital part is almost certainly fatal. The effect of the current is two-fold ; in the first place it acts upon the nerves, causing spasms, secondly it destroys the tissue either by burning or by electrolysis, the blood becoming coagulated. To restore a person who has been rendered insensible by an electric shock, all the same restoratives should be used as for a person drowned. India-rubber gloves are worn by switch-board operators, as a protection, in high voltage stations.

272. Conditions of Muscular Contraction.—To

produce muscular contraction the current must traverse a portion of the nerve longitudinally. In a freshly-prepared frog the current causes a contraction only momentarily when the circuit is made or broken. A rapidly interrupted current will induce a second contraction before the first has had time to pass off, and the muscle may exhibit thus a continuous contraction resembling *tetanus*. The prepared frog after a short time becomes less sensitive, and a "direct" current (that is to say, one passing along the nerve in the direction from the brain to the muscle) only produces an effect when circuit is made, while an "inverse" current only produces an effect when the circuit is broken. Matteucci, who observed this, also discovered by experiments on living animals that there is a distinction between the conductivity of sensory and motor nerves,—a "direct" current affecting the motor nerves on making the circuit, and the sensory nerves on breaking it; while an "inverse" current produced inverse results. Little is, however, yet known of the conditions of conductivity of the matter of the nerves; they conduct better than muscular tissue, cartilage, or bone; but of all substances in the body the blood conducts best. Powerful currents doubtless electrolyse the blood to some extent, coagulating it and the albumin it contains. The power of *contracting* under the influence of the current appears to be a distinguishing property of *protoplasm* wherever it occurs. The amœba, the most structureless of organisms, suffers contractions. Ritter discovered that the *sensitive plant* shuts up when electrified, and Burdon Sanderson showed that this property extends to other vegetables, being exhibited by the *carnivorous plant*, the Dionæa or Venus's Fly Trap.

273. Animal Electricity.—Although, in his later writings at least, Galvani admitted that the electricity thus operating arose from the metals employed, he insisted on the existence of an *animal electricity* resident in the muscular and nervous structures. He showed that contractions could be produced without using any metals at

all by merely touching a nerve at two different points along its length with a morsel of muscle cut from a living frog; and that a conductor of one metal when joining a nerve to a muscle also sufficed to cause contraction in the latter. Galvani and Aldini regarded these facts as a disproof of Volta's contact-theory. Volta regarded them as proving that the contact between nerve and muscle itself produced (as in the case of two dissimilar metals) opposite electrical conditions. Nobili, later, showed that when the nerve and the muscle of the frog are respectively connected by a water-contact with the terminals of a delicate galvanometer, a *current* is produced which lasts several hours: he even arranged a number of frogs' legs in series, like the cells of a battery, and thus increased the current. Matteucci showed that through the muscle alone there may be an electromotive force. Du Bois Reymond has shown that if the end of a muscle be cut across, the *ends* of the muscular fibres of the transverse section are negative, and the *sides* of the muscular fibres are positive, and that this difference of potential will produce a current even while the muscle is at rest. To demonstrate this he employed a fine astatic galvanometer with 20,000 turns of wire in its coils; and to obviate errors arising from the contact of the ends of the wires with the tissues, *unpolarizable electrodes* were used, made by plunging terminal zinc points into a saturated solution of sulphate of zinc, contained in a fine glass tube, the end of which was stopped with a porous plug of moistened china clay. Normal muscle at rest shows no current whatever between its parts. Injured muscle at rest shows a current from the injured toward the uninjured part (returning toward the injured part through the galvanometer). Normal muscle when active shows a current from the active part toward the resting part. Du Bois Reymond obtained currents from his own muscles by dipping the tips of his forefingers into two cups of salt water communicating with the galvanometer terminals. A sudden contraction of the

muscles of either arm produced a current from the contracted toward the uncontracted muscles. Dewar has shown that when light falls upon the retina of the eye an electric current is set up in the optic nerve. Waller has investigated the electromotive-forces set up by the beating of the heart. These are best observed by using a string galvanometer (Art. 232) with photographic registration. In the skin, and especially in the skin of the common eel, there is an electromotive-force from without inwards.

274. Surgical Applications. — Electric currents have been successively employed as an adjunct in restoring persons rescued from drowning; the contraction of the diaphragm and chest muscles serving to start respiration. Since the discovery of the Leyden jar many attempts have been made to establish an electrical medical treatment. Discontinuous currents, particularly those furnished by small induction-coils and magneto-electric machines, are employed by practitioners to stimulate the nerves in paralysis and other affections. Living muscle when stimulated by a single shock such as a single spark from an electric machine causes a single muscular twitch, the contraction lasting about $\frac{1}{10}$ second. A rapid succession of shocks, such as is given by an induction coil or an alternating current, causes a succession of contractions which blend into a permanent state of contraction which lasts as long as the stimulating cause is applied. When a continuous current is used, not exceeding 4 or 5 milliamperes, there is a twitch on making the circuit followed by a relaxation that lasts as long as the current lasts, but with another twitch when the circuit is broken. With currents of 16 to 25 milliamperes the contraction is permanent till the current is cut off. In certain kinds of paralysis all irritability of muscle disappears. Application of electric stimulus in health generally slightly increases muscular power, and in debility after illness may aid nutrition.

The usual pathological dose of current is from 2 to 10 milliamperes. Apparatus pretending to cure, and incapable of furnishing such currents, is worthless. Continuous currents appear to produce a sedative effect around the anode, which is of service in neuralgia and painful affections, and an increase in irritability around the kathode, useful in certain cases of paralysis. In cases of paralysis due to lesion of nerve connexions or degeneration of nerve centres electricity is unavailing. The continuous current is also employed electrolytically to disperse tumours. Alternating currents, and rapidly interrupted uni-directional currents, stimulate the nerves. Bare metal electrodes must never be allowed to touch the skin unless the object is to produce sores. They should be covered with moist washleather.

275. Physiological Action of Magnets. — Magnets exercise no physiological action whatever, and the wearing of magnets in belts, armlets, or rings is of no curative value whatever. The author of these Lessons has however shown [1] that a rapidly-alternating magnetic field applied to the head produces certain curious phenomena as of flickering lights in the perception of vision. This is probably due to the induction of eddy-currents (Art. 500) in the optic nerves, and hence is electrical, not magnetic.

[1] See *Proceedings of the Royal Society*, vol. lxxxii. p. 396, 1910.

Part Second

CHAPTER IV

ELECTROSTATICS

Lesson XXI.—*Theory of Potential*

276. By the lessons in Chapter I. the student will have obtained some elementary notions upon the existence and measurement of definite quantities of electricity. In the present lesson, which is both one of the hardest and one of the most important to the beginner, and which he must therefore study the more carefully, the laws which concern the magnitude of electrical quantities and their measurement are more fully explained. In no branch of knowledge is it more true than in electricity, that "science is measurement." That part of the science of electricity which deals with the measurement of charges of electricity is called **Electrostatics.** We shall begin by discussing first the fundamental laws of electric force, which were brought to light in Chapter I. by simple experimental means.

277. First Law of Electrostatics. — *Electric charges of similar sign repel one another, but electric charges of opposite signs attract one another.* The fundamental facts expressed in this law were fully

explained in Lesson I. Though familiar to the student, and apparently simple, these facts require for their complete explanation the aid of advanced mathematical analysis. They will here be treated as simple facts of observation.

278. Second Law of Electrostatics.—*The force exerted between two charges of electricity* (supposing them to be collected at points or on two small spheres) *is directly proportional to their product and inversely proportional to the square of the distance between them.* This law, discovered by Coulomb, and called Coulomb's Law, was briefly alluded to (on p. 120) in the account of experiments made with the torsion-balance; and examples were then given in illustration of both parts of the law. We saw, too, that a similar law held good for the forces exerted between two magnetic point-poles. Coulomb applied the method of oscillations to verify the indications of the torsion-balance and found the results entirely confirmed. We may express the two clauses of Coulomb's Law in the following symbolic manner. Let f stand for the force, q for the quantity of electricity in one of the two charges, and q' for that of the other charge, and let r stand for the distance between them. Then,

(1) f is proportional to $q \times q'$,

and (2) f is proportional to $\frac{1}{r^2}$.

Choosing our units so that these two expressions may be combined into one, we may write our symbols as an equation:—

$$f = \frac{q \times q'}{r^2}.$$

279. Unit of Electric Quantity.—This equality is correct if our unit of electricity is chosen to accord with the units already fixed for measuring force and distance. Electricians of all nations have agreed in adopting a system based upon three fundamental units: viz. the

Centimetre as the unit of *length*; the **Gramme** as the unit of *mass*; the **Second** as the unit of *time*. All other units can be derived from these, as is explained in the Note at the end of this Lesson, pp. 276 and 277. Now, amongst the derived units of this system is the unit of *force*, named the **Dyne**, which is that force which, acting for one second on a mass of one gramme, imparts to it a velocity of one centimetre per second. Taking the dyne as the unit of force, and the centimetre as the unit of length (or distance), we must find for our equation a unit of electric quantity to agree with them. If q, q', and r have each of them unit value (that is, if we took two charges of value 1 each, and placed them one centimetre apart), the value of $\frac{q \times q'}{r^2}$ would be $\frac{1 \times 1}{1 \times 1}$, which is equal to 1. Hence our **Definition** of a *Unit of Electricity*[1] is:—*One Unit of Electricity is that quantity which, when placed at a distance of one centimetre (in air) from a similar and equal quantity, repels it with a force of one dyne.*

An example will aid the student to understand the application of Coulomb's Law.

Example. — Two small spheres, charged respectively with 6 units and 8 units of + electricity, are placed 4 centimetres apart; find what force they exert on one another. By the formula, $f = \frac{q \times q'}{r^2}$, we find $f = \frac{6 \times 8}{4^2} = \frac{48}{16} = 3$ *dynes.*

The force in the above example would clearly be a force of repulsion. Had one of these charges been negative, the product $q \times q'$ would have had a − value, and the answer would have come out as *minus* 3 dynes. The presence of the negative sign, prefixed to a force, will indicate that it is a force of *attraction*, whilst the plus sign would signify a force of *repulsion*.

[1] That is one unit, in the *electrostatic* system. It is only $\frac{1}{3,000,000,000}$ of the quantity called 1 *coulomb* (See Art. 301, p. 277.)

The intensity of an electric field (Art. 283) being measured by the force it exerts on a unit charge, it at once follows that at a distance of r (in air) from a charge q the intensity of the electric field due to that charge will be q/r^2. If the intervening medium be not air, but have a specific dielectric capacity k (see p. 295), the field will be only q/kr^2.

280. Potential.—We must next define the term *potential*, as applied to electric forces; but to make the meaning plain a little preliminary explanation is necessary. Suppose we had a + charge on a small insulated sphere A (see Fig. 158), placed by itself far from all other electric charges and conductors. If we were to bring another positively charged body B near it, A would repel B. But the repelling force would depend on the *quantity*

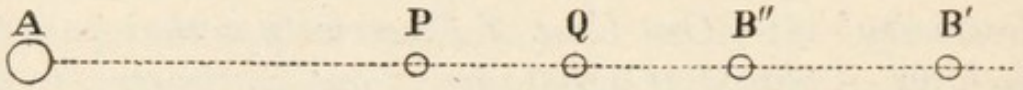


FIG. 158.

of the new charge, and on the *distance* at which it was placed. Suppose the new charge thus brought near to be one + unit; when B was a long way off it would be repelled with a very slight force, and very little work need be expended in bringing it up nearer against the repelling forces exerted by A; but as B was brought nearer and nearer to A, the repelling force would grow greater and greater, and more and more work would have to be done against these opposing forces in bringing up B. Suppose that we had begun at an infinite distance away, and that we pushed up our little test charge B from B′ to B″ and then to Q, and so finally moved it up to the point P, against the opposing forces exerted by A, we should have had to spend a certain amount of *work*; that work represents the *potential*[1] at the point P due to A.

[1] In its widest meaning the term "potential" must be understood as "power to do work." For if we have to do a certain quantity of work against the repelling force of a charge in bringing up a unit of electricity

For the following is the *definition* of **electric potential**:—*The potential at any point is the work that must be spent upon a unit of positive electricity in bringing it up to that point from an infinite distance.* Had the charge on A been a − charge, the force would have been one of attraction, in which case we should have theoretically to measure the potential at P, either by the opposite process of placing there a + unit, and then removing it to an infinite distance against the attractive forces, or else by measuring the amount of work which would be *done by* a + unit in being attracted up to P from an infinite distance.

It can be shown that where there are more electrified bodies than one to be considered, the potential due to them at any point is the sum of the potentials (at that point) of each one taken separately.

It can also be shown [1] that the potential at a point P, near an electrified particle A, is equal to the quantity of electricity at A divided by the distance between A and P. Or, if the quantity be called q, and the distance r, the potential is $q \div r$.

281. **Proof.**—*First determine* the difference of potential between point P and point Q due to a charge of electricity q on a small sphere at A.

Call distance AP $= r$, and AQ $= r'$. Then PQ $= r' - r$. The difference of potential between Q and P is the *work* done in moving a + unit from Q to P against the force; and since

work = (average) force × distance through which it is overcome

$V_P - V_Q = f(r' - r)$.

Force at P exerted by q on a + unit $= q/r^2$,

and the force at Q exerted by q on a + unit $= q/r'^2$.

---

from an infinite distance, just so much work has the charge power to do, for it will spend an exactly equal amount of work in pushing the unit of electricity back to an infinite distance. If we lift a pound five feet high against the force of gravity, the weight of the pound can in turn do five foot-pounds of work in falling back to the ground.

[1] The complete proof would require an elementary application of the integral calculus, but an easy geometrical demonstration, sufficient for present purposes, is given below.

Suppose now that the distance PQ be divided into any number (n) of equal parts rr_1, r_1r_2, r_2r_3, ... $r_{n-1}r'$.

The force at $r = q/r^2$.

" " $r_1 = q/r_1^2$ . . . . etc.

Now since r_1 may be made as close to r as we choose, if we only take n a large enough number, we shall commit no serious error

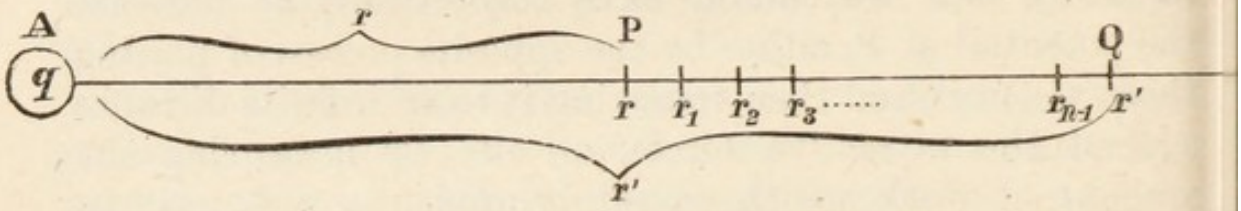


FIG. 159.

in supposing that $r \times r_1$ is a fair mean between r^2 and r_1^2: hence we may assume the *average* force over the short length from r to r_1 to be $\frac{q}{rr_1}$.

Hence the work done in passing from r_1 to r will be

$$= \frac{q}{rr_1}(r_1 - r)$$

$$= q\left(\frac{1}{r} - \frac{1}{r_1}\right).$$

On a similar assumption, the work done in passing from r_2 to r_1 will be

$= q\left(\frac{1}{r_1} - \frac{1}{r_2}\right)$, and that done from r_3 to r_2 will be

$= q\left(\frac{1}{r_2} - \frac{1}{r_3}\right)$, etc., giving us n equations, of which the last will be the work done in passing from r' to r_{n-1}

$$= q\left(\frac{1}{r_{n-1}} - \frac{1}{r'}\right).$$

Adding up all these portions of the work, the intermediate values of r cancel out, and we get for the work done in passing from Q to P

$$V_P - V_Q = q\left(\frac{1}{r} - \frac{1}{r'}\right).$$

Next suppose Q to be an infinite distance from A. Here r' = infinity, and $\frac{1}{r'} = 0$. In that case the equation becomes

$$V_P = \frac{q}{r}.$$

If there are a number of electrified particles at different distances from P, the potential due to each individual charge is unaffected by the presence of the other charges, and therefore *the potential at P can be found by dividing the quantity of each charge by its distance from the point P, and then adding up together the separate amounts so obtained.* The symbol V is generally used to represent potential. The potential at P we will call V_P, then

$$V_P = \frac{q'}{r'} + \frac{q''}{r''} + \frac{q'''}{r'''} + \ldots \text{ etc.}$$

or

$$V_P = \Sigma \frac{q}{r}.$$

This expression $\Sigma q/r$ represents the work done *on* or *by* (according as the potential at P is positive or negative), a unit of + electricity when moved up to the given point P from an infinite distance.

282. Zero Potential.—At a place infinitely distant from all electrified bodies there would be no electric forces and the potential would be zero. For purposes of convenience it is, however, usual to consider the potential of the earth as an arbitrary zero, just as it is convenient to consider "sea-level" as a zero from which to measure heights or depths (see Art. 287).

283. Difference of Potentials.—Since potential represents the work that must be done on a + unit in bringing it up from an infinite distance, the *difference of potential* between two points is *the work to be done on or by a + unit of electricity in carrying it from one point to the other.* Thus if V_P represents the potential at P, and V_Q the potential at another point Q, the difference of potentials $V_P - V_Q$ denotes the work done in moving up the + unit from Q to P. It is to be noted that since this value depends only on the values of the potential at P and at Q, and not on the values at intermediate points, the work done will be the same, whatever the path along which the particle moves from Q to P. In the same way

it is true that the expenditure of energy in lifting a pound (against the earth's attraction) from one point to another on a higher level, will be the same whatever the path along which the pound is lifted.

284. Electric Force.—The definition of "work" is the product of the force overcome into the distance through which the force is overcome; or **work = force × distance** through which it is overcome.

Hence, if the difference of potential between two points is the work done in moving up our + unit from one point to the other, it follows that the average *electric force* between those points will be found by dividing the work so done by the distance between the points; or $\frac{V_P - V_Q}{PQ} = f$ (the average electric force along the line PQ). The (average) electric force is therefore the rate of change of potential per unit of length. If P and Q are near together the force will be practically uniform between P and Q. The term *potential gradient*, or *electromotive intensity* is sometimes used for the force in an electric field.

We may map out the intensity of the electric field at any point by supposing the number of electric lines of force passing perpendicularly through one square centimetre to represent the number of dynes of force on a + unit placed at the point.

285. Equipotential Surfaces.—A charge of electricity collected on a small sphere acts on external bodies as if the charge were all collected into one point at its centre.[1] We have seen that the force exerted by such a charge falls off at a distance from the ball, the force becoming less and less as the square of the distance

[1] The student must be warned that this ceases to be true if other charges are brought very near to the sphere, for then the electricity will no longer be distributed *uniformly* over its surface. It is for this reason that we have said, in describing the measurement of electrical forces with the torsion balance, that "the balls must be very small in proportion to the distances between them."

increases. But the force is the same in amount at all points equally distant from the small charged sphere. And the potential is the same at all points that are equally distant from the charged sphere. If, in Fig. 159, the point A represents the sphere charged with q units of electricity, then the potential at P, which we will call V_P, will be equal to q/r, where r is the distance from A to P. But if we take any other point at the same distance from A its potential will also be q/r. Now all the points that are the same distance from A as P is, will be found to lie upon the surface of a sphere whose centre is

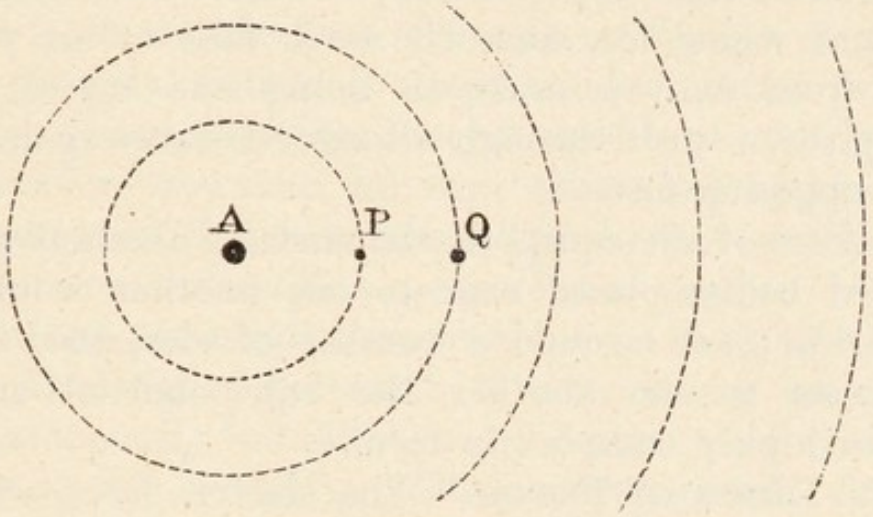


FIG 160.

at A, and which is represented by the circle drawn through P, in Fig. 160. All round this circle the potential will have equal values; hence this circle represents an **equipotential surface.** The work to be done in bringing up a + unit from an infinite distance will be the same, no matter what point of this equipotential surface it is brought to, and to move it about from one point to another in the equipotential surface requires no further overcoming of the electrical forces, and involves therefore no further expenditure of work. At another distance, say at the point Q, the potential will have another value, and through this point Q another equipotential surface may be drawn. Suppose we chose Q so far from P that

to push up a unit of + electricity against the repelling force of A required the expenditure of just one *erg* of work (for the definition of one *erg* see the Note on Units at the end of this lesson); there will be then *unit difference of potential* between the surface drawn through Q and that drawn through P, and it will require one *erg* of work to carry a + unit from any point on the one surface to any point on the other. In like manner we might construct a whole *system* of equipotential surfaces about the point A, choosing them at such distances that there should be unit difference of potential between each one and the next. The widths between them would get wider and wider, for, since the force falls off as you go farther from A, you must, in doing one *erg* of work, bring up the + unit through a longer distance against the weaker opposing force.

The form of the equipotential surfaces about two small electrified bodies placed near to one another would not be spherical; and around a number of electrified bodies placed near to one another the equipotential surfaces would be highly complex in form.

286. Lines of Force.—The electric force, whether of attraction or repulsion, always acts across the equipotential surfaces in a direction normal to the surface. The lines which mark the direction of the resultant electric forces are sometimes called lines of electric force. In the case of the single electrified sphere the lines of force would be straight lines, radii of the system of equipotential spheres. In general, however, lines of force are curved; in this case the resultant force at any point would be in the direction of the tangent to the curve at that point. Two lines of force cannot cut one another, for the resultant force at a point cannot act in two directions at once. The positive direction along a line of force is that direction in which a small positively charged body would be impelled by the electric force if free to move. A space bounded by a number of lines of force is

sometimes spoken of as a *tube of force*. All the space, for example, round a small insulated electrified sphere may be regarded as mapped out into a number of conical tubes, each having its apex at the centre of the sphere. The total electric force exerted across any section of a tube of force is constant wherever the section be taken.

287. Potential within a Closed Conductor.— The experiments related in Arts. 32 to 36 prove most convincingly that there is *no electric force inside a closed conductor due to charges outside or on the surface of the conductor*. Now we have shown above that electric force is the rate of change of potential per unit of length. If there is no electric force there is no change of potential. The potential within a closed conductor (for example, a hollow sphere) due to charges outside or on the surface is therefore the same all over the interior; the same as the potential of the surface. *The surface of a closed conductor is necessarily an equipotential surface.* If it were not at one potential there would be a flow of electricity from the higher potential to the lower, which would instantaneously establish equilibrium and reduce the whole to one potential. The student should clearly distinguish between the surface-density at a point, and the potential at that point due to neighbouring charges of electricity. We know that when an electrified body is placed near an insulated conductor the nearer and farther portions of that conductor exhibit induced charges of opposite kinds. Yet all is at one potential. If the + and − charges on the conductor had not separated by a movement of electricity from one side to the other, a difference of potential would exist between those sides because they are at different distances from the electrified body. But that is a state of affairs which could not continue in the conductor, for the difference of potential would cause electricity to flow until the combined potential due to the electrified body *and the charges at the opposite sides* was the same at every point in the conductor.

The potential at any point in a conducting sphere (hollow or solid) due to an electrified particle A, situated at a point outside (Fig. 162), is equal to the quantity of electricity q at A divided by the distance between A and the centre of the sphere. For if B be the centre of the sphere, the potential at B due to q is q/r, where $r = AB$; but all points in the sphere are at the same potential, therefore they are all at the potential q/r.

The earth is a large conducting sphere. Its potential, due to a positive charge q near to its surface, is q/r, where r may be taken as the radius of the earth; that is, 636,000,000 centimetres. But it is impossible to produce a + charge q without generating also an equal negative charge $-q$; so the potential of the earth due to both charges is $q/r - q/r = 0$ (see Art. 282).

288. Law of Inverse Squares.—An important consequence follows from the absence of electric force inside a closed conductor due to a charge on its surface; this fact enables us to demonstrate the necessary truth of the "law of inverse squares" which was first experimentally, though roughly, proved by Coulomb with the torsion balance. Suppose P to be a point anywhere inside a hollow sphere charged with electricity (Fig. 161). The charge is uniformly distributed over the surface of the sphere and the quantity of electricity on any small portion will be proportional to the area of that portion. Consider a small portion of the surface AB. The charge on AB would repel a + unit placed at P with a certain force. Now draw the lines AD and BC through P, and regard these as mapping out a small conical surface of two sheets, having its apex at P; the small area CD will

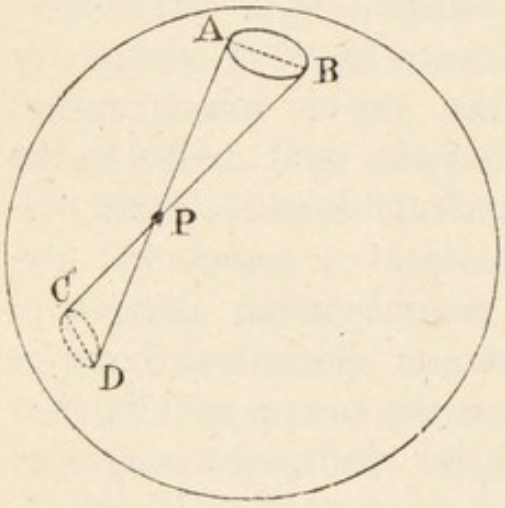


FIG 161

represent the end of the opposed cone, and the electricity on CD will also act on the + unit placed at P, and repel it. Now these areas AB and CD, and the charges on them, will be directly proportional to the *squares* of their respective distances from P. If, then, the forces which they exercise on P exactly neutralize one another (as experiment shows they do), it is clear that the electric force must fall off *inversely as the squares of the distances*; for the whole surface of the sphere can be mapped out similarly by imaginary cones drawn through P. The reasoning can be extended also to hollow conductors of any form.

289. Capacity.—In Lesson IV. the student was given some elementary notions on the subject of the Capacity of conductors. We are now ready to give the precise definition. The Electrostatic **Capacity** of a conductor is measured by *the quantity of electricity which must be imparted to it in order to raise its potential from zero to unity.* A small conductor, such as an insulated sphere of the size of a pea, will not want so much as one unit of electricity to raise its potential from 0 to 1; it is therefore of small capacity—while a large sphere will require a large quantity to raise its potential to the same degree, and would therefore be said to be of large capacity. If C stand for capacity, and Q for a quantity of electricity,

$$C = \frac{Q}{V} \quad \text{and} \quad CV = Q.$$

This is equivalent to saying in words that the quantity of electricity necessary to charge a given conductor to a given potential is numerically equal to the product of the capacity into the potential through which it is raised. The capacity of an insulated body is affected by the presence of neighbouring conductors. Whenever we speak of the capacity of a body, we mean of that body when *isolated* as well as insulated.

290. Unit of Capacity.—*A conductor that required*

only one unit of electricity to raise the potential between it and the earth from 0 to 1, would be said to possess **unit capacity.** A sphere one centimetre in radius possesses unit capacity; for if it be charged with a quantity of one unit, this charge will act as if it were collected at its centre. At the surface, which is one centimetre away from the centre, the potential, which is measured as q/r, will be 1. Hence, as 1 unit of quantity raises it to unit 1 of potential, the sphere possesses unit capacity. *The capacities of spheres (isolated in air) are proportional to their radii.* We may imagine the charge q (Fig. 162) being brought nearer and nearer the sphere until it reaches the surface, then r becomes the radius of the sphere. We may further imagine the surface completely covered with little quantities q, so as to have a total charge Q uniformly distributed. Each little quantity would give to the sphere a potential q/r; the total potential of the sphere due to the charge Q on its surface would be Q/r. The greater the sphere the less would be the potential at any point in it due to the same charge Q. Thus it would be necessary to give a charge of 100 units to a sphere of 100 centimetres' radius in order to raise its potential to unity. It therefore has a capacity of 100. The earth has a capacity of about 630 millions (in electro-static unit).[1] It is difficult to calculate the capacities of conductors of other shapes. It must be noted that the capacity of a sphere, as given above, means its capacity when far removed from other conductors or charges of electricity. The capacity of a conductor is increased by bringing near it a charge of an opposite kind; for the potential at the surface of the conductor is the sum of the potential due to its own charge, and of the potential of opposite sign due to the neighbouring charge. Hence, to bring up the resultant

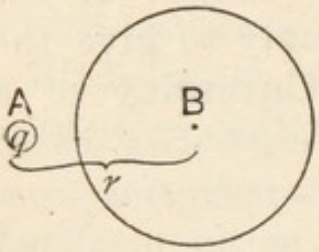


FIG. 162.

[1] Or about 700 microfarads (see Art. 301).

potential to unity, a larger quantity of electricity must be given to it; or, in other words, its capacity is greater. This is the true way of regarding the action of Leyden jars and other condensers, and must be remembered by the student when he advances to the consideration of the theory of condenser action, in Lesson XXIII.

291. Surface-Density.[1] — Coulomb applied this term to denote the amount of electrification per unit of area at any point of a surface. It was mentioned in Lesson IV. that a charge of electricity was never distributed uniformly over a conductor, except in the case of an insulated sphere. Where the distribution is unequal, the density at any point of the surface may be expressed by considering the quantity of electricity which exists upon a small unit of area at that point. If Q be the quantity of electricity on the small surface, and S be the area of that small surface, then the surface-density (denoted by the Greek letter ρ) will be given by the equation,

$$\rho = \frac{Q}{S}.$$

In dry air, the limit to the possible electrification is reached when the density reaches the value of about 20 units of electricity per square centimetre. If charged to a higher degree than this, the electricity escapes in "brushes" into the air. In the case of *uniform* distribution over a surface (as with the sphere, and as approximately obtained on a flat disk by a particular device known as a guard-ring), the density is found by

[1] The word Tension is sometimes used for that which is here precisely defined as Coulomb defined it. The term tension is, however, unfortunate; and it is so often misapplied in text-books to mean not only surface density but also potential, and even electric force (*i.e.* the mechanical force exerted upon a material body by electricity), that we might well avoid its use altogether. The term would be invaluable if we might adopt it to denote only the mechanical stress across a dielectric, as in Art. 297. This was Maxwell's use of the word, denoting a pulling force distributed over an area, just as the word pressure means a distributed pushing force.

dividing the whole quantity of the charge by the whole surface.

292. Surface-Density on a Sphere.—The surface of a sphere whose radius is r, is $4\pi r^2$. Hence, if a charge Q be imparted to a sphere of radius r, the surface-density will be $\rho = Q \div 4\pi r^2$; or, if we know the surface-density, the quantity of the charge will be $Q = 4\pi r^2 \rho$.

The surface-density on *two spheres* joined by a thin wire is an important case. If the spheres are unequal, they will share the charge in proportion to their capacities (see Art. 40), that is, in proportion to their radii. If the spheres are of radii 2 and 1, the ratio of their charges will also be as 2 to 1. But their respective densities will be found by dividing the quantities of electricity on each by their respective surfaces. But the surfaces are proportional to the squares of the radii, *i.e.* as 4 : 1 ; hence, the densities will be 1 : 2, or *inversely as the radii.* Now, if one of these spheres be very small—no bigger than a point — the density on it will be relatively immensely great, so great that the air particles in contact with it will rapidly carry off the charge by convection. This explains the *action of* **points** in discharging conductors, noticed in Chapter I., Arts. 38, 45, and 47.

293. Electric Images.—It can be shown mathematically that if $+q$ units of electricity are placed at a point near a non-insulated conducting sphere of radius r, at a distance d from its centre, the negative-induced charge will be equal to $-qr/d$, and will be distributed over the nearest part of the surface of the sphere with a surface-density inversely proportional to the cube of the distance from that point. Lord Kelvin pointed out that, so far as all external points are concerned, the potential due to this peculiar distribution on the surface would be exactly the same as if this negative charge were all collected at an internal point at a distance of $r - r^2/d$ behind the surface. Such a point may be regarded as a *virtual image* of the external point, in the same way as in optics we regard certain points behind mirrors as the virtual images of the external points from which the rays proceed. Clerk Maxwell has given the following **definition** of an Electric

Image :—*An electric image is an electrified point, or system of points, on one side of a surface, which would produce on the other side of that surface the same electrical action which the actual electrification of that surface really does produce.* If the sphere is not connected to earth, and were unelectrified before $+q$ was brought near it, we may find the surface-density at any point by the following convention. Imagine that there are coexisting on the sphere two charges, $-rq/d$ and $+rq/d$ respectively, the first being distributed so that its surface density is inversely proportional to the cube of the distance from the electrified point, and the second being uniformly distributed. The actual surface-density is the algebraic sum of these two. A + charge of electricity placed 1 inch in front of a flat metallic plate induces on it a negative charge distributed over the neighbouring region of the plate (with a density varying inversely as the cube of the distance from the point); but the electrical action of this distribution, so far as all points in front of the plate are concerned, would be precisely represented by its "image," namely, by an equal quantity of negative electricity placed at a point 1 inch *behind* the plate. Many beautiful mathematical applications of this method have been made, enabling the distribution to be calculated in difficult cases, as, for example, the distribution of the charge on the inner surface of a hollow bowl.

294. Force near a Charged Sphere. — It was shown above that the quantity of electricity Q upon a sphere charged until its surface-density was ρ, was

$$Q = 4\pi r^2 \rho.$$

The problem is to find the force exercised by this charge upon a + unit of electricity, placed at a point infinitely near the surface of the sphere. The charge on the sphere acts as if at its centre. The distance between the two quantities is therefore r. By Coulomb's Law the force $f = \dfrac{Q \times 1}{r^2} = \dfrac{4\pi r^2 \rho}{r^2} = 4\pi\rho.$

This important result may be stated in words as follows :—*The force* (in dynes) *exerted by a charged sphere upon a unit of electricity placed infinitely near to its surface, is numerically equal to* 4π *times the surface-density of the charge.*

295. Force near a Charged Plate of indefinite

size.—Suppose a plate of indefinite extent to be charged so that it has a surface-density ρ. This surface-density will be uniform, for the edges of the plate are supposed to be so far off as to exercise no influence. It can be shown that *the force exerted by such a plate upon a + unit* **anywhere near it,** *will be expressed* (in dynes) *numerically as* $2\pi\rho$. This will be of opposite signs on opposite sides of the plate, being $+ 2\pi\rho$ on one side, and $- 2\pi\rho$ on the other side, since in the two cases the force tends to move the unit in opposite directions. It is to be observed, therefore, that the force changes its value by the amount of $4\pi\rho$ as the point passes through the surface. The same was true of the charged sphere, where the force outside was $4\pi\rho$, and inside was zero. The same is true of all charged surfaces. These two propositions are of the utmost importance in the theory of Electrostatics.

296. Proof of Theorem.—The elementary geometrical proof is as follows :—

Required the Electric Force at a point at any distance from a plane of infinite extent charged to surface-density ρ.

Let P be the point, and PX or a the normal to the plane. Take any *small* cone having its apex at P. Let the solid angle

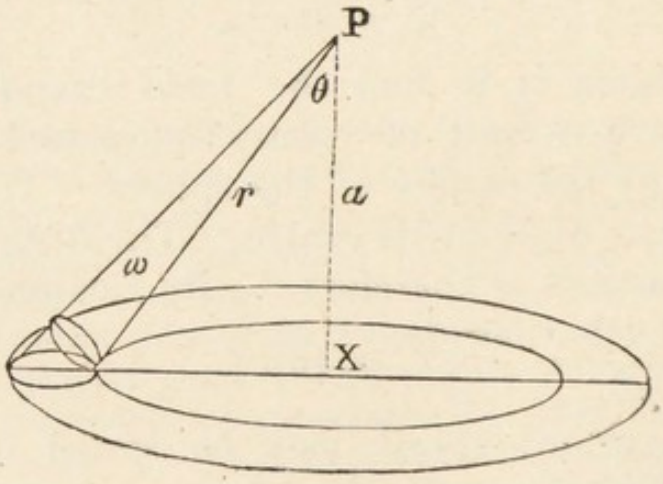


FIG. 163.

of this cone be ω; let its length be r; and θ the angle its axis makes with a. The cone meets the surface of the plane obliquely and if an orthogonal section be made where it meets the plane the angle between these sections will be $= \theta$.

Now solid angle ω is by definition $= \dfrac{\text{orthogonal area of section}}{r^2}$

Hence, area of oblique section $= r^2\omega \times \dfrac{1}{\cos\theta}$

$\therefore$ charge on oblique section $= \dfrac{r^2\omega\rho}{\cos\theta}$.

Hence if a + unit of electricity were placed at P, the force exerted on it by this small charge $= \dfrac{r^2\omega\rho}{\cos\theta} \times 1 \div r^2 = \dfrac{\omega\rho}{\cos\theta}$.

Resolve this force into two parts, one acting along the plane, the other along a, normal to the plane. The normal component along a is $\cos\theta \times \dfrac{\omega\rho}{\cos\theta} = \omega\rho$.

But the whole surface of the plane may be similarly mapped out into small surfaces, all forming small cones, with their summits at P. If we take an infinite number of such small cones meeting every part, and resolve their forces in a similar way, we shall find that the components along the plane will neutralize one another all round, while the normal components, or the resolved forces along a, will be equal to the sum of all their solid angles multiplied by the surface-density ; or

$$\text{Total resultant force along } a = \Sigma\omega\rho.$$

But the total solid angle subtended by an indefinite plane at a point is 2π, for it subtends a whole hemisphere.

$$\therefore \text{ Total resultant force } = 2\pi\rho.$$

297. Electric Stress in Medium. — In every electric field (Art. 13) there exists a *tension* along the lines of electric force accompanied by an equal *pressure* in all directions at right angles to the lines. If F stands for the resultant electric force on a + unit placed at any point in the field (*i.e.* the "electromotive intensity" at that point), the tension will be equal to $F^2/8\pi$ (dynes per square centimetre). In media having dielectric capacities greater than unity the tension is proportionally greater. For the optical effects of these stresses see Art. 612.

NOTE ON FUNDAMENTAL AND DERIVED UNITS

298. Fundamental Units.—All physical qualities, such as force, velocity, etc. can be expressed in terms of the three

fundamental quantities: *length*, *mass*, and *time*. Each of these quantities must be measured in terms of its own units.

The system of units, adopted by almost universal consent, and used throughout these lessons, is the so-called "Centimetre-Gramme-Second" system, in which the fundamental units are:—

The *Centimetre* as a unit of *length*;
The *Gramme* as a unit of *mass*;
The *Second* as a unit of *time*.

The *Centimetre* is equal to 0·3937 inch in length, and nominally represents one thousand-millionth part, or $\frac{1}{1,000,000,000}$ of a quadrant of the earth.

The *Metre* is 100 centimetres, or 39·37 inches.

The *Kilometre* is 1000 metres, or about 1093·6 yards.

The *Millimetre* is $\frac{1}{10}$ of a centimetre, or 0·03937 inch.

The *Gramme* represents the mass of a cubic centimetre of water at 4° C., this is equal to 15·432 grains: the *Kilogramme* is 1000 grammes and corresponds to about 2·2 pounds.

299. Derived Units.—

Area.—The unit of area is the *square centimetre.*

Volume.—The unit of volume is the *cubic centimetre.*

Velocity.—The unit of velocity is the velocity of a body which moves through unit distance in unit time, or the *velocity of one centimetre per second.*

Acceleration.—The unit of acceleration is that acceleration which imparts unit velocity to a body in unit time, or an acceleration of one centimetre-per-second per second. The acceleration due to gravity imparts in one second a velocity considerably greater than this, for the velocity it imparts to falling bodies is about 981 centimetres per second (or about 32·2 feet per second). The value differs slightly in different latitudes. At Greenwich the value of the acceleration of gravity is $g = 981{\cdot}1$; at the Equator $g = 978{\cdot}1$; at the North Pole $g = 983{\cdot}1$.

Force.—The unit of force is that force which, acting for one second on a mass of one gramme, gives to it a velocity of one centimetre per second. It is called one *Dyne.* The force with which the earth attracts any mass is usually called the "weight" of that mass, and its value obviously differs at different points of the earth's surface. The force with which a body gravitates, *i.e.* its weight (in dynes), is found by multiplying its mass (in grammes) by the value of g at the particular place where the force is

exerted. One pound force in England is about 445,000 dynes.

Work.—The unit of work is the work done in overcoming unit force through unit distance, *i.e.* in pushing a body through a distance of one centimetre against a force of one dyne. It is called one *Erg*. Since the "weight" of one gramme is 1×981 or 981 dynes, the work of raising one gramme through the height of one centimetre against the force of gravity is 981 ergs. One foot-pound of work (at London), that is the work done in raising one pound one foot high against the force of gravity (at London), equals 13,563,000 ergs.

Energy.—The unit of energy is also the *erg*; for the energy of a source is measured by the work it can do.

Power.—Power being the rate at which work is being done, the unit of power will be one erg per second. As this unit is inconveniently small, a unit ten million times larger, called the *Watt*, is taken as a practical unit of power. For larger quantities of power the *Kilowatt*, which is 1000 watts, is preferred. One *horse-power*, which by definition is 550 foot-pounds per second, is equal to 746 watts, or to 0·746 kilowatt.

Heat.—The unit of heat, the *calorie*, is the amount of heat required to warm one gramme mass of water one degree (Centigrade); and the dynamical equivalent of this amount of heat is 42 million *ergs*, which is known as Joule's equivalent, as expressed in C.G.S. measure (see also Art. 459).

These units are sometimes called "absolute" units; the term *absolute*, introduced by Gauss, meaning that they are independent of the size of any particular instrument, or of the value of gravity at any particular place, or of any other arbitrary quantities than the three standards of length, mass, and time. It is, however, preferable to refer to them by the more appropriate name of "C.G.S. units," as being derived from the centimetre, the gramme, and the second.

300. Electrical Units.—There are two systems of electrical units derived from the fundamental "C.G.S." units, one set being based upon the force exerted between two quantities of electricity, and the other upon the force exerted between two magnet poles. The former set are termed *electrostatic* units, the latter *electromagnetic* units. The important relation between the two sets is explained in Chap. V., Art. 386, p. 367.

301. Electrostatic Units. — No special *names* have been assigned to the electrostatic units of Quantity, Potential, Capacity, etc. The reasons for adopting the following values as units are given either in Chapter I. or in the present chapter.

Unit of Quantity.—The unit of quantity is that quantity of electricity which, when placed at a distance of one centimetre (in air) from a similar and equal quantity, repels it with a force of one *dyne* (Art. 279), p. 258.

Potential.—Potential being measured by *work* done in moving a unit of + electricity against the electric forces, the unit of potential will be measured by the number of ergs, per unit of electricity.

Unit Difference of Potential.—Unit difference of potential exists between two points, when it requires the expenditure of one *erg* of work to bring a + unit of electricity from one point to the other against the electric force (Art. 283).

Unit of Capacity.—Unit capacity exists between two conductors if the transfer of one unit of electricity from one to the other produces unit difference of potential between them. An isolated sphere of one centimetre radius possesses unit capacity (Art. 290), p. 269.

Specific Inductive Capacity, or *Inductivity*, is defined in Art. 315 as the ratio between two quantities of electricity. The specific inductive capacity of the air is, in the absence of any knowledge of its absolute value, taken as unity.

Electromotive Intensity or *Potential Gradient* is the electric force or intensity of an electric field at any point, and is measured by the force which it exerts on a unit charge placed at that point.

It may be convenient here to append the rules for reducing to their corresponding values in terms of the practical (electro-magnetic) units, values that may have been expressed in terms of the electrostatic units, as follows :—

Potential.	To bring to *volts* multiply by 300.
Capacity.	To bring to *microfarads* divide by 900,000.
Current.	To bring to *amperes* divide by 3×10^9.
Resistance.	To bring to *ohms* multiply by 9×10^{11}.
Quantity.	To bring to *coulombs* divide by 3×10^9.

To bring *coulombs* to *electrons*, multiply by 8×10^{18}.

To bring *electrostatic units of quantity* to *electrons*, multiply by $2{\cdot}67 \times 10^9$.

Example.—Suppose two equally charged spheres whose centres are 40 centimetres apart are found to repel one another with a force of 630 dynes (= about the weight of 10 grains). By the law of inverse squares we find that the charge on each is 1004 (electrostatic) units. Dividing by 3×10^9 we find that this amounts to 0·0000003347 *coulomb*.

302. Dimensions of Units.—It has been assumed above that a velocity can be expressed in centimetres per second; for velocity is rate of change of place, and it is clear that if change of place may be measured as a length in centimetres, the *rate* of change of place will be measured by the number of centimetres through which the body moves in unit of time. It is impossible, indeed, to express a velocity without regarding it as the quotient of a certain number of units of length divided by a certain number of units of time. In other words, a velocity $= \frac{\text{a length}}{\text{a time}}$; or, adopting L as a symbol for length, and T as a symbol for time, $V = L \div T$, which is still more conveniently written, $V = L \times T^{-1}$. In a similar way *acceleration* being rate of change of velocity, we have $A = \frac{V}{T} = \frac{L}{T \times T} = \frac{L}{T} = L \times T^{-2}$.

Now these physical quantities, "velocity" and "acceleration," are respectively *always* quantities of the same nature, no matter whether the centimetre, or the inch, or the mile, be taken as the unit of length, or the second or any other interval be taken as the unit of time. Hence we say that these abstract equations express the *dimensions* of those quantities with respect to the fundamental quantities length and time. A little consideration will show that the dimensions of the various units mentioned above will therefore be as given in the table following (next page).

The dimensions of magnetic units are given in the table in Art. 383, p. 364.

303. Scalar and Vector Quantities.—Scalar quantities are those which can be completely expressed by a number in terms of a unit, or quantities which do not imply direction. Such quantities are :—

time, temperature, numbers, area, volume, work, energy, resistance, inductance, capacity, etc.

Vector quantities are those which express a direction as well as a numerical value of their magnitude as compared with a unit. The following are vector quantities :—

length, velocity, acceleration, force, momentum, etc.

[TABLE

TABLE OF DIMENSIONS OF UNITS

	UNITS.	DIMENSIONS.
	(Fundamental)	
l	Length	L
m	Mass	M
t	Time	T
	(Derived)	
	Area = L × L =	L^2
	Volume = L × L × L =	L^3
v	Velocity = L ÷ T =	LT^{-1}
a	Acceleration = velocity ÷ time =	LT^{-2}
f	Force = mass × acceleration =	MLT^{-2}
	Work = force × length =	ML^2T^{-2}
	Power = work ÷ time =	ML^2T^{-3}
	(Electrostatic)	
q	Quantity $= \sqrt{\text{force} \times (\text{distance})^2}$ =	$M^{\frac{1}{2}}L^{\frac{3}{2}}T^{-1}k^{\frac{1}{2}}$
i	Current = quantity ÷ time =	$M^{\frac{1}{2}}L^{\frac{3}{2}}T^{-2}k^{\frac{1}{2}}$
V	Potential = work ÷ quantity =	$M^{\frac{1}{2}}L^{\frac{1}{2}}T^{-1}k^{-\frac{1}{2}}$
R	Resistance = potential ÷ current =	$L^{-1}T^{1}k^{-1}$
C	Capacity = quantity ÷ potential =	Lk^{1}
k	Sp. Ind. Capacity = quantity ÷ another quantity	a numeral
F	Electromotive Intensity = force ÷ quantity =	$M^{\frac{1}{2}}L^{-\frac{1}{2}}T^{-1}k^{-\frac{1}{2}}$

LESSON XXII.—*Electrometers*

304. In Lesson II. we described a number of *electroscopes* or instruments for *indicating* the presence and sign of a charge of electricity; some of these also served to indicate roughly the amount of these charges, but none of them save the torsion balance could be regarded as affording an accurate means of measuring either the

quantity or the *potential* of a given charge. *An instrument for measuring differences of electrostatic potential is termed an* **Electrometer.** Such instruments can also be used to measure electric *quantity* indirectly, for the quantity of a charge can be ascertained by measuring the potential to which it can raise a conductor of known capacity. The earliest electrometers attempted to measure the quantities directly. Lane and Snow Harris constructed "Unit Jars" or small Leyden jars, which, in order to measure out a certain quantity of electricity, were charged and discharged a certain number of times.

305. Repulsion Electrometers. — The torsion balance, described in Art. 18, measures quantities by measuring the forces exerted by the charges given to the fixed and movable balls. It can only be applied to the measurement of repelling forces, for the equilibrium is unstable in the case of a force of attraction.

Beside the gold-leaf and other electroscopes described in Lesson II., there exist several delicate electrometers based upon the principle of repulsion, some of which resemble the torsion balance in having a movable arm turning about a central axis. Amongst these are the electrometers of Dellmann and of Peltier. In the latter a light arm of aluminium, balanced upon a point, carries also a small magnet to direct it in the magnetic meridian. A fixed arm, in metallic contact with the movable one, also lies in the magnetic meridian. A charge imparted to this instrument produces a repulsion between the fixed and movable arms, causing an angular deviation. Here, however, the force is measured not by being pitted against the torsion of an elastic fibre, or against gravitation, but against the directive magnetic force of the earth acting on the small needle. Now this depends on the intensity of the horizontal component of the earth's magnetism at the place, on the magnetic moment of the needle, and on the sine of the angle of its deviation. Hence, to obtain quantitative values for the readings of this

electrometer, it is necessary to make preliminary experiments and to "calibrate" the degree-readings of the deviation.

306. Attracted-Disk Electrometers. — Snow Harris constructed an electrometer by measuring the attraction between an electrified and a non-electrified disk; and the instrument he devised may be roughly described as a balance for *weighing* a charge of electricity. The force exerted by an electrified *point* falls off inversely as the *square* of the distance, since the lines of force emanate in radial lines. But in the case of a uniformly electrified *plane surface*, the lines of force are normal to the surface, and parallel to one another; and the force is independent of the distance. The distribution over a small sphere nearly fulfils the first of these conditions. The distribution over a flat disk would nearly fulfil the latter condition, were it not for the perturbing effect of the edges of the disk where the surface-density is much greater (see Art. 38).

Lord Kelvin introduced into the construction of attracted-disk electrometers, the employment of the "guard-plate" and the providing of means for working with a definite standard of potential. It would be beyond the scope of these lessons to give a complete description of all the various forms of attracted-disk electrometer;[1] but the main principles of them all can be readily explained.

The disk C, whose attraction is to be measured, is suspended (Fig. 164) within a fixed guard-plate B, which surrounds it without touching it, and which is placed in metallic contact with it by a fine wire. A lever L supports the disk, and is furnished with a counterpoise. In order to know whether the disk is precisely level with the lower surface of the guard-plate a little gauge or

[1] For these the student is referred to the volume of Lord Kelvin's papers, "On Electrostatics and Magnetism"; or to Professor Andrew Gray's *Absolute Measurements in Electricity and Magnetism.*

index is fixed above, and provided with a lens l to observe its indications. Beneath the disk and guard-plate is a second disk A, supported on an insulating stand. This lower disk can be raised or lowered at will by a micrometer screw, great care being taken in the mechanical arrangements that it shall always be parallel to the plane of the guard-plate. Now, since the disk and guard-plate are in metallic connexion with one another, they form virtually part of one surface, and as the irregularities of distribution occur at the edges of the surface, the distribu-

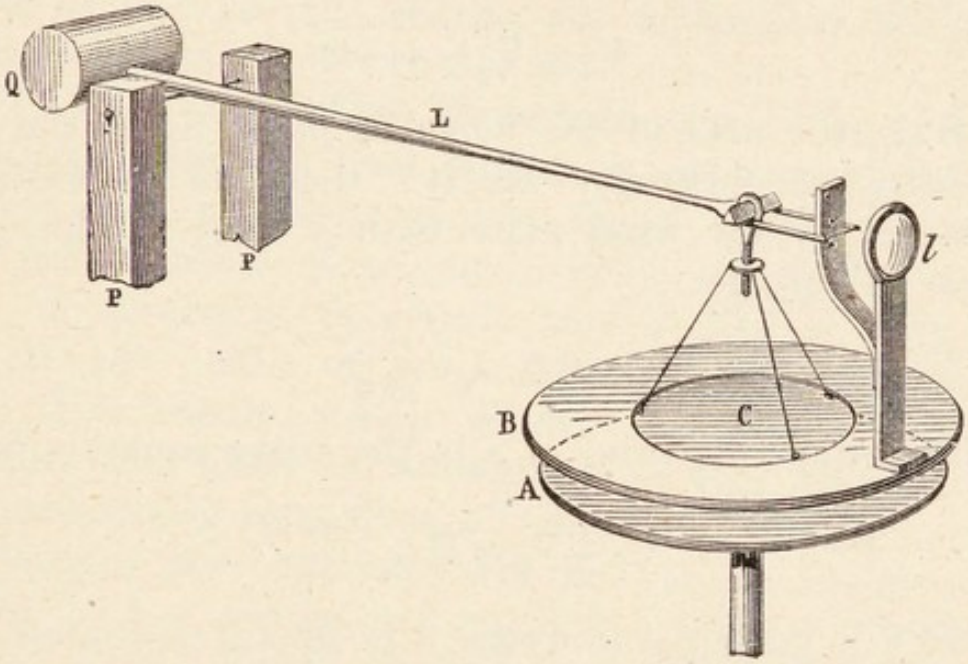


FIG. 164.—Attracted-Disk Electrometer, with Guard-Plate.

tion over the area of the disk is practically uniform. Any attraction of the lower plate upon the disk *might* be balanced either by increasing the weight of the counterpoise, or by putting a torsion on the aluminium wire which serves as a fulcrum; but in practice it is found most convenient to obtain a balance by altering the distance of the lower plate until the electric force of attraction exactly balances the forces (whether of torsion or of gravity acting on the counterpoise) which tend to lift the disk above the level of the guard-plate.

The theory of the instrument is simple also. Let V_1

represent the potential of the movable disk, which has a positive charge of surface-density ρ, and let V_2 be the potential of the fixed plate, upon which is a charge of surface-density $-\rho$. The difference of potential $V_1 - V_2$ is the work which would have to be done upon a unit of positive charge in taking it from V_2 to V_1. Now the force upon such a unit placed between the two plates would be (an attraction of $2\pi\rho$ due to the fixed plate, and a repulsion of $2\pi\rho$ due to the movable plate, see Art. 296) altogether $4\pi\rho$, and if the distance between the plates were D, work = force × distance.

$$V_1 - V_2 = 4\pi\rho D.$$

If S is the area of the movable plate, $S\rho$ is the total quantity of electricity on it; therefore it would be attracted by the fixed plate with a force $F = 2\pi\rho \times S\rho$. From this we get

$$\rho = \sqrt{\frac{F}{2\pi S}}.$$

Substituting this value of ρ in the above equation, we get

$$V_1 - V_2 = D\sqrt{\frac{8\pi F}{S}}.$$

If F is measured in dynes, S in square centimetres, and D in centimetres, the potentials will be in absolute electrostatic units, and must be multiplied by 300 to bring to *volts* (see Art. 301).

From this we gather that, if the force F remain the same throughout the experiments, *the difference of potentials between the disks will be simply proportional to the distance between them* when the disk is in level equilibrium. And the quantity $\sqrt{\frac{8\pi F}{S}}$ may be determined once for all as a "constant" of the instrument.

In the more elaborate forms of the instrument, such as the "**absolute electrometer**," and the "**portable electrometer**," the disk and guard-plate are covered

with a metallic cage, and are together placed in communication with a condenser to keep them at a known potential. This obviates having to make measurements with zero readings, for the *differences of potential* will now be proportional to *differences of micrometer readings*,

or,
$$V_1 - V_2 = (D_1 - D_2)\sqrt{\frac{8\pi F}{S}}.$$

The condenser is provided in these instruments with a *gauge*, itself an attracted disk, to indicate when it is charged to the right potential, and with a *replenisher* to increase or decrease the charge, the replenisher being a little influence machine (see Art. 50).

307. The Quadrant Electrometer.—The Quadrant Electrometer of Lord Kelvin is an example of a different class of electrometers, in which use is made of an auxiliary charge of electricity previously imparted to the needle of the instrument. The needle, which consists of a thin flat piece of aluminium hung horizontally by a fibre of thin wire, charged, say positively, will be attracted by a − charge, but repelled by a + charge. Such attraction or repulsion will be stronger in proportion to these charges, and in proportion to the charge on the needle. Four quadrant-pieces (Fig. 165) of brass are fixed horizontally below the needle without touching it or one another. Opposite quadrants are joined with fine wires. If quadrants 1 and 3 are ever so little + as compared with quadrants 2 and 4, the needle will turn away from the former to a position more nearly over the latter.

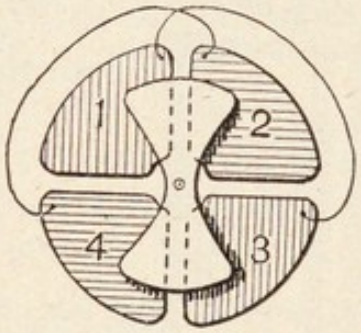


FIG. 165.—Needle and Quadrants of Quadrant Electrometer.

If there is the slightest difference of potential between the pairs of quadrants, the needle, which is held in its zero position by the elasticity of the wire, will turn, and so indicate the difference of potential. When these

deflexions are small, the scale readings will be very nearly proportional to the difference of potential. The instrument is sufficiently delicate to show a difference of potential between the quadrants as small as the $\frac{1}{70}$ of that of the Daniell's cell. If V_1 be the potential of one pair of quadrants, V_2 that of the other pair, and V_3 the potential of the needle, the force tending to turn will be proportional to $V_1 - V_2$, and will also be proportional to the difference between V_3 and the average of V_1 and V_2. Or, in symbols,

$$f = a\,(V_1 - V_2)\left(V_3 - \frac{V_1 + V_2}{2}\right);$$

where a is a constant depending on the construction of the particular instrument.

Fig. 166 shows a very simple form of the Quadrant Electrometer, as arranged for qualitative experiments. The four quadrants are enclosed within a glass case, and the needle, which carries a light mirror M below it, is suspended from a torsion head C by a very thin metallic wire F. It is electrified to a certain potential by being connected, through a wire attached to C, with a charged Leyden jar or other condenser. In order to observe the minutest motions of the needle, a reading-telescope and scale are so placed that the observer looking through the telescope sees an image of the zero of the scale reflected

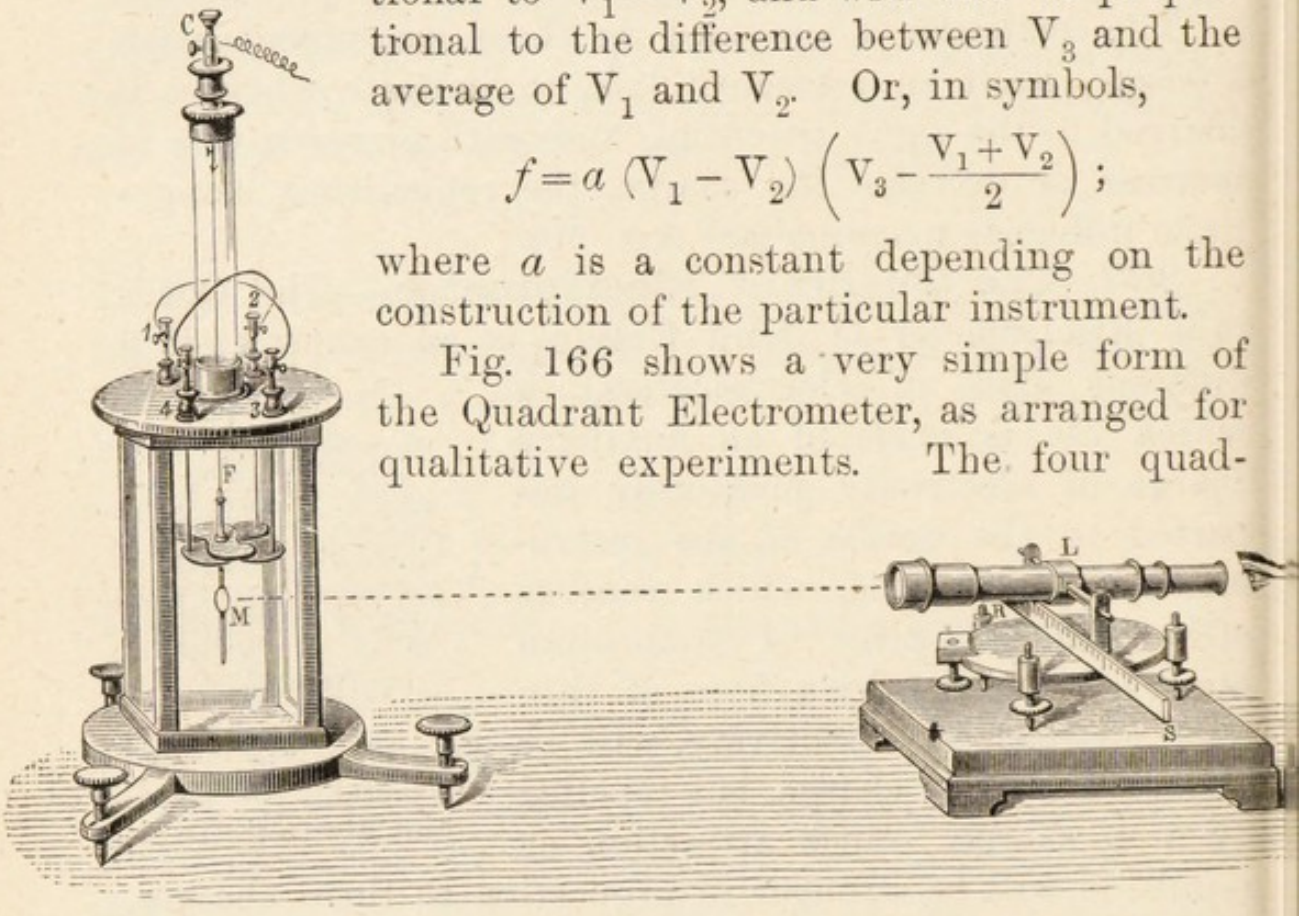


FIG. 166.—Simple Quadrant Electrometer.

in the little mirror. The wires connecting quadrants 1 and 3, 2 and 4, are seen above the top of the case.

For very exact measurements many additional refinements are introduced into the instrument. Two sets of quadrants are employed, an upper and a lower, having the needle between them. The torsion wire is replaced by a delicate bifilar suspension (Art. 132). To keep up the charge of the jar a "replenisher" (Art. 50) is added; and an "attracted-disk," like that of the Absolute Electrometer, is employed in order to act as a gauge to indicate when the jar is charged to the right potential. In these forms the jar consists of a glass vessel placed below the quadrants, coated externally with strips of tinfoil, and containing strong sulphuric acid, which serves the double function of keeping the apparatus dry by absorbing the moisture and of acting as an internal coating for the jar. It is also more usual to throw a spot of light from a lamp upon a scale by means of the little mirror (as described in the case of the Mirror Galvanometer, in Art. 228), than to adopt the subjective method with the telescope, which only one person at a time can use. When the instrument is provided with replenisher and gauge, the measurements can be made in terms of absolute units, provided the "constant" of the particular instrument (depending on the suspension of the needle, size and position of needle and quadrants, potential of the gauge, etc.) is once ascertained. In a recent form, due to Dolezalek, the sensitiveness is increased by suspending the needle by a quartz fibre as thin as $\frac{1}{100}$ millimetre, rendered conductive by depositing a film of silver upon it.

308. Use of Quadrant Electrometer.—An example will illustrate the mode of using the instrument. It is known that when the two ends of a thin wire are kept at two different potentials a current flows through the wire, and that if the potential is measured at different points along the wire, it is found to fall off in a perfectly uniform manner from the end that is at a high potential down to that at the low potential. At a point one quarter along the potential will have fallen off one quarter of the

whole difference. This could be proved by joining the two ends of the wire through which the current was flowing to the terminals of the Quadrant Electrometer, when one pair of quadrants would be at a high potential and the other at a low potential. The needle would turn and indicate a certain deflexion. Now, disconnect one of the pairs of quadrants from the low potential end of the wire, and place them in communication with a point one quarter along the wire from the high potential end. The needle will at once indicate that the difference of potential is but one quarter of what it was before.

Often the Quadrant Electrometer is employed simply as a very delicate electro*scope* in systems of measurement in which a difference of electric potential is measured by being balanced against an equal and opposite difference of potential, exact balance being indicated by there being *no* deflexion of the Electrometer needle. Such methods of experimenting are known as *Null Methods*, or *Zero Methods*.

309. Electrostatic Voltmeter.—We have seen that in the quadrant electrometer it is necessary to give the needle a high initial charge, the reason being that if there did not exist between the quadrants and the needle a much greater difference of potential than the small voltage we are measuring, the force tending to turn the needle would be too small to be conveniently observed. Where, however, we are dealing with high differences of potential a separately charged needle is not requisite; we may simply join one conductor to the needle and the other to a set of quadrants, and the force of attraction, which, other things being equal, increases as the square of the difference of potential, is sufficiently great to give reliable readings. This is known as the *idiostatic* method of using the instrument.

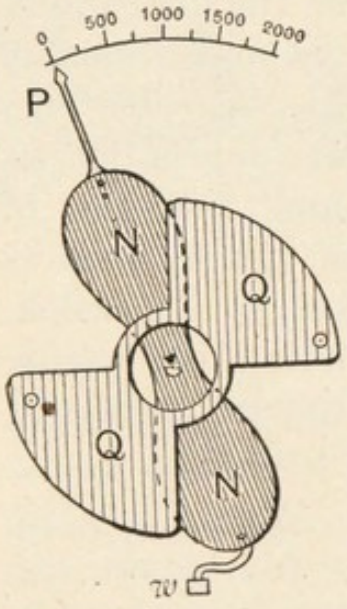


FIG. 167.—Electrostatic Voltmeter.

A front view of the instrument, as commonly used to measure differences of potential of 1000 volts or more, is shown in Fig. 167. The needle NN is a paddle-shaped plate of aluminium

supported by knife edges at its centre; its position is controlled by gravity, little weights being hung on a projection at its lower end. The quadrants Q are both behind and in front of it, and so placed that when a difference of potential exists between the needle and them, the needle is deflected from its normal position and moves its pointer over a graduated scale.

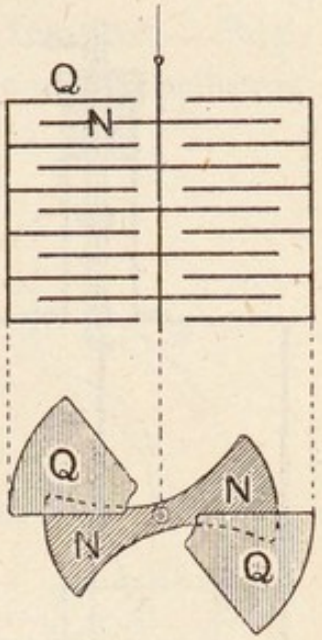


FIG. 168. — Multicellular Electrostatic Voltmeter.

It will be seen that it does not matter whether the needle is positively charged and the quadrants negatively charged or *vice versa*; an attraction between the two will always take place, so a deflexion will be given even when the difference of potential is rapidly alternating. This property of the instrument makes it exceedingly useful for the measurement of voltage when alternating currents are used.

Another advantage of this instrument over the high-resistance galvanometers that are used as voltmeters is, that it does not take any current, and consequently it does not waste any power.

In order to make the electrostatic voltmeter sufficiently delicate to measure down to 100 volts or so, a number of needles or vanes are placed horizontally one above the other on a vertical aluminium wire, and attracted by a tier of quadrants symmetrically placed on each side; this instrument is Lord Kelvin's *multicellular voltmeter*. It is shown in elevation and plan in Fig. 168.

310. Wilson's Electrometer.—In this instrument (Fig. 169) a single gold leaf is suspended in front of a vertical metal strip fixed at the top in an insulating bead of sulphur or to a piece of fused quartz. To charge it, a crooked wire which comes in through an ebonite plug at the top is turned to touch the metal support; then the

charge is imparted, and the charging wire turned out of contact, leaving the gold leaf diverging, by repulsion from the fixed strip. The deflexion of the gold leaf is observed by a microscope through a glass window in the case, or is projected upon a scale.

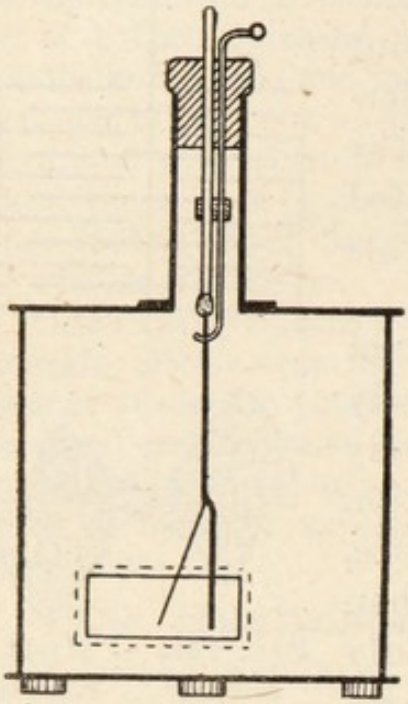


FIG. 169.—Wilson's Electrometer.

311. Dry-Pile Electrometer.—The principle of symmetry observed in the Quadrant Electrometer was previously employed in the Electroscope of Bohnenberger—a much less accurate instrument—in which the charge to be examined was imparted to a single gold leaf, placed symmetrically between the poles of a dry-pile (Art. 203), toward one or other pole of which the leaf was attracted. Fechner modified the instrument by connecting the + pole of the dry-pile with a gold leaf hanging between two metal disks, from the more + of which it was repelled. The inconstancy of dry-piles as sources of electrification led Hankel to substitute a battery of a very large number of small Daniell's cells.

312. Capillary Electrometers.—The Capillary Electrometer of Lippmann was described in Art. 269.

LESSON XXIII.—*Dielectric Capacity, etc.*

313. A Leyden jar or other condenser may be regarded as a conductor, in which (owing to the particular device of bringing near together the two oppositely-charged surfaces) the conducting surface can be made to hold a very large charge without its potential (whether + or −) rising very high. The capacity of a condenser, like that of a simple conductor, will be measured (see

Art. 289) by the quantity of electricity required to produce unit rise of potential.

314. Theory of Spherical Condenser.—Suppose a Leyden jar made of two concentric metal spheres, one inside the other, the space between them being filled by air. The inner one, A, will represent the interior coating of tinfoil, and the outer sphere, B (Fig. 170), will represent the exterior coating. Let the radii of these spheres be r and r' respectively. Suppose a charge of Q units to be imparted to A; it will induce on the inner side of B an equal negative charge $-Q$, and to the outer side of B a charge $+Q$ will be repelled. This latter is removed by contact with "earth," and need be no further considered. The potential[1] at the centre M, calculated by the rule given in Art. 280 will be

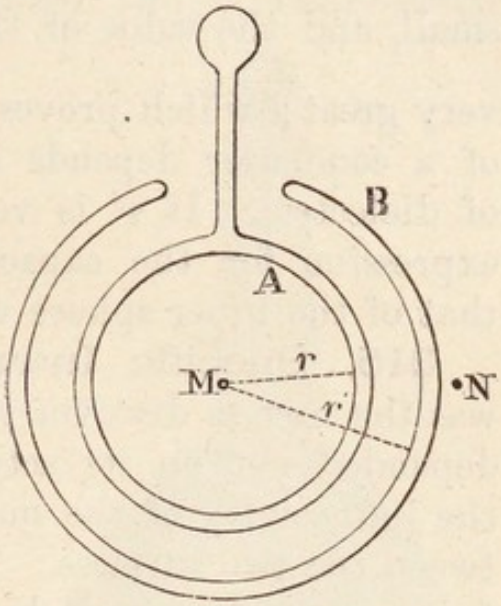


FIG. 170.—Spherical Condenser.

$$V_M = \frac{Q}{r} - \frac{Q}{r'}.$$

At a point N, outside the outer sphere and quite near to it, the potential will be the same as if these two charges, $+Q$ and $-Q$, were both concentrated at M. Hence

$$V_N = \frac{+Q - Q}{r'} = 0.$$

So then the difference of potentials will be

$$V_M - V_N = \frac{Q}{r} - \frac{Q}{r'} = Q\left(\frac{r' - r}{rr'}\right);$$

whence $$\frac{Q}{V_M - V_N} = \frac{rr'}{r' - r}.$$

But by Art. 289 the capacity $C = \frac{Q}{V_M - V_N}$,

therefore $$C = \frac{rr'}{r' - r}.$$

[1] As there is no electric force within a closed conductor, the potential at the middle is just the same as at any other point inside.

We see from this formula that the capacity of the condenser is proportional to the size of the metal globes, and that if the insulating layer is very thin,—that is, if r be very nearly as great as r', $r' - r$ will become very small, and the value of the expression $\frac{rr'}{r' - r}$ will become very great; which proves the statement that the capacity of a condenser depends upon the *thinness* of the layer of dielectric. If r' is very great compared with r, the expression for the capacity becomes equal simply to r, that of the inner sphere when isolated.

315. Specific Inductive Capacity.—Cavendish was the first to discover that the capacity of a condenser depended not on its actual dimensions only, but upon the inductivity of the material used as the dielectric between the two surfaces. If two condensers (of any of the forms to be described) be made of exactly the same size, and in one of them the dielectric be a layer of air, and in the other a layer of some other insulating substance, it is found that equal quantities of electricity imparted to them do not produce equal differences of potentials; or, in other words, it is found that they have not the same capacity. If the dielectric be mica, for example, it is found that the capacity is about six times as great; for mica possesses a high inductivity and allows electrostatic influence to act across it six times as well as air does. The name **inductivity**, or **specific inductive capacity**,[1] or **dielectric capacity**, is given to the ratio between the capacities of two condensers equal in size, one of them filled with the specified dielectric, the other being an air condenser. The inductivity of dry air at the temperature 0° C., and pressure 76 centimetres, is taken as the standard; and, in the absence of any known way of finding its absolute value, is reckoned

[1] This name is not a very happy one,—*inductivity* is better, and is the analogous term, for dielectrics, to the term "conductivity" used for conductors.

as unity. The symbol k is used to denote the inductivity of any material.

Cavendish, about the year 1775, measured the inductivity of glass, bees-wax, and other substances, by forming them into condensers between two circular metal plates, the capacity of these condensers being compared with that of an air condenser (resembling Fig. 41) and with other condensers which he called "trial-plates." He even went so far as to compare the capacities of these "trial-plates" with that of an isolated sphere of $12\frac{1}{2}$ inches diameter hung up in a room.

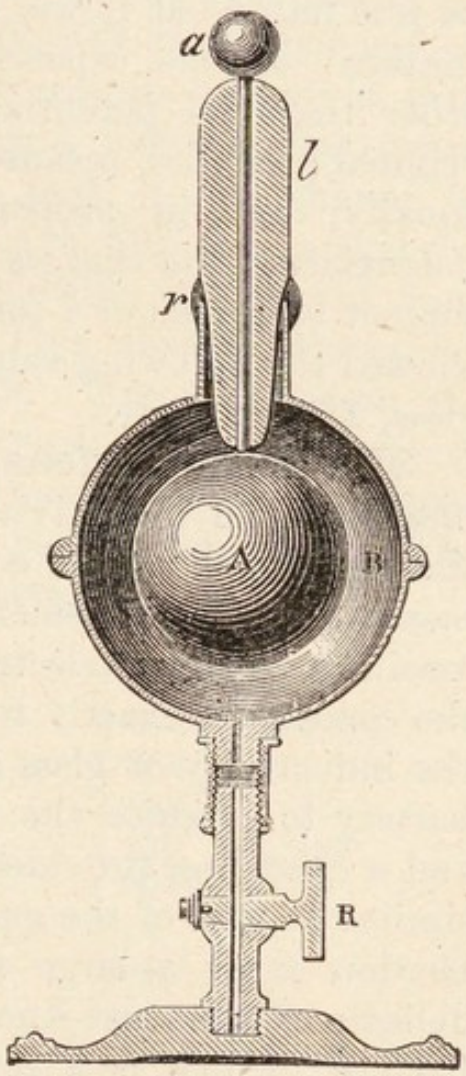


FIG. 171.—Faraday's Spherical Condenser.

316. Faraday's Experiments. — In 1837 Faraday, who did not know of the then unpublished researches of Cavendish, independently discovered inductivity, and measured its value for several substances, using for this purpose two condensers of the form shown in Fig. 171. Each consisted of a brass ball A enclosed inside a hollow sphere of brass B, and insulated by a long plug of shellac, up which passed a wire terminating in a knob a. The outer sphere consisted of two parts which could be separated from each other in order to fill the hollow space with any desired material: the experimental process then was to compare their capacities when one was filled with the substance to be examined, the other containing only dry air. One of the condensers was charged with electricity. It was then made to share its

charge with the other condenser, by putting the two inner coatings into metallic communication with one another; the outer coatings also being in communication with one another. If their capacities were equal they would share the charge equally, and the potential after contact would be just half what it was in the charged condenser before contact. If the capacity of one was greater than the other the final potential would not be exactly half the original potential, because they would not share the charge equally, but in proportion to their capacities. The potentials of the charges were measured before and after contact by means of a torsion balance.[1] Faraday's results showed the following values: Sulphur, 2·26; shellac, 2·0; glass, 1·76 or more.

317. Modern Measurements.—Gibson and Barclay measured the inductivity of paraffin wax by comparing the capacity of an air condenser with one of paraffin by means of an arrangement of sliding condensers, using a sensitive quadrant electrometer to adjust the capacity of the condensers exactly to equality. Hopkinson examined the inductivity of glass of various kinds, using a constant battery to produce the required difference of potentials, and a condenser provided with a guard-ring for a purpose similar to that of the guard-ring in absolute electrometers. Gordon made a large number of observations, using a delicate apparatus known as a statical "inductivity balance," which is a complicated condenser, so arranged in connexion with a quadrant electrometer that when the capacities of the separate parts are adjusted to equality there shall be no deflexion in the electrometer, whatever

[1] The value of the dielectric capacity k could then be calculated as follows:—

$$Q = VC = V'C + V'Ck$$

(where C is the capacity of the first apparatus and V its potential, and V′ the potential after communication with the second apparatus, whose capacity is Ck): hence

$$V = V'(1+k),$$

and

$$k = \frac{V - V'}{V'}$$

be the amount or sign of the electrification at the moment. This arrangement, when employed in conjunction with an induction coil (Fig. 150) and a rapid commutator, admits of the inductive capacity being measured when the duration of the actual charge is only very small, the electrification being reversed 12,000 times per second. Such an instrument, therefore, overcomes one great difficulty besetting these measurements, namely, that owing to the apparent absorption of part of the charge by the dielectric (as mentioned in Art. 62), the capacity of the substance, when measured slowly, is different from its "instantaneous" capacity. This electric absorption is discussed further in Art. 319. For this reason the values assigned by different observers for the inductivity of various substances differ to a most perplexing degree, especially in the case of the less perfect insulators. The following table summarizes the facts :—

Air	1·00	
Glass	3·013	to 3·258
Ebonite	2·284	
Guttapercha	2·462	
Indiarubber	2·220	to 2·497
Paraffin (solid)	1·9936	
Shellac	2·74	
Sulphur	2·58	
Mica	5·5	to 8

Hopkinson, whose method was a "slow" one, found for glass much higher inductivities, ranging from 6·5 to 10·1, the denser kinds having higher inductivity. Cavendish observed that the apparent capacity of glass became much greater at those temperatures at which it begins to conduct electricity. Boltzmann found that in the case of two crystalline substances, Iceland spar and sulphur, the inductivity is different in different directions, according to their position with respect to the axes of crystallization.

318. Inductivity of Liquids and Gases.—

The inductivity of liquids also has specific values, as follows :—

Pure Water	81·07
Aniline	7·30
Turpentine	2·16
Petroleum	2·03 to 2·07
Bisulphide of Carbon	1·81

Gases have inductivities which depend on the pressure at which they are used. If the inductivity of *vacuum* is taken as unity, that of air is slightly higher; the values for various gases being found as follows :—

Air	1·000586
Ammonia	1·00718
Carbon monoxide	1·000695
Carbon dioxide	1·000985
Ethylene	1·00146
Helium	1·000074
Hydrogen	1·000264
Nitrogen	1·000581
Nitrous oxide	1·00099
Sulphur dioxide	1·00905

The effect of using instead of air a medium of higher inductivity k is to change the forces exerted between charged bodies. For given fixed charges the forces vary *inversely* as k; while for given differences of potential between the bodies the forces vary *directly* as k.

319. Mechanical Effects of Dielectric Stress.— That different insulating substances have inductivity sufficiently disproves the idea that influence is merely an "action at a distance," for it is evident that the dielectric medium is itself concerned in the propagation of influence, and that some media allow influence to take place across them better than others. The existence of a residual charge (Art. 62) can be explained either on the supposition that the dielectric is composed of heterogeneous particles which have unequal conducting powers, as Maxwell has suggested, or on the hypothesis that the molecules are actually subjected to a strain from which,

especially if the stress be long continued, they do not recover all at once. Kohlrausch and others have pointed out the analogy between this phenomenon and that of the "elastic recovery" of solid bodies after being subjected to a bending or a twisting strain. A fibre of glass, for example, twisted by a certain force, flies back when released to *almost* its original position, a slight sub-permanent set remains, from which, however, it slowly recovers itself, the rate of its recovery depending upon the amount and duration of the original twisting strain. A quartz fibre never shows any sub-permanent set. Hopkinson has shown that it is possible to superpose several residual charges, even charges of opposite signs, which apparently "soak out" as the strained material gradually recovers itself. Perry and Ayrton also investigated the question, and have shown that the polarization charges in voltameters exhibit a similar recovery.[1] Air condensers exhibit no residual charges. Nor do plates of quartz cut from homogeneous crystal.

When a condenser is discharged a sound is often heard. This was noticed by Lord Kelvin in the case of air condensers; Varley and Dolbear constructed telephones in which the rapid charge and discharge of a condenser gave rise to musical tones and to articulate speech.

As to the precise nature of the molecular or mechanical operations in the dielectric when thus subjected to the stress of electrostatic induction, nothing is known. One pregnant experiment of Faraday is of great importance, by showing that influence is, as he expressed it, "an action of contiguous particles." In a glass trough (Fig. 172) is placed some oil of turpentine, in which are put some fibres of dry silk cut into small bits. Two wires

[1] It would appear, therefore, probable that Maxwell's suggestion of heterogeneity of structure, as leading to residual electrification at the bounding surface of the particles whose electric conductivities differ, is the true explanation of the "residual" charge. The phenomenon of elastic recovery may itself be due to heterogeneity of structure. Glass itself is a mixture of different silicates.

pass into the liquid, one of which is joined to earth, the other being put into connexion with the collector of an electrical machine. The bits of silk come from all parts of the liquid and form a quivering chain of particles from wire to wire, showing the electric lines of force. They at once disperse if the electric discharge is stopped. Faraday regarded this as typical of the internal actions in every case of influence across a dielectric, the particles of which he supposed to be "polarized," that is, to be turned into definite positions, each particle having a positive and a negative end. The student will perceive an obvious analogy, therefore, between the condition of the particles of a dielectric across which influence is taking place, and the molecules of a piece of iron or steel when subjected to magnetizing forces. Instead of silk, crystals of sulphate of quinine may be used in specially dried benzol. Or finely-divided sulphide of antimony may be strewn on the bottom of a glass dish and covered with a layer of petroleum, to show the electric lines of force.

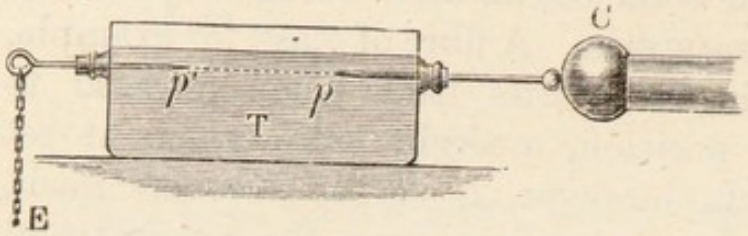


FIG. 172.—Faraday's Experiment on Action of the Dielectric.

Werner Siemens showed that the glass of a Leyden jar is sensibly warmed after being several times rapidly charged and discharged. This obviously implies that molecular movement accompanies the changes of dielectric stress. The phenomenon is called dielectric hysteresis.

320. Electric Expansion.—Fontana noticed that the internal volume of a Leyden jar increased when it was charged. Priestley and Volta sought to explain this by suggesting that the attraction between the two charged surfaces compressed the glass and caused it to expand laterally. Duter showed that the amount of apparent expansion was inversely proportional to the thickness of

the glass, and varied as the square of the potential difference. Quincke has observed that an apparent contraction is shown by resins and oily bodies under electrostatic stress.

321. Submarine Cables as Condensers.—A submarine telegraph cable may act as a condenser, the ocean forming the outer coating, the internal wire the inner coating, while the insulating layers of guttapercha serve as dielectric. When one end of a submerged cable is connected to, say, the + pole of a powerful battery, electricity flows into it. Before any signal can be received at the other end, enough electricity must flow

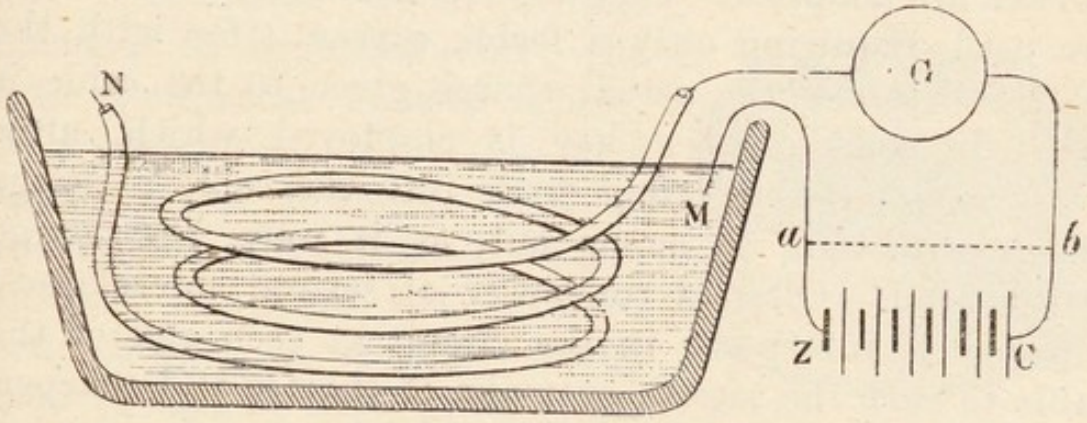


FIG 173.- Submarine Cable acts as a Condenser.

in to charge the cable to a considerable potential, an operation which may in the case of long cables require some seconds. Faraday predicted that this retardation would occur. It is, in actual fact, a serious obstacle to rapid signalling through Atlantic and other cables. Fleeming Jenkin devised the following experimental demonstration of the matter. Let a mile of insulated cable wire be coiled up in a tub of water (Fig. 173), one end N being insulated. The other end is joined up through a long-coil galvanometer G to the + pole of a large battery whose – pole is joined by a wire to the water in the tub. Directly this is done, the needle of the galvanometer will show a violent deflexion, electricity rushing through it into the interior of the

cable, and a – charge being accumulated on the outside of it where the water touches the guttapercha. For perhaps an hour the flow will go on, though diminishing, until the cable is fully charged. Now remove the battery, and instead join up *a* and *b* by a wire; the charge in the cable will rush out through the galvanometer, which will show an opposite deflexion, and the residual charge will continue "soaking out" for a long time.

Long land-lines carried overhead also possess a measurable capacity, and tend to retard the signals.

322. Condensers. — To obviate this retardation and increase the speed of signalling in cables[1] several devices are adopted. Very delicate receiving instruments are used, requiring only a feeble current; for with the feebler batteries the actual charge given to the cable is less. In some cases a key is employed which, after every signal, immediately sends into the cable a charge of opposite sign, to sweep out, as it were, the charge left behind. Often a condenser of several microfarads' capacity is interposed in the circuit at each end of the cable to *curb* the signal, or make it shorter and sharper, and by its reaction assist the discharge. In duplex signalling (Art. 586) the resistance and electrostatic capacity of the cable have to be met by balancing against them an "artificial cable" consisting of a wire of equal resistance, combined with a condenser of equal capacity. Messrs. Muirhead constructed for duplexing the Atlantic cable a condenser containing 100,000 square feet (over two acres of surface) of tinfoil. Condensers are also occasionally used on telegraph lines in single working to obviate disturbances from earth currents. They are constructed by placing sheets of tinfoil between sheets of mica or of paraffined paper, alternate sheets of foil being connected together. The paper is the finest bank-wove, carefully selected to be free from minute holes. Two

[1] The capacity of the "Direct" Atlantic cable from Ballinskelligs (Ireland) to Nova Scotia is 992 microfarads.

thicknesses, drawn through a bath of the purest paraffin wax heated till it melts, are laid between each foil and the next; care being taken to exclude air bubbles. When a sufficient number have been assembled hot they are put under pressure to cool, and afterwards adjusted. Small condensers of similar construction are used in connexion with induction coils (Fig. 150).

323. Standard Condensers.—Electricians adopt a *unit of capacity*, termed one **farad**, based on the system of electromagnetic units. A condenser of one farad capacity would be raised to a potential of one volt by a charge of one coulomb of electricity.[1] In practice such a condenser would be too enormous to be constructed; the earth itself, as an isolated sphere, has a capacity of only $\frac{7}{10000}$ of a farad. As a *practical unit* of capacity the **microfarad**, or one millionth of a farad, has therefore been chosen; a capacity about equal to that of three miles of an Atlantic cable. Condensers of only $\frac{1}{3}$ microfarad are about equal in capacity to one nautical mile of cable. They contain about 1200 square inches of foil. The dielectric in them is usually mica, in thin sheets. Their general form is shown in Fig. 174. The two brass pieces upon the ebonite top are connected respectively with the two series of alternate sheets of tinfoil. The plug between them serves to keep the condenser discharged when not in use.

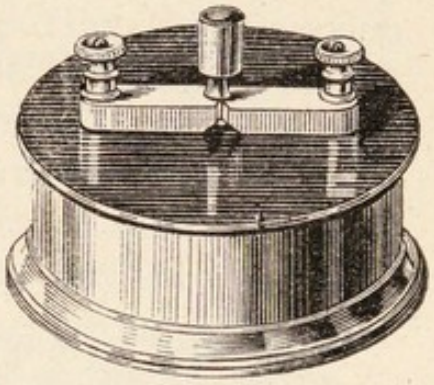


FIG. 174.—Standard Condenser ($\frac{1}{3}$ *microfarad*).

Methods of measuring the capacity of a condenser are given in Art. 451, p. 457.

324. Modern Commercial Condensers.—For telegraph and telephone work Mansbridge has devised condensers consisting of long slips of thin paper coated on one side with tin powder which has been burnished on

[1] See list of Practical Electromagnetic Units, Art. 381.

to the strip. Each condenser is formed of two such strips rolled up, with a blank strip of thin paper between them, into cylindrical form. If the total thickness of paper between the foils is 0·004 of an inch, the two coated surfaces will be about $6\frac{1}{4}$ square feet each, in a condenser of 1 microfarad capacity. Moscicki's high-voltage jar is described in Art. 64.

325. Formulæ for Capacities of Conductors and Condensers.—The following formulæ give the capacity of condensers of all ordinary forms, in electrostatic units :—

Sphere : (radius $= r$. See Art. 290), if in air—

$$C = r ;$$

or, if in a medium of inductivity k,

$$C = kr.$$

Two Concentric Spheres : (radii r and r').

$$C = k\frac{rr'}{r' - r}.$$

Cylinder : (length $= l$, radius $= r$).

$$C = k\frac{l}{2\log_\epsilon \frac{l}{r}}.$$

Two Concentric Cylinders : (length $= l$, internal radius $= r$, external radius $= r'$).

$$C = k\frac{l}{2\log_\epsilon \frac{r'}{r}}.$$

Circular Disk : (radius $= r$, thickness negligible).

$$C = 2\pi k/r.$$

Two Circular Disks : (like air condenser, Art. 57, radii $= r$, surface $= S$, thickness of dielectric $= b$; provided r is very great relatively to b)—

$$C = kr^2/4b,$$

or

$$C = kS/4\pi b.$$

The latter formula applies to any two parallel disks of surface S, whether circular or otherwise, provided they are *large* as compared with the distance *b* between them. To calculate down to microfarads the numbers given by any of the above must be divided by 900,000.

326. Energy of Discharge of Leyden Jar or Condenser.—It follows from the definition of potential, given in Art. 280, that in bringing up one + unit of electricity to the potential V, the work done is V *ergs*. This assumes, however, that the total potential V is not thereby raised, and on this assumption the work [1] done in bringing up Q units would be QV *ergs*. If, however, the potential is nothing to begin with, and is raised to V by the charge Q, the average potential during the operation is only $\frac{1}{2}$V; hence the total work done in bringing up the charge Q from zero potential to potential V is $\frac{1}{2}$QV *ergs*. Now, according to the principle of the conservation of energy, the work done in charging a jar or condenser with electricity is equal to the work which could be done by that quantity of electricity when the jar is discharged. Hence $\frac{1}{2}$QV represents also the energy of the discharge.

Since Q = VC, it follows that we may write $\frac{1}{2}$QV in the form $\frac{1}{2}Q^2 \div C$. That is to say, if a condenser of capacity C is charged by having a charge Q imparted to it, the energy of the charge is proportional directly to the square of the quantity, and inversely to the capacity of the condenser.

327. Symbol for Condenser.—In diagrams of electric circuits electricians use as symbols for condensers those given in Fig. 175. The origin of these symbols is the alternate layers of tinfoil. The symbol on the right suggests six layers of foil, of which the first, third, and fifth

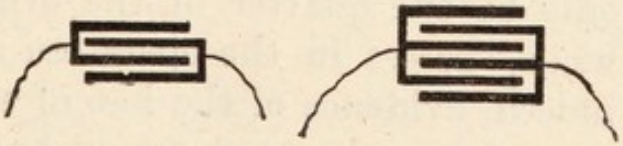


FIG 175.—Symbol for Condensers.

[1] If Q is given in *coulombs* and V in *volts*, the work will be expressed not in *ergs* but in *joules* (Art. 381).

are joined together, and the second, fourth, and sixth are also joined together.

328. Capacities joined in Parallel.—To join two condensers together in parallel the positive foils of one are joined to the positive foils of the other, and their negative foils are also joined together. In Fig. 176 the two condensers C_1 and C_2 are joined in parallel. They will thus act simply like one large condenser of capacity $= C_1 + C_2$. Any charge flowing in on the + side will divide between the two in proportion to their capacities.

If two equal Leyden jars are charged to the same potential, and then their inside and outside coatings are respectively joined, their united charge will be the same as that of a jar of equal thickness, but having twice the amount of surface.

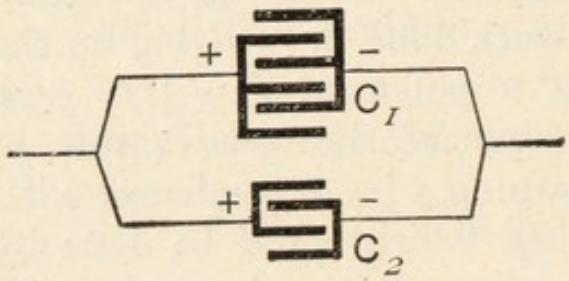


FIG. 176.—Condensers in Parallel

If a charged Leyden jar is placed similarly in communication with an uncharged jar of equal capacity, the charge will be shared equally between the two jars, and the passage of electricity from one to the other will be evidenced by the production of a spark when the respective coatings are put into communication. Here, however, half the energy of the charge is lost in the operation of sharing the charge, for each jar will have only $\frac{1}{2}Q$ for its charge and $\frac{1}{2}V$ for its potential; hence the energy of the charge of each, being half the product of charge and potential, will only be one quarter of the original energy. The spark which passes in the operation of dividing the charge is, indeed, evidence of the loss of energy; it is about half as powerful as the spark would have been if the first jar had been simply discharged, and it is just twice as powerful as the small sparks yielded finally by the discharge of each jar after the charge has been shared between them.

The energy of a charge of the jar manifests itself, as

stated above, by the production of a spark at discharge; the sound, light, and heat produced being the equivalent of the energy stored up. If discharge is effected slowly through a long thin wire of high resistance the air spark may be feeble, but the wire may be perceptibly heated. A wet string being a feeble conductor affords a slow and almost silent discharge; here probably the electrolytic conduction of the moisture is accompanied by an action resembling that of secondary batteries (Art. 572) tending to prolong the duration of the discharge.

329. Capacities joined in Series.—If two condensers are joined in series they will act as a condenser having a lesser capacity than either of them separately. *Their joint capacity in series will be the reciprocal of the sum of the reciprocals of their capacities separately.*

Proof.—Let two condensers C_1 and C_2 be set in series (Fig. 177) between two points across which there is a difference of potential V. This difference of potential will be divided between the two inversely in proportion to their capacities, seeing that the quantities of electricity that are displaced into and out of their respective coatings are necessarily equal. Or, if Q be this quantity, and C_3 the effective or joint capacity of the two together, to find the latter, we have :—

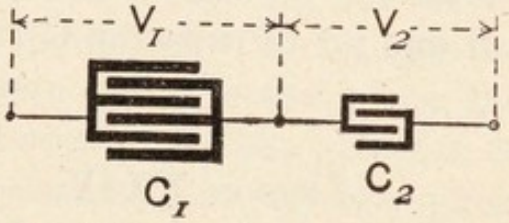


FIG. 177.—Condensers in Series.

$$Q = V_1C_1 = V_2C_2 = VC_3 \quad . \quad . \quad . \quad (1)$$

and $$V = V_1 + V_2 \quad . \quad . \quad . \quad . \quad . \quad (2)$$

From (1) we get

$$V_1 = VC_3/C_1,$$

and

$$V_2 = VC_3/C_2.$$

Inserting these in (2) we get

$$V = VC_3/C_1 + VC_3/C_2;$$

whence, dividing down by VC_3, we get

$$\frac{1}{C_3} = \frac{1}{C_1} + \frac{1}{C_2} \quad . \quad . \quad . \quad . \quad \text{Q.E.D.}$$

Example.—If two condensers, respectively 3 and 2 microfarads, are joined in series, they will act as a single condenser of capacity $= 1/(\frac{1}{3}+\frac{1}{2}) = 1\frac{1}{5}$ microfarads.

Franklin suggested that jars might be arranged in series, the outer coating of one being connected with the inner one of the next, the outer coating of the last being connected to earth. The object of this arrangement was that the second jar might be charged with the electricity repelled from the outer coating of the first, the third from that of the second, and so on. This "cascade" arrangement, however, is of no advantage, the sum of the charges accumulated in the series being only equal to that of one single jar if used alone. For if the inner coating of the first jar be raised to V, that of the outer coating of the last jar remaining at zero in contact with earth, the difference of potential between the outer and inner coating of any one jar will be only V/n, where n is number of jars. And as the charge in each jar is equal to its capacity C, multiplied by its potential, the charge in each will only be CV/n, and in the whole n jars the total charge will be $n \times CV/n$, or CV, or equals the charge of one jar of capacity C raised to the same potential V.

LESSON XXIV.—*Phenomena of Discharge*

330. Conductive Discharge.—An electrified conductor may be discharged in at least *three* different ways, depending on the medium through which the discharge is effected, and varying with the circumstances of the discharge. If the discharge takes place by the passage of a continuous *current*, as when electricity flows through a thin wire connecting the knobs of an influence machine, or joining the positive pole of a battery to the negative pole, the operation is termed a "**conductive**" **discharge.** In some circumstances a conductive discharge takes the nature of an oscillation to and fro (Art. 600).

331. Disruptive Discharge.—It has been shown how influence across a non-conducting medium is always accompanied by a mechanical stress upon the medium;

the tension along the electric lines of force increasing as the square of the intensity of the electric field. If this stress is very great the non-conducting medium will suddenly break down and a *spark* will burst across it. Such a discharge is called a "**disruptive**" **discharge.**

A very simple experiment will set the matter in a clear light. Suppose a metal ball charged with + electrification to be hung by a silk string above a metal plate lying on the ground. If we lower down the suspended ball a spark will pass between it and the plate when they come very near together, and the ball will then be found to have lost all its previous charge. It was charged with a certain quantity of electricity; and as it had, when suspended out of the range of other conductors, a certain capacity (numerically equal to its radius in centimetres), the electricity on it would be at a certain potential (namely = Q/C), and the charge would be distributed uniformly all over it. The plate lying on the earth would be all the while at zero potential. But when the suspended ball was lowered down towards the plate the previous state of things was altered. In the presence of the + charge of the ball the potential[1] of the plate would rise, were it not that, by influence, just enough negative electrification appears on it to keep its potential still the same as that of the earth. The tension in the electric field will draw the + charge of the ball downwards, and alter the distribution of the charge, the surface-density becoming greater at the under surface of the ball and less on the upper. The capacity of the ball will be increased, and therefore its potential will fall correspondingly. The layer of air between the ball and the plate is acting like the glass of a Leyden jar. The more the ball is lowered down the greater is the accumulation of the opposite kinds of charge on each side of the layer

[1] The student must remember that, by the definition of potential in Art. 280, the potential at a point is the sum of all the separate quantities of electricity near it, divided each by its distance from the point.

of air, and the tension across the layer becomes greater and greater, until the limit of the dielectric strength (Art. 335) is reached; the air suddenly gives way and the spark tears a path across.

332. Convective Discharge. — A third kind of discharge, differing from either of those above mentioned, may take place, and occurs chiefly when electricity of a high potential discharges itself at a pointed conductor by accumulating there with so great a density as to electrify the neighbouring particles of air; these particles then flying off by repulsion, conveying away part of the charge with them. Such *convective discharges* may occur either in gases or in liquids, but are best manifested in air and other gases at a low pressure, in tubes exhausted by an air pump.

The discharge of a quantity of electricity in any of the above ways is always accompanied by a transformation of its energy into energy of some other kind—sound, light, heat, chemical actions, and other phenomena being produced. These effects must be treated in detail.

333. Length of Spark.—Generally speaking, the length of spark between two conductors increases with the difference between their potentials. It is also found to increase when the pressure of the air is diminished. Lord Kelvin measured by means of an "absolute electrometer" (Art. 306) the difference of potential necessary to produce a spark discharge between two parallel plates at different distances. He found the distance to increase in a proportion a little exceeding that of the difference of potentials. De la Rue and Müller found with their great battery (Art. 197) that with a difference of potential of 1000 volts the striking distance of the spark was only 0·0127 centimetre (or about $\frac{1}{200}$ of an inch), and with a difference of 10,000 volts only 1·369 cms. Their 11,000 silver cells gave a spark of 1·59 centim. (about $\frac{2}{3}$ of an inch) long. To produce a spark one mile long, through air at the ordinary pressure, would therefore require

a difference of potential exceeding that furnished by 1,000,000,000 Daniell's cells!

The length of the spark differs in different gases, being nearly twice as long in hydrogen as in air at the same density. Or to produce in hydrogen a spark as long as one in air requires less voltage. On the other hand, carbonic acid gas, whilst it is stronger than air for short sparks, is weaker for long ones.

The potential needful to produce a spark of given length in a given gas is almost independent of the kind of metal used as electrodes, but depends upon their shape. If points are used instead of balls it is found that, at equal voltage, points are best for long sparks, but are worst for short sparks.

According to Strutt's observations a *minimum* potential of 341 volts is necessary to start a spark, however short, in air. For sparks not under two millimetres in length the volts necessary to start a spark across a length of l centimetres may, according to Peace, be approximately expressed by the equation—

$$V = 1500 + 30{,}000\ l.$$

The following table, calculated from the results of Heydweiller, gives the volts necessary to produce a spark in air at 15° C. and 76 centimetres pressure between two spheres of various sizes. The figures must be increased 1 per cent for a fall of 3 degrees of temperature, or for a rise of 8 millimetres of pressure.

Radius of Balls.	Distance between Balls (Centims.)			
	0·1	0·5	1·0	1·5
Centims.	Volts.	Volts.	Volts.	Volts.
2·5	4500	18900	33840	47610
1·0	4860	18030	32120	41160
0 5	4950	17790	27810	32400
0·25	4980	16200	20790	22980

For *long* sparks, in air, the potentials to produce them are practically proportional to their lengths.

In rarefied air the spark is longer. Snow Harris stated that the length of spark was inversely proportional to the pressure, but this law is not quite correct, being approximately true only for pressures between that of 11 inches of mercury and that of 30 inches (one atmosphere). At lower pressures, a greater difference of potential must be used to produce a spark than that which would accord with Harris's law. From this it would appear that thin layers of air oppose a proportionally greater resistance to the piercing power of the spark than thick layers, and possess greater dielectric strength.

Faraday, using two spheres of different sizes, found the spark-length greater when the smaller sphere was positive than when it was negative.

With rapidly-alternating differences of potential, smaller virtual voltages suffice for the same spark-length, for the length depends on the maximum, not on the mean value. Using a ball of 1 cm. diameter and a disk, Alexander Siemens found 3200 virtual volts to be needed at 0·1 cm. distance, and 11,000 at 0·5 cm. distance apart.

The dielectric strength of a gas appears to be weaker when field is varying than when it is steady. When the voltage is nearly high enough to produce a spark, reversing the poles will sometimes start a spark. Moreover, when once a spark has passed it is easier for a second one to follow on the same track. Probably the first spark produces in its path chemical dissociations which do not instantly pass away.

Hertz made the singular observation that ultra-violet light (*i.e.* actinic waves) falling upon the kathode surface assist it to discharge (see Art. 619).

A perfect vacuum is a perfect insulator—no spark will cross it. On the other hand, a great increase of pressure also increases the dielectric strength of air, and causes it

to resist the passage of a spark. Cailletet compressed dry air at 40 to 50 atmospheres' pressure, and found that the spark of an induction coil failed to cross a space of 0·05 centimetre's width.

334. Flames and Hot Air.—The *arc* produced by the passage of an electric current between two carbon pencils is treated of in Art. 486. It is a species of flame which conducts the current from the tip of one carbon rod to the other, while volatilizing the carbon, and requires some thirty to fifty volts for its maintenance. The alternating-current arc generated in air by high-frequency discharges at a potential of 10,000 to 50,000 volts is a different phenomenon, and is apparently an endothermic flame of nitrogen and oxygen burned together.

Sparks are longer and straighter through hot air than through cold. If air or other permanent gas is, however, heated in a closed vessel so that its density remains unaltered, the voltage needful to produce discharge remains the same; unless, indeed, the gas be heated to point of dissociation when discharge occurs at low voltage.

Flames and currents of very hot air, such as those rising from a red-hot piece of iron, are extremely good conductors of electricity, and act even better than metallic points in discharging a charged conductor. Gilbert showed that an electrified body placed near a flame lost its charge; and the very readiest way to rid the surface of a charged body of low conducting power of a charge imparted to it by friction or otherwise, is to pass it through, or hold it near to, the flame of a spirit-lamp. Faraday found negative electrification to be thus more easily discharged than positive. Flames powerfully negatively electrified are repelled from conductors, though not so when positively electrified. Sir W. Grove showed that a current is set up in a platinum wire, one end of which touches the tip, and the other the base, of a flame.

Guthrie showed that a red-hot iron ball cannot be

positively, but may be negatively charged. When white-hot it will retain neither kind of charge.

335. Mechanical Effects; Dielectric Strength.—Chief amongst the mechanical effects of the disruptive spark discharge is the shattering and piercing of insulators. The dielectric strength of glass, though much greater than that of air, is not infinitely great. A slab of glass 3 inches thick has been pierced by the discharge of a powerful induction coil. The so-called "toughened" glass has a greater dielectric strength than ordinary glass, and is more difficult to pierce. A sheet of glass may be readily pierced by a spark from a large Leyden jar or battery of jars, by taking the following precautions:—The sheet to be pierced is laid upon a block of glass or resin, through which a wire is led by a suitable hole, one end of the wire being cut off flush with the surface, and the other end being connected with the outer coating of the jar. Upon the upper surface of the sheet of glass that is to be pierced another wire is fixed upright, its end being exactly opposite the lower wire, the other extremity of this wire being armed with a metal knob to receive the spark from the knob of the jar or discharger. To ensure good insulation a few drops of paraffin oil, or of olive oil, are placed upon the glass round the points where the wires touch it. A piece of dry wood similarly treated is split by a powerful spark. A layer of oil resists being pierced as much as a layer of air five or six times as thick would do.

The dielectric strength, or resistance to piercing by a spark, is most conveniently stated in terms of the voltage needed to pierce a layer one millimetre thick. For dry paper the limit varies from 1400 to 8000 volts; for varnished paper, 10,000 to 28,000; guttapercha, 7700 to 19,000; indiarubber, 16,000 to 21,000; ebonite, 28,000 to 31,000; mica, from 60,000 to 200,000; dry paraffin oil, 30,000 to 100,000.

If a spark is led through a tightly-corked glass tube

containing water, the tube will be shattered into small pointed fragments by the sudden expansion of the liquid.

Lullin observed two curious effects when a piece of cardboard is perforated by a spark between two metal points. *First*, there is a slight burr raised on each side, as if the hole had been pierced from the middle outwards, as though the stress in the air had *pulled* at the card. *Secondly*, if the two points are not exactly opposite one another the hole is found to be nearer the *negative* point. But if the experiment is tried under the air pump in a vacuum, there is no such displacement of the hole; it is then midway exactly.

The mechanical action of the brush discharge at points is mentioned in Art. 47, p. 53.

336. Chemical Effects.—The chemical actions produced by currents of electricity have been described in Lessons XIV. and XIX. Similar actions can be produced by the electric spark, and by the silent glow discharge (see Art. 340). Faraday showed, indeed, that electricity from all kinds of different sources produced the same kinds of chemical actions, and he relied upon this as one proof of the essential identity of the electricity produced in different ways. If sparks from an electric machine are received upon a piece of white blotting-paper moistened with a solution of iodide of potassium, brown patches are noticed where the spark has effected a chemical decomposition and liberated the iodine.

When a stream of sparks is passed through moist air in a vessel, the air is found to have acquired the property of changing to a red colour a piece of paper stained blue with litmus. This, Cavendish showed, was due to the presence of nitric acid, produced by the chemical union of the nitrogen and oxygen of the air. The effect is best shown with the stream of sparks yielded by a small induction coil (Fig. 150), in a vessel in which the air has been compressed beyond the usual atmospheric pressure.

The commercial manufacture of nitric acid and of

nitrates from atmospheric air by subjecting it to powerful electric discharges in a special electric furnace has recently been established on a large scale in Norway by Birkeland and Eyde (see p. 609).

Whenever an electric machine is giving out high-voltage discharges a peculiar odour is perceived. This was formerly thought to be evidence of the existence of an electric "effluvium" or fluid; it is now known to be due to the presence of **ozone**, a modification of oxygen gas, which differs from oxygen in being denser, more active chemically, and in having a characteristic smell. The silent discharge of the influence machine and that of the induction coil are particularly favourable to the production of this substance. The spark and brush forms of discharge produce nitric oxide, not ozone.

The spark will decompose ammonia gas, and olefiant gas, and it will also cause chemical combination to take place with explosion, when passed through detonating mixtures of gases. Thus equal volumes of chlorine and hydrogen are exploded by the spark. So are oxygen and hydrogen gases, when mixed in the proportion of two volumes of the latter to one of the former. Even the explosive mixture of common coal gas mixed with from four to ten times its own volume of common air, can be thus detonated. A common experiment with the so-called *electric pistol* consists in filling a small brass vessel with detonating gases and then exploding them by a spark. The spark discharge is sometimes applied to the firing of blasts and mines in military operations.

337. Heating Effects.—The flow of electricity through a resisting medium is in every case accompanied by an evolution of heat. The laws of heating due to currents are given in Art. 462. The disruptive discharge is a transfer of electricity through a medium of great resistance and is accompanied by an evolution of heat. A few drops of ether in a metallic spoon are easily kindled by an electric spark. The spark from an electric machine,

or even from a rubbed glass rod, suffices to kindle an ordinary gas-jet. In certain districts of America, during the driest season of the year, the mere rubbing of a person's shoes against the carpet, as he shuffles across the floor, generates sufficient electrification to enable sparks to be drawn from his body, and he may light the gas by a single spark from his outstretched finger. Gunpowder can be fired by the discharge of a Leyden jar, but the spark should be retarded by being passed through a wet thread, otherwise the powder will simply be scattered by the spark.

The heating powers of the discharge may be investigated by causing it to pass through a glass vessel enclosing air, and communicating with a tube partly filled with water or other liquid, in order to observe changes of volume or of pressure. Into this vessel are led two metal rods, between which is suspended a thin wire, or a filament of gilt paper; or a spark can be allowed simply to cross between them. When the discharge passes the enclosed air is heated, expands, and causes a movement of the indicating column of liquid. The results of observation with these instruments are as follows:—The heating effect produced by a given charge in a wire of given length is inversely proportional to the square of the area of the cross section of the wire. The total heat evolved is jointly proportional to the charge, and to the potential through which it falls. In fact, if the entire energy of the discharge is expended in producing heat, and in doing no other kind of work, then the heat developed will be the thermal equivalent of $\frac{1}{2}QV$ *ergs*, or $QV \div 2J$ *calories*; where J represents the mechanical equivalent of heat (J = 42 million; since 42×10^6 *ergs* = 1 *calorie*), and Q and V are expressed in C.G.S. units.

When a powerful discharge takes place through very thin wires, they may be heated to redness, and even fused by the heat evolved. A narrow strip of tinfoil is readily fused by the charge of a large Leyden jar, or battery of

jars. A piece of gold leaf is in like manner volatilized by a powerful discharge. Franklin utilized this property for a rude process of multiplying *portraits* or other patterns, which, being first cut out in card, were reproduced in a silhouette of metallic particles on a second card, by the device of laying above them a film of gold or silver leaf covered again with a piece of card or paper; a Leyden battery being then discharged through the leaf.

338. Sparking at Contacts.—The sparks which appear at the breaking of any circuit in which a current is flowing (see Art. 503) cause a few particles of the metal to be fused and volatilized; and if repeated, roughen the surface where they occur. To prevent too great deterioration of the contact surfaces, keys and the vibrating contacts of electric bells and induction coils are usually provided with contact pieces of platinum or nickel, or, for cheapness, of german silver. Electric light switches are usually provided with copper contact surfaces, and are, by application of springs, made to snap suddenly apart, on break of circuit, to prevent the spark becoming a persistent arc.

339. Luminous Effects.—The discharge through air exhibits many beautiful and varied luminous effects under different conditions. The **spark** of the disruptive discharge is usually a thin brilliant streak of light. When it takes place between two metallic balls, separated only by a short interval, it usually appears as a single thin and brilliant line. If, however, the distance be as much as a few centimetres, the spark takes an irregular zigzag form. In any case its path is along the line of least resistance, the presence of minute motes of dust floating in the air being quite sufficient to determine the zigzag character. Often the spark exhibits curious ramifications and forkings, of which an illustration is given in Fig. 178, which is drawn one-eighth of the actual size of the spark obtained from an electrical machine. They appear to be drainage lines of electrons flowing from various points and uniting in streams as they proceed to the positive pole.

Photographs of lightning flashes almost always show similar branching. The discharge from a Leyden jar affords a much brighter, shorter, noisier spark than the spark drawn direct from the collector of a machine. The length (see Art. 333) depends upon the potential, and upon the pressure and temperature of the air in which the discharge takes place. The brilliance depends chiefly upon the quantity of the discharge. The colour of the spark varies with the nature of the metal surfaces between which the discharge takes place ; for the spark tears away in its passage small portions of the metal surfaces, and



FIG. 178.—Forked Electric Spark.

volatilizes them. Between copper or silver terminals the spark takes a green tint, while between iron knobs it is of a reddish hue. Examination with the spectroscope reveals the presence in the spark of the rays characteristic of the incandescent vapours of the several metals.

340. Brush Discharge; Glow Discharge.—If an electric machine is vigorously worked, but no sparks be drawn from its collector, a fine diverging **brush** of pale blue light can be seen (in a dark room) streaming from the brass ball at the end of it farthest from the collecting comb; a hissing or crackling sound always accompanies this kind of discharge. The brush discharge consists of innumerable fine twig-like ramifications, presenting a form of which Fig. 179 gives a fine example.

The brightness and size of the *brush* is increased by holding a flat plate of metal a little way from it. With a smaller ball, or with a bluntly-pointed wire, the brush appears smaller, but is more distinct and continuous. When discharge is going on between two balls the brushes are never alike. At the positive ball or anode the brush discharge is larger and more ramified than at the negative ball. But the negative brush is more easily formed than the positive. Wheatstone found by using his

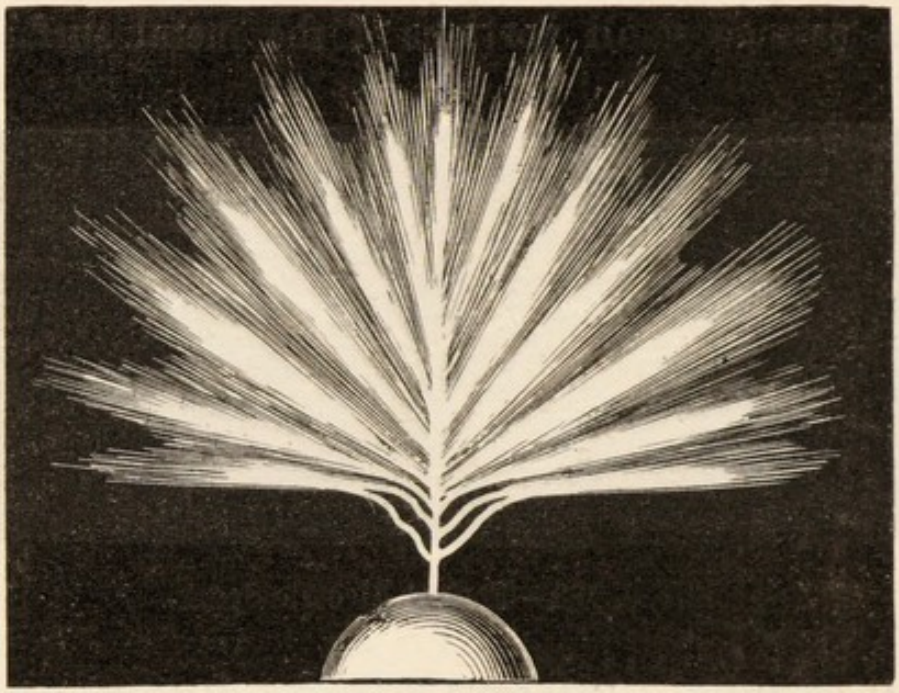


FIG 179.—Electric Brush (Positive) Discharge.

rotating mirror that the brush discharge is really a series of successive partial sparks at rapid intervals. Metallic dust is in every case torn away from the electrode by the brush discharge.

If the blunt or rounded conductor be replaced by a pointed one, the brush disappears and gives place to a silent and continuous **glow** where the electrified particles of air are streaming away at the point. If these convexion-streams are impeded the glow may once more give place to the brush. Where a negative charge is being discharged at a point, the glow often appears to

be separated from the surface of the conductor by a dark space, where the air, without becoming luminous, still conveys the electricity. This phenomenon, to which Faraday gave the name of the "*dark*" *discharge*, is very well seen when electricity is discharged through rarefied air and other gases in vacuum tubes.

A spark discharge may degenerate into a brush if the surface of the electrode becomes pitted or roughened by frequent discharges. Hence in all spark experiments it is important to keep the discharging balls *highly polished.*

341. The Corona Discharge.—When alternating currents are led at high voltage to the opposite faces of a thin glass plate, a pale violet light appears at the edges of the electrodes, when the alternating pressure is raised to 7000 or 8000 volts. On raising the voltage this luminous margin, which is called the *corona*, becomes broader and brighter; and bright, thin, hot streamers dart off in various directions from the edges of the electrodes. At 20,000 volts they dart over the surface of the plate and may even short-circuit over the edges of the plate with noisy coruscations. On transmission lines at extra high voltages the corona sometimes occurs around the wires. It is due to the air becoming conductive when greatly heated.

342. Discharges in Partial Vacua.—If the discharge takes place in glass tubes or vessels from which the air has been partially exhausted, many remarkable and beautiful luminous phenomena are produced. A common form of vessel is the "electric egg," a sort of oval bottle that can be screwed to an air pump, and furnished with brass knobs to lead in the sparks. More often *vacuum tubes*, such as those manufactured by the celebrated Geissler, are employed. These are merely tubes of thin glass blown into bulbous or spiral forms, provided with two electrodes of platinum wire fused into the glass, and sealed off after being partially exhausted of air by a mercurial air pump. Some Geissler tubes consist of two

bulbs joined by a narrow tube (Fig. 180), the luminous effects being usually more intense in the contracted portion. Such tubes are readily illuminated by discharges from an electrophorus or an influence machine; but it is more common to work them with the spark of an induction coil (Fig. 150). A coil capable of producing a $\frac{1}{2}$-inch spark in air will illuminate a vacuum tube 6 or 8 inches long. Where an alternating current supply is available, small transformers (Art. 245) wound to deliver $\frac{1}{50}$ ampere at 5000 volts serve admirably for lighting vacuum tubes.

Through such tubes, before exhaustion, ordinary sparks

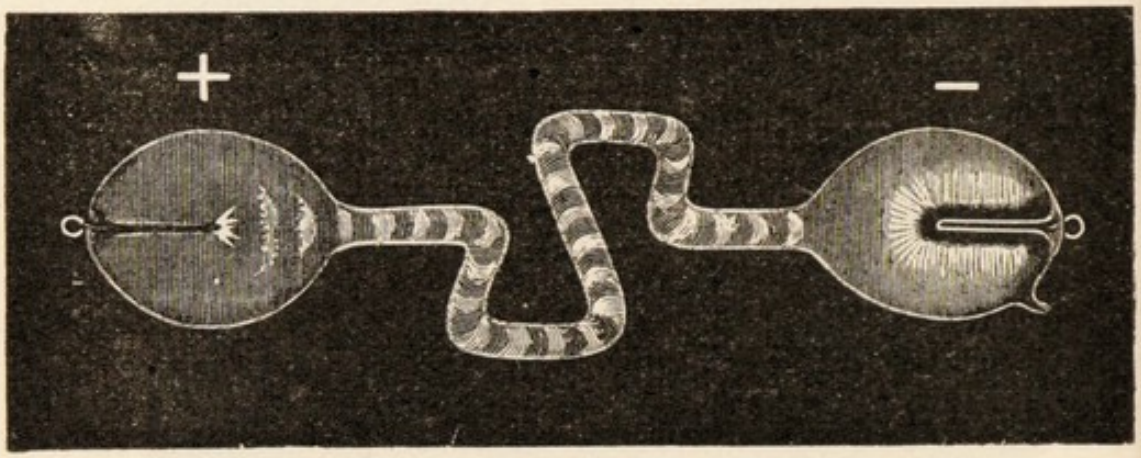


FIG. 180.—Discharge in a Vacuum Tube.

can be sent only by using enormous electromotive forces. As the air is exhausted the sparks become less sharply defined, and widen out to occupy the whole tube, becoming pale in tint and nebulous in form. As the rarefied air offers much less resistance, the discharge passes freely. The kathode exhibits a beautiful bluish or violet glow, separated from the conductor by a narrow *dark space*, while at the anode a single small bright star of light is all that remains. At a certain degree of exhaustion the light in the tube breaks up into a set of *striæ*, or patches of light of a cup-like form, which vibrate to and fro between darker spaces. In nitrogen gas the violet aureole glowing around the kathode is very bright, the rest of

the light being rosy in tint. In oxygen the difference is not so marked. In hydrogen gas the tint of the discharge is bluish, except where the tube is narrow, where a beautiful crimson may be seen. With carbonic acid gas the light is remarkably white. Particles of metal are torn off from the kathode, and projected from its surface. The kathode is usually the hotter of the two electrodes when made of similar dimensions to the anode. If the anode is heated and the kathode kept cool no discharge will pass. If the kathode becomes white-hot the glow disappears, and the gas conducts freely without shining. The luminosity disappears from the rarefied air in the neighbourhood of a red-hot platinum spiral inside the tube. It is also observed that the light of these discharges in vacuo is rich in those rays which produce phosphorescence and fluorescence. Many beautiful effects are therefore produced by blowing tubes in uranium glass (which fluoresces with a fine green light), or by placing solutions of quinine or other fluorescent liquids in outer tubes of glass.

343. Phenomena in High Vacua.—Sir Wm. Crookes found that when exhaustion is carried to a very high degree the dark space separating the negative glow from the negative pole increases in width; and that across this space electrified particles are projected in straight paths in directions normal to the surface of the kathode, and independent of the position of the anode. If exhaustion be carried to such a high degree that about one-millionth part only of the air remains, the dark space fills the entire tube or bulb, the glass walls become beautifully phosphorescent. Diamonds, rubies, and even white powdered alumina placed in the tubes become brilliantly phosphorescent if the kathode discharge is directed upon them. And if a body (whether opaque or transparent) be placed in front of the electrode, a sharply defined *shadow* of the body is projected upon the opposite wall of the vessel, showing by its position that a stream capable of producing phosphorescence

proceeds in straight lines from the kathode and is intercepted by the body. In Fig. 181 the kathode K is a slightly convex disk of aluminium, but the discharge is independent of the metal used as kathode. In the path of the discharge is set a cross cut out of mica. Its shadow S appears on the end of the bulb, which phosphoresces all around the shadowed part. The anode may be either at A or *a*. Lightly-poised vanes, if placed in the path of the discharge, are driven round by the mechanical pressure of the flying particles.

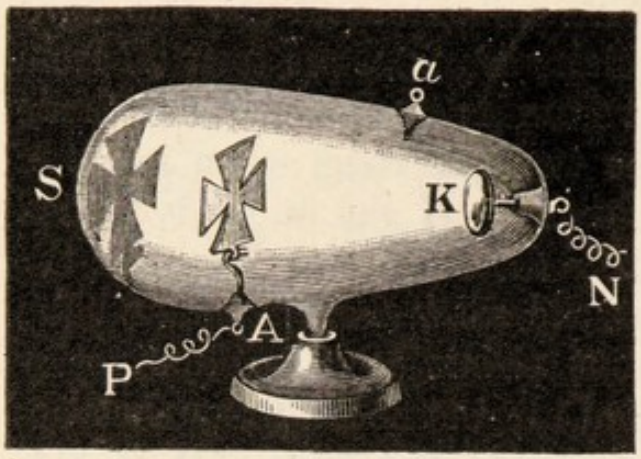


FIG. 181.—Kathode Discharge in Crookes's Tube, showing Shadow.

344. Kathode Rays and Canal Rays.—These kathodic discharges are deflected from their straight path by the action of a magnetic field, and were found by Crookes to be deflected as though they were negative currents, that is as though they conveyed electricity toward the kathode; suggesting that they were negatively charged. Crookes regarded this kathode discharge as exhibiting matter in an ultra-gaseous or *radiant* state. In their physical properties the kathode "rays" closely resemble the "beta" rays emitted by radium (Art. 638). Hertz discovered that these kathode "rays" which will not pass through glass, mica, or any transparent substance, will pass through metal foil. Lenard, using a vacuum tube with a "window" of aluminium foil at one end, succeeded in passing the kathode rays out into the air (in which they cannot be produced at all), and found them to retain their property of exciting phosphorescence. Perrin proved that the kathode discharge beam carried negative charges, by directing the discharge from the kathode K, Fig. 182, into a small hollow cylinder C, surrounded by another

hollow insulated cylinder A. The cylinder C was connected to an electroscope outside, which became negatively charged. But if by means of a magnet the kathode stream was deflected so that it did not enter C, the electroscope remained uncharged.

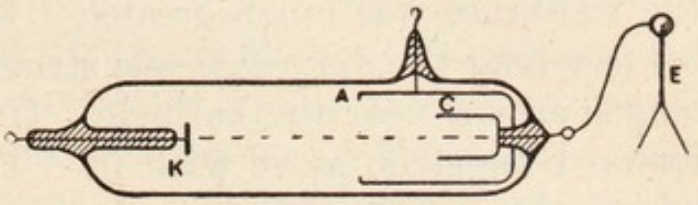


FIG. 182.—Perrin's Experiment with Cylinder.

In a series of brilliant experiments Sir Joseph J. Thomson proved the correctness of Crookes's hypothesis. The kathode "rays" consist of streams of negatively electrical particles or corpuscles whose mass is extraordinarily small, being less than $\frac{1}{1000}$ of the mass of a hydrogen atom. The speed with which they move in the vacuum tube is enormous, being about 50,000 miles per second. These negative corpuscles are usually called *electrons* (see Lesson LXII., Art. 630).

If the kathode is perforated with a hole or holes, "rays" of another kind, called *diakathodic* or *canal rays*, are observed to pass in pale blue lines through the apertures, Fig. 183. These rays, which excite a different kind of phosphoresence, are very slightly affected by a magnet; the deflexion indicating that they are positively charged. Their speed is at least a thousand times less than that of the electrons, and they consist probably of actual atoms of gas positively charged.

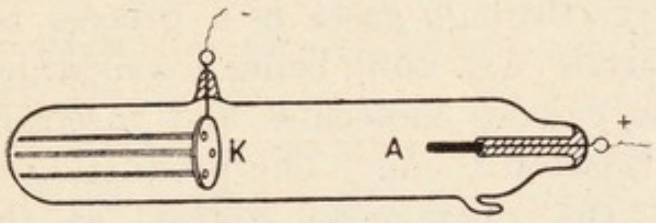


FIG. 183.—Vacuum Tube showing Canal Rays.

345. Striæ or Stratifications.—The striæ, mentioned in Art. 342 above, originate at the anode at a certain pressure, and become more numerous, as the exhaustion proceeds, up to a certain point, when they become thicker and diminish in number, until exhaustion is carried to such a point that no discharge will pass.

Sir Joseph J. Thomson found the column of striæ to exhibit a nearly constant electric resistance all along; though beyond it in the neighbourhood of the kathode the resistance was much greater. In a vacuum tube over 50 feet long the discharge was striated through the whole length except near the kathode. If the kathode is moved forward the striæ move with it. The striæ flicker even when the continuous current from a battery of some thousands of cells (Art. 197) is used. There is a maximum of steadiness with a particular density of current. The striæ are hotter than the spaces between them. The number and position of the striæ vary, not only with the exhaustion, but with the difference of potentials of the electrodes. Each portion of the column of striæ acts as an independent discharge. When striæ are produced by the intermittent discharges of the induction coil, examination of them in a rotating mirror reveals that they move forward from the anode towards the kathode.

346. Ionization by Discharge. — Schuster has shown that the discharge through gases is a process resembling that of electrolysis (Art. 253), being accompanied by breaking up of the gaseous molecules and incessant interchanges of atoms between them. The production of ozone (Art. 336) and the phenomena noticed at the kathode (Art. 343) give support to this view. Amongst other evidence is the striking discovery of Hittorf that quite a few cells can send a current through gas at ordinary pressures provided a spark-discharge is going on in the neighbourhood. Sir Joseph J. Thomson finds that those gases which when heated are decomposed or molecularly dissociated, so that free atoms are present, are then good conductors. Ionization of the gas appears to be an essential feature of gaseous discharge.

The discharges in vacuum tubes, at all degrees of exhaustion, are *affected by the magnet*, behaving like flexible conductors. Under certain conditions also, the discharge is *sensitive* to the presence of a conductor on

the exterior of the tube, retreating from the side where it is touched.

347. Velocity of Propagation of Discharge.— The earliest use of the rotating mirror to analyze phenomena of short duration was made by Wheatstone, who attempted by this means to measure "the velocity of electricity" in conducting wires. What he succeeded in measuring was not, however, *the velocity of electricity*, but the time taken by a certain quantity of electricity to flow through a conductor of considerable resistance and capacity. Viewed in a rotating mirror, a spark of definite duration would appear to be drawn out into an elongated streak. Such an elongation was found to be visible when a Leyden jar was discharged through a copper wire half a mile long; and when the circuit was interrupted at three points, one in the middle and one at each end of this wire, three sparks were obtained, which, viewed in the mirror, showed a lateral displacement, indicating (with the particular rate of rotation employed) that the middle spark took place $\frac{1}{1152000}$ of a second later than those at the ends. Wheatstone argued from this a velocity of 288,000 miles per second. But Faraday showed that the apparent rate of propagation of a quantity of electricity must be affected by the capacity of the conductor; and he even predicted that since a submerged insulated cable acts like a Leyden jar (see Art. 321), and has to be charged before the potential at the distant end can rise, it will *retard* the apparent flow of electricity through it. There is in fact no definite assignable "velocity of electricity." In the case of wires suspended in air the velocity of propagation of any sudden electrical disturbance is equal to the velocity of light. But in the case of slow vibrations, like those of telephonic sounds, being sent through land lines or cables, the velocity may be much less.

A very simple experiment will enable the student to realize the exceedingly short duration of the spark of a Leyden jar. Let a round disk of cardboard painted

with black and white sectors be rotated very rapidly so as to look by ordinary light like a mere grey surface. When this is illuminated by the spark of a Leyden jar it appears to be standing absolutely still, however rapidly it may be turning. A flash of lightning is equally instantaneous; it is utterly impossible to determine at which end the flash begins.[1]

348. Electric Dust-Figures. — Electricity may

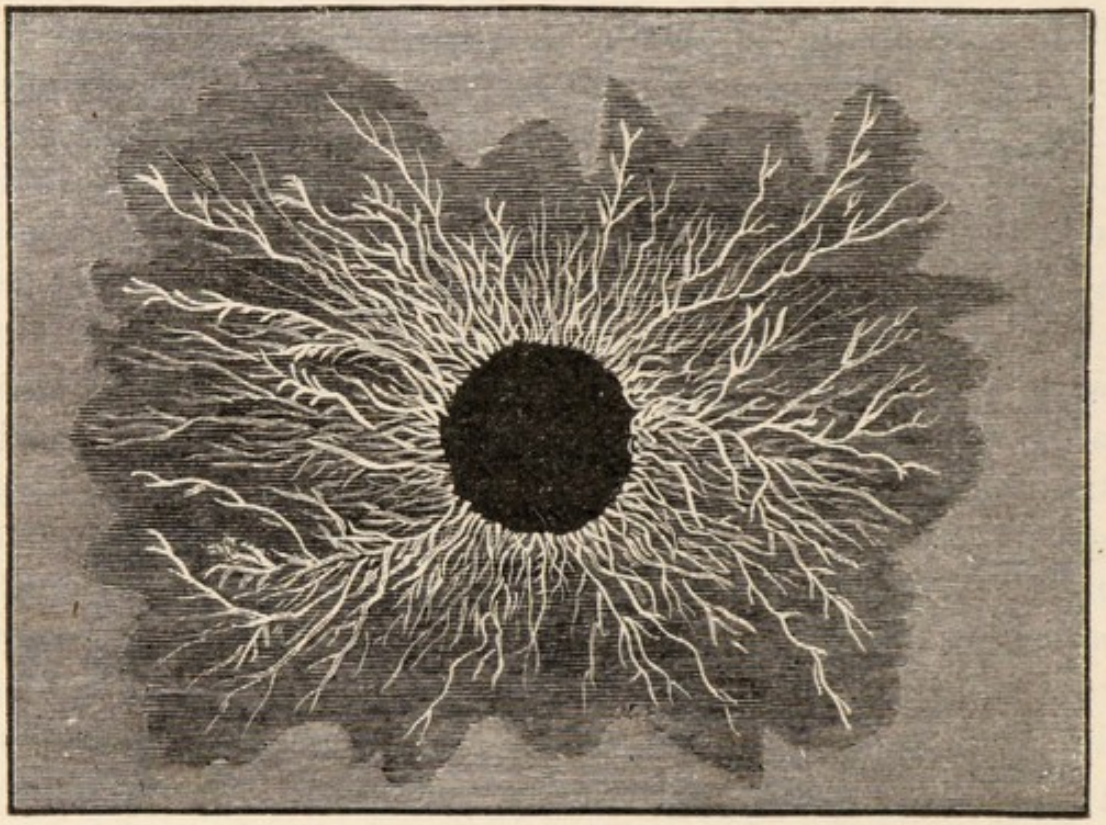


FIG. 184.—Lichtenberg's Figure (Positive).

creep slowly over the surface of bad conductors. Lichtenberg devised an ingenious and easy way of investigating the distribution of electricity by means of certain *electroscopic powders*. Take a charged Leyden jar and write with the knob of it upon a cake of pitch or a dry sheet of glass. Then sift, through a bit of muslin, over the cake a mixture

[1] Sometimes the flash seems to strike downwards from the clouds, sometimes upwards from the earth. This is an optical illusion, resulting from the unequal sensitiveness to light of different portions of the retina of the eye.

of powdered red lead and sulphur (vermilion and lycopodium powder answer equally well). The powders in this process rub against one another, the red lead becoming +, the sulphur −. Hence the sulphur will be attracted to those parts where there is + electrification on the disk, and settles down in curious branching yellow streaks like those shown in Fig. 184. The red lead settles down in little red heaps and patches where the electrification is

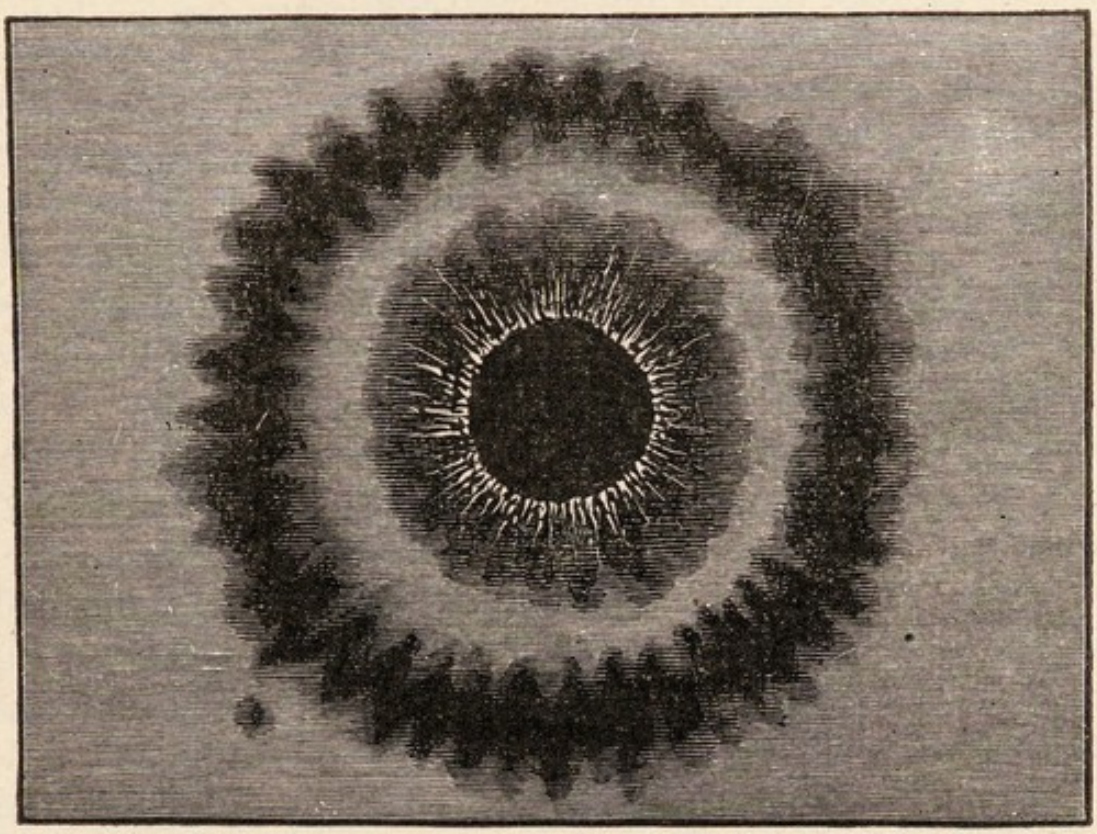


FIG. 185.—Lichtenberg's Figure (Negative).

negative. These rounded red patches indicate that the − discharge has been of the nature of a *wind* or silent discharge. The branching yellow streaks indicate that the positive discharge (as indeed may be heard) is of the nature of a *brush*. They are regarded by Nipher as drainage lines where the electrons pass through the dielectric (air) at the surface of the sheet of pitch, or glass. Fig. 185 shows the general appearance of the *Lichtenberg's figure* produced by holding the knob of the Leyden jar at the centre of a shellac plate that has

previously been rubbed with flannel, the negative electrification being attracted upon all sides toward the central positive charge. These same powders may be used to investigate how surfaces have become electrified by rubbing, and how pyroelectric crystals (Art. 75) are electrified during cooling.

Powdered tourmaline, warmed and then sifted over a sheet of glass previously electrified irregularly, will show similar figures, though not so well defined.

Similar figures can be made by directing a spark at the surface of stiff oil, where they persist for a short time and can be seen without using powders. If a spark is directed (in the dark) on a photographic dry-plate that is then developed, the forms are permanently preserved. In all cases the positive discharge always produces the characteristic ramified lines like those of Fig. 184.

Breath-figures can be made by electrifying a coin or other piece of metal laid upon a sheet of dry glass, and then breathing upon the glass where the coin lay, revealing a faint image of it on the surface of the glass.

Jervis-Smith found that if a coin or engraving laid face-down upon a photographic dry-plate is sparked with an induction coil, the plate receives an invisible image of the object, which can be photographically developed.

349. Physiological Effects.—The physiological effects of the current have been described in Lesson XX. Those produced by the spark-discharge are more sudden in character, but of the same general nature. Death is seldom the direct result. The shock causes a sudden cessation of respiration, resulting in suffocation as from drowning. The bodies of persons struck by the lightning spark frequently exhibit markings of a reddish tint where the discharge in passing through the tissues has lacerated or destroyed them. Sometimes these markings present a singular ramified appearance, like those of Fig. 184.

350. Dissipation of Charge.—However well insulated a charged conductor may be, and however dry

the surrounding air, it nevertheless slowly loses its charge, and in a few days will be found to be completely discharged. The rate of loss of charge is, however, not uniform. It is approximately proportional to the difference of potential between the body and the earth. Hence the rate of loss is greater at first than afterwards, and is greater for highly-charged bodies than for those feebly charged. The law of dissipation of charge therefore resembles Newton's law of cooling, according to which the rate of cooling of a hot body is proportional to the difference of temperature between it and the surrounding objects. If the potential of the body be measured at equal intervals of time it will be found to have diminished in a decreasing geometric series; or the logarithms of the potentials at equal intervals of time will differ by equal amounts. The rate of loss is, however, greater at negatively-electrified surfaces than at positive.

This may be represented by the following equation:

$$V_t = V_o \, \epsilon^{-bt},$$

where V_o represents the original potential and V_t the potential after an interval t. Here ϵ stands for the number 2·71828 . . . (the base of the natural logarithms), and b stands for the "coefficient of leakage," which depends upon the temperature, pressure, and humidity of the air. The same formula serves for the discharge of a condenser of capacity C through a resistance R, if b is written for $1/CR$.

351. Positive and Negative Electrification.—The student will not have failed to notice throughout this lesson frequent differences between the behaviour of positive and negative electrification. The striking dissimilarity in the Lichtenberg's figures, the displacement of the perforation-point in Lullin's experiment, the unequal tendency to dissipation at surfaces, the unequal action of heat on positive and negative charges, the remarkable differences in the various forms of brush and glow discharge, are all points that claim attention. Gassiot described the appearance in vacuum tubes as of a force

emanating from the negative pole. Crookes's experiments in high vacua (Art. 343), show corpuscles to be violently discharged from the kathode; the vanes of a little fly enclosed in such tubes being moved from the side struck by the kathodic discharge. Holtz found that when funnel-like partitions were fixed in a vacuum tube the resistance is much less when the open mouths of the funnels face the kathode; thus constituting a species of valve (see Art. 634). These matters are now accounted for by the electron theory of electricity (Art. 630).

352. Roentgen's Rays.—In 1895 Roentgen discovered that highly exhausted tubes, such as the Crookes tubes (Art. 343), when stimulated by electric discharges, emit some invisible rays, which he called X-rays, having very remarkable properties. They excite brilliant fluorescence on such substances as the platinocyanide of barium; they differ from ultra-violet light and other invisible kinds of radiation in being incapable of refraction, or of regular reflexion. They pass freely through aluminium, zinc, wood, paper, and flesh, but not through lead, platinum, glass, or bone. They also act on ordinary photographic plates. Hence it is possible by using a fluorescent screen to see, and by using sensitive plates to photograph, the shadows of such things as the bones in the living body, or the bullet in the barrel of a gun. It is found that these rays are given off, inside the Crookes tubes, from the solid surface—the glass or a metal target placed inside on purpose—against which the kathode rays are directed. Those substances which have highest atomic weights absorb the

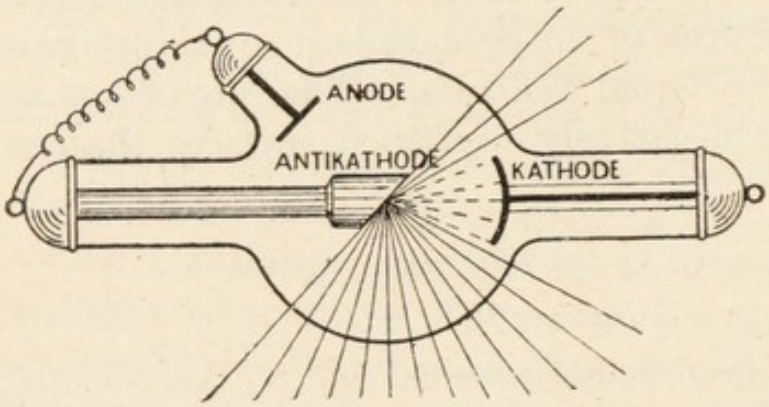


FIG. 186.—Roentgen-ray Tube.

Roentgen rays best, or if used as targets emit them best. Hence the target, or *antikathode*, should be of platinum, uranium, osmium, or tungsten. Fig. 186 depicts a Roentgen-ray tube in which the anode is a disk of aluminium; the kathode shaped as a shallow cup which directs its rays on the target or antikathode. If the skin be exposed for only a few minutes to Roentgen rays, an irritating and even dangerous inflammation may result. These rays closely resemble, in their properties, the penetrating "gamma" rays emitted from radium. (Art. 638, p. 677).

LESSON XXV.—*Atmospheric Electricity*

353. The Thunderstorm an Electrical Phenomenon.—The phenomena of atmospheric electricity are of three kinds. There are the well-known electrical phenomena of thunderstorms; and there are the phenomena of continual slight electrification in the air, best observed when the weather is fine. The phenomena of the polar Aurora constitute a third branch of the subject.

The detonating sparks drawn from electrical machines and from Leyden jars did not fail to suggest to the early experimenters, Hauksbee, Newton, Wall, Nollet, and Gray, that the lightning flash and the thunderclap were due to electric discharges. In 1749, Benjamin Franklin, observing lightning to possess almost all the properties observable in electric sparks,[1] suggested that

[1] Franklin enumerates specifically an agreement between electricity and lightning in the following respects:—Giving light; colour of the light; crooked direction; swift motion; being conducted by metals; noise in exploding; conductivity in water and ice; rending imperfect conductors; destroying animals; melting metals; firing inflammable substances; sulphureous smell (due to *ozone*, as we now know); and he had previously found that needles could be magnetized both by lightning and by the electric spark. He also drew attention to the similarity between the pale blue flame seen during thundery weather playing at the tips of the masts of ships (called by sailors St. Elmo's Fire), and the "glow" discharge at points.

the electric action of points (Art. 47), which was discovered by him, might be tried on thunderclouds, and so draw from them a charge of electricity. He proposed, therefore, to fix a pointed iron rod to a high tower. Before Franklin could carry his proposal into effect, Dalibard, at Marly-la-ville, near Paris, taking up the hint, erected an iron rod 40 feet high, by which, in 1752, he drew sparks from a passing cloud. Franklin shortly after succeeded in another way. He sent up a kite during the passing of a storm, and found the wetted string to conduct electricity to the earth, and to yield abundance of sparks. These he drew from a key tied to the string, a silk ribbon being interposed between his hand and the key for safety. Leyden jars could be charged, and many other electrical effects produced, by the sparks furnished from the clouds. The proof of the identity was complete. The kite experiment was repeated by Romas, who drew from a metallic string sparks 9 feet long, and by Cavallo, who made many important observations on atmospheric electricity.

354. Theory of Thunderstorms.—Solids and liquids cannot be charged throughout their substance; if charged at all, the electrification is upon their surface (see Art. 32). But gases and vapours, being composed of myriads of separate particles, can receive a bodily charge. The air in a room in which an electric machine is worked is found afterwards to be charged. The clouds are usually charged more or less with electricity, derived, probably, from evaporation going on at the earth's surface. The minute particles of water floating in the air become more highly charged. As they fall by gravitation and unite together, the strength of their charges increases. Suppose eight small drops to join into one. That one will have eight times the quantity of electricity distributed over the surface of a single sphere of twice the radius (and, therefore, of twice the capacity, by Art. 291) of one of the original drops; and its electrical potential

will therefore be four times as great. Now a mass of cloud may consist of such charged spheroids, and its potential may gradually rise, therefore, by the coalescence of the drops, and the electrification at the lower surface of the cloud will become greater and greater, the surface of the earth beneath acting as a condensing plate and becoming charged, by influence, with the opposite kind of electrification. Presently the difference of potential becomes so great that the intervening strata of air give way under the strain, and a disruptive discharge takes place at the point where the air offers least resistance. This lightning spark, which may be more than a mile in length, discharges only the electricity that has been accumulating at the surface of the cloud, and the other parts of the cloud will now react upon the discharged portion, producing internal attractions and internal discharges. The internal actions thus set up will account for the usual appearance of a thundercloud, that it is a well-defined flat-bottomed mass of cloud which appears at the top to be boiling or heaving up with continual movements.

355. Lightning and Thunder.—Three kinds of lightning have been distinguished by Arago: (i.) The *Zigzag flash* or "*Forked lightning*," of ordinary occurrence. The zigzag form is probably due either to the presence of solid particles in the air or to local electrification at certain points, making the crooked path the one of least resistance. (ii.) *Sheet lightning*, in which whole surfaces are lit up at once, is probably only the reflexion on the clouds of a flash taking place at some other part of the sky. It is often seen on the horizon at night, reflected from a storm too far away to produce audible thunder, and is then known as "summer lightning." (iii.) *Globular lightning*, in the form of *balls of fire*, which move slowly along and then burst with a sudden explosion. This form is very rare, but must be admitted as a real phenomenon, though some of the accounts of it are greatly exaggerated. Similar phenomena on a small

scale have been produced (though usually accidentally) with electrical apparatus.

The sound of the thunder may vary with the conditions of the lightning spark. The spark heats the air in its path, causing sudden expansion and compression all round, followed by as sudden a rush of air into the partial vacuum thus produced. If the spark be straight and short, the observer will hear but one short sharp *clap*. If its path be a long one and not straight, he will hear the successive sounds one after the other, with a characteristic *rattle*, and the echoes from other clouds will come *rolling* in long afterwards. The lightning-flash itself never lasts more than $\frac{1}{100000}$ of a second, but sometimes is oscillatory in character (see Art. 600).

The damage done by a lightning-flash when it strikes an imperfect conductor appears sometimes as a disruptive mechanical disintegration, as when the masonry of a chimney-stack or church-spire is overthrown, and sometimes as an effect of heat, as when bell-wires and objects of metal in the path of the lightning-current are fused. The physiological effects of sudden discharges are discussed in Arts. 270 and 349.

The "return-stroke" experienced by persons in the neighbourhood of a flash is explained in Art. 29.

Often two or more successive lightning flashes may follow one another down the same path. The probability is that the first flash ionizes (Art. 346) the air in its neighbourhood, thus providing a better conducting track along which a second flash follows.

356. Lightning Conductors.—The first suggestion to protect property from destruction by lightning was made by Franklin in 1749, in the following words:—

"May not the knowledge of this power of points be of use to mankind, in preserving houses, churches, ships, etc., from the stroke of lightning, by directing us to fix on the highest parts of those edifices upright rods of iron made sharp as a needle, and gilt to prevent rusting, and from the foot of those rods a wire down the outside of the building into the ground, or round one of the

shrouds of a ship, and down her side till it reaches the water? Would not these pointed rods probably draw the electrical fire silently out of a cloud before it came nigh enough to strike, and thereby secure us from that most sudden and terrible mischief?"

Maxwell proposed to cover houses with a network of conducting wires, without any main conductor, the idea being that then the interior of the building will, like Faraday's hollow cube (Art. 34), be completely protected from electric force. Much controversy has arisen respecting lightning-rods. Sir Oliver Lodge maintains the lightning flash to be of the nature of an electric oscillation (Art. 600) rather than a current. If so, the conductor of least resistance is not necessarily the best lightning-rod. Sir Oliver Lodge and the author independently, and for different reasons, recommend iron in preference to copper for lightning-rods.

The following points summarize the modern views on the subject:—

1. All parts of a lightning conductor should be of one and the same metal, avoiding joints as far as possible, and with as few sharp bends or corners as may be.

2. The use of copper for lightning-rods is a needless extravagance. Iron is far better. Ribbon is slightly better than round rod; but ordinary galvanized iron telegraph-wire is good enough.

3. The conductor should terminate not merely at the highest point of a building, but be carried to all high points. It is unwise to erect very tall pointed rods projecting several feet above the roof.

4. A good deep *wet* "earth" should be provided, independent of gas or water pipes, to which the conductor should be led down.

5. If in any part the conductor goes near a gas or water pipe it is better to connect them metallically than to leave them apart.

6. In ordinary buildings the conductor should be insulated away from the walls, so as to lessen liability of lateral discharge to metal stoves and things inside the house.

7. Connect all external metal-work, zinc spouts, iron crest ornaments, and the like, to each other, and to the earth, but *not* to the lightning conductor.

8. The cheapest way of protecting an ordinary house is to run common galvanized iron telegraph-wire up all the corners, along all the ridges and eaves, and over all the chimneys; taking them

down to the earth in several places, to a moist stratum, and at each place burying a load of coke.

9. Over the tops of tall chimneys it is well to place a loop or arch of the lightning conductor, made of any stout and durable metal.

357. Steady Strain and Impulsive Rush.—Sir Oliver Lodge distinguishes between two separate cases which may arise. If a thunder-cloud extending over part of the earth becomes gradually charged, or if a charged cloud gradually moves over a particular spot, the air between the cloud and the earth experiences a steadily increasing electric stress, under which points will tend to discharge better than blunt objects; and they are more likely to receive the lighting spark when it occurs; hence in this case pointed rods best protect chimneys of given height. But if a cloud is suddenly charged by receiving a lighting spark from another cloud in a sort of impulsive rush, a pointed rod under it has had no chance of any preparatory action, and is no more likely to take the discharge than a blunt conductor or a chimney-stack of equal height.

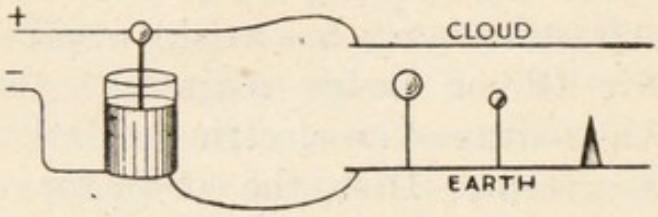


FIG. 187.—Steady Strain.

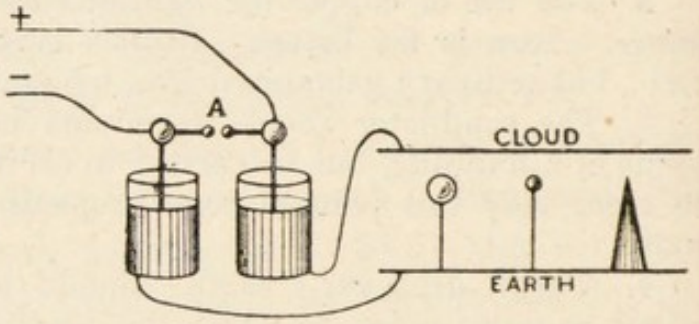


FIG. 188.—Impulsive Rush.

These two cases may be imitated in the laboratory by arranging apparatus as in Figs. 187 and 188; the former of which illustrates *steady strain*, the latter *impulsive rush*. A large flat sheet of metal is placed to represent a cloud, and an influence machine is used to charge the Leyden jars, as shown. If three objects of adjustable

height, one pointed, one tipped with a large metal ball, and one tipped with a small ball are placed below the plate, then in the case of steady strain it is found that at equal heights the pointed conductor is more liable to be struck, and it may be lowered some distance before the blunt conductors are equally often struck by the discharge. In the case of impulsive rush, which occurs whenever a spark passes at A, causing the plate to be suddenly charged, the discharge beneath it occurs equally often when all three conductors are arranged at equal heights.

358. Atmospheric Electricity.—In 1752 Lemonnier observed that the atmosphere was usually in an electrified condition. Cavallo, Beccaria, Ceca, and more recently Quetelet and Lord Kelvin, and others added to our knowledge of the subject. The main result is that the air above the surface of the earth is usually, during fine weather, positively electrified, or at least that it is positive with respect to the earth's surface, the earth's surface being relatively negative. The so-called measurements of "atmospheric electricity" are really measurements of difference of potential between a point of the earth's surface, and a point somewhere in the air above it. In the upper regions of the atmosphere the air is highly rarefied, and conducts like the rarefied gases in Geissler's tubes (Art. 342). The lower air is, when dry, a non-conductor. The upper stratum is believed to be charged with + electricity, while the earth's surface is itself negatively charged; the stratum of denser air between acting like the glass of a Leyden jar in keeping the opposite charges separate. If we could measure the electric potential at different points within the thickness of the glass of a charged jar, we should find that the values of the potential changed in regular order from a + value at one side to a − value at the other, there being a point of zero potential about halfway between the two. Now, the air in fine weather always gives + indications, and the potential of it is higher the higher we go to

measure it. Cavallo found higher electrification just outside the cupola of St. Paul's Cathedral than at a lower point of the building. Lord Kelvin found the potential in the island of Arran to increase from 23 to 46 volts for a rise of one foot in level; but the difference of potential was sometimes eight or ten times as much for the same difference of level, and changed rapidly, as the east wind blew masses of cloud charged with + or − electricity across the sky. Joule and Kelvin, at Aberdeen, found the rise of potential to be equal to 40 volts per foot, or 1·3 volts per centimetre rise of level.

During fine weather a negative electrification of the air is extremely rare. Beccaria only observed it six times in fifteen years, and then with accompanying winds. But in broken weather and during rain it is more often − than +, and exhibits great fluctuations, changing from − to +, and back, several times in half an hour. A definite change in the electrical conditions usually accompanies a change of weather. "If, when the rain has ceased [said Ceca], a strong excessive (+) electricity obtains, it is a sign that the weather will continue fair for several days."

359. Methods of Observation.—The older observers were content to affix to an electroscope (with gold leaves or pith-balls) an insulated pointed rod stretching out into the air above the ground, or to fly a kite, or (as Becquerel did) to shoot into the air an arrow communicating with an electroscope by a fine wire, which was removed before the arrow fell. Gay-Lussac and Biot lowered a wire from a balloon, and found a difference of potential between the upper and lower strata of the air. None of these methods is quite satisfactory, for they do not indicate the potential at any *one* point. To bring the tip of a rod to the same potential as the surrounding air, it is necessary that material particles should be discharged from that point for a short time, each particle as it breaks away carrying with it a + or a − charge until

the potentials are equalized between the rod and the air at that point. Volta did this by means of a small flame at the end of an exploring rod. Lord Kelvin employed a "water-dropper," that is an insulated cistern provided with a nozzle protruding into the air, from which drops issue to equalize the potentials: in winter he uses a small roll of smouldering touch-paper. Dellmann adopted another method, exposing a sphere to influence by the air, and then insulating it, and bringing it within-doors to examine its charge. Peltier adopted the kindred expedient of placing, on or near the ground, a delicate repulsion-electrometer, which during exposure was connected to the ground, then insulated, then removed indoors for examination. This process really amounted to charging the electrometer *by influence* with electrification of opposite sign to that of the air. The "quadrant" electrometer, described in Art. 307, and a "portable" electrometer on the attracted-disk principle, are now used for observations on atmospheric electricity. Using a water-dropping collector and a Kelvin electrometer, Everett made a series of observations in Nova Scotia, and found the highest + electrification in frosty weather, with a dry wind charged with particles of ice.

360. Diurnal Variations.—Quetelet found that at Brussels the daily indications (during fine weather) showed two *maxima* occurring in summer at 8 A.M. and 9 P.M., and in winter at 10 A.M. and 6 P.M. respectively, and two *minima* which in summer were at the hours of 3 P.M. and about midnight. He also found that in January the electricity was about thirteen times as strong as in June. At Kew there is a maximum at 8 A.M. in summer, and at 10 A.M. in winter; and a second minimum at 10 P.M. in summer and 7 P.M. in winter. The *maxima* correspond fairly with hours of changing temperature, the *minima* with those of constant temperature. In Paris, Mascart found but one maximum, just before midnight: at sunrise the electricity diminishes until

about 3 P.M., when it has reached a minimum, whence it rises till nightfall. Our knowledge of this important subject is still very imperfect. We do not even know whether all the changes of the earth's electrification relatively to the air are due to causes operating above or below the earth's surface.

361. The Aurora.—In all the northern regions of the earth the *Aurora borealis*, or "Northern Lights," is an occasional phenomenon; and within and near the Arctic circle is of almost nightly occurrence. Similar lights are seen in the south polar regions of the earth, and are denominated *Aurora australis*. As seen in European latitudes, the usual form assumed by the aurora is that of a number of ill-defined streaks or streamers of a pale tint (sometimes tinged with red and other colours), either radiating in a fan-like form from the horizon in the direction of the (magnetic) north, or forming a sort of arch across that region of the sky, of the general form shown in Fig. 189. A certain flickering or streaming motion is often discernible in the streaks. Under very favourable circumstances the aurora extends over the entire sky. The appearance of an aurora is usually accompanied by a *magnetic storm* (Art. 166), causing the compass-needles over whole regions of the globe to be disturbed with irregular and repeated deviations. This fact, and the position of the auroral arches and streamers with respect to the magnetic meridian, directly suggest an electric origin for the light,—a conjecture which is confirmed by the many analogies found between auroral phenomena and those of discharge in rarefied air (Arts. 342 and 345). Yet the presence of an aurora does not, at least in our latitudes, affect the electrical conditions of the lower regions of the atmosphere. On September 1, 1859, a severe magnetic storm occurred, and auroræ were observed almost all over the globe; at the same time a remarkable outburst of energy took place in the

photosphere of the sun; but no simultaneous development of atmospheric electricity was recorded. Auroræ appear in greater frequency in periods of about $11\frac{1}{2}$ years, which agrees pretty well with the cycles of maximum of magnetic storms (see Art. 166) and of sun-spots.

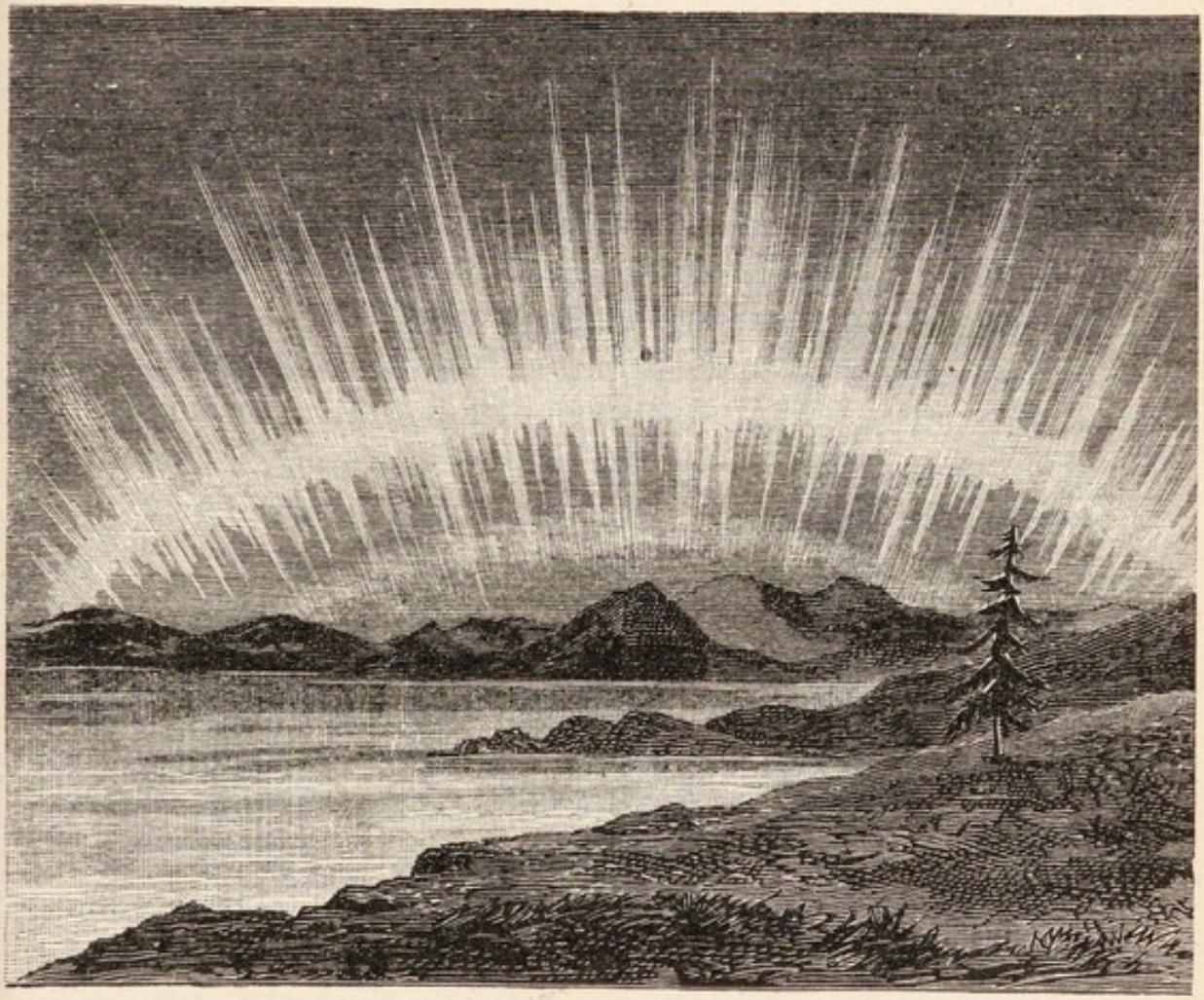


FIG. 189.—The Aurora Borealis.

The spectroscope shows the auroral light to be due to gaseous matter, its spectrum consisting of a few bright lines apparently characteristic of the rarer gases lately discovered as constituents of the atmosphere.

According to Nordenskiold the terrestrial globe is perpetually surrounded at the poles with a ring or crown of light, single or double, to which he gives the name of

the "aurora-glory." The outer edge of this ring he estimates to be at 120 miles above the earth's surface, and its diameter about 1250 miles. The centre of the aurora-glory is not quite at the magnetic pole, being in lat. 81° N., long. 80° E. This aurora-glory usually appears as a pale arc of light across the sky, and, except during magnetic and auroral storms, is destitute of the radiating streaks shown in Fig. 189.

An artificial aurora was produced by Lemström, who erected on a mountain in Lapland a network of wires presenting many points to the sky. By insulating this apparatus and connecting it by a telegraph-wire with a galvanometer at the bottom of the mountain, he was able to observe actual currents of electricity when the auroral beam appeared above the mountain. Birkeland has reproduced the auroral corona experimentally by sending electric discharges into a large partially exhausted vacuum tube in which was suspended a spherical electromagnet as a model of the earth's globe.

The electron theory has been made by Arrhenius to account for the occurrence of auroræ and the allied phenomena of magnetic storms and the solar corona.

The sun is regarded as continually discharging electrons into space. In the approximate vacuum immediately surrounding the sun the flying electrons may well give rise to the appearance of the solar corona. The earth is exposed to a continual bombardment of electrons from the sun, and the auroræ are due to the catching and guiding of the streams of electrons by the earth's magnetic lines of force directed to the poles, where in the rarified upper regions of the atmosphere the phenomena of the vacuum tube are reproduced. A torrent of electrons constitutes an electric current of strength sufficient to produce considerable magnetic effects, and thus the connexion of auroræ and magnetic storms is explained.

CHAPTER V

ELECTROMAGNETICS

LESSON XXVI.—*Magnetic Potential*

362. Electromagnetics. — That branch of the science of electricity which treats of the relation between electric currents and magnetism is termed **Electromagnetics.** In Arts. 130 to 142 the laws of magnetic forces were explained, and the definition of "unit pole" was given. It is, however, much more convenient, for the purpose of study, to express the interaction of magnetic and electromagnetic systems in terms not of "force" but of "*potential*"; *i.e.* in terms of their power to do work. In Art. 280 the student was shown how the electric potential due to a quantity of electricity may be evaluated in terms of the work done in bringing up as a test charge a unit of + electricity from an infinite distance. **Magnetic Potential** can be measured similarly by the ideal process of bringing up a unit magnetic pole (N-seeking) from an infinite distance, and ascertaining the amount of work done in the operation. Hence a large number of the points proved in Lesson XXI. concerning electric potential will also hold true for magnetic potential. The student may compare the following propositions with the corresponding ones in Articles 280 to 285 :—

(a) *The magnetic potential at any point is the work that must be spent upon a unit magnetic* (N-seeking) *pole in bringing it up to that point from an infinite distance.*

(b) *The magnetic potential at any point due to a system of magnetic poles is the sum of the separate magnetic potentials due to the separate poles.*

The student must here remember that the potentials due to S-seeking poles will be of opposite sign to those due to N-seeking poles, and must be reckoned as negative.

(c) *The (magnetic) potential at any point due to a system of magnetic poles may be calculated* (compare with Art. 280) *by summing up the strengths of the separate poles divided each by its own distance from that point.* Thus, if poles of strengths m', m'', m''', *etc.*, be respectively at distances of r', r'', r''', . . . from a point P, then the following equation gives the potential P :—

$$V_P = \frac{m'}{r} + \frac{m''}{r''} + \frac{m'''}{r'''} + \ldots\ldots\ldots\ldots$$

or $$V_P = \Sigma\frac{m}{r}.$$

(d) *The difference of (magnetic) potential between two points is the work to be done* on *or* by *a unit (N-seeking) pole in moving it from one point to the other.* It follows that if m units of magnetism are moved through a difference of potential V, the work W done will be

$$W = mV.$$

(e) *Magnetic force on unit pole is the rate of change of (magnetic) potential per unit of length* : it is numerically equal to the intensity of the field. This is proved thus :—In Art. 142, $\mathfrak{H}$, the intensity of the field is defined by the force exerted by the field on a unit of magnetism, it follows that on m units of magnetism the force f will be m times as great, or,

$$f = m\mathfrak{H}.$$

Now work is the product of a force into the length through which its point of application moves forward; hence it follows that

$$W = fl = m\mathcal{H}l.$$

But

$$W = mV;$$

whence

$$V = \mathcal{H}l,$$

and

$$\mathcal{H} = V/l.$$

$\mathcal{H}$, at any point, is therefore the same as the potential gradient at that point.

Example.—The difference of magnetic potential between two points 5 centims. apart along a magnetic field in which there are 6000 lines per sq. cm., is 30,000. Or, it would require 30,000 ergs of work to be expended to push a unit pole from one point to the other against the magnetic force.

(f) *Equipotential surfaces are those (imaginary) surfaces surrounding a magnetic pole or system of poles, over which the (magnetic) potential has equal values.* Thus, around a single isolated magnetic pole, the potential would be equal all round at equal distances; and the equipotential surfaces would be a system of concentric spheres at such distances apart that it would require the expenditure of one *erg* of work to move a unit pole up from a point on the surface of one sphere to any point on the next (see Fig. 160). Around any real magnet possessing two polar regions the equipotential surfaces would become much more complicated. *Magnetic force, whether of attraction or repulsion, always acts across the equipotential surfaces in a direction normal to the surface; the magnetic lines of force are everywhere perpendicular to the equipotential surfaces.*

363. Magnetic Tubes of Force.—From a single magnetic pole (supposed to be a point far removed from all other poles) the lines of force diverge radially in all directions. The space around may be conceived as thus divided up into a number of conical regions, each having its apex at that pole; and through each cone, as through a tube, a certain number of lines of force will pass. Such a conical space may be called a **tube of force.** The total number of magnetic lines within any tube of force is called the **magnetic flux.**[1] No matter where you cut across a tube of force, the cross-section will cut through the enclosed flux, though the lines diverge more widely as the tube widens. Hence,

(g) *The magnetic flux across any section of a tube of force is constant wherever the section be taken.*

In case the magnetism is not concentrated at one point, but distributed over a surface from which the tubes start, we shall have to speak of the "amount of magnetism" rather than of the "strength of pole," and in such a case the

(h) *Magnetic density is the amount of magnetism per unit of surface.* In the case of a simple magnetic shell over the face of which the magnetism is distributed with uniform density, the "strength" of the shell is defined as the thickness of the shell multiplied by the surface-density.

364. Magnetic Flux.—The term magnetic flux, used above, receives a special significance when we consider magnetic circuits, that is to say, systems (such as electromagnets with their keepers) wherein the magnetic lines traverse definite paths in a circuital manner, and thread their way through the magnetizing

[1] The *magnetic flux* is by some writers called the *total induction*: but the word induction ought to be kept for the *operation* of inducing.

coil which surrounds them. The magnetic flux denotes the total number of such magnetic lines following the course of the circuit. The whole number of lines in the flux of a large electromagnet may amount to several millions, depending on the cross section of the iron core, and the degree to which it is magnetized. The amount of flux divided by the cross-section of the circuit is called the **flux-density** (symbol $\mathfrak{B}$). If a flux of $\mathfrak{F}$ lines passes through area **A**, the flux-density will be

$$\mathfrak{B} = \mathfrak{F} \div \mathbf{A}$$

Example.—In a certain electromagnet the core of which had a cross-section of 72 square centimetres, the magnetic flux was found to be 1,188,000 lines. The flux-density in the iron was therefore 16,500 lines per square centimetre.

365. Intensity of Field.—We have seen (Art. 118) that every magnet is surrounded by a certain "field," within which magnetic force is observable. We may completely specify the properties of the field at any point by measuring the *strength* and the *direction* of that force,—that is, by measuring the "**intensity** *of the field*" and the direction of the lines of force. *The "intensity of the field" at any point is measured by the force with which it acts on a unit pole placed at that point.* Hence, *unit intensity of field is that intensity of field which acts on a unit pole with a force of one dyne.* There is therefore a field of unit intensity at a point one centimetre distant from the pole of a magnet of unit strength. Suppose a magnet pole, whose strength is m, placed in a field at a point where the intensity is $\mathfrak{H}$, then the force will be m times as great as if the pole were of unit strength, and

$$f = m \times \mathfrak{H}.$$

To aid the imagination by a graphic conception we adopt Faraday's notion of representing the properties of a magnetic field by supposing lines to be drawn so that they represent the *direction* and *intensity* of the field by

the *direction* and *density* of the lines. This leads to the empirical rule to **draw as many magnetic lines to the square centimetre (of cross section) as there would be dynes of force on unit pole.** A field of $\mathcal{H}$ units means one where there would be $\mathcal{H}$ dynes on unit pole, or $\mathcal{H}$ lines per square centimetre. *It follows that a unit magnetic pole will have a flux of* 4π *lines proceeding from it*: for there is unit field at unit distance away, or one magnetic line per square centimetre; and there are 4π square centimetres of surface on a sphere of unit radius drawn round the pole. A magnet, whose pole-strength is m, has a flux of $4\pi m$, or $12{\cdot}57 \times m$, lines running through the steel, and diverging at its pole. This is the origin of the 4π symbol which comes in so often into electromagnetic formulæ. Suppose a narrow crevasse between the faces of two opposing magnets, each having σ units of magnetism per square centimetre of their pole surfaces. The field in the space between will have the value

$$\mathcal{H} = 4\pi\sigma.$$

366. Work done by Conductor carrying Current when it cuts across the Lines of a Magnetic Field.—By definition (Art. 280) it follows that the work W done in moving Q units of electricity against an electromotive-force V is equal to QV. Suppose that this electromotive-force is due to the conductor cutting $\mathcal{F}$ magnetic lines during time t. Then if the motion be uniform and the average current during the time is called i, it follows that $Q = it$. And the average electromotive-force is (see Art. 243) $= \mathcal{F}/t$. Inserting these values we get

$$W = it \times \mathcal{F}/t,$$

or

$$W = i\mathcal{F};$$

or, in words, *the work done in moving a current across a magnetic flux is equal to the product of the current into the total number of magnetic lines cut.* It will be noted

that the work done is the same whether the time is long or short. If i and $\mathfrak{F}$ are in absolute (C.G.S.) units, W will be in *ergs*.

367. Force exerted by Magnetic Field on Wire carrying Current.—If a wire is moved sideways across the lines of a magnetic field, through a distance x, it will sweep out an area equal to its own length l multiplied by x. And if $\mathfrak{H}$ is the number of magnetic lines per square centimetre the total number of lines cut will be $= \mathfrak{H}lx$; and the work done if the wire carries current i will be $W = i\mathfrak{H}lx$. But if work W is done in moving the wire through distance x the force f exerted will be W/x. Hence the force, in dynes, on the wire will be

$$f = i\mathfrak{H}l;$$

or, in words, *the force is proportional to the current, to the intensity of the field, and to the length of wire in the field.* It is a force[1] that tends to drag the wire laterally, acting at right angles to the wire and to the lines of the field.

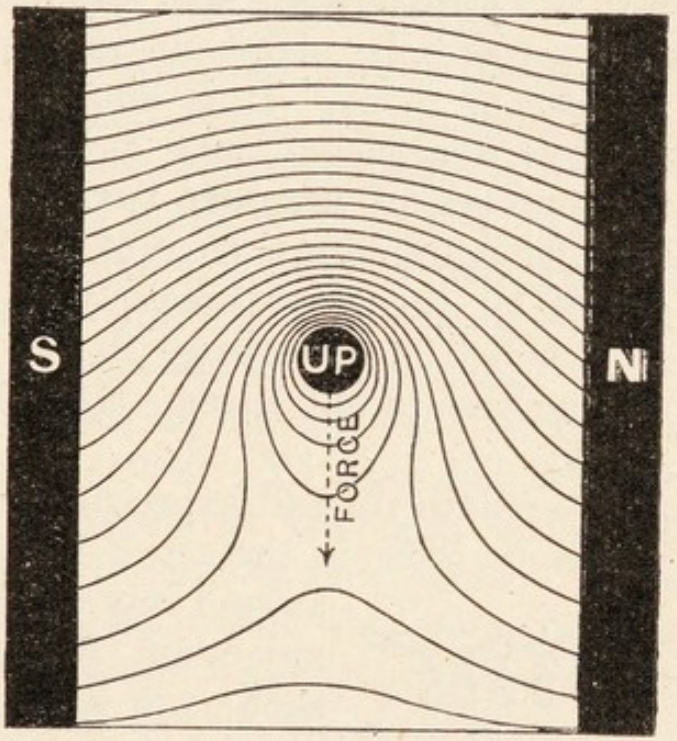


FIG. 190.—Drag of Field on Conductor carrying Conductor.

This action is of course due to stresses going on in the medium, and is worthy of further thought. Consider the magnetic field in a gap between a large N-pole and a similar S-pole. The lines will go nearly uniformly straight across. Let a current flow in a copper wire that lies across the field. In Fig. 190 the wire is seen end-

[1] In calculating by the expression above, if i is given in amperes it must be divided by 10.

ways, with the current flowing "up" or toward the observer. The result will be that the magnetic field of the current (Arts. 215 and 370) will be superposed (Art. 144) upon that of the magnets, and will perturb it: the form of the perturbed field being that shown. In such a field the stresses, which act as though the magnetic lines tended to shorten themselves, will have the effect of urging the wire mechanically in the direction shown. This mechanical force acts on the matter of the wire, though due to the current.

368. Magnetomotive-force (or Total Magnetizing Force) of a Current circulating in a Spiral Conductor.—Let a conductor carrying a current of i amperes be coiled up in a spiral having S as the number of turns. It is known, and easily understood, that the total magnetizing force of such is proportional to the number of **ampere-turns**; for experiment shows that, for example, a current of 10 amperes circulating in a coil of 50 turns has precisely the same magnetic power as a current of 5 amperes in 100 turns, or as a current of 1 ampere in 500 turns. Each of these has 500 *ampere-turns.*

To obtain the full expression let us find the work that would be done in the act of moving a unit magnet-pole around any closed path (Fig. 191) from any point P to the same point again, such path passing through all the turns of the magnetizing coil. The work done on a unit-pole in moving it once around the closed path, against the magnetic forces of the system, is a measure of *the ability of that system to magnetize*; or, in other words, is a measure of its **magnetomotive-force.**[1] Such a closed path may lie, according to circumstances, either wholly in air, or

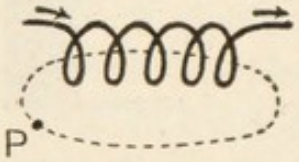


FIG. 191.

[1] Since this magnetomotive-force is made up of a number of small elements distributed variously along the path, it is sometimes called the *line-integral of the magnetizing forces.*

partly in air partly in iron, or wholly in iron. The argument is entirely independent of any materials lying along the ideal path.

Now imagine this unit-pole, with its 4π magnetic lines radiating out of it, to be passed along the closed path (Fig. 191) from P, through the spirals to P again. Each turn of the coil will cut each of the magnetic lines once, and therefore, by Arts. 365 and 366, the total work done will be

$$W = 4\pi i S/10,$$

where we divide by 10 to bring *amperes* to absolute C.G.S. units. Hence the magnetomotive-force of that coil is proportional to the number of ampere-turns.

369. Intensity of Field in a long Tubular Coil, or Solenoid.—A spiral coil wound on a tube is called a *solenoid*. It has, when a current circulates in its coils, a magnetic field along the inside of it, and is, in fact, so long as the current circulates, a magnet without iron. This magnetic field, if the spiral is a very long one—say 20 times as long as the diameter of the spirals,—is very uniform all along the interior, except just toward the ends, where it becomes weaker. To find the intensity of the field $\mathcal{H}$, we may remember that (Art. 362, e) the work done on a unit-pole in moving it through a length l of field $\mathcal{H}$ is equal to $\mathcal{H}l$. But the work done in moving it along the tubular coil of length l is practically equal to that done around the closed path, since nearly all the forces are met along the part of the path inside. Hence we may equate $4\pi i S/10$ to $\mathcal{H}l$; giving the result

$$\mathcal{H} \text{ (in } \textit{gausses}) = \frac{4\pi}{10} \times \frac{iS}{l},$$

or *the intensity of the field in a long spiral is equal to* 1·257 *times the number of ampere-turns per centimetre of length.*

At the mouth of a long spiral the intensity of the field is exactly half what it is midway between the ends.

Example.—A tubular coil 60 cm. long is wound with 8 layers of 280 turns each, of an insulated wire carrying 4 amperes. The value of $\mathfrak{H}$ all along the middle portion of the coil will be 187·5 *gausses*. At the open ends the value will be 94 *gausses*.

370. Magnetic Field due to Indefinitely Long Straight Current. Law of Inverse Simple Distance.—Consider a unit-pole at point P at a distance r (Fig. 192) from an indefinitely long straight conductor carrying a current of i amperes. The force tending to make the pole circulate around the wire may be calculated very simply as follows. If the unit-pole were to be moved once around the wire on a circular path with radius r, each one of the 4π magnetic lines that radiate from it would be cut once by the wire. Hence, by Art. 366, the work done in one such revolution would be equal to $4\pi i/10$. But this work has been done by moving the unit, against the forces of the system, along a path the length of which is $2\pi r$; wherefore

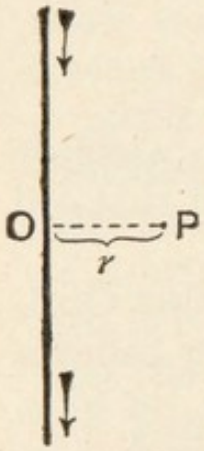


FIG. 192

$$W = f \times 2\pi r = 4\pi i/10,$$

whence

$$f = 2i/10r.$$

From this it appears that the force on unit-pole, and therefore the number of *gausses* or intensity of the field, is *directly proportional to the current*, and *varies inversely as the simple distance* from the wire.

Example.—The force exerted on a pole of 1200 units of magnetism at a distance of 4 centimetres from a long straight wire carrying current of 60 amperes will be 3600 dynes, or 3·66 grammes.

The fact that the force varies inversely as the simple distance, and not as the square, was experimentally discovered by Biot and Savart in 1820.

Around such a straight conductor the magnetic field

consists of a cylindrical whirl of circular lines (Art. 215), their density decreasing as their radius increases. Outside a straight wire carrying a 10-ampere current the values of $\mathcal{H}$ are: 2 at 1 cm.; 1 at 2 cm.; 0·4 at 5 cm., and so forth. Fig. 193 shows the falling off in density of the field around a long straight wire carrying a current in a direction downwards normally through the plane of the diagram. A pole tends to move circularly around the wire.

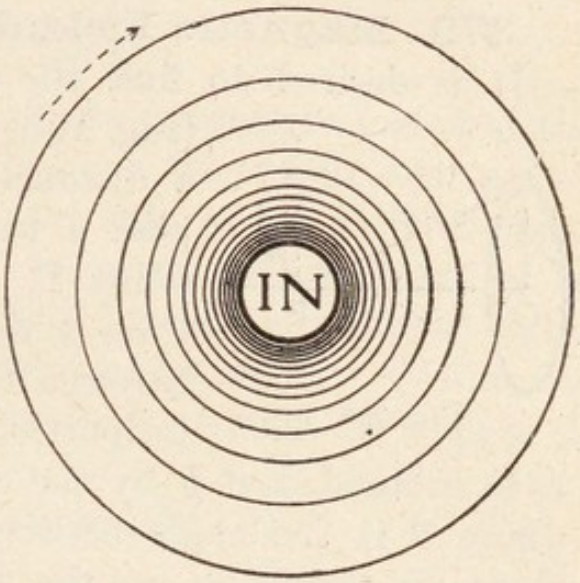


FIG. 193.—Field surrounding Current in a Straight Wire.

371. Mutual Action of Magnet-pole and of Element of Current.—Consider an element of current, that is to say, an indefinitely short piece of a conductor traversed by a current. Calling the length dl, and the current i, we have idl as the magnetic value of the element with respect to all points in its equatorial plane. Suppose the element to be set (Fig. 194) at distance r from a magnet-pole of m units, and at right angles to the line joining them. Then, as the element is small compared with r, the law of inverse squares will hold good: the elementary force df will be

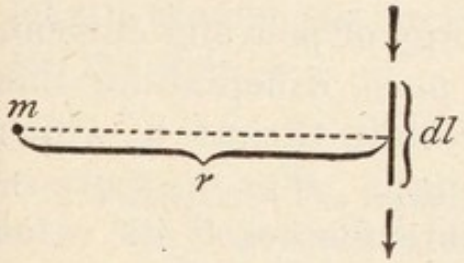


FIG. 194.

$$df = \frac{m \cdot idl}{10 \cdot r^2}.$$

This will be neither an attraction nor a repulsion, but a force at right angles to the element and to the line joining it to m. If the elementary conductor is oblique, making an angle θ with r', the expression must be multiplied by $\sin\theta$, making it :—

$$df = \frac{m \cdot i \cdot \sin\theta \cdot dl}{10 \cdot r^2}.$$

372. Magnetic Field due to Circular Current.—It is desired to find the effect of a circular current (Fig. 195) at any point on the axis, at a distance x from the centre. Suppose a unit-pole were placed at this point P, only a fraction of the 4π lines which radiate from it will pass through the circle; the number being proportional to the solid-angle (Art. 151) subtended at P by the circle, namely $2\pi(1-\cos\theta)$, where θ is the angle between axis and slant distance a. Hence in bringing up the pole to this place, from an infinite distance, the work done by causing these lines to cut across the wire carrying current i amperes will be (by Art. 366)

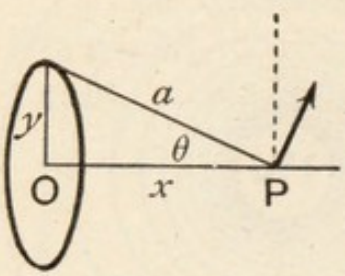


FIG. 195.

$$W = 2\pi i(1-\cos\theta)/10.$$

This represents the mutual energy of pole and current. To calculate the force at P we must differentiate this expression with respect to x, to ascertain the rate at which the mutual energy falls per unit length. For this purpose it will be convenient to substitute for $\cos\theta$ its value $x/(x^2+y^2)^{\frac{1}{2}}$. Substituting and differentiating we get

$$f = dW/dx = \tfrac{2}{10}\pi i y^2/(x^2+y^2)^{\frac{3}{2}}.$$

Now $(x^2+y^2)^{\frac{3}{2}}$ is equal to a^3; whence the rule that the magnetic force at any point P on the axis varies directly as the current, and *inversely as the cube of the slant distance.* (Compare case of a bar-magnet, Art. 140.)

Another way of arriving at this result is as follows. Taking the expression found in Art. 371 for the action of an element of current, we may consider the effect of the topmost element of the ring (Fig. 195), situated at a slant distance $a = \sqrt{x^2+y^2}$. The elementary force df exerted on unit-pole at P by the element idl will be at

right angles to a and to dl (in direction of the arrow), and, by Art. 219, of the value

$$df = idl/10a^2.$$

As the elements such as dl are symmetrical around the axis we must resolve their oblique forces into two parts: part acting at right angles to the axis, which will disappear by mutually cancelling out in pairs, and part acting in the line of the axis, which will for each element be equal to the above expression multiplied by sin θ. So that the elementary axial force due to each element of length dl will be

$$df = idl \cdot \sin\theta / 10a^2;$$

or, since $\sin\theta = y/a$,

$$df = idl \cdot y/10a^3.$$

But the total force f due to all the elements will be the integral due to the sum of their lengths, and this integral length around the circle is $\int dl = 2\pi y$. Whence it at once follows that

$$f = 2\pi i y^2/10a^3.$$

Example.—The force on unit-pole at a point 12 centimetres along the axis from the centre of a circle of wire of 5 centimetres radius, carrying 30 amperes will be $2\pi \times 30 \times 5 \times 5 \div 10 \times 13 \times 13 \times 13 = 2{\cdot}78$ . . . *dynes.*

Note that if P is pushed up to the centre of the circle $a = y$, and we get back to the rule for the tangent galvanometer (Art. 225), $f = 2\pi i/10r$.

Also note that for very great distances of P from centre a becomes sensibly equal to x, the force varying inversely as the cube of the axial distance.

This affords one way of varying the sensitiveness of tangent galvanometers, the needle with its scale being arranged to slide out along the axis of the coil. At a point P, such that $a = 2y$, the force of coil on needle is only $\frac{1}{8}$ of what it is at centre.

373. Moment of Circular Coil.—A circular coil carrying a current acts as a magnet whose axis is the axis of the coil. Its *magnetic moment* (Art. 137) will be the product of the current (in absolute units) into the area enclosed. Or, if i is in amperes, and A the total area of all the turns, its moment will be $Ai/10$. If such a coil is placed in a field of intensity $\mathcal{H}$ it will tend to turn so as to place its axis along the direction of the field. If the angle between those directions is θ, the torque (or turning-moment) will be $= Ai\mathcal{H} \sin \theta/10$.

374. Potential due to a Solenoidal or Circuital Distribution of Magnetism.—A long thin uniformly magnetized magnet exhibits poles only at the two ends, and acts on external objects just as if there were two equal quantities of opposite kinds of magnetism collected at these two points. Such a distribution of magnetism is sometimes called *solenoidal* or *circuital*. The magnetic potential due to a solenoid, and all its magnetic effects, depend only on the position of its two poles, and on their strength, and not on the form of the bar between them, whether straight or curved. In Art. 362 (c) was given the rule for finding the potential due to a system of poles. Suppose the two poles of a solenoid have strengths $+ m$ and $- m$ respectively, and that the distances of these poles from an external point P are r_1 and r_2, then the potential at P will be

$$V_P = m\left(\frac{1}{r_1} - \frac{1}{r_2}\right).$$

Suppose a magnet curled round until its N and S poles touch one another: it will not act as a magnet on an external objeet, and will have no "field"; for if the two poles are in contact, their distances r_1 and r_2 to an external point P will be equal, and

$$\left(\frac{1}{r} - \frac{1}{r_2}\right) \text{ will be } = 0.$$

375. Potential due to a Magnetic Shell.—Gauss demonstrated that *the potential due to a magnetic shell at a point near it is equal to the strength of the shell multiplied by the solid-angle subtended by the shell at that point*; the "strength" of a magnetic shell being the product of its thickness into its surface-density of magnetization.

If ω represents the solid-angle subtended at the point P, and i the strength of the shell, then

$$V_P = \omega i.$$

Here ωi represents the work that would have to be done on or by a unit-pole, to bring it up from an infinite distance to the point P, where the shell subtends the solid-angle ω. To establish this proposition would require the integral calculus. At a point Q where the solid-angle subtended by the shell is different, the potential will be different, the difference of potential between P and Q being

$$V_Q - V_P = i(\omega_Q - \omega_P).$$

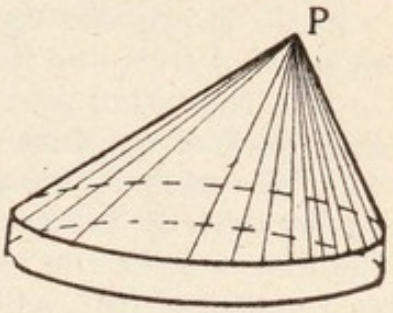


FIG. 196.

If a magnet-pole whose strength is m were brought up to P, m times the work would have to be done, or the mutual potential would be $= m\omega i$.

376. Potential Energy of a Magnet-pole and a Shell.—It is evident that if the shell of strength i is to be placed where it subtends a solid-angle ω at the pole m, it would require the expenditure of the same amount of work to bring up the shell from an infinite distance on the one hand, as to bring up the magnet-pole from an infinite distance on the other; hence $m\omega i$ represents both the potential energy of the pole on the shell and the potential energy of the shell on the pole. Now the lines of force from a pole may be regarded as proportional in number to the strength of the pole, and from a single pole they would radiate out in all directions equally. Therefore, if a magnet-pole was placed at P, at the apex of the solid-angle of a cone, the number of lines of force which would pass through the solid-angle would be proportional to that solid-angle. It is therefore convenient to regard $m\omega$ as representing the number of lines of force of the pole which pass through the shell, and we may call the number so intercepted F. Hence *the potential energy of the system consisting of a magnet-pole and a magnetic shell is equal to the strength of the shell multiplied by the number of lines of force (due to the magnet-pole) which pass through the shell*; or $W = Fi$. To bring up a N-seeking (or +) pole against the repelling force of the N-seeking face of a magnetic shell requires a positive amount of work to be done; and their mutual reaction would enable work to be done afterwards by virtue of their position: in this case then the potential is +. But in moving a N-seeking pole up to the S-seeking face of a shell work will be done *by* the pole, for it is attracted up; and the work done *by* the pole may be regarded as our doing *negative* work.

Again, suppose we could bring up a unit N-seeking pole against the repulsion of the N-seeking face of a shell of strength i, and should push it right up to the shell; when it actually reached the plane of the shell the shell would occupy a whole horizon, or half

the whole space around the pole, the solid-angle[1] it subtended being therefore 2π, and the potential will be $+ 2\pi i$. If we had begun at the S-seeking face the potential at that face would be $- 2\pi i$. It appears then that *the potential alters its value by* $4\pi i$ *on passing from one side of the shell to the other.*

If a N-seeking pole be brought up to the N-seeking face of a shell none of the lines of force of the magnet will cut the shell, but will be repelled out as in Fig. 74 ; whereas if a N-seeking pole be brought up to the S-seeking face of a shell, large numbers of the lines will be run into one another as in Fig. 73 ; and the pole, as a matter of fact, will be attracted up to the shell, where as many lines of force as possible are cut by the shell. We may formulate this action by saying that *a magnetic shell and a magnet-pole* react on one another and *urge one another in such a direction as to make the number of lines of force that are cut by the shell a maximum* (Maxwell's Rule, Art. 217). Outside the attracting face of the shell the potential is $- \omega i$, and the pole moves so as to make this negative quantity as great as possible, or to make the potential a minimum. Which is but another way of putting the matter as a particular case of the general proposition that bodies tend to move so that the energy they possess in virtue of their position tends to run down to a minimum.

377. Magnetic Potential due to Current.—The propositions concerning magnetic shells given in the preceding paragraphs derive their great importance because of the fact laid down in Art. 216 that circuits, traversed by currents of electricity, behave like magnetic shells. Adopting the electromagnetic unit of current (Art. 380), we may at once go back to Art. 374 and take the theorems about magnetic shells as being also true of closed voltaic circuits.

(*a*) **Potential due to closed circuit** (compare Art. 375).

The potential V *due to a closed voltaic circuit* (traversed by a current) *at a point* P *near it, is equal to the strength of the current multiplied by the solid-angle* ω *subtended by the circuit at that point.* If i be the strength of the current in absolute electromagnetic units, then

$$V_P = - \omega i.$$

(*b*) At a point Q, where the solid-angle subtended by the circuit is ω_Q instead of ω_P, the potential will have a different value, the difference of potential being

$$V_Q - V_P = - i (\omega_Q - \omega_P).$$

(*c*) **Mutual Potential of a Magnet-pole and a Circuit.**—If a magnet-pole of strength m were brought up to P, m

[1] See note on Ways of Reckoning Angles, Art. 147 and Appendix A.

times as much work will be done as if the magnet-pole had been of unit strength, and the work would be just as great whether the pole m were brought up to the circuit or the circuit up to the pole. Hence, the *mutual potential energy* will be

$$-m\omega i.$$

But, as in Art. 376, we may regard $m\omega$ as representing the number of lines of force of the pole which are intercepted by and pass through the circuit, and we may write F for that number, and say

$$V = -iF,$$

or *the mutual potential energy of a magnet-pole and a circuit is equal to the strength of the current multiplied by the number of the magnet-pole's lines of force that are intercepted by the circuit*, taken with reversed sign.

(*d*) As in the case of the magnetic shell, so with the circuit, the value of the potential changes by $4\pi i$ from a point on one side of the circuit to a point just on the other side; that is to say, being $-2\pi i$ on one side and $+2\pi i$ on the other side, work equal to $4\pi i$ must be done in carrying a unit-pole from one side to the other round the outside of the circuit. The work done in thus threading the circuit along the path looped S times round it would be $4\pi Si$.

378. (*e*) **Mutual Potential of two Circuits.**—Two closed circuits will have a mutual potential, depending on the strengths of their respective currents, on their distance apart, and on their form and position. If their currents be respectively i and i', and if the distance between two elements ds and ds' of the circuits be called r, and ϵ the angle between the elements, it can be shown that their *mutual potential* is $= -ii' \iint \frac{\cos \epsilon}{r} ds\, ds'$. This expression represents the work that would have to be done to bring up either of the circuits from an infinite distance to its present position near the other, and is a negative quantity if they attract one another. Now, suppose the strength of current in each circuit to be unity; their mutual potential will in that case be $\iint \frac{\cos \epsilon}{r} ds\, ds'$, a quantity which depends purely upon the geometrical form and position of the circuits, and for which we may substitute the single symbol M, which we will call the "*coefficient of mutual potential*": we may now write the mutual potential of the two circuits when the currents are i and i' as $= -ii'M$.

But we have seen in the case of a single loop circuit that we may represent the potential between a circuit and a unit-pole as

the product of the strength of the current $-i$ into the number F of the magnet-pole's lines of force intercepted by the circuit. Hence the symbol M must represent the number of each other's lines of force mutually intercepted by both circuits, if each carried unit current, and if each consisted of one turn only. If the circuits have more than one turn each, then we must think of the *linkages* which each circuit makes with the lines of the other circuit; and for each circuit the linkage it makes will be equal to the product of the number of its turns into the actual number of lines that pass through those turns. If we call the two circuits A and B, then, when each carries unit current, A makes M linkages with the lines of force belonging to B, and B makes M linkages with the lines of force belonging to A.

Now suppose both currents to run in the same (clock-wise) direction; the front or S-seeking face of one circuit will be opposite to the back or N-seeking face of the other circuit, and they will attract one another, and will actually *do* work as they approach one another, or (as the negative sign shows) negative work will be done in bringing up one to the other. When they have attracted one another up as much as possible the circuits will coincide in direction and position as nearly as can ever be. Their potential energy will have run down to its lowest minimum, their mutual potential being a negative maximum, and their coefficient of mutual potential M having its greatest possible value. *Two circuits*, then, *are urged so that their coefficient of mutual potential* M *shall have the greatest possible value.* This justifies Maxwell's Rule (Art. 217), because M represents the number of mutual interlinkages of either circuit with the lines created by unit current in the other circuit. And since, when unit current is turned on or off in either circuit, the induced electromotive-force in the other is proportional to their mutual interlinkage, the coefficient M is also called *the coefficient of mutual inductance* (Art. 497, p. 503).

LESSON XXVII.—*The Electromagnetic System of Units*

379. Magnetic Units.—All magnetic quantities, strength of poles, intensity of magnetization, etc., are expressed in terms of special units derived from the fundamental units of *length*, *mass*, and *time*, explained in the *Note on Fundamental and Derived Units* (Art. 298). Most of the following units have been directly explained in the preceding Lesson, or in Lesson XI.; the others follow from them.

Unit Magnet-Pole.—The unit magnetic pole is one of such a strength, that when placed at a distance of 1 centimetre

(in air) from a similar pole of equal strength, repels it with a force of 1 dyne (Arts. 142 and 299).

Magnetic Potential.—Magnetic potential being measured by *work* done in moving a unit magnetic pole against the magnetic forces, the unit of magnetic potential will be measured by the unit of work done on unit-pole.

Unit Difference of Magnetic Potential.—Unit difference of magnetic potential exists between two points when it requires the expenditure of one *erg* of work to bring a (N-seeking) unit magnetic pole from one point to the other against the magnetic forces.

Intensity of Magnetic Field is measured by the *force* it exerts upon a unit magnetic pole : hence,

Unit Intensity of Field is that intensity of field which acts on a unit (N-seeking) pole with a force of 1 dyne. The name of *gauss* has been assigned to this unit. A field having an intensity of 6000 dynes per unit pole would be described as 6 *kilogausses.*

Magnetic Flux, or total number of magnetic lines. Its unit will be one magnetic *line*, also called one *maxwell.*

Magnetomotive-Force, or line-integral of the magnetizing forces, is proportional to the current and to the number of turns in the magnetizing coil (see Art. 368).

Magnetic Reluctance (see Art. 404) is the ratio of magnetomotive-force to magnetic flux. Unit reluctance will be such that unit magnetomotive-force applied to it generates in it a flux of one line.

380. Electromagnetic Units. — The preceding magnetic units give rise to the following set of electrical units, in which the strength of currents, etc., are expressed *in magnetic measure.* They are sometimes called "absolute C.G.S." units. The relation of this "electromagnetic" set of units to the "electrostatic" set of units of Art. 301 is explained in Art. 386.

Unit Strength of Current.—A current has unit strength when one centimetre length of its circuit bent into an arc of one centimetre radius (so as to be always one centimetre away from the magnet-pole) exerts a force of one dyne on a unit magnet-pole placed at the centre (Art. 220).

Unit of Difference of Potential (or of *Electromotive-force*).—Potential is work done on a unit of electricity ; hence unit difference of potential exists between two points when it requires the expenditure of one *erg* of work to bring a unit of + electricity from one point to the other against the electric force. Also, unit electromotive-force is generated by cutting one magnetic line per second.

Unit of Resistance. — A conductor possesses unit resistance when unit difference of potential between its ends causes a current of unit strength to flow through it.

Unit of Quantity of Electricity is that quantity which is conveyed by unit current in one second.

Unit of Capacity.—Unit capacity requires unit quantity to charge it to unit potential.

Unit of Induction.—Unit induction is such that unit electromotive-force is induced by the variation of the current at the rate of one unit of current per second.

381. Practical Units and Standards.[1]—Several of the above "absolute" units in the C.G.S. system would be inconveniently large and others inconveniently small for practical use. The following are therefore chosen as practical units :—

Resistance.—The **Ohm**, $=10^9$ absolute units of resistance (and theoretically the resistance represented by the velocity of one earth-quadrant per second, see Art. 384), but actually represented by the resistance of a uniform column of mercury 106·3 centimetres long and 14·4521 grammes in mass, at 0° C. Such a column of mercury is represented by a "standard" ohm (see Art. 385).

Current.—The **Ampere**, $=10^{-1}$ absolute units ; practically represented by the current which deposits silver at the rate of 0·001118 gramme per second (see Appendix B).

Electromotive-force.—The **Volt**, $=10^8$ absolute units, is that E.M.F. which applied to 1 ohm will produce in it a current of 1 ampere ; being $\frac{1000}{1434}$ of the E.M.F. of a Clark standard cell at 14° C.

Quantity.—The **Coulomb**, $=10^{-1}$ absolute units of quantity ; being the quantity of electricity conveyed by 1 ampere in one second.

Capacity. — The **Farad**, $=10^{-9}$ (or one one-thousand-millionth) of absolute unit of capacity ; being the capacity of a condenser such as to be changed to a potential of 1 volt by 1 coulomb. The *microfarad* or millionth part of 1 farad $=10^{-15}$ absolute units.

Work.—The **Joule**, $=10^7$ absolute units of work (ergs), is represented by energy expended per second by 1 ampere in 1 ohm.

Power.—The **Watt**, $=10^7$ absolute units of power (ergs per second), is power of a current of 1 ampere flowing

[1] The word "unit" expresses our conception in the abstract of a unit quantity, such as those defined in the preceding Articles. A "standard" is the concrete thing with which we compare quantities to be measured, such as a centimetre scale or a standard cell.

under a pressure of 1 volt. It is equal to 1 joule per second, and is approximately $\frac{1}{746}$ of one horse-power.

Inductance.—The **Henry**, $=10^9$ absolute units of inductance, is the inductance in a circuit when, while the inducing current varies at the rate of 1 ampere per second, the electromotive-force induced in this circuit is 1 volt.

Conductance.—The **Siemens**, $=10^{-9}$ absolute units of conductance, and is the reciprocal of the ohm. (Formerly called the "mho.")

Seeing, however, that quantities a million times as great as some of these, and a million times as small as some, have to be measured by electricians, the prefixes **mega-** and **micro-** are sometimes used to signify respectively "one million" and "one-millionth part." Thus a *megohm* is a resistance of one million ohms, a *microfarad* a capacity of $\frac{1}{1,000,000}$ of a farad, etc. The prefix **kilo-** is used for "one thousand," and **milli-** for "one-thousandth part"; thus a *kilowatt* is 1000 watts, and *milli-ampere* is the thousandth part of 1 ampere.

The "practical" system may be regarded as a system of units derived not from the fundamental units of *centimetre*, *gramme*, and *second*, but from a system in which, while the unit of time remains the second, the units of length and mass are respectively the earth-quadrant and 10^{-11} gramme.

382. Use of Index Notation.—Seeing that electricians have to deal with quantities requiring in some cases very large numbers, and in other cases very small numbers, to express them, a system of *index notation* is adopted, in order to obviate the use of long rows of ciphers. In this system the significant figures only of a quantity are put down, the ciphers at the end, or (in the case of a long decimal) at the beginning, being indicated by an index written above. Accordingly, we may write a thousand $(= 10 \times 10 \times 10)$ as 10^3, and the quantity 42,000 may be written 42×10^3. The British National Debt of £720,000,000 may be written £72×10^7. Fractional quantities will have negative indices when written as exponents. Thus $\frac{1}{100}$ $(= 0{\cdot}01)$ $= 1 \div 10 \div 10 = 10^{-2}$. And so the decimal 0·00028 will be written 28×10^{-5} (being $= 28 \times 0{\cdot}00001$). The convenience of this method will be seen by an example or two on electricity. The electrostatic capacity of the earth is 630,000,000 times that of a sphere of one centimetre radius, $= 63 \times 10^7$ (electrostatic) units. The resistance of selenium is about 40,000,000,000, or 4×10^{10} times as great as that of copper; that of *air* is about 10^{26}, or

100,000,000,000,000,000,000,000,000

times as great. The velocity of light is about 30,000,000,000 centimetres per second, or 3×10^{10}.

383. Dimensions of Magnetic and Electromagnetic Units.—The fundamental idea of "dimensions" is explained in Art. 302. A little consideration will enable the student to deduce for himself the following table, wherein the symbol μ relates (see Art. 390) to the magnetic permeability of the medium :—

	Units.		Dimensions.
	(Magnetic)		
m	Strength of pole / Quantity of magnetism	$= \sqrt{\text{force} \times (\text{distance})^2 \times \mu}$ =	$M^{\frac{1}{2}} L^{\frac{3}{2}} T^{-1} \mu^{\frac{1}{2}}$
V	Magnetic Potential	= work ÷ strength of pole =	$M^{\frac{1}{2}} L^{\frac{1}{2}} T^{-1} \mu^{-\frac{1}{2}}$
$\mathcal{H}$	Intensity of Field	= force ÷ strength of pole =	$M^{\frac{1}{2}} L^{-\frac{1}{2}} T^{-1} \mu^{-\frac{1}{2}}$
$\mathfrak{F}$	Magnetic Flux	= intensity × area =	$M^{\frac{1}{2}} L^{\frac{3}{2}} T^{-1} \mu^{\frac{1}{2}}$
Z	Reluctance	= mag. potential ÷ flux =	$L^{-1} \mu^{1}$
	(Electromagnetic)		
i	Current (strength)	= intensity of field × length =	$M^{\frac{1}{2}} L^{\frac{1}{2}} T^{-1} \mu^{-\frac{1}{2}}$
Q	Quantity (charge)	= current × time =	$M^{\frac{1}{2}} L^{\frac{1}{2}} \mu^{-\frac{1}{2}}$
V / E	Potential / Electromotive-force	= work ÷ quantity =	$M^{\frac{1}{2}} L^{\frac{3}{2}} T^{-2} \mu^{\frac{1}{2}}$
R	Resistance	= E.M.F. ÷ current =	$LT^{-1} \mu^{1}$
C	Capacity	= quantity ÷ potential =	$L^{-1} T^{2} \mu^{-1}$
W	Power	= current × potential =	$ML^2 T^{-3}$
L / M	Self-Inductance / Mutual Inductance	= E.M.F. ÷ current per sec. =	$L^{1} \mu^{1}$
X	Electric-force	= force ÷ quantity	$M^{\frac{1}{2}} L^{\frac{1}{2}} T^{-2} \mu^{\frac{1}{2}}$
Y	Potential gradient	= potential ÷ length =	

For *electrostatic* units, see Art. 302, p. 279.

384. Resistance expressed as a Velocity.—It will be seen, on reference to the above table of "Dimensions" of electromagnetic units, that the dimensions of resistance are given as LT^{-1}, which are the same dimensions (see Art. 302) as those of a **velocity.** Every resistance is capable of being expressed as a velocity. The following considerations may assist the student in forming a physical conception of this. Suppose we have a circuit composed of two horizontal rails (Fig. 197), CS and DT, 1 centim. apart, joined at CD, and completed by means of a sliding piece

AB. Let this variable circuit be placed in a uniform magnetic field of unit intensity, the lines of force being directed vertically downwards through the circuit. If, now, the slider be moved along towards ST with a velocity of n centimetres per second, the number of additional lines of force embraced by the circuit will increase at the rate n per second ; or, in other words, there will be an *induced* electromotive-force (Art. 243) impressed upon the circuit, which will cause a current to flow through the slider from A to B. Let the rails have no resistance, then the strength of the current will

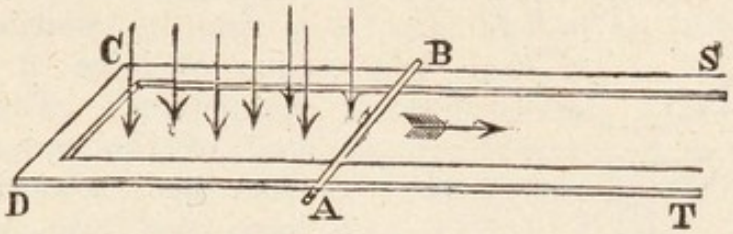


FIG. 197.—Slider cutting the Magnetic Lines of a Field.

depend on the resistance of AB. Now let AB move at such a rate that the current shall be of unit strength. If its resistance be one "absolute" (electromagnetic) unit it need only move at the rate of 1 centim. per second. If its resistance be greater it must move with a proportionately greater velocity ; the velocity at which it must move to keep up a current of unit strength being numerically equal to its resistance. *The resistance known as "one ohm" is intended to be* 10^9 *absolute electromagnetic units, and therefore is represented by a velocity of* 10^9 centimetres, or *ten million metres* (one earth-quadrant) *per second.*

385. Evaluation of the Ohm.—The system of "practical" units was originally devised by a committee of the British Association, who also determined the value of the "ohm" by experiment in 1863, and constructed standard resistance coils of German-silver, called "B.A. Units" or "ohms."

There are several ways of measuring the absolute value of the resistance of a wire. One method (Joule's) is to measure the heat produced in it by a known current and calculate its resistance by Joule's law (Art. 462). Another method (Weber's) is to measure in absolute units the current that is sent through the wire by an electromotive-force which is also measured in some absolute way. The ratio of the latter to the former gives the value of the resistance. Weber's method involved spinning a coil in a magnetic field which would generate alternating currents. Kohlrausch used an induction coil to generate the E.M.F. Lorenz proposed a method in which a disk was spun in a very uniform magnetic field. Foster used a zero method in which the E.M.F. in the spinning coil was balanced. Lord Kelvin proposed to the British Associa-

tion Committee a modification of Weber's method as follows. It being impracticable to give to a horizontal sliding-piece so high a velocity as was necessitated, the velocity which corresponded to the resistance of a wire was measured in the following way :—A ring of wire (of many turns), pivoted about a vertical axis, as in Fig. 198, was made to rotate very rapidly and uniformly. Such a ring in rotating cuts the lines of force of the earth's magnetism. The northern half of the ring, in moving from west toward east, will have (see Rule, Art. 243) an upward current induced in it, while the southern half, in crossing from east toward west, will have a downward current induced in it. Hence, the rotating ring will, as it spins, act as its own galvanometer if a small magnet be hung at its middle ; the magnetic effect due to the rotating coil being proportional directly to the horizontal component of the earth's magnetism, to the velocity of rotation, and to the number of turns of wire in the coil, and inversely proportional to the resistance of the wire of the coils. Hence, all the other data being known, the resistance can be calculated and measured *as a velocity*. The earliest *ohms* or *B.A. units* were constructed by comparison with this rotating coil ; but there being some doubt as to whether the B.A. unit really represented 10^9 centims. per second, a redetermination of the ohm was suggested in 1880 by the British Association Committee. At the first International Congress of Electricians in Paris 1881, the project for a re-

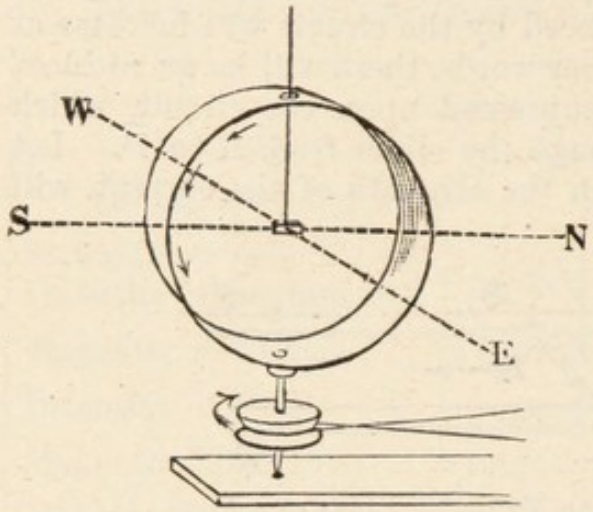


FIG. 198.—Kelvin's Method of determining Value of Resistance.

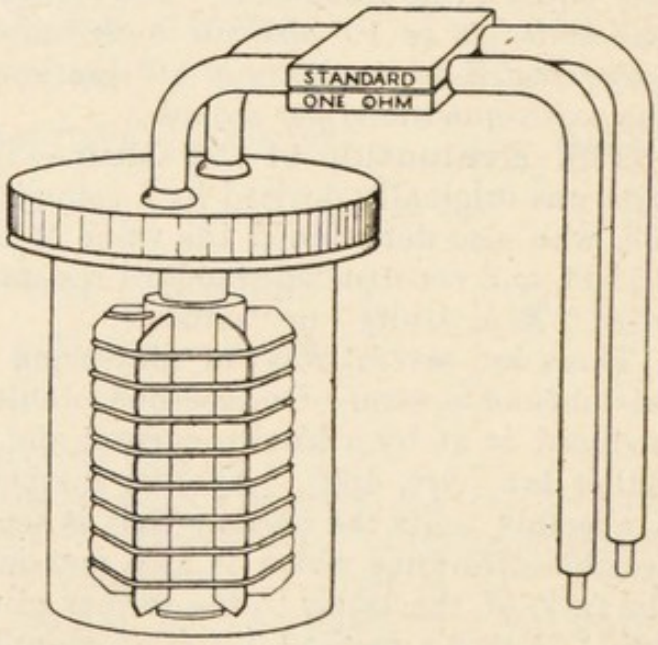


FIG. 199.—Standard One-Ohm Coil.

determination of the ohm was endorsed, and it was also agreed that the practical standards should no longer be constructed in German-silver wire, but that they should be made upon the plan originally suggested by Siemens, by defining the *practical ohm* as the resistance of a column of pure mercury of a certain length, and of one millimetre of cross-section. The original "Siemens' unit" was a column of mercury one metre in length, and one square millimetre in section, and was rather less than an ohm (0·9540 B.A. unit). Acting on measurements made by leading physicists of Europe, the Paris Congress of 1884 decided that the mercury column representing the "*legal*" ohm should be 106 centimetres in length. This was, however, never legalized in this country or in America, as it was known to be incorrect. Lord Rayleigh's determination gave 106·21 centimetres of mercury, as representing the true theoretical ohm ($=10^9$ absolute units); and Rowland's determinations at Baltimore came slightly higher. The British Association Committee in 1892 agreed to lengthen it to 106·3 centims., and to define by mass instead of section. This was decided as the *international ohm* by the Congress of Chicago in 1893 and reaffirmed by the International Conference in London in 1908. These international units are now legalized in England and the United States. The order approved by His Majesty in Council and issued through the Board of Trade is given in Appendix B. Recently F. E. Smith, of the National Physical Laboratory, using Lorenz's method perfected by Viriamu Jones and Ayrton, has found the exact value of the ohm, in terms of the length of mercury column to be 106·245 cms. The old B.A. unit is only 0·9863 of the true ohm; the Siemens' unit is only 0·9408. Fig. 199 depicts a standard one-ohm coil as sold commercially. It consists of a resistance coil (Art. 446) of suitable wire adjusted to be exactly equal to the primary standard ohm that is legal in this country.

386. Ratio of the Electrostatic to the Electromagnetic Units.—If the student will compare the Table of Dimensions of Electrostatic Units of Art. 302 with that of the Dimensions of Electromagnetic Units of Art. 383, he will observe that the dimensions (in length, mass, and time), assigned to similar units are different in the two systems. Thus, the dimensions of "Quantity" in *electrostatic* measure are $M^{\frac{1}{2}} L^{\frac{3}{2}} T^{-1}$, and in *electromagnetic* measure they are $M^{\frac{1}{2}} L^{\frac{1}{2}}$. Dividing the former by the latter we get LT^{-1}, a quantity which we at once see is of the nature of *a velocity*. This velocity occurs in every case in the ratio of the electrostatic to the electromagnetic measure of every unit. It is a definite concrete velocity, and represents that velocity at which two electrified particles must travel along side by side in order that

their mutual electromagnetic attraction (considered as equivalent in so moving (Art. 429) to two parallel currents) shall just equal their mutual electrostatic repulsion (see Art. 277). This velocity, "v," which is of enormous importance in the *electromagnetic theory of light* (Art. 609), has been measured in several ways.

Unit.	Electrostatic.	Electromagnetic.	Ratio.
Quantity.	$M^{\frac{1}{2}}\ L^{\frac{3}{2}}\ T^{-1}\ k^{\frac{1}{2}}$	$M^{\frac{1}{2}}\ L^{\frac{1}{2}}\ \mu^{-\frac{1}{2}}$	$LT^{-1}\ k^{\frac{1}{2}}\ \mu^{\frac{1}{2}} = v$
Potential.	$M^{\frac{1}{2}}\ L^{\frac{1}{2}}\ T^{-1}\ k^{-\frac{1}{2}}$	$M^{\frac{1}{2}}\ L^{\frac{3}{2}}\ T^{-2}\ \mu^{\frac{1}{2}}$	$L^{-1}T\ k^{-\frac{1}{2}}\ \mu^{-\frac{1}{2}} = 1/v$
Capacity.	$L\ k^{1}$	$L^{-1}T^{2}\ \mu^{-1}$	$L^{2}T^{-2}\ k^{1}\ \mu^{1} = v^{2}$
Resistance	$L^{-1}T\ k^{-1}$	$L\ T^{-1}\ \mu^{1}$	$L^{-2}T^{2}k^{-1}\mu^{-1} = 1/v^{2}$

(*a*) Weber and Kohlrausch measured the electrostatic unit of quantity and compared it with the electromagnetic unit of quantity, and found the ratio v to be $= 3{\cdot}1074 \times 10^{10}$ centims. per second.

(*b*) Lord Kelvin compared the two units of potential and found

$$\text{v} = 2{\cdot}825 \times 10^{10},$$

and later, $= 2{\cdot}93 \times 10^{10}$.

(*c*) Professor Clerk Maxwell balanced a force of electrostatic attraction against one of electromagnetic repulsion, and found

$$\text{v} = 2{\cdot}88 \times 10^{10}.$$

(*d*) Professors Ayrton and Perry measured the capacity of a condenser electromagnetically by discharging it into a ballistic galvanometer, and electrostatically by calculations from its size, and found

$$\text{v} = 2{\cdot}980 \times 10^{10}.$$

The mean value, according to the most recent researches, is :—

$$\text{v} = 2{\cdot}999 \times 10^{10}.$$

The velocity of light according to latest values is—

$$= 2{\cdot}9986 \times 10^{10};$$

so we take v as 3×10^{10}, or *thirty thousand million centimetres per second.*

387. Rationalization of Dimensions of Units.—It seems absurd that there should be two different units of electricity ; still more absurd that one unit should be thirty thousand million centimetres per second greater than the other. It also seems absurd

that the dimensions of a unit of electricity should have fractional powers, since such quantities as $M^{\frac{1}{2}}$ and $L^{\frac{3}{2}}$ are meaningless. These irrational things arise from the neglect to take account of the properties of the medium in applying the law of inverse squares to form definitions of the unit of electricity in the electrostatic system, and of the unit-pole in the magnetic system. If we insert (Art. 302) the inductivity k in the former, and the permeability μ in the latter, we might, if we knew the dimensions of these quantities, be able to rationalize the dimensional formulæ. But we do not know their dimensions. Rücker has, however, shown that they can be rationalized, and the two sets of units brought into agreement,[1] by assuming that the product $k\mu$ has the dimensions of the reciprocal of the square of a velocity: or $v = 1/\sqrt{k\mu}$. If k were the reciprocal of the rigidity of the ether, and μ its density, v would represent the velocity of propagation of waves in it. Compare Art. 609 on the electromagnetic theory of light.

388. Earth's Magnetic Force in Absolute Units.—In making absolute determinations of current by the tangent galvanometer, or of electromotive-force by the spinning coil, it is needful to know the absolute value of the earth's magnetic field, or of its horizontal component. The intensity of the earth's magnetic force at any place is the force with which a magnet-pole of unit strength is attracted. As explained in Art. 159, it is usual to measure the horizontal component H of this force, and from this and the cosine of the angle of dip to calculate the total force, as the direct determination of the latter is surrounded with difficulties. To determine H in *absolute* or (C.G.S.) *units*, it is necessary to make two observations with a magnet of magnetic moment M (Art. 137). In one of these observations the product MH is determined by a *method of oscillations* (Art. 135); in the second the quotient M/H is determined by a particular *method of deflexion* (Art. 140). The square root of the quantity obtained by dividing the former by the latter will, of course, give H.

(i.) *Determination of* MH.—The time T of a complete oscillation to and fro of a magnetic bar is

$$T = 2\pi \sqrt{\frac{K}{MH}}, \text{ and } n = \frac{1}{2\pi} \sqrt{\frac{K}{MH}};$$

where K is the "moment of inertia" of the magnet, and n is the frequency of vibration. This formula is, however, only true for very small arcs of vibration. By simple algebra it follows that

$$MH = m\pi^2 K \div T^2.$$

Of these quantities T is ascertained by a direct observation of

[1] See Everett's *Units and Physical Constants*, 4th edition (1893), p. 208.

the time of oscillation of the magnet hung by a torsionless fibre ; and K can be either determined experimentally or by one of the following formulæ :—

For a round bar $$K = w\left(\frac{l^2}{12} + \frac{a^2}{4}\right),$$

For a rectangular bar $$K = w\left(\frac{l^2 + b^2}{12}\right);$$

where w is the mass of the bar in grammes, l its length, a its radius (if round), b its breadth, measured horizontally (if rectangular).

(ii.) *Determination of* M/H.—The magnet is next caused to deflect a small magnetic needle in the following manner, "broadside on." The magnet is laid horizontally at right angles to the magnetic meridian, and so that its middle point is (magnetically) due south or due north of the small needle, and at a distance r from its centre. Lying thus broadside to the small needle its N-pole will repel, and its S-pole attract, the N-pole of the needle, and will exercise contrary actions on the S-pole of the needle. The total action of the magnet upon the needle will be to deflect the latter through an angle δ, whose tangent is directly proportional to M/H, and inversely proportional to the *cube* of the distance r; or

$$M/H = r^3 \tan \delta.$$

Dividing the former equation by this, and taking the square root, we get

$$H = \frac{2\pi}{T}\sqrt{\frac{K}{r^3 \tan \delta}}.$$

LESSON XXVIII.—*Properties of Iron and Steel*

389. Magnetization of Iron.—When a piece of magnetizable metal is placed in a magnetic field, some of the lines of magnetic force run through it and magnetize it. The intensity of its magnetization will depend upon the intensity of the field into which it is put and upon the metal itself. There are two ways of looking at the matter, each of which has its advantages. We may think about the internal condition of the piece of metal, and of the number of magnetic lines that are running through it and emerging from it into the surrounding space. This is the modern way. Or we may think of the magnetism

of the iron or other metal as something resident on the polar surfaces, and expressed therefore in units of magnetism. This is the old way. The fact that soft iron placed in the magnetic field becomes highly magnetic may then be expressed in the following two ways: (1) when iron is placed in the magnetic field, the magnetic lines run in greater quantities through the space now occupied by iron, for iron is very *permeable* to the lines of magnetic induction, being a good conductor of the magnetic lines; (2) iron when placed in the magnetic field develops strong poles on its end-surfaces, being highly *susceptible* to magnetization. Each of these ideas may be rendered exact by the introduction of appropriate coefficients.

390. Permeability.—Suppose a magnetic force—due, let us say, to the circulation of an electric current in a surrounding coil—were to act on a space occupied by air, there would result a certain number of magnetic lines in that space. In fact, the intensity of the magnetic force, symbolized by the letter $\mathcal{H}$, is often expressed by saying that it would produce $\mathcal{H}$ magnetic lines per square centimetre in air. Now, owing to the superior magnetic properties of iron, if the space subjected to this magnetic force were filled with iron instead of air, there would be produced a larger number of magnetic lines per square centimetre. This larger number expresses the degree of magnetization [1] or *density of the magnetic flux* in the iron; it is symbolized by the letter $\mathcal{B}$. The ratio of $\mathcal{B}$ to $\mathcal{H}$ expresses the *permeability* of the material. The usual symbol for the permeability is the Greek letter μ. So we may say that the flux-density $\mathcal{B}$ is equal to μ times the magnetic force $\mathcal{H}$, or

$$\mu = \mathcal{B}/\mathcal{H}.$$

[1] *Flux-density*, the number of magnetic lines that run through unit area of cross-section in the iron or other material—also denoted by the symbol $\mathcal{B}$—is called by several names—"the permeation," "the internal magnetization," or "the induction." The last name, unfortunately used by Maxwell and Hopkinson, is to be avoided, since "induction" was introduced by Faraday to denote the *operation* of inducing electromotive force.

Example.—A certain specimen of iron, when subjected to a magnetic force capable of creating, in air, 50 magnetic lines to the square centimetre, was found to be permeated by no fewer than 16,062 magnetic lines per square centimetre. Dividing the latter figure by the former gives as the value of the permeability at this stage of the magnetization 321, or the permeability of the iron is 321 times that of air.

The permeability is always positive: for empty space it is 1, for air and all non-magnetic substances as cotton, silk, and other insulators and of copper, brass, and the non-magnetic metals, it is practically 1. In all these therefore $\mathfrak{B} = \mathcal{H}$. For magnetic metals, iron, cobalt, and nickel, the permeability is greater than 1. For diamagnetic materials (Art. 399) it is slightly less than 1.

Where the magnetic lines emerge into the air at a polar surface they are of course continuous with the internal lines: the value of $\mathfrak{B}$ just inside the polar surface is the same as that of $\mathfrak{B}$ in the air just outside it.

This mode of expressing the facts is, however, complicated by the fact of the tendency to magnetic saturation in all kinds of iron. In all kinds of iron the magnetizability of the material becomes diminished as the actual magnetization is pushed further. In other words, when a piece of iron has been magnetized up to a certain degree, it becomes, from that degree onward, less permeable to further magnetization, and though actual saturation is never reached, there is a practical limit beyond which it cannot well be pushed. Joule discovered this tendency to a limit. The practical limit of $\mathfrak{B}$ in good wrought iron is about 20,000 lines per square centimetre, or in cast iron about 12,000. Using extraordinary magnetizing forces, Ewing has found it possible to increase $\mathfrak{B}$ to 45,000, and Du Bois has reached 60,000 lines per square centimetre.

391. Curves of Magnetization.—A convenient mode of studying the magnetic facts respecting any particular brand of iron is to plot on a diagram the curve

of magnetization—*i.e.* the curve in which the values, plotted horizontally, represent the magnetic force $\mathcal{H}$, and the values plotted vertically those that correspond to the respective magnetization $\mathcal{B}$. In Fig. 200, which is modified from the researches of Ewing, are given five curves relating to soft iron, hardened iron, annealed steel, hard-drawn steel, and glass-hard steel. It will be noticed that all these curves have the same general form, and that there are three stages. (1) For small values of $\mathcal{H}$ the values of $\mathcal{B}$ are small, and as $\mathcal{H}$ is increased $\mathcal{B}$ increases gradually. (2) The curve rises very suddenly, at least with all the softer sorts of iron. (3) The curve

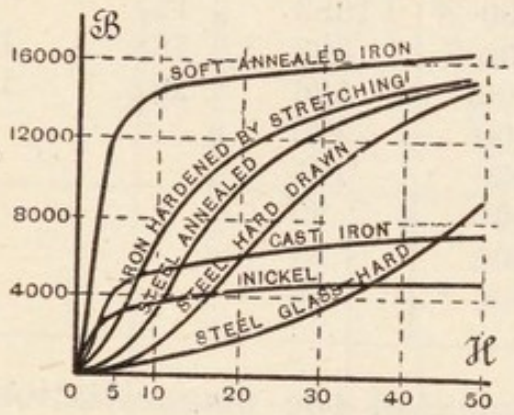


FIG. 200.—Ewing's Curves of Magnetization.

then bends over and becomes nearly horizontal, $\mathcal{B}$ increasing very slowly. The three stages observed in the magnetization are explained in Ewing's molecular theory (Art. 129). When the magnetization is in the stage below the bend of the curve, the iron is said to be far from the state of saturation. But when the magnetization has been pushed beyond the bend of the curve into the third stage, the iron is said to be approaching saturation, because at this stage of magnetization it requires a large increase in the magnetizing force to produce even a very small increase in the magnetization. It will be noted that for soft wrought iron the stage of approaching saturation sets in when $\mathcal{B}$ has attained the value of about 16,000, or when $\mathcal{H}$ has been raised to about 50. The student is

strongly advised to plot for himself similar curves from the subjoined table, which relates to the permeabilities of some samples of iron examined by Hopkinson.

Annealed Wrought Iron.			Grey Cast Iron.		
$\mathfrak{H}$	$\mathfrak{B}$	μ	$\mathfrak{H}$	$\mathfrak{B}$	μ
1·66	5,000	3000	5	4,000	800
4	9,000	2250	10	5,000	500
5	10,000	2000	21·5	6,000	279
6·5	11,000	1692	42	7,000	133
8·5	12,000	1412	80	8,000	100
12	13,000	1083	127	9,000	71
17	14,000	823	188	10,000	53
28·5	15,000	526	292	11,000	37
50	16,000	320			
105	17,000	161			
200	18,000	90			
350	19,000	54			
666	20,000	30			

At early stages of the magnetization, in moderately weak fields where $\mathfrak{H}$ is less than about 5, the permeability reaches 3000 or 4000. But for values of $\mathfrak{H}$ less than about 0·04 the permeability of iron is quite small, usually from 100 to 120. Iron reheated in vacuo may reach a permeability of 10,000 or 12,000.

An alloy of iron with 3·4 per cent of silicon, known as *stalloy*, invented by Hadfield, has a permeability nearly as high as wrought iron, and has low hysteresis with high electrical resistance, being therefore excellent for laminated cores.

In Fig. 201, and in the Table on p. 376, some additional data are given; but here the values of the magnetizing force are stated not in terms of the intensity of field, $\mathfrak{H}$, but in terms of the magnetizing ampere-turns per centimetre length of the substance; this being more convenient for the calculations.

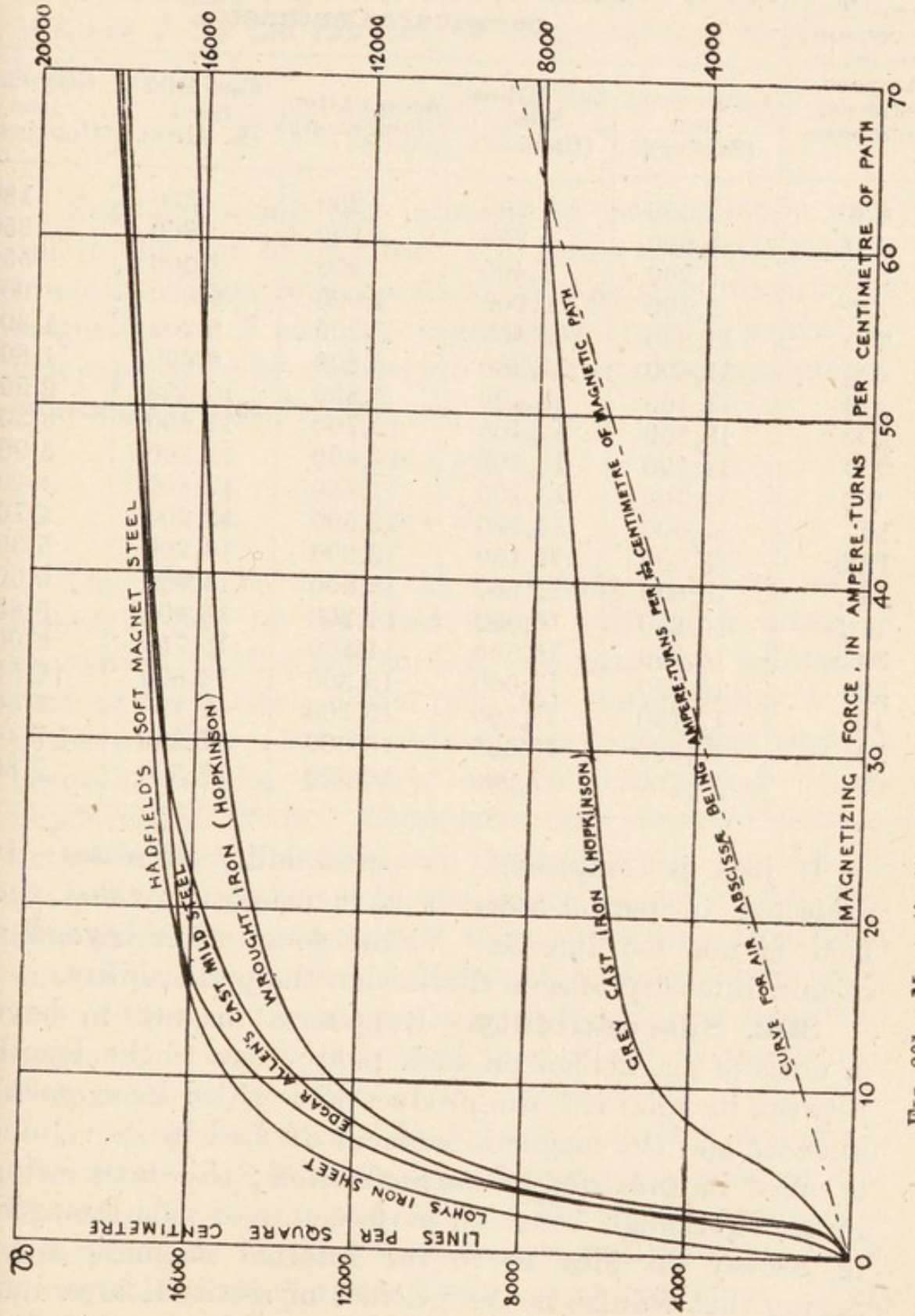


FIG. 201.—Magnetization Curves of some Commercial kinds of Iron and Steel.

Magnetizing Force, expressed in Ampere-turns per centimetre.	Values of Flux-density, $\mathfrak{B}$, in lines per square Centimetre.				
	Lohys Sheet Iron (Sankey).	Soft Magnet Steel (Hadfield).	Wrought Iron (Hopkinson).	Cast Mild Steel (E. Allen).	Grey Cast Iron (Hopkinson).
0·5	2,600	200	200	350	180
1·0	4,600	300	300	800	250
2·0	7,200	1,400	900	3,000	550
3·0	9,700	6,000	4,000	6,000	900
4·0	11,200	8,600	7,100	8,200	1,300
5·0	12,400	10,200	8,800	9,600	1,800
6·0	13,100	11,400	9,850	10,600	2,500
7·0	13,800	12,400	10,700	11,400	3,300
8·0	14,100	13,100	11,400	12,200	3,900
9·0	14,700	13,700	11,950	12,800	4,400
10	15,000	14,300	12,500	13,300	4,700
12·5	15,600	15,150	13,300	14,200	5,300
15	16,000	15,800	13,850	14,900	5,600
17·5	16,250	16,050	14,200	15,400	5,850
20	16,350	16,500	14,500	15,750	6,000
30	16,750	17,000	15,300	16,800	6,550
40	17,150	17,300	15,700	17,150	7,000
50	17,500	17,600	16,000	17,550	7,400
60	17,700	17,900	16,200	17,900	7,800

If iron is compressed its permeability decreases; if subjected to tensile stress it is increased, provided the field is not too intense. Villari found that beyond a certain intensity tension diminishes the permeability.

392. Susceptibility.—Suppose a magnet to have m units of magnetism on each pole; then if the length between its poles is l, the product ml is called its *magnetic moment*, and the magnetic moment divided by its volume is called its *intensity of magnetization*; this term being intended, though based on surface-unit of pole strength, to convey an idea as to the internal magnetic state. Seeing that volume is the product of sectional area into length, it follows that if any piece of iron or steel of uniform section had its surface magnetism situated on its

ends only, its intensity of magnetization would be equal to the strength of pole divided by the area of end surface. Writing $\mathfrak{I}$ for the intensity of magnetization we should have

$$\mathfrak{I} = \frac{\text{mag. moment}}{\text{volume}} = \frac{m \times l}{s \times l} = \frac{m}{s}.$$

Now, supposing this intensity of magnetization were due to the iron having been put into a magnetic field of intensity $\mathcal{H}$, the ratio between the resulting intensity of magnetization $\mathfrak{I}$ and the magnetizing force $\mathcal{H}$ producing it is expressible by a numerical coefficient of magnetization, or *susceptibility*, k. We may write

$$\mathfrak{I} = k\mathcal{H},$$

or

$$k = \mathfrak{I}/\mathcal{H}.$$

This may be looked at as saying that for every magnetic line in the field there will be k units of magnetism on the end surface. In magnetic substances such as iron, steel, nickel, etc., the susceptibility k has positive values; but there are many substances such as bismuth, copper, mercury, etc., which possess feeble negative coefficients. These latter are termed "diamagnetic" bodies (Art. 398) and are apparently repelled by the poles of magnets. It was shown at end of Art. 365 that there are 4π magnetic lines proceeding from each unit of pole magnetism. Hence if, as shown above, each line of force of the magnetizing field produces k units of magnetism there will be $4\pi k$ lines added by the iron to each 1 line in the field, or the permeability of the iron μ is equal to $1 + \pi k$. It follows that $\mathcal{B} = \mathcal{H} + 4\pi k\mathcal{H}$. This shows that $\mathcal{B}$ may go on increasing as long as $\mathcal{H}$ is increased, having no true limit. But since k decreases as saturation sets in, the intrinsic magnetization $\mathfrak{I}$ (or $\mathcal{B} - \mathcal{H}$ to which it is proportional) may have a true limit. This maximum of $\mathfrak{I}$ appears to be about 1700 in wrought iron, 1250 in cast iron, and 450 in nickel.

In the following table are given some figures from the researches of Bidwell on wrought iron.

$\mathcal{H}$	k	$\mathfrak{I}$	μ	$\mathfrak{B}$
3·9	151·0	587	1899·1	7390
10·3	89·1	918	1121·4	11550
40	30·7	1226	386·4	15460
115	11·9	1370	150·7	17330
208	7·0	1452	88·8	18470
427	3·5	1504	45·3	19330
585	2·6	1530	33·9	19820

In weak magnetic fields the susceptibility of nickel exceeds by about five times that of iron; but in strong fields iron is more susceptible.

393. Measurement of Permeability.—There are several ways of measuring the permeability of iron: they all involve a measurement of $\mathfrak{B}$.

(*a*) *Magnetometer Methods.*—The pole strength m of long bars, when magnetized by a coil around them, can be measured by a magnetometer (Art. 140), and from this $\mathfrak{F}$ is found by multiplying by 4π; and dividing by the sectional area of the bar gives $\mathfrak{B}$.

(*b*) *Induction Methods.*—Rings of iron which, having no poles, cannot be measured by the magnetometer are measured inductively. Upon the ring is wound a magnetizing coil, and also an exploring coil (Art. 249) which is connected to a ballistic galvanometer. On turning on or off the magnetizing current, or reversing it, induced currents are generated, giving a throw in the galvanometer proportional to the number of magnetic lines which have been made or destroyed. $\mathcal{H}$ is calculated from the ampere-turns of the magnetizing coil (Art. 368), and $\mathfrak{B}$ from the galvanometer throw. Iron rods can be examined by the same means.

(*c*) *Traction Methods.*—The pull needed to separate the two halves of a divided rod, or divided ring, is (Art 415) proportional to the *square* of $\mathfrak{B}$.

(*d*) *Optical Methods.*—Du Bois has used a method based on Kerr's discovery (Art. 614) of magneto-opti-rotation.

394. Residual Effects.—The retention of magnetism by steel, lodestone, hard iron, and even by soft iron if of elongated shape, has been already described (Art. 101). Some other residual effects must now be noted. It is found that if a new piece of iron or steel is subjected to an increasing magnetizing force, and then the magnetizing force is decreased to zero, some magnetism remains. If the results are plotted out in a curve it exhibits the following peculiarities. On first gradually increasing $\mathcal{H}$ from *o*, $\mathcal{B}$ rises as we have seen in Art. 391. If when the curve has risen to *a* (Fig. 202) $\mathcal{H}$ is now decreased, the descending curve does not follow the ascending curve, owing to the retention of the magnetism. When $\mathcal{H}$ has been reduced to zero the point *b* is reached. This the residual value of $\mathcal{B}$ is called the *remanence*, and depends on the material, and on the degree to which $\mathcal{B}$ was previously pushed. The remanence, after subjection to a very strong field, may be as high as 10,000 in a ring of wrought iron or steel. In cast iron it seldom reaches 3000. If now a reversed magnetizing force $-\mathcal{H}$ is applied it is found that it must be increased to a definite degree in order to demagnetize the iron and bring the curve down to *c*. The amount of reversed magnetic force so needed is a measure of the *retentivity* of the material, and is known as the *coercive force*. In hard steel it may amount to 80; in soft steel to 20; in soft iron to 2 or less. If the reversed magnetizing force is further increased, the curve descends from *c* to *d*, the iron becoming magnetized with

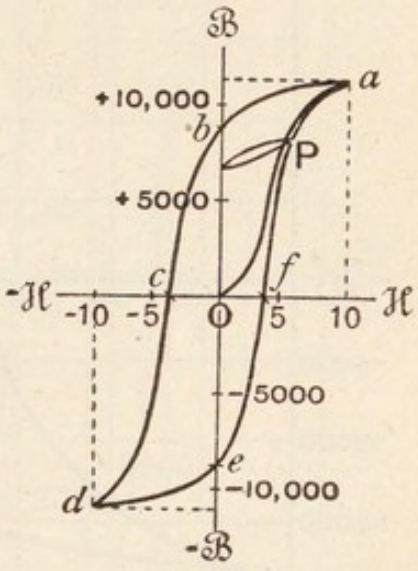


FIG. 202.—Cycle of Magnetization.

reversed polarity, and going toward saturation. On then diminishing the reversed force to zero, the curve turns to e, showing a negative remanence. On again increasing $\mathcal{H}$ as at first the curve ascends to f, and as the former value of $\mathcal{H}$ is reached comes up to a again.

395. Cycles of Magnetization. Hysteresis.— When $\mathcal{H}$ is thus carried through a cycle of increase and decrease, $\mathcal{B}$ also goes through a cycle ; and as we have

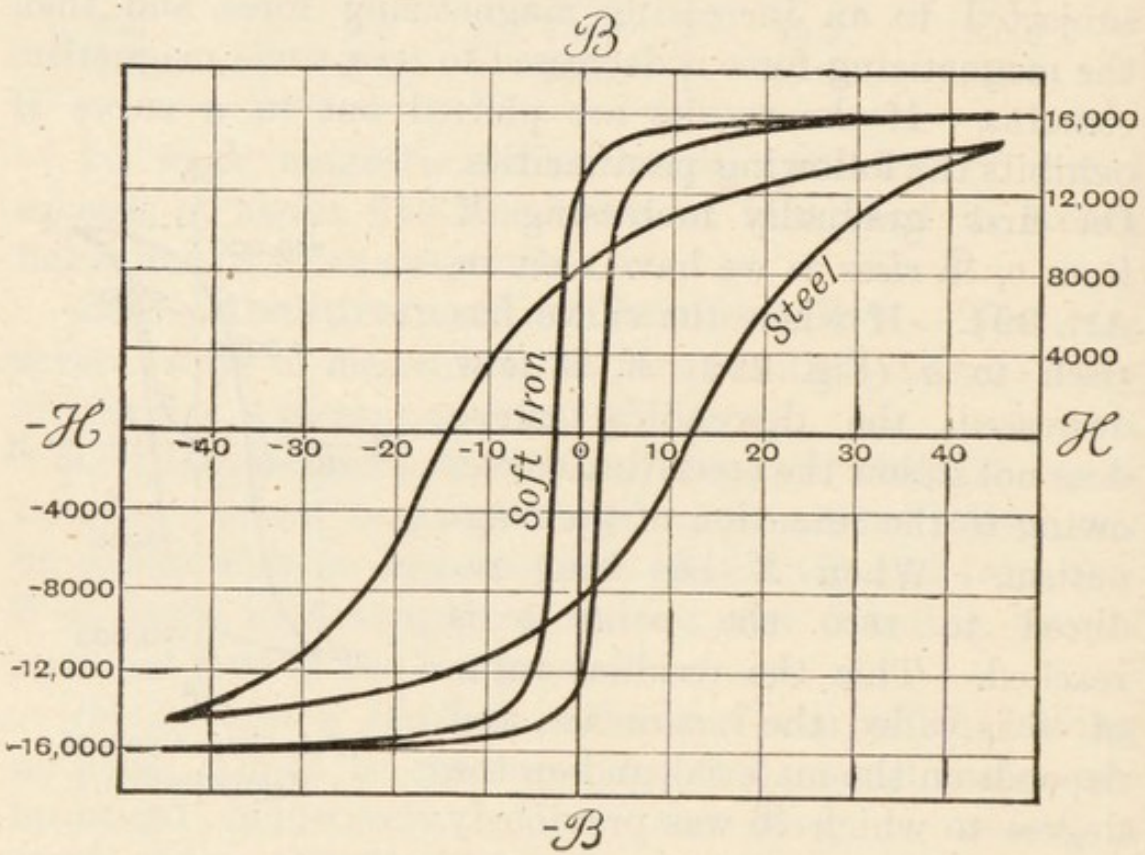


FIG. 203.—Hysteresis Loops for soft Iron and Steel

seen there is a *lagging* in the magnetization, evidenced in Fig. 202 by the formation of a closed *loop*, $a\,b\,c\,d\,e\,f\,a$, in the curve. Warburg and Ewing, who have fully investigated the phenomenon, have remarked that the area enclosed indicates energy of waste in the cycle of operations; this energy, seemingly caused by molecular friction, appearing as heat. In hard steel the areas of these loops are much wider than in the case of soft iron. In Fig. 203 are given the loops for nearly pure iron and a soft kind of steel. Ewing has given

the name of **Hysteresis** to the subject of the lag of magnetic effects behind their causes. From his researches[1] also is taken the case of Fig. 204, a specimen of soft iron, the curve for which shows various partial loops due to the removal and replacement of the magnetizing force. Ewing has devised a *curve-tracer* for describing the curves automatically. The waste of energy per cubic centimetre in a cycle of strong magnetization may vary from 9000 ergs in annealed iron to 200,000 in glass-hard steel. If (as in the iron cores of alternate current transformers) the cycle is repeated 50 times a second, the waste of power by hysteresis will heat the iron. The waste increases greatly with the frequency, and with the degree to which the magnetization is pushed. If $\mathfrak{B}$ does not exceed 5000, the power wasted at 50 cycles per second in every cubic foot of iron may be as low as 130 watts, but if $\mathfrak{B}$ is increased to 10,000 the waste becomes 360 watts. In different kinds of iron, the power loss caused by hysteresis varies in a proportion varying from $\mathfrak{B}^{1.5}$ to $\mathfrak{B}^2$.

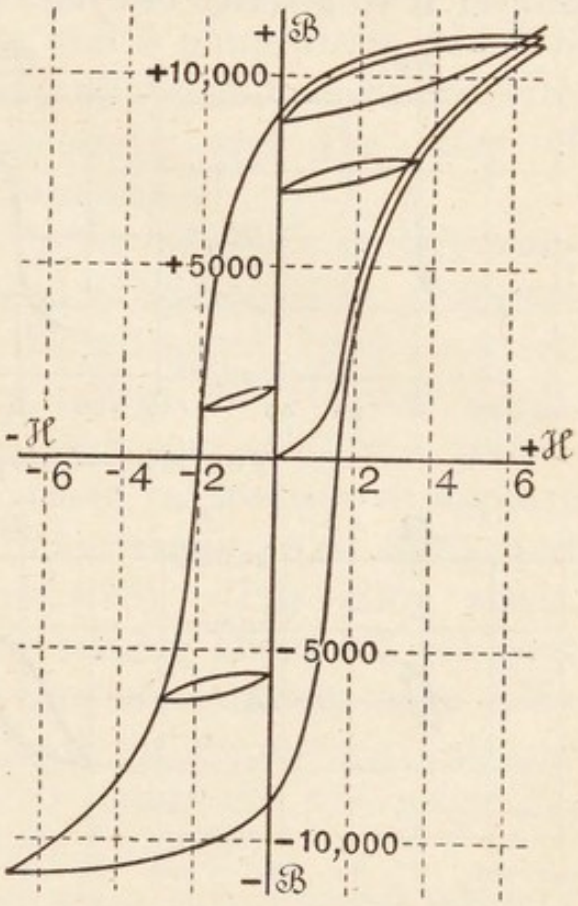


FIG 204.—Hysteresis Loops.

Fig. 205*a* shows the form of the hysteresis curves for very soft iron when subjected to cycles of magnetization in which the maxima of the magnetizing field, $\mathfrak{H}$, are respectively 5, 20, and 40. In fields the intensity of

[1] The student should not fail to consult Ewing's book, *Magnetic Induction in Iron.*

which does not exceed $\mathcal{H} = 5$, the loop is practically a straight line, there being no hysteresis waste. Fig. 205*b* gives for comparison three curves of steel under similar conditions.

Since a reversed force, smaller than was required to produce it, suffices to destroy magnetization, all that is necessary in order completely to demagnetize iron is to subject it to a series of cycles of diminishing intensity.

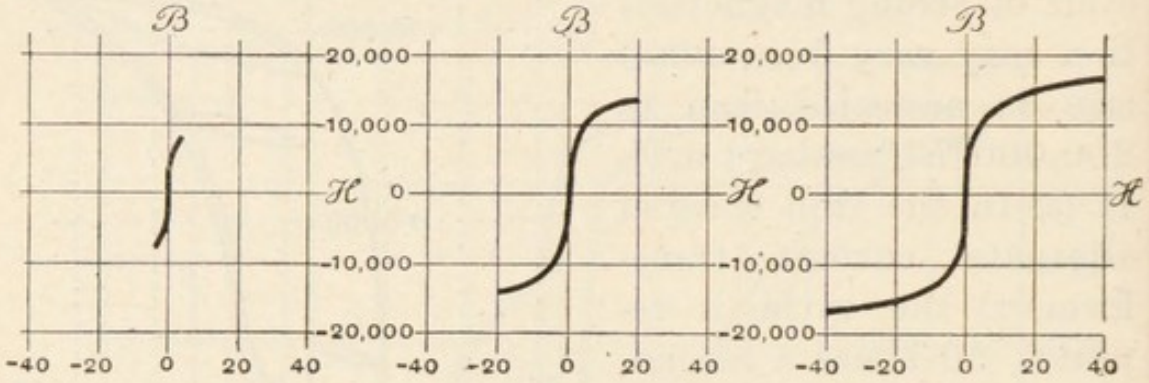


FIG. 205*a*.—Curves for Soft Iron.

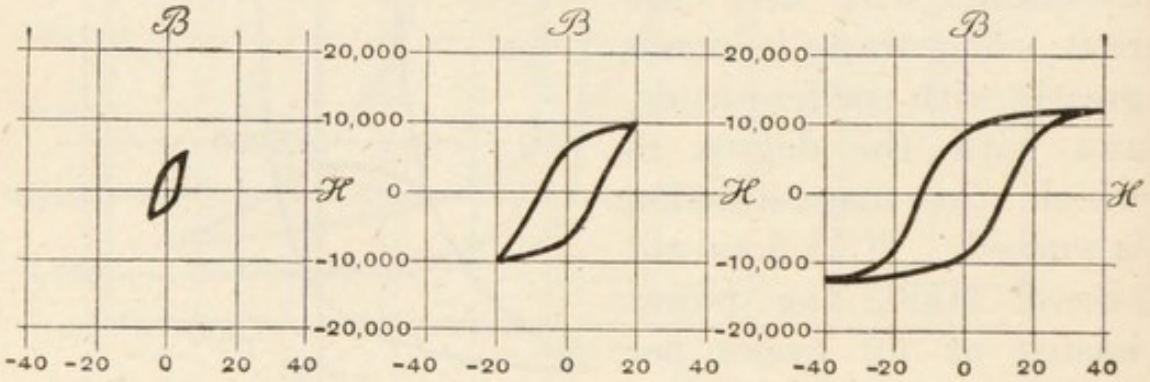


FIG. 205*b*.—Curves for Steel.

Mechanical agitation tends to help the magnetizing forces to act, and lessens all residual and hysteresial effects.

Ewing has also shown that under constant magnetizing force the magnetism will go on slowly and slightly increasing for a long time : this is called magnetic *creeping*, or *viscous hysteresis*.

396. Results of Tests; Ferromagnetic Substances. — The substances which resemble iron in magnetic properties may be classified thus :—

Ferromagnetic Elements: iron; cobalt; nickel.

Ferromagnetic Compounds: magnetite (Fe_3O_4); magnetic pyrites (Fe_7S_8); ferric antimonide (Fe_2Sb_3).

Ferromagnetic Alloys: Cast iron; the carbon steels; certain alloy steels, containing various percentages of carbon with one of the following, tungsten, chromium, molybdenum, vanadium; ferronickel; ferro-chrome. Also Heusler's alloys, such as the alloy containing 74 per cent of copper, 17 manganese, and 9 aluminium, which is as magnetizable as cast iron; alloys of manganese with arsenic, phosphorus, or antimony; and the alloy of bismuth with $\frac{1}{4}$ per cent of manganese.

Ferromagnetic Minerals: A few minerals, such as iron-sand, low-grade iron ores, and tungsten ores. Asbestos is sufficiently magnetic to be attracted by a magnet. All ferromagnetic substances, except the Heusler alloys, are characterized by having a high permeability, a transition temperature at which their magnetism disappears (Art. 114), the property of hysteresis (Art. 395), and optical rotatory power (Art. 613). The alloy steels, particularly tungsten steel containing about 0·5 per cent of carbon and 5 to 6 per cent of tungsten, have very great coercive force and are used for permanent magnets (Art. 103). Manganese steel is practically non-magnetic, having a permeability of 1·2 to 1·5 only.

397. Magnetic Separators.—Advantage is taken of the differing magnetic susceptibilities of different mineral constituents to separate them by use of the magnet, the more susceptible being more strongly attracted. Machines called *magnetic separators* are used in which powdered ore is caused to fall or pass near the poles of electromagnets or permanent magnets, which deflect the more magnetizable constituents. In this way low-grade iron ores can be concentrated; ferruginous sands sorted; the iron impurities extracted from the white sand used for glass-making or from the clay used for porcelain; iron filings can be sorted from brass filings.

LESSON XXIX.—*Diamagnetism*

398. Diamagnetic Experiments. — In 1778 Brugmans of Leyden observed that when a lump of bismuth was held near either pole of a magnet needle it repelled it. In 1827 Le Baillif and Becquerel observed that the metal antimony also could repel and be repelled by the pole of a magnet. In 1845 Faraday, using powerful electromagnets, examined the magnetic properties of a large number of substances, and found that whilst a great many are, like iron, attracted to a magnet, others are feebly repelled. To distinguish between these two classes of bodies, he termed those which are attracted **paramagnetic**, and those which are repelled **diamagnetic**. The property of being thus apparently repelled from a magnet he termed **diamagnetism**.

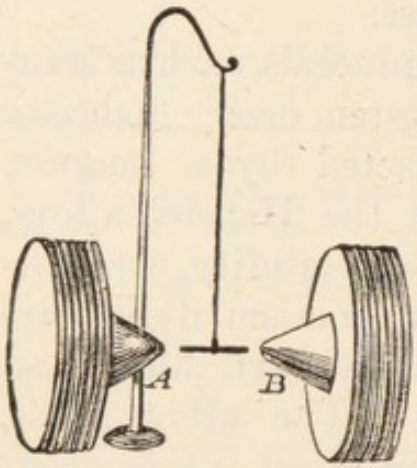


FIG. 206. — Axial Position assumed by a Paramagnetic Bar.

Faraday's method of experiment consisted in suspending a small bar of the substance in a powerful magnetic field between the two poles of an electromagnet, and observing whether the small bar was attracted into an **axial** position, as in Fig. 206, with its length along the line joining the two poles, or whether it was repelled into an **equatorial** position, at right angles to the line joining the poles, across the lines of force of the field, as is shown by the position of the small bar in Fig. 207, suspended between the poles of an electromagnet constructed on Ruhmkorff's pattern.

Liquids were placed in glass vessels and suspended between the poles of the electromagnet. Almost all liquids are diamagnetic, except solutions of salts of the magnetic metals, some of which are feebly magnetic; but

blood is diamagnetic though it contains iron. To examine gases, bubbles were blown with them, and watched as to whether they were drawn into or pushed out of the field. Oxygen gas was found to be magnetic; ozone has been found to be still more strongly so. Dewar found liquid oxygen sufficiently magnetic to rush in drops to the poles of a powerful magnet.

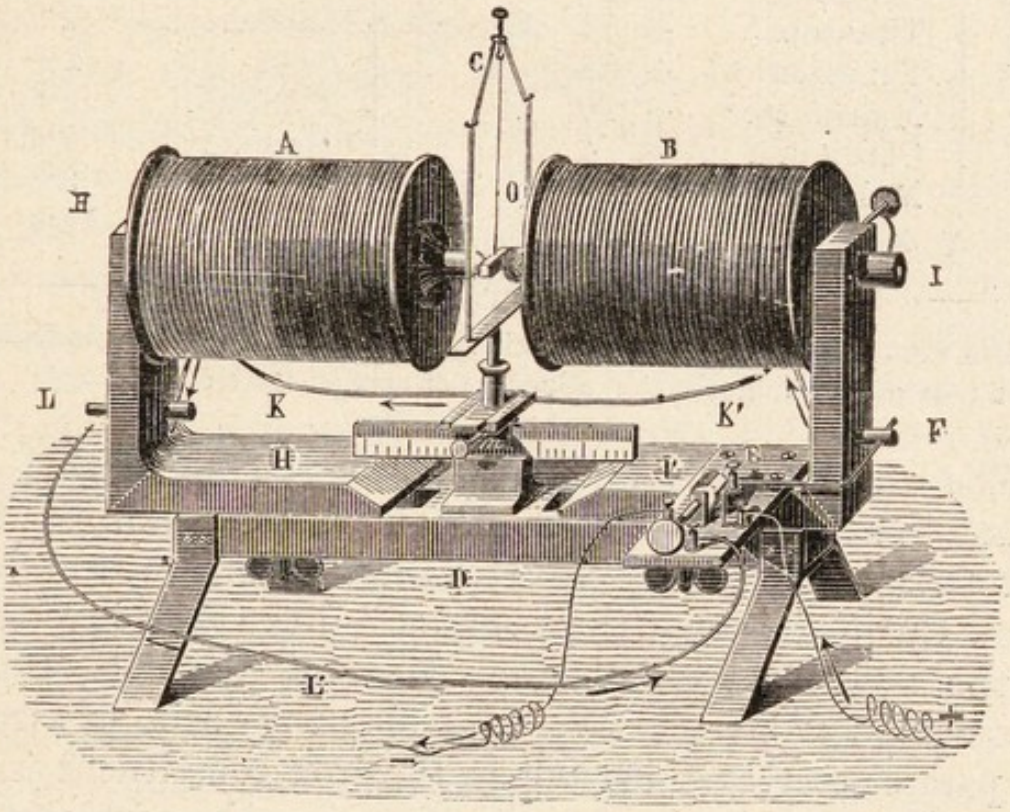


FIG. 207.—Equatorial Position assumed by a Diamagnetic Bar.

399. Paramagnetic and Diamagnetic Data.—In these two classes of feebly magnetic bodies the permeability, μ, scarcely differs from that of air. In the most paramagnetic, the rare metal erbium, $\mu = 1{\cdot}00289$; in the most diamagnetic, bismuth, $\mu = 0{\cdot}999824$. It is more convenient to state their properties in terms of the susceptibility k (Art. 392), which for air is zero, and is negative for the diamagnetic bodies. The following table gives a list of elements, the numbers given being the values of $k \times 10^6$.

Paramagnetic.	Erbium	+231	Diamagnetic.	Tin, Silicon, Potassium, Sodium, Calcium, and Barium are almost neutral.	
	Cerium	+182		Phosphorus	− 0·4
	Didymium	+121		Copper	− 0·66
	Lanthanum	+112		Zinc	− 0·8
	Thorium	+ 81		Lead	− 1·36
	Palladium	+ 58		Silver	− 1·6
	Tantalum	+ 58		Carbon	− 2·5
	Platinum	+ 29		Gold	− 2·8
	Uranium	+ 16		Thallium	− 4·6
	Titanium	+ 14		Mercury	− 2·6
	Tungsten	+ 12		Antimony	− 3·8
	Manganese[1]	+ 10		Bismuth	−14·0
	Chromium	+ 4			
	Molybdenum	+ 2			
	Aluminium	+ 2			

[1] But manganese fused in an electric furnace is said to be ferromagnetic with a maximum magnetization about 1 per cent of that of iron.

The characteristic of paramagnetic bodies is that in them the permeability is small; they exhibit no hysteresis; they have no transition temperature, but follow Curie's law that their susceptibility varies inversely as the absolute temperature. Most of the salts of the ferromagnetic bodies, for example the salt of iron, are paramagnetic, except where the iron constituent is in the acidic radicle, as in the ferrocyanides, which are practically neutral.

It is found that feebly magnetic bodies, when suspended in a more highly magnetic medium, behave as if they were diamagnetic. A small glass tube filled with a weak solution of ferric chloride, when suspended in air between the poles of an electromagnet, points axially, or is paramagnetic; but if it be surrounded by a stronger (and therefore more magnetic) solution of the same substance, it points equatorially, and is apparently repelled like diamagnetic bodies. All that the equatorial pointing of a body proves, then, is that it is less magnetic than the medium that fills the surrounding space. A balloon,

though it possesses mass and weight, rises through the air in obedience to the law of gravity, because the medium surrounding it is more attracted than it is. But it is found that diamagnetic repulsion takes place even in a vacuum: hence it would appear that the ether of space itself is more magnetic than the substances classed as diamagnetic. The susceptibility of air as compared with that of vacuum appears to be about + 0·000000023; that of water + 0·000000804.

400. Diamagnetic Polarity.—At one time Faraday thought that diamagnetic repulsion could be explained on the supposition that there existed a "diamagnetic polarity" the reverse of the ordinary magnetic polarity. According to this view (which, however, Faraday himself quite abandoned), a magnet, when its N-pole is presented to the end of a bar of bismuth, induces in that end a N-pole (the reverse of what it would induce in a bar of iron or other magnetic metal), and therefore repels it. Weber adopted this view, and Tyndall warmly advocated it, especially after discovering that the repelling diamagnetic force varies as the *square* of the magnetic power employed. It has even been suggested that when a diamagnetic bar lies equatorially across a field of force, its east and west poles possess different properties. The experiment named above suggests, however, an explanation less difficult to reconcile with the facts. It has been pointed out (Art. 390) that the degree to which magnetization goes on in a medium depends upon the magnetic permeability of that medium. Now, permeability expresses the number of magnetic lines induced in the medium for every line of magnetizing force applied. A certain magnetizing force applied to a space containing air or vacuum would induce a certain number of magnetic lines through it. If the space considered were occupied by a paramagnetic substance it would concentrate the magnetic lines into itself, as the sphere does in Fig. 208*a*. But if the sphere were of a permeability less than 1, the

magnetic lines would tend rather to pass through the air, as in Fig. 208*b*. If the space considered were occupied by bismuth, the same magnetizing force would induce in the bismuth *fewer* magnetic lines than in a vacuum. But those lines which were induced would still run in the same general *direction* as in the vacuum; *not in the opposite direction*, as Weber and Tyndall maintained. The result of there being a less dense flux through diamagnetic substances can be shown to be that such substances will be urged from places where the magnetic force is strong to places where it is weaker. This is why a ball of bismuth moves away from a magnet, and

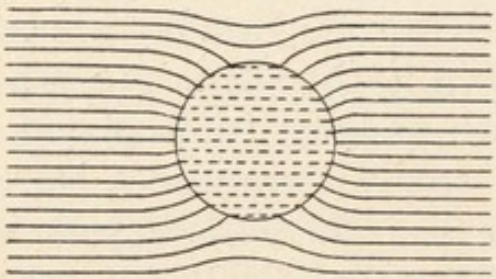


FIG. 208*a*.—Paramagnetic Body.

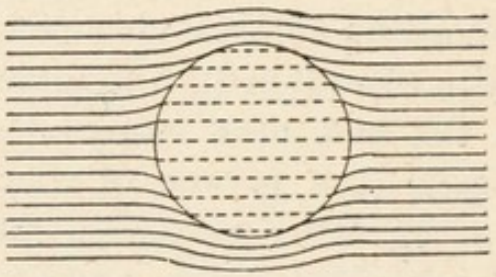


FIG. 208*b*.—Diamagnetic Body.

why a little bar of bismuth between the conical poles of the electromagnet (Fig. 207) turns equatorially so as to put its ends into the regions that are magnetically weaker. There is no reason to doubt that in a magnetic field of *uniform* strength a bar of bismuth would point along the magnetic lines.

401. Magne-Crystallic Action.—In 1822 Poisson predicted that a body possessing crystalline structure would, if magnetic at all, have different magnetic powers in different directions. In 1847 Plücker discovered that a piece of tourmaline, which is itself feebly paramagnetic, behaved as a diamagnetic body when so hung that the axis of the crystal was horizontal. Faraday, repeating the experiment with a crystal of bismuth, found that it tended to point with its axis of crystallization along the lines of the field axially. The magnetic force

acting thus upon crystals by virtue of their possessing a certain structure he named *magne-crystallic force.* Plücker endeavoured to connect the magne-crystallic behaviour of crystals with their optical behaviour, giving the following law: there will be either repulsion *or* attraction of the optic axis (or, in the case of bi-axial crystals, of *both* optic axes) by the poles of a magnet; and if the crystal is a "negative" one (*i.e.* optically negative, having an extraordinary index of refraction *less* than its ordinary index) there will be repulsion, but if a "positive" one there will be attraction. Tyndall endeavoured to show that this law is insufficient in not taking into account the paramagnetic or diamagnetic powers of the substance as a whole. He found that the magne-crystallic axis of bodies is in general *an axis of greatest density, and that if the mass itself be paramagnetic this axis will point axially; if diamagnetic, equatorially.* In bodies which, like slate and many crystals, possess cleavage, the planes of cleavage are usually at right angles to the magne-crystallic axis. Another way of stating the facts is to say that in non-isotropic bodies the induced magnetic lines do not necessarily run in the same direction as the lines of the impressed magnetic field. In natural crystals of magnetite the magnetic susceptibility is a maximum in the four directions normal to the octahedral faces. Pyrrhotine, Fe_7O_8, is non-magnetic along the axis, but strongly paramagnetic transversely.

402. Diamagnetism of Flames.—In 1847 Bancalari discovered that flames are repelled from the axial line joining the poles of an electromagnet. Faraday showed that all kinds of flames, as well as ascending streams of hot air and of smoke, are acted on by the magnet, and tend to move from places where the magnetic forces are strong to those where they are weaker. Gases (except oxygen and ozone), and hot gases especially, are feebly diamagnetic. But the active repulsion and turning

aside of flames may possibly be in part due to an electromagnetic action like that which the magnet exercises on the convexion-current of the voltaic arc (Art. 429) and on other convexion-currents. The electric properties of flame are mentioned in Arts. 9 and 334.

LESSON XXX.—*The Magnetic Circuit*

403. Magnetic Circuits.—A magnetic circuit consists generally of a number of portions, iron or air, through which the magnetic flux passes. Sometimes it consists of a core of iron only, in the form of a ring; sometimes it consists of air only; more often, as in all electromagnets, of an iron core with air-gaps between its parts. There is a magnetic circuit law similar to the law of Ohm for electric circuits. Ritchie, Sturgeon, Joule, and Faraday dimly recognized it. But the law was first put into shape in 1873 by Rowland, who calculated the flow of magnetic lines through a bar by dividing the "magnetizing force of the helix" by the "resistance to lines of force" of the iron. In 1882 Bosanquet introduced the term *magneto-motive-force*, and showed how to calculate the *reluctances* of the separate parts of the magnetic circuit, and, by adding them, to obtain the total *reluctance*.[1]

The law of the magnetic circuit may be stated as follows:—

$$\text{Magnetic Flux} = \frac{\text{magnetomotive-force}}{\text{reluctance}},$$

$$\text{or} \quad \mathfrak{F} = \frac{\mathrm{M}}{\mathrm{Z}}.$$

The magnetomotive force is, as shown in Art. 368, dependent on the strength of the current and on the number of turns by which it is interlinked with the

[1] This useful term, far preferable to "magnetic resistance," was introduced by Oliver Heaviside. The term *reluctivity* is sometimes used for the specific reluctance; it is the reciprocal of permeability.

magnetic circuit. Formerly it was usual to give the name of magnetomotive force to $\frac{4\pi}{10}$ times the number of ampere-turns (see Art. 368); but in modern usage the ampere-turns themselves are taken as the magnetomotive-force, and the numeric $\frac{4\pi}{10}$ then comes as a divisor into the calculation of the reluctance.

404. Reluctance.—As the electric resistance of a prismatic conductor can be calculated from its length, cross-section, and conductivity, so the magnetic reluctance of a bar of iron can be calculated from its length, cross-section, and permeability. The principal difference between the two cases lies in the circumstance that whilst in the electric case the conductivity is the same for small and large currents, in the magnetic case the permeability is not constant, but is less for large magnetic fluxes than for small ones.

Let the length of the bar be l centims., its section A sq. cms., and its permeability μ. Then its reluctance will be proportional directly to l, and inversely to A and μ. Calling the reluctance Z we have

$$Z = \frac{l}{A\mu} \div \frac{4\pi}{10};$$

or,

$$Z = \frac{l}{A\mu} \times 0{\cdot}796.$$

Example.—An iron bar 100 cm. long and 4 sq. cms. in cross-section is magnetized to such a degree that $\mu = 320$: then Z will be 0·062.

The reluctance of a magnetic circuit is generally made up of a number of reluctances in series. We will first take the case of a closed magnetic circuit (Fig. 209*a*) made up of a curved iron core of length l_1, section A_1, and permeability μ_1; and an armature of length l_2, section A_2, and permeability μ_2, in contact with the ends of the former. In this case the reluctance is

$$Z = \left(\frac{l_1}{A_1 \mu_1} + \frac{l_2}{A_2 \mu_2} \right) \times 0{\cdot}796.$$

To the reciprocal of the reluctance the name of *the permeance* is sometimes given.

405. Calculation of Excitation.—Passing on to the more difficult case of a circuit made up partly of iron and partly of air, we will suppose the armature to be moved to a distance, so that there are two air-gaps

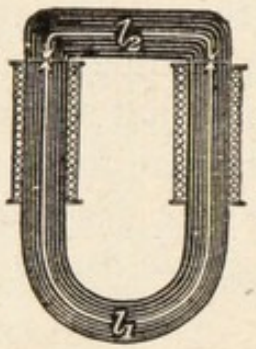


FIG. 209*a*.—Electromagnet, with closed Magnetic Circuit.

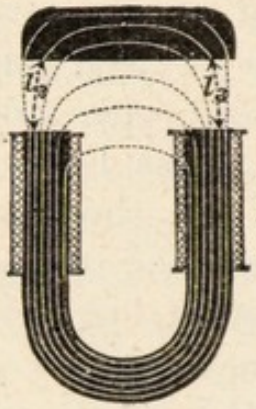


FIG. 209*b*.—Electromagnet, with Gaps in the Magnetic Circuit.

(Fig. 209*b*) in the circuit, each gap of length l_3 (from iron to iron), and section A_3 (equal to area of pole face). This will introduce an additional reluctance $2l_3/A_3$, the permeability for air being = 1. It will also have the effect of making part of the magnetic flux leak out of the circuit. Magnetic *leakage* is due to the circumstance that the permeability of air is not zero, but unity, and therefore part of the flux passes uselessly from pole to pole through the air. That part of the whole flux which thus leaks across instead of going usefully into the armature is called the *stray flux*.

By Art. 368, if the excitation consists of i-amperes circulating in S-spirals around the core, the magnetomotive-force will be iS. Applying this to the preceding example, dividing the magnetomotive-force by the reluctance, we get for the magnetic flux—

$$\mathfrak{F} = \frac{iS}{\frac{10}{4\pi}\left\{\frac{l_1}{A_1\mu_1} + \frac{l_2}{A_2\mu_2} + \frac{2l_3}{A_3}\right\}}$$

But more often the calculation is wanted the other way round, to find how many ampere-turns of excitation will be needed to produce a given flux through a magnetic circuit of given size. Two difficulties arise here. The permeability will depend on the degree of saturation, that is to say on the flux-density in the iron. Also the leakage introduces an error. To meet the first difficulty approximate values of μ must be found. Suppose, for example, it was intended to produce a flux of 1,000,000 lines through an iron bar having a section of 80 sq. centims., then $\mathfrak{B}$ will be 12,500, and reference to the table in Art. 391 shows that if the bar is of wrought iron μ will be about 1247. To meet the second difficulty we must estimate (from experience) an allowance for leakage. Suppose we find that of all the lines created in the U-shaped part only the fraction $1/\nu$ gets through the armature, then to force $\mathfrak{F}$ lines through the armature we must generate $\nu\mathfrak{F}$ lines in the U-shaped piece, where ν is the coefficient of allowance for leakage, an improper fraction increasing with the width of the gaps.

We then proceed to calculate in parts as follows :—

Ampere-turns needed to drive $\nu\mathfrak{F}$ lines through iron of magnet core $= \nu\mathfrak{F} \times \frac{l_1}{A_1\mu_1} \div 1{\cdot}257.$

Ampere-turns needed to drive $\mathfrak{F}$ lines through two gaps $= \mathfrak{F} \times \frac{2l_3}{A_3} \div 1{\cdot}257.$

Ampere-turns needed to drive $\mathfrak{F}$ lines through iron of armature $= \times\, \mathfrak{F}\frac{l_2}{A_2\mu_2} \div 1{\cdot}257.$

Then adding up, we get :—

$$\text{Total ampere-turns needed} = \mathfrak{F}\left\{\frac{\nu l_1}{A_1\mu_1} + \frac{l_2}{A_2\mu_2} + \frac{2l_3}{A_3}\right\} \div 1{\cdot}257.$$

Formulæ similar to this were introduced by Hopkinson and by Kapp in designing electromagnets for dynamos. But it is possible to simplify them by remembering that

if a flux $\mathfrak{F}$ passes through an area of cross-section **A**, the flux-density $\mathfrak{B}$ can be found by dividing $\mathfrak{F}$ by **A**. And if we know what the value of $\mathfrak{B}$ is going to be, then we can find the corresponding value of the ampere-turns per centimetre from tables, or from the corresponding curves (Art. 391), for the brand of iron concerned, and can multiply the values so found by the number of centimetres' length of that part.

Example.—An electromagnet having for its U-shaped core of wrought iron a length of 24 cm. and a cross-section of 4·8 sq. cms. is lightly chamfered to have the area of each pole 4·0 sq. cms. The wrought-iron armature is wide enough to cover the pole surfaces; the mean length of path through it is 5 cm. and its section 3 sq. cms. Find the ampere-turns needed to produce a flux of 36,000 lines through the armature when the air-gaps are each 1 mm. Assume $\nu = 1{\cdot}36$. Here $l_1 = 5$; $l_2 = 0{\cdot}1$; $l_3 = 24$; $A_1 = 3$; $A_2 = 4$; $A_3 = 4{\cdot}8$. If $\mathfrak{F}_1 = 36{,}000$, $\mathfrak{B}_1 = 12{,}000$. Hence, from the curve in Fig. 200, or by the table on p. 376, we see that each centimetre of armature length will require 9 ampere-turns; or the ampere-turns needed for the armature will be 45. In the air-gaps the flux-density is $\mathfrak{F} \div 4 = 9000$; and, dividing by 1·257, we find that each centimetre-length in air will therefore read 7159 ampere-turns; hence, as total air-gap length is 0·2 cm. the ampere-turns needed for that part are 1431·8. The flux through the core will be $1{\cdot}36 \times 36{,}000 = 48{,}960$; the density in the core will be 10,200; whence, by the table or the curves of Fig. 201, the ampere-turns needed per centimetre-length will be 6·2. So the ampere-turns for the 24 cm. length will be 153·6. Adding up $45 + 1431{\cdot}8 + 153{\cdot}6 = 1630$ total ampere-turns needed for the magnetic circuit.

406. Effect of Air-Gap in Circuit.—Air having no remanence, the presence of a gap in the iron circuit tends to make residual magnetism unstable, as though the polar magnetism on the end-faces had a self-demagnetizing effect. In fact it is very difficult to give a permanent magnetism to *short* pieces of steel. Further, the low permeability of air necessitates enormous magneto-motive-forces, compared with those required for iron, to

force a given flux across a gap. The effect is to shear over to the right the curves of magnetization, seeing that a greater $\mathfrak{H}$ is needed to attain an equal value of $\mathfrak{B}$. Joints in the magnetic circuit act as narrow gaps.

The chief reason why the pull exerted by an electromagnet on its keeper falls off so very greatly when the keeper is moved away to a short distance is the diminution of the magnetic flux caused by the great reluctance of the air-gap thus introduced into the circuit.

407. Contrast between Electromagnets and Permanent Magnets.—It is found that with electromagnets the pull on the keeper, when the keeper is removed to a given distance, falls off more rapidly than is the case with permanent magnets. The reason is that with permanent magnets the flux remains constant, while with electromagnets the increase of the reluctance of the air-gap causes the flux in the magnetic circuit to diminish; so that there are two causes at work: (i.) diminution of flux; (ii.) the leakage of the stray flux from pole to pole. Let the reader compare Fig. 91, p. 136, with Fig. 210, p. 396.

408. Magnetic Shunts.—If a magnetic circuit divides at any place into two paths part of the flux goes along each path. The two paths being in parallel with one another the relative fraction of the flux which traverses each will be inversely proportional to their respective reluctances. A piece of iron placed so as to divert a portion of the flux is termed a *magnetic shunt.*

409. General Law of Electromagnetic Systems.—Consider an electromagnetic system consisting of any number of parts—iron masses, coils carrying currents, air, masses of other materials, whether magnetic or diamagnetic—in any given configuration. Any change in the configuration of the parts will in general produce either an increase or a decrease in the magnetic flux. For example, if the armature of an electromagnet is allowed to move up toward the poles, or if the needle of a galvanometer is allowed to turn, there will be a betterment of the

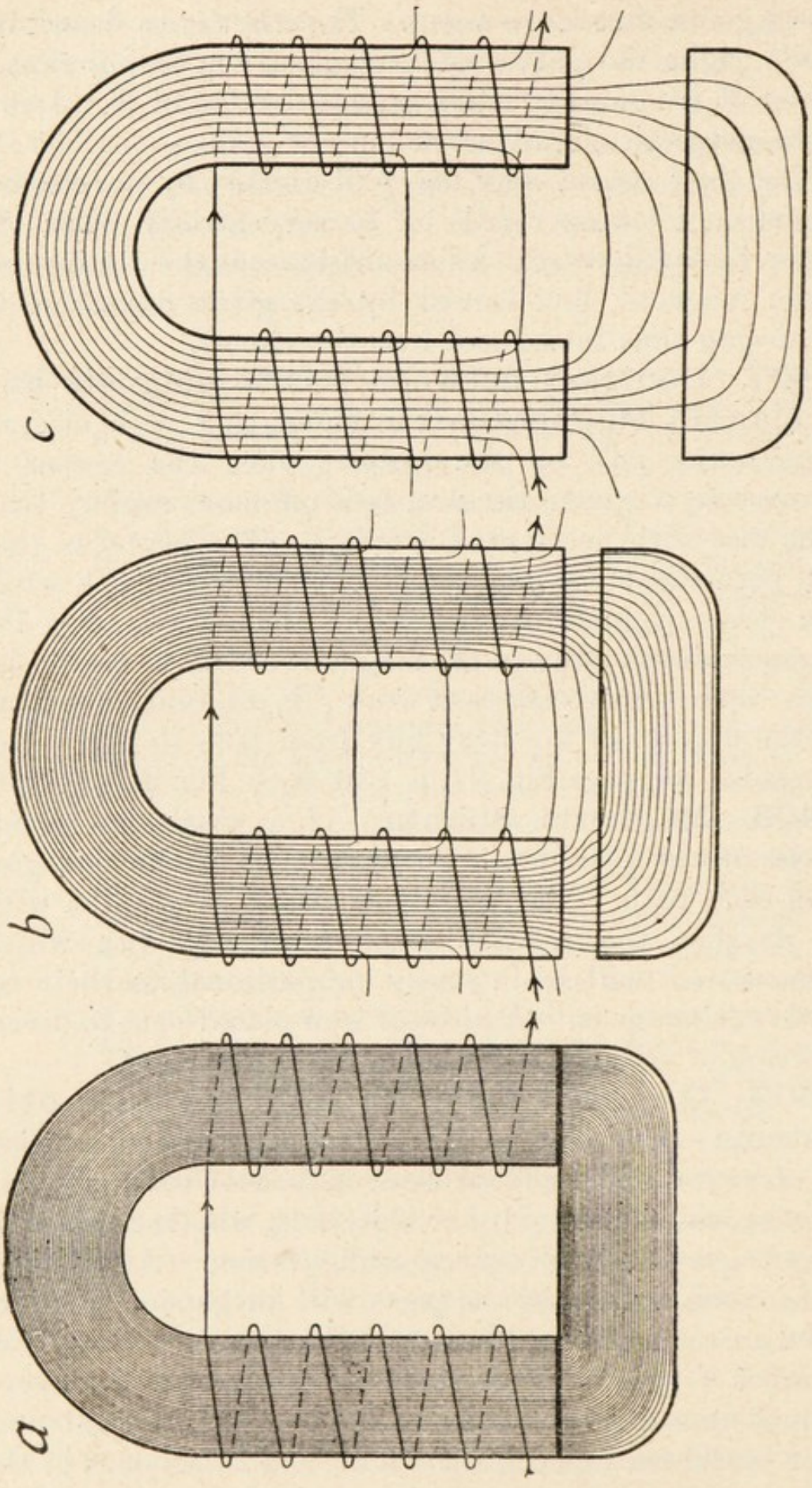


FIG. 210.—Electromagnet with its Keeper in three different Positions.
a, in contact; *b*, with short intervening gaps; *c*, with wide intervening gaps in the magnetic circuit.
The exciting current is supposed to be the same in the three cases.

magnetic circuit, and the magnetic flux through the coils will be increased. Magnetic circuits always tend to close up and become as compact as possible. On the contrary, if we pull away the armature from an electromagnet the magnetic reluctance is increased, and the flux diminished; and this action is resisted by the reaction of the system. All these things may be summed up in the following general law:—

Every electromagnetic system tends so to change the configuration of its parts as to make the interlinkage of the magnetic flux through the exciting coils a maximum.

Suppose (the exciting ampere-turns, iS, remaining the same) a motion of any part through a distance dx to result in a decrease of flux $d\mathfrak{F}$, then the force resisting such motion will be proportional to $i\mathrm{S}d\mathfrak{F}/dx$.

410. Empirical Rules.—Before the law of the magnetic circuit was understood many attempts were made to find algebraic formulæ to express the relation between the strength of current and the amount of magnetism produced. Lenz and Jacobi suggested that *the magnetism of an electromagnet was proportional to the current and to the number of turns of wire in the coil*—in other words, is proportional to the *ampere-turns*. Or in symbols

$$m = ai\mathrm{S},$$

where a is a constant depending on the quantity, quality, and form of iron. This rule is, however, only true when the iron core is still far from being "saturated." If the iron is already strongly magnetized a current twice as strong will not double the magnetization in the iron, as Joule showed in 1847.

Müller gave the following approximate rule:—*The strength of an electromagnet is proportional to the angle whose tangent is the strength of the magnetizing current; or*

$$m = \mathrm{A} \tan^{-1} i,$$

where i is the magnetizing current, and A a constant depending on the construction of the particular magnet. If the student will look at Fig. 133 and imagine the divisions of the horizontal tangent line OT to represent strengths of current, and the number of degrees of arc intercepted by the oblique lines to represent strengths of magnetism, he will see that even if OT be made infinitely long, the intercepted angle can never exceed 90°.

Another formula, known as Frölich's, is—

$$m = a\frac{i}{1+bi},$$

where a and b are constants depending on the form, quality, and quantity of the iron, and on the winding of the coil. The constant b is the reciprocal of that number of amperes which would make m equal to half possible maximum of magnetism.

The author's variety of this formula expresses the number of magnetic lines $\mathfrak{F}$ proceeding from the pole of the electromagnet—

$$\mathfrak{F} = \mathrm{Y}\frac{i}{i \times i'},$$

where Y represents the maximum number of magnetic lines that there would be if the magnetizing current were indefinitely increased and the iron core saturated, and i' stands for that number of amperes which would bring the magnetism up to half-saturation.

None of these empirical formulæ are as useful as the rational formula at the end of Art 405.

LESSON XXXI.—*Electromagnets*

411. Electromagnets.—In 1820, almost immediately after Oersted's discovery of the action of the electric current on a magnet needle, Arago and Davy independently discovered how to magnetize steel and iron by inserting needles or strips into spiral coils of copper wire around which a current was circulating. The method is shown in the simple diagram of Fig. 211, where a current from a single cell is passed through a spiral coil of insulated copper wire, in the hollow of which is placed a strip of iron or steel, which is thereby magnetized. The separate turns of the coil must not touch one another or the central bar, otherwise the current will take the shortest road open to it and will not traverse the whole of the coils. To prevent such short-circuiting by contact the wire of the coil should be overspun with silk or cotton (in the latter case insulation is improved by varnishing it or by steeping the cotton covering in melted paraffin wax) or covered with a layer of enamel. If the bar be of soft iron it will be a magnet only so long as the current flows ;

and an iron core thus surrounded with a coil of wire for the purpose of magnetizing it by an electric current is called an **Electromagnet.** Sturgeon, who gave this

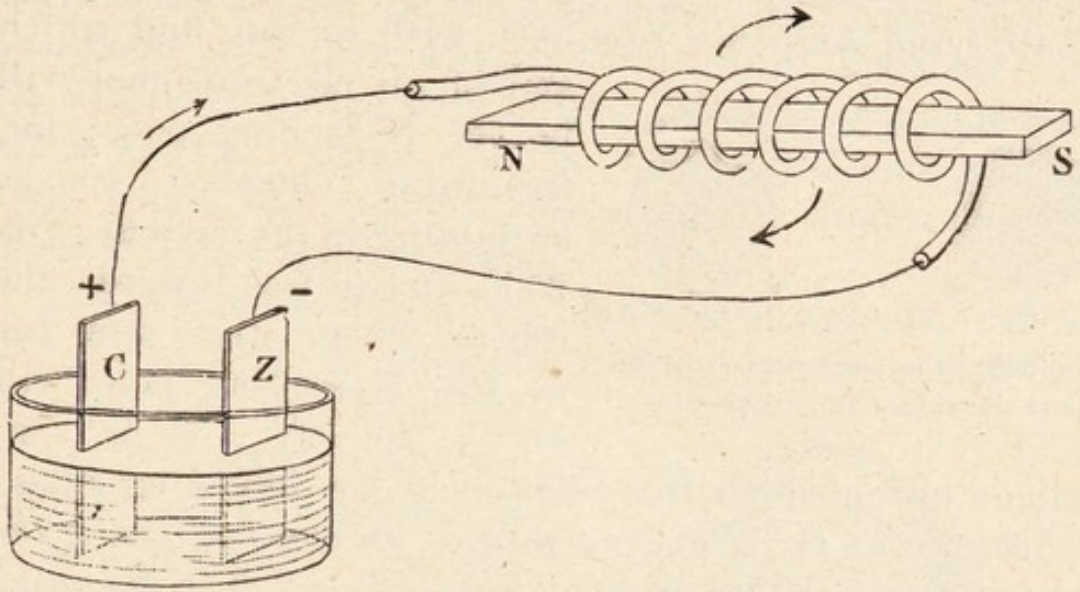


FIG. 211.—Magnetization of Bar of Iron, by Circulation of Current.

name, applied the discoveries of Davy and Arago to the construction of electromagnets far more powerful than any magnets previously made. His first electromagnet was a horseshoe (Fig. 212) made of a rod of iron about 1 foot long and $\frac{1}{2}$ inch in diameter coiled with a single stout copper wire of only 18 turns. With the current from a single cell it lifted 9 lbs.; but with a more powerful battery it lifted 50 lbs. It was first shown by Henry that when electromagnets are required to work at the distant end of a long line they must be wound with many turns of fine wire. The great usefulness of the electromagnet in its application to electric bells and the telegraphic instruments lies in the fact that *its magnetism is under the control of the current*; when circuit is "made" it becomes a magnet, when circuit is "broken" it ceases to act as a magnet. Moreover, it is capable of

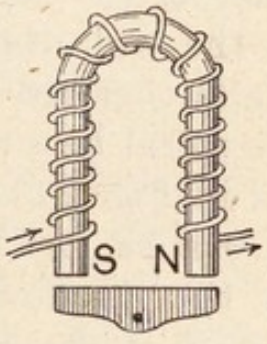


FIG. 212.—Sturgeon's Electromagnet (1825).

being controlled from a distance, the current being "made" or "broken" at a distant point of the circuit by a suitable key or switch.

412. Polarity and Circulation of Current.—By applying Ampère's rule (Art. 210) we can find which end of an electromagnet will be the N-seeking pole; for, imagining ourselves to be swimming in the current (Fig. 211), and to face towards the centre where the iron bar is, the N-seeking pole will be on the left. It is convenient to remember this relation by the following rules:—*Looking at the S-seeking pole of an electromagnet, the magnetizing currents are circulating round it in the same cyclic direction as the hands of a clock move;* and, *looking at the N-seeking pole of an electromagnet, the magnetizing currents are circulating round it in the opposite cyclic direction to that of the hands of a clock.* Fig. 213 shows this graphically. These rules are true, no matter whether the beginning of the coils is at the end near the observer, or at the farther end from him, *i.e.* whether the spiral be a right-handed screw, or (as in Fig. 211) a left-handed screw. It will be just the same thing, so far as the magnetizing power is concerned, if the coils begin at one end and run to the other and back to where they began; or they may begin half-way along the bar and run to one end and then back to the other: the one important thing to know is which way the current flows round the bar when you look at it end-on. The corkscrew rule (Art. 211) leads to the same result.



FIG. 213.—Connexion of Polarity with Direction of Circulation.

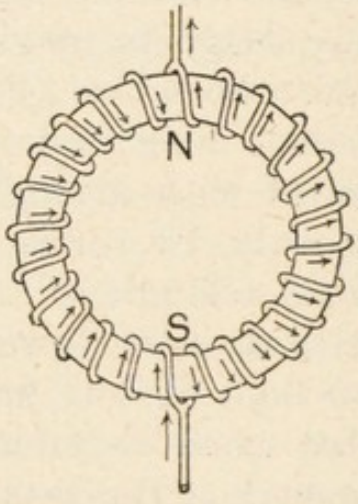


FIG. 214.—Consequent Poles in a Ring-Electromagnet.

Suppose an iron core to be wound with a right-handed coil, and that a current is introduced at some point, and to flow both ways, it will produce oppositely-directed magnetizing actions in the two points, and there will be *consequent poles* (Art. 122) at the point of entrance. In Fig. 214 an iron ring with a right-handedly-wound closed coil is shown. There will be a double S-pole at the point where the current enters, and a double N-pole where it leaves the windings.

413. Construction of Electromagnets.—The most useful form of electromagnet is that in which the iron core is bent into the form of a horseshoe, so that both poles may be applied to one iron armature. In this case it is usual to divide the coils into two parts wound on bobbins, as in Figs. 68 and 215. Often the iron part is made of two straight limbs fixed into a cross-piece or yoke. Sometimes only one coil is wound on the yoke part. The electromagnet depicted in Fig. 216 is of a form adapted for laboratory experiments, and has movable coils which are slipped on over the iron cores. As a rule the iron parts, including the yoke and armature, should form as nearly as possible a closed magnetic circuit. The cross-sections of yokes should be as great as those of the cores.

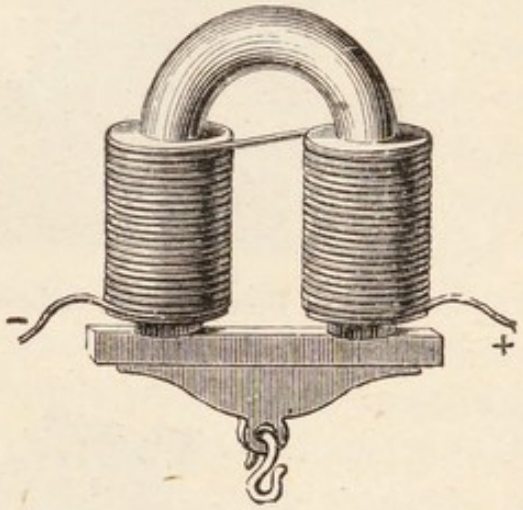


FIG. 215.—A Horseshoe Electromagnet.

Many special forms[1] of electromagnet have been devised for special purposes. A special form of electromagnet devised by Ruhmkorff for experiments on diamagnetism is shown in Fig. 207. A still more powerful

[1] For descriptions of these, as well as for discussion of all other matters relating to the subject, see the author's treatise on *The Electromagnet and Electromagnetic Mechanism.*

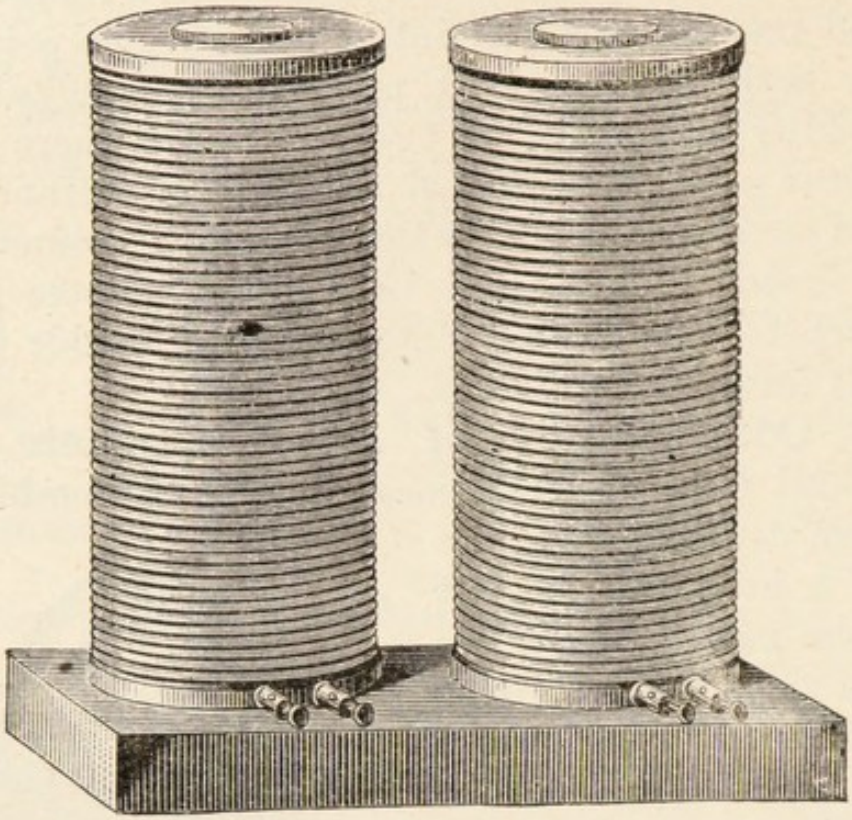


FIG. 216.—A Laboratory Electromagnet.

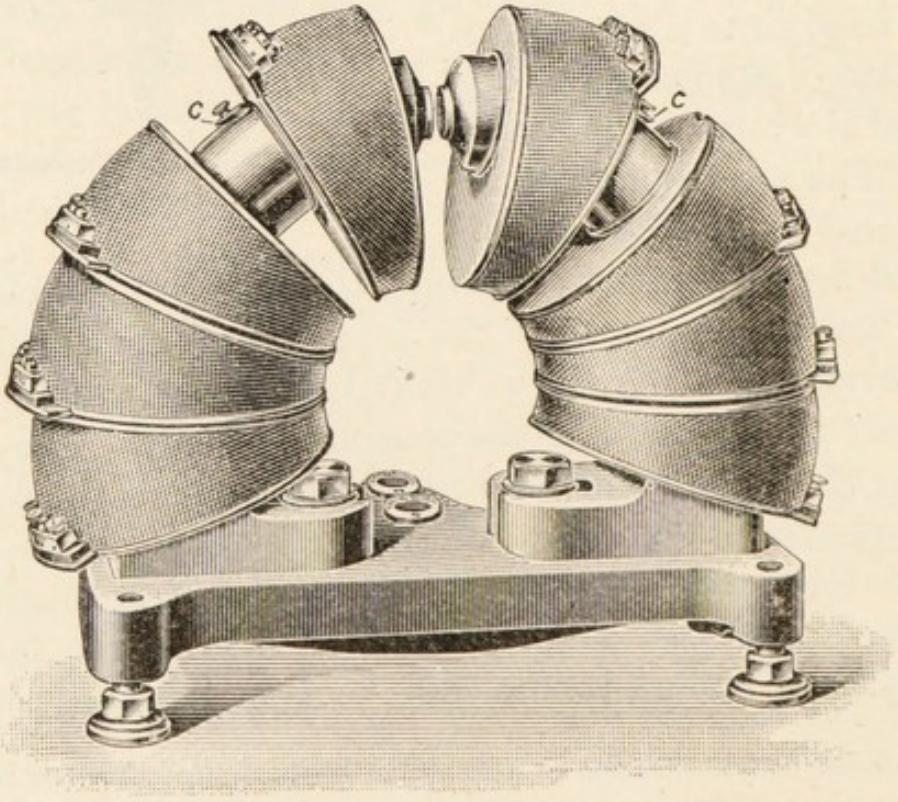


FIG. 217.—Half-ring Electromagnet of Du Bois.

form, designed to produce exceedingly intense magnetic fields in the space between its poles, is the *half-ring* electromagnet designed by H. Du Bois, Fig. 217. It consists of two iron quadrants, circular in section, which are bolted to a massive iron yoke forming the base of the electromagnet. The pole faces are very close together and are reduced to a smaller diameter than the main limbs so as to obtain a highly concentrated and uniform magnetic field. The coils are in sections which enable various degrees of magnetization to be obtained.

To give a very powerful holding-on action, a short cylindrical electromagnet surrounded by an outer iron tube, united at the bottom by iron to the iron core, is found best; the iron jacket constituting a return path for the magnetic lines. This form is known as an *iron-clad* magnet.

To attract iron across a wide gap which offers much reluctance, a horseshoe shape with long cores should be chosen; for it needs long cores on which to wind wire enough to provide sufficient excitation to drive the flux across the gap. To give a gentle pull over a long range a long tubular coil (Art. 416), having a long movable iron core, is used. For very quick-acting magnets the coils should not be wound all along the iron, but only round the poles; and they should be small.

414. Solenoid.—Without any central core of iron or steel a spiral coil of wire traversed by a current acts as an electromagnet (though not so powerfully as when an iron core is placed in it). Such a coil is sometimes termed a **solenoid.** A solenoid has two poles and a neutral equatorial region. Ampère found that it will attract magnets and be attracted by magnets. It will attract another solenoid; it has a magnetic field resembling generally that of a bar magnet. If so arranged that it can turn round a vertical axis, it will set itself in a North and South direction along the magnetic meridian. Fig. 218 shows a solenoid arranged with pivots, by which it can be suspended to a "table," like that shown in Fig. 227.

With an iron core the solenoid becomes far more powerful. The effect of the iron core is, by its greater permeability, to multiply the number of magnetic lines as well as to concentrate them at definite poles. The student has been told (Art. 215) that the lines of force due to a current flowing in a wire are closed curves, approximately circles (Figs. 127, 193, and 223), round the wire. If there were no iron core many of these little circular lines of force would simply remain as small closed curves around their own wire ; but, since iron has a permeability hundreds of times greater than air, wherever the wire passes near an iron core the magnetic lines alter their shape, and instead of being little circles around the separate wires, run through the iron core from end to end, and round outside from one end of the coil back to the other.

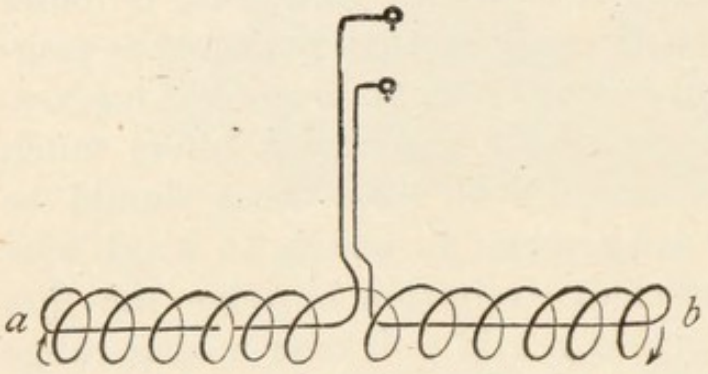


FIG. 218

A *few* of the magnetic lines do this when there is no iron ; almost all of them do this when there is an iron core ; and when there is an iron core there are many more lines to flow back.[1] Hence the electromagnet *with* its iron core has enormously stronger poles than the spiral coil or solenoid would have alone.

In Art. 369 it was shown that the intensity of the magnetic field down the middle of a solenoid of length l, having S-spirals, carrying i-amperes, is—

$$\mathcal{H} = \frac{4\pi}{10} \times \frac{iS}{l}.$$

[1] But, in the case of a permanent steel horseshoe magnet, bringing up the iron keeper, though it concentrates the lines through the poles, *does not increase* the total number of lines through the bend of the U. Compare Figs. 91 *a*, *b*, and *c*, p. 136, with Figs. 210 *a*, *b*, and *c*, p. 396.

Since the area enclosed is πr^2, the flux down the long tubular solenoid (without iron) will be

$$\mathfrak{F} = \frac{4\pi^2 r^2}{10l} \times i\mathrm{S}.$$

And, since 4π magnetic lines go to one unit of magnetism, the solenoid (without iron) will act (if there is no leakage) as though it had at its pole the magnetism—

$$m = \frac{\pi r^2}{10l} i\mathrm{S}.$$

It will be noticed that for any solenoid of given length and radius the three magnetic quantities $\mathcal{H}$ (internal field), $\mathfrak{F}$ (magnetic flux), and m (strength of poles) are proportional to the *amperes* of current and to the number of *turns* in the coil, that is to say, to the *ampere-turns*.

415. Lifting-power of Electromagnets.—The force with which an electromagnet holds on to its armature depends not only on its magnetic strength, but also upon its form, and on the shape of its poles, and on the form of the soft iron armature which it attracts. It should be so arranged that as many lines of force as possible should run through the armature, and the armature itself should contain a sufficient mass of iron. Joule designed a powerful electromagnet capable of supporting over a ton. The maximum pull he could produce between an electromagnet and its armature was 200 lbs. per square inch, or about 13,800,000 dynes per square centimetre. Bidwell found the attraction to go up to 226·3 lbs. per square inch when the wrought-iron core was saturated up to 19,820 magnetic lines to the square centimetre. The law of traction is that the pull per square centimetre is proportional to the square of the number of lines per square centimetre: or in symbols—

$$f = \frac{\mathcal{B}^2 \mathrm{A}}{8\pi},$$

where f is the pull in dynes, and A the area in square

centims. In the following table are given the values of the tractive force for different degrees of magnetization.

$\mathfrak{B}$ lines per sq. cm.	Dynes per sq. centim.	Grammes per sq. centim.	Pounds per sq. inch.
1,000	39,790	40·56	0·577
2,000	159,200	162·3	2·308
3,000	358,100	365·1	5·190
4,000	636,600	648·9	9·228
5,000	994,700	1,014	14·39
6,000	1,432,000	1,460	20·75
7,000	1,950,000	1,987	28·26
8,000	2,547,000	2,596	36·95
9,000	3,223,000	3,286	46·72
10,000	3,979,000	4,056	57·68
12,000	5,730,000	5,841	83·07
14,000	7,800,000	7,950	113·1
16,000	10,170,000	10,390	147·7
18,000	12,890,000	13,140	186·8
20,000	15,920,000	16,230	230·8

It will be noted that doubling $\mathfrak{B}$ makes the pull four times as great. One curious consequence of this law is that to enlarge its poles weakens the pull of an electromagnet or magnet. In some cases—bar magnets, for example—their tractive power is increased by bevelling down or rounding the poles so as to concentrate $\mathfrak{B}$.

416. Plunger Electromagnet.—A solenoid with a movable iron plunger is sometimes called a *plunger electromagnet*, or a *sucking-magnet*. The iron core tends to move into the position in which it best completes (Art. 409) the magnetic circuit. If the core is much longer than the tubular coil, the pull increases as the end of the core penetrates down the coil, being a maximum when the end of the iron rod has about reached the end of the tube. Short iron cores are only pulled while at the mouth of the coil; the maximum pull being when about half their length has entered.

Fig. 219 depicts a form of plunger electromagnet in

very extensive use. The soft iron plunger, which is usually coned at the end, is pulled up, when the exciting current is switched on, inside a heavy coil of insulated wire wound on a brass tube. To increase the pull a short fixed core of iron is inserted at the top; and an iron jacket or external frame provides a good return path for the magnetic flux. Such a magnet may be designed to exert a pull of 100 lbs. or more, with a range of travel of 2 or 3 inches. In this case also the core tends so to move as to close up the gap in the magnetic circuit,[1] and to make the product of the flux and the ampere-turns with which it is interlinked a maximum (Art. 409).

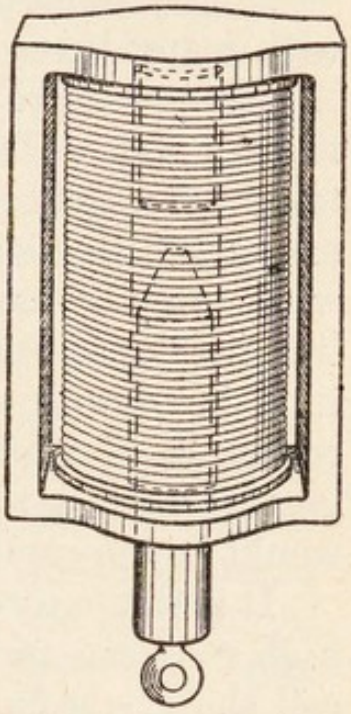


FIG. 219.—Plunger Electromagnet.

417. The Winding of Electromagnets. — The exact laws governing the winding of electromagnets are somewhat complicated; but it is easy to give certain rules which are approximately true. Every electromagnet shows the same general set of facts — that with small exciting power there is little magnetism produced, with larger exciting power there is more magnetism, and that with very great exciting power the iron becomes practically saturated and will take up very little additional magnetism. It follows at once that if the electromagnet is destined to be used at the end of a long line through which only a small current (perhaps only $\frac{1}{100}$ ampere) will flow, the requisite number of ampere-turns to excite the magnetism will not be attained unless some thousands

[1] The following is the law expressing the pull, in dynes, of a plunger magnet:—

$$f = \frac{1}{200}(Si)^2 \times \frac{dP}{dx},$$

wherein dP stands for the change in the permeance (Art. 404) due to a forward travel of the plunger through dx centimetres.

of turns of wire are used; and as the current is small a fine wire may be used.

It may be noted that when electromagnets are wound with many turns of fine wire, these coils will add to the electric resistance of the circuit, and will tend to diminish the current. Herein lies a difference in construction of telegraphic and other instruments; for while electromagnets with "long coils," consisting of many turns of fine wire, must be used on long circuits where there is great line resistance, such an instrument would be of no service in a laboratory circuit of very small resistance, for the resistance of a long thin coil would be disproportionately great: here a short coil of few turns of stout wire would be appropriate (see Art. 207).

It is the nature of the *line*, according to whether it is of high resistance or low, which governs the questions how the coil shall be wound and how the battery shall be grouped.

Similar electromagnets of different sizes must have ampere-turns proportional to their linear dimensions if they are to be raised to equal degree of saturation.

As the magnetism of the magnet depends on the number of ampere-turns, it should make no matter whether the coils are bigger than the core or whether they enwrap it quite closely. If there were no magnetic leakage this would be true in one sense; but for an equal number of turns large coils cost more and offer higher resistance. Hence the coils are wound as closely to the iron core as is consistent with good insulation. Also the iron is chosen as thick as possible, as permeable as possible, and forming as compact a magnetic circuit as possible, so that the magnetic resistance may be reduced to its utmost, giving the greatest amount of magnetism for the number of ampere-turns of excitation. This is why horseshoe-shaped electromagnets are more powerful than straight electromagnets of equal weight; and why also a horseshoe electromagnet will only lift about a quarter as much load if one pole only is used instead of both.

As the coils of electromagnets grow hot with the current, sufficient cooling surface must be allowed, or they may char their insulation. Each square centimetre of surface warmed 1° C. above the surrounding air can get rid of about 0·0029 *watt*. If 50° above the surrounding air be taken as the safe limit of rise of temperature, and the electromagnet has resistance r and surface s sq. cms., the highest permissible current will be $0{\cdot}38\sqrt{s/r}$ amperes.

Where the coils of electromagnets are to be excited from circuits at a given voltage, the excitation (*i.e.* ampere-turns) which they receive depends on the mean resistance of one turn of the coil, and is practically independent of the number of coils. For, supposing the mean resistance per turn to remain the same, doubling the number of turns will double the resistance, and will therefore halve the current. But if half the current goes twice as many times round, the ampere-turns will be unchanged. By this argument, the excitation should also remain unchanged if half the coils were removed; and indeed this would be true if the remaining coils did not overheat.

418. Polarized Mechanism.—An electromagnet moves its armature one way, no matter which way the current flows. Reversing the current makes no difference. There are, however, two means of designing a mechanism that will cause an armature to move in either sense at will. (*a*) The armature's movement is controlled by an adjusted spring so as to be in an intermediate position when a weak current is flowing. Then sending a stronger current will move the armature one way, and weakening or stopping the current will make it move the other way. (*b*) A *polarized* armature or tongue (*i.e.* one that is independently magnetized) is placed *between the poles* of the electromagnet instead of opposite them. The direction in which it tends to move will be reversed by reversing the current in the circuit of the electromagnet.

419. Growth of Magnetism.—It requires time to

magnetize an iron core. This is mainly due to the fact that a current, when first switched on, does not instantly attain its full strength, being retarded by the self-induced counter-electromotive-force (Art. 501); it is partly due to the reaction of transient eddy-currents (Art. 500) induced in the iron itself. Faraday's large electromagnet at the Royal Institution takes about two seconds to attain its maximum strength. The electromagnets of large dynamo machines often take ten minutes or more to rise to their working stage of magnetization.

When electromagnets are used with rapidly alternating currents (Art. 522) there are various different phenomena, for which the student is referred to Art. 533.

LESSON XXXII.—*Electrodynamics*

420. Electrodynamics.—In 1821, almost immediately after Oersted's discovery of the action of a current on a magnet, Ampère discovered that a current acts upon another current, apparently attracting it[1] or repelling it according to certain definite laws. These actions he investigated by experiment, and from the experiments he built up a theory of the force exerted by one current on another. That part of the science which is concerned with the force which one current exerts upon another he termed **Electrodynamics.** It is now known that these actions are purely magnetic, and are due to stresses in the intervening medium. The magnetic field around a single conductor consists of a *magnetic whirl* (Arts. 215 and 370), and any other conductor carrying a current when brought into the field of the first is acted upon by it. We may determine graphically the form of the magnetic field surrounding two parallel conductors carrying currents

[1] It would be more correct to speak of these (mechanical) forces as acting on the *conductors carrying currents* than as acting on the currents themselves.

by applying the *principle of superposition* (Art. 144) as in Figs. 220 and 221 which may be compared with Figs.

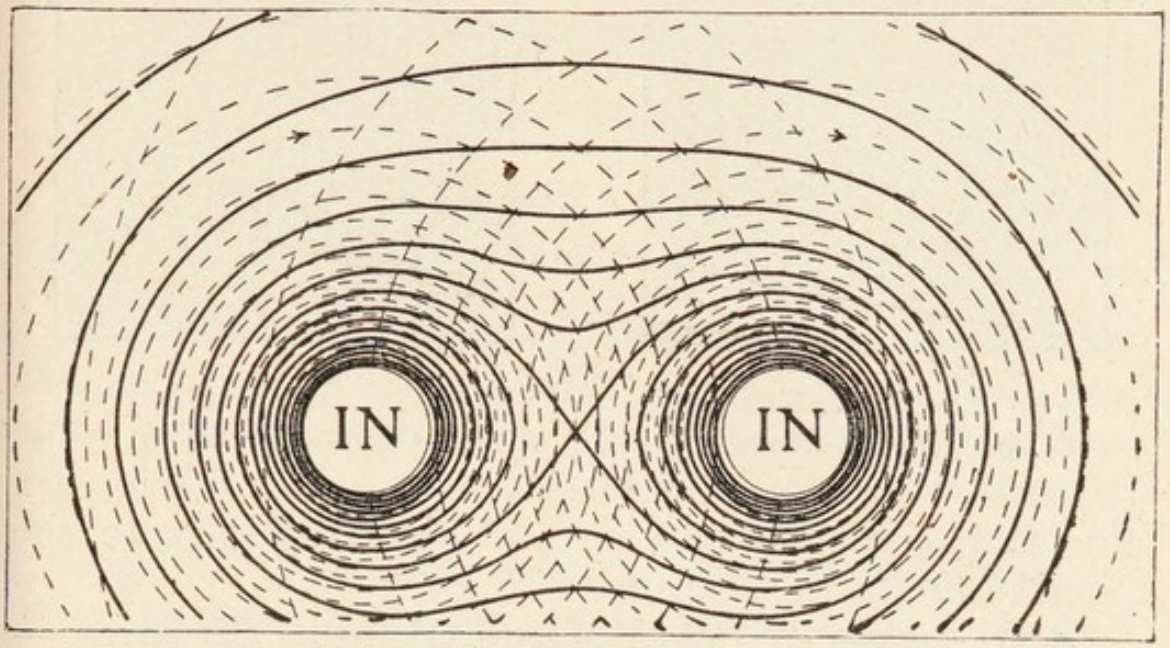


FIG. 220.—Field due to two Currents in the same direction.

222 and 223, obtained when the two conductors were

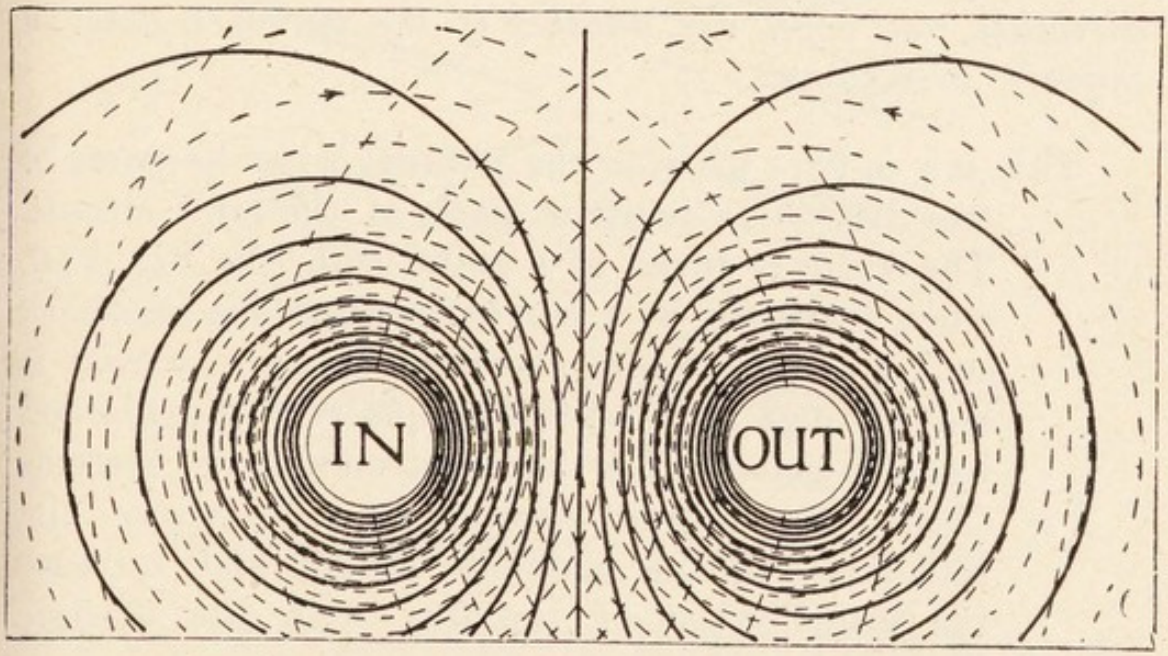


FIG. 221.—Field due to two Currents in opposite directions.

passed through holes in a sheet of glass on which iron filings were sprinkled. In Figs. 220 and 222 the currents

flow in the same direction; in Figs. 221 and 223, in opposite directions. In the first case the stresses in

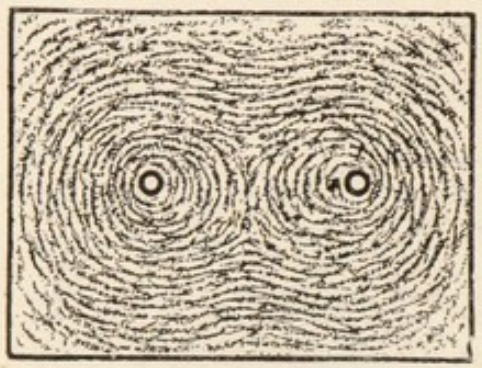


FIG. 222.—Filing Figure of Concurrent Currents.

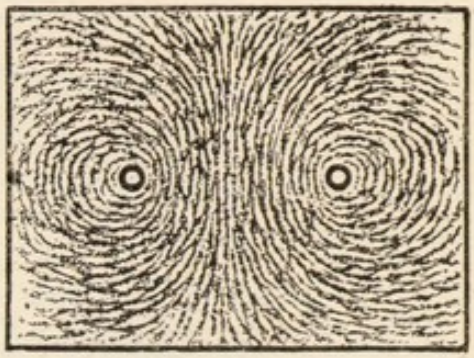


FIG. 223.—Filing Figure of Opposed Currents.

the field (Art. 121) tend to pull them together, in the second to push them apart.[1]

421. Laws of Parallel and Oblique Circuits.—The following are the laws discovered by Ampère :—

(i.) *Two parallel portions of a circuit attract one another if the currents in them are flowing in the same direction, and repel one another if the currents flow in opposite directions.*

This law is true whether the parallel wires be parts of two different circuits or parts of the same circuit. The separate turns of a spiral coil, like Fig. 218, when traversed by a current attract one another; such a coil, therefore, shortens [2] when a current is sent through it. But this is equally well explained by the general law of electromagnetic systems (Art. 409), because shortening will reduce the reluctance of the magnetic circuit and increase the interlinkage of the flux with the electric

[1] See article by the author in the *Philosophical Magazine*, November 1878, p. 348.

[2] This is the mode of operation of Roget's dancing spiral, an open coil of wire fixed at the top, and the lower end of which dips into a mercury cup.

current. If into a circuit a number of thin flexible wires in parallel with one another (Fig.

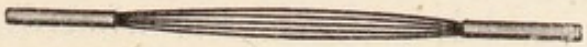


FIG. 224.—Bundle of Thin Flexible Wires.

224) are introduced, then on switching on the current they will tend to close up together.

(ii.) *Two portions of circuits crossing one another obliquely attract one another if both the currents run either towards or from the point of crossing, and repel one another if one runs to and the other from that point.*

Fig. 225 gives three cases of attraction and two of repulsion that occur in these laws.

(iii.) *When an element of a circuit exerts a force on another element of a circuit, that force always tends to*

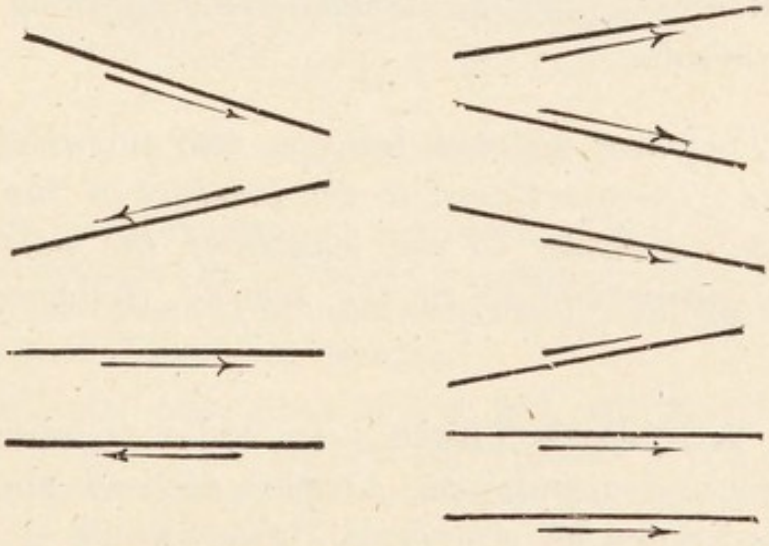


FIG. 225.—Cases of Opposing and Concurrent Currents.

urge the latter in a direction at right angles to its own direction. Thus, in the case of two parallel circuits, the force of attraction or repulsion acts at right angles to the currents themselves.

An example of laws ii. and iii. is afforded by the case

shown in Fig. 226. Here two currents *ab* and *cd* are movable round O as a centre. There will be an apparent *repulsion* between *a* and *d* and between *c* and *b*, while in the other quadrants there will be an apparent *attraction*, *a* attracting *c*, and *b* attracting *d*.

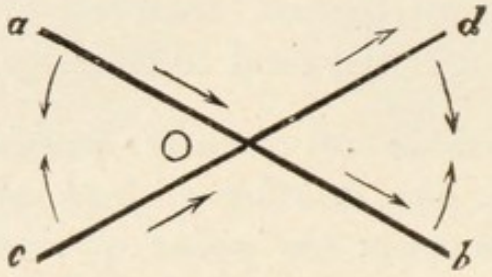


FIG. 226.—Mutual Action of Crossed Currents.

The foregoing laws may be summed up in one, by saying that two portions of circuits, however situated, set up stresses in the surrounding medium tending to set them so that their currents flow as nearly in the same path as possible.

(iv.) *The force exerted between two parallel portions of circuits is proportional to the product of the strengths of the two currents, to the length of the portions, and inversely proportional to the simple distance between them.*

422. Ampère's Table.—In order to observe these attractions and repulsions, Ampère devised the piece of apparatus known as *Ampère's Table*, shown in Fig. 227, consisting of a double supporting stand, upon which wires, shaped in different ways, can be so hung as to be capable of rotation. The ends of the suspended wires dip into two mercury cups, so as to ensure good contact, while allowing freedom to move.

By the aid of this piece of apparatus Ampère further demonstrated the following points :—

(*a*) A circuit doubled back upon itself, so that the current flows back along a path close to itself, exerts no force upon external points.

(*b*) A circuit bent into zigzags or sinuosities produces the same magnetic effects on a neighbouring piece of circuit as if it were straight.

(*c*) There is in no case any force tending to move a conductor in the direction of its own length.

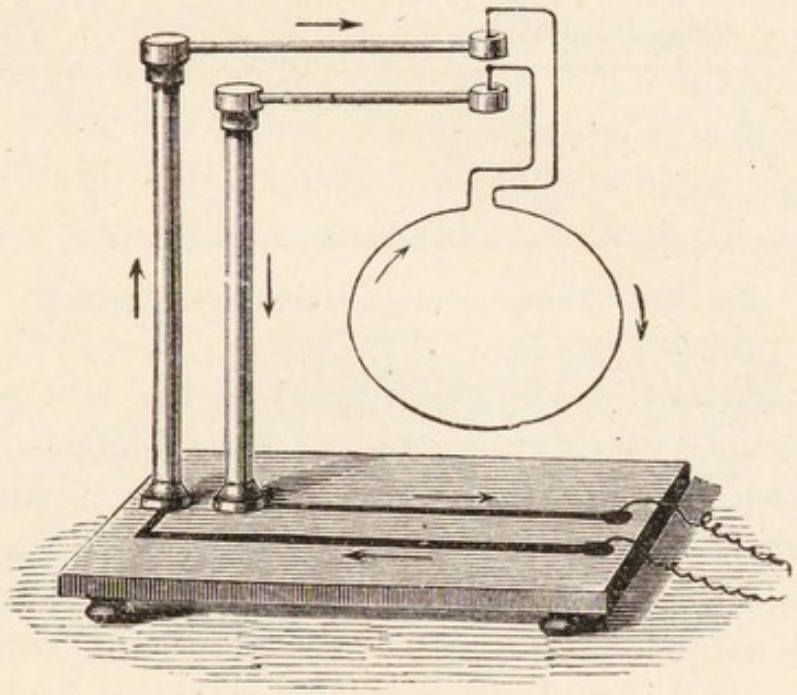


FIG. 227.—Ampère's Table.

(*d*) The force between two conductors of any form is the same whatever the linear size of the system, provided the distances be increased in the same proportion, and that the currents remain the same in strength.

The particular case, given in Fig. 228, will show the value of these experiments. Let AB and CD represent two wires carrying currents, lying neither parallel nor in the same plane. It follows from (*b*) that if we replace the portion PQ by the crooked wire PRSQ, the force will remain the same. The portion PR is drawn vertically downwards, and as it can, by (*c*), experience no force in the direction of its length, this portion will neither be attracted nor repelled by CD. In the portion RS the current runs at right angles to CD, and this portion is neither attracted nor repelled by CD. In the portion SQ the current runs parallel to CD, and in the same direction, and will therefore be attracted downwards. On the whole, therefore, PQ will be urged towards CD. The portions PR and RS will experience forces of rotation, however, P

being urged round R as a centre towards C, and R being urged horizontally round S towards C. These actions would tend to make AB parallel with CD.

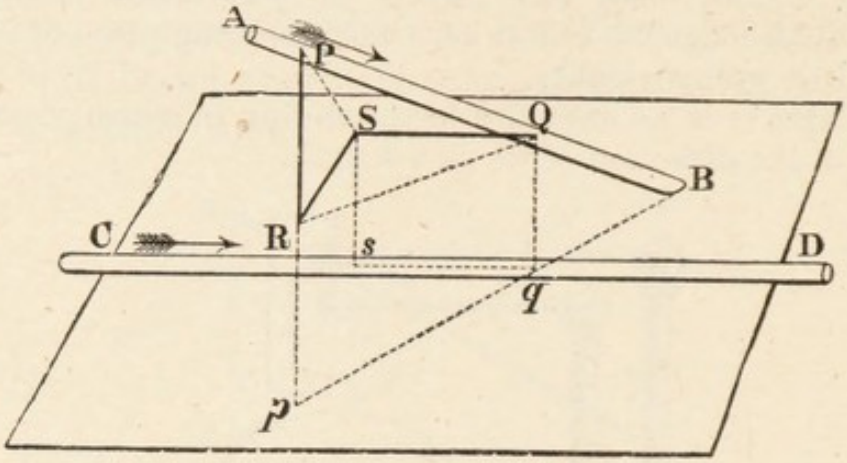


FIG. 228.—Forces between Oblique Conductors.

423. Ampère's Theory.—From the four preceding experimental data, Ampère built up an elaborate mathematical theory, assuming that, in the case of these forces acting apparently at a distance across empty space, the action took place in straight lines between two points, the total attraction being calculated as the sum of the separate attractions on all the different parts.

The briefest summary must suffice. If we deal first with two parallel elements of length dl_1 and dl_2 carrying currents $i_1 i_2$, and set at right angles to the distance r joining them, their mutual force will be

$$df = -i_1 i_2 dl_1 dl_2 / 100 r^2.$$

If, however, they are not parallel or in one plane, let ϕ be the angle they make with one another, while θ_1 and θ_2 are the angles they make with r; when

$$df = -i_1 i_2 dl_1 dl_2 (\cos \phi - \tfrac{3}{2} \cos \theta_1 \cdot \cos \theta_2) / 100 r^2.$$

By integrating this expression one obtains the forces for circuits of any given dimensions. For example, for two parallel straight conductors of lengths $l_1 l_2$, if these lengths are great compared with the distance r between them, we have

$$f = -2 i_1 i_2 l_1 l_2 / 100 r,$$

The researches of Faraday have, however, led to other views; the mutual attractions and repulsions being re-

garded as due to actions taking place in the medium which fills the space around and between the conductors. All these so-called electrodynamic actions are merely magnetic actions.

An interesting experiment, showing an apparent mutual self-repulsion between contiguous portions of the circuit, was devised by Ampère. A trough divided by a partition into two parts, and made of non-conducting materials, is filled with mercury. Upon it floats a metallic bridge formed of a bent wire, of the form shown in Fig. 229, or consisting of a glass tube filled siphonwise with mercury. When a current is sent through the

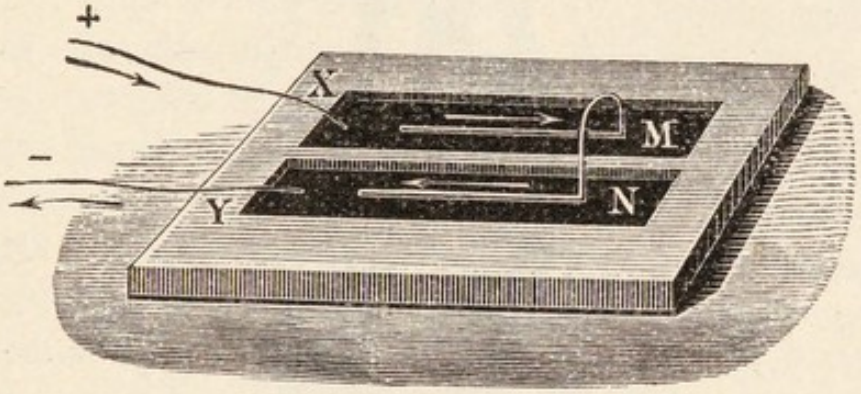


FIG. 229.—Apparent Repulsion between Contiguous Parts of a Circuit.

floating conductor from X over MN, and out at Y, the floating bridge is observed to move so as to increase the area, and therefore the magnetic flux, enclosed by the circuit. But the force would be diminished indefinitely if the two parallel parts could be made to lie quite close to one another.

424. Pinch Effect.—The whirls of magnetic field that surround (Art. 370) the conductor carrying the current tend to contract, producing resultant inward radial forces. If the conductor is a liquid, such as mercury or molten metal in a channel, these external forces tend to squeeze the liquid into a lesser cross-section. The pressure is proportional to the square of the current and inversely proportional to the cross-section. Hence,

if at any place the channel is contracted, the forces tending to pinch the conductor are greater than at the wider places, causing liquid to move away from the pinched place, which therefore is still further reduced in section, and actually parts in two. This is known as the *pinch effect.* It is a mechanical effect due to the self-induced magnetic field of the current.

425. Electrodynamometer.—Weber devised an

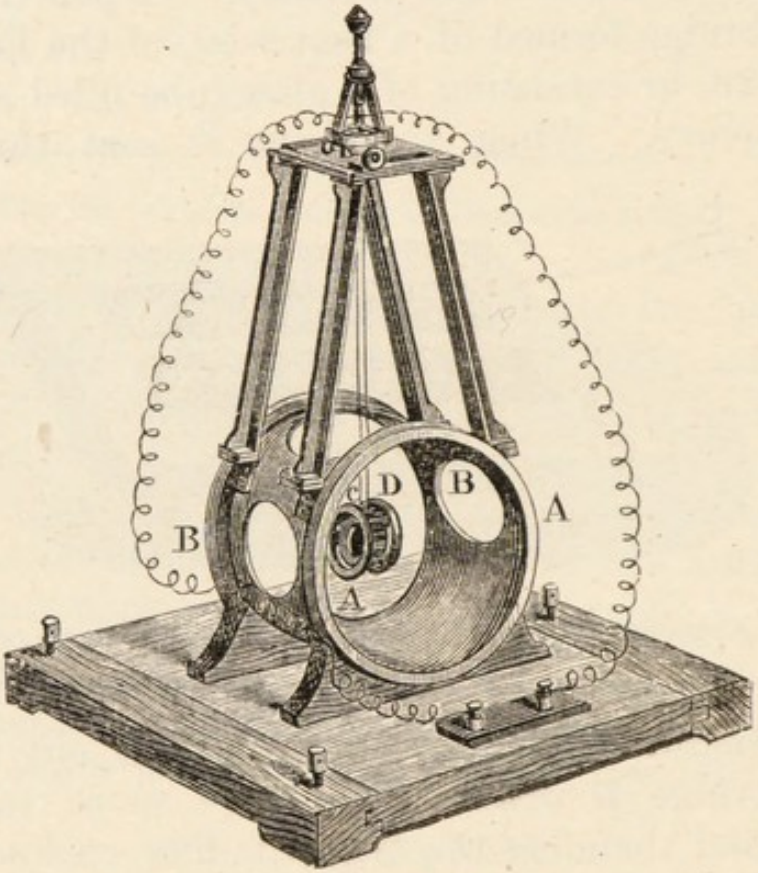


FIG. 230.—Electrodynamometer with Bifilar Suspension.

instrument known as an *electrodynamometer* for measuring the strength of currents by means of the electrodynamic action of one part of the circuit upon another part. It is a sort of galvanometer, in which, instead of a needle, there is a small coil suspended. One form of this instrument, in which both the large outer and small inner coils consist of two parallel coils of many turns, is shown in Fig. 230. The inner coil CD is suspended with its axis at right angles to that of the outer coils AA, BB, and is

supported *bifilarly* (see Art. 132) by two fine metal wires. If one current flows round *both* coils *in either direction* the inner bobbin tends to turn and set its coils parallel to the outer coils; the sine of the angle through which the suspending wires are twisted being proportional to the square of the strength of the current.

If G be the "principal constant" (Art. 226) of the large coils, and g the "moment" of the small coils (Art. 373) when carrying unit current, and $i_1 i_2$ the currents in them, the torque or turning moment will be (in dyne-centimetres),

$$T = G g i_1 i_2 / 100.$$

The chief advantage of this instrument over a galvanometer is, that it may be used for alternating currents; a current in one direction being followed by a reverse current, perhaps thousands of times in a minute. Such currents hardly affect a galvanometer needle at all; the needle simply quivers in its place without turning.

426. Siemens's Electrodynamometer. — In Siemens's dynamometer (Fig. 231), much used for measurement of strong currents, whether of the continuous or the alternating kind, one coil is fixed permanently, whilst the other coil, of one or two turns, dipping with its ends in mercury cups, is hung at right angles, and controlled by a spiral spring below a torsion-head. When current passes, the movable coil tends to turn parallel to the fixed coils, but is prevented; the torsion index being turned until the twist on the spring balances the torque. The angle through which the index has had to be turned is proportional to the product of $i_1 i_2$, the currents in the fixed and movable coils.

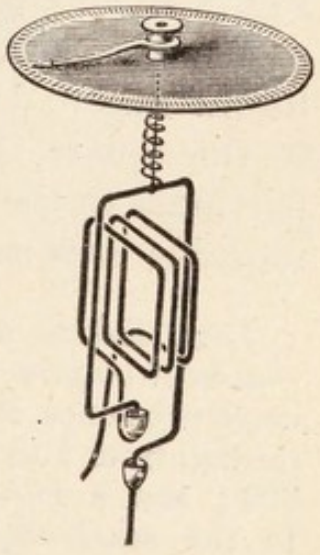


FIG. 231.—Siemens's Electrodynamometer.

For use of dynamometer as *wattmeter*, see Art. 458.

427. Kelvin's Current Balances. — Joule,

Mascart, Lord Rayleigh, and others have measured currents by balances in which gravity was opposed to the attraction or repulsion of two coils. Of such balances the most perfect are those of Lord Kelvin, the principle of which is outlined in Fig. 232. There are four fixed coils, ABCD, between which is suspended, by a flexible metal ligament of fine wires, at the ends of a light beam, a pair of movable coils, E and F. The current flows in such directions through the whole six that the beam tends to rise at F and sink at E. The beam carries a

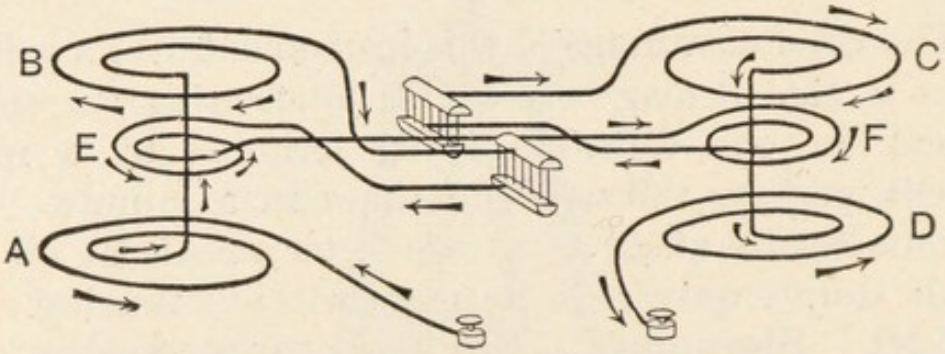


FIG. 232.—Principle of the Kelvin Current Balance.

small pan at the F end, and a light arm, not shown in Fig. 232, but shown in Fig. 233, along which, as on a steelyard, a sliding weight can be moved to balance the torque due to the current. The current is proportional to the square root of this torque, since the force is proportional to the product of the current in the fixed and movable coils as in all electrodynamometers.

Lord Kelvin designed a whole range[1] of these instruments: —a *centi-ampere* balance reading from 0·01 to 1 ampere; a *deci-ampere* balance reading from 0·1 to 10; a *deka-ampere* balance reading from 1 to 100; a *hekto-ampere* balance reading from 6 to 600; and a *kilo-ampere* balance reading up to 2500 amperes. In the *centi-ampere* balance, shown in Fig. 233, the sliding weight is carried on the base of the pointer (shown white), and when at the zero of the scale just balances the weight in the

[1] For a fuller account of these Current Balances, and of the Wattmeters on the same principle, see Gray's *Absolute Measurements in Electricity and Magnetism*, from which Fig. 233 is taken.

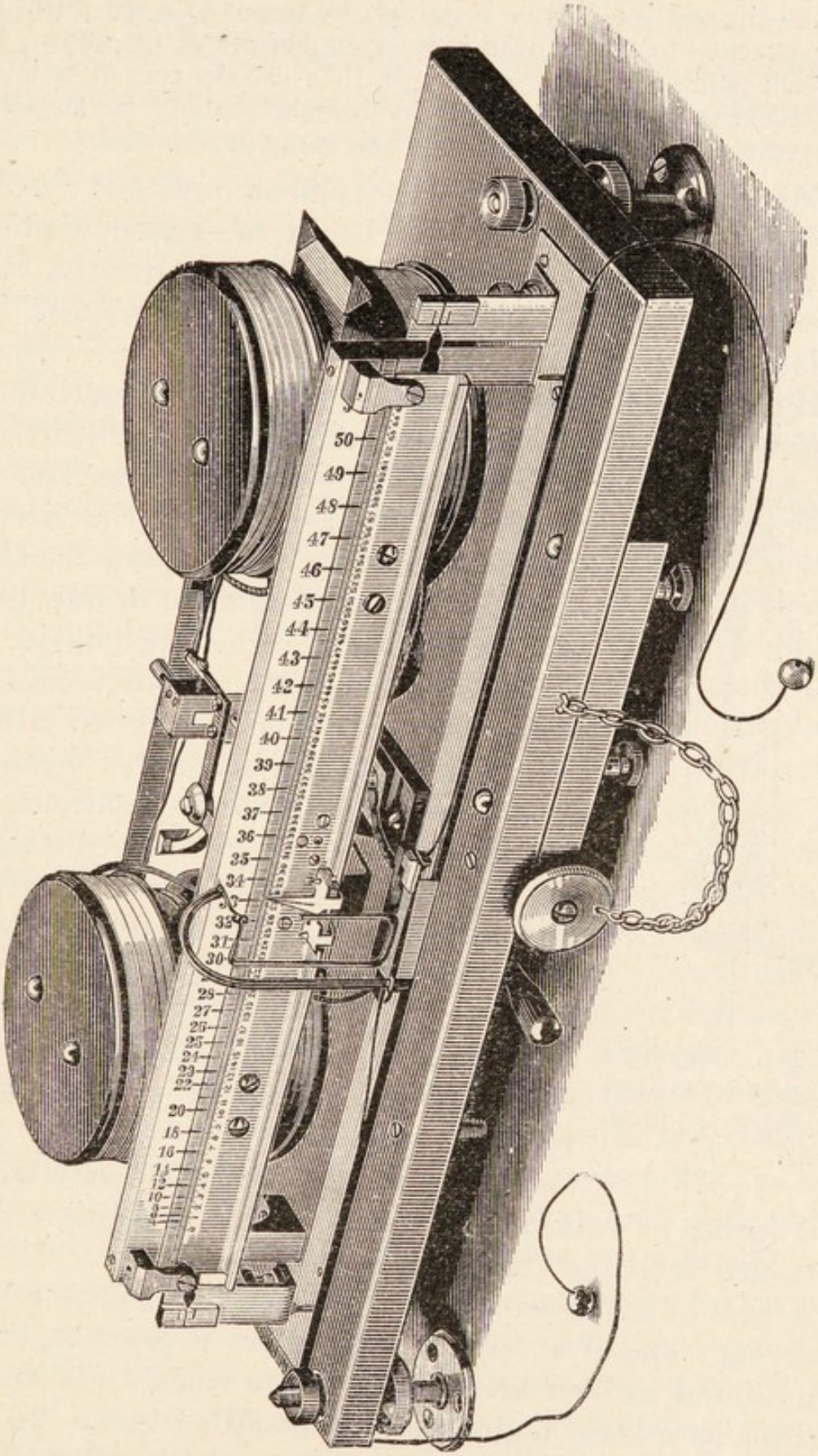


FIG. 233.—Lord Kelvin's Centi-ampere Balance.

V-shaped pan. Any current passing through the coils causes the beam to tilt and the pointer is moved (by means of a self-releasing slider attached to cords) until it is again horizontal (as shown by the black pointer at either end). With a certain pair of weights the fixed scale gives the current in decimal parts of an ampere; but by the use of other weights a wider range is obtained.

The "ampere-standard" instrument, and the "volt-standard" instruments of the Board of Trade, kept at Whitehall as legal standards for Great Britain, are current balances of special construction, designed by the late Major Cardew.

428. Electromagnetic Rotations.—Continuous rotation can be produced between a magnet and a circuit, or between two parts of one circuit, provided that one part of the circuit can move while another part remains fixed, or that the current in one part can be reversed. The latter device is adopted in the construction of *electric motors* (Art. 516). The former alternative is applied in some historic apparatus for showing rotations, a sliding-contact being made between one part of the circuit and another. The earliest form of rotation-apparatus was devised by Faraday in 1822. It is shown in Fig. 234, in which a wire carrying a current is jointed at the top and dips into a cup of mercury surrounding the pole of a magnet. On switching on the current the wire at once begins to walk round the pole with a motion that continues until the current is switched off.

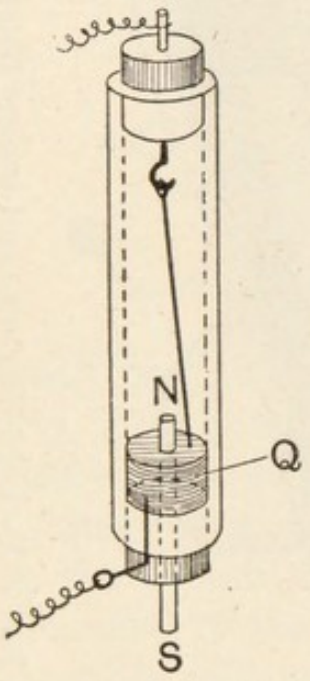


FIG. 234.—Faraday's Apparatus for Electromagnetic Rotations.

A pole of a magnet can also be made to rotate round a current; and if a vertical magnet be pivoted so as to turn around its own axis it will rotate when a current is led into its middle region and out at either end. If the current is led in at one end and out at the other there

will be no rotation, since the two poles would thus be urged to rotate in opposite ways. Liquid conductors too can exhibit electromagnetic rotations. Let a cylindrical metallic vessel connected to one pole of a battery be filled with mercury or dilute acid, and let a wire from the other pole dip into its middle, so that a current may flow radially from the centre to the circumference or *vice versa*; then, if this be placed upon the pole of a powerful magnet, or if a magnet be held vertically over it, the liquid may be seen to rotate.

429. Electromagnetic Actions of Convexion Currents.—According to Faraday a stream of particles charged with electricity acts magnetically like a true conduction current. This was first proved in 1876 by Rowland, who found a rapidly rotated charged disk to act upon a magnet as a feeble circular current would do. If a number of charges, each of equal value, follow one another, so that there are q units per centimetre along the procession, and the procession travels with a velocity of v centimetres per second, the effect will be the same as a current of the value qv. Convexion currents, consisting of streams of electrified particles, are also acted upon by magnets. The convective discharges in vacuum-tubes (Art. 342) can be drawn aside by a magnet, or caused to rotate around a magnet-pole. The brush discharge (Art. 340) when taking place in a strong magnetic field is twisted. The electric arc (Art. 486) also behaves like a flexible conductor, and can be attracted or repelled laterally by a magnet-pole. Two stationary positively-electrified particles repel one another, but two parallel currents attract one another (Art. 421), and if electrified particles flowing along act like currents, there should be an (electromagnetic) attraction between two electrified particles moving along side by side through space. According to Maxwell's theory (Art. 609) the electrostatic repulsion will be just equal to the electromagnetic attraction when the particles move with a velocity equal to the velocity of light

Hall discovered in 1879 that when a powerful magnet is made to act upon a current flowing along in a strip of very thin metal, the equipotential lines are no longer at right angles to the lines of flow of the current in the strip. This action appears to be connected with the magnetic rotation of polarized light (Art. 613), the coefficient of this tranverse thrust of the magnetic field on the current being feebly + in gold, strongly + in bismuth, and – in iron, and immensely strong negatively in tellurium. It was shown by the author, and about the same time by Righi, that those metals which manifest the Hall effect undergo a change in their electric resistance when placed in the magnetic field. The resistance of bismuth increases so greatly that it affords a way of measuring the strength of magnetic fields (Art. 364).

430. Ampère's Theory of Magnetism.—Ampère, finding that solenoids (such as Fig. 218) act precisely as magnets, conceived that all magnets are simply collections of currents, or that around every individual molecule of a magnet an electric current is ceaselessly circulating. We know that such currents could not flow perpetually if there were any resistance to them, and we know that there is resistance when electricity flows from one molecule to another. As we know little about the interior of molecules themselves, we cannot assert that Ampère's supposition is impossible. Since a whirlpool of electricity acts like a magnet, there seems indeed reason to think that magnetic molecules may be merely made up of rotating portions of electrified matter, or of electrons in circulation. See Art. 637.

CHAPTER VI

MEASUREMENT OF CURRENTS, ETC.

LESSON XXXIII.—*Ohm's Law and its Consequences*

431. Law of Dr. Ohm.—Every conductor and every circuit offers a certain resistance to the flow of electricity through it. When an electromotive-force is applied to a circuit it causes a current to flow in the circuit, but the strength of the resulting current depends not only on the amount of the electromotive-force but on the resistance of the circuit. In Art. 206 the law discovered by Dr. G. S. Ohm was stated in the following terms:—*The strength of the current varies directly as the electromotive-force, and inversely as the resistance of the circuit.*

Using the units adopted by practical electricians, and explained in Art. 381, we may now restate Ohm's law in the following definite manner:—*The number of amperes of current flowing through a circuit is equal to the number of volts of electromotive-force divided by the number of ohms of resistance. Or,*

$$\text{amperes} = \text{volts} \div \text{ohms},$$

$$i = \mathrm{E}/\mathrm{R}.$$

Example.—Let an electromotive-force of 100 *volts* be applied to a circuit, the resistance of which is 4 *ohms*; the resulting current will be $100 \div 4$, that is 25 *amperes*.

Transforming the equation we may also write Ohm's law in the following fashion—

$$E = i \times R;$$

or, the number of volts needed to send a prescribed current i through a circuit, the resistance of which is known to be R, is found by multiplying together i and R.

Example.—How many *volts* are required to send a current of 12 *amperes* through a resistance of 9 *ohms*?
Answer.—$12 \times 9 = 108$ *volts.*

A third possible form of Ohm's law is—

$$E/i = R.$$

Example.—If an electromotive-force of 100 *volts* sends a current of 0·5 *amperes* through a glow-lamp, what is the resistance of that lamp?
Answer.—$100 \div 0{\cdot}5 = 200$ *ohms.*

The law in its application is not always quite so simple. If we apply it to a whole circuit we must consider both the total E and the total R. For if a number of cells are used and the circuit be made up of a number of different parts through all of which the current must flow, we have to take into account not only the electromotive-forces of the cells, but their resistances, as well as the resistances of other parts of the circuit. For example, the current may flow from the zinc plate of the first cell through the liquid to the carbon plate, then through a connecting wire or screw to the next cell, through its liquid, through the connecting screws and liquids of the rest of the cells, then through a wire to a galvanometer, then through the coils of the galvanometer, then perhaps through an electrolytic cell, and finally through a return wire to the zinc pole of the battery. In this case there are a number of separate electromotive-forces all tending to produce a flow, and a number of different resistances, each obstructing the flow and adding to the total resistance. If in such a case we knew the separate values of all the different electromotive-

forces and all the different resistances that are in series we could calculate what the current would be, for it would have the value—

$$i = \frac{e' + e'' + e''' + e^{iv} + \ldots\ldots}{r' + r'' + r''' + r^{iv} + \ldots\ldots}$$

$$i = \frac{\text{Total electromotive-force}}{\text{Total resistance}}.$$

Example.—Let there be 5 cells in series each having $e = 1{\cdot}4$ volts, and each an internal $r = 0{\cdot}4$ ohm; and let the external part of circuit have resistance 3 ohms. Total $E = 7$ volts; total $R = 5$ ohms. Current i will be $1\frac{2}{5}$ amperes.

If any one of the cells were set wrong way round its electromotive-force would oppose that of the other cells; an opposing electromotive-force must therefore be subtracted, or reckoned as negative in the algebraic sum. The "polarization" (Arts. 183 and 566) which occurs in battery cells and in electrolytic cells after working for some time is an opposing electromotive-force, and diminishes the total of the electromotive-forces in the circuit. So, also, the induced back E.M.F. which is set up when a current from a battery drives an electric motor (Art. 455) reduces the strength of the working current; in such case, if E is the electromotive-force of the battery, e the opposing electromotive-force, and R the total resistance, we shall have

$$i = \frac{E - e}{R}.$$

Example.—Suppose the battery to generate current at 25 volts, and the motor to generate a back electromotive-force of 20 volts, and the total resistance to be $2\frac{1}{2}$ ohms, there will be a current of 2 amperes.

But we may apply Ohm's law to a *part* of a circuit. If e represents the difference of potential between two ends of a conductor of resistance r, the current i in it must be $= e/r$. Or, to put it the other way round, the

electromotive-force needed to drive i amperes through a resistance of r ohms will be $e = ri$ volts.

Consider the case of a circuit of which the resistance is made up of two parts, an external resistance R consisting of wires, lamps, etc., and of a smaller resistance r internal to the battery or dynamo (viz. the resistance of the liquids in the cells, or of the wire of the armature). Then if E is the whole electromotive-force we shall have as current

$$i = \frac{E}{R + r},$$

or $$i(R + r) = E;$$

or again $$iR + ir = E.$$

This means in words that the total volts may be considered as being employed partly in driving the current through the external resistance R, partly in driving the current through the internal resistance r. This latter part of the electromotive-force is called the *lost volts*; the remainder being the useful or externally available volts, that would be measurable by a voltmeter (Art. 237). set across the terminals. If we call the available volts V we may write $V = iR$, whence

$$V = E - ir;$$

or in words: the volts as measured at the terminals of a cell or dynamo are less than the whole E.M.F. generated therein; being equal to the whole E.M.F. less the lost volts. The lost volts being proportional to internal resistance it is obviously best to keep all internal resistances as low as possible. Only when the cell is giving no current are the external volts V equal to the whole E.M.F.; for when $i = o$, ir is also $= o$.

Example.—A dynamo is designed to generate its currents with an electromotive-force of 105 volts. The internal resistance of its armature is $\frac{1}{30}$ ohm. When it is giving out current of 120 amperes, the lost volts will be $120 \times \frac{1}{30} = 4$ volts. Consequently the volts available in the external circuit will be only 101.

Since $i = \frac{E}{R+r} = \frac{V}{R}$ it follows also that $V = E\frac{R}{R+r}$.

432. Resistance.—Resistance is the name given to that property of materials by virtue of which they obstruct the steady flow of electricity through them, and fritter down into heat the energy of the current. The resistance of any conductor or circuit is measured by the ratio between the volts applied to its terminals and the amperes which result therefrom. It is found that the resistance of a metal wire, if kept at an unvarying temperature, is the same whether a large current or a small current be flowing through it. For example, if a wire has a resistance such that when a difference of potential of 10 volts is applied to its ends a current of 2 amperes flows through it (its resistance being 5 ohms), it will be found that if 1 volt is applied the current will be 0·2 amperes, the ratio between volts and amperes being 5 as before, provided the temperature is kept the same. Resistance of a given conductor is in fact constant so long as its physical properties are unaltered. In certain non-metallic conductors, as for example the arc (Art. 486), resistance is not a constant but alters with the strength of the current that is being used.

The unit of resistance, or *ohm*, is a standard chosen in order that the resistances of other conductors may be expressed in definite numbers. The definition of it is given in Art. 381. It is convenient to remember that 100 yards of ordinary iron telegraph-wire has roughly a resistance about 1 ohm. Or, again, a thin copper wire 1 inch long and $\frac{1}{1000}$ inch in diameter has a resistance of almost exactly 1 ohm at 65° C.

A resistance of a very great number of ohms is called a *high* resistance, and one which is only a few ohms or a fraction of an ohm is called a *low* resistance. A resistance of one million ohms is called a *megohm*: a resistance of one millionth of one ohm is called a *microhm*.

Resistances in a circuit may be of two kinds—*first*, the resistances of the conductors (metals, alloys, liquids)

themselves; *second*, the resistances due to *imperfect contact* at points. The latter kind of resistance is affected by pressure, for when the surfaces of two conductors are brought into more intimate contact with one another, the current passes more freely from one conductor to the other. The contact-resistance of two copper conductors may vary from infinity down to a small fraction of an ohm, according to the pressure. The variation of resistance at a point of imperfect contact is utilized in telephone transmitters (Art. 594). The conduction of *powdered metals* is remarkable. A loose heap of filings scarcely conducts at all, owing to the want of cohesion, or to the existence of films of air or dust. But, as discovered independently by Calzecchi-Onesti and Branly, it becomes instantly a good conductor if an electric spark is allowed to occur anywhere within a few yards of it (see Arts. 606 and 626). The resisting films of air are broken down by minute internal discharges in the mass. A very slight agitation by tapping at once makes the powder non-conductive. The resistance of a wire is the same whether the current in it is flowing in either direction. There are certain crystalline substances such as galena and carborundum which appear to possess unilateral conductivity, that is, they conduct better in one direction than in the opposite. They can be used as *electric valves* (see Art. 634).

For the purpose of regulating the flow of currents, and for electrical measurements (Art. 443), *variable resistances* are employed. *Resistance coils* (Art. 446) are sets of coils made each of a definite value in ohms, of which one or more can be inserted in the circuit at will. *Rheostats* consist of easily-adjustable resistances, the length of wire in circuit being varied by turning a handle, or moving a sliding contact. In some cases the rheostat wire is wound off and on to a roller. In others a handle (Fig. 235) moving over a number of metal studs varies the amount of resistance-wire through which the current

must flow. Carbon rheostats consist of a number of little plates of hard carbon, about 3 inches square, arranged in a pile, with a screw to reduce their resistance by squeezing them together into better contact. Fig. 236 shows a very convenient laboratory rheostat having a resistance wire of constantan alloy (Art. 436) wound non-inductively (Art.

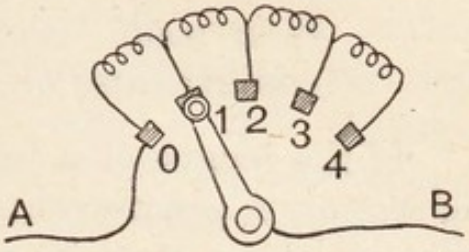


FIG. 235.—A Simple Rheostat.

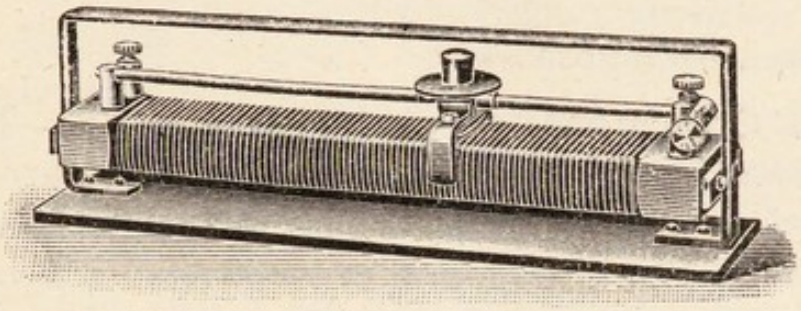


FIG. 236.—Sliding Contact Rheostat

446) upon a slate block, and provided with a sliding contact to bring into circuit more or less of the wire.

433. Laws of Resistance.—The following are the laws of the resistance of conductors :—

(i.) *The resistance of a conducting wire is proportional to its length.* If the resistance of a mile of iron telegraph-wire be 17 ohms, that of 50 miles will be $50 \times 17 = 850$ ohms.

(ii.) *The resistance of a conducting wire is inversely proportional to the area of its cross-section,* and therefore in the usual round wires *is inversely proportional to the square of its diameter.* Ordinary telegraph-wire is about $\frac{1}{6}$ of an inch thick ; a wire twice as thick would conduct four times as well, having four times the area of cross-section ; hence an equal length of it would have only $\frac{1}{4}$ the resistance.

(iii.) *The resistance of a conducting wire of given length and thickness depends upon* the material of which it is made—that is to say, upon *the* **specific resistance,** or **resistivity,** *of the material.*

If the length of a wire be l centimetres, and its area of section A square centimetres, and the resistivity of the material be ρ, then its resistance R will be

$$R = l\rho/A.$$

Example.—Find the resistance of a platinoid wire of section 0·004 sq. cm., and 200 cm. long; for platinoid the resistivity $\rho = 32{\cdot}5 \times 10^{-6}$.

Answer.—R = 1·625 *ohms.*

434. Conductance and Resistance.—The term *conductance* is used as the inverse of resistance; a conductor whose resistance is r ohms is said to have a conductance of $1/r$. The unit of conductance is called the *siemens* (formerly called "*mho*"). When a number of conductors are *in parallel* with one another their united conductance is the sum of their separate conductances.

The conductance of a prism of which the length is 1 cm. and the section is 1 sq. cm., is called its *conductivity* or *specific conductance.*

The resistance of a prism of length 1 cm. and section 1 sq. cm. is sometimes called its *resistivity* or *specific resistance.*

435. Resistivity.—The resistivity of a substance is most conveniently stated as the resistance (in millionths of an ohm) of a centimetre cube of the substance. The Table on p. 434 also gives the relative conductance when that of copper is taken as 100.

Weight for weight, aluminium is a better conductor than silver, and nearly twice as good as copper.

It is found that those substances that possess a high conducting power for heat are also the best conductors of electricity, but the ratio of these conductivities is not constant; it varies as the absolute temperature.

Liquids fall under three heads: (1) molten metals and alloys, which conduct simply as metals without undergoing any decomposition or chemical change; (2) fused salts and solutions of salts and acids, which undergo chemical decomposition, and conduct only *by electrolysis* (Art. 252), such liquids are called *electrolytes*; (3) insulators, such as the oils, turpentine, etc., and bromine. Liquid electrolytes are worse conductors than metals; gases, including steam, are perfect non-conductors, except when ionized; that is, when so dissociated as to admit of discharge by convexion through them (Art. 332).

436. Effects of Heat on Resistance.—Changes of temperature affect temporarily the conducting power of metals. Nearly all the pure metals increase their resistance about 0·4 per cent for a rise of 1° C. in temperature, or about 40 per cent when warmed 100°. When cooled in liquid air the resistance is found to fall greatly. A copper wire which at 0° had a resistance of 17·5 ohms fell to 1·65 ohms at −201° C. Dewar and Fleming find all pure metals to lower their resistance as though at −273° C. (absolute zero of temperature) they would become perfect conductors. Kamerlingh-Onnes finds that at the temperature of liquid helium (−269° C.) the metals tin and lead lose all appreciable resistance and become *super-conductors*. The very small residual resistance at this temperature was found to be 2×10^{10} times smaller than at the ordinary temperature; so that a current induced in a closed coil of lead wire persisted for some hours with only a small diminution of strength. But this current was instantaneously destroyed on lifting the coil out of the helium. The resistance of carbon, unlike that of the metals, diminishes on heating. The filament of a carbon glow-lamp, which when cold was 230 ohms, was only 150 when white hot. German-silver and other alloys do not show so much change, hence they are used in making standard resistance coils. The temperature-coefficient of German-silver is only 0·00044 for 1° C., or

TABLE OF RESISTIVITY

Substance.	Resistivity (microhms of 1 cm. cube).	Metres per ohm, if of 1 sq. mm. Section.	Relative Conductance.
Metals at 0° C.			
Copper (annealed)	1·570	63·70	100
,, (hard)	1·603	62·38	98·1
Silver (annealed)	1·492	67·03	105
,, (hard)	1·620	61·73	98
Gold	2·077	48·15	76
Aluminium (annealed)	2·889	34·61	54
Platinum	8·982	11·13	17
Iron (pure)	9·638	10·37	16
Iron (telegraph-wire)	15	6·66	10
Lead	19·63	5·09	8·3
Mercury	94·34	1·06	1·6
Selenium	6×10^{10}		
Carbon (graphite)	2400 to 42,000		
,, (arc light)	about 4000		
Alloys.			
German-silver (Cu 60, Zn 26, Ni 14)	20·76	4·22	7·6
Platinum-silver (Pt 67, Ag 33)	2·4	41·66	6·5
Platinoid (Cu 59, Zn 25·5, Ni 14, W 1·5)	32·5	3·08	4·8
Manganin (Cu 84, Ni 12, Mn 3·5)	47·5	2·10	3·3
Constantan (Eureka) (Cu 60, Ni 40)	50	2	3·1
Liquids at 18° C.			
Pure Water	$26{\cdot}5 \times 10^8$		
Dilute H_2SO_4, 5%	486×10^4		less than one millionth part
,, H_2SO_4, 30%	137×10^4		
,, H_2SO_4, 80%	918×10^4		
,, $ZnSO_4$, 24%	214×10^5		
,, HNO_3, 30%	129×10^4		
Insulators.			
Glass at 20° C.	91×10^{18}		
Glass at 200° C.	$22{\cdot}7 \times 10^{12}$		less than one billionth
Guttapercha 24° C.	$4{\cdot}5 \times 10^{20}$		

$\frac{1}{10}$ that of the pure metals. Platinoid and platinum-silver have about 0·00011 for their coefficient. Other alloys, such as manganin, constantan ("Eureka"), have a temperature-coefficient which is practically zero. Iron is remarkable in that its temperature-coefficient which is about 0·0005 at ordinary temperatures suddenly increases to about three times that value when the temperature rises to about 855° (or 710° for steel). This great increase of resistivity makes it useful as the material for a ballasting resistance (Art. 485). Those liquids which only conduct by being electrolyzed (Art. 250) conduct better as the temperature rises. The property of changing resistance with temperature is now used for measuring furnace temperatures in Callendar's platinum *pyrometer*. The *bolometer* used by Langley in researches on radiant heat depends on the same property. It consists of a strip or grid of platinum wire blackened on one edge so as to absorb the radiation; the resulting increase in the resistance of the wire being measured by a Wheatstone's Bridge (Art. 445). Some substances show an increase of resistivity, iron slightly, bismuth considerably, when placed in a magnetic field. The effect of *light* in varying the resistance of selenium is stated in Art. 617.

437. Insulators.—The name *insulators* is given to materials which have such high resistances that they can be used as non-conductors. They differ much in their mechanical qualities as well as in their insulation-resistance. They may be classed under several heads: (1) *Vitreous*, including glass of all kinds, slags, and quartz; (2) *Stony*, including slate, marble, stoneware, steatite, porcelain, mica, asbestos; (3) *Resinous*, including shellac, resin, beeswax, pitch, various gums, bitumen, ozokerit, and amber; (4) *Elastic*, including india-rubber, gutta-percha, ebonite; (5) *Oily*, including various oils and fats of animal and vegetable origin, as well as solid paraffin and petroleum oil; (6) *Cellulose*, including dry

wood and paper, and preparations of paper, such as "fibre" and celluloid. All these materials decrease their resistance enormously as the temperature rises, and in general become fairly good conductors as soon as any chemical change begins; some of them (as glass) conduct as electrolytes as soon as they soften. Micanite is a name given to flaked mica cemented together by shellac under pressure while warm. The resistance of insulators is not independent of the voltage. For example, Evershed observed that when tested at 50 volts the resistance of the insulating cotton covering between certain copper wires, after being dried for two hours at 150° C., was 25 megohms, but was only 9 megohms when tested at 500 volts. Moisture is largely responsible for these variations of insulation resistance.

The name *insulators* is also given to the articles used for the insulating supports of stoneware, porcelain, or glass on which telegraph wires are carried (Art. 580).

438. Typical Circuit.—Let us consider the typical case of the circuit shown in Fig. 237, in which a battery, ZC, is joined up in circuit with a galvanometer by means of wires whose resistance is R. The total electromotive-force of the battery we will call E, and the total internal resistance of the liquids in the cells r. The resistance of the galvanometer coils may be called G. Then, by Ohm's law:—

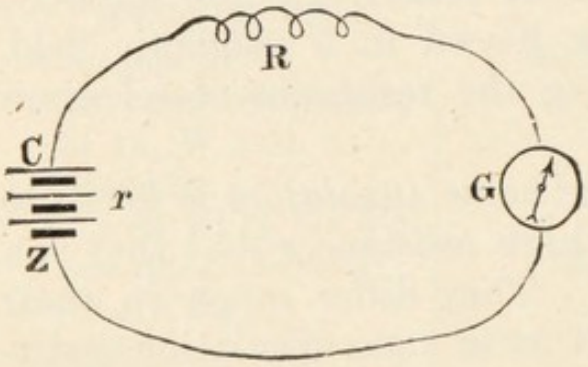


FIG. 237.

$$i = \frac{E}{R + r + G}.$$

The *internal resistance* r of the liquids of the battery bears an important relation to the *external resistance* of the circuit (including R and G), for on this relation depends the best way of arranging the battery cells.

Suppose, for example, that we have a battery of 50 small Daniell's cells at our disposal, of which we may reckon the electromotive-force as one volt (or, more accurately, 1·07 volt) each, and each having an internal resistance of two ohms. If we have to use these cells on a circuit where there is already of necessity a high resistance, we should couple them up "in series" rather than in parallel. For, supposing we have to send our current through a telegraph line 100 miles long, the external resistance R will be (reckoning 13 ohms to the mile of wire) at least 1300 ohms. Through this resistance a single such cell would give a current of less than one milli-ampere, for here $E = 1$, $R = 1300$, $r = 2$, and therefore $i = \frac{E}{R+r} = \frac{1}{1300+2} = \frac{1}{1302}$ of an ampere, a current too weak to work an ordinary telegraph instrument.

With fifty such cells in series we should have $E = 50$, $r = 100$, and then

$i = \frac{50}{1300+100} = \frac{50}{1400} = \frac{1}{28}$ of an ampere, or over 35 milli-amperes. In telegraph work, where the instruments require a current of 5 to 10 milli-amperes to work them, it is usual to reckon an additional Daniell's cell for every 5 miles of line, each instrument in the circuit being counted as having as great a resistance as 10 miles of wire.

If, however, the resistance of the external circuit be small, such arrangements must be made as will keep the total internal resistance of the battery small. Suppose, for example, we wish merely to heat a small piece of platinum wire to redness, using stout copper wires to connect it with the battery. Here the external resistance may possibly not be as much as 1 ohm. In that case a single cell would give a current of $\frac{1}{3}$ of an ampere (or 333 milli-amperes) through the wire, for here $E = 1$, $R = 1$, and $r = 2$. But 10 cells would only give half as much again, or 476 milli-amperes, and fifty cells only

495 milli-amperes, and with an infinite number of such cells *in series* the current could not possibly be more than 500 milli-amperes, because every cell, though it adds 1 to E, adds 2 to R. It is clear then that though linking many cells *in series* is of advantage where there is the resistance of a long line of wire to be overcome, yet where the external resistance is small the practical advantage of adding cells in series soon reaches a limit.

But suppose in this second case, where the external resistance of the circuit is small, we reduce also the internal resistance of our battery by linking cells together *in parallel*, joining several zincs of several cells together, and joining also their copper poles together (as suggested in Art. 207), a different and better result is attained. Suppose we thus join up four cells. Their electromotive-force will be no more, it is true, than that of one cell, but their resistance will be but $\frac{1}{4}$ of one such cell, or $\frac{1}{2}$ an ohm. These four cells would give a current of 666 milli-amperes through an external resistance of 1 ohm, for if E = 1, R = 1, and the internal resistance be $\frac{1}{4}$ of r, or $= \frac{1}{2}$, then

$i = \frac{\mathrm{E}}{\mathrm{R}+r} = \frac{2}{3}$ of an ampere, or 666 milli-amperes.

If we arrange the cells of a battery in p files in parallel, having s cells in series in each file (there being $p \times s = \mathrm{N}$ similar cells altogether), the electromotive-force of each file will be s times the electromotive-force E of each cell, or $s\mathrm{E}$; and the resistance of each file will be s times the resistance r of each cell, or sr. But there being p files in parallel the whole internal resistance will be only $\frac{1}{p}$ of the resistance of any one file, or will be $\frac{s}{p}r$, hence, by Ohm's law, such a battery would give as its current

$$i = \frac{s\mathrm{E}}{\frac{s}{p}r + \mathrm{R}}.$$

439. Best Groupings of Cells.—If the question

arises as to the best way of grouping a given number of cells, it must be replied that there are several best ways.

(1) *Grouping for best Economy.*—So group the cells that their united internal resistance shall be *very small* compared with the external resistance. In this case the materials of the battery will be consumed slowly, and the current will not be drawn off at its greatest possible strength; but there will be a minimum waste of energy (Art. 454).

(2) *Grouping for greatest Current.*—It can be shown mathematically that, for a given battery of cells, the way of grouping them that will give the largest steady current when they are required to work through a given external resistance X, is so to choose s and p, that *the internal resistance* $\left(\frac{s}{p}r\right)$ *shall equal the external resistance.* This can be done by choosing p such that $p = \sqrt{Nr} \div X$; for then the resistance R of the whole battery *as so arranged*, will be $Nr \div p^2$, which equals X. The student should verify this rule by taking examples and working them out for different groupings of the cells. Although this arrangement gives the *largest current* it is not the most economical; for if the internal and external resistances be equal to one another, the useful work in the outer circuit and the useless work done in heating the cells will be equal also, half the energy being wasted.

(3) *Grouping for quickest Action.*—If there are electromagnets, or other objects possessing self-induction (Art. 501) in the circuit, which would tend to prevent the current rising quickly to its proper value, the best grouping to cause the current to rise as quickly as possible is one that will make the internal resistance higher than the external, namely, put all the cells in series (see Art. 504).

440. Long and Short Coil Instruments.—The student will also now have no difficulty in perceiving why a "long-coil" galvanometer, or a "long-coil" electromagnet, or instrument of any kind in which the conductor

is a long thin wire of high resistance, must not be employed on circuits where both R and r are already small. He will also understand why, on circuits of great length, or where there is of necessity a high resistance and where therefore a battery of great electromotive-force is employed, "short-coil" instruments are of little service, for though they add little to the resistances, their few turns of wire are not enough to produce the required action with the small currents that circulate in high-resistance circuits. He will understand, too, why "long-coil" instruments are here appropriate as multiplying the effects of the currents by their many turns, their resistance, though perhaps large, not being a serious addition to the existing resistances of the circuit. The main point to grasp is that it is *the nature of the line*, whether of high resistance or low, which determines not only the grouping of the battery, but also what kind of winding, whether many turns of thin wire or a few turns of thick, is appropriate in the instruments.

441. Divided Circuits.—If a circuit divides, as in Fig. 238, into two branches at A, uniting together again at B, the current will also be divided, part flowing through one branch, part through the other. Any branch which serves as a by-pass to another branch is termed a *shunt*. *The relative strengths of current in the two branches* will be proportional to their conductances, *i.e. inversely proportional to their resistances.*[1] Thus, if r be a wire of 2 ohms resistance and r' be 3 ohms, then current in

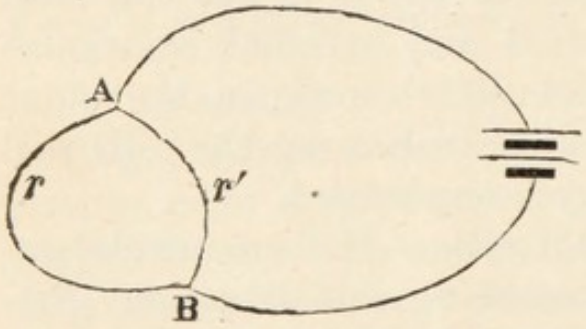


FIG. 238.—A Divided Circuit.

[1] There is a popular fallacy that an electric current "always takes the line of least resistance." It never does, though *part* of the current may flow that way. It divides between the various paths in proportion to their easiness. It is only spark discharges which pierce a non-conductor that can be said to take the line of least resistance.

r is to the current in r' as r' is to r; or as 3 to 2. Hence $\frac{3}{5}$ of the whole current will flow through r, and $\frac{2}{5}$ of the whole current through r'.

The *joint resistance* of the divided circuit between A and B will be **less** than the resistance of either branch singly, because the current has now two paths. In fact, the joint conductance will be the sum of the two separate conductances. And if we call the joint resistance R, it follows that

$$\frac{1}{R} = \frac{1}{r} + \frac{1}{r'} = \frac{r' + r}{rr'},$$

whence $R = \frac{rr'}{r' + r}$, or, in words, *the joint resistance of a divided conductor is equal to the product of the two separate resistances divided by their sum.* This is sometimes called *the law of shunts*, because each of the branches may be regarded as a shunt to the other. A simple construction for finding the value graphically is given in Fig. 239. Let lines representing the two resistances r and

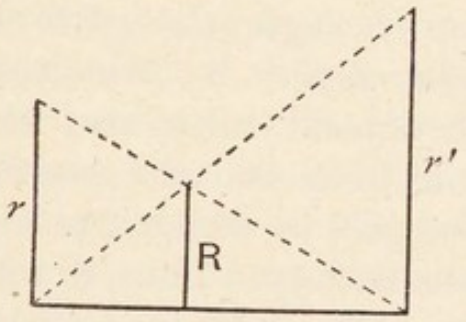


FIG. 239.

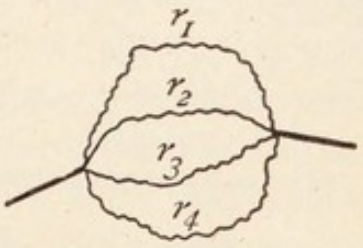


FIG. 240.

r' be erected at the ends of any base line, and the diagonals drawn as shown. The perpendicular at the point of their intersection will be the joint resistance R.

In case there are three or more branches all in parallel, as in Fig. 240, the rule may be generalized as follows:— *The joint resistance of any number of conductors in parallel is the reciprocal of the sum of the reciprocals of the separate resistances.*

Kirchhoff formulated the following important laws, both of them deducible from Ohm's law :—

(i.) *In any branching network of wires the algebraic sum of the currents in all the wires that meet in any point is zero.*

(ii.) *When there are several electromotive-forces acting at different points of a circuit, the total electromotive-force round the circuit is equal to the sum of the resistances of its separate parts multiplied each into the strength of the current that flows through it.*

442. Current Sheets.—When a current enters a wide conductor it never takes the line of least resistance ; instead of flowing in one line it spreads out and flows through the mass of the conductor. When a current is led into a thin plate of conducting matter it spreads out into a *current sheet* and flows through the plate by *stream-lines* in directions that depend upon the form of the plate and the position of the pole by which it returns to the battery. Thus, if wires from the two poles of a battery are brought into contact with two neighbouring points A and B at the edges of a flat sheet of tinfoil, the current flows, invisibly, through the foil not in one straight line from A to B, but in stream-lines, Fig. 241, which start out in all directions from A, and curl round to meet in B, in curves very like those of the magnetic lines of force that run from the N-pole to the S-pole of a magnet (Fig. 69). When the earth is used as a return wire to conduct the telegraph currents (Fig. 344), a similar spreading of the currents into current sheets occurs.

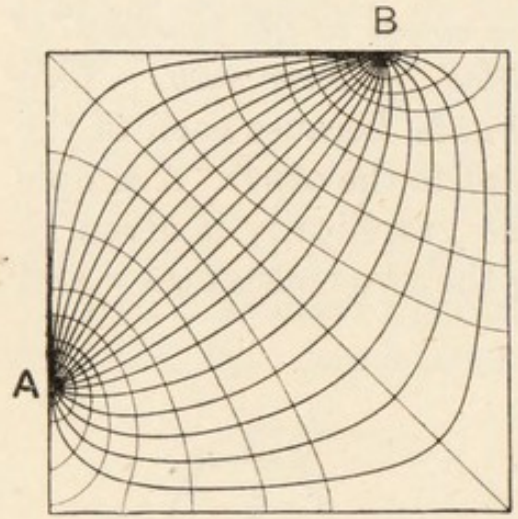


FIG. 241.
Stream-lines of Current.

LESSON XXXIV.—*Electrical Measurements*

443. Measurement of Resistance.—The practical electrician has to measure electrical resistances, electromotive-forces, and the capacities of condensers. Each of these several quantities is measured by comparison with some ascertained standard; the particular methods of comparison varying, however, to meet the circumstances of the case. Only a few simple cases can be here explained.

Ohm's law shows us that the strength of a current due to an electromotive-force falls off in inverse proportion as the resistance in the circuit increases.

(*a*) *Method of Substitution.*—It is therefore possible to compare two resistances with one another by finding out in what proportion each of them will cause the current of a constant battery to fall off. Thus, suppose in Fig. 237 we have a standard battery of a few Daniell's cells, joined up in circuit with a wire of an unknown resistance R, and with a galvanometer, we shall obtain a current of a certain strength, as indicated by the galvanometer needle experiencing a certain deflexion. If we remove the wire R, and substitute in its place in the circuit wires whose resistances we *know*, we may, by trying, find one which, when interposed in the path of the current, gives the same deflexion on the galvanometer. This wire and the one we called R offer equal resistance to the current. This *method of substitution* of equivalent resistances was further developed by Wheatstone, Jacobi, and others, when they proposed to employ as a standard resistance a long thin wire coiled upon a wooden cylinder, so that any desired length of the standard wire might be thrown into the circuit by unwinding the proper number of turns of wire off the cylinder, or by making contact at some point at any desired distance from the end of the wire. This form of *rheostat* was found, however, to be less accurate than the resistance coils described below.

(*b*) *Method of Proportional Deflexion.*—The method explained above can be used with any galvanometer of sufficient sensitiveness, but if a tangent galvanometer is available the process may be shortened by calculation. Suppose the galvanometer and an unknown resistance R to be included in the circuit, as in Fig. 237, and that the current is strong enough to produce a deflexion δ: Now substitute for R any known resistance R′, which will alter the deflexion to δ'; then (provided the other resistances of the circuit be negligibly small) it is clear that since the strengths of the currents are proportional to *tan* δ and *tan* δ' respectively, the resistance R can be calculated by the inverse proportion.

$$\tan \delta : \tan \delta' = R' : R.$$

(*c*) *Method of Differential Galvanometer.*—With a differential galvanometer (Art. 233), and a set of standard resistance coils, it is easy to measure the resistance of a conductor. Let the circuit divide into two branches, as in Fig. 242, so that part of the current flows through the unknown resistance and round one set of coils of the galvanometer, the other part of the current being made to flow through the known resistances and then round the other set of coils in the opposing direction. When we have succeeded in matching the unknown resistance by one equal to it from amongst the known resistances, the currents in the two branches will be equal, and the needle of the differential galvanometer will show *no* deflexion. This null method is very exact.

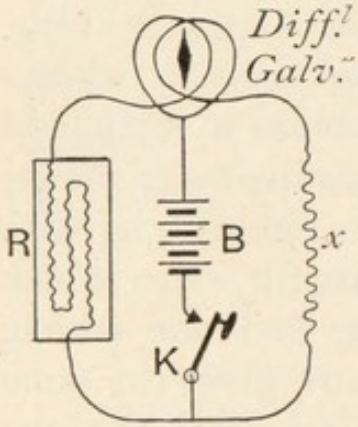


FIG. 242.—Measurement of Resistance by Differential Galvanometer.

(*d*) *Bridge Methods.*—The best of all the ways of measuring resistances is, however, with the important instrument known as Wheatstone's Bridge, described below in Art. 445.

(*e*) *Condenser Methods.*—To measure very high resistances the plan may be adopted of charging a condenser from a standard battery for a definite time through the resistance, and then ascertaining the accumulated charge by discharging it through a ballistic galvanometer (Art. 234). The higher the resistance, the less is the quantity of electricity which it will allow to flow into the condenser during the time of charge. Or in another method the condenser is allowed to discharge itself slowly through the high resistance, and the time taken by the potential to fall through any given fraction of its original value is observed. This time is proportional to the resistance, to the capacity, and to the logarithm of the given fraction.

444. Fall of Potential along a Wire. — To understand the principle of Wheatstone's Bridge we must explain a preliminary point. If the electric potential of different points of a circuit be examined by means of an electrometer, as explained in Art. 308, it is found to decrease all the way round the circuit from the + pole of the battery, where it is highest, down to the – pole, where it is lowest. If the circuit consist of one wire of uniform thickness, which offers, consequently, a uniform resistance to the current, it is found that the potential falls uniformly; if, however, one part of the circuit resists more than another, it is found that the potential falls most rapidly along the conductor of greatest resistance. If with a suitable voltmeter, either an electrometer or a fine-wire galvanometer having a high resistance in series with it, we explore the fall of potential between two points *a* and *b* of a circuit (Fig. 243), we shall find in every case the fall of potential proportional to the resistance between those two points. For $V = iR$, and therefore, for the same i, the V across any part is proportional

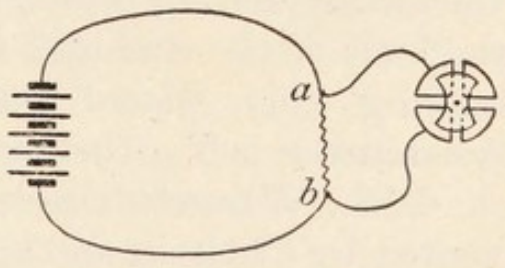


FIG. 243.—Fall of Potential along a Wire.

to the R of that part. We know, for example, that when we have gone round the circuit to a point where the potential has fallen through half its value, the current has at that point gone through half the resistances. The best way to measure a very large current is to measure (with voltmeter arrangement of galvanometer) the drop of potential it produces when sent through a known very low resistance such as a strip of platinoid having exactly $\frac{1}{1000}$ ohm resistance between two measured points. To measure a very small resistance, it should be put in series (Fig. 244), with another known very small resist-

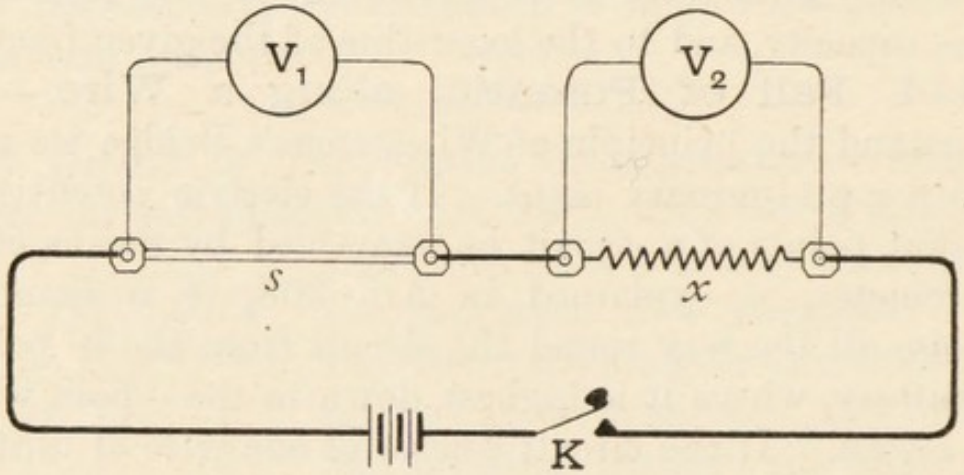


FIG. 244.—Measurement of Resistance by Drop of Potential.

ance, and the drops of potential, when the same current flows through both, are compared: the resistance of each being as the drop in potential between its ends. If the voltmeter reading when the instrument is placed across the ends of the standard resistance s is called V_1, and the reading when placed across the ends of the unknown resistance x is V_2, then $x : s :: V_2 : V_1$.

445. Wheatstone's Bridge.—This instrument, invented by Christie, and applied by Wheatstone to measure resistances, consists of a system of conductors shown in diagram in Fig. 245. This circuit of a battery is made to branch at P into two parts, which reunite at Q, so that part of the current flows through the point M, the other part through the point N. The four conductors,

A, B, C, D, are spoken of as the "arms" of the "balance" or "bridge"; it is by the proportion subsisting between their resistances that the resistance of one of them can be calculated when the resistances of the other three are known. When the current which flows from the battery arrives at P, the potential will have fallen to a certain value. From P the potential of the current in the upper branch falls to M, and continues to fall to Q. The potential of the lower branch falls to N, and again falls till it reaches Q. Now if N be the same proportionate

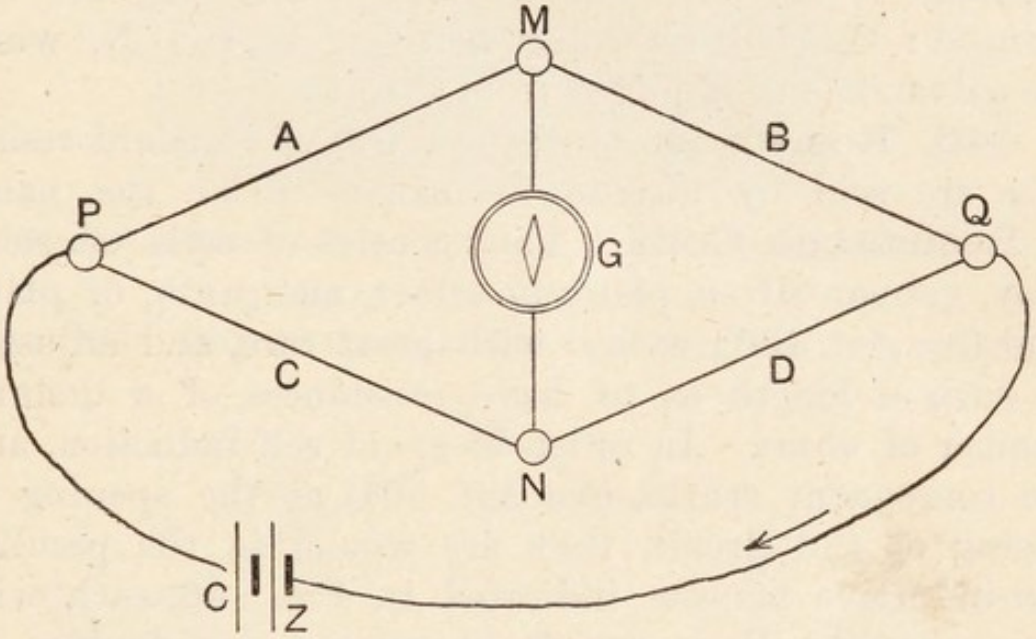


FIG. 245.—Wheatstone's Bridge.

distance along the resistances of the lower branch between P and Q, as M is along the resistances of the upper branch between P and Q, the potential will have fallen at N to the same value as it has fallen to at M; or, in other words, if the ratio of the resistance C to the resistance D be equal to the ratio between the resistance A and the resistance B, then M and N will be at equal potentials. To find out whether they are at equal potentials a sensitive galvanometer is placed in a branch wire between M and N; it will show **no deflexion** when M and N are at equal potentials; or when the four resistances of the arms "balance" one another by being in proportion, thus:—

$$A : C :: B : D.$$

If, then, we know what A, B, and C are, we can calculate D, which will be

$$D = \frac{B \times C}{A}.$$

Example.—Thus if A and C are (as in Fig. 248) 10 ohms and 100 ohms respectively, and B be 15 ohms, D will be $15 \times 100 \div 10 = 150$ ohms.

Note that balance can equally be obtained if the positions of the galvanometer and the battery are exchanged; the battery being between M and N, while the galvanometer is joined from P to Q.

446. Resistance Coils.—Wires of standard resistance are sold by instrument-makers under the name of **Resistance Coils.** They consist of coils of some alloy, german-silver, platinum-silver, manganin, or platinoid (see Art. 436), wound with great care, and adjusted to such a length as to have resistances of a definite number of ohms. In order to avoid self-induction, and the consequent sparks (see Art. 501) at the opening or closing of the circuit, they are wound in the peculiar non-inductive manner indicated in Fig. 246, each wire (covered with silk or paraffined-cotton) being doubled on itself before being coiled up. Each end of a coil is soldered to a solid brass piece, as coil 1 to A and B, coil 2 to B and C; the brass pieces being themselves fixed to a block of ebonite (forming the top of the "resistance box"), with sufficient room between them to admit of the insertion of stout well-fitting plugs of brass. Fig. 247 shows a complete resistance box, as fitted up for electrical

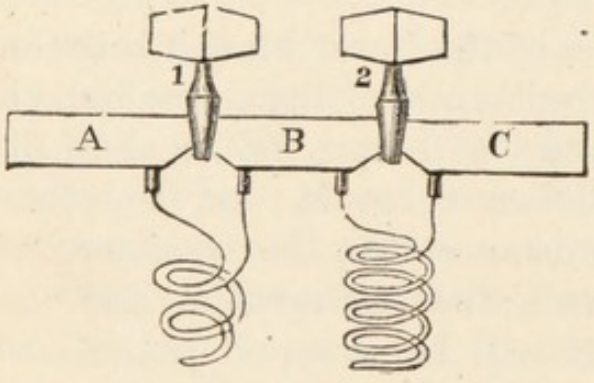


FIG. 246.—Arrangement of Resistance Coils.

testing, with the plugs in their places. So long as the plugs remain in, the current flows through the solid

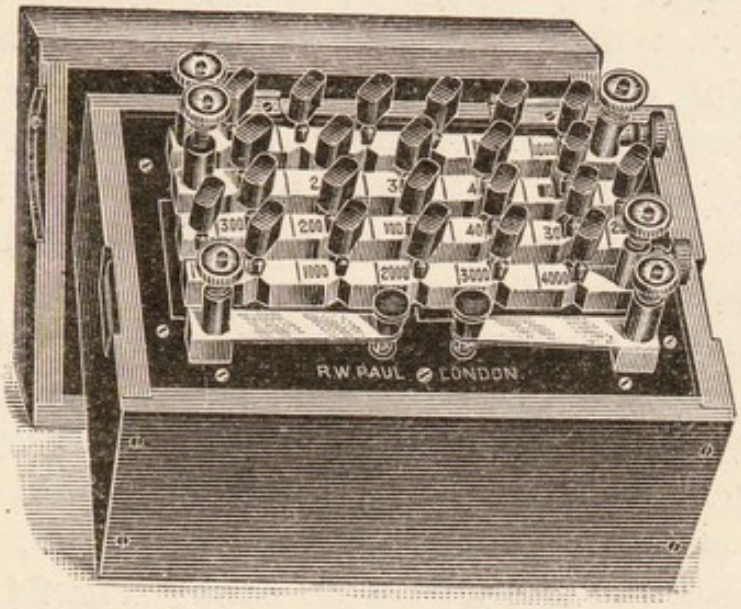


FIG. 247.—Resistance Box arranged as a Wheatstone's Bridge.

brass pieces and plugs without encountering any serious

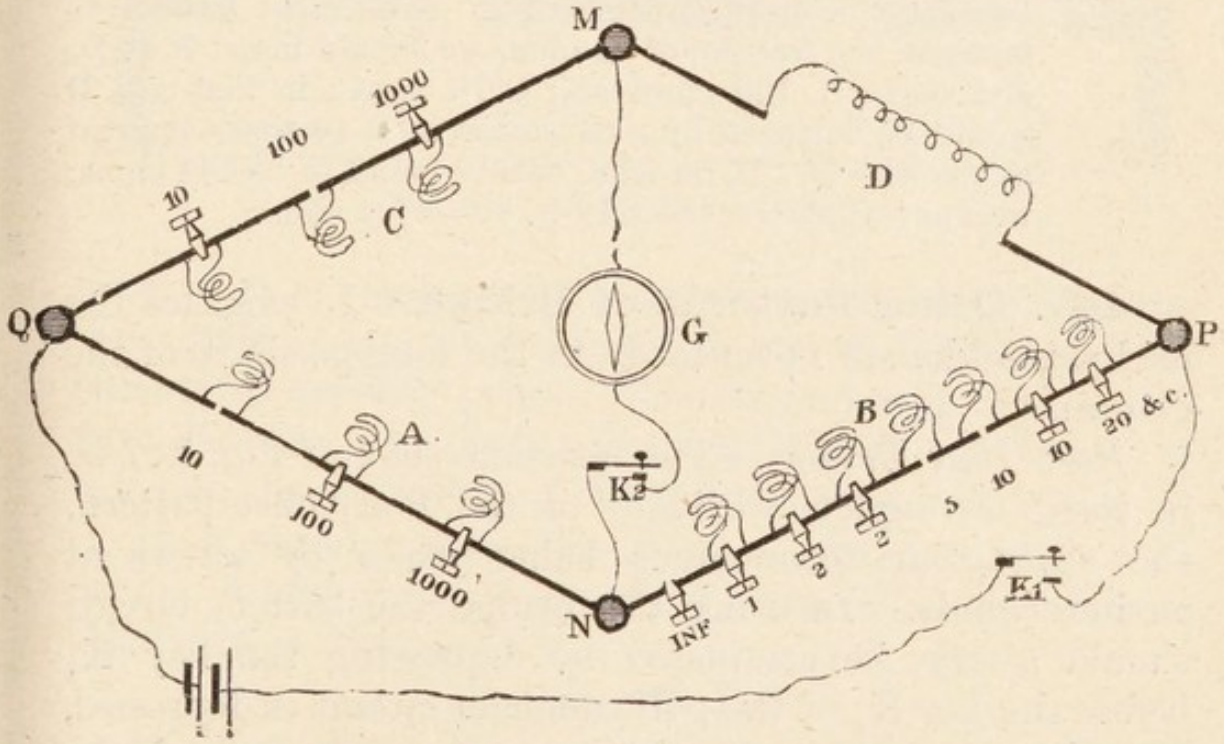


FIG. 248.—Diagram of Wheatstone's Bridge.

resistance; but when any plug is removed, the current can only pass from the one brass piece to the other by

traversing the coil thus thrown into circuit. The series of coils chosen is usually of the following numbers of ohms' resistance—1, 2, 2, 5; 10, 20, 20, 50; 100, 200, 200, 500; . . . up to 10,000 ohms. By pulling out one plug any one of these can be thrown into the circuit, and any desired whole number, up to 20,000, can be made up by pulling out more plugs; thus a resistance of 263 ohms will be made up as $200+50+10+2+1$ by unplugging those five coils.

It is usual to construct Wheatstone's bridges with some balancing resistance coils in the arms A and C, as well as with a complete set in the arm B. The advantage of this arrangement is that by adjusting A and C we determine the proportionality between B and D, and can, indeed, measure to fractions of an *ohm*. Fig. 248 shows a more complete scheme, in which resistances of 10, 100, and 1000 ohms are included in the arms A and C.

Example.—Suppose we had a wire whose resistance we knew to be between 46 and 47 ohms, and wished to measure the fraction of an ohm, we should insert it at D, and make A 100 ohms and C 10 ohms; in that case D would be balanced by a resistance in B 10 times as great as the wire D. If, on trial, this be found to be 464 ohms, we know that $D=464\times10\div100=46{\cdot}4$ ohms.

447. Other Patterns of Bridge.—In practice the bridge is seldom or never made in the lozenge-shape of the diagrams.

Post-Office Bridge.—The resistance-box of Fig. 247 is, in itself, a complete "bridge" of the Post-Office pattern, the appropriate connexions being made by screws at various points. In using the bridge the battery circuit should always be completed by depressing the key K_1 before the key K_2 of the galvanometer circuit is depressed, in order to avoid the sudden violent "throw" of the galvanometer needle, which occurs on closing circuit in consequence of self-induction (Art. 501).

Dial Bridge.—To avoid errors arising from the differ-

ent numbers of plugs in use, the coils of a bridge are sometimes arranged in dials—the units in one, the tens of ohms in another, and so forth—each dial having but one plug, or a movable arm like Fig. 235.

Metre Bridge.—This is a simple form very useful for measuring resistances not exceeding a few hundred ohms. Upon a long board is stretched over a scale one metre long a uniform thin wire of german-silver or other alloy, its ends being joined to stout pieces of copper. Here A, B, C, and D are four resistances joined as shown by stout strips of copper. When the wire from the galvanometer is slid along the wire to such a point that there is no current, it follows that

$$A + a : B + b = C : D.$$

Foster's method of measuring *small differences of resist-*

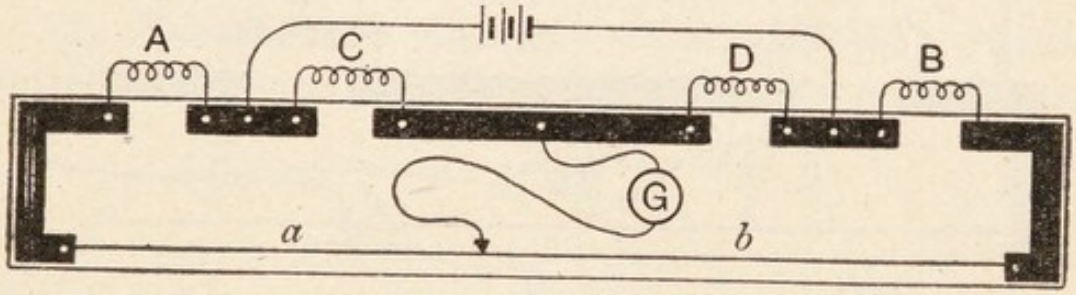


FIG. 249.—Carey Foster's Bridge.

ance is to get balance at a certain point along the wire (Fig. 249), then interchange A and B, and again get balance at another point. The resistance of the piece of wire between the two points of balance will then be equal to the *difference* of the resistances A and B.

In a simpler way, Fig. 250, of using a slide-wire bridge, A and B are replaced by strips of no appreciable resistance, so that

$$a : b : : C : D.$$

If D is the unknown resistance and C a known resistance, the *ratio* of the lengths a and b at once enables the unknown resistance to be calculated.

Yet another way of using a wire-slide bridge is that

shown in Fig. 251, where x is an unknown resistance and s a standard resistance not differing greatly from

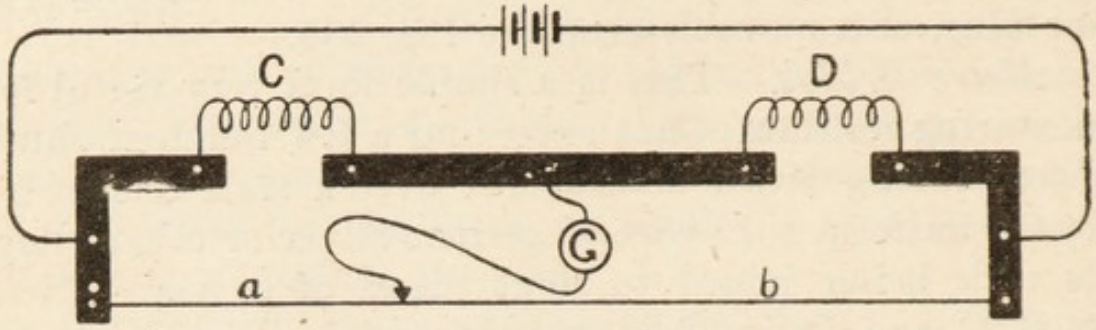


FIG. 250.—Simple Slide-wire Bridge.

that to be measured. If contact with the galvanometer circuit is made at 100 divisions along the slide-wire, and

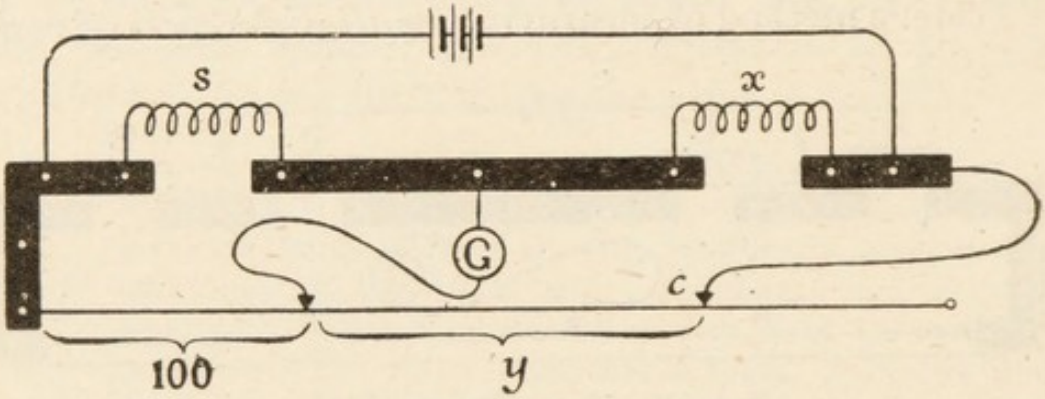


FIG. 251.—Slide-wire Bridge.

the contact c is moved along till balance is obtained, the number of divisions y along the wire will give the value of x as a percentage of s, since $y = 100 \times x \div s$.

For further details of bridge methods consult Gray's *Absolute Measurements in Electricity and Magnetism*, Kempe's *Electrical Measurement*, or Ayrton's *Practical Electricity*.

448. Measurement of Electromotive-Force.—There being no easy absolute method of measuring electromotive-forces, they are usually measured *relatively*, by comparison with the electromotive-force of a standard cell, such as Clark's or the Weston normal

cell (Art. 201). The methods of comparison are various; only five are here mentioned.

(*a*) *Reduced Deflexion Method.*—Call the electromotive-force of the battery to be measured E, and E′ that of a standard battery. Join E with a galvanometer, and let it produce a deflexion of δ_1 degrees through the resistances of the circuit; then add enough resistance r to bring down the deflexion to δ_2 degrees—say 10 degrees less than before. Now substitute the standard battery in the circuit and adjust the resistances till the deflexion is δ_1 as before, and then add enough resistance r' to bring down the deflexion to δ_2. Then

$$r' : r = E' : E,$$

since the resistances that will reduce the strength of the current equally will be proportional to the electromotive-forces. (Not recommended.)

(*b*) *Potentiometer Method.*—If the poles of a constant battery are joined by a long thin wire, the potential will

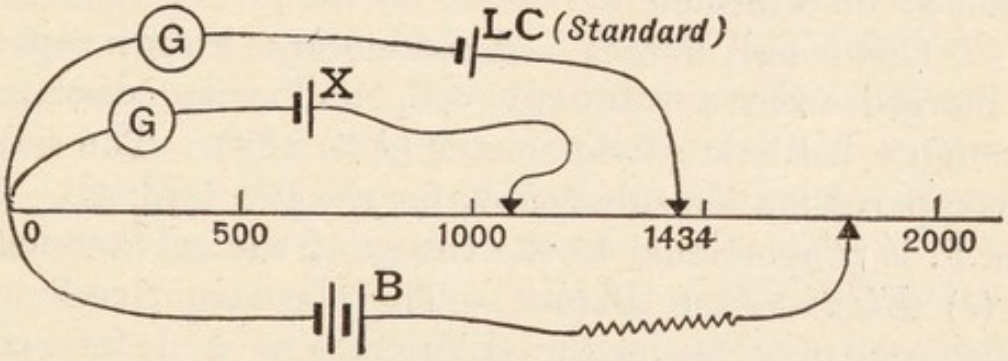


FIG. 252.—Diagram of Potentiometer.

fall uniformly from the + to the − pole. Hence, by making contacts at one pole and at a point any desired distance along the wire, any desired proportional part of the whole electromotive-force can be taken. This proportional part may be balanced against the electromotive-force of any cell as follows:—Let a uniform thin wire of platinoid or german-silver be stretched over a scale divided into say 2000 parts. Connect a Clark standard cell LC through a sensitive galvanometer, as

shown in Fig. 252, to make contact at the 1434 division of the scale. Then connect a single accumulator cell B, or two Daniells, with a sliding contact, as shown, and move it up and down until a point is found such that the galvanometer shows that the Clark cell is balanced. Then connect the cell X whose E.M.F. is to be measured, and slide its contact along the wire until it also is balanced. Suppose it balances at 1024 of the scale, its E.M.F. will be 1·024. A single galvanometer will suffice if the wire to X is joined in between G and the Clark cell.

(*c*) *Voltmeter Method.*—If a galvanometer be used so that the resistance of its circuit is several thousand ohms (in comparison with which the internal resistance of a battery or dynamo machine is insignificant), it will serve as a voltmeter to measure electromotive-forces; for the strength of current through it will depend only on the electromotive-force between the ends of the coil. (See Art. 237 on Voltmeters.)

(*d*) *Condenser Method.*—A condenser of known capacity is charged from a standard cell, and then discharged through a ballistic galvanometer (Art. 234). The cell to be compared is then substituted for the standard cell. The E.M.F. is proportional to the throw of the galvanometer.

(*e*) *Electrometer Method.*—The electromotive-force of a battery may be measured directly as a difference of potentials by a quadrant electrometer (Art. 307). In this case the circuit is never closed, and no current flows.

449. Measurement of Internal Resistance of Cells.—This may be done in several ways.

(*a*) *Condenser Method.*—As in (*d*) of preceding Article, observe throw of galvanometer from condenser charged by the cell. Then shunt the cell with a suitably high resistance R and take another charge and discharge. If the two throws are called d_1 and d_2, the internal resistance will be $= R(d_1 - d_2)/d_2$.

(*b*) *Half-deflexion Method.*—Place the cell in series

with a galvanometer the resistance of which is G, and a resistance-box in which there is unplugged a resistance R such that the deflexion is conveniently large. Now increase the resistance in the box until it is seen by the deflexion that the current has been reduced to half what it was. If this added resistance is called a, then by Ohm's law it follows that the internal resistance is $= a - (R + G)$. This method is suitable for very high internal resistances.

(*c*) *Method of Opposition.*—Take two similar cells and join them in opposition to one another, so that they send no current of their own. Then measure their united resistance just as the resistance of a wire is measured. The resistance of one cell will be half that of the two.

(*d*) *Mance's Method.*—Place the cell itself in one arm of the Wheatstone's bridge, and put a *key* where the battery usually is, adjust the resistances till the permanent galvanometer deflexion is the same whether the key be depressed or not. When this condition of things is attained the battery resistance is balanced by those of the other three arms. (*Not a reliable method.*)

(*e*) *Alternating Current Method.*—If greater accuracy is required in the opposition method, the cells in opposition may be placed in one of the arms of a Wheatstone's bridge in which instead of the usual battery is inserted the secondary coil of a small induction coil (without condenser), while a telephone receiver is used instead of a galvanometer. The ceasing of the buzzing in the telephone corresponds to nul deflexion.

450. Measurement of Resistance of Electrolytes.—Electrolytes have a true resistance which is found to remain constant when measured with currents of different strength, provided the back electromotive-forces at the electrodes, due to polarization (Art. 183), are eliminated. Kohlrausch modified Wheatstone's bridge for this service, by applying alternating currents, and substituting a tele-

phone receiver (Art. 593) for the galvanometer. The bridge is adjusted until the sound in the telephone is a minimum. The usual form of apparatus is shown diagrammatically in Fig. 253.

This method may be modified by the use of Whetham's commutator which renders it more rapid and more accurate. A continuous current is led to an ebonite drum turned by a motor or a hand wheel. On the drum are fixed brass strips with wire brushes touching them in such a manner that the current is reversed several times in each revolution. The wires from the drum are connected with the ends of the wire bridge. A moving coil galvanometer (whose coil possesses a high moment of inertia) is used as indicator, and on the other end of the drum is another set of strips arranged to reverse periodically the galvanometer connexions, so that any residual current flows through it continuously and not alternating. These strips are slightly narrower than the first; set thus the galvanometer circuit is made just after and broken just before the battery circuit. When the measured resistance is not altered by increasing the speed of the commutator, or changing the ratio of the arms of the bridge, the disturbing effects may be considered to be eliminated.

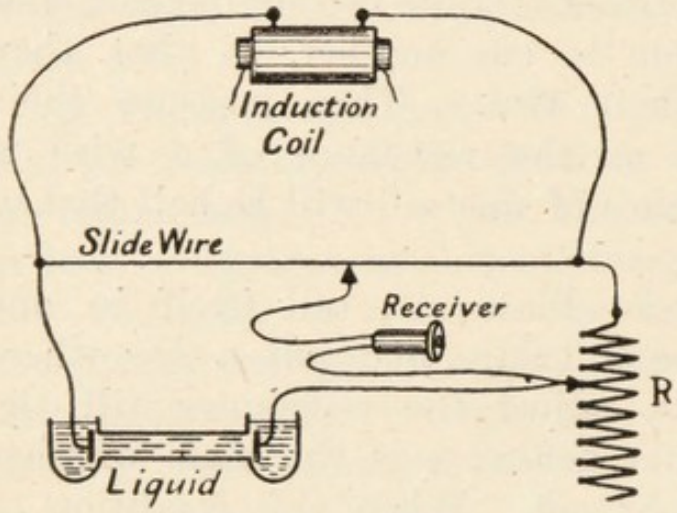


FIG. 253.—Kohlrausch's Bridge.

In this way a measurement is obtained of the resistance of the column of liquid between the electrodes of the cell. To calculate the conductivity of the liquid the area of the electrodes and their distance apart must be observed. As the temperature coefficient of conductivity is large

(2% per degree) it is advisable to place the resistance cell in a water bath and to observe its temperature with some accuracy.

451. Measurement of Capacity.—The capacity of a condenser may be measured by comparing it with the capacity of a standard condenser—such as the $\frac{1}{3}$ microfarad condenser (Fig. 174)—in one of the following ways :—

(*a*) *Electrometer Method.*—Charge the condenser of unknown capacity to a certain potential; then make it share its charge with the condenser of known capacity, and measure the potential to which the charge sinks; then calculate the original capacity, which will bear the same ratio to the joint capacity of the two as the final potential bears to the original potential.

(*b*) *Ballistic Galvanometer Method.* — Charge each condenser to equal differences of potential from the same cell or battery, and then discharge each successively through a ballistic galvanometer (Art. 234). The throw of the needle will be proportional in each case to the charge, and therefore to the capacity.

The law of the ballistic galvanometer is :—

$$CV = Q = \frac{H}{G} \times \frac{T}{\pi} \sin \tfrac{1}{2}\alpha,$$

where Q is the quantity of electricity (in C.G.S. units), C the capacity of the condenser, V the volts applied, H the magnetic field, G the constant of the galvanometer, T the period of one complete swing of the needle, and α the angle of first throw. The factor H/G may be eliminated by passing a continuous current i to produce a steady deflexion β ; when

$$i = \frac{H}{G} \tan \beta.$$

Combining this with the preceding, we have

$$Q = \frac{iT \sin \frac{1}{2}\alpha}{\pi \tan \beta}.$$

If α and β are both small this becomes

$$Q = iT\, \alpha/2\pi\beta ;$$

where if i is in amperes, Q will be in coulombs.

For a d'Arsonval galvanometer, when used ballistically

$$Q = Ti \div 2\pi ;$$

where T = one period, and i is the steady current which produces a deflexion equal to the throw.

(*c*) *Bridge Method.*—Connect the two condensers C_1 and C_2 in two arms of a Wheatstone's bridge and adjust the resistances so that there is no deflexion on charge or discharge (Fig. 254). Then $C_1 : C_2 :: r_2 : r_1$, the *larger* capacity acting as a *smaller* resistance.

(*d*) *Potential-divider Nul Method.*—Two resistances r_1 and r_2 are joined in series to the + and − poles of a battery. The middle point between r_1 and r_2 is connected to one of the terminals of C_1 and also of C_2. The free terminals of C_1 and C_2 are momentarily joined to the + and − poles of the battery respectively and receive charges of opposite sign. They are then connected; and if of equal amount the charges will neutralize each other. The resistances r_1 and r_2 are adjusted until this condition is satisfied, as shown by nul deflexion when the key of a galvanometer circuit across their terminals is depressed. Then $C_1 : C_2 :: r_2 : r_1$.

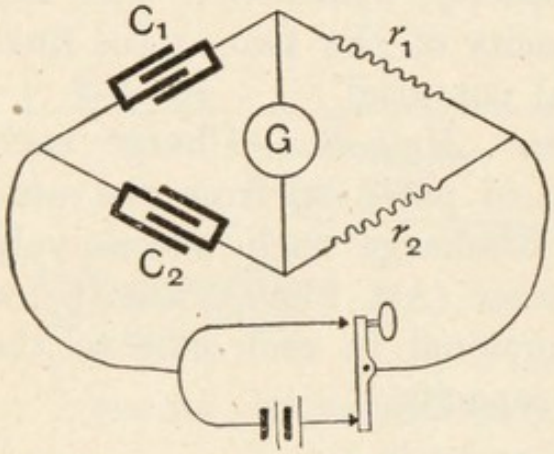


FIG. 254.—Comparison of Capacities by Bridge Method.

(*e*) *Tuning-fork Method.*—A tuning-fork acting as a vibrating two-way switch charges and discharges the condenser n times per second, allowing to pass VCn coulombs per second or VCn amperes. The apparent resistance r of this combination is $1/Cn$, and can be measured by a Wheatstone bridge, whence $C = 1/nr$.

(*f*) *Loss of Charge Method.*—This is the same as the last method in Art. 443*e*, a known high resistance being used.

452. Measurement of Resistance by Amperemeter and Voltmeter.—If an amperemeter is used to measure the amperes going through any conductor, and at the same time a voltmeter is used to measure the difference of potential between its ends, then the resistance of that conductor (assuming that there are no electromotive-forces being generated in it) can be found by dividing the volts by the amperes; since $R = E \div i$. This method can be used, for example, to find the

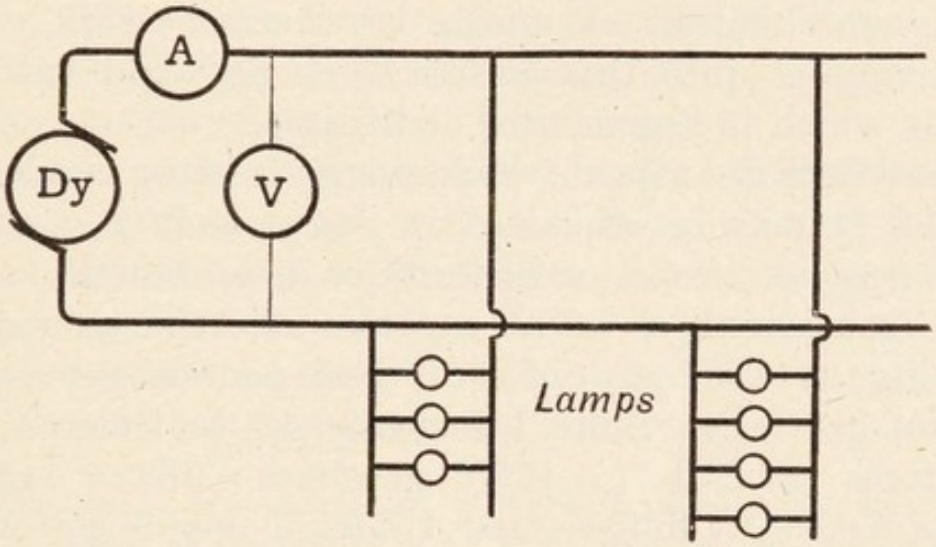


FIG. 255.—Measurement of Resistance by Amperemeter and Voltmeter.

resistance of a glow-lamp while it is alight. Or it may be used (Fig. 255) to ascertain the resistance of a whole circuit of lamps.

453. Ohmmeter.—The Ohmmeter is an instrument to read the ratio which the volts applied to a conductor bear to the current thereby produced in it; that ratio being read off direct on the scale. The instrument (which usually also contains a small generator to provide a current) is a species of galvanometer so arranged that the amperes pass through a fixed coil, and the current proportional to the volts passes through a second fixed coil at right angles to the first. A suitably pivoted needle takes up a diagonal position at an angle the tangent of which is proportional to the ratio of volts to

amperes, and may therefore be graduated to read ohms. In the Ohmmeters employed for testing high resistances such as a megohm or more, an electromotive-force of 500 volts is usually generated.

LESSON XXXV.—*Electric Energy and Measurement.*

454. Electric Energy.—An electric current conveys energy from a battery or dynamo to some other part of the circuit, where it is transformed back into work—mechanical, chemical, or thermal work. We must inquire into this electrical energy and into the rate at which it is generated or utilized.

Power is the rate at which energy is being received or spent. It may be expressed in *foot-pounds per second*, or in *ergs per second*, or in *watts*, or in *kilowatts*. James Watt considered a horse capable on the average of working at the rate of 550 foot-pounds per second (against gravity). Since 1 foot = 30·48 centimetres, and the force of 1 lb. (= 453·6 grammes × 981) = 445,000 dynes, nearly, it follows that 1 *horse-power* is equivalent to 7,460,000,000 (or 746×10^7) *ergs per second*.

If a quantity of electricity Q is moved through a difference of potential V, it follows from the definition (Art. 280) that the work done is equal to QV. If this is occurring in a battery or dynamo, QV represents electrically the work (chemical or mechanical) done on the system, or the energy received (electrically) by the system. Now, suppose this operation to have occupied time t, the *rate* at which the energy is being imparted to the circuit will be QV/t. But (Art. 169) $Q/t = i$. Hence the *power* given to the circuit is equal to iV.

This justifies the statement that *the power of an electric current* to perform useful work, whether in lighting, heating, or producing mechanic actions, *is proportional both to the strength of the current, and to the electromotive-force which drives it.* In other words, *power*

is proportional to both amperes and volts jointly. [Similarly the power of a steam engine is proportional not only to the quantity of steam it uses per second, but also to the pressure at which the steam is supplied.] The electric unit of power will then be the power of a current of 1 ampere driven by an electric pressure of 1 volt. This unit is known as 1 *watt*.

To find the number of watts of power supplied by any dynamo or battery, multiply the number of amperes of current by the number of volts at which the current is driven. The same rule serves to calculate the power electrically delivered to any motor, lamp, accumulator, or other means of spending electric energy.

Since 1 volt $= 10^8$ absolute units of E.M.F., and 1 ampere $= 10^{-1}$ absolute units of current (Art. 381) it follows that 1 watt $= 10^7$ absolute units of power (*i.e.* 10^7 ergs per second). But 1 horse-power $= 746 \times 10^7$ ergs per second (see above). Hence 1 H.P. $= 746$ watts.

$$\text{Horse-power} = i \times \text{V} \div 746.$$

Example.—If a current of 20 *amperes* is supplied to an arc-lamp at a pressure of 56 *volts*, find the amount of power absorbed therein. *Ans.* 1120 *watts* or $1\frac{1}{2}$ H.P.

One thousand watts is called 1 *kilowatt*. The kilowatt is therefore approximately $1\frac{1}{3}$ H.P.

$$\text{Kilowatts} = i \times \text{V} \div 1000.$$

The reader is warned that in the case of alternating currents, if there is any difference of phase between the volts and the amperes, the true power (watts) will be less than the *volt-amperes*, for in such cases the *power-factor* (Art. 531) must also be taken into account.

455. Input and Output. — Any generator of electric power, such as a dynamo, battery, or thermopile, when connected to a circuit to which it supplies the electric power is giving an *output*, which may be expressed in watts or kilowatts. It also is receiving from some source, mechanical, chemical, or thermal, an input

of power. Any motor, electric lamp, electroplating cell, or heater, which is supplied electric power through a circuit is said to be receiving electrically, an *input* which may likewise be expressed in watts or kilowatts and which is being converted into mechanical, luminous, chemical, or thermal energy. Thus a dynamo supplying 300 amperes at a potential difference of 200 volts between its terminals is said to be giving an output[1] of 60 kilowatts: and a motor taking 80 amperes from mains at 500 volts is said to have an input of 40 kilowatts. The question whether the machine through which a current is flowing is *giving out* or *taking in* electric power depends on the question (Art. 264) whether the machine is generating an electromotive-force which *helps* the current (as in dynamos) or *opposes*[2] it (as in motors).

456. Efficiency.—The name of *the efficiency* is given to the ratio between output and input. In a dynamo the input is mechanical, being the power given (by the engine) mechanically to the driving shaft; and the output is electrical, being the power delivered to the circuit, as measured at the terminals of the machine. Both quantities must, of course, be expressed in the same units; both in watts, or both in kilowatts. In a motor the input is electrical, and the output mechanical; the latter being the power delivered at the shaft of the machine. The difference between the output and the input is the power that is lost.

[1] The word *output*, as applied to central station work is sometimes used in the sense of total outflow of amperes irrespective of voltage, but this should rather be called the *load*.

[2] Consider the mechanical analogue of transmission of power from one pulley to another pulley by a belt. The effort in the driving pulley is in the same direction as the motion of the belt. The effort in the driven pulley is opposed in direction to the motion. (See also Art. 264.)

This fundamental principle accounts for the back-electromotive-forces observed in motors, and in accumulators while being charged. Because of it we know (Art. 174) that the seat of the main electromotive-force in a voltaic cell is at the surface of the zinc, and that (Art. 474) bismuth is thermo-electrically positive to antimony.

We may write it thus :—

$$\text{efficiency} = \frac{\text{output}}{\text{input}} = \frac{\text{output}}{\text{output} + \text{losses}}.$$

Example.—Suppose a dynamo generates 736 amperes at 250 volts between its terminals, and that it takes 270 HP as measured at the shaft. The output is $250 \times 736 = 184000$ watts $= 184$ kilowatts. The input is $270 \times 746 = 201420$ watts $= 201{\cdot}42$ kilowatts. The efficiency is $184000 \div 201420 = 0{\cdot}9134$, or $91{\cdot}34$ per cent. The losses amount to $201420 - 184000 = 17420$ watts $= 17{\cdot}12$ kilowatts.

457. Power-Measurement. — To measure the power given electrically to any part *ab* of a circuit by an unvarying current, it suffices to measure the current with an *amperemeter* (Art. 238), and the potentials across the part with a *voltmeter* (Arts. 237, 309), the latter being of course connected as a shunt as in Fig. 256. Then, if the current is unvarying, the product of volts and amperes gives the watts. Or a *wattmeter* may be used as below.

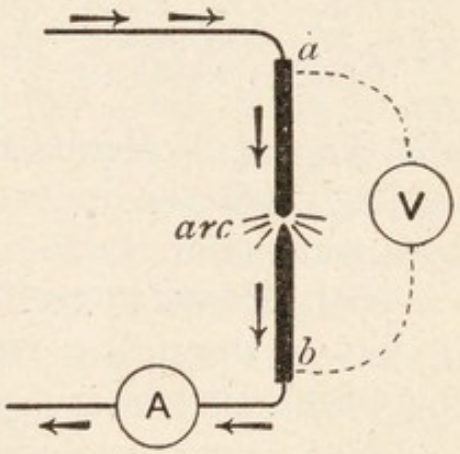


FIG. 256. — Measurement of Power by Amperemeter and Voltmeter.

458. Wattmeters.—The product of amperes and volts may be measured directly by means of a *wattmeter*. This name is given to a variety of electrodynamometer (Art. 425) in which the fixed and movable coils constitute two separate circuits, one being a thick wire of low resistance to carry the *amperes*, the other being, or including, a thin wire of high resistance (as in voltmeters) to receive a current proportional to the *volts*. The latter circuit is to be connected as a shunt to the part *ab* of the circuit in which the supplied power is to be measured. In Fig. 257, as in Fig. 256, the part *ab* is an arc-lamp. The auxiliary resistance r is introduced into the thin-wire

circuit of the instrument, the whole current flowing through the thick-wire circuit.

Wattmeters are made both on the pattern of Siemens's dynamometer (Art. 426) and on that of Kelvin's balances (Art. 427).

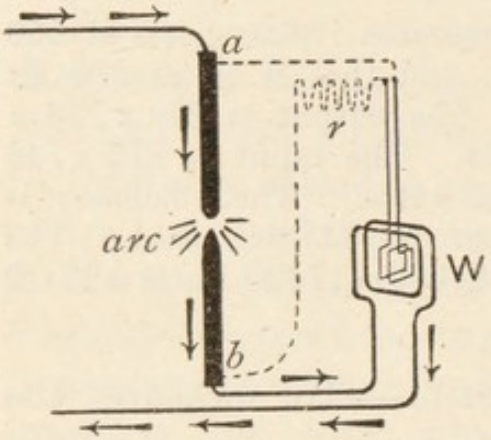


FIG. 257.—Measurement of Power by Wattmeter.

When power-measurements have to be made on alternate-current circuits, separate instruments must not be used, as in Art. 457, to measure volts and amperes. For, owing to the differences of phase (Art. 524) between voltage and current, the *apparent watts*, or *volt-amperes*, calculated by multiplying the separate readings, will be in excess of the *true watts* as measured by a wattmeter.

459. Power wasted in Heating.—If a current i is driven through a resistance R, the volts needed will (by Ohm's law) be

$$V = iR.$$

The power iV so expended will merely heat the resistance. Substitute for V its value as above, and we have

$$\text{Watts wasted} = iV = i^2R = V^2/R.$$

Or, if the expenditure goes on for t seconds, the amount of energy turned into heat (joules) will be

$$\text{Energy} = QV = itV = i^2Rt \text{ (}see\text{ Art. 462).}$$

The *nett* power of a dynamo or battery is always less than its *gross* power, because of internal resistance. If r be the internal resistance, and E the whole electromotive-force, the nett or available volts $V = E - ir$. The *gross* power will be Ei watts. But the *nett* power will be $Vi = Ei - i^2r$. Or, the available watts equal the total watts generated, less the watts wasted in internal heating.

460. Supply Meters.—Meters for measuring the supply to the houses of consumers are of several kinds.

(*a*) *Chemical Meters.*—The current or a known fraction of it is passed through an electrolytic cell, there to deposit copper or dissolve zinc. The amount of chemical action is proportional to the ampere-hours. In another type two electrodes dip into an electrolyte such as acidulated water. The decomposition of the electrolyte lowers the solution, and the lowering is a measure of the ampere-hours.

(*b*) *Motor Meters.*—If the current passes through the armature of a small motor (Art. 516) having a constant field, and having its speed controlled purely by eddy-current friction (Art. 500), in an aluminium disk revolving between magnet poles, its speed will at every instant be proportional to the current. Hence such a motor attached to a suitable counting-train of wheels will serve as a meter, the total number of revolutions being proportional to the ampere-hours. In Perry's meter the revolving part is a copper bell immersed in mercury, revolving around a central magnet pole (as the wire does in Fig. 234), and surrounded by an external S-pole with ribbed projections to promote eddy currents. In Ferranti's meter the mercury, lying as a horizontal circular pool, through which the current flows radially in a vertical magnetic field, rotates and moves the registering wheels in proportion to the current that passes through. In Elihu Thomson's motor meter (Fig. 258) which records the watt-hours, the revolving armature A is of fine wire and high resistance, connected as shunt, while the fixed coils F that serve as field-magnet take the whole current supplied. So the torque is proportional to the watts; while an aluminium disk D revolving between magnet

poles M, by its drag (Art. 500) acts as a brake and keeps the speed proportional to the torque. To compensate for inevitable friction of the pivots, it is arranged to provide a small auxiliary field by

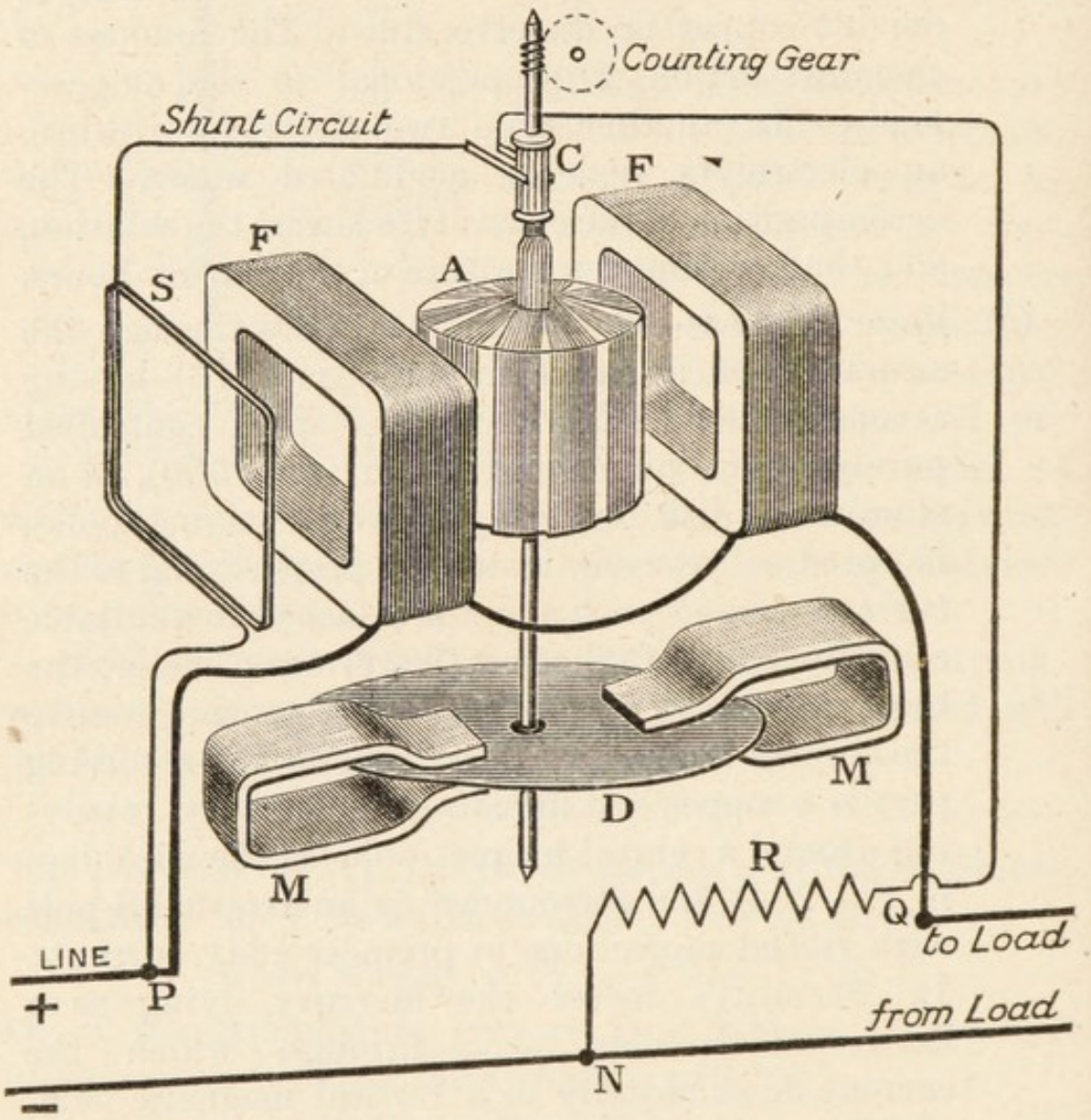


FIG. 258.—Elihu Thomson Supply Meter.

means of an additional coil S which is connected into the shunt circuit. A good meter should start turning when the current going to the lamps is less than 1 per cent of the normal load.

(*c*) *Retarded Clocks.*—Current may be made to act upon the rate of a clock, by flowing in a coil under the pendulum bob if the latter is a magnet.

Any force added thus to gravity or subtracted from it will cause the clock to gain or lose. Ayrton and Perry proposed to measure the supply by the total time gained or lost by a clock. In Aron's meter, of which this is the principle, there is a double clock with two pendulums, only one of which is acted on by the current. A train of counting wheels is geared to record the difference between the two.

(*d*) *Integrating Meters.*—A uniformly-going clock drives a counting apparatus through an intermediate gear operated by the current (or by the watts), this intermediate gear being such that when current is small the counting is small; when current large the counting is large. An integrating disk-and-roller, or an integrating cam, is a usual mechanism, its operation being controlled by the motion of an amperemeter or wattmeter.

(*e*) *Alternating Current Meters.*—For measuring the consumption on an alternating supply, the motor in the meter must be one of such a type as is suitable for alternating currents. In practice there is used a simple form of induction motor (Art. 549), in which the rotor is a simple aluminium disk, and the stator is replaced by a laminated electromagnet having a split-pole winding, so as to create the difference of phase necessary to procure rotation. The same disk, so driven, may at the same time serve also as the eddy-current brake (Art. 500), turning between the poles of a permanent magnet.

CHAPTER VII

ELECTRIC PRODUCTION OF HEAT

LESSON XXXVI.—*Heating Effect of Currents*

461. Heat and Resistance.—A current may do work of various kinds, chemical, magnetic, mechanical, and thermal. In every case where a current does work that work is done by the expenditure of part of the energy that is being supplied to the circuit. We have seen that, by the law of Ohm, the current produced by a given battery is diminished in strength by anything that increases the external resistance. But the current may be diminished, in certain cases, by another cause, namely, the setting up of an opposing electromotive-force at some point of the circuit. Thus, in passing a current through an electrolytic cell (Art. 252) there is a diminution due to the opposing electromotive-force ("polarization") which is generated while the chemical work is being done. So, again, when a current is used to drive an electric motor (Art. 455), the rotation of the motor will itself generate a back E.M.F., which will diminish the current. Whatever energy is, however, not expended in this way in doing work against a back electromotive-force is *frittered down into heat*, either in the generator or in some part of the circuit, or in both. Suppose a quantity of electricity to be set flowing round a closed circuit. If there were no resistance to stop it it would circulate for

ever; just as a waggon sent rolling along a circular railway should go round for ever if it were not stopped by friction. When matter in motion is stopped by friction the energy of its motion is frittered down by the friction into heat. When electricity in motion is stopped by resistance the energy of its flow is frittered down by the resistance into heat. Heat, in fact, appears wherever the circuit offers a resistance to the current. If the terminals of a battery be joined by a short thick wire of small resistance, most of the heat will be developed in the battery and so wasted; whereas, if a thin wire of relatively considerable resistance be interposed in the outer circuit, it will grow hot, while the battery itself will remain comparatively cool.

462. Laws of Development of Heat: Joule's Law.—To investigate the development of heat by a current, Joule and Lenz used instruments on the principle shown in Fig. 259. A thin wire joined to two stout conductors is enclosed within a glass vessel containing water, into which also a thermometer dips. The resistance of the wire being known, its relation to the other resistances can be calculated. Joule found that *the number of units of heat developed in a conductor* is proportional—

(i.) to its resistance;

(ii.) to the square[1] of the strength of the current; and

(iii.) to the time that the current lasts.

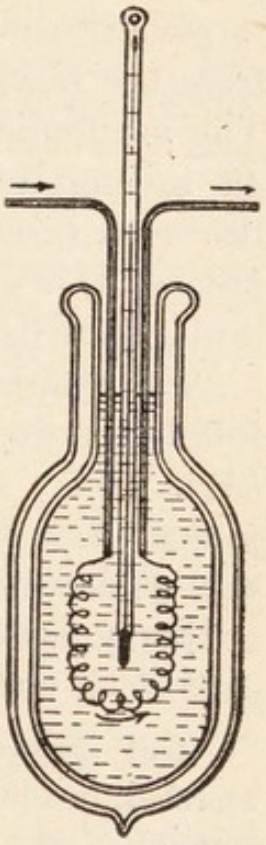


FIG. 259.—Water heated by Electric Current.

[1] The second of the above laws, that the heat is, *caeteris paribus*, proportional to the square of the strength of the current, often puzzles students, who expect the heat to be proportional to the current simply. Such may remember that the consumption of zinc is, *caeteris paribus*, also proportional to the square of the current; for, suppose that in working through a high resistance (so as to get all the heat developed outside the

The equation expressing these relations is known as Joule's Law, and is—

$$U = i^2Rt \times 0{\cdot}24,$$

where i is the current in amperes, R the resistance in ohms, t the time in seconds, and U the heat in calories; one *calorie* being the amount of heat that will raise 1 gramme of water through 1° C. of temperature (Art. 299).

This equation is equivalent to the statement that *a current of one ampere flowing through a resistance of one ohm develops therein* 0·24 *calories per second.* The heat produced thus by the degradation of energy in a resistance is sometimes called the "ohmic" heat to distinguish it from the heat of the reversible Peltier effect (Art. 472). The mechanical equivalent of heat (Joule's equivalent), is 42 million ergs to 1 calorie; so $W = JU$, where W is the work in ergs, U the heat in calories, and $J = 4{\cdot}2 \times 10^7$. Hence $U = i^2Rt/J$. But to reduce to ergs we must multiply i^2Rt by 10^7; whence $U = i^2Rt \times 0{\cdot}24$.

The number 0·24, which appears above, arises in the following way: The product i^2R is the number of *watts* (Art. 454); and i^2Rt is the number of *watt-seconds*, or *joules* (Art. 381) or units of energy expended as heat in the resistance. Experimentally it is found that the ordinary heat-unit or *calorie* is equal to 4·2 *joules*; or 1 *joule* is equal to 0·24 *calories*.

463. Favre's Experiments.—Favre, repeating Joule's researches, made a series of most important experiments on the relation of the energy of a current to the heat it develops. He ascertained that the number of calories evolved when 33 grammes (1 equivalent) of zinc are dissolved in dilute sulphuric acid (from which it causes hydrogen to be given off) is 18,682. This figure was arrived at by conducting the operation in a vessel placed in a

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battery) we double the current by doubling the number of battery cells in series, there will be twice as much zinc consumed as before in *each* cell, and as there are twice as many cells as at first the consumption of zinc is *four times* as great as before.

cavity of his calorimeter, an instrument resembling a gigantic thermometer filled with mercury, the expansion of which was proportional to the heat imparted to it. When a Smee's cell was introduced into the same instrument, the solution of the same amount of zinc was observed to be accompanied by the evolution of 18,674 calories (*i.e.* an amount almost identical with that observed before), and this amount was the same whether the evolution took place in the battery-cell when the circuit was closed with a short thick wire or whether it took place in a long thin wire placed in the external circuit. He then arranged 5 Smee's cells in series, in cavities of the calorimeter, and sent their current round a small electric motor. The amount of heat evolved during the solution of 33 grammes of zinc was then observed in three cases: (i.) when the motor was at rest; (ii.) when the motor was running round and doing no work beyond overcoming the friction of its pivots; (iii.) when the motor was employed in doing 13,124,000 gramme-centimetres ($=12,874 \times 18^6$ *ergs*) of work, by raising a weight by a cord running over a pulley. The amounts of heat evolved in the circuit in the three cases were respectively, 18,667, 18,657, and 18,374 calories. In the last case the work done accounts for the diminution in the heat wasted in the circuit. If we add the heat-equivalent of the work done to the heat evolved in the latter case, we ought to get the same value as before. Dividing the $12,874 \times 18^6$ *ergs* of work by Joule's equivalent (42×10^6), we get as the heat-equivalent of the work done 306 calories. Now $18,374 + 306 = 18,680$, a quantity which is almost identical with that of the first observation, and quite within the limits of unavoidable experimental error.

464. Rise of Temperature. — The elevation of temperature in a resisting wire depends on the *nature* of the resistance. A very short length of a very thin wire may be found which has the same resistance as a long length of stout wire. Each will cause the same number of units of heat to be evolved, but in the former case, as the heat is spent in warming a short thin wire of small mass, it will get very hot, whereas in the latter case it will perhaps only warm to an imperceptible degree the mass of the long thick wire; which, moreover, has a larger surface to get rid of its heat. If the wire weigh w grammes, and have a specific capacity for heat s, then $U = sw\theta$, where θ is the rise of temperature in deg. C. Hence if none of the heat were radiated away,

$$\theta = 0{\cdot}24 \times \frac{i^2 R t}{sw}$$

Since the resistance of metals increases as they rise in temperature, a thin wire heated by the current will resist more, and grow hotter and hotter until its rate of loss of heat by conduction and radiation into the surrounding air equals the rate at which heat is supplied by the current.

The following pretty experiment illustrates the laws of heating. The current from a few cells is sent through a chain made of alternate pieces (Fig. 260*a*) of copper C and iron F wires of equal gauge. The iron links glow red-hot

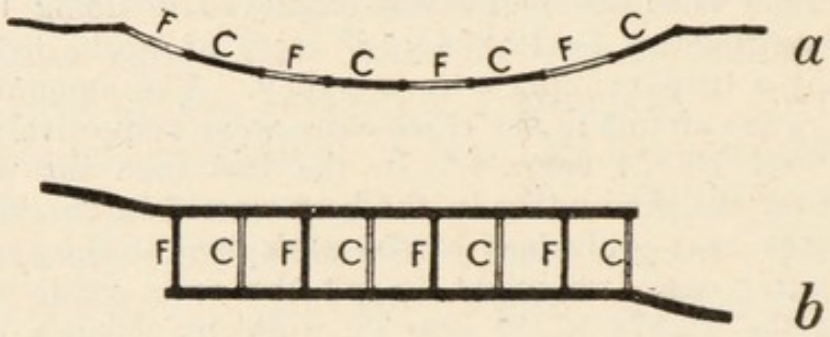


FIG. 260.—Wire Links heated—*a* in Series, *b* in Parallel.

while the copper links remain comparatively cool. The explanation is that the resistivity of iron is about seven times that of copper, and its capacity for heat about three-quarters as great; hence the rise of temperature in wires of equal thickness traversed by the same current is roughly nine times as great for iron as for copper.

Thin wires heat much more rapidly than thick ones carrying the same current; *the rise of temperature in different parts of the same wire* (carrying the same current) *would be*, for different thicknesses, *inversely proportional to the fourth power of the diameters* if they had equal surfaces for radiation.

Thus, suppose a wire at any part to have been reduced to *half* its diameter, the cross-section will have an area $\frac{1}{4}$ as great as in the thicker part. The resistance here

will be 4 times as great, and the number of heat units developed will be 4 times as great as in an equal length of the thicker wire. But 4 times the amount of heat spent on $\frac{1}{4}$ the amount of metal would warm it to a degree 16 times as great : and the thin wire has only half as much surface for getting rid of heat. But the hotter a body becomes the more freely does it radiate heat to things around it. For wires of given material, the current needed to raise them to an equal temperature varies as the square root of the cube of the diameter. This law applies to the sizes of wires used as *safety-fuses* in electric lighting. These are pieces of tin wire interposed in the circuit to melt if by any chance the current becomes abnormally strong.

If supplied *at the same voltage*, thin wires heat *less* than thick ones of the same length and material ; for they offer a greater resistance, and therefore less current flows through them. For this case it is convenient to state Joule's law in another form. Since $iR = V$, and $i^2 = V^2 \div R^2$, the substitution of this in the formula of Art. 462 gives us

$$U = 0{\cdot}24 \times V^2 t \div R.$$

The heat developed in a resistance R at a constant voltage V is *inversely proportional to the resistance.*

If a grid is made of a number of iron and copper wires of equal length and thickness arranged in parallel, as in Fig. 260*b*, and a strong current is sent through them, the copper links will heat while the iron ones remain cool.

465. Hot-wire Instruments.—The current flowing through a long thin platinum wire of high resistance, when it is made to connect two points on a circuit, will measure the potential difference between these two points. Owing to the wire becoming warmed it will expand ; and its expansion may be made to move a hand over a dial graduated to read volts (Fig. 261) ; and it becomes a *hot-wire voltmeter.* Fig. 262 depicts the arrangements in a

modern *hot-wire amperemeter*. The current to be measured passes through a horizontally stretched fine wire, which is pulled downwards by a second wire that is itself stretched sideways by a spring S, by means of a fine thread passing around a small roller. When a current passes through the fine wire it heats it, causing it to expand slightly. As the spring pulls it down through the second wire it turns the roller and moves an indicating hand over a scale. The scale is

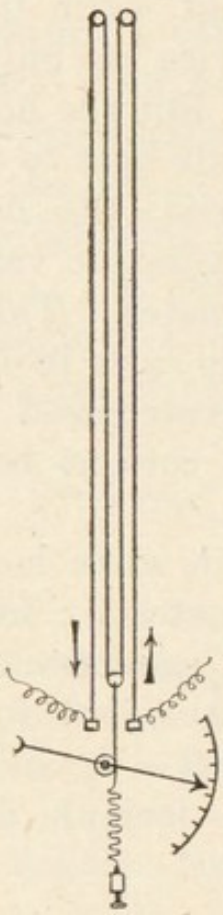


FIG. 261.—Cardew's Hot-wire Voltmeter.

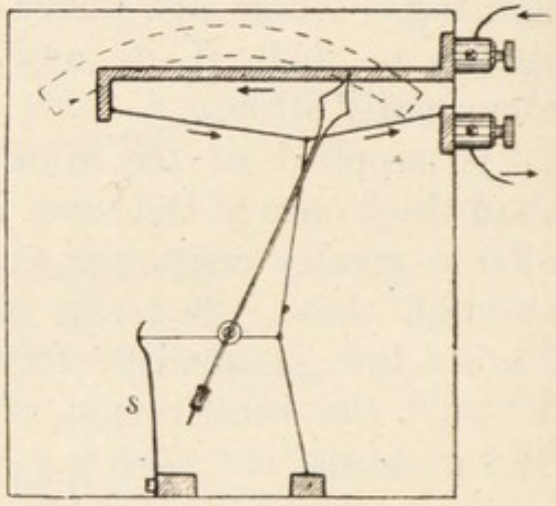


FIG. 262.—Hot-wire Amperemeter.

graduated by finding experimentally the points to which the hand turns when 1 ampere, 2 amperes, etc., are passed through the instrument. Hot-wire instruments are specially applicable for measuring alternating currents, since a wire heats whichever way the current flows along it.

466. Electric Cautery.—For surgical purposes a thin platinum wire, heated red-hot by a current, is sometimes used instead of a knife, as, for example, in the operation of amputating the tongue for cancer. Platinum is chosen on account of its infusibility, but even platinum wires are fused by the current if too strong.

467. Blasting by Electricity.—In consequence of these heating effects, electricity can be applied in blasting

and mining to ignite the charges. Stout conducting wires are carried from an appropriate battery at a distance to a special *fuse*, in which a very thin platinum wire is joined in the circuit. This wire becomes hot when the current flows; and being laid amidst an easily combustible substance to serve as a priming, ignites this and sets fire to the charge of gunpowder. Submarine mines are thus exploded beneath the water, and at any desired distance from the battery.

468. Electric Welding.—If two wires or rods of metal are held together with sufficient force while a very large current is passed through them, much heat is developed at the junction, so that they soften and become welded together. The processes of *electric welding* have been perfected by Elihu Thomson, who has utilized for this purpose alternating-current transformers (Art. 538) to produce currents of many hundred amperes at a pressure of a few volts.

A singular effect is noticed when two iron rods connected to the two poles of a powerful source at 50 or more volts are dipped into water. The rod which serves as kathode is observed to be covered with a luminous layer, and it presently becomes red-hot. Guthrie, who first investigated this phenomenon in 1876, ascribed the heating to the resistance of a film of hydrogen. This effect has been made the basis of a welding method.

469. Electric Furnaces.—Electric furnaces are of three kinds: (i.) *resistance furnaces*, in which a current is sent through a special resistance of platinum, nickel, or other refractory wire, to act as a heater; (ii.) *arc furnaces* in which an electric arc is caused to play inside a crucible to melt the contents; (iii) *induction furnaces*, in which a current is produced, in the material to be melted, inductively, that is by a species of transformer action (see Art. 538). By these means higher temperatures can be attained than those in ordinary combustion furnaces;

moreover the furnace is more compact, more efficient, and free from ordinary products of combustion.

Electric furnaces are now largely used for steel-refining, for the manufacture of aluminium, calcium carbide, carborundum; and for hardening steel tools. Also for the production of nitrates from the nitrogen of the atmosphere. (See Art. 529.)

470. Electric Cooking.—Since public supplies of electricity became common, electric stoves, ovens, and heaters for cooking, stewing, etc., have become articles of commerce. The heating is effected by passing currents through resistance-wires embedded in cement or other suitable insulating material. These wires are usually of nickel, or of an alloy called *nichrome* containing nickel and chromium. Electric cooking probably does not pay, as compared with the use of fuels, if the price charged for electric energy exceeds one penny per unit. But there are obvious advantages in cleanliness and avoidance of products of combustion.

LESSON XXXVII.—*Thermo-Electric Currents*

471. Seebeck Effect.—In 1821 Seebeck discovered that a current may be produced in a closed circuit by heating a point of contact of two dissimilar metals. If a piece of bismuth and a piece of antimony be soldered together, and their free ends connected with a short-coil galvanometer, it is found that if the junction be warmed to a temperature higher than that of the rest of the circuit, a current flows in the direction from bismuth to antimony across the heated point; the current being proportional to the excess of temperature. If the junction is cooled below the temperature of the rest of the circuit a current in the opposite direction is observed. The electromotive-force thus set up will maintain the current so long as the excess of temperature of the heated point

is kept up ; heat being all the while absorbed in order to maintain the energy of the current. Such currents are called **Thermo-electric currents**, and the electromotive-force producing them is known as *Thermo-electromotive-force.*

472. Peltier Effect.—In 1834 Peltier discovered a phenomenon which is the converse of that discovered by Seebeck. He found that if a current of electricity from a battery be passed through a junction of dissimilar metals the junction is either heated or cooled, according to the direction of the current. Thus a current which passes through a bismuth-antimony pair in the direction from bismuth to antimony absorbs heat in passing the junction of these metals, and cools it ; whereas, if the current flow from antimony to bismuth across the

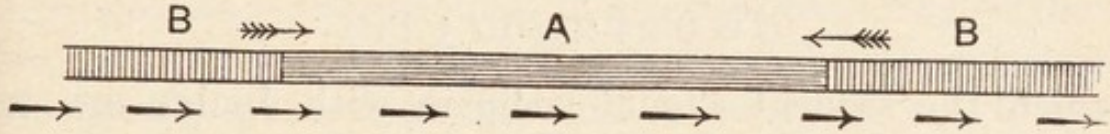


FIG. 263.—Diagram of Peltier Effect.

junction it evolves heat, and the junction rises in temperature. It is clear that if bismuth is positive with respect to antimony, any current that may be caused to flow from bismuth to antimony is aided by the electromotive force at that junction ; whilst any current flowing from antimony to bismuth will meet with an opposing electromotive-force. In the latter case the current will do work and heat the junction ; in the former the current will receive energy at the expense of the junction, which will give up heat. In Fig. 263, the feathered arrows at the junctions represent the Peltier electromotive-forces, and the plain arrows the direction of the current.

This phenomenon of heating (or cooling) by a current, where it crosses the junction of two dissimilar metals (known as the " Peltier effect," to distinguish it from the ordinary heating of a circuit where it offers a resistance to the current, which is sometimes called the " Joule

effect"), is utterly different from the evolution of heat in a conductor of high resistance, for (*a*) the Peltier effect is *reversible*; the current heating or cooling the junction according to its direction, whereas a current meeting with resistance in a thin wire heats it, whichever be the direction it flows; and (*b*) the amount of heat evolved or absorbed in the Peltier effect is proportional simply to the current, not to the *square* of the current as the heat of resistance is.

The complete law of the heat developed in a circuit will therefore require to take into account any Peltier effects which may exist at metal junctions in the circuit. If the letter P stand for the difference of potential due to the heating of the junction, expressed as a fraction of a volt, then the complete law of heat is

$$U = 0{\cdot}24 \times (i^2Rt \pm Pit),$$

which the student should compare with Joule's law in Art. 462. The quantity called P is also known as *the coefficient of the Peltier effect*; it has different values for different pairs of metals, and is numerically equal to the number of *ergs* of work which are evolved as heat at a junction of the particular metals by the passage of one absolute unit (10 *coulombs*) of electricity through the junction. The reversible heat alone $= \pm 0{\cdot}24 \times Pit$.

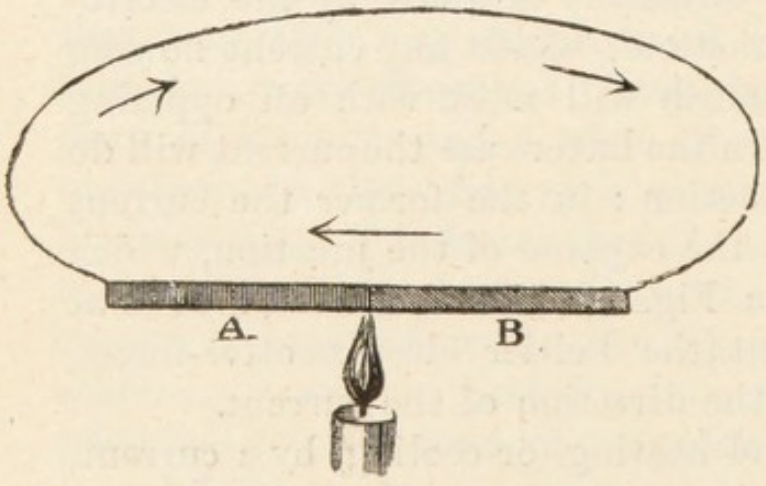


FIG. 264.—Simple Thermo-electric Couple.

473. Thermo-electric Laws.—The thermo-electric properties of a circuit are best studied by reference to the simple circuit of Fig. 264, which represents a bismuth-antimony pair united by a copper wire. If all parts of

the circuit are at one temperature, even though there may be at the junctions electromotive-forces as suggested above, there will be no current, since the electromotive-forces are in equilibrium. But when a junction is heated this equilibrium no longer exists, and there will be a resultant electromotive-force. It is found to obey the following laws :—

(i.) *The thermo-electromotive-force is, for the same pair of metals, proportional* (through limited ranges of temperature) *to the excess of temperature of the junction over the rest of the circuit.*

(ii.) *The total thermo-electromotive-force in a circuit is the algebraic sum of all the separate thermo-electromotive-forces in the various parts.*

It follows from this law that the various metals can be arranged, as Seebeck found, in a series, according to their thermo-electric power, each one in the series being thermo-electrically positive (as bismuth is to antimony) toward one lower down.

474. Thermo-electric Power.—In the following table is shown the *thermo-electric series* of metals, together with the thermo-electric power of each when cold. The term *thermo-electric power* of a metal means the electromotive force per degree (centig.) for a pair made of that metal with the standard metal (lead). In the table the numbers are microvolts per degree.

+ Bismuth	89 to 97
Nickel	22
German-silver . . .	11·75
Lead	0
Platinum . . .	− 0·9
Copper	− 1·36
Zinc	− 2·3
Iron	− 17·5
Antimony . . .	− 22·6 to − 26·4
Tellurium . . .	− 502
− Selenium . . .	− 800

A very small amount of impurity may make a great

difference in the thermo-electric power of a metal; and some alloys, and some of the metallic sulphides, as galena, exhibit extreme thermo-electric properties.

The electromotive-forces due to heating single pairs of metals are very small indeed. If the junction of a copper iron pair be raised 1° C. above the rest of the circuit its electromotive-force is only 16·14 microvolts. That of the more powerful bismuth-antimony pair is for 1° C., about 117 microvolts. Thermo-electric power varies, however, with temperature: for example, that of iron is really $-17{\cdot}5+0{\cdot}049t$ (where t is the mean temperature of the two junctions), iron becoming less negative when hot. Copper is $-1{\cdot}36-0{\cdot}01t$, becoming more negative. There will be obviously one particular temperature or *neutral point*, at which the powers of iron and copper will be equal.

475. Thermo-electric Inversion.—Cumming discovered that in the case of iron and other metals an inversion of their thermo-electric properties may take place at a high temperature. In the case of the copper-iron pair the temperature of 275° is a neutral point; below that temperature the current flows through the hotter junction from the copper to the iron; but when the circuit is above that temperature iron is thermo-electrically positive to copper. The neutral point for a zinc-iron pair is about 200°. The inversion is easily shown by heating the junction of two long strips of these metals, riveted together in a V-form, and watching the effect on a galvanometer connected to their other ends. There will at first be a deflexion which will go on increasing until the temperature of 200° is attained, but on further heating the junction the deflexion diminishes

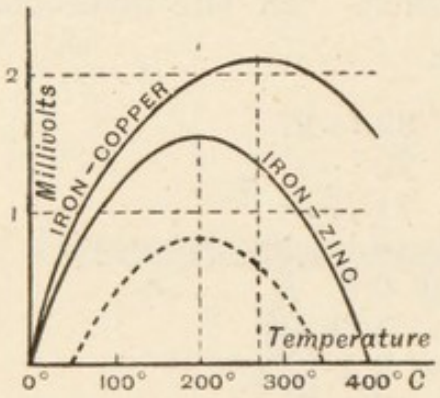


FIG. 265.—Diagram of Thermo-electric Inversion.

and at about 400° reverses, the current flowing the other way. Fig. 265 shows graphically the curves obtained with iron-zinc and iron-copper pairs when one junction is kept at 0° while the other is heated. The dotted line is for the iron-zinc pair when one junction is kept at 50° and the other heated.

476. Thermo-electric Diagram.—The facts of thermo-electricity are best studied by means of the dia-

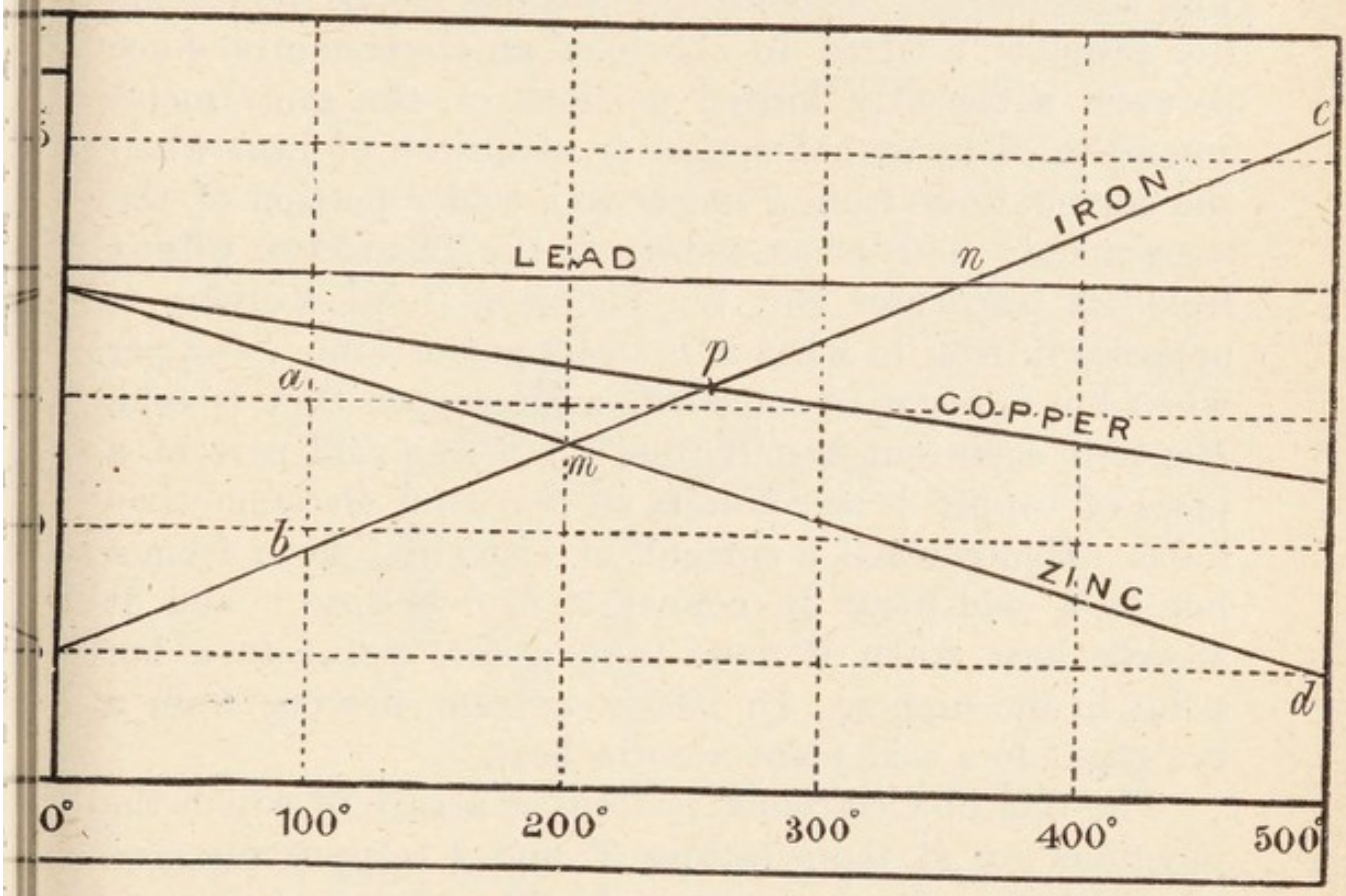


FIG. 266.—Diagram of Thermo-electric Electromotive-forces.

grams suggested by Lord Kelvin and constructed by Professor Tait. In that given in Fig. 266 the horizontal divisions represent the temperatures; the vertical distances indicating the thermo-electric power, in microvolts per degree. These powers are measured with respect to the metal lead, which is taken as the standard of zero at all temperatures, because, while with other metals there appears to be a difference of potentials between the metal hot and the same metal cold, hot lead brought into

contact with cold lead shows no perceptible thermo-electric difference.

An example will illustrate the usefulness of the diagram. Let a circuit be made by uniting at both ends a piece of iron and a piece of zinc; and let the two junctions be kept at 0° and 100° respectively by melting ice and boiling water. Then the total electromotive-force round the circuit is represented by the area a, 0, -15, b. The slope of the lines for the various metals represents the property referred to above, of an electromotive-force between differently-heated portions of the same metal accompanied by an absorption or evolution of heat when the current flows from a hotter to a colder portion of the same metal. This effect, known as the **Thomson effect** from its discoverer Sir W. Thomson (Lord Kelvin), is opposite in iron to what it is in copper or zinc. Copper when hot is negative compared with copper that is cold. Hence if a current is sent from a hot to a cold part of a piece of copper it encounters an opposing electromotive-force. Hence when a current of electricity flows from a hot to a cold point in copper it evolves heat; and it absorbs heat when it flows from a cold point to a hot point in the copper. In iron a current flowing from a hot point to a cold point absorbs heat.

The thermo-electromotive-force of a pair, of which the junctions are at temperatures T and t respectively, and of which n is the temperature of the neutral point, may be conveniently expressed by the following formula:—

$$\mathrm{E} = p\,(\mathrm{T} - t)\left\{1 - \frac{\frac{1}{2}(\mathrm{T}+t)}{n}\right\};$$

where p is the volts per degree (at 0°) as given in the table (Art. 474).

477. Thermo-electric Piles.—The electromotive-force of a bismuth-antimony pair, when the junctions are kept at 0° and 100°, is only 0·0115 volt. In order to increase the electromotive-force of thermo-electric pairs it is usual to join a number of pairs of metals (preferably

bismuth and antimony) in series, but so bent that the *alternate* junctions can be heated as shown in Fig. 267 at BBB, whilst the other set AAA are kept cool. The various electromotive-forces then all act in the same direction, and the current is increased in proportion to the number of pairs of junctions. Powerful thermo-electric batteries have been made by Clamond, Noe, and others. Such batteries have been made of groups of pairs of iron and an alloy of zinc with antimony, arranged

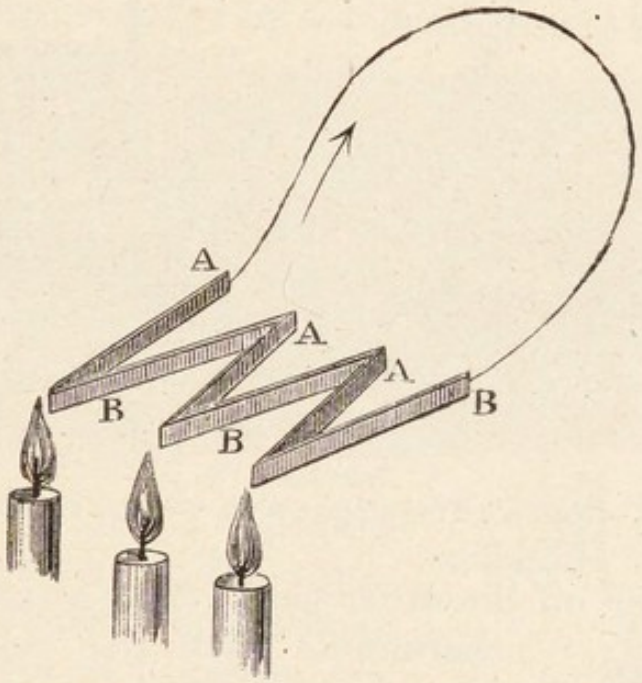


FIG. 267.—Battery of Three Thermo-electric Pairs.

around a small furnace; but it is extremely difficult to maintain them in effective action for long, as they fail after continued use, probably owing to a permanent molecular change at the junctions. In the hands of Melloni the thermo-electric pile or **thermopile**, constructed of many small pairs of antimony and bismuth united in a compact form, proved an excellent electrical thermometer when used in conjunction with a sensitive short-coil astatic galvanometer. For the detection of excessively small differences of temperature the thermo-pile is an invaluable instrument, the currents being proportional to the difference of temperature between the

hotter set of junctions on one face of the thermopile and

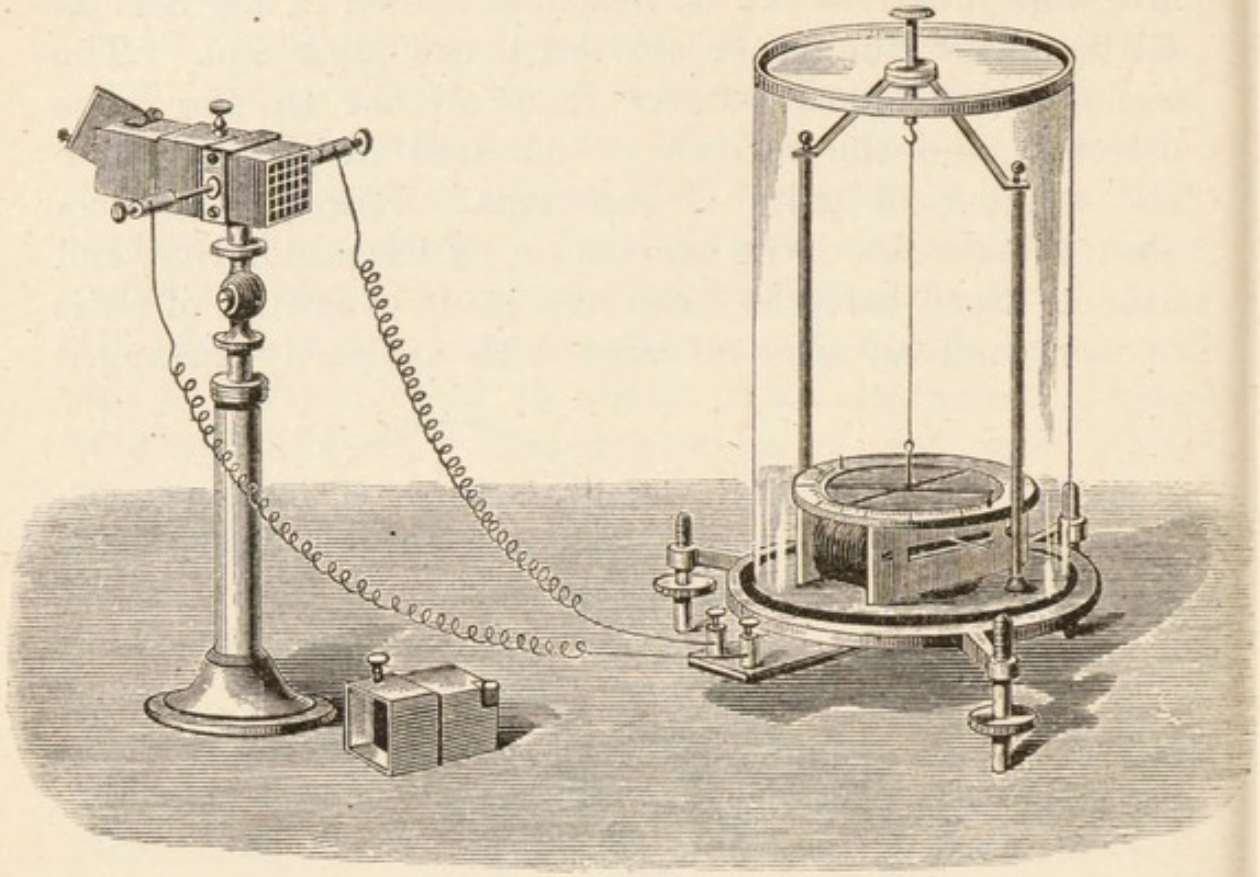


FIG. 268.—Nobili's Thermopile with Astatic Galvanometer.

the cooler set on the other face. The arrangement of a thermopile with the old astatic galvanometer is shown in Fig. 268. A thermopile devised by Rubens, which has a small thermal capacity, and therefore is quick in its action, consists of a number of junctions of iron and constantan wires. The E.M.F. generated is 53 *microvolts* per centigrade degree per couple. The junctions are arranged in a zigzag form (Fig. 269), so that the alternate junctions are in a vertical straight line; the remaining junctions being half to one side and half to the other side, thus escaping being heated. This arrangement of the working junctions

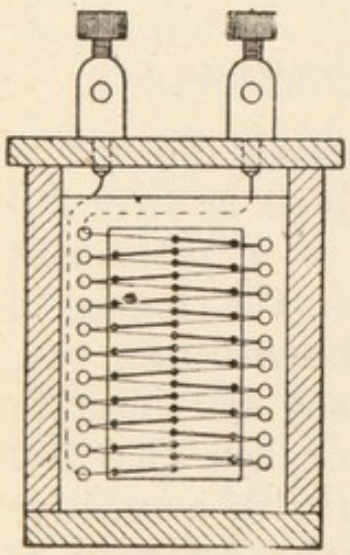


FIG. 269.—Rubens's Thermopile.

in a vertical line is very convenient for the examination of the heat-spectrum.

478. Thermo-galvanometers.—A still more sensitive arrangement for detecting minute heating due to radiation consists in suspending between the poles of a powerful magnet a closed circuit having a bismuth-antimony junction in it. Sturgeon proposed such a thermo-galvanometer in 1835.

In the radio-micrometer of Vernon Boys (1889) a loop of silver wire, suspended by a delicate quartz fibre between the poles of a magnet (Fig. 270), has its circuit closed at its lower end by a piece of antimony and a piece of bismuth (or alloys of these metals) soldered to a minute disk of copper foil. A rise of temperature of the copper foil even so small as one millionth of a degree will generate a current in the loop and give a deflexion over one division of the scale. With an instrument of this kind the radiant heat of a candle can be detected at a distance of two miles.

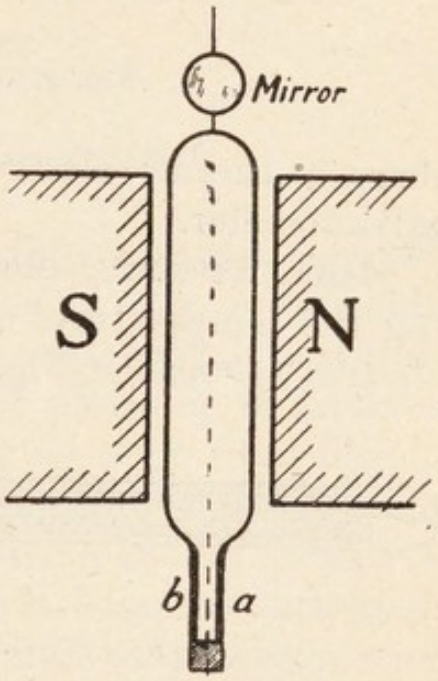


FIG. 270.—Boys's Radio-micrometer.

Duddell's thermo-galvanometer consists of an arrangement like Fig. 270, with the addition of a small heater (a platinum resistance) through which is carried the current to be measured. The deflexions are approximately proportional to the heat developed in the heater. A current of half a micro-ampere can thus be detected.

479. Thermal Cross.—Fig. 271 depicts an arrangement, useful for measuring small alternating currents, in which two wires of metals such as iron and nickel are twisted into a junction J; two ends, *a*, *b*, of the cross being joined to a galvanometer G; the other two ends,

a', b', going to an external circuit. Any current passing along this external circuit heats the junction, evoking

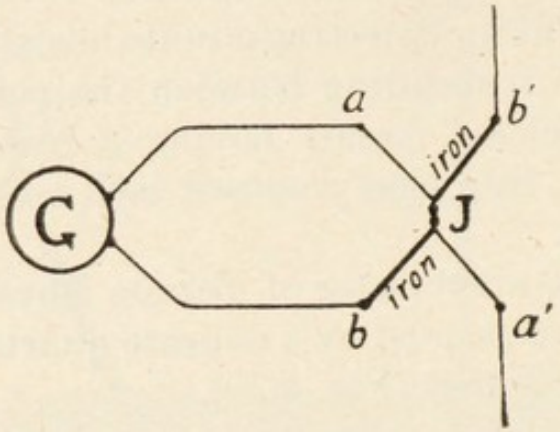


FIG. 271.—Thermo-electric Cross.

there a thermo-electromotive-force and deflecting the galvanometer.

480. Thermo-electric Pyrometers.—For measuring the temperatures of furnaces Le Chatelier devised an *electric pyrometer* (Fig. 272), consisting of a pair of highly

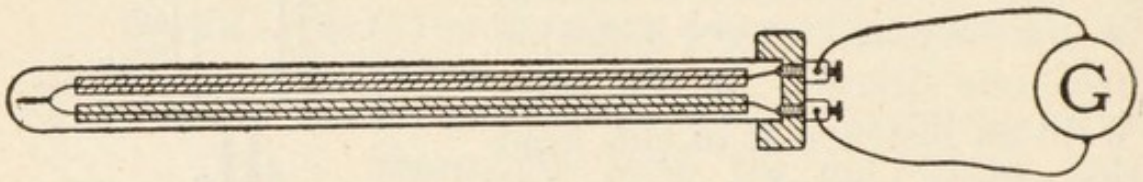


FIG. 272.—Thermo-electric Pyrometer.

infusible wires, one of platinum, the other of a rhodio-platinum alloy, united at a junction that can be introduced into a furnace. They are enclosed in a tube of porcelain. The other ends of the wires are connected to a suitable galvanometer or millivoltmeter, which may be calibrated directly so as to read the furnace temperatures direct in centigrade degrees. In Foster's pyrometer the couple is made of two alloys of chromium and nickel in different proportions.

For other appliances of electric thermometry see Darling's *Pyrometry*.

CHAPTER VIII

ELECTRIC LIGHT

LESSON XXXVIII.—*Glow-lamps*

481. Development of the Glow-lamp.—Glow-lamps consist of a thin wire or filament of some infusible conductor, enclosed in a glass bulb, and heated to whiteness by the current. Thin wires of platinum or iridium were often suggested, but could not be kept from fusing. Edison in 1878 devised a lamp consisting of a platinum spiral combined with a short-circuiting switch to divert the current from the lamp in case it became overheated. Swan in February 1879 publicly showed a carbon wire lamp in a vacuous bulb. Edison in October 1879 devised a vacuum lamp with a coiled filament made of lamp-black and tar carbonized. Swan in January 1880 prepared filaments from cotton thread parchmentized in sulphuric acid, and afterwards carbonized. Edison in 1880 substituted a flat strip of carbonized bamboo for a filament.

For twenty years the carbon glow-lamp held the market, to be superseded by new kinds having metallic filaments. First, Auer von Welsbach (1898) employed wires of osmium, followed by von Bolton (1903) using tantalum, and by Just and Kuzel (1904–5) using tungsten. Whatever the material, it must be exceedingly refractory, it must have a high electric resistance, and it

must be capable of being fashioned into a wire not much thicker than a hair, or even thinner.

482. Carbon Glow-lamps.—Carbon glow-lamps mostly have fine carbon wires prepared from threads of parchmentized cellulose, which are then carbonized in a closed vessel. Sometimes the filaments are "flashed" over with surface carbon by being momentarily heated electrically in a carbonaceous atmosphere. They are mounted upon supports in a glass bulb through which leading-in wires pass out, and into which they are sealed; the bulbs being afterwards exhausted of air and other gases. The vacuum is made very perfect by the employment of special mercurial air-pumps. The bulbs should be heated during exhaustion to drive out residual gases. Two early forms of glow-lamp are shown in Fig. 273: the form used by Swan in England, and that perfected by Edison in America. The resistance of such lamps varies according to size and length of the filament. A 16-candle-power carbon lamp for use on a 100-volt circuit will take about 0·6 ampere. That is to say, its resistance when hot will be about 166 ohms, or over 200 ohms when cold, since carbon has the property of offering a lower resistance when hot than when cold, the reverse of that observed in metals. It will absorb about 60 watts. This is at the rate of less than 4 watts per candle. Used so, it will last on the average over 1000 hours of burning. Lamps are made to give equal light and use less current, by using a thinner and rather shorter filament; but then they do not last so long. The surface disintegrates in time if forced to emit too much light. The power required to operate 12 such 60-watt lamps will be 720 watts, or nearly 1 horse-power.

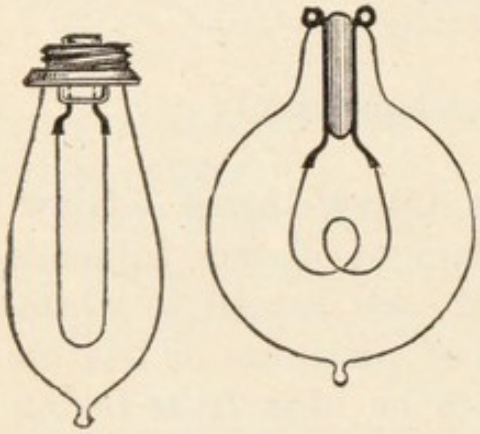


FIG. 273.—Carbon Glow-lamps.

The light increases as about the sixth power of the volts; the energy consumed is only as the second power. But raising the volts a little, shortens the life enormously: an increase of only 6 per cent reduces the life to about one-third of the normal value. The temperature attained is usually under 2000° C. These lamps deteriorate with use; the candle-power going down after 1000 hours' use by some 25 or 30 per cent. Though carbon is practically infusible, carbon glow-lamps must not be supplied with too much current; for, when overrun, though they give more light for the time, they speedily perish owing to a disintegration of the glowing surface.

Glow-lamps are usually grouped in parallel (see Art. 558 and Fig. 330) between mains kept at constant voltage. The usual voltages employed are 100 to 110 volts, and 200 to 220 volts. For higher voltages the thinness of the filaments renders them undesirable. Little fairy-lamps of 1 to 8 candle-power, with short filaments for lighting by batteries, work at from $1\frac{1}{4}$ to 10 volts.

483. Metallic Glow-lamps.—The temperature of fusion of most metals is below a white heat. Amongst the highest are platinum, 1755° C.; titanium, 1900°; iridium, 2300°; osmium, 2700°; tantalum, 2850°; tungsten, 3000°. Most of these are not only refractory but very hard; and there are great mechanical difficulties in drawing them into wires. Osmium, tantalum, and tungsten have all been used with success; but osmium is too dear for commercial use. Tungsten can now be drawn into wires of extreme tenuity and strength and has come into general use for glow-lamps. But when glowing it readily combines with oxygen: hence in tungsten lamps care must be taken that the bulbs shall

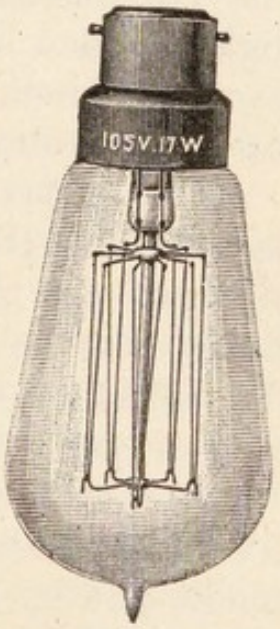


FIG. 274.—Metallic Filament Glow-lamps.

be most perfectly exhausted of air. The fine wires are stretched in zigzags upon an interior frame as seen in Fig. 274, which represents one of the glow-lamps of the Osram Company. Owing to the high resistance and the very high temperature which tungsten can withstand, the tungsten lamps are very efficient, particularly those of large candle-power, in which during their life the efficiency may attain the value of $1\frac{1}{4}$ candles per watt.

The following table gives some data about a 60-watt, 100-volt tungsten lamp if used at different voltages :—

Volts.	Amperes.	Watts.	Candle-power.	Watts per Candle.	Probable Life (Hours).
90	0·565	51	31	1·65	8400
95	0·58	55	38	1·45	3250
100	0·60	60	48	1·25	1200
105	0·62	65	55	1·10	540
110	0·635	70	70	1·00	280

The circumstance that the resistance of the metals rises slightly when heated, whereas that of carbon falls, is in favour of metallic filament lamps, as their light varies less if the voltage of the mains should be unsteady.

484. Nitrogen-filled Lamps.—Recently it has been found that if the bulb is filled with very pure nitrogen gas at about atmospheric pressure, tungsten lamps may be run at still higher temperatures, so that the efficiency of a nitrogen-filled lamp goes up to 2 candles per watt. These are known commercially as "half-watt" lamps, meaning half a watt per candle-power. In many instances large nitrogen-filled lamps of 1000 candle-power, consuming about 500 watts, are being substituted for arc lamps.

485. Nernst Lamps.— Reference was made in Art. 179 to the conductivity of hot solid electrolytes. In Nernst's lamp (1897) a thin rod of mixed metallic oxides, thoria and zirconia with a small proportion of

ceria, looking like a short thread of pipeclay, constitutes the light-giving body. But to make it conduct it must first be heated to dull redness by an auxiliary electric heater—a small wire coil of high resistance placed beside it. So soon as it is heated thus, it suddenly becomes conductive and glows with great brilliancy, the light which it emits depending on the peculiar selective radiating power of the ceria it contains. The glower need not be protected from air: but in order to limit the current through it, there is placed in series with each lamp a ballasting resistance made of iron wire enclosed in a vacuous bulb. The ballasting resistance increases its resistance with increase of temperature, and thus when placed in series with the glower compensates for the decreased resistance of the latter when hot, and a steady current is therefore maintained. Though the efficiency of this lamp may be as high as 0·4 candles per watt, the complications of automatic devices to switch the current from the heater to the glower have militated against its use.

LESSON XXXIX.—*Arc Lamps*

486 The Electric Arc.—If two pointed pieces of carbon are joined by wires to the terminals of a powerful voltaic battery or other generator of electric currents, and are brought into contact for a moment and then drawn apart to a short distance, a kind of electric flame called the **arc**, or "voltaic" arc, is produced between the points of carbon, and a brilliant light is emitted by the white-hot points of the carbon electrodes. This phenomenon was first noticed by Humphry Davy in 1800, and its explanation appears to be the following:—Before contact the difference of potential between the points is insufficient to permit a spark to leap across even $\frac{1}{10000}$ of an inch of air-space, but when the carbons are made to touch, a

current is established. On separating the points the spark at parting volatilizes a small quantity of carbon between the points, and ionizes the vapour by emission of electrons from the hot point of the kathode (Art. 632), or negative carbon. Carbon vapour being a partial conductor allows the current to continue to flow across the gap, provided it be not too wide; but as the carbon vapour has a very high resistance it becomes intensely heated by the passage of the current, and the carbon tips, particularly the tip of the positive carbon, also grow hot. Since, however, solid matter is a better radiator than gaseous matter, the carbons, though they are not so hot, emit far more light than the arc itself, which is of a pale violet tint. The temperature of the arc is simply determined by the temperature at which carbon volatilizes; about 3500° C. according to Violle. In the arc the most infusible substances, such as flint and diamond, melt; and metals such as gold and platinum are even vaporized readily in its intense heat. When the arc is produced in the air the carbons slowly burn away by oxidization. It is observed, also, that particles of carbon are volatilized off and torn away from the positive electrode, which becomes hollowed out to a cup-shape, or *crater*, and if the gap between the carbons is small some of these particles are deposited on the negative electrode, which assumes a pointed form, as shown in Fig. 275. The resistance of the arc varies with the length and section of the flame. The arc also apparently exerts an opposing electromotive-force of its own, amounting to

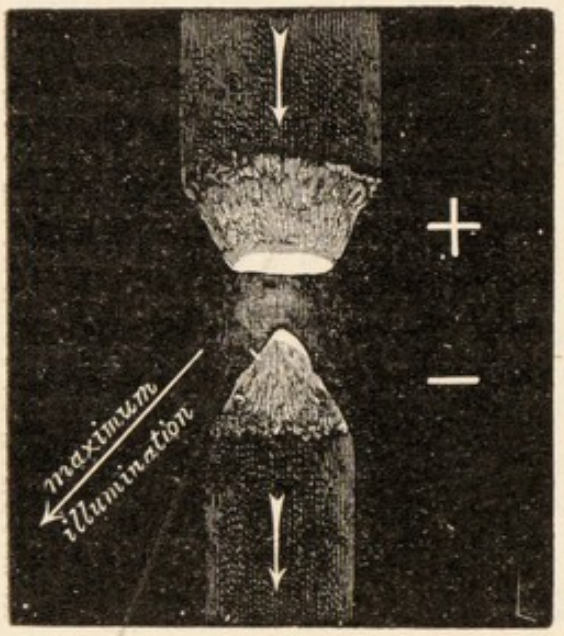


FIG. 275.—The Electric Arc.

about 39 volts when the arc is silent. The seat of this apparent back electromotive-force is at the surface of the crater where the work of volatilizing the carbon is being done. If air gets to the white-hot crater the arc becomes unstable and hisses, and the back electromotive-force is much lower. The voltage V between the carbons of a steady arc may be expressed by the formula :—

$$V = a + \frac{bl}{i},$$

where l is the length of the arc in millimetres, and a and b are constants the values of which for homogeneous carbons are respectively about 39 and 20. Thus a 4-millimetre arc length takes about 47 volts if the current is 10 amperes, or 55 volts if the current is 5 amperes. It is necessary also that there should be in series with the arc a "ballasting" resistance of about 1 ohm or more to steady the current. Without this the arc would practically be a short-circuit.

To produce an electric arc satisfactorily a minimum electromotive-force of 45 to 60 volts is necessary if continuous currents are used. With alternating currents 30 to 35 volts suffice. The usual current for arc lamps of 400 to 800 candle-power is from 5 to 10 amperes. With weaker currents or smaller electromotive-forces it is difficult to maintain a steady arc. For an ordinary arc the efficiency is about 1·5 candles per watt. The common size of carbon rod in use is 10 or 11 millimetres in diameter: the consumption is roughly 1 inch per hour; the + carbon consuming much faster than the − carbon. Being a flexible conductor, the arc can be deflected by a magnet. The arc is sensitive to draughts and must be protected by a globe. For search-lights on board ship and for lighthouses, arc lights of greater power are produced by using thicker carbons and supplying them with currents of 20 to 100 amperes or more. *Enclosed arcs* from which free access of air is excluded, consume their carbons about twenty times slower; they

work with longer arcs and require about 75 to 85 volts. Their efficiency is about 0·9 candle per watt. In practical electric lighting, the generator is always a dynamo-electric machine (Arts. 506 to 514). The internal resistance of ordinary Daniell's or Leclanché's cells is too great to render them serviceable for producing arc lights. Moreover, a battery of 40 to 60 Grove's cells (Art. 190) will not continue the supply more than 2 or 3 hours. The quantity of light emitted by an arc lamp differs in different directions, the greatest amount being emitted (when the + carbon is at the top) at an angle of about 45° downwards. The bottom carbon and its holder cut off much light in the direction vertically downwards. Fig. 276 gives a graphic curve of the distribution, the radial lines showing by their relative lengths the amounts of light emitted.

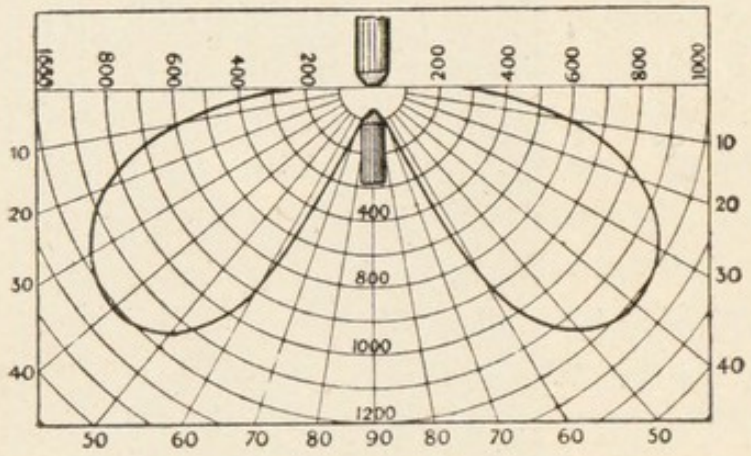


FIG. 276.—Distribution of Light of the Arc.

About 85 per cent of the light comes from the white-hot crater, very little from the negative tip. *Inverted arcs* are those with the + carbon at the bottom in order to throw the light upwards to the ceiling. The name of *flame arcs* is given to those in which certain chemicals such as calcium fluoride or aluminium fluoride are added to the carbon in order to colour the flame. In these much of the light is emitted by the flame itself. Their efficiency is about 4 candles per watt. In the alternating-current arc the carbon points are alike and emit equal light. The frequency of alternation should be at least 40 periods per second. The total quantity of light emitted, when the current is supplied at a fixed voltage, is not quite proportional to the current, but increases in a somewhat

higher ratio. Doubling the current makes rather more than twice as much light: it doubles the size of the luminous crater. Each square millimetre of the crater surface emits normally a light of about 170 candles.

487. Arc Lamps.—Davy employed wood charcoal for electrodes to obtain the arc light. Pencils of hard gas-carbon were later introduced by Foucault. In all the more recent arc lamps, pencils of a more dense and homogeneous artificial coke-carbon are used. These consume away more regularly, and less rapidly, but some automatic contrivance is necessary to push the points of the carbons forward as fast as needed. The mechanism of the arc lamp should "strike" the arc by causing the pencils to touch, and then separate them to the requisite distance, about 5 millimetres; the mechanism should also "feed" the carbons into the arc as fast as they are consumed; and it should also cause the points to approach or recede automatically in case the arc becomes too long or too short; it should further bring the carbons together for an instant to strike the arc again, if by any chance the flame goes out. *Arc Lamps*, fulfilling these conditions, have been invented by a number of persons. The earliest was invented in 1847 by W. E. Staite. If the condition of supply is constant voltage the arc lamps must be connected *in parallel*; if arc lamps are to be run *in series*, the same current flowing in succession through each of the lamps, then the supply must be of a current of unvarying strength. In this case a shunt circuit in each lamp to work the mechanism is necessary.

488. Classification of Arc Lamps.—Arc lamps may also be classified according to the *electrical arrangements* that control the mechanism, there being three types according to whether the electromagnet is of thick wire in the main circuit *in series* with the arc, or is of fine wire and *in shunt* with the arc; or, in the third case, both sorts are present. The accompanying table sets forth these different varieties:—

ARC LAMPS CLASSIFIED ACCORDING TO TYPE ADOPTED FOR THE ELECTRIC CONTROL OF MECHANISM

Type A (**Series** Electromagnet only).	Type B (**Shunt** Electromagnet only).	Type C (**Series** and **Shunt** Electromagnets).
Initial State— Carbons closed by weight (or spring).	Carbons parted by action of counterpoise or counterspring.	Carbons either closed or parted.
Approach— Due to weight (or spring).	Due to shunt magnet overcoming opposing counterpoise or spring.	Due to shunt magnet or to weight or spring.
Recession— Due to series magnet overcoming weight (or spring).	Due to counterpoise or counterspring.	Due to series magnet.
When current is switched on— Series magnet is strong because carbons touch. Recession begins, thus *striking* the arc.	Shunt magnet is strong because carbons are open, and overpowers spring or counterpoise. Approach begins causing carbons to touch. When they touch shunt magnet weakens, causing recession to begin, and *striking* occurs.	(*a*) *If carbons closed initially*, series overcomes shunt (alone, or plus weight or spring), thus *striking* the arc. (*b*) *If carbons open initially*, shunt is strong, producing approach. When carbons touch, series magnet overcomes shunt, thus *striking* the arc.
When arc grows long— Series magnet weakens, thus permitting *feeding* due to weight or spring.	Shunt magnet strengthens, thus overpowering counterpoise and so permitting *feeding* to occur.	Shunt magnet overpowers series magnet, thus permitting *feeding* to occur.

489. Mechanism of Arc Lamps.—Arc lamps may be classified in respect of their mechanism as follows :—

(*a*) *Clockwork Lamps.* — In an early pattern of "regulator" designed by Foucault the carbon-holders were propelled by a train of clockwork wheels actuated by a spring. An electromagnet through which the current runs, attracts an armature and governs the clockwork, causing the carbons to part from or approach to one another as required. In many modern arc lamps the weight of the carbon-holders drives the clockwork mechanism. Of this class was Serrin's lamp, which from 1855 onwards was largely used for light-houses. A modern sort of clockwork lamp is depicted diagrammatically in Fig. 277. Here a flexible band which connects the carbon-holders passes round a pulley and drives a train of geared wheels. The train is mounted to rock about a pivot at C. If the train is rocked over to the left the last wheel of the train is locked against a detent D, and at the same time the pulley is raised a little, thus lifting the top carbon. If the train is rocked over to the right the wheel work is released, and lets the top carbon run down. In the arrangement shown, an electromagnet M (connected in shunt) pulls the train over to the right, and is opposed by a spring S which pulls the train to the left when there is no current on. Hence when

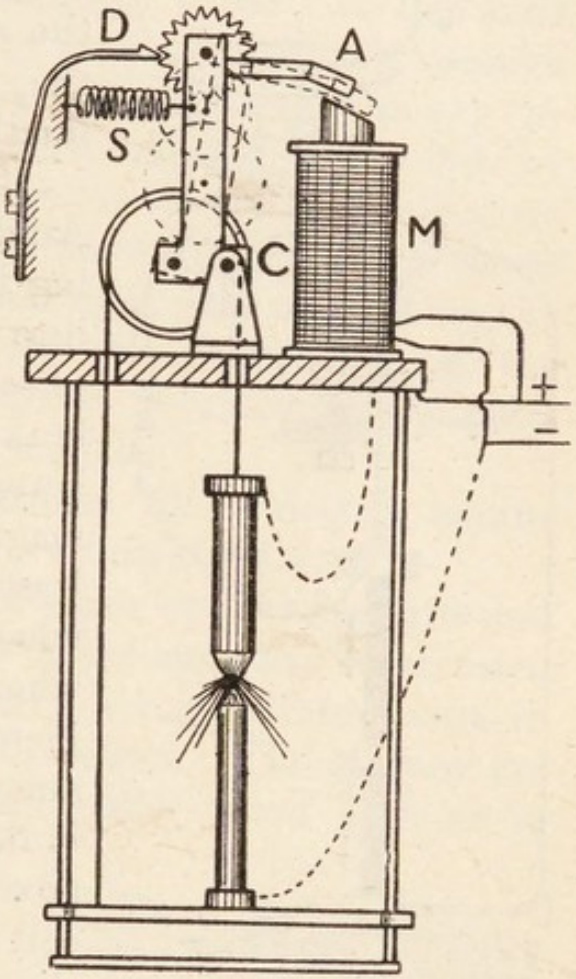


FIG. 277.—Mechanism of a Shunt Lamp.

not in use the carbons are apart. So soon as the current is switched on, the shunt electromagnet pulls strongly, and the top carbon runs down into contact. When the carbons touch, the current in the shunt circuit weakens, and the spring S pulls the rocking frame over and parts the carbons, thus *striking* the arc. When the arc grows long, more current flows round the shunt, which will then rock the frame over to the right, finally causing *feeding* to occur.

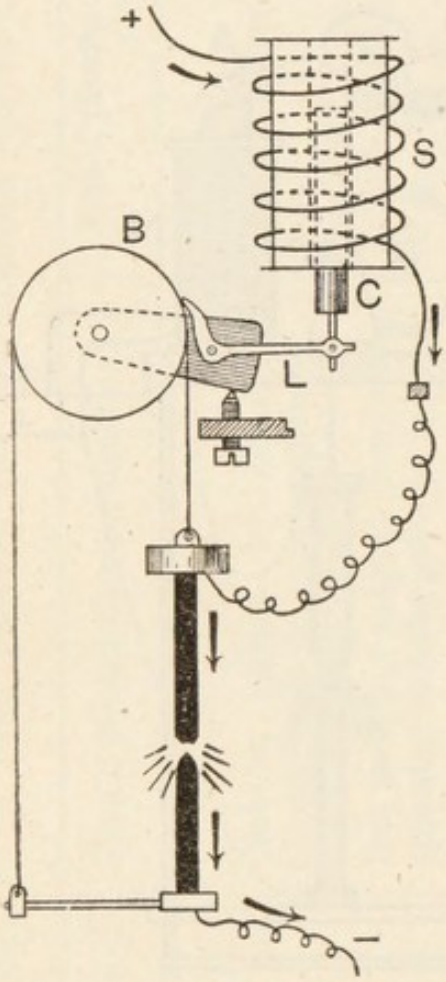


FIG. 278.—Mechanism of a Brake-wheel Lamp.

(*b*) *Brake-wheel Lamps.*—Another mechanism for regulating the rate of feeding the carbon into the arc consists in the application of a brake-wheel; the brake which stops the wheel being actuated by an electromagnet which momentarily releases the brake and allows the wheel to run forward a little when the resistance of the arc increases beyond its normal amount. In Fig. 278 B is the brake-wheel, L the lever which governs it, C an iron core of the coil S inserted in series in the circuit. When current is switched on, the core is drawn up, causing L to grip B and to turn it a little, so parting the carbons and striking the arc.

(*c*) *Solenoid Lamps.*—In this class of arc lamp the movement of one or both of the carbons is governed by an iron plunger capable of sliding vertically up or down inside a hollow coil or solenoid, which, being traversed by the current, thus regulates the length of the arc. Siemens employed two solenoids acting against one another differentially, one being a main-circuit coil, the

other being a fine-wire coil connected as a *shunt* to the arc. The shunt coil acts as a *voltmeter* to watch the arc and feed the carbons forward when the volts rise above the normal; it being set to control the feeding mechanism.

(*d*) *Clutch Lamps.*—A somewhat simpler device is that of employing a clutch to pick up the upper carbon-holder, the lower carbon remaining fixed. In this kind of lamp the clutch is worked by an electromagnet, through which the main current passes. If the lamp goes out the magnet releases the clutch, and the upper carbon falls by its own weight and touches the lower carbon. Instantly the current flows round the electromagnet, which causes the clutch to grip the carbon-holder, and raise it to the requisite distance. Should the arc grow too long, the lessening attraction on the clutch automatically permits the carbon-holder to advance a little.

(*e*) *Motor Lamps.*—Sometimes little electric motors are used to operate the carbons automatically.

490. Projector Lamps.—For optical lanterns and for search-lights, special forms of arc lamp are constructed to throw a concentrated beam in one direction. The carbons are usually either tilted back as in

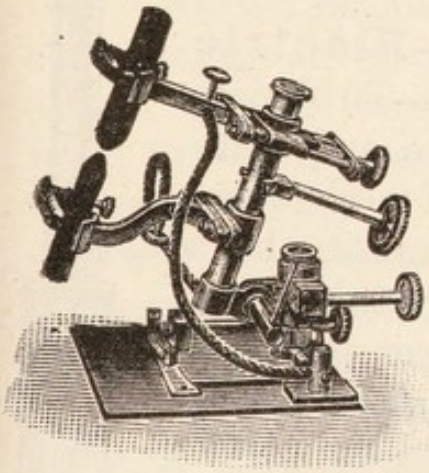


FIG. 279.—Hand-feed Projector Lamp.

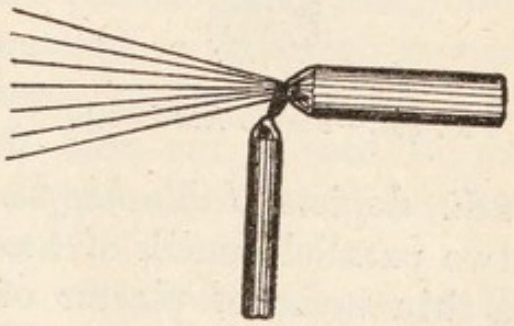


FIG. 280.—Arrangement of Carbons in a Projector Lamp.

Fig. 279, or set at right angles to one another as in Fig. 280, so that the crater throws most of its light forward. The concentration of the beam is effected by condenser lenses, or by parabolic mirrors.

491. Flame Arc Lamps.—Flame arc lamps are generally designed with the carbon-holders sloping downwards like the letter V, and so arranged that one or both of them swing so that the tips can be brought together and moved apart. The flame is therefore at the lowest point, and casts the light chiefly downwards. Fig. 281 shows a design in which the two carbons, sliding in guides, are propelled by a counterpoise weight. Automatic mechanism similar to that already described is necessary to govern the movement; *striking* the arc by momentarily causing the carbons to touch, and *feeding* the carbons downward as they are consumed.

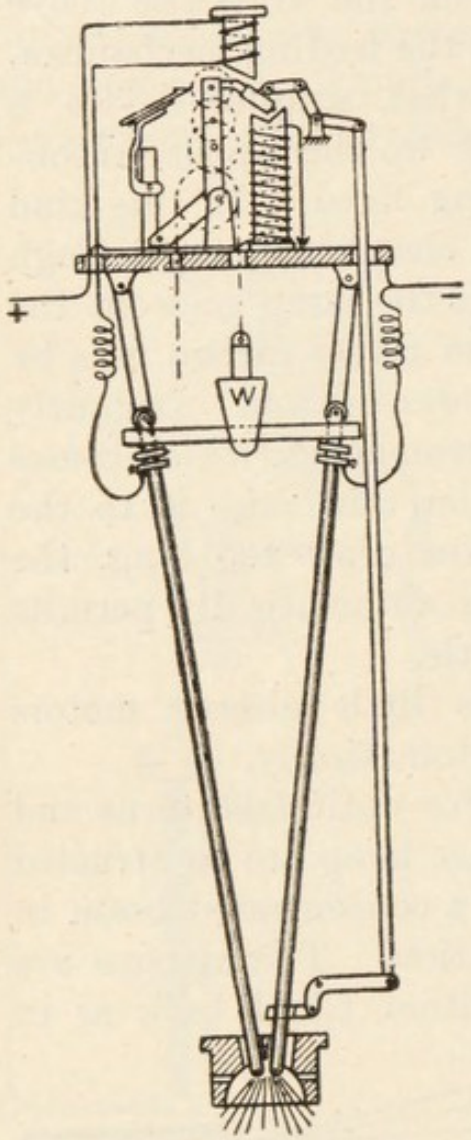


FIG. 281.—Flame Arc Lamp.

492. Electric Candles.—To obviate the expense and complication of mechanism, electric *candles* have been suggested. Fig. 282 depicts *Jablochkoff's candle*, consisting of two parallel pencils of hard carbon separated by a thin layer of plaster of Paris and supported in an upright holder. The arc plays across the summit between the two carbon wicks. In order that both carbons may consume at equal rates, alternating currents were employed.



FIG. 282. Jablochkoff Candle.

493. The Magnetite Arc.—In this American lamp the positive electrode consists of a copper piece which does not consume, while the bottom or negative electrode

is a cartridge about eight inches long packed with a mixture of black oxide of iron (magnetite) with titanium oxide. The light, which in this lamp comes solely from the flame, is thrown out sideways. The arc is about half an inch long. On a 100-volt continuous current circuit it takes about 4 amperes; and as the intensity is about 1000 candles, the efficiency is high, being about 2·5 candles per watt. But the illumination is not always steady.

494. Action of Magnets on the Arc.—An arc being a flexible conductor is capable of being dragged laterally by a magnetic field. The force acting on the arc is at right angles to the current and to the lines of the magnetic field. If a north magnetic pole is presented towards a vertical arc with the current flowing downwards, the arc bends outward towards the right. If a south pole is presented, the downward flowing arc is bent towards the left. It may even be blown out and extinguished if the magnet is strong. An arc may be caused to rotate round a magnetic pole if a tubular carbon is used with the magnet inside it. If the poles of a horseshoe magnet or electromagnet are placed at the sides of an arc, so that the current crosses the field between the poles, the arc is blown out into a pointed form resembling a blow-pipe flame. A process called *arc welding* is used, in which such an electric blow-pipe is employed. An arrangement called a *magnetic blow-out* is used for extinguishing an arc that may be casually formed between the contacts of a circuit-breaker or of a controller.

495. The Singing Arc.—It was independently found by Elihu Thomson and by Duddell that if a continuous current arc is shunted by a circuit containing a self-induction coil or a self-induction coil in series with a condenser, the arc is thrown into rapid oscillations and emits a musical sound, the pitch of which depends on the inductance and capacity of the circuit. Poulsen has made this discovery the basis of his method of radio-telegraphy

(Art. 624). The effect is enhanced if the arc is enclosed in coal-gas or a hydrocarbon vapour.

496. Vapour Lamps.—There are several forms of vapour lamps in which the light is emitted entirely from luminous conducting vapours or gases. The vapour of mercury enclosed in a vacuum tube (Art. 342) gives out an intense green light when a current is passed through it, and is utilized in the Cooper-Hewitt lamp. The light is, however, a combination of violet, blue, green, and yellow, the red rays being entirely absent, and therefore the light is not white. The light of this lamp being rich in ultra-violet rays is strongly actinic, and is very suitable for indoor photographic studios. The efficiency of this type of lamp is about 2 candles per watt.

Another vapour lamp is the Moore tube light, which consists of a long tube containing carbon dioxide or nitrogen at low pressure, and is supplied with a high-tension alternating current. The pressure of the gas is kept constant within the tube by an electromagnetically operated valve. The light given out by the tube when filled with carbon dioxide is nearly white. The efficiency of the lamp is about 0·5 candle per watt. A tube similar to the above, but filled with the rare gas neon, has an efficiency of 2 candles per watt.

CHAPTER IX

INDUCTANCE

LESSON XL.—*Mutual Inductance*

497. Mutual Inductance.— The operation of mutual induction between two circuits, a primary and a secondary, was briefly considered in Art. 241. Let us now consider the electromotive-forces so induced. Suppose the primary coil to have S_1 spirals, and the secondary coil S_2 spirals. At first let them be arranged (by use of an iron core or by geometric juxtaposition) so that all the magnetic lines evoked by the primary coil pass through all the spirals of the secondary coil; both coils being placed close together upon a suitable core of laminated iron.

By Art. 405 the magnetic flux $\mathfrak{F}$ due to current i in the primary coil will be

$$\mathfrak{F} = iS_1/Z,$$

where Z is the reluctance (Art. 404) of the magnetic circuit, and is equal to $\frac{l}{A\mu} \times \frac{10}{4\pi}$ if the core has length l, sectional area A, and permeability μ. The total amount of cutting magnetic lines by the S_2 spirals of the secondary, when current i is turned off or on, will be

$$S_2\mathfrak{F} = iS_1S_2/Z.$$

Hence it follows that the amount of cutting of magnetic lines (*i.e.* the induction in the secondary circuit)

due to turning on or off 1 ampere in the primary, will be S_1S_2/Z. This quantity is denoted for brevity by the symbol M. If the primary and secondary coils are not so arranged that *all* the magnetic lines due to the one pass through the spirals of the other, then M will have a less value than S_1S_2/Z.

The practical unit for coefficients of mutual inductance is the same as for those of self-inductance, namely, the *henry* (Arts. 381 and 501), and is 10^9 C.G.S. units. So, as the ampere is 10^{-1} of the absolute unit of current, in order to bring M to henries we must divide the above value by 10^8.

If the current in the primary is varying at the rate di/dt, the electromotive-force E_2 thereby induced in the secondary circuit will be

$$E_2 = -M \cdot di/dt,$$

where E_2 will be in volts if M is expressed in henries, i in amperes, and t in seconds.

The value of M for the small induction coils used in telephone work is usually about 0·01 henry; for a Ruhmkorff coil capable of giving a spark 10 centimetres long it may be as much as from 5 to 20 henries.

Example.—Suppose in a spark-coil the value of M is 8 henries, and the primary current changes by an amount of 1 ampere in one ten-thousandth of a second (owing to the quick-acting break), the electromotive-force induced in the secondary during that ten-thousandth of a second will be 80,000 volts.

To measure a coefficient of mutual inductance, there are several methods, some of which depend on the use of Wheatstone's bridge; but the best method is one due to Carey Foster. In this the quantity of electricity discharged from a condenser of known capacity C, shunted by a resistance p in the primary circuit, is balanced against the quantity discharged in the secondary circuit by regulating a resistance q in the latter. Then $M = Cpq$.

498. Induced Currents of Higher Orders.—

Joseph Henry, an independent discoverer of magneto-electric induction, observed that the variations in the strength of the secondary current could induce tertiary currents in a third closed circuit, and that variations in the tertiary currents might induce currents of a fourth order, and so on. A single sudden primary current produces two secondary currents (one inverse and one direct), each of these produces two tertiary currents, or four tertiary currents in all. But with alternating currents there are the same number of secondary and tertiary fluctuations as of primary; but the currents of the second, fourth, etc. orders will be inverse, in the direction of their flow, to those of the first, third, fifth, etc.

499. Lenz's Law.—In Art. 240 it was explained how an increase in the number of magnetic lines through a circuit (as by pushing in a magnet) tended to set up an inverse current, or one flowing in such a direction as is opposed to the magnetism, and therefore tends to push the magnet back. Similarly a decrease in the magnetic lines (as by withdrawing the magnet) tends to set up currents that will pull the magnet back again. Lenz[1] summed up the matter by saying that *in all cases of electromagnetic induction caused by mechanical movement, the induced currents have such a direction that their reaction tends to stop the motion which produces them.* This is known as Lenz's law: it is a particular case of the more general **law of reaction** applicable to all electromagnetic systems, namely, that *every action on such a system, which, in producing a change in its configuration or state, involves a transformation of energy, sets up reactions tending to preserve unchanged the configuration or state of that system.* (Compare Arts. 217 and 409.)

500. Eddy-Currents Induced in Masses of Metal.—In 1824 Gambey found that a compass needle oscillating in its box came to rest sooner if the bottom of

[1] Lenz, *Poggendorffs Annalen*, xxi. p. 484, 1834.

the box were made of metal than if of wood. Arago investigated the matter, and found a copper plate under the needle most effective in damping its motions. He then rotated a copper disk in its own plane underneath a compass needle, and found that the needle was dragged round as by some invisible friction. A copper disk suspended over a rotating magnet was found to be dragged by it. Attempts were made to account for these phenomena—known as *Arago's rotations*—by supposing there to be a sort of magnetism of rotation, until Faraday proved them to be due to induction. A magnet moved near a solid mass or plate of metal induces in it currents, which, in flowing through it from one point to another, have their energy eventually frittered down into heat, and which, while they last, produce (in accordance with Lenz's law) electromagnetic forces tending to stop the motion. These currents, circulating wholly within the metal, and not confined to particular paths along insulated wires, are called **eddy-currents**. If a cube or ball of good conducting metal be set spinning between the poles of such an electromagnet as Fig. 207, and the current be suddenly turned on, the spinning metal stops suddenly.

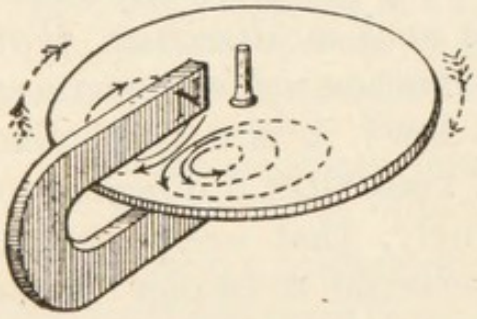


FIG. 283.—Eddy-currents in a Rotating Disk.

In a copper disk revolving between the poles of a magnet (Fig. 283) there are a pair of eddies in the part passing between the poles, and these currents tend to pull the disk back. In fact, any conductor moved forcibly across the lines of a magnetic field experiences a mechanical resistance due to the induced currents which oppose its motion. Joule in 1843, and Foucault in 1855, showed[1] that if, by sheer force, a disk or mass of metal be kept spinning between

[1] Hence some writers call the eddy-currents "Foucault's currents," though they were known years before Foucault's experiments were made.

the poles of a powerful magnet, it will become hot in consequence of the eddy-currents induced in it.

The eddy-current drag on a moving conductor (sometimes called the magnetic friction) is a force proportional to the speed and proportional to the square of the magnetic field; for the force (Art. 367) is proportional to the product of field and current, and the current (circulating round a given path) is proportional both to field and to speed. Hence eddy-current drag is employed in some forms of electric supply meter (Art. 460) as a *brake* to control the speed of the moving part.

Since the drag is proportional to the speed when the field is constant, a *speed-counter* may be made on this principle, by revolving a permanent magnet so that it drags upon a thin aluminium disk or cup that is mounted on a pivot and controlled by a spring. An index attached to the pivoted disk indicates on a scale the number of revolutions per minute of the magnet.

Alternating electric currents also set up parasitic eddy-currents in masses of metal near them; for this reason the iron cores of transformers (Art. 538) and of dynamo armatures (Art. 508) must be carefully laminated, otherwise there will be heating and waste of energy. The high resistance of stalloy (Art. 391) is here advantageous. Further, eddy-currents in any mass of metal between a primary and a secondary circuit will tend to set up, in the secondary circuit, electromotive-forces opposing those set up by the primary. Hence interposed sheets of metal act as *induction-screens.*

LESSON XLI.—*Self-Inductance*

501. Self-Inductance.—It has been pointed out in Art. 241 how when a current in a circuit is increasing or diminishing, it exercises an inductive effect upon any neighbouring circuit; this inductive effect being due to the change in the magnetic field surrounding the varying

current. But since the magnetic lines surrounding a current may, as they move inwards or outwards from the wire, cut across other parts of the *same* circuit, it is evident that a current may act inductively on itself. The self-inductive action is great if the circuit consists of a coil of many turns, and is still greater if the coil possesses an iron core. Suppose a coil of wire to possess S spirals, and that it generates a magnetic flux through these spirals of $\mathfrak{F}$ lines when current i is turned on. Then it is clear that turning on the current will have the same effect as if a magnet of $\mathfrak{F}$ lines were suddenly plunged into the coil; and turning off the current will have the same effect as if the magnet were suddenly withdrawn. Now (Art. 243) the current induced by plunging a magnet into a coil is an *inverse* current tending to push it out, while that induced by withdrawing the magnet is a *direct* current, tending to attract it back. It follows that the self-induced electromotive-force on turning the current on, will tend to oppose the current, and prevent it growing as quickly as it otherwise would do; while that induced on stopping the current will tend to help the current to continue flowing. In both these cases the effect of self-induction is to oppose change: it acts as an *electro-magnetic inertia.*

In the case supposed above, where the coil has S turns, the total cutting of magnetic lines in the operation will $= S \times \mathfrak{F}$, provided all the lines thread through all the spirals. Let the symbol L be used to represent the total amount of cutting of lines by the circuit when a current of 1 ampere is suddenly turned on or off in it. Clearly $L \times i = S \times \mathfrak{F}$. This quantity L is called "the **inductance**" of the circuit. It was formerly called "the *coefficient of self-induction*" of the circuit. The unit of inductance is named the **henry**, and corresponds to a cutting of 10^8 magnetic lines when 1 ampere is turned on or off. Since (in circuits without iron cores) $\mathfrak{F}$ is proportional to S, it follows that L is proportional to

S^2. For since (see Art. 405) $\mathfrak{F} = iS/Z$, the interlinkage of lines is

$$S \times \mathfrak{F} = Li = iS^2/Z.$$

Hence when one ampere is turned on or off the inductance will be

$$L = S^2/Z,$$

which may be expressed in henries by dividing by 10^8. If all the lines do not pass through all the spirals the value of L will be less than this.

The self-induced electromotive-force will depend upon the rate at which the current is changing; for if the total cutting $S\mathfrak{F}$ take place in time t, it follows (Art. 243) that

$$E = -S\mathfrak{F}/t = -Li/t.$$

But since the rate at which the current changes is not uniform, E is also not uniform. If in an element of time dt the current changes by an amount di, the rate of change of the current is di/dt, and the self-induced electromotive-force is $= -L \cdot di/dt$.

The formal definition of the *henry* (Art. 381) is based on this expression in order that it may apply to circuits with iron cores as well as to circuits without them.

The energy of the magnetic field surrounding the current is equal to $\frac{1}{2}Li^2$, since, while the field is growing up to have Li lines in total, the average value of the current is $\frac{1}{2}i$.

502. Measurement of Self-Inductance.—To measure a coefficient of self-inductance there are several methods:—

(*a*) *Alternating-current Method.* — The volts V required to send current i at frequency n through coil having resistance R and coefficient of self-inductance L are $V = i\sqrt{R^2 + 4\pi^2 n^2 L^2}$; or, if the resistance is negligible, $V = 2\pi ni L$; whence $L = V/2\pi ni$ (see Art. 525).

(*b*) *Bridge Methods.*—Of several bridge methods the best is Maxwell's. Let balance be obtained in usual way; key in battery circuit being put down before key

in galvanometer circuit (Art. 446). Then press the keys in reverse order, when the presence of self-induction in one of the four arms will upset balance, the needle giving a kick a proportional to the self-induction. Now introduce in the same arm an additional *small* resistance r, such that when keys are again operated in the usual order there is a small permanent deflexion δ. If the periodic time of swing of the needle be T the following formula then holds :— $L = Tra/2\pi\delta$.

(*c*) *Secohmmeter Method.*—Ayrton and Perry invented an instrument which alternately makes and breaks the battery circuit of the bridge and only allows the galvanometer to be in operation during a short interval of time T immediately after each making of the battery circuit (the galvanometer at other times being short-circuited). As the current is increasing during this interval, the self-induction L of a coil placed in one of the arms of the bridge acts as though there were an additional resistance r in that arm. The formula is then, $L = Tr$. As L is then the product of seconds and ohms, Ayrton and Perry proposed for the unit the name of *secohm*, now abandoned in favour of the name *henry*.

503. Effects of Inductance.—The presence of inductance in a circuit affects the currents in several ways. The special *choking-effect* on alternating currents is dealt with in Art. 530. The effects on battery currents are also important. So long as the current is not changing in strength, inductance has no effect whatever; but while the current is growing or while it is dying away the presence of inductance greatly affects it. In all cases inductance tends to oppose any change in the strength of the current; as may be foreseen from the general law of reaction (Art. 499). When a current is increasing, inductance causes it to increase more slowly. When a current is dying away, inductance tends to prolong it.

The existence of inductance in a circuit is attested by the so-called **extra-current**, which makes its appearance

as a bright spark at the moment of breaking circuit. If the circuit be a simple one, and consist of a straight wire and a parallel return wire, there will be little or no inductance; but if the circuit be coiled up, especially if it be coiled round an iron core, as in an electromagnet, then on breaking circuit there will be a brilliant spark, and a person holding the two ends of the wires between which the circuit is broken may receive a shock, owing to the high electromotive-force of this self-induced extra current. This spark represents the energy, of the magnetic field surrounding the wire, suddenly returning back into the circuit. The extra-current on "making" circuit is an inverse current, and gives no spark, but it prevents the battery current from rising at once to its full value. The extra-current on breaking circuit is a direct current, and therefore tends to keep up the strength of the current just at the moment when it is about to cease. To avoid the perturbing effects of inductance, resistance-coils are always coiled back upon themselves (Art. 446); *i.e.* wound *non-inductively.*

Even when a circuit consists of two parallel straight wires there is a magnetic field set up between them, giving inductive reactions. The coefficient of self-inductance for two wires of length l and radius a at an axial distance b apart in air is

$$\mathrm{L} = l\left(\frac{\mu}{2} + 4\log_{\epsilon}\frac{b}{a}\right)10^{-9};$$

where L is in henries; a, b and l in centimetres; and μ the permeability of the wire.

The self-inductance of a thin wire is greater than that of a thick one of equal length, because, for equal currents, the strength of the external field just outside the periphery is greater. A whisp of wires, like Fig. 224, p. 413, has a lesser self-inductance than a single wire of the same length, and a flat strip than a round wire of equal cross-section.

For a long tubular coil (without iron) of length l, of

S turns, each of area A, the value of the coefficient, in henries, is

$$L = \frac{4\pi S^2 A}{l} \times 10^{-9}.$$

504. Helmholtz's Equation. Time-constant.— From that which precedes it is clear that whenever a current is turned on there is a *variable period* while the current is growing up to the value which it will reach when steady, namely, the value as determined by Ohm's law. During the variable period Ohm's law does not apply.

Von Helmholtz, who investigated mathematically the effect of self-induction upon the strength of a current, deduced the following important equations to express the relation between the inductance of a circuit and the time required to establish the current at full strength :—

Let dt represent a very short interval of time, and let the current increase during that short interval from i to $i + di$. The actual increase during the interval is di, and the rate of increase in strength is di/dt. Hence, if the inductance be L, the electromotive-force of self-induction will be $-L\,di/dt$, and, if the whole resistance of the circuit be R, the strength of the opposing extra-current will be $-\frac{L}{R} \cdot \frac{di}{dt}$ during the short interval dt; and hence the actual strength of current flowing in the circuit during that short interval, instead of being (as by Ohm's law it would be if the current were steady) $i = E/R$, will be

$$i = \frac{E}{R} - \frac{L}{R} \cdot \frac{di}{dt} = \frac{E - L\frac{di}{dt}}{R}.$$

To find out the value to which the current will have grown after a time t made up of a number of such small intervals added together, requires an application of the integral calculus, which at once gives the following result :—

$$i = \frac{E}{R}\left(1 - \epsilon^{-Rt/L}\right)$$

(where ϵ is the base of the natural logarithms, 2·718).

Put into words, this expression amounts to saying that after a lapse of t seconds *the self-inductance in a circuit at make of contact has the effect of diminishing the strength of the current by a quantity, the logarithm of whose reciprocal is inversely proportional to the inductance, and directly proportional to the resistance of the circuit and to the time that has elapsed since closing circuit.*

505. The Time-constant.—The quantity L/R, the reciprocal of which appears in the exponential expression, is known as "the *time-constant*" or "persistence" of the circuit. It is the time required by the current to rise to a certain fraction, namely $(\epsilon - 1)/\epsilon$—or 0·632—of its final value.

A very brief consideration will show that in those cases where the circuit is so arranged that the inductance L is small as compared with the resistance R, so that the time-constant is small, the term $\left(\epsilon^{-Rt/L}\right)$ will vanish from the equation for all appreciable values of t.

On the other hand, if L is great compared with R, the current during its growth will be governed almost entirely by the inductance, and not by the resistance of the circuit, which will act as though its resistance were $= L/t$.

These matters are graphically depicted in Fig. 284, in which there are two curves of rise of current. Consider a circuit having E=10 volts, R=1 ohm, L=10 henries. The time-constant L/R will be 10 seconds. The steady current will be 10 amperes ; it starts off as if it intended to reach the top value at the end of the time-constant ; but at the end of 1 second, as may be calculated by Helmholtz's equation, the current is only 0·95 of an ampere ! In 2 seconds it is 1·81, in 5 seconds 3·95, in 10 seconds 6·34 amperes (see curve A). At the end of a whole minute it is only 9·975 amperes. Suppose now we increase the resistance to 2 ohms, and reduce the inductance to 5 henries. The final value of the current will be only 5 amperes instead of 10 ; but it will rise

more quickly than before (see curve B). At the end of 1 second it will be 1·647 ampere, in 2 seconds 2·755, in 10 seconds 4·91 amperes. We conclude that for all apparatus that is required to be rapid-acting (relays, telephones, chronographs, etc.) it is much

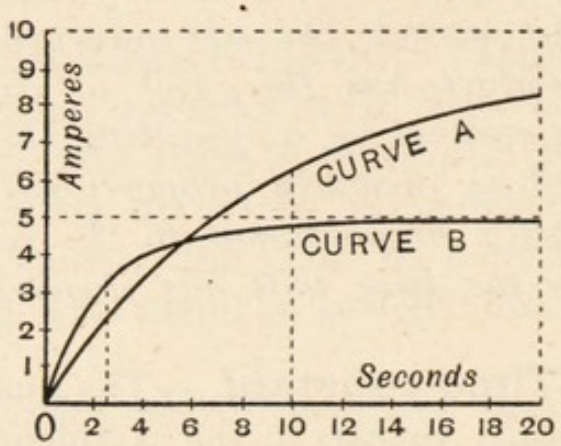


FIG. 284.—Curves of Growth of Current.

more important to keep down the inductance than the resistance of the circuit. We also see that the rule (Art. 439) so often given, about making the resistance of a battery equal to that of the rest of the circuit, is quite wrong for cases of rapid action. If the circuit has self-inductance as well as resistance, then it is better to group the cells of the battery so as to have higher resistance, namely, put them all in series.

In fact everything goes on as though at time t after "make" there were two currents flowing in opposite directions at once; one the ordinary current flowing from the first at full strength, the other the extra-current having the value $-\frac{E}{R}\epsilon^{-Rt/L}$; the actual current being the difference between the two.

At "break" of circuit everything goes on as if, the ordinary current having dropped suddenly to zero, there was superposed an extra-current having the value $+\frac{E}{R}\epsilon^{-Rt/L}$; but here, since there is introduced into the circuit a resistance of unknown amount (the resistance along a spark being indefinite), the calculation becomes impracticable. We know that R is very great; hence we know that the variation will be more sudden, and

that the self-induced E.M.F. at "break" is much greater than that at "make."

In the case of a condenser discharge, CR acts in the same way as the time-constant L/R does in the case of self-inductance.

The actual quantity of electricity conveyed by the "extra-current" is equal to that which would be conveyed by current of strength E/R lasting for time L/R; or $= EL/R^2$. At the "make" of the circuit the retardation causes the flow of electricity to be lessened by the amount $q = EL/R^2$. The energy which is stored up outside the wire while the current grows up from 0 to its final value i is equal to $\frac{1}{2}qE = \frac{1}{2}Li^2$.

CHAPTER X

DYNAMOS, ALTERNATORS, AND TRANSFORMERS

LESSON XLII.—*Magneto-electric and Dynamo-electric Generators*

506. Simple Magneto-electric Machines.—Faraday's discovery of the induction of currents in conductors by moving them across a magnetic field suggested the construction of **magneto-electric machines** to generate currents in place of voltaic batteries, and Faraday himself constructed the first of such machines (Fig. 147) in 1831. In the early attempts of Pixii (1833), Saxton, and Clarke, bobbins of insulated wire were fixed to an axis and spun rapidly in front of the poles of strong steel magnets, or *vice versa*. In 1856 Werner Siemens devised an improved armature, in which the coils of wire were wound shuttle-wise upon a grooved iron core, which concentrated the magnetic lines in a powerful field between the poles of a series of adjacent steel magnets.

The currents thus generated by the rotating coils were necessarily inverse and direct currents alternately, since the wires moved alternately past a N-pole and a S-pole. In Figs. 285 and 286 the wire coil is supposed to be spun around a longitudinal axis, the upper portion coming towards the observer. The arrows show the direction of the induced currents delivered by the coils

to the circuit. It will be seen that if the induced E.M.F. in the wires as they move past the N-pole towards the observer is from left to right, the two slip-rings will alternately become + and − at each half-turn. The little magneto-electric machines, still sold by opticians, and the *magnetos* used on automobiles for procuring ignition, are on this principle.

The machine then consists of two parts: (1) a fixed magnet called *the field magnet*; and (2) a rotating coil, or system of coils, called *the armature*,[1] in which electromotive forces are mechanically generated by induction. If the ends of the armature coil are connected as in Fig.

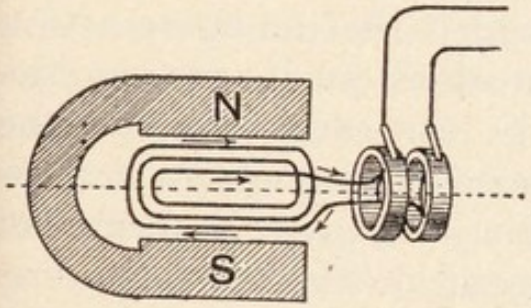


FIG. 285.—Diagrammatic Generator (Alternating-current).

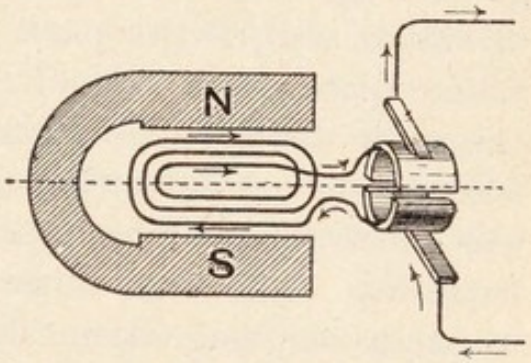


FIG. 286.—Diagrammatic Generator (Continuous-current).

285 to two *slip-rings* by which sliding contact is made with the external circuit, the machine generates *alternating currents*, and is, in fact, an *alternator*. In order to unite these reversed impulses and turn the successive currents into one direction, it was necessary to fix upon the axis a *commutator*. Fig. 286 illustrates the plan adopted by Sturgeon in 1836, using a split tube of copper to commute the connexion to the outer circuit at each half-turn. In this way the machine becomes a *continuous-current generator*.

There are therefore two classes of generators, one for

[1] The armature of a generator or motor is that part of the machine which consists of active windings, core and supports. In the case of a generator it supplies the main current to the terminals; in the case of a motor it receives the main current from the terminals.

producing continuous currents, the other for producing alternating currents (Art. 534).

507. Dynamo-electric Machines.—The name *dynamo-electric machine*, or, briefly, *dynamo*, is given to any machine for converting mechanical power into electrical power by the operation of producing relative motion between magnets and conductors. In continuous-current generators the part which acts as magnet and is termed the *field-magnet* usually stands still, while the armature revolves between its poles. In alternators the field-magnet usually revolves within a stationary armature. The function of a field-magnet is to provide a sufficiently great magnetic flux. The armature, whether it revolves or stands still, is the part in which the inductive action takes place; the copper conductors in it cutting the magnetic lines of the flux. In the early machines the field-magnets were either permanent magnets of steel or else electromagnets independently excited by means of batteries. The next improvement, due to Sinsteden, was to excite the magnetism of the field-magnets by means of currents furnished by a little magneto-electric machine, known as the *exciter*, also kept in rotation. Various suggestions were made by Hjorth, Murray, S. A. Varley, and others to render the machine self-exciting by using the currents generated in the armature to excite the field-magnets. This was done in 1867 by Varley, Werner Siemens, and Wheatstone; the small current induced by the feeble residual magnetism being sent around the electromagnet to exalt its magnetism, and prepare it to induce still stronger currents. The name of **dynamo-electric** machines was at one time given to such generators to distinguish them from those in which permanent steel magnets are employed. In either case the current is due to magneto-electric induction; and in either case also the energy of the currents so induced is derived from the dynamical power of the steam-engine or other motor which performs the work of moving the rotating coils of

wire in the magnetic field. So the name has been extended to all generators, whether self-exciting or not. In all of them the electromotive-force generated is proportional to the number of turns of wire in the rotating armature, and to the speed of revolution. When currents of small electromotive-force but of considerable strength are required, as for electroplating, the rotating armatures of a generator must be made with small internal resistance, and therefore of a *few* turns of stout wire or ribbon or rods of copper. For producing currents at a high electromotive-force the armature must consist of *many* turns of wire or of copper conductors suitably connected.

508. Continuous Current Generators. — The armatures of modern dynamos are complicated structures designed to secure continuity of action. A simple coil, such as Fig. 286, with its 2-part commutator will not yield a steady current; for twice in each revolution the E.M.F. dies away to zero. The coils must be symmetrically grouped so that some of them are always active. In most dynamos the armature winding is constructed as a *closed coil*, the wire being wound on a *ring* core of iron (Pacinotti's core with teeth, Gramme's core without teeth), or as a *drum* over a cylindrical core (Siemens's or Von Hefner's plan). In all these cases the convolutions are joined up so that (like the ring winding in Fig. 287, which illustrates a simple bipolar design) the coil is endless. If the current is brought in at one side of such a coil and taken out at the other side there will be two paths through the coil. As the coil spins between the poles of the field-magnet the electromotive-forces induced in the ascending and descending parts will tend to send the currents in parallel through these parts; and consequently contact-brushes must be set to take off the currents from the revolving coils at the proper places. The brushes are, however, set in contact not with the coils themselves but with a *commutator*, Fig. 288, consisting of a number of copper bars, insulated from one another, and joined up to the

armature coil at regular intervals. Consider, for example, a Gramme ring made as it were of a number of bobbins

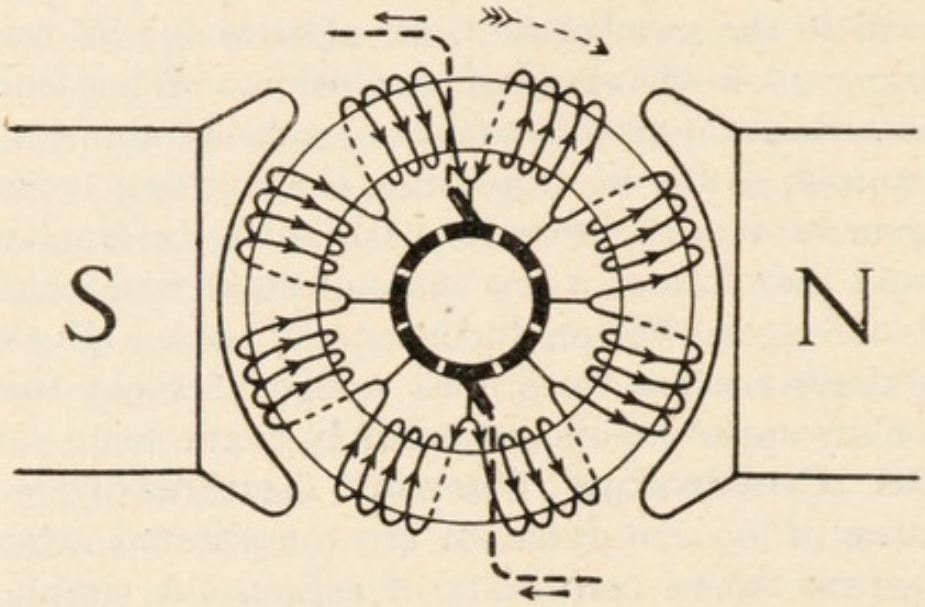


FIG. 287.—Diagrammatic Dynamo with Ring Armature.

wound upon a ring core of iron. Each bobbin constitutes one "section" of the winding, and they are all joined together, the end of one section to the beginning of the next, and each such junction is joined down to a bar of the commutator. The current cannot pass from one bar of the commutator to the next without traversing the intervening turns of the windings. The commutator revolves with the armature; while the *brushes* which convey the current to and from the circuit are clamped in suitable holders to press against its surface, and are set in such a position that the current passes into them with as little sparking as possible. As the current in each turn of the armature winding must be reversed in direc-

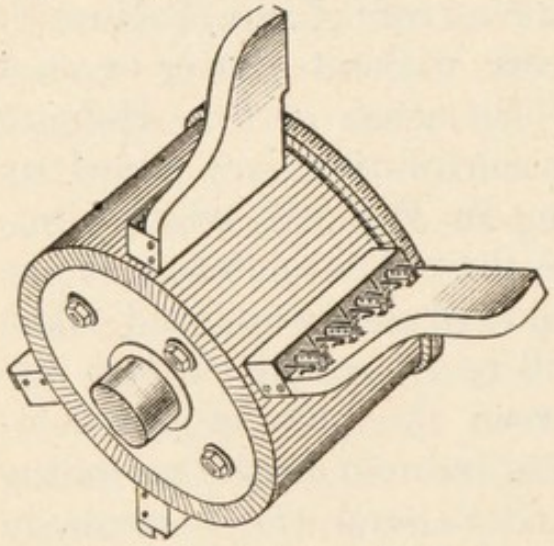


FIG. 288.—Commutator and Brushes.

tion as it passes from the inductive influence of one pole to that of the next pole (and in thus reversing sets up reactive electromotive-forces), the reversal or commutation is apt to be delayed ; with the consequent production of sparks between the commutator and the collecting brushes. To prevent sparking it used to be the practice to set the brushes a little in advance of the diameter that is symmet-

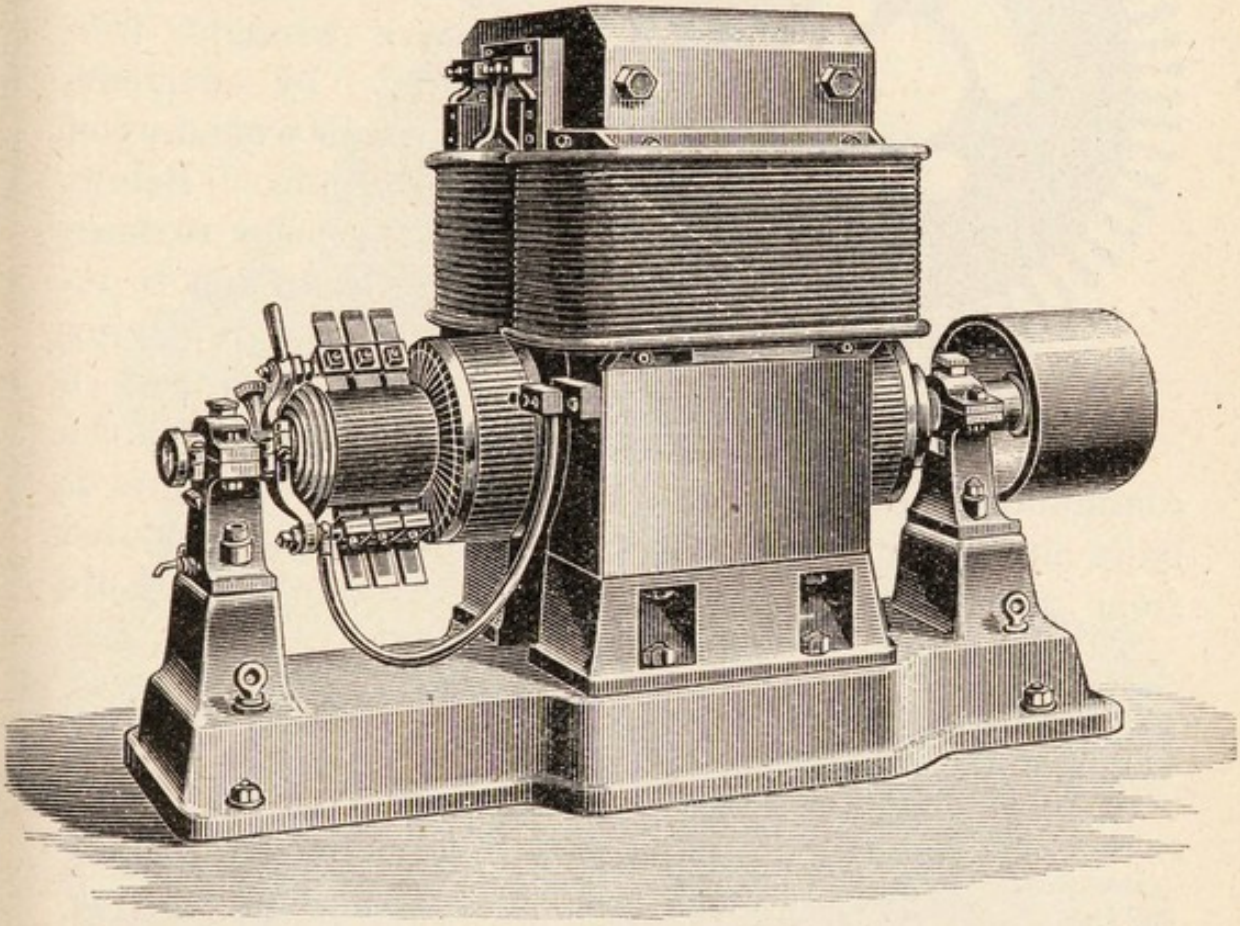


FIG. 289.—Bipolar Dynamo.

rical between the poles ; so that each section of the winding, as it passes under the brush, is at that instant moving in a magnetic field of sufficient strength to generate a small auxiliary electromotive-force to bring about a quick reversal. In many modern dynamos small auxiliary poles are fixed between the principal poles to facilitate sparkless reversal. The current in the armature exercises a magnetizing action, and tends to distort the magnetic field in the direction of the rotation, interfering with the

proper magnetism of the field-magnet. The "brushes" that receive the current were originally bunches of springy wires: in modern machines they consist of small blocks of carbon, or are built up of copper strip or copper gauze. Fig. 289 depicts a *bipolar* type of dynamo, having a vertical magnet of massive wrought iron magnetized by currents flowing in coils wound upon the two limbs. Below, between the polar surfaces which are bored out to receive it, is the revolving armature (in this case a drum armature) with the commutator and brushes. The core of the armature is built up of thin iron disks (Fig. 290) lightly insulated from one another, to prevent eddy-currents. They are

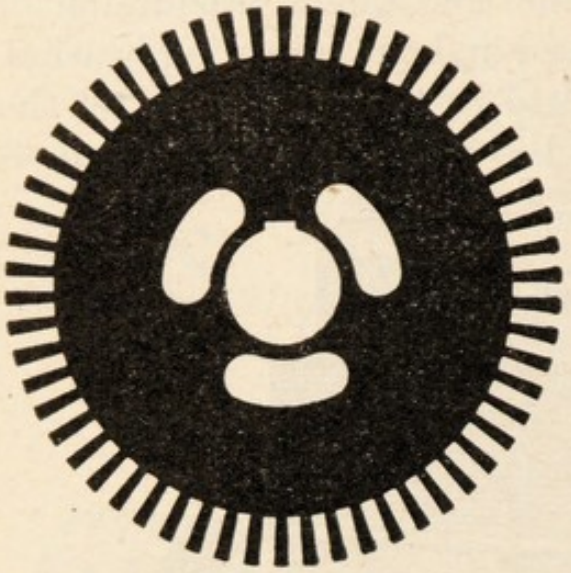


FIG. 290.—Armature Core-disk.

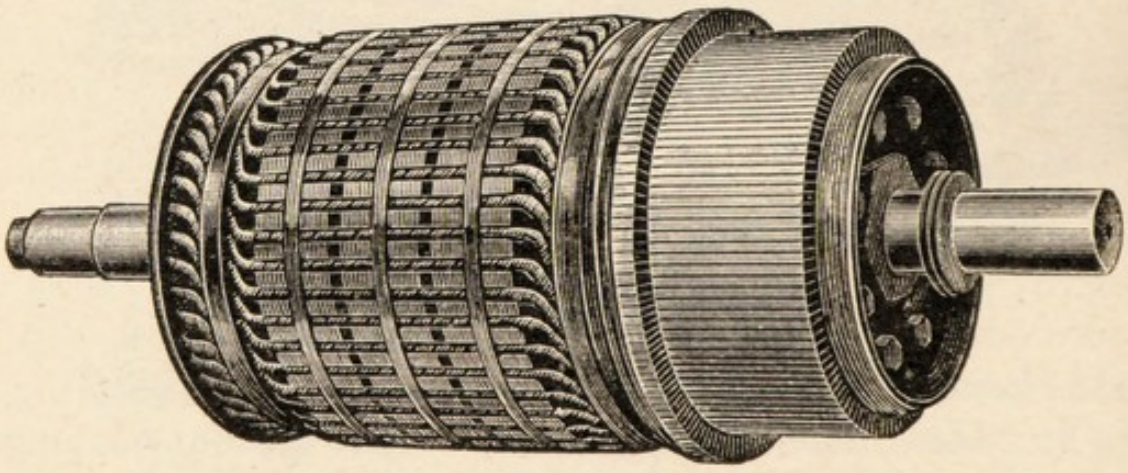


FIG. 291.—Drum Armature.

stamped out with a toothed periphery. When assembled on the shaft the slots between the teeth form channels in which the armature windings are secured. Fig. 291 depicts a modern armature. All continuous-current

dynamos will run as motors (Art. 516), if supplied with current at the proper voltage.

509. Multipolar Dynamos. — All large modern generators are now made *multipolar*, with 4, 6, 8, or more poles; bipolars being used in small sizes only. Fig. 292 depicts a recent 4-pole generator, of 250 kilo-

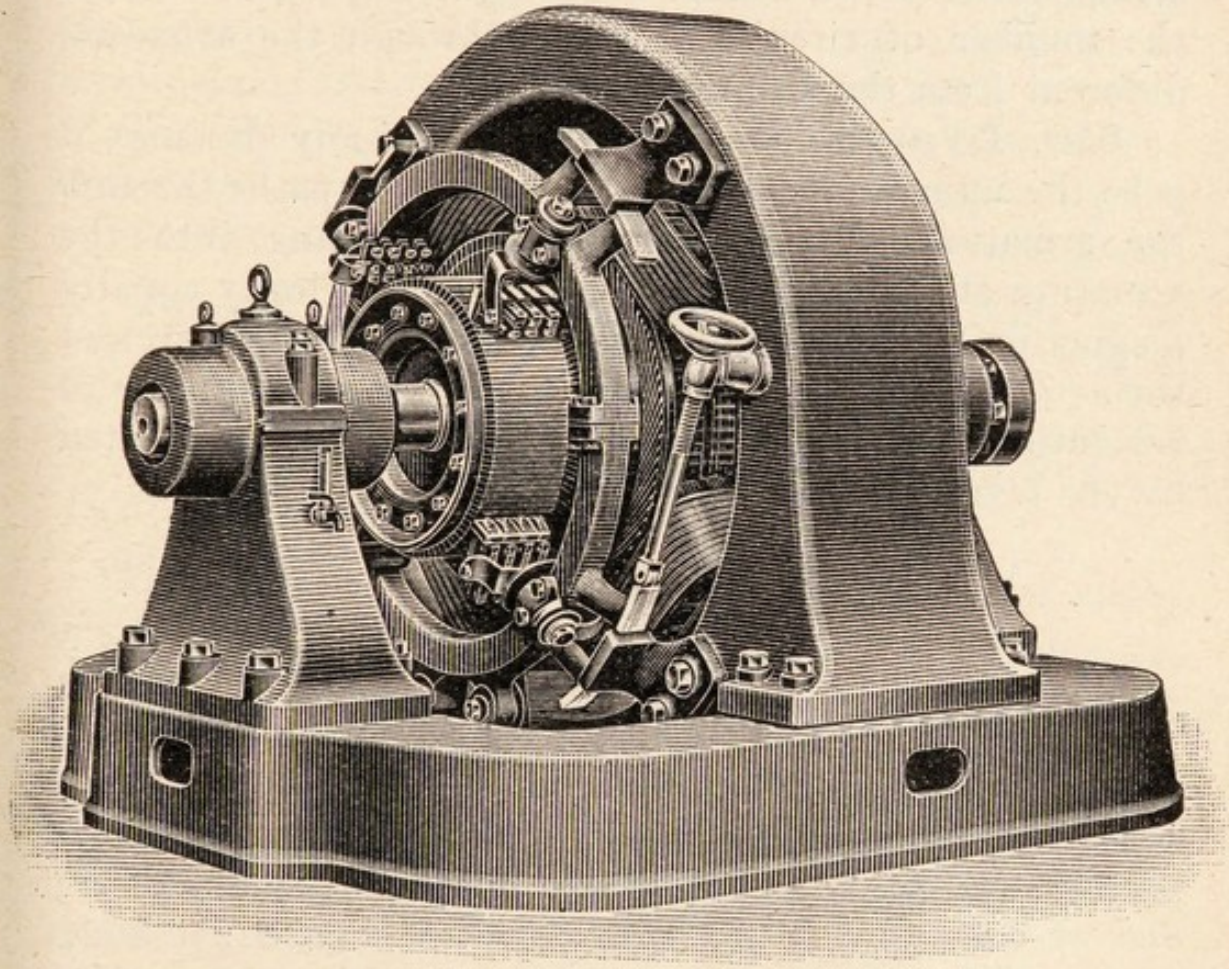


FIG. 292.—Modern Four-pole Dynamo.

watts output, running at 375 revs. per minute, delivering 500 amperes at 500 volts. The poles are alternately North and South. The windings of the armature consist of loops which span across a chord about equal to the pole-pitch, so that when one side of the loop is passing a N-pole, the other shall be passing a S-pole. Successive loops, in a simple drum armature, are joined up to one another so as to form a winding that is re-entrant as the

ring-winding (Fig. 287) is. In a simple drum armature winding such as this (called a *lap-winding*) there will be the same number of paths (or circuits in parallel) through the winding as the machine has poles; and there must be the same number of brushes (or rows of brushes) spaced out around the commutator. In another and less simple arrangement (called a *wave-winding*) it is possible to have the number of circuits or paths through the armature different from the number of poles.

510. Dynamo Calculations.—In any dynamo, if p be the number of poles, c the number of paths through the armature, $\mathfrak{F}$ the magnetic flux passing into the armature at one pole (all poles being numerically equally magnetized), S the number of wires or conductors around the armature (counted all round), and n the number of revolutions per second, the electromotive-force generated by the revolving armature will be

$$\mathrm{E} = \frac{p}{c} \times n\mathrm{S}\mathfrak{F} \div 10^8.$$

Or, in the case of ring-wound and lap-wound armatures, where c is the same number as p, the formula becomes

$$\mathrm{E} = n\mathrm{S}\mathfrak{F} \div 10^8;$$

since the number of magnetic lines cut per second is proportional to each of the three quantities n, S, and $\mathfrak{F}$; and we divide by 10^8 to bring to volts (Art. 381, p. 362).

As with batteries (Art. 205), so with dynamos, if there is an internal resistance r, the available volts at the terminals V will be less than the whole volts generated, by an amount equal to ri, the lost volts.

$$\mathrm{V} = \mathrm{E} - ri.$$

As the electrical efficiency of the machine is the ratio V/E, it is evident that r should be as low as possible.

Example.—A dynamo having $\mathfrak{F} = 7170000$, S = 120, running at 780 revs. per min. (= 13 revs. per sec.), will generate an electromotive-force of 111 volts. If $r = 0{\cdot}033$ ohm, then when $i = 210$ amperes, $ri = 7$ volts. Hence V = 104 volts.

The number of amperes i which a machine is supplying at any time is termed its *load*. It obviously depends on the resistance of the circuit and the number of lamps or motors which are switched on. The maximum load of a dynamo is limited by the heating of its parts, and the sparking at the brushes, which becomes serious if too large a current is drawn from the machine.

The *output* of a dynamo is expressed in *watts*, being the number of amperes multiplied by the volts at terminals, or iV; or in *kilowatts* (Art. 454) as $iV \div 1000$.

The *efficiency* of a dynamo is the ratio between the output and the (mechanical) input; the input being the power supplied to the machine, expressed in the same units.

Example. — A certain dynamo generating 110 volts at its terminals is found when giving out 200 amperes to require 32 HP to be put into it by the engine. The output is 22,000 watts. The input is $32 \times 746 = 23,872$ watts. So the efficiency is $22,000 \div 23,872 = 0{\cdot}92$, *i.e.* 92 per cent.

The causes of inefficiency, that is the sources of waste of power, in a dynamo, are as follows:

(i.) Watts lost in iron of armature, caused by hysteresis and eddy-currents (Arts. 395 and 500).

(ii.) Watts lost in excitation, due to resistance in magnet coils (Art. 461).

(iii.) Watts lost in copper of armature, due to resistance in armature windings (Art. 461).

(iv.) Watts lost in friction, etc., of bearings and brushes.

Of these (i.), (ii.), and (iv.) are nearly constant at all loads; while (iii.), since they follow the i^2r law (Art. 462, p. 469) are variable, being proportional to the square of the load.

All the armature conductors of a dynamo are subject, when the machine is running, to a mechanical drag opposing the rotation. This is due to the action between the magnetic field and the current (Art. 367).

To calculate the field-magnet windings the formulæ of Arts. 405 and 431 must be applied (see p. 394 for an exercise on windings).

511. Excitation of Field-Magnets.—There are several modes of exciting the magnetism of the field-magnets, giving rise to the following classification:

1. *Magneto Machine*, with permanent steel magnets.

2. *Separately excited Dynamo*; one in which the currents used to excite the field-magnets are furnished by a separate machine called an "exciter."

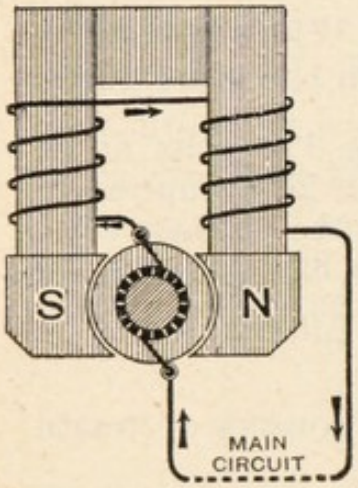


FIG. 293.
Series-wound.

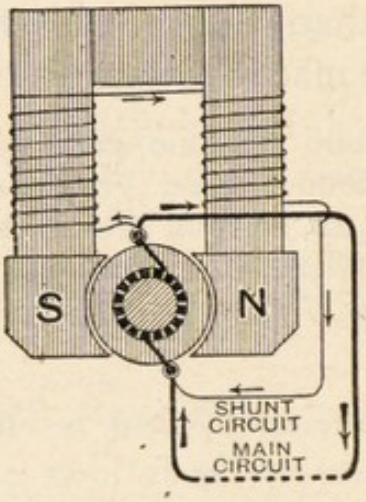


FIG. 294
Shunt-wound.

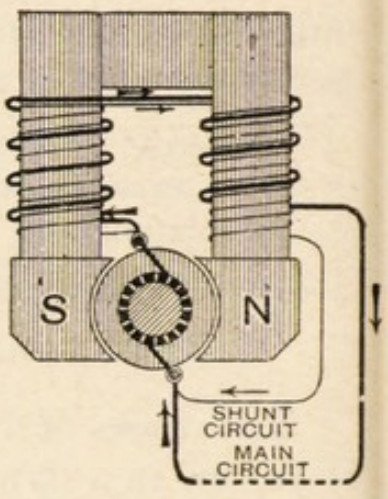


FIG. 295.
Compound-wound.

3. *Separate-coil Dynamo*, with a separate coil wound on the armature to generate the exciting current.

4. *Series-Dynamo*, wherein the coils of the field-magnet are in series with those of the armature and the external circuit (Fig. 293), and consist of a few turns of thick wire.

5. *Shunt-Dynamo*, in which the coils of the field-magnet form a shunt to the main circuit; and, being made of many turns of thin wire, draw off only a small fraction of the whole current (Fig. 294).

6. *Compound-Dynamo*, partly excited by shunt coils, partly by series coils (Fig. 295).

The last three modes are illustrated in the accompany-

ing diagrams. Each variety of winding has certain advantages depending on conditions of use.

512. Characteristic Curves.—To study the behaviour of various types of dynamo, Hopkinson devised the method of *characteristic curves*, wherein the two elements of output—the volts and the amperes—are plotted out. If a series-dynamo is examined with amperemeter and voltmeter, while run at constant speed on various loads, its performance will be found to give a curve like AQV in Fig. 296, where the external volts are plotted vertically, the amperes horizontally. This curve is the external characteristic. The volts rise as the current is increased, because of the increase of magnetization, but when this is near saturation they fall again because of internal resistance and sundry reactions. At any point such as Q the resistance of the external circuit is represented by the slope of the line QO (*i.e.* by the trigonometrical tangent of the angle QOX), since tan QOX is equal to QM/OM (= the volts divided by the amperes). If line OJ be drawn so that tan JOX is equal to the internal resistance, then MN will represent the lost volts when the current = OM. Adding to QM a piece PQ = MN, we obtain PM as the corresponding value of the total electromotive-force. In this way, from the curve OV we can construct the total characteristic OE. It will be evident that if the total resistance (*i.e.* the slope of the line OP) be increased, P will come down the curve toward O, and there will be a certain point at which any further increase in the slope will produce a sudden drop of volts and amperes to almost zero. This is a peculiarity of series

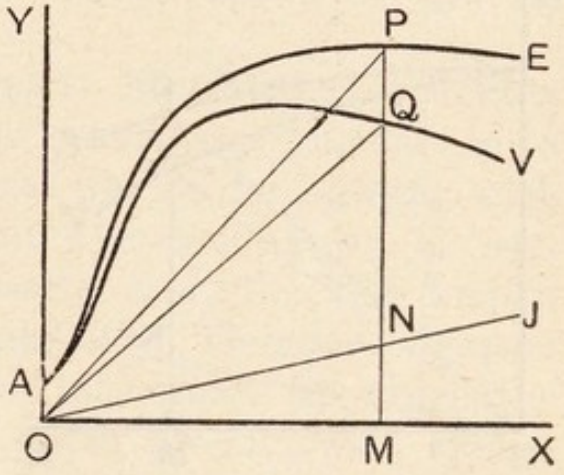


FIG. 296.—Characteristic Curves of Series-Dynamo.

machines; when running at a given speed they cease to yield any current if the resistance exceeds a certain critical value, depending in each machine on its construction.

For a *shunt-dynamo* the characteristic has a different form. When the machine is on open circuit, giving no current externally, the shunt circuit is fully at work exciting the magnet. The curve YV of volts at terminals begins at a high value, and as the current is increased by diminishing the resistance, the voltage gently falls. Part of this drop is due to internal resistance; part is due to armature reactions and magnetic distortion; and part to the reduction of the shunt current. If, as before, we draw OJ to represent by its slope the internal resistance, we can find the lost volts MN and add these on above Q, so obtaining P, a point on the total electromotive-force curve, YPE. This also droops slightly. If a shunt-dynamo be short-circuited, its magnetism is at once reduced to almost zero. To regulate the voltage of a shunt-dynamo a suitable rheostat (Fig. 235) may be introduced into its field-magnet circuit, to vary the exciting current.

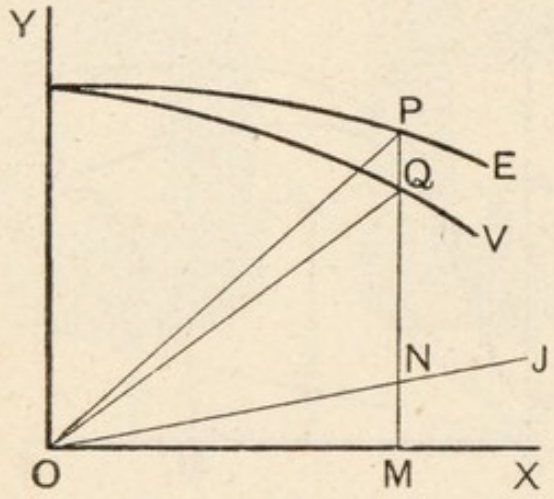


FIG. 297.—Characteristic Curves of Shunt-Dynamo.

513. Constant Voltage Machines.—For glow-lamp lighting, machines are needed that will maintain the voltage constant, whether the current going to the mains be small or large. The current that flows out of the machine will regulate itself exactly in proportion to the demand; more flowing when more lamps are turned on, provided the potential difference between the mains is kept constant. For this purpose neither a series-dynamo nor a shunt-dynamo (driven at a constant speed) will suffice; though by hand-regulation, as above, a shunt-

dynamo may be used. It will be noted that, while in shunt-machines the characteristic drops as the current is increased, in series-machines the curve rises. Consequently, by using a *compound-winding*, consisting of a few coils of thick wire, in series with the main circuit (to raise the excitation in proportion to the load), in addition to the shunt winding (which gives the proper voltage at no-load), the voltage may be kept remarkably constant. By *over-compounding* with more series windings the dynamo may be made to maintain a constant voltage at some distant point in the circuit and so compensate for the drop in voltage caused by the resistance of the cables.

514. Constant Current Machines — Series Lighting.—To maintain an unvarying current in a series of lamps, as is sometimes wanted for lighting with arc lamps (Art. 486), special dynamos known as *arc-lighting machines* were formerly used, the best known of these being the Brush and the Thomson-Houston dynamos. Both had open-coil armatures (in which the coils are not grouped in a closed circuit), with special commutators, and automatic devices to regulate the output, the one by shunting the exciting current, the other by shifting the brushes. The current could thus be kept at 10 amperes, while the volts change (according to the number of lamps in circuit) from 50 to 2000 or more.

515. Homopolar Machines.—There is another class of dynamo-electric machines, differing entirely from any of the preceding, in which a coil or other movable conductor slides round one pole of a magnet and cuts the magnetic lines in a continuous manner without any reversals in the direction of the induced currents. Such machines, sometimes called "uni-polar" machines, have, however, very low electromotive-force, and are not practical. Faraday's disk-machine (Fig. 147) belonged to this class.

For fuller descriptions of dynamos, and technical

details of construction, the reader is referred to the author's treatise on *Dynamo-electric Machinery*.

LESSON XLIII.—*Electric Motors (Continuous Current)*

516. Electric Motors.—An *electric motor* is a species of electromagnetic engine, that is to say a machine in which the motive power is derived from electric currents by means of their electromagnetic action. It transforms electrical energy into mechanical work. Faraday (1821) showed a simple case (Art. 428) of rotation produced between a magnet and a current of electricity. Barlow (1823) produced rotation in a star-wheel, and Sturgeon in a copper disk, when traversed radially by a current while placed between the poles of a horseshoe magnet. Henry (1831) and Ritchie (1833) constructed small engines producing rotation by electromagnetic means. Fig. 298 shows a modification of Ritchie's motor. An electromagnet DC is poised upon a vertical axis between the poles of a fixed magnet (or electromagnet) SN. A current, generated by a suitable battery, is carried by wires which terminate in two mercury-cups, A, B, into which dip the ends of the coil of the movable electromagnet CD. When a current traverses the coil of CD it turns so as to set itself in the line between the poles NS, but as it swings round, the wires that dip into the mercury-cups pass from one cup to the opposite, so

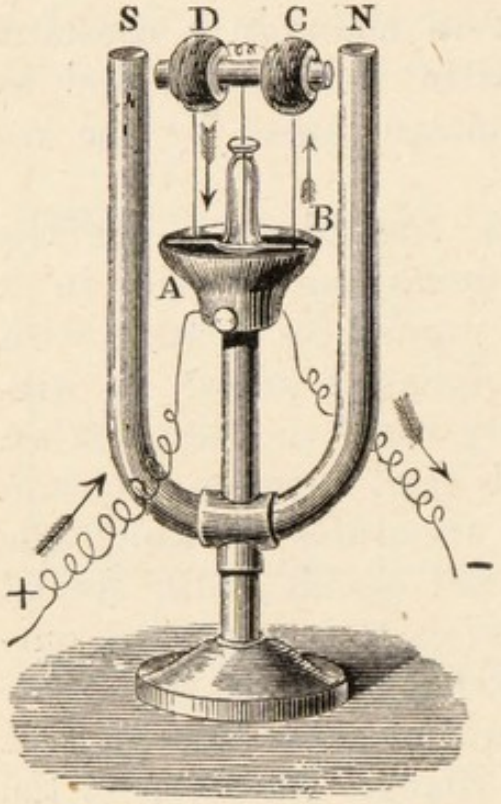


FIG. 298.—Ritchie's Motor.

that, at the moment when C approaches S, the current in CD is reversed, and C is repelled from S and attracted round to N, the current through CD being thus reversed every half turn. The mercury-cup arrangement was superseded by the *commutator* (Art. 508) with metallic brushes pressing on it.

In another early form of motor, devised by Froment, bars of iron fixed upon the circumference of a rotating cylinder are attracted up towards an electromagnet, in which the current is automatically broken at the instant when each bar has come close up to its poles. In a third kind, an electromagnet is made to attract a soft iron armature up and down, with a motion (like the piston of a steam-engine) which is converted by a crank into a rotation. In these cases the difficulty occurs that, as the attraction of an electromagnet falls off rapidly at a distance from its poles, the attracting force can only produce effective motion through very small range. Page (1838–1850) designed various motors, in some of which iron plungers were sucked into hollow tubular coils of wire in which currents were caused to circulate at recurring intervals.

Jacobi (1839) propelled a boat along the river Neva at the rate of $2\frac{1}{4}$ miles per hour with an electromagnetic engine of about one horse-power, worked by a battery of 64 large Grove's cells.

517. Dynamo as Motor.—Daniel Davis appears to have been the first to recognize, about 1842, that the action of the electric motor is the simple converse of that of the dynamo or generator. Every electric *generator*, such as is used in electric lighting, can also work as a *motor*, giving out mechanical power when supplied with electric currents from some other source. Indeed machines designed as generators make far more efficient motors than any of the older sorts of electromagnetic engines, which were little more than toys.

Suppose a machine designed to take 60 amperes at

450 volts, in other words a 27 kilowatt machine. Suppose it to be such that the inevitable losses (due to resistance, hysteresis, etc.) in it amount to 10 per cent, or 2·7 kilowatts. Then if this machine is used as a generator the engine must supply it with power to the amount of 29·7 kilowatts, which is 39·8 HP. But if it is to be used as a motor and only 27 kilowatts are supplied to it from the mains, its output will be 24·3 kilowatts, which is the same as 32·6 HP (Art. 454).

518. Modern Electric Motors.—These are of two kinds: (1) those for use with continuous currents; (2) those for use with alternating currents. The latter are considered in Art. 547, p. 565. The former are constructed precisely on the plan of continuous current dynamos (Art. 508) having fixed *field magnets* and rotating *armature*. The armature is dragged round by the mutual action of the currents flowing in the copper conductors and the magnetic field in which the conductors lie. As explained in Art. 367, the force acting laterally on the conductors is proportional to the product of current and field. Hence if very powerful field-magnets are employed, a great torque (or turning moment) can be produced without requiring too great a current to be sent into the armature. The two factors of mechanical rotatory power are *torque* (=angular force) and angular *speed*. If the field of the motor is maintained constant the torque is proportional to the current, and the speed is proportional to the volts. If E is the electromotive-force generated (in direction opposing the current, see Art. 455) in the revolving armature, and i the current supplied to the armature, the electrical and mechanical expressions for the power (watts) imparted to the armature are

$$iE = an\mathrm{T},$$

where n is revolutions per second, T the torque, and a a coefficient depending on the units chosen. If n is expressed in revolutions per second, and T in pound-

feet, the value of $a = 8{\cdot}52$. Now in a revolving armature E is proportional (see Art. 510) to p the number of poles, to S the number of armature conductors, to $\mathfrak{F}$ the flux per pole, and inversely proportional to c the number of paths through the windings. Hence

$$T = \frac{i\mathrm{S}\mathfrak{F}p}{8{\cdot}52c10^8}.$$

Example.—A 4-pole motor, with 2 circuits through its armature, with a flux of 3,000,000 lines, and 848 conductors in its armature, taking 70 amperes exerts a torque of 420 pound-feet.

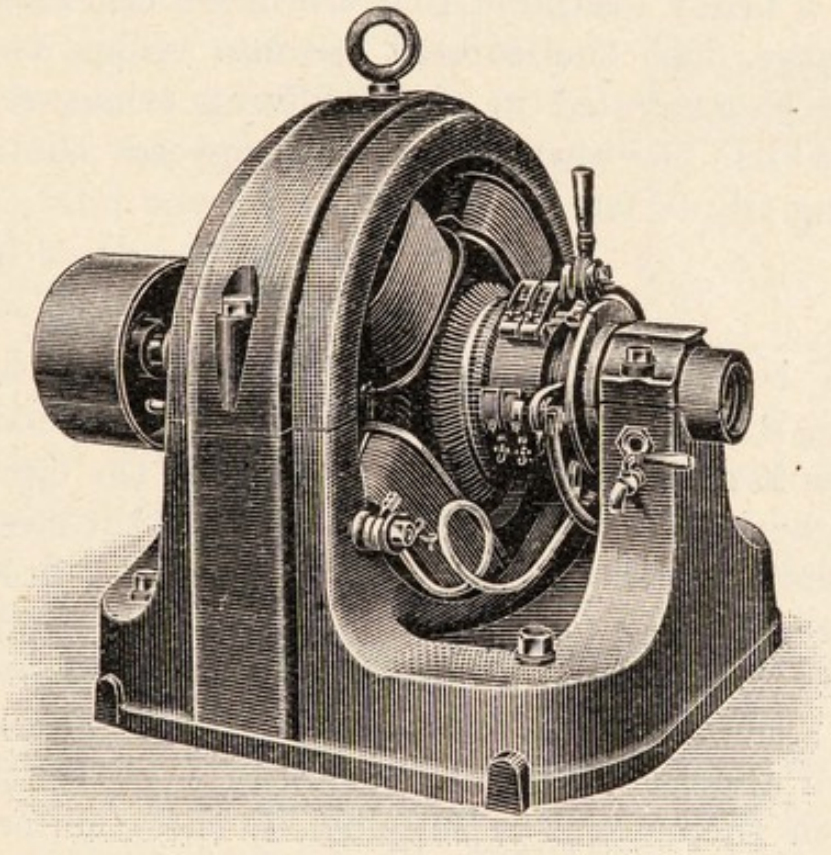


FIG. 299.—Continuous Current Motor (open type).

If the armature current is supplied from mains at constant voltage, strengthening the magnetic field has the effect of slowing speed, for equal power; and weakening the field quickens the speed. Fig. 299 depicts a modern continuous current motor of 90 horse-power, designed to run at 600 revolutions per minute when supplied with 90

amperes at 200 volts. Such motors are made of many sizes and forms. Fig. 299 is an *open* motor, but many are *enclosed* to keep out dust; and if intended for use in mines must be *totally enclosed*, *i.e.* gas-tight. To prevent sparking at the commutator it is usual to give the brushes a backward lead, that is to displace them a little in the opposite direction to that of the rotation.

519. Efficiency of Motors.—If an amperemeter be included in the circuit with a battery and a motor, it is found that the current is *weaker* when the motor is running fast than when the motor is running slow and turning a heavy load, and that the faster the motor runs the weaker does the current become. This is due to the E.M.F. generated in the revolving armature of the motor, which necessarily (Art. 455) opposes the current. Applying Ohm's law we see that

$$i = \frac{V - E}{R},$$

where V is the electromotive-force supplied by battery or dynamo, E the back electromotive-force generated by the motor as it runs, and R the resistance of the circuit. If the magnetic field of the motor is of constant strength, E will increase as the motor gets up speed. Consequently the faster it runs (or the stronger its field-magnet) the more is the current diminished. If the motor only exerts a small back electromotive-force it cannot utilize much of the power of the current. If V be the volts at which the current is supplied, E the counter-electromotive force generated by the motor, and i the current, then Vi = gross power supplied, Ei = nett power utilized; and dividing the latter by former we get, as the *electrical efficiency* of the motor, the ratio E/V.

Example.—Suppose V = 100 volts and E = 90 volts, the electrical efficiency will be 90 per cent.

To make the efficiency as high as possible the motor should be so arranged (either by strengthening its mag-

netic field, or by letting it run faster) that E is very nearly equal to V. In that case the motor will utilize nearly all the energy that flows to it. But since, by Ohm's law, the current is $= (V - E)/r$, where r is the internal resistance of the motor, it follows that when E becomes nearly equal to V the current will be reduced to a small fraction of what it would be if the motor were at rest. The diagram (Fig. 300) makes the matter plainer. Let the line OV represent by its length the volts of supply V, and let OE represent the volts generated in the armature, proportional to speed and to field. On OV describe the square OVWX, and draw the diagonal and the lines EH, KL. Then the area EVWH is proportional to the gross power, being $V(V - E)$, and area GLXH is proportional to the nett power utilized, being $E(V - E)$. These two areas become more nearly equal, though both become small, when E is increased to be nearly equal to V. The area GLXH, the nett power of the motor, is a maximum when $E = \frac{1}{2}V$; but then the efficiency would be only 50 per cent.

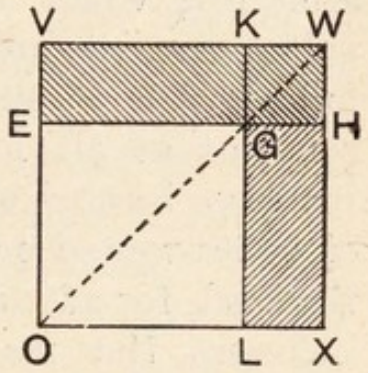


FIG. 300.—Efficiency Diagram.

520. Starting Resistances.—When the motor is only beginning to turn, and E is small, the current would be enormous. This is of importance in the starting of motors; for at starting the great rush of current, which would certainly produce an enormous torque, would destroy the armature by overheating it. Hence it is necessary to use an appliance called a **starter**, which is an arrangement of a number of graduated resistances. By turning a handle a considerable amount of resistance is introduced into the armature circuit so as to limit the rush of current at starting, and then this resistance is gradually cut out as the motor acquires its speed. As the motor speeds up it generates a back electromotive-

force which reduces the current to the working strength at the working speed.

521. Excitation and Speed of Motors.—The field-magnets of motors may be excited, like those of dynamos (Art. 511). For toys and small machines permanent magnets of steel may be used. In larger motors electromagnets are employed, and these may be (i.) separately excited; (ii.) excited by connexion in series with the armature; (iii.) excited in shunt with the armature; (iv.) excited in both shunt and series by using a compound winding. Since (Art. 510) the speed of the armature, when supplied from mains at a constant voltage, varies inversely as the strength of the field, it follows that in shunt-wound motors the speed is nearly constant at all loads, falling off a little as the load increases because of internal resistance. But, in the case of series-wound motors, the speed falls off greatly with the load, for at large loads the current increases and this increases the magnetism, bringing down the speed. Uniform speed can be attained by using a shunt motor having a few series turns so wound as to weaken the magnetism as the load increases.

Hence the speed of motors can be controlled (*a*) by altering the voltage applied to the motor; (*b*) by putting a rheostat into the shunt circuit to weaken the shunt current, and therefore the magnetism, when the motor is required to run faster; (*c*) by putting into the path of the current going to the armature a resistance, producing a drop of the voltage available for the armature and so reducing its speed; but this expedient wastes energy. Rheostats to vary the speed are sometimes combined with starters (Art. 520), so that the movements of a handle start the machine and regulate its speed.

LESSON XLIV.—*Alternating Currents*

522. Periodic Currents.—We have seen that the revolving of a simple coil in a magnetic field sets up electromotive-forces, which change in direction at every half-turn, giving rise to *alternating currents.* In each whole revolution there will be an electromotive-force which rises to a maximum and then dies away, followed immediately by a reversed electromotive-force, which also grows to a maximum and then dies away. Each such complete set of operations is called a *cycle*, and the time taken for one cycle is called a *period.* The number of periods accomplished in a second is called the *frequency* of the alternations, and is denoted by the letter n. In 2-pole machines n is the same as the number of revolutions per second ; but in multipolar machines n is greater, in proportion to the number of pairs of poles. Thus a machine with 24 poles driven at 250 revolutions per minute will work with a frequency of 50 periods per second ; or, in each second it will give 50 successive to-and-fro electromotive impulses or waves.[1] By revolution in a uniform field the electromotive-forces set up are proportional to the sine of the angle through which the coil has turned from the position in which it lay across the field. If in this position the flux of magnetic lines through it were $\mathfrak{F}$, and the number of spirals in the coil that enclose the $\mathfrak{F}$ lines be called S, then the value of the induced electromotive-force at any time t when the coil has turned through angle θ ($\equiv 2\pi nt$ radians, or $= 360nt$ degrees) will be

$$E_\theta = 2\pi n S\mathfrak{F} \sin \theta \div 10^8$$

or, writing D for $2\pi n S\mathfrak{F}/10^8$, we have

$$E_\theta = D \sin \theta.$$

[1] The term is convenient, but these alternating impulses are not strictly *waves*, though the graphic representations of them, such as Fig. 301, exhibit definite *wave-forms*.

In actual alternating current generators (Art. 534) the magnetic fields are not uniform, nor the coils simple loops; so the periodic rise and fall of the electromotive-forces will not necessarily follow a simple sine law. The form of the impressed waves depends on the shape of the polar faces, and on the form and breadth of the coils. But in most cases we are sufficiently justified in assuming that the impressed electromotive-force follows a sine law, so that the value at any instant may be expressed in the above form, where D is the maximum value or *amplitude* attained by E, and θ an angle of *phase* upon an imaginary circle of reference. Consider a point P revolving clock-

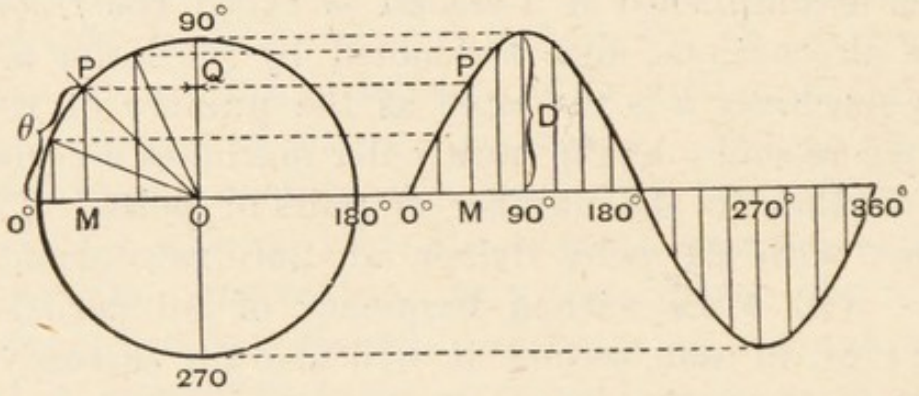


FIG. 301.—Curve of Sines, showing Wave-form of Alternating Electromotive-force.

wise round a circle. If the radius of this circle be taken as unity, PM will be the sine of the angle θ, as measured from 0°. Let the circle be divided into any number of equal angles, and let the sines be drawn similarly for each. Then let these sines be plotted out at equal distances apart along the horizontal line, as in Fig. 301, giving us the *sine curve*, which is a smooth wave-form.

In Fig. 301 one revolution of P around the circle of reference corresponds to one complete cycle of changes. The value of the electromotive-force (which varies between $+D$ and $-D$ as its maximum values) may be represented at any moment either by the sine PM or by projecting P on to the vertical diameter, giving OQ. As

P revolves, the point Q will oscillate up and down the diameter.

The currents which result from these periodic or alternating electromotive-forces are also periodic and alternating; they increase to a maximum, then die away and reverse in direction, increase, die away, and then reverse back again. If the electromotive-force completes 50 such cycles in a second, so also will the current.

523. Virtual Volts and Virtual Amperes.—Measuring instruments for alternating currents, such as electrodynamometers (Art. 425), hot-wire voltmeters (Art. 465), and electrostatic voltmeters (Art. 309), do not measure the arithmetical average values of the amperes or volts. If these instruments are first calibrated by the use of continuous currents, their readings will be the square roots of the means of the squares of the instantaneous values. They measure what are called *virtual amperes* or *virtual volts*. The mean which they read (if we assume the currents and voltages to follow the sine law of variation) is equal to 0·707 of the maximum values; for the average of the squares of the sine (taken over either 1 quadrant or a whole circle) is $\frac{1}{2}$; hence the square-root-of-mean-square value is equal to $1 \div \sqrt{2}$ times their maximum value. If a voltmeter is placed on an alternating circuit in which the volts are oscillating between maxima of $+100$ and -100 volts, it will read 70·7 volts; and 70·7 volts continuously applied would be required to produce an equal reading. If an alternating-current amperemeter, or electrodynamometer (Art. 426), reads 100 amperes, that means that the current really rises to $+141{\cdot}4$ amperes and then reverses to $-141{\cdot}4$ amperes; but the effect is equal to that of 100 continuous amperes, and therefore such a current would be described as 100 *virtual amperes*.

524. Lag and Lead.—Alternating currents do not always keep step with the alternating volts impressed upon the circuit. If there is self-inductance (Art. 501)

in the circuit the currents will *lag*: if there is capacity (Art. 290) in the circuit they will *lead* in phase. Fig. 302 illustrates the lag produced by inductance. The impulses of current, represented by the blacker line, occur a little *later* than those of the volts. But inductance has another effect of more importance than any retardation of phase; it produces reactions on the electromotive-force, choking the current down. While the current is increasing in strength the reactive effect of inductance tends to prevent it rising. To produce a current of 40 amperes in a resistance of $1\frac{1}{2}$ ohms would require—for continuous currents—an E.M.F. of 60 volts. But an alternating voltage of 60 volts will not be enough if

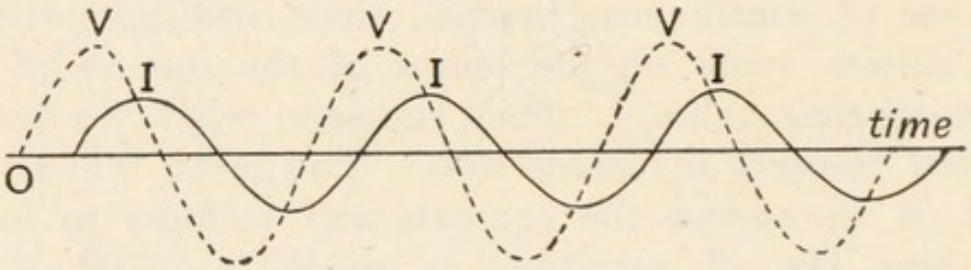


FIG. 302.—Diagram showing Current lagging behind Voltage.

there is inductance in the circuit reacting against the voltage. The matter is complicated by the circumstance that the reactive impulses of electromotive-force are also out of step: they are in fact exactly a quarter period behind the current.

525. Inductive and Non-inductive Circuits.—Any circuit containing self-inductance is described as an *inductive circuit*, as distinguished from a circuit containing resistance only, which is termed a *non-inductive circuit*. In an inductive circuit the reaction which the self-inductance exerts against any change in the strength of the current manifests itself as a self-induced electromotive-force. If an alternating current of i (virtual) amperes is flowing with a frequency of n periods per second through a circuit of inductance L, the reactive electro-

motive-force[1] will be $-2\pi nLi$ (virtual) volts. If, for example, L = 0·002 henry, $n = 50$ periods per second, and $i = 40$ amperes, the reactive electromotive-force will be 25·1 volts. Now if we wish to drive the 40 (virtual) amperes not only through the resistance of $1\frac{1}{2}$ ohms but also against this reaction, we shall require more than 60 volts. But we shall not require 60 + 25·1 volts, since the reaction is out of step with the current. Ohm's law no longer meets this condition. To find out what volts will be needed we have recourse to geometry.

Plot out (Fig. 303) the wave-form OA*bd*, to correspond to the volts necessary to drive the current through the

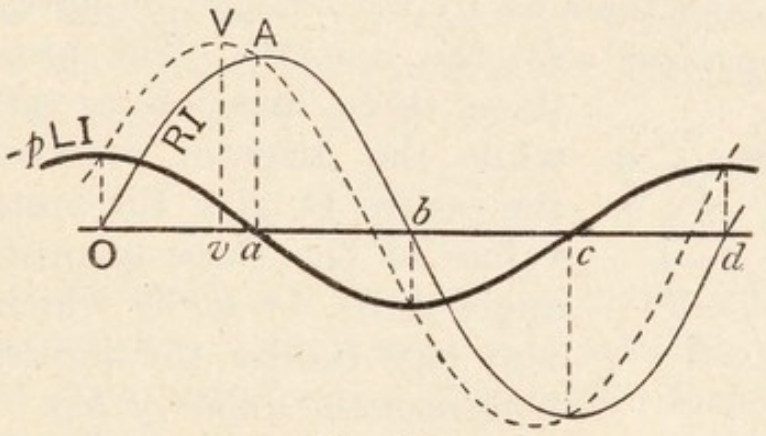


FIG. 303.

resistance, if there were no inductance. The ordinate *a*A may be taken to scale as 60. This we may call the current curve. Then plot out the curve marked $-pLi$ to represent the volts needed to balance the reaction of the inductance. Here p is written short for $2\pi n$. The ordinate at O is 25·1; and the curve is shifted back one quarter of the period: for when the current is increasing at its greatest rate, as at O, the self-inductive action is greatest. Then compound these two curves by adding

[1] This is calculated as follows (from Art. 501), $E = L\,di/dt$. Now i is assumed to be a sine function of the time having instantaneous value $i_0 \sin 2\pi nt$; where i_0 is the maximum value of i. Differentiating this with respect to time we get $di/dt = 2\pi n i_0 \cos 2\pi nt$. The "virtual" values of cosine and sine being equal, we have for E the value $2\pi nLi$, but differing in phase from the current by one quarter of a period.

their ordinates, and we get the dotted curve, with its maximum at V. This is the curve of the volts that must be impressed on the circuit in order to produce the current. It will be seen that the current curve attains its maximum a little after the voltage curve. The current lags in phase behind the volts. If Od is the time of one complete period, the length va will represent the time that elapses between the maxima of volts and amperes. In Fig. 304 the same facts are represented in a revolving diagram of the same sort as Fig. 301. The line OA represents the *active volts* $R \times i$, whilst the line AD at right angles to OA represents the *reactive volts* pLi. Compounding these as by the triangle of forces we have as the *impressed volts* the line OD. The projections of these three lines on a vertical line while the diagram revolves around the centre O, give the instantaneous values of the three quantities. The angle AOD, or ϕ, by which the current lags behind the impressed volts is termed the *angle of lag*. However great the inductance or the frequency, angle ϕ can never be greater than 90°. If OA is 60 and AD is 25·1, OD will be 65 volts. In symbols, the impressed volts will have to be such that $E^2 = (Ri)^2 + (pLi)^2$. This gives us the equation

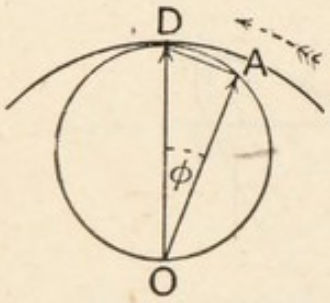


FIG. 304.

$$i = \frac{E}{\sqrt{R^2 + p^2L^2}}.$$

The denominator which comes in here is commonly called *the impedance*, and the product pL is called *the reactance*.

The reciprocal of the impedance is called the *admittance*. It is the quotient obtained by dividing the current in a circuit by the electromotive-force which produces it.

526. Maxwell's Law.—In Figs. 305 and 306 the angle of lag is seen to be such that $\tan\phi = pLi/Ri$ or

$= pL/R$. And it is evident that the effect of the inductance is to make the circuit act as if its resistance instead of being R was increased to $\sqrt{R^2+p^2L^2}$. *In fact the alternating current is governed not by the resistance of the circuit but by its impedance*, which is the conjoint

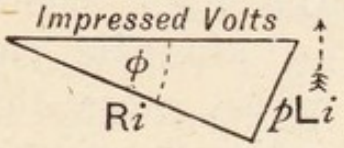


FIG. 305.

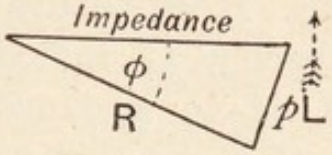


FIG. 306.

effect of resistance and reactance. At the same time the current is lagging as if the angle of reference were not θ but $\theta - \phi$; so that the equation for the instantaneous values of i, when $E = D \sin \theta$, is

$$i = \frac{D \sin(\theta - \phi)}{\sqrt{R^2+p^2L^2}}.$$

This is Maxwell's law for periodic currents as retarded by self-inductance. As instruments take no account of phase, but give virtual values, the simpler form on p. 542 is usually sufficient.

527. Components of Current.—Instead of considering the voltage as resolvable into two components, one driving the current through the resistance, the other driving the current against the reactance, we may regard the matter in another way. We may treat the current as capable of being resolved into two component currents; one, the *active current*, in phase with the voltage; the other, the *reactive current* at right angles in phase to the voltage. If we write i_a for the former, and i_m for the latter, then the whole current i will be equal to $\sqrt{i_a^2+i_m^2}$, as in Fig. 307. Also, $i_a = i \cos \phi$; and $i_m = i \sin \phi$; where ϕ, the angle of phase-difference between i and i_a, is the angle of lag, and is such that

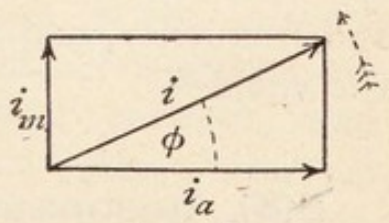


FIG. 307.

tan $\phi = i_m/i$. The in-phase component is called the active component because it is the component which conveys power. The reactive component, also sometimes called the "idle" or "watt-less" component, because it conveys no power but merely reacts, is denoted by i_m to suggest that it is a magnetizing component.

528. Reactance due to Capacity.—The effect of capacity C introduced into an alternate current circuit is to produce a *lead* in phase, since the reaction of a condenser instead of tending to prolong the current tends to drive it back. The reactance is therefore written as $-1/pC$, and the angle ϕ will be such that tan $\phi = -1/pCR$. The impedance will be $\sqrt{R^2 + 1/p^2C^2}$.

If both self-inductance and capacity are present,

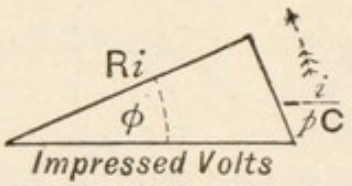


FIG. 308.

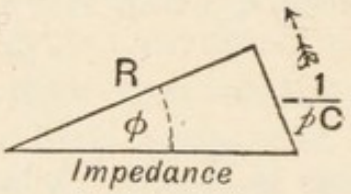


FIG. 309.

tan $\phi = (pL - 1/pC)/R$; the reactance will be $pL - 1/pC$; and the impedance $\sqrt{R^2 + (pL - 1/pC)^2}$.

If the circuit contain no inductance, then the reactance present will be that due to the capacity alone. Suppose the current to be led through a circuit of but small resistance into a condenser of small capacity (say $C = \frac{1}{10}$ microfarad, then $1/pC = 10{,}000$), the current running in and out of the condenser would be governed only by the capacity and frequency, and not by the resistance, and would have the value—

$$i = Epc.$$

529. Resonance.—Since capacity and inductance produce opposite effects they can be used to neutralize one another. They exactly balance if $L = 1/p^2C$. In that case the circuit is non-inductive and the currents

neither lag nor lead, and they obey Ohm's simple law, and the strength of the current depends on the electromotive-force and the resistance only.

Suppose a circuit to have very small resistance but that it has both capacity and inductance. Then it follows that if in that circuit we impress a periodic electromotive-force of the right frequency to make p (*i.e.* $2\pi n$) equal to $1 \div \sqrt{LC}$, there will be a very large alternating current; for at that frequency the circuit is non-inductive, and the inductive reactance pL will be cancelled by the capacitive reactance $1/pC$. But if the frequency is higher than this, pL will be greater than $1/pC$, and the lagging current will be choked by the inductance; whereas if the frequency be too low the capacitive reactance will be too great and the leading current be choked. Hence for every such circuit there is a critical frequency, $n = 1 \div 2\pi \sqrt{LC}$, such that even a small electromotive-force of that frequency may set up a large current. This is the phenomenon of electric *resonance*. (See Art. 602, p. 638.)

530. Choking Coils.—It will be seen that if in a circuit there is little resistance, and much reactance, the current will depend on the reactance. For example if $p(=2\pi n)$ were, say, 628 and $L = 2$ henries while R was only 1 ohm, the resistance part of the impedance would be relatively negligible and the law would become

$$i = \frac{E}{pL};$$

and an impressed electromotive-force of 1000 alternating volts would produce less than 1 ampere in that circuit. Coils with large self-inductance and small resistance are sometimes used to impede alternating currents, and are called *choking coils*, or impedance coils. They are preferred to rheostats for governing alternating currents, because they do not waste power (in heat) as resistances do. If the iron core is made movable, so that the inductance can be varied by moving it into or out of the coil,

the apparatus can be used as a *dimmer* to lower or raise the brightness of lamps.

531. Alternating-current Power.—If to measure the power supplied to a motor, or other part of an alternating-current circuit, we measure separately with amperemeter and voltmeter the amperes and volts, and then multiply together the readings, we obtain as the *apparent watts* a value often greatly in excess of the *true watts*, owing to the difference in phase, of which the separate instruments take no account. The value of the *true watts* divided by the *apparent watts* is called the *power-factor* and is expressed as a decimal or a percentage. The true power (watts) is in reality the product of the voltage with that component of the current which is in phase with it. Hence $W = iV \cos \phi$; where i and V are the virtual values, and ϕ the angle of lag. But the latter is usually an unknown quantity. Hence recourse must be had to a suitable watt-meter; the usual form being an electro-dynamometer (Art. 458) specially constructed so that the high-resistance circuit in it shall be non-inductive.

Whenever the phase-difference (whether lag or lead) is very large, the current, being out of step with the volts, is almost *wattless*. This is the case with currents flowing through a choking-coil or into a condenser, if the resistances are small.

532. High Frequency Currents: Skin-Effect.—The reactive effects of inductance and capacity increase if the frequency is increased. The frequency most used in electric lighting is 50 cycles per second. If high frequencies of 1000 or more cycles per second (see Art. 603) were used the reactions would be excessive. In such cases the currents do not flow equably through the cross-section of the conducting wire, but are confined mainly to its outer surface; even thick rods of copper offering great impedance. At a frequency of 100 the current density at a depth of 12 millimetres from the surface is (in copper) only about $\frac{1}{7}$ of its value in the surface layers. In iron wires the

depth of the skin for $\frac{1}{7}$ value is about 1 millimetre. This phenomenon is known as the *skin-effect*. It is proportional to the conductivity and permeability of the wire, and to the frequency. For such rapid oscillations as the discharge of a Leyden jar, where the frequency is several millions, the conducting skin is probably less than $\frac{1}{100}$ of a millimetre thick. Hollow tubes in such cases conduct just as well as solid rods of the same outer diameter; and flat metal tapes better than round wires of equal weight. The conductance is proportional not to section but to perimeter.

Whenever a current is not distributed equably in the cross-section of any conductor there is a real increase in the resistance it offers; the heating effect being a minimum when the distribution is equal all through the cross-section. The fact that the oscillatory currents are greatest at the skin gives the strongest support to the modern view that the energy in an electric circuit is really transmitted by the surrounding medium and not through the wire (see Art. 610 on energy paths).

533. Alternating-current Electromagnets.—When an alternating current is sent through a coil it produces an alternating magnetic field. An iron core placed in the alternating field will be subjected to a periodic alternating magnetization. Electromagnets for alternating currents must have their iron cores laminated to prevent eddy-currents; and the coils, owing to their choking action, are made with fewer turns of wire than if designed for continuous currents of equal voltage. They repel sheets of copper owing to the eddy-currents which they set up in them; the phase of these eddy-currents being retarded by their self-induction. A remarkable illustration is afforded by constucting an electromagnet with a long core, built up of iron strips, protruding from a magnetizing coil (Fig. 310). If a ring of aluminium is loosely slipped over this core, and an alternating current is switched on into the coil, the ring is violently repelled;

and may even be thrown up some feet into the air The currents induced in the ring are in opposite directions to those in the coil, and hence the repulsion. Moreover the currents in the ring tend to oppose the alternations of the flux in the core and drive the magnetic lines out laterally beneath it. If held down, the ring quickly becomes heated by the induced currents. Elihu Thomson, who discovered these repulsions, constructed some motors based on this principle.

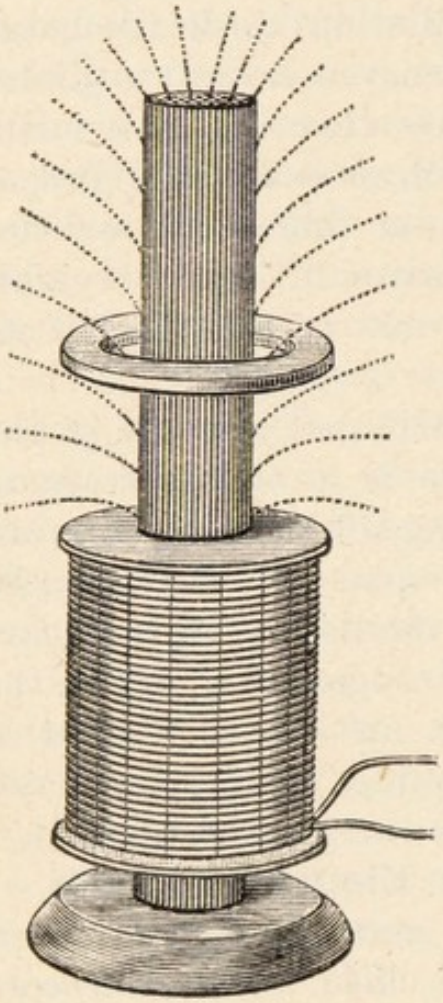


FIG. 310.—Repulsion due to Alternating Currents.

LESSON XLV.—*Alternating Current Generators*

534. Alternators. — The simple alternator (Fig. 285), with its two slip-rings for taking off the current, is merely diagrammatic. In practice machines are wanted which will deliver their currents at pressures of from 1000 to 10,000 volts, with frequencies of from 15 to 50 cycles per second. Lower frequencies than about 40 are unsuitable for lighting; but they are preferred for motor-driving and transmission of power. High voltages are common with alternating currents because of the economy (Art. 551) thereby effected in the copper mains. Under these conditions almost all alternators are designed as multipolar machines; and since the perfect insulation required in the armatures is more readily attained if these parts are stationary, it is usual to fix them, and instead to rotate the field-magnets. One

advantage of alternators over continuous-current generators is that there is no commutator, and no sparking at any collecting brushes.

There are two principal types of alternators :—

(*i.*) Type A. — Field-magnets fixed externally, and consisting of a number of poles, alternately N and S, pointing radially inwards; armature internal, revolving, consisting of a number of coils embedded in slots in the surface of a cylindrical core built up of thin iron disks. In this case the currents generated in the armature are led to 2, 3, or more slip-rings fixed on the shaft, and thence to the circuit through metal brushes which make sliding contact on the rings.

(*ii.*) Type B. — Field-magnet (or *rotor*), revolving internally, consisting of a number of poles, alternately N and S, built upon a foundation wheel, and pointing radially outwards; armature external, fixed, consisting of a number of coils embedded in slots or tunnels just within the face of a laminated iron core. Such a stationary armature is called a *stator*. The terminals of the windings on the stator lead directly to the mains through a suitable switchboard. To excite the magnetism of the revolving field-magnet or magnet-wheel, continuous currents are supplied to it through a pair of slip-rings fixed on the shaft. In all cases, whether the magnets revolve or are stationary, the exciting current is supplied from a suitable source, usually a small continuous-current generator called an *exciter*. Since one whole period corresponds to the passage of a pair of poles N and S, past any conductor, the frequency (*i.e.* number of periods per second) will be equal to the number of pairs of poles in the magnet-wheel multiplied by the number of revolutions per second.

When driven by a slow-speed engine or water-turbine the alternator must have many poles in order to give the required frequency of alternations. When driven by a high-speed steam-turbine the number of poles is

small, usually 4 or 2. For a frequency of 50 periods per second, a 2-pole rotor must revolve at 3000 revolutions per minute; or a 4-pole rotor must run at 1500 R.P.M.; or one with 8-poles at 750 R.P.M., etc. Fig. 311 shows a 24-pole magnet-wheel belonging to a modern alternator of 800 kilowatts output, to be driven at 250 revolutions per minute, by a steam engine of about 1120 horse-power. Fig. 312 depicts the stationary armature of a larger machine requiring a mag-

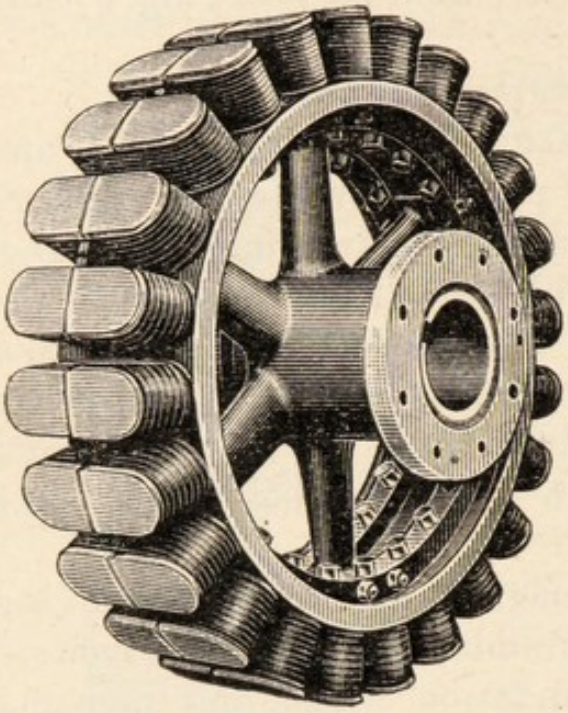


FIG. 311.—Magnet-wheel of an Alternator.

net-wheel with 36 poles, designed to run at 200 revolutions per minute, giving a frequency of 60 periods per second.

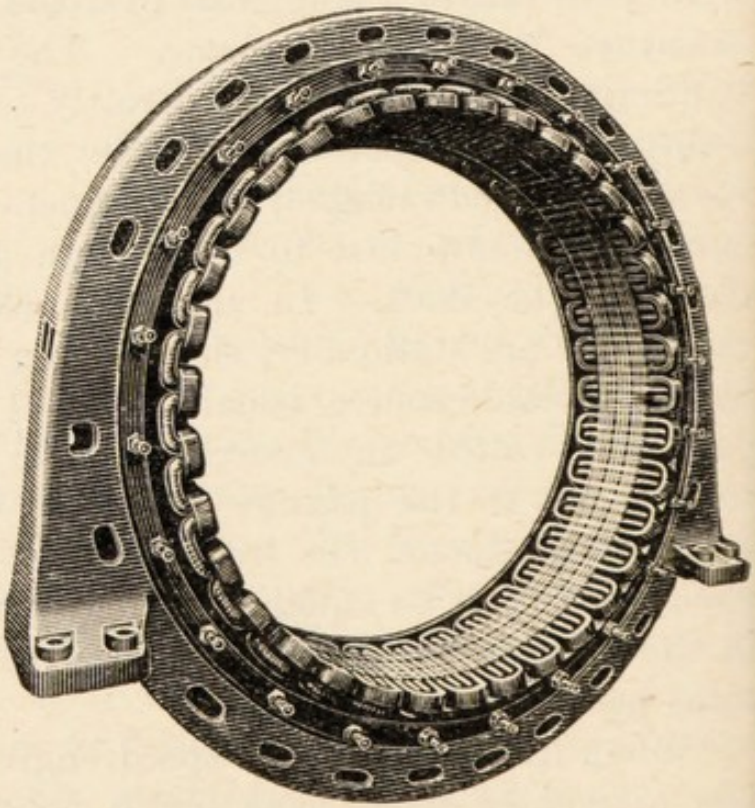


FIG. 312.—Stator of an Alternator.

If the stator of an alternator is wound with but one coil or group of coils opposite each pole of the magnet-wheel, the inductive action in each coil or group as the poles fly past them will be simultaneous, hence the coils may be joined up in one

single circuit, and the (alternating) electromotive-force will be proportional to the number of coils so joined up. A single coil or loop may be regarded as composed of two conductors; and if the whole number of conductors so joined together be called Z, the number of loops or coils will be $\frac{1}{2}$Z. If the flux from any one pole of the magnet-wheel (all poles being supposed to be equally strong) be denoted by $\mathfrak{F}$, and if the frequency is called n, then the generated electromotive-force E expressed in virtual volts is given by the formula

$$E = k \times n \times Z \times \mathfrak{F} \div 10^8;$$

where k is a coefficient of value from 2 to 2·22, depending on the shape of the poles and the distribution of the coils in the slots. A machine with only one such circuit on the stator windings is called a *single-phase* alternator.

Example.—A certain 20-pole alternator having a flux of 1,750,000 lines per pole, has a coil of 24 turns opposite each pole. It revolves at 300 revolutions per minute. Assume $k=2{\cdot}16$. Here $n=50$, because 10 pairs of poles pass each coil 5 times per second; and $Z=960$ because the total number of turns in series is 480. Hence by the formula $E=1814{\cdot}4$ volts.

535. Two-phase and Three-phase Alternators.—If the stator of an alternator is wound with two (or three) independent similar windings which are displaced with respect to one another so that the inductive actions on the different sets of windings are not simultaneous, there will be a difference of *phase* (Art. 524) between the electromotive-forces induced in them. *Two-phase* alternators are those in which the second set of windings is displaced by half a pole-pitch with respect to the first set; and the respective electromotive-forces will consequently differ by a quarter of one period. They furnish two separate alternating currents. *Three-phase* alternators have three separate sets of similar windings, displaced from one another by two-thirds of a pole-pitch, so that there will be three electromotive-forces generated, of

equal amplitude, but differing in phase from one another by one-third of a period. Such machines, furnishing three alternating currents, are the most usual kind of alternator, since the three-phase system is best adapted for the transmission of power. Three lines only, not six, are required to convey the three currents; because if one end of each of the three windings is brought to a common junction, and the other three ends are joined respectively to the three lines, no other return line is needed; each line serving in succession as a return for the currents in the other lines. How this occurs is understood from the diagram of Fig. 313 which shows three successive equal

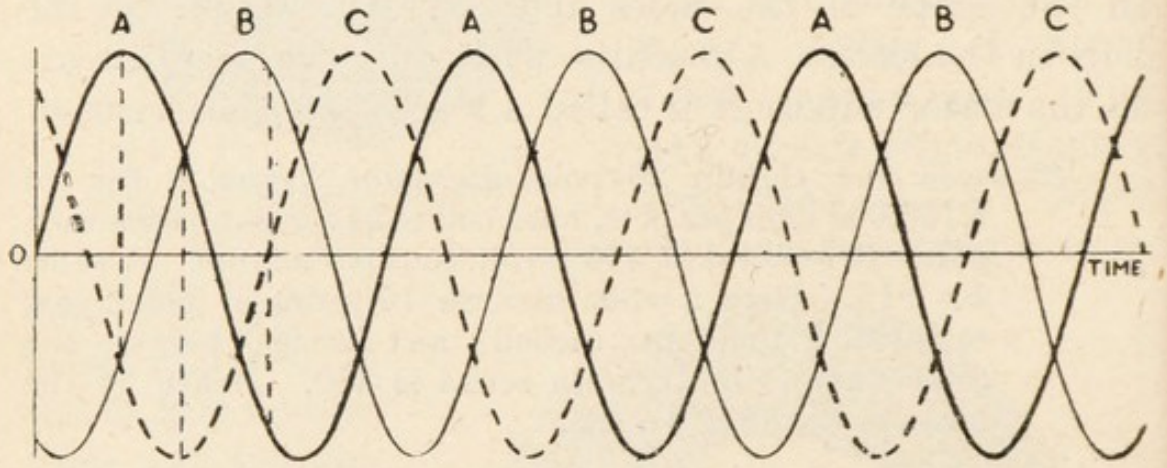


FIG. 313.—The Three Currents of a Three-phase System.

alternating currents, A, B, C, properly spaced out at equal intervals of time. It will be noticed that at the moment when any one is at its positive maximum value the other two are each of half-value and negative: and that at the moment when any one is at zero-value, the other two are at 86·6 of the maximum, one positive, one negative. When the three circuits are joined as described the value of the volts between the lines is equal to $\sqrt{3}$ times that of the volts generated in any one of the three windings.

536. Turbo-Alternators.—For use with steam-turbines a special type of alternator has been evolved. The high speed necessitates few poles, and a most solid and symmetrical construction of the rotor. This is

usually constructed as a steel cylinder, devoid of project-

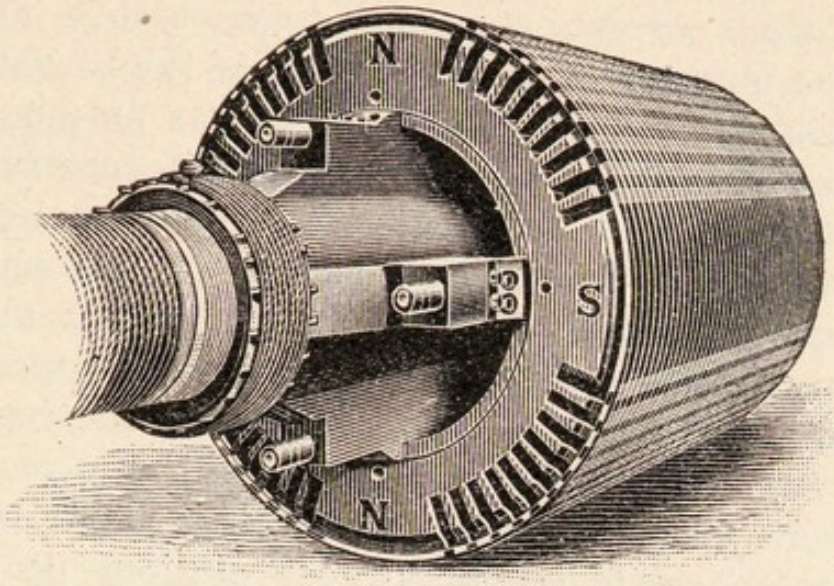


FIG. 314.—Rotor of Parsons's Turbo-alternator of 25,000 Kilowatts Output.

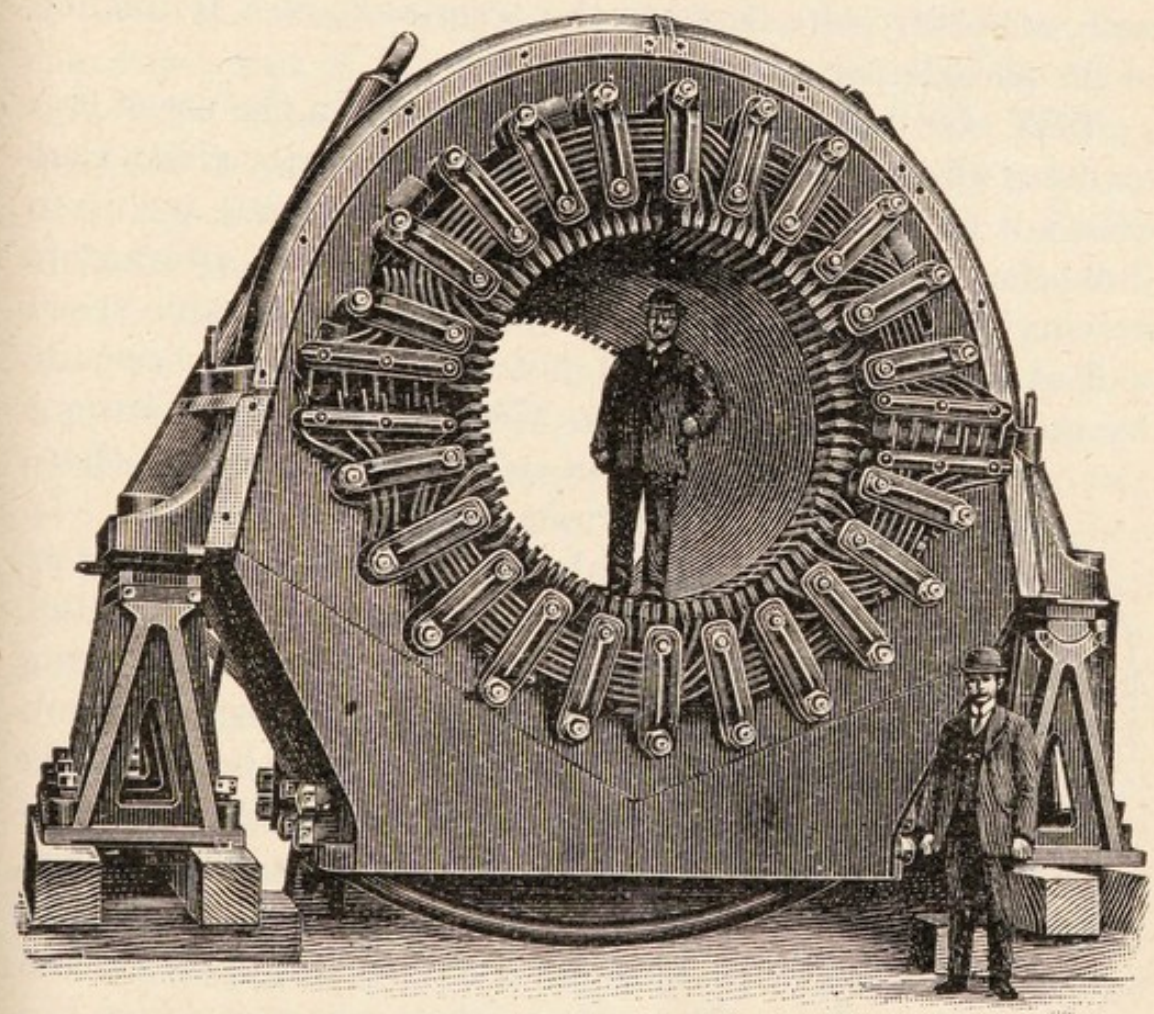


FIG. 315.—Stator of Parsons's Turbo-alternator of 25,000 Kilowatts Output.

ing poles, but in which the magnetic poles are formed

by inserting in deep slots the copper windings wherein the exciting current is caused to circulate. Fig. 314 shows the unwound core of the rotor of the largest turbo-alternator yet made, of 25,000 kilowatts output, requiring about 33,000 horse-power to drive it, constructed by Messrs. Parsons of Newcastle for the Commonwealth Company of Chicago. The diameter of this core is 74 inches and its length $130\frac{1}{4}$ inches: it weighs about 50 tons; and has 4 poles. The stator of this machine is depicted in Fig. 315. The diameter of the bore is 75 inches, and there are 84 slots each enclosing one copper conductor. The complete stator weighs about 100 tons. The machine revolving at 750 revolutions per minute furnishes 3 alternating currents of about 3200 amperes each, at 4500 volts between the terminals, at a frequency of 25 periods per second.

537. Coupling of Alternators.—In the use of two or more alternators on one circuit a peculiarity arises that does not exist with continuous-current dynamos, owing to differences of phase in the currents. If two alternators driven by separate engines are running at the same speed and at equal voltage, it will not do to join their circuits by merely switching them to the mains if they are not also *in phase* with one another; or serious trouble may occur. In central station work it is usual to run several machines all in parallel. Now if two machines are feeding into the same mains each is tending to send current back to the other; and if their electromotive-forces are at any instant unequal, that with the greater will tend to send its current the opposite way through the other. To explain what occurs consider Fig. 316, which is a revolving diagram of the same kind as Figs. 301 and 304. If the two alternators are exactly in

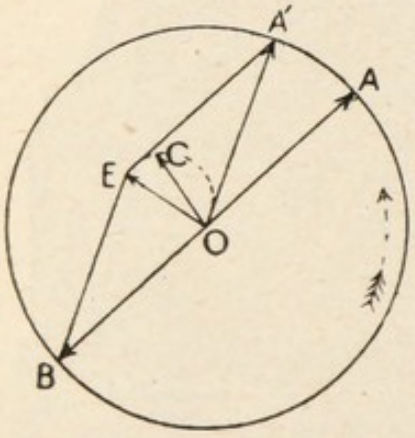


FIG. 316.—Diagram of Alternators in Parallel.

step they will both be sending a pulse of current toward the mains at the same moment, but, so far as the circuit connecting them is concerned, these impulses will be exactly opposed. Let OA and OB represent these two exactly-opposed impulses. Now suppose one of the two machines to gain a little on the other, OA shifting forward to OA′. The two electromotive-forces no longer balance, but will have a resultant OE tending to make a current oscillate through the two machines, this current being out of phase both with the leading machine A and with the lagging machine B. But this local current will itself lag a little in phase behind OE because of the inductance in its path. Let the phase of the current then be indicated by OC, which is set back a little. There is now a current surging to and fro between the two machines, and it is obviously more nearly in phase with OA than with OB. This means that in the leading machine A the volts and amperes are more nearly in phase with one another than in the lagging machine B. Reference to Arts. 455 and 519 will at once show that the current is helping to drive B as a motor, and that a greater mechanical effort will be thrown on A, which is acting more as a generator. Hence this interchange of current tends automatically to bring up the lagging machine and to load the leading machine. They will come back into phase. All alternators of good construction suitably driven will run together in parallel, even though their electromotive-forces are unequal. On the other hand, if two alternators are joined in series, the resulting current, when they are ever so little out of phase, tends to load the lagging machine and hasten the leading one till they get into complete opposition of phase, one running entirely as generator, the other entirely as motor. This is excellent for transmission of power from an alternator at one end of a line to a synchronous alternator at the other: the two machines keep step at all loads. But they will not run together in series if both are to act as

generators, unless rigidly coupled together on the same shaft.

To prevent accidents arising from too sudden a transfer of current between two machines it is usual in lighting stations to employ a *synchronizer*, a device to indicate the phases of the alternations. When an alternator is to be switched into circuit (in parallel with one or more others) the operator does not put the switch in until (speed and volts being both right) the electromotive-force of the machine has come exactly into identical phase with that of the circuit into which it is to be introduced.

LESSON XLVI.—*Transformers and Converters*

538. Alternating-Current Transformers.—Transformers are needed in the distribution of currents to a distance, because glow-lamps in the houses need low pressures of 50 to 100 or 200 volts, whilst for economy of copper in the mains it is necessary (see Art. 551) that the generators should work at high pressures of 1000 to 5000 or more volts. The principle of transformation was briefly touched in Art. 245. Alternating-current transformers are simply induction-coils having well-laminated iron cores, usually of thin, soft sheet-iron strips piled together, and shaped so as to constitute a closed magnetic circuit. Upon the cores are wound the *primary coil* to receive the alternating current, and a *secondary coil* to give out other alternating currents. As the transformer is generally required to reduce the pressure from high to low, the primary usually consists of many turns of fine copper wire, very well insulated, to receive a small current at high pressure; and the secondary of a few turns of thick copper wire or ribbon, to give out a much larger current at low pressure.

To transform down from about 2000 volts to 100 volts, the ratio of the windings, called the *ratio of trans-*

formation, will be 20 : 1. Whatever the ratio of the voltages, the currents will be about in the inverse ratio, since, apart from the inevitable small losses in transformation, the power put in and taken out will be equal. Taking the above case of a transformer having 20 : 1 as the ratio of its windings, if we desire to take out of the secondary 300 amperes at 100 volts, we must put into the primary at least 15 amperes at 2000 volts.

In scattered districts a small transformer is provided for each house, the lamps being in the low pressure circuit. In cities large transformers are placed in sub-stations, from which issue the low-pressure mains distributing the current to the houses. Fig. 317 shows

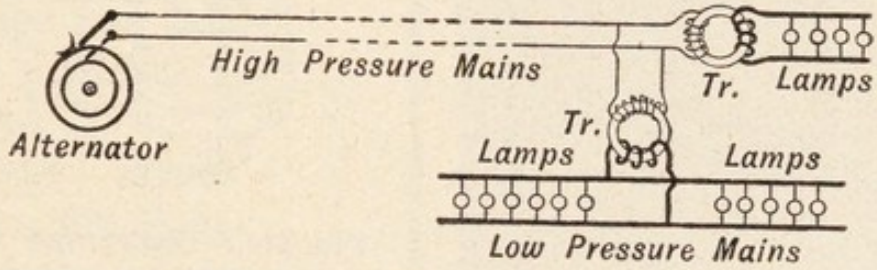


FIG. 317.—Transformers in a Distributing System.

in diagram the simple use of transformers on a distributing system.

539. Energy Relations.—It is clearly impossible to take out from the secondary of a transformer more power than is being supplied to the primary coils. In the above example 15 amperes are being supplied at 2000 volts, that is 30,000 watts are being supplied to the primary, therefore the secondary, working at 1000 volts could not give out more than 300 amperes at 100 volts, at the most. There are inevitable losses of energy in the transformer itself owing to the internal resistance of the copper coils and to the waste of power by hysteresis and eddy-currents (Arts. 395 and 500) in the iron. Suppose these losses amount to $1\frac{1}{2}$ per cent, then if we are to take 300 amperes from the secondary, the

primary will need not 15 but 15·225 amperes. But it will actually take in a little more than this because a small additional magnetizing current is required to magnetize the iron core. Even at times of no-load, when no current is being taken from the secondary windings there will be a small magnetizing current in the primary. In the above example of a 30-kilowatt transformer, the no-load magnetizing current would probably amount to about half an ampere.

540. Construction of Transformers.—The iron cores are always built up of thin sheets of soft iron.

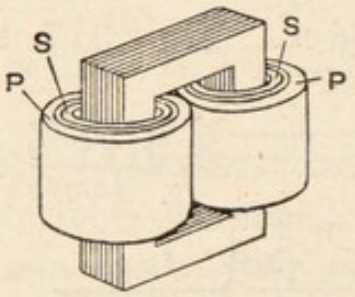


FIG. 318.—Transformer with Concentric Coils.

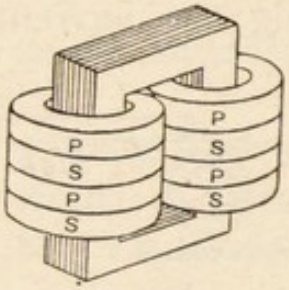


FIG. 319.—Transformer with Sandwiched Coils.

Figs. 318 and 319 show a simple pattern. Both sets of windings, primary and secondary, are wound in coils that surround the two limbs. Sometimes the primary and secondary coils are wound as concentric cylinders that slip one inside the other, as in Fig. 318, sometimes as ring coils sandwiched between one another as in Fig. 319. In either case the primary coils must be most carefully insulated from one another, and from the core. In another common form the core is constructed as in Fig. 320, with the P and S coils surrounding a single core, while the outer parts of the iron stampings complete the magnetic circuits.

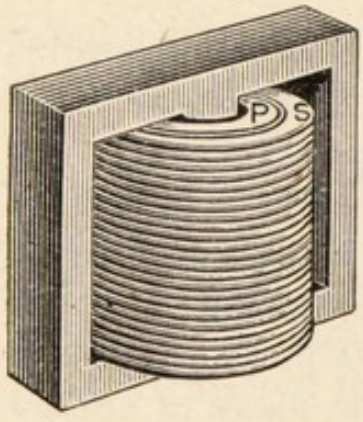


FIG. 320.—Transformer with Divided Magnetic Circuit.

It is most important in transformers that the whole of the magnetic lines created by the currents in one of the coils should pass through the interior of the other coils: in other words, that there should be no magnetic leakage. Hence all gaps or joints in the iron of the magnetic circuit should be as far as possible avoided, and the two sets of coils should be as close to one another as is consistent with good insulation. Fig. 321 shows a small transformer manufactured by Messrs. Ferranti, having terminals insulated on *porcelain supports* at the tops.

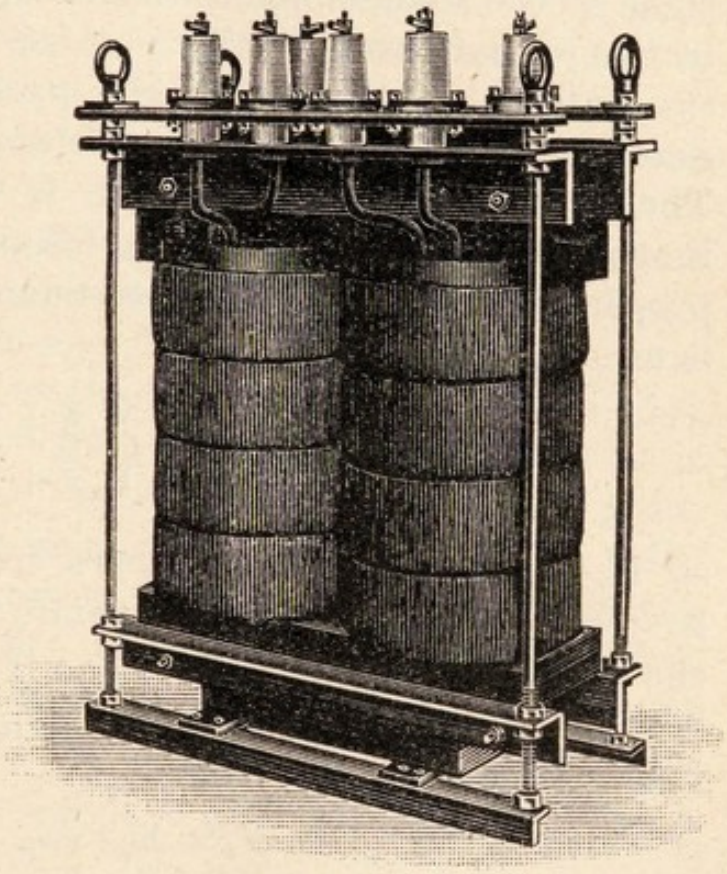


FIG. 321.—A Small Modern Transformer.

Large transformers for lighting and power transmission are usually immersed in oil tanks to preserve good insulation and promote cooling.

For three-phase working (Art. 535), a transformer is needed having three primary and three secondary coils, wound on three connected cores. Or three separate transformers may be used.

541. Elementary Theory of Transformers.—If the primary volts are maintained constant, the secondary volts will be nearly constant also, and the apparatus becomes beautifully self-regulating, more current flowing of itself into the primary when more lamps are turned on in the secondary circuit. This arises from the choking effect of self-induction in the

primary. If no lamps are on the secondary circuit the primary coil simply acts as a choking-coil. When all the lamps are on, the primary acts as a working-coil to induce currents in the secondary. When only half the lamps are on, the primary acts partly as a choking-coil and partly as a working-coil.

Let V_1 be the volts at the primary terminals, V_2 those at the secondary terminals; S_1 the number of turns in the primary coil, S_2 the number in the secondary; r_1 the internal resistance in the primary, r_2 that of the secondary. Call the ratio of transformation $k = S_1/S_2$. The alternations of magnetism in the core will set up in the two coils electromotive-forces E_1 and E_2 strictly proportional to their respective numbers of turns (if there is no magnetic leakage);

$$E_1 = 4{\cdot}44\ n\ S_1 \mathfrak{F} \div 10^8;$$
$$E_2 = 4{\cdot}44\ n\ S_2 \mathfrak{F} \div 10^8;$$

so $E_2 = E_1/k$; and since (apart from magnetizing and hysteresis effects which necessitate a small addition to the primary current) $E_1 i_1 = E_2 i_2$, it follows that $i_1 = i_2/k$. The volts lost in the primary are $r_1 i_1$, those in the secondary $r_2 i_2$. Hence we may write

$$V_1 = E_1 + r_1 i_1,$$
$$V_2 = E_2 - r_2 i_2.$$

Writing the first as $E_1 = V_1 - r_1 i_1 = V_1 - r_1 i_2/k$, and inserting E_1/k for E_2 in the second equation, we get

$$V_2 = \frac{V_1}{k} - \left(\frac{r_1}{k^2} + r_2\right) i_2;$$

which shows that everything goes on in the secondary as though the primary had been removed, and we had substituted for V_1 a fraction of it in proportion to the windings, and at the same time had added to the internal resistance an amount equal to the internal resistance of the primary, reduced in proportion to the square of the

ratio of the windings. We also see that to keep the secondary volts constant the primary generator must be so regulated as to cause the primary volts to rise slightly when much current is being used in the secondary circuit. The currents in the two coils are in almost exact opposition of phase; they reach their maxima at the same instant, flowing in opposite senses round the core. The efficiency of well-constructed transformers is very high (98 per cent, or more), the internal losses being a very small percentage of the working load.

542. Self-inductance and Mutual Inductance in Transformers.—It is obvious that each of the two coils of a transformer, if considered by itself, possesses a coefficient of self-inductance (Art. 501). Let the self-inductance of the primary by itself be called L_1, and that of the secondary by itself be called L_2. When they are considered as working together there will be a coefficient of mutual inductance M between them (Art. 497). We have seen (Art. 497) that if two coils, of S_1 and S_2 turns respectively, are wound around the same core $M = S_1S_2/Z$. From Art. 501 we see that the respective coefficients of self-inductance will be $L_1 = S_1^2/Z$, and $L_2 = S_2^2/Z$. So, if there is no magnetic leakage, $M = \sqrt{L_1L_2}$; and $L_1 = kM$, and $L_2 = \frac{1}{k}M$. And the effect when the transformer is supplying the load is that the mutual inductance neutralizes the effect of the self-inductance in both circuits. But if there is any magnetic leakage M will be less than $\sqrt{L_1L_2}$, leaving uncompensated part of the self-inductances of the circuits, so that in each of them there is some choking action. Moreover, when the secondary is only partly loaded its current neutralizes part only of the self-inductance of the primary, which therefore automatically chokes off a part of the current that would otherwise flow in from the primary mains. In fact, the effective self-inductance of the primary when the transformer is at work is equal to

$L_1 - M\frac{i_2}{i_1}$. At full-load i_2/i_1 is nearly equal to k, so that the primary self-inductance is almost neutralized. At no-load, when $i_2 = 0$, the primary current is choked down by the self-inductance L_1 to a mere dribble of magnetizing current. As a result, the flow of primary current from the primary mains automatically adjusts itself to the requirements of the load on the secondary circuit.

543. Coupling of Circuits by a Transformer.— If the transformer is arranged so that in neither circuit there is any uncompensated self-inductance, so that $M = \sqrt{L_1 L_2}$, circuits are said to be *tight-coupled*; this is the case only when there is no magnetic leakage, so that all the lines of flux interlink with both circuits. But if the transformer is such that a considerable proportion of the magnetic lines due to current in either circuit fail to interlink themselves with the other circuit, M will be much less than $\sqrt{L_1 L_2}$, and the circuits are said to be *loose-coupled*. The effect of loose-coupling can be produced either by keeping the primary windings far away from the secondary windings, or by adding separate self-inductance to either or both of the circuits. The degree of coupling is expressed by the formula $c = M \div \sqrt{L_1 L_2}$; c being called the coefficient of coupling.

544. The Problem of Conversion. Motor-generators. — To convert an electric current of one species into an electric current of another species is a problem that presents itself in many different forms. The general solution of the problem is to set the current of one species to run a motor that mechanically drives a generator supplying current of the other species. Such a group of two coupled machines is called a *motor-generator*. In this way an alternating current may be *converted* into a continuous current by using an alternating motor coupled to a continuous-current generator. Or a two-phase alternating current may be converted into a three-phase alternating current. Or an alternating

current of a given frequency may be converted into another alternating current of a different frequency by the use of two coupled alternators having different numbers of poles, this arrangement being called a *frequency-changer*. In all these cases it is the electrical energy which is mechanically transferred from one machine to another.

545. Continuous-current Converters. — To convert continuous currents from one voltage to another it is necessary to employ a rotating apparatus, which is virtually a motor-generator. For example, a motor receiving a current of 10 amperes at 1000 volts may be made to drive a dynamo giving out nearly 200 amperes at 50 volts. Instead of using two separate machines, one single armature may be wound with two windings and furnished with two commutators; the number of turns in the windings being proportioned to the voltages, and their sectional areas to the amperes. One field-magnet suffices. The elementary theory of these is the same as that in Art. 541, E_1 and E_2 now standing for the electromotive-forces respectively induced in the two windings on the revolving armature.

546. Rotatory Converters, or Synchronous Converters. — Revolving machinery equivalent to a combination of an alternating motor and continuous-current dynamo may be used to transform alternating currents into continuous, or *vice versa*. In this case also two separate machines need not always be used. Fig. 322 represents in diagram an elementary *rotatory converter* having both a simple commutator to collect continuous currents, and a pair of slip-rings for alternating currents. Such a machine may convert continuous currents into

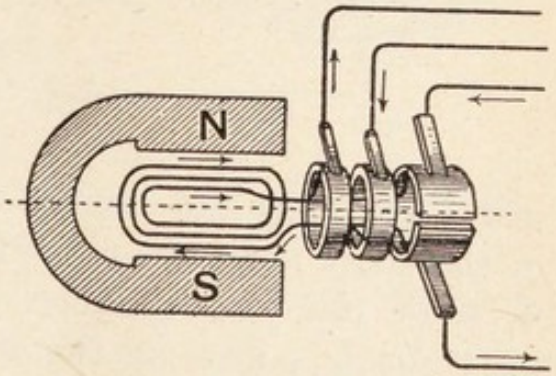


FIG. 322.—Diagram of a Simple Converter.

alternating, or alternating into continuous. Or it may act as a motor if supplied with either kind of current; or may, if driven mechanically, generate both kinds of current at the same time.

The *rotatory converters* of commerce, of which Fig. 323 is an example, have armatures wound exactly like those of ordinary continuous current dynamos, with the

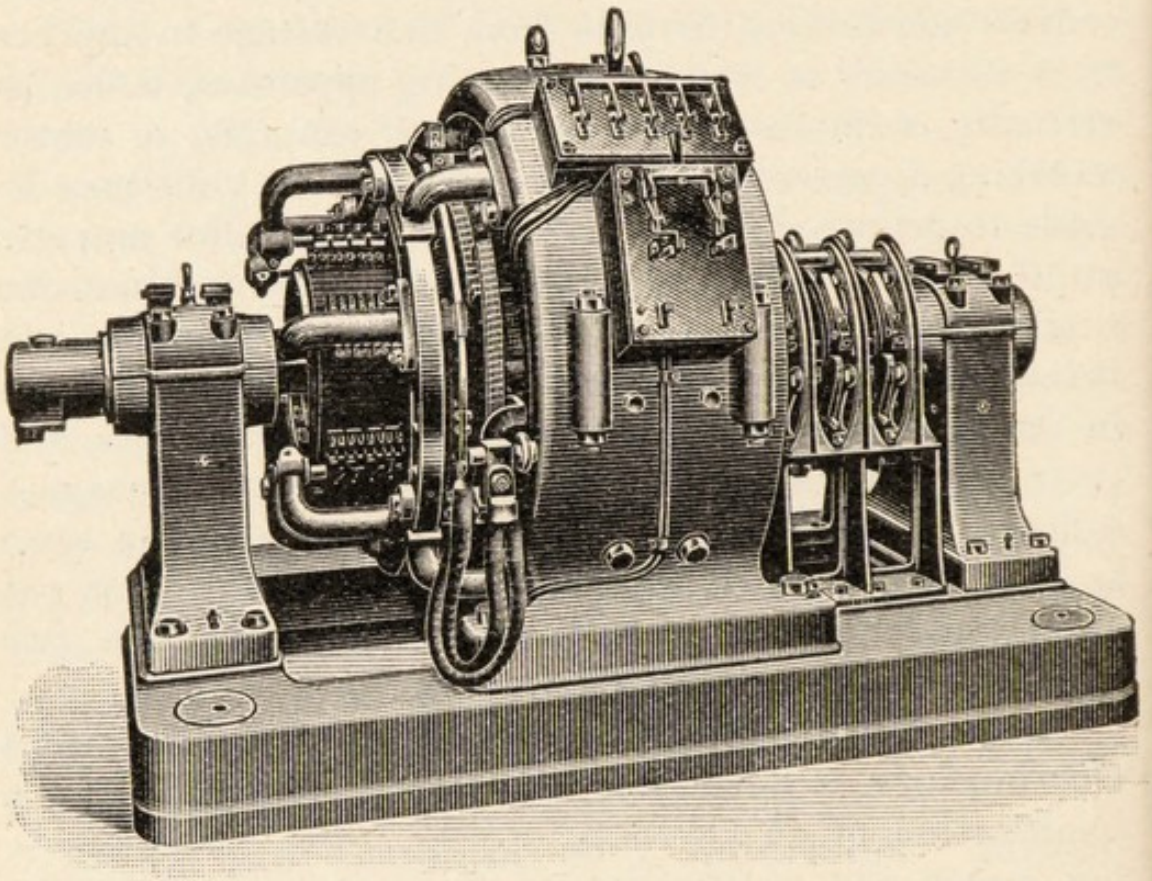


FIG. 323.—A Small Rotatory Converter.

usual windings and commutator. But at the other end of the shaft they are provided with a set of slip-rings, 3, 4, 6 or more in number, connected symmetrically to appropriate points on the winding, to suit the alternating currents with which they have to deal. If supplied through the slip-rings with alternating current they run as synchronous motors (Art. 547) and generate continuous currents which are taken off by the brushes at the commutator. The field-magnets are excited either

separately or by taking a fraction of the current from the continuous-current side.

LESSON XLVII.—*Alternating-current Motors*

547. Synchronous Motors. — We have seen (Art. 537) that one alternator can drive another as a motor, the two machines in series working in synchronism. There are two disadvantages in such motors—(i.) that they are not self-starting, but must be brought up to speed before the current is applied ; (ii.) that their field-magnets must be separately excited with continuous currents. Other forms of motor have consequently been sought. Ordinary continuous-current motors, if made with laminated iron magnets, will work, though not well, with alternating currents.

548. Polyphase Currents.—We have seen that alternators can be designed to generate two, or three, alternating currents of equal frequency but differing from one another in phase. We have now to see how, if two equal alternate currents, differing in phase by one-quarter of a period, are properly combined, they can be made to produce a *rotatory magnetic field.* And in such a rotatory field conductors can be set rotating, as was first suggested by Baily in 1879. Consider an ordinary Gramme ring (Fig. 324) wound with a continuous winding. If a single alternating current were introduced at the points AA′ it would set up an oscillatory magnetic field, a N-pole growing at A, and an S-pole at A′, then dying away and reversing in direction. Similarly, if another alternate current were introduced at BB′, it would produce another

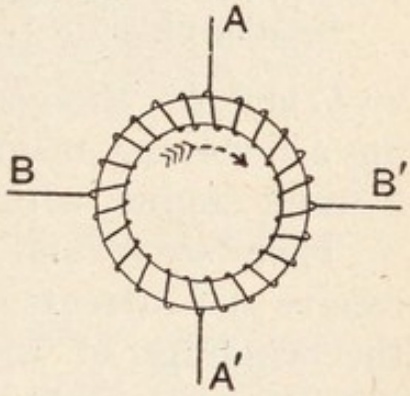


FIG. 324.—Two-phase Rotating Field.

oscillatory magnetic field in the BB′ diameter. If both these currents are set to work but timed so that the BB′ current is $\frac{1}{4}$ period behind the AA′ current, then they will combine to produce a *rotatory* magnetic field, though the coil itself stands still. This is quite analogous to the well-known way in which a uniform rotatory motion, without any dead points, can be produced from two oscillatory motions by using two cranks at right angles to one another, the impulses being given $\frac{1}{4}$ period one after the other. The above combination is called **a two-phase** system of currents. If the BB′ current is $\frac{1}{4}$ period later than the AA′ current, the rotation in Fig. 324 will be clockwise. Another way of generating a rotatory field is by a **three-phase** system[1] (Art. 535) of currents. Let three alternating currents, differing from one another by $\frac{1}{3}$ period (or 120°), be led into the ring at the points A B C. The current flows in first at A (and out by B and C), then at B (flowing out by C and A), then at C (out by A and B), again producing a revolving magnetic field. This is analogous to a 3-crank engine, with the cranks set at 120° apart.

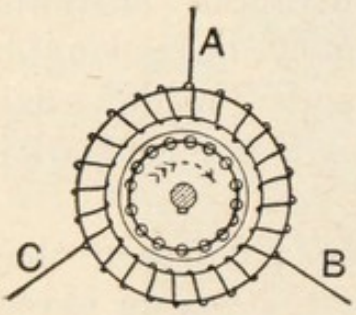


FIG. 325.—Three-phase Rotating Field.

There are several ways of combining the circuits that receive the currents of the various phases. For example, the windings of Fig. 324 might be divided into four separate coils, each having one end joined to a common junction, and the four outer ends joined respectively to the four line wires. Or the windings of Fig. 325 might be arranged as three separate coils, each having one end joined to a common junction, and with the three outer ends joined respectively to the three line wires. Such arrangements would be called *star* groupings, as distinguished from the *mesh* groupings of the cuts. Also

[1] Three-phase currents on a large scale were first used in the famous Frankfort transmission of power in 1891. See Art. 551.

the coils, in whichever way grouped, need not be wound upon a ring. The two-phase coils of Fig. 324 might be wound upon four inwardly-projecting pole-pieces; and the three-phase coils of Fig. 325 might be wound upon three inwardly-projecting pole-pieces. Or in larger multipolar machines a three-phase set of coils might be arranged upon a set of six, nine, twelve, or more projections, in regular succession, or be embedded in slots exactly as in the stators of alternators.

549. Induction Motors.—In such rotating mag-

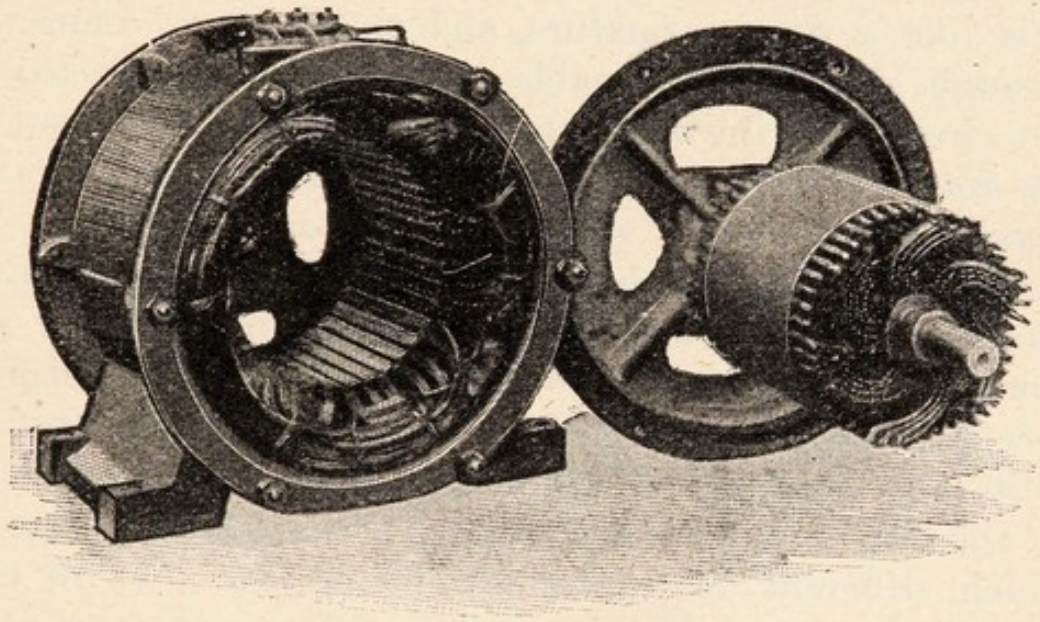


FIG. 326.—A small Induction Motor, showing Stator and Roto.

netic fields any pivoted masses of metal at once begin to rotate, and will acquire a speed a little less than the speed at which the invisible field revolves. In such a centred mass, or *rotor*, eddy-currents are set up (just as in Arago's rotations, Art. 500), which drag the metal mass and tend to turn it. The strength of these currents in the rotating part depends on the relative speed of the field and the rotor. If the rotor were to revolve with speed equal to the revolving field, the eddy-currents would die away, and there would be no driving force. The difference between the speed of the field and the

speed of the rotor is called *the slip*. At full load the slip does not usually exceed 3 or 4 per cent of the synchronous speed. The rotor actually used in such motors consists of a cylindrical core built up of thin iron disks, over which is built up a sort of squirrel cage of copper rods joined together at their ends into a closed circuit. The rods are inserted in slots or holes just below the surface of the core. The rotor need not have any commutator or slip-rings, and is entirely disconnected from any other circuit. It receives its currents wholly by induction. In some forms the rotor is wound with coils like a drum armature, and the coils are connected through slip-rings to enable resistance to be inserted in the circuits of the windings at starting, and cut out as the rotor gets up its speed. Such *induction motors* or *asynchronous motors* start with considerable torque (or turning moment) and have a high efficiency on full load. Similar motors for single-phase alternating currents are now in extensive use. To procure the necessary difference of phase at starting, the alternating current must be split into two currents differing in phase. This is done by the use of a divided circuit, in the two branches of which different reactances are introduced. If in one branch there is a choking-coil to offer inductance, the current in that branch will be retarded. If in the other there is a condenser, the current in this branch will be advanced in phase. Or if a plain resistance is used in that branch, the current in it will be less retarded in phase. Combining these two currents a rotatory field is produced for starting the movement. When once the motor has started a further turn of the switch simply puts on the alternating current, as at AA′ in Fig. 324, and it continues to be driven, though the impulse is now only oscillatory.

550. Commutator Motors. — In recent years alternating motors, both three-phase and single-phase, have been introduced, consisting of a stator, similar to

those already described, to which the currents are supplied, and a rotor that is furnished, like the drum armature of an ordinary dynamo, with a commutator and sets of brushes. In some cases the rotor circuits are in series with those of the stator, in other cases in shunt, or in some cases they are short-circuited. Motors of this class have the advantage that they can be adjusted so as not to lower the power-factor of the circuit, as induction motors are liable to do.

The field-magnets must be built up of thin laminations or stampings of thin sheet-iron or mild steel.

CHAPTER XI

TRANSMISSION AND DISTRIBUTION OF POWER

LESSON XLVIII.—*Electric Transmission of Power*

551. Transmission of Power from Generator to Motor.—Power may be transmitted to great distances electrically from a generator at one end of the circuit to a motor at the other. A mountain stream may be made to turn a turbine which drives a dynamo or alternator, the currents from which are conveyed to some centre of population by insulated wires to motors which reconvert the electrical power into mechanical power. Electric transmission on the large scale may be said to date from 1891 by the striking demonstration at Frankfort, in which 140 horse-power was conveyed from the Falls of the Neckar at Lauffen, 117 miles away, through three wires only 4 millimetres in diameter, with a nett efficiency of 74 per cent, including all losses. This was followed by the erection of the first great power station at Niagara. Since that date power stations have been erected in all quarters of the world, in Switzerland, Lombardy, Norway, Sweden, the United States, and Canada; in fact wherever large waterfalls are available. Millions of horse-power have thus been utilized for driving factories, for lighting, and for electrochemical processes.

Fig. 327 illustrates the case of a simple transmission

between two machines using continuous current. In one the electromotive-force drives the current, in the other the electromotive-force opposes the current. The first acts as generator (by the principle of Art. 455), the second as motor. If their respective electromotive-forces are E_1 and E_2 the electrical efficiency of the transmission is the ratio E_2/E_1.

The power lost in the line by reason of its resistance is the chief difficulty to face in such transmissions, owing to the prohibitive price of copper for carrying large

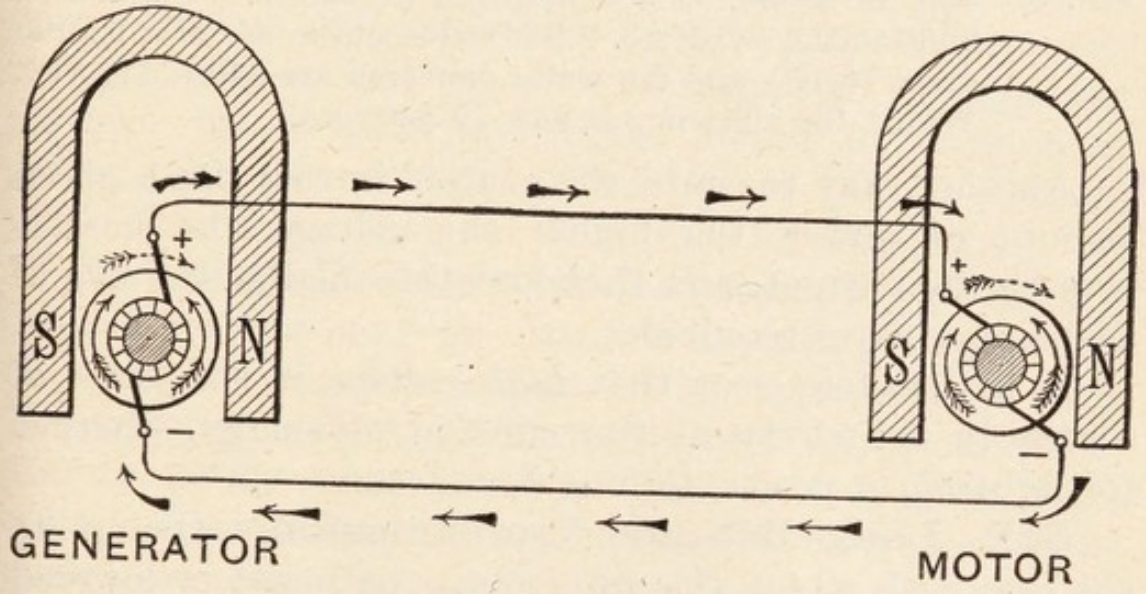


FIG. 327.—Elementary Diagram of Electric Transmission of Power.

currents without overheating. The watts wasted in a line of resistance R (Art. 459) are $= i^2R$. The gross watts utilized are (Art. 454) $= iV_M$, where V_M is the volts at the motor end. Hence the power that must be generated at the sending end of the line is $i^2R + iV_M$ watts. Now it will be obvious that one may keep the i^2R loss constant and yet increase the power that is transmitted by increasing V_M the voltage at the motor—using in fact a high-voltage motor, and of course a high-voltage generator to correspond. To put the matter in another way. Let V_G be the volts at the generator end of the line, $(V_G - V_M)/R$ will be $= i$. Now we may keep i constant

(and therefore the i^2R loss constant) and yet increase the voltages, provided $V_G - V_M$ remains as before.

Example.—Suppose a line of copper-wire 20 miles long has resistance of 100 ohms. A current of 6 amperes in it will waste 3600 watts or nearly 5 horse-power. To send 6 amperes through 100 ohms requires a difference of potentials of 600 volts. Suppose $V_G = 1000$ and $V_M = 400$, $V_G - V_M = 600$. The watts sent in are $iV_G = 6000$, and the watts delivered are $iV_M = 2400$. Of 8 horse-power put in only about $3\frac{1}{4}$ are delivered, the efficiency being $V_M/V_G = 40$ per cent. Now suppose V_G increased to 2000 volts, and V_M to 1400. $V_G - V_M = 600$, as before. $i = 6$ amperes, as before. i^2R loss is 3600 watts, as before. But watts sent in are now 12,000 (over 16 HP), and the watts delivered are 8400 ($11\frac{1}{4}$ HP). Whilst the efficiency is now 70 per cent.

Another way to state the matter is that for a given amount of power, the higher the voltage, the smaller may be the current, and therefore the smaller the size of the copper wires required.

It is therefore clear that *high voltage* is the secret of success in the electrical transmission of energy, whether for lighting or power, to long distances.

552. Long-distance Transmission.—Owing to the ease with which the voltage can be raised or lowered by the use of stationary transformers (Art. 538) alternating currents are almost always preferred for long-distance transmission: and three-phase currents are preferred to single-phase because of the greater economy of copper for equal maxima of potential difference.

There are in Great Britain few examples of long-distance transmission because of the lack of large water-power stations. In the transmission of energy from the Falls of Tivoli to light the city of Rome sixteen miles away, a pressure of 5000 volts is used. At the great power station of Niagara the currents are distributed in the district at 2250 volts, but for transmission to Buffalo, 16 miles distant, the voltage is raised to 11,000. An American transmission system conveys energy at a

pressure of 150,000 volts from Big Creek to Los Angeles, California, 240 miles away. This system is three-phase and transmits 120,000 kilowatts.

The Thury System is a series transmission scheme using high voltage and a constant continuous current; for which the insulation need not be as good as for an alternating current system of the same voltage. In the Moutiers-Lyon transmission line an area of 300 square miles is supplied, the transmission lines being supported overhead. The voltage in use is 58,000 volts on a three-wire system (Art. 559) the earth being used as a middle wire. Motors and generators are all connected in series in this system, and when it is required to stop any machine the brushes are rocked round to their non-acting position and then the machine is short circuited; while the reverse operations are used for starting up.

553. High Voltage and Extra-high Voltage.— Supply systems may be classified according to whether they operate at a *low voltage* (or low pressure), *i.e.* from 100 volts (or under) to 300 volts; *high voltage*, *i.e.* from 300 to 3000 volts; or *extra high voltage*, over 3000 volts. High-voltage systems generally (but not necessarily) employ alternating currents, with *transformers* (Art. 538) to transform to low pressure suitable for use in the consumers' houses.

Example.— The Charing Cross Electric Supply Company generates, at its power station at Bow, alternating currents (three-phase) at 10,000 volts, which are supplied to various substations in London through extra-high pressure feeders placed underground. The substations contain motor-generators (Art. 544) and battery plant. The motor-generators convert the 10,000-volt alternating currents into 400-volt continuous currents, with a corresponding increase of amperes delivered. The 400-volt supply is connected across the outer mains (Art. 559) of a three-wire distributing system which supplies the customers at 200 volts for lighting or 400 volts for motor power.

LESSON XLIX.—*The Distribution of Power*

554. Power Stations.—Electrical energy on a large scale is usually generated at *Central Stations* or **Power-houses.** These buildings contain the prime movers :—steam-engines, steam-turbines, water-turbines, or gas engines, etc., and the generating plant :—dynamos or alternators. Steam-power stations are erected in convenient positions, where coal is easily accessible, generally near a plentiful supply of water for the condensing plant, etc., and should not be erected in the middle of towns.

The generating plant of a power station is in several distinct and complete sets (dynamo and prime mover complete). This is more economical than one large set as the number of sets in use will depend on the demand upon the power station, and so each set can be run at nearly full load, at which load most machines give their best efficiency.

Power stations also contain a switch-board for the central control of all the machines. A separate panel is used for each machine so that in the case of a breakdown of one machine it can be immediately isolated.

The Lot's Road Power Station (Fig. 328) contains eight 6000-kilowatt turbo-generators, which supply energy to most of the London underground electric railways.

A daily record of the performance of each set is made by recording instruments mounted upon the switch-board.

555. Feeders.—The distribution of electrical energy from the power-houses to the several convenient centres in the area supplied is accomplished by cables called *feeders.* The feeders are of sufficient cross-sectional area to convey, without undue heating, the maximum demand of current. Feeders generally connect the power-house to substations, and are laid underground in pipes, or supported on poles or structures above ground.

556. Substations.—The feeders generally convey

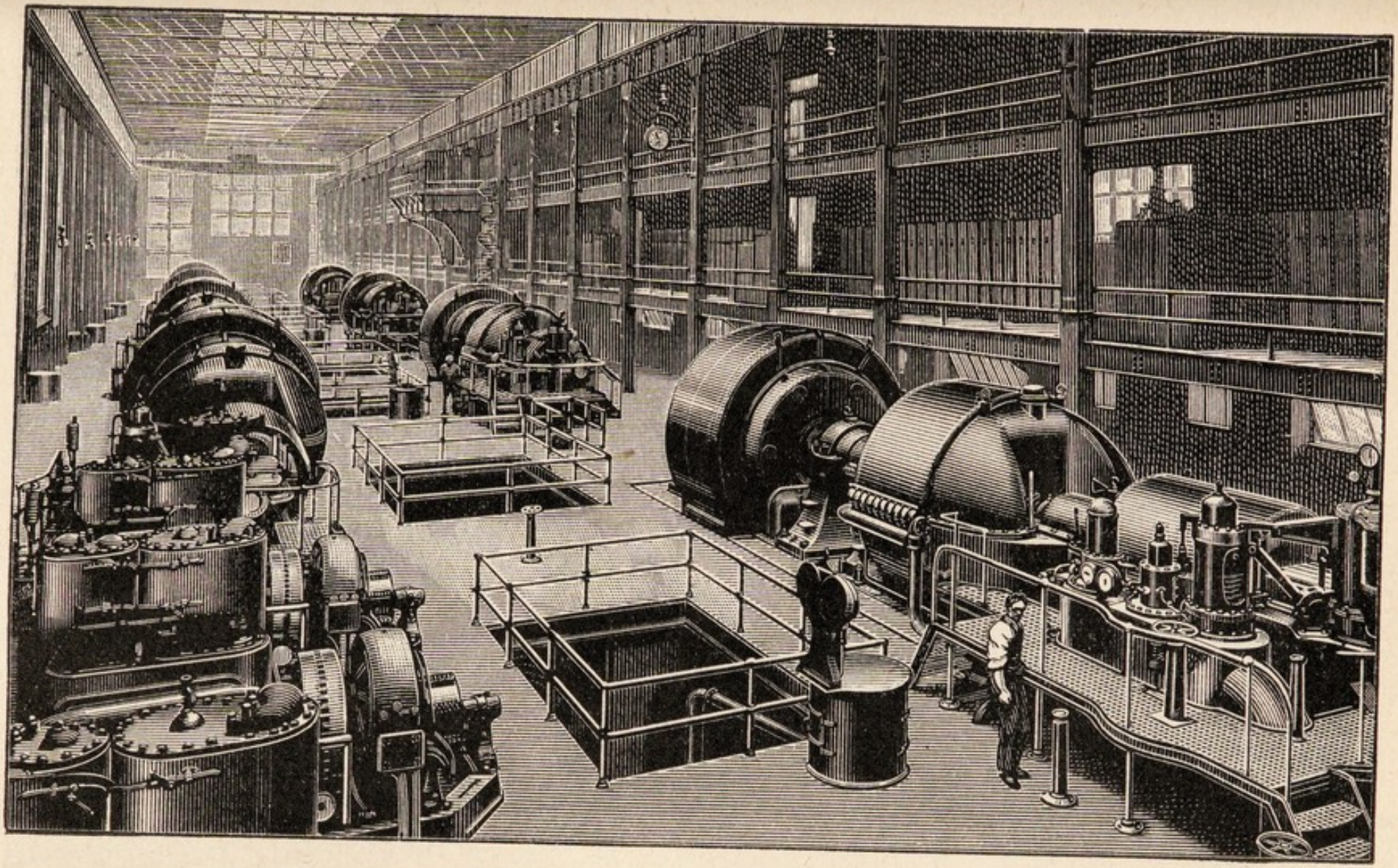


FIG. 328.—The Large Power Station with Turbo-alternators at Lot's Road, London.

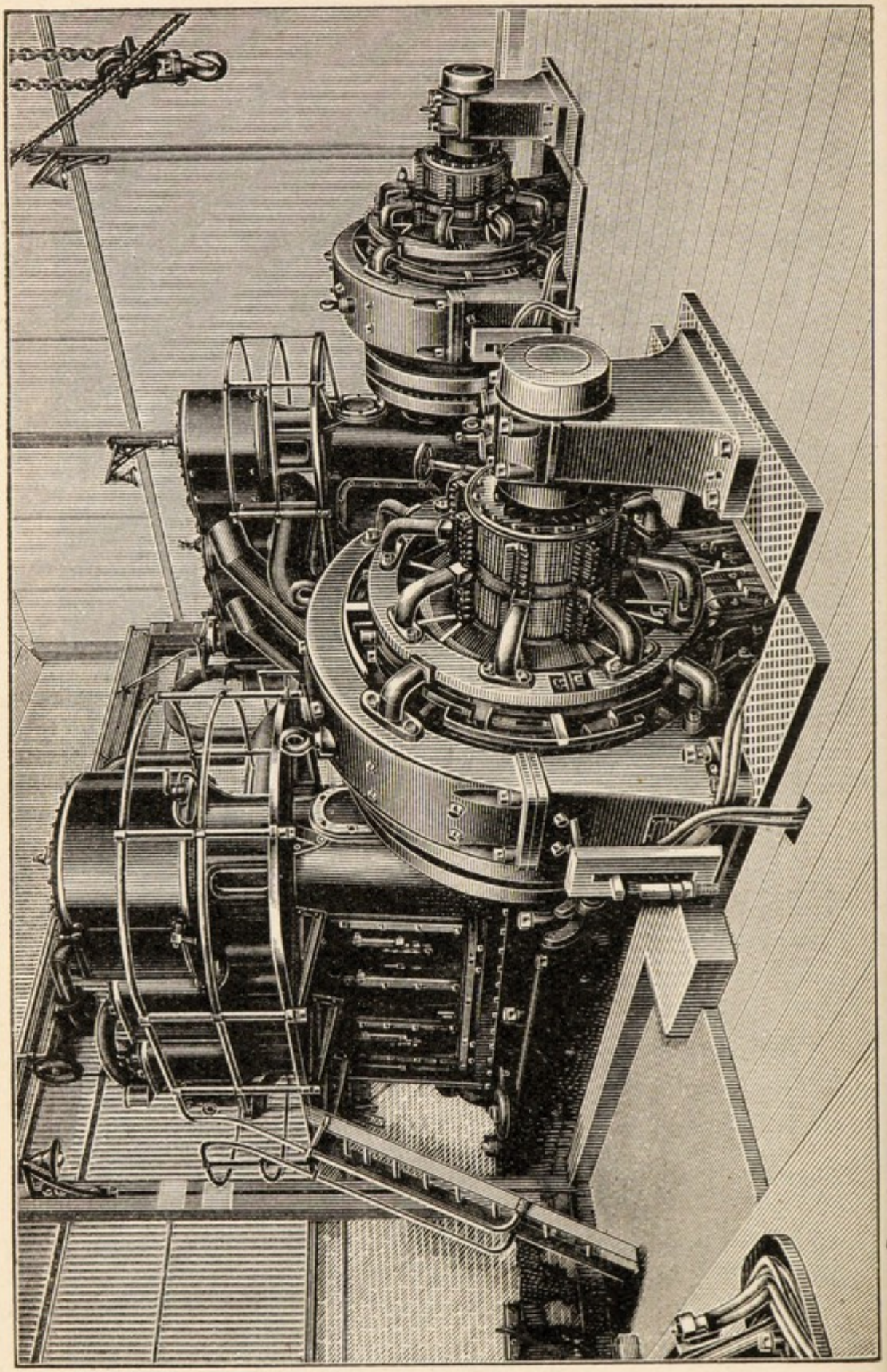


Fig. 296. A Small Power Station with Continuous-current Generators

current at a higher pressure, for economic reasons, than is suitable for conveyance to the consumers' premises. Substations therefore contain electrical plant for the conversion of the voltage into a suitable value. The conversion of continuous current voltage requires rotating machines called motor-generators (Art. 544), whereas alternating currents do not; stationary transformers (Art. 538) being used. To convert continuous current into alternating current or *vice versa*, rotatory converters (Art. 546) are used.

557. Distributors.—From the substations numerous cables connect them to the consumers' premises; these are called *distributors*. The distributors are composed of stranded conductors either copper or aluminium, covered with some insulating compound such as gutta-percha, treated paper, or bitumen, and are laid mostly in conduits underground.

558. Conditions of Electric Supply.—Electric energy is almost always supplied under one of two standard conditions, either—

(*a*) at *Constant Voltage*, or
(*b*) with *Constant Current*.

In the former case the circuit is branched, and the current is supplied (usually at 100 volts) to all the lamps or motors *in parallel*, Fig. 330, each lamp, etc., being independent of all others; and the current varying precisely in proportion to the demand.

The current in the mains subdivides and flows through each lamp independently. When any lamp is switched on it does not diminish the current in the others, but by acting as an additional path it simply causes more current to flow from the source of supply. The method of grouping

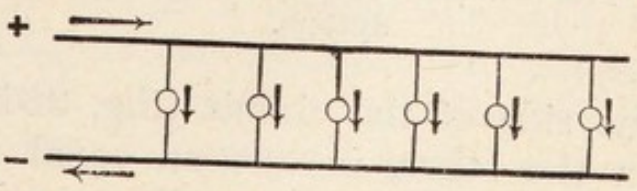


FIG. 330.—Distribution in Parallel.

in series (Art. 176) is seldom used for glow-lamps, since each lamp would then require an automatic cut-out to prevent the rest of the row from being extinguished in case one lamp went out.

In the latter case, seldom used except for long rows of arc-lamps, the circuit is undivided, and the current (usually 10 amperes) flows through all the lamps *in series*. If lamps are turned out (by short-circuiting them) the voltage must be reduced to keep the current constant.

Since the power of a current depends on the voltage at which it is supplied, the *unit of supply* recognized in law is based on the unit of power, the *watt* (Art. 454). The "unit" is defined as 1000 watts supplied for one hour (*i.e.* 1 kilowatt-hour) or its equivalent. The maximum price which the English Board of Trade permits the supply company to charge the consumer for 1 "unit" is eightpence. In London the average price charged by the supply authorities is about 2·15 pence per "unit."

559. Three-wire System.—*Three-wire* systems, in which a third or neutral wire is introduced between the + and the − main, have been devised to enable higher voltages to be used, and thereby enable twice as many lamps to be lit with little additional expenditure in copper. To render the lamps on one side of the circuit (Fig. 331) independent of those on the other, in case an equal number do not happen to be switched on at the same time, the middle wire (which only need be thick enough to carry a current equal to the difference between the currents in the two outer wires) is carried back to the station and kept at mean

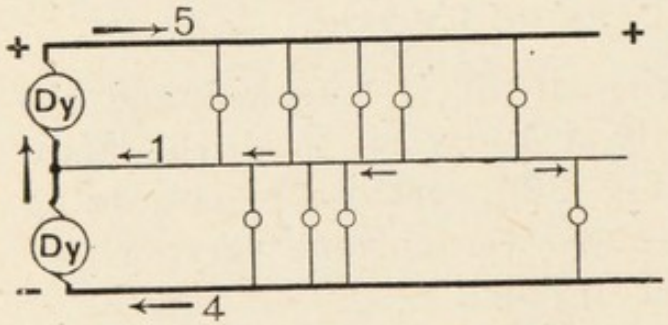


FIG. 331.—Distribution by Three-wire System.

potential between the two outer wires by the use of two dynamos instead of one.

560. Effect of Various Loads.—The load on an average power station may be divided into three chief parts; (i.) for motors, (ii.) lighting, (iii.) heating and miscellaneous requirements. The motor load begins about 7 A.M., when various works commence (see Fig. 332), and lasts throughout the day until about 8 P.M., but before the works leave off there is a demand for power for lighting which causes a peak load about 7 P.M. The time of the peak load varies with the season and weather conditions. Occasionally, due to storms, abnormal demands of power are made for lighting in the day-time and this with the motor and heating load is generally more than the normal full output of the station-machinery. For these periods a battery of accumulators (Art. 572) is usually employed to assist the generating plant in a storm load.

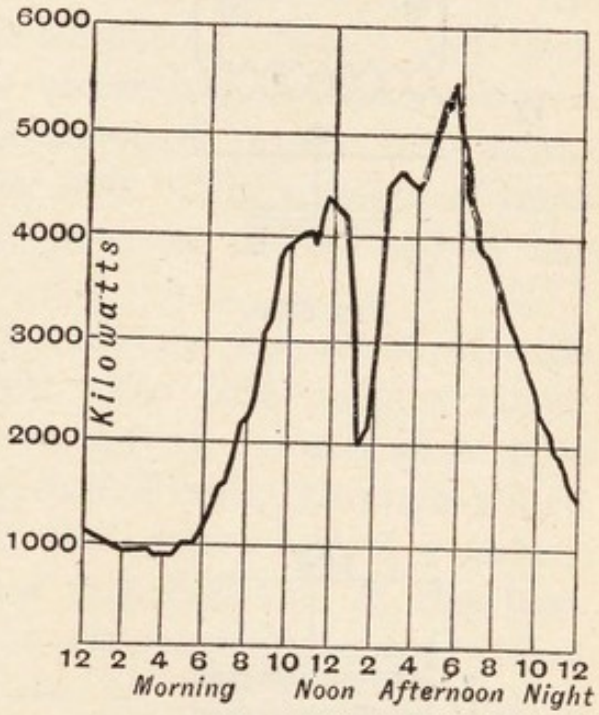


FIG. 332.—A Daily Load-curve.

The load on a generating set continually alters, and this causes a corresponding variation in the voltage, and as the variation must not exceed a certain amount it is necessary periodically to adjust the voltage. The adjustment can either be made by hand regulation which operates a resistance or by an automatic device such as the Tirrill regulator.

561. Protective Devices.—Many devices have been employed to protect overhead transmission lines, telegraph and telephone lines, from the disastrous effects resulting

from being struck by lightning. The oldest of these consist of serrated plates placed nearly in contact, Fig. 333*a*, providing an easy passage to earth for any sudden discharge that is able to jump the gap between the plates. To prevent arcs following the spark, in electric light or

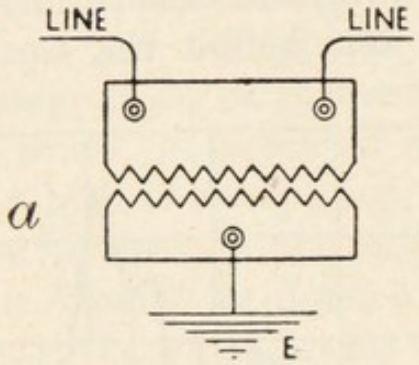


FIG. 333*a*.

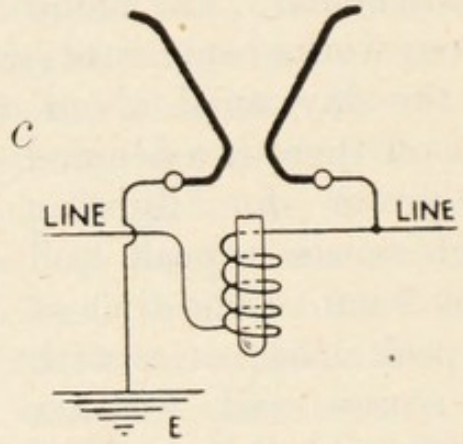


Fig. 333*c*.

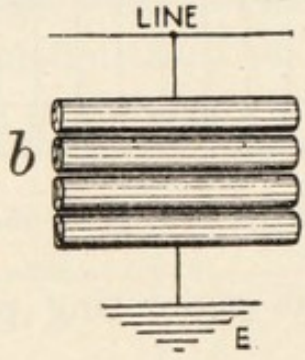


FIG. 333*b*.

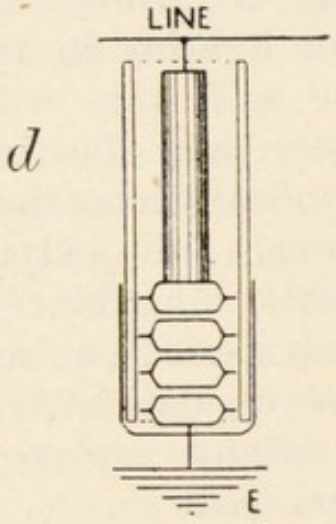


FIG. 333*d*.

Various Forms of Lightning-Arresters.

power lines, a number of zinc cylinders lying close to one another, forming a multiple spark-gap, Fig. 333*b*, are sometimes used. Another device is to give to the discharge surfaces the form of a pair of curved horns, as in Fig. 333*c*, so that any arc, following the discharge, in ascending the horns extends itself and goes out. This is sometimes combined with a copper wire coil, which

acts as an impedance in the line, and at the same time helps to blow out the discharge magnetically. A fourth device, Fig. 333*d*, consists of introducing a resistance rod of carborundum in series with a number of insulated metallic surfaces which act as a multiple spark-gap to quench the spark. *Electrolytic* arresters are also used. These consist of a number of cone-shaped trays of aluminium, on which is coated a film of aluminium hydroxide. These trays are placed together one in the other, but kept apart by insulating spacers and each tray filled with a suitable electrolyte. The resistance of the film of each tray is sufficient to prevent the breakdown of it by voltages below 300. The number of trays to be used will therefore depend on the voltage of the system.

It is also necessary to protect machines and circuits from accidental short-circuit. For this purpose either fuses or circuit-breakers are employed. *Fuses* (Art. 464) consist of specially isolated pieces of metal through which the current passes, so that if the current exceed a certain value, depending on the size and material of the fuse, it melts, thus breaking the circuit. *Circuit-breakers* are automatic contact devices in which the excessive current is made to act electromagnetically on a trip-gear and open the circuit. The trip works against a spring and thus, by adjustments to the strength of the spring, the breaker can be set to open the circuit at any prearranged limit of current. Circuit-breakers which have to operate with heavy currents are generally provided with auxiliary contacts of carbon so that the final break of the current occurs when the copper contacts have already parted. The arc which forms between the carbon contacts is blown out by an electromagnetic device similar to Fig. 333*c* above and thus no damage is done by the arc fusing the contacts.

CHAPTER XII

ELECTRIC TRACTION

LESSON L.—*Electric Tramways and Railways*

562. Electric Locomotion.—After the invention of electric motors many suggestions were made to propel vehicles by electricity, as by Davenport (1835), Davidson (1838), and Roloff (1868), but the great cost and trouble of primary batteries (Art. 176) prevented any success. Only when the dynamo was commercially introduced for generating electric current did electric locomotion become possible. The first practical suggestions for the electric propulsion of tram-cars came independently from Werner Siemens, Stephen Field, and T. A. Edison, in 1879. In 1883 the Portrush Railway in Ireland, in which current was supplied to the cars by means of a third rail, was opened for traffic. In 1888 Daft introduced the method of taking current from an overhead line by an under-running trolley-wheel on the end of an elevated pole; and in 1890 Siemens and Halske devised the under-running contact-bow for the same purpose. The great development of tramways with overhead conductors took place in the United States, beginning in the years 1888 to 1890. In 1890 also the first subterranean tube-railway, using third rail, the City & South London Railway, was opened. The extensive systems of tube-railways in London and Paris followed. There are now 85 miles of

underground railways in London alone. The application of electric propulsion to railway lines of full gauge and with heavy rolling stock, with the use of alternating currents was largely developed in Switzerland and North Italy from 1899 onwards; and in the United States, using continuous currents, at about the same epoch. The three main branches of the subject are the applications to (i.) Tramways, (ii.) Railways, (iii.) Automobiles.

563. Tramways.—There are several ways of conveying the electric current to the moving car:—

(*a*) Current (usually continuous current at 500 volts) is supplied from the power-house or from a substation to an overhead line, with which the car makes contact as it runs by means of a trolley-wheel (or a metal bow) fixed on a jointed pole above the car. The current passes down an insulated lead from the trolley-wheel, through the controller and the motors, to the car wheels and so to the rails, which serve as the return conductor; the rails being bonded together by copper bonds to ensure good conductance. In many cases there are also return feeders from the rails to the power-house (or substation).

(*b*) Current is picked up by the car from conductors laid in a slot-conduit in the road between the rails, by means of a contact-piece, or "plough" let down into the slot.

(*c*) Current is picked up by the car from metal studs slightly projecting from the road-surface between the rails, by means of a long skate fastened under the car; each stud being automatically connected to the underground mains as the car comes up, and disconnected as it passes on. This plan, though cheaper than (*b*), has dropped into disuse through practical difficulties.

For tram-car driving, two series-wound motors (Art. 521) are mounted on the truck of each car, and drive the wheels through a single-reduction gear. The amount of current taken from the line is regulated by moving the handle of a *controller*, a complicated kind of barrel switch, performing the following operations: (i.) at starting,

the controller switches on the current to the two motors in series, with additional resistance in circuit, so that each motor at starting gets less than half the voltage; (ii.) as speed increases, the controller cuts out the added resistance, in stages; (iii.) then puts the two motors in parallel, with resistance; (iv.) cuts out the resistance, in stages; (v.) at highest speed shunts part of the current from the magnet-windings so as to weaken the magnets (Art. 521). The controller also contains devices for reversing the direction of the rotation of the motors. Each motor is usually of 25 to 30 HP, and has four poles. The power required by the car running on the level is from 10 to 25 kilowatts; the current at starting being some 100 amperes (to give the initial starting effort), and from 2 to 5 amperes when running fast.

564. Railways.—For suburban traffic, where there is frequent starting and stopping, and rapid acceleration is essential, the motors must exert great initial torque. If separate electric locomotives are employed to draw a train of six, eight, or ten cars they must be from 600 HP to 1000 HP. But in most cases motor-coaches are provided having the motors under the floors of the cars, each motor-coach being able to propel itself and one or two trailer cars, the trains being made up of such units. In the Liverpool and Southport section of the Lancashire & Yorkshire Railway, motor-coaches are used having four motors of 150 HP each, each train consisting of 4 coaches in total. In most English suburban lines the current is picked up from a third rail. At the usual pressure of 500 to 600 volts (continuous current) the current needed by a 100 HP motor is from 200 to 250 amperes during the period of acceleration; but when a speed of 20 miles per hour has been reached, the current is greatly reduced. An electrically propelled train may attain this speed in the short period of 10 seconds. For long lines, where the traffic is carried on with ordinary cars or waggons, locomotives are a

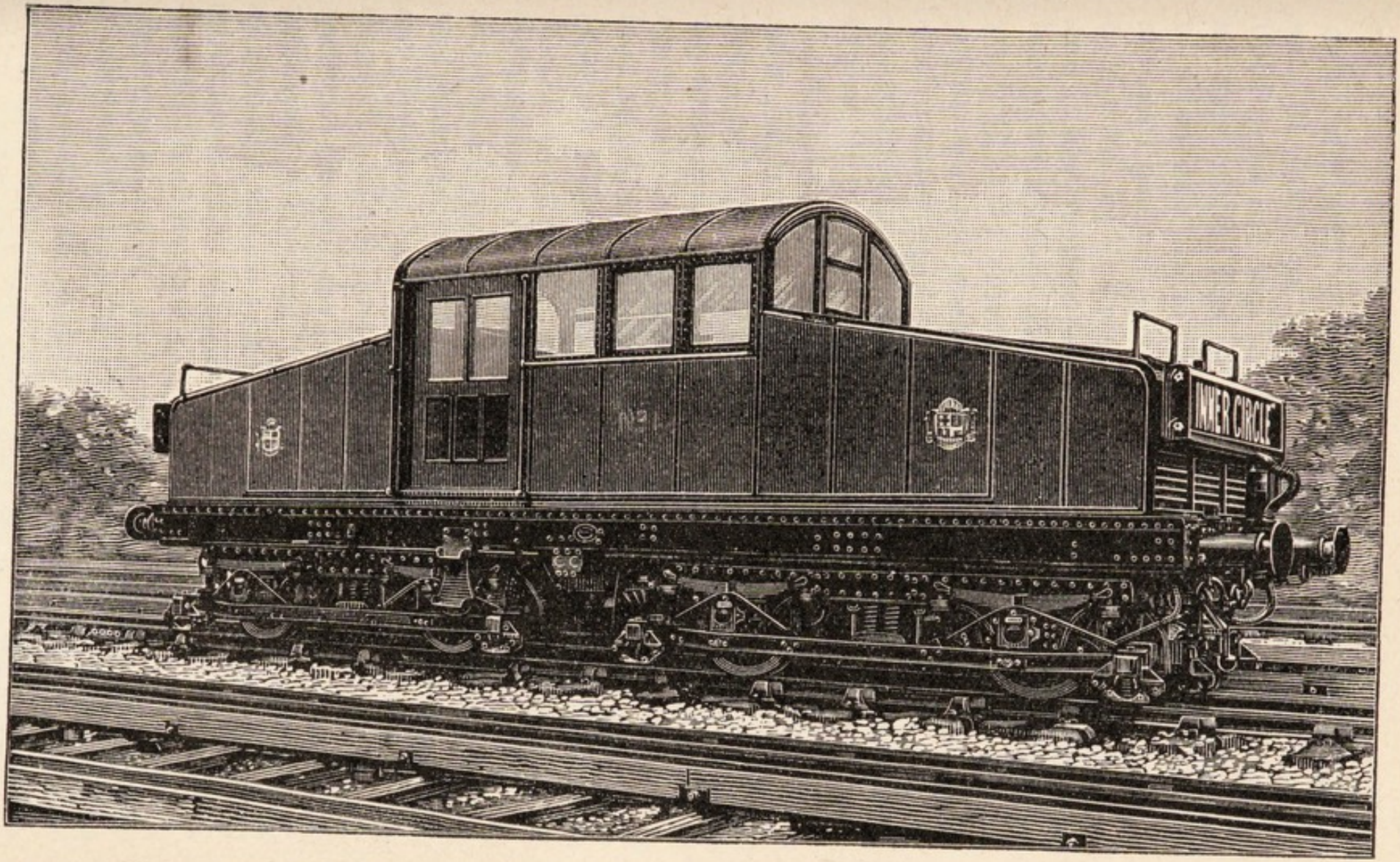


FIG. 334.—Electric Locomotive of the London Underground Service.

necessity. If the supply is at 600 to 750 volts, then for a locomotive actually working at 1000 HP, the amount of current taken will be not far from 1000 amperes; and at starting the amount taken may be double this to give the required effort. In order to diminish the cost of the feeding mains, for long lines, the current (usually alternating) is supplied at extra-high pressures, such as 6000 volts, to sub-stations where converters (Art. 546) are installed. In certain Swiss and Italian railroads three-phase currents (Art. 535) are employed throughout; whilst in other instances single-phase motors are preferred. In these high-pressure three-phase and single-phase lines overhead conductors are used. A modern electric locomotive of 2000 HP weighs from 80 to 100 tons, and is about 40 feet long; while a modern steam locomotive of 1500 HP weighs, with its tender, about 150 tons and is about 60 feet long; further the running cost of the electric locomotive per train-mile is distinctly lower than that of the steam locomotive. The electric locomotive (Fig. 334), as used on the Metropolitan Railway, London, weighs 46 tons, and has four motors of 250 HP each.

565. Electric Automobiles. — An automobile must necessarily carry a battery to drive the electric motors, and this battery must consist of accumulators that are systematically recharged. Lead cells (Art. 572) are heavy, and deteriorate under mechanical shocks. Edison's nickel-oxide accumulator (Art. 573) was designed expressly to be lighter and to withstand jars. For propelling delivery-cars, cabs, and light vehicles electric automobiles have great usefulness. For a daily run of 25 to 40 miles about town the energy consumption is about 0·48 kilowatt-hours (or "units") per mile per ton. For a total weight (vehicle and load) of 5 tons it is usual to provide a battery of 60 cells of accumulators, having a charge-limit of 27,000 ampere-hours. It is usual to fit the vehicle with a series-wound motor.

CHAPTER XIII

ELECTRO-CHEMISTRY

LESSON LI.—*Electrolysis*

566. Electromotive-force of Polarization.—The simple laws of definite chemical action due to the current having been laid down in Lesson XIX., it remains to consider the relations between the chemical energy and its electrical equivalent. Whenever an electrolyte is decomposed by a current, the resolved ions have a tendency to reunite, that tendency being commonly termed "chemical affinity." Thus when zinc sulphate ($ZnSO_4$) is split up into Zn and SO_4 the zinc tends to dissolve again into the solution, and so spend the potential energy of the system. But zinc dissolving into sulphuric acid sets up an electromotive-force of definite amount; and to tear the zinc away from the sulphuric acid requires an electromotive-force at least as great as this, and in an opposite direction to it. So, again, when acidulated water is decomposed in a voltameter, the separated hydrogen and oxygen tend to reunite and set up an opposing electromotive-force of no less than 1·47 volts. This opposing electromotive-force, which is in fact the measure of their "chemical affinity," is termed the electromotive-force of polarization. It can be observed in any water voltameter (Art. 259) by simply disconnecting the wires from the battery and joining them to a galvanometer, when a

current will be observed flowing back through the voltameter from the hydrogen electrode towards the oxygen electrode. The polarization in a voltaic cell (Art. 183) produces an opposing electromotive-force in a perfectly similar way.

Now, since the affinity of hydrogen for oxygen is represented by an electromotive-force of 1·49 volts, it is clear that no cell or battery can decompose water at ordinary temperatures unless it has an electromotive-force of *at least* 1·49 volts. With every electrolyte there is a similar minimum electromotive-force necessary to produce complete continuous decomposition.

567. Electrochemical Energy. — Suppose a current to convey a quantity of electricity Q through a circuit in which there is an opposing electromotive-force E: the work W done in moving Q units of electricity against this electromotive-force will be equal to $E \times Q$. If E and Q are expressed in "absolute" C.G.S. units, $E \times Q$ will be in *ergs*. If E is in *volts* and Q is in *coulombs*, the product will be the work in *joules*. The total energy of the current, as available for producing heat or mechanical motion, will be diminished by this quantity, which represents the work done against the electromotive-force in question.

But we can arrive in another way at an expression for this same quantity of work. The quantity of electricity in passing through the cell will deposit a certain amount of metal: this amount of metal could be burned, or dissolved again in acid, giving up its potential energy as heat, and, the mechanical equivalent of heat being known, the equivalent quantity of work can be calculated. Q units of electricity will cause the deposition of Qz grammes of an ion whose absolute electrochemical equivalent is z. [For example, z for hydrogen is 0·0001044 gramme, being ten times the amount (see Table in Art. 256) deposited by one coulomb, for the coulomb is $\frac{1}{10}$ of the absolute C.G.S. unit of quantity.] If H represents the

number of heat units evolved by one gramme of the substance, when it enters into the combination in question, then QzH represents the value (in heat units) of the chemical work done by the flow of the Q units; and this value can immediately be translated into *ergs* of work by multiplying by Joule's equivalent J ($=42\times10^6$). [See Table on page 241.]

We have therefore the following equality:

$EQ = QzHJ$; whence it follows that

$E = zHJ$; or, in words, *the electromotive-force of any chemical reaction is equal to the product of the electro-chemical equivalent of the separated ion into its heat of combination, expressed in dynamical units.*

Examples.[1]—(1) *Electromotive-force of* **Hydrogen** *tending to unite with Oxygen.* For Hydrogen $z = 0{\cdot}0001044$; H (heat of combination of one gramme) = 34000 gramme-degree-units; $J = 42\times10^6$.

$0{\cdot}0001044\times34000\times42\times10^6 = 1{\cdot}49\times10^8$ "absolute" units of electromotive-force, or $= 1{\cdot}49$ *volts.*

(2) *Electromotive-force of* **Zinc** *dissolving into Sulphuric Acid.* $z = 0{\cdot}00339$; H = 1670 (according to Julius Thomsen); $J = 42\times10^6$.

$0{\cdot}00339\times1670\times42\times10^6 = 2{\cdot}377\times10^8$.
or $= 2{\cdot}377$ *volts.*

(3) *Electromotive-force of* **Copper** *dissolving into Sulphuric Acid.* $z = 0{\cdot}00329$; H = 909·5; $J = 42\times10^6$.

$0{\cdot}00329\times909{\cdot}5\times42\times10^6 = 1{\cdot}256\times10^8$,
or $= 1{\cdot}256$ *volts.*

(4) *Electromotive-force of a* **Daniell's Cell.** Here zinc is dissolved at one pole to form zinc sulphate, the chemical action setting up a + electromotive-force, while at the

[1] The figures given in these examples as well as those on p. 591 for the heat of combination must be taken as only approximate. The heat of combination is different at different temperatures, and the heat evolved by the salt dissolving in water must also be taken into account. In fact von Helmholtz showed that the expression zHJ is incomplete, and that to it should be added a term $\theta\cdot dE/d\theta$ wherein θ is the absolute temperature of the cell.

other pole copper is deposited by the current out of a solution of copper sulphate, thereby setting up an opposing (or −) electromotive-force. That due to zinc is shown above to be + 2·377 *volts*, that to deposited copper to be − 1·256. Hence the nett electromotive-force of the cell is (neglecting the slight electromotive-force where the two solutions touch) 2·377 − 1·256 = 1·121 *volts*. This is nearly what is found (Art. 196) in practice to be the case. It is less than will suffice to electrolyse water, though two Daniell's cells in series electrolyse water easily.

Since 1 horse-power-hour = 746 watt-hours = 746 ampere-hours at 1 volt, it follows that at V volts the number of ampere-hours will = 746 ÷ V. Now as the weight of zinc consumed in a cell is 1·219 grammes per ampere-hour (when there is no waste), and as 1 lb. equals 453·6 grammes, the consumption will be as follows:

$$\left.\begin{matrix}\text{Weight of zinc used}\\ \text{per horse-power-hour}\end{matrix}\right\} = \frac{746}{V} \times 1{\cdot}219 \text{ grm.} = \frac{2}{V} \text{ lbs.}$$

Hence the quantity of zinc that must be consumed to generate 1 horse-power-hour in any battery of cells cannot be less than 2 lbs. ÷ the available volts of a single cell of the battery; and zinc costs about 8 pence per pound.

Example.—If a new cell can be invented to give 2 volts at its terminals when in full work, a battery of such cells, however arranged, will consume 1 lb. of zinc per hour per horse-power, or 1·34 lbs. per "unit" (or kilowatt-hour) of supply.

An equivalent quantity of exciting and depolarizing chemicals will also be used, and these will increase the total cost per unit. It is clear that as a source of public supply primary batteries consuming zinc can never compete in price with dynamos driven by steam. The actual cost of coal to central stations in London is about 0·3 pence per "unit"; and the maximum legal price that a supply company may charge in Great Britain for electric energy is eightpence per "unit." See Art. 558.

568. Electrochemical Power of Metals.—The accompanying Table gives the electromotive-force of the

different metals as calculated (Art. 567) from the heat evolved by the combination with oxygen of a portion of the metal, equivalent electrochemically in amount to one gramme of hydrogen. The figures in the second column are in calories. The figures in the third column are calculated from those in the second by multiplying by the electrochemical equivalent of hydrogen, and by Joule's equivalent (42×10^6) and dividing by 10^8, to reduce to volts. The electromotive-forces as observed (in dilute sulphuric acid) are added for comparison.

Substance.	Heat of Oxidation of Equivalent.	E.M.F. calculated.		E.M.F. observed.
		Relatively to Oxygen.	Relatively to Zinc.	
Potassium . .	69,800	3·01	+1·18	+1·13
Sodium . . .	67,800	2·91	+1·09	
Zinc	42,700	1·83	0	0
Iron	34,120	1·55	−0·28	
Hydrogen . . .	34,000	1·47	−0·36	
Lead	25,100	1·12	−0·71	−0·54
Copper . . .	18,760	0·80	−1·03	−1·047
Silver	9,000	0·39	−1·44	
Platinum . . .	7,500	0·33	−1·50	−1·53
Carbon . . .	2,000	0·09	−1·74	
Oxygen . . .	0	0	−1·83	−1·85
(Nitric Acid) . .	− 6,000	−0·26	−2·09	−1·94
(Black Oxide of Manganese) .	− 6,500	−0·29	−2·12	−2·23
(Peroxide of Lead)	−12,150	−0·52	−2·35	−2·52
(Ozone) . . .	−14,800	−0·63	−2·46	−2·64
(Permanganic Acid) . . .	−25,070	−1·09	−2·92	−3·03

The order in which these metals are arranged is in fact nothing else than the order of oxidizability of the metals (in the presence of dilute sulphuric acid); for that metal tends most to oxidize which can, by oxidizing, give out the most energy. It also shows the order in which the metals stand in their power to replace one another (in a solution containing sulphuric acid). In this order,

too, the lowest on the list first, are the metals deposited by an electric current from solutions containing two or more of them: for that metal comes down first which requires the least expenditure of energy to separate it from the elements with which it was combined.

569. General Laws of Electrolytic Action.—In addition to Faraday's quantitative laws given in Art. 256, the following are important:

(*a*) Every electrolyte is decomposed into two portions, an anion and a kation, which may be themselves either simple or compound. In the case of simple binary compounds, such as fused salt (NaCl), the ions are simple elements. In other cases the products are often complicated by secondary actions. It is even possible to deposit an alloy of two metals—*brass* for example—from a mixture of the cyanides of zinc and of copper.

(*b*) In binary compounds and most metallic solutions, the metal is deposited by the current where it leaves the cell, at the kathode.

(*c*) Aqueous solutions of salts of the metals of the alkalies and alkaline earths deposit no metal, but evolve hydrogen owing to secondary action of the metal upon the water. From *strong* solutions of caustic potash and soda Davy succeeded in obtaining metallic sodium and potassium, which were before unknown. If electrodes of mercury are employed, an amalgam of either of these metals is readily obtained at the kathode. The so-called *ammonium*-amalgam is obtained by electrolysing a warm, strong solution of sal-ammoniac between mercury electrodes.

(*d*) Metals can be arranged in a definite series according to their electrolytic behaviour; each metal on the list behaving as a kation (or being "electropositive") when electrolysed from its compound, in preference to one lower down on the list. In such a series the oxidizable metals, potassium, sodium, zinc, etc., come last; the less oxidizable or "electronegative" metals preceding

them. The order varies with the nature, strength, and temperature of the solution used.

(*e*) From a solution of mixed metallic salts the least electropositive metal is not deposited first, if the current is so strong relatively to the size of the kathode as to impoverish the solution in its neighbourhood. To deposit alloys a solution must be found in which both metals tend to dissolve with equal electromotive-forces.

(*f*) The liberated ions appear only at the electrodes.

(*g*) For each electrolyte a *minimum electromotive-force* is requisite, without which complete electrolysis cannot be effected. (See Art. 570.)

(*h*) If the current be of less electromotive-force than the requisite minimum, electrolysis may begin, and a feeble current may flow at first, but no ions will be liberated, the current being completely stopped as soon as the opposing electromotive-force of polarization has risen to equality with that of the electrolysing current.

(*i*) There is no opposing electromotive-force of polarization when electrolysis is effected from a dissolving anode of the same metal that is being deposited at the kathode. The feeblest cell will suffice to deposit copper from sulphate of copper if the anode be a copper plate.

(*j*) Where the ions are gases, pressure affects the conditions but slightly. Under 300 atmospheres acidulated water is still electrolysed; but in certain cases a layer of acid so dense as not to conduct collects at the anode and stops the current.

(*k*) The chemical work done by a current in an electrolytic cell is proportional to the *minimum* electromotive-force of polarization.

(*l*) Although the electromotive-force of polarization may exceed this minimum, the work done by the current in overcoming this surplus electromotive-force will not appear as chemical work, for no more of the ion will be liberated; but it will appear as an additional quantity of heat (or "local heat") developed in the electrolytic cell.

(*m*) Experiments show that the resistance of a given column of a given electrolyte is a constant, no matter whether larger or smaller currents are used in testing the resistance.

(*n*) Amongst the secondary actions which may occur the following are the chief:—

(1) The ions may themselves decompose; as SO_4 into $SO_3 + O$. (2) The ions may react on the electrodes; as when acidulated water is electrolysed between zinc electrodes, no oxygen being liberated, owing to the affinity of zinc for oxygen. (3) The ions may be liberated in an abnormal state. Thus oxygen is frequently liberated in its allotropic form as ozone, particularly when permanganates are electrolysed. The "nascent" hydrogen liberated by the electrolysis of dilute acid has peculiarly active chemical properties. So also the metals are sometimes deposited abnormally: copper in a black pulverulent film; antimony (from the terchloride solution) in roundish gray masses which possess a curious explosive property. When a solution of lead is electrolysed a film of peroxide of lead forms *upon the anode*. If this be a plate of polished metal placed horizontally in the liquid beneath a platinum point as a kathode, the deposit takes place in symmetrical rings of varying thickness, the thickest deposit being at the centre. These rings, known as Nobili's rings, exhibit all the tints of the rainbow, owing to interference of the waves of light occurring in the film. The colours form, in fact, in reversed order, the "colours of thin plates" of Newton's rings. (4) In certain cases the deposit may be of a non-conducting nature; as for example, where aluminium is the anode in an alkaline solution, and an oxide of aluminium is formed as a film which entirely stops the current. Hence if a cell is arranged with a small plate of aluminium and a large plate of lead, dipping into a solution of carbonate of soda or of ammonium phosphate, a current can flow through it from lead to aluminium, but not from aluminium to lead. Such a cell, called *Nodon's valve*, conducts in one direction only, and can be used to rectify an alternating current.

570. Hypotheses of Grotthuss and of Clausius.—A complete theory of electrolysis must explain—*first*, the transfer of electricity, and *secondly*, the transfer of matter, through the liquid of the cell. The latter point is the one to which most attention has been given, since the "migration of the ions" (*i.e.* their trans-

fer through the liquid) in two opposite directions, and their appearance, in free condition, at the electrodes *only*, are salient facts.

The hypothesis put forward in 1805 by Grotthuss serves fairly, when stated in accordance with modern terms, to explain these facts. Grotthuss supposes that, when two metal plates at different potentials are placed in a cell, the first effect produced in the liquid is that the molecules of the liquid arrange themselves in in-

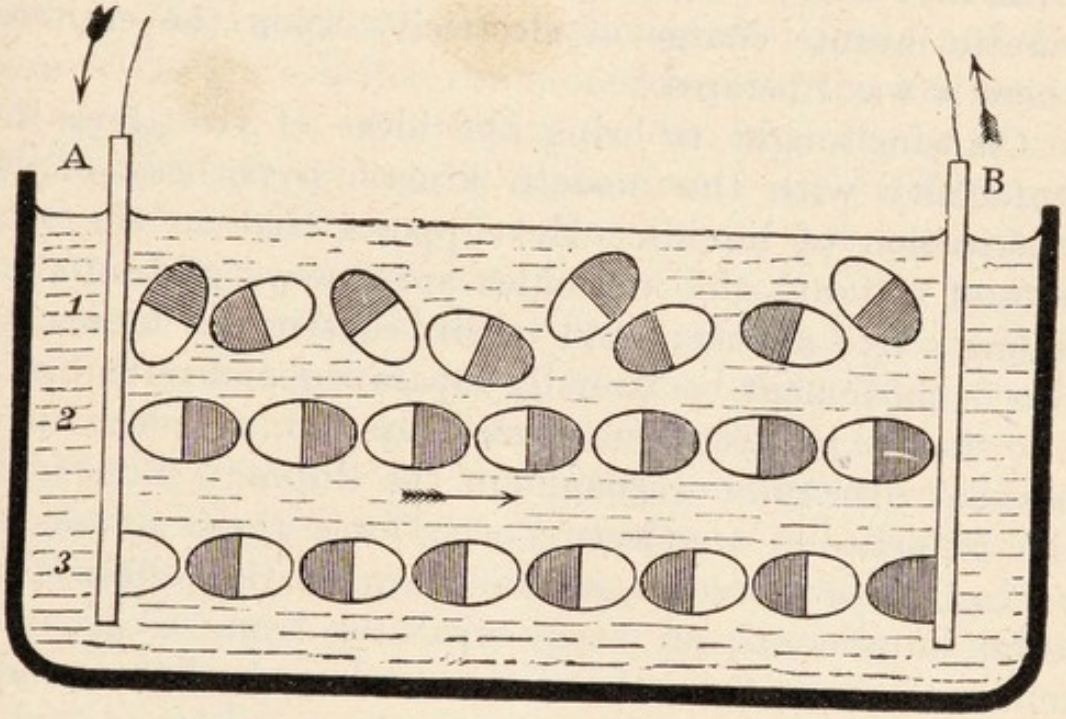


FIG. 335.—Grotthuss's Hypothesis of Electrolytic Action.

numerable chains, in which every molecule has its constituent atoms pointing in a certain direction; the atom of electropositive substance being attracted toward the kathode, and the fellow atom of electronegative substance being attracted toward the anode. (This assumes that the constituent atoms grouped in the molecule retain their individual electric properties.) The diagram of Fig. 335 shows, in the case of hydrochloric acid, a first row of molecules distributed at random, and secondly grouped in a chain as described. The action which Grotthuss then supposes to take place is that an

interchange of partners goes on between the separate atoms all along the line, each H atom uniting with the Cl atom belonging to the neighbouring molecule, a + half molecule of hydrogen being liberated at the kathode, and a − half molecule of chlorine at the anode. This action would leave the molecules as in the third row, and would, when repeated, result in a double migration of hydrogen atoms in one direction and of chlorine atoms on the other; the free atoms appearing only at the electrodes, and every atom so liberated discharging a certain definite minute charge of electricity upon the electrode where it was liberated.[1]

Clausius sought to bring the ideas of Grotthuss into conformity with the modern kinetic hypothesis of the constitution of liquids. He supposes that in the usual state of a liquid the molecules are always gliding about amongst one another, and their constituent atoms are also in movement, continually separating and recombining into similar groups, their movements taking place in all possible directions throughout the liquid. But under the influence of an electromotive-force these actions are controlled *in direction*, so that when, in the course of the usual movements, an atom separates from a group it tends to move either toward the anode or kathode; and if the electromotive-force in question be powerful enough to prevent recombination, these atoms will be permanently separated, and will accumulate around the electrodes. This theory has the advantage of accounting for a fact easily observed, that an electromotive-force *less* than the

[1] Johnstone Stoney reckoned, from considerations founded on the size of atoms (as calculated by Loschmidt and Lord Kelvin), that for every chemical bond ruptured, a charge of 1×10^{-19} of a *coulomb* is transferred. [E. Budde says $1{\cdot}7\times10^{-19}$ coulomb.] This quantity would appear to be the natural atomic charge or *electron* (see Art. 630). To tear one atom of hydrogen from a hydrogen compound this amount of electricity must be sent through it. To liberate an atom of zinc, or any other divalent metal from its compound, implies the transfer of twice this amount of electricity. See Art. 256, page 240.

minimum which is needed to effect complete electrolysis may send a feeble current through an electrolyte for a limited time, until the opposing electromotive-force has reached an equal value. Von Helmholtz, who gave the name of *electrolytic convexion* to this phenomenon of partial electrolysis, assumed that it takes place by the agency of uncombined atoms previously existing in the liquid. Arrhenius, in 1884, made the further suggestion that in every dilute solution of any acid or salt, the great majority of the molecules so dissolved are "ionized," that is, split up into their respective free ions; and the more dilute the solution the more complete the ionization. All conduction in electrolytes is due exclusively to the carrying of electricity by these free ions. Kohlrausch found that specially purified water does not conduct at all: it contains no free ions. But if as little as half of 1 per cent of hydrochloric acid or of sulphuric acid is added, it conducts well, for at that dilution 99 per cent of the acid molecules are ionized and act as carriers.

571. Migration of the Ions.—So far as explained it might be supposed that the migration of the constituents along the molecular chains during electrolysis was merely a continually repeated exchange of partners between the two sets of ions, the anions and kations travelling thus at equal rates, in opposite directions, toward the anode and kathode respectively. There are, however, some additional facts to be observed by experiment which indicate that the anions and kations travel at different rates, and that each ion has, under given circumstances, its own specific rate of migrating. Hittorf, who first drew attention to these facts, tabulated the observed ionic velocities. Since then Kohlrausch, Arrhenius, Ostwald and others have shown that this property is intimately connected with the conductivity of the electrolyte, and with the phenomena of solubility, of osmotic pressure, and of vapour-pressure. In fact, a whole new chapter of electro-chemistry has thus been opened out.

The fundamental experiment upon which is based the modern conception of the velocity of migration of the ions is an exceedingly simple one. Let a simple glass tube about a foot long and one inch in internal diameter be provided with well-fitting corks at its two ends, as in Fig. 336. In this is placed a nearly concentrated and slightly acidified solution of copper sulphate to be electrolysed. Through the corks pass two stout copper wires each furnished at the end with a round disk of sheet-copper, perforated with holes to permit of circulation of liquid. The upper one *k*, which serves as kathode, is just immersed below the surface of the liquid ; the other *a*, which is the anode, is placed two or three inches lower down in the liquid. The current from a few cells of battery is then sent *upwards* through the electrolyte, the current being so regulated that it is not too strong, otherwise bubbles of gas will be given off and disturb the experiment. Copper will, of course, be plated upon the upper or kathode plate, an equal amount of copper being dissolved off the lower or anode plate. After half an hour or so it will be seen that, immediately under the kathode, the blue liquid has become quite colourless, and if the experiment is continued, the surface of separation between the colourless liquid at the top and the blue liquid below it will be found to have moved steadily downward. (If the current is

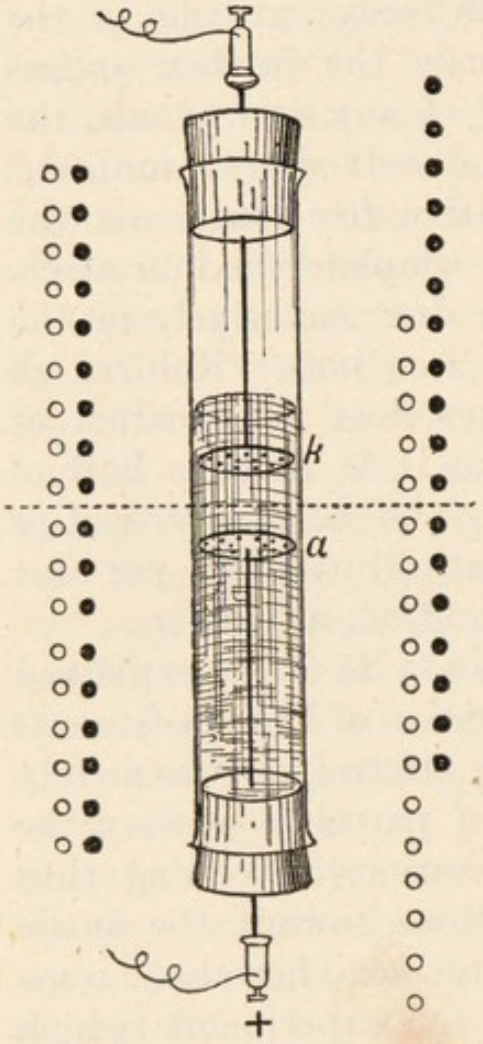


FIG. 336.—Experiment on Migration of Ions.

sent *downwards* no such phenomenon can be seen, owing to the descent by gravity of the heavier blue liquid.) The colourless liquid is simply water slightly acidulated. There are two ways of explaining that which has occurred. One is that, in some way, in addition to the ordinary electrolysis in which the ions Cu and SO_4 have been transferred in opposite directions, there has been a bodily transfer toward the anode of the $CuSO_4$ which was in solution. The other mode of explanation is that the ions Cu and SO_4 have travelled with different velocities; the Cu travelling upward more slowly than the SO_4 downward. In the diagrams to the left and right of the apparatus in Fig. 336 are shown some rows of dots for the purpose of illustrating the relative numbers of the ions in the upper and lower parts of the liquid. The black dots show the kations (Cu), and the white ones the anions (SO_4). Before electrolysis begins the solution is uniform, as shown on the left; there being 9 anions and 9 kations (that is 9 of $CuSO_4$) in each part, upper and lower. Suppose that electrolysis has gone on for so long a time that 6 of the kations have been dissociated and plated on the upper disk, and that 6 of the anions have been likewise liberated and carried down to the anode, there to combine with fresh copper. Now, if the observed state of things is represented by the diagram on the right, it will be seen that while in the upper layer there are 5 $CuSO_4$ molecules, in the lower there are 7 $CuSO_4$ molecules, together with the 6 SO_4 which have gone to dissolve fresh copper. If the migrations of anions and kations had been equal there would have been 6 $CuSO_4$ in each layer. If the anions alone had migrated, downwards, there would have been 15 $CuSO_4$ below and 3 $CuSO_4$ above. If the kations alone had moved, upwards, there would have been 9 $CuSO_4$ in the upper layer, leaving 3 of the original $CuSO_4$ in the lower, together with the newly-formed 6 $CuSO_4$. If, however, the diagram on the right represents the facts, either

2 $CuSO_4$ must have been bodily transferred into the lower layer from the upper, or else the transfer of ions must have been unequal, 4 anions going downwards into the lower layer, while 2 kations have gone upward into the upper layer. In other words, $\frac{2}{6}$ or 0·33 of the total displacement has been that of the copper ions, while $\frac{4}{6}$ or 0·66 has been that of the SO_4 ions. These numbers Hittorf called the *migration constants*: they state the *relative velocities* with which the ions migrate. The numbers vary with the concentration of the solution. Thus, in the case of copper sulphate, if the solution contains 2 gramme-equivalents per litre the migration constant for the anion is about 0·725, while if it contain only $\frac{1}{25}$ as much per litre the constant falls to 0·638. If this number for the anion be called n, then that of the kation will obviously be $1 - n$. If we denote by u and v the actual velocities with which the kations and anions respectively travel under a potential gradient of 1 volt per centimetre of length of the electrolyte, we clearly may write the equation

$$\frac{u}{v} = \frac{1-n}{n}.$$

Further the relative velocity of the ions past one another will be $u + v$. If by using a stronger battery we cause a greater fall of potential than 1 volt per centimetre, the actual velocities will be proportionally greater, but the ratio of u to v will remain as before. The actual velocities u and v Kohlrausch deduced from the specific conductivities of the liquids. For if 0·00001044 grammes be the electro-chemical equivalent of hydrogen, and if there be N gramme-equivalents of the dissolved electrolyte in one cubic centimetre of the solution, then $N \div 0{\cdot}00001044$ will be the number of *coulombs* of electricity concerned in electrolysing this amount of the solution; and if the ions are dragged past one another with a speed of $u + v$ (centimetres per second) the flow of electricity in one second across unit area will

be $(u+v)\mathrm{N} \div 0{\cdot}00001044$ *amperes*. Now if the fall of potential across a length of x centimetres be called V, the potential gradient being therefore $\mathrm{V} \div x$, the current will be equal to this multiplied by the specific conductivity k; and equating these we have—

$$u+v=0{\cdot}00001044\,\frac{k}{\mathrm{N}}\cdot\frac{\mathrm{V}}{x};$$

or for a potential gradient of 1 volt ($=10^8$ C.G.S.) per centimetre—

$$u+v=1044\,\frac{k}{\mathrm{N}};$$

or finally—

$$u+v=1044000\,\frac{k}{n},$$

where n is the number of gramme-equivalents per litre. Kohlrausch determined the values of the molecular conductivity $k \div n$ for many solutions. He found it to increase with dilution; becoming constant for each salt at very extreme dilutions. He also found that the values of this velocity came out the same for the same ion when used in different chemical combinations. Thus for hydrogen at 18° C, and under a gradient of 1 volt per centimetre, the ionic velocity is 0·00323 centimetres per second; that of sodium 0·00045; that of silver 0·00058.

Lesson LII.—*Accumulators*

572. Accumulators or Secondary Batteries.—A voltameter, or series of voltameters, whose electrodes are charged respectively with hydrogen and oxygen, will serve as *secondary batteries*, in which the energy of a current may be stored up and again given out. Ritter, who in 1803 constructed a secondary pile, used electrodes of platinum. It will be seen that such cells do not accumulate or store electricity; what they accumulate is energy, which they store in the form of chemical work. A secondary cell resembles a Leyden jar in that it can

be charged and then discharged. The residual charges of Leyden jars, though small in quantity and transient in their discharge, yet exactly resemble the polarization-charges of voltameters. Varley found 1 sq. centim. of platinum foil in dilute acid to act as a condenser of about 63 microfarads' capacity, when polarized to a potential-difference of 1 volt. Gaston Planté, in 1860, devised a secondary cell consisting of two pieces of sheet lead rolled up (without actual contact) as electrodes, dipping into dilute sulphuric acid, as in Fig. 337. To "form" or prepare the lead it was charged with currents which after a time were reversed in direction, and after a further time again reversed, until, after several reversals, it became coated with a semi-porous film of brown dioxide of lead on the anode plate; the kathode plate assuming a spongy metallic state presenting a large amount of surface of high chemical activity. When such a secondary battery, or *accumulator*, is charged by connecting it with a dynamo (shunt-wound), or other powerful generator of currents, the anode plate becomes peroxidized, while the kathode plate is deoxidized by the hydrogen that is liberated. The plates may remain for many days in this condition, and will furnish a current until the two lead surfaces are reduced to a chemically inactive state. The electromotive-force of such cells is from 2·0 to 1·85 volts during discharge. Planté ingeniously arranged batteries

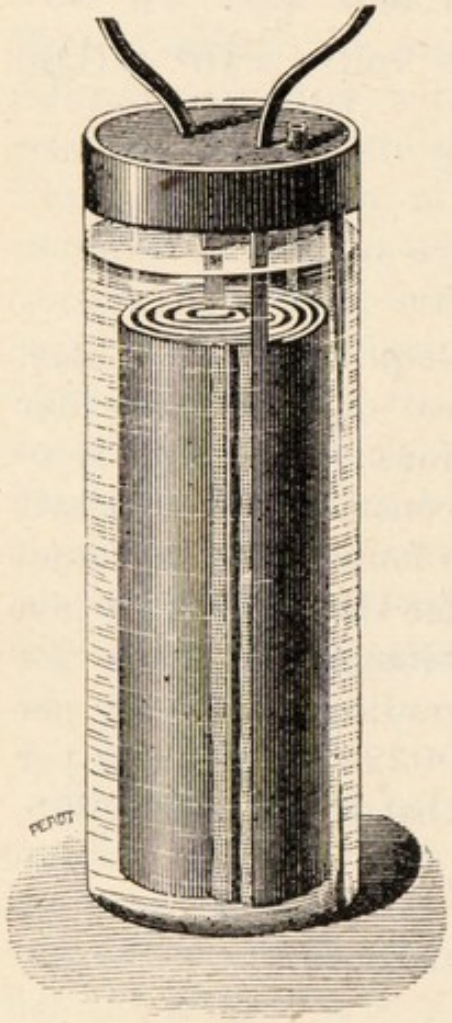


FIG. 337.—Planté's Accumulator.

of such cells so that they can be charged in parallel, and discharged in series, giving (for a short time) strong currents at extremely high voltages. Faure, in 1881, modified the Planté accumulator by giving the two lead plates a preliminary coating of *red-lead* (minium). When a current is passed through the cell to charge it, the red-lead is peroxidized at the anode, and reduced—first to a condition of lower oxide, then to the spongy metallic state—at the kathode, and thus a greater thickness of the working substance is provided, and takes far less time to "form" than is the case with Planté's cells. In modern accumulators the red-lead (or litharge), freshly mixed with dilute sulphuric acid to the form of a paste, is pressed into the holes of a leaden grid, shaped so as to give it a good mechanical attachment. During the subsequent process of "formation" the hardened paste is reduced on one plate (the "negative") and peroxidized on the other (the "positive").

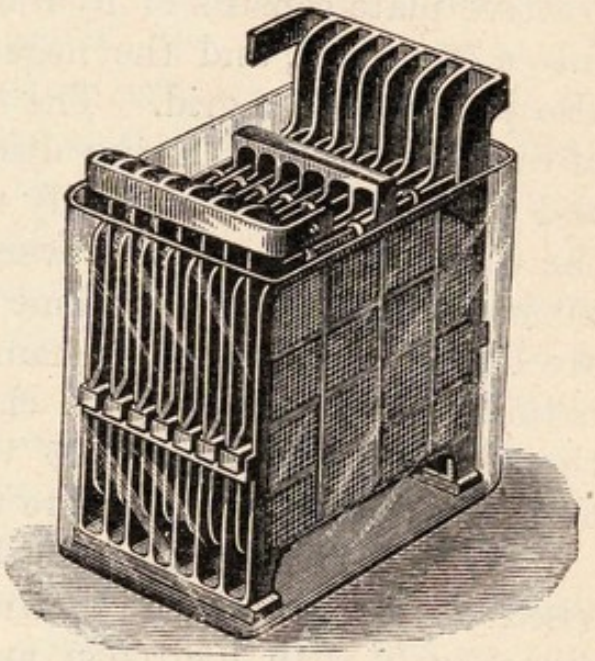


FIG 338.—Cell of Secondary Battery.

A cell of the kind known as the E.P.S. cell is shown in Fig. 338. Positive plates for accumulators are still made on the Planté method from metallic lead, which is first made into ribbons or powder and packed into interstices in a metallic grid, and then "peroxidized" by prolonged charging. Cells of this type are not so subject to disintegration as paste cells, and may be discharged at a greater rate. To keep accumulators in good condition they should be charged up every day till full (known by bubbles rising) and not be discharged too quickly. The density of acid should

never be allowed to exceed 1·21 nor fall below 1·15. The average number of amperes which a cell discharges multiplied by the hours which the discharge lasts, is called its "ampere-hours." If the rate of discharge is increased, the number of ampere-hours is lowered. Stationary accumulators will give from 25 to 33 watt-hours per kilogramme of total weight: portable accumulators about 6 to 10. The efficiency is between 75 and 80 per cent.

573. Edison's Accumulator.—In this cell the positive plate consists of hydrated oxide of nickel packed into a steel grid, and the negative of finely divided iron also packed into a grid. The cell is filled with a solution of caustic potash. During discharge the iron is oxidized and the nickel oxide partially reduced. During charging the chemical actions are reversed. The storage is about 20 watt-hours per kilogramme of total weight. The cells are lighter, and more mechanical than the cells of lead batteries, and they may be charged more rapidly. But the cell has only about 1·25 volts of electromotive force, and the efficiency is not more than 50 per cent.

574. Grove's Gas Battery.—Sir W. Grove devised a cell in which platinum electrodes, in contact respectively with hydrogen and oxygen gas, replaced the usual zinc and copper plates. Each of these gases is partially occluded by the metal platinum, which, when so treated, behaves like a different metal.

Attempts have been made to generate electricity on a larger scale by means of gas batteries. Mond and Lange found that the greatest E.M.F. to be obtained from a cell of hydrogen and oxygen, with finely-divided platinum as collectors, was 0·97, the difference between this and the theoretical 1·47 being lost in heat generated by the condensation of the gases by the platinum.

LESSON LIII.—*Electrodeposition*

575. Electrometallurgy. — The applications of electro-chemistry to the industries are threefold. *First*, to the reduction of metals from solutions of their ores; *secondly*, to the copying of types, plaster-casts, and metal-work by kathode deposits of metal; *thirdly*, to the covering of objects made of baser metal with a thin film of another metal, such as gold, silver, or nickel. All these operations are included under the general term of *electrometallurgy*. The same term is used loosely to include the operation both of electric furnaces (Art. 469) in which the operations are thermal and of those in which they are electrolytic (Art. 579).

Copper of a high degree of purity is refined on a large scale by suspending anodes of impure copper in a solution of copper sulphate and electrolytically depositing pure copper on the kathodes. The impurities such as arsenic, being more electronegative than copper, are left behind as a sludge in the bath.

576. Electrotyping.—In 1836 De la Rue observed that in a Daniell's cell the copper deposited out of the solution upon the copper plate which served as a kathode took the exact impress of the plate, even to the scratches upon it. In 1839 Jacobi in Petrograd, Spencer in Liverpool, and Jordan in London, independently developed out of this fact a method of obtaining, by the electrolysis of copper, impressions (in reversed relief) of coins, stereotype plates and ornaments. A further improvement, due to Murray, was the employment of moulds of plaster or wax, coated with a film of *plumbago* in order to provide a conducting surface upon which the deposit could be made. Bronze in the form of a fine powder is much used instead of plumbago, being a better conductor. Jacobi gave to the process the name of *galvanoplastic*, a term

generally abandoned in favour of the term **electrotyping** or **electrotype process.**

Electrotypes of copper are easily made by hanging a suitable mould in a cell containing a nearly saturated and slightly acidulated solution of sulphate of copper, and passing a current of a battery through the cell, the mould metallized on its surface being the kathode, a plate of copper being employed as an anode, dissolving gradually into the liquid at a rate exactly equal to the rate of deposition at the kathode. This use of a separate cell or "bath" is more convenient than producing the electrotypes in the actual cell of a Daniell's battery. The process is largely employed at the present day to reproduce repoussé and chased ornament and other works of art in facsimile, and to multiply copies of wood blocks for printing. Almost all the illustrations in this book, for example, are printed from electrotype copies, and not from the original wood blocks, which would not wear so well. In all deposition processes success largely depends on having the proper current-density. To deposit metals that are more positive than hydrogen, such as zinc or chromium, it is advisable to use concentrated solutions and high current-densities. For metals that are less positive, such as copper and silver, the current-density may be less. To procure a good tough deposit of copper the current should not exceed 15 amperes per square foot of kathode surface. If a more rapid deposit is required, a solution of nitrate of copper should be used and kept in rapid agitation.

To deposit iron (by the process known as *acierage*, or *steel-facing*) a very large sheet of iron is used as anode, and the liquid used is simply a solution of sal-ammoniac in water. This solution is "charged" with iron by passing the current for a little time through the bath prior to inserting the object to be steel-faced.

577. Electroplating.—In 1801 Wollaston observed that a piece of silver, connected with a more positive

metal, became coated with copper when put into a solution of copper. In 1805 Brugnatelli gilded two silver medals by making them the kathodes of a cell containing a solution of gold. Messrs. Elkington, about the year 1840, introduced the commercial processes of electroplating. In these processes a baser metal, such as german silver (an alloy of zinc, copper, and nickel), is covered with a thin film of silver or gold; the solutions employed being, for *electro-gilding*, the double cyanide of gold and potassium, and for *electro-silvering* the double cyanide of

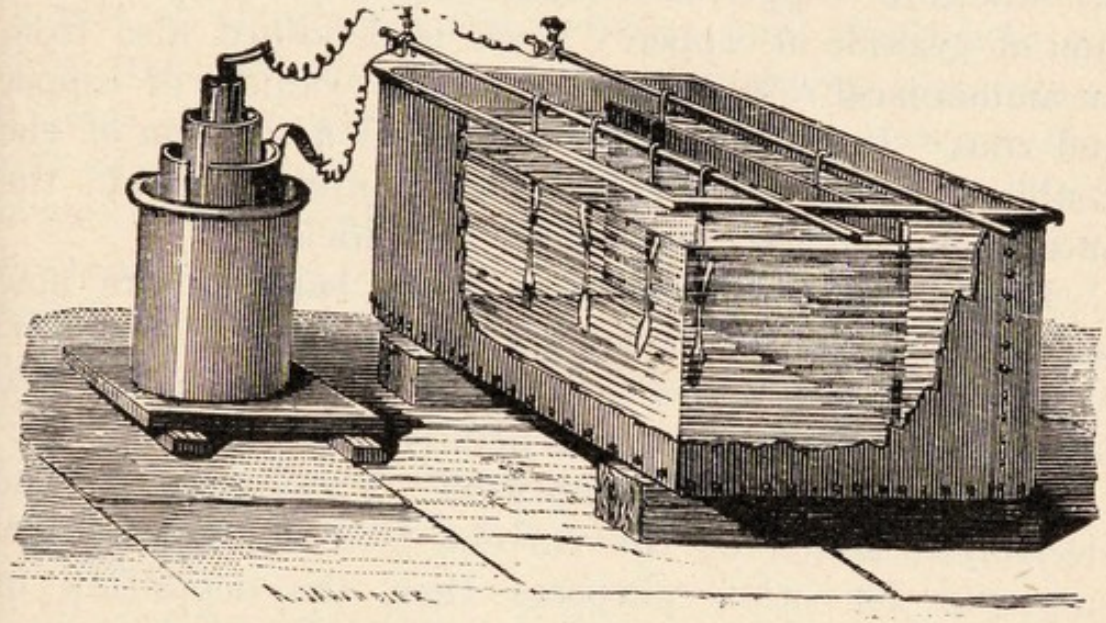


FIG. 339.—Silver-Plating by means of a Primary Cell.

silver and potassium. According to Hittorf the double cyanide $KAgCy_2$ is ionized into K and $AgCy_2$; the potassium ion then reacting on another molecule of cyanide according to the equation $K + KAgCy_2 = 2KCy + Ag$.

Fig. 339 shows a primary cell and a plating-vat containing the silver solution. As anode is hung a plate of metallic silver which dissolves into the liquid. To the kathode are suspended the spoons, forks, or other articles which are to receive a coating of silver. The addition of a minute trace of bisulphide of carbon to the solution causes the deposited metal to have a bright surface. If

the current is too strong, and the deposition too rapid, the deposited metal is grayish and crystalline.

In gilding base metals, such as pewter, they are usually first copper-coated. The gilding of the insides of jugs and cups is effected by filling the jug or cup with the gilding solution, and suspending in it an anode of gold, the vessel itself being connected to the – pole of the battery.

In silvering or gilding objects of iron it is usual first to plate them with a thin coating of copper deposited from an "alkaline" copper bath containing an ammoniacal solution of cyanide of copper. Brass is deposited also from an ammoniacal solution of the mixed cyanides of copper and zinc. In the deposition of nickel a solution of the double sulphate of nickel and ammonium is used: the anode being a sheet of rolled (or cast) nickel.

Except on the very small scale, batteries are now seldom used for electrotyping and plating. A shunt-wound dynamo designed to give a large current at the low pressure of 5 to 10 volts is generally preferred.

578. Other Electrolytic Processes. — The electrolytic action of the current is now commercially employed for other purposes than the deposition of metals. By the electrolysis of chloride of potassium under suitable conditions chlorate of potash is now manufactured in large quantities. Bleaching liquors containing hypochlorites can also be produced from chlorides. Caustic soda is prepared by electrolysis of common salt; and several electrolytic methods of disinfecting sewage are in use.

It has also been shown that the slow processes of tanning can be accelerated by the acid of electric currents, the action being probably osmotic rather than electrolytic.

It seems probable that in the future the use of electric currents will enter largely into the chemical manufactures.

579. Electrolytic Furnaces.—If two stout rods of carbon are introduced into a crucible lined with

magnesia or other refractory substance, and an arc (Art. 486) is formed between them, the internal temperature exceeds that of any other artificial source, enabling many chemical actions to be produced that are otherwise unattainable. Thus if lime mixed with coke is heated in the electric furnace there is produced **calcium carbide** CaC_2, which when mixed with water yields acetylene gas. Many most refractory compounds, such as the oxides of titanium and chromium, can thus be reduced.

Pure **aluminium** is now produced in large quantities by the electrolysis of fused cryolite, which is a double fluoride of aluminium and sodium; pure alumina being added from time to time. In another process aluminium oxide is mixed with charcoal and placed between the ends of two thick carbon rods in a closed fire-brick furnace lined with charcoal. A current of several thousand amperes is passed between the carbon rods, and the aluminium ore is melted and parts with its oxygen to carbon. The liberated aluminium may be allowed to alloy with some other metal, such as copper, or it will combine with the carbon present and form a carbide. It is practically impossible to obtain pure aluminium by this process.

In another kind of electric furnace, invented by Birkeland and Eyde, **nitric acid** is produced by passing atmospheric air through a high-voltage alternating arc between the poles of a magnet. In this case the arc becomes an endothermic flame, absorbing energy, and causing the chemical combination of nitrogen with oxygen. The nitric oxides so produced are absorbed into water to form nitric acid, or neutralized with lime to form nitrate of lime as a fertilizer. This process has become the basis of a large industry, using electric power generated on a large scale by waterfalls working water turbines.

CHAPTER XIV

TELEGRAPHY

LESSON LIV.—*Electric Telegraphs*

580. The Electric Telegraph.—It is difficult to assign the invention of the telegraph to any particular inventor. Lesage (Geneva, 1774), Lomond (Paris, 1787), and Sir F. Ronalds (London, 1816) invented systems for transmitting signals through wires by observing at one end the divergence of a pair of pith-balls when a charge of electricity was sent into the other end. Cavallo (London, 1795) transmitted sparks from Leyden jars through wires "according to a settled plan." Soemmering (Munich, 1808) established a telegraph in which the signals were made by the decomposition of water in voltameters; and the transmission of signals by the chemical decomposition of substances was attempted by Coxe, R. Smith, Bain, and others. Ampère (Paris, 1821) suggested that a galvanometer placed at a distant point of a circuit might serve for the transmission of signals. Schilling and Weber (Göttingen, 1833) employed the deflexions of a galvanometer needle moving to right or left to signal an alphabetic code of letters upon a single circuit. Cooke and Wheatstone (London, 1837) brought into practical application the first form of their *needle* telegraph. Henry (New York, 1831) utilized the attraction of an electromagnet to transmit signals, the movement of the armature

producing audible sounds according to a certain code. Morse (New York, 1837) devised a telegraph in which the attraction of an armature by an electromagnet was made to mark a dot or a dash upon a moving strip of paper. Steinheil (Munich, 1837) discovered that instead of a return-wire the *earth* might be used, contact being made to earth at the two ends by means of earth-plates (see Fig. 344) sunk in the ground. Gintl (1853) and Stearns (New York, 1870) devised methods of *duplex* signalling. Stark (Vienna) and Bosscha (Leyden, 1855) invented *diplex* signalling, and Heaviside (London, 1873) and Edison (Newark, N.J., 1874) invented *quadruplex* telegraphy. Varley (London, 1870) and Elisha Gray (Chicago, 1874) devised *harmonic* telegraphs. For high-speed work Wheatstone devised his automatic transmitter, in which the signs which represent the letters are first punched by machinery on strips of paper; these are then run at a great speed through the transmitting instrument, which telegraphs them off at a much greater rate than if the separate signals were telegraphed by hand. Hughes devised a type-printing telegraph. Wheatstone invented an ABC telegraph in which signals are spelled by a hand which moves over a dial. Cowper (1876) and Elisha Gray (1893) invented autographic writing telegraphs. For cable-working Lord Kelvin invented his mirror galvanometer and his delicate siphon-recorder. It is impossible in these Lessons to describe more than one or two of the simple ordinary forms of telegraph instrument now in use in Great Britain. Students desiring further information should consult the excellent manuals on Telegraphy by A. Crotch and by T. E. Herbert.

581. Single-Needle Instrument. — The single-needle instrument (Fig. 340) consists essentially of a vertical galvanometer, in which a lightly-hung magnetic needle is deflected to right or left when a current is sent, in one direction or the other, around a coil surrounding the needle; the needle visible in front of the dial is but

an index, the real magnetic needle being behind. A code of movements agreed upon comprises the whole alphabet in combinations of motions to right or left. In order to send currents in either direction through the circuit, a "signalling-key" or "tapper" is usually employed. The tapper at one end of the line works the instrument at the other; but for the sake of convenience it is fixed to the receiving instrument. In Fig. 340 the two protruding levers at the base form the tapper, and by depressing the right-hand one or the left-hand one, currents are sent in either direction at will.

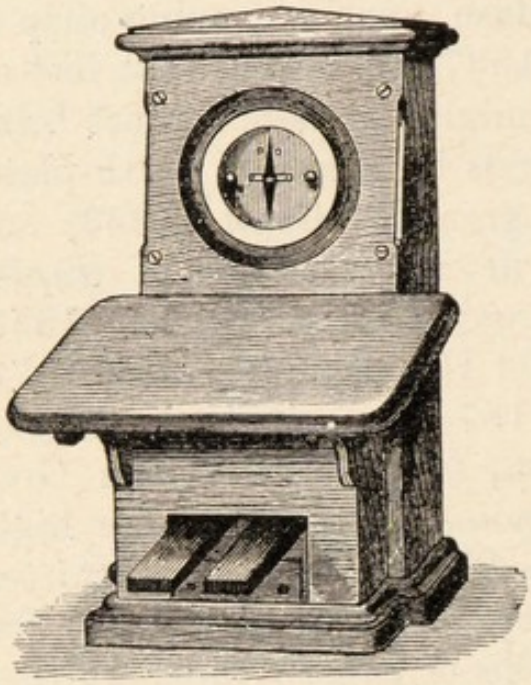


FIG. 340.—Single-needle Instrument.

The principle of action will be made more clear by reference to Fig. 341, which shows a separate signalling key. The two horizontal levers are respectively in com-

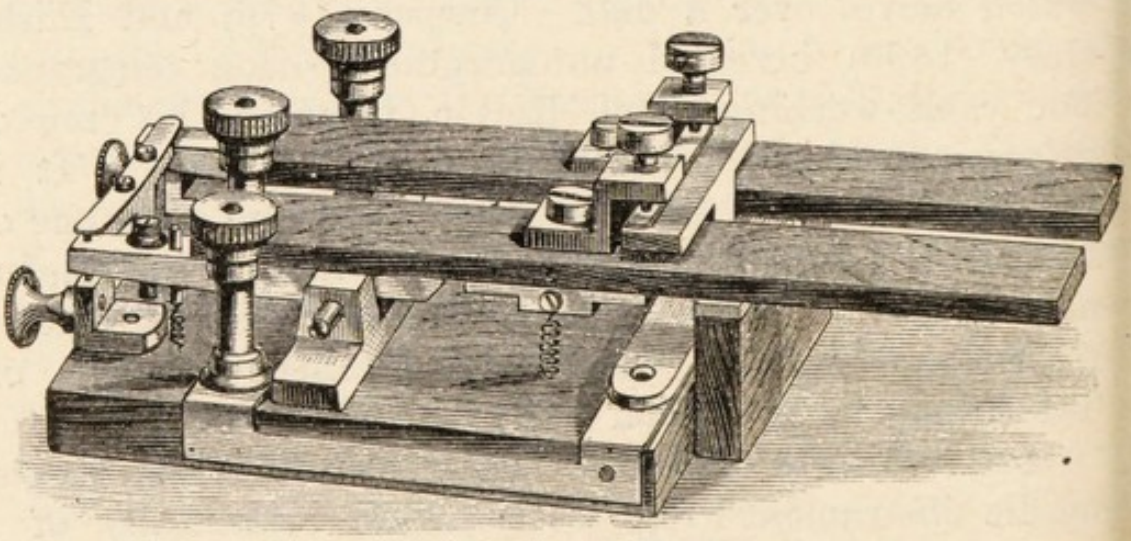


FIG. 341.—Tapper Signalling Key.

munication with the "line," and with the return-line through "earth." When not in use both levers spring up against a cross strip of metal joined to the zinc pole of the battery. At their farther end is another cross strip, which communicates with the copper (or +) pole of the battery. On depressing the "line" key the current runs through the line and back by earth, or in the *positive* direction. On depressing the "earth" key (the line-key remaining in contact with the zinc-connected strip) the current runs through the earth and back by the line, or in the *negative* direction. Telegraphists ordinarily speak of these as positive and negative *currents* respectively.

582. The Morse Instrument.—The most widely used instrument at the present day is the Morse. It con-

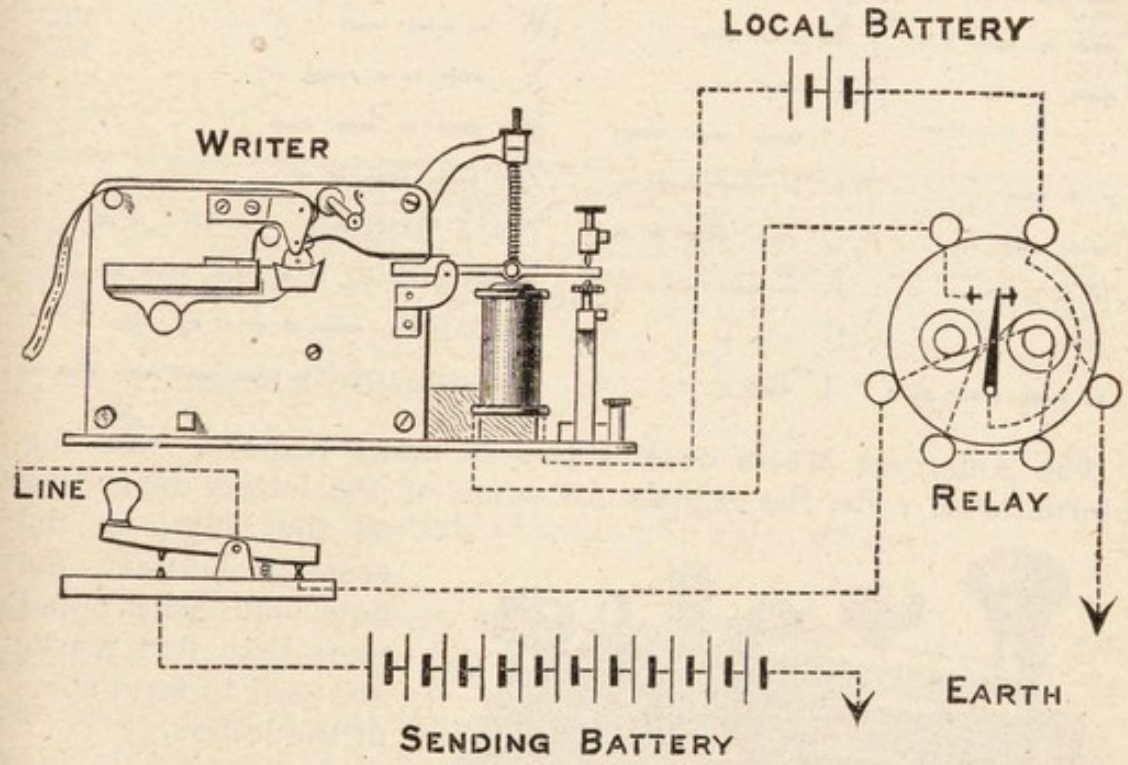


FIG. 342.—Morse Apparatus, with Relay and Local Circuit.

sists essentially of an electromagnet, which, when a current passes through its coils, draws down an armature for a short or a long time. It may either be arranged as a "*sounder*," in which case the operator who is receiving

a message listens to the clicks, and notices whether the intervals between them are long or short; or it may be arranged as an "*embosser*," to print dots and dashes upon a strip of paper drawn by clockwork through the instrument. In the most modern form, however, the Morse instrument is arranged as an "*ink-writer*" (Fig. 342), in which the attraction of the armature downwards lifts a little inky wheel and pushes it against a ribbon of paper. If the current is momentary it prints a mere dot. If the current continues to flow for a longer time while the ribbon of paper moves on, the ink-wheel marks a dash. The International Morse code, or alphabet of dots and dashes, is as follows:

A ·—	K —·—	U ··—
B —···	L ·—··	V ···—
C —·—·	M ——	W ·——
D —··	N —·	X —··—
E ·	O ———	Y —·——
F ··—·	P ·——·	Z ——··
G ——·	Q ——·—	Full stop ·—·—·—
H ····	R ·—·	Repetition ··——··
I ··	S ···	Hyphen —····—
J ·———	T —	Apostrophe ·————·

The American Morse code differs in many respects from the International code, the signals for some of the letters depending on the length of the spacings between the dots and dashes; and more than four marks are used to form some of the letters.

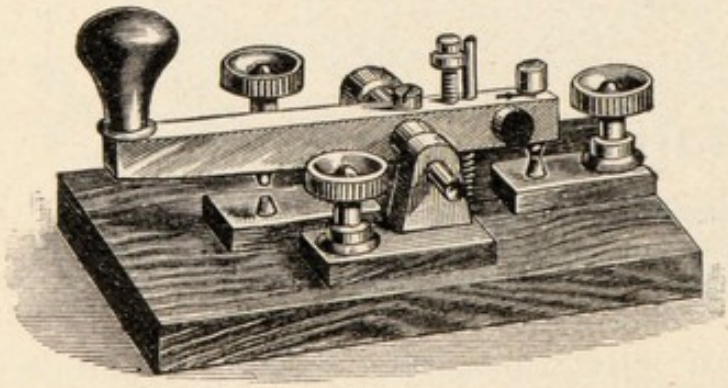


FIG. 343.—Morse Sending Key.

The Morse key is shown in Fig. 343. The line wire is connected with the central pivot A. A spring keeps the front end of the key elevated when not in use, so that the line wire

is in communication through the rear end of the key with the receiving instrument or relay. Depressing the key breaks this communication, and by putting the line wire in communication with the sending battery transmits a current through the line.

583. Open and Closed Circuit Working.—European telegraphs work on the open-circuit plan, the battery being out of circuit when no message is being sent. American telegraphs are usually on the closed-

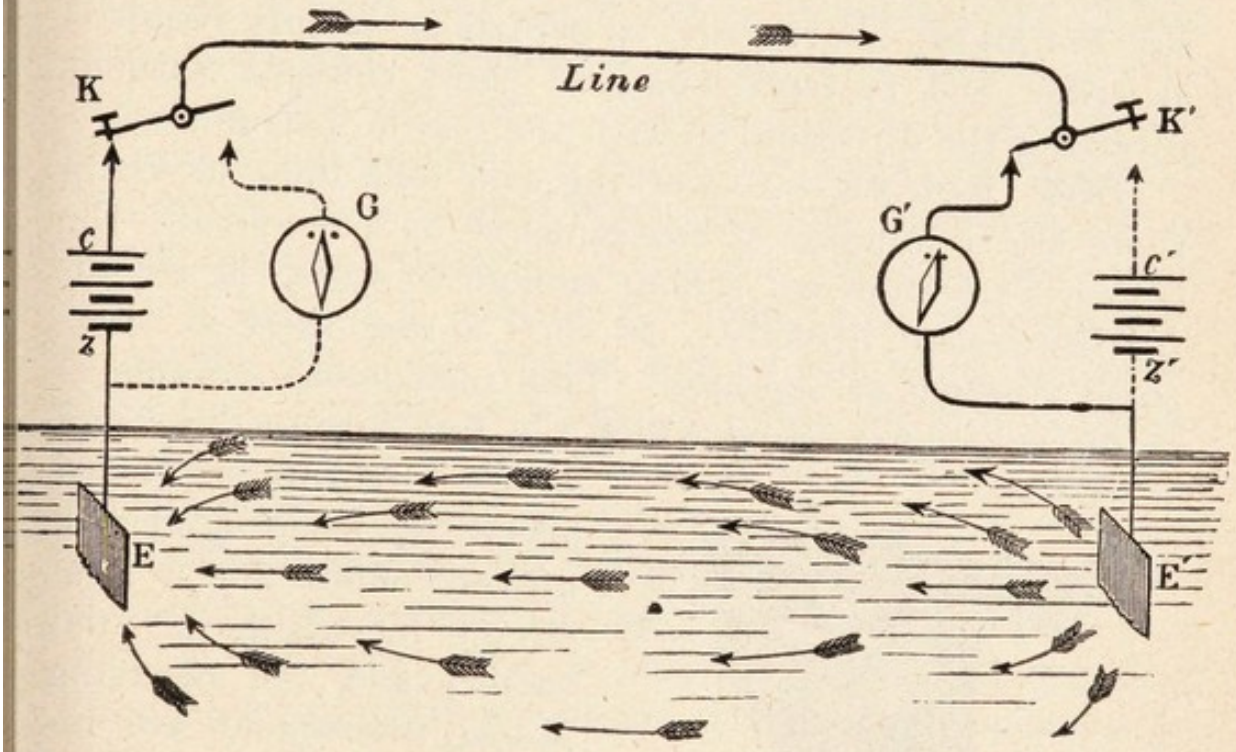


FIG. 344.—Telegraph Circuit with Earth Return.

circuit plan, the current being always on until interrupted to send signals. In the open-circuit method, as it is necessary that a line should be capable of being worked from either end, a battery is used at each, and the wires so connected that when at either end a message is being received, the battery circuit at that end shall be open. Fig. 344 shows the simplest possible case of such an arrangement. At each end is a battery *z c*, one pole of which is put to earth, and the other communicates with a Morse key K. This key is arranged (like that in

Fig. 343) so that when it is depressed to send a signal through the line it quits contact with the receiving instrument at its own end. The current flowing through the line passes through K′ and enters a receiving instrument G′ at the distant end, where it produces a signal, and returns by the earth to the battery whence it started. A similar battery and key at the distant end suffice to transmit signals in the opposite direction to G when K is not depressed. The diagram is drawn as if G were a simple galvanometer; but the arrangement would perfectly suit the Morse instrument, in which it is only required at either end to send long and short currents without reversing the direction, as with the needle instruments.

584. Relays.—In working over long lines, or where there are a number of instruments on one circuit, the currents are often not strong enough to work the recording instrument directly. In such a case there is interposed a **relay** or repeater. This instrument consists of an electromagnet round which the line current flows, and whose delicately poised armature, when attracted, makes contact for a local circuit in which a local battery and the receiving Morse instrument are included. The principle of the relay is, then, that a current too weak to do the work itself may set a strong local current to do its work for it.

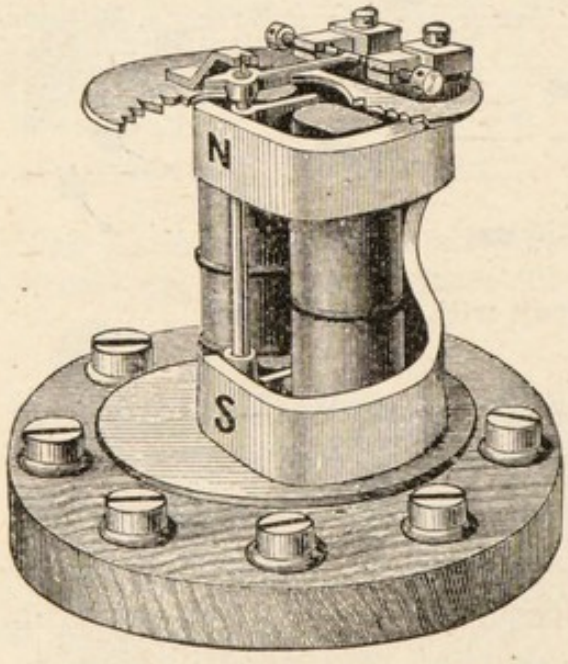


FIG. 345.—Relay (Post-Office Pattern).

In Fig. 342 the Morse receiver (an "ink-writer") M is placed in a local circuit with a local battery LB and a relay of the British Post-Office pattern. Whenever a current in the line circuit moves the tongue of the relay,

it closes the local circuit, and causes the Morse to record either a dot or a dash upon the strip of paper. A view of the P.O. standard relay itself is given in Fig. 345. It is of the "polarized" kind (Art. 418); a permanent steel magnet of compact shape being used to magnetize tongues that are pivoted between the poles of the electromagnet.

585. Faults in Telegraph Lines.—Faults may occur in telegraph lines from several causes: either from the breakage of the wires or conductors, or from the breakage of the insulators, thereby short-circuiting the current through the earth before it reaches the distant station, or, as in overhead wires, by two conducting wires touching one another. Various modes for testing the existence and position of faults are known to telegraph engineers; they depend upon accurate measurements of resistance or of capacity. Thus, if a telegraph cable parts in mid-ocean it is possible to calculate the distance from the shore end to the broken end by comparing the resistance that the cable is known to offer per mile with the resistance offered by the length up to the fault, and dividing the latter by the former.

586. Duplex and Quadruplex Telegraphy.—To send two messages through one wire, one from each end, at the same time, is known as **duplex** working. There are two distinct methods of arranging apparatus for duplex working. The first of these, known as the *differential duplex*, involves the use of instruments wound with differential coils, and is applicable to special cases. The second method of duplex working, known as the *bridge duplex*, is capable of much more general application. The diagram of Fig. 346 will explain the general principle. The first requirement in duplex working is that the instrument at each end shall only move in response to signals from the other end, so that an operator at R may be able to signal to the distant instrument M′ without his own instrument M being affected, M being all the while in circuit and able to receive signals from the distant

operator at R′. To accomplish this the circuit is divided at R into two branches, which go, by A and B respectively, the one to the line, the other through a certain resistance P to the earth. If the ratio between the resistances in the arms RA and RB is equal to the ratio of the resistances of the line and of P, then, by the principle of Wheatstone's Bridge, *no* current will pass through M. So M does not show any currents sent from R; but M′ will show them, for the current on arriving at C will divide into two parts, part flowing round to the earth by R′, the other part flowing through M′ and producing a signal. If, while this is going on, the operator at the

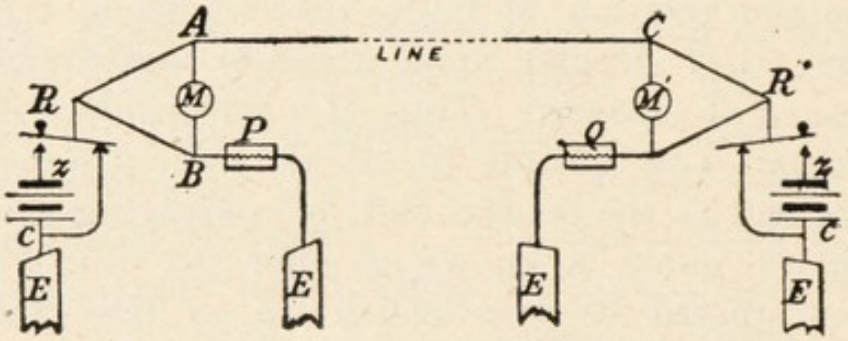


FIG. 346.—Circuit for Duplex Signalling.

distant R′ depresses his key and sends an equal current in the opposite direction, the flow through the line will cease; but M will now show a signal, because, although no current flows through the line, the current in the branch RA will now flow down through M, as if it had come from the distant R′, so, whether the operator at R be signalling or not, M will respond to signals sent from R′. In duplexing long lines and cables condensers are employed in the arms RA and RB of the bridge; and instead of a mere balancing resistance at P and Q there is used an "artificial cable," a combination of condensers and resistances to imitate the electrical properties of the actual line or cable between the stations.

The **Diplex** method of working consists in sending two messages at once through a wire in the same direc-

tion. To do this it is needful to employ two sets of instruments, one of which responds only to currents in one given direction, while the other set responds only when the currents (in either direction) attain a certain strength. The first set therefore consists of polarized relays, which, being themselves permanently magnetized, respond therefore only to currents in one direction. The second set consists of non-polarized relays controlled by springs that are so adjusted as to allow movement of the relay tongue only when the currents are of a certain strength. There must be two sets of operating keys, one of which serves to reverse the direction of the current it transmits; the other to alter the strength of the currents.

The **Quadruplex** method of working combines the duplex and the diplex methods. On one and the same line are used two sets of instruments, one of which (worked by a polarized relay) works only when the *direction* of the current is changed, the other of which (worked by non-polarized relay adjusted with springs to move only with a certain minimum force) works only when the *strength* of the current is changed and is independent of their direction.

LESSON LV.—*Cable Telegraphy*

587. Submarine Cables.—Telegraphic communication between two countries separated by a strait or ocean is carried on through cables, sunk to the bottom of the sea, containing conducting wires carefully protected by an outer sheath of insulating and protecting materials. The conductor is usually of purest copper wire, weighing from 70 to 400 lbs. per nautical mile, made in a sevenfold strand to lessen risk of breaking. Figs. 347 and 348 show respectively, in their natural size, sections of the first Atlantic cable laid in 1857 and of one of the more recent. In the latter, which is of the usual type of cable

for long lines, the core consisting of the copper conductor protected by a stout layer of guttapercha, to secure perfect insulation, is protected externally by a sheathing

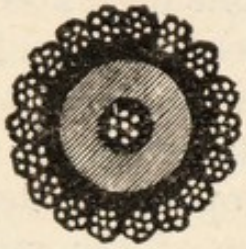


FIG. 347.—Section of 1857 Cable.

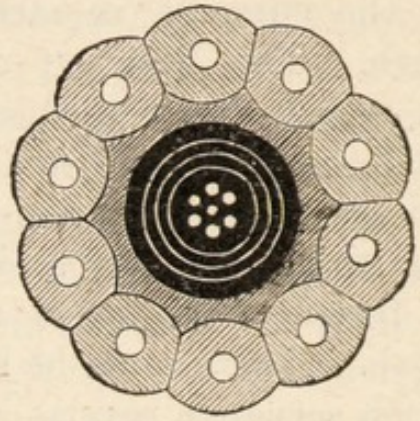


FIG. 348.—Section of 1893 Cable.

of jute or other fibrous material impregnated with bituminous compounds, and in it are embedded a number of strong steel wires. The *shore ends* are even more strongly protected by external wires.

588. Speed of Signalling through Cables.—Signals transmitted through long cables are retarded, the retardation being due to the following causes.

The cable in its insulating coatings, when immersed in water, acts laterally like a Leyden jar of enormous capacity (as explained in Art. 321), and the first portions of the current, instead of flowing through, remain in the cable as an electrostatic *charge* on the surface of the guttapercha. For every separate signal the cable must be at least partially charged and then discharged. Culley states that when a current is sent through an Atlantic cable from Ireland to Newfoundland no effect is produced on the most delicate instrument at the receiving end for two-tenths of a second, and that if the battery were kept on for a sufficient time for the current, rising in an electric wave which travels forward through the cable, to rise to its full strength at the far end, three seconds would be taken by each separate signal. The strength of the current falls gradually also when the

circuit is broken; since it takes time for the dielectric to discharge itself. In order to accelerate the speed of signalling the operator puts on the battery and then almost immediately takes it off again; so that there is no waiting for the current to reach its full strength. The signalling current as sent in to the transmitting end is a short sharp one; but as received it is a much feebler impulse of longer duration. The "curve of arrival" may be contrasted with the shaded "curve of trans-

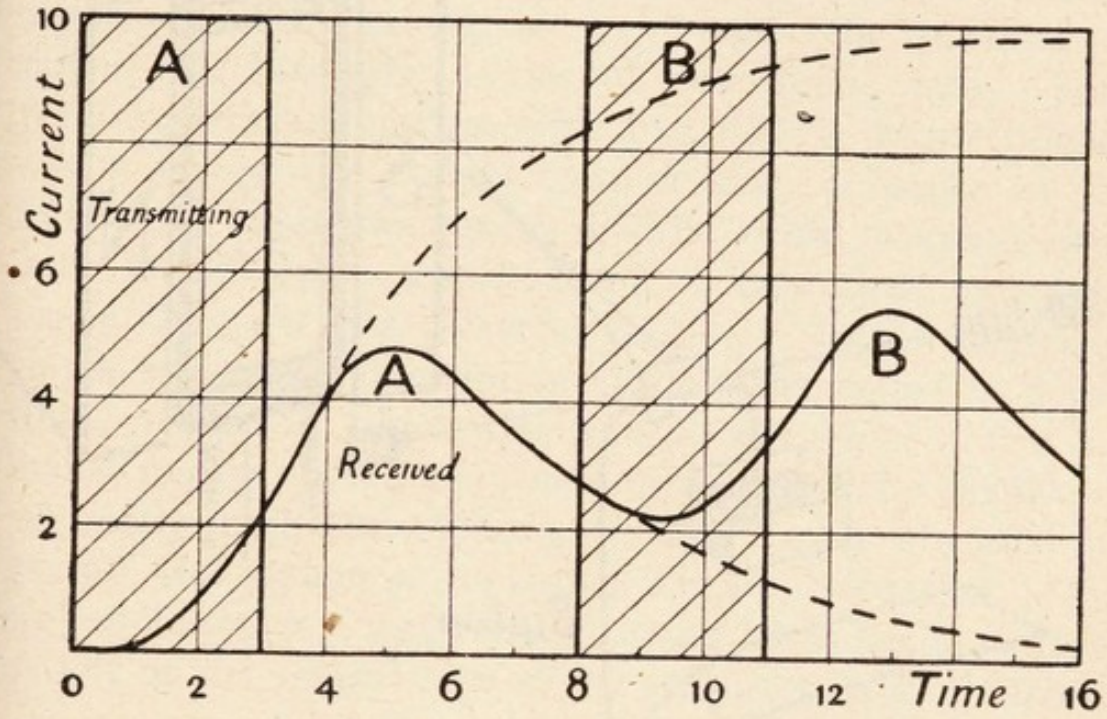


FIG. 349.—Curves of Transmission and Arrival.

mission" (Fig. 349). But even so the time occupied by the arrival impulse is much shortened, and a much larger number of impulses can be sent per minute than would be possible if the sending contact were not short and sharp. The number of signals that can be sent through a cable in a given time is less as the capacity and resistance are greater. The time required to transmit a given number of signals through a cable of capacity C and resistance R is proportional to CR: so the retardation is proportional to the *square of the length* of the cable. Certain means adopted to get rid of this retardation

are explained in Art. 322. It is usual to insert in the circuit at each end of the cable a condenser of several microfarads, through which the signals pass. The tendency of the condenser to discharge helps to *curb* the signals and make each shorter and sharper. It is

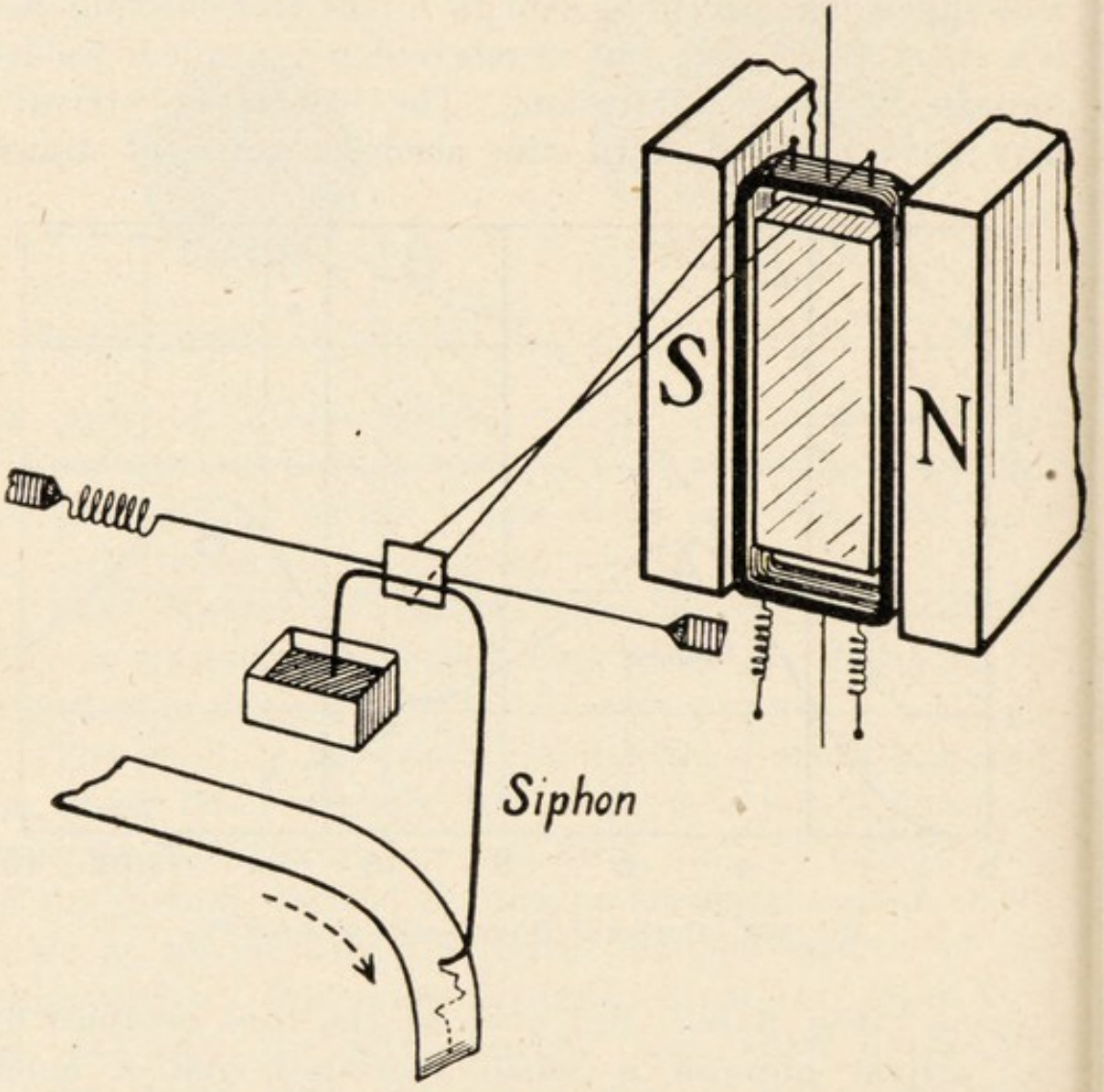


FIG. 350.—Kelvin's Siphon Recorder.

theoretically possible (compare Art. 529) to compensate capacity by self-induction; but as the capacity of a cable is distributed all along it, the self-induction coils to compensate the retardation would have to be applied as at intervals, as suggested by Heaviside, who proposed to *load* the cable with such coils. Pupin has calculated the suitable distances apart for such loading coils. Com-

pensating inductance coils may also be applied as inductive leaks, connected as shunts from the core to the sheath of the cable at suitable intervals. A cable with a self-inductive shunt or leak at a point near its middle transmits signals more rapidly than one not so compensated.

589. Receiving Instruments for Cables.—The *mirror-galvanometer* of Lord Kelvin (Art. 228) was devised for cable signalling, the movements of the spot of light sweeping over the scale to a short or a long distance, or alternating to right and left, sufficing to signal the dots and dashes of the Morse code. Lord Kelvin's *Siphon Recorder* (see Fig. 350) is an instrument which writes the signals upon a strip of paper by the following ingenious means:—The cable communicates with a delicately suspended coil of wire that hangs between the poles of a powerful magnet. To the suspended coil is attached a fine siphon of glass suspended by a silk fibre, one end of which dips into an ink vessel. The ink makes marks upon a strip of paper (moved by clockwork vertically past the siphon), friction being obviated by giving the siphon a continual minute vibration. The siphon record is a wavy line showing little bends to right or left of the central line of the strip, for dots or dashes.

LESSON LVI.—*Miscellaneous Telegraphs*

590. Multiplex Telegraphs.—Varley proposed to send messages by electrically transmitting musical tones, interrupted to sound as dots and dashes. This necessitated the transmission of currents either rapidly alternating or rapidly intermittent. Elisha Gray, who constructed *harmonic telegraphs* on this plan, found it possible to transmit five or six messages simultaneously in one line.

By using at each end of a line two synchronously revolving distributing switches, it is possible to send

several messages at once through a line; the distributors (invented by Delany) causing each transmitting instrument to be in circuit with its corresponding receiving instrument for a small fraction of a second at regular short intervals.

591. Electric Bells.—The common form of *Electric Trembling Bell* (invented 1850 by John Mirand) consists

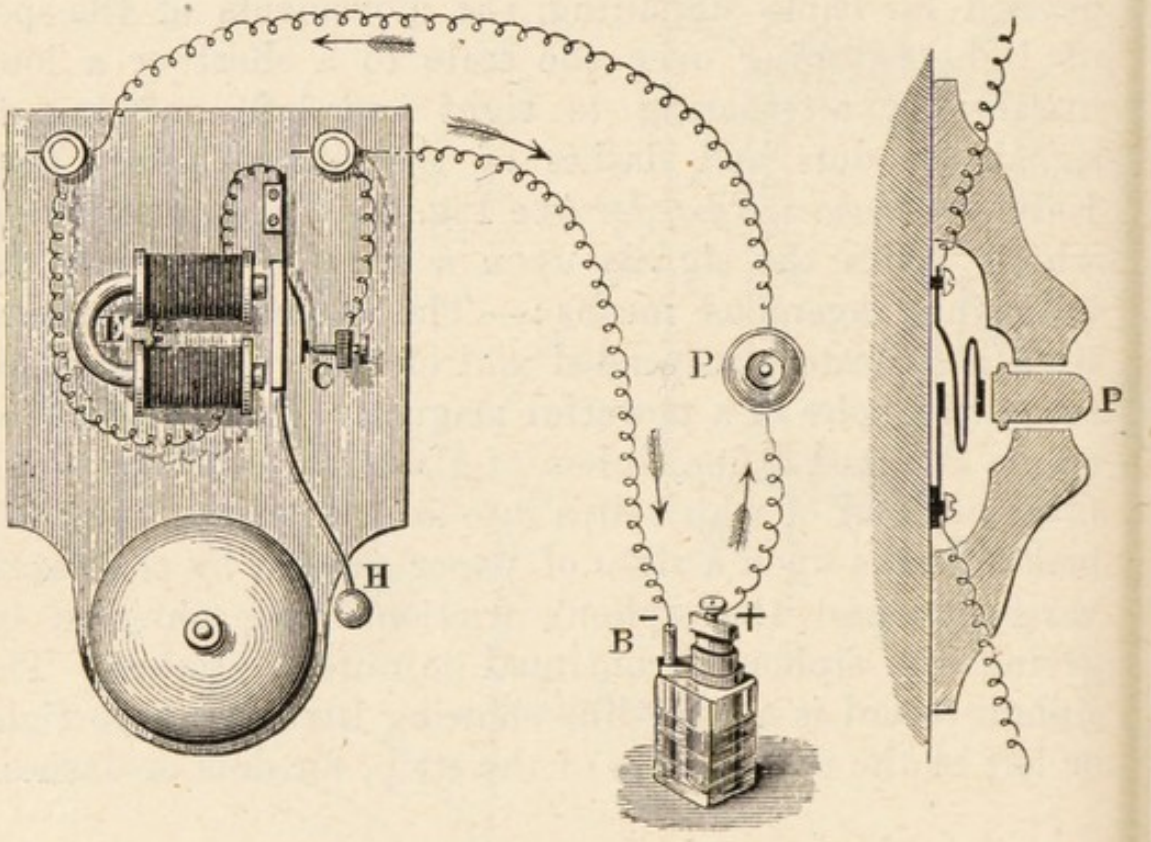


FIG. 351*a*. FIG. 351*b*.

Electric Trembling Bell and Push

of an electromagnet, which moves a hammer backward and forward by alternately attracting and releasing it, so that it beats against a bell. The arrangements of the instrument are shown in Fig. 351*a*, in which E is the electromagnet and H the hammer. A battery, consisting of one or two Leclanché cells placed at some convenient point of the circuit, provides a current when required. By touching the "push" P, the circuit is completed, and a current flows along the line and round the coils of the

electromagnet, which forthwith attracts a small piece of soft iron attached to the lever, which terminates in the hammer H. The lever is itself included in the circuit, the current entering it above and quitting it at C by a contact-breaker, consisting of a spring tipped with platinum resting against the platinum tip of a screw, from which a return wire passes back to the zinc pole of the battery. As soon as the lever is attracted forward the circuit is broken at C by the spring moving away from contact with the screw; hence the current stops, and the electromagnet ceases to attract the armature, but the momentum of the hammer carries it forward. Immediately afterwards, however, the hammer falls back, again establishing contact at C, whereupon the armature is once more attracted forward, and so on. The push P is shown in section on the right (Fig. 351*b*). It usually consists of a cylindrical knob of ivory or porcelain capable of moving loosely through a hole in a circular support of porcelain or wood, and which, when pressed, forces a platinum-tipped spring against a metal pin, and so makes electrical contact between the two parts of the interrupted circuit. Bells having a polarized armature, and without any break, are used as call-bells for telephones; the generator being a small magneto alternator like Fig. 285, driven by a handle.

592. Electric Clocks and Chronographs.— Clocks may be either driven or controlled by electric currents. Bain, Hipp, and others devised electric clocks of the first kind, in which the ordinary motive-power of a weight or spring is abandoned, the clock being driven by its pendulum, the "bob" of which is an electromagnet alternately attracted from side to side. The difficulty of maintaining a perfectly constant battery current delayed progress. Hope-Jones overcame this difficulty by causing the current, acting through an electromagnet, to lift a small weight, which in descending drives the mechanism of the clock with an unvarying force.

Electrically controlled clocks, governed by a standard central clock, have proved a fruitful invention. In these the standard timekeeper is constructed so as to complete a circuit periodically, once every minute or half minute. The transmitted currents set in movement the hands of a system of dials placed at distant points, by causing an electromagnet placed behind each dial to attract an armature, which, acting upon a ratchet wheel by a pawl, causes it to move forward through one tooth at each specified interval, and so carries the hands round at the same rate as those of the standard clock.

Electric *chronographs* are used for measuring very small intervals of time. A stylus fixed to the armature of a small electromagnet traces a line upon a piece of paper fixed to a cylinder revolving by clockwork. A current sent through the coils of the electromagnet moves the armature and causes a lateral notch in the line so traced. A second current marks a second notch; and from the interval of *space* between the two notches the interval of *time* which elapsed between the two currents may be calculated to the ten-thousandth part of a second if the speed of rotation is accurately known. The velocity with which a cannon-ball moves along the bore of the cannon can be measured thus.

Lesson LVII.—*Electric Telephones*

593. Early Telephones. — The first successful attempt to transmit sounds electrically was made in 1861 by Reis, who succeeded in conveying musical and other tones by an imperfect telephone. In this instrument the voice was caused to act upon a point of loose contact in an electric circuit, and by bringing those parts into greater or less intimacy of contact (Art. 432), thereby varied the resistance offered to the circuit. The transmitting part of Reis's telephone consisted of a battery

and a contact-breaker, the latter being formed of a tympanum or diaphragm of stretched membrane, capable of taking up sonorous vibrations, and having attached to it a thin elastic strip of platinum, which, as it vibrated, beat to and fro against the tip of a platinum wire, so making and breaking contact wholly or partially at each vibration in exactly the same manner as is done with the carbon contacts in the modern transmitters of Blake, Berliner, etc. The receiving part of the instrument consisted of an iron wire fixed upon a sounding-board and surrounded by a coil of insulated wire forming part of the circuit. The rapid magnetization and demagnetization of such an iron core will produce audible sounds (Art. 125). If the current vary, the iron wire is partially magnetized or demagnetized, giving rise to corresponding vibrations of varying amplitudes and forms; hence such a wire will serve perfectly as a receiver to reproduce speech if a good transmitter is used. Reis himself transmitted speech with his instrument, but only imperfectly, for all tones of speech cannot be transmitted by abrupt interruptions of the current, to which Reis's transmitter is prone when spoken into, owing to the extreme lightness of the contact: they require gentle undulations, sometimes simple, sometimes complex, according to the nature of the sound. The vowel sounds are produced by periodic and complex movements in the air; the consonants being for the most part non-periodic. Reis also devised a second receiver, in which an electromagnet attracted an elastically supported armature of iron, which vibrated under the attraction of the more or less interrupted current.

In 1876 Elisha Gray devised a transmitter in which a variable water-resistance (made by a platinum wire dipping into water) was acted upon by the voice. He designed an electromagnetic receiver.

Telephone receivers were invented by Varley and Dolbear, in which the attraction between the oppositely

electrified armatures of a *condenser* is utilized in the production of sounds. Dolbear's receiver consists merely of two thin metal disks, separated by a very thin air-space. As the varying currents flow into and out of this condenser the two disks attract one another more or less strongly, and thereby vibrations are set up which correspond to the vibrations of the original sound.

In 1876 Graham Bell invented the magneto-telephone. In this instrument the speaker talks to an elastic plate of thin sheet iron, which vibrates and transmits its every movement electrically to a similar plate in a similar telephone at a distant station, causing it to vibrate in an identical manner, and thereby to emit identical sounds. The transmission of the vibrations depends upon the principles of magneto-electric induction explained in Lesson XVIII. Fig. 352 shows Bell's Telephone in section. The disk D is placed behind a conical mouthpiece, to which the speaker places his mouth or the hearer his ear. Behind the disk is a magnet AA running the length of the instrument; and upon its front pole, which nearly touches the disk, is fixed a small bobbin, on which is wound a coil C of fine insulated wire, the ends of the coil being connected with the terminal screws FF. One such instrument is used to transmit, and one to receive the sounds, the two being connected in simple circuit. No battery is needed, for the transmitting instrument itself generates the induced currents as follows:—The magnet AA induces a certain number of magnetic lines through the coil C. Many of these pass into the iron disk. When the iron disk in vibrating moves toward the magnet pole, more magnetic lines meet it; when it recedes, fewer lines meet it. Its motion to and fro will therefore *alter the number of lines*

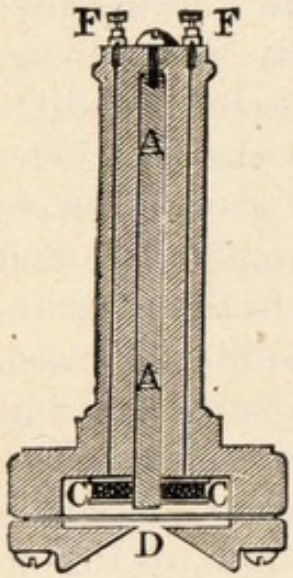


FIG. 352.—Bell's Receiver.

which pass through the hollow of the coil C, and will therefore (Art. 243) generate in the wire of the coils currents whose strength is proportional to the rate of change in the number of the lines. Bell's instrument, when used as a transmitter, may therefore be regarded as a sort of vibrating dynamo, which pumps currents in alternate directions into the wire. At the distant end the currents as they arrive flow round the coils either in one direction or the other, and therefore either add momentarily to or take from the strength of the magnet. When the current in the coils is in such a direction as to reinforce the magnet, the magnet attracts the iron disk in front of it more strongly than before. If the current is in the opposite direction the disk is less attracted and flies back. Hence, whatever movement is imparted to the disk of the transmitting telephone, the disk of the distant receiving telephone is forced to repeat, and it therefore throws the air into similar vibrations, and so reproduces the sound. Bell's method of transmitting was soon abandoned (except for very short lines). In modern telephonic work Reis's plan of using a separate transmitter with a battery is universal, the Bell instrument being used as a receiver only and not as a transmitter.

594. Edison's Transmitter.—Edison constructed a transmitting instrument, in which the vibrations of the voice, actuating a diaphragm of mica, made it exert more or less compression on a button of prepared lamp-black placed in the circuit. The resistance of this is affected by pressure of contacts; hence the varying pressures due to the vibrations cause the button to offer a varying resistance to any current flowing (from a battery) in the circuit, and vary its strength accordingly. This varying current may be received as before in an electromagnetic receiver of the type described above, and there set up corresponding vibrations. This instrument also has been abandoned in favour of transmitters of the microphone type. Edison also invented a receiver of singular power,

which depends upon a curious fact discovered by himself, namely, that if a platinum point presses against a rotating cylinder of moist chalk, the friction is reduced when a current passes between the two. And if the point be attached to an elastic disk, the latter is thrown into vibrations corresponding to the fluctuating currents coming from the speaker's transmitting instrument.

595. Microphones.—Hughes, in 1878, discovered that a *loose contact* between two conductors, forming part

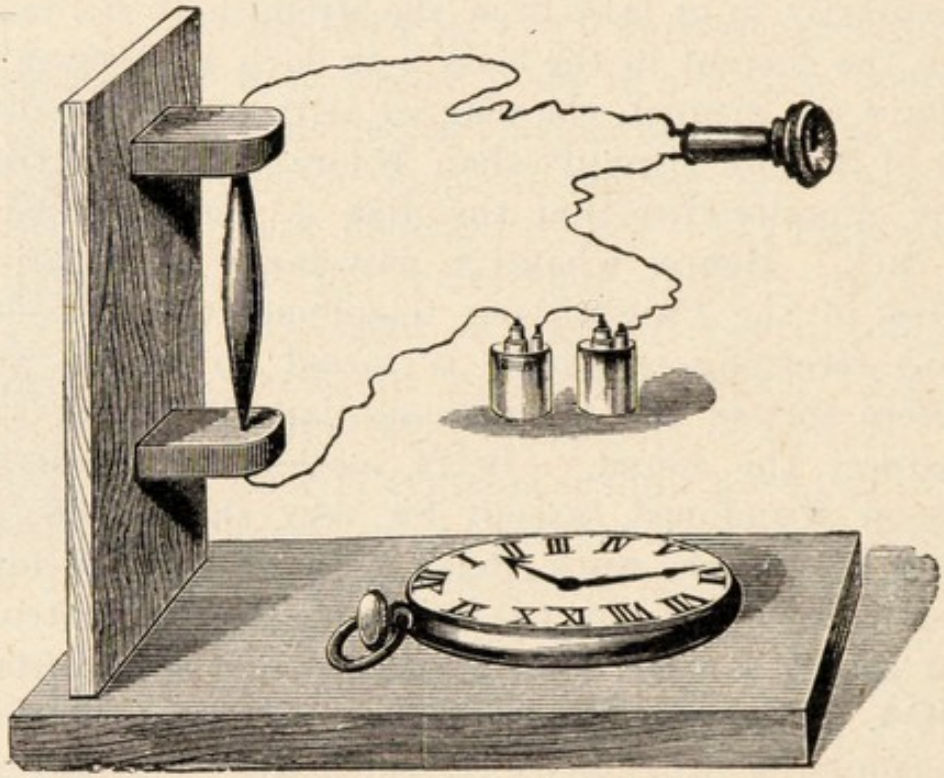


FIG. 353.—Hughes Microphone.

of a circuit in which a small battery and a receiving telephone are included, may serve to transmit sounds without the intervention of any specific tympanum or diaphragm like those of Reis and Edison, because the smallest vibrations will affect the resistance (Art. 432) at the point of loose-contact. The **Microphone** (Fig. 353) embodies this principle. In the form shown in the figure, a small thin pencil of carbon is supported loosely between two little blocks of the same substance fixed to a sounding-board of thin pine-wood, the blocks being con-

nected with one or two small cells and a Bell receiver. The amplitude of the vibrations emitted by the receiver may be much greater than those of the original sounds, and therefore the microphone may serve, as its name indicates, to magnify minute sounds, such as the ticking of a watch or the footfalls of an insect, and render them audible. In modern telephony microphones under the name of *carbon transmitters* are in general use. In the Blake transmitter a pin of platinum is pressed by a light spring against a polished plug of hard carbon, forming a delicate contact through which the current flows. This electrical mechanism is mounted behind a metal disk to take up the vibrations of the speaker's voice. In the Hunnings *loud-speaking transmitter* granulated coke carbon is placed loosely between two metal or carbon surfaces EE, so that the numerous contacts will carry a stronger current. Fig. 354 gives a section of this transmitter, in which M is the mouthpiece, EE the carbon electrodes between which are the carbon granules, and D the diaphragm which responds to the vibrations of the voice communicated to the mouthpiece M, thus causing a variation of the resistance through the granules and a corresponding variation in the current transmitted to the line.

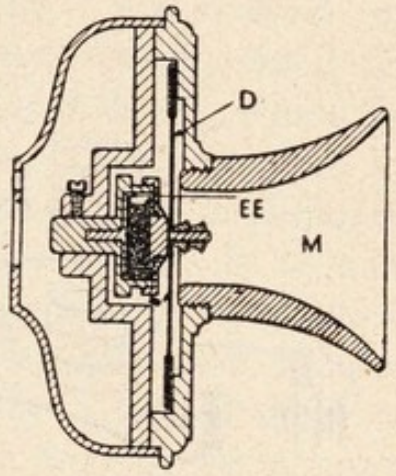


FIG. 354.—Hunnings's Microphonic Transmitter.

For all long-line work the microphone transmitter is included with a battery of one or two cells in a small local circuit of low resistance, in which is inserted the primary wire of a small transformer or induction coil. The secondary wire of this transformer is a coil of fine wire of many turns, which transmits through the line and return circuits smaller currents at a higher voltage.

596. Telephone Exchanges. — For enabling a large number of subscribers to communicate by telephone with one another, the lines from each subscriber's instrument are brought to a central office known as a *telephone exchange.* Here each line terminates on a *switch-board,* which is so arranged that the operator can in an instant make a connexion from the line of any one subscriber to that of any other, so that these two can talk together.

597. Hughes' Induction Balance.—The extreme sensitiveness of Bell's receiver (Art. 593) to the feeblest currents has suggested its employment to detect currents

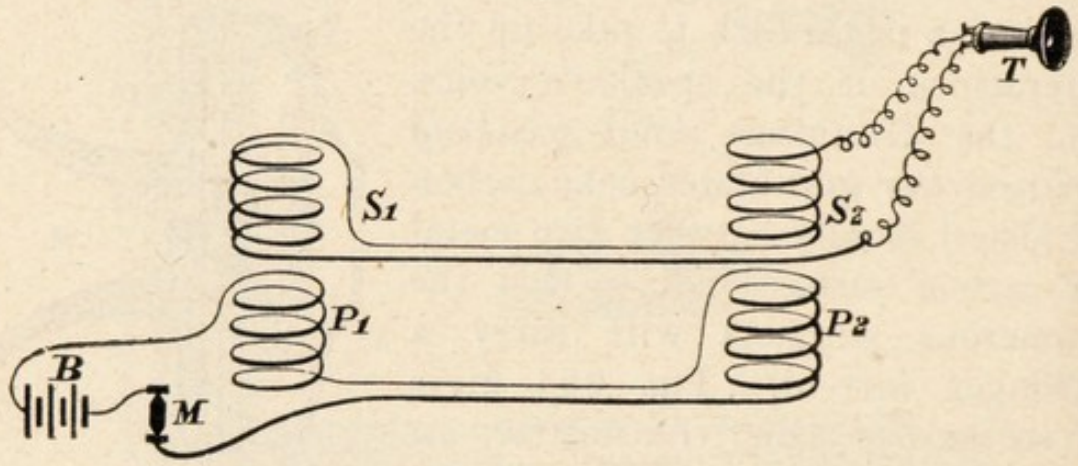


FIG. 355.—Hughes' Induction Balance.

too weak to affect most delicate galvanometers. The currents must be intermittent, or alternating, or they will not keep the disk of the telephone in vibration. Hughes applied this property of the telephone to an instrument named the Induction Balance (Fig. 355). A small battery B, connected with a microphone M, passes through two coiis of wire P_1, P_2, wound on bobbins fixed on a suitable stand. Above each of these primary coils are placed two secondary coils, S_1, S_2, of wire, of the same size, and of exactly equal numbers of turns of wire. The secondary coils are joined to a receiver T, and are wound in opposite directions. The result of this arrangement is that whenever a current either begins or stops flowing in the primary coils, P_1 induces a current in S_1, and P_2

in S_2. As S_1 and S_2 are wound in opposite ways, the two currents thus induced in the secondary wire neutralize one another, and, if they are of equal strength, balance one another so exactly that no sound is heard in the telephone. But a perfect balance cannot be obtained unless the resistances and the coefficients of mutual induction and of self-induction are alike. If a flat piece of silver or copper (such as a coin) be introduced between S_1 and P_1, there will be less induction in S_1 than in S_2, for part of the inductive action in P_1 is now spent on setting up currents in the mass of the metal (Art. 500), and a sound will again be heard in the telephone. But balance can be restored by moving S_2 farther away from P_2, until the induction in S_2 is reduced to equality with S_1, when the sounds in the telephone again cease. It is possible by this means to test the relative conductivity of different metals which are introduced into the coils. It is even possible to detect a counterfeit coin by the indication thus afforded of its conductivity. The induction balance has also been applied in surgery by Graham Bell to detect the presence of a bullet in a wound, for a lump of metal may disturb the induction when some inches distant from the coils.

598. Brown's Relay.—Recently a form of relay has been devised by S. G. Brown which enables telephonic speech to be relayed from one circuit to another with a considerable augmentation of loudness. The relay is constructed with a carefully balanced lever and with working parts made of "invar" steel which does not expand or contract with changes of temperature.

599. The Telegraphone.—Poulsen has contrived an instrument capable of recording and reproducing telephonic speech. In the telephone circuit is included a minute electromagnet which records magnetically the variations of current upon a wire (or plate) of tungsten steel which runs beneath its poles. The series of minute poles thus imprinted on the moving steel is quite invisible;

but when this magnetic record is afterwards caused to run under the poles of a similar electromagnet in a circuit containing a telephone receiver, the listener hears the speech reproduced, the apparatus acting as a magnetic kind of phonograph.

CHAPTER XV

ELECTRIC WAVES

LESSON LVIII.—*Oscillations and Waves*

600. Electric Oscillations.—If a charged condenser or Leyden jar is discharged slowly through a conductor of high resistance, such as a nearly dry linen thread, the charge simply dies away by a discharge which increases in strength at first and then gradually dies away. If, however, the condenser is discharged through a coil of wire of one or more turns (the spark being taken between polished knobs to prevent premature partial discharges by winds or brushes), the effect is wholly different, for then the discharge consists of a number of excessively rapid oscillations or surgings. The snapping sound of an oscillating spark is very distinctive. Oscillations arise because of the self-inductance of the circuit, by reason of which (Art. 501) the current once set up tends to go on. The first rush more than empties the condenser, and charges it the opposite way; then follows a reverse rush, which also overdoes the discharge and charges the condenser the same way as at first, and so forth. Each successive oscillation is feebler than the preceding, so that after a number of oscillations the discharge dies away as in Fig. 356. This effect, whether due to the waste of energy by resistance in the path, or to energy being radiated away in waves, is called *damping*. If there were no loss of energy by resistance or radiation

there would be a long series of undamped oscillations, that is with practically no decrement in the amplitudes of successive oscillations. The spark of a jar discharged through a circuit of low resistance really consists of a number of successive sparks in reverse directions. One proof of this, as pointed out by Henry in 1842 from the experiments of Savery, is that if jar-discharges through a coil are used to magnetize steel needles, the direction of the magnetization is anomalous, being sometimes one way, sometimes the other. Fig. 357 shows two forms of oscillating circuits, as used by Sir Oliver Lodge in his investigations. In any such circuit the three essentials are: (i.) *capacity*, (ii.) *self-inductance*, (iii.) *a spark-gap*. Also, the resistance must be small.

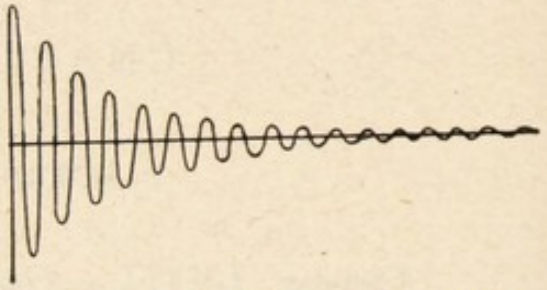


FIG. 356.—Diagram of Electric Oscillations.

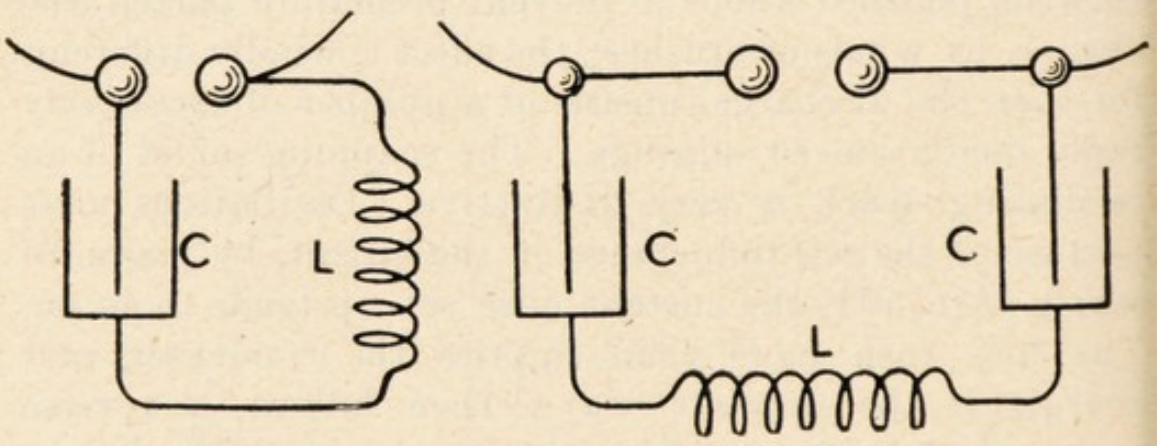


FIG. 357.—Arrangements of Oscillatory Circuits (Lodge).

That a discharge under certain conditions will be oscillatory was noted by von Helmholtz. Lord Kelvin in 1853 predicted these conditions. If the capacity of the condenser is C (farads), the resistance of the circuit R (ohms), and its inductance L (henries), there will be oscillations if

$$R < \sqrt{4L/C};$$

and there will be no oscillations if

$$R > \sqrt{4L/C}.$$

In the former case the frequency n of the oscillations will be such that

$$2\pi n = \sqrt{\frac{1}{CL} - \frac{R^2}{4L^2}} = \sqrt{\frac{4L - CR^2}{4CL^2}}.$$

Example.—If $C = 0{\cdot}01$ microfarad, $L = 0{\cdot}00001$ henry, and $R = 0$, $n = 503{,}000$.

If R is small, n is nearly equal to $1 \div 2\pi\sqrt{CL}$.

The oscillations can be made slower by increasing either C or L. The oscillations of an ordinary Leyden jar discharge may last only from a ten-thousandth to a ten-millionth of a second. By using coils of well-insulated wire and large condensers, Lodge succeeded in slowing down the oscillations to 400 a second; the spark then emitting a musical note. Iron is found to retain its magnetic properties even for oscillations of the frequency of one million per second.

Feddersen in 1859 examined the spark of a Leyden jar by means of a rotating mirror, and found that instead of being a single instantaneous discharge, it exhibited definite fluctuations.[1] With very small resistances in the circuit, there was a true oscillation of the electricity backward and forward for a brief time. The period of the oscillations was found to be proportional to the square root of the capacity of the condenser. With a certain higher resistance the discharge became continuous, but not instantaneous. With a still higher resistance the discharge consisted of a series of partial intermittent discharges, following one another in the same direction. Such sparks when viewed in the rotating mirror showed a series of separate images at nearly equal distances apart.

[1] These electric oscillations were examined also by Schiller, Overbeck, Blaserna, and others, notably by Hertz (see Art. 605 below).

601. Electric Waves.—Though the increasing and dying away of currents, for example in cables, is sometimes loosely described as of "waves" of current, these phenomena are very different from those of true electric or electromagnetic *waves* propagated across space. In the case of true electric waves, portions of the energy of the current or discharge are thrown off from the conductor and do not return back to it, but go travelling on in space. If a current increases in strength the magnetic field around it also increases, the magnetic lines enlarging from the conductor outward, like the ripples on a pond. But as the current is decreased the magnetic lines all return back and close up upon the conductor; the energy of the magnetic field returns back into the system. But if for currents slowly waxing and waning we substitute electric oscillations of excessive rapidity, part of their energy radiates off into the surrounding medium as *electromagnetic waves*, and only part returns back. As will be presently set forth, these waves possess all the optical properties of light-waves, and can be reflected, refracted, polarized, etc. Such waves, when they fall upon suitable conducting circuits can in turn set up electric oscillations therein, the wave-energy being absorbed thereby and transformed into the energy of oscillating currents.

It is a fundamental part of the modern views of electric action that while an electric displacement (Art. 58) is being produced in a dielectric, the effect in surrounding space is the same as if there had been a conductive instead of an inductive transfer of electricity. Maxwell gave the name of **displacement-current** to the rate of change of the displacement. Experiment proves that displacement-currents, while they last, set up magnetic fields around them, just as convexion-currents (Art. 429) and conduction-currents do.

602. Resonating Circuits. Syntony. — The circumstance that when certain definite relations exist

between the capacity and inductance of a circuit and the frequency of the periodic currents, the choking reactions of these properties neutralize one another, has been already alluded to in Art. 529. And we have seen (Art. 600) that a circuit with a certain self-induction, capacity, and

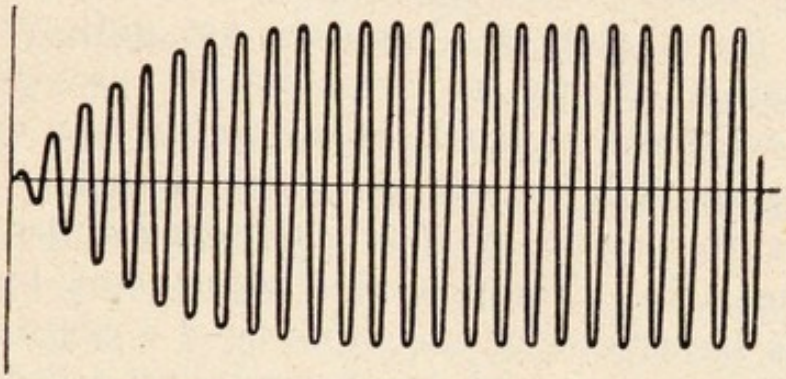


FIG. 358.—Electric Oscillations gradually built up.

resistance tends to oscillate electrically at a certain frequency. If it be placed in a medium through which electric waves of that frequency are passing in such a position that the electric and electromagnetic fields of the successive waves can induce currents in it, each wave will give a slight impulse to the readily excited oscillations, which will grow in intensity, just as small impulses given at the right times to a pendulum will make it swing violently. Fig. 358 illustrates the building-up action of these timed impulses.

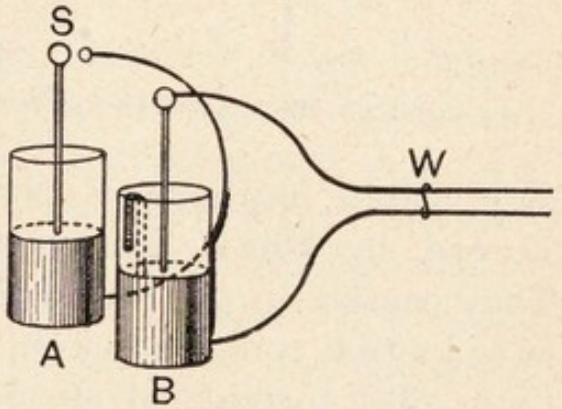


FIG. 359.—Lodge's Experiment on Resonance.

The following experiment of Sir Oliver Lodge beautifully illustrates this phenomenon of *resonance*, or *syntony*, and also illustrates the adjustment by tuning of an oscillatory circuit. Two Leyden jars, Fig. 359, are placed a little way apart from one another. One of them, charged from an influence machine (not shown), is

provided with a bent wire to serve as a discharging circuit, with a spark-gap S between the polished knobs at the top. The second jar is provided with a circuit of wire, the inductance of which can be adjusted by sliding in or out a cross-piece W hooked upon the other portions. A strip of tinfoil is brought up from the inner coating over the lip of this jar, but does not quite touch the outer coating. If the two circuits are properly tuned together, whenever a spark passes in the gap at the top of A, surgings will be set up in the circuit of B which will cause the jar to overflow, producing a spark at the end of the strip. The process of adjustment, by varying either the inductance or the capacity of a circuit, so as to bring it into syntony with another circuit is called **tuning**.

603. High-Frequency Apparatus.—Apparatus for generating oscillatory discharges of frequencies that

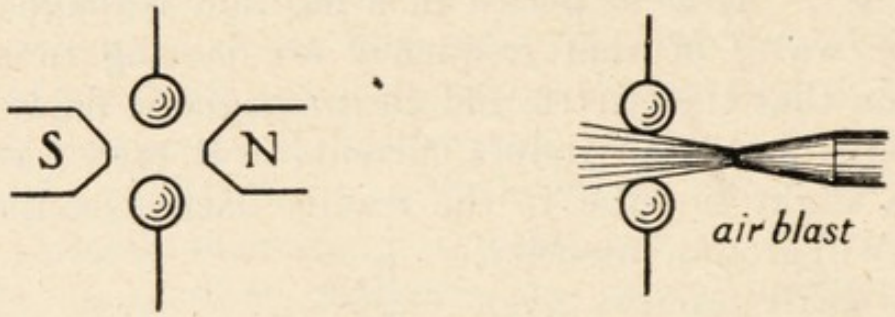


FIG. 360.—Devices for Sudden Extinction of Sparks.

may attain millions of periods per second have been devised by Elihu Thomson, Nikola Tesla, and others. They consist in general of devices for sending, by means of induction coils (Art. 246) or high-voltage transformers (Art. 538), torrents of sparks across a carefully arranged *spark-gap* between metal balls; arrangements being made to blow out the spark with great suddenness by the application of a magnetic field or of an air-blast (Fig. 360). Each of these sudden sparks, of which there may be from 2 or 3 up to 100 or so per second according to the devices adopted, sets up high-frequency oscillations in a special oscillating circuit containing capacity and

inductance; and it is usual to pass these oscillations through the primary circuit of an oscillation-transformer in the secondary of which a corresponding set of oscillations is induced at a very high voltage. The *oscillation-transformer*, commonly called a *Tesla coil*, has no iron core; its coils have comparatively few turns; they must be highly insulated from one another, and are usually immersed in oil. They are often provided with adjustable contacts to vary the number of turns in use; for it is highly advantageous to tune together these two circuits.

Fig. 361 is a generalized diagram of a Tesla or Elihu Thomson apparatus. G is an alternator, or other source such as a battery with a high-speed break (Art. 247),

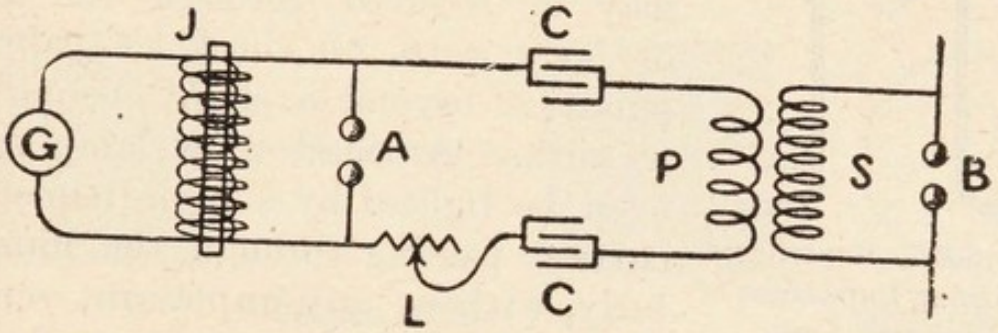


FIG. 361.—Circuit for producing High-Frequency Discharge.

supplying the primary of an ordinary high-voltage induction coil J (Art. 246). The secondary of the induction coil excites the spark in a spark-gap A (or in a pair of spark-gaps) in the oscillating circuit containing a condenser (or condensers) C. The oscillation-transformer PS couples together the oscillation circuit and the working circuit; there being provided an adjustable tuning coil or connexion L in one or both of these circuits. If a second spark-gap B is arranged in the working circuit, long sparks of high frequency may be observed.

These effects can be much augmented by increasing the suddenness of the spark by using a magnetic field (Art. 494) to blow it out. Elihu Thomson used an air-blast across the spark-gap for the same purpose.

High-frequency experiments of striking character can

be shown with such apparatus. If one of the terminals of the working circuit is put to earth a luminous discharge is seen to issue from the other terminal. If the terminals of the working circuit are connected together by an arched piece of stout copper wire, as in Fig. 362, and a small glow-lamp is connected across the arch, the lamp will glow, though apparently short-circuited: the impedance of the copper arch, owing to the skin-effect (Art. 532), will be greater than the resistance of the glow-lamp. The physiological effects of the high-frequency discharge are remarkable in that they are extraordinarily small. The long sparks may be received through the arm or body with no shock or painful sensation beyond a slight feeling of warmth. A small glow-lamp may even be lighted by a high-frequency current passing through the human body, without any unpleasant sensation. The luminous effects produced in vacuum tubes are varied and very brilliant.

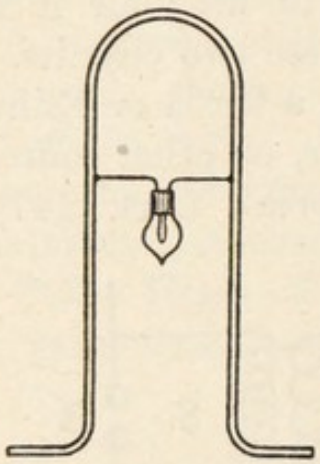


FIG. 362. — Experiment showing Impedance of Copper-wire Loop.

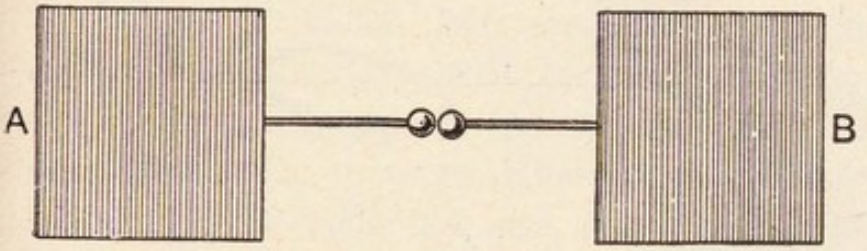
604. Frequency-Measurer.—A simple *frequency-measurer* for high-frequency oscillations may be made of a circuit containing an open-wound inductance coil of 40 or 50 turns of wire in series with an adjustable condenser and a minute glow-lamp or a thermal detector (Art. 479). Then the condenser is adjusted until the glow-lamp or detector indicates that resonance has been attained; and the frequency can be calculated by the formula of Art. 600, viz. $n = 1 \div 2\pi \sqrt{CL}$.

605. Researches of Hertz.—In 1888 Heinrich Hertz succeeded in producing electromagnetic waves in a way which permitted him to examine their propagation through space, and to show that, though invisible, they resembled ordinary waves of light. They possessed many of the same properties, travelled at the same speed,

and were capable of being reflected, refracted, polarized, etc.

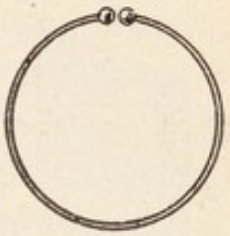
Of the power of oscillatory discharges to propagate disturbances in the surrounding space something was already known. Henry had shown that they set up other sparks in distant conducting circuits. It had been discovered [1] that a spark-gap in the exciting circuit was necessary. Fitzgerald had definitely proposed to start waves by the oscillatory discharges of small condensers. But no one had systematically followed out the phenomena of propagation of the waves.

Hertz employed to start the waves an apparatus called an **oscillator** (Fig. 363), consisting of two metallic con-



OSCILLATOR.

FIG. 363.



RESONATOR.

FIG. 364.

ductors (balls or plates) united by a metal rod, at the middle of which was interposed a spark-gap between two well-polished knobs. And to detect the waves at a distance he employed a *resonator*, simply a circle or square of wire, having in it a spark-gap capable of minute adjustment. In one experiment the *oscillator* consisted of two zinc plates A and B (Fig. 363) with sides 40 cm. long mounted 60 cm. apart, and having stout copper wires leading to a spark-gap between very brightly polished brass balls. A dry wood stand was a sufficient insulator. The **resonator** to match was a wire circle 35 cm. in radius, Fig. 364, or a wire square of 60 cm. sides. To experiment with this apparatus the oscillator

[1] See paper by the author in the *Philosophical Magazine* (September 1876).

is joined to a small induction-coil. When a spark snaps across the gap it sets up a temporary conducting path for the surgings that follow. For a rush of current from left to right overcharges the right-hand plate, and so there follows a rush back from right to left, and so on. Each spark sent by the coil across the gap consists of a dozen or so oscillations, each lasting about 1/100,000,000 of a second, the period being determined (Art. 600) by the capacity and inductance of the apparatus; the discharges surging backward and forward from A to B until they die out (Fig. 356). Let the line drawn horizontally in

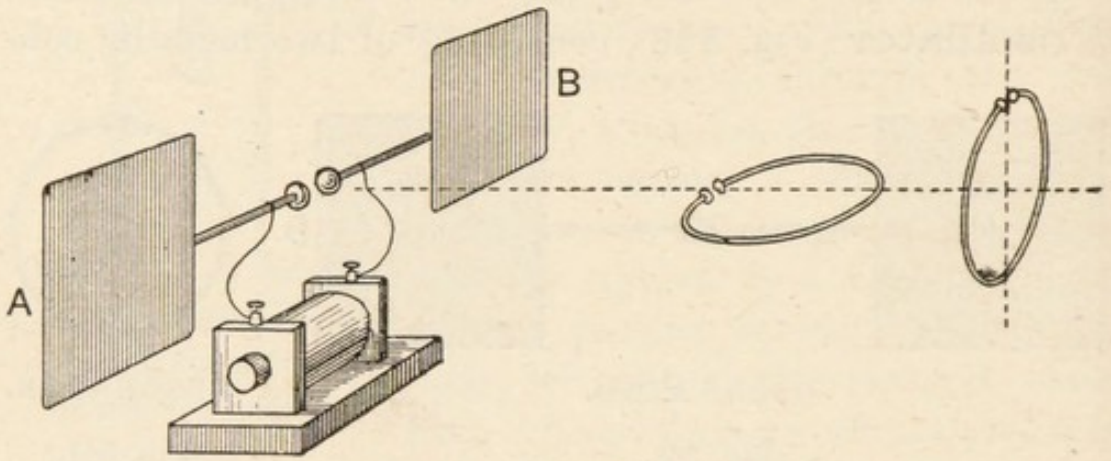


FIG. 365.—Hertz's Apparatus for Production and Detection of Electric Waves.

Fig. 365 be termed the *base line*, and let the line AB be termed the line of oscillation. Then if the resonator is placed with its centre on the base line at a few feet away from the oscillator and is turned into various positions, various effects are observed. If the resonator is set edge-on vertically, no sparks are observed in it whatever the situation of the gap in the circle. If it is laid edge-on horizontally sparks pass between the balls of the resonator. These are brightest when the gap-space is nearest toward the oscillator, so that the induced spark is parallel to the primary spark. If the resonator be now turned broadside on to the oscillator it will be found that there are sparks when the gap is at the top or

bottom of the circle—so that the sparks are parallel to the primary spark; but there are none if the gap is at the side. The primary spark does not here induce sparks at right angles to itself.

The *reflexion* of electric waves was observed in various ways. If right opposite the oscillator, Fig. 365, is set a large metal sheet as a reflector, to send back the waves that pass along the base line, stationary nodes will be produced at regular intervals. If the resonator is put broadside-on, with its gap at the highest point, and moved along the base line till it lies flat against the reflector, there will in this position be no sparks; but if it is slowly moved back from the sheet sparks will show, will come to a maximum, then die out as the first node is reached at about 180 cm. from the reflector. Passing this node the sparks will begin again, nodes occurring at equal intervals apart along the base line. By using large parabolic mirrors Hertz showed that these electric waves can be reflected and brought to a focus exactly as light-waves can be. Hertz also showed refraction with a prism of pitch; and polarization by means of gratings of parallel wires.

606. Detectors of Electric Waves.—The Hertz spark-gap resonator is only one means of detecting electric waves. A prepared frog's leg (Art. 271) may be used instead of a spark-gap. A sensitive vacuum-tube, especially if primed by application with a battery of some hundreds of small cells not quite able of themselves to start a spark, forms a good explorer. Electrometers; thin wires capable of expanding when heated by the induced currents; and galvanometers in parallel with the minute air-gap in the resonator, are amongst the possible means. Branly in 1890 found metallic powders to be sensitive. A good form is a tube partly filled with metallic filings, Fig. 366, inserted in circuit with a galvanometer and a single cell. The resistance of the filings is very great, and little current flows, until an

electric wave impinges upon the tube, when at once the filings conduct (compare Art. 432 on conductance of powders). On lightly tapping the tube the filings fall

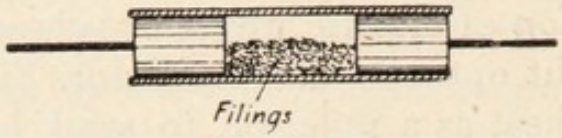


FIG. 366.—Filings Coherer.

back into their former state. Using such a detector, called a **coherer**, and an oscillator consisting of a highly polished brass ball between two smaller balls, Lodge in 1894 publicly showed how these electric waves can pass hundreds of feet through walls and floors of houses and can convey wireless signals. This invention was the basis of so-called *wireless telegraphy*; the coherer current being used in turn to operate a telegraphic receiver (see Art. 582).

607. Properties of Electric Waves.—The universal equation connecting frequency n, wave-length λ, and velocity of propagation v is: $v = n\lambda$. Taking v (in air) as 3×10^{10} (cms. per sec.) as the velocity of light, and the measured length of the red waves (the longest visible) as 0·000076 cm., it follows that the frequency of oscillation of these must be no less than 395×10^{12} per second. The waves artificially produced by electric oscillations are of much lower frequency than these, and their wave-length proportionally longer. Their wave-length depends on the size of the apparatus used as oscillator, just as the note emitted by an iron cylinder when struck on its end depends on the length of the cylinder. The wave-length of waves emitted from an oscillator consisting of a wire with a small capacity at each end is twice the length of the wire. That of waves emitted from a sphere (Fig. 367) of diameter d is $2\pi d/\sqrt{3}$ or 3·6 d; but they die out after about 1 vibration. Righi suggested the form of oscillator having a principal spark-gap

between two large polished spheres, placed between two smaller spheres. If the oscillations are not to radiate away their energy too quickly,, the oscillator must not have so large a fraction of its charging surface exposed. Hertz's oscillator, Fig. 363, resembles a Leyden jar with its coatings opened out widely apart. If they were bent round to face one another they would act as an air-condenser of somewhat larger capacity. But such an oscillator would radiate less freely and would maintain a longer train of waves.

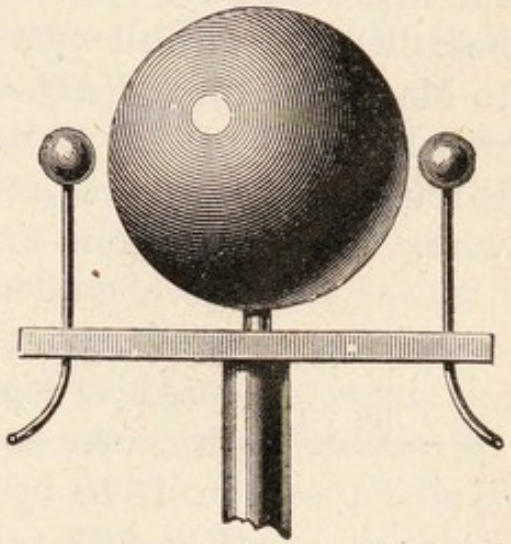


FIG. 367.—Lodge's Oscillator.

The currents produced in wires by oscillations of such enormous frequency are only skin-currents (Art. 532), the inner part of the wire being idle. Hence for such currents the impeding resistance of a stout copper wire may be millions of ohms. One evidence of this is afforded by the tendency to *lateral discharge*. This is readily shown by connecting between the Leyden jars of an influence machine a loop of stout copper wire bent as in Fig. 368. When a discharge takes place between the knobs, there will be an oscillatory current set up between the outer coatings also; and this oscillatory current rather than flow along the metal loop will jump as a spark across the parts that lie nearest together. The tendency of lightning to produce lateral discharges is relied upon by Lodge in his contention as to the oscillatory character of the flash (Art. 356).

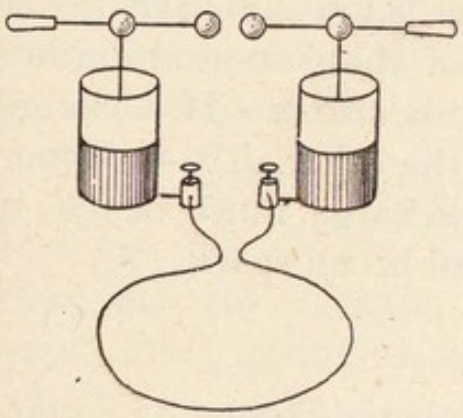


FIG. 368.—Experiment illustrating Impedance of Wire-Loop.

608. Travelling of Waves along Wires.—If an oscillatory spark is sent into one end of a long wire, by the time that the second pulsation reaches its maximum the first will have travelled a certain distance which may be called the wave-length of the disturbance. According to Maxwell's theory (Art. 609) the velocity of propagation will be equal to that of light, the energy really travelling through the air, and settling down laterally into the wire. It appears from experiment that the velocity of a wave guided by a wire is the same as that of a wave travelling in free air. That the speed of travelling is independent of the thickness or materials of the wire was proved in 1870 by Von Bezold using the device of Fig. 369. Let an oscillatory discharge be sent by a wire at G into a rectangular circuit ABCD, having a spark-gap PQ midway between B and D. It is evident that if G is midway between A and C the impulses will arrive simultaneously at P and Q if both sides of the system are alike; and there will be no spark. If now one side, say CD, be made of iron and the other, AB, of copper, it will be found that still the discharge must be led in at G, exactly midway if there is to be no spark.

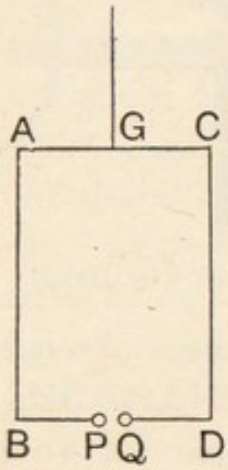


FIG. 369.—Von Bezold's Experiment.

LESSON LIX.—*The Electromagnetic Theory of Light*

609. Maxwell's Theory.—In 1864 Clerk Maxwell put forward the theory that the waves of light are not mere mechanical motions of the ether, but that they are electrical undulations. These undulations are partly electrical and partly magnetic, oscillating electrical displacements being accompanied by oscillating magnetic fields at right angles to them, whilst the direction of propagation of the wave is at right angles to both.

According to this theory the phenomena of electromagnetism and the phenomena of light are all due to certain modes of motion in the ether, electric currents and magnets being due to streams and whirls or other bodily movements in the substance[1] of the ether, while light is due to vibrations to and fro in it.

An electric displacement during its growth or decay produces a magnetic force at right angles to itself; it also produces (by the peculiar action known as induction) an electric force which is propagated at right angles both to the electric displacement and to the magnetic force. Now it is known that in the propagation of light the actual displacements or vibrations which constitute the so-called ray of light are executed in directions at right angles to the direction of propagation. This analogy is an important point in the theory, and immediately suggests the question whether the respective rates of propagation are the same. Now the velocity of propagation of electromagnetic induction is that velocity "v" which was shown (Art. 386) to represent the ratio between the electrostatic and the electromagnetic units, and which (in air) has been found to be

$$2{\cdot}999 \times 10^{10} \text{ centimetres per second.}$$

And the velocity of light (in air) has been repeatedly measured (by Fizeau, Cornu, Michelson, and others) (see p. 368), giving as the approximate value

$$2{\cdot}9986 \times 10^{10} \text{ centimetres per second.}$$

From the equations for the propagation of a disturbance in an electromagnetic medium, having dielectric coefficient k (Art. 315) and permeability μ (Art. 390), it was calculated by Maxwell that the velocity ought to be numerically $= 1 \sqrt{k\mu}$. And, as we have seen, this quantity enters into the ratio of the units (Art. 387), and

[1] Or, as we should now say, movements of the electrons in the ether; the ether itself being relatively at rest. See Art. 630

can be calculated from them. It follows that if there are two transparent media of equal permeability but different dielectric capacities, the velocities in them ought to vary relatively inversely as $\sqrt{k}$. But the ratio of the velocities of light in them is called their refractive index. Hence if Maxwell's theory is true, the dielectric capacity of ordinary transparent media ought to be equal to the square of the refractive index. Experiments by Gordon, Boltzmann, and others, show this to be approximately true for waves of great wave-length. The values are shown below. For gases the agreement is even closer.

	k.	Square of Index.
Flint Glass . .	3·162	2·796
Bisulphide of Carbon .	1·812	2·606
Sulphur (mean) . .	4·151	4·024
Paraffin . . .	2·32	2·33

Another consequence of the theory is that all conductors, since they dissipate the energy of the currents set up in them, ought to be *opaque* to light. Metallic conductors are so, except when in very thin films. But electrolytic liquids are not opaque, the mechanism of their conduction being different (Art. 569). In some crystalline bodies which conduct electricity better in one direction than in another, the opacity to light differs correspondingly. Coloured crystals of tourmaline conduct electricity better *across* the long axis of the crystal than *along* that axis. Such crystals are much more opaque to light passing *along* the axis than to light passing across it. And, in the case of rays traversing the crystal *across* the axis, the vibrations *across* the axis are more completely absorbed than those *parallel* to the axis: whence it follows that the transmitted light will be polarized.

Maxwell's theory was therefore considered in this

country as an established truth for some years before Hertz's striking researches of 1888 gave experimental proof of a direct kind.

610. Energy Paths. — From Maxwell's equations Poynting in 1883 drew the conclusion that in all cases where energy is transferred in an electric system it flows parallel to the surfaces of both electric and magnetic equipotentials. What we call an electric current along a wire is rather a transfer of energy by an invisible mechanism in the medium outside the wire. Wherever in the wire there is resistance, wasting energy by degrading it into heat, at that point energy flows in *laterally* from the medium. According to this view, the service of the wire is merely to guide the energy flow going on outside it.[1] We know that when a current is started much energy is spent in building up around the conductor a magnetic field, the amount spent being $\frac{1}{2} Li^2$ (Art. 501). When the circuit is "broken" this energy flows back laterally into the wire, giving rise to the so-called extra-current sparks. According to Poynting's view, which has been independently elaborated by Heaviside, all energy flows in similarly. In the case of the transfer of energy in an alternating-current transformer from the coils of the primary circuit to those of the secondary, it is pretty obvious that the flow of energy must take place *laterally* to the copper wires; and it also takes place laterally to the iron wires of the core, though this is not so obvious.

LESSON LX.—*Other Relations between Light and Electricity*

611. Electro-optical Phenomena.—Several important relations have been observed between electricity

[1] See particularly Sir Oliver Lodge's *Modern Views of Electricity.*

and light. These observations may be thus classified under the following heads :—

(i.) Production of double refraction by dielectric stress, and by magnetic stress.

(ii.) Rotation of plane of polarization of a wave of light on traversing a transparent medium placed in a magnetic field, or by reflexion at the surface of a magnet.

(iii.) Change in frequency of the light radiated (or absorbed) by atoms in a magnetic field.

(iv.) Change of electric resistance, exhibited by selenium and other bodies during exposure to light.

(v.) Photo-chemical excitation of electromotive-forces.

(vi.) Relation between refractive index and dielectric capacity of transparent bodies.

(vii.) Electric effect of ultra-violet light.

It was announced by Mrs. Somerville, by Zantedeschi, and others, that steel needles could be magnetized by exposing portions of them to the action of violet and ultra-violet rays of light ; the observations were, however, erroneous.

Bidwell found that light falling upon a recently demagnetized piece of iron produces an instantaneous revival of magnetism.

612. Electrostatic Optical Stress. — In 1875 Dr. Kerr of Glasgow discovered that glass when subjected to a severe electrostatic stress undergoes an actual strain, which can be observed by the aid of a beam of polarized light. In the original experiment two wires were fixed into holes drilled in a slab of glass, but not quite meeting, so that when these were placed in connexion with the terminals of an induction coil or of an influence machine the accumulating charges on the wires subjected the intervening dielectric to an electrostatic tension along the electric lines of force. The slab when placed between two Nicol prisms as polarizer and analyser[1] exhibited

[1] A ray of light is said to be *polarized* if the vibrations take place in one plane. Ordinary light can be reduced to this condition by passing it through a suitable polarizing apparatus (such as a Nicol prism, a thin slice of tourmaline crystal, etc.).

double refraction, as if it had been subjected to a pull and had expanded along the direction of the electric force. Bisulphide of carbon and other insulating liquids exhibit similar phenomena, but fatty oils of animal and vegetable origin exhibit an action in the negative direction, as if they had contracted along the electric lines. It is found that the difference of retardation between the ordinary and extraordinary waves per unit thickness of the dielectric *is proportional to the square of the resultant electric force.* The axis of double refraction is along the line of the electric force. Quincke has pointed out that these phenomena can be explained by the existence of electrostatic expansions and contractions, stated in Art. 320.

613. Magneto-optic Rotation of the Plane of Polarization of Light.—In 1845 Faraday discovered that a wave of light polarized in a certain plane can be twisted round by the action of a magnet, so that the vibrations are executed in a different plane. The plane in which a beam is polarized can be detected by observing it through a second Nicol prism (or tourmaline), for each such polarizer is opaque to waves polarized in a plane at right angles to that plane in which it would itself polarize light. Faraday caused a polarized beam to pass through a piece of a certain "heavy glass" (consisting chiefly of borate of lead), lying in a powerful magnetic field, between the poles of a large electromagnet, through the coils of which a current could be sent. In the path of the emerging beam was placed as analyser a second Nicol prism which had been turned round until all the light was extinguished. In this position its own plane of symmetry was at right angles to the plane of polarization of the beam. On completing the circuit, light was at once seen through the analysing Nicol prism, proving that the waves had been twisted round into a new position, in which the plane of polarization was no longer at right angles to the plane of symmetry of the analyser. But if the

analysing Nicol prism was itself turned round, a new position could be found (at right angles to the plane of polarization of the waves) at which the light was once more extinguished. *The direction of the magneto-optic rotation of the plane of polarization is the same* (for *diamagnetic* media) *as that in which the current flows which produces the magnetism.* Verdet discovered the important law that, with a given material, *the amount of rotation is proportional to the strength of the magnetic field* $\mathcal{H}$. In case the waves do not pass straight along the direction of the field, the amount of rotation is proportional *to the cosine of the angle* β *between the direction of the beam and the lines of force.* It is also proportional *to the length* l *of the material through which the waves pass.* These laws are combined in the equation for the rotation : $\theta = w\mathcal{H}\cos\beta l$; where w is a coefficient which represents the specific magnetic rotatory power of the given substance, and is known as *Verdet's constant.* Now, $\mathcal{H}\cos\beta l$ is the difference of magnetic potential between the point A where the wave enters and B where it leaves the medium. Hence $w = \theta \div (V_B - V_A)$.

The value of Verdet's constant for yellow sodium light, at 18° C., has been carefully determined. Its value (in radians per unit fall of magnetic potential) is, in bisulphide of carbon $1{\cdot}222 \times 10^{-5}$; in water $0{\cdot}375 \times 10^{-5}$; in heavy glass $2{\cdot}132 \times 10^{-5}$. For diamagnetic substances the coefficient is usually positive ; but in the case of many magnetic substances, such as solutions of ferric chloride, has a negative value (*i.e.* in these substances the rotation is in the opposite direction to that in which the magnetizing current flows). For light of different colours the rotation is not equal, but varies very nearly inversely as the square of the wave-length.

Gases also rotate the plane of polarization of light in a magnetic field with varying amounts ; coal-gas and carbonic acid being more effective than air or hydrogen ; oxygen and ozone being negative. The rotation is in all

cases very slight, and varies for any gas in proportion to the quantity of gas traversed. Henri Becquerel showed that the plane of the natural polarization of the sky does not coincide with the plane of the sun, but is rotated by the influence of the earth's magnetism through an angle which, however, only reached 59′ of arc at a maximum on the magnetic meridian.

We have seen (Arts. 127, 429, and 430) what evidence there is for thinking that magnetism is a phenomenon of rotation, there being a rotation of *something* around an axis lying in the direction of the magnetization. Such a theory would explain the rotation of the plane of polarization of a ray passing through a magnetic field. For a ray of plane-polarized light may be conceived of as consisting of a pair of (oppositely) circularly-polarized waves, in which the right-handed rotation in one ray is periodically counteracted by an equal left-handed rotation in the other ray; and if such a motion were imparted to a medium in which there were superposed a rotation (such as we conceive to take place in every magnetic field) about the same direction, one of these circularly-polarized rays would be accelerated and the other retarded, so that, when they were again compounded into a single plane-polarized ray, this plane would not coincide with the original plane of polarization, but would be apparently turned round through an angle proportional to the superposed rotation.

614. Kerr's Effect.—Dr. Kerr showed in 1877 that a ray of polarized light is also rotated when *reflected at the surface of a magnet* or electromagnet. When the light is reflected at a pole the plane of polarization is turned in a direction contrary to that in which the magnetizing current flows. If the light is reflected at a point on the side of the magnet it is found that when the plane of polarization is parallel to the plane of incidence the rotation is in the same direction as that of the magnetizing current; but that, when the plane of polarization is perpendicular to the plane of incidence, the rotation is in the same direction as that of the magnetizing current only when the incidence exceeds 75°, being in the opposite direction at lesser angles of incidence.

615. Kundt's Effect.—Kundt found that the plane of polarization of light-waves is also rotated if the light is passed through a film of iron so thin as to be transparent, if placed transversely in a magnetic field.

616. Zeeman Effect. — In 1896 P. Zeeman discovered that when a source of light is placed in a magnetic field the nature of the emitted light undergoes certain modifications. In the simplest case, when the light is that of an incandescent vapour, the spectrum of its rays consists of certain characteristic bright lines. But when the source of the light is magnetized the spectrum lines are split into two or three component lines so close together that a spectroscope of the highest resolving power is required to detect them. Examined in a direction parallel to the magnetic field are observed two lines; their light being circularly polarized in opposite directions. Examined in a direction normal to the field three components are observed; the light of the middle one being found to be polarized normally to the field, while the outer lines of the triplet are polarized in a plane parallel to the field. The dark lines in absorption spectra are similarly split. These phenomena can be interpreted in terms of the theory that the emission is due to the motions of electrons in the atom (Art. 637), as predicted by Lorentz.

617. Photo-electric Properties of Selenium.—In 1873 Willoughby Smith announced the discovery (by J. E. Mayhew) that the element *selenium* possesses the abnormal property of changing its electric resistance under the influence of light. Ordinary fused or vitreous selenium is a very bad conductor; its resistance being nearly forty-thousand-million ($3{\cdot}8 \times 10^{10}$) times as great as that of copper. When carefully annealed (by keeping for some hours at a temperature of about 220° C., just below its fusing point, and subsequent slow cooling) it assumes a crystalline condition, in which its electric resistance is considerably reduced. In the latter condi-

tion, especially, it is sensitive to light. Adams found that greenish-yellow rays were the most effective. He also showed that *the change of electric resistance varies directly as the square root of the illumination*, and that the resistance is less with a high electromotive-force than a low one. In 1879 Graham Bell and Sumner Tainter devised "selenium" cells, in which annealed selenium is formed into narrow strips between the edges of broad conducting plates of brass, thus securing both a reduction of the transverse resistance and a large amount of surface-exposure to light. Thus a cell, whose resistance in the dark was 300 ohms, when exposed to sunlight had a resistance of but 150 ohms. This property of selenium these investigators applied in the construction of the **Photophone,** an instrument which transmits sounds to a distance by means of a beam of light reflected to a distant spot from a thin mirror thrown into vibrations by the voice; the beam falling, consequently, with varying intensity upon a receiver of selenium connected in circuit with a small battery and a Bell telephone receiver (Art. 593) in which the sounds are reproduced by the variations of the current. Selenium cells have been used in the electric transmission of pictures.

Similar properties are possessed, to a smaller degree, by *tellurium*. Carbon is also sensitive to light.

618. Photo-chemical Cells.—About the middle of last century Edmond Becquerel showed that when two plates of silver, coated with freshly-deposited chloride of silver, are placed in a cell with water and connected with a galvanometer, a current is observed to pass when light falls upon one of the two plates, the exposed plate acting as an anode.

619. Photo-electric Loss of Charge.—In 1887 Hertz made the discovery that a spark starts more readily between the balls of a discharger when illuminated by light that is rich in violet and ultra-violet rays (magnesium light, arc light, or spark of induction

coil) than when not so illuminated. The effect varies with different metals, with their cleanness, the nature of the surrounding gas, with the kind of charge, and with the polarization of the light. In ultra-violet light freshly polished zinc in air rapidly discharges a negative charge, but not a positive one. On the other hand the peroxides, in an atmosphere of hydrogen, when so illuminated readily discharge positive charges. The effect is stronger when the plane of the vibration of the incident waves is at right angles to the surface than when the polarization is in a parallel plane. The phenomenon appears to be due to the short light-waves stimulating chemical reactions which do not occur except (Art. 345) by a species of electric exchange. In a strong magnetic field no such discharges occur. Hallwachs charged clean zinc plates positively by exposure to ultra-violet light. Elster and Geitel found that the most oxidizable and electropositive metals, rubidium, potassium, sodium, are also the most active photo-electrically, and discharge negative charges in ordinary daylight. Observations are best made in a vacuous bulb. If in such a tube there is introduced a second unilluminated metal plate, while a constant difference of potential is maintained between them, a current may be observed to pass from one plate to the other, the intensity of the photo-electric current increasing with the intensity of the illumination.

CHAPTER XVI

WIRELESS TELEGRAPHY

LESSON LXI.—*Radiotelegraphy and Radiotelephony*

620. Principles of Wireless Telegraphy.—We have seen (Art. 601) how Hertzian waves can be emitted from apparatus producing electric oscillations by the sudden disturbance by a spark passing an air-gap. An apparatus that thus emits electromagnetic waves is called a *radiator* or *sender*. These waves are conveyed by the ether in all directions at the speed of light. They can be detected at a distance, even through solid walls, by a suitable *detector*, working a galvanometer, or a sensitive telegraphic receiver, or a receiving telephone.

When these points are understood it is obvious that by sending off from the radiator successive flights of waves, by using a Morse key to make impulses of long or short duration, definite signals of the dash-and-dot alphabet of Morse can be transmitted. Such wireless transmission of signals is officially termed *radiotelegraphy*.

In 1894 Sir Oliver Lodge first publicly showed the wireless transmission of dots and dashes. His oscillator or sender was that shown in Fig. 357 : his receiver was a filings coherer resembling Fig. 366, provided with a tapper, acting to relay the impulses to an electric bell, or a galvanometer, or (later) to a siphon recorder. These

signals were sent from one building to another across intervening space and through stone walls.

In 1895 Sir Ernest Rutherford invented the magnetic detector depending on the influence of Hertz waves on the magnetic state of a newly magnetized wire of steel, and detected waves at over half a mile distance.

In 1896 Guglielmo Marconi, using a Righi oscillator (Art. 607) and a filings coherer (Art. 606), proposed to transmit signals by waves which he supposed to be new, but which turned out to be merely Hertz waves; and he suggested various details to render more certain the action of the apparatus; and in particular he introduced the employment of insulated elevated conductors as antennæ (Art. 621) at the sending and receiving stations. His system was not syntonic. In 1899, using the apparatus mentioned above, he succeeded in sending messages across the English Channel.

In 1900 a new method of using a telephone receiver in conjunction with a mercury and carbon coherer, so as to listen to short and long sounds corresponding to dots and dashes, was invented by Paolo Castelli, and this telephonic method of reception has largely superseded the telegraphic methods. In 1901, using Castelli's telephonic method, Marconi detected in Newfoundland signals sent from Cornwall, where he had erected a transmitting station with an alternator generating powerful spark discharges.

In 1897 Sir Oliver Lodge pointed out that for syntonic working it was necessary to employ transmitting apparatus that emits *trains* of waves, otherwise it is useless to try to tune the receiving apparatus into resonance with the sender; and he devised arrangements containing capacity and inductance to tune the circuits together. He also introduced the use of an oscillation-transformer (Art. 603) to intervene between the receiving capacity or area and the coherer.

By resort to such tuning devices, and organizing very

powerful transmitting stations, using many horse-power, Marconi has since been able to signal thousands of miles to distant lands, and he has established an excellent service between ships at sea.

621. Radiotelegraphic Transmitters. — In a modern "wireless" station the sending apparatus consists of an aerial system of wires stretched between elevated supports to form a "capacity area," from which conductors are led down, through a tuning inductance-coil and through the secondary of an oscillation-transformer (Art. 603), to the earth or to a network of conductors stretched over the ground. Electric oscillations are communicated to it by means of the primary coil to which it is directly

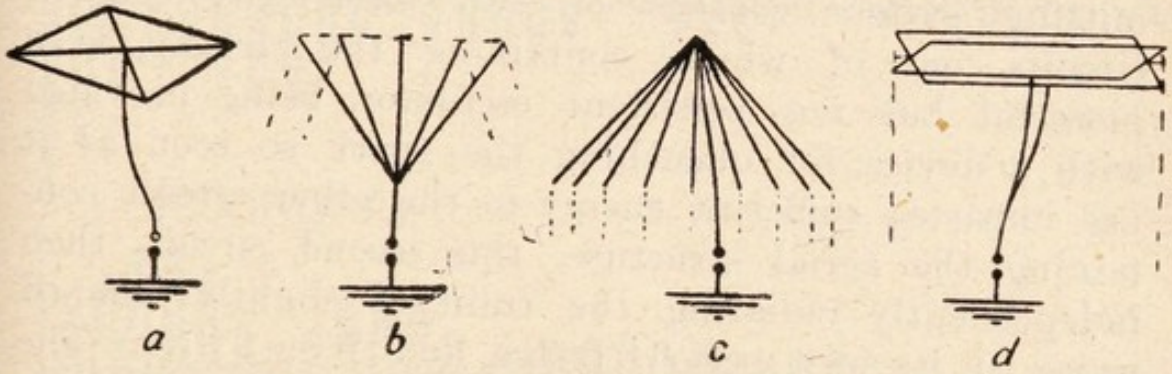


FIG. 370.—Various Forms of Aerial Structures for Radiotelegraphy.

or indirectly coupled; the primary being included in an oscillation-generating circuit of high frequency (Arts. 600 and 603), containing capacity and self-induction and a spark-gap or gaps across which sparks at high voltage are discharged by the agency of an ordinary transformer or induction-coil supplied from a suitable source of current. In small installations the source is a few cells of accumulators, where a town supply is not available. In the great radiotelegraphic stations power is specially generated by dynamos.

Some of the forms of aerial gear are depicted in Fig. 370, in which *a* is a capacity area suitable for stations of moderate size; *b* and *c* are forms of aerial covering many hundreds of square yards and supported on masts a

hundred or more feet high ; while *d* is a form suitable for small stations or for ships.

622. Arrangements of Transmitting Circuits.—There are four chief methods of arranging the transmitting circuits : (i.) The oscillating system, including the aerial structure with its associated inductance-coils and condensers, is designed to be both a sufficiently persistent oscillator and a sufficiently active radiator (Lodge). (ii.) The transmitting system consists of two tuned circuits such that the one containing the spark-gap is a persistent oscillator ; the other, containing the aerial structure, is a free radiator maintained in oscillation by being coupled to the first (Marconi). (iii.) The transmitting system consists of two electrically coupled circuits, one of which, containing the air-gap, is a powerful but not persistent oscillator, being provided with a device for quenching the spark so soon as it has imparted sufficient energy to the other circuit containing the aerial structure, this second circuit then independently radiating the train of slightly damped waves at its own period (Lodge and Wien). (iv.) The transmitting system, by means either of an oscillating arc (Poulsen) or a high-frequency alternator (Goldschmidt), emits a persistent train of undamped waves interrupted only by being broken up into long and short groups by the operator's key.

623. Coupling.—When an oscillation-transformer (Tesla-coil or jigger, Art. 603) is used to couple together two circuits, new complications are introduced respecting the frequency (Art. 600) of the oscillations ; these relations being affected by the tightness of the coupling (Art. 543). If the coupling between two circuits tuned to the same frequency is tight, then a phenomenon of periodic exchange of energy between the two circuits is observed, analogous to the mechanical exchange of energy between two tuned pendulums which alternately stop one another and start again. Fig. 371 illustrates the effect

which in each circuit resembles the acoustic "beats" of mistuned organ-pipes. In fact, in each circuit the oscillation-frequency f is resolved into two slightly differing frequencies, f_1 and f_2, which are related to one another by the expressions $f_1 = f \div \sqrt{1+c}$, and $f_2 = f \div \sqrt{1-c}$, where c is the coefficient of coupling (Art. 543). If the coupling be loosened by increasing the distance between the primary and secondary coils these

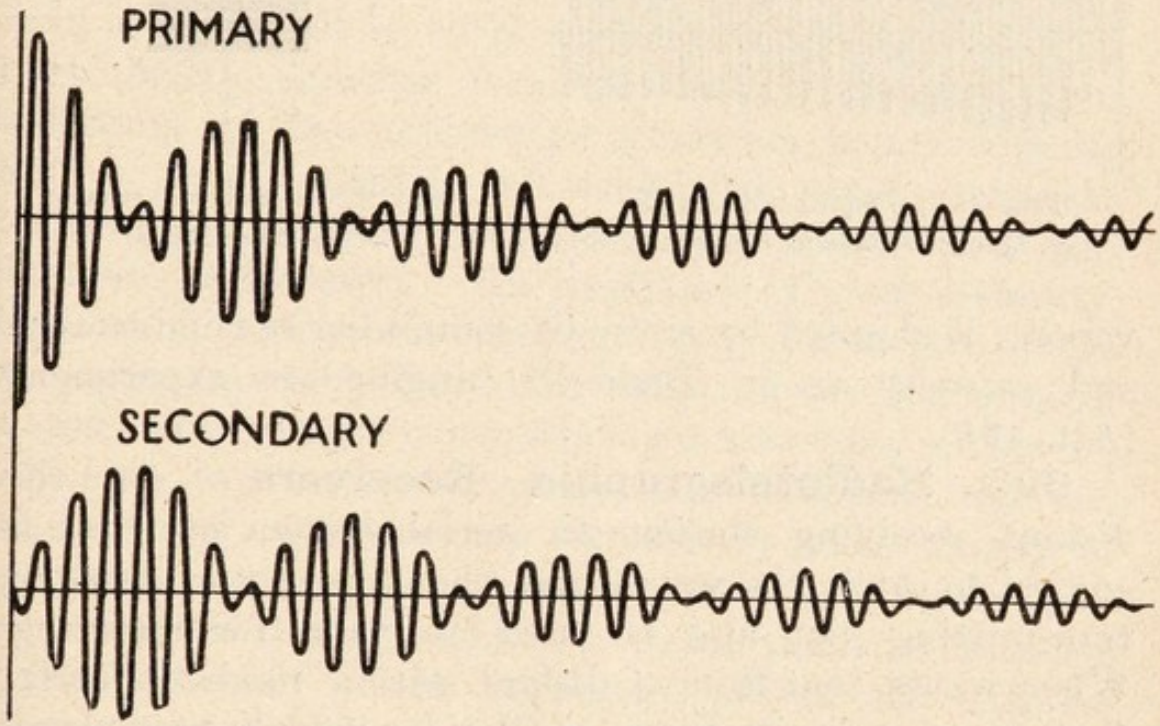


FIG. 371.—Oscillations in a Pair of Coupled Circuits.

interfering frequencies die out. For this reason, method (ii.) above is bad, unless the coupling is a loose one.

624. Quenched-Spark and Oscillating-Arc Systems. — In the quenched-spark system (iii.) no difficulty of this kind occurs, for the primary oscillations are quickly damped out, and only the secondary train of oscillations persists, as illustrated in Fig. 372. The apparatus for producing the quenched spark consists of a multiple spark-gap between a series of solid copper disks separated by very narrow parallel gaps, giving great cooling effect (Fig. 373).

In Poulsen's oscillating arc transmitter, the arc, formed between carbon electrodes, immersed in a hydrocarbon

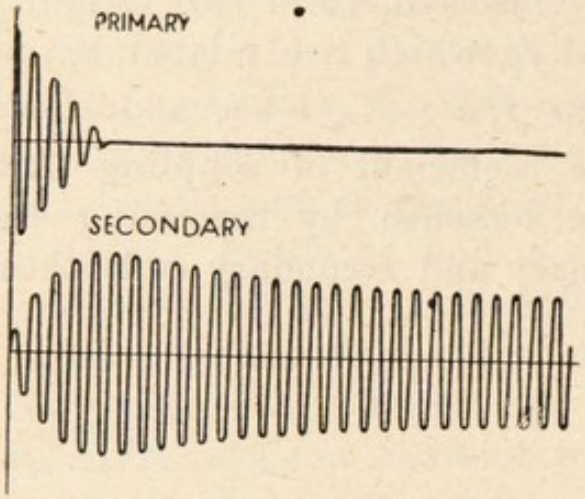


FIG. 372.—Oscillations in the Quenched-Spark System.



FIG. 373.—Multiple Spark-Gap Apparatus.

vapour, is shunted by a circuit containing self-inductance and capacity as in Duddell's singing-arc experiment (Art. 495).

625. Radiotelegraphic Receivers. — At the distant receiving station an aerial system of wires is erected to catch the waves, and the same aerial used for transmitting can also be used in turn for receiving. When waves sent from a distant station reach the aerial they set up in its wires oscillations which pass down through an oscillation-transformer by which they set up oscillations in a circuit containing or connected with a suitable detector. The detector in turn communicates the oscillations to the relay, or, in modern practice, to the receiving telephone. The circuits of the receiving station are tuned to those of the transmitting station, so that the receiving instruments shall be sensitive to waves of that particular frequency only at which the transmitter is emitting its waves, thus excluding as far as possible all waves from other stations. Tuning is not necessary for small installations, though it is always advisable.

626. Detectors.—The detector used in the first wireless transmission by Lodge was a *filings coherer*

(Fig. 366), and in this he was followed by Marconi, who reduced the quantity and improved the quality of the filings: but filings coherers are now obsolete. A much more certain but less sensitive appliance is Lodge's oil-wheel coherer, a small slowly revolving metal wheel the rim of which drags its way through a thin oil-film covering a small pool of mercury. When electric oscillations are led to the wheel they momentarily break down the resistance of the oil-film, and so permit the current from a single cell to effect a signal in a siphon recorder (Art. 589). Another form of detector is *electrolytic* consisting of two microscopic platinum points dipping into a small quantity of acidulated water. At the moment when electric oscillations are led into it its conductance is decreased. An appliance of great certainty, but not of great sensitiveness, is Marconi's variety of the *magnetic detector*, wherein the oscillations are led through a small electromagnet magnetizing a travelling steel wire, which in turn acts inductively on a telephone receiver. The *crystal detectors* now extensively used consist of morsels of zincite, galena, copper pyrites, carborundum, or other crystal against which a metal point or another crystal presses. These substances possess the singular property (Art. 432) of *unilateral conductivity*. When, therefore, oscillations are led through them they offer more resistance to impulses in one direction than to these in the other: hence they deliver in one direction a series of minute currents which affect a telephone receiver, so that the operator hears the dot-and-dash signals. The *thermo-electric cross* (Art. 479) can be used as a detector of oscillations in a similar way.

627. Sending and Receiving.—Arrangements for sending and receiving wireless messages are indicated in Fig. 374. At the sending station for small installations, using a battery E and an interrupter I (Art. 247), and an ordinary spark-coil J, the spark-gap A is in the circuit of the aerial, an inductance-coil L to reduce the

frequency of the oscillations being introduced between the spark-gap and the lower capacity area or earth; K is the operating key, and C a condenser shunting the interrupter. In large installations the precise arrangement of circuits used by Tesla (Fig. 361) may be employed; the aerial structure and the earth or lower capacity area

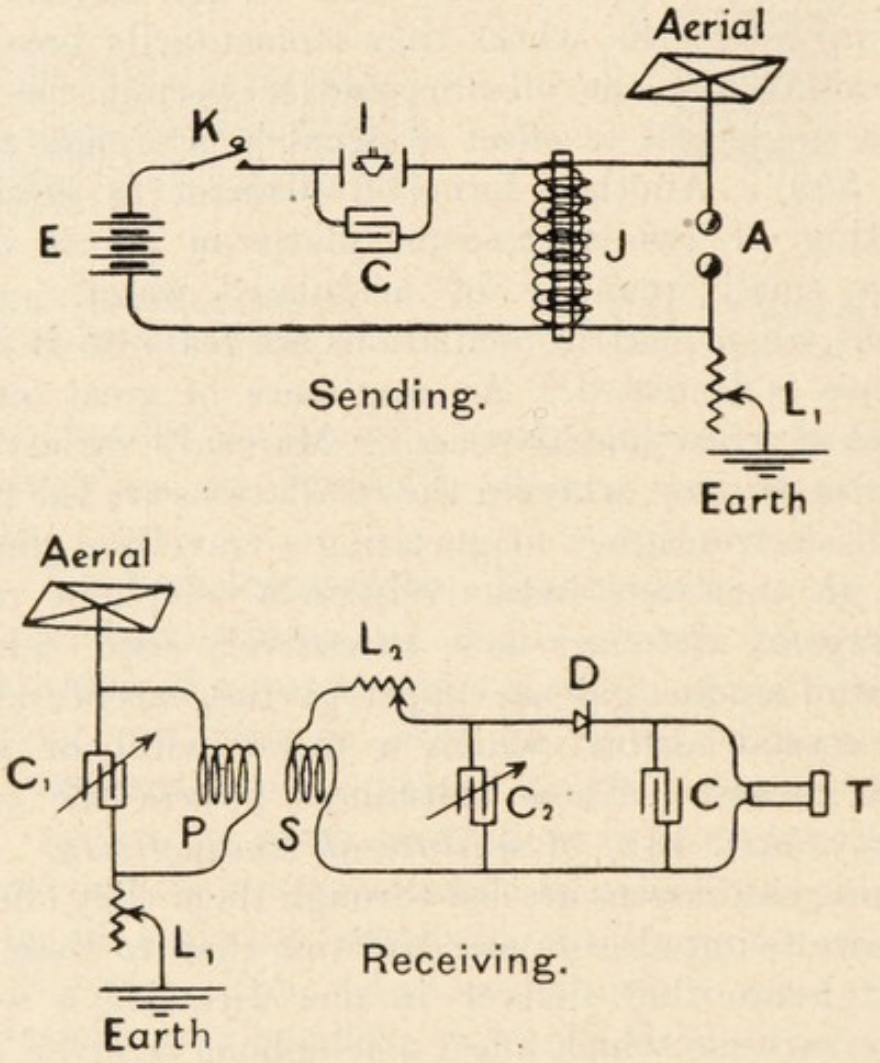


FIG. 374.—Tuned Circuits for Radiotelegraphy.

being respectively connected to the B terminals of that figure. At the receiving station C_1 and C_2 are adjustable condensers; P and S, the primary and secondary of an oscillation-transformer; L_1 and L_2 are tuning inductance-coils. D is the crystal detector, C a blocking condenser, and T the receiving telephone.

628. Wireless Telephony. — If transmitters of

class iv. (Art. 622) are employed, which emit continuous trains of waves with a frequency of 4000 or more periods per second, telephonic speech can be transmitted by substituting for the operating key a special microphone capable of carrying several amperes. The microphone carves the transmitted current (and therefore carves the train of emitted waves) into groups of amplitudes varying in correspondence with the sounds spoken into the microphone. The ordinary telephonic receiver, arranged as in Fig. 374, receives the messages.

629. Other Suggestions for Telegraphing without Wires. — Morse in 1842 and Lindsay in 1854 proposed to transmit signals through earth or water without direct communicating wires, by stray currents between two base lines, in one of which the battery and key were inserted, while the receiving instrument was inserted in the other. Preece proposed a system in which the magnetic field created by the current in an extended circuit induced currents in a second extended circuit at some distance from the first. Lodge improved this plan by tuning the circuits together. None of these proposals has proved hitherto of practical importance.

CHAPTER XVII

ELECTRON THEORY OF ELECTRICITY

LESSON LXII.—*Electrons and Ions*

630. The Electron.—It has been stated in various passages (Arts. 256, 343, and 570) in these Lessons that electricity apparently exists in discrete atomic quantities of a very minute but invariable magnitude. In electrolysis each individual ion is charged, according to its valency, with one, or two, or three such atomic charges. In the phenomena of discharge in the vacuum tube we find kathode "rays" which apparently consist of flights of electric particles or corpuscles travelling with enormous speeds. Their electricity is negative, and their respective charges are all equal. There is good evidence that the single atomic charge of a negative ion in electrolysis is identical with that of one of the kathodic corpuscles, and that no smaller quantity of electricity can exist.

The name *electron* was given by Johnstone Stoney in 1891 to the atomic quantum of electricity; the smallest quantity which can be transferred from one atom of matter to another; the smallest quantity of electricity that is capable of existing alone. The electron is negative; that is, it consists of negative electricity. If positive electricity is atomic at all, its atom is a quantity some thousands of times greater than the atomic quantity of negative electricity. While the electron can exist

either free, or in association with atoms or molecules of matter, the positive atom of electricity is unknown in the free state, and apparently exists only as combined or associated with atoms of matter.

The numerical estimates of the quantity of electricity in an electron vary, since different methods of determining the amount have yielded slightly differing results. These estimates at the present date are comprised between the following limits :—

$$\begin{cases} 1 \text{ electron} = 1{\cdot}03 \times 10^{-19} \text{ coulombs,} \\ 1 \text{ electron} = 1{\cdot}6 \times 10^{-19} \text{ coulombs.} \end{cases}$$

Or

$$\begin{cases} 1 \text{ coulomb} = 9{\cdot}7 \times 10^{18} \text{ electrons,} \\ 1 \text{ coulomb} = 6{\cdot}24 \times 10^{18} \text{ electrons.} \end{cases}$$

Since 1 coulomb (see Art. 381) equals 3×10^9 electrostatic C.G.S. units, the corresponding estimates may be expressed as—

$$\begin{cases} 1 \text{ electron} = 3{\cdot}1 \times 10^{-10} \text{ electrostatic C.G.S. units,} \\ 1 \text{ electron} = 4{\cdot}8 \times 10^{-10} \text{ electrostatic C.G.S. units.} \end{cases}$$

Electrons apparently possess mass (see Art. 639). The numerical estimates vary between the following limits :—

$$\begin{cases} \text{The mass of 1 electron} = 6{\cdot}1 \times 10^{-28} \text{ gramme,} \\ \text{The mass of 1 electron} = 7{\cdot}4 \times 10^{-28} \text{ gramme.} \end{cases}$$

The estimated size of the electron, assuming it to be spherical, is that its radius $= 1{\cdot}5 \times 10^{-13}$ centimetre.

Let us compare these figures with those of a hydrogen atom.

$$\begin{cases} \text{The mass of 1 hydrogen atom} = 1{\cdot}3 \times 10^{-24} \text{ gramme,} \\ \text{The mass of 1 hydrogen atom} = 1{\cdot}735 \times 10^{-24} \text{ gramme.} \end{cases}$$

The estimated size of the molecule of hydrogen, assuming it to be spherical, is that its radius $= 2{\cdot}17 \times 10^{-8}$ centimetre.

Comparing these values we see that an atom of

hydrogen (the lightest of known elements) is from 1756 to 2844 times as massive as an electron; and that the size of the molecule of hydrogen is some 140,000 times as great as that of an electron.

Electrons are therefore far smaller than any of the atoms of matter; and they differ from them in the respect that while all atoms of matter mutually attract one another by the universal law of gravitation, the electrons mutually repel one another: this repulsion of electrons being for equal distances enormously greater than the gravitational attraction between atoms.

631. The Ions of Electrolysis.—The ions concerned in electrolysis (see Arts. 255 and 571) are atoms or groups of atoms carrying electrons. A monovalent negative ion (an anion) is one which in being split off from a neutral molecule has one electron in excess; and by virtue of this negative charge moves, when subjected to an electric field, towards the anode. A monovalent positive ion (a kation) is one which in being split off from a neutral molecule has one electron too few to neutralize its positive electricity, and is therefore positive, and when subjected to an electric field moves towards the kathode. In an electrolytic cell there are two processions of ions travelling in opposite directions. When an anion such as a chlorine ion reaches a soluble anode such as zinc, it enters into combination with an equivalent portion of the zinc (two chlorine atoms to one zinc, since zinc is divalent) and gives its electron or electrons (in this case two) to the zinc. When a kation such as hydrogen reaches a kathode such as copper or platinum, it usually pairs off with another hydrogen ion to form a molecule, and takes up one electron from the kathode, thereby imparting an equal positive charge to the kathode. In all chemical combinations or decompositions each "bond" or "valency" corresponds to one electron. Electrons must be capable of individual existence at the moment when they are transferred from

the ions to the electrodes (or *vice versa*); hence they are regarded as continuing, as individuals, all through the circuit along which they move. A "current" of electricity is therefore regarded as a stream of electrons flowing along the conductor. Metal wires must therefore be regarded as permitting electrons to pass freely between their molecules.

The quantity of electricity in the ionic charge of a hydrogen atom may be reckoned as follows: According to the best estimates in the theory of gases a cubic centimetre of gas at normal pressure and temperature contains $2{\cdot}75 \times 10^{19}$ molecules, or $5{\cdot}5 \times 10^{19}$ atoms; hydrogen being a diatomic gas. Experiment shows that 1 litre of hydrogen (normal) weighs 0·08987 gramme: or 1 cubic centimetre of hydrogen weighs $8{\cdot}987 \times 10^{-5}$ grammes. If $5{\cdot}5 \times 10^{19}$ atoms weigh $8{\cdot}987 \times 10^{-5}$ grammes, it follows that 1 atom of hydrogen weighs $1{\cdot}64 \times 10^{-24}$ grammes. Experiment shows that to produce by electrolysis one gramme-equivalent, viz. 1·008 gramme of hydrogen, requires 96,550 coulombs (Art. 256). Hence to electrolyse 1 gramme of hydrogen requires 95,790 coulombs, so that the quantity of the ionic charge of 1 atom of hydrogen will be $95{,}790 \times 1{\cdot}64 \times 10^{-24} = 1{\cdot}57 \times 10^{-19}$ coulomb. The value of the *electron* so calculated may be compared with those stated above (Art. 630). It falls between the values there given.

632. Ionization.—In Art. 570 the view was stated that when a salt (or acid) is dissolved in water the solvent itself produces a more or less complete ionization of the salt. But ionization may be produced by other means, in gases, and even in solids. Any gas may be rendered conductive by an electric discharge passed through any part of the containing vessel. Flames contain ionized gases, as do the gaseous products of combustion. Hot bodies emit electrons and ionize the neighbouring air. At a dull red heat a metal ball (Art. 334) emits positive ions and can become negatively

charged, but at a white heat it emits electrons also and cannot be charged at all. Hot platinum wires emit electrons; and certain refractory oxides, lime, and baryta emit electrons copiously when heated white hot. In the newest form of Roentgen-ray tube, designed by Coolidge, the kathode is an incandescent flat spiral of tungsten wire. Light, especially ultra-violet light, falling on soft metals, causes them to throw off electrons. The Roentgen rays (Art. 352) striking on bodies causes them to emit electrons. The several rays given out by radium (Art. 638) are capable of ionizing bodies on which they fall, including air. Mere impact of bodies on one another causes ionization; for example, air near a waterfall is found to be ionized. Even ordinary air—probably as the result of exposure to light—is slightly ionized: for it is found impossible to keep an insulated conductor charged if exposed to the air. Its charge slowly disappears; a result formerly attributed to moisture or dust.

633. Conduction in Gases.—We may now apply some of these views to elucidate the conduction of electricity in gases. If a layer of gas is bounded by two parallel plates at a distance of l centimetres apart, between which there is maintained a difference of potential of V volts, the potential gradient between them is V/l volts per centimetre. Any ion in this electric field will be driven along this field in proportion to the gradient of the field and to the charge on the ion. There will therefore be a current between the plates proportional to the number of ions in the field. If, therefore, the gas is exposed to the action of any ionizing rays, it will conduct. But if the electric field is gradually increased in intensity, the current is found not to increase proportionally, but only up to a certain "saturation" value, because as the proportion of ions, positive and negative, present in the gas rises, they tend more and more to recombine, producing neutral atoms which do not act as carriers. It is possible actually to observe and

count the number of ions present in a given volume of gas. It was discovered by Mr. C. T. R. Wilson that ions serve as nuclei on which a droplet of aqueous vapour can condense. Hence if moist dustless air is used, and is suddenly cooled by release of pressure, the droplets formed on each ion are rendered visible and can be counted. This enabled Sir Joseph J. Thomson, in 1898, to make a first estimate of the value of the charge on the gaseous ion. He found it to be $2{\cdot}17 \times 10^{-19}$ coulombs for all gases and for all methods of ionizing. The value is now known to be too high, since some droplets contain more than one ion; a nearer value being $1{\cdot}03 \times 10^{-19}$. The ions in an ionized gas can be filtered off by passing the gas through cotton wool.

634. Electric Valves.—In Art. 351 it was pointed out that if funnel-like glass partitions are fixed in a vacuum tube, the discharge passes much more readily if the open mouths of the funnels face the kathode than is the case if the kathode is opposite the narrow orifice. Such an arrangement therefore acts as a sort of electric *valve* that allows a current to pass in one direction only, and can be used to rectify an alternating discharge. Also since a hot electrode of carbon or one covered with baryta (Art. 632) emits electrons copiously, it is possible to make a valve of a vacuum tube in which *one* of the electrodes is kept hot. Fleming's valve is of this nature. In Lodge's valve (Fig. 375) one electrode is an aluminium spiral presenting large surface, while the other is a small aluminium rod on a protected stem. They are placed in a glass bulb, but the small rod is withdrawn down a narrow elongation of the tube. If the electrons emitted by a kathode cannot reach the anode readily no

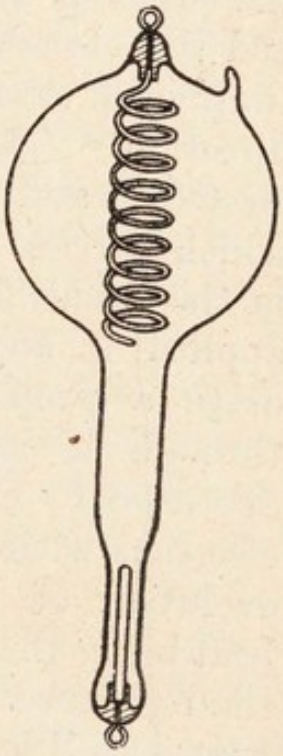


FIG. 375.—Lodge's Electric Valve.

appreciable current passes: so if the spiral is kathode it emits its electrons laterally, and they do not reach the disk, whereas if the disk is kathode it projects its electrons directly towards the spiral. Hence the unequal conductivity in the two directions. Mercury arc vacuum tubes (Art. 496) can also act as rectifiers or valves.

635. Conduction in Solids.—In metal conductors the carriers of electricity are supposed to be electrons, which move freely through the assemblages of molecules of which the conductors consist. This cannot be unless ionization in metals in their natural state is complete. No part of the conductance of a metal is due to positive atoms. A cubic centimetre of copper contains about $1{\cdot}25 \times 10^{24}$ atoms which are constantly exchanging electrons between themselves millions of times a second. Any electric force applied to a metal mass will tend to drive the electrons in the direction from negative to positive; and the electric flow in the ordinary positive current is simply an electronic current or procession in the other direction. One coulomb consists of about 8×10^{18} electrons, and one ampere is the electronic procession which carries that quantity of them past a given point in the circuit in one second. If the electromotive-force applied to any metallic conductor be increased it will drive a proportionately larger number of electrons through it in a given time: that is the fact really expressed by Ohm's law. The frequent collisions of the electrons with the metal atoms doubtless account for the evolution of heat in the conductor, the production of heat being the evidence (and the measure) of what we call the resistance. Moreover the conductance of metals for heat is well known to be greatest in those metals that are the best conductors of electricity; doubtless because both these phenomena are due to the motion of electrons. In the good conducting metals the ratio of their electric conductivity to their thermal conductivity is between 6 and 7 times 10^{10} (C.G.S. units). Also when a stream of

electrons flows across the junction surface between one metal and another, a change of their velocity takes place, evidencing itself by an absorption or evolution of heat; and this is the Peltier effect (Art. 472). If such a junction be heated, the metals will deliver their electrons to one another at different rates, thereby setting up an electromotive-force from one metal to the other; and this is the Seebeck effect (Art. 471).

636. Electrons in Dielectrics.—Bodies which do not conduct have no free ions, and no free electrons in them. Pure water does not sensibly conduct: there are no ions in it. Such dielectrics as glass, india-rubber, or paraffin consist of large complex molecules which imprison their electrons, so that they cannot conduct, nor dissolve in water, nor act chemically at ordinary temperatures. On the other hand a perfect vacuum does not conduct because there are no electrons in it to act as carriers. Suppose a plate of glass (a mixture of silicates of potassium, calcium, etc.) to be placed in an electric field between two charged tin foil plates, the electric forces will tend to electrolyse the molecules striving to separate them into kations and anions, tearing the electrons in the anodic direction, and driving the positive groups in the kathodic direction, and producing molecular strains. But there will be no transfer of electrons and discharges in the mass. When the electric stress is removed the strain is released. The only actual locomotions of electrons in these operations of charge and discharge will be as we know already (Art. 65) *at the surface*, or in the wires leading thereto. If a layer of air is substituted, exactly the same thing will occur, provided the air is not ionized.

But dielectrics can be pierced by a spark; and a spark while it lasts is a current. If the potential gradient at any point becomes great enough to tear a few electrons out of their molecules there begins a breakdown of the material: the disturbance spreads, volatilizing and ionizing some of the molecules, so that conduction along

a limited track is suddenly established, and the electrons rush through the disrupted channel evolving heat and light.

637. Magnetic Forces of Electrons in Motion. —Electrons moving are equivalent to a current, and therefore exercise magnetic forces. One ampere is a current in which the number of electrons passing per second is about 8×10^{18}. If a small electrified body carrying a charge e is travelling with velocity v, and is at a distance r from any specified point in space, the magnetic intensity $\mathcal{H}$ due to it at that point will be $ev \sin\theta/r^2$, where θ is the angle between the directions of v and r; and the direction of that intensity will be normal to the plane in which r and v are. If an electron is travelling around a circular orbit, it will act like a minute magnet.

Since a uniform magnetic field is the equivalent of a continuous procession of electrons in a cylindrical sheet around it, it follows by the principle of action and reaction that the operation of "cutting" a magnetic field by a moving conductor is the equivalent of starting a procession of electrons along that conductor, and the direction of that procession will reverse if the direction of the movement of the conductor is reversed.

Hence, around the line of motion a moving electron creates a magnetic field of circular lines, resembling Fig. 193. The generation of this field tends, by Lenz's law, to oppose the motion, and its collapse, after the electron has passed, tends to help the continuance of the motion. As long as the motion is uniform these effects balance one another; but they tend to oppose any change of speed, in fact tend to resist acceleration. This is a property precisely akin to inertia, the property in virtue of which mass resists acceleration. The apparent mass of an electron, as deduced from its motion, is about $6{\cdot}5 \times 10^{-28}$ grammes, and this is probably entirely electromagnetic.

If the velocity of an electron be altered then an

electromagnetic disturbance of the ether is emitted from it, depending on the acceleration. An electron in uniform revolution around an orbit should therefore emit periodic waves. If a flying electron crosses a magnetic field it is subject to a constant deflecting force at right angles to its path and to the direction of the field, and hence its path tends to become a circle.

638. Radio-activity and Electrons.—In 1896, shortly after the discovery of Roentgen's rays, M. Henri Becquerel and the author of this book independently discovered that some very similar rays capable of passing through black paper and of causing photographic action were emitted by certain fluorescent bodies, for example by the salts of uranium. Becquerel, after whom these rays are named, observed that metallic uranium was particularly active. Two years later Madame Curie found in uranium minerals a constituent more active than uranium itself, and succeeded in isolating this highly radio-active substance, which she named as *radium*. Other radio-active substances have since been found, amongst them thorium. Rutherford showed that radium emits three kinds of "rays," which can be separated by passing them through a strong magnetic field. They are also distinguished by their respective penetrating power, and differ in their properties. Fig. 376 is a diagram representing the action of a magnetic field, perpendicular to the plane of the figure, upon the rays emitted from a piece of radium placed in the bottom of a small lead cylinder. They are known as *alpha*, *beta*, and *gamma* rays respectively. The *Alpha* rays, which have small penetrating power, are slightly deflected in a direction which shows them to be positively

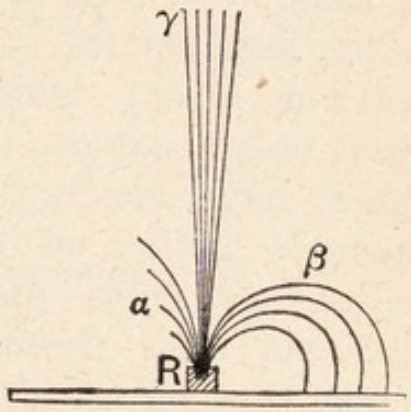


FIG. 376.—Emission of Three Kinds of Rays from Radium.

electrified, and they are now known to be atoms, moving comparatively slowly, and of the same nature as the "canal" rays (Art. 344). The *Beta* rays are corpuscular, negatively electrified, highly penetrative, and identical in nature with the kathode rays (Art. 344), being flights of electrons. The *Gamma* rays are not deflected by the magnet, are of exceedingly high penetrating power, highly ionizing, and are in fact identical in properties with Roentgen's rays (Art. 352). The alpha and beta rays can also be deflected in an electric field, while the gamma rays cannot be. The gamma rays travel with the speed of light; the beta rays at speeds differing among themselves, less than the speed of light, but down to about one-tenth as great; while the alpha particles travel at a speed only about one-twentieth as great. Rutherford and others have shown that the radio-active substances are unstable, giving off emanations and emitting atoms of helium (as alpha particles), and thus degenerating at different rates through a series of transformations in which they have different chemical properties. Radium is itself a product of the degeneration of uranium; and it appears finally to degenerate into an inactive product resembling lead. In Crookes's *spinthariscope* a minute speck of radium bromide shoots off alpha particles, each of which on hitting the surface of a phosphorescent screen produces a minute scintillation.

639. Ratio of Charge to Mass.—Probably the most important and best established magnitude in this complex subject is the ratio between the electric charge of an electron and its mass. This ratio was first ascertained in 1897 by Sir Joseph J. Thomson by a method which also determined the velocity with which they move. That method is known as the *method of crossed fields*. If a beam of kathode rays in a vacuum tube (Fig. 377) is sent between two adjacent parallel plates P and N, between which an electric field is established by connecting them with a battery of a large

number of cells, the beam will be deflected up or down according to the intensity of the electric force. If the intensity of the electric field be called X, then Xe will be the force exerted on the charge e. If now there be applied a magnetic field, of intensity $\mathcal{H}$, in a direction at right angles to the beam and at right angles to the direction of the electric field, there will be a magnetic force tending to deflect the beam down or up according to the polarity of the magnetic field. That force will be of the value $\mathcal{H}ev$, since ev is the equivalent of a current. By suitably adjusting the values of the fields these two forces may be made to balance one another so that the beam is undeviated, and then we have: $\mathcal{H}ev = eX$; or $v = X \div \mathcal{H}$.

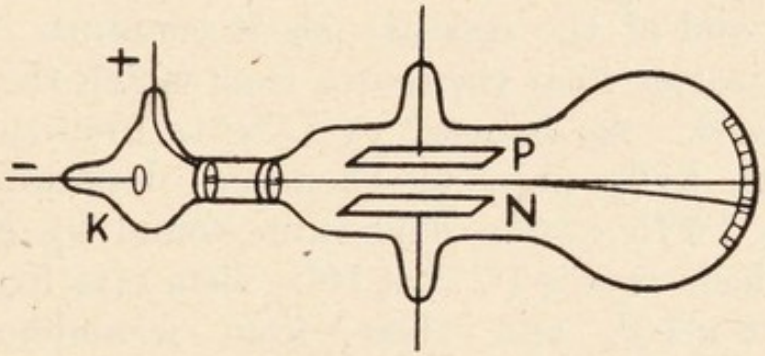


FIG. 377.—Experiment of the Crossed Fields.

Further, if the magnetic field be applied alone, and is a uniform field over a considerable area, the kathode beam will be bent into the arc of a circle, since the deflecting force at every point is at right angles to the line of flight of the electrons. The radius r of this curved path can be measured: it will be directly proportional to the velocity of the electron, and to its charge, and inversely proportional to the mass of the electron and to the intensity of the field, or: $r = \frac{ev}{m\mathcal{H}}$. It follows that $\frac{e}{m} = \frac{\mathcal{H}r}{v}$. In Sir Joseph J. Thomson's earliest experiments he found the velocity to be about one-tenth of that of light; while the value of $\frac{e}{m}$ he found to be, in these first

experiments, about $0{\cdot}9 \times 10^8$ coulombs per gramme. [Subsequent corrections for slow-moving electrons make the value $1{\cdot}77 \times 10^8$.] Now this number was at once seen to be about a thousand times greater than the number found (Art. 631 above) for the charged hydrogen ion as observed in electrolysis, viz. 95,790 coulombs per gramme. Hence the dilemma arose that either the electrons carried vastly bigger charges than the electrolytic hydrogen ions did, or else the electrons were bodies immensely smaller than the atoms of hydrogen. Thomson chose the latter alternative and announced the discovery of corpuscles at least a thousand times smaller than any known atom. The value of the ratio e/m is found to be independent of the metal of the electrodes of the kathode-ray tube, and of the residual gas it contains. It is the same, no matter what the source from which the electrons are obtained. As deduced by Lorentz from the Zeeman effect (Art. 616), prior to Thomson's determinations, it should be $1{\cdot}775 \times 10^8$. The value found by Kaufmann from kathode rays is $1{\cdot}772 \times 10^8$. Beta rays from radium give $1{\cdot}76 \times 10^8$, and those from incandescent lime $1{\cdot}771 \times 10^8$ coulombs per gramme.

Similar methods applied to the alpha particles have shown that for them e/m has a value of about $4{\cdot}7 \times 10^4$ coulombs per gramme. If the alpha particle is really a helium atom, since helium is divalent and has atomic weight 4, the value of its e/m should be half that of hydrogen, which is (Art. 631) 95,790; that is, it should be $4{\cdot}78 = 10^4$ coulombs per gramme. Their velocity is much slower than that of the beta particles.

640. Electronic Constitution of Atoms.—From the constancy of the ratio e/m for electrons from every source, it seems certain that electrons constitute a definite primordial substance. From the circumstance that the mass of the electron appears to be purely electromagnetic, it has been inferred that all mass is also electromagnetic; that all atoms are in fact aggregations

of electrons held together by a nucleus of something that may be vaguely called positive electricity, around which, or within which, the electrons are grouped in systems, probably revolving around in orbits, as in a sort of ultra-minute solar system. Sir Joseph J. Thomson has put forward many hypotheses as to such a possible constitution of the atoms of different elements, but they cannot be discussed here. Neither can the relation of the electron to the ether be here entered upon.

APPENDIX A—

θ in Degrees.	θ in Radians.	Sine θ.	Tangent θ.	Solid Angle $2\pi(1-\cos\theta)$.	Complement of $\theta=\phi$.
0°	0	0	0	0	90°
1	·0175	·0175	·0175	·000957	89
2	·0349	·0349	·0349	·003837	88
3	·0524	·0523	·0524	·00861	87
4	·0698	·0698	·0699	·01532	86
5	·0873	·0872	·0875	·02391	85
6	·1047	·1045	·1051	·03441	84
7	·1222	·1219	·1228	·04683	83
8	·1396	·1392	·1405	·06115	82
9	·1571	·1564	·1584	·07735	81
10	·1745	·1737	·1763	·09545	80
11	·1920	·1908	·1944	·1154	79
12	·2094	·2079	·2126	·1373	78
13	·2269	·2250	·2309	·1610	77
14	·2444	·2419	·2493	·1866	76
15	·2618	·2588	·2680	·2140	75
16	·2793	·2756	·2868	·2434	74
17	·2967	·2924	·3057	·2745	73
18	·3142	·3090	·3249	·3075	72
19	·3316	·3256	·3443	·3423	71
20	·3491	·3420	·3640	·3789	70
21	·3665	·3584	·3839	·4173	69
22	·3840	·3746	·4040	·4575	68
23	·4014	·3907	·4245	·4994	67
24	·4189	·4067	·4452	·5431	66
25	·4363	·4226	·4663	·5886	65
26	·4538	·4384	·4877	·6358	64
27	·4712	·4540	·5095	·6848	63
28	·4887	·4695	·5317	·7354	62
29	·5062	·4848	·5543	·7877	61
30	·5236	·5000	·5774	·8417	60
31	·5411	·5150	·6009	·8974	59
32	·5585	·5299	·6249	·9547	58
33	·5760	·5446	·6494	1·0136	57
34	·5934	·5592	·6745	1·0741	56
35	·6109	·5736	·7002	1·1362	55
36	·6283	·5878	·7265	1·1999	54
37	·6458	·6018	·7536	1·2652	53
38	·6632	·6157	·7813	1·3319	52
39	·6807	·6293	·8098	1·4002	51
40	·6981	·6428	·8391	1·4700	50
41	·7156	·6561	·8693	1·5412	49
42	·7330	·6691	·9004	1·6138	48
43	·7505	·6820	·9325	1·6879	47
44	·7679	·6947	·9657	1·7634	46
45	·7854	·7071	1·0000	1·8402	45
		Cosine ϕ	Cotangent ϕ	$2\pi(1-\sin\phi)$	ϕ in Degrees

ANGLES AND SOLID ANGLES

θ in Degrees.	θ in Radians.	Sine θ.	Tangent θ.	Solid Angle $2\pi(1-\cos\theta)$.	Complement of $\theta=\phi$.
45°	·7854	·7071	1·0000	1·8402	45°
46	·8029	·7193	1·0355	1·9185	44
47	·8203	·7314	1·0724	1·9980	43
48	·8378	·7431	1·1106	2·0789	42
49	·8552	·7547	1·1504	2·1610	41
50	·8727	·7660	1·1918	2·2444	40
51	·8901	·7772	1·2349	2·3290	39
52	·9076	·7880	1·2799	2·4149	38
53	·9250	·7986	1·3270	2·5019	37
54	·9425	·8090	1·3764	2·5900	36
55	·9599	·8192	1·4282	2·6793	35
56	·9774	·8290	1·4826	2·7696	34
57	·9948	·8387	1·5399	2·8611	33
58	1·0123	·8481	1·6003	2·9536	32
59	1·0298	·8572	1·6643	3·0472	31
60	1·0472	·8660	1·7321	3·1416	30
61	1·0647	·8746	1·8041	3·2370	29
62	1·0821	·8830	1 8807	3·3334	28
63	1·0996	·8910	1·9626	3·4307	27
64	1·1170	·8988	2·0503	3·5288	26
65	1·1345	·9063	2·1445	3·6278	25
66	1·1519	·9136	2·2460	3·7276	24
67	1·1694	·9205	2·3559	3·8281	23
68	1·1868	·9272	2·4751	3·9295	22
69	1·2043	·9336	2·6051	4·0315	21
70	1·2217	·9397	2·7475	4·1342	20
71	1·2392	·9455	2·9042	4·2376	19
72	1·2566	·9511	3·0777	4·3416	18
73	1·2741	·9563	3·2709	4·4462	17
74	1·2916	·9613	3·4874	4·5513	16
75	1·3090	·9659	3·7321	4·6570	15
76	1·3265	·9703	4·0108	4·7632	14
77	1·3439	·9744	4·3315	4·8698	13
78	1·3614	·9782	4·7046	4·9768	12
79	1·3788	·9816	5·1446	5·0843	11
80	1·3963	·9848	5·6713	5·1921	10
81	1·4137	·9877	6·3138	5·3003	9
82	1·4312	·9903	7·1154	5·4087	8
83	1·4486	·9926	8·1444	5·5174	7
84	1·4661	·9945	9·5144	5·6264	6
85	1·4835	·9962	11·4301	5·7356	5
86	1·5010	·9976	14·3007	5·8449	4
87	1·5184	·9986	19·0811	5·9543	3
88	1·5359	·9994	28·6363	6·0639	2
89	1·5534	·9999	57·2900	6·1735	1
90	1·5708	1·0000	∞	6·2832	0
		Cosine ϕ	Cotangent ϕ	$2\pi(1-\sin\phi)$	ϕ in Degrees

APPENDIX B

Order in Council legalising Denominations of Standards for the Measurement of Electricity as Board of Trade Standards

The 10th day of January 1910

Whereas by "The Weights and Measures Act, 1889," it is, among other things, enacted that the Board of Trade shall from time to time cause such new denominations of standards for the measurement of electricity as appear to them to be required for use in trade to be made and duly verified.

And whereas by Order in Council dated the 23rd day of August, 1894, Her late Majesty Queen Victoria, by virtue of the power vested in Her by the said Act, by and with the advice of Her Privy Council, was pleased to approve the several denominations of standards set forth in the Schedule thereto as new denominations of standards for electrical measurement.

And whereas in the said Schedule the limits of accuracy attainable in the use of the said denominations of standards are stated as follows:—

For the Ohm within one hundredth part of one per cent.

For the Ampere within one tenth part of one per cent.

For the Volt within one tenth part of one per cent.

And whereas, at an International Conference on Electrical Units and Standards held in London in the month of October, 1908, the International Electrical Units corresponding with the said denominations of standards were defined as follows:—

(1) The International Ohm is the resistance offered to an unvarying electric current by a column of mercury at the temperature of melting ice 14·4521 grammes in mass of a constant cross sectional area and of a length of 106·300 centimetres.

(2) The International Ampere is the unvarying electric current which when passed through a solution of nitrate of silver in water deposits silver at the rate of 0·00111800 of a gramme per second.

(3) The International Volt is the electrical pressure which when steadily applied to a conductor whose resistance is one International Ohm will produce a current of one International Ampere.

And whereas it has been made to appear to the Board of Trade to be desirable that the denominations of standards for the measurement of electricity should agree in value with the said International Electrical Units within the said limits of accuracy attainable.

And whereas the denominations of standards made and duly verified in 1894 and set forth in the Schedule to the said Order in Council have been again verified.

And whereas the Board of Trade are advised that the said denominations of standards agree in value with the said International electrical units within the said limits of accuracy attainable, except that in the case of the Ohm the temperature should be 16·4 C. in place of 15·4 C. as specified in the Schedule to the said Order in Council.

And whereas it has been made to appear to the Board of Trade that the said denominations of standards should be amended so that the aforesaid exception may be remedied.

Now, therefore, His Majesty, by virtue of the power vested in Him by the said Act, by and with the advice of His Privy Council, is pleased to revoke the said Order in Council dated the 23rd day of August, 1894, and is further pleased to approve the several denominations of standards set out in the Schedule hereto as denominations of standards for the measurement of electricity.

Schedule above referred to

I. Standard of Electrical Resistance

A standard of electrical resistance denominated one Ohm agreeing in value within the limits of accuracy aforesaid with that of the International Ohm and being the resistance between the copper terminals of the instrument marked "Board of Trade Ohm Standard Verified, 1894 and 1909," to the passage of an unvarying electrical current when the coil of insulated wire forming part of the aforesaid instrument and connected to the aforesaid terminals is in all parts at a temperature of 16·4 C.

II. Standard of Electrical Current

A standard of electrical current denominated one Ampere agreeing in value within the limits of accuracy aforesaid with that of the International Ampere and being the current which is passing in and through the coils of wire forming part of the instrument marked "Board of Trade Ampere Standard Verified, 1894 and 1909," when on reversing the current in the fixed coils the change in the forces acting upon the suspended coil in its sighted position is exactly balanced by the force exerted by Gravity in Westminster upon the iridioplatinum weight marked A and forming part of the said instrument.

III. Standard of Electrical Pressure

A standard of electrical pressure denominated one Volt agreeing in value within the limits of accuracy aforesaid with that of the International Volt and being one hundredth part of the pressure which when applied between the terminals forming part of the instrument marked "Board of Trade Volt Standard Verified, 1894 and 1909," causes that rotation of the suspended portion of the instrument which is exactly measured by the coincidence of the sighting wire with the image of the fiducial mark A before and after application of the pressure and with that of the fiducial mark B during the application of the pressure these images being produced by the suspended mirror and observed by means of the eyepiece.

In the use of the above standards the limits of accuracy attainable are as follows:—

For the Ohm, within one hundredth part of one per cent.
For the Ampere, within one tenth part of one per cent.
For the Volt, within one tenth part of one per cent.

The coils and instruments referred to in this Schedule are deposited at the Board of Trade Standardizing Laboratory, 8 Richmond Terrace, Whitehall, London.

PROBLEMS AND EXERCISES

QUESTIONS ON CHAPTER I

1. In what respects does an electrified body differ from a non-electrified body?

2. Name some of the different methods of producing electrification.

3. A body is charged so feebly that its electrification will not perceptibly move the leaves of a gold-leaf electroscope. Can you suggest any means of ascertaining whether the charge of the body is positive or negative?

4. How would you prove that the production of a positive charge is accompanied by the production of an *equal* negative charge.

5. Describe an experiment to prove that moistened thread conducts electricity better than dry thread.

6. Why do we regard the two electric charges produced simultaneously by rubbing two bodies together as being of opposite kinds?

7. Explain the action of the electrophorus. Can you suggest any means for accomplishing by a rotatory motion the operations of lifting up and down the cover of the instrument so as to obtain a continuous supply instead of an intermittent one?

8. Describe the state of the medium between two oppositely charged bodies, and state how you would determine the direction of the lines of force at any point.

9. Explain the Torsion Balance, and how it can be used to investigate the laws of the distribution of electricity.

10. Describe what takes place as an electrified conducting ball is made to approach a large conducting surface. Show by a diagram the direction and relative number of the lines of force.

11. Two small balls are charged respectively with +24 and −8 units of electricity. With what force will they attract one another when placed at a distance of 4 centimetres from one another? *Ans.* 12 *dynes.*

12. If these two balls are then made to touch for an instant and then put back in their former positions, with what force will they act on each other?

Ans. They will repel one another with a force of 4 *dynes.*

13. Enumerate the essential parts of an influence machine; and explain how they operate to produce electrification.

14. Take the diagrammatic representation of the Wimshurst machine (Fig. 39) and fill in the lines of electric force, showing their direction and relative number.

15. Explain the action of the Leyden jar by the consideration of electric displacement.

16. Describe four different ways of electrifying a tourmaline crystal.

17. Zinc filings are sifted through a sieve made of copper wire upon an insulated zinc plate joined by a wire to an electroscope. What will be observed?

18. Explain the principle of an *air-condenser*; and state why it is that the two oppositely charged plates show less signs of electrification when placed near together than when drawn apart from one another.

19. There are four Leyden jars A, B, C, and D, of which A, B, and D are of glass, C of guttapercha. A, B, and C are of the same size, D being just twice as tall and twice as wide as the others. A, C, and D are of the same thickness of material, but B is made of glass only half as thick as A or D. Compare their capacities.

Ans. Take capacity of A as 1; that of B will be 2; that of C will be $\frac{3}{4}$; and that of D will be 4.

20. How would you show that a bar made half of zinc and half of copper is capable of producing electrification?

21. How would you prove that there is no electrification within a closed conductor?

22. What prevents the charge of a body from escaping away at its surface?

23. Explain the action of Hamilton's mill (Fig. 34).

24. Two brass balls mounted on glass stems are placed half an inch apart. One of them is gradually charged by a machine until a spark passes between the two balls. State exactly what happened in the other brass ball and in the intervening air up to the moment of the appearance of the spark.

25. Define electric density. A charge of 248 units of electricity was imparted to a sphere of 4 centimetres radius. What is the density of the charge? *Ans.* 1·23 nearly.

QUESTIONS ON CHAPTER II

1. A dozen steel sewing-needles are hung in a bunch by threads through their eyes. How will they behave when hung over the pole of a strong magnet?

2. Explain the operation of an iron screen in protecting a galvanometer needle from magnets in its vicinity, and state why it is not perfectly effectual.

3. Of what material, and of what shape, would you make a magnet which is required to preserve its magnetism unaltered for a very long time? Describe the process of tempering.

4. What is meant by the resultant magnetic force at a point?

5. Six magnetized sewing-needles are thrust vertically through six little floats of cork, and are placed in a basin of water with their N-pointing poles upwards. How will they affect one another, and what will be the effect of holding over them the S-pointing pole of a magnet?

6. What distinction do you draw between magnets and magnetic matter?

7. On board an iron ship which is laying a submarine telegraph cable there is a galvanometer used for testing the continuity of the cable. It is necessary to screen the magnetized needle of the galvanometer from being affected by the magnetism of the ship. How can this be done?

8. How would you prove two magnets to be of equal strength?

9. The force which a small magnet-pole exerts upon another small magnet-pole decreases as you increase the distance between them. What is the exact law of the magnetic force, and how is it proved experimentally?

10. Describe the behaviour of Ewing's model of molecular magnetism in a magnetic field, and show how it corresponds with the behaviour of iron when magnetized. Divide the process of magnetizing into three successive stages.

11. What force does a magnet-pole, the strength of which is 9 units, exert upon a pole whose strength is 16 units placed 6 centimetres away? *Ans.* 4 *dynes.*

12. How would you place a long magnet so that one of its poles deflects a compass while the other does not affect it?

13. Distinguish between the "strength" of a magnet and its "magnetic moment."

14. Describe an instrument for comparing the relative values of magnetic forces. How would you use it to compare the magnetic moments of two magnets? If their distances from the magnetometer are respectively 20 centimetres and 30 centimetres, what is the ratio of their magnetic moments? *Ans.* 8 : 27.

15. Two magnets have the same pole strength, but one is twice as long as the other. The shorter is placed 20 centimetres from a magnetometer (using the "*end-on*" method); state at what distance the other must be placed in order that there may be no deflexion. *Ans.* 25·198 centimetres.

16. Show how the formula for the "*end-on*" magnetometer measurement is obtained, employing the law of inverse squares and remembering that the two poles exert opposite forces upon the needle, so that the force of the farther needle must be subtracted from that of the nearer one.

17. Show how the formula for the "*broadside-on*" method is obtained, employing the law of inverse squares and the parallelogram of forces. (*N.B.*—On constructing the correct diagram it will be observed that the actual force exerted by each pole acts along an oblique line. To obtain the force tending to turn the needle, the oblique force must be resolved into two components, one acting parallel to the axis of the magnet, and tending to turn the needle, and the other acting along the line joining the centres of the magnet and the needle. When the effects of the two poles are added together, the two

forces along the line joining the centres will be found to neutralize one another.)

18. A pole of strength 40 units acts with a force of 32 dynes upon another pole 5 centimetres away. What is the strength of that pole?

Ans. 20 units.

19. A magnet does work in attracting a piece of iron to itself. From whence comes the energy necessary to do this work? What changes are there in the energy stored in the magnet when the iron is once more pulled away?

20. A magnet 10 centimetres long produces on the needle of a magnetometer a deflexion of 45° when their centres are 50 centimetres apart, at a place where H = 0·18. Find the magnetic moment of the magnet, and the strength of its pole if it is in the end-on position.

Ans. $m = 1102{\cdot}6$ and moment = 11026.

21. Find the accurate value of the moment of a magnet when all the values are the same as stated in the previous example, except that the magnet occupies the *broadside-on* position.

Ans. = 22842.

22. Find the value of the moment of the magnet situated as in the previous question, using the approximate formula only, and express the resultant error as a percentage of the correct value.

Ans. moment = 22500; 1·5 per cent low.

23. In comparing together the magnetic moments of two magnets by means of a magnetometer, using the balance method, their respective distances (centre to centre) from the magnetometer needle were found to be 21 centimetres and 31·5 centimetres. What is the ratio of their magnetic moments?

Ans. = 8 : 27.

24. A thin bar magnet having a length of 10 centimetres and a pole-strength of 80 units is placed so that both its poles are 10 centimetres distant from the centre of a very short piece of magnetized watch-spring, of which the magnetic moment is 8. Find the torque experienced by the piece of watch-spring (*a*) when its axis of magnetization is at right angles to that of the bar-magnet; (*b*) when its axis of magnetization is parallel to that of the bar-magnet.

Ans. (*a*) 6·4 *dyne-centimetres*; (*b*) zero.

25. It is desired to compare the magnetic force at a point 10 centimetres from the pole of a magnet with the magnetic force at 5 centimetres' distance. Describe four ways of doing this.

26. Explain the phenomenon of Consequent Poles.

27. In what direction do the lines of magnetic force run in a plane in which there is a single magnetic pole? How would you arrange an experiment by which to test your answer?

28. A steel bar magnet suspended horizontally, and set to oscillate at Bristol, made 110 complete oscillations in five minutes; the same needle when set oscillating horizontally at St. Helena executed 112 complete oscillations in four minutes. Compare the horizontal component of the force of the earth's magnetism at Bristol with that at St. Helena.

Ans. H at Bristol : H at St. Helena : : 484 : 784.

29. Supposing the dip at Bristol to be 70° and that at St. Helena to be 30°, calculate from the data of the preceding question the total force of the earth's magnetism at St. Helena, that at Bristol being taken as 0·48 unit. *Ans.* 0·307.

30. A small magnetic needle was placed magnetically north of the middle point of a strong bar-magnet which lay (magnetically) east and west. When the magnet was 3 feet away from the needle the deflexion of the latter was 2°; when moved up to a distance of 2 feet the deflexion was 6° 30′; and when only 1 foot apart the deflexion was 43°. Deduce the law of the *total action* of one magnet on another.

31. Describe how the daily irregularities of the earth's magnetism are registered at different stations for comparison.

QUESTIONS ON CHAPTER III

1. Trace the successive increases and decreases of potential which go to make up the total electromotive-force of a battery of three similar voltaic cells, in series, starting from the zinc plate of the first cell, and supposing the plates to be immersed in a liquid which excites a potential of 2·364 volts in each zinc plate (when isolated) and a potential of 1·047 in each copper plate (when isolated).

2. Classify the different methods of preventing polarization in voltaic cells, and state the advantages and disadvantages of using a strong depolarizer, such as chromic acid.

3. On what does the internal resistance of a battery depend? Is there any way of diminishing it?

4. A current of 10 amperes flows for half an hour ; find the total quantity of electricity that passes. Also define the unit by which the quantity is measured. *Ans.* 18,000 *coulombs.*

5. State from what source the energy yielded by a voltaic cell is derived.

6. How is local action in a voltaic cell minimized ?

7. Twenty-four similar cells are grouped together in four rows of six cells each ; compare the electromotive-force and the resistance of the battery thus grouped, with the electromotive-force and the resistance of a single cell.

Ans. The E.M.F. of the battery is six times that of one cell. The total internal resistance is one and a half times that of one cell.

8. Describe a form of cell that could be used as a standard of E.M.F. State the essential qualities of such a cell.

9. A piece of silk-covered copper wire is coiled round the equator of a model terrestrial globe. Apply Ampère's rule to determine in which direction a current must be sent through the coil in order that the model globe may represent the condition of the earth magnetically.

Ans. The current must flow across the Atlantic from Africa to America, and across the Pacific from America toward India ; or, in other words, must flow always from east toward west.

10. A current of 0·24 ampere flows through a circular coil of seventy-two turns, the (average) diameter of the coils being 20 centimetres. What is the strength of the magnetic field which the current produces at the centre of the coil ?

Ans. 1·08.

11. Show the direction of the lines of force about a conductor carrying a current (1) when the conductor is straight ; (2) when it is bent into the form of a ring ; (3) when it is wound on a cylinder many times round. What do you mean by the direction of the lines of force ?

12. Suppose a current passing through the above coil produced a deflexion of 35° upon a small magnetic needle placed at its centre (the plane of the coils being in the magnetic meridian), at a place where the horizontal component of the earth's magnetic field is 0·23 unit. Calculate the strength of the current in amperes. (Art. 226.) *Ans.* 0·035.

13. The current generated by a dynamo-electric machine was passed through a large ring of stout copper wire, at the centre of which hung a small magnetic needle to serve as a tangent galvanometer. When the steam engine drove the armature of the generator at 450 revolutions per minute the deflexion of the needle was 60°. When the speed of the engine was increased so as to produce 900 revolutions per minute the deflexion was 74°. Compare the strength of the currents in the two cases.

Ans. The current was twice as great as before, for tan 74° is almost exactly double of tan 60°.

14. State a general law which will enable you to find the way in which the different parts of a magnetic system tend to move.

15. Deduce the law of the force on a magnetic pole due to a current flowing along a long straight conductor.

16. Describe four ways of controlling the needle of a galvanometer.

17. What is meant by a "null method" of observation?

18. Why is the needle of a tangent galvanometer made very short?

19. You are supplied with an ammeter and a voltmeter for the purpose of ascertaining the current supplied to an electrolytic bath, and the voltage at which it is supplied. Show in a diagram how you would join them up.

20. The current from two Grove's cells was passed through a sine-galvanometer to measure its strength. When the conducting wires were of stout copper wire the coils had to be turned through 70° before they stood parallel to the needle. But when long thin wires were used as conductors the coils only required to be turned through 9°. Compare the strength of the current in the first case with that in the second case when flowing through the thin wires which offered considerable resistance. *Ans.* Currents are as 1 to $\frac{1}{6}$, or as 6 to 1.

21. Suggest a way of using a tangent galvanometer as a sine-galvanometer, and describe an appropriate way of marking a scale for this purpose.

22. A plate of zinc and a plate of copper are respectively united by copper wires to the two terminals of a galvanometer. They were then dipped side by side into a glass containing dilute sulphuric acid. The galvanometer needle at first showed

a deflexion of 28°, but five minutes later the deflexion had fallen to 11°. How do you account for this falling off?

23. Classify liquids according to their manner and power of conducting electricity. In which class would molten pewter come?

24. Name the substances produced at the anode and kathode respectively during the electrolysis of the following substances:—*Water*, *dilute sulphuric acid*, *sulphate of copper* (dissolved in water), *hydrochloric acid* (strong), *iodide of potassium* (dissolved in water), *chloride of tin* (fused).

25. A current is sent through three electrolytic cells, the first containing acidulated water, the second sulphate of copper, the third contains a solution of silver in cyanide of potassium. How much copper will have been deposited in the second cell while 2·268 grammes of silver have been deposited in the third cell? And what *volume* of mixed gases will have been given off at the same time in the first cell?

Ans. 0·6837 gramme of copper and 361·5 cubic centimetres of mixed gases.

26. A current passes by platinum electrodes through three cells, the first containing a solution of blue vitriol (cupric sulphate), the second containing a solution of green vitriol (ferrous sulphate), the third containing a solution of ferric chloride. State the amounts of the different substances evolved at each electrode by the passage of 1000 coulombs of electricity.

Ans. First Cell { Anode 0·08292 gramme of oxygen gas. Kathode 0·3294 gramme of copper.
Second Cell { Anode 0·08292 gramme of oxygen. Kathode 0·2893 gramme of iron.
Third Cell { Anode 0·3675 gramme of chlorine. Kathode 0·1929 gramme of iron.

27. The ends of a coil of fine insulated wire are connected with the terminals of a galvanometer having a very light moving part which follows variations of current which are not excessively rapid. A steel bar magnet is pushed *slowly* into the hollow of the coil and then withdrawn suddenly. What actions will be observed on the moving part of the galvanometer? State and explain the differences which would be observed in these actions if the moving part of the galvanometer had a very slow periodic time of vibration and swung so freely that it took a considerable time to come to rest.

28. Round the outside of a deep cylindrical jar are coiled two separate pieces of fine silk-covered wire, each consisting of many turns. The ends of one coil are fastened to a battery, those of the other to a sensitive galvanometer. When an iron bar is poked into the jar a momentary current is observed in the galvanometer coils, and when it is drawn out another momentary current, but in an opposite direction, is observed. Explain these observations.

29. A casement window has a continuous iron frame. The aspect is north, the hinges being on the east side. What happens in the frame when the window is opened?

30. Explain the construction of the induction coil. What are the particular uses of the condenser, the automatic break, and the iron wire core?

31. It is desired to measure the strength of the field between the poles of an electromagnet which is excited by a current from a constant source. How could you apply Faraday's discovery of induction-currents to this purpose?

32. A small battery was joined in circuit with a coil of fine wire and a galvanometer, in which the circuit was found to produce a steady but small deflexion. An unmagnetized iron bar was now plunged into the hollow of the coil and then withdrawn. The galvanometer needle was observed to recede momentarily from its first position, then to return and to swing beyond it with a wider arc than before, and finally to settle down to its original deflexion. Explain these actions, and state what was the source of the energy that moved the needle.

33. A tangent galvanometer, whose "constant" in absolute units was 0·08, was joined in circuit with a battery and an electrolytic cell containing a solution of silver. The current was kept on for one hour; the deflexion observed at the beginning was 36°, but it fell steadily during the hour to 34°. Supposing the horizontal component of the earth's magnetic force to be 0·23, calculate the amount of silver deposited in the cell during the hour, the absolute electro-chemical equivalent of silver being 0·011183. *Ans.* 80·9 *grammes.*

34. A piece of zinc, at the lower end of which a piece of copper wire is fixed, is suspended in a glass jar containing a solution of acetate of lead. After a few hours a deposit of lead in a curious tree-like form ("Arbor Saturni") grows downwards from the copper wire. Explain this.

35. Explain the conditions under which electricity excites muscular contraction. How can the converse phenomenon of currents of electricity produced by muscular contraction be shown?

36. A current from 2 Grove cells in series is sent through a Daniell cell, entering it at the copper pole and leaving it at the zinc pole. Show that *in this case* the potential is higher at the zinc pole than at the copper pole. What becomes of the energy which the 2 Grove cells are supplying to the Daniell cell? (See Art. 264.)

37. Show that if $\mathfrak{F}$ magnetic lines are withdrawn from a circuit of resistance R, the quantity of electricity thereby transferred around the circuit (*i.e.* the time integral of the induced current) will be $Q = \mathfrak{F}/R$. (See Art. 243.)

38. The strength of the field between the poles of an electromagnet was determined by the following means:—A small circular coil, consisting of 40 turns of fine insulated wire, mounted on a handle, was connected to the terminals of a long-coil galvanometer having a heavy needle. On inverting this coil suddenly, at a place where the total intensity of the earth's magnetic force was 0·48 unit, a deflexion of 6° was shown as the first swing of the galvanometer needle. The sensitiveness of the galvanometer was then reduced to $\frac{1}{100}$ by the insertion of a resistance coil in the circuit. The little coil was introduced between the poles of the electromagnet and suddenly inverted, when the first swing of the galvanometer needle reached 40°. What was the strength of the field between the poles?

Ans. 315·7 units.

QUESTIONS ON CHAPTER IV

1. Define the *unit* of electricity as derived in absolute terms from the fundamental units of *length*, *mass*, and *time*.

2. At what distance must a small sphere charged with 28 units of electricity be placed from a second sphere charged with 56 units in order to repel the latter with a force of 32 dynes?

Ans. 7 *centimetres.*

3. Suppose the distance from the earth to the moon to be (in round numbers) 383×10^8 centimetres; and that the radius of the earth is 63×10^7 centimetres, and that of the moon 15×10^7 centimetres; and that both moon and earth are charged until the surface density on each of them is of the

average value of 10 units per square centimetre. Calculate the electrostatic repulsion between the moon and the earth.

4. A small sphere is electrified with 24 units of +electricity. Calculate the *force* with which it repels a unit of +electricity at distances of 1, 2, 3, 4, 5, 6, 8, and 10 centimetres respectively. Then plot out the "*curve of force*" to scale; measuring the respective distances along a line from left to right as so many centimetres from a fixed point as origin; then setting out as vertical ordinates the amounts you have calculated for the corresponding forces; lastly, connecting by a curved line the system of points thus found.

5. Define electrostatic (or electric) "*potential*"; and calculate (by the rule given in *italics* in Art. 281) the potential at a point A, which is at one corner of a square of 8 centimetres side, when at the other three corners B, C, D, taken in order, charges of +16, +34, and +24 units are respectively placed.

Ans. 8 (very nearly).

6. A small sphere is electrified with 24 units of +electricity. Calculate the *potential* due to this charge at points 1, 2, 3, 4, 5, 6, 8, and 10 centimetres' distance respectively. Then plot out the "*curve of potential*" to scale, as described in Question 4.

7. A small sphere charged with 100 units of electricity is dipped into a bath of oil having inductivity 2. Find the force it would exert on a unit charge 5 centimetres away.

Ans. 2 *dynes.*

8. Distinguish between the surface density at a point and the potential at that point due to neighbouring charges.

9. What are equipotential surfaces? Why is the surface of an insulated conductor an equipotential surface? Is it always so?

10. Show that the capacity of an isolated sphere in air of radius r has a capacity equal to r units. What is the electrostatic unit of capacity?

11. Why is the potential of the earth due to charges that we produce practically equal to zero?

12. A sphere whose *radius* is 14 centimetres is charged until the surface density has a value of 10. What *quantity* of electricity is required for this?

Ans. 24,640 units (nearly).

13. In the above question what will be the *potential* at the surface of the sphere? (See Art. 290.) *Ans.* 1760 (very nearly).

14. In the case of Question 12, what will be the *electric force* at a point outside the sphere and indefinitely near to its surface? (Art. 294.) *Ans.* 125·7 (very nearly).

15. Suppose a sphere whose radius is 10 centimetres to be charged with 6284 units of electricity, and that it is then caused to share its charge with a non-electrified sphere whose radius is 15 centimetres, what will the respective charges and surface-densities on the two spheres be when separated?

Ans. Small sphere, $q=2513{\cdot}6$, $\rho=2$.
Large sphere, $q=3770{\cdot}4$, $\rho=1{\cdot}33$.

16. A charge of +8 units is collected at a point 20 centimetres distant from the centre of a metallic sphere whose radius is 10 centimetres. It induces a negative electrification at the nearest side of the sphere. Find a point inside the sphere such that if 4 negative units were placed there they would exercise a potential on all external points exactly equal to that of the actual negative electrification. (See Art. 293.)

Ans. The point must be on the line between the outside positive charge and the centre of the sphere and at 5 centims. from the surface.

17. Two large parallel metal plates are charged both positively but unequally, the density at the surface of A being +6, that at the surface of B being +3. They are placed 2 centimetres apart. Find the force with which a +unit of electricity is urged from A towards B. Find also the work done by a +unit of electricity in passing from A to B.

Ans. Electric force from A towards B=18·85 *dynes*; work done by unit in passing from A to B=37·5 *ergs*.

18. What is meant by the *dimensions* of a physical quantity? Deduce from the Law of Inverse Squares the dimensions of the unit of electricity; and show by this means that electricity is not a quantity of the same physical dimensions as either *matter*, *energy*, or *force*.

19. Explain the construction and principles of action of the quadrant electrometer. How could this instrument be made self-recording?

20. Describe the construction of an electrostatic voltmeter, and state some of the advantages that this instrument possesses.

21. One of the two coatings of a condenser is put to earth, to the other coating a charge of 5400 units is imparted. It is found that the difference of potential thereby produced between the coatings is 15 (electrostatic) units. What was the capacity of the condenser? *Ans.* 360.

22. What is the meaning of *inductivity*? Why does hot glass *appear* to have a higher inductivity than cold glass?

23. Describe a method of mapping out the lines of force in an electrostatic field.

24. Two condensers of capacity 4 and 6 respectively are placed in parallel; and in series with them is placed another condenser having a capacity of 5 microfarads. Find the capacity of the whole combination. *Ans.* 3·3̇.

25. Compare the phenomenon of the residual charge in a Leyden jar with the phenomenon of polarization in an electrolytic cell.

26. A condenser was made of two flat square metal plates, the side of each of them being 35 centimetres. A sheet of indiarubber 0·4 centim. thick was placed between them as a dielectric. The inductivity of indiarubber being taken as 2·25, calculate the capacity of the condenser.
Ans. 548·8 *electrostatic units.*

27. Calculate (in electrostatic units) the capacity of a mile of telegraph cable, the core being a copper wire of 0·18 centim. diameter, surrounded by a sheathing of guttapercha 0·91 centim. thick. [k for guttapercha = 2·46; one mile = 160,933 centims.] *Ans.* 82,164 *units.*

28. A Leyden jar is made to share its charge with two other jars, each of which is equal to it in capacity. Compare the energy of the charge in one jar with the energy of the original charge. *Ans.* One ninth as great.

29. A series of Leyden jars of equal capacity is charged "in cascade." Compare the total *energy* of the charge of the individual jars thus charged with that of a single jar charged from the same source.

30. Classify the various modes of discharge, and state the conditions under which they occur.

31. Suppose a condenser, whose capacity is 10,000 charged to potential 14, to be partially discharged so that the potential fell to 5. Calculate the amount of heat produced by the discharge, on the supposition that all the energy of the spark is converted into heat. *Ans.* 0·020357 of a unit of heat.

32. How do changes of pressure affect the passage of electric sparks through air?

33. Describe some of the properties of matter in its ultra-gaseous or *radiant* state.

34. Why are telegraphic signals through a submerged cable retarded in transmission, and how can this retardation be obviated?

35. How is the difference of potential between the earth and the air above it measured? and what light do such measurements throw on the periodic variations in the electrical state of the atmosphere?

36. What explanation can be given of the phenomenon of a thunderstorm?

37. What are the essential features which a lightning-conductor must possess before it can be pronounced satisfactory? And what are the reasons for insisting on these points?

38. How can the duration of an electric spark be measured?

QUESTIONS ON CHAPTER V

1. Define *magnetic potential*, and find the (magnetic) potential due to a bar-magnet 10 centimetres long, and of strength 80, at a point lying in a line with the magnet poles and 6 centimetres distant from its N-seeking end. *Ans.* 8·3̇.

2. A N-seeking pole and a S-seeking pole, whose strengths are respectively +120 and −60, are in a plane at a distance of 6 centimetres apart. Find the point between them where the potential is =0; and through this point draw the curve of zero potential in the plane.

3. Define "intensity of the magnetic field." A magnet whose strength is 270 is placed in a uniform magnetic field whose intensity is 0·166̇. What are the forces which act upon its poles?
Ans. +45 *dynes* and −45 *dynes.*

4. Define "intensity of magnetization." A rectangular bar-magnet, whose length was 9 centimetres, was magnetized until the strength of its poles was 164. It was 2 centimetres broad and 0·5 centimetre thick. Supposing it to be uniformly magnetized throughout its length, what is the intensity of the magnetization? *Ans.* 164.

5. A certain bipolar electric motor has 100 conductors on its armature, each carrying 10 amperes. The number of lines of force passing through the armature is 500,000. Find the work (in ergs) done in one revolution of the armature.

As each conductor cuts the lines twice in one revolution the answer will be 100,000,000 *ergs.*

6. Find the torque (see Art. 518) on the armature described in the last question. Note that with the above data the torque is independent of the radius of the armature, for the force on each conductor is proportional to the strength of the field, and this is inversely proportional to the radius if $\mathfrak{F}$ remains the same. *Ans.* $\frac{100,000,000}{2\pi}$ *dyne-centimetres.*

7. A current whose strength in "absolute" electromagnetic units was equal to 0·05 traversed a wire ring of 2 centimetres radius. What was the strength of field at the centre of the ring. What was the potential at a point P opposite the middle of the ring and 4 centimetres distant from the circumference of the ring. *Ans.* $f = 0{\cdot}1571$; $V = \pm 0{\cdot}0421$.

8. (*a*) A spiral of wire of 1000 turns 80 centimetres long carries a current of 1 ampere. Find the strength of the magnetic field produced at the middle point of this coil.

Ans. $\mathfrak{H} = 15{\cdot}71$.

(*b*) If this spiral were 1 metre in length and 1 centimetre in diameter, find the force on a unit pole placed (1) in its centre ; (2) at its end. *Ans.* 12·57 *dynes* and 6·28 *dynes.*

9. What limits are there to the pull of an electromagnet?

10. What is the advantage in using an iron core in an electromagnet?

11. A rod of soft iron, 0·32 cm. in diameter and 1 metre long, is uniformly overwound from end to end with an insulated copper wire making 637 turns in one layer. Find (using Bidwell's data in Art. 392) what strength of poles this

rod will acquire when a current of 5 amperes is sent through the coil.

Ans. 98·5 *units.*

12. Enunciate Maxwell's rule concerning magnetic shells, and from it deduce the laws of parallel and oblique currents discovered by Ampère.

13. A circular copper dish is joined to the zinc pole of a small battery. Acidulated water is then poured into the dish, and a wire from the carbon pole of the battery dips into the liquid at the middle. A few scraps of cork are thrown in to render any movement of the liquid visible. What will occur when the N-seeking pole of a strong bar-magnet is held above the dish?

14. Roget hung up a spiral of copper wire so that the lower end *just* dipped into a cup of mercury. When a strong current was sent through the spiral it started a continuous dance, the lower end producing bright sparks as it dipped in and out of the mercury. Explain this experiment.

15. It is believed, though it has not yet been proved, that ozone is more strongly magnetic than oxygen. How could this be put to proof?

16. What is meant by the permeability of a substance? State some substances in which it is constant, and some in which it varies.

17. Describe a method of measuring the permeability of iron.

18. A ring of iron is wound with two coils. One coil is connected to a ballistic galvanometer, and on connecting the other to a battery a throw of the needle of 160 scale divisions is observed. The current is then broken and there is a throw of 40 divisions in the opposite direction. Why are the two throws not equal? What change has taken place in the iron? How would you bring it back to its original condition?

19. Sketch a closed hysteresis curve for hard steel, for which, when $\mathfrak{H}$ is raised to 100, $\mathfrak{B}=12{,}800$, and for which the remanence is $\mathfrak{B}=9500$ and the coercive force 40.

20. An iron bar 30 centimetres long and 10 square centimetres in sectional area is bent into the shape of a horseshoe for the purpose of making an electromagnet which shall have a pull of 66 kilograms upon its armature (a bar 12 centimetres long and 10 square centimetres in section) when it is $\frac{1}{2}$ inch

away from its poles. Find the number of ampere-turns required, assuming a leakage of one-third of the lines of force.

Taking the formula

$$\frac{\mathfrak{B}^2}{8\pi} \times 20 \text{ sq. cms. of pole face} = 66{,}000 \times 981 \text{ dynes},$$

we get $\mathfrak{B} = 9000$. From the table, Art 391, μ_1 for the armature $= 2250$, $\mathfrak{B}$ for the horseshoe $= 1{\cdot}5 \times 9000 = 13{,}500$, so that $\mu_2 = 900$, then ampere-turns =

$$90{,}000\left\{\frac{12}{10 \times 2250} + \frac{1{\cdot}5 \times 30}{10 \times 900} + \frac{2 \times 0{\cdot}5 \times 2{\cdot}54}{10}\right\} \div 1{\cdot}257 = 18{,}650.$$

21. What thickness of copper wire must be used to wind the above magnet in order to obtain 18,650 ampere-turns, the winding on each cylindrical bobbin having a mean diameter of 7 centimetres, if the pressure at the terminals of the magnet is intended to be 100 volts.

If r is the resistance of one turn, and s the number of turns, $r = \frac{E}{is} = \frac{100}{18{,}650}$; but we know that $r = \frac{7 \times \pi}{d^2 \times \frac{1}{4}\pi} \times 1{\cdot}6 \times 10^{-6}$.

Hence diameter of wire, $d = \sqrt{\frac{18{,}650 \times 7 \times 4 \times 1{\cdot}6}{10^6 \times 100}} = 0{\cdot}0914$ cm.

N.B.—The thickness of wire is independent of the number of turns (except in so far as this affects the mean diameter of the bobbin), but the greater the number of turns the less will be the number of watts expended.

22. What is the object of "polarizing" the armature of a magnet in a piece of mechanism, such as a relay?

23. Describe the construction of a current-balance, and the mode of using it.

QUESTIONS ON CHAPTER VI

1. The resistance of telegraph wire being taken as 13 *ohms* per mile, and the E.M.F. of a Leclanché cell as 1·4 *volt*, calculate how many cells are needed to send a current of 12 *milli-amperes* through a line 120 miles long; assuming that the instruments in circuit offer as much resistance as 20 miles of wire would do, and that the return current through *earth* meets with no appreciable resistance. *Ans.* 16 cells.

2. 50 Grove's cells (E.M.F. of a Grove = 1·8 *volt*) are united in series, and the circuit is completed by a wire whose resist-

ance is 15 *ohms*. Supposing the internal resistance of each cell to be 0·3 *ohm*, calculate the strength of the current.

Ans. 3 *amperes*.

3. The current running through an incandescent filament of carbon in a lamp was found to be exactly 1 *ampere*. The difference of potential between the two terminals of the lamp while the current was flowing was found to be 30 *volts*. What was the resistance of the filament?

4. Define resistivity. Taking the resistivity (Art. 435) of copper as 1·642, calculate the resistance of a kilometre of copper wire whose diameter is 1 millimetre. *Ans.* 20·9 *ohms*.

5. On measuring the resistance of a piece of No. 30 B.W.G. (covered) copper wire, 18·12 yards long, I found it to have a resistance of 3·02 *ohms*. Another coil of the same wire had a resistance of 22·65 *ohms*; what length of wire was there in the coil?

Ans. 135·9 yards.

6. Calculate the resistance at 0° Centigrade of a copper conductor one square centimetre in area of cross-section, and long enough to reach from Niagara to New York, reckoning this distance as 480 kilometres. *Ans.* 78·8 *ohms*.

7. Find the drop in *volts* if 400 *amperes* is passed through this conductor. What would be the waste of power (in *watts*)?

Ans. 31,520 *volts*, 12,608,000 *watts*.

8. The resistance from plate to plate in a certain electrolytic bath is 0·9 of an *ohm*. You wish to pass through it the strongest current you can get from 20 Daniell cells, each with a resistance of one *ohm*. How would you group the cells?

Ans. 4 in series, 5 rows in parallel.

9. The specific resistance of guttapercha being $3{\cdot}5 \times 10^{20}$, calculate the number of *coulombs* of electricity that would leak in one *century* through a sheet of guttapercha one centimetre thick and one metre square, whose faces were covered with tinfoil and joined respectively to the poles of a battery of 100 Daniell's cells. *Ans.* 9·7 *coulombs*.

10. Six Daniell's cells, for each of which $E = 1{\cdot}05$ *volt*, $r = 0{\cdot}5$ *ohm*, are joined in series. Three wires, X, Y, and Z, whose resistances are respectively 3, 30, and 300 ohms, can be inserted between the poles of the battery. Determine the current which flows when each wire is inserted separately;

also determine that which flows when they are all inserted at once in parallel. *Ans.* Through X 1·05 *ampere.*
Through Y 0·1909 ,,
Through Z 0·0207 ,,
Through all three 1·105 ,,

11. Calculate the number of cells required to produce a current of 50 *milli-amperes*, through a line 114 miles long, whose resistance is 12½ *ohms* per mile, the available cells of the battery having each an internal resistance of 1·5 *ohm*, and an E.M.F. of 1·5 *volt*. *Ans.* 50 cells.

12. You have 20 large Leclanché cells (E.M.F. = 1·5 *volt*, $r = 0{\cdot}5$ *ohm* each) in a circuit in which the external resistance is 10 *ohms*. Find the strength of current which flows (*a*) when the cells are joined in simple series; (*b*) when all the zincs are united, and all the carbons united, in parallel; (*c*) when the cells are arranged two abreast (*i.e.* in two files of ten cells each); (*d*) when the cells are arranged four abreast.
Ans. (*a*) 1·5; (*b*) 0·1496; (*c*) 1·2; (*d*) 0·702 *ampere.*

13. With the same battery how would you arrange the cells in order to telegraph through a line 100 miles long, reckoning the line resistance as 12½ *ohms* per mile?

14. Show that, if we have a battery of n given cells each of resistance r in a circuit where the external resistance is R, the strength of the current will be a maximum when the cells are coupled up in a certain number of rows equal numerically to $\sqrt{nr \div R}$.

15. Two wires, whose separate resistances are 28 and 24, are placed in parallel, in a circuit so that the current divides, part passing through one, part through the other. What resistance do they offer thus to the current?
Ans. 12·92 *ohms.*

16. Using a large bichromate cell of practically no internal resistance, a deflexion of 9° was obtained upon a tangent galvanometer (also of small resistance) through a wire whose resistance was known to be 435 *ohms*. The same cell gave a deflexion of 5° upon the same galvanometer when a wire of unknown resistance was substituted in the circuit. What was the unknown resistance? *Ans.* 790 *ohms.*

17. In a Wheatstone's bridge in which resistances of 10 and 100 *ohms* respectively were used as the fixed resistances, a wire whose resistance was to be determined was placed: its resistance was balanced when the adjustable coils were arranged to throw 281 *ohms* into circuit. What was its resistance?
Ans. 28·1 *ohms*

18. Describe the method of using a metre bridge to measure resistances.

19. Give the proof of Foster's method of measuring small differences of resistance, from the consideration of Ohm's law.

20. To find the voltage of a dynamo you connect to its brushes the ends of a German silver wire 120 feet long, wound on an insulating cylinder, and find that when one terminal of a Daniell cell (1·05 volt) is joined to a point on the wire, and the other terminal in series with a galvanometer is connected to another point 1 ft. from the first, no deflexion is observed. What is the voltage of the dynamo? *Ans.* 126 *volts.*

21. A battery of 5 Leclanché cells was connected in simple circuit with a galvanometer and a box of resistance coils. A deflexion of 39° having been obtained by adjustment of the resistances, it was found that the introduction of 150 additional *ohms* of resistance brought down the deflexion to 22°. Assuming the galvanometer to have 140 ohms resistance, find the internal resistance of the battery. *Ans.* 10 *ohms.*

22. How are standard resistance coils wound, and why? What materials are they made of, and why?

23. Three very small Daniell's cells gave, with a sine galvanometer (itself of no appreciable resistance), a reading of 57°. On throwing 20 ohms into the circuit the galvanometer reading fell to 25°. Calculate the internal resistance of the cells. *Ans.* 6·6 *ohms* each.

24. A length of telegraph cable was plunged in a tub of water and then charged for a minute from a battery of 120 Daniell's cells. The cable was then discharged through a long-coil galvanometer with a needle of slow swing. The first swing was 40°. A condenser whose capacity was $\frac{1}{3}$ *microfarad* was then similarly charged and discharged; but this time the first swing of the needle was only 14°. What was the capacity of the piece of cable? *Ans.* 0·934 *microfarad.*

25. Using an absolute electrometer, Lord Kelvin found the difference of potential between the poles of a Daniell's cell to be 0·00374 *electrostatic* unit (C.G.S. system). The ratio of the electrostatic to the electromagnetic unit of potential is given in Art. 386, being $=1/v$. The *volt* is defined as 10^8 electromagnetic units. From these data calculate the E.M.F. of a Daniell's cell in *volts.* *Ans.* 1·115 *volt.*

26. The radius of the earth is approximately 63×10^7 centimetres. The ratio of the electrostatic to the electromagnetic unit of capacity is given in Art. 386. The definition of the *farad* is given in Art. 381. Calculate the capacity of the earth (regarded as a sphere) in *microfarads*.

Ans. 700 *microfarads* (nearly).

27. The electromotive force of a Daniell's cell was determined by the following process :—Five newly prepared cells were set up in series with a tangent galvanometer, whose constants were found by measurement. The resistances of the circuit were also measured, and found to be in total 16·9 *ohms*. Knowing the resistance and the absolute strength of current the E.M.F. could be calculated. The deflexion obtained was 45°, the number of turns of wire in the coil 10, the average radius of the coils 11 centimetres, and the value of the horizontal component of the earth's magnetism at the place was 0·18 G.C.S. unit. Deduce the E.M.F. of a Daniell's cell.

Ans. $1{\cdot}0647 \times 10^8$ G.C.S. units, or 1·0647 *volt*.

28. Apply the formula of the ballistic galvanometer (Art. 451, *b*) to determine the number of magnetic lines cut by an exploring coil (Art. 393, *b*) when the magnetism in the core on which it is wound is suddenly reversed. If R is the resistance of the circuit, $Q = 2\mathfrak{F}/R$. Hence the answer is $\mathfrak{F} = RT \sin \frac{1}{2}\alpha/2\pi S$, where S is the number of turns in the exploring-coil.

29. Suppose a copper disk to revolve in a field produced by a fixed coil closely surrounding its circumference. In circuit with the coil is a small battery and a resistance wire. In the wire are found two points such that the fall of potential between them is equal to the volts generated between the centre and circumference of the revolving disk. By balancing these with a galvanometer Lorenz was able to calculate in absolute measure the resistance of the wire. If M be the coefficient of mutual induction between the circumference of the disk and the surrounding coil, and T the period of revolution of the disk, show that R the resistance between the points $= M \div T$.

Ans. Since $\mathfrak{F}$ the magnetic flux through the disk $= Mi$, and $E = \mathfrak{F}/T$, and $i = E/R$, it follows that $iR = Mi/T$, whence $R = M/T$. Q.E.D.

30. A certain motor has a resistance of 0·25 of an ohm. (*a*) Find the value of a starting resistance such that it will limit the starting current to 10 amperes when the supply voltage is 100.

Find the value which the starting current would have if the full voltage were applied to the armature without any starting resistance.

Ans. (*a*) 9·75 ohms.
(*b*) 400 amperes.

31. An unloaded electric motor runs at 500 revolutions per minute and exerts a back electromotive-force of 98·5 when connected to supply mains at 100 volts. The resistance of the armature from brush to brush is 0·75 of an ohm.

(*a*) Find the current taken by the armature.

(*b*) Find the current taken by the armature when mechanically loaded by a pump which reduces its speed to 480 revolutions per minute.

Assume that the back electromotive-force of the armature is directly proportional to the speed.

Ans. (*a*) Current = 2 amperes.
(*b*) Current = 7·33.

32. In order to measure the brush-to-brush resistance of a certain dynamo armature it is connected in circuit with an accumulator cell and an amperemeter which shows the current to be 40 amperes. A voltmeter connected to the two brushes indicates a difference of potential of 1·9 volt.

Calculate the resistance of the armature.

Ans. 0·475 of an ohm.

33. A test similar to that described in the preceding example is arranged for measuring the resistance of a small lamp, the same accumulator being employed. The voltmeter reads 2 volts, but the current is found to be only 0·25 of an ampere.

On substituting another voltmeter the current changes to 0·24 of an ampere.

Explain (*a*) the increase of the voltmeter reading above the value measured in the preceding test, (*b*) the decrease of current produced by the substitution of a second voltmeter. (*c*) Also suggest a test which, without the use of additional apparatus would enable you to obtain a reasonably accurate result with any suitable and correctly calibrated voltmeter. Would this additional test be equally necessary in the preceding example?

34. A current of 30 amperes at 100 volts is required to light a certain building and is supplied through a pair of mains which has a total resistance of a tenth of an ohm. Find the voltage at the terminals of the dynamo which supplies the mains.

Ans. 103.

35. A certain building requires a current of 40 amperes at 200 volts, and is supplied by a dynamo 500 yards distant.

The total fall of potential in the two mains must not exceed 4 per cent of the voltage in the building.

Find the cross-section of the copper mains if their temperature is 20° Centigrade.

Assume that the resistivity of copper is 0·64 microhm for an inch cube and that its resistance rises 0·4 per cent for every degree of temperature rise above 0° Centigrade.

Ans. 0·1244.

36. Fall of potential takes place in the resistance of generators and follows the same laws as for any other resistances. A primary cell having an electromotive-force of 2 volts and an internal resistance of 0·25 of an ohm is inserted successively in two circuits in which it produces currents of one and two amperes.

In both cases find the potential difference at the terminals of the cell. *Ans.* 1·75 volt at 1 ampere.
1·5 volt at 2 amperes.

37. A certain dynamo has a resistance of 0·4 of an ohm from brush to brush and is driven at such speed that its electromotive-force is 500 volts.

When it supplies a circuit which takes a current of 10 amperes what will be the reading of a voltmeter connected across the brushes.

It is assumed that the electromotive-force is constant.

Ans. Voltage = 496.

38. Two different voltmeters read the same value when used for testing the electromotive-force of an accumulator cell, but read different values when used for testing that of a Leclanché cell.

Under suspicion that their scales are not accurately marked, they are subsequently connected in parallel across the Leclanché cell with a view to comparison.

It is found that their readings are now identical, but are lower than either of the readings obtained when they were employed separately.

Explain these facts.

39. A certain old-fashioned but accurate voltmeter is found to take a current of 0·2 of an ampere when connected to supply-mains at 100 volts. The same supply-mains are subsequently connected through an amperemeter to a glow-lamp across the terminals of which the same voltmeter is connected.

The supply voltage having in the meantime risen slightly it is found that the voltmeter reads 105 volts, while the amperemeter reads 0·6 of an ampere.

Calculate the exact value of the resistance of the glow-lamp when burning under these conditions. *Ans.* 269·2 ohms.

40. Show from the definitions of the horse-power and of the watt, and from the relations between the pound and the gramme, the foot and the centimetre, that there are 746 watts in one horse-power.

41. Describe the construction of a watt meter and explain how you would connect it up to measure the power supplied to an electric motor.

42. Mention some of the principles upon which supply meters have been designed.

QUESTIONS ON CHAPTER VII

1. Calculate by Joule's law the number of calories developed in a wire whose resistance is 4 ohms when a steady current of 0·14 ampere is passed through it for ten minutes.

Ans. 11·2 *calories.*

2. Why does a long thin platinum wire, when a steady voltage is applied to it, rise to a certain temperature and then remain at that temperature without alteration?

3. Explain why you would expect the heat produced in a conductor to be proportional to the square of the current.

4. The exciting winding of a certain generator has a resistance of 50 ohms and is at its working temperature energized from mains at 100 volts.

(*a*) Without calculating the current write down the value of the power absorbed by this winding.

(*b*) Find the number of calories of heat per minute dissipated from it when it has reached a constant temperature.

Ans. (*a*) 200 watts.
(*b*) 2857 calories.

5. Give two or three examples of appliances in which i^2R represents the whole power supplied and utilized by the appliance, and also two or three in which i^2R only represents a wasted fraction of the whole power supplied to the appliances.

6. An electric kettle holding 1 quart of water takes five minutes to raise the temperature from 95° Fahrenheit to

boiling point. The supply voltage is 200 and the cost of electrical energy is 3d. per kilowatt hour. Under these conditions the efficiency of the kettle is 75 per cent.

Find (*a*) The current taken by the kettle.

(*b*) The cost of electrical energy required for boiling the water.

N.B.—A gallon of water weighs 10 lbs. One lb. is equal to 453·6 grams.

$$\frac{\text{Temp. F°} - 32}{9} = \frac{\text{Temp. C°}}{5}.$$

Ans. (*a*) 5·16 amperes.
(*b*) ¼d. nearly.

7. Write down four equations giving the value of the horse-power expended in heating a conductor.

(*a*) In terms of V and *i*.
(*b*) In terms of V and R.
(*c*) In terms of *i* and R.
(*d*) In terms of Q, V, and *t*.

Where *i* is the current in amperes,
V is the voltage across the terminals of the conductor,
R is the resistance, in ohms, of the conductor,
Q is the quantity of electricity passed in coulombs,
t is the time in seconds occupied by the passage of the quantity Q.

8. A strong battery-current is sent, for a few moments, through a bar made of a piece of antimony soldered to a piece of bismuth. The battery is then disconnected from the wires and they are joined to a galvanometer which shows a deflexion. Explain this phenomenon.

9. A long strip of zinc is connected to a galvanometer by iron wires. One junction is kept in ice, the other is plunged into water of a temperature of 50° C. Calculate, from the table given in Art. 474, the electromotive-force which is producing the current. *Ans.* 760 microvolts.

10. When heat is evolved at a junction of two metals by the passage of a current, how would you distinguish between the heat due to resistance and the heat due to the Peltier effect.

11. Lord Kelvin discovered that when a current flows through iron it absorbs heat when it flows from a hot point to a cold point; but that when a current is flowing through copper it absorbs heat when it flows from a cold point to a hot point. From these two facts, and from the general law that energy tends to run down to a minimum, deduce which way a

current will flow round a circuit made of two half-rings of iron and copper, one junction of which is heated in hot water and the other cooled in ice.

12. Give a curve showing the increase and decrease of the thermo-electromotive-force as a junction of iron and copper is raised from 0° C. to 400° C., and explain it by means of the thermoelectric diagram of Professor Tait.

QUESTIONS ON CHAPTER VIII

1. Why in a continuous-current arc lamp is the current usually sent downwards rather than upwards.

2. Why does the filament of an incandescent lamp get hotter than the metal leading-in wires.

3. A current of 9 *amperes* worked an electric arc light, and on measuring the difference of potential between the two carbons by an electrometer it was found to be 50 *volts*. What was the amount of horse-power absorbed in this lamp?

Ans. 0·603 H.P.

4. Enumerate the principal parts of an arc lamp.

5. You are required to design a rheostat for the use of a travelling cinematograph operator who may wish to use arcs taking various currents between 20 and 60 amperes in different towns where the supply voltage ranges between 100 volts and 240 volts.

Find the maximum and minimum values of the resistance of the rheostat, and state what considerations besides these values must govern your selection of the size and quantity of the resistance wire required, and your design of the rheostat.

Also calculate the maximum and minimum costs per hour run of the energy wasted in the rheostat, rates from 1d. to 4d. per Board of Trade Unit.

N.B.—Assume the minimum terminal voltage of the arc to be 40 volts.

Ans. Maximum resistance 10 ohms.
Minimum resistance 1 ohm.
Maximum cost 4s. per hour.
Minimum cost less than $1\frac{1}{4}$d.

QUESTIONS ON CHAPTER IX

1. The reluctance (Art. 404) of the core of a certain transformer is 0·002. Find the coefficient of mutual induction between the primary and secondary coils which have 1000 and 50 turns respectively, assuming no magnetic leakage.

Ans. 0·25 *henry.*

2. A battery current is sent through the primary of this transformer. State from first principles the direction (relatively to this current) of the E.M.F.s induced in both the primary and secondary, (*a*) when the current is starting, (*b*) when it is ceasing.

3. Foucault set the heavy bronze wheel of his gyroscope spinning between the poles of a powerful electromagnet, and found that the wheel grew hot. What was the cause of this? Where did the heat come from?

4. A cube is formed by piling small square plates of copper which are bound together with tape. If this is hung up on a twisted thread between the poles of a powerful magnet, why will it twist more rapidly when the plane of the plates is horizontal than when it is vertical? Also in the latter case why is the rotation accelerated at the moments when the plates are at right angles to the lines of magnetic force?

5. You try to turn a copper disk between the poles of a magnet. If you move it slowly it goes quite easily, if you try to move it quickly it resists. Why is this? What is the force required to turn it proportional to?

6. The shunt coil of a certain dynamo has a resistance of 40 ohms. It is switched on to a battery of accumulators yielding 100 volts, and one second afterwards the current has risen to 0·9825 of an ampere. Find the coefficient of self-induction of the shunt coil. Assume $\log 0{\cdot}607 = \bar{1}{\cdot}783$ and $\log \epsilon = 0{\cdot}434$.

Ans. 80 *henries.*

7. If a battery of 10 cells, each of 1·4 volt and 2 ohms resistance, be applied to a circuit which has a resistance of 5 ohms and inductance 0·1 henry, find what modes of grouping the cells are best, (*a*) to give the largest steady current, (*b*) to give the largest current at the end of $\frac{1}{1000}$ second, (*c*) to give the largest amount of external work relatively to the weight of zinc consumed.

Ans. (*a*) 5 in series, 2 rows in parallel. (*b*) All in series. (*c*) All in parallel.

QUESTIONS ON CHAPTER X

1. What devices are employed in continuous current dynamos to obtain (*a*) a current continuously in one direction, (*b*) a current of uniform strength ?

2. Apply Fleming's Rule (Art. 242) to determine which way the electromotive-forces will operate in a ring armature (gramme) wound right-handedly over the core revolving right-handedly in a horizontal magnetic field having the N-pole on the right hand.

Ans. The induced E.M.F.s tend to make the currents climb, in both the ascending and descending halves, toward the highest point of the ring.

3. A bipolar dynamo's field magnet gives a flux of 9,000,000 lines. How many conductors must there be on the armature in order that the dynamo may generate 108 volts when driven at a speed of 600 revolutions per minute ? *Ans.* 120.

4. You have an engine which will drive a dynamo at a fairly constant speed at all loads. How would you excite the dynamo if it were intended for lighting by incandescent lamps ? Make a diagrammatic sketch of all necessary connexions, including the lamp circuit.

5. Take the equation $E = a \sin (2\pi nt)$. Let $a = 140$ and $n = 100$. Now take different values for t, beginning $t = 0{\cdot}0005$ of a second, then $t = 0{\cdot}001$, taking 20 different values until $t = 0{\cdot}01$. Fill in the values in the above equation and find the corresponding 20 values of E. Then plot on squared paper, taking E as ordinate and t as abscissæ. The result will be a curve like that shown in Fig. 301.

6. Repeat the process of the last question, taking the equation $C = b \sin (2\pi nt - \phi)$, where $b = 20$, $n = 100$, and $\phi = 0{\cdot}5$ radian. Plot the results upon the same paper as the curve in the last equation was plotted. One curve represents the E.M.F. at each instant, the other the lagging current.

7. The voltage at the brushes of a certain continuous current shunt motor is 500. At a certain load the mechanical output is 13·5 HP. and the total current 23 amperes. The resistance of the shunt winding under running conditions is 625 ohms and the armature resistance measured from brush to brush is 1·3 ohm.

(*a*) Calculate the total power wasted in small rotational

losses such as eddy-currents, hysteresis, windage and bearing friction.

(*b*) Calculate the efficiency of the motor.

Ans. (*a*) 349·8 watts.
(*b*) 87·5 per cent.

8. An electric motor is supplied at a pressure of 100 volts: the armature resistance is 0·01 ohm. When it is supplying 20 horse-power, what is its electrical efficiency?

Ans. 98·5 per cent.

9. Show under what circumstances an electric motor is most efficient.

10. Find the virtual value—*i.e.* the square root of the mean of the squares—of the following series of numbers:—26, 50, 71, 87, 97, 100, 97, 87, 71, 50, 26, 0.

Ans. The sum of the squares is 60390; the mean of the squares is 5032·5; the square root of the mean of the squares is nearly 71.

11. An alternating pressure of 100 (virtual) volts following a sine law with a frequency of 100 per second is applied to the ends of a coil having a resistance of 8 ohms and a coefficient of self-induction of 0·005 henry, find the current that will flow and the angle of lag.

Ans. Current = 11·6 amperes; lag = 22 degrees.

12. An alternating current magnet with properly laminated core has a coil of 160 turns, and a coefficient of self-induction of 0·005 of a henry. What alternating voltage, of frequency 100 per second, must be applied to it in order to obtain 4800 ampere-turns, assuming the resistance to be negligible?

Ans. 94·25.

13. How much resistance must be put in circuit with the coils of this magnet in order that the angle of lag may be 45°?

Ans. 3·14.

14. An alternating current transformer is designed to give out 40 amperes at a pressure of 50 volts at its secondary terminals. No. of windings 300 primary; 12 secondary. Resistances 12 ohms, primary; 0·014 ohm, secondary. Find the coefficient of transformation, and the volts that must be applied at the primary terminals.

Ans. Coefficient of transformation is 25; volts at primary terminals 1283.

15. An electric welding machine has its secondary circuit consisting of one turn of copper conductor, and its primary

consisting of 80 turns of copper wire. If a current of 2000 amperes is to be induced in the secondary circuit, how many amperes must be imparted to the primary ?

Ans. At least 25 amperes.

16. State the principles by which a continuous current of, say, 25 amperes supplied at 1000 volts can be converted into a continuous current of nearly 125 amperes at 200 volts. Why is it necessary to have a moving part in continuous-current transformers and not in alternating current transformers ?

17. Enumerate three distinct kinds of alternating current motors, and state which kind is synchronous and which not.

18. An alternating current synchronous motor is supplied from the street mains. It is found that when fully loaded it takes more current than when lightly loaded, though it always goes at the same speed and the volts remain constant. Explain how this comes about.

19. How can you produce a rotatory magnetic field ? Describe some of its properties.

QUESTIONS ON CHAPTER XI

1. Certain mains carry a current of 60 amperes along their whole length and their resistance is such that the voltage at one end is 100 and at the other 104. Find (*a*) the power supplied to the mains, (*b*) the power wasted in the mains.

Ans. (*a*) 6¼ kilowatts, nearly. (*b*) 240 watts.

2. Explain why it is advantageous to distribute electric energy at a high voltage. There is already laid a copper main having a resistance of 0·5 of an ohm along which it is desired to transmit 4 kilowatts, and to deliver it at the far end at a pressure of 100 volts. Which would be the more efficient method of the two following, to send 40 amps. at an initial pressure of 120 volts, or to send a current at a pressure of 2400 volts, using a transformer with an efficiency of 85 per cent ?

Ans. The latter method would have an efficiency of 84·9 per cent, the former of 83·3 per cent.

3. Explain by a diagram the system of three-wire distribution, and point out its advantage over a two-wire distribution.

QUESTIONS ON CHAPTER XII

1. What are the main points in the problem of supplying an electric current to a moving vehicle, without risk of failure of supply? How have these conditions been met in practice?

2. It is usual to provide electric tramcars with two motors each, rather than with one, and those motors series-wound, rather than shunt-wound. What are the reasons for these preferences?

3. What is an electric controller? What are the operations which it effects?

4. Suppose a motor, supplied at 550 volts, to take from the lines, during the period of acceleration, a current of 220 amperes, how many electric horse-power are being supplied at that time? *Ans.* 162·4.

5. Describe the arrangements for electric propulsion of railway trains, as adopted on English suburban lines.

QUESTIONS ON CHAPTER XIII

1. It is found that a single Daniell's cell will not electrolyse acidulated water, however big it may be made. It is found, on the other hand, that two Daniell's cells, however small, will suffice to produce continuous electrolysis of acidulated water. How do you account for this?

2. From the table of electro-chemical equivalents (Art. 256) calculate how many coulombs it will take to deposit one grain of the following metals: — Copper (from sulphate), silver, nickel, gold. *Ans.* Cu 196·7, Ag 57·9, Ni 213·1, Au 95·1.

3. A battery of 2 Grove cells in series yields a current of 5 amperes for two hours, how much zinc will be consumed, assuming no waste? *Ans.* 24·39 grams.

4. Calculate the E.M.F. of a Daniell cell from considerations of the heat value of the combinations which take place and the quantity of the elements consumed, taking the heat value for zinc in sulphuric acid as 1670 and that for copper as 909·5. *Ans.* 1·11 *volt.*

5. Describe the construction and working of a modern secondary battery.

6. Most liquids which conduct electricity are decomposed

(except the melted metals) in the act of conducting. How do you account for the fact observed by Faraday that the amount of matter transferred through the liquid and deposited on the electrodes is proportional to the amount of electricity transferred through the liquid ?

7. Describe the process for multiplying by electricity copies of engravings on wood-blocks.

8. How would you make arrangements for silvering spoons of nickel-bronze by electro-deposition ?

QUESTIONS ON CHAPTER XIV

1. Sketch an arrangement by which a single line of wire can be used by an operator at either end to signal to the other ; the condition of working being that whenever you are not sending a message yourself your instrument shall be *in circuit* with the line wire, and *out of* circuit with the battery at your own end.

2. What advantages has the Morse instrument over the needle instruments introduced into telegraphy by Cooke and Wheatstone ?

3. Explain the use and construction of a relay.

4. Show, from the law of traction (Art. 415), that the *change* of attracting force resulting from a *change* in the number of magnetic lines that enter an armature will be greater if the system is polarized (*i.e.* magnetized to begin with) than if it is non-polarized.

Ans. Since $f \propto \mathfrak{F}^2$, it follows that $f+df$ will be proportional to $(\mathfrak{F}+d\mathfrak{F})^2$. Expanding, and subtracting the former, and neglecting the small term $(d\mathfrak{F})^2$, we find $df \propto 2\mathfrak{F}.\, d\mathfrak{F}$; which shows that, for a given $d\mathfrak{F}$, $df \propto \mathfrak{F}$.

5. It is desirable in certain cases (duplex and quadruplex signalling) to arrange telegraphic instruments so that they will respond only to currents which come in one direction through the line. How can this be done ?

6. It is wished to make a sort of duplex telegraph by using one set of instruments that work with continuous currents, the other set with rapidly alternating currents, at the same time on the same line. To carry out this idea there must be found (*a*) an apparatus which will let continuous currents flow through it, but will choke off alternate currents ; (*b*) an

apparatus which will transmit alternate currents, but cut off continuous currents. What apparatus will do these things?

7. A battery is set up at one station. A galvanometer needle at a station 80 miles away is deflected through a certain number of degrees when the wire of its coil makes 12 turns round the needle; wire of the same quality being used for both line and galvanometer. At 200 miles the same deflexion is obtained when 24 turns are used in the galvanometer-coil. Show by calculation (*a*) that the internal resistance of the battery is equal to that of 40 miles of the line-wire; (*b*) that to produce an equal deflexion at a station 360 miles distant the number of turns of wire in the galvanometer-coil must be 40.

8. Suppose an Atlantic cable to snap off short during the process of laying. How can the distance of the broken end from the shore end be ascertained?

9. Suppose the copper core of a submarine cable to part at some point in the middle without any damage being done to the outer sheath of guttapercha. How could the position of the fault be ascertained by tests made at the shore end?

10. Explain the construction and action of an electric bell.

11. Describe and explain how electric currents are applied in the instruments by which very short intervals of time are measured.

12. Explain the use of Graham Bell's telephone (1) to transmit vibrations; (2) to reproduce vibrations.

13. Describe a form of telephone in which the vibrations of sound are transmitted by means of the changes they produce in the resistance of a circuit in which there is a constant electromotive-force

14. Two coils, A and B, of fine insulated wire, made exactly alike, and of the same number of windings in each, are placed upon a common axis, but at a distance of 10 inches apart. They are placed in circuit with one another and with the secondary wire of a small induction-coil of Ruhmkorff's pattern, the connexions being so arranged that the currents run round the two coils in opposite directions. A third coil of fine wire, C, has its two ends connected with a Bell's telephone, to which the experimenter listens while he places this third coil between the other two. He finds that when C is exactly midway between A and B no sound is audible in the

telephone, though sounds are heard if C is nearer to either A or B. Explain the cause of this. He also finds that if a bit of iron wire is placed in A silence is not obtained in the telephone until C is moved to a position nearer to B than the middle. Why is this? Lastly, he finds that if a disk of brass, copper, or lead is interposed between A and C, the position of silence for C is now nearer to A than the middle. How is this explained?

QUESTIONS ON CHAPTER XV

1. What apparatus would you use to produce electric oscillations? Show how you would operate it, and explain why the oscillations take place.

2. Explain how electric oscillations in a condenser circuit produce electric waves in the surrounding medium.

3. The capacity of an air-condenser is 0·001 of a microfarad. It is charged and then discharged through a circuit having a self-induction of 0·004 of a henry and a resistance of 4 ohms. Find the frequency of the vibration. *Ans.* $n=79600$.

4. In what circumstances do oscillations not take place when a condenser is discharged?

5. If the frequency of oscillation of a Hertz oscillator is 3,000,000 per second, find the length of the waves it will produce. *Ans.* 10,000 centimetres.

6. Explain the action of a resonator.

7. What is the frequency of the oscillation that corresponds to electric waves having a wave-length of 6000 metres? *Ans.* 50,000 per second.

8. Give the reasons which exist for thinking that light is an electromagnetic phenomenon.

9. How is the action of magnetic forces upon the direction of the vibrations of light shown? and what is the difference between magnetic and diamagnetic media in respect of their magneto-optic properties?

10. The resistance of crystalline selenium is less when exposed to light than in the dark. Describe the apparatus you would employ to investigate this phenomenon. How would you proceed to experiment if you wished to ascertain

whether the amount of electric effect was proportional to the amount of illumination?

QUESTIONS ON CHAPTER XVI

1. Describe the apparatus necessary for a transmitting system in radiotelegraphy, and draw a diagram of connections of the system described.

2. What is meant by coupling? Two circuits, inductively coupled, and tuned to the same frequency, have impressed on them an oscillation frequency of 500000. It is found that this oscillation is resolved into two slightly different frequencies of 527050 and 476730. What is the coefficient of coupling of the two circuits? *Ans.* $c=0{\cdot}1$.

3. Explain the difference between the Quenched-Spark and Oscillating-Arc systems of transmission.

4. Describe the different detectors in use, and explain the action of each form.

5. Describe a receiving set suitable for wireless telephony.

QUESTIONS ON CHAPTER XVII

1. State what are "The Ions of Electrolysis," and explain their supposed production.

2. Explain the phenomenon of ionization of a gas.

3. Describe an electric valve, and explain its action.

4. What is the electronic theory of dielectrics?

5. Describe what is meant by a radio-active substance. What are the rays that emanate from radium? Distinguish between their properties.

6. How is the ratio between the electric charge of an electron and its mass determined?

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