

An enquiry into the laws of falling bodies, etc / By Robert Anstice.

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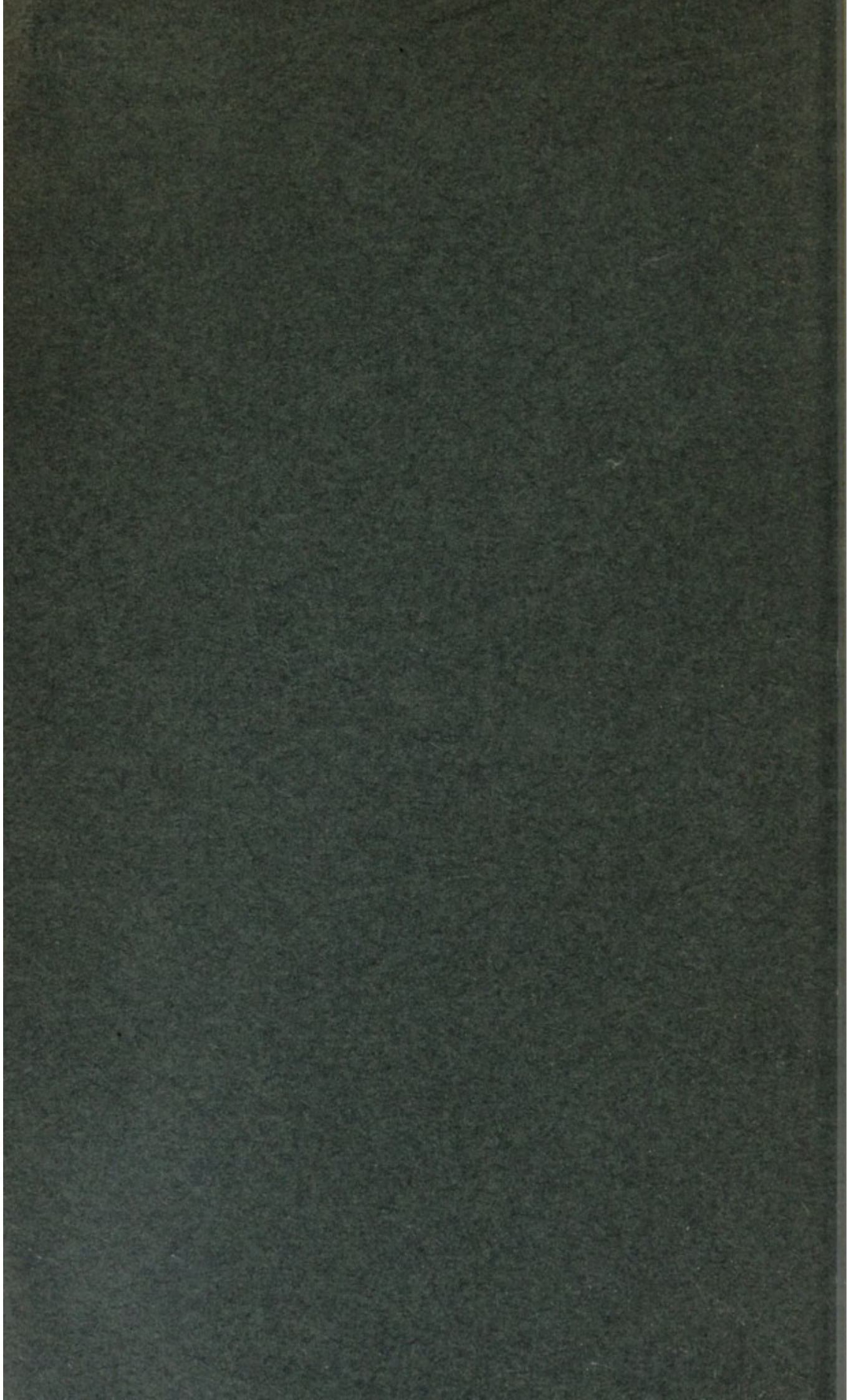
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FALLING BODIES

1794



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I N T O T H E

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F A L L I N G B O D I E S , & c .

BY ROBERT ANSTICE.

L O N D O N :

PRINTED FOR JOHN AND ARTHUR ARCH, NO 23, CRACK-
CHURCH STREET.

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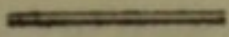
of your learned Body will be its best

those for whose Use it is intended; it

is therefore respectfully submitted to

*To the President, Council, and Fellows
of the Royal Society of London, for
the improving of Natural Knowledge.*

THE AUTHOR



GENTLEMEN,

IF the following Treatise may
answer the Purpose of extending
useful Knowledge, or clearing up any
doubt, as to the true operation of
Mechanical Powers, the Approbation
of

of your learned Body will be its best
recommendation to the perusal of
those for whose Use it is intended; it
is therefore respectfully submitted to
your determination by

Your Obedient,

Humble Servant,

THE AUTHOR.

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INDEPENDENTLY of the Satisfaction arising from the investigation of abstract Truth, the utility of duly understanding whatever relates to the Subject of the following Pages, must be acknowledged by all who consider the general application of Machinery to almost every branch of our Manufactories, to be both expedient and necessary; expedient, as much cheaper than manual labour, and necessary, as manual labour is inadequate in many cases to the Fabrication, and in others to the demand of our Manufactures.

The

ADVERTISEMENT.

The very respectable authorities to which the Author found he had to oppose his Opinions in several parts of this Enquiry, for some time prevented his publishing them; but having been successful in the application of those of his Principles which he has reduced to Practice, and his Treatise on Wheel Carriages having met with a favourable reception, he is induced to lay them before the Public.

C O N-

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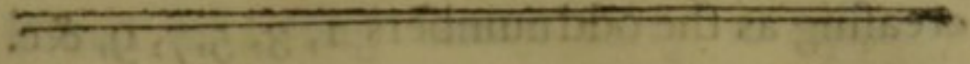
Of Fly Wheels, and their Effect on Machines.

S E C T I O N X.

Of the proportion of Resistance, proper to be applied to a Machine worked by the second kind of Power, or Percussion.

S E C T I O N XI.

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AN ENQUIRY, &c.

SECTION. I.

Of the Descent of Heavy Bodies near the

Surface of the Earth.

EXPERIMENTS have discovered, that

a heavy body, near the surface of the earth,

will fall in one second of time through

16 ft. 2 in. of void space, and that this velo-

city constantly accelerates in the ratio of the

squares of the times in which the body falls;

from which we may determine, that in two

seconds it will be carried through a fall of

64 ft. 8 in. or 4 (square of 2) times 16 ft. 2 in.

in 3 seconds through 145 ft. 6 in. which is 9

(square of 3) times 16 ft. 2 in. and so on, in-

creasing

creasing as the odd numbers 1, 3, 5, 7, 9, &c. For if it fell through one given space in a certain time, in the next equal time it would fall through three such spaces; which added to 1 is 4, (the square of 2); in the 3d equal time it would go through 5, which added to what it went before, is 9 (the square of 3) and so on.—And the reason of this proportion in the acceleration will be evident, if we consider that a body first yielding to the action of gravity, begins to fall with a motion, the smallest possible; but by the continuation of that action upon it, it's motion is constantly and regularly increased, till we suppose it arrived to a certain place in a correspondent time, both which space and time we will denote by the number 1.—Now as it began it's fall (from a state of rest,) with the least motion possible, which was uniformly increased by the action of gravity, a medium of the degree of motion
it

it had in falling would carry it equably through the same space, in the same time, if the cause of the first motion ceased to act on, and accelerate it;—the motion therefore it has acquired at it's arrival at this place must be double the *medium* of that acting on it in it's fall; consequently, in the same time would carry it through double the space, without the cause continuing to act on it; but as that cause, when it does act, is sufficient to carry it through the same space in the second given time as in the first, that 1 added to 2 (the independent motion it acquired by the first time's fall,) makes 3, and this added to the 1 it fell in the first time, makes 4 (square of 2 as before).—When it arrives here, it has by the same reasoning acquired an independent motion of 8, in 2 times, which is 4 in 1, and that added to 1, which it falls by the action of gravity in each time makes

B 2

5, which

5, which added to 4 it has fallen in the preceding times, makes 9, the square of 3.— Therefore at every period the independent motion acquired by the falling body is in geometrical proportion to the times, and double the square root of the distance fallen through, agreeably to the table below.

If the first time be fixed to a quarter of a second, the body will fall in the following progression.

T A B L E.

Times.	Fall in each Time.		Fall at the different Periods.		Independent Fall acquired.	
	F.	I.	F.	I.	F.	I.
1ft — $\frac{1}{4}$ of sec.	1	$\frac{1}{8}$	1	$\frac{1}{8}$	2	$\frac{2}{8}$
2d — $\frac{1}{4}$	3	$\frac{3}{8}$	4	$\frac{4}{8}$	4	$\frac{4}{8}$
3d — $\frac{1}{4}$	5	$\frac{5}{8}$	9	$\frac{9}{8}$	6	$\frac{6}{8}$
4th — $\frac{1}{4}$	7	$\frac{7}{8}$	16	$\frac{16}{8}$	8	$\frac{8}{8}$

N. B. The last column shews the actual and independent velocity the body has acquired at the end of each term; which is what it would continue to move with per $\frac{1}{4}$ second, if the action of gravity were removed. So that a body having fallen through 16 ft. 2 in. in one second, it would acquire a velocity of 32 ft. 4 in. per second, independent.

Thus,

Thus it is demonstrable, that if a number of balls of any weighty matter were placed on the wall of a tower, or other eminence, and were to be pushed forward in such a manner that they should successively fall, as fast as one gave place to the other, yet would they run from each other, as described by plate 1. fig. 1. For if the ball (a) were to fall to b, and then another took its place;—while this last was falling through the first space, the first ball would reach to c, and so successively to d, f, &c.

S E C.

SECTION II.

*Of the Descent of Water, and the effect of
it's passing through Tubes, and other Vessels.*

WATER, like other heavy bodies, would observe the same rules in open space; and therefore if it be poured from an eminence, though the stream may be continued from the vessel, yet would it not remain so during it's fall, but the first escaping, would fall away from the last, and increase in distance from it till it reached the end of the fall. The reason why it should be otherwise, when confined, and falling through a tube such as plate 1. fig. 2d. will arise from the following consideration; that, although by filling the reservoir on the top, and the water falling into the tube, it's parts would have a

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tendency to divide, and have separate motions, according to their successive times of beginning their falls; yet if the tube be regular, and equal in it's bore, no portion of the column of fluid can go faster than another; because the pressure of the surrounding atmosphere would keep it together, and not suffer by it's division a vacuum between it's parts:--therefore in such a case, instead of falling out of the lower end of the tube, with a velocity sufficient by an equable motion (if gravity were suspended) to carry it, through a space *double* the height of the tube, in the time a body would fall the length of it, as shewn above; it's impetus would only carry it through a space *as long* as the tube, in the same time that it would fall the length of it; for it would all fall with the *medium* of the velocity of a solid body in falling that length. But this defect of natural motion may be remedied, by forming the tube

like a trumpet, and of the proportion of fig. 3d. plate 1. or of any other exceeding it in it's upper parts;—for then it will contain such quantities of a fluid in it's different proportionate heights, as are equal to the spaces through which they would fall by their natural weight, (making up in bulk what is wanting in length); if therefore, there were a supply at top, by a proportionate descent of the fluid in each part the motion would be agreeable to the descent of a body falling by accelerated motion; for as much would descend by it's fall from a to b, as from b to c, or c to d, &c. which are the natural falls, and the fluid would have no tendency to divide in the tube. In this case, therefore, the issuing of a fluid through a hole in the bottom of the vessel would be with a velocity equal to that which a heavy body would acquire by falling through a space equal to the height of the fluid, and which, as said before,

is

is double the *medium* of velocity it had in falling, or in other words, sufficient independently to carry it through double the space it had fallen in the same time.—This reasoning is new, (at least to myself, not having met with the cause of the effect before mentioned any where explained;) but the common doctrine of bodies falling in open space is accepted by most philosophers, and was that of the excellent Sir Isaac Newton, who in the process of his investigation, lays it down as a law of Nature, “ That the comparative
 “ impetus or force of bodies in motion, is, as
 “ the velocity with which they move multi-
 “ plied into their quantities of matter.”

I should have thought it highly assuming in me, to contradict in any terms such great authority; but having occasionally had some cases to investigate, in which this law was concerned, and not finding it to solve

in a very satisfactory way the doubts I had to determine, and considering a blind adherence to any doctrine, without a conviction of the justness of it's principles, as a bar to knowledge and discovery, I thought it right to express my objections to that doctrine, hoping, that it may be the means of exciting to a further investigation some person better able to pursue it, and tend to settle a subject, so worthy, by it's general concern, the attention of all.

In this having had occasion to refer to some books which I had never before consulted on the subject, I soon discovered that the opinion which I had taken up (and which was, that the comparative force of bodies in motion was as the square of their velocity, multiplied into the quantities of their matter,) was not new, as I had conceived, but had been hinted by Huygens, and
adopted

adopted by Leibnitz and his followers ; who in many publications had supported their opinions against the Newtonians, with arguments and experiments many of which I had previously conceived.—

Some of these I consider as conclusive but, as they are in print, I shall not here repeat them ; offering only such as appear to be new, and are convincing to me of the justness of the latter doctrine, at least till other arguments are presented than those which I am at present acquainted with.—Preparatory to this, the following considerations and positions are necessary, and require the assent of the reader.

S E C T. III.

*Of the various kinds of Forces, and their
Effects on Mechanical Powers.*

POWERS, or forces, in a mechanical sense, are of three kinds, under two distinct heads; first, the inactive, resisting power, or *vis mortua*, which admits of no variation, neither can have any thing in it relative to quantities of matter, space, time, or velocity, (which last is a compound of the two preceding it) for should it yield to the force applied, it's distinction alters.---Such is the resistance which a table, wall, &c. makes to any power, or thing placed on, or against them.

Second,

Second, That kind of active force, or *vis viva*, which ariseth from the percussion or stroke of any body in motion, (however that motion might have been received) whose quantity of power or force must be a certain compound of it's quantity of matter, and quantity of velocity at the time of percussion, without regard to the space it might have before past over, for that can have no reference to a *post* action; thus, any independent body, having a certain degree of motion once given it, would continue to move equally till it were opposed by some other body, against which it's action would be equal, in whatever point of it's course they should meet.

Third, That other kind of *vis viva* which is produced by gravity or otherwise, on two bodies connected by some machinery to each other, and is compounded equally of
 quantity

quantity and space, without regard to time or velocity.—Such is the *action* of matter yielding to gravity, or the attraction of the earth, and constantly expending itself on some opposing power; in which case it is evident, that a certain power lies in a given quantity of matter, in respect to a given perpendicular distance, however fast or slow that power be used, and is subject to a number of variations by the use of mechanical powers; thus, if I have an hundred pounds weight of any matter to lift through a foot of space in a line directly contrary to the earth's attraction, (or upwards,) I may effect it by the least possible quantity more than an hundred pounds weight, moving by the action of gravity through the space of one foot downwards, either by means of an equal balance, by a simple pulley, or by a double plane of any equal inclination.

Ex:

Ex: In the double inclined place E C F plate 2d. fig. 1ft. suppose the weight A to be one hundred pounds, from which let a line be carried over the pulley C and fastened to B, (a weight of little more than one hundred pounds) it would, (if the planes E C and C F were equal,) raise the ball A up the inclined plane, just as much as B descended, and no more, which suppose to be a foot perpendicular descent, A would be just so much raised, and the same would happen by inverting the planes, and making use of two pulleys instead of one, as in figure 2d.

Or it may be effected by the action of little more than fifty pounds through two feet descent, or twenty five pounds through four feet descent by means of any of the mechanical powers,---converting the equal balance into a lever, the single pulley into a
com-

compound set, or the equally inclined planes into unequal ones; those powers, therefore which are made up of *matter* and *space*, such as one hundred pounds raised one foot, fifty pounds two feet, or twenty-five four feet, (whether this be an hour, a day, or month in the operation, or whether the motion or velocity be swift or slow) are a balance to each other, and may be considered as equal, and expressing the same power.

S E C

SECTION IV.

Of the Application of the preceding Considerations to prove the Leibnitzian Doctrine of the Percussion of Bodies in Motion.

THESE premises being allowed, (and I think they are incontrovertible) it will be no difficult matter to prove, that the comparative force, momentum, impetus, or powers of equal bodies in motion, are as to the effect of their *percussion*, as the *square* of their velocities, and consequently that the same powers of bodies of unequal weight, are as the *square* of their velocities multiplied into their respective weights, or quantities of matter.—For it is a generally well
D known

known and acknowledged fact, that a pendulum, (such as is used in clocks,) raised to any given height, and let swing freely, (some small allowance being made for the resistance of the medium in which it vibrates and the friction of it's axis,) will rise by the power gained in it's fall, to the same height on the other side of the perpendicular, then return back to it's first place, and continue to make equal vibrations ad infinitum.—So would it happen to a ponderous ball, (the same allowances being made for friction, &c.) if it were let run down such a double inclined plane, as fig. 2. plate 2. for instance suppose from B; the power it would acquire by the descent to E. F. would be sufficient to raise it an equal height on the opposite plane, to which it's direction would be diverted, provided it be contrived by curvating the angle at E. F. to make that diversion gradual and free from

from shock; and this would happen in the same manner let the ball run from whatever part of the inclined plane it may; corresponding exactly with the action on the inclined plane, considered as a balance when the figure was before treated of. It cannot be objected to this reasoning, that the ball's ascending on one plane, by its descent on the other from an equal height, affords not a fair argument, as the power is not communicated to a second body; for whatever power exists in any body may be communicated in equal degree, provided that by the *contrivance* or mode of communication none of that power be lost and although no such contrivance or mode can be found out, yet such defects never make part of calculations of this sort. Nor can it be fairly objected, that the raising a body in motion is not equal to the raising an equal body deprived of it

to the same height; for in this case we are considering the effect of that motion, which is the raising the ball, and without which it would not be raised;—the height therefore to which it is raised, expresses the power, as in other mechanical operations before stated.

We may here just mention that bodies perfectly elastic, falling on solid bodies, and water spouting upwards from a hole in the side of a vessel, will both rise to the height of their sources of action.

If we now take a retrospect of fig. 1. plate 1. and the explanation of it, we shall there see, that the comparative, actual, and independent velocity of a falling body, is not as the height, or distance through which the body falls, but as the *square root* of that distance, as marked in the last column ;

column;—therefore presuming it is shewn above, that the powers of equal bodies are as the heights from which they fall, those powers must be as the squares of those velocities, which are as the heights.—And the further to confirm the preceding doctrine, I will endeavour to shew in it's true light the chief argument which has been advanced against it, and, which confounding the two distinct powers before-mentioned, is founded on the following principle;—that if to a lever two unequal weights be applied, at such distances from the fulcrum or center of suspension as that they shall balance each other, such as 4 pounds at 1 foot distance, balanced by 1 pound at 4 feet from the fulcrum, they will not only be in equilibrio to each other when they are at rest, but also when put in vertical motion, which it has been said could not happen if the square of the velocity

city

city measured the force. For in the lever fig. 3. pl. 2, if the weight A of 1 pound be put in motion downwards to C, it will raise the weight B of 4 pounds to D—Now as the square of 1 (the velocity of B) is 1, which multiplied by 4 (the quantity of matter) is 4;—and as the velocity of A is 4, whose square is 16,—it should therefore seem, that according to the new doctrine these numbers express the comparative powers of each when in motion, and that therefore that of A, would overcome that of B, and instead of vibrating as it is found to do, would increase in velocity till it reached the lowest point which the length of the lever would permit: but this reasoning gives way when we consider that no motion can take place in A, without it's acting and expending it's power at *the same instant* on B, therefore no free motion through any quantity of space, or *percussion*, can possibly

possibly happen; in which case no *velocity* can be estimated in the calculation of the power or effort, for the same reason—If I have a ball of matter of any given weight, (4 pounds for instance,) whose power in it's descent through 49 feet of space, I can make use of, and I suffer it to fall through the whole, it's power by percussion at the end of it's fall may be estimated as the square of 7, (it's velocity,) multiplied into 4, (it's weight or quantity of matter,) which is 196.—Now, if instead of making use of the percussion acquired by it's going through the whole fall, I take it at twice;—as first, it's percussion or force when fallen through 25 feet it will then have acquired a comparative velocity equal to 5, whose square 25, multiplied by 4 the weight, is 100; and by the same reckoning, it will by running through the remaining 24 feet acquire a momentum equal to 96, which
together

together is as the first force gained by the whole fall. And such will be the result, if we calculate the percussion or force of the fall through each foot of the space, separately ;---for the square of 1, is 1, and multiplied by 4, is 4, and this on each of the 49 feet makes together 196, as before. What is most observable in this, is, that in calculating the percussion or force of the body in the fall of 49 ft. taken together, the square of the velocity is 49; but as the distances of the separate falls decrease, notwithstanding the effect produced on the whole of the falls be equal, yet the velocity has less and less proportion in the calculation, till it comes to that point in which there is no difference between the action of the power and effect, (as to time and space;) as is the case with the lever or ballance, and being a power of the third sort here enumerated, in which velocity
and

and percussive are quite out of the question; therefore, although this doctrine be not confirmed by the action of weights so suspended, yet that is by no means an argument against it.

It may not perhaps be deemed superfluous just to remark, that, as the comparative powers of bodies in motion are as the square of their velocities, so are the comparative velocities of a body, (as obtained from any powers,) as the square root of the powers. This indeed stands or falls with the preceding doctrine, for its best proof depends on the same argument.--- And what test have we of the degree of power or force in any body, but the quantity of work it will do, before its power be expended? therefore whatever power will raise a certain weight of matter 4 feet must certainly be 4 times as great as that,

E

which

which can raise the same but 1 foot. Now it has been shewn, that a body falling through 1 foot of space, will raise an equal weight 1 foot and a body falling through 4 feet will raise an equal weight 4 feet and so on; consequently, their powers or forces are as the distances fallen through; but as is above said, their velocities will be but as the square *root* of these powers, the first being 1 and the latter 2, and the same rule obtains in every distance*.

* I am aware that much has been written, to shew, that the *time* required to expend the power contained in any independent body in motion, by its percussion or impulse on another, varies according to the degree of its velocity, and therefore that this difference of *time* should be taken into the account of its action or power; but waving the very intricate discussion and experiments which have been offered on the subject, the question may be reduced to the following simple one;—Will any two independent non-elastic bodies meeting in contrary directions, and having quantities of matter and velocities, which by the above rules constitute equal percussion or impetus, instantly deprive each other of motion or not? I have no opportunity of making the experiment as it ought to be tried, but have little doubt of its success in proving the above doctrine.

If this be clear to the conviction of the reader, he will have cause to admire the unity and simplicity of the laws of nature and their operations; as, if it were otherwise than I have stated, there would be in effect, a diversity unaccountable, and without cause; for what reason can be assigned, why a body, falling through one measure of space, (without acting on any thing in it's fall, so as to expend it's power,) should not double that power by falling through two such measures, just, as a body of double the weight of another, has double the power by falling through the same height.

SECTION V.

Of Water on overshoot Wheels.

BEFORE we apply this reasoning to the power of a fluid spouting through a hole in the side of a vessel, or rather to its re-action on that vessel, let us consider the effect of waters on overshoot wheels; and in these, we shall find the power in exact proportion to their size, or the height of the water's action.---For instance, if I have a stream of water, which will afford a constant loss of 1 gallon per second, and have also a sufficient fall to allow it to pass over a wheel of 14 feet diameter, which is equal to 44 feet in circumference, and if there be a bucket capable of containing a gallon, in

in each foot, and the wheel revolves in 44 seconds; consequently if the buckets are contrived to discharge themselves as they arrive at the lower part, and are gradually filled at the top of the wheel, the expence of the water will be according to the above allowance of 1 gal. per second, and there will be 22 gals. constantly acting by their weight on one side of the wheel, and none on the other; but, as the perpendicular bearing of the weight of each bucket will be at different distances from the perpendicular of the wheel's center, it will be necessary to delineate such a wheel, in order to make it's action clear to the understanding as we proceed.

Let A B C D, fig. 1. plate 3. represent such a wheel having 44 buckets, each containing 1 gal. of water, and so contrived, that there shall be no vacant space between them, and that they shall not
 discharge

discharge themselves, till they arrive at the bottom of the wheel, or near it; then it will be found, that the aggregate action of the buckets will be as centered on the point E, and will therefore be a balance to two thirds the weight of the 22 gallons if suspended at B, (which is 1 and an half the distance of E from the center of the wheel;) this weight therefore, which I suppose to be 132 pounds, it would nearly raise, at the rate of one ft. per second.---Now suppose the wheel to be double the size, as fig. 2. it will then contain 88 buckets on it's circumference, or 44 gals. acting by the weight on the point E, and would support 2-thirds of the weight of 44 gals. suspended at B, which is equal to 264, double 132 pounds.) If each wheel therefore revolves at the rate of 1 ft. circumference per second, (which it must do to keep the expence of water equal) the power of such wheels must evidently be

in exact proportion to their size,---or in other words, the power of descending water by it's application to such wheels, is in exact proportion to it's descent, the expence remaining equal,

SECTION VI.

Of the Re-action of Spouting Fluids.

WE come now to treat of the effort or power produced by the pressure of a continued body of fluid, contained in one vessel; in which is concerned, that certain and evident law in hydrostatics; “that on equal surfaces the quantity of such pressures is in geometrical proportion to the height of the superincumbent fluid, without regard to the size of the containing vessel,” “and also,” that (on account of the yielding property of such as are pretty perfect, occasioning a re-action from one side or part of the vessel to it’s opposite,) the pressures are equal in every direction.—Thus,
if

if a vessel 10 inches deep be full of water, the pressure on every square inch of the bottom, will be equal to the weight of 10 cubic inches of water, and on every square inch of the sides will be equal to the weight of as many cubic inches of water as are perpendicularly above it; the direction of which pressure will be at right angles to the part on which it acts:---So in a vessel 10 feet square, and 20 deep, full of water, there will be the weight of 20 cubic feet of water on every square foot of it's bottom; and on each square foot of it's side, whose center shall be 16 feet from the top of the fluid, there will be the weight of 16 cubic feet of water, pressing in a lateral direction against it.---If, therefore, a hole of a foot square be made at this depth, and some independent body be put against it to hinder the water from running out, there will be the pressure of 16 cubic feet of water pressing more on the opposite

F side

side than on this; and if the vessel be put afloat, or in any situation free to move, it will require the action of such weight to keep it from motion; if this presented body be removed, the water will issue with a velocity equal to that which a body would acquire by falling from the height of 18 feet which we will call 8 feet per second; now as the vessel is so large in proportion to the quantity of water running off, and we suppose it by some supply kept constantly full, the pressure on the foot opposite will not be much disturbed or lessened; if therefore the vessel were to move in the direction of the superabundant pressure, and with the whole velocity of the issuing water, all the power of so much issuing water will be expended on the vessel, and it will raise a weight of 16 cubic feet of water through 8 feet of space, which is equal to the expence and height of the fluid.---If this hole be shut, and the vessel

vessel remaining in the like circumstances, a hole of the same size be opened in the side, whose center shall be 1 foot below the surface of the fluid, it will in the same proportion run 2 feet per second, and there will be a superabundant pressure on the opposite side, equal to the weight of 1 cubic foot of water; if then, as before, the motion of the liquid be supposed to expend itself on the vessel, it will move it 8 feet in the time that so much is run out as above stated; and will raise, by the contrivance of a pulley, the weight of 1 square foot of water through 8 feet of space; which is one 16th of the effect of that issuing from the lower hole, and is in exact proportion to the height.

It is true the motion of the vessel would not be as here supposed, but that part of the power or motion of the issuing water, which was not expended on the vessel,

would be retained by it, and might be used on any other body opposed to it's motion. And if the vessel were kept stationary, the power of the issuing water would remain entire in itself, and would (leaving the waste of power by the dashing of the water out of the calculation) be such, as any other body in motion would have, agreeably to the law we have supported, viz. As the square of it's velocity multiplied into the quantity of it's matter, which is in geometrical proportion to it's height.—For, if we estimate it's velocity from the upper hole as 1, and quantity 1,---the power would be 1.---If from the lower hole as 4, the square of 4 is 16, for every quantity equal to the above, which is 1.---It is also evident, that 4 times more would issue from the lower hole than from the upper hole *in the same time*; but then it's work will be 4 times more than *it's proportion* in the same

same time, and we are not to measure work by time, but by the quantity done, or expence of power applied to it:---For the same reason, if I have 3 hundred weight of matter to lift through 1 ft. of space, and have three men to effect it, each of whose strength is equal to lift 1 hundred weight through that space, I may accomplish it either by their joint effort on a single pulley, or their alternate efforts by means of a three-fold pulley; and although the latter means will be three times as long in action as the first, yet the power expended, and the effect produced must be allowed to be the same in both cases;---and arguments before urged tend to prove the same thing.

A similar reasoning holds, if instead of the large vessel mentioned above, a regular small tube with a reservoir at the top were used; for although in this case the water would

would not issue from a hole near the bottom, but with half the velocity actual to the pressure of such a height, (for reasons before given;) yet the relative and comparative action of the water issuing, would be in proportion to the square of it's natural velocity and expanse, or to it's height and expanse, which keeps the same proportion; and this is demonstrable, whether we found the consideration of it on that certain law, that action and re-action are equal, and in contrary directions, or trace the mere action of the column of fluid pressing on the part immediately opposite to the aperture of the same size, and the motion of the issuing water, for they are dependent on each other.

Thus, if such a tube as A, B, fig. 4. pl. 2, one inch square in cavity, and 50 inches long, contained water to the height of 49 inches from B, the pressure on a square

square inch about that point would be equal to the weight of 49 cubic inches of water, and the pressure on the square inch opposite to it would be (from their mutual action) the same; therefore the tube would have no more tendency to move one way than another; but if a hole of 1 inch square be opened at B, the pressure would be taken off from that side;---and if the vessel were large enough, to suffer the water to run off with it's natural velocity from the aperture, it would also continue to press with it's natural weight on the square inch opposite, and act as in the former mentioned vessel; but as that is not the case, whatever pressure be destroyed, and becomes wanting to force the water out at B, must also be wanting to press towards C;—if then we suppose each of these to be but half it's natural weight, it will be just as if the column were divided, and a weight, equal to that of 49 cubic inches

2

of

of water, were requisite to keep the balance against the re-action of that issuing at B, which instead of running off with the velocity of $\frac{7}{7}$ (the square root of 49,) would do so but with the square root of 24 and an half which is a trifle less than $4\frac{5}{100}$, the power in the action and re-action of which quantity is but as 24 and an half, whereas if the vessel were large it would be as 49. The power or quantity of work this will do will therefore be as the expence and fall of water in the overshot wheel, and all other cases.

SEC-

SECTION VII.

Of Barker's Mill.

THIS, therefore, determines the power of Barker's mill, a contrivance intended to direct the re-action of spouting water to the purpose of grinding corn or other work, and which is recommended for it's simplicity, and small degree of friction, (having no wheels,) but turning on an upright spindle, passing through an erect and cross tube ; as in the fig. [pl. 4. fig. 1.] the tubes A, B, and C D receiving water from a reservoir ; at the extremity of each arm, and on opposite sides, holes are opened, and by the re-action of the water spouting

G through

through them, the whole continues to revolve, turning a millstone fixed to the spindle at E.

If this machine be prevented from turning, the power of the water issuing from the holes will be, as before shewn, a compound equal to the height and expence of the water, just as in overshot wheels * ; but

* The philosophical reader will be here struck with the appearance of an accession of power to this machine, by the action of the centrifugal force, co-operating with the weight or pressure of the water in the upright tube, by which the work effected seems to increase beyond the quantity of the power applied, but the fallacy of this appearance will be seen, on recollecting, that this machine is no other than an inverted centrifugal pump, and as in that machine, the resistance to the power applied to work it, proceeds from new matter constantly arising to be put in circular motion, which is in exact proportion to the water raised and the height it is raised to—so in this the diminution of the power of the machine by fresh matter falling into the cross tubes to be put in circular motion is in exact proportion to the seeming increase of power by the centrifugal force acquired: therefore although the work done by the machine be increased by the centrifugal force acting on the water, yet the expence of power keeps exact pace with it.

for

for their action to be equally great on this machine, it is necessary, that the whole motion of the issuing water be expended on it, which cannot well be done, but by receiving it's action on some moveable body, which will communicate it to the former, and that may be effected by applying a recipient horizontal wheel, and connecting it to the cross tube by a vertical wheel.— This it must be allowed, complicates the whole to such a degree, that it leaves it no other preference to the overshot method, but that a wheel (or circle formed by the revolution of the cross arms,) of a moderate or even small size will do the same work, as a larger one at an equal expence of water, as to quantity and fall. For in the former, if the water acts by it's weight only, it is certain, that the wheel must be equal in diameter to the fall of the water ; but in the latter case, the action does not

depend on the length of the cross arms, but on the height of the upright tube, or rather that of the water contained in it, and even this part may be improved by connecting the pipe, which brings the water for it's supply to the upright tube, by a water-tight joint, guarded by a leather flap, as in the pl. 4. fig. 2. which also represents the before mentioned addition, intended to communicate the whole action of the issuing water to the performing the work of the machine;—but that this may compleat the whole intention, it will be necessary, for boards to be so fitted within the trough of the recipient wheel, that, by the action of the water, they may rise and obstruct the current, which might otherwise take place round it, and thereby waste part of the power. No such contrivance as this last is necessary, to prevent the loss of power, by the yielding of over-shot wheels to the impulse of the descending

ing

ing fluid, for they are in themselves admirably adapted to avoid such loss, which will appear if we consider the different motions as to perpendicular fall, of the water contained in each bucket, whilst the wheel revolves.

Description of fig. 2, plate 4.

- A B C D—The frame of the Machine.
- F G The upright Tube, }
 H I The cross Tube, } Corresponding to those of fig. 1.
- K L The recipient wheel, which, by the action of the water issuing from the cross tube, is turned (in a direction contrary to it) round the Spindle S, on which it is supported by a Nut under the Block R, being kept in its horizontal position by working round the Spindle by a Collar in the centre of the Wheel M.
- M N O Wheels, which connect the cross Tube and recipient Wheel, so as to resolve their action to the same effect, the axis of the Wheel N being fixed to the Spindle S.
- P The upright Spindle, which passing down through the upright tube and turning on the head of that round which the recipient wheel turns, revolves with the Machine and works the Stones.
- Q A close Pipe, which brings the water to the Machine, and ending in the Box E, is there connected with the upright Tube by an iron Collar, guarded by a leather Flam, which hinders the water from escaping, but through the Tube.

SECTION VIII.

Of the due proportion of Resistance, applicable to a Machine worked by the third kind of Power, or Percussion, in order to cause it to effect the most Work.

BUT leaving at present the consideration of this particular, it will be proper to investigate, and form our judgment on a doctrine generally received, which is, that in order for any power to produce the greatest effect in a given time, by it's application to any given machinery, it is necessary that it should move the part on which it acts, with one certain degree of it's own independent motion.

Thus

Thus far must be true, for if either the machinery remained unmoved, or had a velocity equal to the power, that power could effect no work by it; the due proportionate difference must therefore lie between those extremes; and that difference, it is alledged, should be just double in the power of what would be a balance to the weight, or work done; or in other words, a machine should never be loaden with more or less weight or opposition to the power, than just half of that, which would be an equal balance to it.—And the reason which has led to this position, is; that under these circumstances any power (unlimited in it's duration,) will effect that portion of work in the shortest time; and this so far as it is confined to such particular circumstances, agrees with the theory laid down in the preceding ages, as will be clearly explained in the diagram, Plate 5, in which A B is intended

intended to represent a lever, (or rather wheel and axle in peritrechio,) having wheels imagined at each division of the lever, whereby to suspend the weight C, to represent the power acting on A, the raising which represents the work effected, and as their weights are equal, the first being hung on at C, will be just a balance to the latter.

As it has been shewn, that when a body falls from any height, it's strokes or percussion are in simple proportion to the heights, and it's velocities as the square root of the heights, so, if such a body be attached to any machinery, &c. whereby part of it's power in the fall may be expended, the difference between the power exerted, and that expended, will remain in the body, and it's average velocity throughout will be consequently as the square

square root of that difference.—Suppose therefore the weight at A were to be raised, no motion could take place; but if it be moved one division further from the center, (and no friction supposed,) it would then descend to F 101, in which time it would raise the weight A 100; the difference between them, therefore, represents the comparative difference between the power expended, and the work effected, which is 1, whose square root 1, is the velocity with which it would move, compared to that it would acquire by being placed further onwards; which suppose to be at 125;—that number is the distance to which it must fall, to raise the weight to 100.—The square root of the difference being 5, is therefore the velocity of the weight of falling from this part, and so on as expressed by the figures in the diagram.

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This

This being the case, if the distances through which the power must descend, (to bring the lever into the direction D E as before,) be divided by the comparative velocities from each place of suspension, the products will be the comparative times in which the same weight will raise the weight A as required, and this time will invariably be found to be least, when that power is double the distance from the center or fulcrum of the lever of that point at which it would balance the weight.

Description of Plate 5.

Plate 5 includes three diagrams expressed by the three different kinds of lines, viz. full, short dots, and long dots, the first being included in the second, and both in the third. In each, the spaces above their respective cross-lines shew the distance through which the power (expressed by the Weight C) must fall, before as much be expended as is equal to raising the Weight A by the whole fall of the lever. The length of the several lines below the cross-lines, shews therefore the excess by which the average velocities are found (by extracting the Square Root). The lengths of the several lines are selected to answer to such velocities as may be expressed by whole Numbers.

The times of falling through the distances as expressed by the *full lines* in the diagram, Plate 5, will be according to the following proportion :

Distances to fall to bring the lever to the angle of 45 deg.		Comparative velocity.		Comparative times.
101	-	1	-	101
125	-	5	-	25
149	-	7	-	$21\frac{2}{7}$
164	-	8	-	$20\frac{1}{2}$
181	-	9	-	$20\frac{1}{9}$
200	-	10	-	20 least
221	-	11	-	$20\frac{1}{4}$
244	-	12	-	$20\frac{1}{3}$
269	-	13	-	$20\frac{2}{13}$
296	-	14	-	$21\frac{1}{7}$

Nor would this rule vary, with the alterations of proportion between the power and weight, or the angle to which the lever descends; for if a weight of one quarter of

H 2

A were

A were hung on at 400 it would balance, then would it be found that at 800, (double according to the rule,) it would fall to the angle of 45 degrees in the shortest time, as follows :

500	-	10	-	50
596	-	14	-	$52\frac{4}{7}$
689	-	17	-	$50\frac{9}{17}$
724	-	18	-	$40^{\frac{9}{9}}$
761	-	19	-	$40\frac{1}{19}$
800	-	20	-	40 least
841	-	21	-	$40\frac{7}{21}$
884	-	22	-	$40\frac{4}{22}$
929	-	23	-	$40\frac{9}{23}$
1025	-	25	-	41
1076	-	26	-	$41\frac{5}{26}$
1184	-	28	-	$42\frac{8}{28}$
1300	-	30	-	$43\frac{7}{3}$

or if it had to fall to the lower angle G H, or any other, it would be found to make no difference in the proper point of suspension, for the comparative velocities and distances would be as marked in the *dotted lines*

lines in the diagram, which will shew that the weight will fall to 1584, in the shortest time on the same line as before, according to the following scheme.

900	-	10	-	90
996	-	14	-	$71\frac{1}{2}$
1200	-	20	-	60
1425	-	25	-	57
1584	-	28	-	$56\frac{2}{11}$ least
1700	-	30	-	$56\frac{2}{3}$
1889	-	33	-	$57\frac{8}{11}$

Hence it appears clear, (without the use of Algebra,) that under all circumstances, in which the duration or continuance of the power is not considered, such as that of a machine worked by a wheel limited in size, receiving water without percussive, and passing through an indefinite fall or power acting by gravity, to draw a weight up an inclined plane, or work pulleys, &c. the greatest

greatest advantage is made of the power when the machinery on which it acts is laden (by work and friction,) with no more than half of that which would be a balance to it. But to extend the same law to cases in which the continuance of the power is limited, and of which every advantage might be taken, such as any certain quantity of water in a reservoir, acting by its descent through a limited fall, is using that power to great waste, and suffers such water to run off with a considerable part of the power it acquired in the fall. For if the fall of the weight from 401, were limited to the line I K, and it were to be hung on the wheel, supposed to be on the lever, at 800, it would fall with a velocity twice as great as if it were hung at 500; but if it were discharged at the line I K, another power equal to it must at the same instant take its place at 800, so as to bring the lever to the
line

line E. In the same time that this would be effected an equal weight at 500 would have reached the *dotted line*; therefore, although at 800, twice the quantity of power would have been expended, yet at 500, it would have wanted but one-fifth of effecting the same work in equal time, and, by various applications of machinery this work might be varied *in infinitum* by an exchange of quantity of work, for velocity or quickness of time, and *vice versa*.

If we apply this doctrine to overshot wheels, receiving water from a reservoir circumstanced as above, we shall find that the slower the wheel goes, so as it be fast enough to keep on it's motion, the more work will be done at the same expence of power. Experience it is true, opposes itself in some measure to this doctrine, but I think the apparent contradiction between theory and
 practice

practice may be satisfactorily accounted for, not only by the friction of the machine making a considerable difference in favour of the usual method but also on the following principle.

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SECTION IX.

Of Fly Wheels, and their Effect on Machines.

IN all machines to which water is applied, the work intended to be performed by it is not perfectly regular and uniform, and therefore a Fly Wheel, or some substitute for it, is necessary to regulate the motion and prevent a stoppage, when any extraordinary obstacle to the movement occurs in the work.

When the motion is very slow in a water wheel it cannot act as such a substitute, but if it has considerable velocity it may. The

power lost by such velocity is, therefore, not so great a disadvantage as the loss of the wheel's action as a regulator.

Whether then, by the application of such a fly that office might be taken from the wheel, and an advantage gained by it's being made to move slower than is generally done, is certainly worth enquiry; and to proceed in it we must investigate the laws on which the action of such Fly Wheels depends, in which it is more necessary to be particular, as their use in most kinds of machinery deserves such attention.

As action and re-action are equal, and in opposite directions, and it being impossible that an effect can be greater than it's cause, therefore a Fly Wheel can only regulate, not increase the power of any machine; it's use being to act as a reservoir to receive
the

the redundancy of the power applied, when either by a variation in it, or the work, the proportion of the former to the latter shall be greatest; and to return that power when it bears the least proportion to the work.

It has been before shewn, that the power or force of bodies in motion by their percussion, is as the square of their velocities multiplied into their quantities of matter; consequently, that the velocities of bodies as acquired by power impressed, are as the square root of the powers divided by the quantities of matter;—if then, that power be derived from a body in accelerating motion (such as a Fly Wheel receiving motion from a falling body,) the Fly will also receive an accelerating motion in such proportion, but it's degree of motion at the same distance of falling will be less.

Thus, suppose one pound weight of matter having fallen through 16 feet, the velocity it has acquired at that point we will call 4; the square of which multiplied by 1, the weight, is 16, which expresses it's power of percussion. Now, if a Fly of 3 pounds weight had been so attached to the 1 pound, that it's motion should act with it, (without the 3 pounds falling at all, and that the motion of each should be equal to the other,) for the reason above assigned, the velocity of the 4 pounds could be but as 2, for the square of 2 is 4, which multiplied by 4 the quantity is 16 as before;—at 100 feet fall, the velocity of the single pound would be as 10, the square root of 100.—Thus do the proportions of acceleration continue the same, at the different distances of fall; but the actual proportion of motion will be less, as the Fly is heavier than the weight, which occasions the power. If the Fly be
so

so connected with the power, that it's velocity shall exceed that of the other, then will the retardation of the motion of the power exceed the preceding statement in proportion to the square of the excess.

Should the work to be done by a machine be perfectly regular and uniform, as well as the power applied, no advantage can be gained by the application of a Fly Wheel to it; for the expence of power in communicating motion to it, must be as great at least as that which the wheel can return; but in proportion as the work or power is subject to variations, so should the proportionate weight of the Fly, and it's velocity be greater or less, it will therefore be difficult to fix a general standard; we may however conclude, that such an auxiliary power should never be greater than that which would just answer the purpose of regulating

gulating the machinery, as it must be attended with some friction, (however nicely suspended;) which, as it depends much on the weight should therefore be as little as needs be; besides, that the heavier the Fly, the greater will be the difficulty of stopping the machine when necessary, and therefore the greater the power lost in that operation.

SEC.

SECTION X.

Of the Proportion of Resistance proper to be applied to a Machine worked by the second kind of Power, or Percussion.

IT is to be noted, that the preceding investigation of the degree of motion necessary to be obtained in a machine, in order to work it to the greatest advantage, applies only to such as are impelled by a power of the third sort, being connected with the machinery from the beginning of it's motion—but in such as are acted on by percussion, another law obtains, which we will therefore proceed to enquire into, after recapitulating

lating that we have endeavoured to shew, that the primary and obvious modes or qualities of independent matter in motion are three, viz.

Weight or quantity of matter,
Velocity, or quantity of motion,
Impetus or quantity of power.

The comparative quantity of either two of these in two bodies being given, to find a third agreeably to the preceding doctrine.

Two bodies differing only in quantities of matter. } Their comparative Impetus will be in geometrical proportion to their weights or quantities of matter.

Bodies differing only in velocity or quantity of motion. } Their comparative Impetus will be as the squares of their comparative velocities in whatever numbers expressed.

Hence two bodies differing both in velocity and weight. } Their comparative Impetus will be as the square of their velocity multiplied by their respective quantities of matter; 1lb. with the velocity of 10, is equal to 100lb. with the velocity 1lb. &c. &c.

there-

Therefore two bodies whose impetus and velocities are known. } Their comparative quantities of matter are found, by dividing their impetus by the square of their velocities.

Two bodies whose impetus and quantities of matter are known, } Their comparative velocities are found, by dividing the impetus by the quantities of matter respectively, and extracting the square roots, which are the comparative velocities.

Hence if two bodies have different quantities of matter and equal impetus } Their comparative velocities will be as the square root of each other's quantity of matter inverfely.

If two bodies have the same quantities of matter and different impetus } Their comparative velocities will be as the square root of their impetus respectively.

If two bodies have different velocities and equal impetus } Their comparative quantities of matter will be as the square of each others velocities.

If two bodies have the same velocities and different impetus } Their comparative quantities of matter must be as their impetus respectively

matter velocity inches

1 - 4 - 16

4 - 4 - 64

- - - - —

4 - 1 - 4

4 - 4 - 64

K

It

It is evident that agreeably to these data, if an independent body, having a certain degree of velocity overtake and strike or impinge on another independent body, moving in the same direction, but with less degree of velocity, the impetus which they jointly possess after their union will be the same as that which they had in their separate states of motion; therefore to find the velocity with which they will proceed conjointly—add their separate impetus or percussions together, which divide by their joint weight, and from the product extract the square root, it will be their joint velocity. Thus, a body of 6, with the velocity of 3, overtaking and striking a body of 4 with the velocity of 1, they will proceed together with the velocity of 2, 402 nearly; but if the latter body be so attached to any matter in motion as to be hindered from moving on with the former, the impulse

finite distance; it will not therefore be necessary to take the quantity (or number of parts in the direction of the current,) into the account of their action, as it would be if the parts were unconnected, and only such a quantity possessing a given space, as that one should have finished it's effect before the other impinged.

Therefore, the square of the difference of the velocities of the stream and wheel will represent the quantity of power which the latter will receive, or the work it will do, and the line A B the velocity or celerity with which it will do it; and it will be found, that this proportion is the most advantageous of any other, as is proved by trying the effect of that proportion, and varying it to a measure on either side, thus :

Square 20 is 400	which mult. by vel. of work 10	is 4000
Now Sq. 21 is 441	do.	do. 9 is 3971
So sq. 19 is 361	do.	do. 11 is 3969

And

And yet less would it be found by trying any further proportion ; it therefore follows from this position, that as the square of 30 is 900, (the whole action of the stream,) and the square of 20 is 400, (the action of the stream on the wheel, when in motion as above) such wheels should be laden with $\frac{400}{900}$ or $\frac{4}{9}$ of the whole power of the stream, in order to do the most work to the best advantage.

S E C.

SECTION XI.

*Of the Action of Fluids in Motion on Plane
Surfaces inclined to their Currents.*

HAVING thus far treated of the *direct* action of fluids in motion, or bodies whose surfaces are opposed perpendicularly to their current, it remains only to enquire into their lateral effects on those bodies whose surfaces decline from that position, and which are so confined as to yield only to the action, in a direction crossing that of the stream; such as the vanes of windmills, rudders of ships, &c.

Much

Much has been written on the subject of these machines, to prove that there is one certain angle of position between the current of fluid, and the inclined surface which gives it the greatest advantage; and this is generally agreed to be 54 deg. 44 min.—Why I cannot assent to this opinion will appear from the following investigation, in which to proceed with perspicuity, it is necessary to simplify the action and effect as much as possible.—Now it has been shewn, that the comparative powers of fluids (like those of other bodies) in motion, are in their perpendicular effect, on equal surfaces of bodies at rest, as the square of their velocities; and should the extent of their surfaces vary, it is evident that they must be as the square of the fluid's velocity, multiplied by the surfaces of the supposed bodies;—which surfaces represent the quantity of fluid acting on them.—Thus, should
a body

a body at rest, present a plain surface of 2 square feet (or 288 inches) to a current, it will be acted on by a force double of that by which a surface would which measured but 1 square foot (or 144 inches) and as we are now only enquiring into the relative action of a current of the same velocity on different inclined planes this example is sufficient to our purpose.---To understand the effect of a power applied to such an inclined plane as is above mentioned, we may be assisted by figure 3. plate 3.

Suppose the line A C, to represent the inclination of a plane, which with A B and B C form a triangular body so placed on friction wheels as to prevent it's moving but in a direction parallel to C B or B C; now, if a weight of 10 pounds be applied at A, and confined to a perpendicular action by a rod passing between rollers, &c. it's effect

effect to move the triangle C B will be equal to 10 pounds, and it would sustain a weight of 10 pounds attached to a line and carried over a pulley in the opposite direction, because the base and side which form the triangle are equal; but if the line of inclination be carried to D, and A E and E D form the figure as before, so as to make A D double of A E, the weight 10 pounds would in that case support 5 pounds only, and so on in the same proportion; that is in all cases, as the line of the side of the triangle in the direction of the weight's action is to that which forms its base, so will be the weight sustained, (which represents the lateral action of the 10 pounds so confined as above,) to 10 pounds, which represents the direct action of the power;---it is therefore evident, that the less the angle made by the inclined plane with the line A B is, (being the direction of the perpendicular

L dicular

dicular action of the weight,) the greater will be it's action on the plane in a lateral direction ; and as the action of the weight may represent the action of a column of fluid of any determinate volume, (*provided that fluid were not liable to be diverted from it's course by the re-action of the plane,*) we may fairly conclude from thence, that the less inclined any plane be when presented to such a volume, the greater power would the fluid have upon it, to put it in some degree of motion ; and that, in proportion as is the product of the side of the triangle divided by the base, (which represents the mechanical power of the inclined plane) multiplied by the base, (which also represents the direction of the volume of the fluid ;) but it is obvious, that if the inclination of a determined surface vary, the volume of the fluid it will embrace must also vary in
the

the following proportion, according to the angle here laid down.

o. I		base of triangle		side of ditto.
5.44	-	1,000	-	9,950
11.33	-	2,000	-	9,797
17.27	-	3,000	-	9,540
23.35	-	4,000	-	9,165
30.00	-	5,000	-	8,660
36.52	-	6,000	-	8,000
45.00	-	7,071	-	7,071
44.26	-	7,000	-	7,140
53.08	-	8,000	-	6,000
64.09	-	9,000	-	4,360
90.00	-	10,000	-	0,000

For as the base is the division of the side, to find the power of the plane, and also the multiplier of the product, (as representing the volume of the fluid,) the power of action will still be *as the side of the triangle*, and therefore greatest, the less the angle which the inclined plane makes with the

direction of the current, although not in the degree of the former case; but this conclusion (as was before observed) is under the premise, that “ the fluid is not liable to be diverted in it’s course by the re-action of the plane,” as is the case with the weight of 10lb. acting as above:—what alteration of effect takes place by this re-action therefore remains to be considered, and I believe we shall find, that this important matter is subject to variation according to the circumstances attending the fluid, which is the moving power; as first, in respect to the elasticity of the fluid; for should it have much of that property, and the angle of the inclined plane on which it strikes be very acute, it will have a greater tendency to fly off with more force, and therefore less of it’s power will be expended on the plane than if it had less of it. The same inclination therefore cannot be proper for air and water;—secondly,
the

the more the acting power be perfect as a fluid, the more easily will it admit of an alteration in the direction of it's course by the re-action of the plane; and thirdly, if the current be more or less confined against the plane of an adjacent body, it will occasion it to act with more or less of the disadvantage that arises by the easy diversion of it's course.

These considerations, I fear, render it impossible to reduce the subject of the action of Fluids in general when in motion, on inclined planes, to any fixed or determinate rule; and were it otherwise, it is obvious, that the action of the Fluid as before defined, would apply only to the effort it would exert on the plane before it began to move, when no quantity of *time* can be taken into the calculation of it's effect upon it; but it is clear, (considering the inclined

1

plane

plane as a mechanical power opposed to the current,) that if the angle made by the plane be very acute with the direction of the current, it must not only be subject to the inconveniences we have before observed, and also lessen exceedingly the volume of current it embraces, but must of it's remaining proportion lose as much in time or space as it gains in power.—On the other hand, if we apply it to the rudder of a ship, and it's angle to the current be brought near to a perpendicular, it will much impede the velocity of the ship; and if to the sails of a windmill, it will divert the force of the wind applied to the sails too much to that part of the axis which hinders their yielding to it's direct impulse, and thereby occasion the greater friction; in both cases counteracting the desired effect.

It

It may be also considered, that when the plane be laid, either very near or very remote from the direction of the current, the least alteration in that direction may reduce it either to a parallel, or perpendicular line to it, and thereby destroy the whole intention.—Upon the whole of these considerations, therefore, I cannot think that any precise angle is determinable as possessing the greatest advantage; but should suppose that of 50 degrees from the current would be found as advantageous as any, making allowances for the various circumstances attending the power as before mentioned: perhaps 54 deg. 44 min. may be as near, but the objection I make to it arises not only from the above reasoning, but also from the appearance of false premises in determining on it.

If

If my mode of considering it be just, the variation of the angle can be considered only in the same view as any other mechanical contrivance presented to a power, and in respect to the work to be accomplished by it, subject to the same rule as was laid down in the preceding section; that is, if the moving force and the power of the machinery be determined, it will do the same proportion of work to the best advantage, as a water-wheel (considered as a continued lever) was there said to do; which is equal to four-ninths of what it would sustain, (whether the lever contained in the wheel be long or short,) and if the work and moving power be determined, the angle and extent of the inclined surface exposed to the moving power must be regulated accordingly.

S U P P L E M E N T.

MANY of the preceding thoughts were thrown together, with a view to improve in the best manner a mill worked by a stream of water, the power of which was in a great degree wasted ; and having succeeded in it by a mode, which, though simple, appears to be new, I shall therefore attempt a description of it, as it may not be altogether useless to such as have any concern with machinery under the like circumstances.

The stream alluded to is from a constant spring, affording about 400 cubic feet of water per diem, issuing from the side of a hill, which falls gradually through 48 perpendicular feet in the course of about 50 yards.—At this distance was a Corn Mill, having an overshot wheel of 23 feet diameter;—from this spring therefore to the crown

M

of

of the wheel is 25 feet fall, which ran to waste, (except the action of the head of water in a reservoir just above the wheel, of about 6 feet when full.)—Had not the Mill been already built, the erecting a wheel equal in diameter to so great a fall, and the inconvenience of connecting the machinery to it's shaft or axis at such a height, would have been obstacles too great to have permitted the application of the whole fall of the stream to one mill in the common way, and the reasonings in the preceding part of this treatise determined the preference in my mind to the principle of overshot wheels receiving water without percussion. I therefore considered that if an additional water-wheel, equal in diameter to the loss of fall were erected on the side of the hill, wholly above the level of the old one, and both connected together, the same water might turn both, and perform (at least)

double the work which it did before: in consequence I occasioned a reservoir to be made nearer the spring, from which pipes of six inches and an half bore were led down the hill to an upright tube which so delivered the water near the crown of the upper wheel as to turn it backwards.

The two water-wheels are connected by a chain passed round grooved wheels fixed to the arms of each, and as I conceived the first wheel went too fast, when it gave a proper velocity to the stones, the upper chain-wheel was made of 15 feet diameter, and the under but of 10—which consequently occasioned the fall of water in the buckets, or revolution of the former, to be slower than the latter.

I had the satisfaction to find the success exceed my expectation, as instead of double,

ble,

ble, the Mill will now do treble the work it would before with the same quantity of water, which is accounted for by the friction being but little encreased, though the power of the Mill be more than doubled. The figure will perhaps give a better idea of it than any description by words only.

E X P L A N A T I O N .

A, the tube which brings the water from the reservoir to B, an upright tube, open on the top to suffer the water to rise when suddenly stopt.

C, a horizontal tube which conveys the water to the upper wheel, and which has an aperture in the wider part of it's extremity, being opened and shut by a sliding hatch connected to an upright lever which turns on a fulcrum at D, and which being joined to a horizontal one at E, and that leading to a small lever at F, the hatch is opened and shut by a person within the Mill-house.

G and H, the upper and under wheel, connected by the

two

two grooved chain-wheels I and K---the chain being 113 feet long and weighing one pound to a foot.

L, a double grooved roller in the interfection of the chain, to keep it's parts afunder to prevent rubbing.

M, the trunk which conveys the water to the lower wheel after it has passed the upper one.

I fhall conclude this treatife with the following description of a Machine, which I have lately constructed, for a prefs in the procefs of Cyder making, but which is applicable to many other fimilar operations, and is more fimple and lefs liable to injury or difficulty of repair than any other which has fallen under my obfervation; the power is alfo very great, being as 1 to 1136 nearly, and capable by a trifling addition of any other proportion.

A A Two pieces of timber 21 feet long, 12 by 6 inches, laid fide by fide at the diftance of 12 inches, and fecured in
that

that situation by blocks placed between and bolts passing through them; this frame forms the bed of the machine.

B B Two uprights 12 feet long 6 by 8 inches morticed, upon them, and secured in their position by pins, and iron squares.

C C Two uprights 5 feet long 6 by 10 inches, morticed near the end of the under frame, and secured as before.

D a lever 17 feet long, 12 by 13 inches, turning on a large bolt which passes through the short uprights—also through iron straps, which secure them to the bed inside, and a stirrup of iron which passes over the end of the lever, and which makes the turning point in the line of it's lower side and not through it's middle.

E a lever

E a lever 20 feet long, 6 by 8 inches at it's largest part, and tapering towards the other end: this lever turns on a bolt in the uprights BB.

F 1, 2, 3, 4. Four pieces of oak (which I call needles 10 feet long) 4 by 2½ inches, morticed loosely into the upper lever, and hung thereto by bolts, so as to swing perpendicularly, and play in a long mortice or channel cut through the large lever to receive them. These needles have inch-holes pretty closely bored through them (in a direction crossing the machine,) from the lower ends, as far upwards as the great lever will reach, when it is as high as it can go.

G a bed to receive what is to be pressed.

H a frame to support a winch worked by a handle at I.—At the end of the small lever two blocks or pulleys are fixed, one above
and

and the other below it—a rope of about half an inch diameter is then fastened to the cieling, (or continuation of the uprights of the winch frame if necessary,) at **R** ; then rove through the upper block on the lever, from thence passed through a block at **L**, and then goes with four turns round the winch, from whence it is carried through the block under the lever and fastens to the machine at **M** ; by this means, if the winch be turned one way it raises the end of the small lever, if the other depresses it.

To work the Machine.

If we suppose the great lever bearing on the matter to be pressed, an iron pin must be put into one of the holes in the needles above the great lever, and when the small
 lever

lever is worked as far as it will go, either up- or down, another bolt is to be put into the hole, which comes nearest above the great lever on the other side of the uprights BB. and the winch then turned the contrary way, by which means the pressing goes on whether the small lever rises or falls ;—before the resistance is very great, the needles farthest from the fulcrum of the small lever are used, after that the nearest are employed, which doubles the power of the machine.

In raising the great lever or lowering it to its bearing, the needles most distant from the fulcrum of the small lever are used *under* instead of *over* it.

As the rope is liable to stretch and get slack I pass it, (after taking two turns on the winch, through a pulley, to which is sus-

N

pended

pended a weight of half a hundred, and then take two turns more before it is carried through the other block, by which means the flack is constantly gathered in, and the weight *holds on* without increasing the friction, as by hanging under the winch it counteracts the pressure upwards on it's axis.

The direction of the pressure of this Machine is not perpendicularly downwards, which is in some cases an inconvenience; but by applying a sharp or round billet between the lever, and the follower, which presses immediately on the subject of the work, it is in a great degree obviated—and an advantage of no small import in addition to those before mentioned, attending this Press above most others, especially wooden screws of the common kind, is the elasticity of the levers which follow the pressure after
the

the winch is stoppt from working; not to mention the *bevel* of a wooden (or other such) screw acting as a mechanical power to increase friction.

F I N I S.

Also, published by the same Author, Price 2s. 6d.
Remarks on the comparative Advantages of Wheel Carriages of
different Structure and Draught.

(10)

ERRATA.

In advertisement line 4, for *io* read *to*.

Page 9 lines 7 and 8, for *Doc rine* read *Doctrine*.

13 line 13, for *Equally* read *Equably*.

34 line 7, for 18 read 16.

38 line 2, for *aētual* read *natural*.

40 line 4, for $\frac{1}{7}$ read 7.

47 line 20, for *ages* read *pages*.

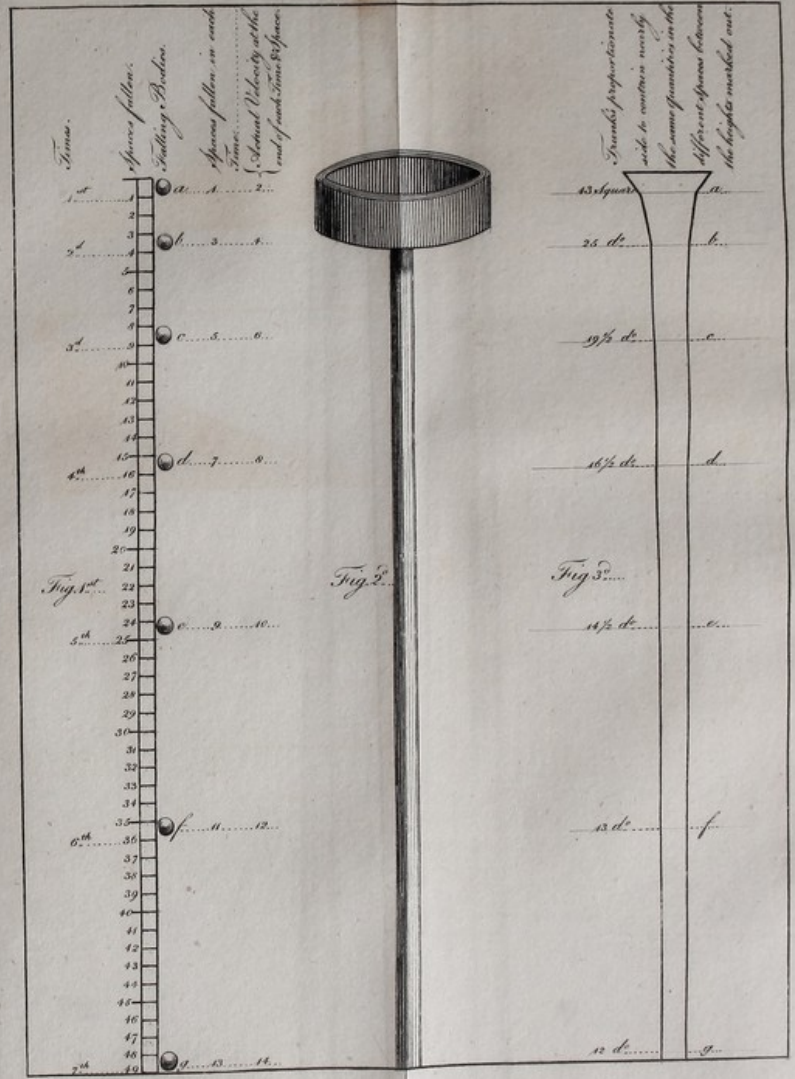
48 line 2, for *peritrechio* read *peritrochio*.

65 head of 3d column of figures, for *inches* read *Impetus*.

75 head of 1st column of figures, for 01 read *Angle*.

86 line 9, for *morti ed* read *morticed*.

Plate 2, Fig 1st, *E F* wanting.



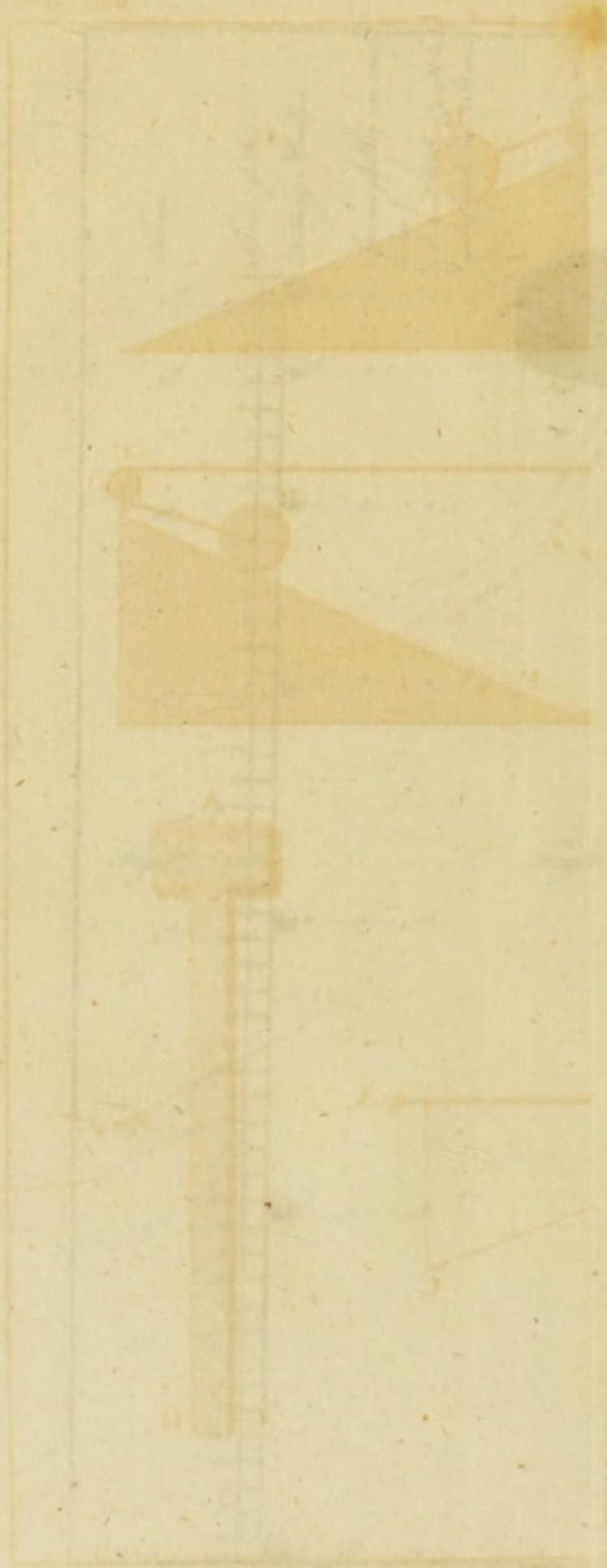


Fig. 1.^d

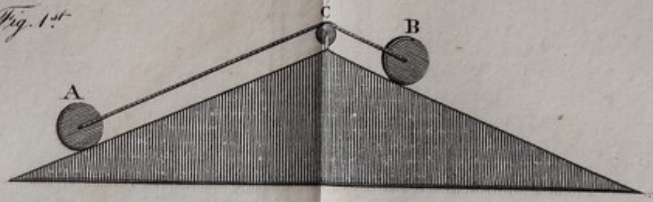


Fig. 2.^d

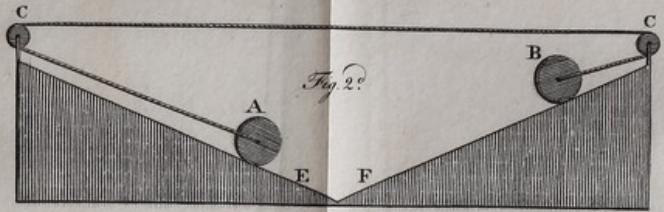


Fig. 3.^d

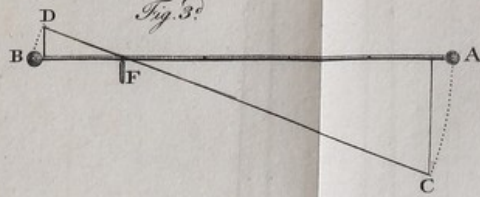
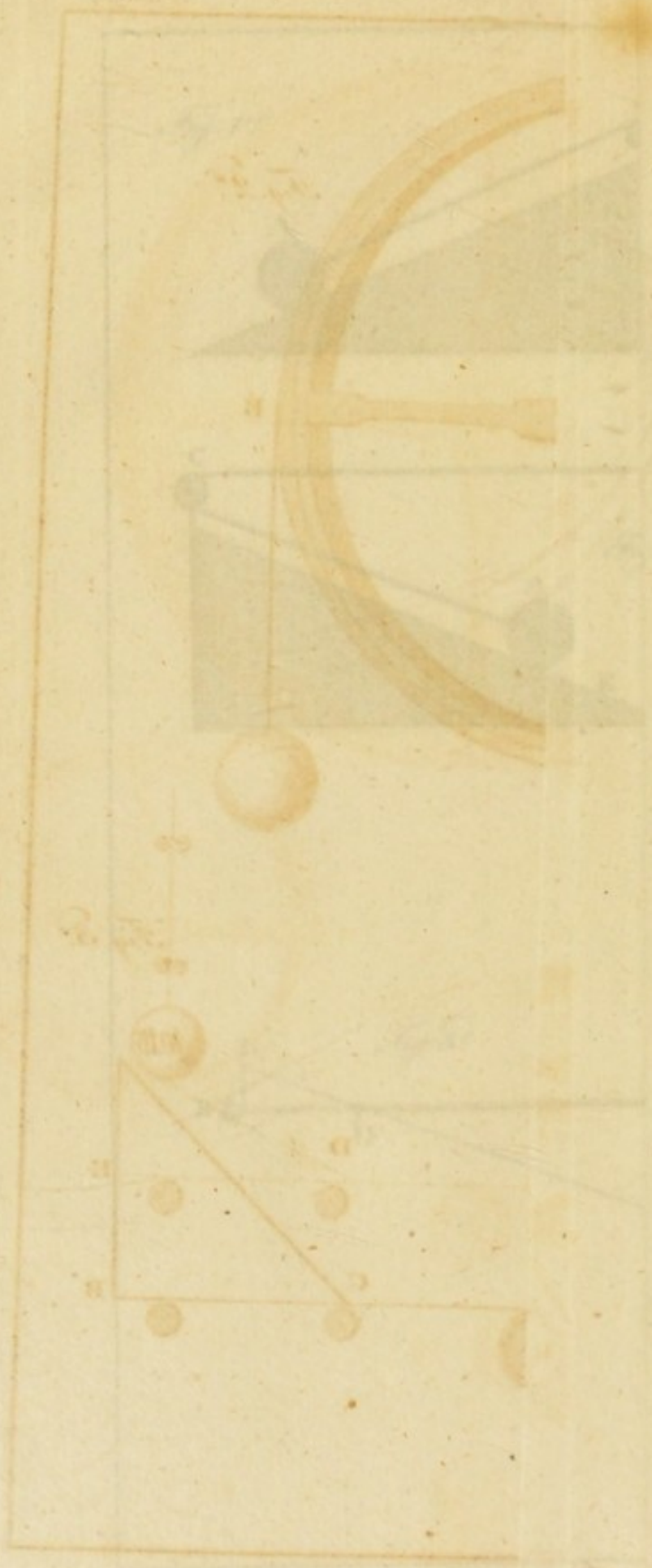
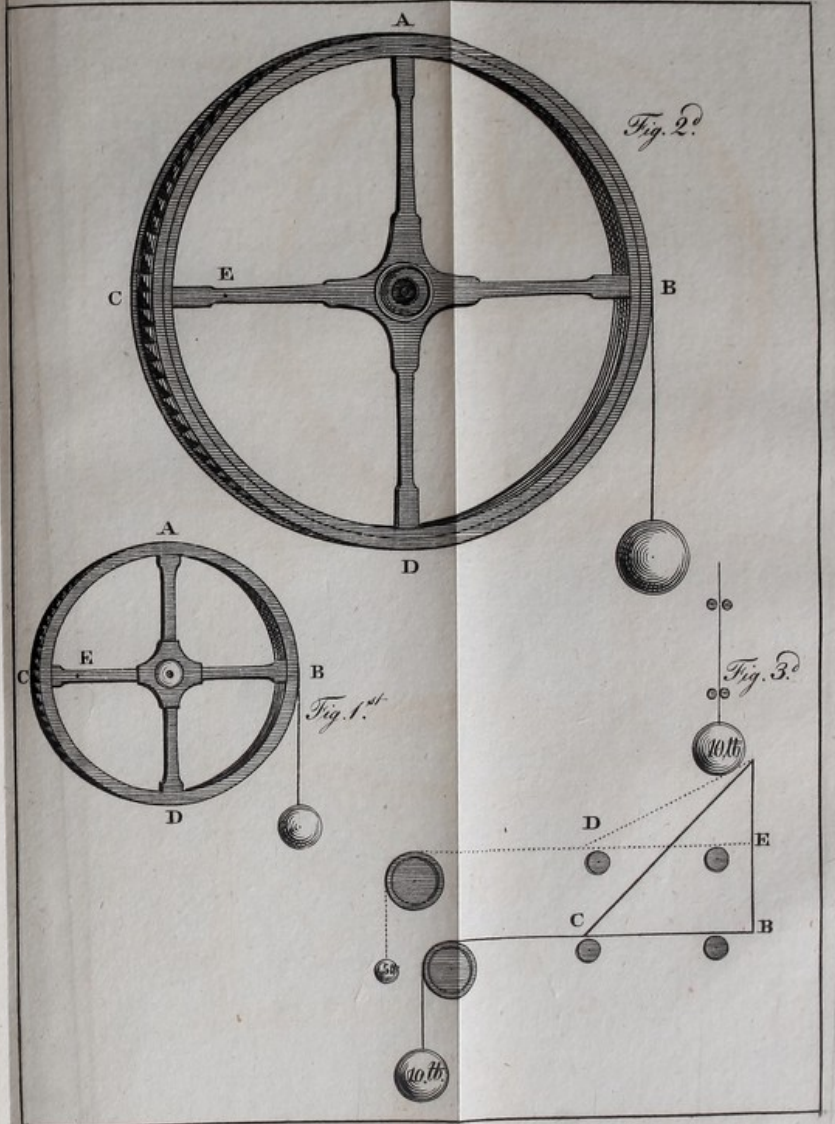


Fig. 4.^d







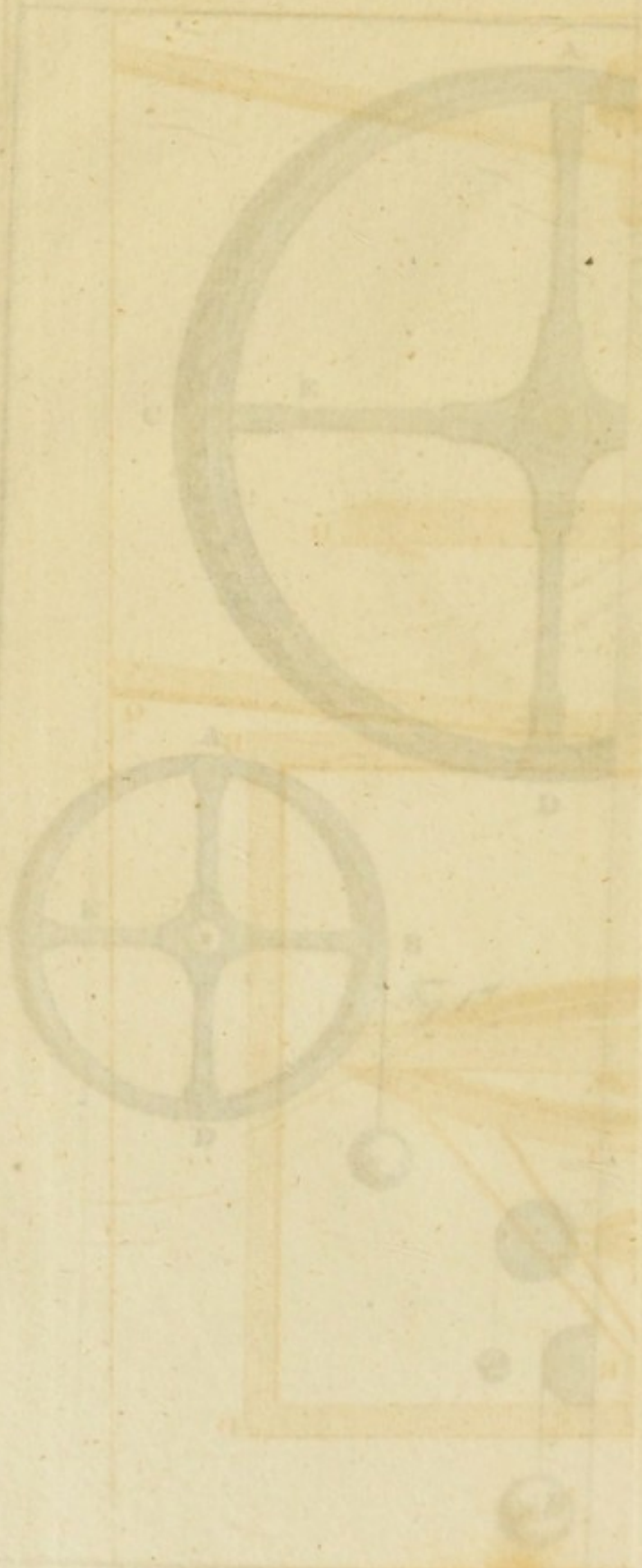


Fig. 1.

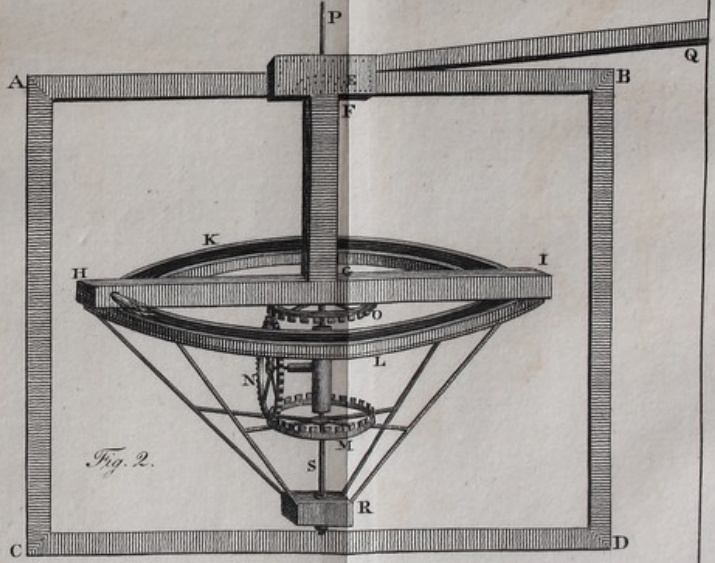
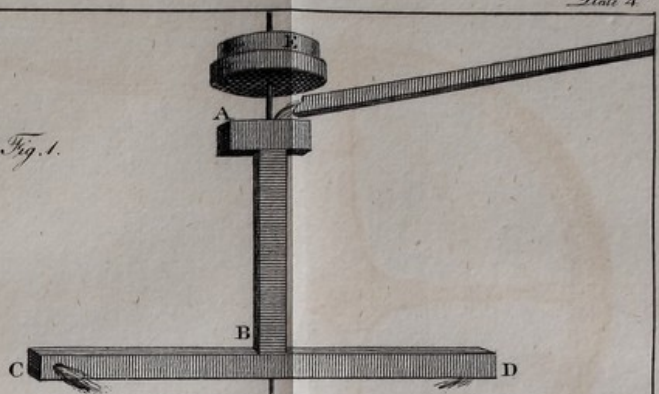
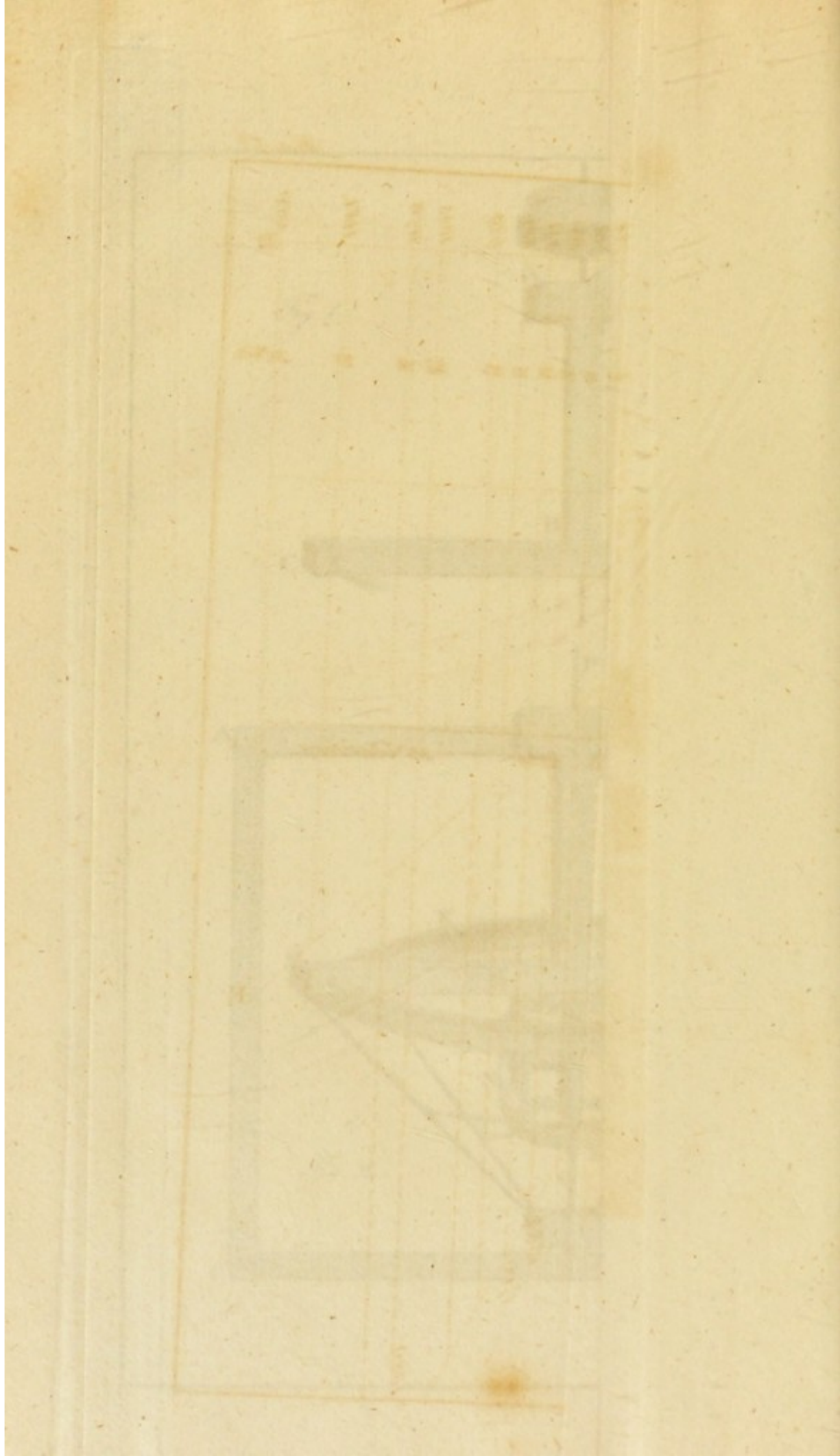
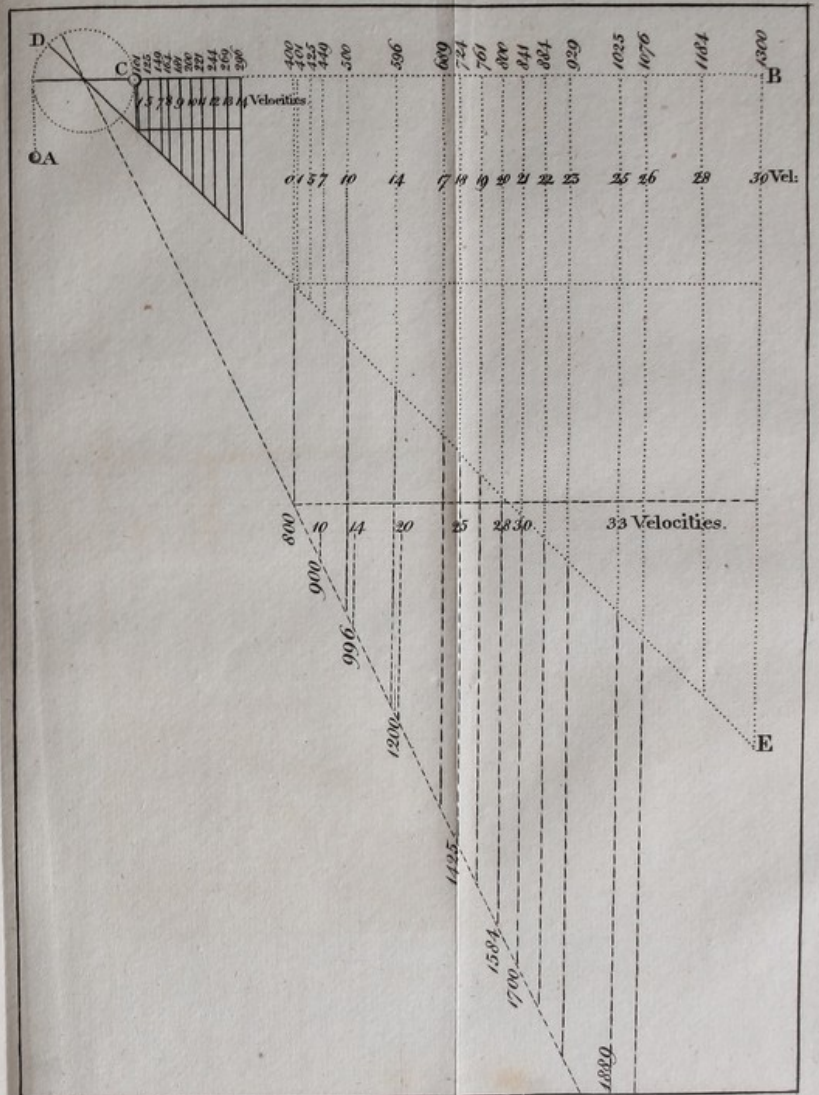
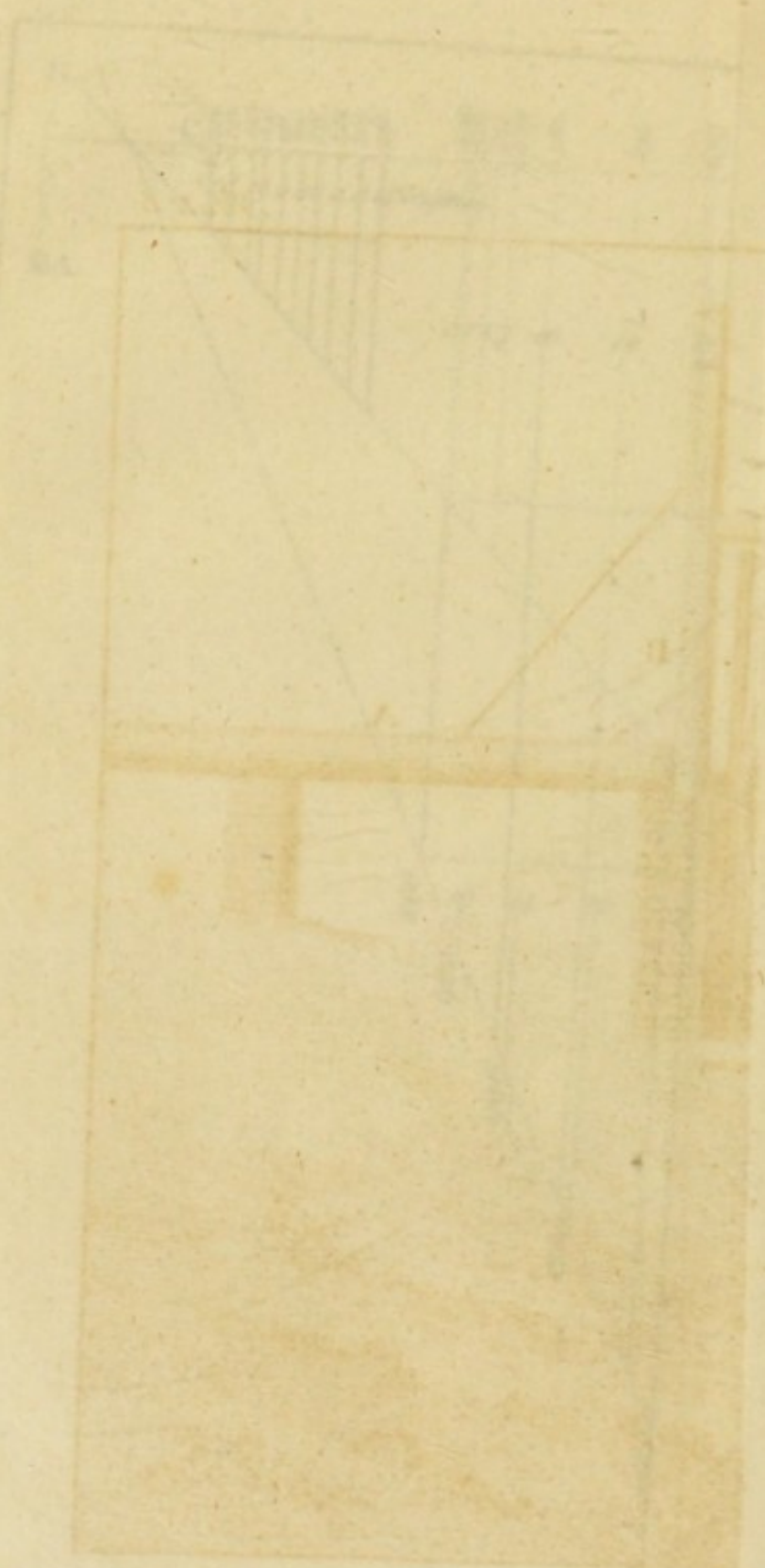
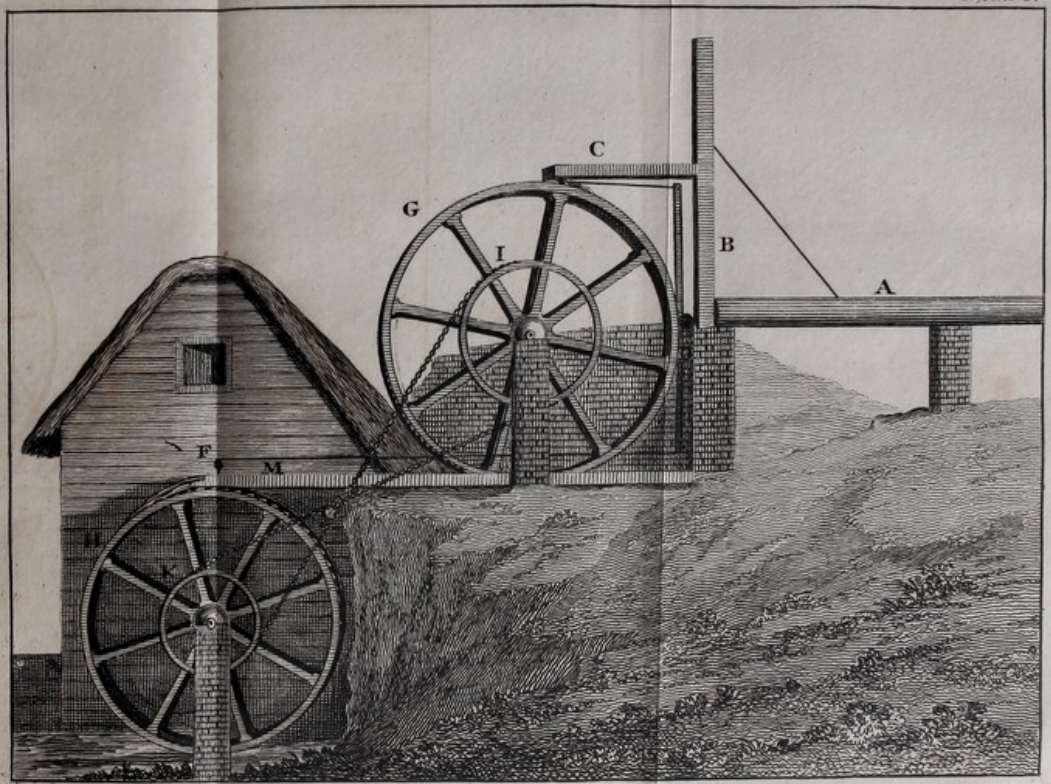


Fig. 2.

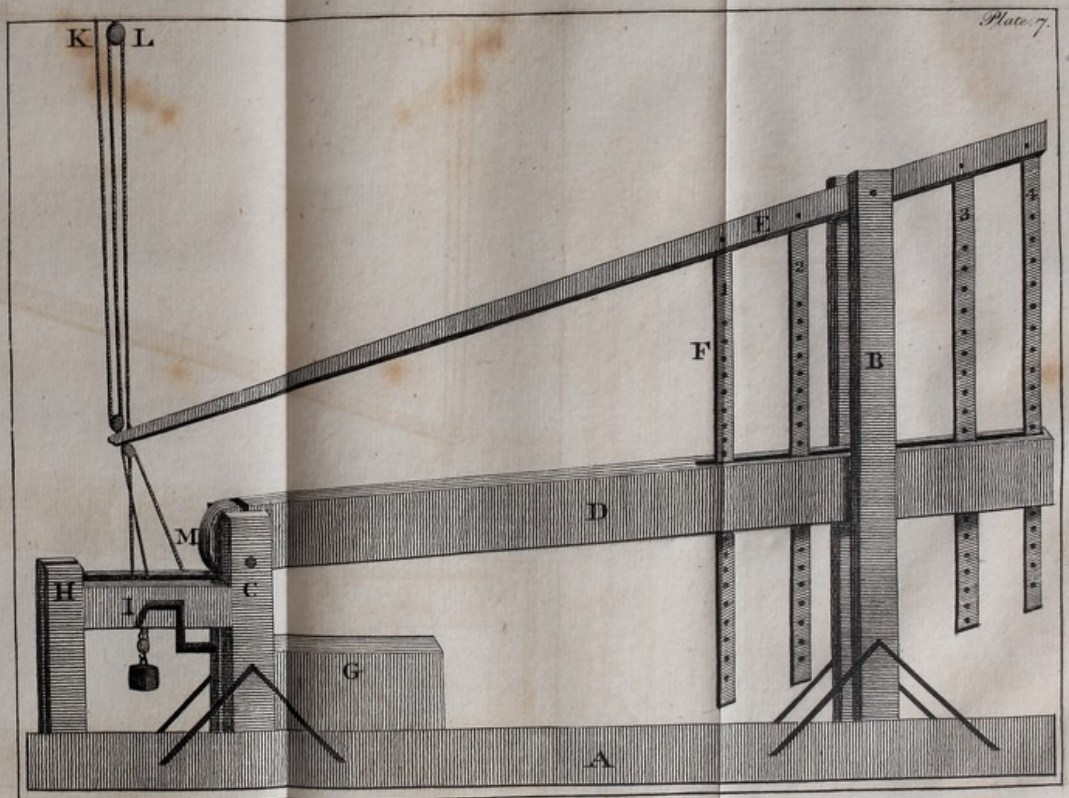


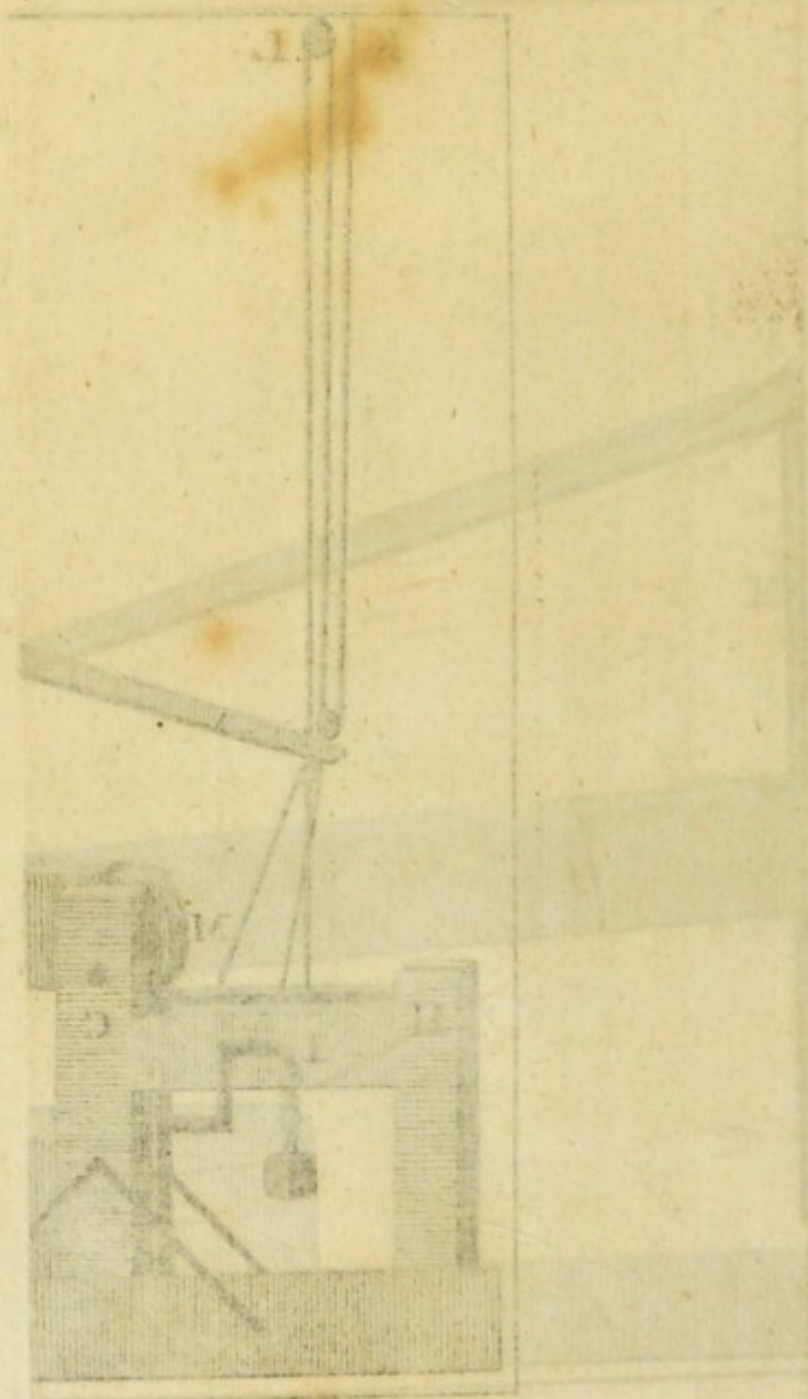












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